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THAPAR INSTITUTE OF ENGINEERING & TECHNOLOGY-PATIALA Department of Computer Science and Engineering U-grade / Axillary Exam (March 11, 2022)

Probability and Statistics (UCS410)

M.M. 45 Time: 2 Hours

Instructors: AMT

Note: Attempt any FIVE questions. Assume missing data suitably, if any. Some useful data P(Z > 1.67) = 0.04746, P(Z < -3) = 0.00135, P(Z < 3) = 0.99865, P(Z < 0) = 0.5, P(Z < -1.5) = 0.06681, P(-2 < Z < 2) = 0.9544, P(-1 < Z < 1) = 0.6826 Here, Z is the standard Normal variable.

Q1 (a)	Two computers A and B are to be marketed. A salesman who is assigned the job of finding customers for them has 70% and 40% chances respectively of succeeding in case of computer A and B. The two computers can be sold independently. Given that he was able to sell at least one computer, what is the probability that computer A has been sold?		
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Q1 (b)	 (i) State Bayes Theorem. (ii) Suppose that a product is produced in three factories X, Y, and Z. It is known that factory X produces thrice as many items as factory Y, and that factories Y and Z produce the same number of items. Assume that it is known that 2 per cent of the items produced by each factories X and Z are defective while 4 percent of those manufactured by factory Y are defective. All the items produced in the three factories are stocked, and an item of product is selected at random. 		
ļ	 What is the probability that this item is defective? If an item selected at random is found to defective, what is the probability that it was produced by factory X, Y and Z respectively? 		
Q2(a)	Consider a random variable X with possible outcomes as 0, 1, 2, 3 Suppose that $P(X = j) = (1 - a)a^{j}, j = 0, 1, 2, 3$ a) Find the values of 'a' so that this model represents a legitimate probability mass function.	3+3 Marks	
	b) Show that the probability $P(X > s + t X > s) = P(X \ge t)$.		
Q2 (b)	Suppose X has exponential distribution with parameter $\lambda = 4$. Find the Cumulative Distribution Function (CDF) $F(t)$ of this distribution and hence calculate $P(X \ge 1)$ using this $F(t)$.	3 Marks	
Q3 (a)	Find Moment Generating Function(MGF) for exponential distribution.	3 Marks	
Q3 (b)	A component exhibits Normal Distribution for failure rate with mean of 3750 hrs. and standard deviation of 500 hrs. What percentage of parts will survive up to 4500 hrs.?	4 Marks	

Q3(c)	What is the probability that at least two out of n people have the same birthday? Assume 365 days in a year and that all days are equally likely.								
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Q4 (a)	Fit the curve $y = ax^b$ for the following data								
	x: 1 2 3 4 5 6								
	y: 1200 90	00 600	200	110	50				
Q4 (b)	Suppose X has exponential distribution with parameter $\lambda = 4$. Find the Cumulative Distribution Function (CDF) $F(t)$ of this distribution and hence calculate $P(X \ge 1)$ using this $F(t)$.								
Q5 (a)	Random variable <i>X</i> follows the continuous uniform distribution over the interval 0 to 1 i.e. [0,1]. Find the probability density function (pdf) of $Y = \frac{1}{X}$?								
Q5(b)	The first four moments of a distribution about the value 4 of the variable are -1·5, 17, -30 and 108. Find the first four moments about the mean.								
Q6	Let the joint probability density function for (X, Y) be $f(x, y) = \begin{cases} \frac{x+y}{2}, & 0 < x, \ 0 < y, \ and \ 3x + y < 3 \\ 0, & Otherwise \end{cases}$ i. Find the probability $P(X < Y)$. Draw the clear target region under consideration ii. Find the marginal probability density function of X . iii. Find the marginal probability density function of Y . iv. Are X and Y independent? If not, find $Cov(X, Y)$.								
Q7 (a)	Suppose that the marks of students in a course are normally distributed with mean 55 and standard deviation 17. We take a sample of size 35, and note that the marks of students are: 82, 70, 45, 80, 49, 52, 59, 43, 36, 76, 72, 48, 64, 60, 38, 54, 46, 68, 35, 55, 61, 58, 76, 56, 62, 38, 63, 37, 78, 37, 60, 47, 38, 14, 32. Find the 95.44% confidence interval µ.								
Q7(b)	Define a Sample and Sample Mean. Also, Show that Sample Mean is an unbiased estimate of population mean.								