

## Problem Set 1

1.

### Results from Terminal:

```
~ — Python
Edgeworth:~ yanshi$ python2
Python 2.7.13 (default, Jul 18 2017, 09:16:53)
[GCC 4.2.1 Compatible Apple LLVM 8.0.0 (clang-800.0.42.1)] on darwin
Type "help", "copyright", "credits" or "license" for more information.
>>> import numpy as np
>>> import cv2
>>> import matplotlib.pyplot as plt
>>> import scipy
>>> from scipy import misc
>>>
```

### 2. Basic Matrix/Vector Manipulation (20 points)

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 0 & 2 & 2 \end{bmatrix}, a = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}, b = \begin{bmatrix} -1 \\ 2 \\ 5 \end{bmatrix}, c = \begin{bmatrix} 0 \\ 2 \\ 3 \\ 2 \end{bmatrix}$$

a. Define Matrix M and Vectors a, b, c in Python. Use Numpy.

```
Matrix M:
[[1 2 3]
 [4 5 6]
 [7 8 9]
 [0 2 2]]
Vector a:
[[1]
 [1]
 [0]]
Vector b:
[[-1]
 [ 2]
 [ 5]]
Vector c:
[[0]
 [2]
 [3]
 [2]]
```

- b. Find the dot product of vectors  $a$  and  $b$ . Save this value to the variable `aDotb` and write its value in your report.

```
aDotb = np.dot(a.T, b)
```

The dot product is:

```
[[1]]
```

- c. Find the element-wise product of  $a$  and  $b$   $[a_1, b_1, a_2, b_2, a_3, b_3]^T$ .

```
[a1, b1, a2, b2, a3, b3].T=[-1 2 0]
```

```
print("%s" % "Element-wise product:")
```

```
print((np.multiply(a, b)).T) newA = np.matlib.repmat(a.T, 4, 1)
```

```
answer2c = np.multiply(newA, M)
```

Element-wise product:

```
[[ -1  2  0]]
```

- d. Find  $(a^T b)Ma$ .

In order to multiply a vector with another vector, we must transpose the first vector before proceeding, otherwise an error will be thrown due to vector/matrix multiplication rules regarding columns and rows. What we obtain with a vector multiplied by another vector is a scalar. This one value is then multiplied to every element in the dot product of matrix  $M$  and vector  $a$ .

```
(a^Tb)Ma =
```

```
[[ 3]
```

```
 [ 9]
```

```
 [15]
```

```
 [ 2]]
```

- e. Without using a loop, multiply each row of  $M$  element-wise by  $a$ . (Hint: the function `repmat()` may come in handy).

```
newA = np.matlib.repmat(a.T, 4, 1)
```

```
answer2e = np.multiply(newA, M)
```

I first needed to transpose vector  $a$  before I could properly use `repmat` to create a new array that I could then properly multiply the  $4 \times 3$  and to adhere to matrix multiplication rules in regards to columns and rows.

```
[[1 2 0]
```

```
 [4 5 0]
```

```
 [7 8 0]
```

```
 [0 2 0]]
```

- f. **Without using a loop, sort all of the values of the new M from (e) in increasing order.**

In order to do this, I used numpy's sort method.

```
[[0 1 2]
 [0 4 5]
 [0 7 8]
 [0 0 2]]
```

### 3. Basic Image Manipulation:

- a. Read in the images, image1.jpg and image2.jpg. there are many different ways to read in images. Matplotlib.image is a good one. Cv2.imread() is another good one. You can also use scipy.misc.imread().



```
image1 = misc.imread('image1.jpg', flatten = 1)
```



```
image2 = misc.imread('image2.jpg', flatten = 1)
```

**\*Images are not according to their original size, they are reduced to show which image is which for grading purposes.**

- b. **Convert the images to double precision and rescale them to stretch from minimum value 0 to maximum value 1.**

```
image1 = np.float64(misc.imread('image1.jpg', flatten = 1, mode='F'))
```

```
image2 = np.float64(misc.imread('image2.jpg', flatten = 1, mode='F'))
```

This is self-explanatory, as I casted the images as I read them in in float64.

- c. **Add the images together and renormalize them to have minimum, value 0 and maximum value 1.**

```
#normalization
normalizedImage1 = np.zeros((720, 652))
normalizedImage1 = cv2.normalize(image1, normalizedImage1, 0, 1,
cv2.NORM_MINMAX)
normalizedImage2 = np.zeros((720, 652))
normalizedImage2 = cv2.normalize(image2, normalizedImage2, 0, 1,
cv2.NORM_MINMAX)
```

In order to normalize, I used cv2's normalization method for this purpose. I needed a place to store the normalized results, thus the variables.

**Results:**



- d. **Create a new image such that the left half of the image is the left half of image1 and the right half of the image is the right half of image 2.**  
I spliced the images in half using my knowledge of matrices' columns and rows. I knew that since I needed half of each image, that I would be dividing my columns in half but keeping my rows the same.

```
croppedImage1 = normalizedImage1[0:720, 0:652/2]  
croppedImage2 = normalizedImage2[:, 652/2:]
```

**Results:**



- e. Using a for loop, create a new image such that every odd numbered row is the corresponding row from image1 and that every even row is the corresponding row from image2. Remember that indices start at 0 and not 1 in Python.

```
frankensteinImage = np.empty((720, 652))  
for row in range(len(normalizedImage1)):  
    if row % 2 == 1: #odd  
        frankensteinImage[row] = normalizedImage1[row]  
    else: #even  
        frankensteinImage[row] = normalizedImage2[row]
```

I checked for the indices of the rows and then determined whether or not it was even or odd by finding its remainder by modulus 2. I would then fill in the rows in frankensteinImage based on the calculations done within the for loop to obtain my results.

**Results:**



- f. Accomplish the same task as part e without using a for-loop (functions `reshape` and `repmat` may be helpful here).

```
oddMatrix = normalizedImage1[1::2]
evenMatrix = normalizedImage2[::2]
frankensteinImage2 = np.empty((720, 652))
frankensteinImage2[1::2] = oddMatrix
frankensteinImage2[::2] = evenMatrix
```

Here, I had spliced the images based on the indices given in steps. The `oddMatrix` contained the image's first row and every other two rows. The even row was the second row, and then every two rows. `frankensteinImage2`'s rows were then filled in based on its own start point and step points and swapping with `oddMatrix`.

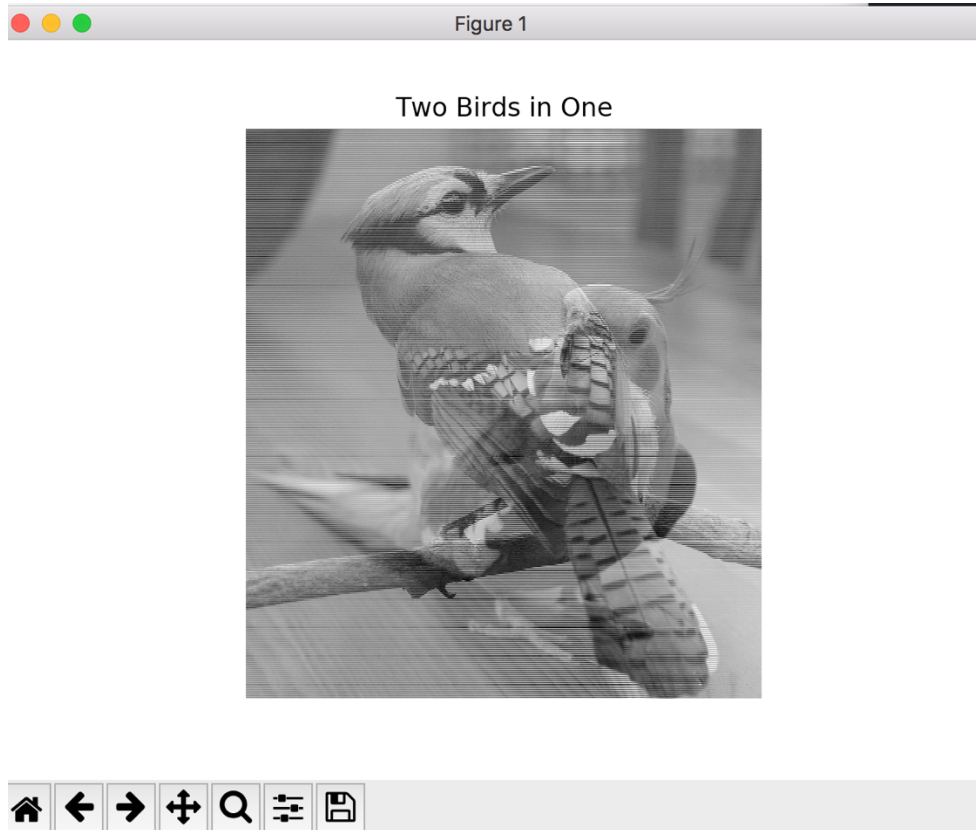
**Results:**



- g. Convert the result from part f to a grayscale image. Display the grayscale image with a title in your report.**

I used a color map provided by the matplotlib that turned my image into a grayscale image.

The result:



#### 4. Compute the average face: (20 pts)

- Download labeled dataset. (google: [LFW face dataset](#) or click the link).  
Pick a face with at least 100 images.  
Dataset can be found in George\_W\_Bush folder.

- Call `numpy.zeros` to create a 250 x 250 x 3 float64 tensor to hold the results.

```
average_array = np.zeros((250, 250, 3), dtype=np.float64)
```

This is self-explanatory, I called `numpy.zeros` to create an empty array that will hold my average face calculations.

- Read each image with `skimage.io.imread`, convert to float and accumulate.

# images\_array requires an array that holds the multiple arrays of the images

```
images_array = np.float64(np.array([np.array(io.imread('George_W_Bush/' +  
fname)) for fname in folder]))
```



I require the first matrix to hold all the other matrices that will be generated by my for loop as I loop through the files in the George\_W\_Bush folder and save the image's matrices information.

- d. Write the averaged result with `skimage.io.imsave`. Post your resulted image in the report.**

In the code, you will find that I used numpy's `mean()` function in order to calculate the average result. I could have also taken the sum of all the arrays in the image arrays and divided it by the number of images (100) as well. That method would have required a for loop.

**Result:**

