

Syntax

Literals	lit	$::= None \mid True \mid False \mid "a" \mid \dots \mid 1 \mid \dots$
Expression	Exp	$::= lit @ (\overline{A}) \mid Exp.id \mid f(\overline{Exp}) \mid Exp.f(\overline{Exp}) \mid C[\overline{A}](\overline{Exp})$
Typed Expression	$TExp$	$::= lit @ (\overline{A}) : \tau \mid \dots$
Assign Op.	$AsgOp$	$\in \{=, +=, -=, *=, /=, \%=, //=\}$
Binary Op.	$BinOp$	$\in \{ , \&\&, , \&, ==, !=, <, >, <=, >=, +, -, *, /, \%, **\}$
Statement	Stm	$::= \text{pass} \mid \text{return } Exp \mid Exp ; Stm \mid id = Exp ; Stm$ $\mid Exp_1 \text{ AsgOp } Exp_2 ; Stm \mid \text{if } Exp : Stm_1 ; \text{else} : Stm_2 ; Stm$ $\mid \text{try} : Stm \text{ except} : Exp ; Stm \mid \text{raise } Exp$

Projection To Python

$$\begin{aligned}
(Exp) \quad \langle lit @ (\overline{B}) : \tau \rangle^A &= \begin{cases} lit & \text{if } A \in \overline{B} \\ \text{Unit.id} & \text{otherwise} \end{cases} \\
\langle Exp.id : \tau \rangle^A &= \begin{cases} \langle Exp \rangle^A.id & \text{if } A \in \text{rolesOf}(Exp.id) \\ \text{absent} & \text{otherwise} \end{cases} \\
\langle f(\overline{Exp}) : \tau \rangle^A &= \begin{cases} f(\langle \overline{Exp} \rangle^A) & \text{if } A \in \text{rolesOf}(f(\overline{Exp})) \\ \text{Unit.id}(f(\langle \overline{Exp} \rangle^A)) & \text{if } A \in \text{rolesOf}(\overline{Exp}) \wedge A \notin \text{rolesOf}(f(\overline{Exp})) \\ \text{Unit.id}(\langle \overline{Exp} \rangle^A) & \text{otherwise} \end{cases} \\
\langle Exp.f(\overline{Exp}) : \tau \rangle^A &= \begin{cases} \langle Exp \rangle^A.f(\langle \overline{Exp} \rangle^A) & \text{if } A \in \text{rolesOf}(Exp) \wedge A \in \text{rolesOf}(\overline{Exp}) \\ & \wedge A \in \text{rolesOf}(Exp.f(\overline{Exp})) \\ \text{Unit.id}(\langle Exp \rangle^A.f(\langle \overline{Exp} \rangle^A)) & \text{if } A \in \text{rolesOf}(Exp) \wedge A \notin \text{rolesOf}(Exp.f(\overline{Exp})) \\ \text{Unit.id}(\langle Exp \rangle^A, \langle \overline{Exp} \rangle^A) & \text{otherwise} \end{cases} \\
\langle C[\overline{B}](\overline{Exp}) : \tau \rangle^A &= \begin{cases} \langle C[\overline{B}] \rangle^A(\langle \overline{Exp} \rangle^A) & A \in \overline{B} \\ \text{Unit.id}(\langle \overline{Exp} \rangle^A) & \text{otherwise} \end{cases} \\
\text{rolesOf}(_ : \tau @ (\overline{B})) &= \overline{B} \\
\text{rolesOf}(\overline{Exp}) &= \bigcup_i \text{rolesOf}(Exp_i) \\
\langle \overline{Exp} \rangle^A &= Exp'_1, Exp'_2, \dots, Exp'_n \text{ where } Exp'_i = \langle Exp_i \rangle^A
\end{aligned}$$

$$\begin{aligned}
(Stm) \quad \llbracket \text{pass} \rrbracket^A &= \text{pass} \\
\llbracket \text{return } Exp; \rrbracket^A &= \text{return} \llbracket Exp \rrbracket^A \\
\llbracket Exp; Stm \rrbracket^A &= \begin{cases} \text{match } \llbracket Exp \rrbracket^A : \\ \quad \text{case } id : \llbracket Stm \rrbracket^A; \\ \quad \llbracket Exp \rrbracket^A; \llbracket Stm \rrbracket^A & \text{otherwise} \end{cases} \\
\llbracket id = Exp ; Stm \rrbracket^A &= \begin{cases} id = \llbracket Exp \rrbracket^A; \llbracket Stm \rrbracket^A & \text{if } A \in \text{rolesOf}(id) \\ \llbracket Exp \rrbracket^A; \llbracket Stm \rrbracket^A & \text{otherwise} \end{cases} \\
\llbracket Exp_1 \text{ AsgOp } Exp_2 ; Stm \rrbracket^A &= \begin{cases} \llbracket Exp_1 \rrbracket^A \text{ AsgOp } \llbracket Exp_2 \rrbracket^A; \llbracket Stm \rrbracket^A & \text{if } A \in \text{rolesOf}(Exp_1 \wedge Exp_2) \\ \llbracket Stm \rrbracket^A & \text{otherwise} \end{cases} \\
\llbracket \text{if } Exp : Stm_1 ; \text{else} : Stm_2 ; Stm \rrbracket^A &= \\
\begin{cases} \text{if } \llbracket Exp \rrbracket^A : \llbracket Stm_1 \rrbracket^A ; \text{else} : \llbracket Stm_2 \rrbracket^A ; \llbracket Stm \rrbracket^A & \text{if } \text{typesOf}(Exp) = \text{boolean}@A \\ \llbracket Exp \rrbracket^A ; \llbracket \llbracket Stm_1 \rrbracket^A \rrbracket \sqcup \llbracket \llbracket Stm_2 \rrbracket^A \rrbracket ; \llbracket Stm \rrbracket^A & \text{otherwise} \end{cases} \\
\llbracket \text{try} : Stm \text{ except} : Exp ; Stm \rrbracket^A &= \\
\begin{cases} \text{try} : \llbracket Stm \rrbracket^A \text{ except} : \llbracket Exp \rrbracket^A ; \llbracket Stm \rrbracket^A & \text{if } A \in \text{rolesOf}(Exp) \\ \text{try} : \llbracket Stm \rrbracket^A ; \llbracket Stm \rrbracket^A & \text{otherwise} \end{cases} \\
\llbracket \text{raise } Exp \rrbracket^A &= \begin{cases} \text{raise } \llbracket Exp \rrbracket^A & \text{if } A \in \text{rolesOf}(Exp) \\ \text{absent} & \text{otherwise} \end{cases}
\end{aligned}$$