

## Syntax

Literals	$lit$	$::= None \mid True \mid False \mid "a" \mid \dots \mid 1 \mid \dots$
Expression	$Exp$	$::= lit@(\overline{A}) \mid Exp.id \mid f(\overline{Exp}) \mid Exp.f(\overline{Exp}) \mid C[\overline{A}](\overline{Exp})$
Typed Expression	$TExp$	$::= lit@(\overline{A}) : \tau \mid \dots$
Assign Op.	$AsgOp$	$\in \{=, +=, -=, *=, /=, \%=, /\} = \}$
Binary Op.	$BinOp$	$\in \{  , \&\&,  , \&, ==, !=, <, >, <=, >=, +, -, *, /, \%, **\}$
Statement	$Stm$	$::= \text{pass} \mid \text{return } Exp \mid Exp; Stm \mid id = Exp; Stm$ $\mid Exp_1 \text{ AsgOp } Exp_2; Stm \mid \text{if } Exp : Stm \text{ else } : Stm$ $\mid \text{try} : Stm \text{ except} : Exp ; Stm \mid \text{raise } Exp$

## Projection To Python

$$\begin{aligned}
(Exp) \quad \llbracket lit@(\overline{B}) : \tau \rrbracket^A &= \begin{cases} lit & \text{if } A \in \overline{B} \\ \text{Unit.id} & \text{otherwise} \end{cases} \\
\llbracket Exp.id : \tau \rrbracket^A &= \begin{cases} \llbracket Exp \rrbracket^A.id & \text{if } A \in \text{rolesOf}(Exp.id) \\ \text{absent} & \text{otherwise} \end{cases} \\
\llbracket f(\overline{Exp}) : \tau \rrbracket^A &= \begin{cases} f(\llbracket \overline{Exp} \rrbracket^A) & \text{if } A \in \text{rolesOf}(f(\overline{Exp})) \\ \text{Unit.id}(f(\llbracket \overline{Exp} \rrbracket^A)) & \text{if } A \in \text{rolesOf}(\overline{Exp}) \wedge A \notin \text{rolesOf}(f(\overline{Exp})) \\ \text{Unit.id}(\llbracket \overline{Exp} \rrbracket^A) & \text{otherwise} \end{cases} \\
\llbracket Exp.f(\overline{Exp}) : \tau \rrbracket^A &= \begin{cases} \llbracket Exp \rrbracket^A.f(\llbracket \overline{Exp} \rrbracket^A) & \text{if } A \in \text{rolesOf}(Exp) \wedge A \in \text{rolesOf}(\overline{Exp}) \\ & \wedge A \in \text{rolesOf}(Exp.f(\overline{Exp})) \\ \text{Unit.id}(\llbracket Exp \rrbracket^A.f(\llbracket \overline{Exp} \rrbracket^A)) & \text{if } A \in \text{rolesOf}(Exp) \wedge A \notin \text{rolesOf}(Exp.f(\overline{Exp})) \\ \text{Unit.id}(\llbracket Exp \rrbracket^A, \llbracket \overline{Exp} \rrbracket^A) & \text{otherwise} \end{cases} \\
\llbracket C[\overline{B}](\overline{Exp}) : \tau \rrbracket^A &= \begin{cases} \llbracket C[\overline{B}] \rrbracket^A(\llbracket \overline{Exp} \rrbracket^A) & A \in \overline{B} \\ \text{Unit.id}(\llbracket \overline{Exp} \rrbracket^A) & \text{otherwise} \end{cases} \\
\text{rolesOf}(\_ : \tau@(\overline{B})) &= \overline{B} \\
\text{rolesOf}(\overline{Exp}) &= \bigcup_i \text{rolesOf}(Exp_i) \\
\llbracket \overline{Exp} \rrbracket^A &= Exp'_1, Exp'_2, \dots, Exp'_n \text{ where } Exp'_i = \llbracket Exp_i \rrbracket^A
\end{aligned}$$

$$\begin{aligned}
(Stm) \quad & \llbracket \text{pass} \rrbracket^A = \text{pass} \\
& \llbracket \text{return } Exp; \rrbracket^A = \text{return} \llbracket Exp \rrbracket^A \\
& \llbracket Exp; Stm \rrbracket^A = \begin{cases} \text{match} \llbracket Exp \rrbracket^A : & a \\ \text{caseid} : \llbracket Stm \rrbracket^A; & a \\ \text{case\_} : \llbracket Stm \rrbracket^A; & a \\ \llbracket Exp \rrbracket^A; \llbracket Stm \rrbracket^A & a \\ \llbracket Stm \rrbracket^A & a \end{cases}
\end{aligned}$$