

# Type Inference Rules For Container Types in CCL

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## Abstract

We present the type inference rules introducing the notion of container types in the CCL programming language. This redesign required a number of substantial changes to the major aspects of the language, including the type system, the syntax, and the definitional semantics.

## The <: Relation

$$\frac{}{\mathcal{Box}(\mathit{Triv}) <: \mathcal{Box}(\mathit{Triv})} \quad (1)$$

$$\frac{}{\mathcal{Box}(\mathit{Int}) <: \mathcal{Box}(\mathit{Int})} \quad (2)$$

$$\frac{\mathcal{T} <: \mathcal{Box}(\mathcal{U}) \quad \mathcal{Box}?(T)}{\mathcal{T} <: \mathit{Immut} \mathcal{Box}(\mathcal{U})} \quad (3)$$

$$\frac{\mathcal{Box}(T) <: \mathit{Immut} \mathcal{Box}(\mathcal{U})}{\mathit{immut} \mathcal{Box}(T) <: \mathit{Immut} \mathcal{Box}(\mathcal{U})} \quad (4)$$

$$\frac{\mathcal{T} <: \mathcal{U} \quad \mathcal{Box}?(T) \quad \mathcal{Box}?(U)}{\mathcal{Ref} \mathcal{T} <: \mathcal{Ref} \mathcal{U}} \quad (5)$$

$\mathcal{Box}?$  statement checks for both mutable and immutable containers. In other words,  $\mathcal{Box}(\mathit{Int})$  and  $\mathit{immut} \mathcal{Box}(\mathit{Int})$  would both satisfy the  $\mathcal{Box}?$  condition.

## The $:$ and $::$ Relations

$$\frac{\text{triv } x}{x : \text{Triv}} \quad (6)$$

$$\frac{\text{triv } x}{x :: \text{Box}(\text{Triv})} \quad (7)$$

$$\frac{\text{int } x}{x : \text{Int}} \quad (8)$$

$$\frac{\text{int } x}{x :: \text{Box}(\text{Int})} \quad (9)$$

$$\frac{x :: \text{Box}(T)}{\text{immut } x :: \text{Immut } \text{Box}(T)} \quad (10)$$

$$\frac{x :: T \quad \text{Box}?(T)}{\text{ref } x :: \text{Box}(\text{Ref } T)} \quad (11)$$

$$\frac{x :: T \quad \text{Box}?(T)}{(x) :: T} \quad (12)$$

$$\frac{x :: T \quad \text{Box}?(T)}{\& x : \text{Ref } T} \quad (13)$$

$$\frac{x :: \text{Ref } T}{x @ : T} \quad (14)$$

$$\frac{x : \text{Ref } T}{x @ : T} \quad (15)$$

$$\frac{x :: \text{Box}(T) \quad y :: \mathcal{U} \quad T <: \mathcal{U}}{x := y : \text{Box}(T)} \quad (16)$$

$$\frac{x :: \text{Box}(T) \quad y :: \mathcal{U} \quad T <: \mathcal{U} \quad \text{Box}?(U)}{x := y : \text{Box}(T)} \quad (17)$$

$x : T$  is read as “expression  $x$  is of type  $T$  and is in an *r-context*.”

$x :: T$  is read as “variable  $x$  is of type  $T$  and is in an *l-context*.”

The operators could also be referred to as the “r-type of” and “l-type of” operators.

*l-context* denotes everything that is *assignable* (indicated as a storable memory). *r-context*, on the other hand, denotes everything that is *expressible* (can be produced by an expression).

There is no r-value (e.g. expression) of the type  $\text{Box}(T)$ .

We omit rules for *Con* types as they only operate on r-values.

We omit rules for *Fun* types as they only accept r-values. Any variable and/or primitive type has both r-value and l-value (when it comes to primitive types, only r-value). In all cases, the r-value part of the actual parameter is passed when the function is being called.

## Resulting Relationships (A Short List)

<code>int i</code>	$\rightarrow i$	$\rightarrow \mathcal{B}\chi(Int)$
<code>immut int ii</code>	$\rightarrow ii$	$\rightarrow \text{Immut } \mathcal{B}\chi(Int)$
<code>ref int ri</code>	$\rightarrow ri$	$\rightarrow \mathcal{B}\chi(\mathcal{R}\text{ef } \mathcal{B}\chi(Int))$
<code>immut ref int iri</code>	$\rightarrow iri$	$\rightarrow \text{Immut } \mathcal{B}\chi(\mathcal{R}\text{ef } \mathcal{B}\chi(Int))$
<code>ref immut int rii</code>	$\rightarrow rii$	$\rightarrow \mathcal{B}\chi(\mathcal{R}\text{ef } (\text{Immut } \mathcal{B}\chi(Int)))$
<code>immut ref immut int irii</code>	$\rightarrow irii$	$\rightarrow \text{Immut } \mathcal{B}\chi(\mathcal{R}\text{ef } (\text{Immut } \mathcal{B}\chi(Int)))$

Type  $\text{Immut } \mathcal{B}\chi(\text{Immut } \mathcal{B}\chi(Int))$  cannot exist. Nested  $\mathcal{B}\chi$  types are only possible when there is at least one  $\mathcal{R}\text{ef}$  type.

$$\mathcal{B}\chi(\text{Triv}) <: \mathcal{B}\chi(\text{Triv})$$

$$\mathcal{B}\chi(Int) <: \mathcal{B}\chi(Int)$$

$$\mathcal{B}\chi(\text{Triv}) <: \text{Immut } \mathcal{B}\chi(\text{Triv})$$

$$\mathcal{B}\chi(Int) <: \text{Immut } \mathcal{B}\chi(Int)$$

$$\text{Immut } \mathcal{B}\chi(\text{Triv}) <: \text{Immut } \mathcal{B}\chi(\text{Triv})$$

$$\text{Immut } \mathcal{B}\chi(Int) <: \text{Immut } \mathcal{B}\chi(Int)$$

All the rules above should work with  $\mathcal{R}\text{ef}$  types in the similar manner:

$$\mathcal{R}\text{ef } \mathcal{B}\chi(\text{Triv}) <: \mathcal{R}\text{ef } \mathcal{B}\chi(\text{Triv})$$

$$\mathcal{R}\text{ef } \mathcal{B}\chi(Int) <: \mathcal{R}\text{ef } \mathcal{B}\chi(Int)$$

$$\mathcal{R}\text{ef } \mathcal{B}\chi(\text{Triv}) <: \mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(\text{Triv})$$

$$\mathcal{R}\text{ef } \mathcal{B}\chi(Int) <: \mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(Int)$$

$$\mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(\text{Triv}) <: \mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(\text{Triv})$$

$$\mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(Int) <: \mathcal{R}\text{ef } \text{Immut } \mathcal{B}\chi(Int)$$