

Math 327, Simple Linear Regression, Example R output

This document illustrates what values, as notated in the textbook, are produced by the R functions, `summary()`, `anova()`, and `confint()`.

```
> car.fit = lm (travel.time ~ dist.Decorah, data=car.data)
> summary (car.fit)
```

Call:

```
lm(formula = travel.time ~ dist.Decorah, data = car.data)
```

Residuals:

| Min | 1Q | Median | 3Q | Max |
|----------|----------|----------|---------|---------|
| -0.37660 | -0.19209 | -0.08742 | 0.23370 | 0.34867 |

Summary statistics of the sample residuals.

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) |
|--------------|-----------|------------|---------|--------------|
| (Intercept) | 0.3765987 | 0.1406053 | 2.678 | 0.0253 * |
| dist.Decorah | 0.0154366 | 0.0006381 | 24.190 | 1.69e-09 *** |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

In the table above, we find these values:

Coefficients:

| | Estimate | Std. Error | t value | Pr(> t) |
|--------------|-----------------|---------------------|---------------------------------------|-------------------------------|
| (Intercept) | $\hat{\beta}_0$ | $se(\hat{\beta}_0)$ | $t = \hat{\beta}_0/se(\hat{\beta}_0)$ | $P(T > t \mid \beta_0 = 0)$ |
| dist.Decorah | $\hat{\beta}_1$ | $se(\hat{\beta}_1)$ | $t = \hat{\beta}_1/se(\hat{\beta}_1)$ | $P(T > t \mid \beta_1 = 0)$ |

The “Signif. codes” mean that p-values between 0 and 0.001 are marked with ‘***’; p-values between 0.001 and 0.01 are marked with ‘**’; p-values between 0.01 and 0.05 are marked with ‘*’; p-values between 0.05 and 0.1 are marked with ‘.’; and p-values greater than 0.1 are not marked.

Residual standard error: 0.2659 on 9 degrees of freedom
Multiple R-squared: 0.9849, Adjusted R-squared: 0.9832
F-statistic: 585.2 on 1 and 9 DF, p-value: 1.687e-09

In the three lines above, Residual standard error = $\hat{\sigma} = MS_{res} = SS_{res}/(n - 2)$;
degrees of freedom = $n - 2$;

Multiple R-squared = $R^2 = \hat{\beta}_1 SS_{xy} / SS_{xx} = 1 - \frac{SS_{res}}{SS_T}$;

Adjusted R-squared = $R^2_{Adj} = 1 - \frac{SS_{res}/(n-p)}{SS_T/(n-1)}$

F-statistic = MS_{reg} / MS_{res}

p-value = $P(F > F_{stat} \mid \beta_1 = 0)$

```
> anova(car.fit)
Analysis of Variance Table

Response: travel.time
      Df Sum Sq Mean Sq F value    Pr(>F)
dist.Decorah  1 41.362   41.362   585.15 1.687e-09 ***
Residuals    9  0.636    0.071
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

In the ANOVA table above, we find these values:

| | Df | Sum Sq | Mean Sq | F value | Pr(>F) |
|--------------|---------|---------------------------------|--------------------|---------------------|---|
| dist.Decorah | 1 | $\hat{\beta}_1 SS_{xy}/SS_{xx}$ | $SS_{reg}/1$ | MS_{reg}/MS_{res} | $P(F > MS_{reg}/MS_{res} \mid \beta_i = 0)$ |
| Residuals | $n - 2$ | SS_{res} | $SS_{res}/(n - 2)$ | | |

The row with totals is not listed in the `anova()` function output. Only the “Df” and “Sum Sq” totals are relevant. Total Df = $n - 1$, and Total Sum of Squares is $SS_T = \sum_{i=1}^n (y_i - \bar{y})^2$.

The `confint()` function produces confidence intervals for the parameter estimates. The `round(..., 3)` function rounds the values to 3 decimal places.

```
> round(confint(car.fit), 3)
              2.5 % 97.5 %
(Intercept) 0.059 0.695
dist.Decorah 0.014 0.017
```

The table above has these values:

Intercept: $\hat{\beta}_0 - t_{1-\alpha/2}se(\hat{\beta}_0), \hat{\beta}_0 + t_{1-\alpha/2}se(\hat{\beta}_0)$

Slope: $\hat{\beta}_1 - t_{1-\alpha/2}se(\hat{\beta}_1), \hat{\beta}_1 + t_{1-\alpha/2}se(\hat{\beta}_1)$

Interpretation templates:

- Slope:
 - For every one unit increase in the predictor variable, the mean response changes by slope units, $p = p\text{-value}$
 - Or: The mean response {increases | decreases} |slope| y-units per x-unit
 - Or: The mean response changes between LCL and UCL y-units per x-unit with 95% confidence
- Intercept:
 - The mean response when X is zero is between LCL and UCL y-units with 95% confidence
- Predicted responses:
 - Mean: The estimated mean response when X is X-value is between LCL and UCL y-units with 95% confidence
 - Individual: The predicted response for an individual when X is X-value is between LCL and UCL y-units with 95% confidence