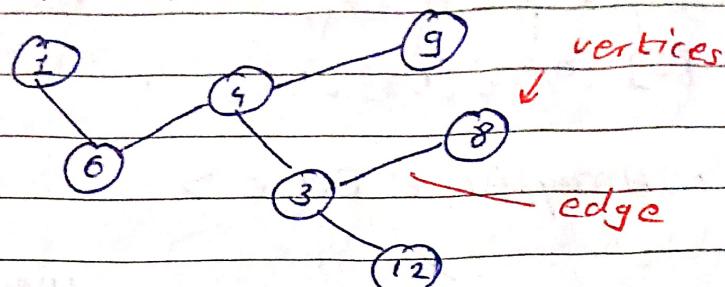


* Graphs :

DATE 19092024

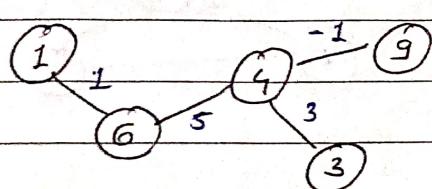
- networks of nodes



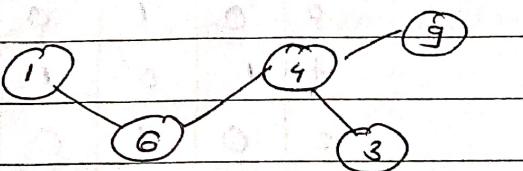
* Edges :

- 1) Unidirectional \rightarrow
- 2) Undirected \rightarrow
- 3) Bidirected \rightarrow

* Types :



weighted graph



unweighted graph

* Storing a graph :

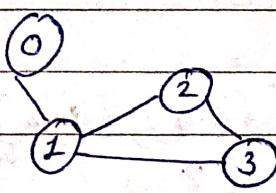
- 1) Adjacency List :
- List of lists

0 - (1)

1 - (0, 2, 3)

2 - (1, 3)

3 - (2, 1)



Create graph ,

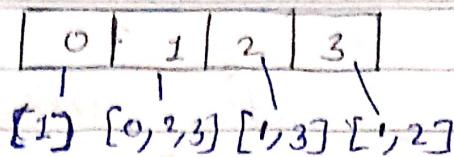
ArrayList < ArrayList >

Array < ArrayList >

HashMap < Integer, ArrayList > — mostly use

min edge in graph = $2V - 1$
max edge in graph = $nC_2 = \frac{n(n-1)}{2}$

DATE



• vertex is the index

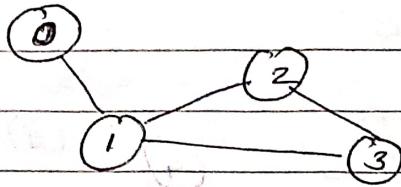
3) Adjacency List < Edge >

source destination weight.

- does not stored extra information
- optimized.

2) Adjacency matrix:

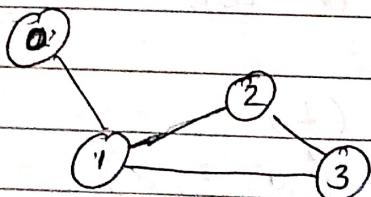
	0	1	2	3
0	0	1	0	0
1	1	0	1	1
2	0	1	0	1
3	0	1	1	0



when weight are present then stored wt instead of 1.

3) Edge list

edges = $\{ \{0, 1\}, \{1, 2\}, \{1, 3\}, \{2, 3\} \}$



- this type structure mostly used when graph is sort.

4) implicit graph.

mostly use when

travers in 2D array.

(i, j)

$(i, j-1) \leftarrow (i, j) \rightarrow (i+1, j)$

$(i+1, j)$

$(0, 0)$						

Sparse graph - no. of edge is minimum,
dense graph - no. of edge is maximum (almost cpt graph).

DATE

--	--	--	--	--	--	--

* Applications of graphs :

- a) MAPS : (shortest path)
- b) Social network : One person connect more people.
- c) Delivery Network : shortest cyclic route
- d) Physics & Chemistry :
- e) Routing algorithms.
- f) Machine learning : (computation graphs, neural networks, for calculation).

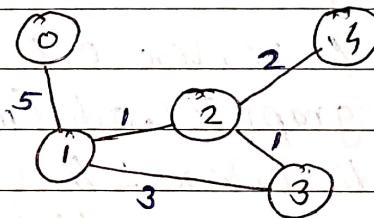
g) Dependency graph :

- h) computer vision : image segmentation, flood fill
~~connected components~~, algorithm (fill the color in image).
- i) Graph database : nebula, neo4j.
- j) Research : (map humans brain (in brain present neurons)).

* Create a graph :

1) Adjacency List :

ArrayList<Edge> graph;
edge = (src, dest, wt)



$$0 \rightarrow \{0, 1, 5\}$$

$$1 \rightarrow \{1, 0, 5\}, \{1, 2, 1\}, \{1, 3, 3\}$$

$$2 \rightarrow \{2, 1, 1\}, \{2, 3, 1\}, \{2, 3, 2\}$$

$$3 \rightarrow \{3, 1, 3\}, \{3, 2, 1\}$$

$$4 \rightarrow \{4, 2, 2\}$$

Note: when given

```
// code 11 static class Edges {  
    int src;  
    int dest;  
    int wt;  
    Edges(int s, int d, int w) {  
        src = s;  
        dest = d;  
        wt = w;  
    }  
}  
public static void main(String args[]) {  
    int v = 5;  
    ArrayList<Edges> graph = new ArrayList[v];  
    for (int i = 0; i < v; i++) {  
        graph[i] = new ArrayList();  
    }  
    // vertex 0 //  
    graph[0].add(new Edges(0, 1, 5));  
    // vertex 1 //  
    graph[1].add(new Edges(1, 0, 5));  
    graph[1].add(new Edges(1, 2, 1));  
    graph[1].add(new Edges(1, 3, 3));  
    // vertex 2 //  
    graph[2].add(new Edges(2, 1, 5));  
    graph[2].add(new Edges(2, 3, 1));  
    graph[2].add(new Edges(2, 4, 2));  
    // vertex 3 //  
    graph[3].add(new Edges(3, 1, 3));  
    graph[3].add(new Edges(3, 2, 1));  
    // vertex 4 //  
    graph[4].add(new Edges(4, 2, 2));
```

```
// print only 2th index neighbors //
for(int i=0; i<graph[2].size(); i++) {
```

Edges e = graph[2].get(i);

System.out.println(e.dest); O/P: 1

}

}

3

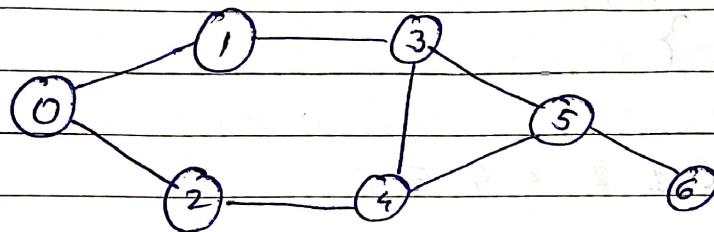
4

* Graph Traversals:

1) Breadth First Search (BFS):

2) Depth First Search (DFS):

1) Breadth First Search :



- traverse by level wise & used queue data structure.
- go to immediate neighbors first.

queue - [0|1|2|3|0|4|0|1|5|1|3|6|5|1]

visit [] = |T|T|T|T|T|T|T|

O/P: 0 1 2 3 4 5 6

- when remove vertex from queue then add neighbors of this vertex in queue & store T or F if vertex is print or not./ repeat or not

1) code

```

public static void BFS (ArrayList<Edge> graph[]) {
    Queue <Integer> q = new LinkedList<>();
    boolean visit[] = new boolean[graph.length];
    q.add(0);
    while (!q.isEmpty()) {
        int curr = q.remove();
        if (!visit[curr]) {
            System.out.print(curr + " ");
            visit[curr] = true;
            for (int i=0; i<graph[curr].size(); i++) {
                Edge e = graph[curr].get(i);
                q.add(e.dest);
            }
        }
    }
}
%P: 0 1 2 3 4 5 6

```

2)

DFS (depth first search):**2) code**

```

public static void DFS (ArrayList<Edge> graph,
                      int curr, boolean[] visit) {
    System.out.print(curr + " ");
    visit[curr] = true;
    for (int i=0; i<graph[curr].size(); i++) {
        Edge e = graph[curr].get(i);
        if (!visit[e.dest]) {
            DFS(graph, e.dest, visit);
        }
    }
}

```

%P: 0 1 3 4 2 5 6

g. Has Path?

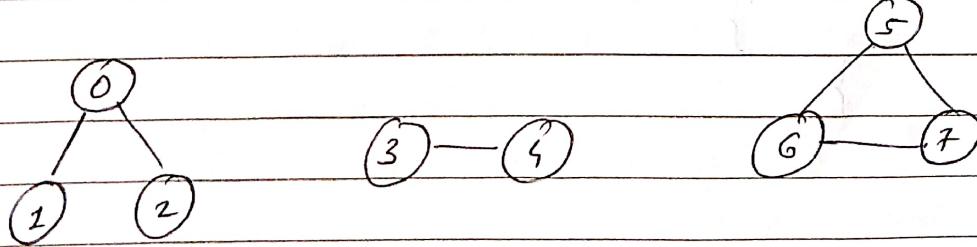
- for given src & dest, tell if path exists src to dest.

Ex: src = 0, dest = 5 ans = true.

```
Model public static boolean hasPath(graph, int src, int dest,
    if (src == dest) return boolean visit[] ) {
    if (src == dest) return true;
    visit[src] = true;
    for( int i=0; i< graph[src].size(); i++ ) {
        Edge e = graph[src].get(i);
        // e.dest = neighbour //
        if (!visit[e.dest] && hasPath( graph,
            e.dest, dest, visit )) {
            return true;
        }
    }
    return false;
}
```

* Connected Components:

Ex:



// These are one graph in diff.
component //

0	1	2	3	4	5	6	7
1 2	0	0	4	3	5 7	5 7	5 6

// This code is traverse of all component of graph //

```

// Code 11
public static void bst(ArrayList<Edge> graph[]) {
    boolean[] visit = new boolean[graph.length];
    for(int i=0; i<graph.length; i++) {
        if(!visit[i]) {
            bstUtil(graph, i, visit);
        }
    }
}

// This method travers each index of array
public static void bstUtil(graph, cur, visit) {
    Queue<Integer> q = new LinkedList<>();
    q.add(cur);
    while(!q.isEmpty()) {
        int temp = q.remove();
        if(!visit[temp]) {
            System.out.print(temp + " ");
            visit[temp] = true;
            for(int i=0; i<graph[temp].size(); i++) {
                Edge e = graph[temp].get(i);
                q.add(e.dest);
            }
        }
    }
}

```

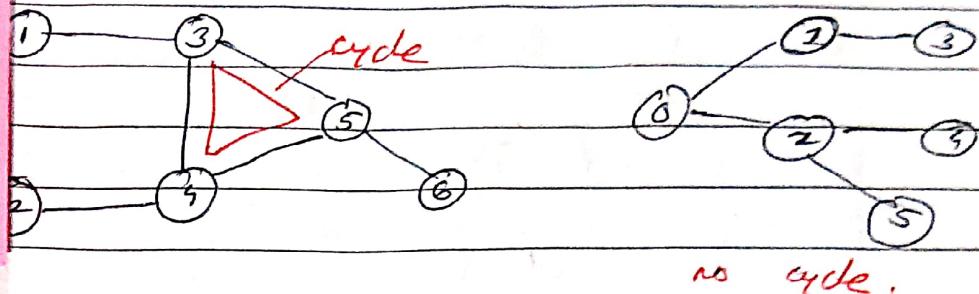
Note: detect cycle by BFS method. (191 page). undirected

DATE 22 09 2024

* Cycle in graphs :

- 1) cycle detection:
 - a) Directed → BFS - kann algos
 - b) DFS - visit & path boolean array.
- 2) Undirected → BFS - Create pair store pair & node
 - b) DFS - pair curr in recursive fun.

Time complexity in undirected graph : (DFS) $O(V+E)$



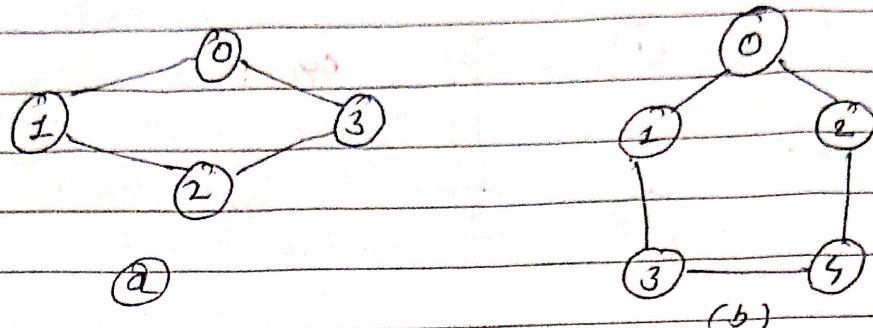
```
//code1 public static boolean detectcycle ( graph ) {  
    boolean visit [] = new boolean [graph.length];  
    for( int i=0; i< graph.length; i++ ) {  
        if( !visit [i] ) {  
            if( detectcycleUtil (graph, i, -1, visit) )  
                return true;  
        }  
    }  
    return false;  
}
```

```
public static boolean detectCycleUtil ( graph, curr, par, visit ) {  
    visit [curr] = true;  
    for( int i=0; i< graph[curr].size (); i++ ) {  
        Edge e = graph[curr].get (i);  
        if( visit [e.dest] && e.dest != par ) {  
            return true;  
        } else if( !visit [e.dest] &&  
                  detectCycleUtil (graph, e.dest, curr, visit) )  
            return true;  
    }  
    // if par == e.dest → continue //  
    return false;  
}
```

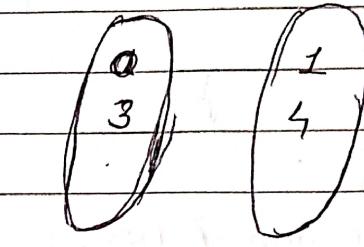
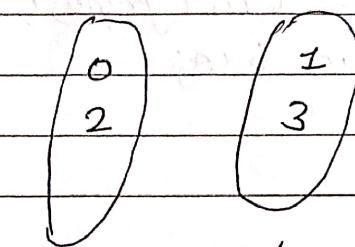
Q. Bipartite :

check given graph is partite or not.

Ex:



- creating two set of ~~is~~ add element in different set when two vertex connected by edge.
- for dia.(a) for ex dia (b)



Set A Set B

Set A Set B

bipartite

not bipartite, because
2 not add any set

- explanation : dia(B).
- if 2 add in set A but 0 & 2 are connected by edge and 2 add in set B but 4 & 2 are connected by edge, hence gives graph is not bipartite.

approach :

fill the colour colors of node yellow & blue.

case 1: neighbor colour - same \Rightarrow return false

case 2: neighbor color - diff. \Rightarrow continue

case 3: neighbor no colour \Rightarrow fill colour.

* day run & code write *

DATE

```
//code11 public static boolean isPartite (ArrayList<Edge> graph[]) {  
    int color[] = new int [graph.length];  
    for( int i=0; i<color.length; i++ ) {  
        color[i] = -1;  
    }  
  
    queue<Integer> q = new LinkedList<>();  
    for( int i=0; i<graph.length; i++ ) {  
        if (color[i] == -1) {  
            q.add(i);  
            color[i] = 0;  
            while ( !q.isEmpty() ) {  
                int cur = q.remove();  
                for( int j=0 ; j<graph[cur].size(); j++ ) {  
                    Edge e = graph[cur].get(j);  
                    if (color[e.dest] == -1) {  
                        if (color[cur] == 0) {  
                            color[e.dest] = 1;  
                        } else if (color[cur] == 1) {  
                            color[e.dest] = 0;  
                        } q.add(e.dest);  
                    } else if (color[cur] == color[e.dest]) {  
                        return false;  
                    }  
                }  
            }  
        }  
    }  
    return true;  
}
```

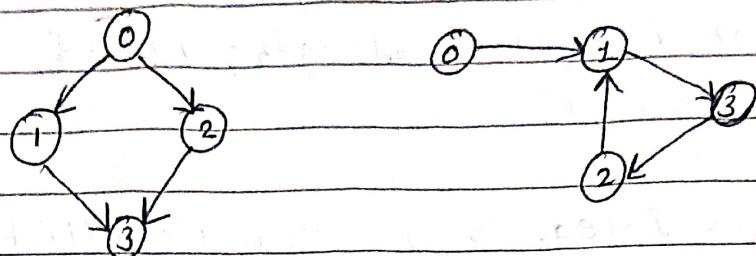
* dry run * write code *

DATE

--	--	--	--	--	--	--

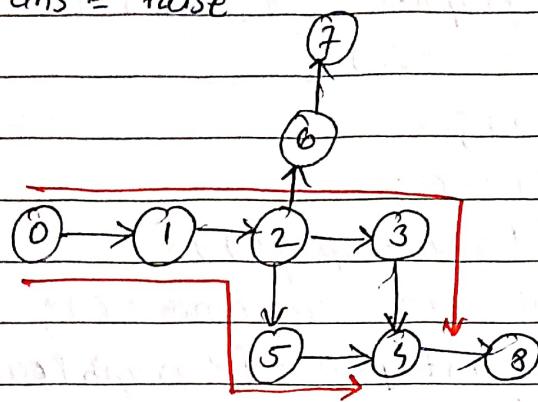
2) cycle detection in directed graph :

ex:



ans = false

ans = true.



track only current path.

// code

```

public static boolean isCycle(graph) {
    boolean visit[] = new boolean[graph.length];
    boolean stack[] = new boolean[graph.length];
    for (int i=0; i<graph.length; i++) {
        if (!visit[i]) {
            if (isCycleUtil(graph, i, visit, stack))
                return true;
        }
    }
    return false;
}

```

DATE

```
public static boolean isCycleUtil(graph, cur, visit, stack){  
    visit[cur] = true;  
    stack[cur] = true;  
  
    for( int i=0; i<graph[cur].size(); i++ ) {  
        Edge e = graph[cur].get(i);  
        if( stack[e.dest] ) {  
            return true;  
        }  
        if( !visit[e.dest] && isCycleUtil(g, e.dest, v, s))  
            return true;  
    }  
    stack[cur] = false;  
    return false;  
}
```

* g) cycle detect using BFS: (undirected graph)

```
// code 11
public class Pair {
    int first; int second;
    Pair (int f, int s) {
        first = f;
        second = s;
    }
}

public boolean BFS (adj, int curr, boolean visit[]) {
    Queue<Pair> q = new LinkedList();
    q.add (new Pair (curr, -1));
    visit[curr] = true;

    while (!q.isEmpty ()) {
        int node = q.peek().first;
        int par = q.peek().second;
        q.remove();

        for (int i=0; i<adj.get(node).size(); i++) {
            int neighbor = adj.get(node).get(i);
            if (par == neighbor) {
                continue;
            }

            if (visit[neighbor]) return true;
            q.add (new Pair (neighbor, node));
            visit[neighbor] = true;
        }
    }
    return false;
}
```

```
public boolean isCycle (ArrayList<ArrayList<Integer>> adj) {  
    boolean visit[] = new boolean [adj.size()];  
    for (int i=0; i<adj.size(); i++) {  
        if (!visit[i]) {  
            if (BFS (adj, i, visit)) {  
                return true;  
            }  
        }  
    }  
    return false;  
}
```

g. Cycle detect using BFS : (directed graph)
approach : (Kahn's algorithm)

- 1) Calculate indegree of all vertices
- 2) Add 0 degree index in queue
- 3) Perform BFS & count the visited vertexes vertex.
- 4) Check if countvertex == V return false otherwise
return true (cycle is exist).

1) code

```
public boolean isCyclic (int V, ArrayList<ArrayList<Integer>> adj)  
{  
    int [] indeg = new int [V];  
    for (int i=0; i<V; i++) {  
        for (int j : adj.get(i)) {  
            indeg[adj.get(i).  
            indeg[j]++;  
        }  
    }  
}
```

```
queue<Integer> q = new LinkedList();
```

```
for(int i=0; i<indeg.length; i++){
    if(indeg[i]==0) {
        q.add(i);
    }
}
```

// BFS //

int count=0;

```
while(!q.isEmpty()) {
```

int node=q.remove();

count++;

// reduce indegree of neighbors //

```
for(int neighbor : adj.get(node)) {
```

indegree[neighbor]--;

if(indeg[neighbor]==0) {

q.add(neighbor);

count==V: no cycle

count!=V: present

return (count==V)? 1: 0; // count < V: present cycle.

}

Complexity: O(V+E) time | O(V+E) space | O(V+E) building graph

graph is connected

graph has cycles

graph has no cycles

graph has multiple components

graph has one component

graph has no edges

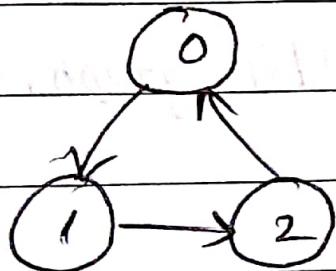
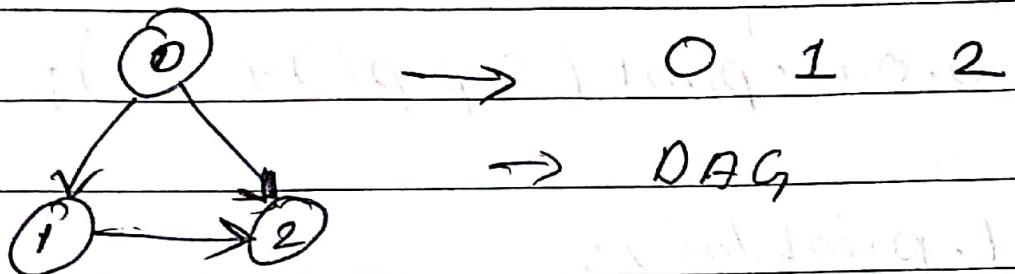
graph has one edge

graph has two edges

graph has three edges

g. Topological Sorting :

- Topological sorting only Directed Acyclic Graph (DAG) is directed graph with no cycle.
- It is linear order of vertices such that every directed edge $u \rightarrow v$, the vertex u comes before v in the order



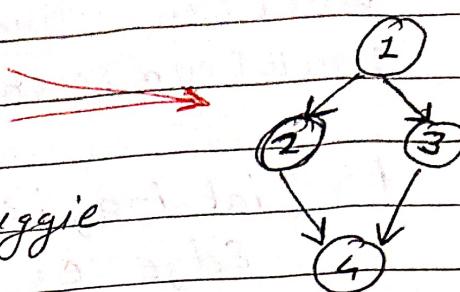
Topological sort use for check dependency.

ex: Action 1 - boil water

any work do first Action 2 - add masala

Action 3 - add maggie

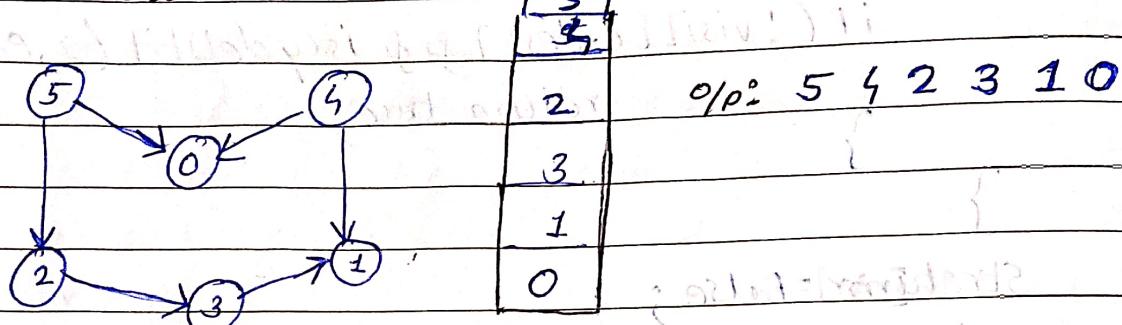
Action 4 - add serve maggie



O/P: 1 2 3 4 (also 1 3 2 4)

approach: used modified DFS.

- used stack for stored curr data



```

// code
public static void topologicalSort (graph) {
    boolean visit[] = new boolean [graph.length];
    Stack < Integer > s = new Stack ();
    for (int i=0; i<graph.length; i++) {
        if (!visit[i]) {
            topologicalSortUtil (graph, i, visit, s);
        }
    }
}
  
```

while (!s.isEmpty ()) {

System.out.print (s.pop () + " ");

System.out.println ();

```

public static void topologicalSortUtil (graph, curr, visit, s) {
    visit[curr] = true;
}
  
```

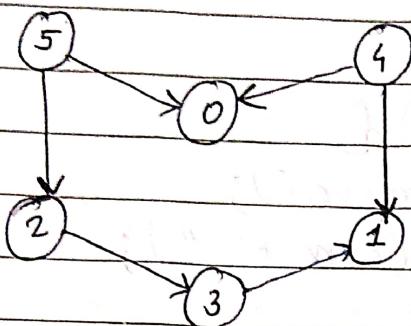
```

    for(int i=0; i<graph[&utr].size(); i++) {
        Edge e = graph[cur].get(i);
        if(!visit[e.dest]) {
            topo.logicalSortUtil(graph, e.dest, visit, s);
        }
    }
    s.push(cur);
}

```

* Topological sort using BFS : (Kahn's algorithm)

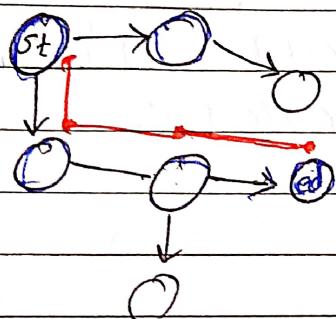
approach :



① first calculate indegree & outdegree of every node/vertex.

ex: ① → indegree = 2
outdegree = 0.

Fact : A DAG has at least one vertex with in-degree 0 & one vertex with out-degree 0.



5t - indegree - 0

ed - outdegree - 0.

- Here is longest path
hence starting pt indegree 0 &
ending pt outdegree 0.

② then add 0 indegree vertex in queue

③ apply BFS & remove queue element &
subtract indegree of their neighbors.

	0	1	2	3	4	5
indegree	2	2	1	1	0	0

```

Method public static void topSort(DirectedEdgeGraph graph) {
    int indeg[] = new int[graph.length];
    calDeg(graph, indeg);
    Queue<Integer> q = new LinkedList<>();
    for (int i = 0; i < indeg.length; i++) {
        if (indeg[i] == 0) {
            q.add(i);
        }
    }
    // BFS
    while (!q.isEmpty()) {
        int cur = q.remove();
        System.out.print(cur + " ");
        for (int i = 0; i < graph[cur].size(); i++) {
            Edge e = graph[cur].get(i);
            indeg[e.dest]--;
            if (indeg[e.dest] == 0) {
                q.add(e.dest);
            }
        }
    }
}

```

```

public static void calDeg(DirectedEdgeGraph graph, int indeg[]) {
    for (int i = 0; i < graph.length; i++) {
        int v = i;
        for (int j = 0; j < graph[v].size(); j++) {
            Edge e = graph[v].get(j);
            indeg[e.dest]++;
        }
    }
}

```

```

11 code || public static void topSort(ArrayList<Edge> graph) {
    int indeg[] = new int[graph.length];
    calDeg(graph, indeg);
    Queue<Integer> q = new LinkedList<>();
    for (int i=0; i<indeg.length; i++) {
        if (indeg[i] == 0) {
            q.add(i);
        }
    }
    // BFS
    while (!q.isEmpty()) {
        int cur = q.remove();
        System.out.print(cur + " ");
        topological sort → print
        for (int i=0; i<graph[cur].size(); i++) {
    }
}

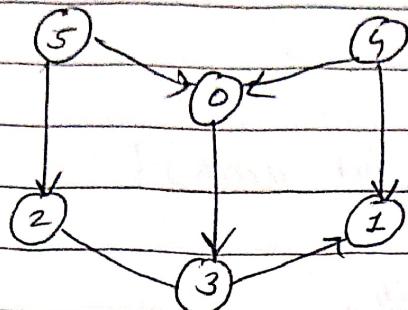
```

```

public static void calDeg(ArrayList<Edge> graph, int indeg[]) {
    for (int i=0; i<graph.length; i++) {
        int v = i;
        for (int j=0; j<graph[v].size(); j++) {
            Edge e = graph[v].get(j);
            indeg[e.dest]++;
        }
    }
}

```

g. All paths from source to target :



$src = 5, dest = 1$

o/p : 5 0 3 1

5 2 3 1

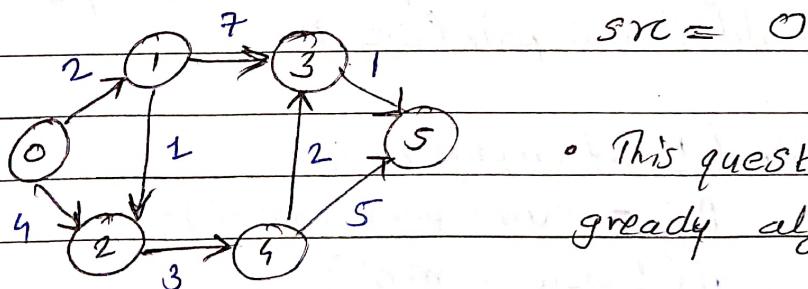
$O(V^V)$

```
public static void printAllPath (graph, src, dest, path) {
    if( src == dest ) {
        System.out.println (path + dest);
        return;
    }
    for( int i=0; i<graph[src].size(); i++ ) {
        Edge e = graph[src].get(i);
        printAllPath (graph, e.dest, dest, path+src);
    }
}
```

g Dijkstra's algorithm : (weighted graph)

- shortest paths from the source to all vertices

o ex :



This question base on greedy algorithm

ans	0 2 3 8 6 9
	0 1 2 3 4 5

- This logic same for directed & undirected graph.
- ~~Dijkstra (dijkstra algo)~~

DATE

--	--	--	--	--	--	--

// code4 static class pair implements Comparable<Pair> {

int n;

int path;

public pair(int n, int path) {

this.n = n;

this.path = path;

}

@Override

public int compareTo(Pair p2) {

return this.path - p2.path;

}

}

public static void dijkstra(graph, int src) {

int dist[] = new int[graph.length];

also use

inbuilt

function

for (int i=0; i < graph.length; i++) {

if (i != src) {

dist[i] = Integer.MAX_VALUE;

Arrays.fill()

}

boolean visit[] = new boolean[graph.length];

PriorityQueue<Pair> pq = new PriorityQueue<>();

pq.add(new pair(src, 0));

while (!pq.isEmpty()) {

Pair curr = pq.remove();

if (!visit[curr.n]) {

visit[curr.n] = true;

for (int i=0; i < graph[curr.n].size(); i++) {

Edge e = graph[curr.n].get(i);

```
int u = e.src;
int v = e.dest;
int wt = e.wt;
```

```

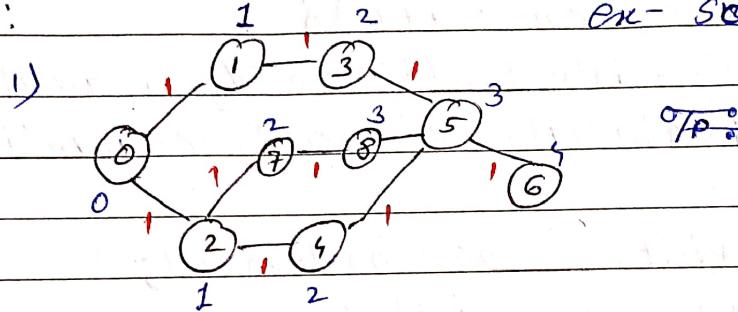
if (dist[u] + wt < dist[v]) {
    dist[v] = dist[u] + wt;
    pq.add(new pair(v, dist[v]));
}

```

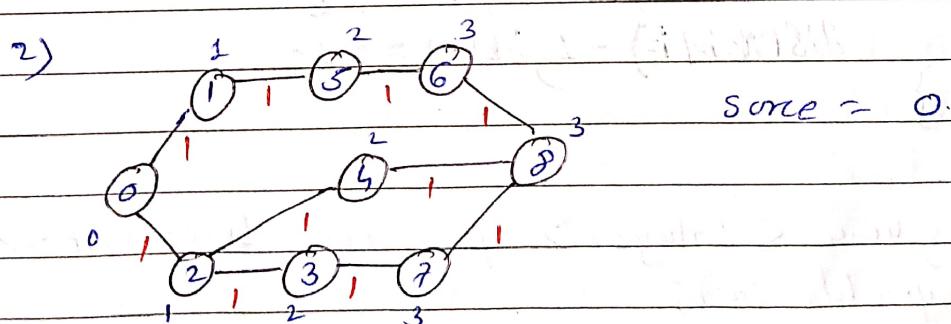
A handwritten musical score on lined paper. It consists of two staves. The top staff has four measures, each starting with a C-clef and a common time signature. The bottom staff has three measures, each starting with a G-clef and a common time signature. The notes are represented by vertical stems with small horizontal dashes above them, indicating pitch. Measures are separated by vertical bar lines. There are two large, curly brace-like symbols: one spanning the first two measures of the top staff and another spanning the first two measures of the bottom staff.

g. Shortest path in Undirected graph from Source:

$$en: \quad \begin{matrix} 1 & 2 & \dots \end{matrix} \quad ex - source = 0.$$



O/P :- 0 1 1 2 2 3 3 2 3



$\%_P$: [0] 1 | 1 | 2 [2 | 2] 3 | 3. | 3 |

traverse level wise (use BFS) .

approach :

- 1) Create distance array array to stored distance from source to vertex/node. & its initialise by -1 & apply BFS.

//code //

```

public static int[] shortestPath(int[][] arr, int n,
                                int m, int src) {
    ArrayList<Edge> graph = new ArrayList[n];
    for (int i=0; i<n; i++) {
        graph[i] = new ArrayList();
    }
    // create graph // length of 2D matrix
    for (int i=0; i<m; i++) {
        graph[arr[i][0]].add(new Edge(i, arr[i][1]));
        graph[arr[i][1]].add(new Edge(i, arr[i][0]));
    }
    boolean visit[] = new boolean[n];
    int dist[] = new int[n];
    // initialise by -1 //
    for (int i=0; i<n; i++) {
        if (src != i) dist[i] = -1;
    }
    queue < Integer > q = new LinkedList<>();
    dist[src] = 0;
    q.add(src);
    visit[src] = true;
}

```

```

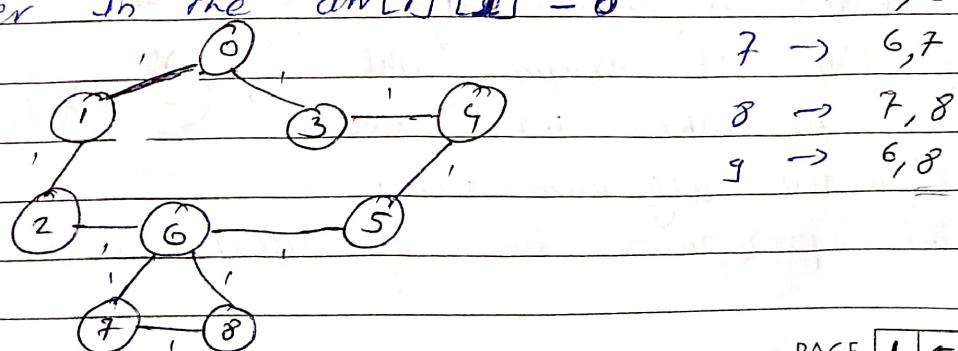
while(!q.isEmpty()) {
    int curr = q.remove();
    for(int i=0; i<graph[curr].size(); i++) {
        Edge e = graph[curr].get(i);
        if(!visit[e.dest]) {
            visit[e.dest] = true;
            q.add(e.dest);
            dist[e.dest] = dist[curr] + 1;
        }
    }
}
return dist;
}

```

Note: when input 2D array & you convert it
graph/connect edge. (Undirected graph):

arr = [[0,1], [0,3], [3,4], [4,5], [5,6], [1,2], [2,6],
[6,7], [7,8], [6,8]]:

- arr[i][0] → are the index/node of graph.
- arr[i][1] → are the data of arr[i][0]th index.
- size of graph/edge is max number in the arr[i][1] = 8



Un-
directed
graph.

```
for( int i=0; i< arr.length; i++ ) {
    graph[ arr[i][0] ].add( arr[i][1] );
    graph[ arr[i][1] ].add( arr[i][0] );
}
```

0	1	2	3	4	5	6	7	8
1	0	1	0	3	5	5	6	7
3	2	6	4	5	6	2	8	6
						7		8

If edge class
Present:

```
for( int i=0; i< arr.length; i++ ) {
    graph[ arr[i][0] ].add( new Edge( arr[i][0], arr[i][1], 1 ) );
    graph[ arr[i][1] ].add( new Edge( arr[i][1], arr[i][0], 1 ) );
}
```

dir-
cted
graph

```
for( int i=0; i< arr.length; i++ ) {
    graph[ arr[i][0] ].add( arr[i][1] );
}
```

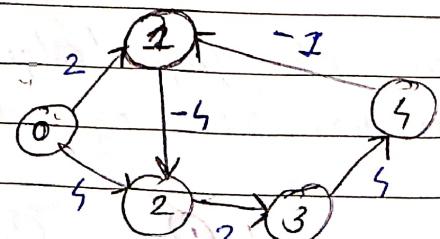
g. Bellman Ford algorithm:

- Shortest paths from the source to all vertices (negative edge).

- Dijkstra's algorithm only positive wt graph & but this fail when wt is -ve

Dijkstra's algorithm fail.

- This problem solve by Bellman Ford algorithm.



for all edge (u, v) :

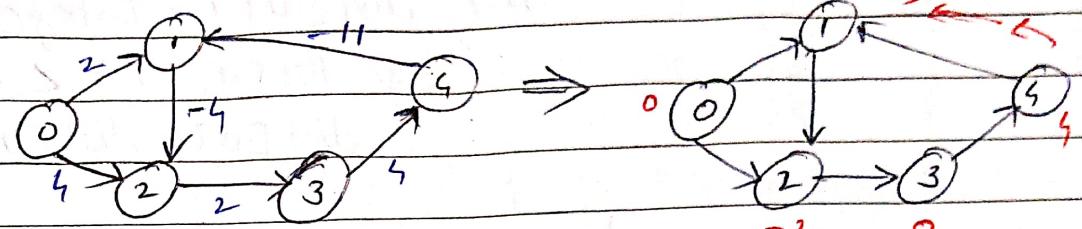
```
if ( dist[u] + wt(u, v) < dist[v] ) {
```

```
    dist[v] = dist[u] + wt(u, v);
```

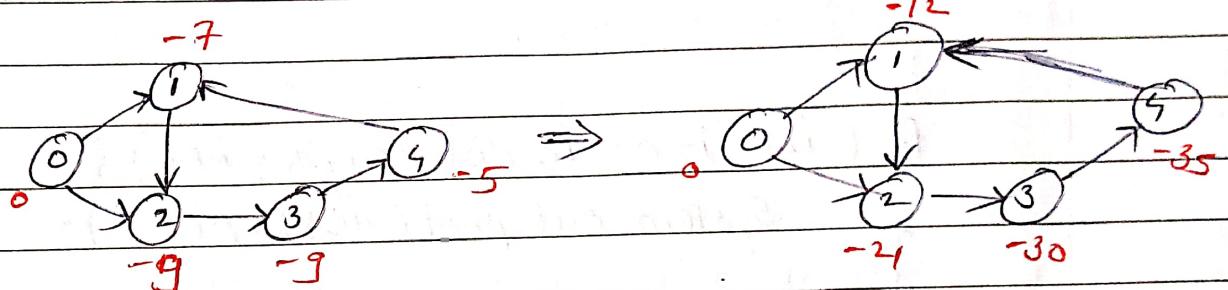
} perform this
operation
 $v-1$ times.

Note: this algorithm doesn't work for -ve wt. graph cyclic graph.

ex:



second iteration.



- this loop is continuous run.

```
//code11 public static void bellmanford (graph, int src) {
    int dist[] = new int[graph.length];
    for (int i=0; i<dist.length; i++) {
        if (i != src) {
            dist[i] = Integer.MAX_VALUE;
        }
    }
    int v = graph.length;
    for (int i=0; i<v-1; i++) { - // O(v)
        // edge - O(E) //
        for (int j=0; j<graph.length; j++) {
            for (int k=0; k<graph[i].size(); k++)

```

Edge e = graph[i].get(k);

int u = e.src;

int v = e.dest;

int wt = e.wt;

// relaxation //

if (dist[u] == Integer.MAX_VALUE

&& dist[u] + wt < dist[v]) {

dist[v] = dist[u] + wt;

}

}

for (int i=0; i<dist.length; i++) {

System.out.print(dist[i] + " ");

}

System.out.println();

}

O/P : 0 2 -2 0 5

// another method //

public static void bellmanFord(graph, int src, int v) {

int dist[] = new int[v];

for (int i=0; i<dist.length; i++) {

if (i != src) {

dist[i] = Integer.MAX_VALUE;

}

}

```

for( int i=0; i< v-1; i++){
    // edge || O(E)
    for( int j=0; j< graph.size(); j++){
        Edge e = graph.get(i);
        int u= e.src;
        int v = e.dest;
        int wt = e.wt;
        // relaxation ||
        if( dist[u] != Integer.MAX_VALUE
            && dist[u]+wt < dist[v]){
            dist[v] = dist[u]+wt;
        }
    }
    // print ||
    for( int i=0 ; i< dist.length; i++){
        System.out.print(dist[i] + " ");
    }
    System.out.println();
}

public static void main( String args[]){
    int v= 5;
    ArrayList <Edge> edges = new ArrayList <>();
    // create a edge graph || call BellmanFord
}
}

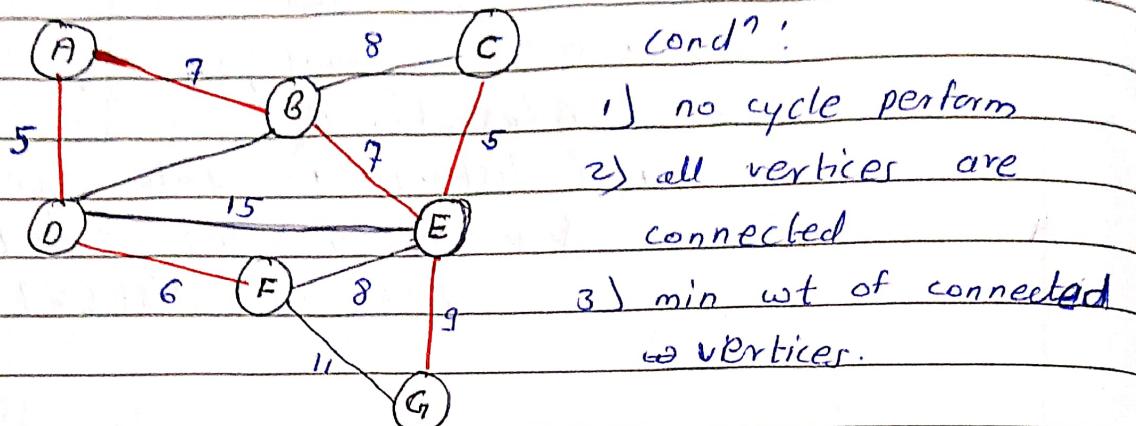
public static void createGraph( ArrayList <Edge> graph){
    graph.add( new Edge( 0,1,2));
    graph.add( new Edge( 0,2,4));
    graph.add( new Edge( 1,2,-4));
    graph.add( new Edge( 2,3,2));
    graph.add( new Edge( 3,4,4));
    graph.add( new Edge( 4,1,-1));
}

```

classmate

- * Minimum Spanning Tree (MST) :
- It is the subset of edges-weighted undirected graph that connects all the vertices together without any cycles and with the minimum possible total edge weight.

Ex:



g. Prim's algorithm

- find the min cost of MST

approach: create pair & store it vertices & cost

// code // static class Pair implements Comparable<Pair> {

int vertex;

int cost;

public Pair(int v, int c){

vertex = v;

cost = c;

}

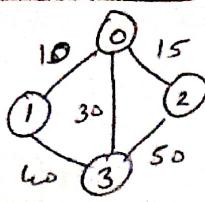
@Override

public int compareTo(Pair p2){

return this.cost - p2.cost;

}

}



DATE: _____

```

public static void mstCost(ArrayList<Edge> graph[]){
    boolean visit[] = new boolean[graph.length];
    Priority Queue<Pair> pq = new Priority Queue<>();
    pq.add(new Pair(0, 0));
    int totalCost = 0;

    while (!pq.isEmpty()) {
        Pair curr = pq.remove();
        if (!visit[curr.vertex]) {
            visit[curr.vertex] = true;
            totalCost += curr.cost;

            for (int i = 0; i < graph[curr.vertex].size(); i++) {
                Edge e = graph[curr.vertex].get(i);
                pq.add(new Pair(e.dest, e.wt));
            }
        }
    }

    System.out.println("final cost of MST = " + totalCost);
}

```

O/P : final cost of MST = 55.

g) Corona Spread

- find the time of hospital when corona virus is spread in all patient.

Ex:	1	2	1	1	0	1
	1	1	0	1	1	2
	0	1	0	2	1	1
	1	1	0	1	0	1
	1	0	1	2	0	1

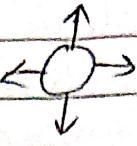
0 - Empty room

1 - normal patient

2 - corona patient

Convoluted spread in 4 directions

- in 1 unit - each covid patient spread corona near by there



1	2	2	1	0	2		2	2	2	2	0	2
1	2	0	2	2	2		2	2	0	2	2	2
0	1	0	2	2	2		0	2	0	2	2	2
1	1	0	2	0	1		1	1	0	2	0	2
1	0	2	2	0	1		1	0	2	2	0	1

14

ans = Unit 5

- This question solve by BFS.

11) code for static int arr;

Static int c;

Static class Pair {

int St;

int ed.

Pair (int r, int c) {

$$St = \gamma$$

$$ed = c^{\circ}$$

})

{

```
public static boolean valid (int i, int j){
```

return i < r && j > 0 && j < c && j > o;

1

```
public static int covid5pread( int [ ] [ ] hosp ) {
```

r = hosp. length?

c = hosp[0].length;

```
queue<Pair> q = new LinkedList<>();
```

```

for (int i=0; i<r; i++) {
    for (int j=0; j<c; j++) {
        if (hosp[i][j] == 2) {
            q.add(new Pair(i, j));
        }
    }
}
if (q.isEmpty()) return 0;

int time = 0;
while (!q.isEmpty()) {
    time++;
    int currPatient = q.size();

    while (currPatient > 0) {
        Pair curr = q.remove();
        int i = curr.st;
        int j = curr.ed;

        int row[] = {-1, 1, 0, 0};
        int col[] = {0, 0, -1, 1};

        for (int k=0; k<4; k++) {
            int newR = i + row[k];
            int newC = j + col[k];
            if (valid(newR, newC) &&
                hosp[newR][newC] == 1) {
                hosp[newR][newC] = 2;
                q.add(new Pair(newR, newC));
            }
        }
        currPatient--;
    }
}

```

```
for (int i=0; i<r; i++) {
    for (int j=0; j<c; j++) {
        if (hasp[i][j] == 1) {
            return -1;
        }
    }
}
return time-1;
}
```

g. find the number of Island :

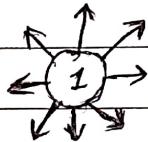
ex:

1	1	1	0	1	1
0	1	1	0	0	1
1	0	0	0	0	0
1	0	1	0	1	1
1	1	0	0	1	1

condn:

- if 1-1 near each other then there are one island

total island = 3.



Note: In this question check 8 cond' for checking near 1-1

//code//

```
static int r, c;
static class Pair {
    int row;
    int col;
    Pair (int r, int c) {
        row = r;
        col = c;
    }
}
```

```
public static boolean valid (int rn, int cn) {
    return rn < r && rn >= 0 && cn < c && cn >= 0;
}
```

```

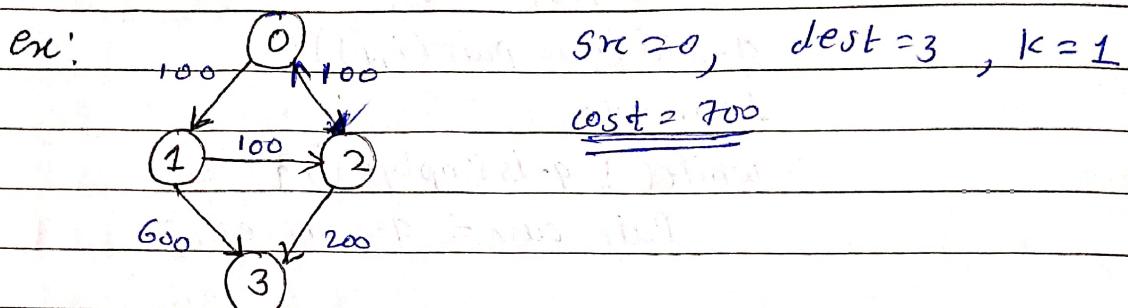
public static int findIsland( int [][] land ) {
    r = land.length;
    c = land[0].length;
    boolean [][] visit = new boolean [r][c];
    Queue<Pair> q = new Queue<r>[c];
    int lNum = 0;

    for( int i=0; i < r; i++ ) {
        for( int j=0; j < c; j++ ) {
            if( !visit[i][j] && land[i][j] == 1 ) {
                visit[i][j] = true;
                q.add( new Pair(i,j) );
                lNum++;
                while( !q.isEmpty() ) {
                    Pair curr = q.remove();
                    int n = curr.row;
                    int m = curr.col;
                    int newR[] = { 0, 0, 1, 1, 1, -1, -1, -1 };
                    int newC[] = { 1, -1, 1, -1, 0, 1, 0, -1 };
                    // Check only condn near 1-2 //
                    for( int k=0; k < 8; k++ ) {
                        if( valid( n+newR[k], m+newC[k] ) &&
                            !visit[n+newR[k]][m+newC[k]] ) {
                            visit[n+newR[k]][m+newC[k]] = true;
                            q.add( new Pair(n+newR[k], m+newC[k]) );
                        }
                    }
                }
            }
        }
    }
    return lNum;
}

```

g. Cheapest flights within k stops

- There are n cities connected by some number of flights. You are given an array flights where $\text{flights}[i] = [\text{from}, \text{to}, \text{price}]$ indicates that there is a flight.
- You are also given three integer src , dest & k . Return the cheapest price from src to dest with at most k stops. If there is no such route, return -1 ; (all values are true).



// code // public static int cheapestFlight(int n, int flight[][], int src, int dest, int k){

ArrayList<Edge> graph[] = new ArrayList<>[n];
createGraph(flight, graph);

```
int dist[] = new int[n];
for (int i = 0; i < n; i++) {
    if (i != src) {
        dist[i] = Integer.MAX_VALUE;
    }
}
```

Queue<Info> q = new LinkedList<>();
q.add(new Info(src, 0, 0));

```
while (!q.isEmpty()) {
    Info curr = q.remove();
    if (curr.stops > 10) {
        break;
    }
    for (int i=0; i<graph[curr.v].size(); i++) {
        Edge e = graph[curr.v].get(i);
        int u = e.src;
        int v = e.dest;
        int wt = e.wt;
        if (curr.cost + wt < dist[v] && curr.stops <= 10) {
            dist[v] = curr.cost + wt;
            q.add(new Info(v, dist[v], curr.stops+1));
        }
    }
    if (dist[dest] == Integer.MAX_VALUE) {
        return -1;
    } else {
        return dist[dest];
    }
}

static class Info {
    int v, cost, stops;
    public Info (int v, int c, int s) {
        this.v = v;
        cost = c;
        stops = s;
    }
}
```

g. Connecting cities :

- find the minimum cost of connecting all cities on the map (MST).

ex: cities [][] = {{0, 1, 2, 3, 4},

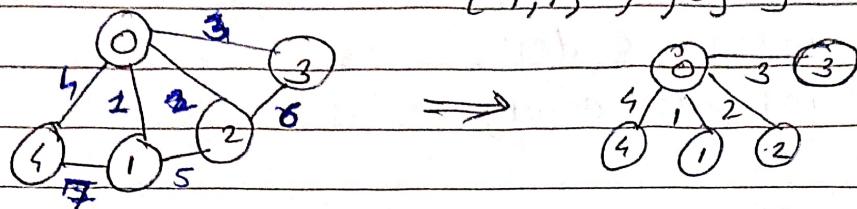
{1, 0, 5, 0, 7},

{2, 5, 0, 6, 0},

{3, 0, 6, 0, 0},

{4, 7, 0, 0, 0}}

ans = 10



- for this question use queue

- only store edge cost & dest.

// code // static class Edge implements Comparable<Edge> {

int dest;

int cost;

public Edge (int d, int c) {

this.dest = d;

this.cost = c;

}

@Override

public int compareTo(Edge e2) {

return this.cost - e2.cost;

}

}

public static int connectingCities (int cities [][]){

PriorityQueue<Edge> pq = new PriorityQueue();

boolean [] visit = new boolean [cities.length];

pq.add (new Edge (0,0));

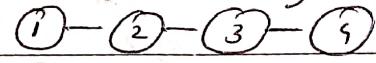
int finalCost = 0;

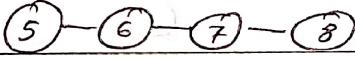
```
while (!pq.isEmpty()) {
    Edge curr = pq.remove();
    if (!visit[curr.dest]) {
        visit[curr.dest] = true;
        finalCost += curr.cost;

        for (int i=0; i<cities[curr.dest].length; i++) {
            if (cities[curr.dest][i] != 0) {
                pq.add(new Edge(i, cities[curr.dest][i]));
            }
        }
    }
}
return finalCost;
}
```

* Disjoint set DS : (Union)

- In this two operation find & Union.

Ex: set(1) = 

set(2) = 

Union of 4 & 8 : $\text{Union}(4, 8) = \{1-2-3-4\} \cup \{5-6-7-8\}$ } one set.

operation :

$\text{find}(2) = \text{ans: set1}$ } before $\text{Union}(4, 8)$

$\text{find}(6) = \text{ans: set2}$

$\text{find}(2) = \text{ans: set1}$

$\text{find}(6) = \text{ans: set1}$

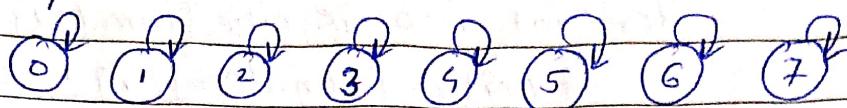
- Implementation (Optimized):

Parent + Union by rank

ex: $n=8$.

	0	1	2	3	4	5	6	7
par =	0	1	2	3	4	5	6	7

initially par node is parent itself.



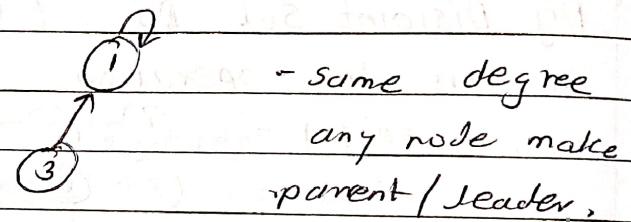
rank =	0	0	0	0	0	0	0	0
	0	1	2	3	4	5	6	7

initially rank is zero of all node.

- find() - this method is use to find parent of a given node.
- Union() - it is use to join two groups

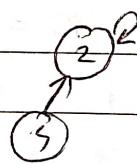
for example some operation :

1) Union (1,3) :

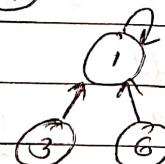


$O(4k^2)$ find(3) - op: 1 - o/p is leader.

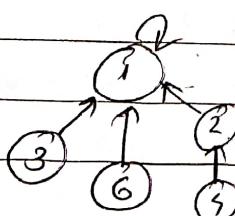
$O(4k^3)$ Union (2,4) -



3) Union(3,6) -

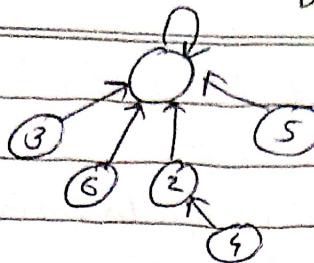


5) Union (1,5) -



6) find(4) - 1

7) Union (1,5) -



Par =	0 1 1 1 1 1 1 1 7
rank =	0 2 1 0 0 0 0 0 0
	0 1 2 3 4 5 6 7

```

//code1
static int n=7;
static int par[] = new int[n];
static int rank[] = new int[n];
public void static void init() {
    for( int i=0; i<n; i++ ){
        par[i] = i;
    }
}
public static int find( int x ) {
    if( x == par[x] ) {
        return x;
    }
    return par[x] = find( par[x] );
}
public static void union( int a, int b ) {
    int parA = find(a);
    int parB = find(b);
    if( rank[parA] == rank[parB] ){
        par[parB] = parA; rank[parA]++;
    } else if( rank[parA] < rank[parB] ){
        par[parA] = parB;
    } else {
        par[parB] = parA;
    }
}

```

```

public static void main (String [] args) {
    init ();
    System.out.println (find (3));
    Union (1, 3);
    System.out.println (find (3));
    Union (2, 4);
    Union (3, 6);
    Union (1, 4);
    System.out.println (find (3));
    System.out.println (find (4));
    Union (1, 5);
}

```

O/P: 3 1 1 1 - (in next line).

g. Kruskal algorithm : (MST Greedy), $O(V + E \log E)$
 - find min cost of src to dest.

Model Static class Edge implements Comparable<Edge>{
 int src;
 int dest;
 int wt;
 public Edge (int s, int d, int w) {
 src = s;
 dest = d;
 wt = w;
 }
 @Override
 public int compareTo (Edge e2) {
 return this.wt - e2.wt;
 }
}

```

public static void createGraph(ArrayList<Edge> edge)
    edge.add(new Edge(0, 1, 10));
    edge.add(new Edge(0, 2, 15));
    edge.add(new Edge(0, 3, 30));
    edge.add(new Edge(1, 3, 40));
    edge.add(new Edge(2, 3, 50));
}

```

Static int n = 4;

Static int par[] = new int[n];

Static int rank[] = new int[n];

```

public static void kruskalAlg (ArrayList<Edge> edge
                                int v) {

```

collection.sort(edge); // O(E log E)

int cost = 0;

```

for(i=0; count < v-1; i++) { // O(V)

```

Edge e = edge.get(i);

// src, dest, wt //

int parA = find(e.src);

int parB = find(e.dest);

if(parA != parB) {

union(e.src; e.dest);

cost += e.wt;

count++;

}

System.out.println("min cost : " + cost);

}

Imp 0 Create graph from 2D matrix.

ex:

```
matrix [][] = { { 0, 1, 1, 0 },
                { 1, 0, 0, 1 },
                { 1, 0, 0, 1 },
                { 0, 1, 1, 0 } };
```

	0	1	2	3
0	0	1	1	0
1	1	0	0	1
2	1	0	0	1
3	0	1	1	0

• if i & j are vertices

& $\text{matrix}[i][j] = \text{value}$

hence value is wt of

edge bet i & j vertices.

edge

graph:

```
ArrayList<Edge> graph = new ArrayList<>();
for( int i=0; i<matrix.length; i++ ) {
    for( int j=0; j<matrix[i].length; j++ ) {
        if( matrix[i][j] != 0 ) {
            graph.add( new Edge( i, j, matrix[i][j] ) );
        }
    }
}
```

```
* ArrayList<Edge> graph[] = new ArrayList[3];
for( int i=0; i<matrix.length; i++ ) {
    for( int j=0; j<matrix[i].length; j++ ) {
        if( matrix[i][j] != 0 ) {
            graph[i].add( new Edge( i, j, matrix[i][j] ) );
        }
    }
}
```

* Flood fill Algorithm:

- Fill the color in the image. Image is given in the form of grid [T][C].
- :- 1 - pixel present
:- 0 - pixel not present.

Ex: $\text{image} = \begin{bmatrix} 1, 1, 1 \\ 1, 1, 0 \\ 1, 0, 1 \end{bmatrix}$, $sr = 1$, $sc = 1$, $\text{color} = 2$.

O/P : $\text{image} = \begin{bmatrix} 2, 2, 2 \\ 2, 2, 0 \\ 2, 0, 1 \end{bmatrix}$

```
//code11 public static void helper ( int [] [ ] img , int sr , int sc ,
                                int color , visit , int orgCol ) {
    if ( sr < 0 || sc < 0 || sr > = img . length || sc > = img [ 0 ] . length || visit [ sr ] [ sc ] || img [ sr ] [ sc ] != orgCol )
        return ;
    }
    img [ sr ] [ sc ] = color;
    // left
    helper ( img , sr , sc - 1 , color , visit , orgCol );
    // right
    helper ( img , sr , sc + 1 , color , visit , orgCol );
    // up
    helper ( img , sr - 1 , sc , color , visit , orgCol );
    // down
    helper ( img , sr + 1 , sc , color , visit , orgCol );
}
```

```

public static int[][] floodFill(int[][] img, int sr,
                                int sc, int color) {
    boolean visit[][] = new boolean[img.length]
                           [img[0].length];
    helper(img, sr, sc, color, visit, img[sr][sc]);
    return img;
}

```

Q - 1 Floyd warshall Algorithm :

```

// code1 public void shortestPath(int [][] matrix) {
    int n = matrix.length;
    for( int i=0; i<n; i++ ) {
        for( int j=0; j<n; j++ ) {
            if( matrix[i][j] == -1 ) {
                matrix[i][j] = Integer.MAX_VALUE;
            }
        }
    }
    for( int k=0; k<n; k++ ) {
        for( int i=0; i<n; i++ ) {
            for( int j=0; j<n; j++ ) {
                if( matrix[i][k] == Integer.MAX_VALUE )
                    matrix[k][j] == Integer.MAX_VALUE );
                continue;
            }
            matrix[i][j] = Math.min( matrix[i][j],
                                    matrix[i][k] + matrix[k][j] );
        }
    }
}

```

```

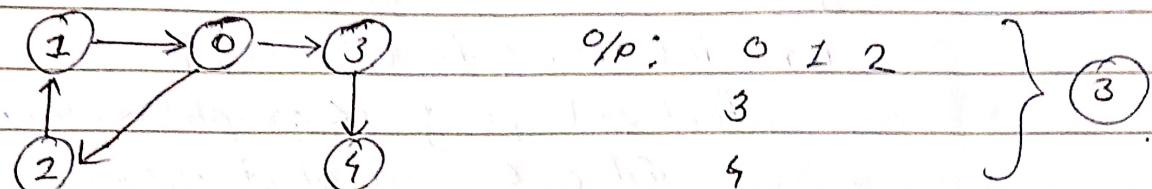
for (int i=0; i<n; i++) {
    for (int j=0; j<n; j++) {
        if (matrix[i][j] == Integer.MAX_VALUE) {
            matrix[i][j] = -1;
        }
    }
}
return matrix;
}

```

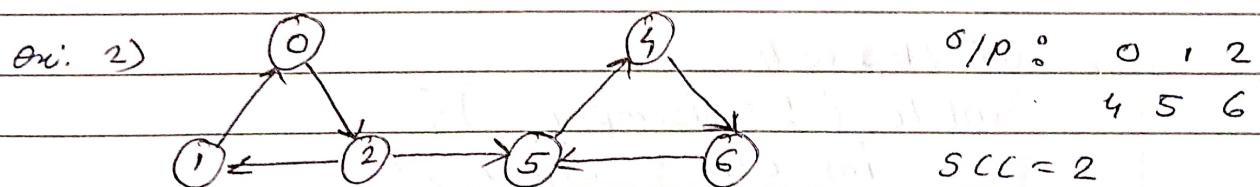
Q) Strongly connected component : (SCC) (Kosaraju).

- SCC is a component in which we can reach every vertex of the component from every other vertex in that component.

ex: 1)



- which vertex is maximum reach ~~to~~ other vertex but maximum number of SCC



approach: Use Kosaraju's Algorithm:

- 1) get nodes in stack (topological sort).
- 2) Transpose the graph.
- 3) do the DFS according to stack nodes on the transpose graph

```

// code11 public static void KosarajuAlgo(graph, int v) {
    // Step 1 //
    boolean visit[] = new boolean[v];
    Stack<Integer> s = new Stack<>();
    for( int i=0; i<v; i++ ) {
        if(!visit[i]) {
            (topSortUBI  
function.) → topSort( graph, i, visit, s );
        }
    }

    // Step 2 //
    ArrayList<Edge> transpose[] = new ArrayList[v];
    for( int i=0; i<graph.length; i++ ) {
        initialise → transpose[i] = new ArrayList();
        visit[i] = false;
    }

    for( int i=0; i<v; i++ ) {
        for( int j=0; j<graph[i].length; j++ ) {
            Edge e = graph[i].get(j);
            transpose[e.dest].add(new Edge(e.dest, e.src));
        }
    }

    // Step 3 //
    while( !s.isEmpty() ) {
        int cur = s.pop();
        if( !visit[cur] ) {
            System.out.print(" SCC: ");
            dfs(transpose, cur, visit);
            System.out.println();
        }
    }
}

```

CLASSMATE PAGE 174

Q. Bridge in graph : (Tarjan Algorithm)

- Bridge is an edge whose deletion increase the graph number of connected components.

Model public static void dfs(graph, int curr, int par, int dt[],
int low[], boolean visit[], int time)

visit[curr] = true;

dt[curr] = low[curr] = ++time;

for(int i=0; i<graph[curr].size(); i++) {

Edge e = graph[curr].get(i);

int nei = e.dest;

if(nei == par) {

continue;

} else if(!visit[nei]) {

dfs(graph, nei, curr, dt, low, visit, time);

low[curr] = Math.min(low[curr], low[nei]);

if(dt[curr] < low[nei]) {

System.out.println("Bridge: " + curr +

" ---- " + nei);

} else {

low[curr] = Math.min(low[curr], dt[nei]);

}

}

public static void tarjanBridge(graph, int v) {

int dt[] = new int[v]; int low[] = new int[v];

int time = 0; boolean visit[] = new boolean[v];

for(int i=0; i<v; i++) {

if(!visit[i]) {

classmate } dfs(graph, i, -1, dt, low, visit, time); } } } }

9. Articulation Point : (Tarjan's Algorithm)

```

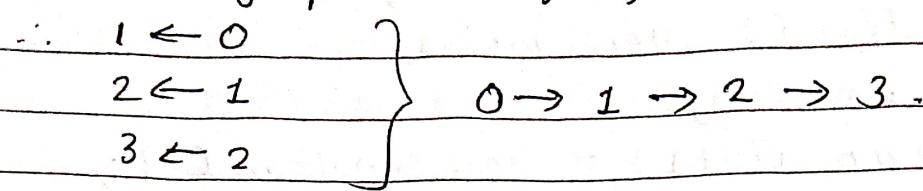
// Code // public static void dfs(graph, int curv, int par, int dt[])
    int low[], int time, boolean visit[], boolean ap[]);
    visit[curv] = true;
    dt[curv] = low[curv] = ++time;
    int children = 0;
    for (int i=0; i<graph[curv].size(); i++) {
        Edge e = graph[curv].get(i);
        int nei = e.dest;
        if (par == nei) {
            continue;
        } else if (visit[nei]) {
            low[curv] = Math.min(low[curv], dt[nei]);
        } else {
            dfs(graph, nei, curv, dt, low, time, visit, ap);
            low[curv] = Math.min(low[curv], low[nei]);
            if (par != -1 && dt[curv] <= low[nei]) {
                ap[curv] = true;
            }
            children++;
        }
    }
    if (par == -1 && children > 1) {
        ap[curv] = true;
    }
}

```

```
public static void getAP (graph, int v) {  
    int dt [] = new int [v];  
    int low [] = new int [v];  
    int time = 0;  
    boolean visit [] = new boolean [v],  
    boolean ap [] = new boolean [v];  
  
    for( int i=0 ; i<v ; i++ ) {  
        if ( !visit [i] ) {  
            dfs ( graph, i, -1, dt, low, time, visit, ap );  
        }  
    }  
    // print all Aps.  
    for( int i=0 ; i<v ; i++ ) {  
        if ( ap[i] ) {  
            System.out.println ("AP: " + i);  
        }  
    }  
}
```

9

Preq Pre-requisite Tasks

ex \Rightarrow graph = [[0, 1], [2, 1], [3, 2]].

• approach :

- create adjacency list (graph).
- apply topological sort by Kahn's algorithm
- if all count vertex, if count is equal to no. of task then return true otherwise false.

// code11 public static boolean isPossible (int N, int P,
int [][] prerequisites) {

// N - no. of tasks, P - pairs //

// create adjacency list //

List<Integer> graph [] = new ArrayList[N];

for (int i=0; i < N; i++) {

graph[i] = new ArrayList();

int indeg [] = new int[N];

for (int i=0; i < P; i++) {

graph[prerequisites[i][1]].add(prerequisites[i][0]);

indeg[prerequisites[i][0]]++;

}

// Kahn's algorithm //

queue<Integer> q = new LinkedList();

for (int i=0; i < N; i++) {

if (indeg[i] == 0) {

q.add(i);

}

}

int count=0;

```

while(!q.isEmpty()){
    int curv = q.remove();
    count++;
    for( int i=0; i<graph[curv].size(); i++ ){
        int ele = graph[curv].get(i);
        indeg[ele] -= 1;
        if( indeg[ele] == 0 ){
            q.add(ele);
        }
    }
}
return count == N;
}

```

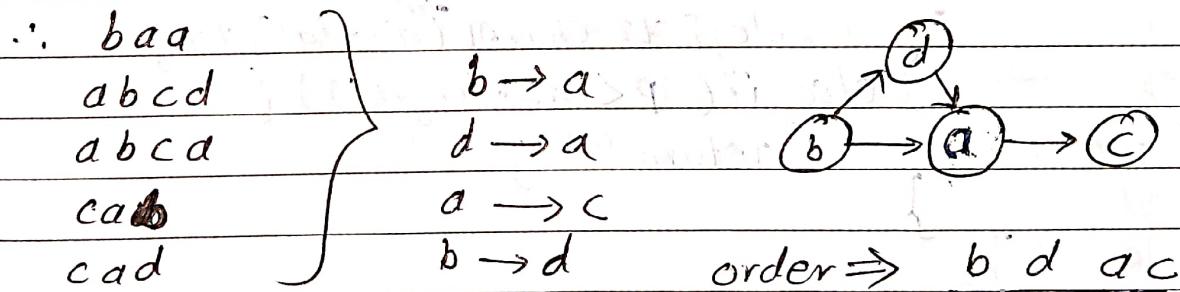
Q. Alien Dictionary : // dry run //

- find the order of character given string.

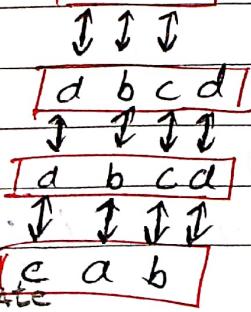
ex: human dictory order

- a, b, c, d ...

ex: dict[] = {"baa", "abcd", "caab", "cad", "abcad"};



compare b a d



classmate

```

for( int i=0; i<dict.length; i++ ){
    String st1 = dict[i];
    String st2 = dict[i+1];
    int j=0, k=0;
    while( j<st1.length && k<st2.length ) {
        if( st1[j] != st2[k] )
            break;
        j++; k++;
    }
    if( j == st1.length )
        System.out.println("order");
    else
        System.out.println("not order");
}

```

```

// code 11 public String findOrder(String[] dict, int n, int k) {
    // create adjacency list //
    ArrayList<Integer> adj[] = new ArrayList[k];
    for (int i=0; i<k; i++) {
        adj[i] = new ArrayList();
    }
    int indeg[] = new int[k];
    // stored "a"=0, "b'=1, 'c'=2, ... so on //
    for (int i=0; i<n-1; i++) {
        String st1 = dict[i];
        String st2 = dict[i+1];
        int p=0, q=0;
        while (p<st1.length() && q<st2.length() &&
               st1[p] == st2[q]) {
            p++; q++;
        }
        if (p<st1.length() && q<st2.length()) {
            adj[st1.charAt(p)].add(st2.charAt(q)-'a');
            indeg[st2.charAt(q)-'a']++;
        } else if (p<st1.length()) {
            return "";
        }
    }
}

```

meaning. → } else if (p < st1.length()) {
 $k \geq st2.length.$ } return "";

ex: abcd
 abc } }

```

// Kahn's algorithm //
Queue<Integer> q = new LinkedList<>();
for (int ele : indeg) {
    if (ele == 0) q.add(ele);
    for (int i=0; i<k; i++) {
        if (indeg[i] == 0) q.add(i);
    }
}

```

```

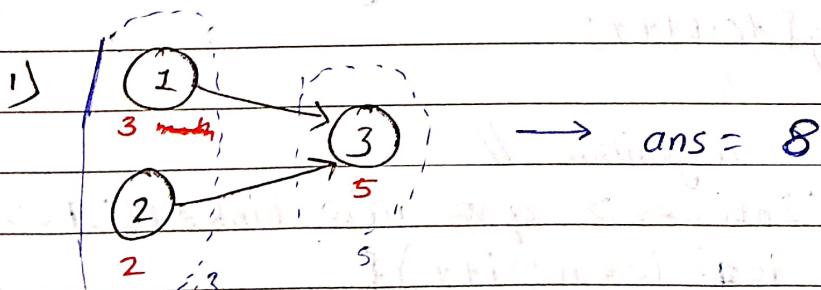
StringBuilde st = new StringBuilde("");
while( !q.isEmpty() ) {
    int cur = q.remove();
    char ch = (char) ('a') + cur;
    st.append(st);
}

for( int i = 0; i < adj[cur].size(); i++ ) {
    int ele = adj[cur].get(i);
    indeg[ele]--;
    if( indeg[ele] == 0 ) {
        q.add(ele);
    }
}
if( st.length() < k ) { → cycle condn.
    return "";
}
return st.toString();
}

```

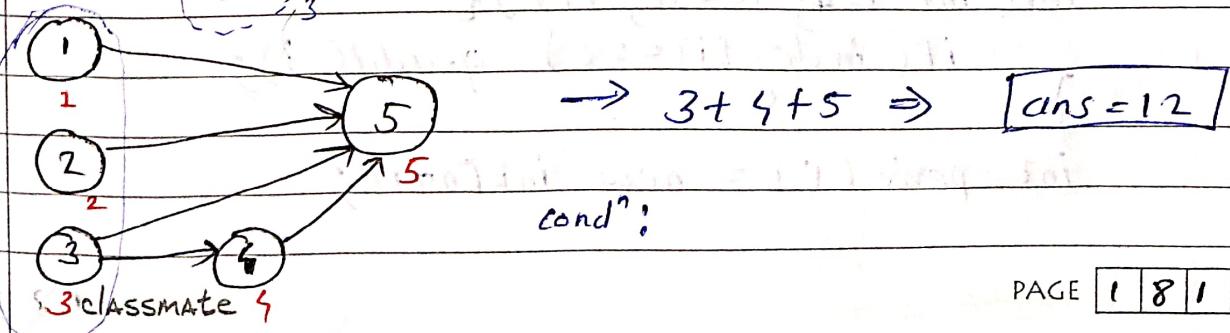
g. Parallel course III : (Leetcode ~~easy~~)

ex:



$$\rightarrow 3 + 4 + 5 \Rightarrow \boxed{\text{ans} = 12}$$

condn:



approach: create adj. list & apply topological sort (kann's algo).

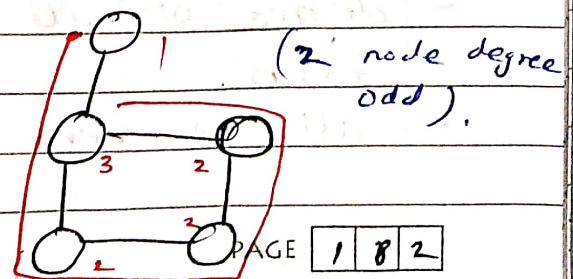
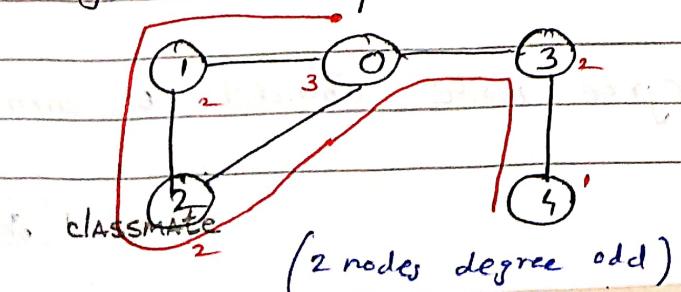
DATE 13 10 2024

```
// code11 class Edge {  
    int src, dest, swt;  
    Edge (int s, int d, int w){  
        src = s; dest = d; swt = w;  
    }  
}  
  
public int minimumTime (int n, int [][] relations, int [] time)  
// create adjacency list //  
int newTime [] = new int [n+1];  
for( int i=0; i<n; i++) {  
    newTime [i+1] = time[i];  
}  
  
ArrayList <Edge> graph [] = new ArrayList <>();  
for( int i=0; i<=n; i++) {  
    graph [i] = new ArrayList();  
}  
  
int indeg [] = new int [n+1];  
for( int i=0; i< relations.length; i++) {  
    int src = relations [i][0],  
    int dest = relations [i][1],  
    int swt = newTime [src];  
    graph [src].add (new Edge (src, dest, swt));  
    indeg [dest]++;  
}  
  
// kann's algorithm //  
Queue <Integer> q = new LinkedList <>();  
for( int i=0; i<=n; i++) {  
    if( indeg [i] == 0) q.add (i);  
}  
  
int period [] = new int [n+1],
```

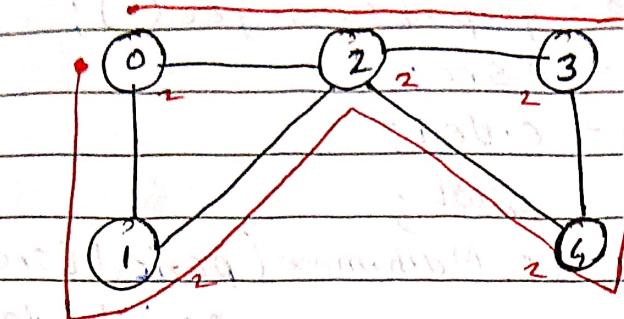
```

while (! q.isEmpty()) {
    int curv = q.remove();
    for (int i = 0; graph[curv].size() > i; i++) {
        Edge e = graph[curv].get(i);
        int src = e.src;
        int dest = e.dest;
        int swt = e.swt;
        period[dest] = Math.max(period[src] + swt,
                               period[dest]);
        indeg[dest]--;
        if (indeg[dest] == 0) {
            q.add(dest);
        }
    }
}
int max = 0;
for (int i = 0; i < period.length; i++) {
    period[i] += newTime[i];
    if (max < period[i]) {
        max = period[i];
    }
}
return max;
}
    
```

Q. Euler Path & Euler Circuit
 - It is the path in a graph that visit every edge exactly once



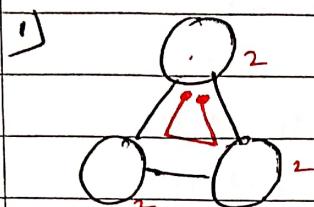
but in euler circuit starting & ending point same & vertex does not visit more than one time.



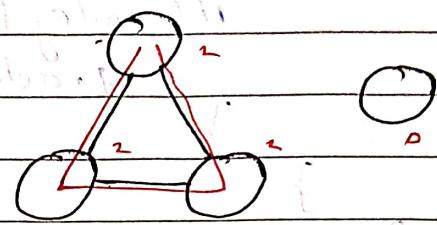
Starting pt = ending pt.

all degrees are even

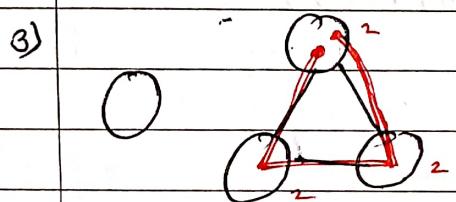
Some example :



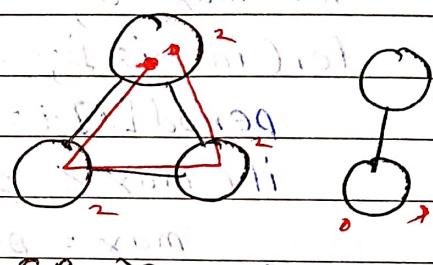
EP ✓
EC ✓



EP ✓
EC ✓



EP ✓
EC ✓



EP X
EC ✓

Euler path : all edges are visited.

Euler ckt : Starting pt == ending point. & all edges are visited.

condt:

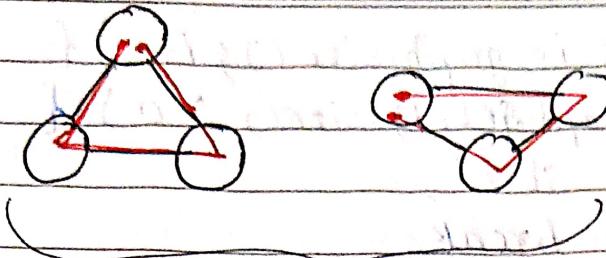
- degree of all nodes / vertex must be even.
- all non-zero degree node should be connected

// dry run remaining //

DATE

--	--	--	--	--	--	--	--

ex:



⇒ not connected

: EC - ➔

: This is not
EC.

one graph.

approach : (DFS).(EC).

- 1) find degree of every node
- 2) if degree of any node is odd return false.
- 3) hence also check non visited vertex (connected graph) degree is zero.

approach for Euler path:

- Same as EC approach but extra cond is 0 or 2 nodes have odd degree.

// code of Euler ckt //

```
private boolean DFS (int curv, graph, boolean visit[]) {  
    visit[curv] = true;  
    for (int i = 0; i < graph.get(curv).size();)  
        for (int ele : graph.get(curv)) {  
            if (!visit[ele]) {  
                DFS (ele, graph, visit);  
            }  
        }  
}
```

```
public static boolean isEulerCkt (int v, graph) {  
    boolean visit [] = new boolean [v];  
    int start = -1;
```

this loop
finding the
vertex whose
degree is
greater than
0 for start

```
for(int i=0; i< graph.size(); i++) {
    if(graph.get(i).size() > 0) {
        st = i;
        break;
    }
}
```

Starts here.

```
if(Start == -1) {
    return true;
}
```

```
DFS(start, graph, visit);
```

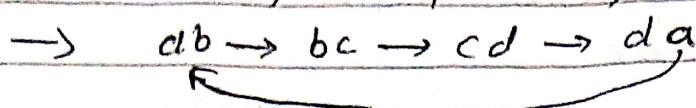
```
for(int i=0; i< v; i++) {
    if(!visit[i] && graph.get(i).size() > 0) {
        return false;
    }
}
```

if(v % 2 != 0 || oddDegree) {
 for(int i=0; i< graph.size(); i++) {
 if(graph.get(i).size() % 2 != 0) {
 return false;
 }
 }
 return true;
}

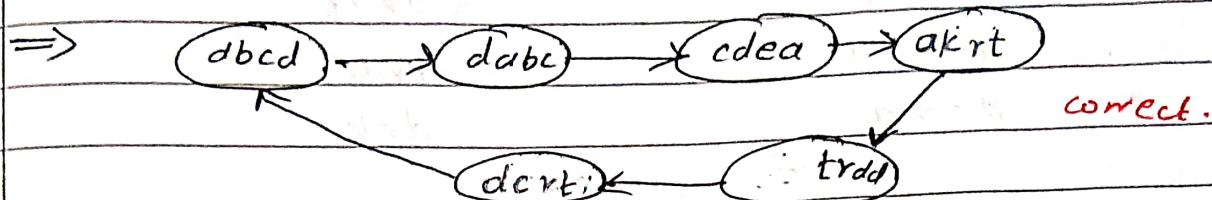
if(v % 2 == 0 && oddDegree) {
 int count = 0;
 for(int i=0; i< graph.size(); i++) {
 if(graph.get(i).size() % 2 != 0) {
 count++;
 }
 }
 if(count > 1) {
 return false;
 }
}

Q. Circle of string : (easy).

ex: 1) "ab", "bc", "cd", "da".

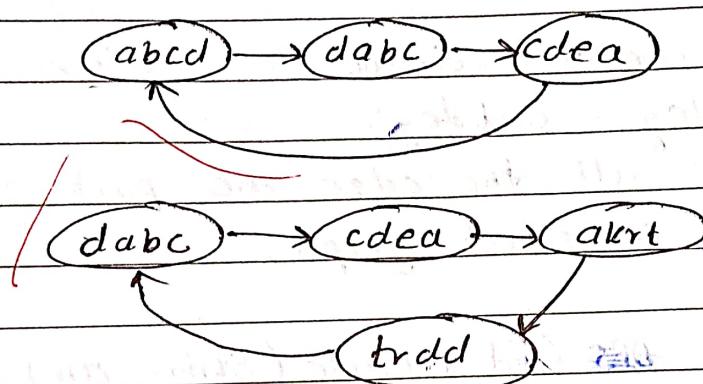


2) "abcd", "dabc", "cdea", "akrt", "trdd", "dck'a".



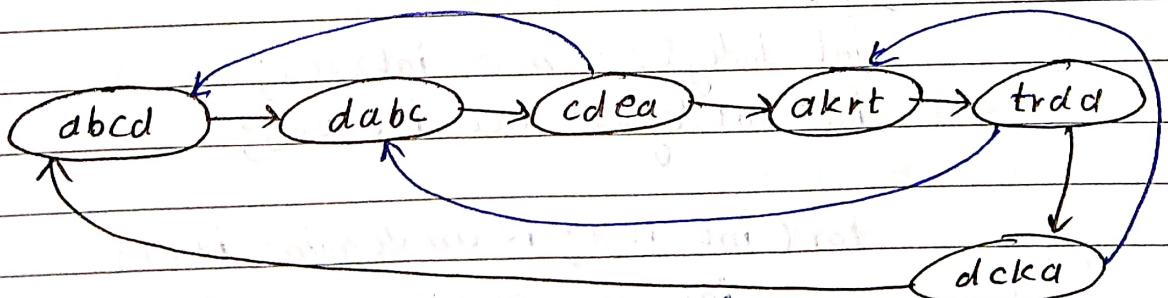
but. cycle also

create by given like given.



hence,

when circle present in string means all string are visited & first & last string are connected each other, called as Hamiltonian cycle.



That's, the permutation generate because every time check all vertex. Time complexity ~~O(N!)~~ $O(N!)$.

approach :-

- 1) In string given important character is first & last, hence create edge b/w them.
i.e. "ad", "de"

$a \rightarrow d$ abad

$d \rightarrow c$ dabc

$c \rightarrow a$ cdea

$a \rightarrow t$ akrt

$t \rightarrow d$ brdd

$d \rightarrow a$ dcika

∴ $a \rightarrow d \rightarrow c \rightarrow a \rightarrow t \rightarrow d \rightarrow a$.

- 2) Check given created circuit is euler or not.

→ Indeg = outdeg

→ DFS : all the edges are part of single connected graph.

```
// code // public void DFS (int IsCircle (String arr[])) {
    // create adjacency list //
    ArrayList<Integer> adj[] = new ArrayList[26];
    for( int i=0; i<26; i++ ) {
        adj[i] = new ArrayList();
    }
    int indeg[] = new int[26];
    int outdeg[] = new int[26];
}
```

for(int i=0; i<arr.length; i++) {

int u= arr[i].charAt(0)-'a';

int v= arr[i].charAt(arr[i].length()-1)-'a';

convert

char into

integer .

```
adj[u].add(v);
indeg[v]++;
outdeg[u]++;
}

// check indeg == outdeg //
for( int i=0; i< 26; i++ ){
    if( indeg[i] != outdeg[i] ){
        return 0;
    }
}

// Euler circuit //
DFS('a' + charAt(0) - 'a', adj, visit);

for( int i=0; i< 26; i++ ){
    if( indeg[i] != 0 && !visit[i] ){
        return 0;
    }
}

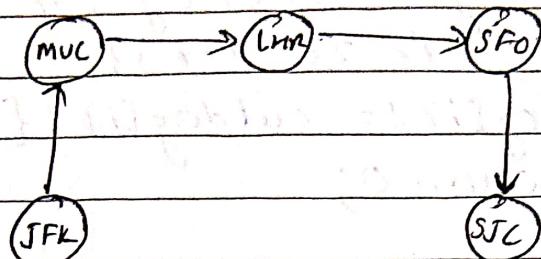
return 1;
}
```

Q. Reconstruct Itinerary :

- given the tickets like [from, to place] of, reconstruct the itinerary in order and return it
- All the tickets belong to man who departs from JFK, thus the itinerary must begin with JFK. If there are multiple valid itineraries you should return the itinerary that has the smallest lexical order when read as a single string.

ex 1) tickets = [["MUC", "LHR"], ["JFK", "MUC"],
["SFO", "STC"], ["LHR", "SFO"]] .

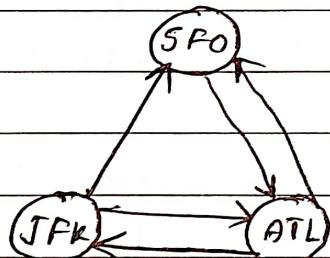
create graph:



return the path in the form of path.

itinerary : ["JFK", "MUC", "LHR", "SFO", "STC"] .

ex 2) tickets = [["JFK", "SFO"], ["JFK", "ATL"], ["SFO", "ATL"],
["ATL", "JFK"], ["ATL", "SFO"]] .



a) itinerary : ["JFK", "SFO", "ATL", "JFK", "ATL", "SFO"] .

b) itinerary : ["JFK", "ATL", "JFK", "SFO", "ATL", "SFO"] .

but (b) ans is larger in lexicical order. (ATL > SFO)

q.poll() \leftrightarrow q.remove()

DATE

--	--	--	--	--	--	--

// code 11 private void DFS(String cur, Map<String, PriorityQueue<String>> graph, List<String> itinerary) {

while (map.containsKey(cur) && !map.get(cur).isEmpty()) {

private static void DFS(String s, Map<String, PriorityQueue<String>> map, List<String> list) {

while (map.containsKey(s) && !map.get(s).isEmpty()) {

String d = map.get(s).poll();

DFS(d, map, list);

}

list.add(0, s);

}

public List<String> findItinerary(List<List<String>> tickets) {

Map<String, PriorityQueue<String>> map = new HashMap();

for (List<String> ~~lK~~: tickets) {

String s = ~~lK~~.get(0);

String d = ~~lK~~.get(1);

PriorityQueue<String> pq = map.getOrDefault(s, new PriorityQueue());

pq.add(d);

map.put(s, pq);

List<String> list = new ArrayList();

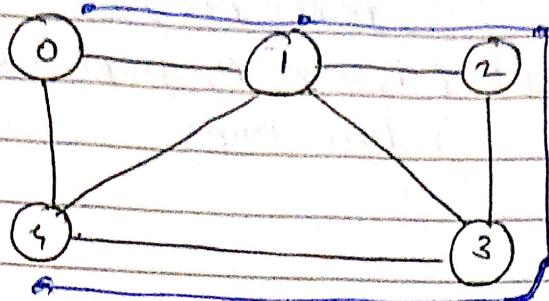
DFS("JFK", map, list);

return list;

Q Hamiltonian Path :-

- Visit all the vertex exactly ones once time and does not visit again.

ex: 1)



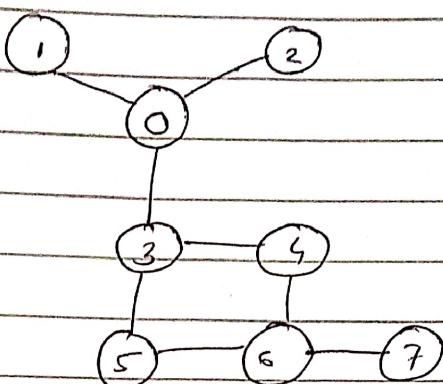
• Hamiltonian path

0 - 1 - 2 - 3 - 4

• Hamiltonian circuit

0 - 1 - 2 - 3 - 4 - 0

ex: 2)

It does not
have hamiltonian path

```

// Code 11
public static boolean check (graph, int count, int N, visit) {
    boolean DFS (int curr, int count, int N, graph, visit) {
        visit[curr] = true;
        count++;
        if (count == N) return true;
        for (int i=0; i< graph[curr].size(); i++) {
            int ele = graph[curr].get(i);
            if (!visit[ele] && DFS(ele, count, N, graph, visit)) {
                return true;
            }
        }
        visit[curr] = false;
        count--;
        return false;
    }
}

```

classmate

```
public boolean hamiltonian ( int N, ArrayList<Integer> graph ) {  
    boolean visit[] = new boolean[N];  
    int count = 0;  
    for( int i=0; i < N; i++ ) {  
        if( DFS( i, count, N, graph, visit ) ) {  
            return true;  
        }  
    }  
    return false;  
}
```