

\* Imp Information for strong resume : hard work \*

- 1) CGPA → 9.5 +
- 2) Unique experience : eg. best rank in hackathon, good company Internship, best rank in competitive programming.
- 3) consistency : atleast 1 hr code each & every day.
- 4) Strong project : atleast 2 project of web dev. + 1 project base on ML.

- In these course → 4 month DSA

4.5 month web development

full stack web dev → MERN (probable)

M - mongo DB

E - express

R - React

N - Node.js

- PPO - pre placement offer - after 3<sup>rd</sup> year
- PPI - pre placement Internship. - after 2<sup>nd</sup> year.

- website Stack overflow :  
- all answer related to coding errors, exceptions etc present in these website.

- The harder you work the luckier you get

\* flowchart of pseudo code:

- diagram to represent sol'n of problems

methodology in solving problem  
divide into small parts

plan too, identify purpose → logically arrange

• components:

1) Start / end →

start

end

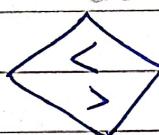
2) I/O →

I/P num

print()

(parallelogram)

4) Decision →



check → true or  
false.

5)



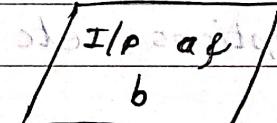
→ arrow.

Ex: Sum of two numbers:

I/p : number of a & b

Start

O/p : sum of a & b, of both numbers



pseudo code:

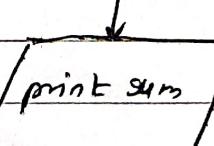
1) Start wh. sets a & b on screen

2) I/p numbers a & b

sum = a+b

3) calculate sum = a+b;

4) print sum



5) end

End

2) Calculate simple Interest  $\frac{P \times R \times T}{100}$

I/P: ~~def~~, P, R, T || Principle, rate & time

O/P: ~~Sum~~  $\frac{P \times R \times T}{100}$

• Pseudo code.

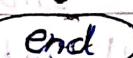
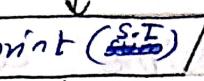
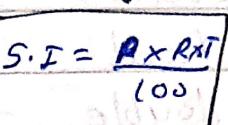
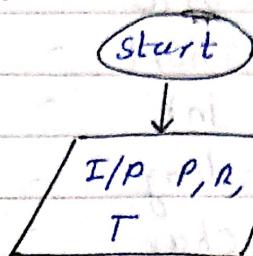
1) Start

2) I/P P, R, T.

3) calculate simple interest of P, R, T.

4) print the S.I.

5) end



3) find max of 3 numbers

I/P: a, b & c

O/P: max of 3.

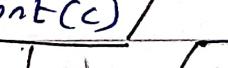
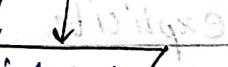
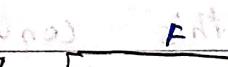
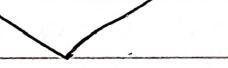
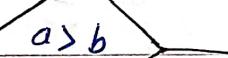
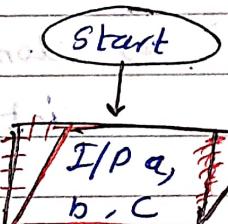
• pseudo code.

1) Start

2) I/P a, b & c numbers

3) compare three number

4) end



Literals - 1, 2, 3, 4, 5

variable - a, b, ... any (declare to store) the data.

classmate

Date \_\_\_\_\_  
Page \_\_\_\_\_

\* Data type & size :

- 1) byte - 8 bit
- 2) short - 2 byte
- 3) int - 4 byte
- 4) long - 8 byte
- 5) char - 2 byte
- 6) boolean - 1 byte
- 7) float - 4 byte
- 8) double - 8 byte

1 bit



1 byte

32 bit

operating system

[Note: for 16 bit OS size of all data type is half of these. ex- int - 2 byte]

\* Possible conversion :

byte → short → int → float → long → double

ex: 1) int a = 100; } possible

long b = a;

2) long a = 200; } through error.  
int b = a;

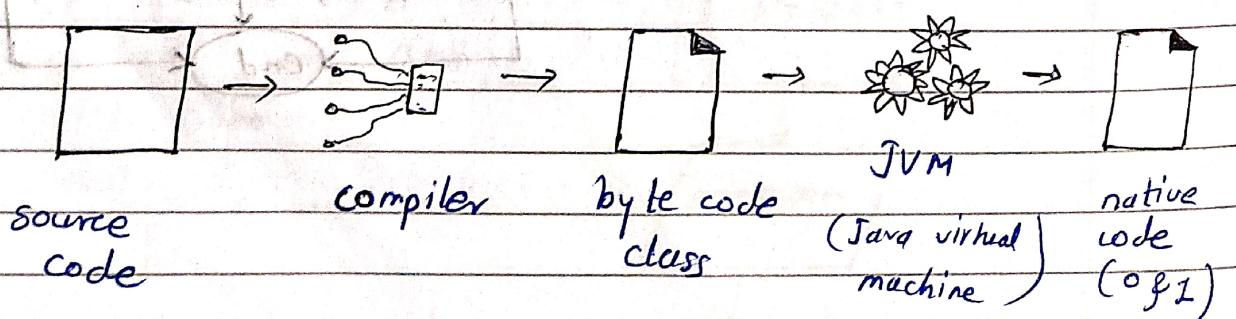
In ex: 2 convert forcefully (coercion)

ex: 3) int marks = (int) (99.99f)

int b = (int) (a) ex: (2)

this conversion called type casting / narrowing / explicit conversion.

\* How to java code run/compile :



## \* Type of operation:

- 1) Arithmetic  $\rightarrow +, -, /, *, \%, \text{ etc.}$
- 2) Unary  $\rightarrow ++, --, \text{ etc.}$
- 3) Relation operator  $\rightarrow <, >, ==, != \text{ etc.}$
- 4) Logical operator  $\rightarrow \&, \&&, ||, !, \text{ etc.}$
- 5) Bitwise operator  $\rightarrow \wedge, \vee, \wedge\wedge, \vee\vee, \text{ etc.}$
- 6) Ternary operator  $\rightarrow \text{variable} = \text{cond"? state1 : state2;}$

$\text{cond?}$  is true then execute  $\text{state1}$  otherwise  $\text{state2}$

$\text{state1}$  otherwise execute statement 2

Ex:  $\text{int boolean larger} = (5 > 3) ? 5 : 3;$   
 $\text{println(larger)} \rightarrow 5$

## \* Switch Statement:

Syntax: `switch (variable){ case 1: { } case 2: { } ... case n: { }`

$\text{case 1: } \{ \dots \}$

$\text{case 2: } \{ \dots \}$

$\vdots$  =  $\text{default: } \{ \dots \}$

$\text{Note: In switch statement if many cases are true then this case is execute but does not write break keyword in this case then after this cases all other cases are execute i.e. if i not}$

$\text{(" " + " ) not writing two times } \{ \dots \}$



## \* Array:

- g1) print the possible pair of in the array

Ex: arr = {1, 2, 3}.two, one, two

O/P: (1, 2); (1, 3)

(1, 3); (2, 3); (2, 1); (3, 1); (3, 2)

total pair = 3

$\text{int a[3][3] = {{1, 2, 3}, {4, 5, 6}, {7, 8, 9}}; }$

//code1// public static void possiblePair(int arr[]) {  
 int l = arr.length;  
 int count = 0;  
 for (int i=0; i<l-1; i++) {  
 for (int j=i+1; j<l; j++) {  
 System.out.print(" (" + arr[i] + ", " + arr[j] + ")");  
 count++;  
 }  
 System.out.println();  
 }  
 System.out.println("total pair: " + count);  
}

Q2) print all subarray of array  
 ex: arr = {1, 2, 3};  
 O/P: 1; 1 2; 1 2 3;  
 2;  
 2 3;  
 3;  
 thus total subarray = 6;

//code1// public static void subArr(int arr[]) {  
 int l = arr.length;  
 int count = 0;  
 for (int i=0; i<l; i++) {  
 for (int j=i; j<l; j++) {  
 for (int k=i; k<=j; k++) {  
 System.out.print(" (" + arr[k] + " ");  
 }  
 System.out.print(");  
 count++;  
 }  
 System.out.println();  
 }  
 System.out.println("total subarray : " + count);  
}

Q3) maximum sum of subarray : (prefix sum).

Code:

```
public static int maxSumOfSubArr(int arr[]) {
```

```
    int l = arr.length;
```

```
    int maxSum = Integer.MIN_VALUE;
```

```
    int currSum = 0;
```

```
    int arr2[] = new int[l];
```

```
    arr2[0] = arr[0];
```

```
    for (int i = 1; i < l; i++) {
```

```
        arr2[i] = arr2[i - 1] + arr[i];
```

```
}
```

```
for (int j = 0; j < l; j++) {
```

```
    for (int k = j; k < l; k++) {
```

```
        currSum = j == 0 ? arr2[k] : arr2[k] - arr2[k - 1];
```

```
        if (maxSum < currSum) {
```

```
            maxSum = currSum;
```

```
        }
```

```
}
```

```
}
```

```
return maxSum;
```

Ex: arr = {2, 3, 4, -1, 2, 3};

sumArr = [2 | 5 | 9 | 8 | 10 | 13]

subarrays;

i=0 2; 2 3 4; 2 3 4 -1; 2 3 4 -1 2; 2 3 4 -1 2 3

i=1 3; 3 4; 3 4 -1; 3 4 -1 2; 3 4 -1 2 3

j=0 j=1 j=2 j=3 j=4 j=5

for i=0 sum of subarrays  $\Rightarrow$  sumArr[j]

for i=1 sum of subarrays  $\Rightarrow$  sumArr[j] - sumArr[i-1]

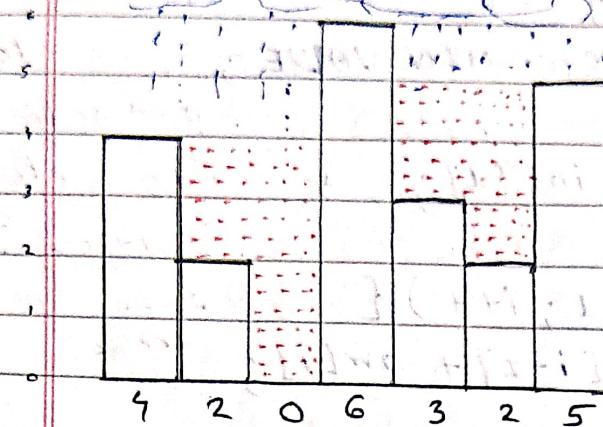
for second row arr[0] not included then subtract.

arr[0] - for from arr2[j] - for each element.]

then gives. sum of subarray for second row.

### Q 4) Trapping rain water.

ex: height = {4, 2, 0, 6, 3, 2, 5};

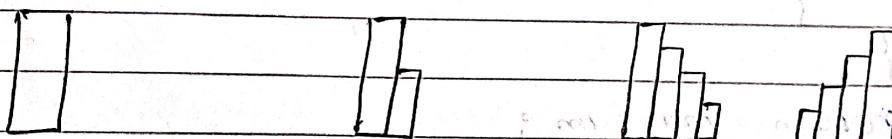


these are building  
and height is given  
and width is 1 of  
all building.

process:

- 1) calculate max height of left & right building.  
by using loop:  $i=1$  to  $n-1$
- 2) calculate water level
- water level =  $\text{Math.min}(\text{left bound}, \text{right bound})$ ;
- 3) trapped water = water level - height[i];

(case 1)



one building

two building

ascending or descending order

Step:

No water trapped. ( ~~$t=1$  if  $t=2$~~ )

- 1) Create two helper arr & store max height

1)  $[4 | 4 | 4 | 6 | 6 | 6 | 6]$   $\rightarrow$  left to right

2)  $[6 | 6 | 6 | 6 | 5 | 5 | 5]$   $\rightarrow$  right to left

- 2) water level = min value from these arrays.

$\{4, 4, 4, 6, 5, 5, 5\}$   $\Rightarrow$  4, 4, 4, 6, 5, 5

- 3) trapped water = water level - height

$\Rightarrow 4-4; 4-2; 4-0; 6-6; 5-3; 5-2; 5-5$

$\Rightarrow 0+2+4+0+2+3+0 \Rightarrow \underline{\underline{11}}$

```

//code// public static void rainWaterTrapped ( int height [] ) {
    int l = height.length;
    if ( l == 1 || l == 2 ) {
        System.out.println (" No water Trapped ");
        return;
    }
    leftMaxBound [ 0 ] = height [ 0 ];
    int leftMax = height [ 0 ];
    int leftMaxBound = new int [ l ];
    for ( int i = 0 ; i < l ; i ++ ) {
        if ( leftMax < height [ i ] ) {
            leftMax = height [ i ];
        }
        leftMaxBound [ i ] = leftMax;
    }
    rightMax = height [ l - 1 ];
    int rightMaxBound [ ] = new int [ l ];
    rightMaxBound [ l - 1 ] = height [ l - 1 ];
    for ( int j = l - 2 ; j >= 0 ; j -- ) {
        if ( rightMax < height [ j ] ) {
            rightMax = height [ j ];
        }
        rightMaxBound [ j ] = rightMax;
    }
    int waterLevel = 0 ;
    int waterTrapped = 0 ;
    for ( int i = 0 ; i < l ; i ++ ) {
        waterLevel = Math . min ( leftMaxBound [ i ] , rightMaxBound [ i ] );
        waterTrapped + = waterLevel - height [ i ];
    }
    System.out.println (" Water Trapped " + waterTrapped );
}

```

left max  
boundary  
calculate

right max  
boundary  
calculate

calculate  
water  
level

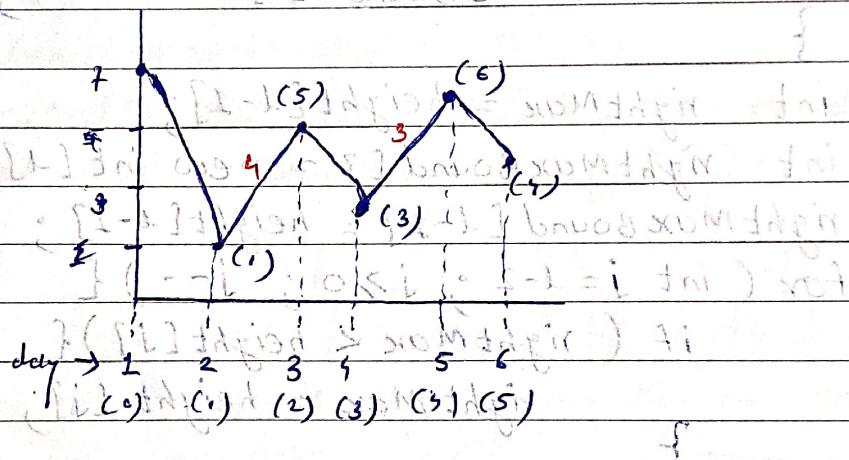
- Q. 5) By Buy & sell stock in one transaction.
- you are given an array prices where prices [i] is the price of given stock on the  $i^{\text{th}}$  day. You want to maximum your profit by choosing a single day to buy one stock & choosing a different day in the future to sell that stock. Return the maximum profit you can achieve from this transaction. If you cannot achieve any profit return 0.

$\rightarrow \text{Profit} = \text{max}(\text{buying price}, \text{selling price})$

(max)

ex:  $\text{prices}[] = \{7, 1, 5, 3, 6, 4\}$ ;

graph:



for day 1  $\rightarrow$  only buying of stock

buy stock = 7 ; Profit = 0;

for day 2  $\rightarrow$  selling price = 1 (loss)

buy stock = selling price ; Profit = 0

for day 3  $\rightarrow$  selling price = 5 ; Profit = 5

buy stock = 2 ; Profit = 5 - 2 = 3

for day 4  $\rightarrow$  selling price = 3 ; Profit = 2 < 3 = 0

buy stock = 5 ; Profit = 5 - 5 = 0

for day 5  $\rightarrow$  selling price = 6 ; Profit = 6 - 3 = 3

buy stock = 3 ; Profit = 3 - 3 = 0

Creating 2 variable to store the min stock price and maximum stock price in maxProfit.

```

//code11 public static void maxProfitOfStock(int prices[]) {
    int l = prices.length;
    int buyPrice = prices[0];
    int minPrice = 0; MaxPrice = 0;
    int maxProfit = Integer.MIN_VALUE;
    for (int i=0; i<l; i++) {
        if (buyPrice < prices[i]) {
            int profit = prices[i] - buyPrice;
            if (profit > maxProfit) {
                maxPrice = prices[i];
                maxProfit = profit;
            }
        } else {
            buyPrice = prices[i];
            minPrice = prices[i];
        }
    }
    System.out.println("Min Price of stock : " + minPrice);
    System.out.println("Max Price of stock : " + maxPrice);
    System.out.println("Max Profit of stock : " + maxProfit);
}

```

Q6) Sorting :

1) bubble sort

2) selection sort

3) Insertion sort

Q7) // book I - present question related to I-D array //

## \* 2-D Array \*

- 1) // basic, I/p - O/p of 2-D array
- 2) // addition of two matrices
- Imp** 3) // spiral matrix
- 4) // multiplication of two matrix
- 5) // rotate matrix etc. present in book-I

Q. Sum of diagonals using extra fns

Ex:

	1	2	3		1	2	3	4
4	5	6	7		5	6	7	8
7	8	9	10		10	11	12	
					1	2	3	4

$$\text{Sum} = 15 + 10 = 25$$

$$\text{Sum} = 22 + 22 = 44$$

// brute force logic  $\Rightarrow$  primary diagonal  $\Rightarrow i=j$   
 $\Rightarrow$  secondary diagonal  $\Rightarrow i+j = l-1$

// create two nested loop & write down these condn //  
 time complexity =  $O(n^2)$

// code // public static void sumOfDiagonal (int arr [ ] [ ]) {

    int l = arr.length;

    int sum = 0;

    for (int i = 0; i < l; i++) {

        sum += arr[i][i];

        sum += arr[i][l - 1 - i];

}

    int num = 0;

    if (l % 2 == 0) {

        num = l / 2;

        sum -= arr[num][num];

        System.out.println (sum);

    } else {

        System.out.println (sum); }

}

g7) find key in sorted array (2D).

ex: arr[ ][ ]  $\Rightarrow$

10	20	30	40
15	25	35	45
27	28	38	48
29	33	49	50

} both row & column are sorted.

\* Step:

cond consider first key is start to find from position (0,3) and (3,0). choose any one position check key is ( $<$  or  $>$ ), then move position.

//code

```
public static void findKeyInSortedArr(
```

```
int arr[ ][ ], int r, int c, int key ) {
```

```
int top = 0; int bott = r - 1; int left = 0; int right = c - 1;
```

```
while ( top <= bott || right <= left ) {
```

```
if ( key == arr[top][right] ) {
```

```
printf("key is present (%d, %d)", top, right);
```

(2, 4), (0, 3) error serial returning show a error

```
else if ( key < arr[top][right] ) {
```

```
right = right - 1; // right - 1
```

```
}
```

```
top++;
```

```
}
```

```
}
```

```
System.out.println ("key does not present in array");
```

```
}
```

g8) transpose of matrix [i][j]  $\Rightarrow$  [j][i]

g9) pascal triangle using 2D array.

## \* Strings \*

- String is Immutabile; they are does not change
- if change the string then create another variable of string & store changed string.

Q 1) Check string is palindrome.

→ ex: "madam", "noon", "racecar".

```
// code11 public static boolean checkPalindrome(String st) {
    int l = st.length();
    for (int i=0; i<l/2; i++) {
        if (st.charAt(i) != st.charAt(l-i-1)) {
            return false;
        }
    }
    return true;
}
```

Q 2) Given a route containing 4 directions (E, W, N, S)  
find the shortest distance/path to reach destination;

→ Ex: "WNEENESENNS"  
dist. =  $\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$

The diagram shows a 2D Cartesian coordinate system with a horizontal x-axis and a vertical y-axis. The origin is labeled (0,0). A path is drawn starting from the origin. It moves right (E) to (1,0), up (N) to (1,1), right (E) to (2,1), up (N) to (2,2), right (E) to (3,2), up (N) to (3,3), right (E) to (3,4), and up (N) to (3,5). The path ends at the point (3, 4).

```
// code11 public static void shortDistances(String st) {
```

```
    int x=0; int y=0;
    for (int i=0; i<st.length(); i++) {
        if (st.charAt(i) == 'W') {
            x--;
        } else if (st.charAt(i) == 'E') {
            x++;
        } else if (st.charAt(i) == 'N') {
```

```

    y++;
}
else {
    y--;
}
}
}

```

```
int dist = (x*x) + (y*y);
```

```
float shortDist = Math.sqrt(dist); // (float) Math.sqrt(dist);
```

```
System.out.println(dist);
```

```
}
```

Q.3) Print largest string lexicographically.

→ ex: "apple", "mango", "banana";

$a < b < m$ , hence largest string = "mango";  
use the method `st.compareTo(string)`;

```
Model1 public static void main(String args[]) {
```

```
String fruits[] = {"apple", "mango", "banana"};
```

```
String large = fruits[0];
```

```
for (int i = 1; i < fruits.length; i++) {
```

```
if (large.compareTo(fruits[i]) < 0) {
```

```
large = fruits[i];
```

```
System.out.println(large);
```

In internally `st1.compareTo(st2) > 0` → `st1 > st2`

`st1.compareTo(st2) < 0` → `st1 < st2`

`st1.compareTo(st2) = 0` → equal.

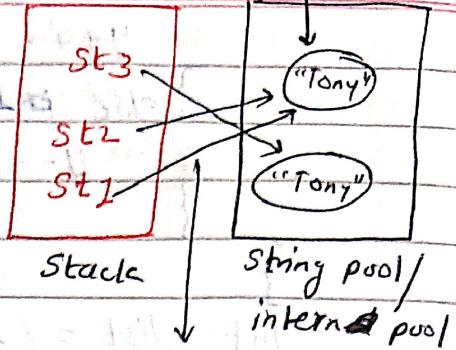
(Time complexity =  $O(n \times d)$ ),

\* String In memory

1) ex: st1 = "Tony";

st2 = "Tony";

st3 = new string ("Tony");



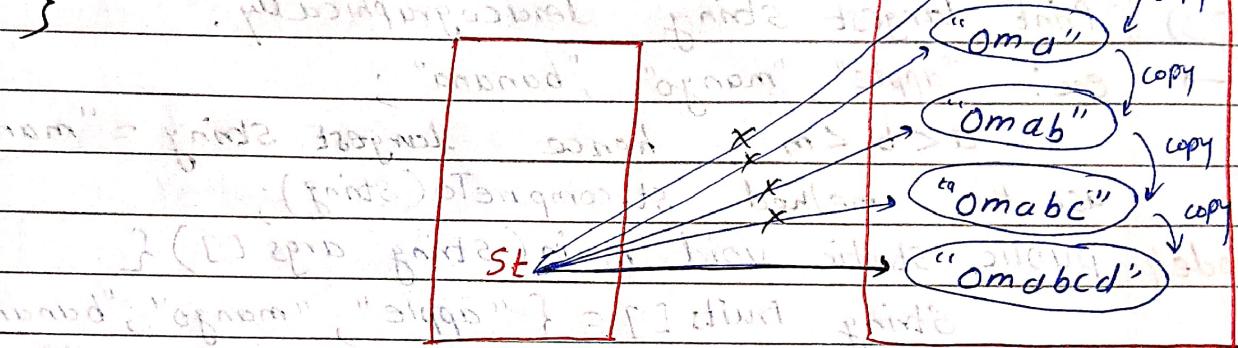
2) String st = "Om"; char = 'a'; interning

for ( int i=0 ; i<n ; i++ ) {

st += char;

char++;

In memory.



Note: when adding character in string then pointing the 1st string (in memory) to second string (removal of pointing) removes pointing from 1st string.

- In case n is 1000 - 1000000, then string is copying n times & loop is O(n^2).

In these case, string is many time change then you use new data structure StringBuilder.

\* String Builder :

Syntax: StringBuilder sb = new StringBuilder ("");

Ex: for( char ch = 'a'; ch <= 'z'; ch++ ) {  
    sb.append(ch);  
}

time complexity =  $O(n)$ ;

calculate length  $\rightarrow$  `sb.length();`

q4) for given string convert each first letter of each word to uppercase;

$\rightarrow$  ex: String st = "onkar appasahab shinde";

String ans = "Onkar Appasahab Shinde"

//code11 public static String toUpperCase(String st);

StringBuilder sb = new StringBuilder("");

char ch = st.Character.toUpperCase(st.charAt(0));

sb.append(ch);

for (int i=0; i<st.length()-1; i++) {

char curChar = st.charAt(i+1);

if (st.charAt(i) == '?') {

curChar = Character.toUpperCase(st.curChar);

}

sb.append(curChar);

}

return sb.toString();

}

q5) Compress the String into another string.

$\rightarrow$  ex: "aabbbbccddd"  $\xrightarrow{\text{compress}}$  "a2b3c2d3"

//code11 public static String compressString(String st) {

StringBuilder sb = new StringBuilder("");

Integer count = new Integer(1);

for (int i=0; i<st.length(); i++) {

char curChar = st.charAt(i);

sb.append(curChar);

while (i<st.length()-1 && st.charAt(i) == st.charAt(i+1)) {

count++;

i++;

}

```

        if(count > 1) {
            String newst = count.toString();
            sb.append(newst);
        }
    }
    return sb.toString();
}

```

Time complexity =  $O(n)$

// You can also solve by string concatenation //

time complexity =  $O(n)$

### \* Bit Manipulation

Note: Operator for bitwise operators & binary number system  $\rightarrow$  book-I page 42 to 45.

\* one's complement ( $\sim$ ) actual working:

Ex: in 5.  $\swarrow$  MSB (most significant bit)

$\therefore 5 = 00000101 \swarrow$  (MSB) List significant bit

$\therefore \sim 5 = 111110\swarrow 0$

$\therefore \sim(5+1) = 00000110 \swarrow 1$  addition of binary numbers.

MSB = 0  $\rightarrow$  +ve value  $(6)_{10}$   $1+0=1$

MSB = 1  $\rightarrow$  -ve value  $(-7)_{10}$

Step of 2's complement

Ex: 1) 1's complement  $\sim = \sim(5)$

2) and  $\oplus 1$  binary

3) check step 1 MSB & put sign in step 2 answer.

Ex 1:  $\sim 5 = \sim(00000101) = 1111010$  MSB = 1 (-ve)

Step 1:  $\sim(5) = 00000101$

Step 2: add 1  $\Rightarrow \begin{array}{r} 00000101 \\ + 1 \\ \hline 00000110 \end{array} \Rightarrow (6)_0$

$\therefore \sim 5 = (-6)_0$

Ex 2)  $(\sim 0) = (-1)_0$

Ex 3)  $(\sim 1) = (-2)_0$

Q. Check the given number is even or odd by using bitwise operator.

→ ex: num = 4  $\sim 4 = 11110010$

if  $((num \& 1) == 0) \rightarrow$  even  $11110010 \& 0100 = 0100$

if  $((num \& 1) == 1) \rightarrow$  odd  $11110010 \& 0101 = 0101$

```
//Code
public static void evenOddNum(int num) {
    int bitmask = num & 0010; // num & 000001
    if (bitmask == 0) {
        System.out.println("Given number is even");
    } else {
        System.out.println("Given number is odd");
    }
}
```

Q. Get bit of  $i^{th}$  position.

→ ex: num = 00101 ; posi = 2 (3rd bit).

Step: consider bit = 1 (0001).

Move 1 in left shift by using ( $<<$ ) by posi times.

$\therefore num \& bitmask = num \& (bit << pos);$

if ( $bitmask == 0$ )  $\Rightarrow 0$  present  $= 00101 \& (00100)$ .

otherwise  $\Rightarrow 1$  present  $= 00100$ .

```
//code11 public static void get_ith_Term(int num, int pos){
    int bitmask = num & (1 << pos);
    if (bitmask == 0) {
        System.out.println("0");
    } else {
        System.out.println("1");
    }
}
```

Q. Set bit in ith term.

→ ex: 10101 set 1 position 1. 3rd position.

Step 1)  $bit = 1 << pos$ .

2)  $num | bit$

```
//code11 public static void set_ith_Term(int num, int pos) {
    int bitmask = num | (1 << pos);
    System.out.println(bitmask);
}
```

Q. Clear bit in ith position.

→ ex: 10101 1st bit, pos=1, 2nd.

Step 1)  $ope = \sim(1 << pos)$

2)  $bitmask = num \& ope$

```
//code11 public static void clear_ith_Term(int num, int pos) {
    int ope = ~(1 << pos);
    int bitmask = num & ope;
    System.out.println(bitmask);
}
```

Q. Clear last n bits. 1st is given

→ ex: num= 1111 (15) n=2, 2nd

1111 & 0011 = 1100 = decimal 8

(0011) & 10100 = 10000 & 10000 = 10000 = decimal 16

**Imp:** Note:  $\sim(0) = 1111111111111111$  (all 1's)

 $\sim(-1) = 1111111111111111$  (all 1's)

for  $\sim(-1) \ll 2 = 1111100$  then and with num.

~~Header~~ C. num = 1111 ... num & 1100

$\therefore \text{bitmask} = \text{num} \& (-1 \ll n); \Rightarrow \text{bitmask} = 1100$

**Code:** public static void clearLast-N-Bits(int num, int n){  
 int bitmask = num & (-1 << n);  
 System.out.println(bitmask);  
}

Q. clear bits from  $i$  (to  $j$  terms).

Ex: num =  $(01101011)_2$  } clear bits  $i=2$   
 position  $\rightarrow$  9 8 7 6 5 4 3 2 1 0 } to  $j=7$ .

O/P: 1000000011

logic :  $000001 = 2^1 - 1 \quad \therefore 1 \ll b = 2^b$   
 $000011 = (3)_2 = 2^2 - 1 \quad \therefore 1 \ll i = 2^i$   
 $000111 = (7)_2 = 2^3 - 1$   
 $001111 = (15)_2 = 2^4 - 1$   
 $011111 = (31)_2 = 2^5 - 1$

Step 1 :  $a = (-1) \ll (j+1);$

$(b = (1 \ll i) - 1);$  ~~bitmask = num & (a | b);~~

bitmask = num & (a | b);

**Code:** public static void clear\_i-to\_j-bits(int num, int i, int j){  
 int a = (0) << (j+1);  
 int b = (1 << i) - 1; ←  $(0 \ll i) + 1$   
 int bitmask = num & (a | b);  
 System.out.println(bitmask);  
}

**Imp:**  $2^1 = 10$

$2^2 = 100$

$2^3 = 1000$

$2^4 = 10000$

$1 = 1$

$3 = 011$

$7 = 0111$

$15 = 01111$

$n \& (n-1) = 0$

T number of

$n$  is ~~power~~ ~~of~~

power 2

**IMP** *amazon, google*

g. count set bits in number (count 1 in number).

→ Ex: num = 1010

Step: In while loop → check if  $num \& 1 == 1$  (0001)

then  $num = num \gg 1$

$0011 | num = num \gg 1 (= 0101)$  & num = 0101

~~if (num & num >> 1 == 0010) break; situation arising below~~

~~num = num >> 1 = 0001 num = 0001~~

~~num = num >> 1 = 0000~~ failing to stop if  $num == 0$ ;

// code //

public static void countSetBits (int num){

int count = 0;

while (num != 0) {

if ( $(num \& 1) == 1$ ) {

count++; } }

~~num = num >> 1; 10000000000000000000000000000000~~

~~is = is >> 1; 1 - is = 110000~~

System.out.println(count); 1000

$n = \log n + 1$

$10000$  5 digit

∴ time complexity =  $O(\log(n))$

g. Fast Exponential function  $a^n$  ( $= a^3$ ).

→ Ex: ans =  $5^3$  (125) → ans = 125

Step: ~~assume~~ convert power in binary

∴ ans =  $\frac{011}{5} \cdot a^{(1)} \gg (000) = 125$

∴ if ( $n != 0$ ) → ans = ans \* a

$a = 5$   $a^3 = a \cdot a \cdot a$

Ex 2:  $a = 3$ ,  $n = 5$  (125)

∴ ans =  $3^5 \Rightarrow (3)^{\frac{0101}{2}}$

$d^6 \downarrow d^5 \downarrow d^4 \downarrow d^3 \downarrow d^2 \downarrow d^1 \downarrow$

$0 = (0-0) \cdot a^0 + a^0 = 1$

$1 = (1-0) \cdot a^1 + a^1 = 3$

$9 = (10-8) \cdot a^2 + a^2 = 9$

$27 = (100-81) \cdot a^3 + a^3 = 27$

```
//code11 public static void powerOfNumber(int a, int n) {  
    int ans = 1;  
    while (n != 0) {  
        if ((n & 1) == 1) {  
            ans = ans * a;  
        }  
        a = a * a;  
        n = n >> 1;  
    }  
    System.out.println(ans);  
}
```

## \* Oops : object oriented programming

group of entities ↗ entities in real word.

### \* Class & object :

- object store in Heap type memory.
- always write first letter of class is capti Capital and first of method/function is small.
- object is use to define real word object in code.
- and the set of objects store the class

ex: all property of pen is object of pen is class.

g. create class of pen & set its color & tip.

// code 11

class pen {

    String color;

    int tip;

    // function //

    void setColor(String newColor) {

        color = newColor;

}

    void setTip(int newTip) {

        tip = newTip;

}

}

- In main public class, & main method create object of these class & access.
- In java runtime first find public class & main method.

In main method =>

Pen p1 = new Pen();

p1.setColor("red");

p1.setTip(5);

System.out.println(p1.color);

~~IMP~~

## access modifier:

- It is used to which type of data can be access or not access by user. i.e. in outside of the class, method or package.
- There are 4 types:

### 1) Private :

- private variable/object does not access within package, other class & outside package.
- It is access only within the class.

Syntax: ex: ~~private password~~  
~~private~~ password

- Syntax: private type obj = m;
- ex: private String password = "onkar77\*77";

### 2) Default :

- It is access only within class & within package, does not access by outside package of class.

Syntax: type obj = m;

ex: String username = "ShindeOnkar";

### 3) Protected :

- It is access within class, within package of outside package of subclass.
- does not access outside package.

Syntax: protected type obj = m;

### 4) Public :

- It can be access to anywhere.

Syntax: public type obj = m;

## \* four pillars of oops:

1) Encapsulation

2) Inheritance

3) Polymorphism

4) Data abstraction

### ① 1) Encapsulation:

- Encapsulation is the wrapping up of data & methods under a single unit. It is also implement data hiding.



- It is a single entity to wrap data & functions in class structure.
- by using access modifier and implementing data hiding.

### \* Constructor:

- constructor is special method which is called automatically at the time to create object of class.

- Name of the constructor is same as class
- it does not any return type
- memory allocation happens when constructor is called.

ex: class onkar { }

onkar() { } (which is constructor)

it is automatically called when object is created.

{ } (which is body of constructor)

}

- There are three type of constructor

1) No argument

2) with argument:

3) copy constructor:

### 3) Copy Constructor:

- In java copy constructor create by users, but in C++ copy constructor is present by the fault.
  - copy constructor is the copy properties of one object to another object.
- ex: obj1 ≠ obj2 ⇒ obj2 = copy(obj1).

```

Model class Student {
    String name; // "Pradyumna" name
    int rollNo; // 101 student id
    int marks[]; // marks
    Student() {
        this.marks = new int[3];
    }
    Student(Student obj1) {
        this.name = obj1.name;
        this.rollNo = obj1.rollNo;
        this.marks = obj1.marks;
    }
    void getInfo() {
        System.out.println(name);
        System.out.println(rollNo);
        for (int i = 0; i < marks.length; i++) {
            System.out.print(marks[i] + " ");
        }
        System.out.println();
    }
}

```

main method → Student obj1 = new Student();  
 obj1.name = "Onkar Shinde";  
 obj1.rollNo = 77;  
 obj1.marks;

```
obj1.marks[0] = 90;
```

```
obj1.marks[1] = 85;
```

```
obj1.marks[2] = 80;
```

```
obj1.getInfo();
```

// copy properties of obj1 to another object //

```
Student obj2 = new Student(obj1);
```

```
obj2.getInfo();
```

// change the property of obj1 //

```
obj1.name = "Ramu";
```

```
obj1.marks[0] = 100;
```

```
obj2.getInfo();
```

O/P:

onkar shinde is an student } obj2.

77

90 85 80 (kids Institute) Institute

onkar shinde is an student } obj2.

77

90 85 80 (kids Institute) Institute

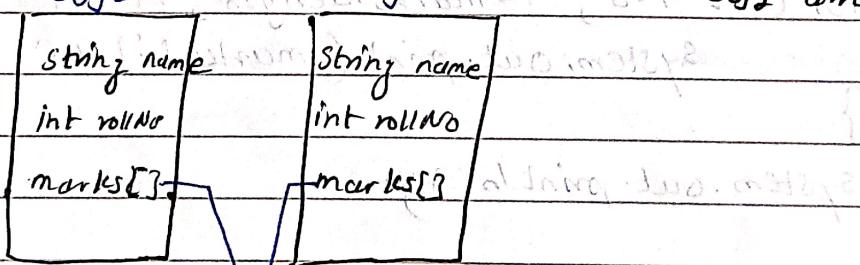
onkar shinde

77

100 85 80 (kids Institute) Institute but print obj2 property

but array can change because array point on

obj1 but print obj2 property because array point on obj1 array,



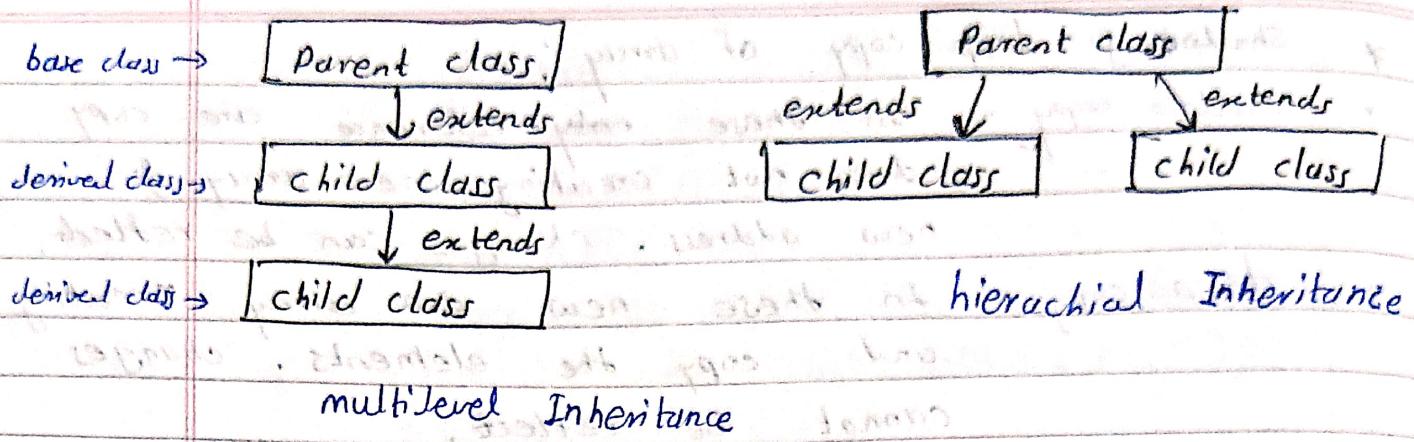
90 85 80

(kids Institute) Institute

(kids Institute) Institute

(kids Institute) Institute





Note: multiple inheritance does not present in ~~java~~, but same as present in interfaces, ~~multiple~~ & in C++ multiple inheritance present.

### 3) Polymorphism:

#### 1) Compile time polymorphism

- method overloading
  - same method name but different type of arguments parameters. (Same class).

Ex: ~~void~~ void sum (int a, int b)

~~void~~ void sum (float a, float b)

void sum (int a, int b, int c)

#### 2) Runtime polymorphism

##### • method overriding

- same method & same argument but diff. class

#### \* Packages in Java:

- package is the ~~group~~ group of similar type of classes, interfaces & sub packages,

### 3) Abstraction : (Idea)

- Hiding all the unnecessary details & showing only the important parts to the users
- user does not creating object of abstract class.
- you can also write abstract or non-abstract method in abstract class.
- It can have constructor.

Syntax: abstract class Animal {  
void eat () {

System.out.println ("animal eats");

does not

implementation →

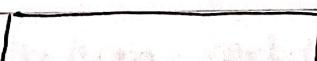
abstract void walks();

(not write inside the )

class)

- If Animal class extends in another class then abstract methods can be implemented if it is compulsory
- In abstract class constructor is used to by default value ~~not~~ initialise in these class , it can change in another class .

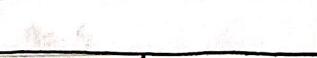
①



- abstract class

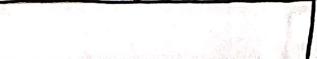
↓ extends

②



- derived class ~~extends~~

③



- derived class

- If creating object 3<sup>rd</sup> derived class but ~~constructor~~ 1<sup>st</sup> constructor called of abstract class

## (viii) mathematical

problems related to finding the area of the garden  
and the cost of the labour required for digging the

garden. To calculate the area of the garden  
we have to find the length and width of the

garden and then multiply them to get the area.  
The cost of the labour will depend on the area  
of the garden and the rate per hour.

Example 1 If a rectangular garden is 20 m long  
and 15 m wide, calculate the area of the garden.

Solution) Given dimensions of the garden are  
length = 20 m and width = 15 m.

Area of the garden = length × width

= 20 × 15 = 300 m<sup>2</sup>

Cost of labour = ₹ 10 per hour

∴ Total cost of labour = ₹ 10 × 300 = ₹ 3000

∴ Area of the garden = 300 m<sup>2</sup> and cost of labour = ₹ 3000.

Example 2 A rectangular garden is 12 m long and 8 m wide.

Calculate the area of the garden and the cost of labour if the cost of labour is ₹ 12 per hour.

Solution) Given dimensions of the garden are  
length = 12 m and width = 8 m.

Area of the garden = length × width

= 12 × 8 = 96 m<sup>2</sup>

Cost of labour = ₹ 12 per hour

∴ Total cost of labour = ₹ 12 × 96 = ₹ 1152.

∴ Area of the garden = 96 m<sup>2</sup> and cost of labour = ₹ 1152.

Example 3 A rectangular garden is 15 m long and 10 m wide.

Calculate the area of the garden and the cost of labour if the cost of labour is ₹ 15 per hour.

Solution) Given dimensions of the garden are  
length = 15 m and width = 10 m.

Area of the garden = length × width

= 15 × 10 = 150 m<sup>2</sup>

Cost of labour = ₹ 15 per hour

## \* Recursion:

- theory: basic  $\rightarrow$  Page 826 - 92

+ questions: Page 852 - 55.

Page 109 - 114

*amazon*  
S.

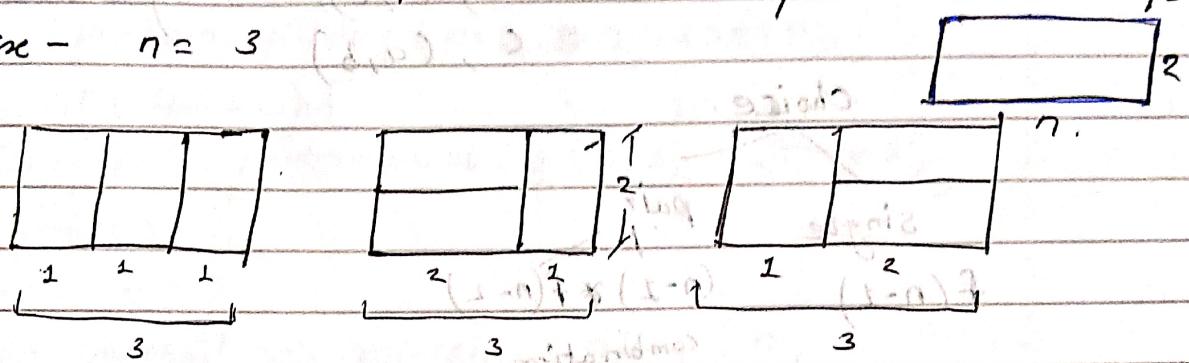
Tiling problem:

Given "2x n" board and tiles of size "2x 1".

Count the number of ways to tile the given board using the 2x1 tiles.

(A tiles can be placed horizontally or vertically).

→ ex -  $n = 3$



3 ways to place tiles in 2x3 of size.

Size 2 (of tile)  $\rightarrow$  2x1

// code

```
public static void int tilingCount (int n) {
```

```
    if (n == 0 || n == 1) return 1;
```

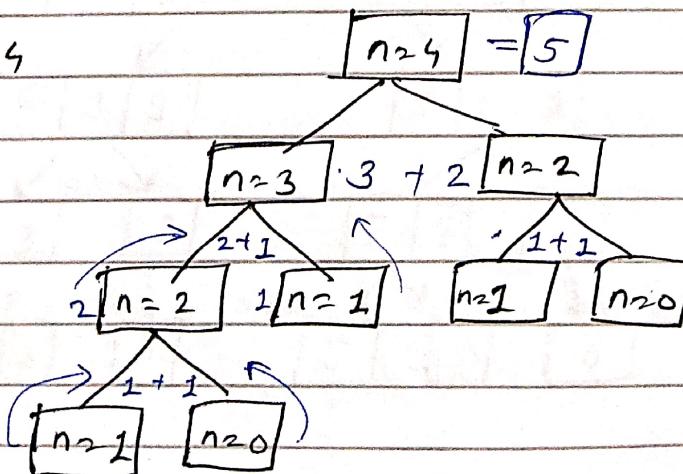
```
    int vert = tilingCount (n-1);
```

```
    int horiz = tilingCount (n-2);
```

```
    return vert + horiz;
```

}

ex :  $n=4$



## g. friends Pairing :

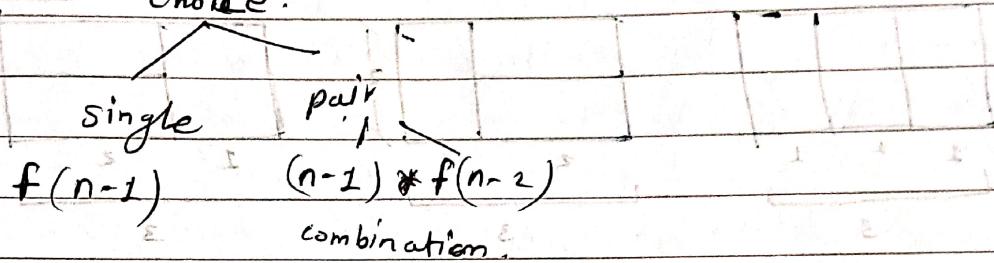
- Given  $n$  friends each one can remain single or can be paired up with some other friends.
- each friend can be paired only once. find out the total number of ways in which friends can remain single or can be paired up.

→ Ex: If  $n=2$  pair  $\rightarrow$   $a, b$ ;  $(a, b)$  is 2 way.

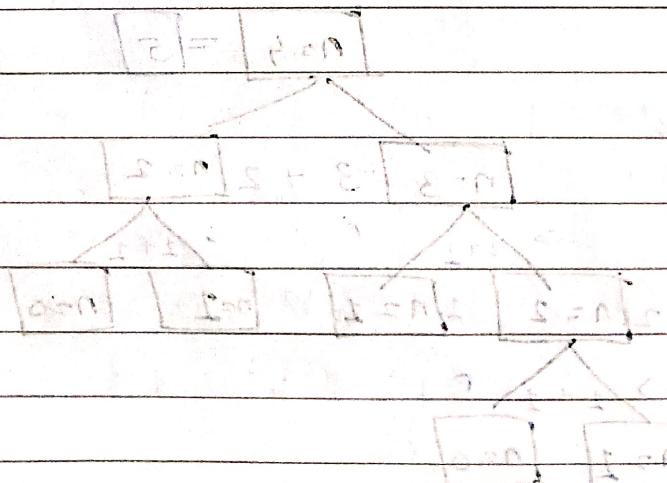
pair  $\rightarrow$   $a, b, c$  } 3 ways  
 valid  $a, (b, c)$  } 6 ways.

(Allison is not paired with  $b, (a, c)$  and valid  $b, (a, c)$ )

choice.



```
// code
public static int friendPairing(int n) {
    if(n==1 || n==2) return n;
    int f1 = friendPairing(n-1);
    int f2 = friendPairing(n-2) * (n-1);
    return (f1 + f2);
}
```



## # Python

### Q. Binary String problem

- Print all binary strings of size  $N$  without consecutive ones.

→ ex: 0000, 0101, 10101, 1001 etc.

```
// code in public static void printBinaryString(int n, int lp, String str) {
    if (n == 0) {
        System.out.println(str);
        return;
    }
    printBinaryString(n-1, lp, str+0);
    if (lp == 0) {
        printBinaryString(n-1, 1, str+1);
    }
}
```

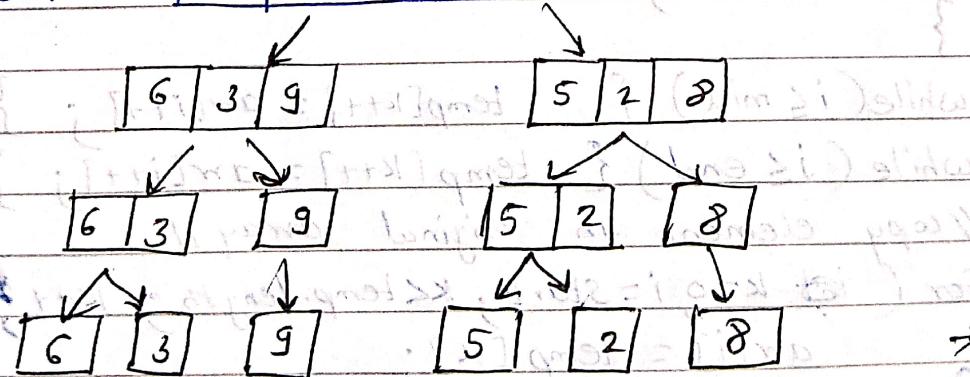
main method  $\Rightarrow$  printBinaryString( $n=0$ , "", "");

## \* Divide & Conquer :-

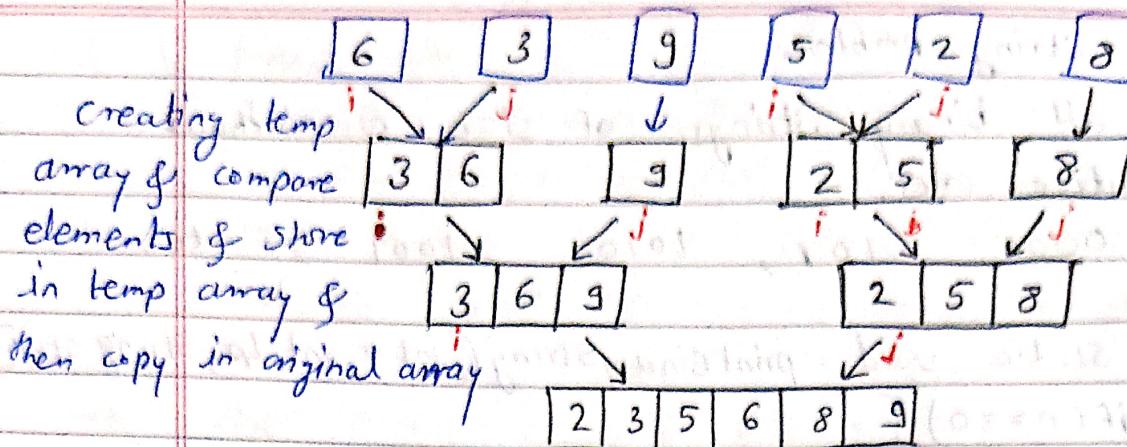
- that means divide the big problems in shortest problem and find the soln then combine the solns.

### 1) Merge Sort :

ex: arr = [6 3 9 5 1 2 8] {



→ they are already sorted.



**Code 1**

```
public static void mergesort(int arr[], int start, int end){
```

```
    if(start > end) return;
```

```
    int mid = start + (end - start)/2;
```

**Time**  
 $O(\log n)$

```
    mergeSort(arr, start, mid);
```

```
    mergeSort(arr, mid+1, end);
```

```
    merge(arr, start, end, mid); // time  $O(n)$ 
```

```
}
```

public static void merge(arr, start, end, mid){

```
    int [] temp = new int [end - start + 1];
```

```
    int i = start, j = mid + 1;
```

```
    int k = 0;
```

while ( $i \leq mid$  & &  $j \leq end$ ) {

    if ( $arr[i] < arr[j]$ ) {

```
        temp[k] = arr[i]; i++;
```

} else {

```
        temp[k] = arr[j]; j++;
```

} k++;

while ( $i \leq mid$ ) { temp[k++] = arr[i++]; }

while ( $j \leq end$ ) { temp[k++] = arr[j++]; }

// copy elements in original array

```
for (int k=0, i=start, k<temp.length, i++, k++) {
```

```
    arr[i] = temp[k];
```

}

} time complexity =  $O(n \log n)$

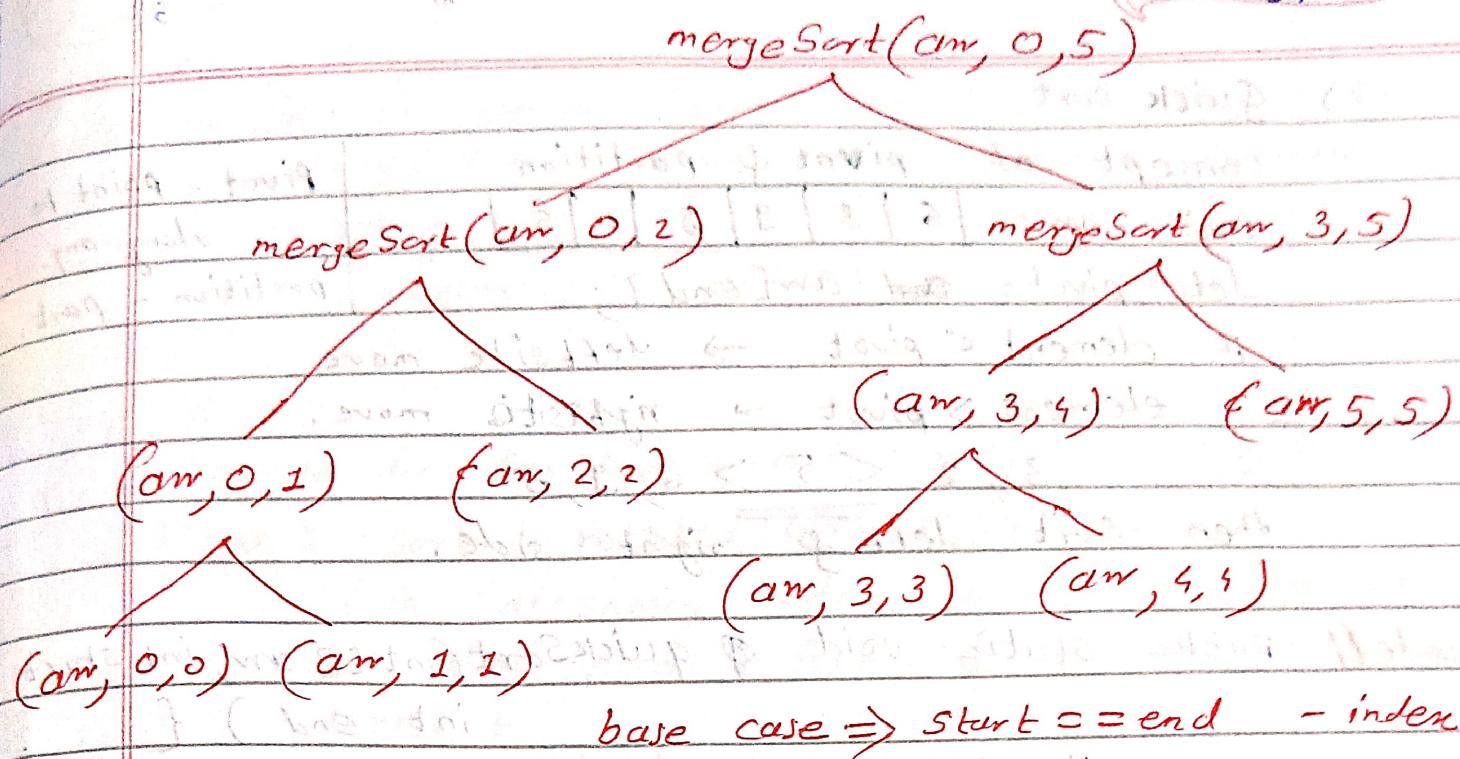
line 4 & 5 function calling tree.

classmate

Date \_\_\_\_\_

Page \_\_\_\_\_

37



Time complexity of recursion:

time =  $(\text{number of calls})^{\text{height of tree}}$  other work.

~~$\approx (\log n)^n$~~

$\{$  (base, start, end) initiating the while loop  $\}$

$\{$  if  $\{ \text{base} > \text{end} \}$  then  $\{ \text{return} \}$   $\}$

$\{$  if  $\{ \text{base} < \text{end} \}$  then  $\{ \text{mid} = \text{base} + \text{end} / 2 \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{temp} = \text{array}[\text{mid}] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{temp} = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid}] = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid} + 1] = \text{array}[\text{mid}] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid}] = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid} + 1] = \text{array}[\text{mid}] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{temp} = \text{array}[\text{mid}] \}$   $\}$

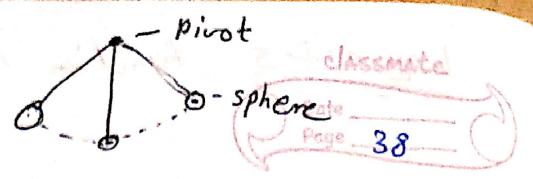
$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{temp} = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid}] = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid} + 1] = \text{array}[\text{mid}] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] > \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid}] = \text{array}[\text{mid} + 1] \}$   $\}$

$\{$  if  $\{ \text{array}[\text{mid}] < \text{array}[\text{mid} + 1] \}$  then  $\{ \text{array}[\text{mid} + 1] = \text{array}[\text{mid}] \}$   $\}$



## 2) Quick sort

concept of pivot & partition

e.g.: arr = [ 6 | 3 | 9 | 8 | 2 | 5 ]

let pivot = arr[end];

if element < pivot  $\rightarrow$  leftsite move

element > pivot  $\rightarrow$  rightsite move.

$\therefore 3, 2 < 5 > 6, 9, 8$

then sort left & right side.

Pivot - point to  
along any....  
partition - part.

//code// public static void quickSort(int[] arr, int start  
int end) {

int if(start > end) return;

int pIdx = partition(arr, start, end);

quickSort(arr, start, pIdx - 1);

quickSort(arr, pIdx + 1, end);

}

public static int partition(arr, start, end) {

int pivot = arr[end];

int i = start - 1;

for (int j = 0; j < end; j++) {

if (arr[j] < pivot) {

i++;

int temp = arr[i];

arr[i] = arr[j];

arr[j] = temp;

}

i++;

int temp = pivot;

arr[end] = arr[i];

arr[i] = temp;

return i;

}

**Note:** The worst case of quick sort is when pivot is always the smallest or the largest element in array.  
time complexity =  $O(n^2)$

g. Search in rotated sorted array

**Input:** sorted, rotated with distinct numbers

(in ascending order) it is rotated at a pivot point, find the index of given element.

eg: arr = [4 | 5 | 6 | 7 | 0 | 1 | 2 ]

target = 0

ans = 4

```
1) code
public static int searchInRotatedArr(int arr[],  

                                     int start, int end, int target) {  

    int mid = start + (end - start) / 2;  

    if (target == arr[mid]) return mid;  

    // case 1  

    if (arr[start] <= arr[mid]) {  

        if (arr[start] <= target && target <= arr[mid]) {  

            return searchInL(arr, start, mid-1, target);  

        } else {  

            return searchInR(arr, mid+1, end, target);  

        }
    } else {  

        if (arr[end] >= target && target > arr[mid]) {  

            return searchInR(arr, mid+1, end, target);  

        } else {  

            return searchInL(arr, start, mid-1, target);  

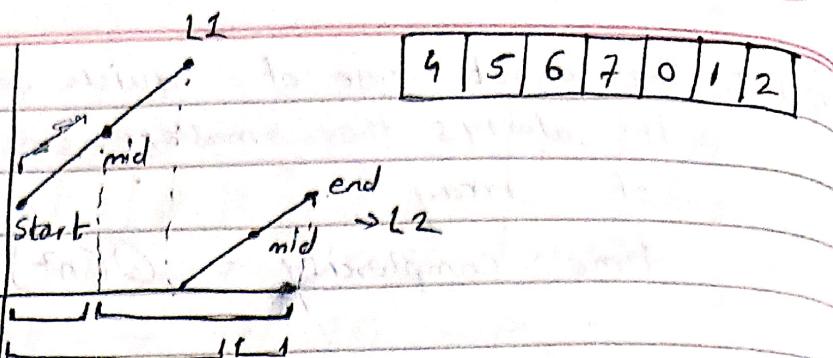
        }
    }
}
```

explanation:

- 1)  $\text{start} \leq \text{target} \leq \text{mid}$  ( $L_1$ )
- 2)  $\text{mid} \leq \text{target} \leq \text{end}$  ( $L_2$ )

otherwise search in

remaining part.



Search algorithm in array

do something difficult plus bad code, better to just do whatever it is in C++ programming etc.

using the standard `l` & `r` of `l` & `r` for loop

if  $(\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

then  $\text{start} = \text{mid} + 1$  &  $\text{end} = \text{mid} - 1$

else  $\text{start} = \text{start} + 1$  &  $\text{end} = \text{end} - 1$

$\{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \text{else } \text{start} = \text{start} + 1 \text{ and } \text{end} = \text{end} - 1$

$\quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \quad \quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \quad \quad \quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \quad \quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

$\quad \quad \quad \quad \quad \quad \quad \{\text{if } (\text{start} \leq \text{target} \leq \text{mid}) \text{ or } (\text{mid} \leq \text{target} \leq \text{end})$

$\quad \quad \quad \quad \quad \quad \quad \quad \text{then } \text{start} = \text{mid} + 1 \text{ and } \text{end} = \text{mid} - 1$

g. Practice set question  $\rightarrow$  Inversion count.

Ex: 1) arr = {2, 4, 1, 3, 5}; cond? arr[i] > arr[j]

ans = 3  $\Rightarrow$  (2, 4), (4, 1), (4, 3).

2) arr = {5, 4, 3, 2, 1}

ans = 10  $\Rightarrow$  (5, 4), (5, 3), (5, 2), (5, 1),

(4, 3), (4, 2), (4, 1),

(3, 2), (3, 1), (2, 1).

How to calculate?

Ans: If we consider 4 pairs at a time then how many pairs

are there and then if we do it in below way

[2] pair can make  $\leftarrow$

[2][8][2][1]  $\leftarrow$  also possible ratio

[2][8][2][0][1]  $\leftarrow$  also possible (5-7) sort pattern ratio

and so on for other ratios

(arr[i], j) for (arr[i] < arr[j]) which is the below slide will help you

for better understanding of how to calculate

(arr[0], m = i) for i = 0 to n-1

①  $\rightarrow$  arr[0] < (arr[1], m = i) for i = 1 to n-1

arr[0] < arr[1]

arr[0] < arr[2]  $\rightarrow$  arr[0] < arr[1] and arr[0] < arr[2]

②  $\rightarrow$  arr[0] < (arr[1], m = i) for i = 1 to n-1

arr[0] < arr[1] and arr[0] < arr[2]  $\rightarrow$  arr[0] < arr[1] and arr[0] < arr[2]

(arr[0], m = i) so possible ratio is increasing on i: ① arr[0] <

arr[1] < arr[2] ... mth last letter is ② arr[0] <

What if now 5 is given and consider in ③ arr[0] < arr[1] and

arr[0] < arr[2] and arr[0] < arr[3] and arr[0] < arr[4]

.(5, 0, m = i) which is the above  $\leftarrow$  abnormal

ratio because if we take 5 then 5 is not less than 5

## \* Backtracking:

Type of Backtracking.

1) Decision Decision :

2) Optimization :

3) Enumeration : (possible soln list)

- backtracking is also recursion, but do work by recursion when it will be return for ex. given.

g. for odd element in array & subtract by 2 each value when it will be return.

$\rightarrow$  arr = new int[5]

after adding ele  $\rightarrow$ 

1	2	3	4	5
---	---	---	---	---

when return the (-2) each ele  $\rightarrow$ 

-1	0	1	2	3
----	---	---	---	---

II code || public static void addEleInArr(int[] arr, int i, int val){

// base case //

if(i == arr.length)

printArr(arr);

return;

}

arr[i] = val;

addEleInArr(arr, i+1, val+1);

arr[i] = arr[i]-2;

}

- ⑦

- ⑧

- ⑨

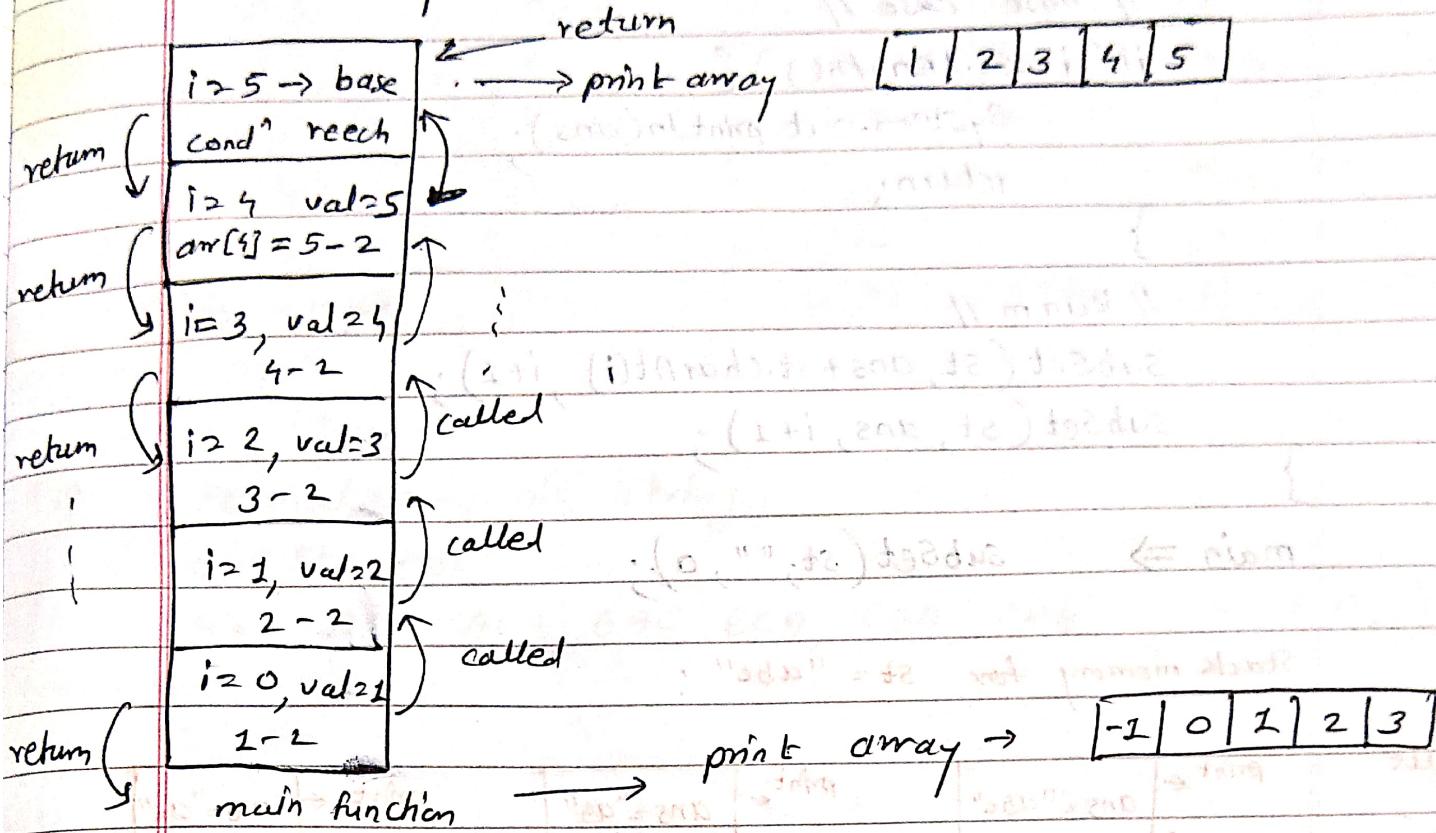
- Line ⑦ is the print arr ele when adding ele (function)
- Line ⑧ is called function
- Line ⑨ is subtract each value by 2 when it will be return

main  $\Rightarrow$  addEleInArr(arr, 0, 1);

O/P : 1, 2, 3, 4, 5

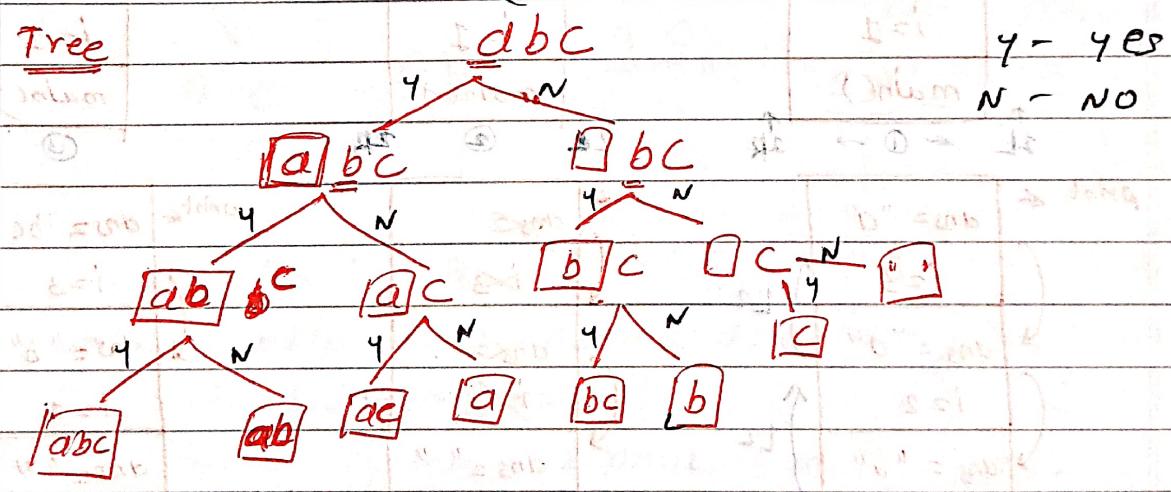
-1, 0, 1, 2, 3

## Stack memory



## Q. Subset of string

→ ex: st = "abc" → abc, ab, ac, a, bc, b, c, ...  
 total = 8 subset ( $2^3$ ).

Tree

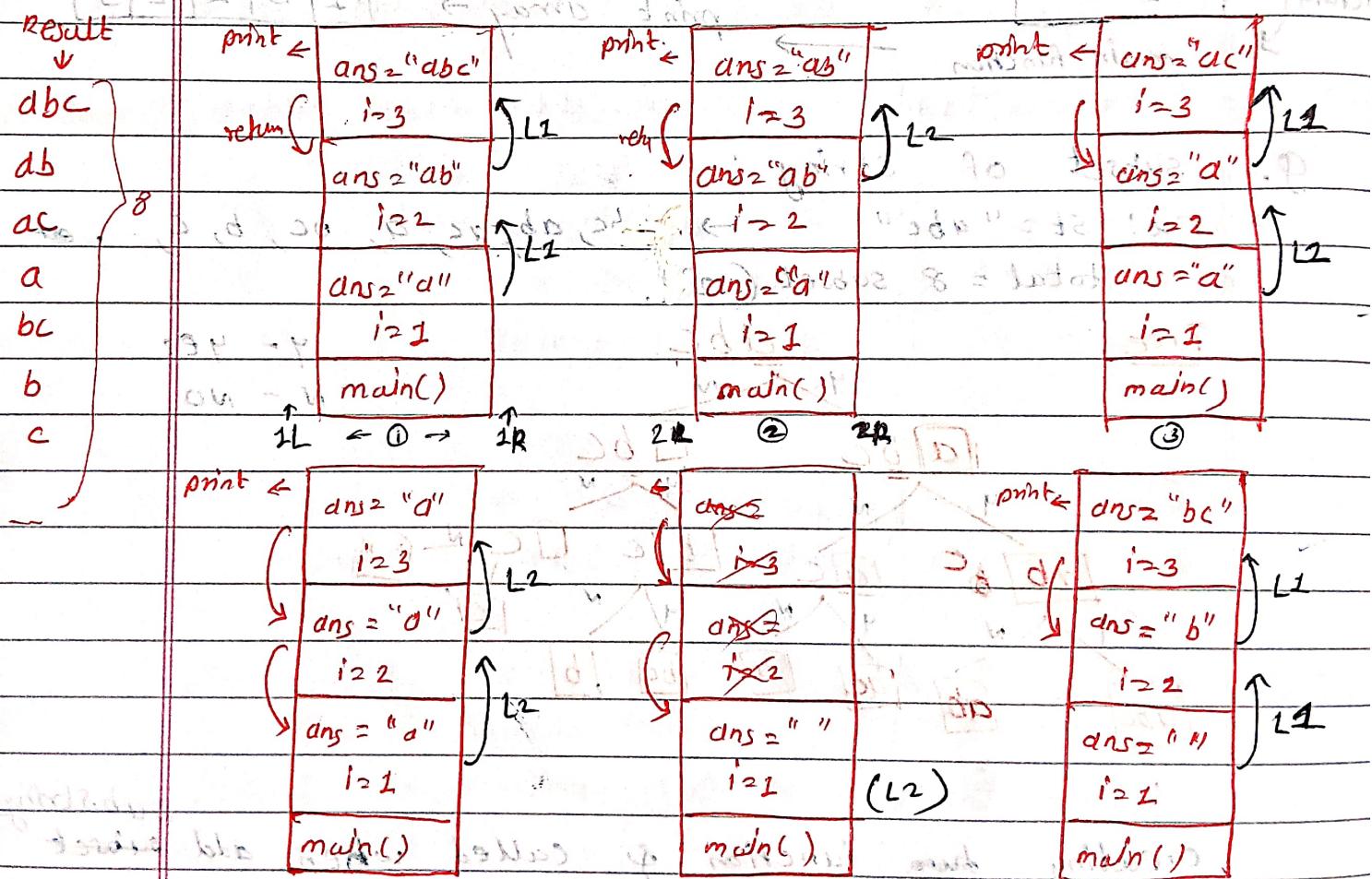
Creating two function & called when add subset.  
 & called when no add  
 subset (st, ans + st.charAt(i), i+2)  
 subset (st, ans, i+1).

```
// Code 11 public static void subset(String st, String ans, int i) {
    // base case //
    if(i == st.length()) {
        System.out.println(ans);
        return;
    }

    // kaam //
    subset(st, ans + st.charAt(i), i + 1);
    subset(st, ans, i + 1);
}

main => subset(st, "", 0);
```

Stack memory for  $st = "abc"$ :



Now read this stack:  $\rightarrow (i+1)$

print $\leftarrow$	ans = "b"
(	i = 3
(	ans = "b"
(	i = 2
(	ans = ""
(	i = 1
(	main()

print $\leftarrow$	ans = "c"
(	i = 3
(	ans = "c"
(	i = 2
(	ans = "
(	i = 1
(	main()

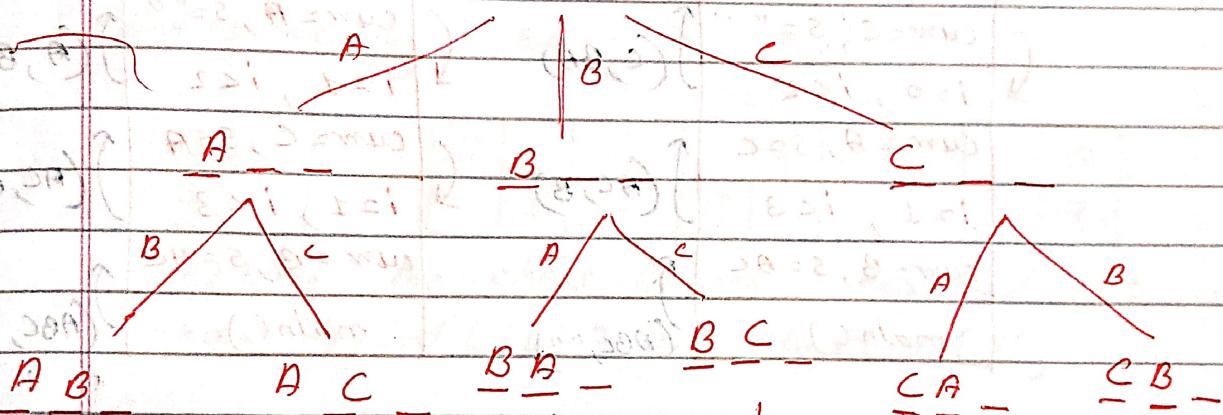
print $\leftarrow$	ans = "
(	i = 3
(	ans = "
(	i = 2
(	ans = "
(	i = 1
(	main()

\* q.

Permutation of String.

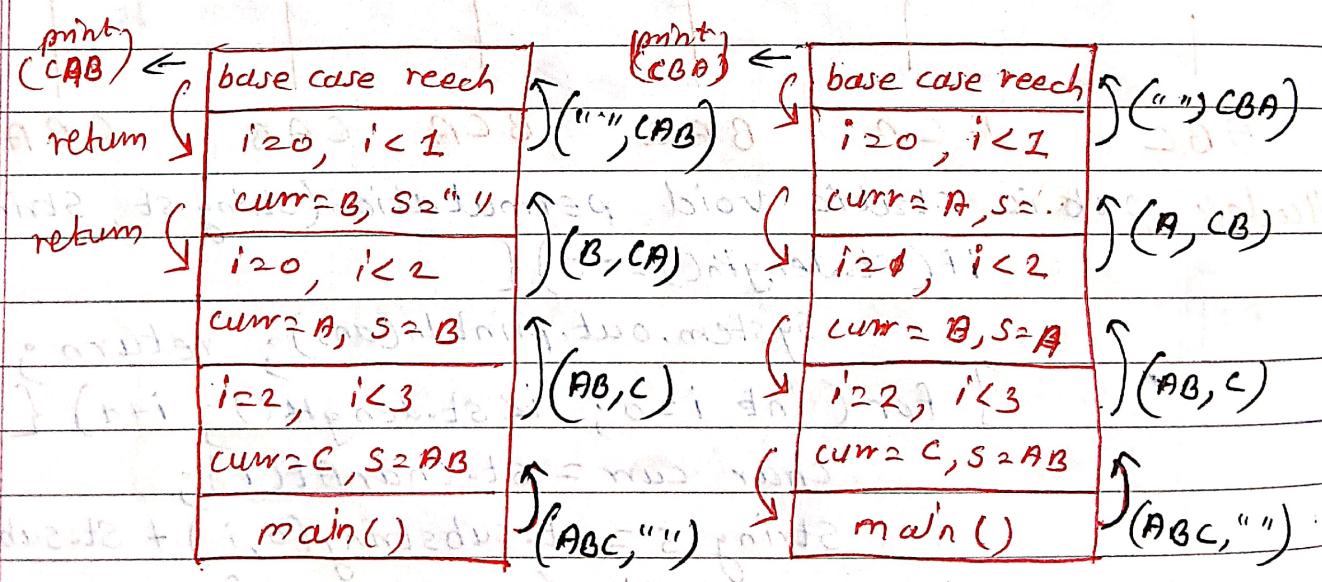
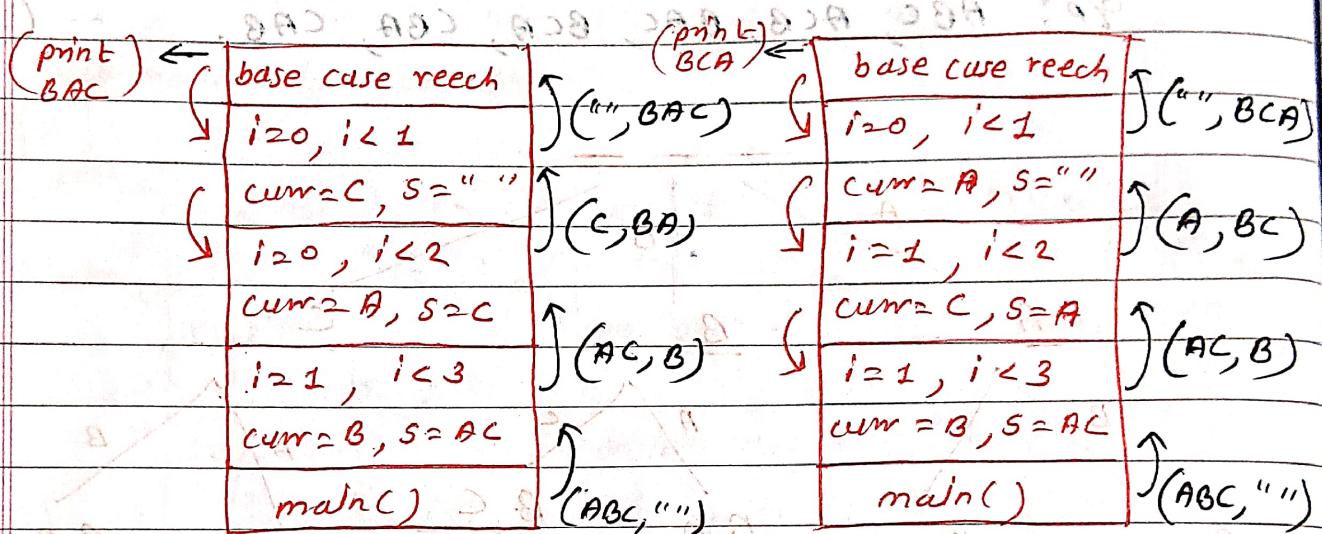
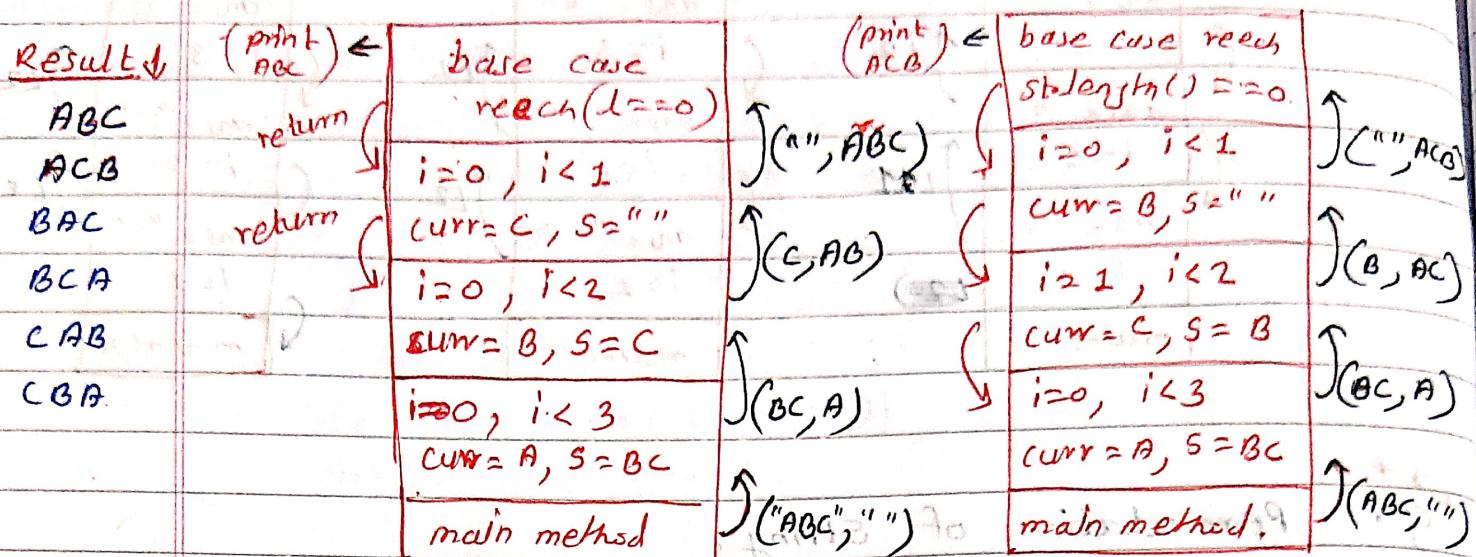
$\rightarrow$  ex: st = "ABC"

O/P: ABC, ACB, BAC, BCA, CBA, CAB. ... ( $n!$ )



```
// code
public static void permutation(string st, string ans) {
    if (st.length() == 0) {
        System.out.println(ans);
        return;
    }
    for (int i = 0; i < st.length(); i++) {
        char curr = st.charAt(i);
        String s = st.substring(0, i) + st.substring(i+1);
        permutation(s, ans + curr);
    }
}
```

## \* Stack memory : \*



(end recursion)

## Q. N-queens

- Place ~~N~~ N-queens on an  $N \times N$  chessboard such that no 2 queens can attack each other.

- ex:  $N=4$

ans:

	Q		
			Q
		Q	
			Q

ans:

	Q		
			Q
		Q	
			Q

direction of queen does not attack to each other.

## Approach

- 1) Set one queen in each row but diff. column.
- 2) check which places can be safe for queen.
- 3) print no. of ways of soln.

line 1 meaning: (ex -  $N=2$ )

Q	
Q	
	Q
	Q

creating the chessboard required 2D - array.

char board[ ][ ] = new char[N][N];

Logic:

- creating function ~~using~~ placing queen & pass the parameter board[ ][ ], & row[ ].
- then place the one queen in every row but ~~diff. column~~.

① For (int j=0 ; j< board.length ; j++) {

②     board [row] [j] = 'Q' ;

③ } else nQueens (board, row+1);     recursion

④     board [row] [j] = '-' ;     - backtrack

}

- line ③ → place the N-queens, by calling function  
 when base reach then print board & return  
 then board is clean for second possible set seating queen  
 - when function return, then required board is  
 clean for second possible set seating queen  
 - by using line ④ backtrack for board clean.

wrote down the code for check every queen  
 can be safe to place in every place.  
 this cond apply before seating the queen.

```
//code
public static void nqueens(char board[][], int row){
    // base case
    if (row == board.length) {
        printBoard(board);
        return;
    }
    // kaam
    for (int j = 0; j < board.length; j++) {
        if (isSafe(board, row, j)) {
            board[row][j] = 'Q';
            nqueens(board, row + 1);
            board[row][j] = '-';
        }
    }
}

function → printBoard(char board[][]) {
    // nested loop to print
    // 2D array
}
```

time complexity =  $O(n!)$

classmate

Date \_\_\_\_\_

Page \_\_\_\_\_

49

// function to check - queen is safe //

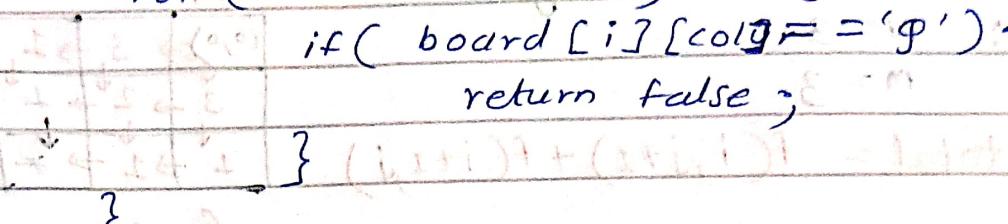
public static void boolean issafe( board, row, col) {

// In column // i < n (1-n)

for( int i = row-1 ; i >= 0 ; i-- ) {

if( board [i] [col] == 'Q' ) {

return false;



// In left upper diagonal //

for( int i = row-1, j = col-1 ; i >= 0 && j >= 0 ; i--, j-- ) {

if( board [i] [j] == 'Q' ) {

return false;

}

// In right upper diagonal //

for( int i = row-1, j = col+1 ; i >= 0 && j < board.length

- 1 ; i-- , j++ ) {

if( board [i] [j] == 'Q' ) {

return false;

}

} { const char (char) = 'Q'; } = queen

return true;

}

public static void main( String [] args ) {

Scanner sc = new Scanner( system.in );

int n = sc.nextInt();

for( int i = 0 ; i < n ; i++ ) {

for( int j = 0 ; j < n ; j++ ) {

board [i] [j] = '-' ;

}

}

nqueens( board, 0 );

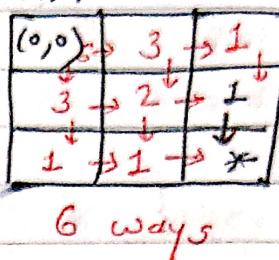
}

## Q. Gridways:

- find numbers of ways to reach from  $(0, 0)$  to  $(N-1, m-1)$  in a  $N \times M$  grid grid.
- Allowed moves - right or down.

 $\rightarrow$  ex:  $N = 3$  $M = 3$ 

$$\text{total} = f(i, j+1) + f(i+1, j)$$



```
// code1
public static int gridWays(int i, int j, int right, int down){
```

```
    if(i == right-1 && j == down-1) {
```

```
        return 1;
```

```
    } else if(i == right || j == down) {
```

```
        return 0;
```

```
    }
```

```
    int w1 = gridWays(i, j+1, right, down);
    int w2 = gridWays(i+1, j, right, down);
    return w1+w2;
}
```

time complexity =  $O(2^{n+m})$

right turn = no. of col =  $m$   
down turn = no. of row =  $n$

shortcut trick:  $\text{ans} = \frac{(n-1 + m-1)!}{(n-1)!(m-1)!}$

ex: n=3, m=3 ans = 6 ways

$$\text{ans} = \frac{(3-1 + 3-1)!}{(3-1)!(3-1)!} = \frac{4!}{2! \cdot 2!} = 6 \text{ ways}$$

(0, blank) example

g. write the function to complete sudoku.

- rule: same column & same row does not repeat number.



## \* ArrayList :

\* Multidimensional ArrayList

↳ `ArrayList<ArrayList<Integer>> list = new ArrayList<>();`

Normal → `list = new ArrayList<type>();`

g. create 2D array list like

`[[3,3,4],[5,6,7],[8,9,10]]`

~~Code~~ public static void main(String [] args) {

`ArrayList<ArrayList<Integer>> list =`

`new ArrayList<>();`

`// list 1 //`

`ArrayList<Integer> list1 = new ArrayList<>();`

`list1.add(2);`

`list1.add(3);`

`list1.add(4);`

`// list 2 //`

`ArrayList<Integer> list2 = new ArrayList<>();`

`list2.add(5);`

`list2.add(6);`

`list2.add(7);`

`ArrayList<Integer> list3 = new ArrayList<>();`

`list3.add(8);`

`list3.add(9);`

`list3.add(10);`

`// add all list in 2D list //`

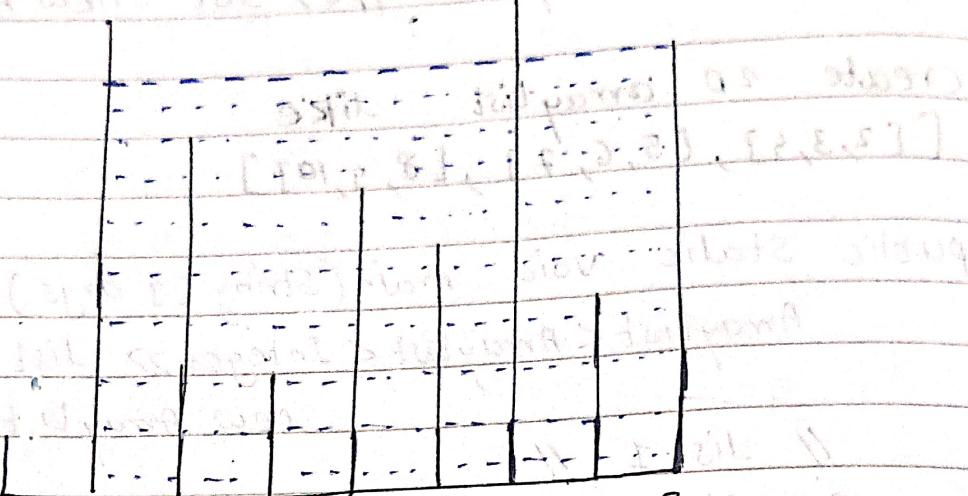
`list.add(list1);`

`list.add(list2);`

`list.add(list3);`

`}`

- Q. Calculate stored water in container gives height of container.  
 $\rightarrow \text{height} = [1, 8, 6, 2, 5, 4, 8, 3, 7]$



height  $\rightarrow 1 \ 8 \ 6 \ 2 \ 5 \ 4 \ 8 \ 3 \ 7$

idx  $\rightarrow (0) \ (1) \ (2) \ (3) \ (4) \ (5) \ (6) \ (7) \ (8)$

$\rightarrow$  Solve this question by assume any two pole & assume two pole is container then calculate the max store water.

- bet" two pole width is 1.

assume: for ex:

1) bet" i=0 & i=2  $\rightarrow$   $(1 \ 8 \ 6 \ 2 \ 5 \ 4 \ 8 \ 3 \ 7)$

2) bet" i=1 to i=5  $\rightarrow$   $(1 \ 8 \ 6 \ 2 \ 5 \ 4 \ 8 \ 3 \ 7)$

3) bet" i=3 to i=4  $\rightarrow$   $(1 \ 8 \ 6 \ 2 \ 5 \ 4 \ 8 \ 3 \ 7)$

etc selecting any two pole & calculate all container area & compare area with current and print max area.

for this approach use the concept of possible pair of Array.

```
// code11
public static void storedWater(ArrayList<Integer> height)
{
    // brute force approach //
    int l = height.size();
    int maxWater = 0;
    int b1 = 0, b2 = 0;
    for (int i = 0; i < l; i++) {
        for (int j = i + 1; j < l; j++) {
            int hei = Math.min(height.get(i), height.get(j));
            int wei = j - i;
            time complexity = O(n^2)
            int curWater = hei * wei;
            if (maxWater < curWater) {
                b1 = height.get(i);
                b2 = height.get(j);
                maxWater = curWater;
            }
        }
    }
    System.out.println("Max water height boundaries :" + b1 + "," + b2);
    System.out.println("Max water contains :" + maxWater);
}
```

// two pointer approach //

```
// code11
public static void storedWater(ArrayList<Integer> height) {
    int l = height.size(), lp = 0, rp = 0, storedWater = 0;
    while (lp < rp) {
        if (height.get(lp) < height.get(rp)) {
            time complexity = O(n)
            lp++;
        } else {
            linear t.c.
            rp--;
        }
        int hei = Math.min(height.get(lp), height.get(rp));
        int wei = rp - lp;
        int curWater = hei * wei;
```

```

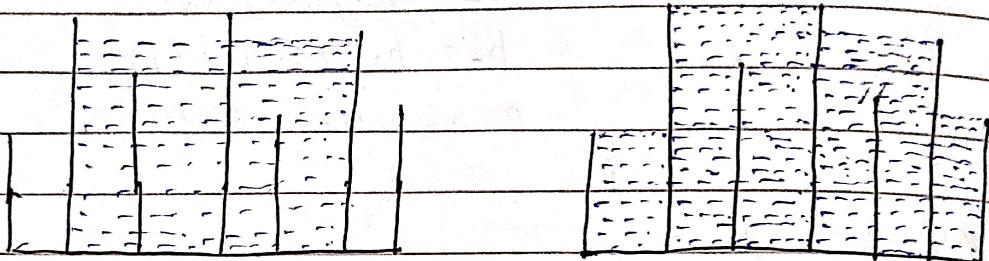
if( storedWater < curWater ){
    storedWater = curWater;
}
}

```

```
System.out.println("Max stored water : " + storedWater);
```

- \* Trapping rain water  $\rightarrow$  stored all water betw  
all poles
- \* contain max stored water  $\rightarrow$  water stored betw  
two poles.

ex:



water store container. Trapping rain water

Q. Pair sum to equal target number in sorted list

$\rightarrow$  ex: list = [1, 2, 3, 4, 5] target = 8

ans = 2, 4  $\rightarrow$  idx.

// code //

brute force approach  $O(n^2)$

```

public static void pairSum(List list, int target) {
    int l = list.size();
    for (int i = 0; i < l; i++) {
        for (int j = i + 1; j < l; j++) {
            if (list.get(i) + list.get(j) == target) {
                printf("Index : %d, %d", i, j);
                break;
            }
        }
    }
}

```

this approach use sorted &  
unsorted list/array.

// two pointer approach //  $O(n)$

```
public static void pairSum(List<Integer> list, int target) {
    int l = list.size();
    int lp = 0, rp = l - 1;
    while (list.get(lp) + list.get(rp) != target) {
        if (list.get(lp) + list.get(rp) < target) {
            lp++;
        } else {
            rp--;
        }
    }
    System.out.printf("Index : %d, %d", lp, rp);
}
```

Q. Pair sum of sorted Rotated List.

→ ex: list = [4, 5, 6, 1, 2, 3]. target = 10  $\rightarrow$  (0, 2).

Step 1: First find pivot point

Step 2: then point the lp & rp

Step 3: use formula  $lp = (lp + 1) \% d$  &  $rp = (rp - 1 + l) \% d$  } for cyclic more.

Note: % is use in diff. place in competitive programming (search it).

Code // public static void pairSumRotatedList(List<Integer> list, int target) {

int lp = 0, rp = 0;

int l = list.size();

for (int i = 0; i < l - 1; i++) {

if (list.get(i) > list.get(i + 1)) {

rp = i; lp = i + 1;

break;

}

$O(n)$

```

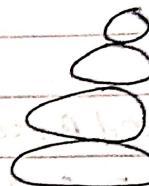
        while(jist.get(lp) + jist.get(rp) != target) {
            if(jist.get(lp) < target) {
                lp = (lp + 1) % l;
            } else {
                rp = (rp - 1 + l) % l;
            }
        }
        System.out.printf("Index : %d, %d, lp, rp);
```

### \* Stack :

- ex: coins, books in stack.



coins



stones

- \* operation :

- 1) push :  $O(1)$
- 2) pop :  $O(1)$
- 3) peek :  $O(1)$

- \* LIFO  $\rightarrow$  Last in first out or先进后出

- \* Implementation :

Array

ArrayList

LinkedList

fixed size

1	2	3
---	---	---

variable size

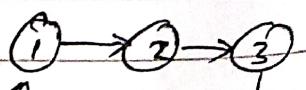
1	2	3
---	---	---

top

1	2	3	4	5
---	---	---	---	---

top

variable size



head

head

Note: for implement stack best is ArrayList  
linkedlist.

1) Implement stack by using ArrayList,

first import java.util.ArrayList;

// code

```
static class Stack {  
    public static boolean isEmpty() {  
        return list.size() == 0;  
    }
```

// push //

```
public static void push(int data) {  
    list.add(data);  
}
```

// peek //

```
public static int peek() {  
    return list.get(list.size() - 1);  
}
```

// pop //

```
public static int pop() {  
    int top = list.get(list.size() - 1);  
    list.remove(list.size() - 1);  
    return top;  
}
```

}

```
public static void main(String[] args) {
```

```
    Stack stack = new Stack();
```

```
    stack.push(1); stack.push(2); stack.push(3);
```

```
    while (!stack.isEmpty()) {
```

```
        System.out.println(stack.peek());
```

```
        stack.pop();
```

}

%p: 3

2

1

Q70  
By using linkedlist implement stack.

```

//code1 static class Node {
    int data;
    Node next;
    Node (int data) {
        this.data = data;
        this.next = null;
    }
}

static class Stack {
    static Node head = null;

    // empty
    public static boolean isEmpty() {
        return head == null;
    }

    // push
    public static void push(int val) {
        Node temp = new Node(val);
        if (head == null) {
            head = temp;
            return;
        }
        temp.next = head;
        head = temp;
        return;
    }

    // peek
    public static int peek() {
        return head.data;
    }
}

```

```

// pop()
public static int pop() {
    int top = head.data;
    head = head.next;
    return top;
}

public static void main(String[] args) {
    Stack s = new Stack();
    s.push(1);
    s.push(2);
    s.push(3);
    while (!isEmpty()) {
        System.out.println(stack.peek());
        stack.pop();
    }
}

```

## 4. Stack using framework:

```

// code
import java.util.*;

public static void main(String args[]) {
    Stack<Integer> s = new Stack();
    s.push(1);
    s.push(2);
    s.push(3);
    while (!isEmpty()) {
        System.out.println(s.peek());
        s.pop();
    }
}

```

amazon

g. Push at the bottom of the stack.

→ stack = 

3
---

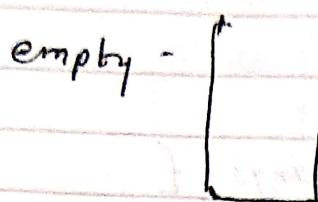
 and add 4 in bottom

Ex:

3
2
1

• first to do empty or

stack then add 4 then  
add push odd data.



add 4 →

4

odd odd →  
data

3
2
1
4

- These question also solve by using loop.  
but better ans by recursively.

// code

```
public static void putBottomOfStack(Stack<Integer> s1, int num) {
```

// base case //

if(s1.isEmpty()) {

s1.push(num);

return;

}

// Recur //

int data = s1.pop();

putBottomOfStack(s1, num);

s1.push(data);

public static void main(String[] args) {

Stack<Integer> s1 = new Stack();

s1.push(1); s1.push(2); s1.push(3);

putBottomOfStack(s1, 4);

while(!s1.isEmpty()) {

System.out.println(s1.pop());

O(n)

O/P: 3

2

1

4

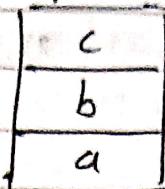
IMP

- Reverse the string by using stack.

→ In method pass String as parameter & create Character Stack in method & stored each character in stack and print.

Ex: St = "abc"

→



→ "cba"

- when then create String builder and append each character (in present of stack) by using sb.append(s.pop()). (use while loop).
- In last convert StringBuilder to string [sb.toString();]

```
//code11 public static void reverseString(Stack<Character> st) {
    Stack<Character> s = new Stack();
    int i=0, l=st.length();
    while (i != l) {
        s.push(st.charAt(i));
        i++;
    }
    String Builder sb = new String Builder("");
    while (!s.isEmpty()) {
        sb.append(s.pop());
    }
    return sb.toString();
}
```

IMP

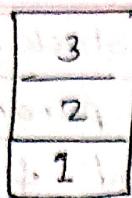
9. Reverse stack. (by recursion)

→ - by using recursion to do empty stack.

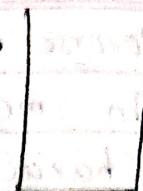
- when recursion is return then backtrace by function → putAtBottom();

- using this function each each element go to the bottom when recursion is return,

ex: d = 1 2 3



→ by using recursion →

(but store each value  
in top variable)

empty

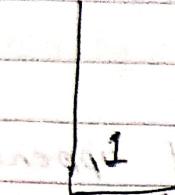
start of algorithm

2 nodes

3 nodes

↑ return back stack to arguments

1) when return



→

d

.

1

base case has reached

value 1 (starts to call by putAtBottom(top))

reverseStack

1

2

3

2 nodes, stack needs

base case has reached

value 2 (starts to call by putAtBottom(top))

reverseStack

1

2

3

3 nodes, stack needs

base case has reached

value 3 (starts to call by putAtBottom(top))

reverseStack

1

2

3

stack is empty

return;

{

}

int top = s.pop();

reverseStack(s);

putAtBottom(s, top);

{

}

start of algorithm

3 nodes, stack needs

base case has reached

value 3 (starts to call by putAtBottom(top))

reverseStack

stack is empty

return;

~~very imp logic~~

- Q. Next greater element in array (time comp =  $O(n)$ ).  
 → this question also solve by nested loop but time complexity is  $O(n^2)$ . hence, these question solve by stack.

arr:	arr = [8   6   4   7   5   9   10   8   12]
	ans = [9   7   7   9   9   10   12   12   -1]

```

public static void int[] nextGreaterEle (int arr[], int ans[]){
    Stack<Integer> s = new Stack();
    int l = arr.length;
    for (int i=0; i < l; i++) {
        while (!s.isEmpty() && arr[s.peek()] < arr[i]) {
            ans[s.pop()] = arr[i];
        }
        s.push(i);
    }
    if (s.isEmpty() || i == l-1) ans[i] = -1;
    return ans;
}
  
```

Time complexity: O(n) + O(n) = O(2n) = O(n)

Space complexity: O(n) (stack space)

Optimized approach: O(n) + O(n) = O(2n) = O(n)

Space complexity: O(1) (no extra space)

Approach: Using two stacks

Stack 1: arr >= 2 <= nextGreaterElement

Stack 2: arr <= 2 <= nextGreaterElement

Approach: Using two stacks

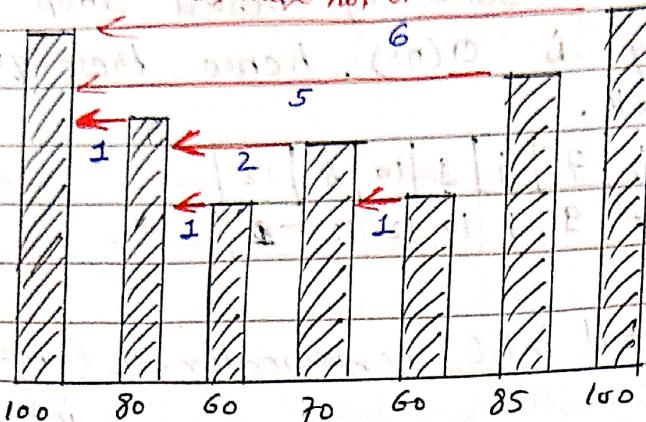
Stack 1: arr >= 2 <= nextGreaterElement

Stack 2: arr <= 2 <= nextGreaterElement

Approach: Using two stacks

### Q. Stock Span problem.

↳ max no. of consecutive day.



time complexity,  
 $O(n)$

Stock [] =	100	80	80	70	60	85	100
Span []	1	1	1	2	1	5	6

- return this ans

Note: these question also solve by nested loop

- Step 1) create stack of Integer type & push 0.
- 2) stored 1 in Span array at zeroth index.
- 3) while stack is not empty & prices < today price  
that mean  $\text{stock}[\text{s.peek}()] < \text{stock}[\text{i}]$  then pop out of the top value.
- 4) Store in Span  $\rightarrow \text{i} - \text{s.peek}()$  in out of while loop
- 5) push each index in stack  $\rightarrow \text{s.push}(\text{i})$ ;
- 6) print /return span array.

```

1 code
public static int[] stockSpan(int[] stock) {
    Stack<Integer> s = new Stack();
    int span[] = new int[stock.length];
    s.push(0);
    span[0] = 1;
    for (int i=1; i<stock.length; i++) {
        while (stock[s.peek()] < stock[i]) {
            s.pop();
        }
        span[i] = i - s.peek();
        s.push(i);
    }
    return span;
}
  
```

### 9. Valid Parentheses:

- Given a string  $s$  containing just the characters ' $($ ', ' $)$ ', ' $[$ ', ' $]$ ', ' $\{$ ', ' $\}$ ', determine if the input string is valid.
- An input string is valid if:
    - 1) Open brackets must be closed by the same type of brackets.
    - 2) Open brackets must be closed in the correct order.
    - 3) Every close bracket has a corresponding open bracket of the same type.

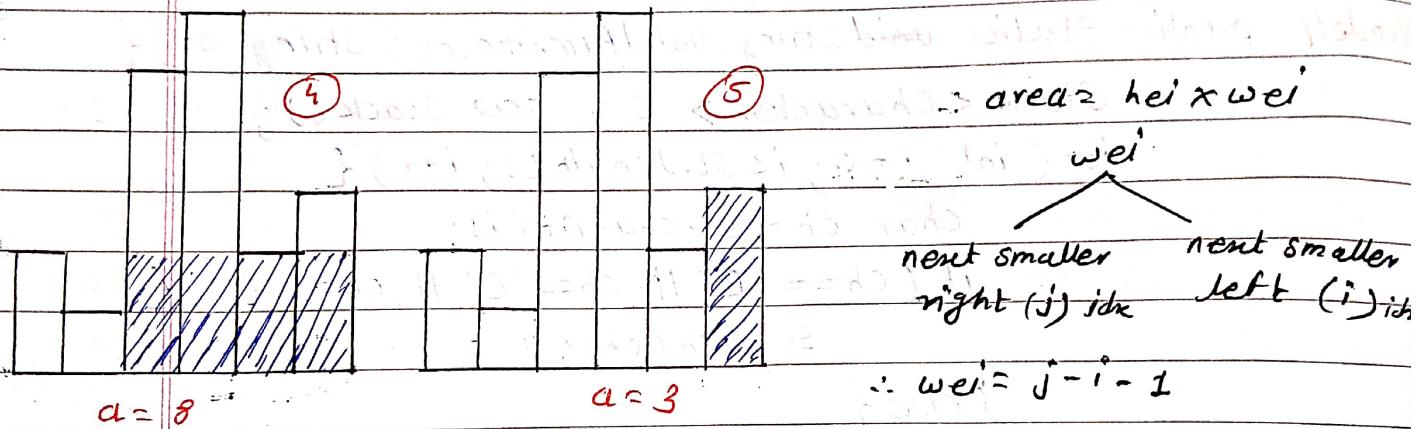
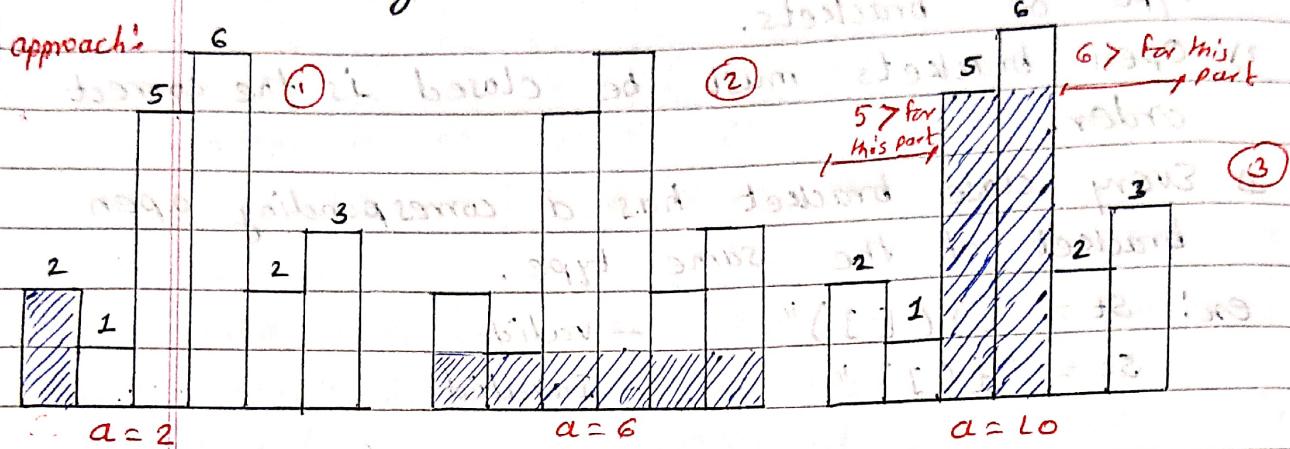
ex:  $s = "[]{}()$ " - valid  
 $s = "[()]"$  - Invalid

```
//code11
public static void string ValidParentheses (String st) {
    Stack<Character> s = new Stack();
    for (int i=0; i < st.length(); i++) {
        char ch = st.charAt(i);
        if (ch == '[' || ch == ']' || ch == '{' || ch == '}') {
            s.push(ch);
        } else {
            if (s.isEmpty()) {
                return "Invalid";
            }
            if (s.peek() == '(' && ch == ')' || s.peek() == '[' && ch == ']' || s.peek() == '{' && ch == '}') {
                s.pop();
            } else {
                return "Invalid";
            }
        }
    }
    if (s.isEmpty()) return "Valid";
    else return "Invalid";
}
```

\*\*\* hard.

9. Max Area in Histogram! (use logic of next greater number)
- Given an array of integers heights representing the histogram's bar height where the width of each bar is 1, return the area of the largest rectangle in the histogram.
- Ex: height [7] = [2, 1, 5, 6, 2, 3]

approach:



∴ next smaller left (nsl) $i = \begin{bmatrix} -1 & -1 & 1 & 5 & 1 & 2 \end{bmatrix}$  } for understanding stored value but actual stored the index.

∴ next smaller right (nsr) $j = \begin{bmatrix} 1 & 6 & 2 & 2 & 6 & 6 \end{bmatrix}$  } for understanding stored value but actual stored the index.

for ①

$$a = h \times w$$

$$a = 2 \times (j - i - 1)$$

$$a = 2 \times (1 + 1 - 1)$$

$$a = 2$$

for ②:  $a = h \times w$ 

$$a = 1 \times (6 + 1 - 1)$$

$$a = 6$$

for ③:

$$a = h \times w$$

$$a = 5 \times (4 - 1 - 1)$$

$$a = 10$$

for ④:

$$a = 6 \times (4 - 2 - 1)$$

$$a = 6$$

$$a = 3 \times (6 - 4 - 1)$$

$$a = 3 \times (3 - 2 - 1)$$

// code 11: public static void maxArea(int arr[]) { // O(n).

```

    int maxArea = 0, l = arr.length;
    int nsr = new int[l];
    int nsL = new int[l];
    // next smaller right //
    Stack<Integer> s = new Stack();
    for (int i = l - 1; i >= 0; i--) {
        while (!s.isEmpty() && arr[s.peek()] > arr[i]) {
            s.pop();
        }
        if (s.isEmpty()) {
            nsr[i] = -1;
        } else {
            nsr[i] = s.peek();
        }
        s.push(i);
    }
    // next smaller left //
    s = new Stack();
    for (int i = 0; i < l; i++) {
        while (!s.isEmpty() && arr[s.peek()] > arr[i]) {
            s.pop();
        }
        if (s.isEmpty()) {
            nsL[i] = -1;
        } else {
            nsL[i] = s.peek();
        }
        s.push(i);
    }

```

$O(n)$

// curr area = width = j - i - 1 = nsR[i] - nsL[i] - 1 //

```

 $\Theta(n)$  {
    for( int i=0; i<l; i++ ) {
        int hei = arr[i];
        int wid = nsr[i] - nsf[i] - 1;
        int curArea = hei * wid;
        maxArea = Math.max( curArea, maxArea );
    }
}

```

```

System.out.print("Max area in histogram: ");
System.out.println(maxArea);

```

```

public class Histogram {
    public static void main( String[] args ) {
        int[] arr = { 2, 1, 4, 5, 1, 3 };
        System.out.println( "Max area = " + maxArea( arr ) );
    }

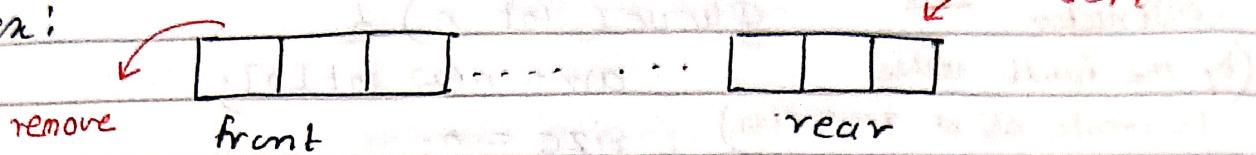
    public static int maxArea( int[] arr ) {
        int n = arr.length;
        int[] nsf = new int[n];
        int[] nsr = new int[n];
        nsf[0] = 1;
        nsr[n-1] = 1;
        for( int i=1; i<n; i++ ) {
            nsf[i] = Math.max( nsf[i-1], arr[i-1] );
        }
        for( int i=n-2; i>=0; i-- ) {
            nsr[i] = Math.max( nsr[i+1], arr[i+1] );
        }
        int maxArea = 0;
        for( int i=0; i<n; i++ ) {
            int hei = arr[i];
            int wid = nsr[i] - nsf[i] - 1;
            int curArea = hei * wid;
            maxArea = Math.max( curArea, maxArea );
        }
        return maxArea;
    }
}

```

## \* Queues:

- queue is base on FIFO me logic:
- it is linear data structure that used to stored elements
- there are two end of the queue collection i.e. front & rear,

ex:



- The queue is an interface in the java that belongs to java.util package. It is also extends the Collection interface
- there are two different classes that are used to implement the queue interface. These class are LinkedList & PriorityQueue.

### Implementation:

Array      ~~vector~~      LinkedList      Stack

- fixed size • does not
- time complexity of fix size  
remove() is  $O(n)$  • time complexity
- circular queue for remove  $O(1)$

Note: queue data structure also present in java collection.

`import java.util.*;`      if interface, does not make obj

- `Queue<Integer> q = new LinkedList<>();`
- `Queue<Integer> q2 = new ArrayDeque<>();`

Note: find difference bet' them.

```

public static class QueueImp {
    static class Queue {
        static int arr[3];
        static int size;
        static int rear;
        Queue(int n) {
            arr = new int[n];
            size = n;
            rear = -1;
        }
        public static boolean isEmpty() {
            return rear == -1;
        }
        public static void add(int data) {
            if (rear == size - 1) {
                System.out.println("Queue is full");
                return;
            }
            rear = rear + 1;
            arr[rear] = data;
        }
        public static int remove() {
            if (!isEmpty()) {
                System.out.println("Queue is empty");
                return -1;
            }
            int front = arr[0];
            for (int i = 0; i < rear; i++) {
                arr[i] = arr[i + 1];
            }
            rear = rear - 1;
            return front;
        }
    }
}

```

O(1)

O(n)

```

// peek function //
public static int peek() {
    if (isEmpty()) {
        System.out.println("empty queue");
        return -1;
    }
    return arr[0];
}

public static void main(String[] args) {
    Queue q = new Queue(5);
    q.add(2);
    q.add(3);
    q.add(4);
    while (!q.isEmpty()) {
        System.out.println(q.peek());
        q.remove();
    }
}

```

O/P: 2  
3  
4

### \* circular queue:

```

public static class Queue {
    static int size;
    static int arr[];
    static int rear;
    static int front;
}

```

// constructor //

```
queue(int n){
```

```
    size = n;
```

```
    arr = new int[n];
```

```
    rear = -1;
```

```
    front = -1;
```

```
}
```

```
// is empty //
```

```
public static boolean isEmpty() {
```

```
    return front == -1 && rear == -1;
```

```
}
```

```
// is Full //
```

```
public static boolean isFull() {
```

```
    return (rear + 1) % size == front;
```

```
}
```

```
// add ele //
```

```
public static void add(int data) {
```

```
    if (isFull()) {
```

```
        System.out.println("queue is empty");
```

```
        return;
```

```
}
```

```
    if (front == -1) {
```

```
        front = 0;
```

```
}
```

```
    rear = (rear + 1) % size;
```

```
    arr[rear] = data;
```

```
}
```

```
// peek ele //
```

```
public static int peek() {
```

```
    if (isEmpty()) {
```

```
        System.out.println("queue empty");
```

```
        return -1;
```

```
}
```

```
return arr[front];
```

```
}
```

```
}
```

```
// remove element //
public static int remove() {
    if (isEmpty()) {
        System.out.println("queue empty");
        return -1;
    }
    int result = arr[front];
    if (front == rear) {
        front = rear = -1;
    } else {
        front = (front + 1) % size;
    }
    return result;
}
}

public static void main(String[] args) {
    Queue q = new Queue(4);
    q.add(1);
    q.add(2);
    q.add(3);
    q.add(4);
    while (!q.isEmpty()) {
        System.out.println(q.peek());
        q.remove();
    }
}
```

classmate  
Date \_\_\_\_\_  
Page 76

for all methods time complexity  $O(2)$ .

### \* Queue using Linked-List

```
// code 1 public static void  
static class Node {  
    int data;  
    Node next;  
    Node(int data) {  
        this.data = data;  
        next = null;  
    }  
}
```

— constructor.

```
static class Queue {  
    — class.
```

```
    static Node head = null;
```

```
    static Node tail = null;
```

```
// null list //
```

```
public static boolean isEmpty() {
```

```
    return head == null && tail == null;
```

```
}
```

```
// add element //
```

```
public static void add(int data) {
```

```
    Node temp = new Node(data);
```

```
    if (head == null) {
```

```
        head = temp;
```

```
} else {
```

```
    tail.next = temp;
```

```
}
```

```
    tail = temp;
```

```
}
```

```
// peek element //
```

```
public static void int peek() {
```

```
    return head.data;
```

```
}
```

```

    // remove head / first ele //
    public static int remove() {
        if (isEmpty()) {
            System.out.println("Empty queue");
            return -1;
        }
        Node temp = head;
        head = head.next;
        return temp.data;
    }
}

```

```

public static void main(String[] args) {
    Queue q = new Queue();
    q.add(1);
    q.add(2);
    q.add(3);
    while (!q.isEmpty()) {
        System.out.print(q.peek());
        q.remove();
    }
}

```

\* queue implement by using java collection.

**Code 11**

```

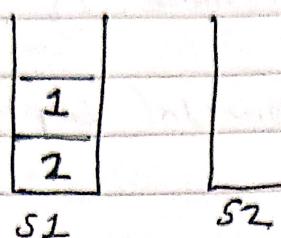
public static void main(String[] args) {
    Queue<Integer> q = new LinkedList();
    q.add(11);
    q.add(22);
    q.add(33);
    // also implement by
    Queue<Integer> q2 = new ArrayDeque();
}

```

### Q. Queue using two stacks.

Approach:

1)

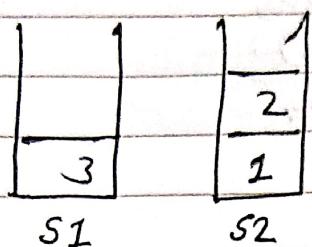


For add

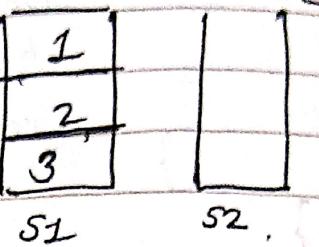
3

- 1) all ele push in S2 stack
- 2) push new data
- 3) push all data in S1 from S2.

2)



3)



Code

```
static class Queue {
    static Stack<Integer> S1 = new Stack<>();
    static Stack<Integer> S2 = new Stack<>();
    // is empty // - O(1)
    public static boolean isEmpty() {
        return S1.isEmpty();
    }
}
```

// add // - O(n)

```
public static void add(int data) {
```

```
    while (!S1.isEmpty()) {
```

```
        S2.push(S1.pop());
    }
```

```
    S1.push(data);
```

```
    while (!S2.isEmpty()) {
```

```
        S1.push(S2.pop());
    }
```

```
}
```

// peek // - O(1)

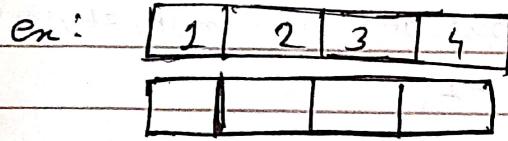
```

public static int peek(){
    if(s1.isEmpty()){
        System.out.println("empty queue");
        return -1;
    }
    return s1.peek();
}

// remove // - O(1)
public static int remove(){
    if(s1.isEmpty()){
        System.out.println("empty queue");
        return -1;
    }
    return s1.pop();
}

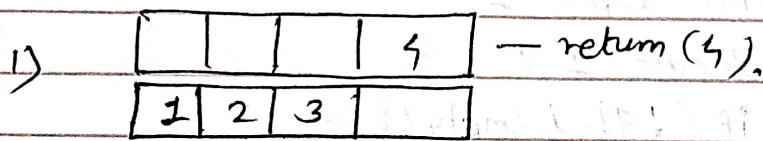
```

### g. Stack using two queue.

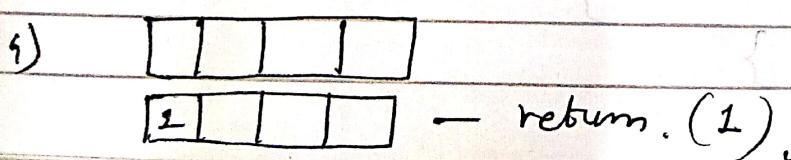


1) add all element

In second queue, if  
last ele then return  
approach.



O/P: 4  
3  
2  
1



```

1) Model public static class Stack {
    static queue<Integer> q1 = new LinkedList<>();
    static queue<Integer> q2 = new LinkedList<>();

    public static boolean isEmpty() {
        return q1.isEmpty() && q2.isEmpty();
    }

    // push function //
    public static void push(int data) {
        if (q1.isEmpty()) {
            q2.add(data);
        } else {
            q2.add(data);
        }
    }

    // pop function //
    public static int pop() {
        if (isEmpty()) {
            System.out.println("Empty stack");
            return -1;
        }

        int top = -1;
        // case 1 //
        if (!q1.isEmpty()) {
            while (!q1.isEmpty()) {
                top = q1.remove();
                if (q1.isEmpty()) {
                    break;
                }
                q2.add(top);
            }
        }
    }
}

```

```
else {
```

```
    while (!q2.isEmpty()) {
```

```
        top = q2.remove();
```

```
        if (q2.isEmpty()) {
```

```
            break;
```

```
}
```

```
} (if q2.isEmpty() q2.add(top));
```

```
}
```

```
}
```

```
}
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Note: In any competitive programming contest  
question is stream of character/etc.  
These are solve by max. time by queue.

Q. first non-repeating letter in a stream of character  
ex: str = aabccxb      ans = x.  
Stream = ydig, flow,

approach:

- ① create freq array to track elem character how many times repeat:
- ② create Queue to store current character,
- ③ for (int i=0; i<str.length(); i++) {  
    ch = str.charAt(i);  
    q.add(ch);  
    freq[ch-'a']++;      ← Imp logic  
    if (q.isEmpty()) → return -1;  
}  
return q.peek();

```
//code!! public static void firstNonRepeatingEle(String str){  
    int freq[] = new int[26];  
    Queue<Character> q = new LinkedList();  
    for (int i=0; i<str.length(); i++) {  
        char ch = str.charAt(i);  
        q.add(ch);  
        freq[ch-'a']++;  
        // check ele is repeat //  
        while (!q.isEmpty() && freq[q.peek()]->1)  
            q.remove();  
    }  
    if (q.isEmpty()) {  
        System.out.println(q.peek());  
    } else {  
        System.out.print(-1+");  
    }  
}
```

O/P : a - 1 b b b x ;

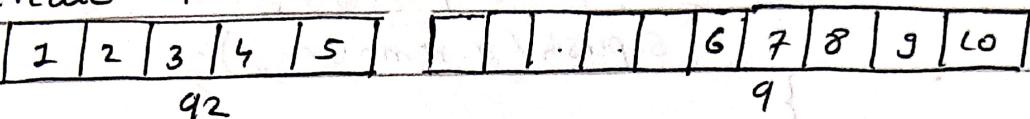
Interleave 2 halves of a queue (even len)

Q.

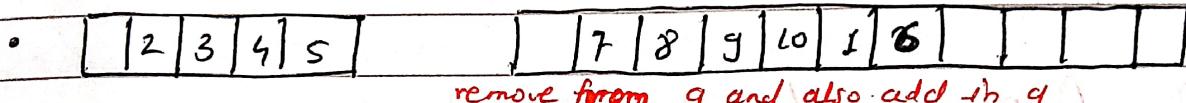
Ex: Input queue  $\rightarrow 1, 2, 3, 4, 5, 6, 7, 8, 9, 10$   
 break this queue betw them and add given type  
 ans = 1, 6, 2, 7, 3, 8, 4, 9, 5, 10.

approach:

1) create queue and stored first half data.



2) add simultaneously element in q (original I/p queue).  
 and remove from q.



remove from q and also add in q.)



3) return q.

```
//code
public static Queue<Integer> interleaveHalves(
    Queue<Integer> q) {
    Queue<Integer> q2 = new LinkedList<>();
    int l = q.size();
    for (int i = 0; i < l / 2; i++) {
        q2.add(q.remove());
    }
    for (int i = 0; i < l; i++) {
        if (i % 2 == 0) {
            q.add(q2.remove());
        } else {
            q.add(q.remove());
        }
    }
    return q;
}
```

Q. Note: learn & study of how to implement <sup>classmate</sup> vector in java & what is your use  
and difference of vector, ArrayList etc.

Date \_\_\_\_\_  
Page 84

Q. Reverse of queue:

ex: q = 1, 2, 3, 4, 5

ans = 5 4 3 2 1

- approach:
- 1) create new stack
  - 2) push all ele in stack from queue
  - 3) add all ele in queue from stack

// code

```
public static void reverseQueue (Queue<Integer> q){
```

```
Stack<Integer> s = new Stack();
```

```
while (!q.isEmpty()) {
```

```
s.push(q.remove());
```

```
}
```

```
while (!s.isEmpty()) {
```

```
q.add(s.pop());
```

```
}
```

```
}
```

```
System.out.println(q);
```

### (\*) Deque: double ended queue

Note: dequeue - remove element from queue (action)

- Deque & Queue are different.

- first import java.util.\*;

methods:

- 1) addFirst(data);
- 2) addLast(data);
- 3) getFirst();
- 4) getLast();
- 5) removeFirst();
- 6) removeLast();

// code

```
Deque<Integer> deg = new LinkedList();
```

```
deg.add(11);
```

```
deg.add(22);
```

```
deg.add(33);
```

```
System.out.println(deg);
```

```
}
```

O/P: [11, 22, 33]

g. Stack & queue using deque.

Model

```
static class Stack {
    static Deque<Integer> d = new LinkedList();
    public static void push(int data) {
        d.addLast(data);
    }
    public static int peek() {
        return d.getLast();
    }
    public static int pop() {
        return d.removeLast();
    }
    public static void main(String[] args) {
        Stack s = new Stack();
        s.push(11);
        s.push(22);
        s.push(33);
        System.out.println(s.pop()); // O/P: 33
        System.out.println(s.pop()); // O/P: 22
        System.out.println(s.pop()); // O/P: 11
    }
}
```

g. Queue using Deque.

Model

```
Static class Queue {
    static Deque<Integer> d = new LinkedList();
    public static void add(int data) {
        d.addLast(data);
    }
    public static void remove() {
        return d.removeFirst();
    }
}
```

## (1) Greedy Algorithm:

Greedy - ~~intuitive~~ (English meaning)

- In Java: Greedy algorithm is the problem solving technique where we make the locally optimum choice at each stage & hope to achieve a global optimum.

Pros : Simple & Easy good enough TC (time. complex).

Cons : A lot of time, global optimal is not achieved.

\* \* \*

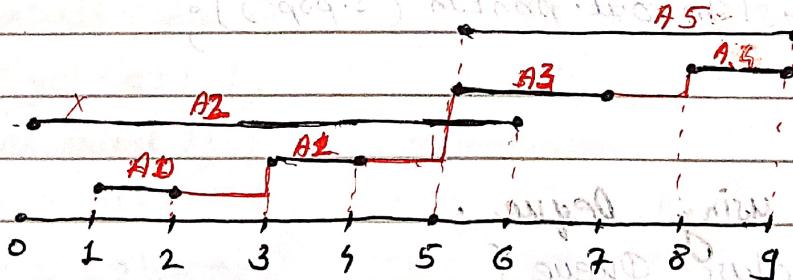
### 9. Activity Selection (Imp logic)

- Some logic use  $\rightarrow$  disjoint set, max meeting in room etc.
- You are given  $n$  activities with their start and end times. Select the maximum number of activities that can be performed by a single person, assuming that a person can only work on a single activity at a time. Activities are sorted according to end time.

ex: start [] = [1, 3, 0, 5, 8, 5]

end [] = [2, 5, 6, 9, 7, 9]

A0 A1 A2 A3 A4 A5



ans: A0 A1 A3 A4 Total = 5 slots

approach:

lastend = end[0]

if (lastend <= start[i]) {      start loop for i=2 to l.  
count++;

- first process is end then second process start,
- after end of the first does not consider the second process is start before end of the first process.

```

public static int maxActivity(int[] start, int[] end) {
    int l = start.length;
    ArrayList<Integer> ans = new ArrayList();
    ans.add(0);
    int maxAct = 1;
    int lastEnd = end[0];
    for (int i = 1; i < l; i++) {
        if (lastEnd <= start[i]) {
            maxAct++;
            lastEnd = end[i];
            ans.add(i);
        }
    }
    for (int i = 0; i < ans.size(); i++) {
        System.out.print("A" + ans.get(i) + " ");
    }
    System.out.println();
    return maxAct;
}

```

O/P: A0 A1 A3 A4  
Max Activity: 4.

- Note: for this question end time is sorted mandatory.  
start time any type sorted or unsorted they will be ok.
- If end time is not sorted then sort the end time.

approach: create 2D array of  $n \times 3$  size  
store each column of idx, start, end time.

Note: read the comparator material of java in course documents.



for ex: start = [0, 1, 3, 5, 5, 8]      end = [6, 2, 4, 7, 3, 9]

0	0	6
1	1	2
2	3	4
3	5	7
4	5	9
5	8	9

index start end

by using inbuilt function

sort array by choose : column  
they have sort.

Arrays.sort (Array Name, Comparator.comparingDouble (o → o[2])) -

outphat. ↑ ↑

hyphen greater than

- this is lambda function (shortcut of big functions)
- In java Comparator is interface for sorting java objects.

```
// code // public static int maxActivity2 [int start[], int [] end] {  
    int l = end.length; // size of array  
    ArrayList<Integer> ans = new ArrayList();  
    // for sorting //  
    int activities [] [] = new int [l] [3];  
    for (int i = 0; i < l; i++) {  
        activities [i] [0] = i;  
        activities [i] [1] = start [i];  
        activities [i] [2] = end [i];  
    }  
    // Lambda function //
```

$O(n \log n) \rightarrow$  Arrays.sort (activities, Comparator.comparingDouble (o → o[2])).  
ans.add (activities [0] [0]);  
int maxAct = 1; // max no of events : answer  
int lastEnd = activities [0] [2]; // max end time

```

for (int i=0; i<L; i++) {
    if (lastEnd < activities[i][1]) {
        maxAct++;
        lastEnd = activities[i][2];
        ans.add(activities[i][0]);
    }
}

for (int i=0; i<ans.size(); i++) {
    System.out.print("A" + ans.get(i) + " ");
}
System.out.println();
return maxAct;
}
}

```

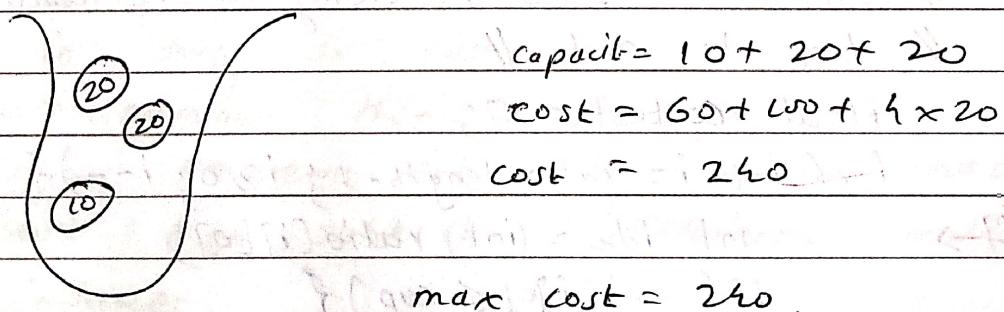
### g. Fraction knapsack(bag):

- Given the weights and values of  $N$  items, put these items in a knapsack of capacity  $W$  to get the maximum total value in the knapsack.

(Note : 0-1 knapsack problem solve by DP).

(This question solve by greedy method).

→ Ex: cost = [60, 100, 120] capacity( $w$ ) = 50 kg.  
weight = [10, 20, 30]



- A man is greedy, bag capacity is 50 but put like that max cost get & capacity is complete.

approach: 1) first find ratio of cost & weight.

$$\text{ratio}[i] = \text{cost}[i] / \text{wei}[i]$$

+ because  $\boxed{\text{cost} \uparrow \text{ & weight} \downarrow}$

2) check always  $\text{weight}[i] \leq \text{capacity}$  then subtract weight from capacity & add cost in object.

3) if otherwise add cost.

3) if space is remain but weight is max.  
then  $\text{cost} = \text{ratio}[i] * \text{capacity}$

4) break & return.

Note: ratio[ ][ ] ; because in 0<sup>th</sup> column stored the index, they are help to trace the position of weight & cost.

```
// code // public static void maxCost(int wei[], int cost[], int cap) {
    float ratio[][] = new float [cost.length][2];
    for (int i=0; i<ratio.length; i++) {
        ratio[i][0] = i;
        ratio[i][1] = cost[i]/wei[i];
    }
}
```

// sort the ratio //

sort.  $\rightarrow$  Arrays.sort(ratio, Comparator.comparingDouble(o->o[1]));  
 $O(n \log n)$

// but you required max ratio and array is //  
// sorted in decreasing order, hence start //  
// loop + to end //

float maxCost = 0;

for (int i = ratio.length-1; i>0; i--) {

int idc = (int) ratio[i][0];

if (wei[idc] <= cap) {

~~cap~~ cap -= wei[idc];

maxCost += cost[idc];

}

type casting  $\rightarrow$

```

        else {
            maxCost += (ratio[i][j] * cap);
            break;
        }
    }
    System.out.println("Max Cost : " + maxCost);
}

```

O/P: Max Cost : 240.0

### g. Min Absolute Differences Pairs :

- Given two Array A & B of equal length n. pair each element of array A to an element in Array B, such that sum S of absolute differences of all the pairs is minimum.

$$\text{ex: } A = [1, 2, 3]$$

$$B = [2, 1, 3]$$

$$\text{case 1: } |1-2| + |2-1| + |3-3| = 1+1+0 = 2$$

$$\text{case 2: } |1-1| + |2-3| + |3-2| = 0+1+1 = 2$$

$$\text{case 3: } |1-3| + |2-2| + |3-1| = 2+0+2 = 4$$

$$\text{case 4: } |1-1| + |2-2| + |3-3| = 0 \quad \text{--- ans,}$$

#### approach:

- If any two number maximum is closed to each other then their difference is minimum

$$\text{ex: } 1-3 \text{ & } 2-10 \Rightarrow \text{diff. } 2 \text{ & } 8,$$

- but in array in case one number is closed to two number then logic is wrong.

- for these problems solve by, given two array are sort then subt find difference simultaneously of indexes.

$$\text{ex: } A = [1, 2, 3]$$

$$B = [1, 2, 3]$$

$$\text{diff} = 0+0+0 = 0$$

both min is oneside & maximum is another side  
there are closed to each other.

```
//code11 public static int minAbsoluteVal(int A[], int B[]){
    int l = A.length;
    Arrays.sort(A);
    Arrays.sort(B);
    int minVal = 0;
    for(int i=0; i<l; i++){
        minVal = Math.abs(A[i] - B[i]);
    }
    return minVal;
}
```

Q. Max length of Chain of pairs

You are given  $n$  pairs of numbers. In every pair, the first number is always smaller than the second number. A pair  $(c, d)$  can come after pair  $(a, b)$  if  $b < c$ . Find the longest chain which can be formed from a given set of pairs.

Ex: pairs =  $(5, 24), (5, 8), (39, 60), (5, 28), (27, 40), (50, 90)$

$(5, 24)$	$(5, 8)$	$(39, 60)$	$(5, 28)$	$(27, 40)$	$(50, 90)$
5	24	39	28	40	50

- 1) Sort the array (base on 2nd column)
- 2) one pair can be selected.
- 3) apply loop from (i). if cond' is true  
 $\text{second pair (first index)} > \text{first pair (last index)}$

Note: also print the pairs stored the index  
 In 2D array list like Max Activity problem,  
 and, also print given written code.

	0	1
row → 0	5	24
→ 1	5.	28
2	27	40
3	39	60
4	50	90

$[5, 24] \rightarrow [27, 40] \rightarrow [50, 90]$

max chain = 3.

```
// code // public static void maxLengthOfChainPair(int pairs[][]){  
    // first sort array //  
    Arrays.sort(pairs, Comparator.comparingDouble(o->o[1]));  
    because also → int count = 1;  
    one pair.    int prevIdx = pairs[0][1];  
    System.out.print("[" + pairs[0][0] + ", " + pairs[0][1] + "]");  
    for (int i = 1; i < pairs.length; i++) {  
        } (int nextIdx = pairs[i][0]);  
        if (prevIdx < nextIdx) {  
            System.out.println("[" + pairs[i][0] + ", " + );  
            count++;  
            prevIdx = pairs[i][1];  
        }  
    }  
    System.out.println());  
    System.out.println("Max Pairs: " + count);  
}
```

### g. Indian coins:

- we are given an infinite supply of denominations

$[1, 2, 5, 10, 20, 50, 100, 500, 2000]$ , to find min. no.

of coins/notes to make change for a value V,

Ex: rupee = 590      ans: 500 50 20 20

approach:

total min coin : 9.

Coin array is in decreasing order and apply loop to  
if( coin[i] ≤ rupee).

classmate  
Date \_\_\_\_\_  
Page 94

```

//code// public static void minNumberCoin( int rupee ){
    Integer coin[] = { 2000, 500, 100, 50, 20, 10, 5, 2, 1 };
    ArrayList<Integer> ans = new ArrayList();
    int count = 0;
    for( int i=0; i<coin.length; i++ ){
        if( rupee >= coin[i] ){
            while( rupee >= coin[i] ){
                ans.add( coin[i] );
                rupee -= coin[i];
                count++;
            }
        }
    }
    for( int i=0; i<ans.size(); i++ ){
        System.out.print( ans.get(i) + " " );
    }
    System.out.println();
    System.out.println("total Min coin used : " + count );
}

```

#### Q. Job sequencing problem:

- Given an array of jobs where every job has a deadline and profit if the job is finished before the deadline. It is also given that every job takes a single unit of time, so the min possible deadline for any job is 1. Maximize the total profit if only one job can be scheduled at a time.



Hard

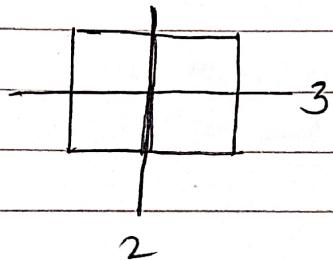
9

Chocolate problem // Min cost to cut board into squares.

- we are given a bar of chocolate composed of  $m \times n$  square pieces. One should break the chocolate into single squares. Each break of a part of the chocolate is charged a cost expressed by a positive integer. This cost does not depend on the size of the part that is being broken but only depends on the line the break goes along. Let us denote the costs of breaking along consecutive vertical lines with  $x_1, x_2, x_3, \dots, x_{m-1}$ , and along horizontal lines with  $y_1, y_2, y_3, \dots, y_{n-1}$ .

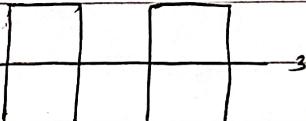
Compute the min cost of breaking the whole chocolate into single squares.

ex:



Case 1: 1) cut first vertical

$$\text{cost} = 2$$



2) then cut horizontal

$$\begin{array}{c} \boxed{\quad} \quad \boxed{\quad} \\ \boxed{\quad} \quad \boxed{\quad} \end{array} \quad \text{cost} = 2 + 3 + 3 = 8$$

approach:

1) use all cuts because cuts in square in all possible

2) first cut expensive cuts.  
then cut cheap cuts.

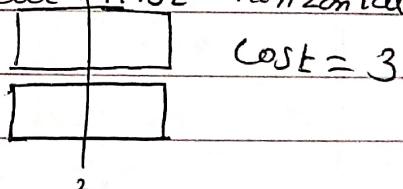
For this sort array in decreasing order.

3) cost of vertical cut =  $h \times x_e$ .

$$\text{cost of horizontal cut} = v_p \times y_f$$

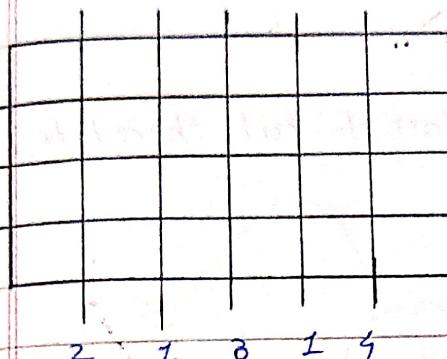
4) then apply two point of V & H cuts array & compare which is greater the cut

Case 2: 1) cut first horizontal

2) cut ~~first~~ vertical.

$$\begin{array}{c} \boxed{\quad} \quad \boxed{\quad} \\ \boxed{\quad} \quad \boxed{\quad} \end{array} \quad \text{cost} = 3 + 2 + 2 = 7$$

Ex:- cost of vertical cuts = [4, 3, 2, 1, 1], } sorted.  
 cost of horizontal cuts = [4, 2, 1]. }



```

int h=0, v=0;
int hp=1, vp=1;
while(h < hor.length && v < length)
  if(h < v)
    vertical cut.
  } else {
    Horizontal cut.
  }
}
  
```

// Code // public static void minCost(Integer[] vertPrices, Integer[] horPrice) {

// First sort prices //

```

Arrays.sort(vertPrice, Collections.reverseOrder());
Arrays.sort(horPrice, Collections.reverseOrder());

```

int vp=1, hp=1; int v=0, h=0, cost=0;

while(v < vertPrice.length && h < horPrice.length) {

if(vertPrice[v] < horPrice[h]) {

cost += (vp \* horPrice[h]);

h++; hp++;

} else {

cost += (hp \* vertPrice[v]);

v++; vp++;

}

}

// remaining cuts in vertical //

while(v < vertPrice.length) {

cost += (hp \* vertPrice[v]);

v++; vp++;

}.

// remaining cuts in horizontal //

```

while( h < horiPrice.length) {
    cost += (vp * horiPrice[h]);
    h++; hp++;
}
    
```

System.out.println("Min cost to cut chocolate : " + cost);

- Summary :

- for max activity end time are sorted.
- fraction knapsack - max cost  $\rightarrow$  sort by ratio  
for cost ↑ & weight ↓.
- for min absolute pair  $\rightarrow$  sort two array.
- max length chain pair  $\rightarrow$  sort by start index.
- Indian coin  $\rightarrow$  sorted coins.
- ~~the number of distinct pairs formed by selecting one element from each of two sets A and B is  $(|A| \times |B|)$~~
- Chocolate problem  $\rightarrow$  sort by cost of cuts  
 $\rightarrow$  (horizontal & vertical) = HLD  
 $\rightarrow$  HLD = FHD

$$\rightarrow (H \times V) = 4 \times 2 = 8$$

$$\rightarrow (H \times V) + (V \times H) = 4 \times 2 + 2 \times 4 = 16$$

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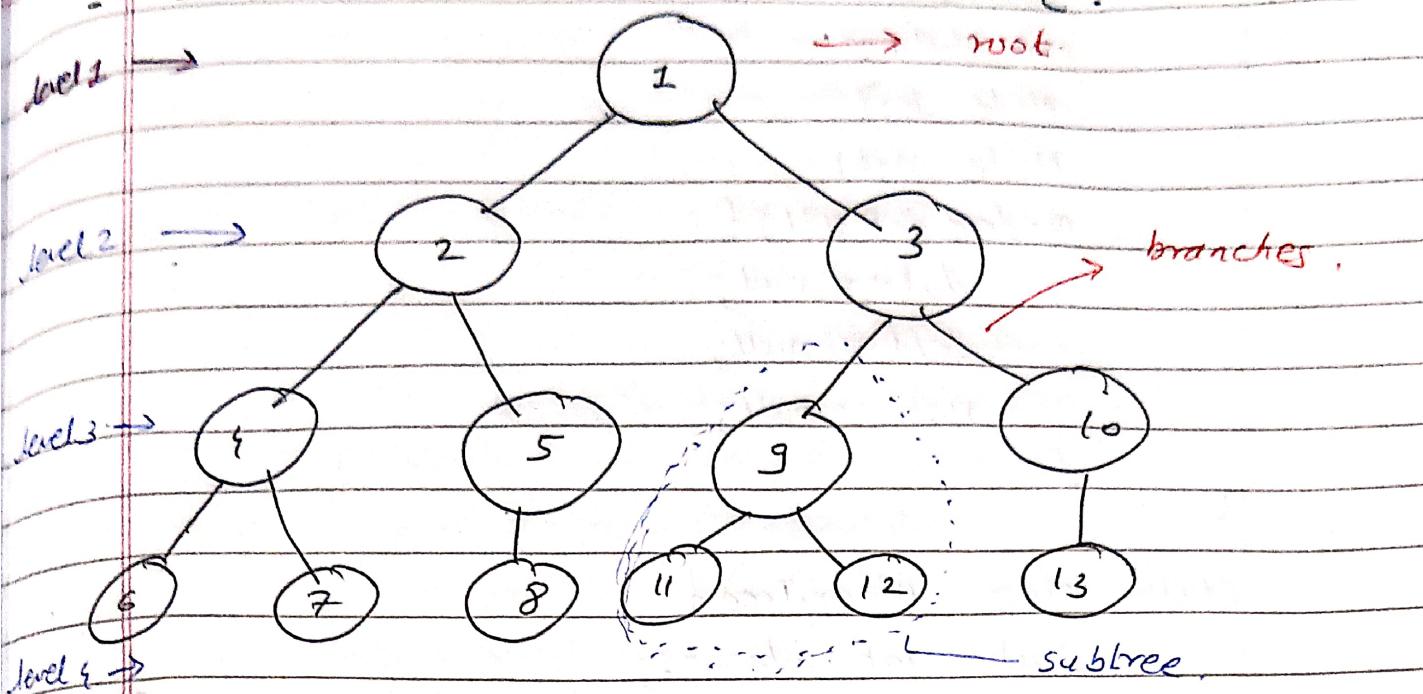
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## \* Binary Trees: (Part - 1)

It is Hierarchical data structure.



- depth = 4.

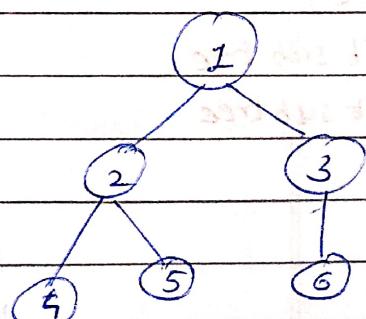
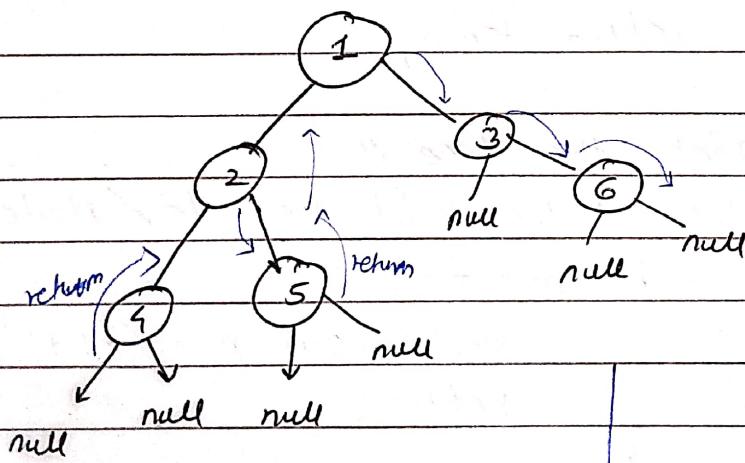
- Ancestors : all parent node

Ex: ancestors of 8 : {5, 2, 1}.

### \* Build Tree Preorder:

[1, 2, 4, -1, -1, 5, -1, -1, 3, -1, 6, -1, -1].

→



All code in public class //

```
// code1) static class Node {
    int data;
    Node left;
    Node right;
    Node( int val ) {
        data = val;
        left = null;
        right = null;
    }
}
```

```
static class BinaryTree {
```

```
    static int idx = -1;
    public static Node buildTree( int[] nodes ) {
```

```
        idx++;
    
```

```
        if( nodes[ idx ] == -1 ) {
```

```
            return null;
        }
    }
```

```
    Node temp = new Node( nodes[ idx ] );

```

```
    temp.left = buildTree( nodes );

```

```
    temp.right = buildTree( nodes );

```

```
    return temp;
}
```

// print the tree //

```
public static void preOrder( Node root ) {
```

```
    if( root == null ) {
```

```
        System.out.print( "-1 " );
    
```

```
    return;
}
```

root

left sub tree

right sub tree

```
    System.out.print( root.data + " " );

```

```
    preOrder( root.left );

```

```
    preOrder( root.right );
}
```

```
// print tree in order //
public static void inOrder(Node root) {
    if (root == null) {
        return;
    }
    inOrder(root.left);
    System.out.print(root.data + " ");
    inOrder(root.right);
}
```

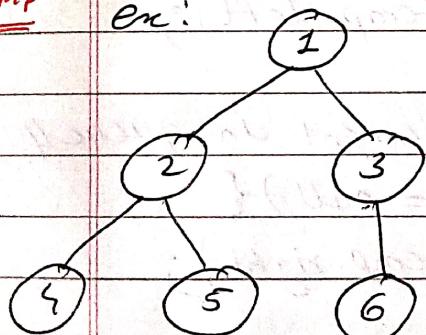
// post order traversal //

```
public static void postOrder(Node root) {
    if (root == null) {
        return;
    }
    postOrder(root.left);
    postOrder(root.right);
    System.out.print(root.data + " ");
}
```

## \* Q. Level order of Binary tree.

IMP

ex:



approach :

1) use the stack because they are work ~~LIFO~~ LIFO.

2) find first add root node if null.

1	null	
---	------	--

3) after each level print nextline.

O/P: 1

2 3

4 5 6

JMP.

// this code in BinaryTree class // never page

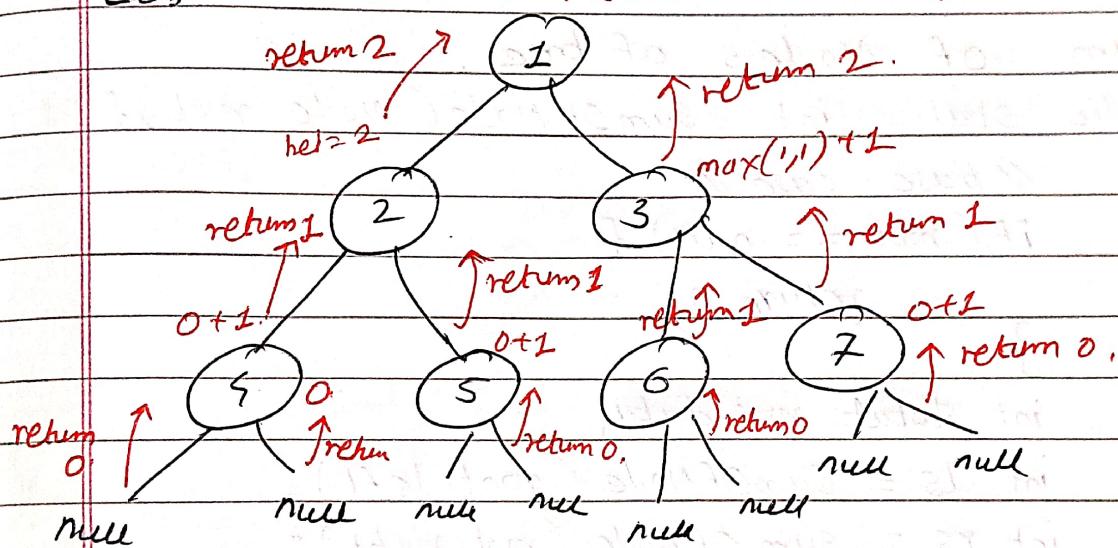
```
// code() public static void levelOrder (Node root) {  
    if (root == null) {  
        return null;  
    }  
  
    Queue <Node> q = new LinkedList ();  
    q.add (root);  
    q.add (null);  
    while (!q.isEmpty ()) {  
        Node temp = q.remove ();  
        // temp == null print newline //  
        if (temp == null) {  
            System.out.println ();  
            if (q.isEmpty ()) {  
                break;  
            } else {  
                q.add (null);  
            }  
        } else {  
            System.out.print (temp.data + " ");  
            // add left element in queue //  
            if (temp.left != null) {  
                q.add (temp.left);  
            }  
            // add right element in queue //  
            if (temp.right != null) {  
                q.add (temp.right);  
            }  
        }  
    }  
}
```

Height of a tree :

```
Model public static int height(Node root) {
    // base case //
    if (root == null) {
        return 0;
    }
    // recursion //
    int lh = height(root.left);
    int rh = height(root.right);
    int hei = Math.max(lh, rh) + 1;
    return hei;
}
```

Ex:

$$\max(2, 2) + 1 = 3$$



```
public static void main(String args[]) {
```

```
    Node root = new Node(1);
```

```
    root.left = new Node(2);
```

```
    root.left.left = new Node(4);
```

```
    root.left.right = new Node(5);
```

```
    root.right = new Node(3);
```

```
    root.right.left = new Node(6);
```

```
    root.right.right = new Node(7);
```

```
    System.out.println("Height of tree : " + height(root));
```

}

g

Count of Nodes of tree,

```
// code11 public static int countNode(Node root) {  
    // base case //  
    if (root == null) {  
        return 0;  
    }  
    // recursion // kaam //  
    int lc = countNode(root.left);  
    int rc = countNode(root.right);  
    int totalCount = lc + rc + 1;  
    return totalCount;  
}
```

g

Sum of Nodes of tree,

```
// code11 public static int sumOfNode(Node root) {  
    // base case //  
    if (root == null) {  
        return 0;  
    }  
    int sum = root.data;  
    int ls = sumOfNode(root.left);  
    int rs = sumOfNode(root.right);  
    int total = ls + rs + sum;  
    return total;  
}
```