

In a **Context-Free Grammar (CFG)**, useless symbols are those that do not contribute to generating any valid strings in the language defined by the grammar. There are two main types of useless symbols:

1. Non-Generating Symbols

A symbol (terminal or non-terminal) is **non-generating** if it **never produces a string of terminals**.

- These symbols cannot contribute to generating valid strings in the language.

Example:

Given the CFG:

mathematica



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Edit

$S \rightarrow AB$

$A \rightarrow aA \mid a$

$B \rightarrow C$

$C \rightarrow D$

$D \rightarrow C$

- A is generating because $A \rightarrow aA$ and $A \rightarrow a$ allow it to produce a terminal string.
- B , C , and D are non-generating because C depends on D , D depends on C , and they never produce terminals.

2. Unreachable (Inaccessible) Symbols

A symbol is **unreachable** if it **cannot be derived from the start symbol (S)**.

- These symbols are useless because they are never involved in deriving any valid string.

Example:

Given the CFG:

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Edit

$S \rightarrow AB$

$A \rightarrow aA \mid a$

$B \rightarrow bB \mid b$

$C \rightarrow cC \mid c$

- S , A , and B are reachable from S .
- C is **unreachable** because no rule starting from S ever introduces C .

Steps to Remove Useless Symbols

1. Identify and remove non-generating symbols.
2. Identify and remove unreachable symbols.
3. Remove any redundant rules caused by their removal.