



$path2 \mapsto \{“value3”, “value4”\},$   
 $path3 \mapsto \{“value4”, “value5”\}]]]$

CONSTANT *Target*

A record of per-target proposals

VARIABLE *proposal*

A record of per-target configurations

VARIABLE *configuration*

A record of target states

VARIABLE *target*

A record of target *masterships*

VARIABLE *mastership*

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LOCAL *InitState*  $\triangleq$

$[proposal \mapsto proposal,$   
 $configurations \mapsto configuration,$   
 $targets \mapsto target,$   
 $masterships \mapsto mastership]$

LOCAL *NextState*  $\triangleq$

$[proposal \mapsto proposal',$   
 $configurations \mapsto configuration',$   
 $targets \mapsto target',$   
 $masterships \mapsto mastership']$

LOCAL *Trace*  $\triangleq$  INSTANCE *Trace* WITH

$Module \leftarrow “Proposal”,$   
 $InitState \leftarrow InitState,$   
 $NextState \leftarrow NextState$

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Reconcile a proposal

*Reconcile*(*n*, *t*, *i*)  $\triangleq$

$\wedge \vee \wedge proposal[t][i].phase = Initialize$   
 $\wedge proposal[t][i].state = InProgress$   
 $\wedge proposal' = [proposal \text{ EXCEPT } ![t] =$   
 $\quad [proposal[t] \text{ EXCEPT } ![i].state = Complete,$   
 $\quad \quad \quad ![i].dependency.index = configuration[t].proposal.index]]$   
 $\wedge configuration' = [configuration \text{ EXCEPT } ![t].proposal.index = i]$   
 $\wedge \text{UNCHANGED } \langle target \rangle$

While in the *Validate* phase, validate the proposed changes.

If validation is successful, the proposal also records the changes

required to roll back the proposal and the index to which to roll back.

$$\vee \wedge \text{proposal}[t][i].\text{phase} = \text{Validate}$$

$$\wedge \text{proposal}[t][i].\text{state} = \text{InProgress}$$

$$\wedge \text{configuration}[t].\text{commit.index} = \text{proposal}[t][i].\text{dependency.index}$$

For *Change* proposals validate the set of requested changes.

$$\wedge \vee \wedge \text{proposal}[t][i].\text{type} = \text{Change}$$

$$\wedge \text{LET } \text{rollbackIndex} \triangleq \text{configuration}[t].\text{config.index}$$

$$\text{rollbackValues} \triangleq [p \in \text{DOMAIN } \text{proposal}[t][i].\text{change.values} \mapsto$$

$$\text{IF } p \in \text{DOMAIN } \text{configuration}[t].\text{config.values} \text{ THEN}$$

$$\text{configuration}[t].\text{config.values}[p]$$

$$\text{ELSE}$$

$$[\text{delete} \mapsto \text{TRUE}]]$$

Model validation successes and failures with *Valid* and *Invalid* results.

IN  $\exists r \in \{ \text{Valid}, \text{Invalid} \} :$

If the *Change* is *Valid*, record the changes required to roll back the proposal and the index to which the rollback changes will roll back the configuration.

$$\vee \wedge r = \text{Valid}$$

$$\wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] =$$

$$[\text{proposal}[t] \text{ EXCEPT } ![i].\text{rollback} = [i.\text{index} \mapsto \text{rollbackIndex},$$

$$\text{values} \mapsto \text{rollbackValues}],$$

$$![i].\text{state} = \text{Complete}]]$$

$$\vee \wedge r = \text{Invalid}$$

$$\wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] =$$

$$[\text{proposal}[t] \text{ EXCEPT } ![i].\text{state} = \text{Failed}]]$$

For *Rollback* proposals, validate the rollback changes which are proposal being rolled back.

$$\vee \wedge \text{proposal}[t][i].\text{type} = \text{Rollback}$$

Rollbacks can only be performed on *Change* type proposals.

$$\wedge \vee \wedge \text{proposal}[t][\text{proposal}[t][i].\text{rollback.index}].\text{type} = \text{Change}$$

Only roll back the change if it's the lastest change made to the configuration based on the configuration index.

$$\wedge \vee \wedge \text{configuration}[t].\text{config.index} = \text{proposal}[t][i].\text{rollback.index}$$

$$\wedge \text{LET } \text{changeIndex} \triangleq \text{proposal}[t][\text{proposal}[t][i].\text{rollback.index}].\text{rollback.index}$$

$$\text{changeValues} \triangleq \text{proposal}[t][\text{proposal}[t][i].\text{rollback.index}].\text{rollback.values}$$

$$\text{rollbackValues} \triangleq \text{proposal}[t][\text{proposal}[t][i].\text{rollback.index}].\text{change.values}$$

IN  $\exists r \in \{ \text{Valid}, \text{Invalid} \} :$

If the *Rollback* is *Valid*, record the changes required to roll back the target proposal and the index to which the configuration is being rolled back.

$$\vee \wedge r = \text{Valid}$$

$$\wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] =$$

$$[\text{proposal}[t] \text{ EXCEPT } ![i].\text{change} = [i.\text{index} \mapsto \text{changeIndex},$$

$$\text{values} \mapsto \text{changeValues}],$$

$$![i].\text{change} = [i.\text{index} \mapsto \text{proposal}[t][i].\text{change.index}]]$$

$$\begin{aligned}
& \text{values} \mapsto \text{changeValues}], \\
& \text{!}[i].\text{state} = \text{Complete}] \\
\vee \wedge r = \text{Invalid} \\
& \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = \\
& \quad [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Failed}]] \\
& \text{If the Rollback target is not the most recent change to the configuration,} \\
& \text{fail validation for the proposal.} \\
& \vee \wedge \text{configuration}[t].\text{config.index} \neq \text{proposal}[t][i].\text{rollback.index} \\
& \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Failed}]] \\
& \text{If a Rollback proposal is attempting to roll back another Rollback,} \\
& \text{fail validation for the proposal.} \\
& \vee \wedge \text{proposal}[t][\text{proposal}[t][i].\text{rollback.index}].\text{type} = \text{Rollback} \\
& \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = \\
& \quad [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Failed}]] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{target} \rangle \\
& \text{While in the Commit state, commit the proposed changes to the configuration.} \\
\vee \wedge \text{proposal}[t][i].\text{phase} = \text{Commit} \\
& \wedge \text{proposal}[t][i].\text{state} = \text{InProgress} \\
& \text{Only commit the proposal if the prior proposal has already been committed.} \\
& \wedge \text{configuration}[t].\text{commit.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}' = [\text{configuration EXCEPT !}[t].\text{config.values} = \text{proposal}[t][i].\text{change.values}, \\
& \quad \text{!}[t].\text{config.index} = \text{proposal}[t][i].\text{change.index}, \\
& \quad \text{!}[t].\text{commit.index} = i] \\
& \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Complete}]] \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \text{While in the Apply phase, apply the proposed changes to the target.} \\
\vee \wedge \text{proposal}[t][i].\text{phase} = \text{Apply} \\
& \wedge \text{proposal}[t][i].\text{state} = \text{InProgress} \\
& \wedge \text{configuration}[t].\text{target.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}[t].\text{target.term} = \text{mastership}[t].\text{term} \\
& \wedge \text{mastership}[t].\text{master} = n \\
& \text{Model successful and failed target update requests.} \\
& \wedge \exists r \in \{\text{Success}, \text{Failure}\} : \\
& \quad \vee \wedge r = \text{Success} \\
& \quad \wedge \text{target}' = [\text{target EXCEPT !}[t] = \text{proposal}[t][i].\text{change.values} @@ \text{target}[t]] \\
& \quad \wedge \text{configuration}' = [\text{configuration EXCEPT} \\
& \quad \quad \text{!}[t].\text{target.index} = i, \\
& \quad \quad \text{!}[t].\text{target.values} = \text{proposal}[t][i].\text{change.values} \\
& \quad \quad @@ \text{configuration}[t].\text{target.values}] \\
& \quad \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Complete}]] \\
& \text{If the proposal could not be applied, update the configuration's applied index} \\
& \text{and mark the proposal Failed.} \\
& \vee \wedge r = \text{Failure} \\
& \quad \wedge \text{configuration}' = [\text{configuration EXCEPT !}[t].\text{target.index} = i] \\
& \quad \wedge \text{proposal}' = [\text{proposal EXCEPT !}[t] = [\text{proposal}[t] \text{ EXCEPT !}[i].\text{state} = \text{Failed}]]
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
\vee & \wedge \text{proposal}[t][i].\text{phase} = \text{Abort} \\
& \wedge \text{proposal}[t][i].\text{state} = \text{InProgress} \\
& \text{The } \text{commit.index} \text{ will always be greater than or equal to the } \text{target.index}. \\
& \text{If only the } \text{commit.index} \text{ matches the proposal's } \text{dependency.index}, \text{ update} \\
& \text{the } \text{commit.index} \text{ to enable commits of later proposals, but do not} \\
& \text{mark the } \text{Abort} \text{ phase } \text{Complete} \text{ until the } \text{target.index} \text{ has been incremented.} \\
\wedge & \vee \wedge \text{configuration}[t].\text{commit.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{commit.index} = i] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \text{If the configuration's } \text{target.index} \text{ matches the proposal's } \text{dependency.index}, \\
& \text{update the } \text{target.index} \text{ and mark the proposal } \text{Complete} \text{ for the } \text{Abort} \text{ phase.} \\
\vee & \wedge \text{configuration}[t].\text{commit.index} \geq i \\
& \wedge \text{configuration}[t].\text{target.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{target.index} = i] \\
& \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{state} = \text{Complete}]] \\
& \text{If both the configuration's } \text{commit.index} \text{ and } \text{target.index} \text{ match the} \\
& \text{proposal's } \text{dependency.index}, \text{ update the } \text{commit.index} \text{ and } \text{target.index} \\
& \text{and mark the proposal } \text{Complete} \text{ for the } \text{Abort} \text{ phase.} \\
\vee & \wedge \text{configuration}[t].\text{commit.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}[t].\text{target.index} = \text{proposal}[t][i].\text{dependency.index} \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{commit.index} = i, \\
& \quad \quad \quad ![t].\text{target.index} = i] \\
& \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{state} = \text{Complete}]] \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{mastership} \rangle
\end{aligned}$$


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Formal specification, constraints, and theorems.

*Init*  $\triangleq$

$$\begin{aligned}
& \wedge \text{proposal} = [t \in \text{DOMAIN } \text{Target} \mapsto \\
& \quad [i \in \{\} \mapsto \\
& \quad \quad [\text{phase} \mapsto \text{Initialize}, \\
& \quad \quad \text{state} \mapsto \text{InProgress}]]] \\
& \wedge \text{Trace!Init}
\end{aligned}$$

*Next*  $\triangleq$

$$\begin{aligned}
& \vee \exists n \in \text{Node} : \\
& \quad \exists t \in \text{DOMAIN } \text{proposal} : \\
& \quad \exists i \in \text{DOMAIN } \text{proposal}[t] : \\
& \quad \text{Trace!Step}(\text{"Reconcile"}, \text{Reconcile}(n, t, i), [\text{node} \mapsto n, \text{target} \mapsto t, \text{index} \mapsto i])
\end{aligned}$$


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\\* Modification History

\\* Last modified Sun Feb 20 08:17:38 PST 2022 by jordanhalterman

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