MODULE *Transaction*

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

An empty constant
CONSTANT *Nil*

Transaction phase constants
CONSTANTS
Change,
Rollback

Proposal phase constants
CONSTANTS
Commit,
Apply

Status constants
CONSTANTS
Pending,
Complete,
Aborted,
Failed

$Status \triangleq \{Pending, Complete, Aborted, Failed\}$

$Done \triangleq \{Complete, Aborted, Failed\}$

The set of all nodes
CONSTANT *Node*

$Empty \triangleq [p \in \{\} \mapsto Nil]$

Variables defined by other modules.
VARIABLES
configuration,
mastership,
conn,
target

A transaction log. Transactions may either request a set
of changes to a set of targets or rollback a prior change.

VARIABLE *transaction*

A proposal log.

VARIABLE *proposal*

A sequence of configuration changes used for model checking.

VARIABLE *history*

$$
\begin{array}{l}
\mathit{TransactionOK} \triangleq \\
\quad \forall\, i \in \text{DOMAIN } \mathit{transaction} : \\
\qquad \land\ \mathit{transaction}[i].\mathit{phase} \in \{\mathit{Change}, \mathit{Rollback}\} \\
\qquad \land\ \mathit{transaction}[i].\mathit{change}.\mathit{proposal} \in \mathit{Nat} \\
\qquad \land\ \mathit{transaction}[i].\mathit{change}.\mathit{revision} \in \mathit{Nat} \\
\qquad \land\ \forall\, p \in \text{DOMAIN } \mathit{transaction}[i].\mathit{change}.\mathit{values} : \\
\qquad\quad \mathit{transaction}[i].\mathit{change}.\mathit{values}[p] \neq \mathit{Nil} \Rightarrow \\
\qquad\qquad \mathit{transaction}[i].\mathit{change}.\mathit{values}[p] \in \text{STRING} \\
\qquad \land\ \mathit{transaction}[i].\mathit{rollback}.\mathit{proposal} \in \mathit{Nat} \\
\qquad \land\ \mathit{transaction}[i].\mathit{rollback}.\mathit{revision} \in \mathit{Nat} \\
\qquad \land\ \forall\, p \in \text{DOMAIN } \mathit{transaction}[i].\mathit{rollback}.\mathit{values} : \\
\qquad\quad \mathit{transaction}[i].\mathit{rollback}.\mathit{values}[p] \neq \mathit{Nil} \Rightarrow \\
\qquad\qquad \mathit{transaction}[i].\mathit{rollback}.\mathit{values}[p] \in \text{STRING}
\end{array}
$$

$$
\begin{array}{l}
\mathit{ProposalOK} \triangleq \\
\quad \forall\, i \in \text{DOMAIN } \mathit{proposal} : \\
\qquad \land\ \mathit{proposal}[i].\mathit{transaction} \in \mathit{Nat} \\
\qquad \land\ \mathit{proposal}[i].\mathit{commit} \in \mathit{Status} \\
\qquad \land\ \mathit{proposal}[i].\mathit{apply} \in \mathit{Status}
\end{array}
$$

$$\mathit{TypeOK} \triangleq \mathit{TransactionOK} \land \mathit{ProposalOK}$$

$$
\begin{array}{l}
\text{LOCAL } \mathit{State} \triangleq [\\
\quad \mathit{transactions} \mapsto [i \in \text{DOMAIN } \mathit{transaction} \mapsto \mathit{transaction}[i] \mathbin{@@} [\mathit{index} \mapsto i]], \\
\quad \mathit{proposals} \mapsto [i \in \text{DOMAIN } \mathit{proposal} \mapsto \mathit{proposal}[i] \mathbin{@@} [\mathit{index} \mapsto i]], \\
\quad \mathit{configuration} \mapsto \mathit{configuration}]
\end{array}
$$

$$
\begin{array}{l}
\text{LOCAL } \mathit{Transitions} \triangleq \\
\quad \text{LET} \\
\qquad \mathit{transactions} \triangleq \{i \in \text{DOMAIN } \mathit{transaction}' : \\
\qquad\qquad\qquad i \in \text{DOMAIN } \mathit{transaction} \Rightarrow \mathit{transaction}'[i] \neq \mathit{transaction}[i]\} \\
\qquad \mathit{proposals} \triangleq \{i \in \text{DOMAIN } \mathit{proposal}' : \\
\qquad\qquad\qquad i \in \text{DOMAIN } \mathit{proposal} \Rightarrow \mathit{proposal}'[i] \neq \mathit{proposal}[i]\} \\
\quad \text{IN} \\
\qquad [\mathit{transactions} \mapsto [i \in \mathit{transactions} \mapsto \mathit{transaction}'[i] \mathbin{@@} [\mathit{index} \mapsto i]], \\
\qquad\ \mathit{proposals} \mapsto [i \in \mathit{proposals} \mapsto \mathit{proposal}'[i] \mathbin{@@} [\mathit{index} \mapsto i]]]
\end{array}
$$

$Test \triangleq$ INSTANCE $Test$ WITH
  $File \leftarrow$ "Transaction.log"

This section models configuration changes and rollbacks. Changes are appended to the transaction log and processed asynchronously.

Add a set of changes 'c' to the transaction log

$AppendChange(p,\ v) \triangleq$
  $\land\ transaction' = Append(transaction,\ [$
                  $phase \mapsto Change,$
                  $change \mapsto [$
                    $proposal \mapsto 0,$
                    $revision \mapsto Len(transaction) + 1,$
                    $values \mapsto (p :> v)],$
                  $rollback \mapsto [$
                    $proposal \mapsto 0,$
                    $revision \mapsto 0,$
                    $values \mapsto Empty]])$
  $\land$ UNCHANGED $\langle proposal,\ configuration,\ mastership,\ conn,\ target,\ history\rangle$

Add a rollback of transaction 't' to the transaction log

$RollbackChange(i) \triangleq$
  $\land\ i \in$ DOMAIN $transaction$
  $\land\ transaction[i].phase = Change$
  $\land\ transaction[i].change.proposal \neq 0$
  $\land\ proposal[transaction[i].change.proposal].commit \neq Pending$
  $\land\ transaction' = [transaction$ EXCEPT $![i].phase = Rollback]$
  $\land$ UNCHANGED $\langle proposal,\ configuration,\ mastership,\ conn,\ target,\ history\rangle$

$ReconcileChange(n,\ i) \triangleq$
  $\land\ transaction[i].phase = Change$
    The change proposal has not yet been created.
  $\land\ \lor\ \land\ transaction[i].change.proposal = 0$
      The prior transaction must have created a change proposal.
    $\land\ i - 1 \in$ DOMAIN $transaction \Rightarrow transaction[i-1].change.proposal \neq 0$
    $\land\ proposal' = Append(proposal,\ [transaction \mapsto i,\ commit \mapsto Pending,\ apply \mapsto Pending])$
    $\land\ transaction' = [transaction$ EXCEPT $![i].change.proposal = Len(proposal')]$
    $\land$ UNCHANGED $\langle configuration,\ target,\ history\rangle$
    The change proposal has been created.
  $\lor\ \land\ transaction[i].change.proposal \neq 0$
      The change is pending commit. Validate and commit the change once the prior change has been committed.
    $\land\ \lor\ \land\ proposal[transaction[i].change.proposal].commit = Pending$

The prior proposal has been committed.

$\land\ transaction[i].change.proposal - 1 \in \text{DOMAIN}\ proposal \Rightarrow$
$\quad proposal[transaction[i].change.proposal - 1].commit \in Done$

The prior change has been committed.

$\land\ configuration.committed.index = i - 1$

Valid change is committed to the configuration.

$\land\ \lor\ \land\ transaction' = [transaction\ \text{EXCEPT}\ ![i].rollback.revision = configuration.committed.revis$
$\qquad ![i].rollback.values = [$
$\qquad\quad p \in \text{DOMAIN}\ transaction[i].change.values \mapsto$
$\qquad\quad \text{IF}\ p \in \text{DOMAIN}\ configuration.committed.values$
$\qquad\qquad configuration.committed.values[p]$
$\qquad\quad \text{ELSE}$
$\qquad\qquad Nil]]$
$\qquad\land\ configuration' = [configuration\ \text{EXCEPT}\ !.committed.index = i,$
$\qquad\qquad !.committed.revision = i,$
$\qquad\qquad !.committed.values = transaction[i].change.val$
$\qquad\qquad\qquad configuration.committ$
$\qquad\land\ proposal' = [proposal\ \text{EXCEPT}\ ![transaction[i].change.proposal].commit = Complete]$
$\qquad\land\ history' = Append(history, [type \mapsto Change, phase \mapsto Commit, index \mapsto i])$

The change is invalid. Increment the committed index and mark the change *Failed*.

$\quad\lor\ \land\ configuration' = [configuration\ \text{EXCEPT}\ !.committed.index = i]$
$\qquad\land\ proposal' = [proposal\ \text{EXCEPT}\ ![transaction[i].change.proposal].commit = Failed]$
$\qquad\land\ \text{UNCHANGED}\ \langle transaction, history\rangle$
$\land\ \text{UNCHANGED}\ \langle target\rangle$

The change apply is pending.

$\lor\ \land\ proposal[transaction[i].change.proposal].apply = Pending$

The prior proposal has been applied.

$\land\ transaction[i].change.proposal - 1 \in \text{DOMAIN}\ proposal \Rightarrow$
$\quad proposal[transaction[i].change.proposal - 1].apply \in Done$

The prior change has been applied.

$\land\ configuration.applied.index = i - 1$

If the transaction proposal was committed, attempt to apply the transaction.

$\land\ \lor\ \land\ proposal[transaction[i].change.proposal].commit = Complete$
$\qquad\land\ configuration.state = Complete$
$\qquad\land\ configuration.term = mastership.term$
$\qquad\land\ conn[n].id = mastership.conn$
$\qquad\land\ conn[n].connected$
$\qquad\land\ target.running$

The change is successfully applied to the target.

$\qquad\land\ \lor\ \land\ target' = [target\ \text{EXCEPT}\ !.values = transaction[i].change.values\ @@\ target.values]$
$\qquad\qquad\land\ configuration' = [configuration\ \text{EXCEPT}\ !.applied.revision = i,$
$\qquad\qquad\qquad !.applied.values = transaction[i].change.va$
$\qquad\qquad\qquad\qquad configuration.applied$
$\qquad\qquad\land\ proposal' = [proposal\ \text{EXCEPT}\ ![transaction[i].change.proposal].apply = Complete]$
$\qquad\qquad\land\ history' = Append(history, [type \mapsto Change, phase \mapsto Apply, index \mapsto i])$

The change fails being applied to the target.

The configuration's applied index is not incremented here to block applying

subsequent changes until the failed change is rolled back.

$\lor \land proposal' = [proposal \text{ EXCEPT } ![transaction[i].change.proposal].apply = Failed]$

$\land \text{UNCHANGED } \langle configuration, target, history \rangle$

If the transaction proposal failed commit, abort applying the transaction.

$\lor \land proposal[transaction[i].change.proposal].commit = Failed$

$\land configuration' = [configuration \text{ EXCEPT } !.applied.index = i]$

$\land proposal' = [proposal \text{ EXCEPT } ![transaction[i].change.proposal].apply = Aborted]$

$\land \text{UNCHANGED } \langle target, history \rangle$

$\land \text{UNCHANGED } \langle transaction \rangle$

$ReconcileRollback(n, i) \triangleq$

$\land transaction[i].phase = Rollback$

The rollback proposal has not yet been created.

$\land \lor \land transaction[i].rollback.proposal = 0$

The subsequent transaction must have created a rollback proposal.

$\land i + 1 \in \text{DOMAIN } transaction \Rightarrow transaction[i + 1].rollback.proposal \neq 0$

$\land proposal' = Append(proposal, [transaction \mapsto i, commit \mapsto Pending, apply \mapsto Pending])$

$\land transaction' = [transaction \text{ EXCEPT } ![i].rollback.proposal = Len(proposal')]$

$\land \text{UNCHANGED } \langle configuration, target, history \rangle$

The rollback proposal has been created.

$\lor \land transaction[i].rollback.proposal \neq 0$

The rollback commit is pending.

$\land \lor \land proposal[transaction[i].rollback.proposal].commit = Pending$

The change has been committed. Commit the rollback.

$\land \lor \land proposal[transaction[i].change.proposal].commit \in Done$

If the change proposal completed, commit the rollback proposal.

$\land \lor \land proposal[transaction[i].change.proposal].commit = Complete$

$\land configuration.committed.revision = i$

$\land configuration' = [configuration \text{ EXCEPT } !.committed.revision = transaction[i].rollbac$

$!.committed.values = transaction[i].rollbac$

$configuration.com$

$\land proposal' = [proposal \text{ EXCEPT } ![transaction[i].rollback.proposal].commit = Complete$

$\land history' = Append(history, [type \mapsto Rollback, phase \mapsto Commit, index \mapsto i])$

If the change proposal failed, complete the rollback commit.

$\lor \land proposal[transaction[i].change.proposal].commit = Failed$

$\land proposal' = [proposal \text{ EXCEPT } ![transaction[i].rollback.proposal].commit = Complete$

$\land \text{UNCHANGED } \langle configuration, history \rangle$

The change has not been committed. Abort the change once the prior change is committed.

$\lor \land proposal[transaction[i].change.proposal].commit = Pending$

$\land i - 1 \in \text{DOMAIN } transaction \Rightarrow$

$proposal[transaction[i - 1].change.proposal].commit \in Done$

$\land proposal' = [proposal \text{ EXCEPT } ![transaction[i].change.proposal].commit = Aborted]$

$\land \text{UNCHANGED } \langle configuration, history \rangle$

$\land$ UNCHANGED $\langle target \rangle$

The rollback commit is complete, increment the configuration's committed index if necessary.

$\lor \land proposal[transaction[i].rollback.proposal].commit = Complete$
$\land configuration.committed.index = i - 1$
$\land configuration' = [configuration$ EXCEPT $!.committed.index = i]$
$\land$ UNCHANGED $\langle proposal, target, history \rangle$

The rollback apply is pending.

$\lor \land proposal[transaction[i].rollback.proposal].apply = Pending$

The change has been applied and the rollback has been committed.

Apply the rollback.

$\land \lor \land proposal[transaction[i].change.proposal].apply \in Done$
$\land proposal[transaction[i].rollback.proposal].commit = Complete$

If the change apply was completed or failed, apply the rollback.

Rollbacks are applied when change apply failed to account for
partial failures in changes to the target.

$\land \lor \land proposal[transaction[i].change.proposal].apply \in \{Complete, Failed\}$
$\land configuration.applied.revision = i$
$\land configuration.state = Complete$
$\land configuration.term = mastership.term$
$\land conn[n].id = mastership.conn$
$\land conn[n].connected$
$\land target.running$

Rollbacks are applied until successful.

$\land target' = [target$ EXCEPT $!.values = transaction[i].rollback.values$ @@ $target.values]$
$\land configuration' = [configuration$ EXCEPT $!.applied.target = target.id,$
$!.applied.revision = transaction[i].rollback.r$
$!.applied.values = transaction[i].rollback.v$
$configuration.applied$
$\land proposal' = [proposal$ EXCEPT $![transaction[i].rollback.proposal].apply = Complete]$
$\land history' = Append(history, [type \mapsto Rollback, phase \mapsto Apply, index \mapsto i])$

If the change apply was aborted, complete the rollback apply without changes to the target.

$\lor \land proposal[transaction[i].change.proposal].apply = Aborted$
$\land proposal' = [proposal$ EXCEPT $![transaction[i].rollback.proposal].apply = Complete]$
$\land$ UNCHANGED $\langle configuration, target, history \rangle$

The change has not been applied. Abort the change once the prior change is applied.

$\lor \land proposal[transaction[i].change.proposal].apply = Pending$
$\land i - 1 \in$ DOMAIN $transaction \Rightarrow$
$proposal[transaction[i - 1].change.proposal].apply \in Done$
$\land proposal' = [proposal$ EXCEPT $![transaction[i].change.proposal].apply = Aborted]$
$\land$ UNCHANGED $\langle configuration, target, history \rangle$

The rollback apply is complete, increment the configuration's applied index if necessary.

$\lor \land proposal[transaction[i].rollback.proposal].apply = Complete$
$\land configuration.applied.index = i - 1$
$\land configuration' = [configuration$ EXCEPT $!.applied.index = i]$
$\land$ UNCHANGED $\langle proposal, target, history \rangle$

$\land$ UNCHANGED $\langle transaction \rangle$

$ReconcileTransaction(n,\ i) \triangleq$
$\land\ i \in$ DOMAIN $transaction$
$\land\ \lor\ ReconcileChange(n,\ i)$
$\lor\ ReconcileRollback(n,\ i)$
$\land$ UNCHANGED $\langle mastership,\ conn \rangle$