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MODULE *Proposal*

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INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

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An empty constant

CONSTANT *Nil*

Event constants

CONSTANTS

*Change,*  
*Rollback*

Phase constants

CONSTANTS

*Commit,*  
*Apply*

*Phase*  $\triangleq$

$\{Nil,$   
*Commit,*  
*Apply\}*

Status constants

CONSTANTS

*Pending,*  
*InProgress,*  
*Complete,*  
*Failed*

*Status*  $\triangleq$

$\{Nil,$   
*Pending,*  
*InProgress,*  
*Complete,*  
*Failed\}*

The set of all nodes

CONSTANT *Node*

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Variables defined by other modules.

VARIABLES

*configuration*,  
*mastership*,  
*conn*,  
*target*

A record of per-target proposals

VARIABLE *proposal*

A sequence of configuration changes used for model checking.

VARIABLE *history*

*TypeOK*  $\triangleq$

$\forall i \in \text{DOMAIN } \text{proposal} :$   
 $\wedge \text{proposal}[i].\text{change.phase} \in \text{Phase}$   
 $\wedge \text{proposal}[i].\text{change.state} \in \text{Status}$   
 $\wedge \forall p \in \text{DOMAIN } \text{proposal}[i].\text{change.values} :$   
 $\wedge \text{proposal}[i].\text{change.values}[p].\text{index} \in \text{Nat}$   
 $\wedge \text{proposal}[i].\text{change.values}[p].\text{value} \neq \text{Nil} \Rightarrow$   
 $\text{proposal}[i].\text{change.values}[p].\text{value} \in \text{STRING}$   
 $\wedge \text{proposal}[i].\text{rollback.phase} \in \text{Phase}$   
 $\wedge \text{proposal}[i].\text{rollback.state} \in \text{Status}$   
 $\wedge \text{proposal}[i].\text{rollback.revision} \in \text{Nat}$   
 $\wedge \forall p \in \text{DOMAIN } \text{proposal}[i].\text{rollback.values} :$   
 $\wedge \text{proposal}[i].\text{rollback.values}[p].\text{index} \in \text{Nat}$   
 $\wedge \text{proposal}[i].\text{rollback.values}[p].\text{value} \neq \text{Nil} \Rightarrow$   
 $\text{proposal}[i].\text{rollback.values}[p].\text{value} \in \text{STRING}$

LOCAL *CurrState*  $\triangleq$  [

*proposals*  $\mapsto [i \in \text{DOMAIN } \text{proposal} \mapsto \text{proposal}[i] @@ [\text{ordinal} \mapsto i]],$   
*configuration*  $\mapsto \text{configuration},$   
*mastership*  $\mapsto \text{mastership},$   
*conn*  $\mapsto \text{conn},$   
*target*  $\mapsto \text{target}]$

LOCAL *SuccState*  $\triangleq$

LET

*proposals*  $\triangleq \{i \in \text{DOMAIN } \text{proposal}' : \\ i \in \text{DOMAIN } \text{proposal} \Rightarrow \text{proposal}'[i] \neq \text{proposal}[i]\}$

IN

$[\text{proposals} \mapsto [i \in \text{proposals} \mapsto \text{proposal}'[i] @@ [\text{ordinal} \mapsto i]]] @@$   
 $(\text{IF } \text{configuration}' \neq \text{configuration} \text{ THEN } [\text{configuration} \mapsto \text{configuration}'] \text{ ELSE } \langle \rangle) @@$   
 $(\text{IF } \text{mastership}' \neq \text{mastership} \text{ THEN } [\text{mastership} \mapsto \text{mastership}'] \text{ ELSE } \langle \rangle) @@$   
 $(\text{IF } \text{conn}' \neq \text{conn} \text{ THEN } [\text{conn} \mapsto \text{conn}'] \text{ ELSE } \langle \rangle) @@$   
 $(\text{IF } \text{target}' \neq \text{target} \text{ THEN } [\text{target} \mapsto \text{target}'] \text{ ELSE } \langle \rangle)$

$Test \triangleq$  INSTANCE  $Test$  WITH  
 $File \leftarrow$  "Proposal.log"  
 LOCAL  $Max(s) \triangleq$  CHOOSE  $i \in s : \forall j \in s : i > j$

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$CommitChange(n, i) \triangleq$   
 $\wedge proposal[i].change.phase = Commit$   
 $\wedge proposal[i].change.state = InProgress$   
 If the committed index does not match the proposal index, commit the change.  
 $\wedge \vee \wedge configuration.committed.index = i - 1$   
 If the change is valid, update the committed index, revision, and values.  
 $\wedge \vee \wedge configuration' = [configuration \text{ EXCEPT } !.committed.index = i,$   
 $!.committed.revision = i,$   
 $!.committed.values = proposal[i].change.values @@$   
 $configuration.committed.values]$   
 $\wedge history' = Append(history, [type \mapsto Change, phase \mapsto Commit, index \mapsto i])$   
 If the change is invalid, update only the committed index.  
 $\vee \wedge configuration' = [configuration \text{ EXCEPT } !.committed.index = i]$   
 $\wedge UNCHANGED \langle history \rangle$   
 $\wedge UNCHANGED \langle proposal \rangle$   
 If both the committed index and committed revision were updated, the proposal was successful.  
 $\vee \wedge configuration.committed.index = i$   
 $\wedge configuration.committed.revision = i$   
 $\wedge proposal' = [proposal \text{ EXCEPT } ![i].change.state = Complete]$   
 $\wedge UNCHANGED \langle configuration, history \rangle$   
 If the committed index was updated but the revision was not, the proposal failed validation.  
 $\vee \wedge configuration.committed.index = i$   
 $\wedge configuration.committed.revision \neq i$   
 $\wedge proposal' = [proposal \text{ EXCEPT } ![i].change.state = Failed]$   
 $\wedge UNCHANGED \langle configuration, history \rangle$   
 $\wedge UNCHANGED \langle target \rangle$

$ApplyChange(n, i) \triangleq$   
 $\wedge proposal[i].change.phase = Apply$   
 $\wedge proposal[i].change.state = InProgress$   
 If the applied index does not match the proposal index, apply the change.  
 $\wedge \vee \wedge configuration.applied.index = i - 1$   
 $\wedge configuration.state = Complete$   
 $\wedge configuration.term = mastership.term$   
 $\wedge conn[n].id = mastership.conn$   
 $\wedge conn[n].connected$   
 $\wedge target.running$   
 If the change can be applied, update the index, revision, and values.  
 $\wedge \vee \wedge target' = [target \text{ EXCEPT } !.values = proposal[i].change.values @@ target.values]$

$$\begin{aligned}
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i, \\
& \quad !.\text{applied.revision} = i, \\
& \quad !.\text{applied.values} = \text{proposal}[i].\text{change.values} @@ \\
& \quad \quad \quad \text{configuration.applied.values}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\text{type} \mapsto \text{Change}, \text{phase} \mapsto \text{Apply}, \text{index} \mapsto i]) \\
& \text{If the change is invalid, update only the applied index.} \\
& \vee \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i] \\
& \quad \wedge \text{UNCHANGED } \langle \text{target}, \text{history} \rangle \\
& \quad \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \text{If the applied index and revision both match the proposal index, the change was successful.} \\
& \vee \wedge \text{configuration.applied.index} = i \\
& \quad \wedge \text{configuration.applied.revision} = i \\
& \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{change.state} = \text{Complete}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{configuration}, \text{target}, \text{history} \rangle \\
& \text{If the applied index matches the proposal index but the revision does not, the proposal failed.} \\
& \vee \wedge \text{configuration.applied.index} = i \\
& \quad \wedge \text{configuration.applied.revision} \neq i \\
& \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{change.state} = \text{Failed}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{configuration}, \text{target}, \text{history} \rangle \\
\\
& \text{CommitRollback}(n, i) \triangleq \\
& \quad \wedge \text{proposal}[i].\text{rollback.phase} = \text{Commit} \\
& \quad \wedge \text{proposal}[i].\text{rollback.state} = \text{InProgress} \\
& \quad \text{If the committed revision matches the proposal revision, roll back to the previous revision.} \\
& \quad \wedge \vee \wedge \text{configuration.committed.revision} = i \\
& \quad \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.revision} = \text{proposal}[i].\text{rollback.revision}, \\
& \quad \quad \quad !.\text{committed.values} = \text{proposal}[i].\text{rollback.values} @@ \\
& \quad \quad \quad \text{configuration.committed.values}] \\
& \quad \wedge \text{history}' = \text{Append}(\text{history}, [\text{type} \mapsto \text{Rollback}, \text{phase} \mapsto \text{Commit}, \text{index} \mapsto i]) \\
& \quad \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \quad \text{If the committed index matches the rollback index, complete the rollback.} \\
& \quad \vee \wedge \text{configuration.committed.revision} = \text{proposal}[i].\text{rollback.revision} \\
& \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.state} = \text{Complete}] \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
& \quad \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
\\
& \text{ApplyRollback}(n, i) \triangleq \\
& \quad \wedge \text{proposal}[i].\text{rollback.phase} = \text{Apply} \\
& \quad \wedge \text{proposal}[i].\text{rollback.state} = \text{InProgress} \\
& \quad \text{If the applied revision matches the proposal revision, roll back to the previous revision.} \\
& \quad \wedge \vee \wedge \text{configuration.applied.revision} = i \\
& \quad \quad \wedge \text{configuration.state} = \text{Complete} \\
& \quad \quad \wedge \text{configuration.term} = \text{mastership.term} \\
& \quad \quad \wedge \text{conn}[n].\text{id} = \text{mastership.conn} \\
& \quad \quad \wedge \text{conn}[n].\text{connected}
\end{aligned}$$

$$\begin{aligned}
& \wedge target.running \\
& \wedge target' = [target \text{ EXCEPT } !.values = proposal[i].rollback.values @@ target.values] \\
& \wedge configuration' = [configuration \text{ EXCEPT } !.applied.revision = proposal[i].rollback.revision, \\
& \hspace{15em} !.applied.values = proposal[i].rollback.values @@ \\
& \hspace{15em} configuration.applied.values] \\
& \wedge history' = Append(history, [type \mapsto Rollback, phase \mapsto Apply, index \mapsto i]) \\
& \wedge \text{UNCHANGED } \langle proposal \rangle \\
& \text{If the committed index matches the rollback index, complete the rollback.} \\
& \vee \wedge configuration.committed.revision = proposal[i].rollback.revision \\
& \wedge proposal' = [proposal \text{ EXCEPT } ![i].rollback.state = Complete] \\
& \wedge \text{UNCHANGED } \langle configuration, target, history \rangle
\end{aligned}$$

Reconcile a proposal

$$\begin{aligned}
ReconcileProposal(n, i) & \triangleq \\
& \wedge i \in \text{DOMAIN } proposal \\
& \wedge mastership.master = n \\
& \wedge \vee CommitChange(n, i) \\
& \quad \vee ApplyChange(n, i) \\
& \quad \vee CommitRollback(n, i) \\
& \quad \vee ApplyRollback(n, i) \\
& \wedge \text{UNCHANGED } \langle mastership, conn \rangle
\end{aligned}$$


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