
MODULE *ConfigImpl*

INSTANCE *Naturals*
 INSTANCE *FiniteSets*
 INSTANCE *Sequences*
 LOCAL INSTANCE *TLC*

This section specifies constant parameters for the model.
 CONSTANT *LogEnabled*
 ASSUME *LogEnabled* ∈ BOOLEAN
 CONSTANT *None*
 ASSUME *None* ∈ STRING
 CONSTANT *Node*
 ASSUME $\forall n \in \text{Node} : n \in \text{STRING}$
 CONSTANTS
 Change,
 Rollback
 $\text{Event} \triangleq \{ \text{Change}, \text{Rollback} \}$
 ASSUME $\forall e \in \text{Event} : e \in \text{STRING}$
 CONSTANTS
 Commit,
 Apply
 $\text{Phase} \triangleq \{ \text{Commit}, \text{Apply} \}$
 ASSUME $\forall p \in \text{Phase} : p \in \text{STRING}$
 CONSTANTS
 Pending,
 InProgress,
 Complete,
 Aborted,
 Failed
 $\text{State} \triangleq \{ \text{Pending}, \text{InProgress}, \text{Complete}, \text{Aborted}, \text{Failed} \}$
 $\text{Done} \triangleq \{ \text{Complete}, \text{Aborted}, \text{Failed} \}$

ASSUME $\forall s \in State : s \in \text{STRING}$

CONSTANT *Path*

ASSUME $\forall p \in Path : p \in \text{STRING}$

CONSTANT *Value*

ASSUME $\forall v \in Value : v \in \text{STRING}$

$AllValues \triangleq Value \cup \{None\}$

CONSTANT *NumProposals*

ASSUME $NumProposals \in Nat$

This section defines model state variables.

$proposal \triangleq [i \in 1 \dots Nat \mapsto [$
 $phase \mapsto Phase,$
 $change \mapsto [$
 $values \mapsto Change,$
 $commit \mapsto State,$
 $apply \mapsto State],$
 $rollback \mapsto [$
 $index \mapsto Nat,$
 $values \mapsto Change,$
 $commit \mapsto State,$
 $apply \mapsto State]]]$

$configuration \triangleq [$
 $committed \mapsto [$
 $index \mapsto Nat,$
 $values \mapsto Change],$
 $applied \mapsto [$
 $index \mapsto Nat,$
 $values \mapsto Change,$
 $term \mapsto Nat]]]$

$mastership \triangleq [$
 $master \mapsto \text{STRING},$
 $term \mapsto Nat,$
 $conn \mapsto Nat]$

$conn \triangleq [n \in Node \mapsto [$
 $id \mapsto Nat,$
 $connected \mapsto \text{BOOLEAN}]]$

$target \triangleq [$
 $id \mapsto Nat,$
 $values \mapsto Change,$
 $running \mapsto \text{BOOLEAN}]$

VARIABLE *proposal*

VARIABLE *configuration*

VARIABLE *mastership*

VARIABLE *conn*

VARIABLE *target*

VARIABLE *history*

VARIABLE *mapping*

$\text{vars} \triangleq \langle \text{proposal}, \text{configuration}, \text{mastership}, \text{conn}, \text{target}, \text{history}, \text{mapping} \rangle$

LOCAL *MastershipLog* \triangleq INSTANCE *Log* WITH

File \leftarrow "Mastership.log",

CurrState \leftarrow [

target \mapsto *target*,

mastership \mapsto *mastership*,

conns \mapsto *conn*],

SuccState \leftarrow [

target \mapsto *target'*,

mastership \mapsto *mastership'*,

conns \mapsto *conn'*],

Enabled \leftarrow *LogEnabled*

LOCAL *ConfigurationLog* \triangleq INSTANCE *Log* WITH

File \leftarrow "Configuration.log",

CurrState \leftarrow [

configuration \mapsto *configuration*,

target \mapsto *target*,

mastership \mapsto *mastership*,

conns \mapsto *conn*],

SuccState \leftarrow [

configuration \mapsto *configuration'*,

target \mapsto *target'*,

mastership \mapsto *mastership'*,

conns \mapsto *conn'*],

Enabled \leftarrow *LogEnabled*

LOCAL *ProposalLog* \triangleq INSTANCE *Log* WITH

File \leftarrow "Proposal.log",

CurrState \leftarrow [

proposals $\mapsto [i \in \{i \in \text{DOMAIN } \text{proposal} : \text{proposal}[i].\text{phase} \neq \text{None}\} \mapsto \text{proposal}[i]],$

$$\begin{aligned}
& configuration \mapsto configuration, \\
& target \mapsto target, \\
& mastership \mapsto mastership, \\
& conns \mapsto conn], \\
SuccState \leftarrow [\\
& proposals \mapsto [i \in \{i \in \text{DOMAIN } proposal' : proposal'[i].phase \neq \text{None}\} \mapsto proposal'[i]], \\
& configuration \mapsto configuration', \\
& target \mapsto target', \\
& mastership \mapsto mastership', \\
& conns \mapsto conn'], \\
Enabled \leftarrow LogEnabled
\end{aligned}$$

This section models configuration target.

$$\begin{aligned}
StartTarget & \triangleq \\
& \wedge \neg target.running \\
& \wedge target' = [target \text{ EXCEPT } !.id = target.id + 1, \\
& \quad !.running = \text{TRUE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, conn, history \rangle \\
StopTarget & \triangleq \\
& \wedge target.running \\
& \wedge target' = [target \text{ EXCEPT } !.running = \text{FALSE}, \\
& \quad !.values = [p \in \{\} \mapsto [value \mapsto \text{None}]]] \\
& \wedge conn' = [n \in Node \mapsto [conn[n] \text{ EXCEPT } !.connected = \text{FALSE}]] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, history \rangle
\end{aligned}$$

This section models nodes connection to the configuration target.

$$\begin{aligned}
ConnectNode(n) & \triangleq \\
& \wedge \neg conn[n].connected \\
& \wedge target.running \\
& \wedge conn' = [conn \text{ EXCEPT } ![n].id = conn[n].id + 1, \\
& \quad ![n].connected = \text{TRUE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, target, history \rangle \\
DisconnectNode(n) & \triangleq \\
& \wedge conn[n].connected \\
& \wedge conn' = [conn \text{ EXCEPT } ![n].connected = \text{FALSE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, target, history \rangle
\end{aligned}$$

This section models *mastership* reconciliation.

If the index is less than the *targetIndex*, this indicates a rollback of a prior proposal is being processed, and the *targetIndex* cannot be incremented until that rollback is complete. The index represents the index to which the proposal at *changeIndex* + 1 rolls back.

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$!.applied.changeIndex = i]$

$\wedge \text{UNCHANGED } \langle proposal, target, history \rangle$

$CommitRollback(n, i) \triangleq$

'index' is the current index committed to the configuration
 'changeIndex' is the maximum change index committed to the configuration
 'targetIndex' is the index of the proposal currently being committed
targetIndex is always changed first. Once the rollback is committed, the index will be decremented to match the *targetIndex*. The next time a change is committed, the index will increase again. If the committed index is equal to this proposal index, this proposal is the next to be rolled back. To roll back a proposal, the target index is set to the proposal's rollback index. When the rollback is committed, the committed index is set to the proposal's rollback index, thus matching the *targetIndex*. This unblocks new changes to be committed.

$\wedge \vee \wedge proposal[i].rollback.commit = Pending$
 $\wedge configuration.committed.changeIndex \geq i$
 $\wedge configuration.committed.index = i$
 $\wedge \vee \wedge configuration.committed.targetIndex = i$
 $\wedge configuration' = [configuration \text{ EXCEPT } !.committed.targetIndex = proposal[i].rollback.index]$
 $\wedge \text{UNCHANGED } \langle proposal \rangle$
 $\vee \wedge configuration.committed.targetIndex = proposal[i].rollback.index$
 $\wedge \vee \wedge proposal[i].change.commit \neq Aborted$
 $\wedge proposal' = [proposal \text{ EXCEPT } ![i].rollback.commit = InProgress]$
 $\vee \wedge proposal[i].change.commit = Aborted$
 $\wedge proposal' = [proposal \text{ EXCEPT } ![i].rollback.commit = Complete]$
 $\wedge \text{UNCHANGED } \langle configuration \rangle$
 $\wedge \text{UNCHANGED } \langle history \rangle$
 $\vee \wedge proposal[i].rollback.commit = InProgress$
 $\wedge \vee \wedge configuration.committed.index = i$
 $\wedge \text{LET } values \triangleq [p \in \text{DOMAIN } configuration.committed.values \mapsto$
 $\text{IF } p \in \text{DOMAIN } proposal[i].change.values \text{ THEN}$
 $\quad proposal[i].rollback.values[p]$
 ELSE
 $\quad configuration.committed.values[p]]$
 $\text{IN } configuration' = [configuration \text{ EXCEPT } !.committed.index = proposal[i].rollback.index,$
 $\quad !.committed.values = values]$
 $\wedge history' = Append(history, [type \mapsto Rollback, phase \mapsto Commit, index \mapsto i])$
 $\wedge \text{UNCHANGED } \langle proposal \rangle$
 $\vee \wedge configuration.committed.index = proposal[i].rollback.index$
 $\wedge proposal' = [proposal \text{ EXCEPT } ![i].rollback.commit = Complete]$
 $\wedge \text{UNCHANGED } \langle configuration, history \rangle$
 $\vee \wedge proposal[i].rollback.commit = Complete$
 $\wedge configuration.committed.targetIndex = proposal[i].rollback.index$
 $\wedge configuration.committed.index \neq proposal[i].rollback.index$

$\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = \text{proposal}[i].\text{rollback.index}]$
 $\wedge \text{UNCHANGED } \langle \text{proposal}, \text{history} \rangle$
 $\wedge \text{UNCHANGED } \langle \text{target} \rangle$

$\text{ApplyRollback}(n, i) \triangleq$

'index' is the current index applied to the configuration
 'changeIndex' is the maximum change index applied to the configuration
 'targetIndex' is the index of the proposal currently being applied
targetIndex is always changed first. Once the rollback is applied, the index will be decremented to match the *targetIndex*. The next time a change is applied, the index will increase again. If the applied index is equal to this proposal index, this proposal is the next to be rolled back. To roll back a proposal, the target index is set to the proposal's rollback index. When the rollback is applied, the applied index is set to the proposal's rollback index, thus matching the *targetIndex*. This unblocks new changes to be applied.

$\wedge \vee \wedge \text{proposal}[i].\text{rollback.apply} = \text{Pending}$
 $\wedge \text{configuration.committed.index} \leq \text{proposal}[i].\text{rollback.index}$
 $\wedge \text{configuration.applied.changeIndex} \geq i$
 $\wedge \text{configuration.applied.index} = i$
 $\wedge \vee \wedge \text{configuration.applied.targetIndex} = i$
 $\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.targetIndex} = \text{proposal}[i].\text{rollback.index}]$
 $\wedge \text{UNCHANGED } \langle \text{proposal} \rangle$
 $\vee \wedge \text{configuration.applied.targetIndex} = \text{proposal}[i].\text{rollback.index}$
 $\wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.apply} = \text{InProgress}]$
 $\wedge \text{UNCHANGED } \langle \text{configuration} \rangle$
 $\wedge \text{UNCHANGED } \langle \text{target}, \text{history} \rangle$
 $\vee \wedge \text{proposal}[i].\text{rollback.apply} = \text{InProgress}$
 $\wedge \vee \wedge \text{configuration.applied.index} = i$
 Verify the applied term is the current *mastership* term to ensure the configuration has been synchronized following restarts.
 $\wedge \text{configuration.applied.term} = \text{mastership.term}$
 Verify the node's connection to the target.
 $\wedge \text{conn}[n].\text{connected}$
 $\wedge \text{target.running}$
 $\wedge \text{LET } \text{values} \triangleq [p \in \text{DOMAIN } \text{configuration.applied.values} \mapsto$
 IF $p \in \text{DOMAIN } \text{proposal}[i].\text{change.values}$ THEN
 $\text{proposal}[i].\text{rollback.values}[p]$
 ELSE
 $\text{configuration.applied.values}[p]$
 IN $\wedge \text{target}' = [\text{target} \text{ EXCEPT } !.\text{values} = \text{proposal}[i].\text{rollback.values} @@ \text{target.values}]$
 $\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = \text{proposal}[i].\text{rollback.index},$
 $!\text{applied.values} = \text{values}]$
 $\wedge \text{history}' = \text{Append}(\text{history}, [\text{type} \mapsto \text{Rollback}, \text{phase} \mapsto \text{Apply}, \text{index} \mapsto i])$
 $\wedge \text{UNCHANGED } \langle \text{proposal} \rangle$

$$\begin{aligned}
& index \mapsto 0, \\
& values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]], \\
& commit \mapsto None, \\
& apply \mapsto None]] \\
\wedge configuration = [\\
& committed \mapsto [\\
& \quad index \mapsto 0, \\
& \quad changeIndex \mapsto 0, \\
& \quad targetIndex \mapsto 0, \\
& \quad values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]], \\
& applied \mapsto [\\
& \quad index \mapsto 0, \\
& \quad changeIndex \mapsto 0, \\
& \quad targetIndex \mapsto 0, \\
& \quad term \mapsto 0, \\
& \quad target \mapsto 0, \\
& \quad values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]], \\
& \quad status \mapsto Pending] \\
\wedge mastership = [master \mapsto None, term \mapsto 0, conn \mapsto 0] \\
\wedge conn = [n \in Node \mapsto [id \mapsto 0, connected \mapsto FALSE]] \\
\wedge target = [\\
& \quad id \mapsto 0, \\
& \quad values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]], \\
& \quad running \mapsto FALSE] \\
\wedge history = \langle \rangle \\
\wedge mapping = [\\
& \quad configuration \mapsto [\\
& \quad \quad committed \mapsto [\\
& \quad \quad \quad values \mapsto configuration.committed.values], \\
& \quad \quad applied \mapsto [\\
& \quad \quad \quad term \mapsto configuration.applied.term, \\
& \quad \quad \quad target \mapsto configuration.applied.target, \\
& \quad \quad \quad values \mapsto configuration.applied.values], \\
& \quad \quad status \mapsto configuration.status], \\
& \quad proposal \mapsto [i \in \text{DOMAIN } proposal \mapsto [\\
& \quad \quad phase \mapsto proposal[i].phase, \\
& \quad \quad values \mapsto [p \in \text{DOMAIN } proposal[i].change.values \mapsto proposal[i].change.values[p].value], \\
& \quad \quad change \mapsto [\\
& \quad \quad \quad commit \mapsto \text{IF } \wedge proposal[i].change.commit = InProgress \\
& \quad \quad \quad \quad \wedge configuration.committed.changeIndex \geq i \\
& \quad \quad \quad \quad \text{THEN } Complete \\
& \quad \quad \quad \quad \text{ELSE } proposal[i].change.commit, \\
& \quad \quad \quad apply \mapsto \text{IF } \wedge proposal[i].change.apply = InProgress \\
& \quad \quad \quad \quad \wedge configuration.applied.changeIndex \geq i \\
& \quad \quad \quad \quad \text{THEN } Complete
\end{aligned}$$

$\text{rollback} \mapsto [$
 $\quad \text{commit} \mapsto \text{IF } \wedge \text{proposal}[i].\text{rollback.commit} = \text{InProgress}$
 $\quad \quad \wedge \text{configuration.committed.index} \neq i$
 $\quad \quad \text{THEN Complete}$
 $\quad \quad \text{ELSE proposal}[i].\text{rollback.commit},$
 $\quad \text{apply} \mapsto \text{IF } \wedge \text{proposal}[i].\text{rollback.commit} = \text{InProgress}$
 $\quad \quad \wedge \text{configuration.applied.index} \neq i$
 $\quad \quad \text{THEN Complete}$
 $\quad \quad \text{ELSE proposal}[i].\text{rollback.apply}]]]$

$\text{Next} \triangleq$

$\wedge \vee \exists i \in 1 \dots \text{NumProposals} :$
 $\quad \vee \text{ProposeChange}(i)$
 $\quad \vee \text{ProposeRollback}(i)$
 $\vee \exists n \in \text{Node}, i \in \text{DOMAIN proposal} :$
 $\quad \text{ProposalLog!Action}(\text{ReconcileProposal}(n, i), [\text{node} \mapsto n, \text{index} \mapsto i])$
 $\vee \exists n \in \text{Node} :$
 $\quad \text{ConfigurationLog!Action}(\text{ReconcileConfiguration}(n), [\text{node} \mapsto n])$
 $\vee \exists n \in \text{Node} :$
 $\quad \text{MastershipLog!Action}(\text{ReconcileMastership}(n), [\text{node} \mapsto n])$
 $\vee \exists n \in \text{Node} :$
 $\quad \vee \text{ConnectNode}(n)$
 $\quad \vee \text{DisconnectNode}(n)$
 $\vee \text{StartTarget}$
 $\vee \text{StopTarget}$
 $\wedge \text{mapping}' = [$
 $\quad \text{configuration} \mapsto [$
 $\quad \quad \text{committed} \mapsto [$
 $\quad \quad \quad \text{values} \mapsto \text{configuration}'.\text{committed.values},$
 $\quad \quad \text{applied} \mapsto [$
 $\quad \quad \quad \text{term} \mapsto \text{configuration}'.\text{applied.term},$
 $\quad \quad \quad \text{target} \mapsto \text{configuration}'.\text{applied.target},$
 $\quad \quad \quad \text{values} \mapsto \text{configuration}'.\text{applied.values},$
 $\quad \quad \quad \text{status} \mapsto \text{configuration}'.\text{status}],$
 $\quad \text{proposal} \mapsto [i \in \text{DOMAIN proposal}' \mapsto [$
 $\quad \quad \text{phase} \mapsto \text{proposal}'[i].\text{phase},$
 $\quad \quad \text{values} \mapsto [p \in \text{DOMAIN proposal}'[i].\text{change.values} \mapsto \text{proposal}'[i].\text{change.values}[p].\text{value}],$
 $\quad \quad \text{change} \mapsto [$
 $\quad \quad \quad \text{commit} \mapsto \text{IF } \wedge \text{proposal}'[i].\text{change.commit} = \text{InProgress}$
 $\quad \quad \quad \quad \wedge \text{configuration}'.\text{committed.changeIndex} \geq i$
 $\quad \quad \quad \quad \text{THEN Complete}$
 $\quad \quad \quad \quad \text{ELSE proposal}'[i].\text{change.commit},$
 $\quad \quad \quad \text{apply} \mapsto \text{IF } \wedge \text{proposal}'[i].\text{change.apply} = \text{InProgress}$
 $\quad \quad \quad \quad \wedge \text{configuration}'.\text{applied.changeIndex} \geq i$

$$\begin{aligned}
& \text{THEN } \textit{Complete} \\
& \text{ELSE } \textit{proposal}'[i].\textit{change.apply}], \\
\textit{rollback} \mapsto [& \\
& \textit{commit} \mapsto \text{IF } \wedge \textit{proposal}'[i].\textit{rollback.commit} = \textit{InProgress} \\
& \quad \wedge \textit{configuration}'.\textit{committed.index} \neq i \\
& \quad \text{THEN } \textit{Complete} \\
& \quad \text{ELSE } \textit{proposal}'[i].\textit{rollback.commit}, \\
& \textit{apply} \mapsto \text{IF } \wedge \textit{proposal}'[i].\textit{rollback.apply} = \textit{InProgress} \\
& \quad \wedge \textit{configuration}'.\textit{applied.index} \neq i \\
& \quad \text{THEN } \textit{Complete} \\
& \quad \text{ELSE } \textit{proposal}'[i].\textit{rollback.apply}]]] \\
\textit{Spec} \triangleq & \\
& \wedge \textit{Init} \\
& \wedge \Box[\textit{Next}]_{\textit{vars}} \\
& \wedge \forall i \in 1 \dots \textit{NumProposals} : \text{WF}_{\langle \textit{proposal}, \textit{configuration}, \textit{mastership}, \textit{conn}, \textit{target}, \textit{history} \rangle} (\textit{ProposeChange}(i) \vee \textit{Propose}) \\
& \wedge \forall n \in \textit{Node}, i \in 1 \dots \textit{NumProposals} : \text{WF}_{\langle \textit{proposal}, \textit{configuration}, \textit{mastership}, \textit{conn}, \textit{target}, \textit{history} \rangle} (\textit{ReconcilePropose}) \\
& \wedge \forall n \in \textit{Node} : \text{WF}_{\langle \textit{configuration}, \textit{mastership}, \textit{conn}, \textit{target} \rangle} (\textit{ReconcileConfiguration}(n)) \\
& \wedge \forall n \in \textit{Node} : \text{WF}_{\langle \textit{mastership}, \textit{conn}, \textit{target} \rangle} (\textit{ReconcileMastership}(n)) \\
& \wedge \forall n \in \textit{Node} : \text{WF}_{\langle \textit{conn}, \textit{target} \rangle} (\textit{ConnectNode}(n) \vee \textit{DisconnectNode}(n)) \\
& \wedge \text{WF}_{\langle \textit{target} \rangle} (\textit{StartTarget}) \\
& \wedge \text{WF}_{\langle \textit{target} \rangle} (\textit{StopTarget}) \\
\textit{Mapping} \triangleq & \text{INSTANCE } \textit{Config} \text{ WITH} \\
& \textit{proposal} \leftarrow \textit{mapping.proposal}, \\
& \textit{configuration} \leftarrow \textit{mapping.configuration} \\
\textit{Refinement} \triangleq & \textit{Mapping!Spec} \\
\textit{Order} \triangleq & \textit{Mapping!Order} \\
\textit{Consistency} \triangleq & \textit{Mapping!Consistency} \\
\textit{Liveness} \triangleq & \textit{Mapping!Liveness}
\end{aligned}$$
