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MODULE *ConfigImpl*

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INSTANCE *Naturals*  
 INSTANCE *FiniteSets*  
 INSTANCE *Sequences*  
 LOCAL INSTANCE *TLC*

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This section specifies constant parameters for the model.  
 CONSTANT *LogEnabled*  
 ASSUME *LogEnabled* ∈ BOOLEAN  
 CONSTANT *None*  
 ASSUME *None* ∈ STRING  
 CONSTANT *Node*  
 ASSUME  $\forall n \in \text{Node} : n \in \text{STRING}$   
 CONSTANTS  
     *Change*,  
     *Rollback*  
 $\text{Event} \triangleq \{\text{Change}, \text{Rollback}\}$   
 ASSUME  $\forall e \in \text{Event} : e \in \text{STRING}$   
 CONSTANTS  
     *Commit*,  
     *Apply*  
 $\text{Phase} \triangleq \{\text{Commit}, \text{Apply}\}$   
 ASSUME  $\forall p \in \text{Phase} : p \in \text{STRING}$   
 CONSTANTS  
     *Pending*,  
     *InProgress*,  
     *Complete*,  
     *Aborted*,  
     *Failed*  
 $\text{State} \triangleq \{\text{Pending}, \text{InProgress}, \text{Complete}, \text{Aborted}, \text{Failed}\}$   
 $\text{Done} \triangleq \{\text{Complete}, \text{Aborted}, \text{Failed}\}$

ASSUME  $\forall s \in State : s \in \text{STRING}$

CONSTANT *Path*

ASSUME  $\forall p \in Path : p \in \text{STRING}$

CONSTANT *Value*

ASSUME  $\forall v \in Value : v \in \text{STRING}$

$AllValues \triangleq Value \cup \{None\}$

CONSTANT *NumProposals*

ASSUME  $NumProposals \in Nat$

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This section defines model state variables.

$proposal \triangleq [ i \in 1 \dots Nat \mapsto [$   
     $phase \mapsto Phase,$   
     $change \mapsto [$   
         $values \mapsto Change,$   
         $commit \mapsto State,$   
         $apply \mapsto State],$   
     $rollback \mapsto [$   
         $index \mapsto Nat,$   
         $values \mapsto Change,$   
         $commit \mapsto State,$   
         $apply \mapsto State]]]$

$configuration \triangleq [$   
     $committed \mapsto [$   
         $index \mapsto Nat,$   
         $values \mapsto Change],$   
     $applied \mapsto [$   
         $index \mapsto Nat,$   
         $values \mapsto Change,$   
         $term \mapsto Nat]]]$

$mastership \triangleq [$   
     $master \mapsto \text{STRING},$   
     $term \mapsto Nat,$   
     $conn \mapsto Nat]$

$conn \triangleq [ n \in Node \mapsto [$   
     $id \mapsto Nat,$   
     $connected \mapsto \text{BOOLEAN} ]]$

$target \triangleq [$   
     $id \mapsto Nat,$   
     $values \mapsto Change,$   
     $running \mapsto \text{BOOLEAN} ]]$

VARIABLE *proposal*

VARIABLE *configuration*

VARIABLE *mastership*

VARIABLE *conn*

VARIABLE *target*

VARIABLE *history*

VARIABLE *mapping*

$\text{vars} \triangleq \langle \text{proposal}, \text{configuration}, \text{mastership}, \text{conn}, \text{target}, \text{history}, \text{mapping} \rangle$

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LOCAL *MastershipLog*  $\triangleq$  INSTANCE *Log* WITH

*File*  $\leftarrow$  "Mastership.log",

*CurrState*  $\leftarrow$  [

*target*  $\mapsto$  *target*,

*mastership*  $\mapsto$  *mastership*,

*conns*  $\mapsto$  *conn*],

*SuccState*  $\leftarrow$  [

*target*  $\mapsto$  *target'*,

*mastership*  $\mapsto$  *mastership'*,

*conns*  $\mapsto$  *conn'*],

*Enabled*  $\leftarrow$  *LogEnabled*

LOCAL *ConfigurationLog*  $\triangleq$  INSTANCE *Log* WITH

*File*  $\leftarrow$  "Configuration.log",

*CurrState*  $\leftarrow$  [

*configuration*  $\mapsto$  *configuration*,

*target*  $\mapsto$  *target*,

*mastership*  $\mapsto$  *mastership*,

*conns*  $\mapsto$  *conn*],

*SuccState*  $\leftarrow$  [

*configuration*  $\mapsto$  *configuration'*,

*target*  $\mapsto$  *target'*,

*mastership*  $\mapsto$  *mastership'*,

*conns*  $\mapsto$  *conn'*],

*Enabled*  $\leftarrow$  *LogEnabled*

LOCAL *ProposalLog*  $\triangleq$  INSTANCE *Log* WITH

*File*  $\leftarrow$  "Proposal.log",

*CurrState*  $\leftarrow$  [

*proposals*  $\mapsto [i \in \{i \in \text{DOMAIN } \text{proposal} : \text{proposal}[i].\text{phase} \neq \text{None}\} \mapsto \text{proposal}[i]],$

$$\begin{aligned}
& configuration \mapsto configuration, \\
& target \mapsto target, \\
& mastership \mapsto mastership, \\
& conns \mapsto conn], \\
SuccState \leftarrow [ \\
& proposals \mapsto [i \in \{i \in \text{DOMAIN } proposal' : proposal'[i].phase \neq \text{None}\} \mapsto proposal'[i]], \\
& configuration \mapsto configuration', \\
& target \mapsto target', \\
& mastership \mapsto mastership', \\
& conns \mapsto conn'], \\
Enabled \leftarrow LogEnabled
\end{aligned}$$


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This section models configuration target.

$$\begin{aligned}
StartTarget & \triangleq \\
& \wedge \neg target.running \\
& \wedge target' = [target \text{ EXCEPT } !.id = target.id + 1, \\
& \quad !.running = \text{TRUE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, conn, history \rangle \\
StopTarget & \triangleq \\
& \wedge target.running \\
& \wedge target' = [target \text{ EXCEPT } !.running = \text{FALSE}, \\
& \quad !.values = [p \in \{\} \mapsto [value \mapsto \text{None}]]] \\
& \wedge conn' = [n \in Node \mapsto [conn[n] \text{ EXCEPT } !.connected = \text{FALSE}]] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, history \rangle
\end{aligned}$$


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This section models nodes connection to the configuration target.

$$\begin{aligned}
ConnectNode(n) & \triangleq \\
& \wedge \neg conn[n].connected \\
& \wedge target.running \\
& \wedge conn' = [conn \text{ EXCEPT } ![n].id = conn[n].id + 1, \\
& \quad ![n].connected = \text{TRUE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, target, history \rangle \\
DisconnectNode(n) & \triangleq \\
& \wedge conn[n].connected \\
& \wedge conn' = [conn \text{ EXCEPT } ![n].connected = \text{FALSE}] \\
& \wedge \text{UNCHANGED } \langle proposal, configuration, mastership, target, history \rangle
\end{aligned}$$


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This section models *mastership* reconciliation.







$$\begin{aligned}
& \wedge \text{configuration.applied.changeIndex} = i - 1 \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i, \\
& \quad !.\text{applied.changeIndex} = i] \\
& \wedge \text{UNCHANGED } \langle \text{proposal}, \text{target}, \text{history} \rangle
\end{aligned}$$

$\text{CommitRollback}(n, i) \triangleq$

'index' is the current index committed to the configuration  
'changeIndex' is the maximum change index committed to the configuration  
'targetIndex' is the index of the proposal currently being committed  
*targetIndex* is always changed first. Once the rollback is committed, the index will be decremented to match the *targetIndex*. The next time a change is committed, the index will increase again. If the committed index is equal to this proposal index, this proposal is the next to be rolled back. To roll back a proposal, the target index is set to the proposal's rollback index. When the rollback is committed, the committed index is set to the proposal's rollback index, thus matching the *targetIndex*. This unblocks new changes to be committed.

$$\begin{aligned}
& \wedge \vee \wedge \text{proposal}[i].\text{rollback.commit} = \text{Pending} \\
& \quad \wedge \text{configuration.committed.changeIndex} \geq i \\
& \quad \wedge \text{configuration.committed.index} = i \\
& \quad \wedge \vee \wedge \text{configuration.committed.targetIndex} = i \\
& \quad \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.targetIndex} = \text{proposal}[i].\text{rollback.index}] \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \quad \vee \wedge \text{configuration.committed.targetIndex} = \text{proposal}[i].\text{rollback.index} \\
& \quad \quad \wedge \vee \wedge \text{proposal}[i].\text{change.commit} \neq \text{Aborted} \\
& \quad \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.commit} = \text{InProgress}] \\
& \quad \quad \quad \vee \wedge \text{proposal}[i].\text{change.commit} = \text{Aborted} \\
& \quad \quad \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.commit} = \text{Complete}] \\
& \quad \quad \quad \wedge \text{UNCHANGED } \langle \text{configuration} \rangle \\
& \quad \wedge \text{UNCHANGED } \langle \text{history} \rangle \\
& \vee \wedge \text{proposal}[i].\text{rollback.commit} = \text{InProgress} \\
& \quad \wedge \vee \wedge \text{configuration.committed.index} = i \\
& \quad \quad \wedge \text{LET } \text{values} \triangleq [p \in \text{DOMAIN } \text{configuration.committed.values} \mapsto \\
& \quad \quad \quad \text{IF } p \in \text{DOMAIN } \text{proposal}[i].\text{rollback.values} \text{ THEN} \\
& \quad \quad \quad \quad \text{proposal}[i].\text{rollback.values}[p] \\
& \quad \quad \quad \text{ELSE} \\
& \quad \quad \quad \quad \text{configuration.committed.values}[p]] \\
& \quad \quad \text{IN } \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = \text{proposal}[i].\text{rollback.index}, \\
& \quad \quad \quad !.\text{committed.values} = \text{values}] \\
& \quad \quad \wedge \text{history}' = \text{Append}(\text{history}, [\text{type} \mapsto \text{Rollback}, \text{phase} \mapsto \text{Commit}, \text{index} \mapsto i]) \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \quad \vee \wedge \text{configuration.committed.index} = \text{proposal}[i].\text{rollback.index} \\
& \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.commit} = \text{Complete}] \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
& \vee \wedge \text{proposal}[i].\text{rollback.commit} = \text{Complete}
\end{aligned}$$



$\wedge \text{proposal}[i].\text{change.commit} = \text{Aborted}$   
 $\wedge \text{configuration.committed.targetIndex} = \text{proposal}[i].\text{rollback.index}$   
 $\wedge \text{configuration.committed.index} \neq \text{proposal}[i].\text{rollback.index}$   
 $\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = \text{proposal}[i].\text{rollback.index}]$   
 $\wedge \text{UNCHANGED } \langle \text{proposal}, \text{history} \rangle$   
 $\wedge \text{UNCHANGED } \langle \text{target} \rangle$

$\text{ApplyRollback}(n, i) \triangleq$

'index' is the current index applied to the configuration  
 'changeIndex' is the maximum change index applied to the configuration  
 'targetIndex' is the index of the proposal currently being applied  
*targetIndex* is always changed first. Once the rollback is applied, the index will be decremented to match the *targetIndex*. The next time a change is applied, the index will increase again. If the applied index is equal to this proposal index, this proposal is the next to be rolled back. To roll back a proposal, the target index is set to the proposal's rollback index. When the rollback is applied, the applied index is set to the proposal's rollback index, thus matching the *targetIndex*. This unblocks new changes to be applied.

$\wedge \vee \wedge \text{proposal}[i].\text{rollback.apply} = \text{Pending}$   
 $\wedge \text{configuration.committed.index} \leq \text{proposal}[i].\text{rollback.index}$   
 $\wedge \text{configuration.applied.changeIndex} \geq i$   
 $\wedge \text{configuration.applied.index} = i$   
 $\wedge \vee \wedge \text{configuration.applied.targetIndex} = i$   
 $\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.targetIndex} = \text{proposal}[i].\text{rollback.index}]$   
 $\wedge \text{UNCHANGED } \langle \text{proposal} \rangle$   
 $\vee \wedge \text{configuration.applied.targetIndex} = \text{proposal}[i].\text{rollback.index}$   
 $\wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![i].\text{rollback.apply} = \text{InProgress}]$   
 $\wedge \text{UNCHANGED } \langle \text{configuration} \rangle$   
 $\wedge \text{UNCHANGED } \langle \text{target}, \text{history} \rangle$   
 $\vee \wedge \text{proposal}[i].\text{rollback.apply} = \text{InProgress}$   
 $\wedge \vee \wedge \text{configuration.applied.index} = i$   
 Verify the applied term is the current *mastership* term to ensure the configuration has been synchronized following restarts.  
 $\wedge \text{configuration.applied.term} = \text{mastership.term}$   
 Verify the node's connection to the target.  
 $\wedge \text{conn}[n].\text{connected}$   
 $\wedge \text{target.running}$   
 $\wedge \text{LET } \text{values} \triangleq [p \in \text{DOMAIN } \text{configuration.applied.values} \mapsto$   
     IF  $p \in \text{DOMAIN } \text{proposal}[i].\text{rollback.values}$  THEN  
          $\text{proposal}[i].\text{rollback.values}[p]$   
     ELSE  
          $\text{configuration.applied.values}[p]$   
 IN    $\wedge \text{target}' = [\text{target} \text{ EXCEPT } !.\text{values} = \text{proposal}[i].\text{rollback.values} @@ \text{target.values}]$   
        $\wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = \text{proposal}[i].\text{rollback.index},$



$$\begin{aligned}
& \text{commit} \mapsto \text{None}, \\
& \text{apply} \mapsto \text{None}], \\
& \text{rollback} \mapsto [ \\
& \quad \text{index} \mapsto 0, \\
& \quad \text{values} \mapsto [p \in \{\} \mapsto [\text{index} \mapsto 0, \text{value} \mapsto \text{None}]], \\
& \quad \text{commit} \mapsto \text{None}, \\
& \quad \text{apply} \mapsto \text{None}]] \\
\wedge \text{configuration} = [ \\
& \quad \text{committed} \mapsto [ \\
& \quad \quad \text{index} \mapsto 0, \\
& \quad \quad \text{changeIndex} \mapsto 0, \\
& \quad \quad \text{targetIndex} \mapsto 0, \\
& \quad \quad \text{values} \mapsto [p \in \{\} \mapsto [\text{index} \mapsto 0, \text{value} \mapsto \text{None}]]], \\
& \quad \text{applied} \mapsto [ \\
& \quad \quad \text{index} \mapsto 0, \\
& \quad \quad \text{changeIndex} \mapsto 0, \\
& \quad \quad \text{targetIndex} \mapsto 0, \\
& \quad \quad \text{term} \mapsto 0, \\
& \quad \quad \text{target} \mapsto 0, \\
& \quad \quad \text{values} \mapsto [p \in \{\} \mapsto [\text{index} \mapsto 0, \text{value} \mapsto \text{None}]]], \\
& \quad \text{status} \mapsto \text{Pending}] \\
\wedge \text{mastership} = [\text{master} \mapsto \text{None}, \text{term} \mapsto 0, \text{conn} \mapsto 0] \\
\wedge \text{conn} = [n \in \text{Node} \mapsto [\text{id} \mapsto 0, \text{connected} \mapsto \text{FALSE}]] \\
\wedge \text{target} = [ \\
& \quad \text{id} \mapsto 0, \\
& \quad \text{values} \mapsto [p \in \{\} \mapsto [\text{index} \mapsto 0, \text{value} \mapsto \text{None}]], \\
& \quad \text{running} \mapsto \text{FALSE}] \\
\wedge \text{history} = \langle \rangle \\
\wedge \text{mapping} = [ \\
& \quad \text{configuration} \mapsto [ \\
& \quad \quad \text{committed} \mapsto [ \\
& \quad \quad \quad \text{values} \mapsto \text{configuration.committed.values}, \\
& \quad \quad \text{applied} \mapsto [ \\
& \quad \quad \quad \text{term} \mapsto \text{configuration.applied.term}, \\
& \quad \quad \quad \text{target} \mapsto \text{configuration.applied.target}, \\
& \quad \quad \quad \text{values} \mapsto \text{configuration.applied.values}, \\
& \quad \quad \text{status} \mapsto \text{configuration.status}], \\
& \quad \text{proposal} \mapsto [i \in \text{DOMAIN proposal} \mapsto [ \\
& \quad \quad \text{phase} \mapsto \text{proposal}[i].\text{phase}, \\
& \quad \quad \text{values} \mapsto [p \in \text{DOMAIN proposal}[i].\text{change.values} \mapsto \text{proposal}[i].\text{change.values}[p].\text{value}], \\
& \quad \quad \text{change} \mapsto [ \\
& \quad \quad \quad \text{commit} \mapsto \text{IF } \wedge \text{proposal}[i].\text{change.commit} = \text{InProgress} \\
& \quad \quad \quad \quad \wedge \text{configuration.committed.changeIndex} \geq i \\
& \quad \quad \quad \quad \text{THEN Complete} \\
& \quad \quad \quad \quad \text{ELSE proposal}[i].\text{change.commit},
\end{aligned}$$

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apply   $\mapsto$  IF  $\wedge$  proposal[i].change.apply = InProgress
            $\wedge$  configuration.applied.changeIndex  $\geq$  i
           THEN Complete
           ELSE proposal[i].change.apply],
rollback  $\mapsto$  [
  commit  $\mapsto$  IF  $\wedge$  proposal[i].rollback.commit = InProgress
                 $\wedge$  configuration.committed.index  $\neq$  i
                THEN Complete
                ELSE proposal[i].rollback.commit,
  apply   $\mapsto$  IF  $\wedge$  proposal[i].rollback.commit = InProgress
                 $\wedge$  configuration.applied.index  $\neq$  i
                THEN Complete
                ELSE proposal[i].rollback.apply]]]

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*Next*  $\triangleq$

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 $\wedge \vee \exists i \in 1 \dots \text{NumProposals} :$ 
   $\vee \text{ProposeChange}(i)$ 
   $\vee \text{ProposeRollback}(i)$ 
 $\vee \exists n \in \text{Node}, i \in \text{DOMAIN } \text{proposal} :$ 
  ProposalLog! Action(ReconcileProposal(n, i), [node  $\mapsto$  n, index  $\mapsto$  i])
 $\vee \exists n \in \text{Node} :$ 
  ConfigurationLog! Action(ReconcileConfiguration(n), [node  $\mapsto$  n])
 $\vee \exists n \in \text{Node} :$ 
  MastershipLog! Action(ReconcileMastership(n), [node  $\mapsto$  n])
 $\vee \exists n \in \text{Node} :$ 
   $\vee \text{ConnectNode}(n)$ 
   $\vee \text{DisconnectNode}(n)$ 
 $\vee \text{StartTarget}$ 
 $\vee \text{StopTarget}$ 
 $\wedge \text{mapping}' = [$ 
  configuration  $\mapsto$  [
    committed  $\mapsto$  [
      values  $\mapsto$  configuration'.committed.values],
    applied  $\mapsto$  [
      term  $\mapsto$  configuration'.applied.term,
      target  $\mapsto$  configuration'.applied.target,
      values  $\mapsto$  configuration'.applied.values],
    status  $\mapsto$  configuration'.status],
  proposal  $\mapsto$  [i  $\in$  DOMAIN proposal'  $\mapsto$  [
    phase  $\mapsto$  proposal'[i].phase,
    values  $\mapsto$  [p  $\in$  DOMAIN proposal'[i].change.values  $\mapsto$  proposal'[i].change.values[p].value],
    change  $\mapsto$  [
      commit  $\mapsto$  IF  $\wedge$  proposal'[i].change.commit = InProgress
                     $\wedge$  configuration'.committed.changeIndex  $\geq$  i
                    THEN Complete

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$$\begin{aligned}
& \text{ELSE } \text{proposal}'[i].\text{change.commit}, \\
\text{apply} \mapsto & \text{IF } \wedge \text{proposal}'[i].\text{change.apply} = \text{InProgress} \\
& \wedge \text{configuration}'.\text{applied.changeIndex} \geq i \\
& \text{THEN } \text{Complete} \\
& \text{ELSE } \text{proposal}'[i].\text{change.apply}], \\
\text{rollback} \mapsto & [ \\
& \text{commit} \mapsto \text{IF } \wedge \text{proposal}'[i].\text{rollback.commit} = \text{InProgress} \\
& \wedge \text{configuration}'.\text{committed.index} \neq i \\
& \text{THEN } \text{Complete} \\
& \text{ELSE } \text{proposal}'[i].\text{rollback.commit}, \\
& \text{apply} \mapsto \text{IF } \wedge \text{proposal}'[i].\text{rollback.apply} = \text{InProgress} \\
& \wedge \text{configuration}'.\text{applied.index} \neq i \\
& \text{THEN } \text{Complete} \\
& \text{ELSE } \text{proposal}'[i].\text{rollback.apply}]]]
\end{aligned}$$

$$\text{Spec} \triangleq$$

$$\begin{aligned}
& \wedge \text{Init} \\
& \wedge \square[\text{Next}]_{\text{vars}} \\
& \wedge \forall i \in 1 \dots \text{NumProposals} : \text{WF}_{\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{conn}, \text{target}, \text{history} \rangle} (\text{ProposeChange}(i) \vee \text{ProposeChange}(i)) \\
& \wedge \forall n \in \text{Node}, i \in 1 \dots \text{NumProposals} : \text{WF}_{\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{conn}, \text{target}, \text{history} \rangle} (\text{ReconcileProposals}(i, n)) \\
& \wedge \forall n \in \text{Node} : \text{WF}_{\langle \text{configuration}, \text{mastership}, \text{conn}, \text{target} \rangle} (\text{ReconcileConfiguration}(n)) \\
& \wedge \forall n \in \text{Node} : \text{WF}_{\langle \text{mastership}, \text{conn}, \text{target} \rangle} (\text{ReconcileMastership}(n)) \\
& \wedge \forall n \in \text{Node} : \text{WF}_{\langle \text{conn}, \text{target} \rangle} (\text{ConnectNode}(n) \vee \text{DisconnectNode}(n)) \\
& \wedge \text{WF}_{\langle \text{target} \rangle} (\text{StartTarget}) \\
& \wedge \text{WF}_{\langle \text{target} \rangle} (\text{StopTarget})
\end{aligned}$$

$$\begin{aligned}
\text{Mapping} & \triangleq \text{INSTANCE } \text{Config} \text{ WITH} \\
& \text{proposal} \leftarrow \text{mapping.proposal}, \\
& \text{configuration} \leftarrow \text{mapping.configuration}
\end{aligned}$$

$$\text{Refinement} \triangleq \text{Mapping!Spec}$$

$$\text{Order} \triangleq \text{Mapping!Order}$$

$$\text{Consistency} \triangleq \text{Mapping!Consistency}$$

$$\text{Liveness} \triangleq \text{Mapping!Liveness}$$


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