```
— Module Config
INSTANCE Naturals
INSTANCE FiniteSets
Instance Sequences
INSTANCE TLC
 An empty constant
Constant Nil
 Transaction type constants
CONSTANTS
   Change,
   Rollback
 Transaction isolation constants
CONSTANTS
   Read Committed,\\
   Serializable \\
 Phase constants
CONSTANTS
   Initialize,
   Validate,
   Abort,
   Commit,
   Apply
Phase \stackrel{\triangle}{=}
   LET phases \triangleq \langle Initialize,
                     Validate,
                     Abort,
                     Commit,
                     Apply\rangle
        [p \in \{phases[i] : i \in \text{DOMAIN } phases\} \mapsto
          CHOOSE i \in \text{DOMAIN } phases: phases[i] = p]
 Status constants
CONSTANTS
   Pending,
   Complete,
   Failed
Status \triangleq
```

```
LET statuses \stackrel{\triangle}{=} \langle Pending,
                           Complete,
                           Failed
         [s \in \{statuses[i] : i \in DOMAIN \ statuses\} \mapsto
            CHOOSE i \in DOMAIN \ statuses : statuses[i] = s]
CONSTANTS
    Valid.
   Invalid
CONSTANTS
   Success,
    Failure
 The set of all nodes
CONSTANT Node
Target is the set of all targets and their possible paths and values.
Example: Target \stackrel{\Delta}{=} [
    target1 \mapsto [persistent \mapsto FALSE, values \mapsto [
         path1 \mapsto \{"value1", "value2"\},\
         path2 \mapsto \{"value2", "value3"\}]],
    target2 \mapsto [persistent \mapsto TRUE, values \mapsto [
         path2 \mapsto \{\text{``value3''}, \text{``value4''}\},
         path3 \mapsto \{"value4", "value5"\}]]
CONSTANT Target
```

Configuration update/rollback requests are tracked and processed through two data types. Transactions represent the lifecycle of a single configuration change request and are stored in an appendonly log. Configurations represent the desired configuration of a gNMI target based on the aggregate of relevant changes in the Transaction log.

```
\begin{split} & \text{TYPE Type} ::= type \in \\ & \{Change, \\ & Rollback\} \\ & \text{TYPE Phase} ::= phase \in \\ & \{Initialize, \\ & Validate, \\ & Abort, \\ & Commit, \\ & Apply\} \\ & \text{TYPE Status} ::= status \in \\ & \{Pending, \\ & Initializing, \\ & Initialized, \\ & Validating, \\ & Validated, \\ \end{split}
```

```
Committing,
  Committed,
  Applying,
  Applied,
  Synchronizing,
  Synchronized,\\
  Persisted,
  Failed}
TYPE Transaction \stackrel{\Delta}{=} [
  type ::= type \in Type,
  index ::= index \in Nat,
  isolation ::= isolation \in \{IsolationDefault, IsolationSerializable\}
  values ::= [
   target \in SUBSET (DOMAIN Target) \mapsto [path \in SUBSET (DOMAIN Target[target].values) \mapsto
        value ::= value \in STRING,
        delete ::= delete \in BOOLEAN ]]],
  rollback ::= index \in Nat,
  targets ::= targets \in SUBSET (DOMAIN Target)
  phase ::= phase \in Phase
  status ::= status \in Status]
TYPE Proposal \stackrel{\Delta}{=} [
  type
          ::= type \in Type,
              ::=index \in Nat,
  index
  values
              ::= [path \in SUBSET (DOMAIN Target[target].values) \mapsto [
      value ::= value \in STRING,
      delete := delete \in BOOLEAN ]],
  rollback ::= index \in Nat,
  dependencyIndex ::= dependencyIndex \in \mathit{Nat},
  rollbackIndex ::= rollbackIndex \in Nat,
  rollbackValues ::= [path \in SUBSET (DOMAIN Target[target].values) \mapsto [
      value ::= value \in STRING,
      delete := delete \in BOOLEAN ]],
         ::= phase \in Phase
  phase
            ::= status \in Status]
  status
TYPE Configuration \stackrel{\Delta}{=} [
          ::=id\in STRING,
  id
          target
  values
      value ::= value \in STRING,
      index ::= index \in Nat,
      deleted ::= delete \in BOOLEAN ]],
  configIndex ::= configIndex \in \mathit{Nat},
  configTerm ::= configTerm \in Nat,
  proposedIndex ::= proposedIndex \in Nat,
  committedIndex ::= committedIndex \in Nat,
  appliedIndex ::= appliedIndex \in Nat,
  appliedTerm := appliedTerm \in Nat,
```

```
appliedValues ::= [path \in SUBSET (DOMAIN Target[target]) \mapsto [
       value ::= value \in STRING,
       index ::= index \in Nat,
       deleted ::= delete \in BOOLEAN ]],
   status ::= status \in Status
 A transaction log. Transactions may either request a set
 of changes to a set of targets or rollback a prior change.
VARIABLE transaction
A record of per-target proposals
VARIABLE proposal
 A record of per-target configurations
VARIABLE configuration
 A record of target states
Variable target
 A record of target masterships
VARIABLE mastership
```

This section models *mastership* for the configuration service.

 $vars \triangleq \langle transaction, proposal, configuration, mastership, target \rangle$

Mastership is used primarily to track the lifecycle of individual configuration targets and react to state changes on the southbound. Each target is assigned a master from the Node set, and masters can be unset when the target disconnects.

This section models configuration changes and rollbacks. Changes are appended to the transaction \log and processed asynchronously.

```
Value(s, t, p) \triangleq
LET value \triangleq CHOOSE v \in s : v.target = t \land v.path = p
IN
```

```
[value \mapsto value.value,
        delete \mapsto value.delete
Paths(s, t) \triangleq
   [p \in \{v.path : v \in \{v \in s : v.target = t\}\} \mapsto Value(s, t, p)]
Changes(s) \triangleq
   [t \in \{v.target : v \in s\} \mapsto Paths(s, t)]
ValidValues(t, p) \triangleq
   UNION \{\{[value \mapsto v, delete \mapsto FALSE] : v \in Target[t].values[p]\}, \{[value \mapsto Nil, delete \mapsto TRUE]\}\}
ValidPaths(t) \triangleq
   UNION \{\{v @@ [path \mapsto p] : v \in ValidValues(t, p)\} : p \in DOMAIN Target[t].values\}
ValidTargets \triangleq
   UNION \{\{p@@[target \mapsto t] : p \in ValidPaths(t)\} : t \in DOMAIN Target\}
 The set of all valid sets of changes to all targets and their paths.
 The set of possible changes is computed from the Target model value.
ValidChanges \triangleq
   LET changeSets \stackrel{\triangle}{=} \{s \in \text{SUBSET } ValidTargets :
                                 \forall t \in \text{DOMAIN } Target :
                                   \forall p \in \text{DOMAIN } Target[t].values:
                                     Cardinality(\{v \in s : v.target = t \land v.path = p\}) \le 1\}
   IN
       \{Changes(s): s \in changeSets\}
 The next available index in the transaction log.
 This is computed as the max of the existing indexes in the log to
 allow for changes to the \log (e.g. \log \text{ compaction}) to be modeled.
NextIndex \triangleq
   IF DOMAIN transaction = \{\} THEN
      1
    ELSE
      LET i \stackrel{\triangle}{=} \text{CHOOSE } i \in \text{DOMAIN } transaction :
            \forall j \in \text{DOMAIN } transaction : i \geq j
      IN i+1
 Add a set of changes 'c' to the transaction log
RequestChange(c) \triangleq
    \land \exists isolation \in \{ReadCommitted, Serializable\}:
         \land transaction' = transaction @@ (NextIndex:> [type])
                                                                                   \mapsto Change.
                                                                       index
                                                                                   \mapsto NextIndex,
                                                                       isolation \mapsto isolation,
                                                                       values
                                                                                   \mapsto c,
                                                                       targets \mapsto \{\},\
```

```
\mapsto Initialize,
                                                                   phase
                                                                               \mapsto Pending)
                                                                   status
   ∧ UNCHANGED ⟨proposal, configuration, mastership, target⟩
 Add a rollback of transaction 't' to the transaction log
RequestRollback(t) \triangleq
   \land \exists isolation \in \{ReadCommitted, Serializable\}:
         \land transaction' = transaction @@ (NextIndex:> [type])
                                                                               \mapsto Rollback.
                                                                               \mapsto NextIndex,
                                                                   isolation \mapsto isolation,
                                                                   rollback \mapsto t,
                                                                   targets
                                                                              \mapsto {},
                                                                   phase
                                                                               \mapsto Initialize,
                                                                               \mapsto Pending)
                                                                   status
   \land UNCHANGED \langle proposal, configuration, mastership, target <math>\rangle
```

This section models the Transaction log reconciler.

Transactions come in two flavors: - Change transactions contain a set of changes to be applied to a set of targets - Rollback transactions reference a prior change transaction to be reverted to the previous state

Transacations proceed through a series of phases:

- * Initialize create and link Proposals
- * Validate validate changes and rollbacks
- * Commit commit changes to Configurations
- * Apply commit changes to Targets

Reconcile a transaction

```
ReconcileTransaction(n, i) \stackrel{\Delta}{=}
```

Initialize is the only transaction phase that's globally serialized. While in the *Initializing* phase, the reconciler checks whether the prior transaction has been *Initialized* before creating Proposals in the *Initialize* phase. Once all of the transaction's proposals have been *Initialized*, the transaction will be marked *Initialized*. If any proposal is *Failed*, the transaction will be marked *Failed* as well.

If the transaction is a change, the targets are taken from the change values.

```
\land \lor \land transaction[i].type = Change
         \land transaction' = [transaction \ EXCEPT \ ![i].targets = DOMAIN \ transaction[i].values]
         \land proposal' = [t \in DOMAIN \ proposal \mapsto
               If t \in \text{DOMAIN } transaction[i].values \text{ THEN}
                  proposal[t]@@(i:>[type]
                                                                  \mapsto Change,
                                            index
                                                                  \mapsto i,
                                            values
                                                                  \mapsto transaction[i].values[t],
                                            dependencyIndex \mapsto 0,
                                            rollbackIndex
                                                                  \mapsto 0,
                                            rollbackValues
                                                                 \mapsto \langle \rangle,
                                            phase
                                                                 \mapsto Initialize,
                                                                 \mapsto Pending)
                                            status
                ELSE
                  proposal[t]]
       If the transaction is a rollback, the targets affected are
       the targets of the change transaction being rolled back.
      \lor \land transaction[i].type = Rollback
         \land \lor \land transaction[i].rollback \in DOMAIN transaction
               \land transaction[transaction[i].rollback].type = Change
               \land transaction' = [transaction \ EXCEPT \ ![i].targets =
                                       DOMAIN transaction[transaction[i].rollback].values]
               \land proposal' = [t \in DOMAIN \ proposal \mapsto
                     If t \in \text{DOMAIN}\ transaction[transaction[i].rollback].values\ \text{THEN}
                        proposal[t]@@(i:>[type]
                                                                        \mapsto Rollback,
                                                  index
                                                                        \mapsto i,
                                                  rollback
                                                                        \mapsto transaction[i].rollback,
                                                  dependencyIndex \mapsto 0,
                                                  rollbackIndex
                                                                        \mapsto 0.
                                                  rollbackValues
                                                                       \mapsto \langle \rangle,
                                                                        \mapsto Initialize,
                                                  phase
                                                  status
                                                                        \mapsto Pending)
                      ELSE
                         proposal[t]]
            \lor \land \lor \land transaction[i].rollback \in DOMAIN transaction
                      \land transaction[transaction[i].rollback].type = Rollback
                   \vee transaction[i].rollback \notin DOMAIN transaction
               \land transaction' = [transaction \ EXCEPT \ ![i].status = Failed]
               \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].targets \neq \{\}
       If all proposals have been Complete, mark the transaction Complete.
   \land \lor \land \forall t \in transaction[i].targets:
              \land proposal[t][i].phase = Initialize
              \land proposal[t][i].status = Complete
         \land transaction' = [transaction \ \texttt{except} \ ![i].status = Complete]
         \land UNCHANGED \langle proposal \rangle
```

```
If any proposal has been Failed, mark the transaction Failed.
                  \lor \land \exists t \in transaction[i].targets:
                          \land proposal[t][i].phase = Initialize
                          \land proposal[t][i].status = Failed
                     \land transaction' = [transaction \ EXCEPT \ ![i].status = Failed]
                     \land UNCHANGED \langle proposal \rangle
       Once the transaction has been Initialized, proceed to the Validate phase.
       If any of the transaction's proposals depend on a Serializable transaction,
       verify the dependency has been Validated to preserve serializability before
       moving the transaction to the Validate phase.
      \vee \wedge transaction[i].status = Complete
         \land \forall t \in transaction[i].targets:
              \land proposal[t][i].dependencyIndex > 0 \Rightarrow
                    \vee transaction[proposal[t][i].dependencyIndex].isolation \neq Serializable
                    \lor Phase[transaction[proposal[t][i].dependencyIndex].phase] > Phase[Validate]
                    \lor \land transaction[proposal[t][i].dependencyIndex].phase = Validate
                       \land \ transaction[proposal[t][i].dependencyIndex].status \in \{Complete, Failed\}
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Validate,
                                                       ![i].status = Pending]
         \land UNCHANGED \langle proposal \rangle
      \lor \land transaction[i].status = Failed
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Abort,
                                                       ![i].status = Pending
         \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].phase = Validate
   \land \lor \land transaction[i].status = Pending
             Move the transaction's proposals to the Validating state
         \land \lor \land \exists t \in transaction[i].targets : proposal[t][i].phase \neq Validate
               \land proposal' = [t \in DOMAIN \ proposal \mapsto
                                  If t \in transaction[i].targets then
                                     [proposal[t] \text{ EXCEPT } ![i].phase = Validate,
                                                              ![i].status = Pending
                                   ELSE
                                     proposal[t]]
               ∧ UNCHANGED ⟨transaction⟩
            If all proposals have been Complete, mark the transaction Complete.
            \lor \land \forall t \in transaction[i].targets:
                    \land proposal[t][i].phase = Validate
                    \land proposal[t][i].status = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].status = Complete]
               \land UNCHANGED \langle proposal \rangle
            If any proposal has been Failed, mark the transaction Failed.
            \vee \wedge \exists t \in transaction[i].targets:
                    \land proposal[t][i].phase = Validate
                    \land proposal[t][i].status = Failed
```

```
\land transaction' = [transaction \ EXCEPT \ ![i].status = Failed]
              \land UNCHANGED \langle proposal \rangle
      Once the transaction has been Validated, proceed to the Commit phase.
      If any of the transaction's proposals depend on a Serializable transaction,
      verify the dependency has been Committed to preserve serializability before
      moving the transaction to the Commit phase.
      \lor \land transaction[i].status = Complete
         \land \forall t \in transaction[i].targets:
              \land proposal[t][i].dependencyIndex > 0 \Rightarrow
                    \lor transaction[proposal[t][i].dependencyIndex].isolation \neq Serializable
                    \lor Phase[transaction[proposal[t][i].dependencyIndex].phase] > Phase[Commit]
                    \lor \land transaction[proposal[t][i].dependencyIndex].phase = Commit
                       \land transaction[proposal[t][i].dependencyIndex].status \in \{Complete, Failed\}
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Commit,
                                                      ![i].status = Pending
         \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].phase = Commit
   \land \lor \land transaction[i].status = Pending
            Move the transaction's proposals to the Committing state
         \land \lor \land \exists t \in transaction[i].targets : proposal[t][i].phase \neq Commit
              \land proposal' = [t \in DOMAIN \ proposal \mapsto
                                 If t \in transaction[i].targets THEN
                                    [proposal[t] \text{ EXCEPT } ![i].phase = Commit,
                                                            ![i].status = Pending
                                  ELSE
                                    proposal[t]]
              \land UNCHANGED \langle transaction \rangle
            If all proposals have been Complete, mark the transaction Complete.
           \lor \land \forall t \in transaction[i].targets:
                   \land proposal[t][i].phase = Commit
                   \land proposal[t][i].status = Complete
              \land transaction' = [transaction \ EXCEPT \ ![i].status = Complete]
              \land UNCHANGED \langle proposal \rangle
      Once the transaction has been Committed, proceed to the Apply phase.
      If any of the transaction's proposals depend on a Serializable transaction,
      verify the dependency has been Applied to preserve serializability before
      moving the transaction to the Apply phase.
      \lor \land transaction[i].status = Complete
         \land \forall t \in transaction[i].targets:
              \land proposal[t][i].dependencyIndex > 0 \Rightarrow
                    \lor transaction[proposal[t][i].dependencyIndex].isolation \neq Serializable
                    \lor Phase[transaction[proposal[t][i].dependencyIndex].phase] > Phase[Apply]
                    \lor \land transaction[proposal[t][i].dependencyIndex].phase = Apply
                       \land transaction[proposal[t][i].dependencyIndex].status \in \{Complete, Failed\}
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Apply,
```

```
![i].status = Pending]
             \land UNCHANGED \langle proposal \rangle
   \lor \land transaction[i].phase = Apply
      \land transaction[i].status = Pending
          Move the transaction's proposals to the Applying state
      \land \lor \land \exists t \in transaction[i].targets : proposal[t][i].phase \neq Apply
             \land proposal' = [t \in DOMAIN \ proposal \mapsto
                                If t \in transaction[i].targets Then
                                   [proposal[t] \text{ EXCEPT } ![i].phase = Apply,
                                                             ![i].status = Pending
                                   proposal[t]]
             \land UNCHANGED \langle transaction \rangle
          If all proposals have been Complete, mark the transaction Complete.
         \lor \land \forall t \in transaction[i].targets:
                  \land proposal[t][i].phase = Apply
                  \land proposal[t][i].status = Complete
             \land transaction' = [transaction \ EXCEPT \ ![i].status = Complete]
             \land UNCHANGED \langle proposal \rangle
          If any proposal has been Failed, mark the transaction Failed.
         \lor \land \exists t \in transaction[i].targets:
                  \land proposal[t][i].phase = Apply
                  \land proposal[t][i].status = Failed
             \land transaction' = [transaction \ EXCEPT \ ![i].status = Failed]
             \land UNCHANGED \langle proposal \rangle
    The Aborting state is used to clean up transactions that have failed during
    the Initializing or Validating phases.
   \lor \land transaction[i].phase = Abort
      \land transaction[i].status = Pending
          Move the transaction's proposals to the Aborting state
      \land \lor \land \exists t \in transaction[i].targets: proposal[t][i].phase \neq Abort
             \land proposal' = [t \in DOMAIN \ proposal \mapsto
                                IF t \in transaction[i].targets THEN
                                   [proposal[t] \ EXCEPT \ ![i].phase = Abort,
                                                             ![i].status = Pending
                                 ELSE
                                   proposal[t]]
             \land UNCHANGED \langle transaction \rangle
          If all proposals have been Complete, mark the transaction Complete.
         \lor \land \forall t \in transaction[i].targets:
                  \land proposal[t][i].phase = Abort
                  \land proposal[t][i].status = Complete
             \land transaction' = [transaction \ EXCEPT \ ![i].status = Complete]
             \land UNCHANGED \langle proposal \rangle
\land UNCHANGED \langle configuration, mastership, target <math>\rangle
```

```
Reconcile a proposal
ReconcileProposal(n, t, i) \stackrel{\Delta}{=}
   \land \lor \land proposal[t][i].phase = Initialize
         \land proposal[t][i].status = Pending
         \land proposal' = [proposal \ \texttt{EXCEPT} \ ![t] = [
               proposal[t] EXCEPT ![i] = [
                                        \mapsto Complete,
                   dependencyIndex \mapsto configuration[t].proposedIndex] @@ proposal[t][i]]]
         \land configuration' = [configuration \ EXCEPT \ ![t].proposedIndex = i]
         \land UNCHANGED \langle target \rangle
       While in the Validate phase, validate the proposed changes.
       If validation is successful, the proposal also records the changes
       required to roll back the proposal and the index to which to roll back.
      \lor \land proposal[t][i].phase = Validate
         \land proposal[t][i].status = Pending
         \land configuration[t].committedIndex = proposal[t][i].dependencyIndex
             For Change proposals validate the set of requested changes.
         \land \lor \land proposal[t][i].type = Change
                \land LET rollbackIndex \triangleq configuration[t].configIndex
                       rollbackValues \stackrel{\Delta}{=} [p \in DOMAIN \ proposal[t][i].values \mapsto
                                                IF p \in DOMAIN \ configuration[t].values \ THEN
                                                    configuration[t].values[p]
                                                 ELSE
                                                    [value \mapsto Nil,
                                                     delete \mapsto \text{TRUE}
                   Model validation successes and failures with Valid and Invalid results.
                      \exists r \in \{Valid, Invalid\}:
                           If the Change is Valid, record the changes required to roll
                           back the proposal and the index to which the rollback changes
                           will roll back the configuration.
                          \lor \land r = Valid
                             \land proposal' = [proposal \ EXCEPT \ ![t] = [
                                                 proposal[t] \text{ EXCEPT } ![i].rollbackIndex = rollbackIndex,
                                                                          ![i].rollbackValues = rollbackValues,
                                                                                                = Complete
                                                                          ![i].status
                          \lor \land r = Invalid
                             \land proposal' = [proposal \ EXCEPT \ ![t] = [
                                                 proposal[t] \text{ EXCEPT } ![i].status = Failed]]
             For Rollback proposals, validate the rollback changes which are
             proposal being rolled back.
             \lor \land proposal[t][i].type = Rollback
                   Rollbacks can only be performed on Change type proposals.
                \land \lor \land proposal[t][proposal[t][i].rollback].type = Change
                          Only roll back the change if it's the lastest change made
                          to the configuration based on the configuration index.
```

```
\land \lor \land configuration[t].configIndex = proposal[t][i].rollback
                     \land LET rollbackIndex \stackrel{\triangle}{=} proposal[t][proposal[t][i].rollback].rollbackIndex
                             rollbackValues \triangleq proposal[t][proposal[t][i].rollback].rollbackValues
                            \exists r \in \{Valid, Invalid\}:
                                If the Rollback is Valid, record the changes required to
                                roll back the target proposal and the index to which the
                                configuration is being rolled back.
                               \lor \land r = Valid
                                  \land proposal' = [proposal \ EXCEPT \ ![t] = [
                                        proposal[t] \text{ EXCEPT } ![i].rollbackIndex = rollbackIndex,
                                                                ![i].rollbackValues = rollbackValues,
                                                                                      = Complete
                                                                ![i].status
                               \lor \land r = Invalid
                                  \land proposal' = [proposal \ EXCEPT \ ![t] = [
                                                      proposal[t] \text{ EXCEPT } ![i].status = Failed]]
                  If the Rollback target is not the most recent change to the configuration,
                  fail validation for the proposal.
                  \lor \land configuration[t].configIndex \neq proposal[t][i].rollback
                     \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].status = Failed]]
            If a Rollback proposal is attempting to roll back another Rollback,
            fail validation for the proposal.
            \lor \land proposal[t][proposal[t][i].rollback].type = Rollback
              \land proposal' = [proposal \ EXCEPT \ ![t] = [
                    proposal[t] \text{ EXCEPT } ![i].status = Failed]]
  \land UNCHANGED \langle configuration, target \rangle
While in the Commit state, commit the proposed changes to the configuration.
\lor \land proposal[t][i].phase = Commit
  \land proposal[t][i].status = Pending
   Only commit the proposal if the prior proposal has already been committed.
  \land configuration[t].committedIndex = proposal[t][i].dependencyIndex
      If the proposal is a change, commit the change values and set the configuration
      index to the proposal index.
  \land \lor \land proposal[t][i].type = Change
        \land configuration' = [configuration \ EXCEPT \ ![t].values
                                                                                   = proposal[t][i].values,
                                                          ![t].configIndex
                                                          ![t].committedIndex = i]
      If the proposal is a rollback, commit the rollback values and index. This
      will cause the configuration index to be reverted to the index prior to
      the transaction/proposal being rolled back.
      \lor \land proposal[t][i].type = Rollback
        \land configuration' = [configuration \ EXCEPT \ ![t].values]
                                                                                   = proposal[t][i].rollbackValues,
                                                                                  = proposal[t][i].rollbackIndex,
                                                          ![t].configIndex
                                                          ![t].committedIndex = i]
  \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].status = Complete]]
  \land UNCHANGED \langle target \rangle
```

```
\lor \land proposal[t][i].phase = Apply
          \land proposal[t][i].status = Pending
          \land configuration[t].appliedIndex = proposal[t][i].dependencyIndex
          \land configuration[t].appliedTerm = mastership[t].term
          \land mastership[t].master = n
          Model successful and failed target update requests.
          \land \exists r \in \{Success, Failure\}:
               \vee \wedge r = Success
                     If the proposal is a change, apply the change values to the target
                      and update the configuration's applied index and values.
                  \land \lor \land proposal[t][i].type = Change
                        \land target' = [target \ EXCEPT \ ![t] = proposal[t][i].values @@ target[t]]
                        \land configuration' = [configuration \ EXCEPT]
                              ![t].appliedIndex = i,
                              [t].appliedValues = proposal[t][i].values @@ configuration[t].appliedValues]
                      If the proposal is a rollback, apply the rollback values and update the
                     configuration's applied values with the rolled back values.
                     \lor \land proposal[t][i].type = Rollback
                        \land target' = [target \ EXCEPT \ ![t] = proposal[t][i].rollbackValues @@ target[t]]
                        \land configuration' = [configuration \ EXCEPT]
                              ![t].appliedIndex = i,
                              ![t].appliedValues = proposal[t][i].rollbackValues @@ configuration[t].appliedValues]
                  \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].status = Complete]]
                If the proposal could not be applied, update the configuration's applied index
               and mark the proposal Failed.
               \lor \land r = Failure
                  \land configuration' = [configuration \ EXCEPT \ ![t].appliedIndex = i]
                  \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].status = Failed]]
                  \land UNCHANGED \langle target \rangle
       \lor \land proposal[t][i].phase = Abort
          \land proposal[t][i].status = Pending
          \land configuration' = [configuration \ EXCEPT \ ![t].committedIndex = i]
          \land proposal' = [proposal \ \texttt{EXCEPT} \ ![t] = [proposal[t] \ \texttt{EXCEPT} \ ![i].status = Complete]]
          \land UNCHANGED \langle target \rangle
   \land UNCHANGED \langle transaction, mastership \rangle
This section models the Configuration reconciler.
ReconcileConfiguration(n, t) \stackrel{\Delta}{=}
    \land \lor \land Target[t].persistent
          \land configuration[t].status \neq Complete
          \land \ configuration' = [configuration \ \ \texttt{EXCEPT} \ ![t].status = Complete]
```

While in the Apply phase, apply the proposed changes to the target.

 \land UNCHANGED $\langle target \rangle$

```
\lor \land \neg Target[t].persistent
          \land \lor mastership[t].term > configuration[t].configTerm
             \lor \land mastership[t].term = configuration[t].configTerm
                 \land mastership[t].master = Nil
          \land configuration' = [configuration \ EXCEPT \ ![t].configTerm = mastership[t].term,
                                                               ![t].status
                                                                                   = Pending
          \land UNCHANGED \langle target \rangle
       \lor \land configuration[t].status = Pending
          \land mastership[t].term = configuration[t].configTerm
          \land mastership[t].master = n
          \land target' = [target \ EXCEPT \ ![t] = configuration[t].appliedValues]
          \land configuration' = [configuration EXCEPT ![t].appliedTerm = mastership[t].term,
                                                               ![t].status
                                                                                    = Complete
    \land UNCHANGED \langle proposal, transaction, mastership <math>\rangle
Formal specification, constraints, and theorems.
Init \triangleq
    \land transaction = \langle \rangle
    \land proposal = [t \in DOMAIN \ Target \mapsto
                        [p \in \{\} \mapsto [phase
                                                     \mapsto Initialize,
                                      status
                                                     \mapsto Pending]]]
    \land configuration = [t \in DOMAIN \ Target \mapsto
                               [target \mapsto t,
                                status \mapsto Pending,
                                values \mapsto
                                   [path \in \{\}] \mapsto
                                        [path]
                                                 \mapsto path,
                                        value \mapsto Nil,
                                        index \mapsto 0,
                                         deleted \mapsto \text{FALSE}[],
                                configIndex
                                                    \mapsto 0,
                                configTerm
                                                    \mapsto 0.
                                proposedIndex \mapsto 0,
                                committedIndex \mapsto 0,
                                appliedIndex\\
                                                    \mapsto 0,
                                applied Term
                                                    \mapsto 0.
                                applied Values
                                   [path \in \{\}] \mapsto
                                        [path]
                                                  \mapsto path,
                                        value \mapsto Nil,
                                        index \mapsto 0,
                                         deleted \mapsto \text{FALSE}[]]
```

 $\land target = [t \in DOMAIN \ Target \mapsto$

```
[path \in \{\} \mapsto
                             [value \mapsto Nil]]
    \land mastership = [t \in DOMAIN \ Target \mapsto [master \mapsto Nil, \ term \mapsto 0]]
Next \triangleq
    \vee \exists c \in ValidChanges:
          RequestChange(c)
    \vee \exists t \in \text{DOMAIN } transaction :
          RequestRollback(t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN } Target:
            SetMaster(n, t)
      \vee \exists t \in \text{DOMAIN } Target :
          UnsetMaster(t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN} \ transaction:
              Reconcile Transaction(n, t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN } proposal :
            \exists i \in \text{DOMAIN } proposal[t]:
                 ReconcileProposal(n, t, i)
    \vee \exists n \in Node:
         \exists c \in \text{DOMAIN} \ configuration:
               ReconcileConfiguration(n, c)
Spec \stackrel{\Delta}{=} Init \wedge \Box [Next]_{vars}
Order \triangleq
    \land \ \forall i, j \in \text{DOMAIN} \ transaction:
           \forall j \leq i
           \lor Phase[transaction[i].phase] \ge Phase[transaction[j].phase]
           \lor transaction[i].targets \cap transaction[j].targets = \{\}
           \lor transaction[j].status \in \{Pending, Failed\}
    \land \forall t \in \text{DOMAIN } proposal :
          \forall i, j \in \text{DOMAIN } proposal[t]:
             \lor Phase[proposal[t][i].phase] \ge Phase[proposal[t][j].phase]
             \lor proposal[t][j].status \in \{Pending, Failed\}
Consistency \triangleq
    \forall t \in \text{DOMAIN } target :
      LET
             Compute the transaction indexes that have been applied to the target
           appliedIndexes \stackrel{\Delta}{=} \{i \in DOMAIN \ transaction : \}
                                         \land transaction[i].type = Change
                                         \land i \in \text{DOMAIN } proposal[t]
```

```
\land proposal[t][i].phase = Apply
                                     \land proposal[t][i].status = Complete
                                     \land t \in \text{DOMAIN} \ transaction[i].values
                                     \wedge \neg \exists j \in DOMAIN \ transaction :
                                            \wedge i > i
                                            \land transaction[j].type = Rollback
                                            \land transaction[j].rollback = i
                                            \land transaction[j].phase = Apply
                                            \land transaction[j].status = Complete
           Compute the set of paths in the target that have been updated by transactions
          appliedPaths
                              \stackrel{\triangle}{=} UNION {DOMAIN transaction[i].values[t]: i \in appliedIndexes}}
           Compute the highest index applied to the target for each path
                              \stackrel{\triangle}{=} [p \in appliedPaths \mapsto \text{CHOOSE } i \in appliedIndexes :
          pathIndexes
                                         \forall j \in appliedIndexes:
                                              \wedge i \geq j
                                               \land p \in \text{DOMAIN} \ transaction[i].values]
           Compute the expected target configuration based on the last indexes applied
           to the target for each path.
          expectedConfig \triangleq [p \in DOMAIN \ pathIndexes \mapsto transaction[pathIndexes[p]].values[p]]
     IN
          target[t] = expectedConfig
Isolation \triangleq
   \forall i, j \in \text{DOMAIN} \ transaction:
         \forall j \leq i
         \lor transaction[i].targets \cap transaction[j].targets = \{\}
         \vee transaction[i].isolation \neq Serializable
         \lor \land \lor \land transaction[i].phase \in \{Commit, Abort\}
                   \land transaction[i].status \in \{Complete, Failed\}
               \lor Phase[transaction[i].phase] > Phase[Commit]
               \lor Phase[transaction[j].phase] < Phase[Commit]
            \land \lor \land transaction[i].phase \in \{Apply, Abort\}
                   \land transaction[i].status \in \{Complete, Failed\}
               \lor Phase[transaction[j].phase] < Phase[Apply]
         \lor transaction[j].status = Failed
THEOREM Safety \stackrel{\triangle}{=} Spec \Rightarrow \Box(Order \land Consistency \land Isolation)
Completion \triangleq
    \land \forall i \in DOMAIN \ transaction :
         \land transaction[i].phase = Commit
         \land transaction[i].status \in \{Complete, Failed\}
    \land \forall i \in \text{DOMAIN} \ transaction :
         \land transaction[i].phase = Apply
         \land transaction[i].status \in \{Complete, Failed\}
    \land \forall t \in DOMAIN \ proposal :
```

```
\forall i \in \text{DOMAIN } proposal[t] : \\ \land proposal[t][i].phase = Commit \\ \land proposal[t][i].status \in \{Complete, Failed\} \\ \land \forall t \in \text{DOMAIN } proposal : \\ \forall i \in \text{DOMAIN } proposal[t] : \\ \land proposal[t][i].phase = Apply \\ \land proposal[t][i].status \in \{Complete, Failed\} \\ \text{THEOREM } Liveness \triangleq Spec \Rightarrow \lozenge Completion
```

```
Type assumptions.
```

```
Assume Nil \in \text{string}
```

Assume $\forall phase \in \text{domain } Phase : phase \in \text{string}$

Assume $\forall status \in domain Status : status \in string$

 $\begin{array}{l} \text{Assume} \ \land \textit{IsFiniteSet}(Node) \\ \ \, \land \forall \, n \in \textit{Node} : \\ \ \, \land \, n \notin \text{Domain} \, \, \textit{Target} \\ \ \, \land \, n \in \text{String} \end{array}$

Assume $\land \forall t \in \text{domain } Target :$

 $\setminus * \ {\it Modification History}$

* Last modified Mon Feb 07 02:45:30 PST 2022 by jordanhalterman

IsFiniteSet(Target[t].values[p])

\^* Created Wed Sep 22 13:22:32 PDT 2021 by jordanhalterman