
MODULE *Config*

EXTENDS

Northbound,
Proposals,
Configurations,
Mastership,
Southbound,
Target

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

LOCAL INSTANCE *TLC*

vars \triangleq $\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{target} \rangle$

Formal specification, constraints, and theorems.

Init \triangleq

\wedge *InitNorthbound*
 \wedge *InitProposal*
 \wedge *InitConfiguration*
 \wedge *InitMastership*
 \wedge *InitSouthbound*
 \wedge *InitTarget*

Next \triangleq

$\vee \wedge$ *NextNorthbound*
 \wedge UNCHANGED $\langle \text{configuration}, \text{mastership}, \text{conn}, \text{target} \rangle$
 $\vee \wedge$ *NextProposal*
 \wedge UNCHANGED $\langle \text{mastership}, \text{conn} \rangle$
 $\vee \wedge$ *NextConfiguration*
 \wedge UNCHANGED $\langle \text{proposal}, \text{conn} \rangle$
 $\vee \wedge$ *NextMastership*
 \wedge UNCHANGED $\langle \text{proposal}, \text{configuration}, \text{conn}, \text{target} \rangle$
 $\vee \wedge$ *NextSouthbound*
 \wedge UNCHANGED $\langle \text{proposal}, \text{configuration}, \text{mastership} \rangle$
 $\vee \wedge$ *NextTarget*
 \wedge UNCHANGED $\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{conn} \rangle$

Spec \triangleq *Init* \wedge $\Box[\text{Next}]_{\text{vars}} \wedge \text{WF}_{\text{vars}}(\text{Next})$

Order \triangleq

$$\begin{aligned}
& \forall t \in \text{DOMAIN } \textit{proposal} : \\
& \quad \forall i \in \text{DOMAIN } \textit{proposal}[t] : \\
& \quad \quad \wedge \wedge \textit{proposal}[t][i].\textit{phase} = \textit{ProposalCommit} \\
& \quad \quad \wedge \textit{proposal}[t][i].\textit{state} = \textit{ProposalInProgress} \\
& \quad \quad \Rightarrow \neg \exists j \in \text{DOMAIN } \textit{proposal}[t] : \\
& \quad \quad \quad \wedge j > i \\
& \quad \quad \quad \wedge \textit{proposal}[t][j].\textit{phase} = \textit{ProposalCommit} \\
& \quad \quad \quad \wedge \textit{proposal}[t][j].\textit{state} = \textit{ProposalComplete} \\
& \quad \wedge \wedge \textit{proposal}[t][i].\textit{phase} = \textit{ProposalApply} \\
& \quad \quad \wedge \textit{proposal}[t][i].\textit{state} = \textit{ProposalInProgress} \\
& \quad \quad \Rightarrow \neg \exists j \in \text{DOMAIN } \textit{proposal}[t] : \\
& \quad \quad \quad \wedge j > i \\
& \quad \quad \quad \wedge \textit{proposal}[t][j].\textit{phase} = \textit{ProposalApply} \\
& \quad \quad \quad \wedge \textit{proposal}[t][j].\textit{state} = \textit{ProposalComplete}
\end{aligned}$$

Consistency \triangleq

$$\forall t \in \text{DOMAIN } \textit{proposal} :$$

LET

Compute the transaction indexes that have been applied to the target

$$\begin{aligned}
\textit{targetIndexes} & \triangleq \{i \in \text{DOMAIN } \textit{proposal}[t] : \\
& \quad \wedge \textit{proposal}[t][i].\textit{phase} = \textit{ProposalApply} \\
& \quad \wedge \textit{proposal}[t][i].\textit{state} = \textit{ProposalComplete} \\
& \quad \wedge \neg \exists j \in \text{DOMAIN } \textit{proposal}[t] : \\
& \quad \quad \wedge j > i \\
& \quad \quad \wedge \textit{proposal}[t][j].\textit{type} = \textit{ProposalRollback} \\
& \quad \quad \wedge \textit{proposal}[t][j].\textit{rollback.index} = i \\
& \quad \quad \wedge \textit{proposal}[t][j].\textit{phase} = \textit{ProposalApply} \\
& \quad \quad \wedge \textit{proposal}[t][j].\textit{state} = \textit{ProposalComplete}\}
\end{aligned}$$

Compute the set of paths in the target that have been updated by transactions

$$\textit{appliedPaths} \triangleq \text{UNION } \{\text{DOMAIN } \textit{proposal}[t][i].\textit{change.values} : i \in \textit{targetIndexes}\}$$

Compute the highest index applied to the target for each path

$$\begin{aligned}
\textit{pathIndexes} & \triangleq [p \in \textit{appliedPaths} \mapsto \text{CHOOSE } i \in \textit{targetIndexes} : \\
& \quad \forall j \in \textit{targetIndexes} : \\
& \quad \quad \wedge i \geq j \\
& \quad \quad \wedge p \in \text{DOMAIN } \textit{proposal}[t][i].\textit{change.values}]
\end{aligned}$$

Compute the expected target configuration based on the last indexes applied to the target for each path.

$$\textit{expectedConfig} \triangleq [p \in \text{DOMAIN } \textit{pathIndexes} \mapsto \textit{proposal}[t][\textit{pathIndexes}[p]].\textit{change.values}[p]]$$

IN

$$\textit{target}[t] = \textit{expectedConfig}$$

$$\textit{Safety} \triangleq \Box(\textit{Order} \wedge \textit{Consistency})$$

THEOREM $\textit{Spec} \Rightarrow \textit{Safety}$

$$\textit{Terminated}(t, i) \triangleq$$

$$\begin{aligned}
& \wedge i \in \text{DOMAIN } \textit{proposal}[t] \\
& \wedge \textit{proposal}[t][i].\textit{phase} \in \{\textit{ProposalApply}, \textit{ProposalAbort}\} \\
& \wedge \textit{proposal}[t][i].\textit{state} = \textit{ProposalComplete}
\end{aligned}$$

$$\begin{aligned}
\textit{Termination} & \triangleq \\
& \forall t \in \text{DOMAIN } \textit{proposal} : \\
& \quad \forall i \in 1 \dots \textit{Len}(\textit{proposal}[t]) : \\
& \quad \quad \textit{Terminated}(t, i)
\end{aligned}$$

$$\textit{Liveness} \triangleq \Diamond \textit{Termination}$$

THEOREM $\textit{Spec} \Rightarrow \textit{Liveness}$

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