```
— MODULE Config
INSTANCE Naturals
INSTANCE FiniteSets
Instance Sequences
INSTANCE TLC
 An empty constant
Constant Nil
 Transaction type constants
CONSTANTS
   Change,
   Rollback
 Transaction isolation constants
CONSTANTS
   Read Committed,\\
   Serializable \\
 Phase constants
CONSTANTS
   Initialize,
   Validate,
   Abort,
   Commit,
   Apply
Phase \triangleq
   \{Initialize,
    Validate,
    Abort,
    Commit,
    Apply
 Status constants
CONSTANTS
   InProgress,
   Complete,
   Failed
State \triangleq
   \{InProgress,
    Complete,
```

```
Failed }
 State constants
CONSTANTS
   Pending,
    Validated,
    Committed,
   Applied,
   Aborted
Status \triangleq
   \{Pending,
     Validated,
     Committed,
     Applied,
     Aborted
CONSTANTS
    Valid,
   Invalid
CONSTANTS
   Success,
   Failure
 The set of all nodes
CONSTANT Node
Target is the set of all targets and their possible paths and values.
Example:
  Target \stackrel{\triangle}{=}
    [target1 \mapsto
      [persistent \mapsto FALSE, values \mapsto [
        path1 \mapsto \{"value1", "value2"\},\
        path2 \mapsto \{\,"value2",\,\,"value3"\,\}]],
    target2 \mapsto
      [persistent \mapsto TRUE, values \mapsto [
        path2 \mapsto \{"value3", "value4"\},
        path3 \mapsto \{"value4", "value5"\}]]]
```

Configuration update/rollback requests are tracked and processed through two data types. Transactions represent the lifecycle of a single configuration change request and are stored in an appendonly log. Configurations represent the desired configuration of a gNMI target based on the aggregate of relevant changes in the Transaction log.

```
TYPE Type ::= type \in
```

CONSTANT Target

```
\{Change,
   Rollback\}
\mathbf{TYPE}\ \mathit{Phase} ::= \mathit{phase} \in
  {Initialize,}
   Validate,
   Abort,
   Commit,
   Apply
\mathbf{TYPE}\ \mathit{State} ::= \mathit{state} \in
  \{InProgress,
   Complete,
   Failed\}
\mathbf{TYPE}\ \mathit{Status} ::= \mathit{status} \in
  \{Pending,
   Validated,
   Committed,\\
   Applied,
   Aborted
\mathbf{TYPE}\ \mathit{Isolation} ::= \mathit{isolation} \in
  \{ReadCommitted,
   Serializable
TYPE Transaction \stackrel{\Delta}{=}
           := type \in Type,
  [type
   isolation ::= isolation \in \mathit{Isolation}
   change ::=
     [target \in SUBSET (DOMAIN Target) \mapsto
       [path \in SUBSET (DOMAIN Target[target].values) \mapsto
          [value ::= value \in STRING,
          delete ::= delete \in BOOLEAN ]]],
   rollback ::= index \in Nat,
   targets := targets \in SUBSET (DOMAIN Target)
   phase \quad ::= phase \in Phase,
   state ::= state \in State,
   status ::= status \in Status]
TYPE Proposal \stackrel{\triangle}{=}
  [type ::= type \in Type,
   change \quad ::= \quad
     [index ::= index \in Nat,
     values ::=
       [path \in \texttt{SUBSET} \ (\texttt{DOMAIN} \ Target[target].values) \ \mapsto
          [value ::= value \in STRING,
          delete ::= delete \in BOOLEAN ]]],
   rollback ::=
     [index ::= index \in Nat,
     values ::=
       [path \in SUBSET (DOMAIN Target[target].values) \mapsto
          [value ::= value \in STRING,
```

```
delete ::= delete \in BOOLEAN ]]],
     dependency ::= [index \in Nat],
    phase
               ::= phase \in Phase,
    state
              ::= state \in State]
  TYPE Configuration \stackrel{\Delta}{=}
    [config ::=
      [index ::= index \in Nat,
       term ::= term \in Nat,
       values ::=
        [path \in SUBSET (DOMAIN Target[target]) \mapsto
          [value ::= value \in STRING,
           index ::= index \in Nat,
           deleted ::= delete \in BOOLEAN ]]],
     proposal ::= [index ::= index \in Nat],
     commit ::= [index ::= index \in Nat],
     target ::=
      [index ::= index \in Nat,
      term ::= term \in Nat,
       values ::=
        [path \in SUBSET (DOMAIN Target[target]) \mapsto
          [value ::= value \in STRING,
           index ::= index \in Nat,
           deleted ::= delete \in BOOLEAN ]]],
     state ::= state \in State]
 A transaction log. Transactions may either request a set
 of changes to a set of targets or rollback a prior change.
VARIABLE transaction
 A record of per-target proposals
VARIABLE proposal
 A record of per-target configurations
VARIABLE configuration
 A record of target states
VARIABLE target
 A record of target masterships
{\tt VARIABLE}\ mastership
```

This section models *mastership* for the configuration service.

 $vars \triangleq \langle transaction, proposal, configuration, mastership, target \rangle$

Mastership is used primarily to track the lifecycle of individual configuration targets and react to state changes on the southbound. Each target is assigned a master from the Node set, and masters can be unset when the target disconnects.

Set node n as the master for target t

```
SetMaster(n, t) \triangleq
    \land mastership[t].master \neq n
    \land mastership' = [mastership EXCEPT ![t].term = mastership[t].term + 1,
                                                     ![t].master = n
    \land UNCHANGED \langle transaction, proposal, configuration, target <math>\rangle
UnsetMaster(t) \triangleq
    \land mastership[t].master \neq Nil
    \land mastership' = [mastership \ EXCEPT \ ![t].master = Nil]
    \land UNCHANGED \langle transaction, proposal, configuration, target <math>\rangle
This section models configuration changes and rollbacks. Changes are appended to the transaction
log and processed asynchronously.
Value(s, t, p) \triangleq
   LET value \stackrel{\Delta}{=} CHOOSE v \in s : v.target = t \land v.path = p
   IN
       [value \mapsto value.value,
        delete \mapsto value.delete
Paths(s, t) \triangleq
   [p \in \{v.path : v \in \{v \in s : v.target = t\}\} \mapsto Value(s, t, p)]
Changes(s) \triangleq
   [t \in \{v.target : v \in s\} \mapsto Paths(s, t)]
ValidValues(t, p) \triangleq
   UNION \{\{[value \mapsto v, delete \mapsto FALSE] : v \in Target[t], values[p]\}, \{[value \mapsto Nil, delete \mapsto TRUE]\}\}
    \text{UNION } \left\{ \left\{ v @@ \left[ path \mapsto p \right] : v \in \mathit{ValidValues}(t, \, p) \right\} : p \in \mathsf{DOMAIN} \ \mathit{Target}[t]. values \right\} 
ValidTargets \triangleq
   UNION \{\{p@@[target \mapsto t] : p \in ValidPaths(t)\} : t \in DOMAIN Target\}
 The set of all valid sets of changes to all targets and their paths.
 The set of possible changes is computed from the Target model value.
ValidChanges \triangleq
   Let changeSets \triangleq \{s \in Subset \ ValidTargets : \}
                                  \forall t \in \text{DOMAIN } Target :
                                    \forall p \in \text{DOMAIN } Target[t].values:
                                      Cardinality(\{v \in s : v.target = t \land v.path = p\}) \le 1\}
   IN
       \{Changes(s): s \in changeSets\}
```

The next available index in the transaction log.

This is computed as the max of the existing indexes in the log to

```
allow for changes to the \log (e.g. \log \text{ compaction}) to be modeled.
NextIndex \triangleq
   IF DOMAIN transaction = \{\} THEN
      1
    ELSE
      LET i \stackrel{\Delta}{=} CHOOSE i \in DOMAIN \ transaction:
            \forall j \in \text{DOMAIN } transaction : i \geq j
      in i+1
 Add a set of changes 'c' to the transaction log
RequestChange(c) \triangleq
   \land \exists isolation \in \{ReadCommitted, Serializable\}:
         \land transaction' = transaction @@ (NextIndex:> [type])
                                                                                 \mapsto Change,
                                                                     isolation \mapsto isolation,
                                                                     change
                                                                                \mapsto c,
                                                                     targets
                                                                                \mapsto {},
                                                                                 \mapsto Initialize,
                                                                     phase
                                                                                 \mapsto InProgress,
                                                                     state
                                                                     status
                                                                                 \mapsto Pending)
   \land UNCHANGED \langle proposal, configuration, mastership, target <math>\rangle
 Add a rollback of transaction 't' to the transaction log
RequestRollback(i) \stackrel{\Delta}{=}
   \land \exists isolation \in \{ReadCommitted, Serializable\}:
         \land transaction' = transaction @@ (NextIndex:> [type])
                                                                                 \mapsto Rollback,
                                                                     isolation \mapsto isolation,
                                                                     rollback \mapsto i,
                                                                     targets
                                                                                \mapsto {},
                                                                     phase
                                                                                 \mapsto Initialize,
                                                                                 \mapsto InProgress,
                                                                     state
                                                                                 \mapsto Pending
   ∧ UNCHANGED ⟨proposal, configuration, mastership, target⟩
```

This section models the Transaction log reconciler.

Transactions come in two flavors: - Change transactions contain a set of changes to be applied to a set of targets - Rollback transactions reference a prior change transaction to be reverted to the previous state

Transacations proceed through a series of phases:

- * Initialize create and link Proposals
- * Validate validate changes and rollbacks
- * Commit commit changes to Configurations
- * Apply commit changes to Targets

Reconcile a transaction

 $ReconcileTransaction(n, i) \stackrel{\Delta}{=}$

```
While in the Initializing phase, the reconciler checks whether the
    prior transaction has been Initialized before creating Proposals in
    the Initialize phase. Once all of the transaction's proposals have
    been Initialized, the transaction will be marked Initialized. If any
    proposal is Failed, the transaction will be marked Failed as well.
\land \lor \land transaction[i].phase = Initialize
      \land \lor \land transaction[i].state = InProgress
             All prior transaction must be initialized before proceeding
             to initialize this transaction.
             \land \neg \exists j \in DOMAIN \ transaction :
                   \wedge j < i
                   \land transaction[j].phase = Initialize
                    \land transaction[j].state = InProgress
                If the transaction's targets are not yet set, create proposals
                 and add targets to the transaction state.
             \land \lor \land transaction[i].targets = \{\}
                      If the transaction is a change, the targets are taken
                      from the change values.
                   \land \lor \land transaction[i].type = Change
                         \land transaction' = [transaction \ EXCEPT \ ![i].targets = DOMAIN \ transaction[i].change]
                         \land proposal' = [t \in DOMAIN \ proposal \mapsto
                               IF t \in \text{DOMAIN } transaction[i].change \text{ THEN}
                                  proposal[t]@@(i:>[type]
                                                                         \mapsto Change,
                                                           change
                                                                         \mapsto
                                                              [index \mapsto i,
                                                              values \mapsto transaction[i].change[t]],
                                                           rollback \mapsto
                                                             [index \mapsto 0,
                                                              values \mapsto Nil,
                                                           dependency \mapsto [index \mapsto 0],
                                                           phase
                                                                          \mapsto Initialize.
                                                                          \mapsto InProgress)
                                                           state
                                ELSE
                                  proposal[t]]
                      If the transaction is a rollback, the targets affected are
                      the targets of the change transaction being rolled back.
                      \lor \land transaction[i].type = Rollback
                             If the rollback index is a valid Change transaction,
                             initialize proposals for all of the Change targets.
                         \land \lor \land transaction[i].rollback \in domain transaction
                               \land transaction[transaction[i].rollback].type = Change
                               \land transaction' = [transaction \ EXCEPT \ ![i].targets =
                                                       DOMAIN transaction[transaction[i].rollback].change]
                               \land proposal' = [t \in DOMAIN \ proposal \mapsto
```

Initialize is the only transaction phase that's globally serialized.

```
proposal[t]@@(i:>[type]
                                                                   \mapsto Rollback,
                                                       change \mapsto
                                                         [index \mapsto 0,
                                                          values \mapsto Nil,
                                                       rollback \mapsto
                                                         [index \mapsto transaction[i].rollback,
                                                          values \mapsto Nil,
                                                       dependency \mapsto [index \mapsto 0],
                                                       phase
                                                                      \mapsto Initialize,
                                                                      \mapsto InProgress)
                                                       state
                            ELSE
                              proposal[t]]
                  If the rollback index is not a valid Change transaction
                  fail the Rollback transaction.
                  \lor \land \lor \land transaction[i].rollback \in DOMAIN transaction
                           \land transaction[transaction[i].rollback].type = Rollback
                        \lor transaction[i].rollback \notin DOMAIN transaction
                     \land transaction' = [transaction \ EXCEPT \ ![i].state = Failed]
                     \land UNCHANGED \langle proposal \rangle
      If the transaction's proposals have been initialized, check proposals
      for completion or failures.
      \lor \land transaction[i].targets \neq \{\}
             If all proposals have been Complete, mark the transaction Complete.
         \land \lor \land \forall t \in transaction[i].targets:
                    \land proposal[t][i].phase = Initialize
                    \land proposal[t][i].state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].state = Complete]
               \land UNCHANGED \langle proposal \rangle
            If any proposal has been Failed, mark the transaction Failed.
            \lor \land \exists t \in transaction[i].targets:
                    \land proposal[t][i].phase = Initialize
                    \land \ proposal[t][i].state = Failed
               \land transaction' = [transaction \ EXCEPT \ ![i].state = Failed]
               \land UNCHANGED \langle proposal \rangle
Once the transaction has been Initialized, proceed to the Validate phase.
If any of the transaction's proposals depend on a Serializable transaction,
verify the dependency has been Validated to preserve serializability before
moving the transaction to the Validate phase.
\lor \land transaction[i].state = Complete
  \land \forall t \in transaction[i].targets:
        \land proposal[t][i].dependency.index \in DOMAIN transaction
       \land transaction[proposal[t][i].dependency.index].isolation = Serializable
        \Rightarrow transaction[proposal[t][i].dependency.index].status \in \{Validated, Committed, Applied, A
  \land transaction' = [transaction \ EXCEPT \ ![i].phase = Validate,
```

IF $t \in \text{DOMAIN} \ transaction[transaction[i].rollback].change \ \text{THEN}$

```
![i].state = InProgress]
         \land UNCHANGED \langle proposal \rangle
       If the transaction failed initialization, proceed to the Abort phase
       to ensure indexes are still updated for the target configurations.
      \lor \land transaction[i].state = Failed
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Abort,
                                                        ![i].state = InProgress]
         \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].phase = Validate
   \land \lor \land transaction[i].state = InProgress
             Move the transaction's proposals to the Validating state
         \land \lor \land \exists t \in transaction[i].targets:
                    \land proposal[t][i].phase \neq Validate
                    \land proposal' = [proposal \ EXCEPT \ ![t] =
                                        [proposal[t] \text{ EXCEPT } ![i].phase = Validate,
                                                                 ![i].state = InProgress]]
               \land UNCHANGED \langle transaction \rangle
            If all proposals have been Complete, mark the transaction Complete.
            \lor \land \forall t \in transaction[i].targets:
                    \land proposal[t][i].phase = Validate
                    \land proposal[t][i].state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].state = Complete,
                                                              ![i].status = Validated]
               \land UNCHANGED \langle proposal \rangle
             If any proposal has been Failed, mark the transaction Failed.
            \vee \wedge \exists t \in transaction[i].targets:
                    \land proposal[t][i].phase = Validate
                    \land proposal[t][i].state = Failed
               \land transaction' = [transaction \ EXCEPT \ ![i].state = Failed]
               \land UNCHANGED \langle proposal \rangle
       Once the transaction has been Validated, proceed to the Commit phase.
       If any of the transaction's proposals depend on a Serializable transaction,
       verify the dependency has been Committed to preserve serializability before
       moving the transaction to the Commit phase.
      \lor \land transaction[i].state = Complete
         \land \forall t \in transaction[i].targets:
              \land proposal[t][i].dependency.index \in DOMAIN transaction
              \land transaction[proposal[t][i].dependency.index].isolation = Serializable
              \Rightarrow transaction[proposal[t][i].dependency.index].status \in \{Committed, Applied, Aborted\}
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Commit,
                                                        ![i].state = InProgress]
         \land UNCHANGED \langle proposal \rangle
       If the transaction failed validation, proceed to the Abort phase
       to ensure indexes are still updated for the target configurations.
      \lor \land transaction[i].state = Failed
```

```
\land transaction' = [transaction \ EXCEPT \ ![i].phase = Abort,
                                                       ![i].state = InProgress]
         ∧ UNCHANGED ⟨proposal⟩
\lor \land transaction[i].phase = Commit
   \land \lor \land transaction[i].state = InProgress
             Move the transaction's proposals to the Committing state
         \land \lor \land \exists t \in transaction[i].targets:
                    \land proposal[t][i].phase \neq Commit
                    \land proposal' = [proposal \ EXCEPT \ ![t] =
                                       [proposal[t] \text{ EXCEPT } ![i].phase = Commit,
                                                                ![i].state = InProgress]]
               \land UNCHANGED \langle transaction \rangle
            If all proposals have been Complete, mark the transaction Complete.
            \lor \land \forall t \in transaction[i].targets:
                    \land proposal[t][i].phase = Commit
                    \land proposal[t][i].state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].state = Complete,
                                                             ![i].status = Committed]
               \land UNCHANGED \langle proposal \rangle
      Once the transaction has been Committed, proceed to the Apply phase.
      If any of the transaction's proposals depend on a Serializable transaction,
      verify the dependency has been Applied to preserve serializability before
      moving the transaction to the Apply phase.
      \lor \land transaction[i].state = Complete
         \land \forall t \in transaction[i].targets:
              \land proposal[t][i].dependency.index \in DOMAIN transaction
              \land transaction[proposal[t][i].dependency.index].isolation = Serializable
              \Rightarrow transaction[proposal[t][i].dependency.index].status \in \{Applied, Aborted\}
         \land transaction' = [transaction \ EXCEPT \ ![i].phase = Apply,
                                                       ![i].state = InProgress]
         \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].phase = Apply
   \land transaction[i].state = InProgress
      Move the transaction's proposals to the Applying state
   \land \lor \land \exists t \in transaction[i].targets:
              \land proposal[t][i].phase \neq Apply
              \land proposal' = [proposal \ EXCEPT \ ![t] =
                                 [proposal[t] \text{ EXCEPT } ![i].phase = Apply,
                                                          ![i].state = InProgress]]
         \land UNCHANGED \langle transaction \rangle
      If all proposals have been Complete, mark the transaction Complete.
      \lor \land \forall t \in transaction[i].targets:
              \land proposal[t][i].phase = Apply
              \land proposal[t][i].state = Complete
         \land transaction' = [transaction \ EXCEPT \ ![i].state = Complete,
```

```
![i].status = Applied]
                \land UNCHANGED \langle proposal \rangle
              If any proposal has been Failed, mark the transaction Failed.
             \lor \land \exists t \in transaction[i].targets:
                     \land proposal[t][i].phase = Apply
                     \land proposal[t][i].state = Failed
                \land transaction' = [transaction \ EXCEPT \ ![i].state = Failed]
                \land UNCHANGED \langle proposal \rangle
        The Aborting state is used to clean up transactions that have failed during
        the Initializing or Validating phases.
       \lor \land transaction[i].phase = Abort
          \land transaction[i].state = InProgress
              Move the transaction's proposals to the Aborting state
          \land \lor \land \exists t \in transaction[i].targets:
                     \land proposal[t][i].phase \neq Abort
                     \land proposal' = [proposal \ EXCEPT \ ![t] =
                                         [proposal[t] \text{ EXCEPT } ![i].phase = Abort,
                                                                   ![i].state = InProgress]]
                \land UNCHANGED \langle transaction \rangle
              If all proposals have been Complete, mark the transaction Complete.
             \lor \land \forall t \in transaction[i].targets:
                     \land proposal[t][i].phase = Abort
                      \land proposal[t][i].state = Complete
                \land transaction' = [transaction \ EXCEPT \ ![i].state = Complete,
                                                               ![i].status = Aborted]
                \land UNCHANGED \langle proposal \rangle
   \land UNCHANGED \langle configuration, mastership, target <math>\rangle
Reconcile a proposal
ReconcileProposal(n, t, i) \stackrel{\Delta}{=}
   \land \lor \land proposal[t][i].phase = Initialize
         \land \ proposal[t][i].state \ = InProgress
         \land proposal' = [proposal \ EXCEPT \ ![t] =
                [proposal[t] \text{ EXCEPT } ![i].state = Complete,
                                         ![i].dependency.index = configuration[t].proposal.index]]
         \land configuration' = [configuration \ EXCEPT \ ![t].proposal.index = i]
         \land UNCHANGED \langle target \rangle
       While in the Validate phase, validate the proposed changes.
       If validation is successful, the proposal also records the changes
       required to roll back the proposal and the index to which to roll back.
      \lor \land proposal[t][i].phase = Validate
         \land proposal[t][i].state = InProgress
         \land configuration[t].commit.index = proposal[t][i].dependency.index
             For Change proposals validate the set of requested changes.
         \land \lor \land proposal[t][i].type = Change
```

```
\land LET rollbackIndex \triangleq configuration[t].config.index
           rollbackValues \stackrel{\Delta}{=} [p \in \text{domain } proposal[t][i].change.values \mapsto
                                   IF p \in DOMAIN \ configuration[t].config.values \ THEN
                                       configuration[t].config.values[p]
                                      [value \mapsto Nil,
                                       delete \mapsto TRUE
      Model validation successes and failures with Valid and Invalid results.
         \exists r \in \{Valid, Invalid\}:
              If the Change is Valid, record the changes required to roll
              back the proposal and the index to which the rollback changes
              will roll back the configuration.
             \lor \land r = Valid
                \land proposal' = [proposal \ EXCEPT \ ![t] =
                                    [proposal[t] \ EXCEPT \ ![i].rollback.index = rollbackIndex,
                                                             ![i].rollback.values = rollbackValues,
                                                                            = Complete
             \lor \land r = Invalid
                \land proposal' = [proposal \ EXCEPT \ ![t] =
                                    [proposal[t] \text{ EXCEPT } ![i].state = Failed]]
For Rollback proposals, validate the rollback changes which are
proposal being rolled back.
\lor \land proposal[t][i].type = Rollback
      Rollbacks can only be performed on Change type proposals.
  \land \lor \land proposal[t][proposal[t][i].rollback.index].type = Change
            Only roll back the change if it's the lastest change made
            to the configuration based on the configuration index.
        \land \lor \land configuration[t].config.index = proposal[t][i].rollback.index
               \land LET changeIndex
                                           \stackrel{\Delta}{=} proposal[t][proposal[t][i].rollback.index].rollback.index
                                          \overset{\Delta}{=} \ proposal[t][proposal[t][i].rollback.index].rollback.values
                       change Values
                       rollbackValues \stackrel{\triangle}{=} proposal[t][proposal[t][i].rollback.index].change.values
                 IN \exists r \in \{Valid, Invalid\}:
                          If the Rollback is Valid, record the changes required to
                          roll back the target proposal and the index to which the
                          configuration is being rolled back.
                         \lor \land r = Valid
                            \land proposal' = [proposal \ EXCEPT \ ![t] =
                                  [proposal[t]] EXCEPT ![i].change.index
                                                                                    = changeIndex,
                                                           ![i].change.values
                                                                                    = change Values.
                                                           ![i].rollback.values = rollbackValues,
                                                           ![i].state
                                                                                    = Complete
                         \lor \land r = Invalid
                            \land proposal' = [proposal \ EXCEPT \ ![t] =
                                                [proposal[t] \text{ EXCEPT } ![i].state = Failed]]
```

If the Rollback target is not the most recent change to the configuration,

```
fail validation for the proposal.
                 \lor \land configuration[t].config.index \neq proposal[t][i].rollback.index
                    \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Failed]]
            If a Rollback proposal is attempting to roll back another Rollback,
            fail validation for the proposal.
            \lor \land proposal[t][proposal[t][i].rollback.index].type = Rollback
              \land proposal' = [proposal \ EXCEPT \ ![t] =
                    [proposal[t] \text{ EXCEPT } ![i].state = Failed]]
  \land UNCHANGED \langle configuration, target \rangle
While in the Commit state, commit the proposed changes to the configuration.
\lor \land proposal[t][i].phase = Commit
   \land proposal[t][i].state = InProgress
   Only commit the proposal if the prior proposal has already been committed.
  \land configuration[t].commit.index = proposal[t][i].dependency.index
  \land configuration' = [configuration \ EXCEPT \ ![t].config.values = proposal[t][i].change.values,
                                                         ![t].config.index = proposal[t][i].change.index,
                                                         ![t].commit.index = i]
  \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Complete]]
  \land UNCHANGED \langle target \rangle
While in the Apply phase, apply the proposed changes to the target.
\lor \land proposal[t][i].phase = Apply
  \land proposal[t][i].state = InProgress
  \land configuration[t].target.index = proposal[t][i].dependency.index
  \land configuration[t].target.term = mastership[t].term
  \land mastership[t].master = n
   Model successful and failed target update requests.
  \land \exists r \in \{Success, Failure\}:
       \vee \wedge r = Success
          \land target' = [target \ EXCEPT \ ![t] = proposal[t][i].change.values @@ target[t]]
          \land configuration' = [configuration \ EXCEPT]
                                    ![t].target.index = i,
                                    ![t].target.values = proposal[t][i].change.values
                                        @@ configuration[t].target.values]
          \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Complete]]
        If the proposal could not be applied, update the configuration's applied index
        and mark the proposal Failed.
       \lor \land r = Failure
          \land configuration' = [configuration \ EXCEPT \ ![t].target.index = i]
          \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Failed]]
          \land UNCHANGED \langle target \rangle
\lor \land proposal[t][i].phase = Abort
  \land proposal[t][i].state = InProgress
      The commit.index will always be greater than or equal to the target.index.
      If only the commit.index matches the proposal's dependency.index, update
```

the *commit.index* to enable commits of later proposals, but do not

```
mark the Abort phase Complete until the target.index has been incremented.
         \land \lor \land configuration[t].commit.index = proposal[t][i].dependency.index
               \land configuration' = [configuration \ EXCEPT \ ![t].commit.index = i]
               \land UNCHANGED \langle proposal \rangle
             If the configuration's target.index matches the proposal's dependency.index,
             update the target.index and mark the proposal Complete for the Abort phase.
             \lor \land configuration[t].commit.index \ge i
               \land configuration[t].target.index = proposal[t][i].dependency.index
               \land configuration' = [configuration \ EXCEPT \ ![t].target.index = i]
               \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Complete]]
             If both the configuration's commit.index and target.index match the
             proposal's dependency.index, update the commit.index and target.index
             and mark the proposal Complete for the Abort phase.
             \lor \land configuration[t].commit.index = proposal[t][i].dependency.index
               \land configuration[t].target.index = proposal[t][i].dependency.index
               \land configuration' = [configuration \ EXCEPT \ ![t].commit.index = i,
                                                                 ![t].target.index = i]
               \land proposal' = [proposal \ EXCEPT \ ![t] = [proposal[t] \ EXCEPT \ ![i].state = Complete]]
         \land UNCHANGED \langle target \rangle
   \land UNCHANGED \langle transaction, mastership \rangle
This section models the Configuration reconciler.
ReconcileConfiguration(n, t) \stackrel{\Delta}{=}
   \land \lor \land Target[t].persistent
         \land configuration[t].state \neq Complete
         \land configuration' = [configuration \ EXCEPT \ ![t].state = Complete]
         \land UNCHANGED \langle target \rangle
       \vee \wedge \neg Target[t].persistent
         \land \lor mastership[t].term > configuration[t].config.term
            \vee \wedge mastership[t].term = configuration[t].config.term
               \land mastership[t].master = Nil
         \land configuration' = [configuration EXCEPT ![t].config.term = mastership[t].term,
                                                           ![t].state
                                                                             = InProgress
         \land UNCHANGED \langle target \rangle
       \lor \land configuration[t].state = InProgress
         \land mastership[t].term = configuration[t].config.term
         \land mastership[t].master = n
         \land target' = [target \ EXCEPT \ ![t] = configuration[t].target.values]
         \land configuration' = [configuration EXCEPT ![t].target.term = mastership[t].term,
                                                           ![t].state
                                                                             = Complete
   \land UNCHANGED \langle proposal, transaction, mastership <math>\rangle
```

Formal specification, constraints, and theorems.

```
Init \triangleq
    \land transaction = [i \in \{\} \mapsto
                              [type \mapsto Change,
                              phase \mapsto Initialize,
                              state \mapsto InProgress,
                              status \mapsto Pending
    \land proposal = [t \in \text{DOMAIN } Target \mapsto
                         [i \in \{\}] \mapsto
                            [phase \mapsto Initialize,
                            state \mapsto InProgress]]]
    \land configuration = [t \in DOMAIN \ Target \mapsto
                                [state \mapsto InProgress,
                                 config \mapsto
                                    [index \mapsto 0,
                                     term \mapsto 0,
                                     values \mapsto
                                         [path \in \{\} \mapsto
                                            [path
                                                        \mapsto path,
                                             value \mapsto Nil,
                                             index \quad \mapsto 0,
                                             deleted \mapsto \text{FALSE}]]],
                                 proposal \mapsto [index \mapsto 0],
                                 commit \mapsto [index \mapsto 0],
                                 target
                                               \mapsto
                                    [index \mapsto 0,
                                     term \mapsto 0,
                                     values \; \mapsto \;
                                       [path \in \{\} \mapsto
                                           [path]
                                                      \mapsto path,
                                            value \mapsto Nil,
                                            index \mapsto 0,
                                            deleted \mapsto \text{False}[]]]]
    \land target = [t \in DOMAIN \ Target \mapsto
                      [path \in \{\} \mapsto
                         [value \mapsto Nil]]
    \land mastership = [t \in DOMAIN \ Target \mapsto [master \mapsto Nil, term \mapsto 0]]
Next \triangleq
    \vee \exists c \in ValidChanges:
          RequestChange(c)
    \vee \exists t \in \text{DOMAIN} \ transaction:
          RequestRollback(t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN } Target :
```

```
SetMaster(n, t)
     \lor \exists t \in \text{domain } Target :
         UnsetMaster(t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN} \ transaction:
              Reconcile Transaction(n, t)
    \vee \exists n \in Node:
         \exists t \in \text{DOMAIN } proposal :
            \exists i \in \text{DOMAIN } proposal[t]:
                ReconcileProposal(n, t, i)
    \vee \exists n \in Node:
         \exists c \in \text{DOMAIN} \ configuration:
               ReconcileConfiguration(n, c)
Spec \stackrel{\Delta}{=} Init \wedge \Box [Next]_{vars}
Order \triangleq
   \forall t \in \text{DOMAIN } proposal :
     \forall i \in DOMAIN \ proposal[t]:
        \land \land proposal[t][i].phase = Commit
            \land proposal[t][i].state = InProgress
            \Rightarrow \neg \exists j \in \text{DOMAIN } proposal[t]:
                     \wedge j > i
                      \land proposal[t][j].phase = Commit
                      \land proposal[t][j].state = Complete
        \land \land proposal[t][i].phase = Apply
            \land proposal[t][i].state = InProgress
            \Rightarrow \neg \exists j \in \text{DOMAIN } proposal[t]:
                     \wedge j > i
                      \land proposal[t][j].phase = Apply
                      \land proposal[t][j].state = Complete
Consistency \triangleq
   \forall t \in \text{DOMAIN } target :
      LET
            Compute the transaction indexes that have been applied to the target
           targetIndexes \stackrel{\triangle}{=} \{i \in DOMAIN \ transaction : \}
                                        \land transaction[i].type = Change
                                        \land i \in \text{DOMAIN } proposal[t]
                                        \land proposal[t][i].phase = Apply
                                        \land proposal[t][i].state = Complete
                                        \land t \in \text{DOMAIN} \ transaction[i].change
                                        \wedge \neg \exists j \in \text{DOMAIN} \ transaction:
                                                \wedge i > i
                                                \land transaction[j].type = Rollback
                                                \land transaction[j].rollback = i
```

```
\land transaction[j].phase = Apply
                                             \land transaction[j].state = Complete
            Compute the set of paths in the target that have been updated by transactions
          appliedPaths
                              \stackrel{\triangle}{=} UNION {DOMAIN transaction[i].change[t]: i \in targetIndexes}}
            Compute the highest index applied to the target for each path
          pathIndexes
                              \stackrel{\Delta}{=} [p \in appliedPaths \mapsto \text{CHOOSE } i \in targetIndexes :
                                          \forall j \in targetIndexes:
                                               \land i \geq j
                                               \land p \in \text{DOMAIN} \ transaction[i].change[t]]
            Compute the expected target configuration based on the last indexes applied
            to the target for each path.
          expectedConfig \triangleq [p \in DOMAIN \ pathIndexes \mapsto transaction[pathIndexes[p]].change[t][p]]
     IN
          target[t] = expectedConfig
Isolation \triangleq
   \forall i \in \text{DOMAIN} \ transaction:
      \land \land transaction[i].phase = Commit
         \land transaction[i].state = InProgress
         \land transaction[i].isolation = Serializable
         \Rightarrow \neg \exists j \in \text{DOMAIN } transaction :
                  \wedge j > i
                  \land transaction[j].targets \cap transaction[i].targets \neq \{\}
                  \land transaction[j].phase = Commit
      \land \land transaction[i].phase = Apply
         \land transaction[i].state = InProgress
         \land transaction[i].isolation = Serializable
         \Rightarrow \neg \exists j \in \text{DOMAIN} \ transaction:
                  \wedge j > i
                  \land transaction[j].targets \cap transaction[i].targets \neq \{\}
                  \land transaction[j].phase = Apply
Safety \triangleq \Box(Order \land Consistency \land Isolation)
THEOREM Spec \Rightarrow Safety
Completion \triangleq
   \forall i \in \text{DOMAIN } transaction :
      \land transaction[i].phase \in \{Apply, Abort\}
      \land transaction[i].state = Complete
Liveness \triangleq \Diamond Completion
Theorem Spec \Rightarrow Liveness
```

```
Type assumptions. 
 ASSUME Nil \in STRING
```

Assume $\forall phase \in Phase : phase \in String$

Assume $\forall state \in State : state \in String$

Assume $\forall status \in Status : status \in String$

Assume $\land IsFiniteSet(Node)$

 $\land \, \forall \, n \in \mathit{Node} :$

 $\land n \notin \text{DOMAIN } Target$

 $\land n \in \text{STRING}$

Assume $\land \forall t \in \text{domain } Target :$

 $\land \ t \not \in Node$

 $\land t \in \text{STRING}$

 $\land \ Target[t].persistent \in \texttt{BOOLEAN}$

 $\land \, \forall \, p \in \text{DOMAIN} \, \, \textit{Target}[t].values:$

IsFiniteSet(Target[t].values[p])

 $[\]backslash * \ {\it Modification History}$

^{*} Last modified $\mathit{Thu}\ \mathit{Feb}\ 10\ 11:36:59\ \mathit{PST}\ 2022$ by $\mathit{jordanhalterman}$

^{\^*} Created Wed Sep 22 13:22:32 PDT 2021 by jordanhalterman