
MODULE *Transaction*

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

An empty constant

CONSTANT *Nil*

Transaction phase constants

CONSTANTS

Change,

Rollback

Transaction phase constants

CONSTANTS

Commit,

Apply

Status constants

CONSTANTS

Pending,

InProgress,

Complete,

Aborted,

Canceled,

Failed

$Status \triangleq \{Pending, InProgress, Complete, Aborted, Canceled, Failed\}$

$Done \triangleq \{Complete, Aborted, Canceled, Failed\}$

The set of all nodes

CONSTANT *Node*

The set of possible paths and values

CONSTANT *Path, Value*

$Empty \triangleq [p \in \{\} \mapsto Nil]$

Variables defined by other modules.

VARIABLES

configuration,
mastership,
conn,
target

A transaction log. Transactions may either request a set of changes to a set of targets or rollback a prior change.

VARIABLE *transactions*

A history of transaction change/rollback commit/apply events used for model checking.

VARIABLE *history*

TypeOK \triangleq

$\forall i \in \text{DOMAIN } transactions :$
 $\wedge transactions[i].index \in Nat$
 $\wedge transactions[i].phase \in \{Change, Rollback\}$
 $\wedge transactions[i].change.commit \in Status$
 $\wedge transactions[i].change.apply \in Status$
 $\wedge \forall p \in \text{DOMAIN } transactions[i].change.values :$
 $\quad transactions[i].change.values[p] \neq Nil \Rightarrow$
 $\quad \quad transactions[i].change.values[p] \in \text{STRING}$
 $\wedge transactions[i].rollback.commit \neq Nil \Rightarrow$
 $\quad transactions[i].rollback.commit \in Status$
 $\wedge transactions[i].rollback.apply \neq Nil \Rightarrow$
 $\quad transactions[i].rollback.apply \in Status$
 $\wedge \forall p \in \text{DOMAIN } transactions[i].rollback.values :$
 $\quad transactions[i].rollback.values[p] \neq Nil \Rightarrow$
 $\quad \quad transactions[i].rollback.values[p] \in \text{STRING}$

LOCAL *State* \triangleq [
 transactions $\mapsto transactions$,
 configuration $\mapsto configuration$,
 mastership $\mapsto mastership$,
 conn $\mapsto conn$,
 target $\mapsto target$]

LOCAL *Transitions* \triangleq

LET

indexes $\triangleq \{i \in \text{DOMAIN } transactions' :$
 $\quad i \in \text{DOMAIN } transactions \Rightarrow transactions'[i] \neq transactions[i]\}$

IN [*transactions* $\mapsto [i \in indexes \mapsto transactions'[i]]$] @@
 (IF *configuration'* $\neq configuration$ THEN [*configuration* $\mapsto configuration'$] ELSE *Empty*) @@
 (IF *target'* $\neq target$ THEN [*target* $\mapsto target'$] ELSE *Empty*)

Test \triangleq INSTANCE *Test* WITH

File \leftarrow "Transaction.log"

$$\begin{aligned}
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.target} = i] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Change}, \\
& \quad \text{phase} \mapsto \text{Commit}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{InProgress}]) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
\vee & \wedge \text{configuration.committed.target} = i \\
& \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{change.commit} = \text{InProgress}, \\
& \quad ![i].\text{rollback.index} = \text{configuration.committed.revision}, \\
& \quad ![i].\text{rollback.values} = [\\
& \quad \quad p \in \text{DOMAIN } \text{transactions}[i].\text{change.values} \mapsto \\
& \quad \quad \text{IF } p \in \text{DOMAIN } \text{configuration.committed.values} \text{ THEN } \\
& \quad \quad \quad \text{configuration.committed.values}[p] \\
& \quad \quad \text{ELSE } \text{Nil}]] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
\vee & \wedge \text{transactions}[i].\text{change.commit} = \text{InProgress} \\
& \wedge \vee \wedge \text{configuration.committed.index} \neq i \\
& \quad \wedge \vee \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = i, \\
& \quad \quad !.\text{committed.change} = i, \\
& \quad \quad !.\text{committed.revision} = i, \\
& \quad \quad !.\text{committed.ordinal} = \text{configuration.committed.ordinal}, \\
& \quad \quad !.\text{committed.values} = \text{transactions}[i].\text{change.values} \cup \text{configuration.committed.values}] \\
& \quad \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \quad \text{type} \mapsto \text{Change}, \\
& \quad \quad \text{phase} \mapsto \text{Commit}, \\
& \quad \quad \text{index} \mapsto i, \\
& \quad \quad \text{status} \mapsto \text{Complete}]) \\
& \vee \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = i, \\
& \quad !.\text{committed.change} = i] \\
& \quad \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \quad \text{type} \mapsto \text{Change}, \\
& \quad \quad \text{phase} \mapsto \text{Commit}, \\
& \quad \quad \text{index} \mapsto i, \\
& \quad \quad \text{status} \mapsto \text{Failed}]) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
\vee & \wedge \text{configuration.committed.index} = i \\
& \wedge \vee \wedge \text{configuration.committed.revision} = i \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{change.commit} = \text{Complete}, \\
& \quad \quad ![i].\text{change.ordinal} = \text{configuration.committed.ordinal}] \\
& \vee \wedge \text{configuration.committed.revision} \neq i \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{change.commit} = \text{Failed}, \\
& \quad \quad ![i].\text{change.apply} = \text{Canceled}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{UNCHANGED } \langle \text{mastership}, \text{conn}, \text{target} \rangle \\
\text{CommitRollback}(n, i) & \triangleq \\
& \wedge \vee \wedge \text{transactions}[i].\text{rollback.commit} = \text{Pending} \\
& \wedge \text{configuration.committed.revision} = i \\
& \wedge \vee \wedge \text{configuration.committed.target} = i \\
& \wedge \text{configuration.committed.index} = \text{configuration.committed.target} \\
& \wedge \vee \wedge \text{configuration.committed.index} = i \\
& \wedge \text{transactions}[\text{configuration.committed.index}].\text{change.commit} = \text{Complete} \\
& \vee \wedge \text{configuration.committed.index} > i \\
& \wedge \text{transactions}[\text{configuration.committed.index}].\text{rollback.commit} = \text{Complete} \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.target} = \text{transactions}[i].\text{rollback.index}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Rollback}, \\
& \quad \text{phase} \mapsto \text{Commit}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{InProgress}]) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
& \vee \wedge \text{configuration.committed.revision} = i \\
& \wedge \text{configuration.committed.target} = \text{transactions}[i].\text{rollback.index} \\
& \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{rollback.commit} = \text{InProgress}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
& \vee \wedge \text{transactions}[i].\text{rollback.commit} = \text{InProgress} \\
& \wedge \vee \wedge \text{configuration.committed.revision} = i \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{committed.index} = i, \\
& \quad !.\text{committed.ordinal} = \text{configuration.committed.ordinal}, \\
& \quad !.\text{committed.revision} = \text{transactions}[i].\text{rollback.index}, \\
& \quad !.\text{committed.values} = \text{transactions}[i].\text{rollback.values} \\
& \quad \text{configuration.committed.values}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Rollback}, \\
& \quad \text{phase} \mapsto \text{Commit}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{Complete}]) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
& \vee \wedge \text{configuration.committed.revision} = \text{transactions}[i].\text{rollback.index} \\
& \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{rollback.commit} = \text{Complete}, \\
& \quad ![i].\text{rollback.ordinal} = \text{configuration.committed.ordinal}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{mastership}, \text{conn}, \text{target} \rangle \\
\text{ApplyChange}(n, i) & \triangleq \\
& \wedge \text{transactions}[i].\text{change.commit} = \text{Complete} \\
& \wedge \vee \wedge \text{transactions}[i].\text{change.apply} = \text{Pending} \\
& \wedge \vee \wedge \text{configuration.applied.ordinal} = \text{transactions}[i].\text{change.ordinal} - 1
\end{aligned}$$

configuration.applied

$$\begin{aligned}
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Change}, \\
& \quad \text{phase} \mapsto \text{Apply}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{Complete}]) \\
& \vee \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i, \\
& \quad !.\text{applied.ordinal} = \text{transactions}[i].\text{change.ordinal}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Change}, \\
& \quad \text{phase} \mapsto \text{Apply}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{Failed}]) \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \text{transactions}[i].\text{phase} = \text{Rollback} \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i, \\
& \quad !.\text{applied.ordinal} = \text{transactions}[i].\text{change.ordinal}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Change}, \\
& \quad \text{phase} \mapsto \text{Apply}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{Failed}]) \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
& \text{If the change has been applied, update the transaction status.} \\
& \vee \wedge \text{configuration.applied.ordinal} = \text{transactions}[i].\text{change.ordinal} \\
& \wedge \vee \wedge \text{configuration.applied.revision} = i \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{change.apply} = \text{Complete}] \\
& \quad \vee \wedge \text{configuration.applied.revision} = \text{transactions}[i].\text{rollback.index} \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{change.apply} = \text{Failed}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{target}, \text{history} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{mastership}, \text{conn} \rangle \\
& \text{ApplyRollback}(n, i) \triangleq \\
& \quad \wedge \text{transactions}[i].\text{rollback.commit} = \text{Complete} \\
& \quad \wedge \vee \wedge \text{transactions}[i].\text{rollback.apply} = \text{Pending} \\
& \quad \wedge \vee \wedge \text{configuration.applied.ordinal} = \text{transactions}[i].\text{rollback.ordinal} - 1 \\
& \quad \wedge \vee \wedge \text{configuration.applied.target} \neq \text{transactions}[i].\text{rollback.index} \\
& \quad \wedge \vee \wedge \text{configuration.applied.index} = i \\
& \quad \quad \wedge \text{transactions}[\text{configuration.applied.index}].\text{change.apply} \in \text{Done} \\
& \quad \vee \wedge \text{configuration.applied.index} > i \\
& \quad \quad \wedge \text{transactions}[\text{configuration.applied.index}].\text{rollback.apply} \in \text{Done} \\
& \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.target} = \text{transactions}[i].\text{rollback.index}] \\
& \quad \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \quad \text{type} \mapsto \text{Rollback},
\end{aligned}$$

$$\begin{aligned}
& \text{phase} \mapsto \text{Apply}, \\
& \text{index} \mapsto i, \\
& \text{status} \mapsto \text{InProgress}) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
& \vee \wedge \text{configuration.applied.target} = \text{transactions}[i].\text{rollback.index} \\
& \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{rollback.apply} = \text{InProgress}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{history} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \text{transactions}[i].\text{rollback.apply} = \text{InProgress} \\
& \quad \text{If this transaction has not yet been applied, attempt to apply it.} \\
& \wedge \vee \wedge \text{configuration.applied.ordinal} \neq \text{transactions}[i].\text{rollback.ordinal} \\
& \wedge \text{configuration.state} = \text{Complete} \\
& \wedge \text{configuration.term} = \text{mastership.term} \\
& \wedge \text{conn}[n].\text{id} = \text{mastership.conn} \\
& \wedge \text{conn}[n].\text{connected} \\
& \wedge \text{target.running} \\
& \wedge \text{target}' = [\text{target} \text{ EXCEPT } !.\text{values} = \text{transactions}[i].\text{rollback.values} @@ \text{target.values}] \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } !.\text{applied.index} = i, \\
& \quad !.\text{applied.ordinal} = \text{transactions}[i].\text{rollback.ordinal}, \\
& \quad !.\text{applied.revision} = \text{transactions}[i].\text{rollback.index}, \\
& \quad !.\text{applied.values} = \text{transactions}[i].\text{rollback.values} @@ \\
& \quad \text{configuration.applied.values}] \\
& \wedge \text{history}' = \text{Append}(\text{history}, [\\
& \quad \text{type} \mapsto \text{Rollback}, \\
& \quad \text{phase} \mapsto \text{Apply}, \\
& \quad \text{index} \mapsto i, \\
& \quad \text{status} \mapsto \text{Complete}]) \\
& \wedge \text{UNCHANGED } \langle \text{transactions} \rangle \\
& \quad \text{If the change has been applied, update the transaction status.} \\
& \vee \wedge \text{configuration.applied.ordinal} = \text{transactions}[i].\text{rollback.ordinal} \\
& \wedge \text{configuration.applied.revision} = \text{transactions}[i].\text{rollback.index} \\
& \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![i].\text{rollback.apply} = \text{Complete}] \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{target}, \text{history} \rangle \\
& \wedge \text{UNCHANGED } \langle \text{mastership}, \text{conn} \rangle \\
& \text{ReconcileTransaction}(n, i) \triangleq \\
& \wedge i \in \text{DOMAIN } \text{transactions} \\
& \wedge \text{mastership.master} = n \\
& \wedge \vee \text{CommitChange}(n, i) \\
& \quad \vee \text{ApplyChange}(n, i) \\
& \quad \vee \text{CommitRollback}(n, i) \\
& \quad \vee \text{ApplyRollback}(n, i)
\end{aligned}$$
