

EXTENDS

Northbound,
Proposal,
Configuration,
Mastership,
Southbound

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

LOCAL INSTANCE *TLC*

vars \triangleq $\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{target} \rangle$

Formal specification, constraints, and theorems.

Init \triangleq

$\wedge \text{InitNorthbound}$
 $\wedge \text{InitProposal}$
 $\wedge \text{InitConfiguration}$
 $\wedge \text{InitMastership}$
 $\wedge \text{InitSouthbound}$

Next \triangleq

$\vee \wedge \text{NextNorthbound}$
 $\wedge \text{UNCHANGED } \langle \rangle$
 $\vee \wedge \text{NextProposal}$
 $\wedge \text{UNCHANGED } \langle \rangle$
 $\vee \wedge \text{NextConfiguration}$
 $\wedge \text{UNCHANGED } \langle \text{proposal} \rangle$
 $\vee \wedge \text{NextMastership}$
 $\wedge \text{UNCHANGED } \langle \text{proposal}, \text{configuration} \rangle$
 $\vee \wedge \text{NextSouthbound}$
 $\wedge \text{UNCHANGED } \langle \text{proposal}, \text{configuration}, \text{mastership} \rangle$

Spec $\triangleq \text{Init} \wedge \Box[\text{Next}]_{\text{vars}} \wedge \text{WF}_{\text{vars}}(\text{Next})$

Order \triangleq

$\forall i \in \text{DOMAIN } \text{proposal} :$
 $\wedge \text{proposal}[i].\text{type} = \text{ProposalChange}$
 $\wedge \text{proposal}[i].\text{phase} = \text{ProposalApply}$
 $\wedge \text{proposal}[i].\text{state} \in \{\text{ProposalComplete}, \text{ProposalFailed}\}$

$$\begin{aligned}
& \Rightarrow \forall j \in \text{DOMAIN } \text{proposal} : \\
& \quad j < i \Rightarrow \\
& \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalCommit} \Rightarrow \text{proposal}[j].\text{state} = \text{ProposalFailed} \\
& \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \Rightarrow \text{proposal}[j].\text{state} \in \{\text{ProposalComplete}, \text{ProposalFailed}\} \\
& \text{IsConsistent}(\text{indexes}, \text{values}) \triangleq \\
& \quad \text{LET} \\
& \quad \quad \text{Compute the set of paths in the target that have been updated by transactions} \\
& \quad \quad \text{appliedPaths} \triangleq \text{UNION } \{\text{DOMAIN } \text{proposal}[i].\text{change.values} : i \in \text{indexes}\} \\
& \quad \quad \text{Compute the highest index applied to the target for each path} \\
& \quad \quad \text{pathIndexes} \triangleq [p \in \text{appliedPaths} \mapsto \text{CHOOSE } i \in \text{indexes} : \\
& \quad \quad \quad \forall j \in \text{indexes} : \\
& \quad \quad \quad \quad \wedge i \geq j \\
& \quad \quad \quad \quad \wedge p \in \text{DOMAIN } \text{proposal}[i].\text{change.values}] \\
& \quad \quad \text{Compute the expected target configuration based on the last indexes applied} \\
& \quad \quad \text{to the target for each path.} \\
& \quad \quad \text{expectedConfig} \triangleq [p \in \text{DOMAIN } \text{pathIndexes} \mapsto \text{proposal}[\text{pathIndexes}[p]].\text{change.values}[p]] \\
& \quad \quad \text{Compute the actual configuration by converting missing path values to Nil} \\
& \quad \quad \text{actualConfig} \triangleq [p \in \text{DOMAIN } \text{expectedConfig} \mapsto \text{IF } p \in \text{DOMAIN } \text{values} \text{ THEN } \text{values}[p] \text{ ELSE } [value \mapsto \dots]] \\
& \quad \text{IN} \\
& \quad \quad \text{actualConfig} \neq \text{expectedConfig} \Rightarrow \neg(\text{PrintT}(\text{indexes}) \wedge \text{PrintT}(\text{appliedPaths}) \wedge \text{PrintT}(\text{pathIndexes}) \wedge P) \\
& \text{Consistency} \triangleq \\
& \quad \wedge \text{LET } \text{indexes} \triangleq \{i \in \text{DOMAIN } \text{proposal} : \wedge \vee \wedge \text{proposal}[i].\text{type} = \text{ProposalChange} \\
& \quad \quad \quad \wedge \text{proposal}[i].\text{phase} = \text{ProposalCommit} \\
& \quad \quad \quad \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete} \\
& \quad \quad \quad \vee \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \quad \quad \quad \wedge \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \quad \quad \quad \wedge j > i \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{type} = \text{ProposalRollback} \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{rollback.index} = i \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalCommit} \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}\} \\
& \quad \text{IN } \text{IsConsistent}(\text{indexes}, \text{configuration.committed.values}) \\
& \quad \wedge \text{LET } \text{indexes} \triangleq \{i \in \text{DOMAIN } \text{proposal} : \wedge \text{proposal}[i].\text{type} = \text{ProposalChange} \\
& \quad \quad \quad \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \quad \quad \quad \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete} \\
& \quad \quad \quad \wedge \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \quad \quad \quad \wedge j > i \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{type} = \text{ProposalRollback} \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{rollback.index} = i \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \\
& \quad \quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}\} \\
& \quad \text{IN } \text{IsConsistent}(\text{indexes}, \text{configuration.applied.values}) \\
& \text{Safety} \triangleq \Box(\text{Order} \wedge \text{Consistency})
\end{aligned}$$

THEOREM $Spec \Rightarrow Safety$

$$\begin{aligned} Terminated(i) &\triangleq \\ &\wedge i \in \text{DOMAIN } proposal \\ &\wedge \vee \wedge proposal[i].phase = ProposalApply \\ &\quad \wedge proposal[i].state = ProposalComplete \\ &\quad \vee proposal[i].state = ProposalFailed \end{aligned}$$

$$\begin{aligned} Termination &\triangleq \\ &\forall i \in 1 \dots Len(proposal) : \\ &\quad Terminated(i) \end{aligned}$$

$$Liveness \triangleq \Diamond Termination$$

THEOREM $Spec \Rightarrow Liveness$

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