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MODULE *Config*

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INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

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An empty constant

CONSTANT *Nil*

Transaction status constants

CONSTANTS

*TransactionPending*,  
*TransactionValidating*,  
*TransactionApplying*,  
*TransactionComplete*,  
*TransactionFailed*

Configuration status constants

CONSTANTS

*ConfigurationPending*,  
*ConfigurationInitializing*,  
*ConfigurationUpdating*,  
*ConfigurationComplete*,  
*ConfigurationFailed*

The set of all nodes

CONSTANT *Node*

Target is the possible targets, paths, and values

Example:  $Target \triangleq$  [  
   $target1 \mapsto$  [  
     $path1 \mapsto \{“value1”, “value2”\}$ ,  
     $path2 \mapsto \{“value2”, “value3”\}$ ],  
   $target2 \mapsto$  [  
     $path2 \mapsto \{“value3”, “value4”\}$ ,  
     $path3 \mapsto \{“value4”, “value5”\}$ ]]

CONSTANT *Target*

ASSUME *Nil* ∈ STRING

ASSUME *TransactionPending* ∈ STRING

ASSUME *TransactionValidating* ∈ STRING

ASSUME *TransactionApplying* ∈ STRING

ASSUME  $TransactionComplete \in \text{STRING}$   
 ASSUME  $TransactionFailed \in \text{STRING}$   
  
 ASSUME  $ConfigurationPending \in \text{STRING}$   
 ASSUME  $ConfigurationInitializing \in \text{STRING}$   
 ASSUME  $ConfigurationUpdating \in \text{STRING}$   
 ASSUME  $ConfigurationComplete \in \text{STRING}$   
 ASSUME  $ConfigurationFailed \in \text{STRING}$   
  
 ASSUME  $\wedge IsFiniteSet(Node)$   
        $\wedge \forall n \in Node :$   
            $\wedge n \notin \text{DOMAIN } Target$   
            $\wedge n \in \text{STRING}$   
  
 ASSUME  $\wedge \forall t \in \text{DOMAIN } Target :$   
        $\wedge IsFiniteSet(Target[t])$   
        $\wedge t \notin Node$   
        $\wedge t \in \text{STRING}$

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TYPE TransactionStatus ::= status ∈
  { TransactionPending,
    TransactionValidating,
    TransactionApplying,
    TransactionComplete,
    TransactionFailed }
TYPE Transaction ≜ [
  id      ::= id ∈ STRING,
  index   ::= index ∈ Nat,
  revision ::= revision ∈ Nat,
  atomic  ::= atomic ∈ BOOLEAN ,
  sync    ::= sync ∈ BOOLEAN ,
  changes ::= [ target ∈ SUBSET (DOMAIN Target) ↦ [
    path ∈ SUBSET (DOMAIN Target[target]) ↦ [
      value ::= value ∈ STRING,
      delete ::= delete ∈ BOOLEAN ]],
  status ::= status ∈ TransactionStatus]
TYPE ConfigurationStatus ::= status ∈
  { ConfigurationPending,
    ConfigurationInitializing,
    ConfigurationUpdating,
    ConfigurationComplete,
    ConfigurationFailed }
TYPE Configuration ≜ [
  id      ::= id ∈ STRING,
  revision ::= revision ∈ Nat,
  target  ::= target ∈ STRING,

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paths ::= [ path ∈ SUBSET (DOMAIN Target[target]) ↦ [
  value ::= value ∈ STRING,
  index ::= index ∈ Nat,
  deleted ::= delete ∈ BOOLEAN ]],
txIndex ::= txIndex ∈ Nat,
syncIndex ::= syncIndex ∈ Nat,
mastershipTerm ::= mastershipTerm ∈ Nat,
status ::= status ∈ ConfigurationStatus]

```

A sequence of transactions

Each transactions contains a record of 'changes' for a set of targets

VARIABLE *transactions*

A record of target configurations

Each configuration represents the desired state of the target

VARIABLE *configurations*

A record of target states

VARIABLE *targets*

A record of target masters

VARIABLE *masters*

*vars*  $\triangleq$   $\langle transactions, configurations, targets \rangle$

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$ChangeMaster(n, t) \triangleq$   
 $\wedge masters[t].master \neq n$   
 $\wedge masters' = [masters \text{ EXCEPT } ![t].term = masters[t].term + 1,$   
 $\phantom{\wedge masters' = [masters \text{ EXCEPT } } ![t].master = n]$   
 $\wedge \text{UNCHANGED } \langle transactions, configurations \rangle$

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This section models the northbound *API* for the configuration service.

This crazy thing returns the set of all possible sets of valid changes

$ValidChanges \triangleq$   
 LET  $allPaths \triangleq \text{UNION } \{ (DOMAIN \ Target[t]) : t \in DOMAIN \ Target \}$   
 $allValues \triangleq \text{UNION } \{ \text{UNION } \{ Target[t][p] : p \in DOMAIN \ Target[t] \} : t \in DOMAIN \ Target \}$   
 IN  
 $\{ targetPathValues \in SUBSET (Target \times allPaths \times allValues \times BOOLEAN) :$   
 $\wedge \forall target \in DOMAIN \ Target :$   
 LET  $targetIndexes \triangleq \{ i \in 1 \dots Len(targetPathValues) : \wedge targetPathValues[i][1] = target \}$   
 IN  $\vee Cardinality(targetIndexes) = 0$   
 $\vee \wedge Cardinality(targetIndexes) = 1$   
 $\wedge \text{LET } targetPathValue \triangleq targetPathValues[\text{CHOOSE } index \in targetIndexes : \text{TRUE}]$   
 $\phantom{\wedge \text{LET } } targetPath \triangleq targetPathValue[2]$   
 $\phantom{\wedge \text{LET } } targetValue \triangleq targetPathValue[3]$

$$\begin{aligned}
& \text{IN} \\
& \wedge \text{targetPath} \setminus (\text{DOMAIN } \text{Target}[\text{target}]) = \{\} \\
& \wedge \text{targetValue} \in \text{Target}[\text{target}][\text{targetPath}]
\end{aligned}$$

Add a set of changes to the transaction log

$$\begin{aligned}
\text{Change} & \triangleq \\
& \wedge \exists \text{changes} \in \text{ValidChanges} : \\
& \quad \wedge \text{transactions}' = \text{Append}(\text{transactions}, [\text{index} \mapsto \text{Len}(\text{transactions}) + 1, \\
& \quad \quad \quad \text{atomic} \mapsto \text{FALSE}, \\
& \quad \quad \quad \text{sync} \mapsto \text{FALSE}, \\
& \quad \quad \quad \text{changes} \mapsto \text{changes}, \\
& \quad \quad \quad \text{status} \mapsto \text{TransactionPending}]) \\
& \wedge \text{UNCHANGED } \langle \text{configurations}, \text{targets} \rangle
\end{aligned}$$

This section models the Transaction log reconciler.

Reconcile the transaction log

$$\begin{aligned}
\text{ReconcileTransaction}(n, i) & \triangleq \\
& \text{If the transaction is } \text{Pending}, \text{ begin validation if the prior transaction} \\
& \text{has already been applied. This simplifies concurrency control in the controller} \\
& \text{and guarantees transactions are applied to the configurations in sequential order.} \\
& \wedge \vee \wedge \text{transactions}[i].\text{status} = \text{TransactionPending} \\
& \quad \wedge \vee \wedge \text{transactions}[i].\text{index} > 1 \\
& \quad \quad \wedge \text{transactions}[\text{transactions}[i].\text{index} - 1].\text{status} \in \{\text{TransactionComplete}, \text{TransactionFailed}\} \\
& \quad \quad \vee \text{transactions}[i].\text{index} = 1 \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{transactions}[i].\text{index}].\text{status} = \text{TransactionValidating}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{configurations} \rangle \\
& \text{If the transaction is in the } \text{Validating} \text{ state, compute and validate the} \\
& \text{Configuration for each target.} \\
& \vee \wedge \text{transactions}[i].\text{status} = \text{TransactionValidating} \\
& \quad \text{If validation fails any target, mark the transaction } \text{Failed}. \\
& \quad \text{If validation is successful, proceed to } \text{Applying}. \\
& \quad \wedge \exists \text{valid} \in \text{BOOLEAN} : \\
& \quad \quad \vee \wedge \text{valid} \\
& \quad \quad \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{transactions}[i].\text{index}].\text{status} = \text{TransactionApplying}] \\
& \quad \quad \vee \wedge \neg \text{valid} \\
& \quad \quad \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{transactions}[i].\text{index}].\text{status} = \text{TransactionFailed}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{configurations} \rangle \\
& \text{If the transaction is in the } \text{Applying} \text{ state, update the Configuration for each} \\
& \text{target and } \text{Complete} \text{ the transaction.} \\
& \vee \wedge \text{transactions}[i].\text{status} = \text{TransactionApplying} \\
& \quad \wedge \vee \wedge \text{transactions}[i].\text{atomic} \\
& \quad \quad \text{TODO: Apply atomic transactions here} \\
& \quad \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{transactions}[i].\text{index}].\text{status} = \text{TransactionComplete}] \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{configurations} \rangle
\end{aligned}$$

$$\begin{aligned}
& \wedge \vee \wedge \neg \text{transactions}[i].\text{atomic} \\
& \quad \text{Add the transaction index to each updated path} \\
& \wedge \text{configurations}' = [ \\
& \quad t \in \text{DOMAIN } \text{Target} \mapsto [ \\
& \quad \quad \text{configurations}[t] \text{ EXCEPT} \\
& \quad \quad \quad !.\text{paths} = [\text{path} \in \text{DOMAIN } \text{transactions}[i].\text{changes} \mapsto \\
& \quad \quad \quad \quad \text{transactions}[i].\text{changes}[\text{path}] @@ [\text{index} \mapsto \text{transactions}[i].\text{index}] @@ \text{configurations}[i] \\
& \quad \quad \quad !.\text{txIndex} = \text{transactions}[i].\text{index}, \\
& \quad \quad \quad !.\text{status} = \text{ConfigurationPending}] \\
& \quad \wedge \text{transactions}' = [\text{transactions} \text{ EXCEPT } ![\text{transactions}[i].\text{index}].\text{status} = \text{TransactionComplete}] \\
& \wedge \text{UNCHANGED } \langle \text{targets} \rangle
\end{aligned}$$


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This section models the Configuration reconciler.

$\text{ReconcileConfiguration}(n, c) \triangleq$

$$\begin{aligned}
& \wedge \vee \wedge \text{configurations}[c].\text{status} = \text{ConfigurationPending} \\
& \quad \text{If the configuration is marked } \text{ConfigurationPending} \text{ and mastership} \\
& \quad \text{has changed (indicated by an increased mastership term), mark the} \\
& \quad \text{configuration } \text{ConfigurationInitializing} \text{ to force full re-synchronization.} \\
& \wedge \vee \wedge \text{masters}[\text{configurations}[c].\text{target}].\text{term} > \text{configurations}[c].\text{mastershipTerm} \\
& \quad \wedge \text{configurations}' = [\text{configurations} \text{ EXCEPT } ![c].\text{status} = \text{ConfigurationInitializing}, \\
& \quad \quad \quad ![c].\text{mastershipTerm} = \text{masters}[\text{configurations}[c].\text{target}].\text{term}] \\
& \quad \text{If the configuration is marked } \text{ConfigurationPending} \text{ and the values have} \\
& \quad \text{changed (determined by comparing the transaction index to the last } \text{sync} \\
& \quad \text{index), mark the configuration } \text{ConfigurationUpdating} \text{ to push the changes} \\
& \quad \text{to the target.} \\
& \vee \wedge \text{configurations}[c].\text{syncIndex} < \text{configurations}[c].\text{txIndex} \\
& \quad \wedge \text{configurations}' = [\text{configurations} \text{ EXCEPT } ![c].\text{status} = \text{ConfigurationUpdating}] \\
& \vee \wedge \text{configurations}[c].\text{status} = \text{ConfigurationInitializing} \\
& \quad \wedge \text{masters}[\text{configurations}[c].\text{target}].\text{master} = n \\
& \quad \text{Merge the configuration paths with the target paths, removing paths} \\
& \quad \text{that have been marked deleted} \\
& \wedge \text{targets}' = [\text{targets} \text{ EXCEPT } ![\text{configurations}[c].\text{target}] = \\
& \quad \quad [p \in \{p \in \text{DOMAIN } c.\text{paths} : \neg \text{configurations}[c].\text{paths}[p].\text{deleted}\} \mapsto [\text{value} \mapsto \text{configurations}[c].\text{paths}[p].\text{value}], \\
& \quad \quad [p \in \{p \in \text{DOMAIN } \text{targets}[\text{configurations}[c].\text{target}] : \neg \text{configurations}[c].\text{paths}[p].\text{deleted}\} \mapsto \text{targets}[c].\text{paths}[p].\text{value}]] \\
& \quad \text{Set the configuration's status to } \text{Complete} \\
& \wedge \text{configurations}' = [\text{configurations} \text{ EXCEPT } ![c].\text{status} = \text{ConfigurationComplete}, \\
& \quad \quad \quad ![c].\text{syncIndex} = \text{configurations}[c].\text{txIndex}] \\
& \quad \text{If the configuration is marked } \text{ConfigurationUpdating}, \text{ we only need to} \\
& \quad \text{push paths that have changed since the target was initialized or last} \\
& \quad \text{updated by the controller. The set of changes made since the last} \\
& \quad \text{synchronization are identified by comparing the index of each path-value} \\
& \quad \text{to the last synchronization index, } \text{syncIndex} \\
& \vee \wedge \text{configurations}[c].\text{status} = \text{ConfigurationUpdating}
\end{aligned}$$

$\wedge \text{masters}[\text{configurations}[c].\text{target}].\text{master} = n$   
 Compute the set of updated and deleted paths by comparing  
 their indexes to the target's last sync index.  
 $\wedge \text{LET } \text{updatedPaths} \triangleq \{p \in \text{DOMAIN } \text{configurations}[c].\text{paths} : \text{configurations}[c].\text{paths}[p].\text{index} > \text{conf}\}$   
 $\text{deletedPaths} \triangleq \{p \in \text{updatedPaths} : \text{configurations}[c].\text{paths}[p].\text{deleted}\}$   
 IN  
 Update the target paths by adding/updating paths that have changed and  
 removing paths that have been deleted since the last sync.  
 $\wedge \text{targets}' = [\text{targets} \text{ EXCEPT } ![\text{configurations}[c].\text{target}] =$   
 $\quad [p \in \text{updatedPaths} \setminus \text{deletedPaths} \mapsto \text{configurations}[c].\text{paths}[p]] @@$   
 $\quad [p \in \text{DOMAIN } \text{targets}[\text{configurations}[c].\text{target}] \setminus \text{deletedPaths} \mapsto \text{targets}[\text{configurations}[c].\text{target}]]$   
 $\wedge \text{configurations}' = [\text{configurations} \text{ EXCEPT } ![c].\text{status} = \text{ConfigurationComplete},$   
 $\quad ![c].\text{syncIndex} = \text{configurations}[c].\text{txIndex}]$   
 If the configuration is not already *ConfigurationPending* and mastership  
 has been lost revert it. This can occur when the connection to the  
 target has been lost and the mastership is no longer valid.  
 TODO: We still need to model mastership changes  
 $\vee \wedge c.\text{status} \neq \text{ConfigurationPending}$   
 $\wedge \text{masters}[\text{configurations}[c].\text{target}].\text{master} = \text{Nil}$   
 $\wedge \text{configurations}' = [\text{configurations} \text{ EXCEPT } ![c].\text{status} = \text{ConfigurationPending}]$   
 $\wedge \text{UNCHANGED } \langle \text{transactions} \rangle$

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Init and next state predicates

$\text{Init} \triangleq$   
 $\wedge \text{transactions} = \langle \rangle$   
 $\wedge \text{configurations} = [t \in \text{Target} \mapsto$   
 $\quad [id \mapsto t,$   
 $\quad \text{config} \mapsto$   
 $\quad \quad [path \in \{\} \mapsto$   
 $\quad \quad \quad [path \mapsto path,$   
 $\quad \quad \quad value \mapsto \text{Nil},$   
 $\quad \quad \quad index \mapsto 0,$   
 $\quad \quad \quad deleted \mapsto \text{FALSE}]]]]$   
 $\wedge \text{targets} = [t \in \text{Target} \mapsto$   
 $\quad [path \in \{\} \mapsto$   
 $\quad \quad [value \mapsto \text{Nil}]]]$   
 $\wedge \text{masters} = [t \in \text{Target} \mapsto [master \mapsto \text{Nil}, term \mapsto 0]]$   
 $\text{Next} \triangleq$   
 $\vee \text{Change}$   
 $\vee \exists n \in \text{Node} :$   
 $\quad \vee \exists t \in \text{DOMAIN } \text{Target} :$   
 $\quad \quad \text{ChangeMaster}(n, t)$   
 $\quad \vee \exists t \in \text{DOMAIN } \text{transactions} :$

$$\begin{array}{c}
\textit{ReconcileTransaction}(n, t) \\
\vee \exists t \in \text{DOMAIN configurations} : \\
\textit{ReconcileConfiguration}(n, t)
\end{array}$$

$$Spec \triangleq Init \wedge \Box[Next]_{vars}$$


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