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——— MODULE ConfigImpl -
INSTANCE Naturals
INSTANCE FiniteSets
{\tt INSTANCE}\ Sequences
LOCAL INSTANCE TLC
This section specifies constant parameters for the model.
Constant LogEnabled
Assume LogEnabled \in Boolean
CONSTANT None
Assume None \in \text{string}
CONSTANT Node
Assume \forall n \in Node : n \in String
CONSTANTS
   Change,
   Rollback
Event \triangleq \{Change, Rollback\}
Assume \forall e \in Event : e \in String
CONSTANTS
   Commit,
   Apply
Phase \triangleq \{Commit, Apply\}
\texttt{ASSUME} \ \forall \ p \in Phase: p \in \texttt{STRING}
CONSTANTS
   Pending,
   In Progress,
   Complete,
   Aborted,
   Failed
State \triangleq \{Pending, InProgress, Complete, Aborted, Failed\}
Working \triangleq \{Pending, InProgress\}
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Finished \triangleq \{Complete, Aborted, Failed\} ASSUME \ \forall s \in State : s \in STRING CONSTANT \ Path ASSUME \ \forall p \in Path : p \in STRING CONSTANT \ Value ASSUME \ \forall v \in Value : v \in STRING All Values \triangleq Value \cup \{None\} CONSTANT \ NumProposals ASSUME \ NumProposals \in Nat
```

This section defines model state variables.

```
proposal \ \stackrel{\Delta}{=} \ \ [ \ i \in 1 \ldots Nat \mapsto \ [
     phase \mapsto Phase,
      change \mapsto [
        values \mapsto Change,
         commit \mapsto State,
        apply \mapsto State,
      rollback \mapsto [
         index \mapsto Nat,
         values \mapsto Change,
         commit \mapsto State,
         apply \mapsto State]]]
configuration \stackrel{\Delta}{=} [
   committed \mapsto [
      index \mapsto Nat,
      values \mapsto Change,
   applied \mapsto \ [
      index\mapsto Nat,
      values \mapsto Change,
     term \mapsto Nat]]
mastership \; \stackrel{\Delta}{=} \; \; [
   master \mapsto \text{STRING},
   term\mapsto Nat,
   conn \mapsto Nat]
conn \ \stackrel{\Delta}{=} \ \ [ \ n \in \mathit{Node} \mapsto \ [
     id \qquad \mapsto Nat,
     connected \mapsto \texttt{BOOLEAN} ]]
target \stackrel{\Delta}{=} [
   id \mapsto Nat,
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values \mapsto Change,
  running \mapsto BOOLEAN
VARIABLE proposal
VARIABLE configuration
{\tt VARIABLE}\ mastership
VARIABLE conn
Variable target
Variable history
vars \triangleq \langle proposal, configuration, mastership, conn, target, history \rangle
LOCAL MastershipLog \stackrel{\triangle}{=} \text{INSTANCE } Log \text{ WITH}
                 ← "Mastership.log",
   File
    CurrState \leftarrow [
       target
                         \mapsto target,
       mastership
                       \mapsto mastership,
       conns
                         \mapsto conn],
   SuccState \leftarrow [
       target
                         \mapsto target',
       mastership
                         \mapsto mastership',
                         \mapsto conn'],
       conns
    Enabled \leftarrow LogEnabled
LOCAL ConfigurationLog \stackrel{\triangle}{=} INSTANCE Log WITH
                 \leftarrow "Configuration.log",
   File
    CurrState \leftarrow \lceil
       configuration \mapsto configuration,
       target
                         \mapsto target,
                        \mapsto mastership,
       mastership
                        \mapsto conn],
       conns
    SuccState \leftarrow [
       configuration \mapsto configuration',
       target
                         \mapsto target',
                         \mapsto mastership',
       mastership
                        \mapsto conn'],
       conns
   Enabled
                \leftarrow LogEnabled
LOCAL ProposalLog \stackrel{\Delta}{=} INSTANCE Log WITH
                 \leftarrow \text{``Proposal.log''},
    File
    CurrState \leftarrow [
                        \mapsto [i \in \{i \in DOMAIN \ proposal : proposal[i].phase \neq None\} \mapsto proposal[i]],
       proposals
```

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configuration \mapsto configuration,
       target
                        \mapsto target,
       mastership
                        \mapsto mastership,
       conns
                       \mapsto conn],
   SuccState \leftarrow [
      proposals
                       \mapsto [i \in \{i \in DOMAIN \ proposal' : proposal'[i].phase \neq None\} \mapsto proposal'[i]],
      configuration \mapsto configuration',
                        \mapsto target',
       target
      mastership
                        \mapsto mastership',
       conns
                       \mapsto conn'],
   Enabled \leftarrow LogEnabled
This section models configuration target.
StartTarget \triangleq
   \land \neg target.running
   \wedge target' = [target \ EXCEPT \ !.id]
                                                  = target.id + 1,
                                     !.running = TRUE
   ∧ UNCHANGED ⟨proposal, configuration, mastership, conn, history⟩
StopTarget \triangleq
   \land target.running
   \land target' = [target \ EXCEPT \ !.running = FALSE,
                                     !.values = [p \in \{\} \mapsto [value \mapsto None]]]
   \land conn' = [n \in Node \mapsto [conn[n] \text{ EXCEPT } !.connected = \text{FALSE}]]
   \land UNCHANGED \langle proposal, configuration, mastership, history <math>\rangle
This section models nodes connection to the configuration target.
ConnectNode(n) \triangleq
   \wedge \neg conn[n].connected
   \land \ target.running
   \wedge conn' = [conn \ EXCEPT \ ![n].id]
                                                     = conn[n].id + 1,
                                   ![n].connected = TRUE]
   ∧ UNCHANGED ⟨proposal, configuration, mastership, target, history⟩
DisconnectNode(n) \triangleq
   \land conn[n].connected
   \wedge conn' = [conn \ EXCEPT \ ![n].connected = FALSE]
   \land UNCHANGED \langle proposal, configuration, mastership, target, history <math>\rangle
```

This section models mastership reconciliation.

```
ReconcileMastership(n) \stackrel{\Delta}{=}
   \land \lor \land conn[n].connected
          \land mastership.master = None
          \land mastership' = [master \mapsto n, term \mapsto mastership.term + 1, conn \mapsto conn[n].id]
       \vee \wedge \neg conn[n].connected
          \land mastership.master = n
          \land mastership' = [mastership \ EXCEPT \ !.master = None]
   \land UNCHANGED \langle proposal, configuration, conn, target, history <math>\rangle
This section models configuration reconciliation.
ReconcileConfiguration(n) \stackrel{\Delta}{=}
    \land mastership.master = n
   \land \lor \land configuration.status \neq InProgress
          \land configuration.applied.term < mastership.term
          \land configuration' = [configuration EXCEPT !.status = InProgress]
          \land UNCHANGED \langle target \rangle
       \lor \land configuration.status = InProgress
          \land configuration.applied.term < mastership.term
          \land conn[n].connected
          \land target.running
          \land target' = [target \ Except \ !.values = configuration.applied.values]
          \land configuration' = [configuration EXCEPT !.applied.term = mastership.term,
                                                            !.applied.target = target.id,
                                                             !.status
                                                                                 = Complete
   \land UNCHANGED \langle proposal, mastership, conn, history \rangle
This section models proposal reconcilation.
CommitChange(n, i) \triangleq
   \land \lor \land proposal[i].change.commit = Pending
           To apply a change, the prior change must have been committed. Additionally,
           the configuration's applied index must match the proposed index to prevent
           commits while a prior change is still being rolled back.
          \land i-1 \in \text{DOMAIN } proposal \Rightarrow proposal[i-1].change.commit \in Finished
          \land proposal[i].rollback.commit = None
          \land \lor \land configuration.committed.proposal < i
                \land configuration.committed.index = configuration.committed.proposal
                \land configuration' = [configuration \ EXCEPT \ !.committed.proposal = i]
                \land UNCHANGED \langle proposal \rangle
             \lor \land configuration.committed.proposal = i
                \land configuration.committed.index \neq i
                \land \lor \texttt{LET} \ rollbackIndex \stackrel{\triangle}{=} \ configuration.committed.index
                           rollbackValues \stackrel{\Delta}{=} [p \in DOMAIN \ proposal[i].change.values \mapsto
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IF p \in DOMAIN configuration.committed.values THEN
                                                      configuration.committed.values[p]
                                                   ELSE
                                                      [index \mapsto 0, value \mapsto None]]
                         proposal' = [proposal \ EXCEPT \ ![i].rollback.index = rollbackIndex,
                                                              ![i].rollback.values = rollbackValues,
                                                              ![i].change.commit = InProgress]
                  \lor proposal' = [proposal \ EXCEPT \ ![i].change.commit = Failed]
               \land UNCHANGED \langle configuration \rangle
         \land UNCHANGED \langle history \rangle
      \lor \land proposal[i].change.commit = InProgress
         \land \lor \land configuration.committed.index \neq configuration.committed.proposal
               \land LET values \stackrel{\triangle}{=} [p \in DOMAIN \ proposal[i].change.values <math>\mapsto
                                       proposal[i].change.values[p] @@ [index \mapsto i]] @@
                                          configuration. committed. values\\
                       \land configuration' = [configuration \ EXCEPT \ !.committed.index = i,]
                 IN
                                                                         !.committed.values = values
                       \land history' = Append(history, [type \mapsto Change, phase \mapsto Commit, index \mapsto i])
                        \land UNCHANGED \langle proposal \rangle
            \lor \land configuration.committed.proposal = i
               \land configuration.committed.index = i
               \land proposal' = [proposal \ EXCEPT \ ![i].change.commit = Complete]
               ∧ UNCHANGED ⟨configuration, history⟩
      \lor \land proposal[i].change.commit = Failed
         \land configuration.committed.proposal = i
         \land configuration.committed.index \neq i
         \land configuration' = [configuration \ EXCEPT \ !.committed.index = configuration.committed.index]
         \land UNCHANGED \langle proposal, history \rangle
   \land UNCHANGED \langle mastership, conn, target \rangle
ApplyChange(n, i) \triangleq
   \land \lor \land proposal[i].change.apply = Pending
         \land proposal[i].rollback.apply = None
         \land \lor \land proposal[i].change.commit = Complete
               \land \forall j \in \text{DOMAIN } proposal : j < i \Rightarrow
                    \lor \land proposal[i].change.apply = Complete
                       \land proposal[j].rollback.apply \notin Working
                    \lor \land proposal[j].change.apply = Failed
                       \land proposal[j].rollback.apply = Complete
               \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = InProgress]
            \lor \land proposal[i].change.commit \in \{Aborted, Failed\}
               \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Aborted]
         \land UNCHANGED \langle configuration, target, history \rangle
      \lor \land proposal[i].change.apply = InProgress
          Verify the applied term is the current mastership term to ensure the
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configuration has been synchronized following restarts.
         \land configuration.applied.term = mastership.term
          Verify the node's connection to the target.
         \land conn[n].connected
         \land mastership.conn = conn[n].id
         \land target.running
          Model successful and failed target update requests.
         \land \lor \land \texttt{LET} \ values \stackrel{\triangle}{=} [p \in \texttt{DOMAIN} \ proposal[i].change.values \mapsto
                                       proposal[i].change.values[p]@@[index \mapsto i]]
                        \land target' = [target \ EXCEPT \ !.values = values @@ target.values]
                 IN
                        \land configuration' = [configuration \ EXCEPT \ !.applied.index = i,
                                                                           !.applied.values = values @@
                                                                             configuration.applied.values
                        \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Complete]
                        \land history' = Append(history, [type \mapsto Change, phase \mapsto Apply, index \mapsto i])
            \lor \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Failed]
               \land UNCHANGED \langle configuration, target, history \rangle
   \land UNCHANGED \langle mastership, conn \rangle
CommitRollback(n, i) \triangleq
   \land \lor \land proposal[i].rollback.commit = Pending
         \land i + 1 \in \text{DOMAIN } proposal \Rightarrow proposal[i + 1].rollback.commit = Complete
         \land \lor \land proposal[i].change.commit = Pending
               \land proposal' = [proposal \ EXCEPT \ ![i].change.commit = Aborted,
                                                       ![i].rollback.commit = Complete]
               \land UNCHANGED \langle configuration \rangle
            \lor \land proposal[i].change.commit \neq Pending
               \land configuration.committed.proposal = i
               \land configuration.committed.index = i
               \land configuration' = [configuration \ EXCEPT \ !.committed.proposal = proposal[i].rollback.index]
               \land UNCHANGED \langle proposal \rangle
            \lor \land proposal[i].change.commit \neq Pending
               \land configuration.committed.proposal = proposal[i].rollback.index
               \land configuration.committed.index = i
               \land proposal' = [proposal \ EXCEPT \ ![i].rollback.commit = InProgress]
               \land UNCHANGED \langle configuration \rangle
         \land UNCHANGED \langle history \rangle
      \lor \land proposal[i].rollback.commit = InProgress
         \land \lor \land configuration.committed.index \neq configuration.committed.proposal
               \land LET index \stackrel{\triangle}{=} proposal[i].rollback.index
                        values \triangleq proposal[i].rollback.values @@ configuration.committed.values
                        \land configuration' = [configuration EXCEPT !.committed.index = index,
                                                                           !.committed.values = values
                        \land history' = Append(history, [type \mapsto Rollback, phase \mapsto Commit, index \mapsto i])
                        \land UNCHANGED \langle proposal \rangle
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```
\lor \land configuration.committed.proposal = i
                \land \ configuration.committed.index = i
                \land proposal' = [proposal \ EXCEPT \ ![i].rollback.commit = Complete]
                \land UNCHANGED \langle configuration, history \rangle
   \land UNCHANGED \langle mastership, conn, target \rangle
ApplyRollback(n, i) \triangleq
   \land \lor \land proposal[i].rollback.apply = Pending
         \land proposal[i].rollback.commit = Complete
         \land \forall j \in DOMAIN \ proposal: j > i \land proposal[j].phase \neq None \Rightarrow
              proposal[j].rollback.apply \in Finished
         \land \lor \land proposal[i].change.apply = Pending
                \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Aborted,
                                                      ![i].rollback.apply = Complete]
            \lor \land proposal[i].change.apply \in Finished
                \land proposal' = [proposal \ EXCEPT \ ![i].rollback.apply = InProgress]
         \land UNCHANGED \langle configuration, target, history \rangle
      \lor \land proposal[i].rollback.apply = InProgress
          Verify the applied term is the current mastership term to ensure the
          configuration has been synchronized following restarts.
         \land configuration.applied.term = mastership.term
          Verify the node's connection to the target.
         \land conn[n].connected
         \land target.running
         \land target' = [target \ EXCEPT \ !.values = proposal[i].rollback.values @@ target.values]
         \land LET index \stackrel{\triangle}{=} proposal[i].rollback.index
                  values \triangleq proposal[i].rollback.values @@ configuration.applied.values
            IN
                \land configuration' = [configuration \ EXCEPT \ !.applied.index = index,]
                                                                  !.applied.values = values
                \land proposal' = [proposal \ EXCEPT \ ![i].rollback.apply = Complete]
                \land history' = Append(history, [type \mapsto Rollback, phase \mapsto Apply, index \mapsto i])
   \land UNCHANGED \langle mastership, conn \rangle
ReconcileProposal(n, i) \triangleq
   \land mastership.master = n
   \land \lor CommitChange(n, i)
      \vee ApplyChange(n, i)
      \vee CommitRollback(n, i)
      \vee ApplyRollback(n, i)
   \land UNCHANGED \langle mastership, conn \rangle
```

This section models changes to the proposal queue.

```
Propose change at index 'i'
ProposeChange(i) \triangleq
    \land proposal[i].phase = None
    \land i-1 \in \text{DOMAIN } proposal \Rightarrow proposal[i-1].phase \neq None
    \land \exists p \in Path, v \in AllValues:
         \land proposal' = [proposal \ EXCEPT \ ![i].phase]
                                                                          = Change,
                                                 ![i].change.values = (p:>[value \mapsto v]),
                                                 ![i].change.commit = Pending,
                                                 ![i].change.apply = Pending
    \land UNCHANGED \langle configuration, mastership, conn, target, history <math>\rangle
 Rollback proposed change at index 'i'
ProposeRollback(i) \triangleq
    \land proposal[i].phase = Change
    \land proposal' = [proposal \ EXCEPT \ ![i].phase]
                                                                     = Rollback,
                                            ![i].rollback.commit = Pending,
                                            ![i].rollback.apply = Pending]
    \land UNCHANGED \langle configuration, mastership, conn, target, history <math>\rangle
Formal specification, constraints, and theorems.
Init \triangleq
    \land proposal = [
          i \in 1 \dots NumProposals \mapsto [
            phase
                       \mapsto None,
            change \mapsto [
                values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],
                commit \mapsto None,
                apply \mapsto None].
            rollback \mapsto [
                index \mapsto 0,
                values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],
                commit \mapsto None,
                apply \mapsto None
    \land configuration = [
          committed \mapsto [
             proposal \mapsto 0,
```

 $\mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]]],$

 $\mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]]],$

index

 $values \mapsto [p]$ $applied \mapsto [$ $proposal \mapsto 0.$

index

term

 $target \mapsto 0,$

 $\mapsto 0$,

 $\mapsto 0,$ $\mapsto 0,$

```
status \mapsto Pending
    \land mastership = [master \mapsto None, term \mapsto 0, conn \mapsto 0]
    \land conn = [n \in Node \mapsto [id \mapsto 0, connected \mapsto FALSE]]
    \wedge target = [
          id
          values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],
          running \mapsto FALSE
    \wedge history = \langle \rangle
Next \triangleq
    \vee \exists i \in 1 ... NumProposals :
         \vee ProposeChange(i)
         \vee ProposeRollback(i)
    \vee \exists n \in Node, i \in DOMAIN \ proposal :
         ProposalLog!Action(ReconcileProposal(n, i), [node \mapsto n, index \mapsto i])
    \vee \exists n \in Node:
         ConfigurationLog!Action(ReconcileConfiguration(n), [node \mapsto n])
    \vee \exists n \in Node:
         MastershipLog!Action(ReconcileMastership(n), [node \mapsto n])
    \vee \exists n \in Node:
       \vee ConnectNode(n)
       \vee DisconnectNode(n)
    \vee StartTarget
    \vee Stop Target
Spec \triangleq
    \wedge Init
    \wedge \Box [Next]_{vars}
    \land \forall i \in 1 ... NumProposals : WF_{vars}(ProposeChange(i) \lor ProposeRollback(i))
    \land \forall n \in Node, i \in 1...NumProposals : WF_{vars}(ReconcileProposal(n, i))
    \land \forall n \in Node : WF_{(configuration, mastership, conn, target)}(ReconcileConfiguration(n))
    \land \forall n \in Node : WF_{\langle mastership, conn, target \rangle}(ReconcileMastership(n))
    \land \forall n \in Node : WF_{\langle conn, target \rangle}(ConnectNode(n) \lor DisconnectNode(n))
    \wedge \operatorname{WF}_{\langle target \rangle}(StartTarget)
    \wedge \operatorname{WF}_{\langle target \rangle}(StopTarget)
Mapping \stackrel{\Delta}{=} INSTANCE Config WITH
   proposal \leftarrow [i \in DOMAIN \ proposal \mapsto [
       phase
                   \mapsto proposal[i].phase,
                   \mapsto [p \in DOMAIN \ proposal[i].change.values \mapsto proposal[i].change.values[p].value],
       values
       change \mapsto |
           commit \mapsto \text{IF} \land proposal[i].change.commit = InProgress
                             \land configuration.committed.index = i
                          THEN Complete
                          ELSE proposal[i].change.commit,
                   \mapsto IF \land proposal[i].change.apply = InProgress
```

```
\land \ configuration.applied.index = i
                        Then Complete
                        ELSE proposal[i].change.apply],
      rollback \mapsto [
         commit \mapsto \text{IF } \land proposal[i].rollback.commit = InProgress
                         \land configuration.committed.index = proposal[i].rollback.index
                      Then Complete
                       ELSE proposal[i].rollback.commit,
                 \mapsto IF \land proposal[i].rollback.apply = InProgress
         apply
                         \land configuration.applied.index = proposal[i].rollback.index
                        THEN Complete
                        ELSE proposal[i].rollback.apply]]],
   configuration \gets
      committed \mapsto |
         values \mapsto configuration.committed.values,
      applied \mapsto [
         term \mapsto configuration.applied.term,
         target \mapsto configuration.applied.target,
         values \mapsto configuration.applied.values,
      status \mapsto configuration.status
Refinement \triangleq Mapping! Spec
Order \triangleq Mapping! Order
Consistency \triangleq Mapping! Consistency
Liveness \triangleq Mapping!Liveness
Sequential \triangleq Mapping! Sequential
```