
MODULE *Config*

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

An empty constant

CONSTANT *Nil*

Transaction type constants

CONSTANTS

TransactionChange,
TransactionRollback

Transaction isolation constants

CONSTANTS

IsolationDefault,
IsolationSerializable

Transaction status constants

CONSTANTS

TransactionInitializing,
TransactionInitialized,
TransactionValidating,
TransactionValidated,
TransactionCommitting,
TransactionCommitted,
TransactionApplying,
TransactionApplied,
TransactionFailed

TransactionStatus \triangleq

\langle *TransactionInitializing*,
TransactionInitialized,
TransactionValidating,
TransactionValidated,
TransactionCommitting,
TransactionCommitted,
TransactionApplying,
TransactionApplied,
TransactionFailed \rangle

Proposal type constants

CONSTANTS

ProposalChange,
ProposalRollback

Proposal status constants

CONSTANTS

ProposalInitializing,
ProposalInitialized,
ProposalValidating,
ProposalValidated,
ProposalCommitting,
ProposalCommitted,
ProposalApplying,
ProposalApplied,
ProposalFailed

$ProposalStatus \triangleq$
 $\langle ProposalInitializing,$
 $ProposalInitialized,$
 $ProposalValidating,$
 $ProposalValidated,$
 $ProposalCommitting,$
 $ProposalCommitted,$
 $ProposalApplying,$
 $ProposalApplied,$
 $ProposalFailed \rangle$

Configuration status constants

CONSTANTS

ConfigurationUnknown,
ConfigurationSynchronizing,
ConfigurationSynchronized,
ConfigurationPersisted,
ConfigurationFailed

CONSTANTS

Valid,
Invalid

CONSTANTS

Success,
Failure

The set of all nodes

CONSTANT *Node*

Target is the set of all targets and their possible paths and values.

Example: $Target \triangleq [$
 $\quad target1 \mapsto [\text{persistent} \mapsto \text{FALSE}, \text{values} \mapsto [$
 $\quad \quad path1 \mapsto \{ "value1", "value2" \},$
 $\quad \quad path2 \mapsto \{ "value2", "value3" \}]],$
 $\quad target2 \mapsto [\text{persistent} \mapsto \text{TRUE}, \text{values} \mapsto [$
 $\quad \quad path2 \mapsto \{ "value3", "value4" \},$
 $\quad \quad path3 \mapsto \{ "value4", "value5" \}]]]$

CONSTANT $Target$

$Phase(S, s) \triangleq \text{CHOOSE } i \in \text{DOMAIN } S : S[i] = s$

$TransactionPhase(s) \triangleq Phase(TransactionStatus, s)$

$ProposalPhase(s) \triangleq Phase(ProposalStatus, s)$

ASSUME $Nil \in \text{STRING}$

ASSUME $TransactionInitializing \in \text{STRING}$

ASSUME $TransactionInitialized \in \text{STRING}$

ASSUME $TransactionValidating \in \text{STRING}$

ASSUME $TransactionValidated \in \text{STRING}$

ASSUME $TransactionCommitting \in \text{STRING}$

ASSUME $TransactionCommitted \in \text{STRING}$

ASSUME $TransactionApplying \in \text{STRING}$

ASSUME $TransactionApplied \in \text{STRING}$

ASSUME $TransactionFailed \in \text{STRING}$

ASSUME $ProposalInitializing \in \text{STRING}$

ASSUME $ProposalInitialized \in \text{STRING}$

ASSUME $ProposalValidating \in \text{STRING}$

ASSUME $ProposalValidated \in \text{STRING}$

ASSUME $ProposalCommitting \in \text{STRING}$

ASSUME $ProposalCommitted \in \text{STRING}$

ASSUME $ProposalApplying \in \text{STRING}$

ASSUME $ProposalApplied \in \text{STRING}$

ASSUME $ProposalFailed \in \text{STRING}$

ASSUME $ConfigurationUnknown \in \text{STRING}$

ASSUME $ConfigurationSynchronizing \in \text{STRING}$

ASSUME $ConfigurationSynchronized \in \text{STRING}$

ASSUME $ConfigurationPersisted \in \text{STRING}$

ASSUME $ConfigurationFailed \in \text{STRING}$

ASSUME $\wedge IsFiniteSet(Node)$

$\wedge \forall n \in Node :$

$\wedge n \notin \text{DOMAIN } Target$

$\wedge n \in \text{STRING}$

ASSUME $\wedge \forall t \in \text{DOMAIN } Target :$
 $\wedge t \notin Node$
 $\wedge t \in \text{STRING}$
 $\wedge Target[t].persistent \in \text{BOOLEAN}$
 $\wedge \forall p \in \text{DOMAIN } Target[t].values :$
 $IsFiniteSet(Target[t].values[p])$

Configuration update/rollback requests are tracked and processed through two data types. Transactions represent the lifecycle of a single configuration change request and are stored in an append-only log. Configurations represent the desired configuration of a *gNMI* target based on the aggregate of relevant changes in the Transaction log.

```

TYPE TransactionType ::= type ∈
  { TransactionChange,
    TransactionRollback }

TYPE TransactionStatus ::= status ∈
  { TransactionInitializing,
    TransactionInitialized,
    TransactionValidating,
    TransactionValidated,
    TransactionCommitting,
    TransactionCommitted,
    TransactionApplying,
    TransactionApplied,
    TransactionFailed }

TYPE Transaction  $\triangleq$  [
  type      ::= type ∈ TransactionType,
  index     ::= index ∈ Nat,
  isolation ::= isolation ∈ { IsolationDefault, IsolationSerializable }
  values ::= [
    target ∈ SUBSET (DOMAIN Target)  $\mapsto$  [ path ∈ SUBSET (DOMAIN Target[target].values)  $\mapsto$ 
      [
        value ::= value ∈ STRING,
        delete ::= delete ∈ BOOLEAN ]]],
  rollback ::= index ∈ Nat,
  targets ::= targets ∈ SUBSET (DOMAIN Target)
  status ::= status ∈ TransactionStatus]

TYPE ProposalStatus ::= status ∈
  { ProposalInitializing,
    ProposalInitialized,
    ProposalValidating,
    ProposalValidated,
    ProposalCommitting,
    ProposalCommitted,
    ProposalApplying,
    ProposalApplied,
    ProposalFailed }

```

```

TYPE Proposal  $\triangleq$  [
  index      ::= index  $\in$  Nat,
  values     ::= [ path  $\in$  SUBSET (DOMAIN Target[target].values)  $\mapsto$  [
    value ::= value  $\in$  STRING,
    delete ::= delete  $\in$  BOOLEAN ]],
  rollback   ::= index  $\in$  Nat,
  prevIndex  ::= prevIndex  $\in$  Nat,
  nextIndex  ::= nextIndex  $\in$  Nat,
  rollbackIndex ::= rollbackIndex  $\in$  Nat,
  rollbackValues ::= [ path  $\in$  SUBSET (DOMAIN Target[target].values)  $\mapsto$  [
    value ::= value  $\in$  STRING,
    delete ::= delete  $\in$  BOOLEAN ]],
  status     ::= status  $\in$  ProposalStatus]

TYPE ConfigurationStatus ::= status  $\in$ 
{ ConfigurationUnknown,
  ConfigurationSynchronizing,
  ConfigurationSynchronized,
  ConfigurationPersisted,
  ConfigurationFailed}

TYPE Configuration  $\triangleq$  [
  id          ::= id  $\in$  STRING,
  target      ::= target  $\in$  STRING,
  values      ::= [ path  $\in$  SUBSET (DOMAIN Target[target])  $\mapsto$  [
    value ::= value  $\in$  STRING,
    index ::= index  $\in$  Nat,
    deleted ::= delete  $\in$  BOOLEAN ]],
  configIndex ::= index  $\in$  Nat,
  proposedIndex ::= proposedIndex  $\in$  Nat,
  committedIndex ::= committedIndex  $\in$  Nat,
  appliedIndex ::= appliedIndex  $\in$  Nat,
  appliedTerm ::= appliedTerm  $\in$  Nat,
  appliedValues ::= [ path  $\in$  SUBSET (DOMAIN Target[target])  $\mapsto$  [
    value ::= value  $\in$  STRING,
    index ::= index  $\in$  Nat,
    deleted ::= delete  $\in$  BOOLEAN ]],
  status ::= status  $\in$  ConfigurationStatus]

```

A transaction log. Transactions may either request a set of changes to a set of targets or rollback a prior change.

VARIABLE *transaction*

A record of per-target proposals

VARIABLE *proposal*

A record of per-target configurations

VARIABLE *configuration*

A record of target states

VARIABLE *target*

A record of target masterships

VARIABLE *mastership*

$vars \triangleq \langle transaction, proposal, configuration, mastership, target \rangle$

This section models *mastership* for the configuration service.

Mastership is used primarily to track the lifecycle of individual configuration targets and react to state changes on the southbound. Each target is assigned a master from the *Node* set, and masters can be unset when the target disconnects.

Set node n as the master for target t

$SetMaster(n, t) \triangleq$
 $\wedge mastership[t].master \neq n$
 $\wedge mastership' = [mastership \text{ EXCEPT } ![t].term = mastership[t].term + 1,$
 $\phantom{\wedge mastership' = [mastership \text{ EXCEPT } } ![t].master = n]$
 $\wedge \text{UNCHANGED } \langle transaction, proposal, configuration, target \rangle$

$UnsetMaster(t) \triangleq$

$\wedge mastership[t].master \neq Nil$
 $\wedge mastership' = [mastership \text{ EXCEPT } ![t].master = Nil]$
 $\wedge \text{UNCHANGED } \langle transaction, proposal, configuration, target \rangle$

This section models configuration changes and rollbacks. Changes are appended to the transaction log and processed asynchronously.

$Value(s, t, p) \triangleq$
 $\text{LET } value \triangleq \text{CHOOSE } v \in s : v.target = t \wedge v.path = p$
 IN
 $[value \mapsto value.value,$
 $ delete \mapsto value.delete]$

$Paths(s, t) \triangleq$
 $[p \in \{v.path : v \in \{v \in s : v.target = t\}\} \mapsto Value(s, t, p)]$

$Changes(s) \triangleq$
 $[t \in \{v.target : v \in s\} \mapsto Paths(s, t)]$

$ValidValues(t, p) \triangleq$
 $\text{UNION } \{ \{ [value \mapsto v, delete \mapsto \text{FALSE}] : v \in Target[t].values[p] \}, \{ [value \mapsto Nil, delete \mapsto \text{TRUE}] \} \}$

$ValidPaths(t) \triangleq$
 $\text{UNION } \{ \{ v @@ [path \mapsto p] : v \in ValidValues(t, p) \} : p \in \text{DOMAIN } Target[t].values \}$

$ValidTargets \triangleq$
 $\text{UNION } \{ \{ p @@ [target \mapsto t] : p \in ValidPaths(t) \} : t \in \text{DOMAIN } Target \}$

The set of all valid sets of changes to all targets and their paths.

The set of possible changes is computed from the *Target* model value.

$$\begin{aligned} \text{ValidChanges} &\triangleq \\ \text{LET } \text{changeSets} &\triangleq \{s \in \text{SUBSET } \text{ValidTargets} : \\ &\quad \forall t \in \text{DOMAIN } \text{Target} : \\ &\quad \quad \forall p \in \text{DOMAIN } \text{Target}[t].\text{values} : \\ &\quad \quad \quad \text{Cardinality}(\{v \in s : v.\text{target} = t \wedge v.\text{path} = p\}) \leq 1\} \\ \text{IN} & \\ &\{ \text{Changes}(s) : s \in \text{changeSets} \} \end{aligned}$$

The next available index in the transaction log.

This is computed as the max of the existing indexes in the log to allow for changes to the log (*e.g.* log compaction) to be modeled.

$$\begin{aligned} \text{NextIndex} &\triangleq \\ \text{IF DOMAIN } \text{transaction} &= \{\} \text{ THEN} \\ &1 \\ \text{ELSE} & \\ \text{LET } i &\triangleq \text{CHOOSE } i \in \text{DOMAIN } \text{transaction} : \\ &\quad \forall j \in \text{DOMAIN } \text{transaction} : i \geq j \\ \text{IN } &i + 1 \end{aligned}$$

Add a set of changes 'c' to the transaction log

$$\begin{aligned} \text{Change}(c) &\triangleq \\ \wedge \exists \text{isolation} \in \{ &\text{IsolationDefault}, \text{IsolationSerializable} \} : \\ &\quad \wedge \text{transaction}' = \text{transaction} @@ (\text{NextIndex} :> [\text{type} \quad \mapsto \text{TransactionChange}, \\ &\quad \text{index} \quad \mapsto \text{NextIndex}, \\ &\quad \text{isolation} \mapsto \text{isolation}, \\ &\quad \text{values} \quad \mapsto c, \\ &\quad \text{targets} \quad \mapsto \{\}, \\ &\quad \text{status} \quad \mapsto \text{TransactionInitializing}]) \\ \wedge \text{UNCHANGED } &\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{target} \rangle \end{aligned}$$

Add a rollback of transaction 't' to the transaction log

$$\begin{aligned} \text{Rollback}(t) &\triangleq \\ \wedge \exists \text{isolation} \in \{ &\text{IsolationDefault}, \text{IsolationSerializable} \} : \\ &\quad \wedge \text{transaction}' = \text{transaction} @@ (\text{NextIndex} :> [\text{type} \quad \mapsto \text{TransactionRollback}, \\ &\quad \text{index} \quad \mapsto \text{NextIndex}, \\ &\quad \text{isolation} \mapsto \text{isolation}, \\ &\quad \text{rollback} \mapsto t, \\ &\quad \text{targets} \quad \mapsto \{\}, \\ &\quad \text{status} \quad \mapsto \text{TransactionInitializing}]) \\ \wedge \text{UNCHANGED } &\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{target} \rangle \end{aligned}$$

This section models the Transaction log reconciler.

Transactions come in two flavors : – *Change* transactions contain a set of changes to be applied to a set of *targets* – *Rollback* transactions reference a prior change transaction to be reverted to the previous state

Both types of transaction are reconciled in stages:

- * Pending - waiting for prior transactions to complete
- * Validating - validating the requested changes
- * Applying - applying the changes to target configurations
- * Complete - completed applying changes successfully
- * Failed - failed applying changes

Reconcile a transaction

$\text{ReconcileTransaction}(n, i) \triangleq$

$$\begin{aligned}
& \wedge \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionInitializing} \\
& \wedge i - 1 \in \text{DOMAIN transaction} \Rightarrow \\
& \quad \text{TransactionPhase}(\text{transaction}[i - 1].\text{status}) > \text{TransactionPhase}(\text{TransactionInitializing}) \\
& \wedge \vee \wedge \text{transaction}[i].\text{targets} = \{\} \\
& \quad \wedge \vee \wedge \text{transaction}[i].\text{type} = \text{TransactionChange} \\
& \quad \quad \wedge \text{transaction}' = [\text{transaction EXCEPT ![i].targets} = \text{DOMAIN transaction}[i].\text{values}] \\
& \quad \quad \wedge \text{proposal}' = [t \in \text{DOMAIN proposal} \mapsto \text{proposal}[t] @@ \\
& \quad \quad \quad (i :> [\text{type} \mapsto \text{ProposalChange}, \\
& \quad \quad \quad \quad \text{index} \mapsto i, \\
& \quad \quad \quad \quad \text{values} \mapsto \text{transaction}[i].\text{changes}[t], \\
& \quad \quad \quad \quad \text{status} \mapsto \text{ProposalInitializing}])] \\
& \quad \vee \wedge \text{transaction}[i].\text{type} = \text{TransactionRollback} \\
& \quad \quad \wedge \vee \wedge \text{transaction}[i].\text{rollback} \in \text{DOMAIN transaction} \\
& \quad \quad \quad \wedge \text{transaction}[\text{transaction}[i].\text{rollback}].\text{type} = \text{TransactionChange} \\
& \quad \quad \quad \wedge \text{transaction}' = [\text{transaction EXCEPT ![i].targets} = \\
& \quad \quad \quad \quad \text{DOMAIN transaction}[\text{transaction}[i].\text{rollback}].\text{values}] \\
& \quad \quad \quad \wedge \text{proposal}' = [t \in \text{DOMAIN proposal} \mapsto \text{proposal}[t] @@ \\
& \quad \quad \quad \quad (i :> [\text{type} \mapsto \text{ProposalRollback}, \\
& \quad \quad \quad \quad \quad \text{index} \mapsto i, \\
& \quad \quad \quad \quad \quad \text{rollback} \mapsto \text{transaction}[i].\text{rollback}, \\
& \quad \quad \quad \quad \quad \text{status} \mapsto \text{ProposalInitializing}])] \\
& \quad \vee \wedge \vee \wedge \text{transaction}[i].\text{rollback} \in \text{DOMAIN transaction} \\
& \quad \quad \quad \wedge \text{transaction}[\text{transaction}[i].\text{rollback}].\text{type} = \text{TransactionRollback} \\
& \quad \quad \quad \vee \text{transaction}[i].\text{rollback} \notin \text{DOMAIN transaction} \\
& \quad \quad \quad \wedge \text{transaction}' = [\text{transaction EXCEPT ![i].status} = \text{TransactionFailed}] \\
& \quad \quad \quad \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \text{transaction}[i].\text{targets} \neq \{\} \\
& \quad \wedge \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \\
& \quad \quad \wedge \text{proposal}[t][i].\text{status} = \text{ProposalFailed} \\
& \quad \quad \wedge \text{transaction}' = [\text{transaction EXCEPT ![i].status} = \text{TransactionFailed}] \\
& \quad \vee \wedge \forall t \in \text{transaction}[i].\text{targets} : \\
& \quad \quad \wedge \text{proposal}[t][i].\text{status} = \text{ProposalInitialized} \\
& \quad \quad \wedge \text{transaction}' = [\text{transaction EXCEPT ![i].status} = \text{TransactionInitialized}]
\end{aligned}$$

$$\begin{aligned}
& \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionInitialized} \\
& \wedge \forall t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{proposal}[t][i].\text{prevIndex} \neq 0 \Rightarrow \\
& \quad \quad (\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{isolation} = \text{IsolationSerializable} \Rightarrow \\
& \quad \quad \quad \text{TransactionPhase}(\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{status}) \geq \\
& \quad \quad \quad \text{TransactionPhase}(\text{TransactionValidated})) \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionValidating}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionValidating} \\
& \wedge \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{ProposalPhase}(\text{proposal}[t][i].\text{status}) < \text{ProposalPhase}(\text{ProposalValidating}) \\
& \wedge \text{proposal}' = [t \in \text{DOMAIN } \text{proposal} \mapsto \\
& \quad \text{IF } t \in \text{transaction}[i].\text{targets} \text{ THEN} \\
& \quad \quad [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalValidating}] \\
& \quad \text{ELSE} \\
& \quad \quad \text{proposal}[t]] \\
& \wedge \text{UNCHANGED } \langle \text{transaction} \rangle \\
& \vee \wedge \forall t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalValidated} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionValidated}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalFailed} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionFailed}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionValidated} \\
& \wedge \forall t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{proposal}[t][i].\text{prevIndex} \neq 0 \Rightarrow \\
& \quad \quad (\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{isolation} = \text{IsolationSerializable} \Rightarrow \\
& \quad \quad \quad \text{TransactionPhase}(\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{status}) \geq \\
& \quad \quad \quad \text{TransactionPhase}(\text{TransactionCommitted})) \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionCommitting}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionCommitting} \\
& \wedge \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{ProposalPhase}(\text{proposal}[t][i].\text{status}) < \text{ProposalPhase}(\text{ProposalCommitting}) \\
& \wedge \text{proposal}' = [t \in \text{DOMAIN } \text{proposal} \mapsto \\
& \quad \text{IF } t \in \text{transaction}[i].\text{targets} \text{ THEN} \\
& \quad \quad [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalCommitting}] \\
& \quad \text{ELSE} \\
& \quad \quad \text{proposal}[t]] \\
& \wedge \text{UNCHANGED } \langle \text{transaction} \rangle \\
& \vee \wedge \forall t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalCommitted} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionCommitted}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalFailed} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionFailed}]
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
\vee & \wedge \text{transaction}[i].\text{status} = \text{TransactionCommitted} \\
& \wedge \forall t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{proposal}[t][i].\text{prevIndex} \neq 0 \Rightarrow \\
& \quad \quad (\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{isolation} = \text{IsolationSerializable} \Rightarrow \\
& \quad \quad \quad \text{TransactionPhase}(\text{transaction}[\text{proposal}[t][i].\text{prevIndex}].\text{status}) \geq \\
& \quad \quad \quad \text{TransactionPhase}(\text{TransactionApplied})) \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionApplying}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
\vee & \wedge \text{transaction}[i].\text{status} = \text{TransactionApplying} \\
& \wedge \vee \wedge \exists t \in \text{transaction}[i].\text{targets} : \\
& \quad \text{ProposalPhase}(\text{proposal}[t][i].\text{status}) < \text{ProposalPhase}(\text{ProposalApplying}) \\
& \wedge \text{proposal}' = [t \in \text{DOMAIN } \text{proposal} \mapsto \\
& \quad \text{IF } t \in \text{transaction}[i].\text{targets} \text{ THEN} \\
& \quad \quad [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalApplying}] \\
& \quad \text{ELSE} \\
& \quad \quad \text{proposal}[t]] \\
& \wedge \text{UNCHANGED } \langle \text{transaction} \rangle \\
\vee & \wedge \forall t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalApplied} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionApplied}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
\vee & \wedge \exists t \in \text{transaction}[i].\text{targets} : \text{proposal}[t][i].\text{status} = \text{ProposalFailed} \\
& \wedge \text{transaction}' = [\text{transaction} \text{ EXCEPT } ![i].\text{status} = \text{TransactionFailed}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal} \rangle \\
& \vee \wedge \text{transaction}[i].\text{status} = \text{TransactionApplied} \\
& \wedge \text{UNCHANGED } \langle \text{configuration}, \text{mastership}, \text{target} \rangle
\end{aligned}$$

Reconcile a proposal

$\text{ReconcileProposal}(n, t, i) \triangleq$

$$\begin{aligned}
& \wedge \vee \wedge \text{proposal}[t][i].\text{status} = \text{ProposalInitializing} \\
& \wedge \vee \wedge \text{configuration}[t].\text{proposedIndex} > 0 \\
& \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT} \\
& \quad \quad \quad ![i] = [\text{status} \mapsto \text{ProposalInitialized}, \\
& \quad \quad \quad \text{prevIndex} \mapsto \text{configuration}[t].\text{proposedIndex}] @@ \text{proposal}[t][i], \\
& \quad \quad \quad ![\text{configuration}[t].\text{proposedIndex}] = [\text{nextIndex} \mapsto i] @@ \\
& \quad \quad \quad \text{proposal}[t][\text{configuration}[t].\text{proposedIndex}]]] \\
& \vee \wedge \text{configuration}[t].\text{proposedIndex} = 0 \\
& \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalInitialized}]] \\
& \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{proposedIndex} = i] \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \text{proposal}[t][i].\text{status} = \text{ProposalValidating} \\
& \wedge \text{configuration}[t].\text{committedIndex} = \text{proposal}[t][i].\text{prevIndex} \\
& \wedge \vee \wedge \text{proposal}[t][i].\text{type} = \text{ProposalChange} \\
& \wedge \text{LET } \text{rollbackIndex} \triangleq \text{configuration}[t].\text{configIndex} \\
& \quad \text{rollbackValues} \triangleq [p \in \text{DOMAIN } \text{proposal}[t][i].\text{values} \mapsto [
\end{aligned}$$

$$\begin{aligned}
& p \mapsto \text{IF } p \in \text{DOMAIN configuration}[t].\text{config THEN} \\
& \quad \text{configuration}[t].\text{values}[p] \\
& \quad \text{ELSE} \\
& \quad [delete \mapsto \text{TRUE}]] \\
\text{IN } & \exists r \in \{\textit{Valid}, \textit{Invalid}\}: \\
& \quad \vee \wedge r = \textit{Valid} \\
& \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [\\
& \qquad \qquad \qquad proposal[t] \text{ EXCEPT !}[i].rollbackIndex = rollbackIndex, \\
& \qquad \qquad \qquad \qquad \qquad \! [i].rollbackValues = rollbackValues, \\
& \qquad \qquad \qquad \qquad \qquad \! [i].status = ProposalValidated]] \\
& \quad \vee \wedge r = \textit{Invalid} \\
& \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [\\
& \qquad \qquad \qquad proposal[t] \text{ EXCEPT !}[i].status = ProposalFailed]] \\
& \vee \wedge proposal[t][i].type = \textit{ProposalRollback} \\
& \quad \wedge \vee \wedge configuration[t].index = proposal[t][i].rollback \\
& \quad \wedge \vee \wedge proposal[t][proposal[t][i].rollback].type = \textit{ProposalChange} \\
& \quad \wedge \text{LET } rollbackIndex \triangleq proposal[t][proposal[t][i].rollback].rollbackIndex \\
& \quad \quad \quad rollbackValues \triangleq proposal[t][proposal[t][i].rollback].rollbackValues \\
& \quad \text{IN } \exists r \in \{\textit{Valid}, \textit{Invalid}\}: \\
& \quad \quad \vee \wedge r = \textit{Valid} \\
& \quad \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [\\
& \qquad \qquad \qquad proposal[t] \text{ EXCEPT !}[i].rollbackIndex = rollbackIndex, \\
& \qquad \qquad \qquad \qquad \qquad \! [i].rollbackValues = rollbackValues, \\
& \qquad \qquad \qquad \qquad \qquad \! [i].status = ProposalValidated]] \\
& \quad \quad \vee \wedge r = \textit{Invalid} \\
& \quad \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [\\
& \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \! [i].status = ProposalFailed]] \\
& \quad \vee \wedge proposal[t][proposal[t][i].rollback].type = \textit{ProposalRollback} \\
& \quad \wedge configuration' = [configuration \text{ EXCEPT !}[t].committedIndex = i] \\
& \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [\\
& \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \qquad \! [i].status = ProposalFailed]] \\
& \quad \vee \wedge configuration[t].index \neq proposal[t][i].rollback \\
& \quad \wedge configuration' = [configuration \text{ EXCEPT !}[t].committedIndex = i] \\
& \quad \wedge proposal' = [proposal \text{ EXCEPT !}[t] = [proposal[t] \text{ EXCEPT !}[i].status = ProposalFailed]] \\
& \wedge \text{UNCHANGED } \langle target \rangle \\
& \vee \wedge proposal[t][i].status = \textit{ProposalCommitting} \\
& \quad \wedge configuration[t].committedIndex = proposal[t][i].prevIndex \\
& \quad \wedge \vee \wedge proposal[t][i].type = \textit{ProposalChange} \\
& \quad \quad \wedge configuration' = [configuration \text{ EXCEPT !}[t].values = proposal[t][i].values, \\
& \qquad \qquad \qquad \qquad \qquad \! [t].configIndex = i, \\
& \qquad \qquad \qquad \qquad \qquad \! [t].committedIndex = i] \\
& \quad \vee \wedge proposal[t][i].type = \textit{ProposalRollback} \\
& \quad \quad \wedge configuration' = [configuration \text{ EXCEPT !}[t].values = proposal[t][i].rollbackValues, \\
& \qquad \qquad \qquad \qquad \qquad \! [t].configIndex = proposal[t][i].rollbackIndex, \\
& \qquad \qquad \qquad \qquad \qquad \! [t].committedIndex = i]
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalCommitted}]] \\
& \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
\vee & \wedge \text{proposal}[t][i].\text{status} = \text{ProposalApplying} \\
& \wedge \text{configuration}[t].\text{appliedIndex} = \text{proposal}[t][i].\text{prevIndex} \\
& \wedge \text{configuration}[t].\text{appliedTerm} = \text{mastership}[t].\text{term} \\
& \wedge \text{mastership}[t].\text{master} = n \\
& \wedge \exists r \in \{\text{Success}, \text{Failure}\} : \\
& \quad \vee \wedge r = \text{Success} \\
& \quad \quad \wedge \text{target}' = [\text{target} \text{ EXCEPT } ![t] = \text{proposal}[t][i].\text{values} @@ \text{target}[t]] \\
& \quad \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } \\
& \quad \quad \quad ![t].\text{appliedIndex} = i, \\
& \quad \quad \quad ![t].\text{appliedValues} = \text{proposal}[t][i].\text{values} @@ \text{configuration}[i].\text{appliedValues}] \\
& \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalApplied}]] \\
& \quad \vee \wedge r = \text{Failure} \\
& \quad \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{appliedIndex} = i] \\
& \quad \quad \wedge \text{proposal}' = [\text{proposal} \text{ EXCEPT } ![t] = [\text{proposal}[t] \text{ EXCEPT } ![i].\text{status} = \text{ProposalFailed}]] \\
& \wedge \text{UNCHANGED } \langle \text{transaction}, \text{mastership} \rangle
\end{aligned}$$

This section models the Configuration reconciler.

$\text{ReconcileConfiguration}(n, t) \triangleq$

$$\begin{aligned}
& \wedge \vee \wedge \text{target}[t].\text{persistent} \\
& \quad \wedge \text{configuration}[t].\text{status} \neq \text{ConfigurationPersisted} \\
& \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{status} = \text{ConfigurationPersisted}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \neg \text{target}[t].\text{persistent} \\
& \quad \wedge \text{mastership}[t].\text{term} > \text{configuration}[t].\text{term} \\
& \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{term} = \text{mastership}[t].\text{term}, \\
& \quad \quad \quad ![t].\text{status} = \text{ConfigurationSynchronizing}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \neg \text{target}[t].\text{persistent} \\
& \quad \wedge \text{configuration}[t].\text{status} \neq \text{ConfigurationUnknown} \\
& \quad \wedge \text{mastership}[t].\text{term} = \text{configuration}[t].\text{term} \\
& \quad \wedge \text{mastership}[t].\text{master} = \text{Nil} \\
& \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{status} = \text{ConfigurationUnknown}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{target} \rangle \\
& \vee \wedge \text{configuration}[t].\text{status} = \text{ConfigurationSynchronizing} \\
& \quad \wedge \text{mastership}[t].\text{master} = n \\
& \quad \wedge \text{target}' = [\text{target} \text{ EXCEPT } ![t] = \text{configuration}[t].\text{values}] \\
& \quad \wedge \text{configuration}' = [\text{configuration} \text{ EXCEPT } ![t].\text{appliedTerm} = \text{mastership}[t].\text{term}, \\
& \quad \quad \quad ![t].\text{status} = \text{ConfigurationSynchronized}] \\
& \wedge \text{UNCHANGED } \langle \text{proposal}, \text{transaction}, \text{mastership} \rangle
\end{aligned}$$

Init and next state predicates

$$\begin{aligned}
Init &\triangleq \\
&\wedge transaction = \langle \rangle \\
&\wedge proposal = [t \in \text{DOMAIN } Target \mapsto \\
&\quad [p \in \{ \} \mapsto [status \mapsto ProposalInitializing]]] \\
&\wedge configuration = [t \in \text{DOMAIN } Target \mapsto \\
&\quad [target \mapsto t, \\
&\quad \quad status \mapsto ConfigurationUnknown, \\
&\quad \quad values \mapsto \\
&\quad \quad \quad [path \in \{ \} \mapsto \\
&\quad \quad \quad \quad [path \mapsto path, \\
&\quad \quad \quad \quad \quad value \mapsto Nil, \\
&\quad \quad \quad \quad \quad index \mapsto 0, \\
&\quad \quad \quad \quad \quad deleted \mapsto FALSE]], \\
&\quad \quad configIndex \mapsto 0, \\
&\quad \quad proposedIndex \mapsto 0, \\
&\quad \quad committedIndex \mapsto 0, \\
&\quad \quad appliedIndex \mapsto 0, \\
&\quad \quad appliedTerm \mapsto 0, \\
&\quad \quad appliedValues \mapsto \\
&\quad \quad \quad [path \in \{ \} \mapsto \\
&\quad \quad \quad \quad [path \mapsto path, \\
&\quad \quad \quad \quad \quad value \mapsto Nil, \\
&\quad \quad \quad \quad \quad index \mapsto 0, \\
&\quad \quad \quad \quad \quad deleted \mapsto FALSE]]]] \\
&\wedge target = [t \in \text{DOMAIN } Target \mapsto \\
&\quad [path \in \{ \} \mapsto \\
&\quad \quad [value \mapsto Nil]]] \\
&\wedge mastership = [t \in \text{DOMAIN } Target \mapsto [master \mapsto Nil, term \mapsto 0]] \\
Next &\triangleq \\
&\vee \exists c \in ValidChanges : \\
&\quad Change(c) \\
&\vee \exists t \in \text{DOMAIN } transaction : \\
&\quad Rollback(t) \\
&\vee \exists n \in Node : \\
&\quad \exists t \in \text{DOMAIN } Target : \\
&\quad \quad SetMaster(n, t) \\
&\vee \exists t \in \text{DOMAIN } Target : \\
&\quad \quad UnsetMaster(t) \\
&\vee \exists n \in Node : \\
&\quad \exists t \in \text{DOMAIN } transaction : \\
&\quad \quad ReconcileTransaction(n, t) \\
&\vee \exists n \in Node : \\
&\quad \exists c \in \text{DOMAIN } configuration :
\end{aligned}$$

ReconcileConfiguration(*n*, *c*)

Spec \triangleq *Init* \wedge $\Box[Next]_{vars}$

Order \triangleq TRUE *TODO* redefine order spec

THEOREM *Safety* \triangleq *Spec* \Rightarrow $\Box Order$

Completion \triangleq $\forall i \in \text{DOMAIN } transaction :$
 $transaction[i].status \in \{TransactionApplied, TransactionFailed\}$

THEOREM *Liveness* \triangleq *Spec* \Rightarrow $\Diamond Completion$

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