```
— Module Transaction -
INSTANCE Naturals
INSTANCE FiniteSets
Instance Sequences
INSTANCE TLC
 An empty constant
Constant Nil
 {\bf Transaction\ type\ constants}
CONSTANTS
   Change,
   Rollback
Type \triangleq \{Change, Rollback\}
 Proposal phase constants
CONSTANTS
   Commit,
   Apply
 Status constants
CONSTANTS
   Pending,
   InProgress,
   Complete,
   Aborted,
   Failed
Status \ \triangleq \ \{Pending, InProgress, \ Complete, \ Aborted, \ Failed\}
Done \triangleq \{Complete, Aborted, Failed\}
 The set of all nodes
CONSTANT Node
Empty \stackrel{\triangle}{=} [p \in \{\} \mapsto Nil]
 Variables defined by other modules.
VARIABLES
   proposal,
   configuration\\
```

```
A transaction log. Transactions may either request a set
 of changes to a set of targets or rollback a prior change.
Variable transaction
TypeOK \triangleq
   \forall i \in \text{DOMAIN} \ transaction:
      \land transaction[i].type \in Type
      \land transaction[i].index \in Nat
      \land transaction[i].init \in Status
      \land transaction[i].commit \in Status
      \land transaction[i].apply \in Status
      \land \forall p \in \text{DOMAIN} \ transaction[i].values:
           transaction[i].values[p] \neq Nil \Rightarrow transaction[i].values[p] \in STRING
LOCAL CurrState \triangleq [
    transactions \mapsto [i \in DOMAIN \ transaction \mapsto transaction[i] @@ [ordinal \mapsto i]],
                  \mapsto [i \in DOMAIN \ proposal \mapsto proposal[i] @@ [ordinal \mapsto i]],
   configuration \mapsto configuration]
LOCAL SuccState \triangleq
   LET
       transactions \stackrel{\triangle}{=} \{i \in DOMAIN \ transaction' : \}
                                  i \in \text{DOMAIN } transaction \Rightarrow transaction'[i] \neq transaction[i]
                         \stackrel{\Delta}{=} \{i \in \text{DOMAIN } proposal' : 
       proposals
                                  i \in \text{DOMAIN } proposal \Rightarrow proposal'[i] \neq proposal[i]
   IN
      [transactions \mapsto [i \in transactions \mapsto transaction'[i] @@[ordinal \mapsto i]],
                     \mapsto [i \in proposals \mapsto proposal'[i] @@[ordinal \mapsto i]]]
Test \stackrel{\triangle}{=} INSTANCE \ Test \ WITH
    File \leftarrow "Transaction.log"
```

This section models configuration changes and rollbacks. Changes are appended to the transaction log and processed asynchronously.

```
Add a set of changes 'c' to the transaction log RequestChange(p, v) \stackrel{\triangle}{=} \\ \wedge transaction' = Append(transaction, [\\ type \mapsto Change, \\ index \mapsto 0, \\ values \mapsto (p:>v), \\ init \mapsto InProgress, \\ commit \mapsto Pending, \\ apply \mapsto Pending]) \\ \wedge \text{UNCHANGED } \langle proposal, configuration \rangle
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Add a rollback of transaction 't' to the transaction log
RequestRollback(i) \triangleq
    \land transaction' = Append(transaction, [
                                       \mapsto Rollback,
                             type
                             index
                                       \mapsto i,
                             values \mapsto Empty,
                             init
                                       \mapsto InProgress,
                             commit \mapsto Pending,
                             apply \mapsto Pending
    \land UNCHANGED \langle proposal, configuration \rangle
This section models the Transaction log reconciler.
LOCAL IsInitialized(i) \stackrel{\triangle}{=}
   i \in \text{DOMAIN} \ transaction \Rightarrow transaction[i].init \in Done
LOCAL IsCommitted(i) \triangleq
   i \in \text{DOMAIN } transaction \Rightarrow transaction[i].commit \in Done
LOCAL IsApplied(i) \stackrel{\Delta}{=}
   i \in \text{DOMAIN } transaction \Rightarrow transaction[i].apply \in Done
InitChange(n, i) \triangleq
    \land \lor \land transaction[i].init = InProgress
           If the prior transaction has been initialized, initialize the transaction by
           appending the proposal and updating the transaction index.
          \wedge IsInitialized(i-1)
          \land proposal' = Append(proposal, [
                                change \mapsto [
                                   phase \mapsto Commit,
                                   state \mapsto Pending,
                                   values \mapsto [
                                       p \in \text{DOMAIN } transaction[i].values \mapsto [
                                          index \mapsto Len(proposal) + 1,
                                          value \mapsto transaction[i].values[p]]]],
                                rollback \mapsto [
                                   phase
                                               \mapsto Nil,
                                   state
                                               \mapsto Nil,
                                   revision \mapsto 0,
                                   values
                                              \mapsto Empty]])
          \land transaction' = [transaction \ EXCEPT \ ![i].index = Len(proposal'),
                                                           ![i].init = Complete]
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CommitChange(n, i) \triangleq
   \land \ \lor \ \land transaction[i].commit = Pending
         \land transaction[i].init = Complete
          A transaction cannot be committed until the prior transaction has been committed.
         \wedge IsCommitted(i-1)
         \land transaction' = [transaction \ EXCEPT \ ![i].commit = InProgress]
         \land UNCHANGED \langle proposal \rangle
       \lor \land transaction[i].commit = InProgress
         \land proposal[transaction[i].index].change.phase = Commit
             If the change commit is still in the Pending state, set it to InProgress.
         \land \lor \land proposal[transaction[i].index].change.state = Pending
               \land proposal' = [proposal \ EXCEPT \ ![transaction[i].index].change.state]
                                                                                                     = InProgress,
                                                      ![transaction[i].index].rollback.revision = configuration.commit
                                                      ![transaction[i].index].rollback.values
                                                          p \in DOMAIN \ proposal[transaction[i].index].change.values \mapsto
                                                            IF p \in DOMAIN configuration.committed.values THEN
                                                                configuration.committed.values[p]
                                                                [index \mapsto 0, value \mapsto Nil]]]
               \land UNCHANGED \langle transaction \rangle
             If the change commit is Complete, mark the transaction Complete.
             \lor \land proposal[transaction[i].index].change.state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].commit = Complete]
               \land UNCHANGED \langle proposal \rangle
             If the change commit Failed, mark the transaction Failed.
             \lor \land proposal[transaction[i].index].change.state = Failed
               \land transaction' = [transaction \ EXCEPT \ ![i].commit = Failed]
               \land UNCHANGED \langle proposal \rangle
ApplyChange(n, i) \stackrel{\Delta}{=}
   \land \lor \land transaction[i].apply = Pending
             If the commit phase was completed successfully, start the apply phase.
         \land \lor \land transaction[i].commit = Complete
                   If the proposal is not in the apply phase, update the proposal phase.
               \land \lor \land proposal[transaction[i].index].change.phase \neq Apply
                     \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].change.phase = Apply,
                                                            ![transaction[i].index].change.state = Pending]
                     \land UNCHANGED \langle transaction \rangle
                   If the proposal is in the apply phase and the previous transaction has completed
                   the apply phase, start applying the change.
                   \lor \land proposal[transaction[i].index].change.phase = Apply
                     \land proposal[transaction[i].index].change.state = Pending
                      A transaction cannot be applied until the prior transaction has been applied.
                     \wedge IsApplied(i-1)
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new changes can be applied.
                     \land \land transaction[i].index - 1 \in DOMAIN proposal
                        \land proposal[transaction[i].index - 1].change.phase = Apply
                        \land proposal[transaction[i].index - 1].change.state = Failed
                        \Rightarrow \land proposal[transaction[i].index - 1].rollback.phase = Apply
                            \land proposal[transaction[i].index - 1].rollback.state = Complete
                     \land transaction' = [transaction \ EXCEPT \ ![i].apply = InProgress]
                     \land UNCHANGED \langle proposal \rangle
             If the commit phase was aborted or failed, abort the apply phase once the previous
             transaction has completed the apply phase.
            \lor \land transaction[i].commit \in \{Aborted, Failed\}
                A transaction cannot be applied until the prior transaction has been applied.
               \wedge IsApplied(i-1)
                If the prior change failed being applied, it must be rolled back before
                new changes can be applied.
               \land \land transaction[i].index - 1 \in domain proposal
                  \land proposal[transaction[i].index - 1].change.phase = Apply
                  \land proposal[transaction[i].index - 1].change.state = Failed
                  \Rightarrow \land proposal[transaction[i].index - 1].rollback.phase = Apply
                      \land proposal[transaction[i].index - 1].rollback.state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].apply = Aborted]
               \land UNCHANGED \langle proposal \rangle
      \lor \land transaction[i].apply = InProgress
         \land proposal[transaction[i].index].change.phase = Apply
             If the change apply is still in the Pending state, set it to InProgress.
         \land \lor \land proposal[transaction[i].index].change.state = Pending
               \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].change.state = InProgress]
               \land UNCHANGED \langle transaction \rangle
             If the change apply is Complete, mark the transaction Complete.
            \lor \land proposal[transaction[i].index].change.state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].apply = Complete]
               \land UNCHANGED \langle proposal \rangle
             If the change apply Failed, mark the transaction Failed.
            \lor \land proposal[transaction[i].index].change.state = Failed
               \land transaction' = [transaction \ EXCEPT \ ![i].apply = Failed]
               \land UNCHANGED \langle proposal \rangle
ReconcileChange(n, i) \triangleq
   \land transaction[i].type = Change
   \land \lor InitChange(n, i)
      \vee CommitChange(n, i)
      \vee ApplyChange(n, i)
```

If the prior change failed being applied, it must be rolled back before

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InitRollback(n, i) \triangleq
   \land \lor \land transaction[i].init = InProgress
           Rollbacks cannot be initialized until all prior transactions have been initialized.
          \land IsInitialized(i-1)
              Rollback transactions must target valid proposal index.
          \land \lor \land transaction[i].index \in DOMAIN proposal
                    To roll back a transaction, all subsequent transactions must be rolled back first.
                    Check whether the following proposal is being rolled back.
                \land \lor \land transaction[i].index + 1 \in DOMAIN \ proposal \Rightarrow
                           proposal[transaction[i].index + 1].rollback.phase \neq Nil
                      \land transaction' = [transaction \ EXCEPT \ ![i].init = Complete]
                    If the subsequent proposal is not being rolled back, fail the rollback transaction.
                   \lor \land transaction[i].index + 1 \in DOMAIN proposal
                      \land proposal[transaction[i].index + 1].rollback.phase = Nil
                      \land transaction' = [transaction \ EXCEPT \ ![i].init = Failed]
             If the rollback index is not a valid proposal index, fail the rollback request.
             \lor \land transaction[i].index \notin DOMAIN proposal
                \land transaction' = [transaction \ EXCEPT \ ![i].init = Failed]
   \land UNCHANGED \langle proposal \rangle
CommitRollback(n, i) \triangleq
    \land \lor \land transaction[i].commit = Pending
           A transaction cannot be committed until the prior transaction has been committed.
           In the case of rollbacks, we serialize all state changes to ensure consistency
           when rolling back changes.
          \wedge IsCommitted(i-1)
             If the transaction was initialized successfully, commit the rollback.
          \land \lor \land transaction[i].init = Complete
                    If the target proposal is not yet being rolled back, transition the proposal.
                \land \lor \land proposal[transaction[i].index].rollback.phase = Nil
                          Update the proposal's rollback state based on its change state.
                      \land \lor \land proposal[transaction[i].index].change.phase = Commit
                                If the target change is still pending, abort the change and rollback.
                            \land \lor \land proposal[transaction[i].index].change.state = Pending
                                  \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].change.state = Aborted,
                                                                         ![transaction[i].index].rollback.phase = Commit
                                                                         ![transaction[i].index].rollback.state = Aborted]
                                  \land UNCHANGED \langle transaction \rangle
                                If the target change is complete, start the rollback commit phase.
                                 \land proposal[transaction[i].index].change.state = Complete
                                  \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].rollback.phase = Commit.
                                                                         ![transaction[i].index].rollback.state = Pending
                                  \land UNCHANGED \langle transaction \rangle
```

If the target change failed commit, complete the rollback commit.

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\lor \land proposal[transaction[i].index].change.state \in \{Aborted, Failed\}
                                 \land transaction' = [transaction \ EXCEPT \ ![i].commit = Complete]
                                 \land UNCHANGED \langle proposal \rangle
                         If the target change is in the Apply phasee, commit the rollback.
                        \lor \land proposal[transaction[i].index].change.phase = Apply
                           \land proposal' = [proposal \ EXCEPT \ ![transaction[i].index].rollback.phase = Commit,
                                                                  ![transaction[i].index].rollback.state = Pending]
                           ∧ UNCHANGED ⟨transaction⟩
                   If the target rollback is being committed, transition the underlying proposal.
                  \lor \land proposal[transaction[i].index].rollback.phase = Commit
                         If the target proposal is being rolled back, begin the rollback commit
                         once the prior transaction has completed the commit phase.
                     \land \lor \land proposal[transaction[i].index].rollback.state = Pending
                           \land transaction' = [transaction \ EXCEPT \ ![i].commit = InProgress]
                           \land UNCHANGED \langle proposal \rangle
                         If the target rollback was aborted, abort the transaction rollback
                         once the prior transaction has completed the commit phase.
                        \lor \land proposal[transaction[i].index].rollback.state = Aborted
                           \land transaction' = [transaction \ EXCEPT \ ![i].commit = Aborted]
                           \land UNCHANGED \langle proposal \rangle
             If the transaction failed initialization, abort the commit phase.
            \lor \land transaction[i].init \in \{Aborted, Failed\}
               \land transaction' = [transaction \ EXCEPT \ ![i].commit = Aborted]
               \land UNCHANGED \langle proposal \rangle
      \lor \land transaction[i].commit = InProgress
         \land proposal[transaction[i].index].rollback.phase = Commit
             If the rollback commit is still in the Pending state, set it to InProgress.
         \land \lor \land proposal[transaction[i].index].rollback.state = Pending
               \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].rollback.state = InProgress]
               \land UNCHANGED \langle transaction \rangle
             If the rollback commit is Complete, mark the transaction Complete.
            \lor \land proposal[transaction[i].index].rollback.state = Complete
               \land transaction' = [transaction \ EXCEPT \ ![i].commit = Complete]
               \land UNCHANGED \langle proposal \rangle
             If the rollback commit Failed, mark the transaction Failed.
            \lor \land proposal[transaction[i].index].rollback.state = Failed
               \land transaction' = [transaction \ EXCEPT \ ![i].commit = Failed]
               \land UNCHANGED \langle proposal \rangle
ApplyRollback(n, i) \triangleq
   \land \lor \land transaction[i].apply = Pending
          A transaction cannot be applied until the prior transaction has been applied.
          In the case of rollbacks, we serialize all state changes to ensure consistency
          when rolling back changes.
```

```
\wedge IsApplied(i-1)
      If the commit phase was completed successfully, start the apply phase.
  \land \lor \land transaction[i].commit = Complete
            If the target rollback is not yet being applied, transition the rollback.
        \land \lor \land proposal[transaction[i].index].rollback.phase = Commit
                  Update the proposal's rollback state based on its change state.
              \land \lor \land proposal[transaction[i].index].change.phase = Apply
                        If the target change is still pending, abort the change and rollback.
                    \land \lor \land proposal[transaction[i].index].change.state = Pending
                           \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].change.state = Aborted,
                                                                 ![transaction[i].index].rollback.phase = Apply,
                                                                 ![transaction[i].index].rollback.state = Aborted]
                           \land UNCHANGED \langle transaction \rangle
                        If the target change is complete, start the rollback apply phase.
                       \lor \land proposal[transaction[i].index].change.state = Complete
                           \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].rollback.phase = Apply,
                                                                 ![transaction[i].index].rollback.state = Pending
                           \land UNCHANGED \langle transaction \rangle
                        If the target change failed apply, complete the rollback apply.
                       \lor \land proposal[transaction[i].index].change.state \in \{Aborted, Failed\}
                           \land transaction' = [transaction \ EXCEPT \ ![i].apply = Complete]
                           \land UNCHANGED \langle proposal \rangle
                  If the target change is in the Commit phase, abort the change and rollback.
                 \lor \land proposal[transaction[i].index].change.phase = Commit
                    \land proposal' = [proposal \ EXCEPT \ ![transaction[i].index].change.state = Aborted,
                                                           ![transaction[i].index].rollback.phase = Apply,
                                                           ![transaction[i].index].rollback.state = Aborted]
                    \land UNCHANGED \langle transaction \rangle
            If the target rollback is being applied, transition the underlying proposal.
           \lor \land proposal[transaction[i].index].rollback.phase = Apply
                  If the target proposal is being rolled back, begin the rollback apply
                  once the prior transaction has completed the apply phase.
              \land \lor \land proposal[transaction[i].index].rollback.state
                    \land transaction' = [transaction \ EXCEPT \ ![i].apply = InProgress]
                    \land UNCHANGED \langle proposal \rangle
                  If the target rollback was aborted, abort the transaction rollback
                  once the prior transaction has completed the apply phase.
                 \lor \land proposal[transaction[i].index].rollback.state
                    \land transaction' = [transaction \ EXCEPT \ ![i].apply = Aborted]
                    \land UNCHANGED \langle proposal \rangle
      If the transaction failed initialization, abort the apply phase.
      \lor \land transaction[i].init \in \{Aborted, Failed\}
        \land transaction' = [transaction \ EXCEPT \ ![i].apply = Aborted]
        \land UNCHANGED \langle proposal \rangle
\lor \land transaction[i].apply = InProgress
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```
\land proposal[transaction[i].index].rollback.phase = Apply
              If the rollback apply is still in the Pending state, set it to InProgress.
          \land \lor \land proposal[transaction[i].index].rollback.state = Pending
                \land proposal' = [proposal \ EXCEPT \ ! [transaction[i].index].rollback.state = InProgress]
                \land UNCHANGED \langle transaction \rangle
              If the rollback apply is Complete, mark the transaction Complete.
             \lor \land proposal[transaction[i].index].rollback.state = Complete
                \land transaction' = [transaction \ EXCEPT \ ![i].apply = Complete]
                \land UNCHANGED \langle proposal \rangle
              If the rollback apply Failed, mark the transaction Failed.
             \lor \land proposal[transaction[i].index].rollback.state
                \land transaction' = [transaction \ EXCEPT \ ![i].apply = Failed]
                \land UNCHANGED \langle proposal \rangle
ReconcileRollback(n, i) \triangleq
   \land transaction[i].type = Rollback
   \wedge \vee InitRollback(n, i)
       \vee CommitRollback(n, i)
       \vee ApplyRollback(n, i)
 Reconcile a transaction
ReconcileTransaction(n, i) \triangleq
   \land i \in \text{DOMAIN} \ transaction
   \land \lor ReconcileChange(n, i)
       \vee ReconcileRollback(n, i)
   \land UNCHANGED \langle configuration \rangle
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