
MODULE *Config*

EXTENDS

Northbound,
Proposal,
Configuration,
Mastership,
Southbound

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

LOCAL INSTANCE *TLC*

vars \triangleq $\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{target} \rangle$

Formal specification, constraints, and theorems.

Init \triangleq

\wedge *InitNorthbound*
 \wedge *InitProposal*
 \wedge *InitConfiguration*
 \wedge *InitMastership*
 \wedge *InitSouthbound*

Next \triangleq

$\vee \wedge$ *NextNorthbound*
 \wedge UNCHANGED $\langle \rangle$
 $\vee \wedge$ *NextProposal*
 \wedge UNCHANGED $\langle \rangle$
 $\vee \wedge$ *NextConfiguration*
 \wedge UNCHANGED $\langle \text{proposal} \rangle$
 $\vee \wedge$ *NextMastership*
 \wedge UNCHANGED $\langle \text{proposal}, \text{configuration} \rangle$
 $\vee \wedge$ *NextSouthbound*
 \wedge UNCHANGED $\langle \text{proposal}, \text{configuration}, \text{mastership} \rangle$

Spec \triangleq *Init* \wedge $\Box [Next]_{vars} \wedge \text{WF}_{vars}(Next)$

Order \triangleq

$\forall i \in \text{DOMAIN } \text{proposal} :$
 $\wedge \wedge \text{proposal}[i].\text{phase} = \text{ProposalCommit}$
 $\wedge \text{proposal}[i].\text{state} = \text{ProposalInProgress}$
 $\Rightarrow \neg \exists j \in \text{DOMAIN } \text{proposal} :$

$$\begin{aligned}
& \wedge j > i \\
& \wedge \text{proposal}[j].\text{phase} = \text{ProposalCommit} \\
& \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete} \\
& \wedge \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \wedge \text{proposal}[i].\text{state} = \text{ProposalInProgress} \\
& \Rightarrow \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \wedge j > i \\
& \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \\
& \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}
\end{aligned}$$

Consistency \triangleq

LET

Compute the transaction indexes that have been applied to the target

$$\begin{aligned}
\text{targetIndexes} & \triangleq \{i \in \text{DOMAIN } \text{proposal} : \\
& \quad \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \quad \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete} \\
& \quad \wedge \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \quad \wedge j > i \\
& \quad \quad \wedge \text{proposal}[j].\text{type} = \text{ProposalRollback} \\
& \quad \quad \wedge \text{proposal}[j].\text{rollback.index} = i \\
& \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \\
& \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}\}
\end{aligned}$$

Compute the set of paths in the target that have been updated by transactions

$$\text{appliedPaths} \triangleq \text{UNION } \{\text{DOMAIN } \text{proposal}[i].\text{change.values} : i \in \text{targetIndexes}\}$$

Compute the highest index applied to the target for each path

$$\begin{aligned}
\text{pathIndexes} & \triangleq [p \in \text{appliedPaths} \mapsto \text{CHOOSE } i \in \text{targetIndexes} : \\
& \quad \forall j \in \text{targetIndexes} : \\
& \quad \quad \wedge i \geq j \\
& \quad \quad \wedge p \in \text{DOMAIN } \text{proposal}[i].\text{change.values}]
\end{aligned}$$

Compute the expected target configuration based on the last indexes applied to the target for each path.

$$\text{expectedConfig} \triangleq [p \in \text{DOMAIN } \text{pathIndexes} \mapsto \text{proposal}[\text{pathIndexes}[p]].\text{change.values}[p]]$$

IN

$$\text{target} = \text{expectedConfig}$$

$$\text{Safety} \triangleq \Box(\text{Order} \wedge \text{Consistency})$$

THEOREM $\text{Spec} \Rightarrow \text{Safety}$

$$\text{Terminated}(i) \triangleq$$

$$\begin{aligned}
& \wedge i \in \text{DOMAIN } \text{proposal} \\
& \wedge \vee \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \quad \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete} \\
& \vee \text{proposal}[i].\text{state} = \text{ProposalFailed}
\end{aligned}$$

$$\text{Termination} \triangleq$$

$\forall i \in 1 \dots \text{Len}(\text{proposal}) :$
 $\text{Terminated}(i)$

$\text{Liveness} \triangleq \Diamond \text{Termination}$

THEOREM $\text{Spec} \Rightarrow \text{Liveness}$

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