
MODULE *Config*

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

INSTANCE *TLC*

GenerateTestCases \triangleq TRUE

Nil \triangleq "<nil>"

Change \triangleq "Change"

Rollback \triangleq "Rollback"

Commit \triangleq "Commit"

Apply \triangleq "Apply"

Pending \triangleq "Pending"

InProgress \triangleq "InProgress"

Complete \triangleq "Complete"

Aborted \triangleq "Aborted"

Canceled \triangleq "Canceled"

Failed \triangleq "Failed"

Node \triangleq {"node1"}

NumTransactions \triangleq 3

NumTerms \triangleq 1

NumConns \triangleq 1

NumStarts \triangleq 1

Path \triangleq {"path1"}

Value \triangleq {"value1", "value2"}

A transaction log.

VARIABLE *transactions*

A record of per-target configurations

VARIABLE *configuration*

A record of target masterhips

VARIABLE *mastership*

A record of node connections to the target

VARIABLE *conn*

The target state

VARIABLE *target*

A sequence of state changes used for model checking.

VARIABLE *history*

$vars \triangleq \langle transactions, configuration, mastership, conn, target, history \rangle$

LOCAL *Transaction* \triangleq INSTANCE *Transaction*

LOCAL *Configuration* \triangleq INSTANCE *Configuration*

LOCAL *Mastership* \triangleq INSTANCE *Mastership*

LOCAL *Target* \triangleq INSTANCE *Target*

$AppendChange(i) \triangleq$
 $\wedge Transaction!AppendChange(i)$

$RollbackChange(i) \triangleq$
 $\wedge Transaction!RollbackChange(i)$

$ReconcileTransaction(n, i) \triangleq$
 $\wedge i \in \text{DOMAIN } transactions$
 $\wedge \vee \wedge Transaction!ReconcileTransaction(n, i)$
 $\wedge GenerateTestCases \Rightarrow Transaction!Test!Log([node \mapsto n, index \mapsto i])$
 $\vee \wedge GenerateTestCases$
 $\wedge \neg \text{ENABLED } Transaction!ReconcileTransaction(n, i)$
 $\wedge \text{UNCHANGED } vars$
 $\wedge Transaction!Test!Log([node \mapsto n, index \mapsto i])$

$ReconcileConfiguration(n) \triangleq$
 $\vee \wedge Configuration!ReconcileConfiguration(n)$
 $\wedge \text{UNCHANGED } \langle transactions, history \rangle$
 $\wedge GenerateTestCases \Rightarrow Configuration!Test!Log([node \mapsto n])$
 $\vee \wedge GenerateTestCases$
 $\wedge \neg \text{ENABLED } Configuration!ReconcileConfiguration(n)$
 $\wedge \text{UNCHANGED } vars$
 $\wedge Configuration!Test!Log([node \mapsto n])$

$ReconcileMastership(n) \triangleq$
 $\vee \wedge Mastership!ReconcileMastership(n)$
 $\wedge \text{UNCHANGED } \langle transactions, configuration, target, history \rangle$

$$\begin{aligned}
& \wedge \text{GenerateTestCases} \Rightarrow \text{Mastership!Test!Log}([node \mapsto n]) \\
\vee & \wedge \text{GenerateTestCases} \\
& \wedge \neg \text{ENABLED Mastership!ReconcileMastership}(n) \\
& \wedge \text{UNCHANGED vars} \\
& \wedge \text{Mastership!Test!Log}([node \mapsto n]) \\
\text{ConnectNode}(n) & \triangleq \\
& \wedge \text{Target!Connect}(n) \\
& \wedge \text{UNCHANGED } \langle \text{transactions}, \text{configuration}, \text{mastership}, \text{history} \rangle \\
\text{DisconnectNode}(n) & \triangleq \\
& \wedge \text{Target!Disconnect}(n) \\
& \wedge \text{UNCHANGED } \langle \text{transactions}, \text{configuration}, \text{mastership}, \text{history} \rangle \\
\text{StartTarget} & \triangleq \\
& \wedge \text{Target!Start} \\
& \wedge \text{UNCHANGED } \langle \text{transactions}, \text{configuration}, \text{mastership}, \text{history} \rangle \\
\text{StopTarget} & \triangleq \\
& \wedge \text{Target!Stop} \\
& \wedge \text{UNCHANGED } \langle \text{transactions}, \text{configuration}, \text{mastership}, \text{history} \rangle
\end{aligned}$$

Formal specification, constraints, and theorems.

$$\begin{aligned}
\text{Init} & \triangleq \\
& \wedge \text{transactions} = [\\
& \quad i \in \{\} \mapsto [\\
& \quad \quad \text{phase} \mapsto \text{Nil}, \\
& \quad \quad \text{values} \mapsto [\\
& \quad \quad \quad p \in \{\} \mapsto \text{Nil}], \\
& \quad \quad \text{change} \mapsto [\\
& \quad \quad \quad \text{commit} \mapsto \text{Nil}, \\
& \quad \quad \quad \text{apply} \mapsto \text{Nil}], \\
& \quad \quad \text{rollback} \mapsto [\\
& \quad \quad \quad \text{commit} \mapsto \text{Nil}, \\
& \quad \quad \quad \text{apply} \mapsto \text{Nil}]]] \\
& \wedge \text{configuration} = [\\
& \quad \text{state} \mapsto \text{Pending}, \\
& \quad \text{term} \mapsto 0, \\
& \quad \text{committed} \mapsto [\\
& \quad \quad \text{index} \mapsto 0, \\
& \quad \quad \text{change} \mapsto 0, \\
& \quad \quad \text{target} \mapsto 0, \\
& \quad \quad \text{ordinal} \mapsto 0, \\
& \quad \quad \text{revision} \mapsto 0, \\
& \quad \quad \text{values} \mapsto [
\end{aligned}$$

$$\begin{aligned}
& p \in \{\} \mapsto Nil]], \\
& applied \mapsto [\\
& \quad index \mapsto 0, \\
& \quad target \mapsto 0, \\
& \quad ordinal \mapsto 0, \\
& \quad revision \mapsto 0, \\
& \quad values \mapsto [\\
& \quad \quad p \in \{\} \mapsto Nil]]] \\
& \wedge target = [\\
& \quad id \mapsto 1, \\
& \quad running \mapsto TRUE, \\
& \quad values \mapsto [\\
& \quad \quad p \in \{\} \mapsto [\\
& \quad \quad \quad index \mapsto 0, \\
& \quad \quad \quad value \mapsto Nil]]] \\
& \wedge mastership = [\\
& \quad master \mapsto \text{CHOOSE } n \in Node : TRUE, \\
& \quad term \mapsto 1, \\
& \quad conn \mapsto 1] \\
& \wedge conn = [\\
& \quad n \in Node \mapsto [\\
& \quad \quad id \mapsto 1, \\
& \quad \quad connected \mapsto TRUE]] \\
& \wedge history = \langle \rangle \\
Next & \triangleq \\
& \vee \exists i \in 1 \dots NumTransactions : \\
& \quad \vee AppendChange(i) \\
& \quad \vee RollbackChange(i) \\
& \vee \exists n \in Node, i \in 1 \dots NumTransactions : \\
& \quad ReconcileTransaction(n, i) \\
& \vee \exists n \in Node : \\
& \quad ReconcileConfiguration(n) \\
& \vee \exists n \in Node : \\
& \quad ReconcileMastership(n) \\
& \vee \exists n \in Node : \\
& \quad \vee ConnectNode(n) \\
& \quad \vee DisconnectNode(n) \\
& \vee StartTarget \\
& \vee StopTarget \\
Spec & \triangleq \\
& \wedge Init \\
& \wedge \Box [Next]_{vars} \\
& \wedge \forall i \in 1 \dots NumTransactions :
\end{aligned}$$

$$\begin{aligned}
& \text{WF}_{\langle \text{transactions} \rangle}(\text{Transaction!RollbackChange}(i)) \\
& \wedge \forall n \in \text{Node}, i \in 1 \dots \text{NumTransactions} : \\
& \quad \text{WF}_{\langle \text{transactions}, \text{configuration}, \text{mastership}, \text{conn}, \text{target}, \text{history} \rangle}(\text{Transaction!ReconcileTransaction}(n, i)) \\
& \wedge \forall n \in \text{Node} : \\
& \quad \text{WF}_{\langle \text{configuration}, \text{mastership}, \text{conn}, \text{target} \rangle}(\text{Configuration!ReconcileConfiguration}(n)) \\
& \wedge \forall n \in \text{Node} : \\
& \quad \text{WF}_{\langle \text{mastership}, \text{conn} \rangle}(\text{Mastership!ReconcileMastership}(n)) \\
& \wedge \forall n \in \text{Node} : \\
& \quad \text{WF}_{\langle \text{conn}, \text{target} \rangle}(\text{Target!Connect}(n) \vee \text{Target!Disconnect}(n)) \\
& \wedge \text{WF}_{\langle \text{conn}, \text{target} \rangle}(\text{Target!Start} \vee \text{Target!Stop})
\end{aligned}$$

$$\begin{aligned}
\text{LimitTerms} & \triangleq \\
& \vee \text{mastership.term} < \text{NumTerms} \\
& \vee \wedge \text{mastership.term} = \text{NumTerms} \\
& \quad \wedge \text{mastership.master} \neq \text{Nil}
\end{aligned}$$

$$\begin{aligned}
\text{LimitConns} & \triangleq \\
& \forall n \in \text{DOMAIN conn} : \\
& \quad \vee \text{conn}[n].\text{id} < \text{NumConns} \\
& \quad \vee \wedge \text{conn}[n].\text{id} = \text{NumConns} \\
& \quad \quad \wedge \text{conn}[n].\text{connected}
\end{aligned}$$

$$\begin{aligned}
\text{LimitStarts} & \triangleq \\
& \vee \text{target.id} < 2 \\
& \vee \wedge \text{target.id} = 2 \\
& \quad \wedge \text{target.running}
\end{aligned}$$

$$\begin{aligned}
\text{TypeOK} & \triangleq \\
& \wedge \text{Transaction!TypeOK} \\
& \wedge \text{Configuration!TypeOK} \\
& \wedge \text{Mastership!TypeOK}
\end{aligned}$$

$$\begin{aligned}
\text{StatusCommitted}(i) & \triangleq \\
& \wedge \text{Len}(\text{history}) = \text{Len}(\text{history}') \\
& \wedge \vee \wedge \text{transactions}'[i].\text{change.commit} \notin \{\text{Pending}, \text{Canceled}\} \\
& \quad \wedge \text{transactions}[i].\text{change.commit} \neq \text{transactions}'[i].\text{change.commit} \\
& \vee \wedge \text{transactions}'[i].\text{rollback.commit} \notin \{\text{Pending}, \text{Canceled}\} \\
& \quad \wedge \text{transactions}[i].\text{rollback.commit} \neq \text{transactions}'[i].\text{rollback.commit}
\end{aligned}$$

$$\begin{aligned}
\text{StatusApplied}(i) & \triangleq \\
& \wedge \text{Len}(\text{history}) = \text{Len}(\text{history}') \\
& \wedge \vee \wedge \text{transactions}'[i].\text{change.apply} \notin \{\text{Pending}, \text{Canceled}, \text{Aborted}\} \\
& \quad \wedge \text{transactions}[i].\text{change.apply} \neq \text{transactions}'[i].\text{change.apply}
\end{aligned}$$

$$\begin{aligned} & \vee \wedge \text{transactions}'[i].\text{rollback.apply} \notin \{\text{Pending}, \text{Canceled}, \text{Aborted}\} \\ & \wedge \text{transactions}[i].\text{rollback.apply} \neq \text{transactions}'[i].\text{rollback.apply} \end{aligned}$$

$$\begin{aligned} \text{ValidStatus}(t, i, j) & \triangleq \\ & \wedge j \in \text{DOMAIN } \text{history} \\ & \wedge \text{history}[j].\text{index} = i \\ & \wedge \vee \wedge \text{history}[j].\text{phase} = \text{Change} \\ & \quad \wedge \text{history}[j].\text{event} = \text{Commit} \\ & \quad \wedge t[i].\text{change.commit} = \text{history}[j].\text{status} \\ & \vee \wedge \text{history}[j].\text{phase} = \text{Change} \\ & \quad \wedge \text{history}[j].\text{event} = \text{Apply} \\ & \quad \wedge t[i].\text{change.apply} = \text{history}[j].\text{status} \\ & \vee \wedge \text{history}[j].\text{phase} = \text{Rollback} \\ & \quad \wedge \text{history}[j].\text{event} = \text{Commit} \\ & \quad \wedge t[i].\text{rollback.commit} = \text{history}[j].\text{status} \\ & \vee \wedge \text{history}[j].\text{phase} = \text{Rollback} \\ & \quad \wedge \text{history}[j].\text{event} = \text{Apply} \\ & \quad \wedge t[i].\text{rollback.apply} = \text{history}[j].\text{status} \end{aligned}$$

$$\begin{aligned} \text{ValidCommit}(t, i) & \triangleq \\ \text{LET } j & \triangleq \text{CHOOSE } j \in \text{DOMAIN } \text{history} : \\ & \quad \wedge \text{history}[j].\text{event} = \text{Commit} \\ & \quad \wedge \neg \exists k \in \text{DOMAIN } \text{history} : \\ & \quad \quad \wedge \text{history}[k].\text{event} = \text{Commit} \\ & \quad \quad \wedge k > j \\ \text{IN } & \text{ValidStatus}(t, i, j) \end{aligned}$$

$$\begin{aligned} \text{ValidApply}(t, i) & \triangleq \\ \text{LET } j & \triangleq \text{CHOOSE } j \in \text{DOMAIN } \text{history} : \\ & \quad \wedge \text{history}[j].\text{event} = \text{Apply} \\ & \quad \wedge \neg \exists k \in \text{DOMAIN } \text{history} : \\ & \quad \quad \wedge \text{history}[k].\text{event} = \text{Apply} \\ & \quad \quad \wedge k > j \\ \text{IN } & \text{ValidStatus}(t, i, j) \end{aligned}$$

$$\begin{aligned} \text{AtomicStatusChange} & \triangleq \\ \forall i \in 1 \dots \text{NumTransactions} : \\ & \quad \wedge i \in \text{DOMAIN } \text{transactions} \Rightarrow \\ & \quad \quad \wedge \text{StatusCommitted}(i) \Rightarrow \text{ValidCommit}(\text{transactions}', i) \\ & \quad \quad \wedge \text{StatusApplied}(i) \Rightarrow \text{ValidApply}(\text{transactions}', i) \end{aligned}$$

$$\text{Transition} \triangleq \Box[\text{AtomicStatusChange}]_{\langle \text{transactions}, \text{history} \rangle}$$

$$\begin{aligned} \text{LOCAL } \text{IsOrderedChange}(p, i) & \triangleq \\ & \quad \wedge \text{history}[i].\text{phase} = \text{Change} \\ & \quad \wedge \text{history}[i].\text{event} = p \\ & \quad \wedge \text{history}[i].\text{status} = \text{Complete} \end{aligned}$$

$$\begin{aligned}
& \wedge \neg \exists j \in \text{DOMAIN } history : \\
& \quad \wedge j < i \\
& \quad \wedge history[j].phase = Change \\
& \quad \wedge history[j].event = p \\
& \quad \wedge history[j].status = Complete \\
& \quad \wedge history[j].index \geq history[i].index \\
\text{LOCAL } IsOrderedRollback(p, i) & \triangleq \\
& \wedge history[i].phase = Rollback \\
& \wedge history[i].event = p \\
& \wedge history[i].status = Complete \\
& \wedge \exists j \in \text{DOMAIN } history : \\
& \quad \wedge j < i \\
& \quad \wedge history[j].phase = Change \\
& \quad \wedge history[j].status = Complete \\
& \quad \wedge history[j].index = history[i].index \\
& \wedge \neg \exists j \in \text{DOMAIN } history : \\
& \quad \wedge j < i \\
& \quad \wedge history[j].phase = Change \\
& \quad \wedge history[j].event = p \\
& \quad \wedge history[j].status = Complete \\
& \quad \wedge history[j].index > history[i].index \\
& \quad \wedge \neg \exists k \in \text{DOMAIN } history : \\
& \quad \quad \wedge k > j \\
& \quad \quad \wedge k < i \\
& \quad \quad \wedge history[k].phase = Rollback \\
& \quad \quad \wedge history[k].event = p \\
& \quad \quad \wedge history[j].status = Complete \\
& \quad \quad \wedge history[k].index = history[j].index \\
\text{Order} & \triangleq \\
& \wedge \forall i \in \text{DOMAIN } history : \\
& \quad history[i].status = Complete \Rightarrow \\
& \quad \vee IsOrderedChange(Commit, i) \\
& \quad \vee IsOrderedChange(Apply, i) \\
& \quad \vee IsOrderedRollback(Commit, i) \\
& \quad \vee IsOrderedRollback(Apply, i) \\
& \wedge \forall i \in \text{DOMAIN } transactions : \\
& \quad \wedge transactions[i].change.apply = Failed \\
& \quad \wedge transactions[i].rollback.apply \neq Complete \\
& \quad \Rightarrow \neg \exists j \in \text{DOMAIN } transactions : \\
& \quad \quad \wedge j > i \\
& \quad \quad \wedge transactions[i].change.apply \in \{InProgress, Complete\} \\
\text{LOCAL } IsChangeCommitted(i) & \triangleq \\
& \wedge configuration.committed.revision = i
\end{aligned}$$

$\text{LOCAL } \text{IsChangeApplied}(i) \triangleq$
 $\quad \wedge \quad \text{configuration.applied.revision} = i$

$\text{Consistency} \triangleq$
 $\quad \wedge \forall i \in \text{DOMAIN } \text{transactions} :$
 $\quad \quad \wedge \text{IsChangeCommitted}(i)$
 $\quad \quad \wedge \neg \exists j \in \text{DOMAIN } \text{transactions} :$
 $\quad \quad \quad \wedge j > i$
 $\quad \quad \quad \wedge \text{IsChangeCommitted}(j)$
 $\quad \quad \Rightarrow \forall p \in \text{DOMAIN } \text{transactions}[i].\text{change.values} :$
 $\quad \quad \quad \wedge \text{configuration.committed.values}[p] = \text{transactions}[i].\text{change.values}[p]$

$\wedge \forall i \in \text{DOMAIN } \text{transactions} :$
 $\quad \wedge \text{IsChangeApplied}(i)$
 $\quad \wedge \neg \exists j \in \text{DOMAIN } \text{transactions} :$
 $\quad \quad \wedge j > i$
 $\quad \quad \wedge \text{IsChangeApplied}(j)$
 $\quad \Rightarrow \forall p \in \text{DOMAIN } \text{transactions}[i].\text{change.values} :$
 $\quad \quad \wedge \text{configuration.applied.values}[p] = \text{transactions}[i].\text{change.values}[p]$
 $\quad \quad \wedge \text{target.running}$
 $\quad \quad \wedge \text{configuration.applied.target} = \text{target.id}$
 $\quad \quad \wedge \text{configuration.state} = \text{Complete}$
 $\quad \quad \Rightarrow \text{target.values}[p] = \text{transactions}[i].\text{change.values}[p]$

$\text{Safety} \triangleq \Box(\text{Order} \wedge \text{Consistency})$

$\text{THEOREM } \text{Spec} \Rightarrow \text{Safety}$

$\text{LOCAL } \text{IsChanging}(i) \triangleq$
 $\quad \wedge \quad i \in \text{DOMAIN } \text{transactions}$
 $\quad \wedge \quad \text{transactions}[i].\text{phase} = \text{Change}$

$\text{LOCAL } \text{IsChanged}(i) \triangleq$
 $\quad \wedge \quad i \in \text{DOMAIN } \text{transactions}$
 $\quad \wedge \quad \text{transactions}[i].\text{change.commit} \in \{\text{Complete}, \text{Failed}\}$
 $\quad \wedge \quad \text{transactions}[i].\text{change.apply} \in \{\text{Complete}, \text{Aborted}, \text{Failed}\}$

$\text{LOCAL } \text{IsRollingBack}(i) \triangleq$
 $\quad \wedge \quad i \in \text{DOMAIN } \text{transactions}$
 $\quad \wedge \quad \text{transactions}[i].\text{phase} = \text{Rollback}$

$\text{LOCAL } \text{IsRolledBack}(i) \triangleq$
 $\quad \wedge \quad i \in \text{DOMAIN } \text{transactions}$
 $\quad \wedge \quad \text{transactions}[i].\text{rollback.commit} \in \{\text{Complete}, \text{Failed}\}$
 $\quad \wedge \quad \text{transactions}[i].\text{rollback.apply} \in \{\text{Complete}, \text{Aborted}, \text{Failed}\}$

$\text{Terminates}(i) \triangleq$
 $\quad \wedge \text{IsChanging}(i) \rightsquigarrow \text{IsChanged}(i)$

$$\wedge IsRollingBack(i) \rightsquigarrow IsRolledBack(i)$$

$$Termination \stackrel{\Delta}{=} \forall i \in 1 \dots NumTransactions : Terminates(i)$$

$$Liveness \stackrel{\Delta}{=} Termination$$

THEOREM $Spec \Rightarrow Liveness$
