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- Module Transaction -
INSTANCE Naturals
INSTANCE FiniteSets
Instance Sequences
INSTANCE TLC
 An empty constant
Constant Nil
 Transaction phase constants
CONSTANTS
   Change,
   Rollback
 Transaction phase constants
CONSTANTS
   Commit,
   Apply
 Status constants
CONSTANTS
   Pending,
   InProgress,
   Complete,
   Aborted,
   Canceled,
   Failed
Status \triangleq \{Pending, InProgress, Complete, Aborted, Canceled, Failed\}
Done \triangleq \{Complete, Aborted, Canceled, Failed\}
 The set of all nodes
CONSTANT Node
 The set of possible paths and values
CONSTANT Path, Value
Empty \stackrel{\triangle}{=} [p \in \{\} \mapsto Nil]
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VARIABLES

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mastership,
   conn.
   target
 A transaction log. Transactions may either request a set
 of changes to a set of targets or rollback a prior change.
Variable transactions
 A history of transaction change/rollback commit/apply events used for model checking.
Variable history
TypeOK \triangleq
   \forall i \in \text{DOMAIN } transactions:
      \land transactions[i].index \in Nat
      \land transactions[i].phase \in \{Change, Rollback\}
      \land transactions[i].change.commit \in Status
      \land transactions[i].change.apply \in Status
      \land \forall p \in DOMAIN \ transactions[i].change.values :
          transactions[i].change.values[p] \neq Nil \Rightarrow
              transactions[i].change.values[p] \in STRING
      \land transactions[i].rollback.commit \neq Nil \Rightarrow
            transactions[i].rollback.commit \in Status
      \land transactions[i].rollback.apply \neq Nil \Rightarrow
            transactions[i].rollback.apply \in Status
      \land \forall p \in DOMAIN \ transactions[i].rollback.values :
          transactions[i].rollback.values[p] \neq Nil \Rightarrow
              transactions[i].rollback.values[p] \in STRING
LOCAL State \triangleq [
   transactions \mapsto transactions,
   configuration \mapsto configuration,
   mastership
                   \mapsto mastership,
   conn
                    \mapsto conn,
   target
                    \mapsto target
LOCAL Transitions \triangleq
   LET
         indexes \stackrel{\triangle}{=} \{i \in \text{DOMAIN } transactions' : \}
                                 i \in \text{DOMAIN } transactions \Rightarrow transactions'[i] \neq transactions[i]
        [transactions \mapsto [i \in indexes \mapsto transactions'[i]]] @@
            (IF configuration' \neq configuration THEN [configuration \mapsto configuration'] ELSE Empty) @@
            (IF target' \neq target \text{ THEN } [target \mapsto target'] \text{ ELSE } Empty)@@
            (IF Len(history') > Len(history) THEN [event \mapsto history'[Len(history')]] ELSE Empty)
Test \stackrel{\triangle}{=} INSTANCE \ Test \ WITH
   File \leftarrow "Transaction.log"
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configuration,

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Add a change for revision 'i' to the transaction log
AppendChange(i) \triangleq
   \wedge Len(transactions) = i - 1
   \land \exists p \in Path, v \in Value:
       LET transaction \triangleq [
               index
                          \mapsto Len(transactions) + 1,
               phase
                          \mapsto Change,
               change \mapsto [
                   index \mapsto Len(transactions) + 1,
                   ordinal \mapsto 0,
                   values \mapsto (p:>v),
                   commit \mapsto Pending,
                   apply \mapsto Pending,
               rollback \mapsto [
                   index \mapsto 0,
                   ordinal \mapsto 0,
                   values \mapsto Empty,
                   commit \mapsto Nil,
                   apply \mapsto Nil
             \land transactions' = Append(transactions, transaction)
   \land UNCHANGED \langle configuration, mastership, conn, target, history <math>\rangle
 Add a rollback of revision 'i' to the transaction log
RollbackChange(i) \triangleq
   \land i \in \text{domain} \ transactions
   \land transactions[i].phase = Change
   \land transactions[i].change.commit = Complete
   \land transactions' = [transactions \ EXCEPT \ ![i].phase]
                                                                          = Rollback,
                                                   ![i].rollback.commit = Pending,
                                                   ![i].rollback.apply = Pending]
   \land UNCHANGED \langle configuration, mastership, conn, target, history <math>\rangle
CommitChange(n, i) \triangleq
   \land \lor \land transactions[i].change.commit = Pending
         \land configuration.committed.change = i-1
         \land \lor \land configuration.committed.target \neq i
               \land configuration.committed.index = configuration.committed.target
               \land configuration.committed.index \in DOMAIN transactions \Rightarrow
                     \vee \wedge configuration.committed.target = configuration.committed.index
                        \land transactions[configuration.committed.index].change.commit \in Done
                     \lor \land configuration.committed.target < configuration.committed.index
                        \land transactions[configuration.committed.index].rollback.commit \in Done
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\land configuration' = [configuration \ EXCEPT \ !.committed.target = i]
        \land history' = Append(history, [
                          phase \mapsto Change,
                          event \mapsto Commit,
                          index \mapsto i,
                          status \mapsto InProgress)
        \land \lor transactions' = [transactions \ EXCEPT \ ![i].change.commit
                                                                                = InProgress,
                                                        ![i].rollback.index
                                                                                = configuration.committed.revis
                                                        ![i].rollback.values
                                                                                = [
                                                           p \in \text{DOMAIN } transactions[i].change.values \mapsto
                                                              IF p \in \text{DOMAIN } configuration.committed.values
                                                                 configuration.committed.values[p]
                                                               ELSE Nil]
           ∨ UNCHANGED ⟨transactions⟩
     \lor \land configuration.committed.target = i
        \land transactions' = [transactions \ EXCEPT \ ![i].change.commit
                                                                             = InProgress,
                                                     ![i].rollback.index
                                                                              = configuration.committed.revision
                                                     ![i].rollback.values
                                                                              = [
                                                        p \in \text{DOMAIN } transactions[i].change.values \mapsto
                                                           If p \in \text{DOMAIN } configuration.committed.values \ \text{TH}
                                                              configuration.committed.values[p]
                                                            ELSE Nil]]
        \land UNCHANGED \langle configuration, history \rangle
\lor \land transactions[i].change.commit = InProgress
  \land \lor \land configuration.committed.change \neq i
        \land \lor \land configuration' = [configuration \ EXCEPT \ !.committed.index]
                                                             !.committed.change = i,
                                                             !.committed.revision = i,
                                                             !.committed.ordinal = configuration.committed.
                                                             !.committed.values
                                                                                    = transactions[i].change.va
                                                                                            configuration.committ
              \land history' = Append(history, [
                                phase \mapsto Change,
                                event \mapsto Commit,
                                index \mapsto i,
                                status \mapsto Complete)
              \land \lor transactions' = [transactions \ EXCEPT \ ![i].change.commit = Complete,
                                                              ![i].change.ordinal = configuration'.committed.
                 \vee UNCHANGED \langle transactions \rangle
           \vee \wedge transactions' = [transactions \ EXCEPT \ ![i].change.commit = Failed,
                                                           ![i].change.apply = Canceled]
              \wedge history' = Append(history, [
                                phase \mapsto Change,
                                event \mapsto Commit,
                                index \mapsto i,
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status \mapsto Failed)
                    \land \lor configuration' = [configuration \ EXCEPT \ !.committed.index = i,
                                                                        !.committed.change = i]
                       ∨ UNCHANGED ⟨configuration⟩
            \lor \land configuration.committed.change = i
               \land transactions' = [transactions \ EXCEPT \ ![i].change.commit = Complete,
                                                             ![i].change.ordinal = configuration.committed.ordinal]
               \land UNCHANGED \langle configuration, history \rangle
      \lor \land transactions[i].change.commit = Failed
         \land configuration.committed.change < i
         \land configuration' = [configuration EXCEPT !.committed.index = i,
                                                         !.committed.change = i]
         \land UNCHANGED \langle transactions, history \rangle
   \land UNCHANGED \langle mastership, conn, target \rangle
ApplyChange(n, i) \triangleq
   \land transactions[i].change.commit = Complete
   \land \lor \land transactions[i].change.apply = Pending
         \land \lor \land configuration.applied.ordinal = transactions[i].change.ordinal - 1
               \land \lor \land configuration.applied.target \neq i
                     \land configuration.applied.index \in DOMAIN \ transactions \Rightarrow
                           \lor \land configuration.applied.target = configuration.applied.index
                              \land transactions[configuration.applied.index].change.apply \in Done
                          \lor \land configuration.applied.target < configuration.applied.index
                              \land transactions[configuration.applied.index].rollback.apply \in Done
                    \land \lor \land configuration.applied.revision = transactions[i].rollback.index
                          \land configuration' = [configuration \ EXCEPT \ !.applied.target = i]
                          \wedge history' = Append(history, [
                                             phase \mapsto Change,
                                             event \mapsto Apply,
                                             index \mapsto i,
                                             status \mapsto InProgress)
                          \land \lor transactions' = [transactions \ EXCEPT \ ![i].change.apply = InProgress]
                             \vee UNCHANGED \langle transactions \rangle
                       \lor \land configuration.applied.revision < transactions[i].rollback.index
                          \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Aborted]
                          \land history' = Append(history, [
                                             phase \mapsto Change,
                                             event \mapsto Apply,
                                             index \mapsto i,
                                             status \mapsto Aborted)
                          \land \lor configuration' = [configuration \ EXCEPT \ !.applied.target = i,
                                                                             !.applied.index = i,
                                                                             !.applied.ordinal = transactions[i].change
                             ∨ UNCHANGED ⟨configuration⟩
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\lor \land configuration.applied.target = i
              \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = InProgress]
              \land UNCHANGED \langle configuration, history \rangle
     \lor \land configuration.applied.ordinal = transactions[i].change.ordinal
        \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Aborted]
        ∧ UNCHANGED ⟨configuration, history⟩
  \land UNCHANGED \langle target \rangle
\lor \land transactions[i].change.apply = InProgress
      If the change has not yet been applied, attempt to apply it.
  \land \lor \land configuration.applied.ordinal \neq transactions[i].change.ordinal
        \land configuration.state = Complete
        \land configuration.term = mastership.term
        \land \mathit{conn}[\mathit{n}].\mathit{id} = \mathit{mastership}.\mathit{conn}
        \land conn[n].connected
        \land target.running
        \land \lor \land target' = [target \ Except \ !.values = transactions[i].change.values @@ target.values]
              \land configuration' = [configuration \ EXCEPT \ !.applied.index]
                                                                !.applied.ordinal = transactions[i].change.ordin
                                                                !.applied.revision = i,
                                                                !.applied.values = transactions[i].change.values
                                                                                           configuration.applied.value
              \wedge history' = Append(history, [
                                  phase \mapsto Change,
                                  event \mapsto Apply,
                                  index \mapsto i,
                                  status \mapsto Complete)
              \land \lor transactions' = [transactions \ EXCEPT \ ![i].change.apply = Complete]
                 ∨ UNCHANGED ⟨transactions⟩
           \lor \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Failed]
              \land history' = Append(history, [
                                  phase \mapsto Change,
                                  event \mapsto Apply,
                                  index \mapsto i,
                                  status \mapsto Failed)
              \land \lor configuration' = [configuration \ EXCEPT \ !.applied.index = i,
                                                                   !.applied.ordinal = transactions[i].change.ordinal
                 ∨ UNCHANGED ⟨configuration⟩
              \land UNCHANGED \langle target \rangle
      If the change has been applied, update the transaction status.
      \lor \land configuration.applied.ordinal = transactions[i].change.ordinal
        \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Complete]
        \land UNCHANGED \langle configuration, target, history \rangle
\lor \land transactions[i].change.apply \in \{Aborted, Failed\}
  \land configuration.applied.ordinal < transactions[i].change.ordinal
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 $\land configuration' = [configuration \ EXCEPT \ !.applied.target = i,$ 

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!.applied.index = i,
                                                         !.applied.ordinal = transactions[i].change.ordinal]
         \land UNCHANGED \langle transactions, target, history \rangle
   \land UNCHANGED \langle mastership, conn \rangle
ReconcileChange(n, i) \triangleq
   \land transactions[i].phase = Change
   \land \lor CommitChange(n, i)
      \vee ApplyChange(n, i)
CommitRollback(n, i) \triangleq
   \land \lor \land transactions[i].rollback.commit = Pending
         \land configuration.committed.revision = i
         \land \lor \land configuration.committed.target = i
               \land configuration.committed.index = configuration.committed.target
               \land \lor \land configuration.committed.index = i
                    \land transactions[configuration.committed.index].change.commit = Complete
                 \lor \land configuration.committed.index > i
                    \land transactions[configuration.committed.index].rollback.commit = Complete
               \land configuration' = [configuration \ EXCEPT \ !.committed.target = transactions[i].rollback.index]
               \land history' = Append(history, [
                                 phase \mapsto Rollback,
                                 event \mapsto Commit,
                                 index \mapsto i,
                                 status \mapsto InProgress)
              \land \lor transactions' = [transactions \ EXCEPT \ ![i].rollback.commit = InProgress]
                 \vee UNCHANGED \langle transactions \rangle
            \lor \land configuration.committed.target = transactions[i].rollback.index
               \land transactions' = [transactions \ EXCEPT \ ![i].rollback.commit = InProgress]
              \land UNCHANGED \langle configuration, history \rangle
      \lor \land transactions[i].rollback.commit = InProgress
         \land \lor \land configuration.committed.revision = i
               \land configuration' = [configuration \ EXCEPT \ !.committed.index]
                                                              !.committed.ordinal = configuration.committed.ordin
                                                              !.committed.revision = transactions[i].rollback.index,
                                                              !.committed.values = transactions[i].rollback.values
                                                                                             configuration.committed.va
               \wedge history' = Append(history, [
                                 phase \mapsto Rollback,
                                 event \mapsto Commit,
                                 index \mapsto i,
                                 status \mapsto Complete)
               \land \lor transactions' = [transactions \ EXCEPT \ ![i].rollback.commit = Complete,
                                                               ![i].rollback.ordinal = configuration'.committed.ordi
                 \vee UNCHANGED \langle transactions \rangle
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\lor \land configuration.committed.revision = transactions[i].rollback.index
               \land transactions' = [transactions \ EXCEPT \ ![i].rollback.commit = Complete,
                                                             ![i].rollback.ordinal = configuration.committed.ordinal
               \land UNCHANGED \langle configuration, history \rangle
   \land UNCHANGED \langle mastership, conn, target \rangle
ApplyRollback(n, i) \triangleq
   \land transactions[i].rollback.commit = Complete
   \land \lor \land transactions[i].rollback.apply = Pending
         \land \lor \land transactions[i].change.apply = Pending
               \land configuration.applied.ordinal = transactions[i].change.ordinal - 1
               \land \ configuration.applied.target \neq i
               \land configuration.applied.index \in DOMAIN transactions \Rightarrow
                     \lor \land configuration.applied.target = configuration.applied.index
                        \land transactions[configuration.applied.index].change.apply \in Done
                     \lor \land configuration.applied.target < configuration.applied.index
                        \land transactions[configuration.applied.index].rollback.apply \in Done
               \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Aborted]
               \land history' = Append(history, [
                                  phase \mapsto Change,
                                  event \mapsto Apply,
                                  index \mapsto i,
                                  status \mapsto Aborted)
               \land \lor configuration' = [configuration \ EXCEPT \ !.applied.target = i,
                                                                  !.applied.index = i,
                                                                  !.applied.ordinal = transactions[i].change.ordinal]
                  \vee UNCHANGED \langle configuration \rangle
            \lor \land transactions[i].change.apply = InProgress
               \land configuration.applied.ordinal \neq transactions[i].change.ordinal
               \land transactions' = [transactions \ EXCEPT \ ![i].change.apply = Failed]
               \land history' = Append(history, [
                                  phase \mapsto Change,
                                  event \mapsto Apply,
                                  index \mapsto i,
                                  status \mapsto Failed)
               \land \lor configuration' = [configuration \ EXCEPT \ !.applied.index = i,
                                                                  !.applied.ordinal = transactions[i].change.ordinal]
                  \vee UNCHANGED \langle configuration \rangle
            \lor \land transactions[i].change.apply \in \{Aborted, Failed\}
               \land configuration.applied.ordinal < transactions[i].change.ordinal
               \land configuration' = [configuration \ EXCEPT \ !.applied.target = i,
                                                               !.applied.index = i,
                                                               !.applied.ordinal = transactions[i].change.ordinal]
               \land UNCHANGED \langle transactions, history \rangle
            \lor \land transactions[i].change.apply \in Done
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\land configuration.applied.ordinal = transactions[i].rollback.ordinal - 1
           \land \lor \land configuration.applied.target \neq transactions[i].rollback.index
                 \land \lor \land configuration.applied.index = i
                       \land transactions[configuration.applied.index].change.apply \in Done
                    \lor \land configuration.applied.index > i
                       \land transactions[configuration.applied.index].rollback.apply \in Done
                 \land configuration' = [configuration \ EXCEPT \ !.applied.target = transactions[i].rollback.index]
                 \land history' = Append(history, [
                                    phase \mapsto Rollback,
                                    event \mapsto Apply,
                                    index \mapsto i,
                                    status \mapsto InProgress])
                 \land \lor transactions' = [transactions \ EXCEPT \ ![i].rollback.apply = InProgress]
                    ∨ UNCHANGED ⟨transactions⟩
              \lor \land configuration.applied.target = transactions[i].rollback.index
                 \land transactions' = [transactions \ EXCEPT \ ![i].rollback.apply = InProgress]
                 \land UNCHANGED \langle configuration, history \rangle
     \land UNCHANGED \langle target \rangle
   \lor \land transactions[i].rollback.apply = InProgress
         If this transaction has not yet been applied, attempt to apply it.
     \land \lor \land configuration.applied.ordinal \neq transactions[i].rollback.ordinal
           \land configuration.state = Complete
           \land configuration.term = mastership.term
           \land conn[n].id = mastership.conn
           \land conn[n].connected
           \land target.running
           \land target' = [target \ Except \ !.values = transactions[i].rollback.values@@target.values]
           \land configuration' = [configuration \ EXCEPT \ !.applied.index]
                                                            !.applied.ordinal = transactions[i].rollback.ordinal,
                                                            !.applied.revision = transactions[i].rollback.index,
                                                            !.applied.values = transactions[i].rollback.values @@
                                                                                       configuration.applied.values
           \wedge history' = Append(history, [
                              phase \ \mapsto Rollback,
                              event \mapsto Apply,
                              index \mapsto i,
                              status \mapsto Complete)
           \land \lor transactions' = [transactions \ EXCEPT \ ![i].rollback.apply = Complete]
              ∨ UNCHANGED ⟨transactions⟩
            If the change has been applied, update the transaction status.
         \lor \land configuration.applied.ordinal = transactions[i].rollback.ordinal
           \land configuration.applied.revision = transactions[i].rollback.index
           \land transactions' = [transactions \ EXCEPT \ ![i].rollback.apply = Complete]
           \land UNCHANGED \langle configuration, target, history \rangle
\land UNCHANGED \langle mastership, conn \rangle
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\begin{aligned} ReconcileRollback(n,\,i) &\triangleq \\ &\land transactions[i].phase = Rollback \\ &\land \lor CommitRollback(n,\,i) \\ &\lor ApplyRollback(n,\,i) \end{aligned} \begin{aligned} ReconcileTransaction(n,\,i) &\triangleq \\ &\land i \in \text{DOMAIN}\ transactions \\ &\land mastership.master = n \\ &\land \lor ReconcileChange(n,\,i) \\ &\lor ReconcileRollback(n,\,i) \end{aligned}
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