
MODULE *Config*

EXTENDS

Northbound,
Proposal,
Configuration,
Mastership,
Southbound

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

LOCAL INSTANCE *TLC*

$vars \triangleq \langle proposal, configuration, mastership, target \rangle$

Formal specification, constraints, and theorems.

Init \triangleq

$\wedge InitNorthbound$
 $\wedge InitProposal$
 $\wedge InitConfiguration$
 $\wedge InitMastership$
 $\wedge InitSouthbound$

Next \triangleq

$\vee \wedge NextNorthbound$
 $\wedge UNCHANGED \langle \rangle$
 $\vee \wedge NextProposal$
 $\wedge UNCHANGED \langle \rangle$
 $\vee \wedge NextConfiguration$
 $\wedge UNCHANGED \langle proposal \rangle$
 $\vee \wedge NextMastership$
 $\wedge UNCHANGED \langle proposal, configuration \rangle$
 $\vee \wedge NextSouthbound$
 $\wedge UNCHANGED \langle proposal, configuration, mastership \rangle$

Spec $\triangleq Init \wedge \Box [Next]_{vars} \wedge WF_{vars}(Next)$

Order \triangleq

$\forall i \in \text{DOMAIN } proposal :$
 $\wedge \wedge proposal[i].phase = ProposalCommit$
 $\wedge proposal[i].state = ProposalInProgress$
 $\Rightarrow \neg \exists j \in \text{DOMAIN } proposal :$

$$\begin{aligned}
& \wedge j > i \\
& \wedge \text{proposal}[j].\text{phase} = \text{ProposalCommit} \\
& \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete} \\
& \wedge \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \wedge \text{proposal}[i].\text{state} = \text{ProposalInProgress} \\
& \Rightarrow \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \wedge j > i \\
& \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \\
& \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}
\end{aligned}$$

Consistency \triangleq

LET

Compute the transaction indexes that have been applied to the target

$$\begin{aligned}
\text{targetIndexes} & \triangleq \{i \in \text{DOMAIN } \text{proposal} : \\
& \quad \wedge \text{proposal}[i].\text{phase} = \text{ProposalApply} \\
& \quad \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete} \\
& \quad \wedge \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
& \quad \quad \wedge j > i \\
& \quad \quad \wedge \text{proposal}[j].\text{type} = \text{ProposalRollback} \\
& \quad \quad \wedge \text{proposal}[j].\text{rollback.index} = i \\
& \quad \quad \wedge \text{proposal}[j].\text{phase} = \text{ProposalApply} \\
& \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalComplete}\}
\end{aligned}$$

Compute the set of paths in the target that have been updated by transactions

$$\text{appliedPaths} \triangleq \text{UNION } \{\text{DOMAIN } \text{proposal}[i].\text{change.values} : i \in \text{targetIndexes}\}$$

Compute the highest index applied to the target for each path

$$\begin{aligned}
\text{pathIndexes} & \triangleq [p \in \text{appliedPaths} \mapsto \text{CHOOSE } i \in \text{targetIndexes} : \\
& \quad \forall j \in \text{targetIndexes} : \\
& \quad \quad \wedge i \geq j \\
& \quad \quad \wedge p \in \text{DOMAIN } \text{proposal}[i].\text{change.values}]
\end{aligned}$$

Compute the expected target configuration based on the last indexes applied to the target for each path.

$$\text{expectedConfig} \triangleq [p \in \text{DOMAIN } \text{pathIndexes} \mapsto \text{proposal}[\text{pathIndexes}[p]].\text{change.values}[p]]$$

IN

$$\text{target} = \text{expectedConfig}$$

$$\text{Safety} \triangleq \Box(\text{Order} \wedge \text{Consistency})$$

THEOREM $\text{Spec} \Rightarrow \text{Safety}$

$$\text{Terminated}(i) \triangleq$$

$$\begin{aligned}
& \wedge i \in \text{DOMAIN } \text{proposal} \\
& \wedge \text{proposal}[i].\text{phase} \in \{\text{ProposalApply}, \text{ProposalAbort}\} \\
& \wedge \text{proposal}[i].\text{state} = \text{ProposalComplete}
\end{aligned}$$

$$\text{Termination} \triangleq$$

$$\forall i \in 1 \dots \text{Len}(\text{proposal}) :$$

$Terminated(i)$

$Liveness \stackrel{\Delta}{=} \Diamond Termination$

THEOREM $Spec \Rightarrow Liveness$

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