```
——— MODULE ConfigImpl -
INSTANCE Naturals
INSTANCE FiniteSets
{\tt INSTANCE}\ Sequences
LOCAL INSTANCE TLC
This section specifies constant parameters for the model.
Constant LogEnabled
Assume LogEnabled \in Boolean
CONSTANT None
Assume None \in \text{string}
CONSTANT Node
Assume \forall n \in Node : n \in String
CONSTANTS
   Change,
   Rollback
Event \triangleq \{Change, Rollback\}
Assume \forall e \in Event : e \in String
CONSTANTS
   Commit,
   Apply
Phase \triangleq \{Commit, Apply\}
\texttt{ASSUME} \ \forall \ p \in Phase : p \in \texttt{STRING}
CONSTANTS
   Pending,
   In Progress,
   Complete,
   Aborted,
   Failed
State \triangleq \{Pending, InProgress, Complete, Aborted, Failed\}
```

 $Done \triangleq \{Complete, Aborted, Failed\}$

```
ASSUME \forall s \in State : s \in String Constant Path Assume \forall p \in Path : p \in String Constant Value Assume \forall v \in Value : v \in String AllValues \triangleq Value \cup \{None\} Constant NumProposals Assume NumProposals \in Nat
```

This section defines model state variables.

```
proposal \stackrel{\Delta}{=} [i \in 1.. Nat \mapsto [
     phase \mapsto Phase,
     change \mapsto [
        values \mapsto Change,
        commit \mapsto State,
        apply \mapsto State],
      rollback \mapsto [
        index\mapsto Nat,
        values \mapsto Change,
        commit \mapsto State,
        apply \mapsto State]]]
configuration \stackrel{\Delta}{=} [
   committed \mapsto [
     index \mapsto Nat,
     values \mapsto \mathit{Change}],
   applied \mapsto [
     index\mapsto Nat,
      values \mapsto Change,
     term \mapsto Nat]]
mastership \stackrel{\Delta}{=} [
   master \mapsto STRING,
  term \mapsto Nat,
  conn \mapsto Nat]
conn \; \stackrel{\Delta}{=} \; \; [ \; n \in \mathit{Node} \mapsto \; [ \;
     id \qquad \mapsto Nat,
     connected \mapsto BOOLEAN ]]
target \stackrel{\Delta}{=} [
  id \mapsto Nat,
  values \mapsto Change,
  running \mapsto BOOLEAN]
```

```
VARIABLE proposal
{\tt VARIABLE}\ configuration
VARIABLE mastership
VARIABLE conn
VARIABLE target
VARIABLE history
VARIABLE mapping
vars \triangleq \langle proposal, configuration, mastership, conn, target, history, mapping \rangle
LOCAL MastershipLog \stackrel{\triangle}{=} INSTANCE \ Log \ WITH
   File
                 \leftarrow "Mastership.log",
   CurrState \leftarrow [
       target
                         \mapsto target,
                         \mapsto mastership,
       mastership
       conns
                         \mapsto conn],
   SuccState \leftarrow [
       target
                         \mapsto target',
       mastership
                         \mapsto mastership',
       conns
                         \mapsto conn'],
   Enabled
               \leftarrow LogEnabled
LOCAL ConfigurationLog \stackrel{\triangle}{=} INSTANCE Log WITH
                 \leftarrow \text{``Configuration.log''}\,,
   CurrState \leftarrow [
       configuration \mapsto configuration,
       target
                        \mapsto target,
       mastership
                       \mapsto mastership,
       conns
                        \mapsto conn],
   SuccState \leftarrow [
       configuration \mapsto configuration',
       target
                         \mapsto target',
       mastership
                        \mapsto mastership',
       conns
                        \mapsto conn'],
   Enabled \leftarrow LogEnabled
LOCAL ProposalLog \stackrel{\triangle}{=} INSTANCE Log WITH
                 \leftarrow \text{``Proposal.log''},
   CurrState \leftarrow [
                        \mapsto [i \in \{i \in DOMAIN \ proposal : proposal[i].phase \neq None\} \mapsto proposal[i]],
       proposals
```

```
configuration \mapsto configuration,
       target
                        \mapsto target,
       mastership
                        \mapsto mastership,
       conns
                       \mapsto conn],
   SuccState \leftarrow [
      proposals
                       \mapsto [i \in \{i \in DOMAIN \ proposal' : proposal'[i].phase \neq None\} \mapsto proposal'[i]],
      configuration \mapsto configuration',
                        \mapsto target',
       target
      mastership
                        \mapsto mastership',
       conns
                       \mapsto conn'],
   Enabled \leftarrow LogEnabled
This section models configuration target.
StartTarget \triangleq
   \land \neg target.running
   \wedge target' = [target \ EXCEPT \ !.id]
                                                  = target.id + 1,
                                     !.running = TRUE
   ∧ UNCHANGED ⟨proposal, configuration, mastership, conn, history⟩
StopTarget \triangleq
   \land target.running
   \land target' = [target \ EXCEPT \ !.running = FALSE,
                                     !.values = [p \in \{\} \mapsto [value \mapsto None]]]
   \land conn' = [n \in Node \mapsto [conn[n] \text{ EXCEPT } !.connected = \text{FALSE}]]
   \land UNCHANGED \langle proposal, configuration, mastership, history <math>\rangle
This section models nodes connection to the configuration target.
ConnectNode(n) \triangleq
   \wedge \neg conn[n].connected
   \land \ target.running
   \wedge conn' = [conn \ EXCEPT \ ![n].id]
                                                     = conn[n].id + 1,
                                   ![n].connected = TRUE]
   ∧ UNCHANGED ⟨proposal, configuration, mastership, target, history⟩
DisconnectNode(n) \triangleq
   \land conn[n].connected
   \wedge conn' = [conn \ EXCEPT \ ![n].connected = FALSE]
   \land UNCHANGED \langle proposal, configuration, mastership, target, history <math>\rangle
```

This section models mastership reconciliation.

```
ReconcileMastership(n) \stackrel{\Delta}{=}
   \land \lor \land conn[n].connected
         \land mastership.master = None
         \land mastership' = [master \mapsto n, term \mapsto mastership.term + 1, conn \mapsto conn[n].id]
       \vee \wedge \neg conn[n].connected
         \land mastership.master = n
         \land mastership' = [mastership \ EXCEPT \ !.master = None]
   \land UNCHANGED \langle proposal, configuration, conn, target, history <math>\rangle
This section models configuration reconciliation.
ReconcileConfiguration(n) \stackrel{\Delta}{=}
    \land mastership.master = n
   \land \lor \land configuration.status \neq InProgress
         \land configuration.applied.term < mastership.term
         \land configuration' = [configuration EXCEPT !.status = InProgress]
         \land UNCHANGED \langle target \rangle
       \lor \land configuration.status = InProgress
         \land configuration.applied.term < mastership.term
         \land conn[n].connected
         \land target.running
         \land target' = [target \ Except \ !.values = configuration.applied.values]
         \land configuration' = [configuration EXCEPT !.applied.term = mastership.term,
                                                           !.applied.target = target.id,
                                                           !.status
                                                                               = Complete
   \land UNCHANGED \langle proposal, mastership, conn, history \rangle
This section models proposal reconcilation.
CommitChange(n, i) \triangleq
    'index' is the current index committed to the configuration
    'changeIndex' is the maximum change index committed to the configuration
    'targetIndex' is the index of the proposal currently being committed
    targetIndex is always changed first. Once the change is committed, the
    changeIndex and index will be incremented to match the targetIndex.
    If the index is less than the targetIndex, this indicates a rollback
    of a prior proposal is being processed, and the targetIndex cannot be incremented
    until that rollback is complete. The index represents the index to which
    the proposal at changeIndex + 1 rolls back.
    \land \lor \land proposal[i].change.commit = Pending
         \land configuration.committed.changeIndex = i - 1
         \land \lor \land configuration.committed.targetIndex \neq i
               \land configuration.committed.index = configuration.committed.targetIndex
               \land configuration' = [configuration \ EXCEPT \ !.committed.targetIndex = i]
```

```
\land UNCHANGED \langle proposal \rangle
            \lor \land configuration.committed.targetIndex = i
                \land \ \lor \ \land \ proposal[i].rollback.commit = None
                      \land LET rollbackIndex \triangleq configuration.committed.index
                              rollbackValues \stackrel{\triangle}{=} [p \in DOMAIN \ proposal[i].change.values \mapsto
                                                      IF p \in \text{DOMAIN} configuration.committed.values THEN
                                                          configuration.committed.values[p]
                                                       ELSE
                                                          [index \mapsto 0, value \mapsto None]]
                              \lor \land proposal[i].rollback.commit = None
                                  \land proposal' = [proposal \ EXCEPT \ ![i].change.commit
                                                                                                   = InProgress,
                                                                         ![i].rollback.index
                                                                                                   = rollbackIndex,
                                                                         ![i].rollback.values
                                                                                                   = rollbackValues
                              \lor \land proposal[i].rollback.commit = Pending
                                  \land proposal' = [proposal \ EXCEPT \ ![i].change.commit = Aborted,
                                                                         ![i].rollback.index = rollbackIndex]
                \land UNCHANGED \langle configuration \rangle
         \land UNCHANGED \langle history \rangle
      \lor \land proposal[i].change.commit = InProgress
         \land \lor \land configuration.committed.changeIndex = i-1
                \land \lor \land \texttt{LET} \ values \stackrel{\triangle}{=} [p \in \texttt{DOMAIN} \ proposal[i].change.values \mapsto
                                              proposal[i].change.values[p]@@[index \mapsto i]]@@
                                                 configuration.committed.values\\
                              \land configuration' = [configuration \ EXCEPT \ !.committed.index]
                                                                                                                =i.
                                                                                 !.committed.changeIndex = i,
                                                                                 !.committed.values
                                                                                                                = values
                              \land history' = Append(history, [type \mapsto Change, phase \mapsto Commit, index \mapsto i])
                              \land UNCHANGED \langle proposal \rangle
                  \lor \land proposal' = [proposal \ EXCEPT \ ![i].change.commit = Failed]
                      \land UNCHANGED \langle configuration, history \rangle
             \lor \land configuration.committed.changeIndex > i
                \land proposal' = [proposal \ EXCEPT \ ![i].change.commit = Complete]
                \land UNCHANGED \langle configuration, history \rangle
      \lor \land proposal[i].change.commit \in \{Aborted, Failed\}
         \land configuration.committed.changeIndex = i - 1
         \land configuration' = [configuration \ EXCEPT \ !.committed.index]
                                                            !.committed.changeIndex = i]
         \land UNCHANGED \langle proposal, history \rangle
   \land UNCHANGED \langle target \rangle
ApplyChange(n, i) \triangleq
    'index' is the current index applied to the configuration
    'changeIndex' is the maximum change index applied to the configuration
    'targetIndex' is the index of the proposal currently being applied
```

targetIndex is always changed first. Once the change is applied, the

```
changeIndex and index will be incremented to match the targetIndex.
If the index is less than the targetIndex, this indicates a rollback
of a prior proposal is being processed, and the targetIndex cannot be incremented
until that rollback is complete. The index represents the index to which
the proposal at changeIndex + 1 rolls back.
\land \lor \land proposal[i].change.apply = Pending
     \land configuration.committed.changeIndex \ge i
     \land configuration.applied.changeIndex = i-1
     \land \lor \land configuration.applied.targetIndex \neq i
           \land configuration.applied.index = configuration.applied.targetIndex
           \land i-1 \in \text{DOMAIN } proposal \land proposal[i-1].change.apply = Failed \Rightarrow
                    proposal[i-1].rollback.apply = Complete
           \land configuration' = [configuration \ EXCEPT \ !.applied.targetIndex = i]
           \land UNCHANGED \langle proposal \rangle
        \lor \land configuration.applied.targetIndex = i
           \land \lor \land proposal[i].change.commit \in \{Aborted, Failed\}
                 \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Aborted]
               \lor \land proposal[i].change.commit = Complete
                  \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = InProgress]
           \land UNCHANGED \langle configuration \rangle
     \land UNCHANGED \langle target, history \rangle
  \lor \land proposal[i].change.apply = InProgress
      Verify the applied term is the current mastership term to ensure the
      configuration has been synchronized following restarts.
     \land configuration.applied.term = mastership.term
      Verify the node's connection to the target.
     \land conn[n].connected
     \land mastership.conn = conn[n].id
     \land target.running
     \land \lor \land configuration.applied.changeIndex = i-1
           \land \lor \land \text{LET } values \stackrel{\triangle}{=} [p \in \text{DOMAIN } proposal[i].change.values \mapsto
                                          proposal[i].change.values[p]@@[index \mapsto i]]
                          \land target' = [target \ EXCEPT \ !.values = values @@ target.values]
                          \land configuration' = [configuration \ EXCEPT \ !.applied.index = i,]
                                                                             !.applied.changeIndex = i,
                                                                             !.applied.values = values @@
                                                                                configuration.applied.values
                          \land history' = Append(history, [type \mapsto Change, phase \mapsto Apply, index \mapsto i])
                          \land UNCHANGED \langle proposal \rangle
              \lor \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Failed]
                 \land UNCHANGED \langle configuration, target, history \rangle
        \lor \land configuration.applied.changeIndex \ge i
           \land proposal' = [proposal \ EXCEPT \ ![i].change.apply = Complete]
           \land UNCHANGED \langle configuration, target, history \rangle
  \lor \land proposal[i].change.apply = Failed
```

```
\land configuration' = [configuration \ EXCEPT \ !.applied.index]
                                                           !.applied.changeIndex = i
         \land UNCHANGED \langle proposal, target, history \rangle
CommitRollback(n, i) \triangleq
    'index' is the current index committed to the configuration
    'changeIndex' is the maximum change index committed to the configuration
    'targetIndex' is the index of the proposal currently being committed
    targetIndex is always changed first. Once the rollback is committed, the
    index will be decremented to match the targetIndex. The next time a change
    is committed, the index will increase again. If the committed index is equal
    to this proposal index, this proposal is the next to be rolled back. To roll
    back a proposal, the target index is set to the proposal's rollback index.
    When the rollback is committed, the committed index is set to the proposal's
    rollback index, thus matching the targetIndex. This unblocks new changes
    to be committed.
   \land \lor \land proposal[i].rollback.commit = Pending
         \land configuration.committed.changeIndex > i
         \land configuration.committed.index = i
         \land \lor \land configuration.committed.targetIndex = i
               \land configuration' = [configuration \ EXCEPT \ !.committed.targetIndex = proposal[i].rollback.index]
               \land UNCHANGED \langle proposal \rangle
            \lor \land configuration.committed.targetIndex = proposal[i].rollback.index
               \land \lor \land proposal[i].change.commit \neq Aborted
                     \land proposal' = [proposal \ EXCEPT \ ![i].rollback.commit = InProgress]
                  \lor \land proposal[i].change.commit = Aborted
                     \land proposal' = [proposal \ EXCEPT \ ![i].rollback.commit = Complete]
               \land UNCHANGED \langle configuration \rangle
         \land UNCHANGED \langle history \rangle
      \lor \land proposal[i].rollback.commit = InProgress
         \land \lor \land configuration.committed.index = i
               \land LET values \stackrel{\triangle}{=} [p \in DOMAIN \ configuration.committed.values <math>\mapsto
                                       IF p \in \text{DOMAIN } proposal[i].rollback.values THEN
                                          proposal[i].rollback.values[p]
                                          configuration.committed.values[p]]
                       configuration' = [configuration \ EXCEPT \ !.committed.index = proposal[i].rollback.index,
                                                                      !.committed.values = values
               \land history' = Append(history, [type \mapsto Rollback, phase \mapsto Commit, index \mapsto i])
               \land UNCHANGED \langle proposal \rangle
            \vee \wedge configuration.committed.index = proposal[i].rollback.index
               \land proposal' = [proposal \ EXCEPT \ ![i].rollback.commit = Complete]
               \land UNCHANGED \langle configuration, history \rangle
      \lor \land proposal[i].rollback.commit = Complete
```

 \land configuration.applied.changeIndex = i-1

```
\land proposal[i].change.commit = Aborted
         \land configuration.committed.targetIndex = proposal[i].rollback.index
         \land configuration.committed.index \neq proposal[i].rollback.index
         \land configuration' = [configuration \ EXCEPT \ !.committed.index = proposal[i].rollback.index]
         \land UNCHANGED \langle proposal, history \rangle
   \land UNCHANGED \langle target \rangle
ApplyRollback(n, i) \stackrel{\Delta}{=}
    'index' is the current index applied to the configuration
    'changeIndex' is the maximum change index applied to the configuration
    'targetIndex' is the index of the proposal currently being applied
    targetIndex is always changed first. Once the rollback is applied, the
    index will be decremented to match the targetIndex. The next time a change
    is applied, the index will increase again. If the applied index is equal
    to this proposal index, this proposal is the next to be rolled back. To roll
    back a proposal, the target index is set to the proposal's rollback index.
    When the rollback is applied, the applied index is set to the proposal's
    rollback index, thus matching the targetIndex. This unblocks new changes
    to be applied.
   \land \lor \land proposal[i].rollback.apply = Pending
         \land configuration.committed.index < proposal[i].rollback.index
         \land configuration.applied.changeIndex \ge i
         \land configuration.applied.index = i
         \land \lor \land configuration.applied.targetIndex = i
               \land configuration' = [configuration \ EXCEPT \ !.applied.targetIndex = proposal[i].rollback.index]
               \land UNCHANGED \langle proposal \rangle
            \lor \land configuration.applied.targetIndex = proposal[i].rollback.index \\
               \land proposal' = [proposal \ EXCEPT \ ![i].rollback.apply = InProgress]
               \land UNCHANGED \langle configuration \rangle
         \land UNCHANGED \langle target, history \rangle
      \lor \land proposal[i].rollback.apply = InProgress
         \land \lor \land configuration.applied.index = i
                Verify the applied term is the current mastership term to ensure the
                configuration has been synchronized following restarts.
               \land configuration.applied.term = mastership.term
                Verify the node's connection to the target.
               \land conn[n].connected
               \land target.running
               \land LET values \stackrel{\triangle}{=} [p \in DOMAIN \ configuration.applied.values <math>\mapsto
                                       IF p \in DOMAIN \ proposal[i].rollback.values \ THEN
                                           proposal[i].rollback.values[p]
                                        ELSE
                                           configuration.applied.values[p]]
                        \land target' = [target \ EXCEPT \ !.values = proposal[i].rollback.values @@ target.values]
                        \land configuration' = [configuration \ EXCEPT \ !.applied.index = proposal[i].rollback.index,
```

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!.applied.values = values
                \land history' = Append(history, [type \mapsto Rollback, phase \mapsto Apply, index \mapsto i])
                \land UNCHANGED \langle proposal \rangle
             \lor \land configuration.applied.index \neq i
                \land proposal' = [proposal \ EXCEPT \ ![i].rollback.apply = Complete]
                \land UNCHANGED \langle configuration, target, history \rangle
ReconcileProposal(n, i) \triangleq
   \land mastership.master = n
   \land \lor CommitChange(n, i)
       \vee ApplyChange(n, i)
       \vee CommitRollback(n, i)
       \vee ApplyRollback(n, i)
   \land UNCHANGED \langle mastership, conn \rangle
This section models changes to the proposal queue.
 Propose change at index 'i'
ProposeChange(i) \triangleq
   \land proposal[i].phase = None
   \land i-1 \in \text{DOMAIN } proposal \Rightarrow proposal[i-1].phase \neq None
   \land \exists p \in Path, v \in AllValues:
         \land proposal' = [proposal \ EXCEPT \ ![i].phase]
                                                                       = Change,
                                                ![i].change.values = (p:>[value \mapsto v]),
                                                ![i].change.commit = Pending,
                                                ![i].change.apply = Pending
   ∧ UNCHANGED ⟨configuration, mastership, conn, target, history⟩
 Rollback proposed change at index 'i'
ProposeRollback(i) \triangleq
   \land proposal[i].phase = Change
   \land proposal' = [proposal \ EXCEPT \ ![i].phase]
                                                                   = Rollback,
                                           ![i].rollback.commit = Pending,
                                           ![i].rollback.apply = Pending]
   \land UNCHANGED \langle configuration, mastership, conn, target, history <math>\rangle
Formal specification, constraints, and theorems.
Init \triangleq
    \land proposal = \lceil
         i \in 1 \dots NumProposals \mapsto [
           phase
                      \mapsto None,
            change \mapsto [
```

 $values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],$

```
commit \mapsto None,
                                  apply \mapsto None,
                       rollback \mapsto [
                                  index \mapsto 0,
                                  values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],
                                  commit \mapsto None,
                                  apply \mapsto None
\land \ configuration = \lceil
                 committed \mapsto [
                           index
                                                                        \mapsto 0,
                           changeIndex \mapsto 0,
                           targetIndex \mapsto 0,
                                                                       \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]]],
                           values
                 applied \mapsto [
                          index
                                                                       \mapsto 0.
                           changeIndex \mapsto 0,
                           targetIndex \mapsto 0,
                                                                        \mapsto 0,
                           term
                           target
                                                                        \mapsto 0,
                                                                       \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]]],
                           values
                 status \mapsto Pending
\land mastership = [master \mapsto None, term \mapsto 0, conn \mapsto 0]
\land conn = [n \in Node \mapsto [id \mapsto 0, connected \mapsto FALSE]]
\land target = [
                 id
                                               \mapsto 0,
                 values \mapsto [p \in \{\} \mapsto [index \mapsto 0, value \mapsto None]],
                 running \mapsto FALSE
\wedge history = \langle \rangle
\land mapping = [
                 configuration \mapsto [
                                     committed \mapsto [
                                               values \mapsto configuration.committed.values,
                                     applied \mapsto [
                                              term \mapsto configuration.applied.term,
                                               target \mapsto configuration.applied.target,
                                               values \mapsto configuration.applied.values,
                                     status \mapsto configuration.status,
                 proposal \mapsto [i \in DOMAIN \ proposal \mapsto [i \in DOM
                           phase
                                                           \mapsto proposal[i].phase,
                           values
                                                         \mapsto [p \in DOMAIN \ proposal[i].change.values \mapsto proposal[i].change.values[p].value],
                           change \mapsto [
                                     commit \mapsto \text{IF } \land proposal[i].change.commit = InProgress
                                                                                \land configuration.committed.changeIndex > i
                                                                       THEN Complete
                                                                        ELSE proposal[i].change.commit,
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\mapsto IF \land proposal[i].change.apply = InProgress
                                                                                 \land configuration.applied.changeIndex \ge i
                                                                                  THEN Complete
                                                                                  ELSE proposal[i].change.apply],
                                  rollback \mapsto [
                                          commit \mapsto \text{IF } \land proposal[i].rollback.commit = InProgress
                                                                                 \land \ configuration.committed.index \neq i
                                                                          THEN Complete
                                                                          ELSE proposal[i].rollback.commit,
                                                                 \mapsto IF \land proposal[i].rollback.commit = InProgress
                                                                                 \land configuration.applied.index \neq i
                                                                          THEN Complete
                                                                          ELSE proposal[i].rollback.apply]]]]
Next \triangleq
          \land \lor \exists i \in 1 ... NumProposals :
                               \vee ProposeChange(i)
                               \vee ProposeRollback(i)
                  \forall \exists n \in Node, i \in DOMAIN \ proposal :
                              ProposalLog!Action(ReconcileProposal(n, i), [node \mapsto n, index \mapsto i])
                  \vee \exists n \in Node:
                              ConfigurationLog! Action(ReconcileConfiguration(n), [node \mapsto n])
                  \vee \exists n \in Node:
                              MastershipLog!Action(ReconcileMastership(n), [node \mapsto n])
                  \vee \exists n \in Node:
                         \vee ConnectNode(n)
                         \vee DisconnectNode(n)
                  \vee StartTarget
                  \lor StopTarget
          \land mapping' = [
                         configuration \mapsto [
                                          committed \mapsto [
                                                   values \mapsto configuration'.committed.values],
                                          applied \mapsto [
                                                   term \mapsto configuration'.applied.term,
                                                   target \mapsto configuration'.applied.target,
                                                   values \mapsto configuration'.applied.values],
                                          status \mapsto configuration'.status,
                         proposal \mapsto [i \in DOMAIN \ proposal' \mapsto [i \in 
                                                               \mapsto proposal'[i].phase,
                                                               \mapsto [p \in DOMAIN \ proposal'[i].change.values \mapsto proposal'[i].change.values[p].value],
                                  values
                                  change \mapsto [
                                          commit \mapsto \text{IF } \land proposal'[i].change.commit = InProgress
                                                                                      \land configuration'.committed.changeIndex \ge i
                                                                          THEN Complete
```

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ELSE proposal'[i].change.commit,
                                                                           \mapsto IF \land proposal'[i].change.apply = InProgress
                                                 apply
                                                                                                   \land configuration'.applied.changeIndex \ge i
                                                                                              THEN Complete
                                                                                              ELSE proposal'[i].change.apply],
                                       rollback \mapsto [
                                                 commit \mapsto \text{IF } \land proposal'[i].rollback.commit = InProgress
                                                                                                   \land configuration'.committed.index \neq i
                                                                                     THEN Complete
                                                                                     {\tt ELSE} \ \ proposal'[i].rollback.commit,
                                                                          \mapsto IF \land proposal'[i].rollback.apply = InProgress
                                                                                                   \land configuration'.applied.index \neq i
                                                                                    THEN Complete
                                                                                     ELSE proposal'[i].rollback.apply]]]]
Spec \triangleq
           \wedge Init
           \wedge \, \, \Box [Next]_{vars}
           \land \forall \, i \, \in 1 \dots \textit{NumProposals} : \text{WF}_{\langle proposal, \, configuration, \, mastership, \, conn, \, target, \, history \rangle} (\textit{ProposeChange}(i) \vee \textit{Proposal}, \, configuration, \, mastership, \, conn, \, target, \, history \rangle) (\textit{ProposeChange}(i)) \vee \textit{Proposal}, \, configuration, \, mastership, \, conn, \, target, \, history)) (\textit{ProposeChange}(i)) \vee \textit{Proposal}, \, configuration, \, mastership, \, conn, \, target, \, history)) (\textit{ProposeChange}(i)) \vee \textit{Proposal}, \, configuration, \, mastership, \, conn, \, target, \, history)) (\textit{ProposeChange}(i)) \vee \textit{Proposal}, \, configuration, \, mastership, \, conn, \, target, \, history)) (\textit{ProposeChange}(i)) \vee \textit{ProposeChange}(i)) \vee \textit{ProposeCha
           \land \forall \ n \in \textit{Node}, \ i \in 1 \ldots \textit{NumProposals} : \text{WF}_{\langle proposal, \ configuration, \ mastership, \ conn, \ target, \ history \rangle}(\textit{ReconcileProposals}) \\
           \land \forall n \in Node : WF_{(configuration, mastership, conn, target)}(ReconcileConfiguration(n))
           \land \forall n \in Node : WF_{\langle mastership, conn, target \rangle}(ReconcileMastership(n))
           \land \forall n \in Node : WF_{\langle conn, target \rangle}(ConnectNode(n) \lor DisconnectNode(n))
           \wedge \operatorname{WF}_{\langle target \rangle}(StartTarget)
           \wedge \operatorname{WF}_{\langle target \rangle}(StopTarget)
 Mapping \stackrel{\triangle}{=} \text{Instance } Config \text{ with}
                                                          \leftarrow mapping.proposal,
          proposal
          configuration \leftarrow mapping.configuration
 Refinement \triangleq Mapping!Spec
 Order \triangleq Mapping! Order
 Consistency \triangleq Mapping! Consistency
Liveness \triangleq Mapping!Liveness
```