

EXTENDS

*Northbound*,  
*Proposal*,  
*Configuration*,  
*Mastership*,  
*Southbound*

INSTANCE *Naturals*

INSTANCE *FiniteSets*

INSTANCE *Sequences*

LOCAL INSTANCE *TLC*

*vars*  $\triangleq$   $\langle \text{proposal}, \text{configuration}, \text{mastership}, \text{node}, \text{target} \rangle$

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Formal specification, constraints, and theorems.

*Init*  $\triangleq$

$\wedge$  *InitNorthbound*  
 $\wedge$  *InitProposal*  
 $\wedge$  *InitConfiguration*  
 $\wedge$  *InitMastership*  
 $\wedge$  *InitSouthbound*

*Next*  $\triangleq$

$\vee \wedge$  *NextNorthbound*  
 $\wedge$  UNCHANGED  $\langle \rangle$   
 $\vee \wedge$  *NextProposal*  
 $\wedge$  UNCHANGED  $\langle \rangle$   
 $\vee \wedge$  *NextConfiguration*  
 $\wedge$  UNCHANGED  $\langle \text{proposal} \rangle$   
 $\vee \wedge$  *NextMastership*  
 $\wedge$  UNCHANGED  $\langle \text{proposal}, \text{configuration} \rangle$   
 $\vee \wedge$  *NextSouthbound*  
 $\wedge$  UNCHANGED  $\langle \text{proposal}, \text{configuration}, \text{mastership} \rangle$

*Spec*  $\triangleq$  *Init*  $\wedge$   $\Box[\text{Next}]_{\text{vars}} \wedge \text{WF}_{\text{vars}}(\text{Next})$

*IsCommittedChange*(*i*)  $\triangleq$

$\wedge$  *proposal*[*i*].*state* = *ProposalChange*  
 $\wedge \vee \wedge$  *proposal*[*i*].*change.phase* = *ProposalCommit*  
 $\wedge$  *proposal*[*i*].*change.status* = *ProposalFailed*  
 $\vee$  *proposal*[*i*].*change.phase* = *ProposalApply*

$$\begin{aligned}
\text{IsAppliedChange}(i) &\triangleq \\
&\wedge \text{proposal}[i].\text{state} = \text{ProposalChange} \\
&\wedge \text{proposal}[i].\text{change.phase} = \text{ProposalApply} \\
&\wedge \text{proposal}[i].\text{change.status} = \text{ProposalComplete} \\
\\
\text{IsCommittedRollback}(i) &\triangleq \\
&\wedge \text{proposal}[i].\text{state} = \text{ProposalRollback} \\
&\wedge \vee \wedge \text{proposal}[i].\text{change.phase} = \text{ProposalCommit} \\
&\quad \wedge \text{proposal}[i].\text{change.status} = \text{ProposalFailed} \\
&\quad \vee \text{proposal}[i].\text{change.phase} = \text{ProposalApply} \\
\\
\text{IsAppliedRollback}(i) &\triangleq \\
&\wedge \text{proposal}[i].\text{state} = \text{ProposalRollback} \\
&\wedge \vee \text{proposal}[i].\text{rollback.phase} = \text{ProposalCommit} \\
&\quad \vee \wedge \text{proposal}[i].\text{rollback.phase} = \text{ProposalApply} \\
&\quad \wedge \text{proposal}[i].\text{rollback.status} \in \{\text{ProposalPending}, \text{ProposalComplete}\} \\
\\
\text{Order} &\triangleq \\
&\forall i \in \text{DOMAIN } \text{proposal} : \\
&\quad \wedge \text{IsCommittedChange}(i) \Rightarrow \\
&\quad \quad \forall j \in \text{DOMAIN } \text{proposal} : j < i \Rightarrow \\
&\quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalChange} \Rightarrow \text{IsCommittedChange}(j) \\
&\quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalRollback} \Rightarrow \text{IsCommittedRollback}(j) \\
&\quad \wedge \text{IsAppliedChange}(i) \Rightarrow \\
&\quad \quad \forall j \in \text{DOMAIN } \text{proposal} : j < i \Rightarrow \\
&\quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalChange} \Rightarrow \text{IsAppliedChange}(j) \\
&\quad \quad \quad \wedge \text{proposal}[j].\text{state} = \text{ProposalRollback} \Rightarrow \text{IsAppliedRollback}(j) \\
\\
\text{Consistency} &\triangleq \\
&\wedge \text{target.running} \\
&\wedge \text{configuration.state} = \text{ConfigurationComplete} \\
&\wedge \text{configuration.apply.incarnation} = \text{target.incarnation} \\
&\Rightarrow \forall i \in \text{DOMAIN } \text{proposal} : \\
&\quad \text{IsAppliedChange}(i) \Rightarrow \\
&\quad \quad \forall p \in \text{DOMAIN } \text{proposal}[i].\text{change.values} : \\
&\quad \quad \quad \wedge \neg \exists j \in \text{DOMAIN } \text{proposal} : \\
&\quad \quad \quad \quad \wedge j > i \\
&\quad \quad \quad \quad \wedge \text{proposal}[j].\text{change.phase} = \text{ProposalApply} \\
&\quad \quad \quad \quad \wedge \text{proposal}[j].\text{change.status} = \text{ProposalComplete} \\
&\quad \quad \quad \quad \wedge \text{proposal}[j].\text{rollback.phase} = \text{ProposalApply} \\
&\quad \quad \quad \quad \Rightarrow \text{proposal}[j].\text{rollback.status} \neq \text{ProposalComplete} \\
&\quad \quad \quad \wedge p \in \text{DOMAIN } \text{proposal}[j].\text{change.values} \\
&\quad \Rightarrow \wedge p \in \text{DOMAIN } \text{target.values} \\
&\quad \quad \wedge \text{target.values}[p].\text{value} = \text{proposal}[i].\text{change.values}[p].\text{value} \\
&\quad \quad \wedge \text{target.values}[p].\text{index} = \text{proposal}[i].\text{change.values}[p].\text{index}
\end{aligned}$$

$Safety \triangleq \Box (Order \wedge Consistency)$

THEOREM  $Spec \Rightarrow Safety$

$Terminates(i) \triangleq$   
     $\wedge proposal[i].state = ProposalChange \leadsto$   
     $\wedge proposal[i].change.phase = ProposalApply$   
     $\wedge proposal[i].change.status = ProposalComplete$   
     $\wedge proposal[i].state = ProposalRollback \leadsto$   
     $\wedge proposal[i].rollback.phase = ProposalApply$   
     $\wedge proposal[i].rollback.status = ProposalComplete$

$Termination \triangleq$   
     $\forall i \in 1 \dots NumProposals : Terminates(i)$

$Liveness \triangleq Termination$

THEOREM  $Spec \Rightarrow Liveness$

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