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CHAPTER 1 INTRODUCTION Process mining is a relatively young and developing research area with the roots in computational intelligence, data mining; and process modeling and analysis [34]. Main idea in this research area is to discover, monitor and improve processes by extracting information from event logs. With this idea, process mining creates a bridge between data mining and business process modeling and analysis. Interest in this research area has two origins; firstly, events are recorded and easily avail- able in the modern information systems. Secondly, highly competitive and rapidly changing business life requires improvement and support for business processes [34]. Traditional process mining approaches work on a single organization; however, with the increase of cloud computing and shared infrastructures, event logs of multiple organizations are currently available for analysis. In principle, there are two main environments where <u>cross-organizational process mining</u> stands out. Firstly, when organizations work together to execute the same process, it is insufficient to analyze only logs of one organization and gathered information from all stakeholders should be merged prior to analysis. Secondly, organizations essentially execute the same processes with different needs and configurations on a common infrastructure, where cross-organizational process mining can help the organizations to learn from each other's experience, knowledge and processes. Process mining spectrum is extensive and highly inter-related with a different sets of

activities grouped under categories of Cartography, Auditing and Navigation [33]. In this spectrum, Cartography activities aim to create maps of the real world tasks by using process models whereas Auditing activities confront the models and reality; and the last activity group of Navigation activities use process mining methods like a navigation application. This thesis study proposes a hybrid approach and exploits approaches from different categories to create a new point of view. In other words, this study aims to create maps using the discovery techniques from Cartography and promotes the better operating locations in the process models from Auditing to create recommendations for users like a Navigation application. In cross-organizational process mining area, recent studies focus on commonality and collaboration between organizations; however, they only present results based on how similar the process models and behaviors of organizations under cross compar- ison [10]. In addition, challenges based on partitioning of tasks and process models between organizations are presented in the literature [32]. This thesis study is based on the environment where processes are executed on several organizations and cross- organizational process mining is applied with the idea of unsupervised learning where predictor variables related to performances of organizations are used. Recent studies in process mining and similarity area include various different ap- proaches to define relationships between process models. These studies include cre- ating similarity metrics for node matching, structural and behavioral similarities [14] and alignment matrices between models [9]. In addition, differences between process models are tried to be explained by mismatch patterns with the help of comprehen- sive case studies [13]. In this study, mismatch patterns are mathematically defined and implemented; as it is known to be the first implementation of mismatch patterns. Applicability and performance of using mismatch patterns is also analyzed by com- paring to the similarity metrics that are defined in the literature. In the light of these motivations, approach proposed in this thesis study is a four- stage solution and it starts by mining the process models of organizations with a user defined noise threshold. With the mined models and event logs, second stage calcu- lates the performance indicators for each organization and then clusters organizations based on how well they are operating. Third stage aims to find differences between process models of each organization. Final stage combines the information from all stages and provides a set of recommendations. With this approach it is aimed to help business process management users to focus on the potentially important parts of their business maps. In addition, this approach includes implementation of mismatch pat- terns and performance indicator based clustering of organizations. As an extensible framework, approach stages are designed with minimum inter-dependency and they are open to include new process mining approaches, performance indicators, cluster- ing approaches and mismatch patterns. Moreover, every stage of the methodology is intended to be configurable for user needs and business environment requirements. Within this thesis study, proposed methodology is implemented in ProM framework [42] as a set of plugins corresponding for each stage and packaged under the name of CrossOrgProcMin. Since ProM is the most popular open-source environment for academia and industry at the time of this thesis published, developed set of plugins are built over this framework. With the help of this implementation, approach pro- posed in this thesis is tested on a synthetic and real-life event logs. Performance of methodology is assessed with a defined evaluation metrics for each stage and result- ing recommendations are presented to show how this approach helps users to focus on learning opportunities between organizations with a performance improvement potential. Rest of the thesis is constructed as following: • In Chapter 2, related studies in process mining area are presented. • In Chapter 3, background information for the relevant topics to this thesis study is explained. • In Chapter 4, methodology proposed in this thesis is presented with detail. • In Chapter 5, methodology of this thesis is applied on datasets and results are discussed. • In Chapter 6, summary of this study is presented with the final

remarks and pointers for future work. CHAPTER 2 RELATED WORK In this chapter, studies related to the work presented in this thesis are summarized. Firstly, latest trends and studies in the process mining area are explained. Then stud- ies from cross-organizational process mining, which is the main topic of this research, is introduced. Following these, studies related to similarity in process mining is men-tioned. Finally, performance and conformance analysis approaches in process mining area are presented. 2.1 State of the Art in Process Mining In this section, important milestones in process mining and current research trends will be presented. Studies in process mining area have roots based on process discovery techniques for software engineering. These original techniques are studied to discover workflows using neural networks, finite state machines and Markovian approaches [40]. However, using process mining in the workflow management area is introduced by Agrawal et al. and this study aims to find workflow graphs given event logs and identify edge conditions between nodes [4]. In the following efforts, various different approaches based on hierarchical structuring, dependency and fre- quency graphs; and heuristic methods are suggested to address the same problem. While some of these algorithms are focused on creating partial solutions, some of the algorithms are used as a foundation for further expansions such as "Alpha Algorithm" of van der Aalst et al.[41]. Spread of process mining is not only in kept in academia, but also many vendors presented tools and software to discover processes and help Figure 2.1: Process Mining Framework organizations manage their workflows [1]. Current challenges in the process mining area can be presented best through men-tioning spectrum and its relations. As diagrammed in Figure 2.1 and presented in the research of van der Aalst [33], process mining spectrum is extensive and highly inter-related. Starting with the provenance, process mining deals with gathering and keeping event logs as current data and historic data. In this level, post mortem data means the logs and information gathered from completed events whereas pre mortem data means information related to ongoing cases. This separation helps us to use historical knowledge to exploit and gain advantage over current business operations. At the right end of the diagram, models are presented as de facto models and de jure models. De jure models are created with the aim of describing reality as it should be whereas de facto models aims to describe reality as it is. Within each model category a mixture of perspectives, in other words point of views from different information levels, can be mixed. In order to fill the gap between event logs and models, ten different process mining activities are listed under three categories [33] as follows: Cartography: In this category the main aim is to create maps of the real world ac-tivities by using process models. Discovery: Discovery is focused on extracting process models from event logs. Enhancing: Enhancing activities are based on improving de facto models with the information hidden in the event logs. Diagnose: Diagnose activities stand for identifying the problems caused by directly process models. Auditing: In this category, activities related to confronting the model and the reality are collected. Detect: Detection is based on comparing the de jure models with the ongoing processes to generate alerts if shifts occur in the reality. Check: Checking is defined to identify deviations occurred in the past. Compare: Comparison of de facto models and de jure models shows the dif-ference between planned and the reality. Promote: Promotion includes partially updating de jure models from the in- formation gathered from de facto models. Navigation: In this category, process mining methods are used like a navigation ap- plication. Explore: Event data and models are used in combination to explore business processes. Predict: Prediction activities combine the information from past events and make predictions about ongoing processes. Recommend: Suitable actions can be suggested by using the prediction and contextual information. Within this framework, the study presented in this thesis is a combination of discovery from cartography, promoting from auditing and recommendation from navigation. In other words and within the metaphor of spectrum, this study aims to discover maps using the discovery techniques and promotes the partially best locations in the map

to create recommendations for travelers in their navigation applications. 2.2 Process Discovery in Process Mining In this section, process discovery studies will be presented briefly. Within the pro- cess mining framework, there are various different process mining algorithms pro- posed which have the same aim of discovering underlying processes. Considering the approaches undertaken with the proposed algorithms, the following grouping is provided [24]. a-algorithm: This algorithm is based on the causality relationship that can be dis- covered from the event logs and proposed by van der Aalst et al. [41]. However, this approach cannot handle loops and therefore extensions like a++ algorithm [12] is proposed to overcome this problem. Outputs of this approach and its extensions are workflow nets with XOR, AND splits and joins to represent un-derlying process models. Inductive Approach: Methods proposed in inductive approach [22, 21] are based on finding the best Hidden Markov Models (HMMs) that represents the under-lying process model. Workflow nets are constructed by using HMM nodes and inductive learning. Hierarchical Clustering: This method [19] firstly splits the event logs into clusters and creates a dependency graph. Using this dependency graph, clusters are defined with a hierarchy tree which is then merged into a single workflow model. Genetic Approach: The first method provided in this group [36] constructs models based on causal matrix of activities and tries to handle noise, incompleteness, concurrency, hidden and duplicate activities. However, there are many config- uration parameters and fine-tuning to handle noise and irrelevant data to use this method. Second method in this group [17] applies genetic algorithms to discover process models using from-to charts and this method finds optimal or sub-optimal solutions for a relatively complex processes within a reasonable processing time. Heuristic Approach: Heuristic approach for process discovery is an extension of aalgorithm which is based on likelihood calculation of activities and constructs dependency and frequency graphs while handling the noise in the event log. In addition, heuristic approach is used to locate the immediate successors with the help of evaluation metrics generated over raw from-to charts [18]. Proposed methods in process discovery are based on solving different challenges in the process mining area. Considering the scope of this thesis study; process discovery operations are undertaken with inductive methods which is a robust, repeatable and mature set of approaches. 2 .3 Cross-organizational Process Mining In this section, related studies and trends in <u>cross-organizational process mining</u> will be presented. Cross-organizational mining is based on cross-correlation of workflows and the realized activities in different organizations. The main challenge of this topic in process mining is that comparing processes and their performances of different organizational units in an objective approach. This objective approach is open to be enhanced with the process context, namely the environment of the process that is executed. Most of the studies in this area are currently studying to reveal the possible opportunities and some initial approaches to address main challenges. In the study of Bujis et al. [10], the authors indicated the importance of the increase of Software-as-a-Service (SaaS) and cloud computing infrastructure usages. As a re- sult of this increase, more and more organizations will use a Shared Business Process Management Infrastructure (SBPMI) and it is an opportunity for different organiza-tional units to learn from each other in such infrastructure. The approach presented in this study is based on three questions and three metric groups to answer these questions: 1. Which organizations support my behavior with better process models? 2. Which organizations have better behavior which my process model supports? and 3. Which set of organizations can I support with my process model? While answering these questions, they used simplification based metrics to indicate better process models; and throughput time metrics to indicate better behaviors. In this study, it is shown how a generic framework can be used to highlight the main idea behind cross-organizational process mining. In the study of van der Aalst [31], using configurable process models is proposed for the organizations sharing the same infrastructure and doing the similar work. Config- urable

process models are defined as a family of process models where each organi- zation can use this family with their configurations according to their business needs. This approach not only creates behaviors needed by each organization but also creates a basis to compare and learn within process mining framework. The configurable pro- cess models are formalized by "Causal Nets", which is a notational language based on input and output bindings of each node. Although this study does not provide answer to all challenges related to cross-organizational-process-mining, a formalism of configurable processes models is presented to address learning and conformance checking. Cross-organizational process mining is divided into intra -organizational and inter- organizational process mining subcategories with two basic ideas: collaboration and exploiting commonality [32]. In his study, van der Aalst defined collaboration for distributed work between multiple organizations and commonality as ability of using the same process models and infrastructure between the organizations. In order to exploit these two ideas, two partitioning dimensions are suggested in [32]: Vertical Partitioning: Process instances, namely cases, distributed over several or- ganizations which collaborate to complete a complex activity. Horizontal Partitioning: Process parts, namely tasks or activities, are shared within organizations like jigsaw puzzle parts. For these orthogonal dimensions, a number of questions and challenges are presented in the study [32]. For the vertical partitioning, where organizations are aiming to share infrastructure and knowledge to learn from each other, it is mentioned that supervised learning methods like classification can be used. Notion of this thesis is based on vertical partitioning of cross-organizational process mining with the idea of unsuper- vised learning where predictor variables related to performances of organizations are used. 2.4 Process Similarity in Process Mining In this section, prominent studies related to similarity in process mining will be pre- sented with their results. With the emerging attention in business processes, organiza- tions become aware of the fact that they can exploit the business processes and their similarities [9]. In addition, most of the large organizations have repository of process models of similar business operations [14]. There are four main different approaches proposed to this solution in the literature currently. The first approach, proposed by Dijkman et al. [14], is based on similarity metrics as a) node matching similarity; b) structural similarity; and c) behavioral similarity. Result of the study [14] indicates that using these three similarities can differentiate comparable process models and within these metrics structural similarity is the most prominent one. The second approach by Bujis and Reijis is an analytical approach [9] to compare the process models of different organizations that does similar works. Proposed algo- rithm is based on creating an alignment matrix between observed and realized models. This inter-relation is also used to compare different variants of the same process by different organizations. In addition, they suggested their method as a framework to further standardize a process of common interest. The third approach proposed by Esgin and Senkul focuses on delta analysis between predefined models and discovered models. In [16], a hybrid model which considers the dependencies of process activities and process structure is presented to measure the similarity between process models. In addition, sequences alignment notion is applied on delta analysis in [15], which aims to arrange structures to identify similar regions such as protein sequences in bioinformatics. The fourth and final approach is based on frequently occurring mismatches between similar business processes [13]. In this study [13], a set of mismatch patterns are derived from the different departments of the same organization. Although this re- search does not present a complete set of possible mismatch patterns, the provided set is comprehensive to identify similarities and differences of the processes of same operations. In this thesis, combination of metric and mismatch pattern approaches are used to identify variations between process models of different organizations. 2.5 Performance and Conformance Analysis in Process Mining In this section summary of the studies related to performance and conformance anal- ysis will be presented. Event logs do

not only contain task sequences but also contain time, resource and contextual information. Analysis of process models with these ad- ditional information is used within performance analysis framework to highlight bottlenecks or make predictions. However, in order to undertake a performance analysis there is a need of replaying reality (event logs) on the expectation (process models) and check the conformance of reality to plan [35]. In the study conducted by Rozinat and van der Aalst [29], a conformance frame- work is proposed by two metrics fitness metrics and appropriateness metrics. In this study [29], fitness metric is based on replaying the event log on the process model and counting the number of missing or remaining tokens. In other words, replaying and conformance of event logs over process models is modelled as a token passing formalism. On the other hand, appropriateness metrics are based on how accurate the process model in describing reality within a degree of clarity. Simplicity, preci- sion and generalization attributes of the process models are taken into account while calculating appropriateness metrics. Token passing approach to conformance has a major drawback when the process model and reality of event logs do not fit completely. In this case, there are overestimated process models that are too general, in other words with too much behavior other than the reality. In order to overcome this drawback, heuristic and optimization based methods are proposed by other researchers. In this thesis study, an extended version of optimization based approach presented in [2] is used to replay logs on the process models. Since the main goal of this study is not to evaluate conformance of logs and process models, the method presented by Adriansyah et al. is extended to calculate performance indicators while replaying the logs. CHAPTER 3 BACKGROUND In this chapter background information is presented for the relevant topics to this the- sis study. Topics are mentioned starting with the building blocks and then approaches with the order of their usage in the methodology presented in this thesis study. Firstly, event logs and process models are mentioned with their mathematical formalization and background. Following these, process discovery approaches are explained and then performance analysis methodologies are presented. Then, machine learning and clustering topics are mentioned. Finally, mismatch patterns in process models are presented. All topics in this chapter are limited to the scope of this thesis study with the aim of constructing a necessary background. 3.1 Event Log Event logs are the main inputs to any process mining methodology including this the- sis study and they include information related to real life activities. Event logs which are the outputs of the software systems like Enterprise Resource Planning (ERP) or Business Process Management (BPM) have common properties that are also assumed in the literature as the properties of event logs. General structure of event logs in- cludes multiple layers as diagrammed in Figure 3.1. Processes have cases which are simply single process instances. Within each case, there are events that are gener- ally represented as a sequence of activities performed. Each event is enhanced with the attributes such as timestamps, resource assignments and other contextual data. A fragment of this structure is presented in Table 3.1 for the Loan Application Process Figure 3.1: Structure of Event Logs [6], which shows the footprints of a financial organization that provides consumer credits [8]. In the table, each line represents an event with its attributes which are collected under cases to form a complete event log. Event log structure and related notions are formalized in [33] as following: Definition 3.1.1. (Event and Event Attributes) Let E be the universe of events which include all possible event identifiers and in this universe any event $e \in E$. Events are enhanced with contextual information, namely attributes. For any event $e \in E$ and attribute A, #A (e) is the value of the attribute A for event e. Possible attributes for events include timestamps, people and resource assignments, transaction types and other contextual data. Definition 3.1.2. (Case and Case Attributes) Let C be the universe of cases which include all possible case identifiers and in this universe any case $c \in C$. Like events, cases are also enhanced with contextual information, namely attributes. For any case $\underline{c} \in C$ and attribute A, #A $\underline{(c)}$ is the value of the attribute A for case c.

Each <u>case has</u> at least one <u>attribute</u> which is trace. Definition 3.1.3. (Trace) Trace is a sequence of events, $t \in E*$ such that each event is restricted to occur only once. Table 3.1: Fragment of event log from Loan Application Process (Variation #1) Event Log Attributes Event Date Time Transition Case #1 Register Application 16.04.2013 14:37:27 Complete Check Credit 16.04.2013 14:41:19 Complete Check System 16.04.2013 14:47:35 Complete Calculate Capacity 16.04.2013 14:50:21 Complete Accept 16.04.2013 14:53:22 Complete Send decision e-mail 16.04.2013 14:55:11 Complete Case #2 Register Application 16.04.2013 16:28:19 Complete Check Credit 16.04.2013 16:36:22 Complete Check System 16.04.2013 16:43:10 Complete Calculate Capacity 16.04.2013 16:52:40 Complete Reject 16.04.2013 16:53:53 Complete Send decision e-mail 16.04.2013 17:01:32 Complete Definition 3.1.4. (Event Log) Event log is set of cases $L \subseteq C$ such that each event occurs at most once in the event log. In this study, event logs from different organizations are exploited, thus organization related attributes are used for cases. Within these event logs, traces of cases for each organization are used to discover underlying process models. In addition, timestamps and resource related attributes of events are used to collect performance related data for further analysis. 3.2 Process Modeling Process modeling is the foundation of process management applications and main tools of people in this profession. Although process modeling can be defined with informal process workflows to document procedures, there is a number of formalized notations which are more suitable to cross-applicability and mathematical analysis. In the control-flow view of process modeling, a process model is aimed to give decisions on which activities to take place with their orders. In this study, control-flow of process models are used to find mismatch patterns between different organizations that execute the same activities. Considering the scope of this thesis, only Petri nets, Workflow Nets and Business Process Modeling Notation (BPMN) will be presented in this section. 3 .2.1 Petri Nets Petri net is a mathematical modeling language that is aimed to describe concurrent systems. Graphical notation of Petri nets seems intuitive and simple; however, it is powerful in terms of being executable and applicability of analysis techniques [37]. Petri nets are directed bipartite graphs where nodes represent transitions and places represent conditions. Structure represented by Petri nets is static and the state of the net is described by placing tokens, namely the process of marking. Formalization of Petri nets are explained in [28] as follows: Definition 3.2.1. (Petri Nets) A Petri net is a triplet N = (P, T, F) where P is finite set of places, T is finite set of transitions and F is set of flow relations where: 1. (Separation) $P \cap T = \emptyset$ 2. (Flow relation) $F \subseteq (P \times T)$ \cup (T \times P) 3.2.2 Workflow Nets Process models in the real life have additional properties to be executable and they are defined in the Workflow net formalization, which is simply a subset of Petri nets. These additional properties can be formalized in [39] as follows: Definition 3.2.2. (Workflow Nets) Let N = (P, T, F) be a Petri net and t is a new identifier not in $P \cup T$. N is a workflow net (WF-net) if and only if: Figure 3.2: Workflow net of Loan Application Process (Variation #1) 1. (Start Node) P contains a source place i where no token can be fired to. 2. (End Node) P contains a sink <u>place o</u> where <u>no</u> token can be fired from. <u>3. (Connectedness) $N^- = (P, T \cup P)$ </u> $\{t\}$, $F \cup \{(o, t), (t, i)\}$) is strongly connected; in other words, there is a <u>directed path between any pair of nodes in N</u>. In simple terms, a Workflow net is a Petri net with a source place to start the process and a sink place to end; furthermore, all nodes are on a path from source place to sink place [30]. In order to illustrate this formalization, the Workflow net for the event log mentioned in Section 3.1 is presented in Figure 3.2. In the figure, places are indicated by circles, transitions are indicated by rectangles, and flow relations are represented by arcs. Workflow nets are representatives of real life processes; however, they can result with processes including deadlocks, live-locks and never-reached activities. In order to avoid process models from these problems, soundness definition is suggested in [30] and it is simplified as follows with the context of this thesis: Definition 3.2.3. (Soundness) Let N be a Workflow net and it is

sound if and only if: 1. (Safeness) Places cannot hold more than one tokens at the same time. 2. (Proper completion) Any marking of net can reach to sink place. 3. (Absence of dead tasks) Net does not contain any dead transitions. In this thesis, Workflow nets are used to discover and present underlying process models of different organizations. Considering the applicability of well-known pro- Figure 3.3: Process Model of Loan Application Process (Variation #1) using BPMN cess mining algorithms on Workflow nets and implementations in ProM Framework [42], Workflow nets are used as the notation for discovery and analysis. 3.2.3 Business <u>Process Modeling Notation (BPMN) Business Process Modeling Notation</u> (BPMN) is one of the most popular and widely used modeling language implemented by many vendors. In addition to its popularity, this notation is standardized by the Object Management Group (OMG) since 2004. In this notation, atomic activities are named as tasks and routing decision logic is imple- mented by gateways. These gateways include split and join gateways with AND, OR and XOR logic operations. In addition, deferred choice pattern is implemented by event-based XOR gateway in BPMN to handle race conditions between tasks that are running parallel [38]. Since the primary goal of BPMN is to provide a standardized notation that is easy to understand by business stakeholders, in this study resulting nets are converted to BPMN diagrams for visual analysis by the plugin implemented in ProM [23]. BPMN diagram of the Workflow net from Figure 3.2 is presented in Figure 3.3. As can be seen from the diagram, gateways help to understand the rela- tions and dependencies of the tasks. 3.3 Process Discovery In process mining field, one of the most challenging tasks is to construct a process model based on the behavior in the event logs, namely process discovery. Many process discovery algorithms are proposed to address different challenges in process discovery and using different notations. However, in this thesis focus of the study is learning from the cross-organizational process mining rather than addressing all process discovery challenges. With this reasoning, Inductive Process Mining [25] is selected as appropriate since it is simple, highly applicable and configurable. In the literature, its derivatives which handles infrequent behaviors [26]; incomplete logs [27]; and model optimization [43] are also available. Inductive Miner (IM), which is proposed as an extensible framework in [25], aims to discover block-structured process models that are sound and well-fitting to the behavior represented in event log. In addition, this approach focuses on creating rediscoverable models that is a significant attribute for this thesis study. Formalization of the key points in the study [25] is as follows: Definition 3.3.1. (Block-structured Workflow Nets) Block-structured WF-nets are subset of WF-nets where the workflow can be divided recursively into parts with single entry and exit points. Definition 3.3.2. (Rediscoverability) Let a process is expressible by a model M which is unknown priori. Given a log L of M, L is a subset of language used to describe model M. M is isomorphic-rediscoverable from L by mining algorithm B if and only if $M \in B(L)$. Framework developed in the study [25] uses a divide-and-conquer approach to dis- cover subprocesses of sublogs obtained by splitting the event log and its main steps can be listed as follows: 1. Activity Sets: Split the activities in log to disjoint sets. 2. Sublogs: Split the log by using activity sets. 3. Recursive Mining: Mine sublogs with these steps until a sublog contains only single activity. In the study [25], an algorithm based on this framework is presented that guarantees returning a sound and fitting process model in finite time. Therefore, this frame- work is selected as appropriate and its extension that can handle infrequent behavior is used within this thesis study to address challenges of different event logs. In real life, most of the cases in the events are samples of frequent behavior; however, there are also infrequent behaviors according to the nature of process execution environment. In real life, these different paths are used infrequently; however, their effect in discovery is still significant. Inductive Miner Infrequent (IMi) is proposed in [26] as an extension to Inductive Miner to handle noise in the event logs. By filtering the infrequent behavior, it is aimed that IMi succeeds with improved models discov- ered. After each recursive step of

IM, filtering is applied if the discovered model is a flower model which represents infrequent behavior. Basic idea behind filtering is set-ting a user-defined threshold between 0 to 1 and with the help of this threshold, both log splittings and mining operations are done on a cleaner subset of logs. When the discovered models compared to IM, IMi results with lower fitness, higher precision and equal generalization. In this thesis study, infrequent behavior capable implemen- tation is used for experimenting the cross-organizational mining of process models with their implementation of ProM framework [42]. 3.4 Process Performance Analysis In the main and traditional tasks of process mining spectrum, event logs are used to discover and enhance process models. In addition to these main tasks, process mining enables to discover relationships between event logs and process models for conformance and performance analysis. Within conformance, any deviations from modeled behavior can be discovered; moreover when the logs are replayed on the models, bottleneck analysis can be undertaken with the help of timestamps on the event logs. However, in order to replay event logs on the process models there is a need for alignment which is formalized in [35]. Formalization and notions presented in the study [35] are based on the assumption that process models and event logs use the same set of activity labels and therefore they can be related. The first notion in alignment of process model and event log is defining the relation- ship between moves in the model and log. The necessity of this notion is based on the fact that some moves in the event log cannot be operated with the process model and vice versa. In the study [35], move and alignment are defined as follows: Definition 3.4.1. (Move) For the event log L, A \perp L = AL \cup { \perp } is defined where x \in AL refers to "move x in log" and \perp refers to "no move in log". Similarly, $A\perp M$ = AM \cup $\{\bot\}$ is defined where $y \in AM$ refers to "move y in model" and \bot refers to "no move in model". One step in alignment is represented as $(x, y) \in \underline{A} \perp L$ \times ALM such that: 1. (x, y) is a move in log if $x \in AL$ and $y = \bot$, 2. (x, y)is a move in model if $x = \bot$ and $y \in AM$, 3. (x, y) is a move in both if $x \in$ AL and $y \in AM$, 4. (x, y) is an illegal move if $x = \bot$ and $y = \bot$. In this AL \vee y \in AM $\}$ Definition 3.4.2. (Alignment) Let σ L \in L a trace in event log L and let $\sigma M \in \beta$ (M) a full execution sequence of process model M. An <u>alignment of σL and σM can be defined as a sequence $\gamma \in ALM*$ where the</u> projection of first element yieldsσL and the projection of second element <u>yields</u>σM. In order to qualify the alignment operations, <u>distance function on</u> <u>legal moves</u> is de- fined <u>in</u> [35] as follows: Definition 3.4.3. (Distance Function) Distance function is defined on legal moves as $\delta \in ALM \to N$ to associate costs to moves in alignment: 1. If $x \in AL$ and $y = \bot$, then $\delta(x, y)$ is the cost of move x in log. 2. If $x = \bot$ and $y \in AM$, then $\delta(x, y)$ is the <u>cost of move y in model.</u> 3. <u>If $x \in AL$ and $y \in AM$, then $\delta(x, y)$ is the <u>cost</u></u> of move x in log and move y in model and this cost is generally $\delta(x, y) = 0$ if x = y. According to this distance function definition, various different functions can be de- fined using costs. For instance, in [35] a standard distance function is defined as no cost when log and model agree and cost of 1 otherwise. In addition, optional align- ment between process model and event logs is defined as follows: Definition 3.4.4. (Optimal Alignment) Let $\sigma L \in \underline{L}$ be a trace in event log L, M a pro- cess model and $\Gamma \sigma L$, $\underline{M} = \{y \in \underline{L}\}$ ALM* | $\exists \sigma M \in \beta(M)$ y is an alignment of σL and σM }. An alignment $v \in \Gamma L$, M <u>is optimal for</u> event <u>log trace</u> σL <u>and model M if for any $\gamma' \in \Gamma \sigma L$,M : $\delta(\gamma')$ </u> $\geq \delta(y)$. This optimal alignment can be found with the help of different approaches and within process mining field, proposed methods [2, 3] are <u>based on A* algorithm</u> which <u>is</u> a path-finding <u>algorithm</u> based on graphs. In principle, any optimization methodology <u>can be</u> used <u>to find</u> the <u>optimal</u> alignment and in this thesis study an A* based im- plementation in ProM Framework [42] is used to find optimal alignments. Although this thesis study has no direct focus on conformance of process models by event logs, these steps were necessary to replay the event logs over process models. With the help of replay, any performance indicator can be calculated to compare performances of cross-organizational processes. Using the timestamp information or resource uti- lization in the event logs,

performance indicators can be discovered while replaying the log after alignment. These performance indicators can include lead time, service time, waiting time in time dimension; and utilization or activity costs in cost dimen- sion [33]. 3.5 Machine Learning and Clustering Machine learning is a study area of computer science which have roots in pattern recognition and computational learning theory of artificial intelligence. Machine learning approaches work on construction and learning from data to make further predictions. There are various approaches proposed in this area and clustering ap- proach will be presented in this section. Cluster analysis is based on assigning the set of observations into subsets (clusters) so that observations within the same clust ter are similar whereas the observations from different clusters are dissimilar, where the similarity criteria is predefined. Clustering is a method in unsupervised learning, where the main problem is learning a hidden structure in unlabeled data. Since the provided data is unlabeled there is no error or reward assignment to the potential so- lutions provided by these approaches; however, quality metrics on clusters are used to evaluate results. With these characteristics, clustering is a common technique in exploratory data mining and statistical data analysis and it is used in many fields like image analysis, information retrieval and bioinformatics. In cluster analysis, various algorithms are proposed with different approaches on defining clusters and how to efficiently find them. Popular approaches are based on the idea of decreasing the distance among the members of same cluster, space density of data space, intervals or particular statistical distributions. Within this thesis study, centroid-based clustering is used in which the <u>clusters are</u> defined <u>by a central vector</u>, <u>which</u> might <u>not be a</u> member of data set. When number of clusters are fixed to k, the approach is named as k-means clustering and the problem is finding k cluster centers and assigning data members to nearest cluster center while minimizing the squared distances of data members to the assigned cluster centers. Although seems easy, this optimization problem is NP-hard and most of the implementations include approxi- mate solutions. A well-known algorithm in k-means clustering is Lloyd's algorithm and it is referred as k-means algorithm and its variation based on random initialization k-means++ are formalized in the study of Arthur and Vassilvitskii [5]: Definition 3.5 .1. kmeans Algorithm 1. Arbitrarily choose initial \underline{k} centers: $\underline{C} = c1$, c2, ...ck 2. For each $i \in 1, ...k$; set the cluster Ci to be the set of points that are closer to ci than they are to cj for all $i \neq j$. 3. For each $j \in 1, ...k$, set ci to be the <u>center of mass of all points in Ci</u> where $\underline{ci} = |C1i| \times Ci \times 4$. Repeat S\Step 2 and 3 until C no longer changes. Definition 3.5.2. k-means++ Algorithm 1. Take one center c1, chosen uniformly from the set of data points X. 2. Take a new center ci, chosen from the set of data points X with probability the closest c∑luster center. 3. Repeat Step 2 until k cluster centers are selected. Figure 3.4: Example of Skipped Activity Pattern 4. Proceed with the 2-4 steps of k-means Algorithm. In this thesis study, clustering of performance analysis results is undertaken and since the number of data instances low, an approach focused on initialization is se-lected. Implementation of k-means++ in WEKA (Waikato Environment for Knowledge Analysis) [20] is used as Java API to call from ProM Framework [42]. 3.6 Mismatch Patterns in Process Models In cross-organizational process mining environment, there is a need to align processes of different organizations and in this scope both the organizations and their processes are similar but have significant differences. In order to align these processes and or- ganizations, there is a need for spotting differences between process models. In the study of Dijkman [13], a collection of patterns to describe frequent mismatches be- tween the similar process models are presented. Mismatch patterns are grouped into three as authorization, activity and control flow mismatch patterns. Authorization mismatch patterns are based on assignment of the same tasks to different roles in dif- ferent processes and left outside the scope of this thesis. Activity mismatch patterns are based on representing the tasks of a process by a different collection of activities in a different process, or not

representing at all. Within the scope of this study, the related activity mismatch patterns are defined in study [13] as follows: Skipped Activity An activity exists in one process but no equivalent activity is found in the other process as illustrated in Figure 3.4. Refined Activity An activity exists in one process but, as an equivalent, a collection of activities are existing in the other process to achieve the same task. An illustration is provided in Figure 3.5. Figure 3.5: Example of Refined Activity Pattern Figure 3.6: Example of Activities at Different Moments in Process Pattern Control flow mismatch patterns are based on using different control-flow relations and dependencies for the same activities in different processes. Within the scope of this thesis study, the following related control flow mismatch patterns are defined as given in [13]: Activities at Different Moments in Processes Set of activities are undertaken with different orders in different processes as shown in Figure 3.6. Different Conditions for Occurrence Set of dependencies are same for two pro- cesses; however, occurrence condition is different. An example is provided in Figure 3.7. Different Dependencies Dependency set of activities differ in different organizations. An example of this pattern is shown in Figure 3.8. Additional Dependencies This pattern is a special case of different dependencies where one set of activities includes the other and results with additional dependencies as illustrated in Figure 3.9. Figure 3.7: Example of Different Conditions for Occurrence Pattern Figure 3. 8: Example of Different Dependencies Pattern Figure 3.9: Example of Additional Dependencies Pattern As mentioned in the study [13], their approach does not create a comprehensive list to resolve all mismatches but the most common ones spotted during case studies. In ad- dition, from their definitions and examples it can be easily seen that these patterns are not orthogonal. Moreover, there are no algorithms provided to spot these mismatches in [13] or consequent studies, and thus implementation of spotting mismatch patterns are kept within the scope of this thesis study. CHAPTER 4 METHODOLOGY In this chapter, methodology proposed in this thesis study is presented. Firstly, ap- proach overview is described from a high-level perspective. Then, each stage in the methodology is presented together with their importance in the study, mathematical representations and definitions; and black-box diagrams. In the last section of this chapter, implementation details of this methodology in ProM framework is explained in detail with a software architecture overview. 4.1 Approach Overview Approach proposed in this study consists of four main stages and general information about these stages can be summarized as follows: Process Model Mining: Process models are extracted from event logs for each organization with a user specified noise threshold. Performance Indicator Analysis: Event logs are replayed on process models and performance indicators are calculated for each organization. Using these indi-cators, organizations are clustered based on how well they are operating. Mismatch Pattern Analysis: Differences between process models of organizations are extracted with a well-established mismatch patterns. Recommendation Generation: Using the performance indicator clusterings and dif- ferences between process models, a set of recommendation for each organiza-tion is generated. Figure 4.1: Overview of Methodology Flow of these stages with the important input and outputs can be visualized in Fig- ure 4.1. In the following sections, each stage will be explained in detail with their mathematical backgrounds. 4.2 Process Model Mining Process model mining stage in the proposed approach has the aim of creating repro- ducible and generalized process models from event logs. In order to achieve this aim, implementation of Inductive Miner Infrequent (IMi), which is proposed in [26] as an extension to Inductive Miner to handle noise in the event logs, is used in this study. The selected implementation has the ability of pruning data to handle noise in the event logs. Like the other data mining approaches, event logs include data related to the infrequent behaviors occurred in real life. Although these infrequent behaviors might be caused by important structural or case related issues that should be analyzed; they make the process of mining and results more complex. Within the scope of this study, without cleaning the data, most of the process model mining

further analyze. Since this thesis focuses on learning from the crossorganizational process mining rather than creat- ing the best-fitting process models, data cleaning and noise handling is a necessary step. Therefore preprocessing steps are undertaken with a compatible approach of Inductive Miner Infrequent (IMi), where data is cleaned in every inductive step. Considering the scope of this study, instead of computational details of Inductive Miner Infrequent (IMi); black-box representation is used to explain its usage in the methodology. In order to set a filtering threshold, a user-provided value between 0 to 1 is added as input to method in addition to event logs. As a result, workflow net Figure 4.2: Process Model Mining Stage as Black-box is produced which is a sound and properly completed Petri net without deadlocks. Black-box of this stage is illustrated in Figure 4.2 and this stage is called for every organization's event logs to create their own process models in Workflow net formal- ization. 4.3 Performance Indicator Analysis Performance indicator analysis stage focuses on calculating and analyzing the perfor- mance values using the event logs and mined process models. This stage consists of mainly two concepts as a) alignment and calculation of performance indicators; and b) clustering of organizations based on their performance values. In order to evaluate the performance of an organization based on their process models and past activi- ties; there is a number of indicators in time dimension, cost dimension and utilization [33]. However, in this study, process related performance values are considered since differences in the process models are studied in the next stages. With this reason-ing, the following performance indicators are calculated and analyzed in this stage of methodology: Average Time Between Activities For each activity in the process model, average time to reach other activity is calculated. This is a simple but powerful perfor- mance metric for organizations since it can yield the average time to complete one task based on a starting point. From the performance perspective, orga- nizations want to minimize average time between activities to increase their throughput [35]. This notion can be defined as follows: Definition 4.3.1. Average time between activity A and B in organization i is AvgT imeiA→B = Case c∈EventLogi T imeBetweenc(A, B)/|OccurencesEvent Logi(A, B)| where Σ 1. T imeBetweenc(A, B) = EndT imec(B) - StartT imec(A) 2. StartT imec(A) isstart time of activity A in case c, 3. EndT imec(B) is end time of activity B in case c, 4. |OccurencesEventLogi (A, B)| is number of occurrences of activity A fol- lowed by B in Event Logi. Standard Deviation of Time Between Activities Time between activities in real life is not stable and they deviate due to various reasons such as people responsible of tasks, size and the content of tasks or seasonality [33]. On the other hand, organizations want to be confident about their processes and therefore they want to minimize the deviation in the time between activities. Minimized deviation in time helps organizations to plan, act and re-organize the activities in the pro- cesses with high accuracy [35]. With the same approach above, the following formulation can be defined: Definition 4.3.2. Standard deviation time between activity A and B in organi- zation i is StdDevT imeiA \rightarrow B = Case c∈EventLOocgciu[TriemnceeBsEetvweneetnLco(qAi(,BA,)B−)AvqTimeiA→B]2 $\sqrt{\Sigma}$ In addition to average and standard deviation, minimum and maximum times between activities can also be analyzed. However, these performance values are mostly result of rare cases in the event logs and these rare occurrences have the probability of being eliminated as noise in process mining stage. Therefore, the minimum and maximum values have the risk of not representing the actual performances. Thus, only average and standard deviation of the time between activities are selected in the study. 4.3.1 Replay and Performance Indicator Calculation Replay of event logs on process models is based on the idea of alignment which is formalized in [35] and the basic assumption in this concept is that process models and event logs have the same activity labels. Alignment is based on moves in the model and log and in order to have a successful replay where optimal

alignment should be achieved. As proposed in [2, 3], A* algorithm which is

approaches result with spaghetti-like models [33] which are difficult to

a path-finding algorithm based on graphs is used to find optimal alignment of event logs on the process models. In order to appropriately apply A* algorithm, there are number of manual and com- putational steps that should be undertaken. The following prerequisite steps are im- plemented in [3] to apply A* algorithm: Set Label Patterns between Process Model and Event Log: In the event logs, there are various different transitions of the same activity which are generally not rep- resented in process models. For instance, there can be "Activity A, Start" and "Activity A, End" in the event log; however they are reflected as "Activity A" in the process model. Therefore, a list of all transitions and events are asked to the user to match to the ones in the process model in terms of patterns or regular expressions. Create Initial and Final Markings: In case of there is no definite starting or ending point in the process model, user input is necessary to define these activities. Set Cost Values: Since A* algorithm is based on alignments which are basically moves along process models and event logs, the following cost values for each move is necessary to be set: a) move on process model, b) move on event log; and c) synchronous move. In order to use replay as an intermediate stage in this thesis, some of the mentioned steps are automatized with the help of the assumptions in the prior and post stages of methodology. With this reasoning, initial and final markings are created with the first and last activities in the process models. In addition, since there is no explicit priority of process model over event log or vice versa, cost values are set to 1 for both move on process model and move on event log. Since there is no penalty for synchronous moves, its cost value is set to 0. However, since each event log has different set of transition labels, manual user input is still necessary to map label patterns between process model and event log. With the generated and user-specified inputs, replay and performance indicator calculation in the methodology can be visualized in Figure 4.3. Figure 4.3: Replay and Performance Indicator Calculation Stage as Black-box For each organization, the steps in the diagram are followed with the corresponding event logs and process models; and the resulting process summaries are used for further analysis. Performance summary calculation step at the end of this stage is used to create a summary of data consists of average and standard deviation of time between activities. Resulting data can be defined as follows: Definition 4.3.3. Performance Summary data for any organization i is P erf S umi = {Av q T imeS umi ∪ S tdDev T imeS umi } where 1. Av g T imeS umi = {Av g T imeiA \rightarrow B |A, B \in E v ent Logi } 2. S tdDev T imeS umi = {S tdDev T imeiA→B |A, B ∈ E v ent Logi } 4.3.2 Performance Indicator Clustering Clustering is based on the idea of collecting the set of observations into clusters so that observations within the same cluster are similar whereas the observations from dif- ferent clusters are dissimilar. Being an unsupervised learning method, it aims to find hidden structures in unlabeled data. In this thesis study, clustering is used to gather organizations based on their performance indicator data. In other words, organiza- tions will be set into groups based on how much time in average and with variation takes to complete an activity given a starting point. Within clustering analysis, various algorithms are proposed to find clusters based on the idea of decreasing in-cluster distances, increasing space density or fitting to particular statistical distributions. However, in this study, a generic approach based on centroid-based clustering is exploited. For the fixed number of k clusters, the approach is well-known as k-means clustering. Considering the popularity of this approach and its extensions, random initialization based k-means++ approach from the study of Arthur and Vassilvitskii [5] is used to cluster organizations. Clustering methods can be evaluated by the internal and external methods. Internal methods are based on the data that is clustered itself whereas external methods use the additional information such as labels or benchmarks. Although there are various well- established metrics in external methods such as Rand Measure, F-measure, Jaccard index or Confusion Matrices; in this thesis study there is no pre-labeled organizations based on their performance indicators. Therefore, internal evaluation methods are used to assess the quality of clusters. Considering

the fact that actual data to cluster is time interval and centroid-based clustering is applied in this study, a metric based on decreasing the incluster distances is selected. With this consideration, Sum of Squared Error (SSE) is calculated with the following definition. When the clustering results are compared, it is reasonable to choose the one with the least SSE; however, it is a fact that as k converges to the number of original sample size SSE value decreases. Therefore, SSE values and number of clusters are plotted and presented to the end user of the methodology to select optimal number of clusters. Definition 4.3.4. Sum of Squared Error (SSE) is SSE = ki=1 $x \in ci$ EuclideanDistance(meani, x)2 where $\sum \sum 1$. x is a data point in cluster ci. 2. meani is the mean vector of the cluster ci. For each organization, Performance Summary data is used as the data source in clus- tering. It is aimed that the organizations with the similar average or standard deviation time between tasks will be assigned to same sets to further reveal the dissimilarities that the other clusters can learn from. Since not every activity exists in every organi- zation, performance summary data is cleaned and merged to include only all shared activities. This cleaning step removes the non-existing activity related performance indicators from all the organizations so that clustering is applied on the data with no process model related information. Since number of clusters are not known priori, k- means clustering is applied starting k from 1 to the number of organizations. For each clustering with different number of clusters, SSE values are plotted and user is made to select the appropriate cluster size. For the selected cluster size, clustering related information is used to generate recommendations in the further steps. This stage of methodology can be visualized as an input-output system in Figure 4.4. Resulting cluster analysis data is formulated as follows: Definition 4.3.5. Cluster Analysis Data is a tuple (k, Assignments, Cluster Centroids) where 1. k is the number of clusters, 2. Assignments is a set of tuple (Organizationi, Clusterj) where i is identifier for organization and $j \le k$ is identifier for cluster, 3. Cluster Centroids is a set of tuple (Clusterj, Type, Astart, Aend, V alue) where (a) Type is performance indicator type which is Average or StandardDev, (b) Astart and Aend are starting and ending points of performance indicator, (c) V alue is the actual value of performance indicator, (d) Cluster Centroidsj is a function that returns a set of Centroid which is a tuple (Type, Astart, Aend, V alue) for Clusterj. 4.4 Mismatch Pattern Analysis In order to learn from other organizations, it is necessary to spot the differences be- tween process models of different organizations. In this phase of methodology, dif- ferences between process models will be revealed by the mismatch patterns which are defined by Dijkman [13]. In the process mining stage, process models are mined Figure 4.4: Performance Indicator Clustering Stage as Black-box to create Workflow nets; however, mismatch pattern definitions are closer to business environment and it is more suitable spot patterns in BPMN notation. Thus, mined process models are converted to BPMN models and then mismatch pattern analysis is applied. After spotting differences, mismatch patterns for activities and control flows are revealed for the organizations. Business Process Modeling Notation (BPMN) is one of the widely accepted modeling language in the industry and its a standardized notation by the Object Management Group (OMG) since 2004. Main aim of BPMN is to provide a notation that is eas- ily understood by business stakeholders. In the preceding stages, Petri nets and their subset as Workflow nets are used for mining since they have stronger mathematical background. However, in this stage, BPMN formulation is used since mismatch pat- terns have roots in real-life business environment [13]. The following definition and conversion are defined in the study [23] and they are used in the mismatch pattern analysis. Definition 4.4.1. A BPMN model is a tuple BPMNmodel = (N,A,GXOR,GAND,estart,Eend,SF,λ), where 1. N is a set of flow nodes, 2. A \subseteq N is a set of activities, 3. GXOR \subseteq N, GAND \subseteq N are sets of exclusive and parallel gateways, 4. estart $\in N$ is a start event, 5. Eend $\in N$ is a set of end events, 6. Sets A, GXOR, GAND, {estart}, Eend form a partition of N, 7. SF $\subseteq N \times N$ is a set of sequence flows, 8. $\underline{N} : N \to UA$ is a labeling function, where UA is some universe of activity labels, 9. Start event estart does not

have incoming sequence flows and more than one outgoing sequence flows, 10. End events Eend do not have outgoing sequence flows. Definition 4.4.2. Constructing BPMN Model from Petri nets, which are N = (P, T, F) where P is finite set of places, T is finite set of transitions and F is set of flow relations to BPMN models consists of the following steps: 1. Initialize BPMN model with a start node estart. 2. Convert all transitions, T, in the Petri net by creating an activity in BPMN model for each transition in Petri net. 3. Convert all places, P, from Petri net to BPMN routing constructs by finding the corresponding sequence flows. For each organization, mined process models are converted to BPMN models and mismatch patterns analysis is undertaken on them, in order to locate differences be- tween two process models or cluster of process models. In addition, since perfor- mance indicators are calculated based on a starting and ending points in the process model, same approach is applied to locate mismatch patterns. In other words, differ- ences of process models are located through a starting activity to an ending activity. When the complete set of mismatches between process models are required, this ap- proach is used with starting and ending points as source and sink activities. Mismatch patterns are formulated and their importance in the methodology are listed as following: Skipped Activity Skipped activities are the operations that are not undertaken with some of the organizations. In business environment there could be various dif- ferent reasons for an organization to exclude any activity in their process flows which are followed by other organizations. Therefore, this mismatch pattern should not be utilized solely but taken in to care with the other patterns. In this study, for each organization a list of activities that they do not include are listed as Skipped Activity with the following definition. In addition, these differences are checked for the activities with a particular start and end point. Definition 4.4.3. Skipped Activity pattern is a tuple Skipped Activity = (O, SA, Astart, Aend) where 1. O is the identifier for organization, 2. BPMN model of organization is BP M NO and BP M N* is the set of all BPMN models in analysis, 3. SA is a set of skipped activities and SA = BP M N*(A) \ BP M NO(A), 4. Astart and Aend are starting and ending points to check mismatch patterns and Astart, Aend ∈ BP M NO(A). Definition 4.4.4. Skipped Activity Analyzer is a function SkippedActivityAnalyzer(O, Astart, Aend) and it returns a Skipped Activity for the organization O and the activities between Astart and Aend. Refined Activity Refined activities exist in one process; however, as equivalent a collection of activities are undertaken in another organization's process to achieve the same task. Since there is no activity ontology information is kept in event logs and process models, there is no direct way to define whether the tasks can be classified as other tasks' refined state. In this study, assuming the labels of activities are correct and explanatory about their enclosures, similarity between labels are utilized for this aim. Using Levenshtein distance, which is very pop- ular in information retrieval area and also known as edit distance, similarity of activity labels are calculated for each activity in respect to activities of other or- ganizations' process models. This mismatch pattern presents information about the similar but not same activities in different process models which can be used to make organizations learn from each other. With a user-defined threshold for similarity based on the nature of business environment, most similar tasks can be listed for being refined. Definition 4.4.5. Refined Activity pattern is a tuple Ref ined Activity = (O1, O2, RA, SimilarityM ap, Astart, Aend) where 1. O1 is the first organization where the refined activity is undertaken with the BPMN model of BP M NO1, 2. O2 is the second organization where a collection of activities checked for similarity with the BPMN model of BP M NO2 , 3. RA is the refined activity and RA \in BP M NO1 (A) and RA \in / BP M NO2 (A), 4. SimilarityM ap is a set of tuples (SimilarityV alue, B) where Similarity V alue indicates the similarity between RA and B \in BP M NO2 (A), 5. Astart and Aend are starting and ending points to check mismatch patterns and Astart, Aend ∈ BP M NO1,2 (A). Definition 4.4.6. Refined Activity Analyzer is a function Ref inedActivityAnalyzer(O1, O2, Astart, Aend) and it returns a set of Refined Activity for the organization O1 compared to O2 for the activities between Astart and Aend. Activities at

Different Moments in Processes Activities at different moments means that organizations are undertaking activities at different orders in their process flows. This mismatch pattern indicates that the organizations could achieve the same task when they change the order of activities and this information can be used by others to enhance their process models. Therefore, formulation of this pattern includes an activity; and its previous and next tasks at different organi- zations. Definition 4.4.7. Activities at Different Moments in Processes pattern is a tuple Dif f erent M oments = (O1, O2, A, Prev1, Next1, Prev2, Next2, Astart, Aend) where 1. O1 is the first organization with the BPMN model of BP M NO1 , 2. O2 is the second organization with the BPMN model of BP M NO2 , 3. A is the activity that is undertaken in different order and A ∈ BP M NO1,2 (A), 4. P rev1, N ext1, are previous and next tasks of A in O1 and P rev1, N ext1 ∈ BP M NO1 (A), 5. P rev2, N ext2, are previous and next tasks of A in O2 and P rev2, N $ext2 \in BP M NO2 (A), 6.$ In order to ensure different moments P rev1 \neq P rev2 or N ext1 \neq N ext2, 7. Astart and Aend are starting and ending points to check mismatch patterns and Astart, Aend ∈ BP M NO1,2 (A). Definition 4.4.8. Different Moments Analyzer is a function Dif f erentM omentsAnalyzer(O1, O2, Astart, Aend) and it returns a set of Dif- ferent Moments for the organization O1 compared to O2 for the activities between Astart and Aend. Different Conditions for Occurrence Different conditions for occurrence take place where an activity has the same dependencies in different organizations but with different conditions. For instance, an organization needs to complete all depen- dency tasks before starting the next one; though another organization checks for the completion of only one of these dependencies. This difference between organizations can lead to loosening or tightening of the conditions based on the application of other organizations. Considering the representation of different conditions for occurrence and other control flow mismatch patterns, a generic definition is developed firstly to use and further customize. Different conditions for occurrence pattern definition is developed based on this generic definition as following. Definition 4.4.9. Control Flow Mismatch pattern is a tuple Control F low M ismatch = (O1, O2, A, P rev1, G1, P rev2, G2, Astart, Aend) where 1. O1 is the first organization with the BPMN model of BP M NO1 , 2. O2 is the second organization with the BPMN model of BP M NO2 , 3. A is the activity that is in front of control flow and $A \in BP M NO1,2 (A), 4. P rev1 and P rev2 are$ set of tasks that are connected to gateway G1 and G2 in organizations O1 and O2 respectively with the following requirements: 41 (a) P rev1 ⊂ BP M NO1 (A), (b) P rev2 \subset BP M NO2 (A), (c) G1 \in BP M NO1 (GXOR, GAND), (d) $G2 \in BP M NO2$ (GXOR, GAND). 5. Astart and Aend are starting and ending points to check mismatch patterns and Astart, Aend \in BP M NO1,2 (A). Definition 4.4.10. Different Conditions for Occurrence pattern is a Control Flow Mismatch where 1. P rev1 = P rev2, 2. G1 \neq G2. Definition 4.4.11. Different Conditions Analyzer is a function Dif f erentConditionsAnalyzer(O1, O2, Astart, Aend) and it returns a set of Different Conditions for Occurrence for the organization O1 compared to O2 for the activities between Astart and Aend. Different Dependencies When the dependency set of a specific activity is different in organizations, it can be concluded that this activity and the relation between its dependency sets should be reviewed since it can be achieved in both en- vironments. Organizations can learn from each other to eliminate or enhance their process flows by changing these dependency sets. This can include reorganization of activities as well as removing and adding new activities. The idea is structured in the following simplified definition. Definition 4.4.12. Different Dependencies pattern is a Control Flow Mismatch where 1. P rev1 ≠ P rev2, 2. G1 = G2. Definition 4.4.13. Different Dependency Analyzer is a function Dif f erentDependencyAnalyzer(O1, O2, Astart, Aend) and it returns a set of Different Dependency for the organization O1 compared to O2 for the activities between Astart and Aend. 42 Figure 4.5: Mismatch Pattern Analysis Stage as Black-box Additional Dependencies Additional dependency pattern is a special case of Dif- ferent Dependencies where additional tasks are required in one organization in order to start an

activity. These additional dependencies can include pro- visional tasks that are related to the original activity such as checking system before starting application. Definition 4.4.14. Additional Dependencies pattern is a Different Dependen- cies Mismatch where P rev1 \subset P rev2 or P rev2 \subset P rev1. Definition 4.4.15. Additional Dependency Analyzer is a function AdditionalDependencysAnalyzer(O1, O2, Astart, Aend) and it returns a set of Additional Dependency for the organization O1 compared to O2 for the activi- ties between Astart and Aend. Mismatch pattern analysis stage in methodology can be visualized as a black-box diagram in Figure 4.5. Each organization's mined process models are converted to BPMN models and these models are sent to mismatch pattern analyzers with the starting and ending activities. For each organization, mismatch patterns are gathered and stored for the further analysis as presented in Algorithm 1. 4.5 Recommendation Generation Recommendation generation stage in the methodology is the final and core stage where all information retrieved from event logs until now are utilized. Until this point, all event logs are used to mine process models of each organization and then these Algorithm 1: Mismatch Pattern Analysis Input: O1 first organization, O2 second organization, Astart starting activity, Aend ending activity Output: MismatchPatterns a set of mismatch patterns 1 MismatchPatterns \leftarrow {} 2 MismatchPatterns ← SkippedActivityAnalyzer(O1,Astart,Aend) 3 MismatchPatterns ← RefinedActivityAnalyzer(O1,O2,Astart,Aend) 4 MismatchPatterns ← DifferentMomentsAnalyzer(O1,O2,Astart,Aend) 5 MismatchPatterns ← DifferentConditionsAnalyzer(O1,O2,Astart,Aend) 6 M ismatchP atterns ← Dif f erentDependencysAnalyzer(O1,O2,Astart,Aend) 7 M ismatchP atterns ← AdditionalDependencysAnalyzer(O1,O2,Astart,Aend) 8 return M ismatchP atterns event logs are replayed on the process models to calculate performance indicators. Following these steps, the organizations are clustered based on their performance in- dicators and mismatches between their process models are listed. In this stage, clus- tering results, which are performance indicator vectors for each cluster will be used to generate recommendations for each cluster of organizations based on the differences between their mismatch patterns. In this study, idea of recommendation is based on providing a set of mismatch pat- terns for each organization so that they can enhance their processes. These mismatch patterns are generated by comparing the process models of other organizations, par- ticularly which are performing better in terms of their performance indicator values. In addition, clustering of organizations is undertaken to generalize the way of identi- fying which organizations perform better in this environment. Recommendation idea and recommendation generation function is defined as following: Definition 4.5.1. Recommendation is a tuple Recommendation = (O, Astart, Aend, M ismatch P atterns) where 1. O is identifier for organization, 2. Astart and Aend are starting and ending activities in between the recommenda- tions are checked, 3. M ismatch P atterns is collection of mismatch patterns. Definition 4.5.2. Recommendation generation is a function that is RecGen(O, C, P) and it returns a set of Recommendation where 1. O is identifier for organization, 2. C is Cluster Analysis Data which is result of cluster analysis stage, 3. P is Performance Threshold which is a real number larger than or equal to 0 and it is calculated over the same type of performance indicators of different organizations in Cluster Analysis Data. Algorithm of recommendation generation function is based on the idea of checking other clusters for a significant change in performance indicators, where significance is defined by the threshold provided by user. After finding significant difference, all organizations in other clusters are checked against mismatch patterns with the start- ing and ending activities defined in performance indicators. With this constraining, only mismatches which are located between the activities that causes high level of difference in performance indicators are analyzed. This approach is formalized in Algorithm 2. This stage of methodology can be visualized as gathering inputs of mismatch patterns data and cluster analysis data in Figure 4.6. In addition, a performance difference threshold is gathered from the user to specify how much difference between clusters is necessary to check for

mismatch patterns and generate recommendations. This stage generates recommendation data for each organization which contains a set of mismatch patterns. Algorithm 2: Recommendation Generation Input: O organization, C Cluster Analysis Data, P performance difference threshold Output: Recommendations a set of recommendations 1 Recommendations \leftarrow {} 2 i \leftarrow C (Assignments(O)) 3 for C entroid ∈ C (C lusterC entroidsi) do 4 for Centroid' \in C(ClusterCentroidsj) i \neq j do 5 if Centroid(Astart) = Centroid'(Astart) & Centroid(Aend) = Centroid'(Aend) then 6 if (|Centroid(V alue) - Centroid'(V alue)| ÷ Centroid(V alue)) ≥ P then 7 Astart ← Centroid(Astart) 8 Aend ← Centroid(Aend) 9 MismatchPatterns ← {} 10 for $O' \in C(Assignments(j))$ do 11 MismatchPatterns \leftarrow MismatchPatternAnalysis(O,O',Astart,Aend) 12 Recommendations ← Recommendation(O,Astart,Aend, MismatchPatterns) 13 return Recommendations Figure 4.6: Recommendation Generation Stage as Blackbox 4.6 Implementation in ProM Framework Methodology of this thesis study is implemented in ProM [42], which is an exten-sible framework that supports a wide variety of process mining techniques in form of plugins. ProM is an open source framework for process mining algorithms which provides a platform to users and developers. Aim of this framework is to create a standard process mining platform that is accepted in industry and academia with an active community. Approach of this thesis study is implemented with its each stage as a standalone plugin that enables extensions for further studies. Developed set of plu- gins are packaged with the name of CrossOrgProcMin1 and published open-source2 being available in the latest version of ProM release. Implementation details are presented from two perspectives in this section. Firstly, software architecture of implementation will be explained with the relationships and dependencies with the other plug-ins and ProM framework. Then, user experience perspective will be presented to show how the end user of this methodology can pro- vide inputs, make analysis and gather results. 1 http://www.promtools.org/prom6/packages/CrossOrgProcMin 2 http://github.com/onuryilmaz/cross-org-proc-min Figure 4.7: Software Architecture for Cross-Organizational Process Miner 4.6.1 Software Architecture Approach of this study is divided into stand-alone stages where inputs and outputs between them are defined strictly. With the help of this understanding, each stage is developed as a stand-alone plug-in in ProM framework which can be called sep- arately. For this aim, five plug-ins are developed which are visualized in Figure 4.7 to provide a high-level perspective. In addition, a set of utilities are developed to visualize and persistence of data in ProM environment. Cross-Organizational Process Miner Plugin is the core plugin which handles man- agement and data flow between other plugins. It basically calls each other plu- gin and gathers outputs from them to proceed to next stages. Process Miner Plugin is the implementation of Section 4.2 where Inductive Miner [26] package in the ProM environment is utilized. Automated Replayer Plugin is developed to execute the approach in Section 4.3.1 and it replays the event logs over process models using the libraries in PNRe- player package [3]. Cluster Analysis Plugin aims to cluster the organizations based on their performance indicators as presented in Section 4.3.2 and this plugin uses WEKA libraries [20] which are external to the ProM environment. Mismatch Analysis Plugin is developed to discover differences between the process models as explained in Section 4.4. This plugin is developed from scratch since there is no implementation of mismatch patterns [13] in ProM framework. Utilities are developed to handle data operations of the plugins in CrossOrgProcMin package. Import and export libraries are used to enable data specific persistence in ProM framework for these plugins. Visualization libraries are developed to represent the recommendation output to the end user in ProM screens. 4.6.2 User Experience Approach proposed in this study is a composition of different stages and it is very difficult for an end user to be capable of each step's details. Therefore, the plug- ins are developed with a high level of automation by minimizing the manual inputs required. In addition, each reporting step is well-documented so that user can easily understand and provide inputs without help of another guide. In

this section, example screens will be presented to explain the story of end user for the developed plug-ins. Assuming the user is familiar with the ProM framework, only the steps specific to the developed plug-ins are illustrated. Intermediate steps are included in Appendix A.1 and result screens are presented in this section. When the user selects a number of event logs and starts Cross-Organizational Process Miner, an informative screen about the plugin and the following steps are presented to the user as shown in Figure A.1. Following this screen, user is required to provide names for organizations of the event logs in a very simple form as can be seen in Figure A.2. This step is added to provide user-friendly reports in the following stages with the names provided. In the stage of process mining, for each organization, user is expected to provide a noise threshold and naming convention which is illustrated in Figure A.3 and this screen is an extension of Inductive Miner [26] screens. Fol-lowing this, in the replay stage, user input is required for matching activity names in Figure 4.8: Select Cluster Size Screen of Cross-Organizational Process Miner Plugin the event logs to process models as shown in Figure A.4 and this screen is derived from PNReplayer package [3] screens. When replay stage is completed, clustering of organizations based on performance indicators starts and user input is required for selecting the appropriate cluster size (k) with the SSE values plotted as shown in Figure 4.8. With the successful execution of plugin, recommendation outputs are presented to the end user. Recommendations are visualized in two ways to create comparable outputs with and without performance clustering. When the user selects to check mismatch patterns without performance clustering, an organization should be selected at the left top of the screen in Figure 4.9. For the selected organization, all other organizations are compared and mismatch patterns are listed in separate tabs as shown in the main panel of Figure 4.9. Main idea behind adding this visualization is to provide an insight to user that how much mismatch patterns can be discovered between organizations when no performance clustering is applied. When the user selects to check mismatch patterns with performance clustering, in addition to organization, performance difference threshold should be selected. For Figure 4.9: Mismatch Patterns without Performance Clustering Screen of Cross-Organizational Process Miner Plugin the selected organization's cluster, all performance indicators are listed as tabs in the main panel as visualized in Figure 4.10. For each performance indicator, difference percentages between clusters are tabulated and highlighted if there is any other cluster that performs better than the threshold. For the clusters performing better than threshold, mismatch patterns between the organizations of these clusters are listed in the second level tabs. This visualization aims to list mismatch patterns for an organi- zation, compared to other clusters which perform better than the difference threshold. Figure 4.10: Mismatch Patterns with Performance Clustering Screen of Cross-Organizational Process Miner Plugin CHAPTER 5 RESULTS AND DISCUSSIONS In this chapter, methodology presented in this thesis study is applied on datasets and results are presented. Firstly, evaluation metrics are defined for each stage of method- ology to assess the performance of approach. Following this, methodology is applied on two datasets and results are explained with discussions. 5.1 Evaluation Metrics Approach in this study is an aggregation of various methods and they are significantly different from each other in their mathematical background. Therefore, instead of a global evaluation metric for the complete methodology, each stage will be evaluated within its evaluation metrics. Since these stages are executed sequentially, it is im- portant for each stage to perform well enough to yield a successful outcome. In this section, evaluation metrics for each stage are presented and they will be used to de-termine the success of methodology on experiments. 5.1.1 Process Model Mining Process model mining stage takes input as event logs of organizations and creates process models using process mining algorithms, which is Inductive Miner [26] in this thesis. Performance of this stage can be measured by the conformance of the process models to the event logs. Four competing quality criteria are defined in [33] as fitness, simplicity, precision and generalization for

process model mining. Fitness is based on the idea of being able to replay event log over process model whereas pre- cision focuses not underfitting the event log. Simplicity idea is based on the fact that the simplest model is the best model, on the other hand generalization supports not overfitting the event logs. These four competing criteria are mathematically defined in [29] and grouped into two dimensions for analysis purposes: Fitness Event log and the process model should fit to each other, in other words process model should be able to parse the event log. Appropriateness Since fitness does not provide information about the meaningful- ness of process models, this dimension is defined. Two notions comprise this idea; Structural Appropriateness considers the simplicity whereas **Behavioral** Appropriateness analyzes balance between overfitting and underfitting. In this thesis study, process model mining stage will be evaluated by the Fitness and Appropriateness of the mined process models for each organization. It is expected to have higher fitness, closer to 1, and a high level of appropriateness to continue to the next stages with the high quality process models. While evaluating, fitness will be more dominant since appropriateness without fitness results with irrelevant process models. 5.1.2 Performance Indicator Analysis Performance indicator analysis stage consists of two parts as replaying event logs over process models and clustering organizations based on the performance indicators. In the replay phase, main operation is to align [35] event logs and process models. This alignment is the based on the idea of finding the optimal alignment where total cost of move on process model and move on event log are minimized. Since there is no baseline information for alignment costs of organizational logs, total cost information will be used together with the process model mining evaluation metrics. In other words, for the event logs and process models with known conformance metrics, total cost of alignments will create a secondary check if there are any problems related to replaying events over process models. It is expected to have less total cost of alignment for the organizations with higher conformance since it is easy to align event logs and processes with higher fitness values. For the second stage of performance indicator analysis, there is a need to evaluate performance of clustering organizations. In this stage, organizations are clustered based on their performance indicator values that are calculated over replaying. Since there is no labeled data in the context of this thesis study, any cross-validation techniques could not be applied and thus internal evaluation metrics are exploited. As mentioned in the Section 4.3.2, within-SSE values for clusters are plotted to the end user to select an appropriate number of clusters. It is expected that within-SSE values decreases as number of clusters increases; however, number of clusters should be selected without causing overfitting. 5.1.3 Mismatch Pattern Analysis Mismatch pattern analysis stage aims to find differences between the process models of different organizations. In this thesis study mismatch patterns presented in [13] are mathematically defined and analyzers are developed to locate these patterns. At the time of this study, it is known to be first to use mismatch patterns in a generic method, therefore evaluation is based on comparing with well-defined prior similarity metrics. Structural similarity between process models is presented in [14] by the graph-edit distance notion. In graph theory, graph <a>-edit distance is the minimum number of graph-edit operations necessary to get one graph from another. In process mining field, graph-edit operations are simply node addition, deletion or substitution. In the study [14], both graph-edit distance and graph-edit similarity definitions are provided with their mathematical background. In this study, mismatch pattern analysis stage is evaluated by comparing the number of mismatch patterns and the graph-edit similar- ity of process models. Without any performance indicator clustering, it is expected to have larger number of mismatch patterns when the similarity between process mod- els is low. This will ensure the performance and suitability of using mismatch pattern analysis to spot differences of organizations' process models in the methodology. 5.1.4 Recommendation Generation In the recommendation generation stage, set of mismatch patterns are presented to end user based on the selected organization and

performance difference threshold. This stage aims to list whole mismatch patterns that can cause the other organiza- tions perform better than a difference threshold. Idea of using performance threshold should be evaluated in this stage with its responsiveness. In other words, it is expected that this stage will help the end user to focus on the most important performance im- provements for the organization analyzed. Therefore, different threshold values will be tried to check how many mismatch patterns are generated for organizations and how they could be used for focused analysis. In addition, quality and applicability of the recommendations should be analyzed and this requires a high level of special- ization. Knowledge required to analyze recommendations should include know-how about process changes, domain knowledge about the field of organizations' activity and structural attributions of the organizations. 5.2 Dataset Selection Cross-organizational mining aims to find cross-correlation of workflows and activi- ties in different organizations and this yields the necessity of organizations that do the same main activity with comparable process flows. From the business environment point of view, this field needs alignment of the tasks from different organizations with different business needs, priorities and organizational structures and culture. Consid- ering these characteristics, there are few dataset available in the literature that are well-structured, documented and valuable. In this thesis study, one synthetic and one real-life event log datasets are presented and used in the following sections to evaluate the performance of the proposed methodology. Loan Application Process [6] This synthetically created dataset consists of event log variants of a simple loan application in a financial institute. In this appli- cation process, a customer fills a form and starts a request over website and it triggers the different approaches of variants in different organizations that ends with notifying the customer about the acceptance of application. This dataset includes artificial event logs of 4 variants where each variant includes differ- ent sets of approaches such as parallelism, choices and sequential tasks. These event logs are <u>used to</u> test <u>different</u> approaches <u>of</u> discovering <u>a</u> configurable process model from a collection of event logs [7]. Environmental Permit Application Process [11] This dataset originates from the "Configurable Services for Local Governments (CoSeLoG)" project [31] which investigates the similarities and dissimilarities between several processes of different municipalities in Netherlands. Dataset contains records of receiving phase for the building permit application process in 5 municipalities, which are comparable since activity labels in the different event logs refer to the same ac- tivities performed in five municipalities. This dataset is also mentioned in the literature as "Processing applications for building and/or environmental per- mits (Wet Algemene Bepalingen omgevingsrecht (WABO) in Dutch)". When the organizations that have similar processes are considered, municipal- ities are one of the prominent candidates. In Netherlands there are more than 400 municipalities and they offer between 400 and 500 different products and services with their own processes. Unlike corporations, municipalities have the advantage that they can seek for collaboration since they are not direct com- petitions [10] and this advantage makes them valuable for cross-organizational analysis. CoSeLoG research project aims to develop a business process man- agement system within a shared Software-as-a-Service environment using the commonalities between the processes of municipalities [7]. In the scope of CoSeLoG research, five different processes of municipalities are analyzed and at the time of this thesis study only Environmental Permit Application Process dataset is publicly shared. 5.3 Loan Application Process 5.3.1 General Information In this section, methodology proposed in this thesis study will be applied on the Loan Application Process dataset [6] and evaluation results will be presented. Statistical Table 5.1: Statistical summary of Loan Application Process dataset Cases Events Percentage Variant #1 100 590 24 % Variant #2 70 420 17 % Variant #3 200 800 33 % Variant #4 105 630 26 % Total 475 2440 information about this dataset is presented in Table 5.1 to provide an insight about this dataset. As shown in Table 5.1, total of 475 cases and 2440 events included in this dataset with a

fairly even distribution between variants. In the following section, these variants will be used as organizational logs and the methodology presented in this thesis study will be applied. 5.3.2 Methodology Stages In Process Model Mining stage, variants of the dataset are used as organizational event logs and they are used to mine process models. Since dataset is synthetically generated, noise threshold in Inductive Miner is set to 0 and perfect log fitness is ensured. Appropriateness and fitness evaluation metrics are summarized in Table 5.2 and it can be seen that each event log is successful in terms of representing reality and being appropriate as a process model. Especially for the variants other than Variant #1, there is a perfect fitness and appropriateness as it is expected from a synthetically generated dataset without noise. In addition, process models for each event log is visualized in Figure 5.1. In Performance Indicator Analysis stage, firstly event logs are replayed over pro- cess models and performance indicators are calculated. For replaying step, alignment costs should be checked with respect to process model mining evaluation metrics; however, since all fitness values of variants are 100 % in Table 5.2, corresponding alignment costs are 0 for this dataset. This ensures that event logs are successfully (a) Variant #1 (b) Variant #2 (c) Variant #3 (d) Variant #4 Figure 5.1: Process models of Loan Application Process dataset Table 5.2: Process Model Mining Evaluation of Loan Application Process Dataset Fitness Structural Behavioral Average Appropriateness Appropriateness Appropriateness Variant #1 100 % 70 % 98.5 % 84.2 % Variant #2 100 % 100 % 100 % 100 % Variant #3 100 % 100 % 100 % Variant #4 100 % 100 % 98.2 % 99.1 % Average 100 % 92.5 % 99.7 % 96.06 % Figure 5.2: Number of Clusters vs. within-SSE for Loan Application Process dataset replayed over process models and performance indicators are calculated. With these performance indicators, organizations are clustered and internal evaluation of clusters are presented with different number of clusters in Figure 5.2. As expected, within- SSE value decreases when number of clusters, k, increases. Considering the effects of overfitting after the elbow point in the plot, number of clusters is selected to be 2 for this dataset. For two clusters, Variant #1, #2, and #4 are grouped into one cluster where only Variant #3 is left to other cluster. In Mismatch Pattern Analysis stage, number of mismatch patterns are analyzed with the graphedit similarity between each two organization. For each two organiza- tion, their graph-edit similarity values are calculated and then our mismatch pattern analyzers are executed to spot differences. As the similarity between process mod- els decreases our method spots more mismatch patterns for most of the variants and it ensures that the developed mismatch pattern analyzers work as expected for this dataset. Correlation between graph-edit similarity and number of mismatch patterns are plotted in Figure 5.3. Figure 5.3: Mismatch Patterns vs. Graph-Edit Similarity for Loan Application Pro- cess variants Figure 5.4: Mismatch pattern types for Loan Application Process variants When the mismatch patterns are analyzed according to their types as diagrammed in Figure 5.4, "Skipped Activity" and "Activities at Different Moments" patterns are spotted mostly and no "Different Conditions for Occurrence" or "Additional Depen- dencies" patterns are discovered. Considering the small amount of this dataset, these numbers and distribution can be counted as acceptable in this stage of methodology. In Recommendation Generation stage, an organization and performance difference threshold is selected as analysis input. For the selected organization's cluster, all other clusters are checked for performing better than the specified threshold. Instead of all mismatch patterns between organizations, only the mismatch patterns that are potential causes of other organizations to perform better are listed. For different threshold Figure 5.5: Recommendation Generation analysis for Loan Application Process dataset values, number of performance indicators that are performing better for the selected organization and spotted mismatch patterns are plotted in Figure 5.5. In order to construct the data in Figure 5.5, every organization is selected one-by-one with different threshold values. For every analysis, number of performance indicators and average number of mismatch patterns causing them are plotted. In addition, total

number of mismatch patterns without clustering for each organization is added to the plot as an upper bound. With the help of this upper bound, responsiveness and degree of helping the user to focus on the performance improvement can be analyzed. As can be seen, for each threshold value, average number of mismatch patterns with performance indicator clustering are very low compared to without clustering. In other words, when user wants to improve its performance with any threshold, there is significantly less number of mismatch patterns on average to check. This shows the methodology proposed in this thesis can help users to focus on differences between organizations given this dataset. Table 5.3: Statistical summary of Environmental Permit Application Process dataset Cases Events Percentage Municipality #1 54 131 6.1 % Municipality #2 302 586 27.3 % Municipality #3 37 73 3.4 % Municipality #4 340 507 23.7 % Municipality #5 481 845 39.4 % Total 1214 2142 5.4 Environmental Permit Application Process 5.4.1 General Information In this section, methodology proposed in this thesis study will be applied on the En- vironmental Permit Application Process dataset [11] and evaluation results will be presented with a similar previous approach. Since this dataset consists of real-life event logs, preprocessing is undertaken prior to start analysis. Incomplete traces, which started but not ended in the time frame of log collection, and exceptional cases are removed from event logs using ProM log visualization tools with a similar ap- proach in [7]. Statistical information about the dataset that is used in this section can be summarized in Table 5.3 after preprocessing. As shown in Table 5.3, total of 1214 cases and 2142 events included in this dataset with a variable distribution between event logs of municipalities. In the following section, these municipalities will be used as organizational logs and the methodology presented in this thesis study will be applied. 5.4.2 Methodology Stages In Process Model Mining stage, event logs of each municipality in the dataset are used as organizational event logs and they are used to mine process models. Considering preprocessing is undertaken on the event logs, noise threshold in Inductive Miner is set to a low value of 10% to achieve a higher fitness. Table 5.4: Process Model Mining Evaluation of Environmental Permit Application Process dataset Fitness Structural Behavioral Average Appropriateness Appropriateness Appropriateness Municipality #1 86 % 97.5 % 54.4 % 76 % Municipality #2 100 % 100 % 100 % 100 % Municipality #3 92.3 % 71.1 % 67.2 % 69.1 % Municipality #4 96.8 % 65.7 % 64 % 64.9 % Municipality #5 94.5 % 58.8 % 39.7 % 49.3 % Average 93.9 % 78.6 % 65.1 % 71.9 % Appropriateness and fitness evaluation metrics are summarized in Table 5.4 and it can be seen that each event log is successful in terms of representing reality with high fitness values. However, some of the process models like Municipality #5 and #4 re- sulted with low appropriateness values. Process models for each event log are visual- ized with a detail simplification based on number of activities and paths in Figure 5.6. Detail simplification is only used for visualization and it draws the mainstream pro- cess flows instead of whole set of paths and activities. When process model diagrams are checked it can be seen that low appropriateness values resulted with complicated process models that are difficult to analyze visually. It should be kept in mind that actual process models are 10 to 20 times more complicated in terms of number of activities and paths than the ones presented in Figure 5.6. In Performance Indicator Analysis stage, alignment costs are calculated over replay of event logs on process models. As presented in the Table 5.5, as appropriateness and fitness decrease; alignment costs increase for the municipalities. This is an expected behavior since decrease in fitness indicates that process model cannot parse event log well and low appropriateness means the process models are not structured in terms of quality metrics. These results indicates the fact that both process model mining stage and replay stage is in conformity and performance indicators calculated over replay are acceptable. After calculating the performance indicators, municipalities are clustered based on these values and this stage is evaluated by the within-SSE values for different number of clusters as plotted in Figure 5.7. In order to avoid overfitting of clusters, number of clusters, k, is selected to be 2 for this dataset for further analysis. For two

clusters, (a) Municipality #1 (b) Municipality #2 (c) Municipality #3 (d) Municipality #4 (e) Municipality #5 Figure 5.6: Process models of Environmental Permit Application Process Dataset Table 5.5: Replay Evaluation of Environmental Permit Application Process Dataset Fitness Average Appropriateness Alignment Cost Municipality #1 86 % 76 % 173.2 Municipality #2 100 % 100 % 0 Municipality #3 92,3 % 69,1 % 332.3 Municipality #4 96,8 % 64,9 % 9,1 Municipality #5 94,5 % 49,3 % 35.8 Figure 5.7: Number of Clusters vs. within-SSE for Environmental Permit Application Process dataset Municipality #1 is located in one cluster where municipalities #2, #3, #4 and #5 are grouped into to other cluster. In Mismatch Pattern Analysis stage, number of mismatch patterns are analyzed with the graph-edit similarity between each two municipality. In order to check correlation between graph-edit similarity and number of mismatch patterns, data is plotted in Figure 5.8. When the plot is checked, it can be seen that as the similarity between process models of municipalities increases, number of mismatch patterns decreases on most of the cases. When further analyzed, it can be seen that Municipalities #4 and #5, which have significantly more complex process model compared to others, fails in spotting mismatch patterns according to graph-edit similarity. When the mismatch patterns are analyzed according to their types as diagrammed in Figure 5.9, Skipped Activity pattern is spotted most frequently. Following this, Differ- ent Dependencies and Additional Dependencies are spotted widely and there are on average of 78 mismatch patterns for process models of municipalities. Unfortunately, Refined Activity pattern analyzers could not be applied on this dataset since activity Figure 5.8: Mismatch Patterns vs. Graph-Edit Similarity for Environmental Permit Application Process Dataset Figure 5.9: Mismatch pattern types for Environmental Permit Application Process dataset names are not provided and activity codes without any semantic meaning are used in- stead. Considering the implementation of Refined Activity pattern in this study, which is based on the similarity between labels, they are eliminated in the analysis of this dataset. In Recommendation Generation stage, an organization and performance difference threshold is selected as analysis input likewise the previous dataset. For different threshold values, number of performance indicators that are performing better for the selected organization and spotted mismatch patterns are plotted in Figure 5.10. In the analysis of Figure 5.10, it can be seen that only the cluster that the Municipality #1 has the potential of learning from other cluster since it performs worse in all per- formance indicators. For the threshold of 50%, cluster of Municipality #1 performs Figure 5.10: Recommendation Generation analysis for Environmental Permit Appli- cation Process dataset (2 Clusters) worse in 6 performance indicators and proposed approach lists total of 30 mismatch patterns. On the average it show 5 patterns for each performance indicator to the user as the potential causes of performance improvement. With the same approach, cluster of Municipality #1 performs worse in 3 indicators with the difference of 75 % and on average 10 mismatch patterns are listed for each performance indicator. When it is compared to the total mismatch patterns of Municipality 1, which is 357, proposed approach helps significantly to the user for focusing performance improvement. Since selecting number of clusters as 2 did not yield high learning potential for per- formance improvement, analysis is repeated with selecting number of clusters as 3. When three clusters are created, Municipality #1 is located in the first cluster; Mu- nicipality #2 and #4 are located in the second cluster; and Municipality #3 and #5 are grouped in to the last cluster. For these three clusters analysis is repeated for the thresholds of 25 %, 50 % and 75 % since these are the breaking points for perfor- mance indicator changes. As plotted in Figure 5.11, in addition to Municipality #1, now Municipality #3 and #5 have the learning potential from other clusters. However, Municipality #2 and #4 performs better in all performance indicators which yielded no mismatch pattern analysis data for them. Increasing cluster sizes in this analy- sis shows that organizations can learn more from each other but it has the potential danger of overfitting to other organizations process model. Figure 5.11:

Recommendation Generation analysis for Environmental Permit Application Process dataset (3 Clusters) 5.5 Discussions When the evaluation of the stages for Loan Application Process and Environmental Permit Application Process datasets are gathered together, the following results can be expressed: • Process mining stage of the proposed methodology can mine the process mod- els with perfect fitness and high appropriateness from event logs which have no noise. When the noise level increases in the dataset, fitness values of mined models decreases to 90 % levels with a decreasing appropriateness of models. • For the successfully mined models with high fitness values, replay and perfor- mance indicator calculation stage works seamlessly as expected. With this step, average and standard deviation time between each activity can be measured for each organization. Number of these metrics are quadratic to the number of activities in each organization's process model and difficult to analyze with a cross comparison. • Internal measure of clusters indicates that the organizations can be clustered according to their performance indicators which yields a collective approach of organizations for their subprocesses. In other words, within-SSE values decrease significantly when the organizations are divided into clusters which shows that they can be grouped based on how well they are executing in their performance indicators. • Mismatch analysis spots the differences between process models in coherence with structural similarity of them. This indicates that the idea of using mis- match patterns to reveal differences between process models is a feasible approach since its results are comparable to the similarity metrics of process mod- els in the literature. However, only the total number of mismatch patterns are taken into consideration in this study where their importance and occurrence is variable. For instance, it can be a very useful information for a Skipped Activity in a small dataset like Loan Application Example; however it is very likely to see huge number of Skipped Activity patterns in an immense dataset like En- vironmental Permit Application Process. With this consideration, distributions of mismatch patterns are presented for each dataset to reveal any tendencies for occurrence. • Recommendation generation aims to gather all generated information in this thesis study to help focusing on the potentially important mismatch patterns for performance improvement. For this aim, different thresholds and different clus- ter sizes are analyzed to check responsiveness of this stage. When the number of mismatch patterns with and without performance clusterings are checked, it shows that in a small dataset, where even the mismatch patterns can be spotted by visual analysis, performance clustering lists 3 times less number of differ- ences in Loan Application Example dataset. When it is impossible to locate mismatch patterns manually like in Environmental Permit Application Process, performance clustering spots 100 times less number of differences. This dif- ference helps user to focus on the differences with a potential performance improvement which is one of the aims in this thesis study. • Although each step of methodology can be counted as successful based on their evaluation metrics, mismatch patterns recommended at the end of methodol- ogy can yield important observations as well as being irrelevant and infeasi- ble. Since this decision is based on the business environment of organizations, evaluation of the quality of recommendations for business usefulness requires domain expertise. However, some example recommendations can be presented to provide an insight: - In the analysis of Loan Application Process, for Variant #3 performance 72 clustering results indicate that other cluster of variants perform 27 % better on average time and 12 % better on standard deviation time between activities "Calculate Capacity" and "Accept". In other words, cluster of other variants complete the path between these activities in a short amount time with less variance. When the mismatch patterns for these perfor- mance indicators are checked the following ones can be mentioned: * "Check Credit" is a Skipped Activity in the other cluster. * "Check Credit" is a Refined Activity of with "Check System (50 %)"; "Check Paper Archive (42 %)"; "Send Credit Check Request (32 %)"; "Process Credit Check Reply (31 %)" where the corresponding simi-larity values provided in parentheses. *

"Calculate Capacity" is a Different Moments in Processes which have different previous activities in clusters. When these example mismatch patterns are checked, removing "Check Credit" activity and putting other activities instead of it might be the cause of performance improvement. With the same approach, putting "Calcu- late Capacity" on different orders in processes can effect the average and variance of time between activities. These mismatch patterns are also vi- sualized on process model of Variant #3 and a variant from other cluster in Figure 5.12. In the process models, refined activities of "Check Credit" and different positions of "Calculate Capacity" are indicated. – In the analysis of Environmental Permit Application Process with 3 clus- ters, Cluster #3 performs 40 % better on average time and 53 % better on standard deviation time between the activities "01_HOOFD_010" and "01_HOOFD_015". When the mismatch patterns between these clusters for the performance indicator is listed the following ones can be men-tioned: * Activity "03 GBH 005" and "16 LGSV 010" are Different Moments in Processes which have different next activities in clusters. * Activity "01 HOOFD 015" and "01 HOODF 065" are Different De- pendencies patterns and they have a different set of dependencies in clusters. 73 Figure 5.12: Visualization of example recommendation for Loan Application Process dataset Although the activity codes in mismatch patterns do not reveal any in-formation about their context, they are listed as potential cause of perfor- mance improvement. For the municipalities in Cluster #3, the mentioned mismatch patterns are visualized on the fragments of process models in Figure 5.13 and Figure 5.14 since it is difficult to visualize the complete process models. In the process models, each mismatch pattern is marked and this shows how the proposed approach helps to focus on differences between process models. Figure 5.13: Visualization of example recommendation for Environmental Permit Application Process dataset (Municipality #3) Figure 5.14: Visualization of example recommendation for Environmental Permit Application Process dataset (Municipality #5) CHAPTER 6 CONCLUSION AND FUTURE WORK 6.1 Conclusion In this thesis study, a new approach is proposed and tested for generating recommen- dations using crossorganizational process mining for process performance improve- ment. Cross-organizational <u>process mining is applied</u> with <u>the</u> idea <u>of</u> unsupervised learning where predictor variables related to performances of organizations are used in an environment where processes are executed on several organizations. Results show that it is possible to use crossorganizational process mining and mismatch pat- terns for performance improvement recommendations. Process mining is a large- spectrum field where different set of activities and approaches are gathered together to discover, monitor and improve processes. In this thesis study, a four-stage solution is presented and their performances are explained. Process mining stage mines the process models of different organizations and it is shown that a generic, noise-capable process mining method can create process mod- els with high fitness and appropriateness values. This indicates that mining process models of different organizations under a generic method can yield comparable and appropriate process models. Success of this stage directly affects the quality of calcu- lated performance indicators since they are collected through the replay of event logs over process models. Performance indicator analysis stage in the methodology clusters the organizations based on their performance indicators and internal evaluation metrics show that it is suitable to cluster organizations based on how well they are operating. Although there are studies that clusters organizations based on their process models for structural analysis [19], this approach showed that organizations can be clustered based on their performance indicators. Mismatch analysis stage in this thesis has the aim of spotting differences between processes of organizations and it is known to be the first implementation of mismatch patterns [13]. When the results of this stage is checked against well-established sim- ilarity metrics in the literature, it can be concluded that mismatch pattern finding can be used when there is a need for spotting differences in similar processes. Recommendation generation stage collects the generated and extracted

information in all prior stages to list what the organizations can learn from other organizations which perform better. In order to define performing better, different thresholds are checked for each organization and resulting recommendations show that clustering organizations based on performance indicators and then checking mismatch patterns significantly helps user to focus on the differences with a potential performance im- provement. In addition, quality of recommendations in business usefulness is tried to be explained with example outputs and these examples show that the approach yields recommendations difficult to spot manually and visually, which are also potential causes of performance improvement. In addition, proposed methodology is developed as extensible and configurable set of plugins in ProM framework [42] and published as open-source. This makes the methodology open to include new process mining methods, mismatch patterns and clustering approaches as well as testing with different datasets. 6.2 Future Work For the approach proposed in this thesis study, the following issues can be listed as pointers to future work: • In the process mining stage, instead of Inductive Miner, different techniques can be used which can mine complex process models with higher appropriateness levels while keeping the current high fitness values. • In the performance indicator analysis stage, new indicators can be defined based on the business environment, event log attributes and user needs. For instance, personnel and resource allocation indicators can be included as well as cost dimension. • For mismatch pattern analysis, new and business oriented mismatch patterns can be included in the analysis. In addition analyzers can fail when there are loops in the process models in current implementations, therefore more robust implementations for process models with loops can be developed in the future. • For the generated recommendation, their quality for business environment are not assessed within the scope of this thesis. However, when any feedback from a domain expert or BPM people is provided, the learning approach can be con-verted to semi-supervised learning from unsupervised learning. • For ProM implementation of this study, currently user selects an organization to list recommendations; in the future user might be able to select area of interest as well as starting and ending points visually on a process model. APPENDIX A APPENDIX A.1 Methodology Steps Figure A.1: Information Screen of Cross-Organizational Process Miner Plugin Figure A.2: Organization Naming Screen of Cross-Organizational Process Miner Plu- gin Figure A.3: Process Miner Screen of Cross-Organizational Process Miner Plugin Figure A.4: Automated Replayer Screen of Cross-Organizational Process Miner Plu- gin 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 74 75 76 77 78 79 80 85 86 87