

tut2

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$(x1, y1) \rightarrow (xm, ym)$

close: $xm=x1, y1=ym$

smooth: $d^n x/dt^n, dy^n/dt^n$ exists

$$x^2 + y^2 = 1,$$

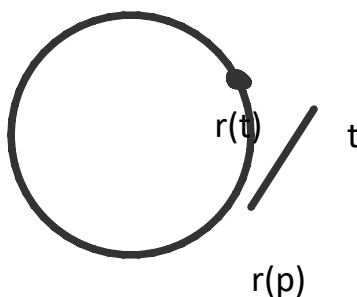
let angle t on curve, $x = \cos t, y = \sin t, t \in [0, 2\pi], r(t) = (x, y) = (\cos t, \sin t)$

tangent, normal

$$r(t) = (x(t), y(t)) = \left(x(0) + \frac{tdx(0)}{dt}, y(0) + \frac{tdy(0)}{dt} \right)$$

$$r(0) = (x(0), y(0))$$

now we have 2 points r_0 and r_t



on y it's right hand, on x is left hand

it's actually match from t to a 2dim matrix, $\frac{dr}{dt} = \left(\frac{dx}{dt}, \frac{dy}{dt} \right)$

unit tangent $T(t) = \frac{dr}{dt} * \frac{1}{\left\| \frac{dr}{dt} \right\|}$, length is 1

unit normal $N(t) = \left(-\frac{dy}{dt}, \frac{dx}{dt} \right) \frac{1}{\left\| \frac{dr}{dt} \right\|}$

$$N(t) \cdot T(t) = 0$$

unit tangent

