

Data Types & Structures

Physical Media, Abstractions, Programs & Performance

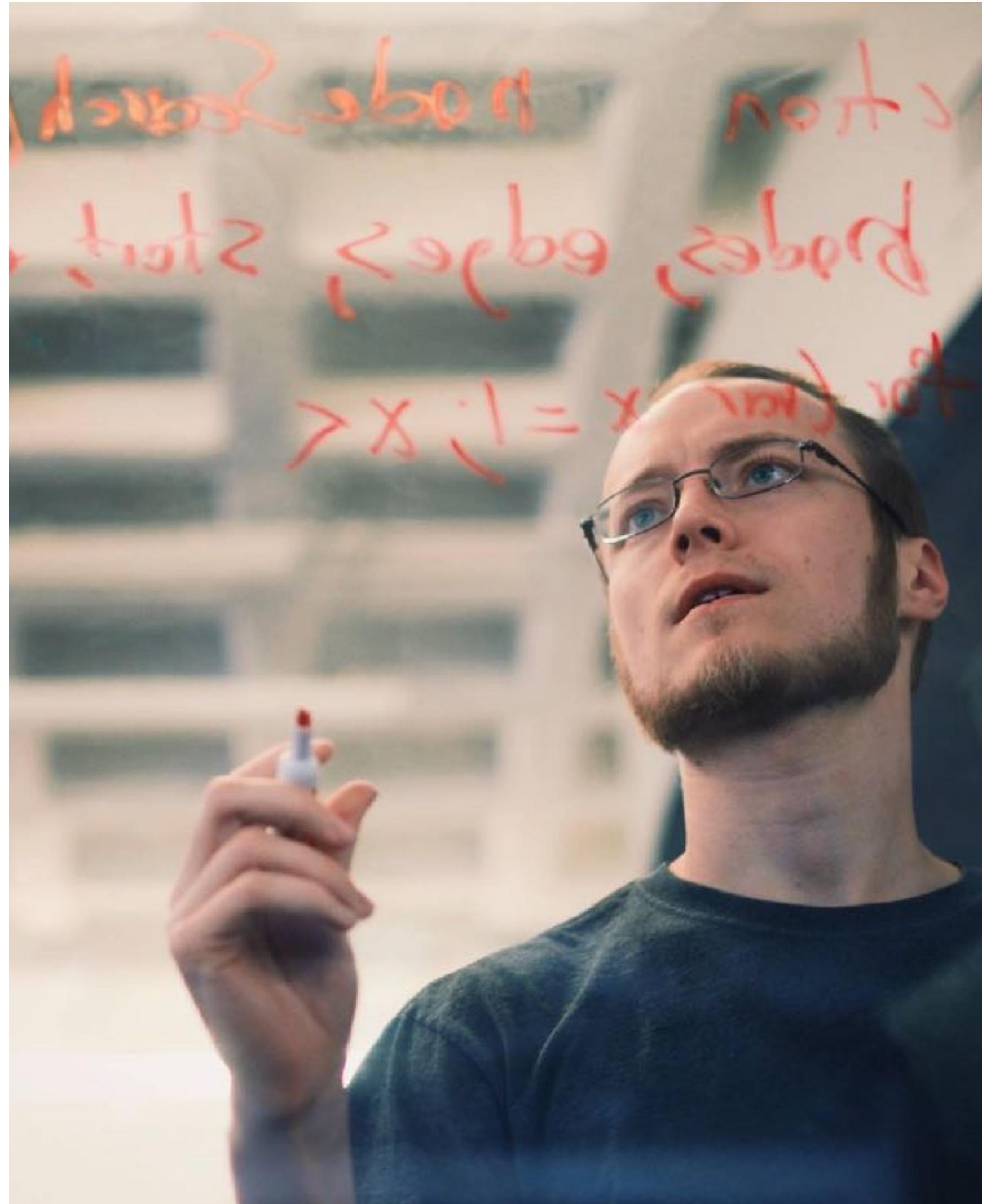
"[The files are] in the computer... it's so simple."



MakeAGIF.com

(Just Some) Motivations

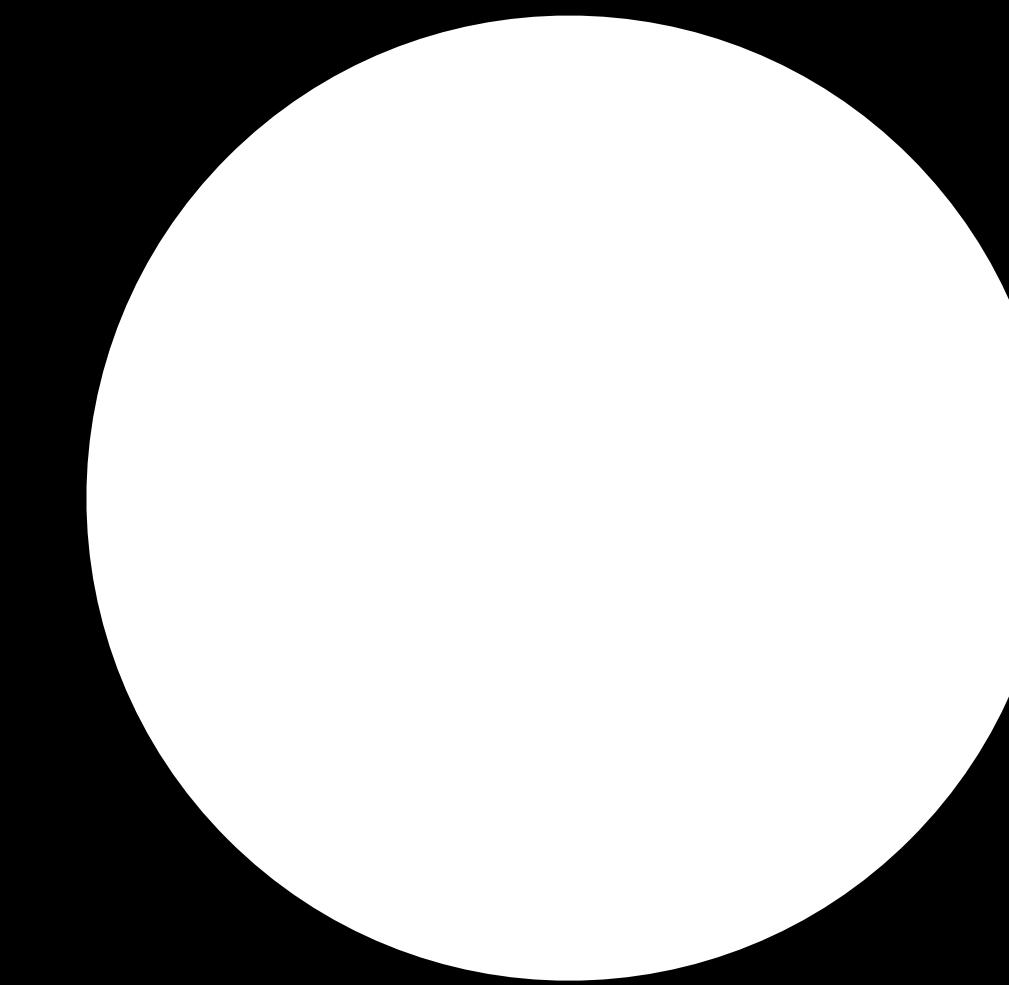
- ❖ *Demystify foundations*
- ❖ *Gain insight & perspective*
- ❖ *Recognize solutions*
- ❖ *Write performant code*
- ❖ *Continue practicing OOP*
- ❖ *Interview well*



Coming Up

- I. Information Theory & Hardware
- II. Representations & Encodings
- III. Abstractions & Languages
- IV. Abstract Data Types & Data Structures
 - IV.a. Queues
 - IV.b. Linked Lists
 - IV.c. Hash Tables
 - IV.d. Trees
- V. Extras

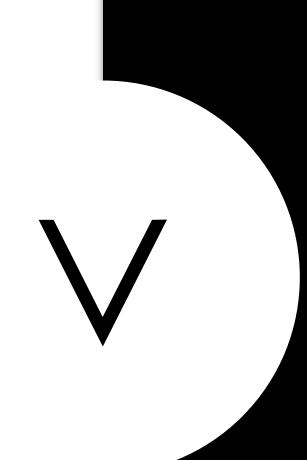
Part I: Information Theory & Hardware



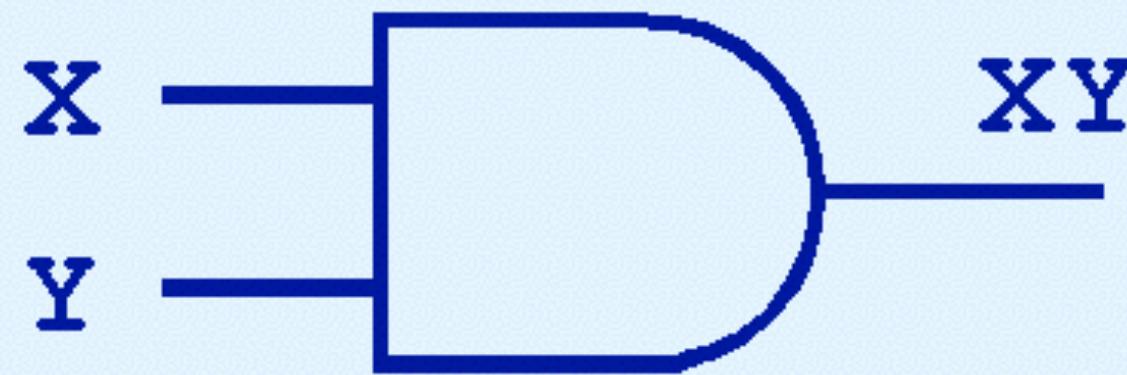
T
-0



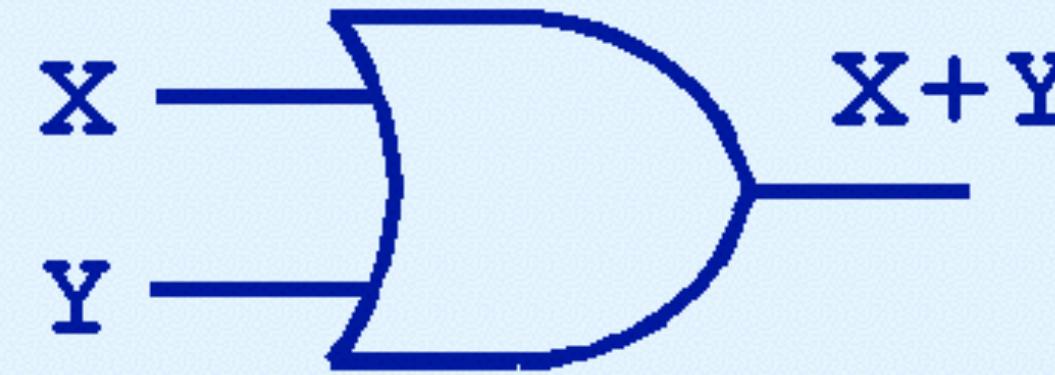
B
-1



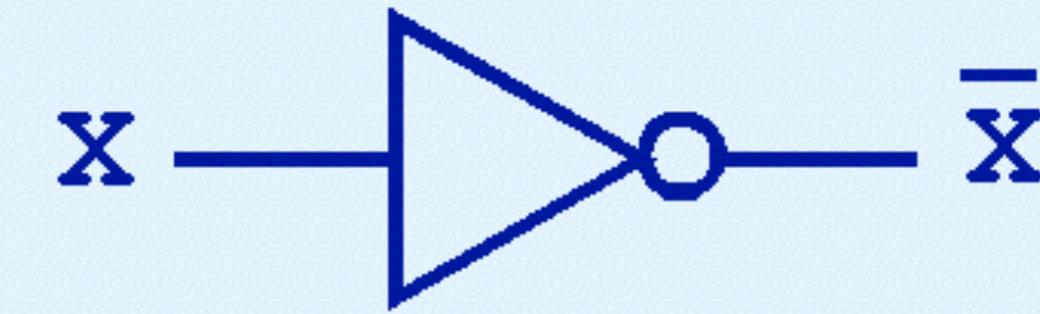
My name is Boole AND I invented boolean algebra!



X AND Y



X OR Y



NOT X

X	Y	XY
0	0	0
0	1	0
1	0	0
1	1	1

X	Y	X+Y
0	0	0
0	1	1
1	0	1
1	1	1

X	X̄
0	1
1	0

Law	Example	Example
Identity	$A \wedge I = A$	$A \vee 0 = A$
Idempotent	$A \wedge A = A$	$A \vee A = A$
Associative	$A \wedge (B \wedge C) = (A \wedge B) \wedge C$	$A \vee (B \vee C) = (A \vee B) \vee C$
Commutative	$A \wedge B = B \wedge A$	$A \vee B = B \vee A$
Absorption	$A \wedge (A \vee B) = A$	$A \vee (A \wedge B) = A$
Complementation	$A \wedge \neg A = 0$	$A \vee \neg A = I$
Distributive	$A \wedge (B \vee C) = (A \wedge B) \vee (A \wedge C)$	$A \vee (B \wedge C) = (A \vee B) \wedge (A \vee C)$
De Morgan's	$\neg(A \wedge B) = \neg A \vee \neg B$	$\neg(A \vee B) = \neg A \wedge \neg B$
Common Identities	$A \wedge (\neg A \vee B) = A \wedge B$	$A \vee (\neg A \wedge B) = A \vee B$
Double Negation	$\neg(\neg A) = A$	

\wedge means logical AND

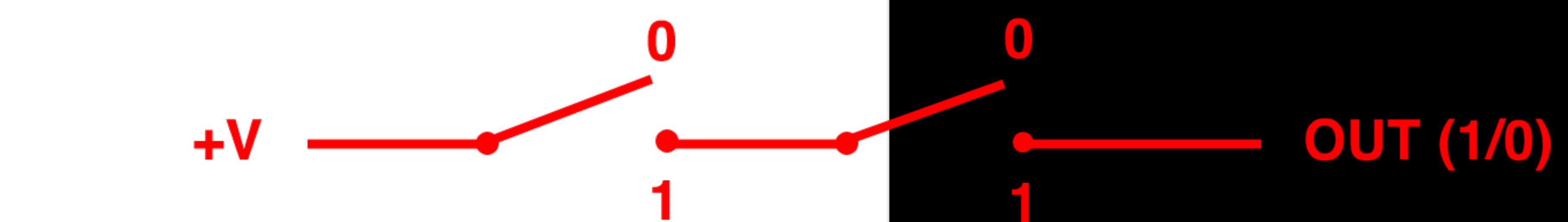
\vee means logical OR

\neg means logical NOT

I means true

0 means false

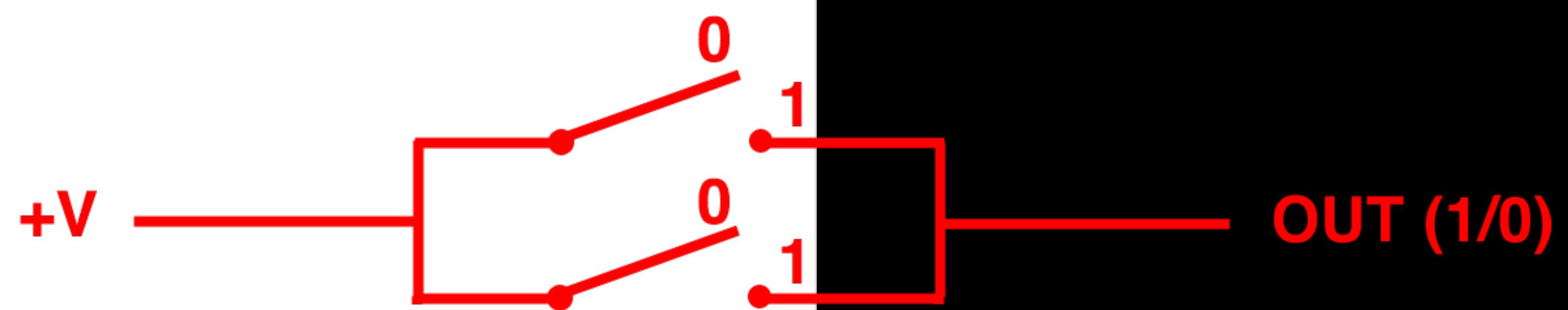
A/B/C are conditions
(what goes inside the parentheses of an `if` statement)



ON



OFF



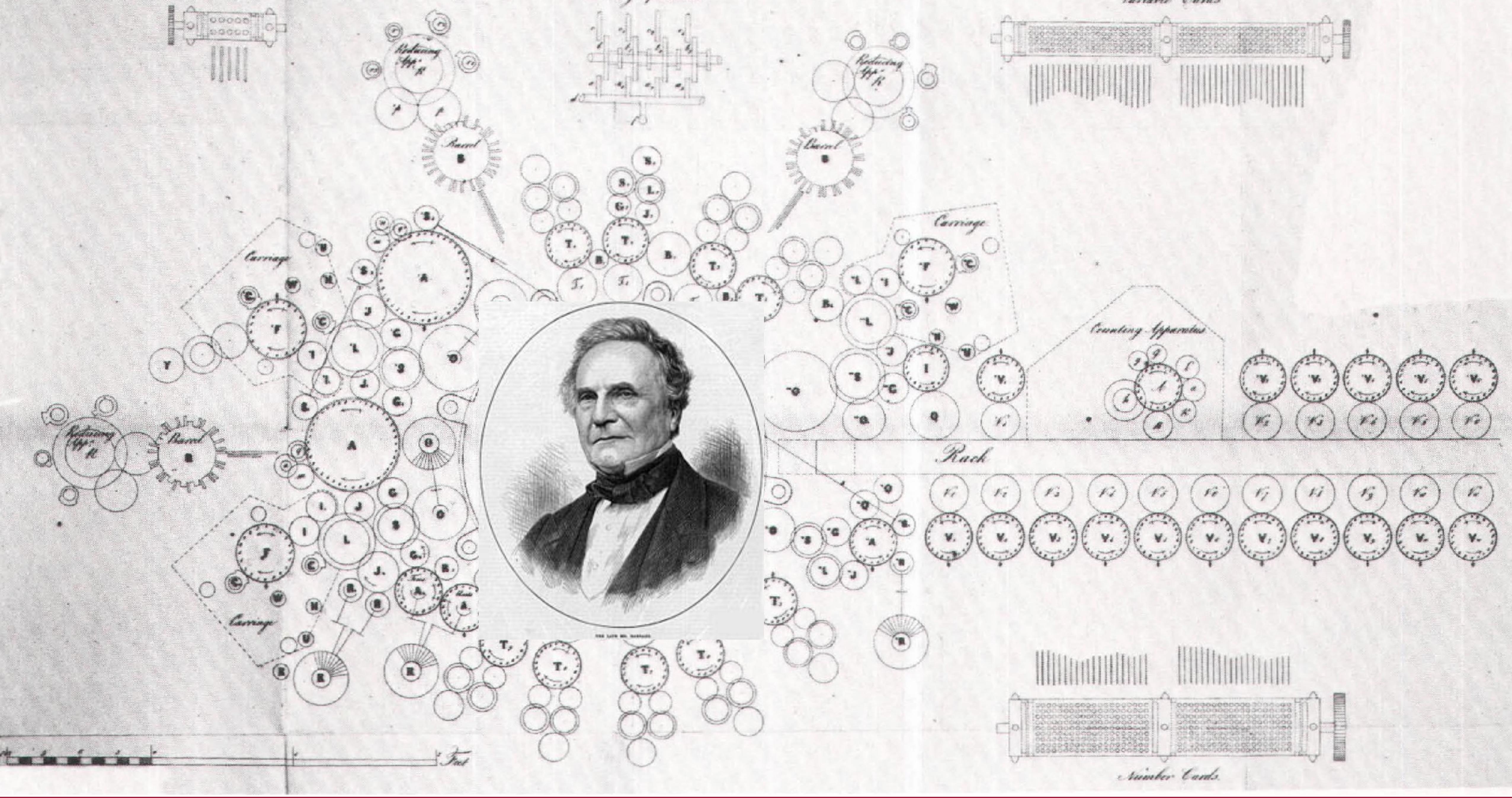
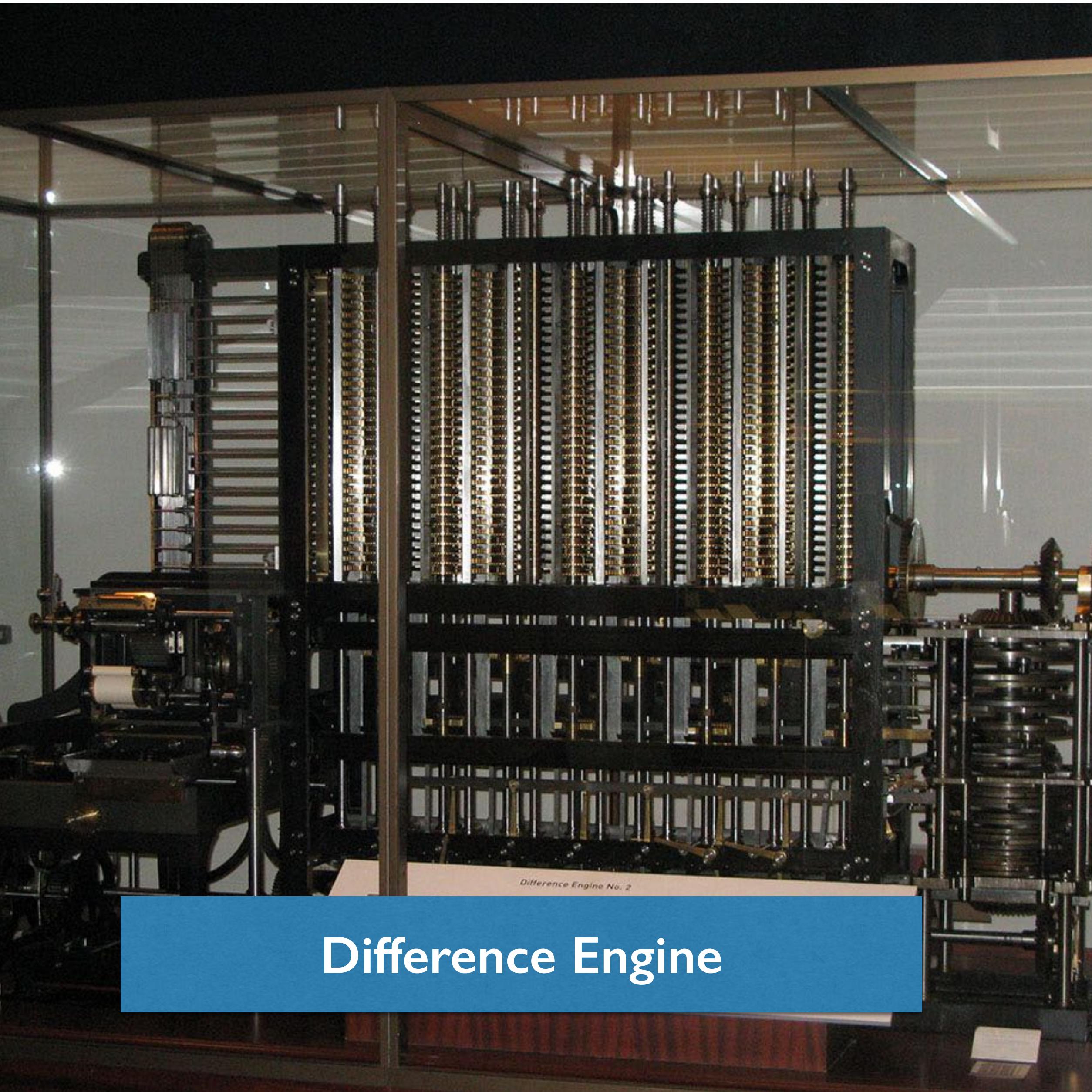
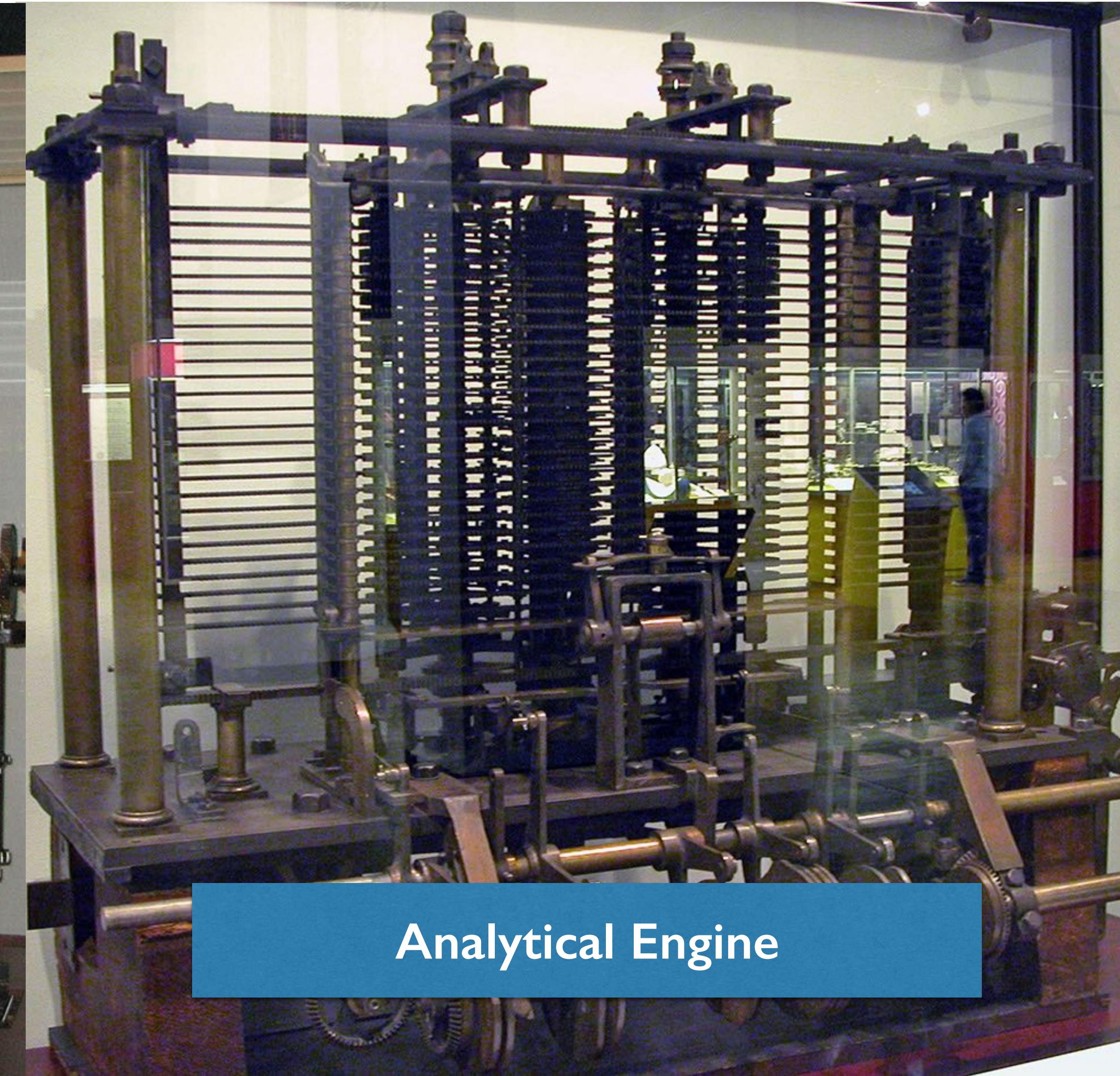


Diagram for the computation by the Engine of the Numbers of Bernoulli. See Note G. (page 722 *et seq.*)

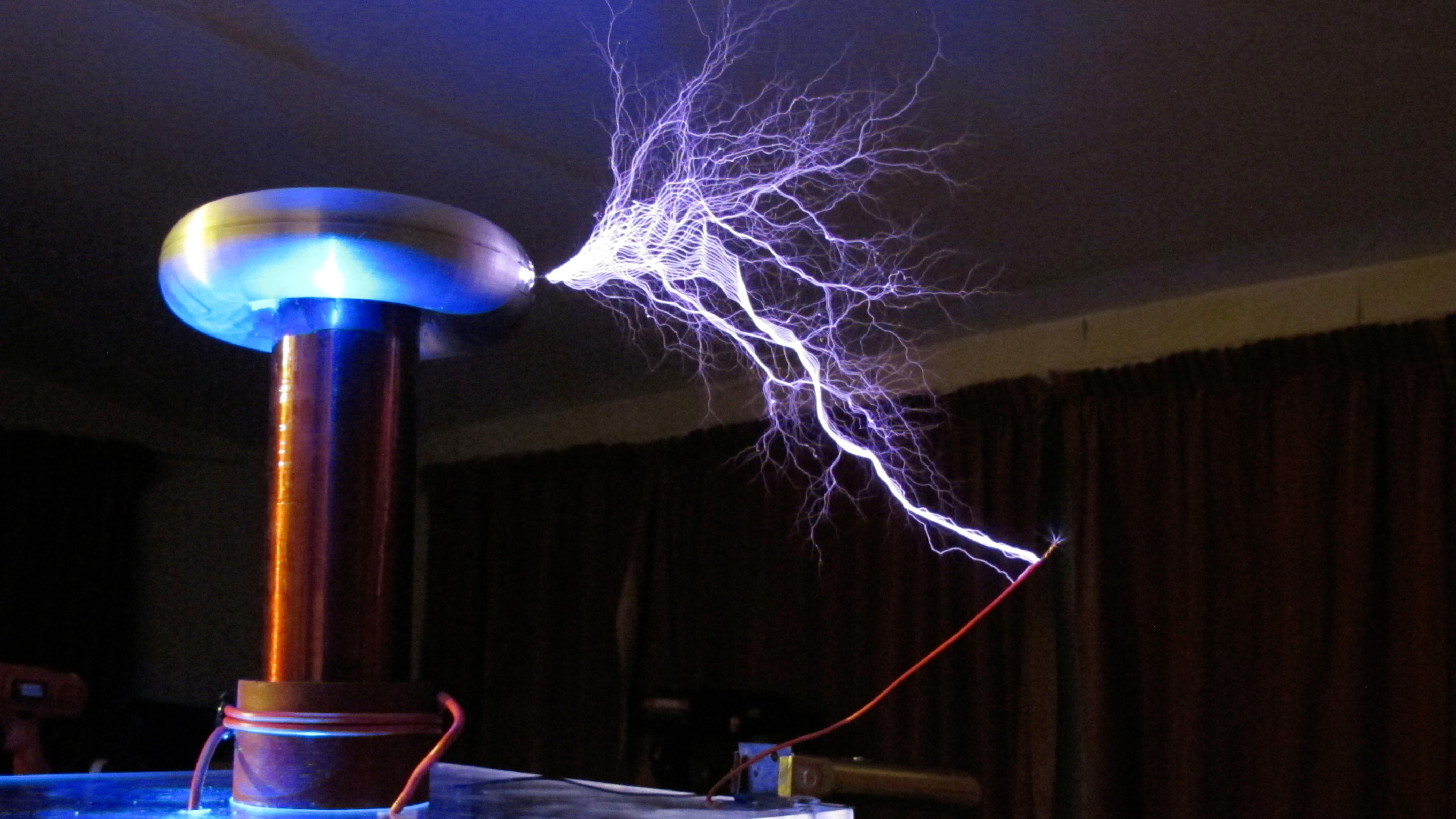
Number of Operation.	Nature of Operation.	Variables acted upon.	Variables receiving results.	Indication of change in the value on any Variable.	Data.			Working Variables.								Result Variables.						
					1V_1	1V_2	1V_3	0V_4	0V_5	0V_6	0V_7	0V_8	0V_9	$^0V_{10}$	$^0V_{11}$	$^0V_{12}$	$^0V_{13}$	B_1	B_2	B_3	B_4	
					○	○	○	○	○	○	○	○	○	○	○	○	○	B_1	B_2	B_3	B_4	
1	\times	$^1V_2 \times ^1V_3$	$^1V_4, ^1V_5, ^1V_6$	$\begin{cases} ^1V_2 = ^1V_2 \\ ^1V_3 = ^1V_3 \end{cases}$	= 2 n														B_1	B_2	B_3	B_4
2	$-$	$^1V_4 - ^1V_1$	2V_4	$\begin{cases} ^1V_4 = ^2V_4 \\ ^1V_1 = ^1V_1 \end{cases}$	= 2 n - 1	1													B_1	B_2	B_3	B_4
3	$+$	$^1V_2 + ^1V_1$	2V_5	$\begin{cases} ^1V_5 = ^2V_5 \\ ^1V_1 = ^1V_1 \end{cases}$	= 2 n + 1	1													B_1	B_2	B_3	B_4
4	\div	$^2V_5 \div ^2V_4$	$^1V_{11}$	$\begin{cases} ^2V_5 = ^0V_5 \\ ^2V_4 = ^0V_4 \end{cases}$	= $\frac{2n-1}{2n+1}$													B_1	B_2	B_3	B_4	
5	\div	$^1V_n \div ^1V_2$	$^2V_{11}$	$\begin{cases} ^1V_{11} = ^2V_{11} \\ ^1V_2 = ^1V_2 \end{cases}$	= $\frac{1}{2} \cdot \frac{2n-1}{2n+1}$		2											B_1	B_2	B_3	B_4	
6	$-$	$^0V_{13} - ^2V_{11}$	$^1V_{13}$	$\begin{cases} ^2V_{11} = ^0V_{11} \\ ^0V_{13} = ^1V_{13} \end{cases}$	= $-\frac{1}{2} \cdot \frac{2n-1}{2n+1} = A_0$													B_1	B_2	B_3	B_4	
7	$-$	$^1V_3 - ^1V_1$	$^1V_{10}$	$\begin{cases} ^1V_3 = ^1V_3 \\ ^1V_1 = ^1V_1 \end{cases}$	= n - 1 (= 3)	1												B_1	B_2	B_3	B_4	
8	$+$	$^1V_2 + ^0V_7$	1V_7	$\begin{cases} ^1V_2 = ^1V_2 \\ ^0V_7 = ^1V_7 \end{cases}$	= 2 + 0 = 2		2															
9	\div	$^1V_6 \div ^1V_7$	$^3V_{11}$	$\begin{cases} ^1V_6 = ^1V_6 \\ ^0V_{11} = ^3V_{11} \end{cases}$	= $\frac{2n}{2} = A_1$													B_1	B_2	B_3	B_4	
10	\times	$^1V_{21} \times ^3V_{11}$	$^1V_{12}$	$\begin{cases} ^1V_{21} = ^1V_{21} \\ ^3V_{11} = ^3V_{11} \end{cases}$	= $B_1 \cdot \frac{2n}{2} = B_1 A_1$													B_1	B_2	B_3	B_4	
11	$+$	$^1V_{12} + ^1V_{13}$	$^2V_{13}$	$\begin{cases} ^1V_{12} = ^0V_{12} \\ ^1V_{13} = ^2V_{13} \end{cases}$	= $-\frac{1}{2} \cdot \frac{2n-1}{2n+1} + B_1 \cdot \frac{2n}{2}$													B_1	B_2	B_3	B_4	
12	$-$	$^1V_{10} - ^1V_1$	$^2V_{10}$	$\begin{cases} ^1V_{10} = ^2V_{10} \\ ^1V_1 = ^1V_1 \end{cases}$	= n - 2 (= 2)	1												B_1	B_2	B_3	B_4	
13	$-$	$^1V_6 - ^1V_1$	2V_6	$\begin{cases} ^1V_6 = ^2V_6 \\ ^1V_1 = ^1V_1 \end{cases}$	= 2 n - 1	1																
14	$+$	$^1V_1 + ^1V_7$	2V_7	$\begin{cases} ^1V_1 = ^1V_1 \\ ^1V_7 = ^2V_7 \end{cases}$	= 2 + 1 = 3	1																
15	\div	$^2V_6 \div ^2V_7$	1V_8	$\begin{cases} ^2V_6 = ^2V_6 \\ ^2V_7 = ^2V_7 \end{cases}$	= $\frac{2n-1}{3}$																	
16	\times	$^1V_8 \times ^3V_{11}$	$^4V_{11}$	$\begin{cases} ^1V_8 = ^0V_8 \\ ^3V_{11} = ^4V_{11} \end{cases}$	= $\frac{2n}{2} \cdot \frac{2n-1}{3}$													B_1	B_2	B_3	B_4	
17	$-$	$^2V_6 - ^1V_1$	3V_6	$\begin{cases} ^2V_6 = ^3V_6 \\ ^1V_1 = ^1V_1 \end{cases}$	= 2 n - 2	1																
18	$+$	$^1V_1 + ^2V_7$	3V_7	$\begin{cases} ^2V_7 = ^3V_7 \\ ^1V_1 = ^1V_1 \end{cases}$	= 3 + 1 = 4	1																
19	\div	$^3V_6 \div ^3V_7$	1V_9	$\begin{cases} ^3V_6 = ^3V_6 \\ ^3V_7 = ^3V_7 \end{cases}$	= $\frac{2n-2}{4}$													B_1	B_2	B_3	B_4	

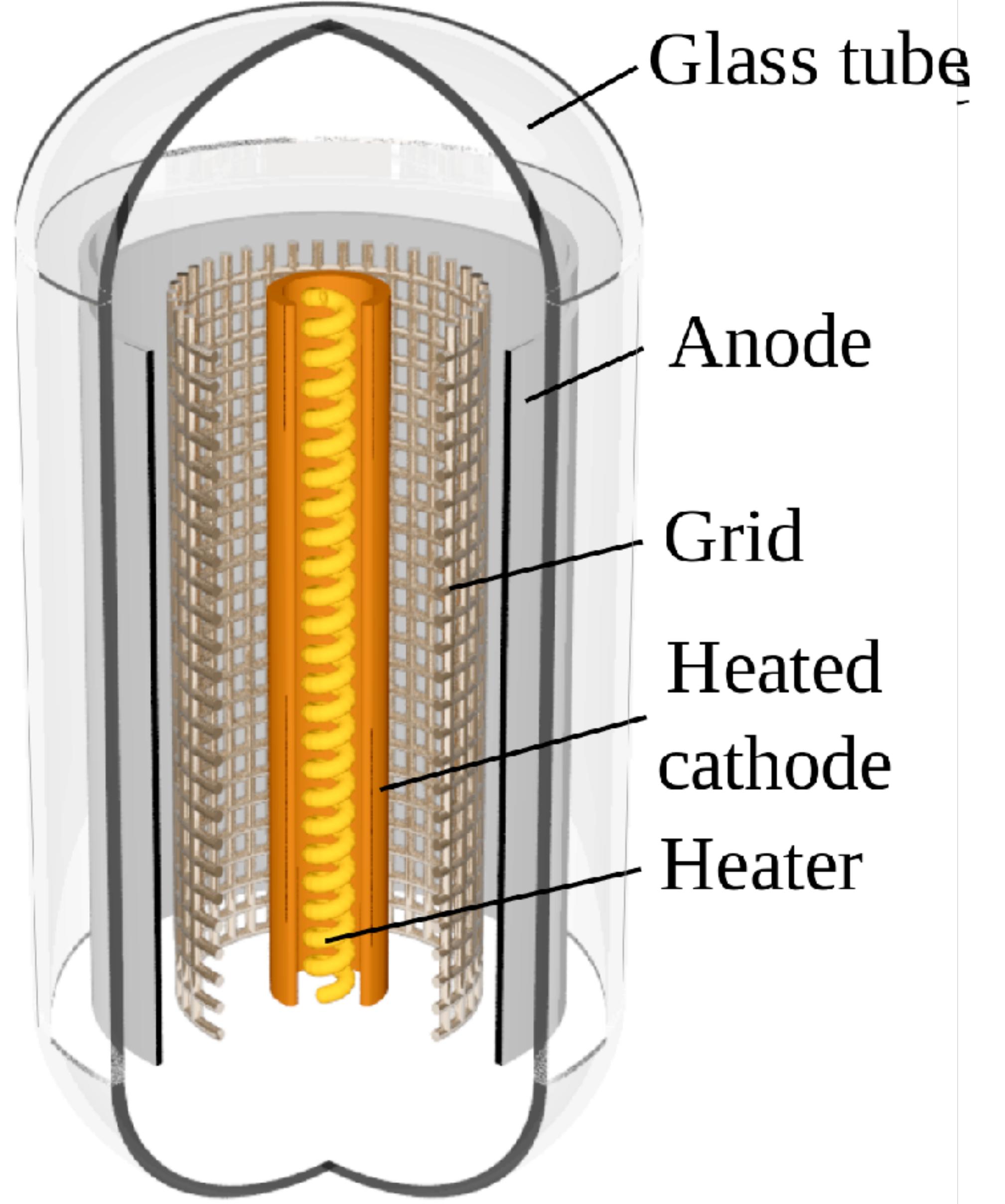


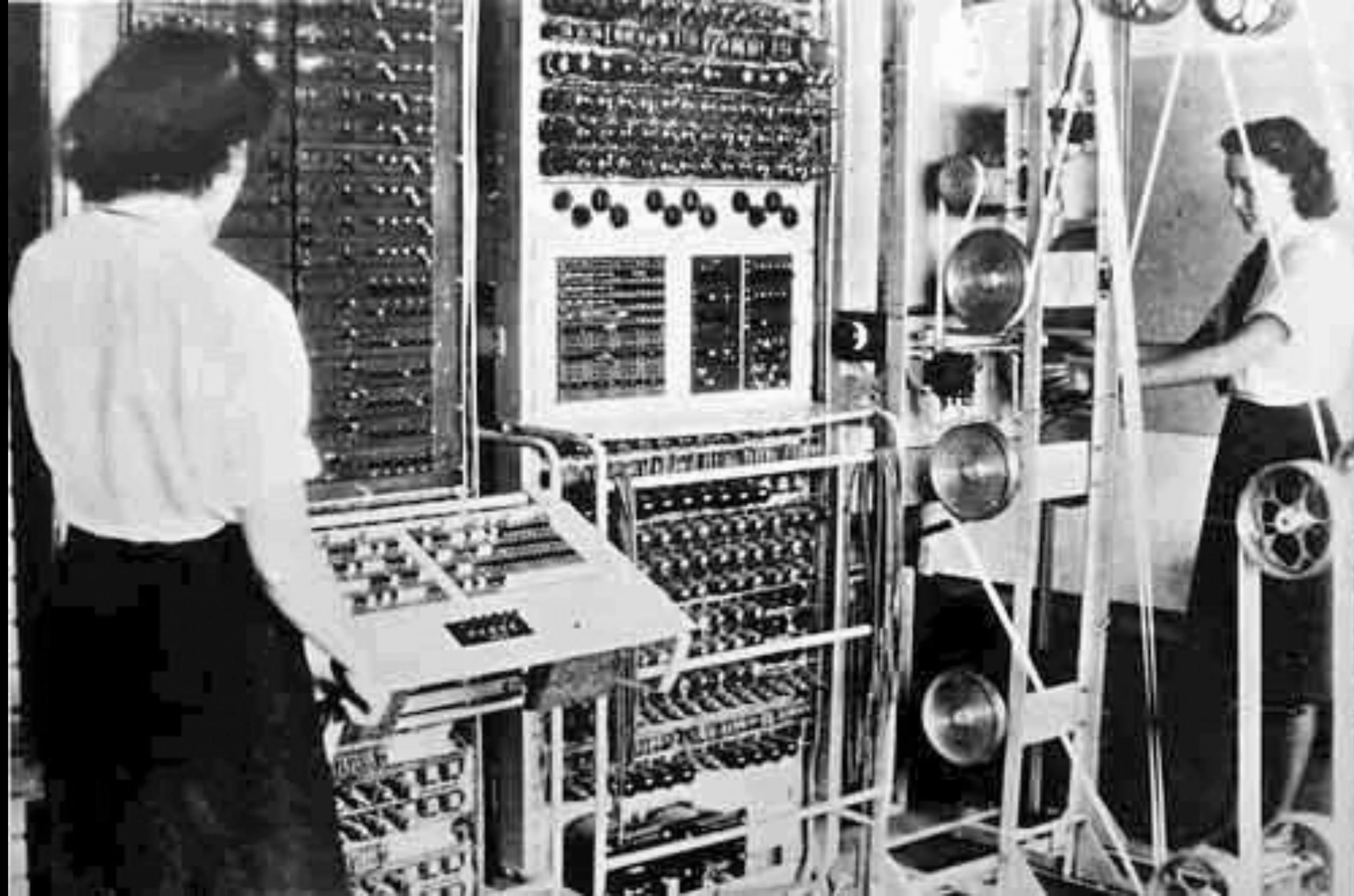
Difference Engine

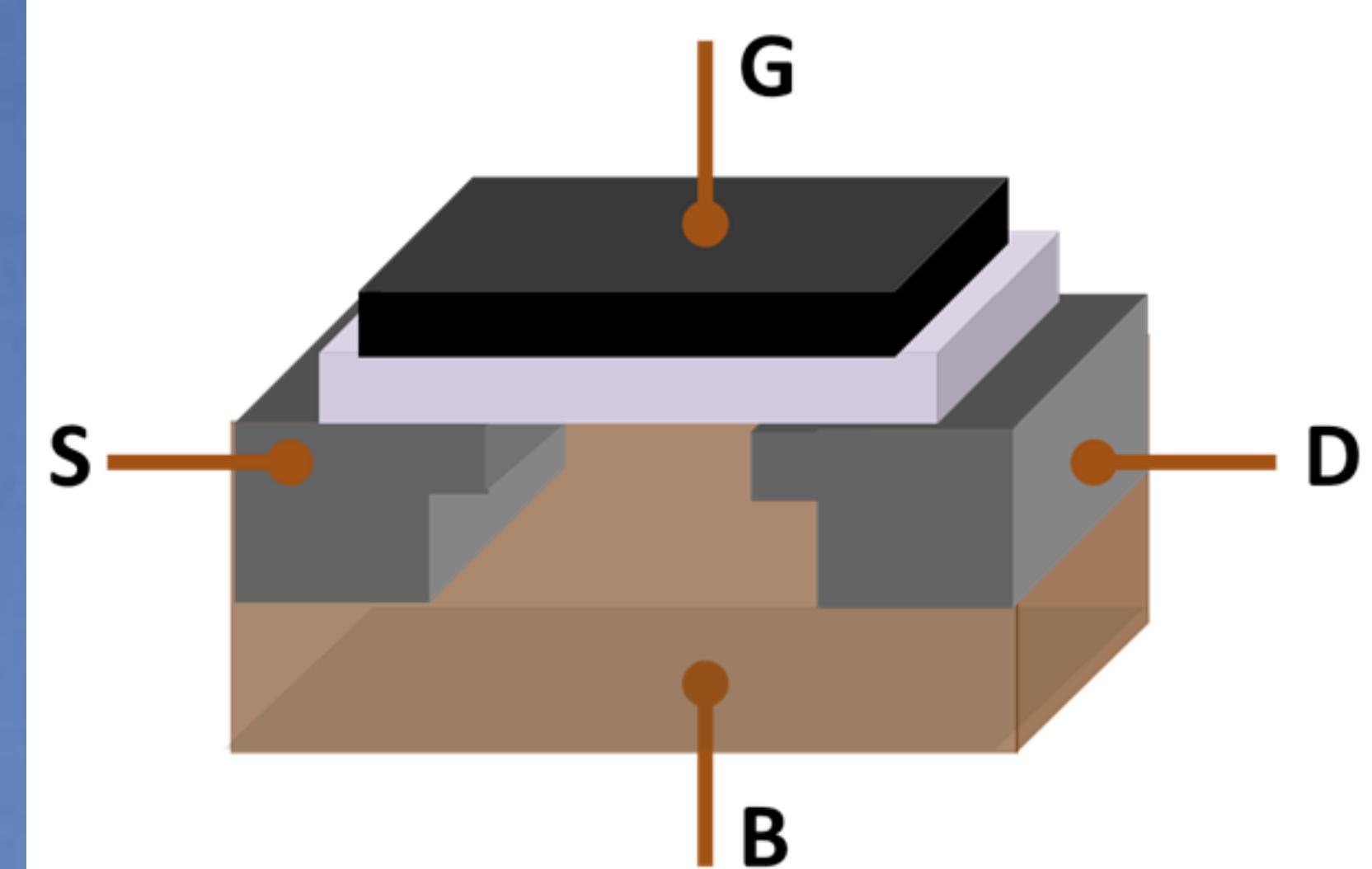
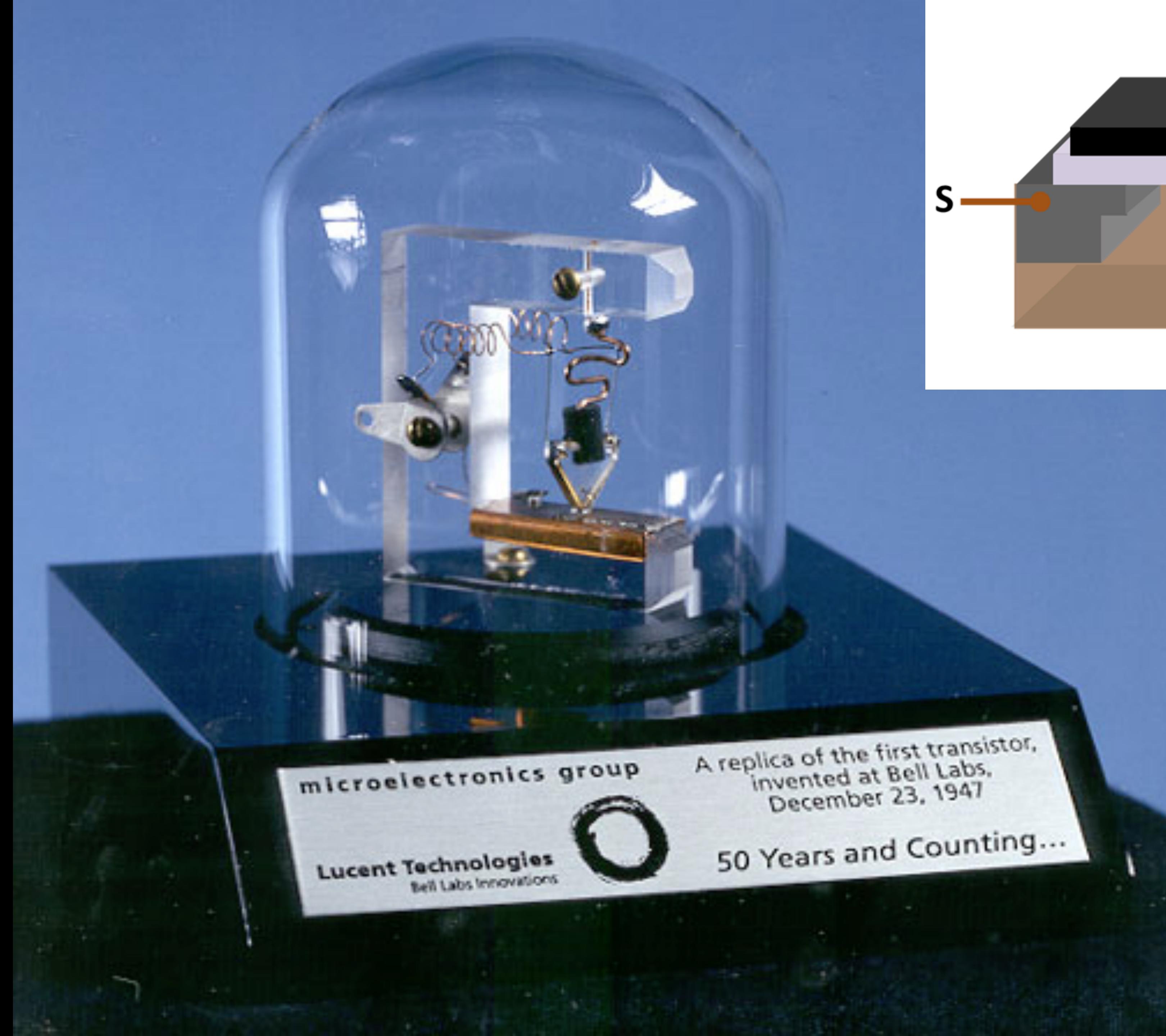


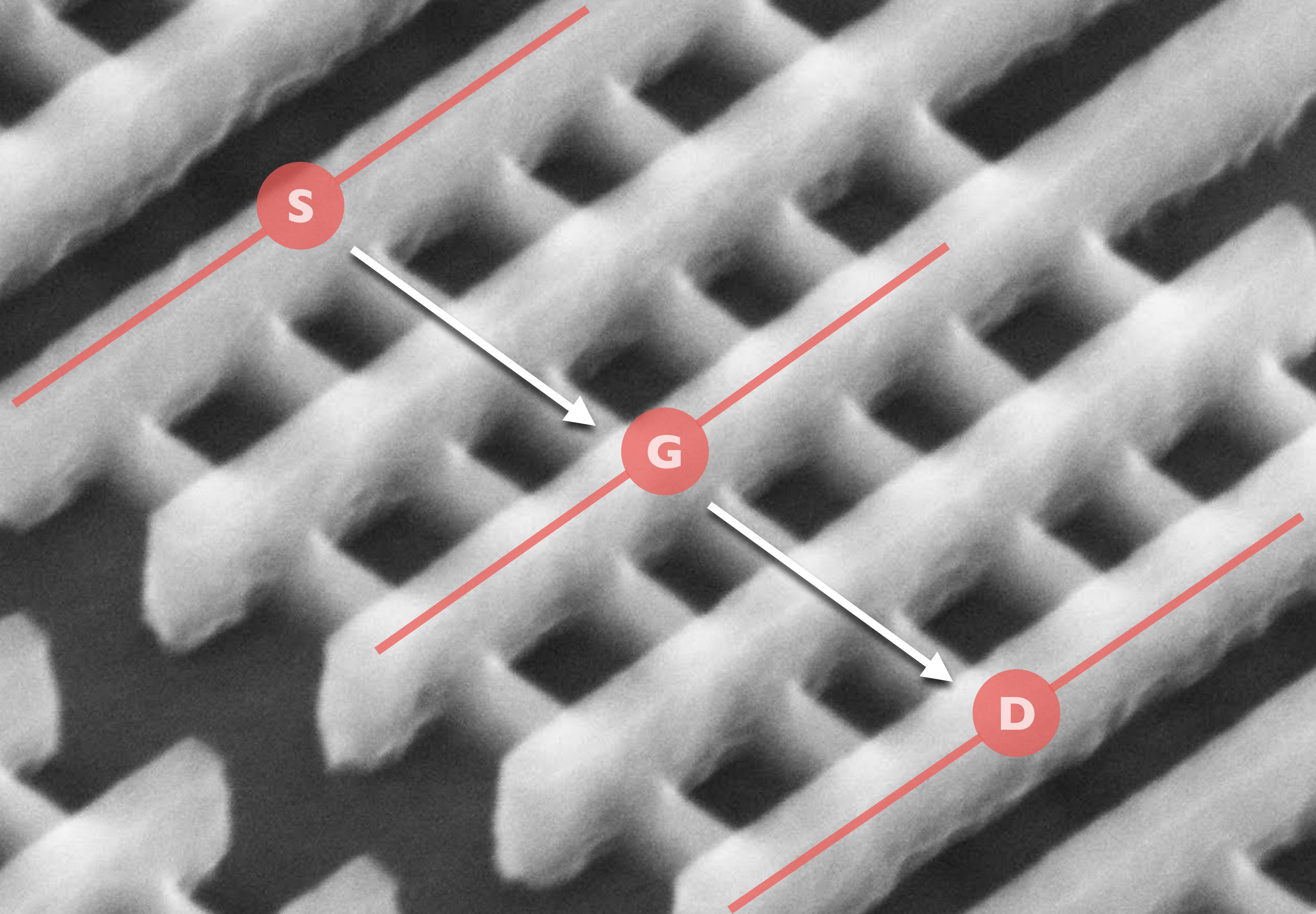
Analytical Engine



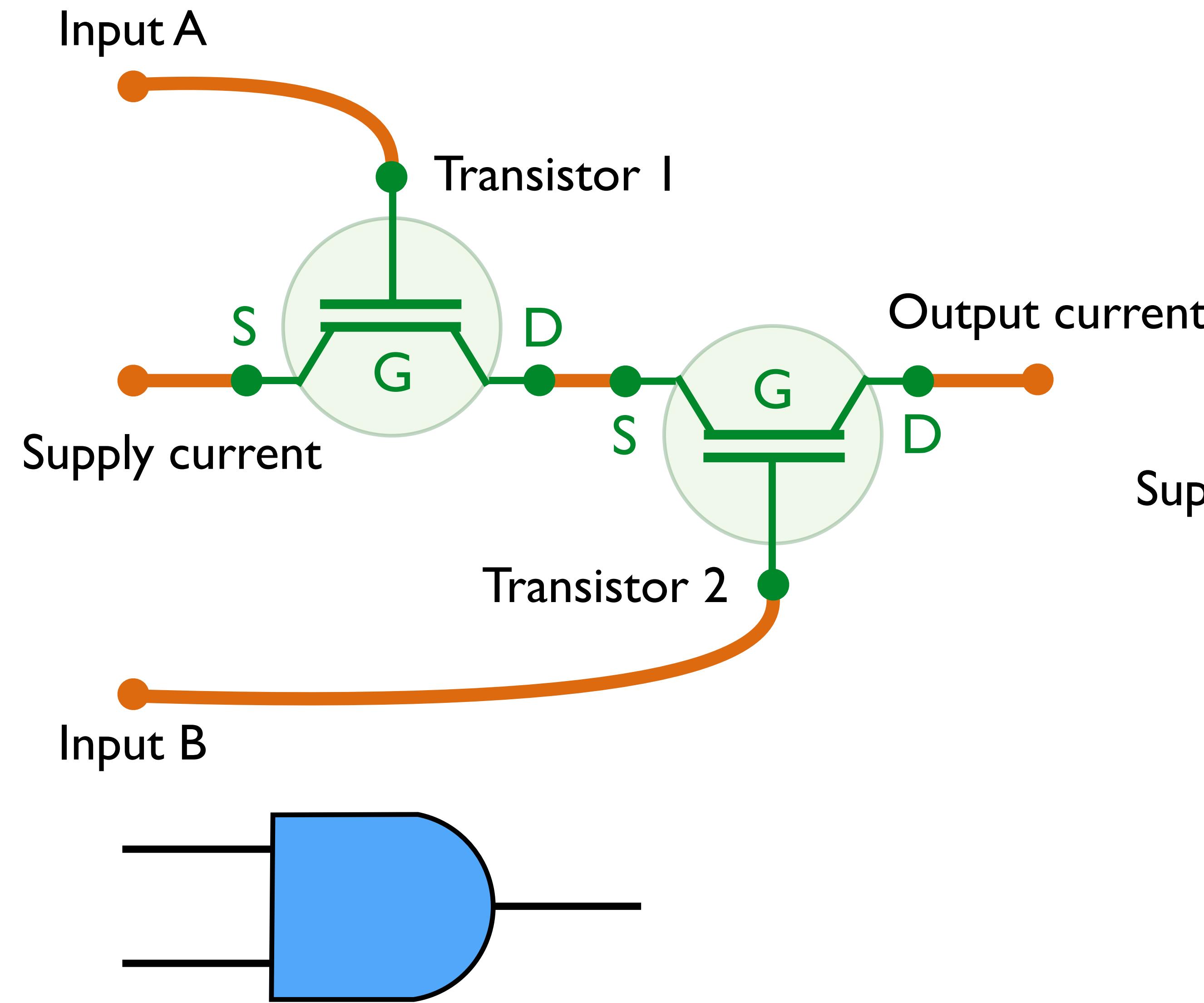




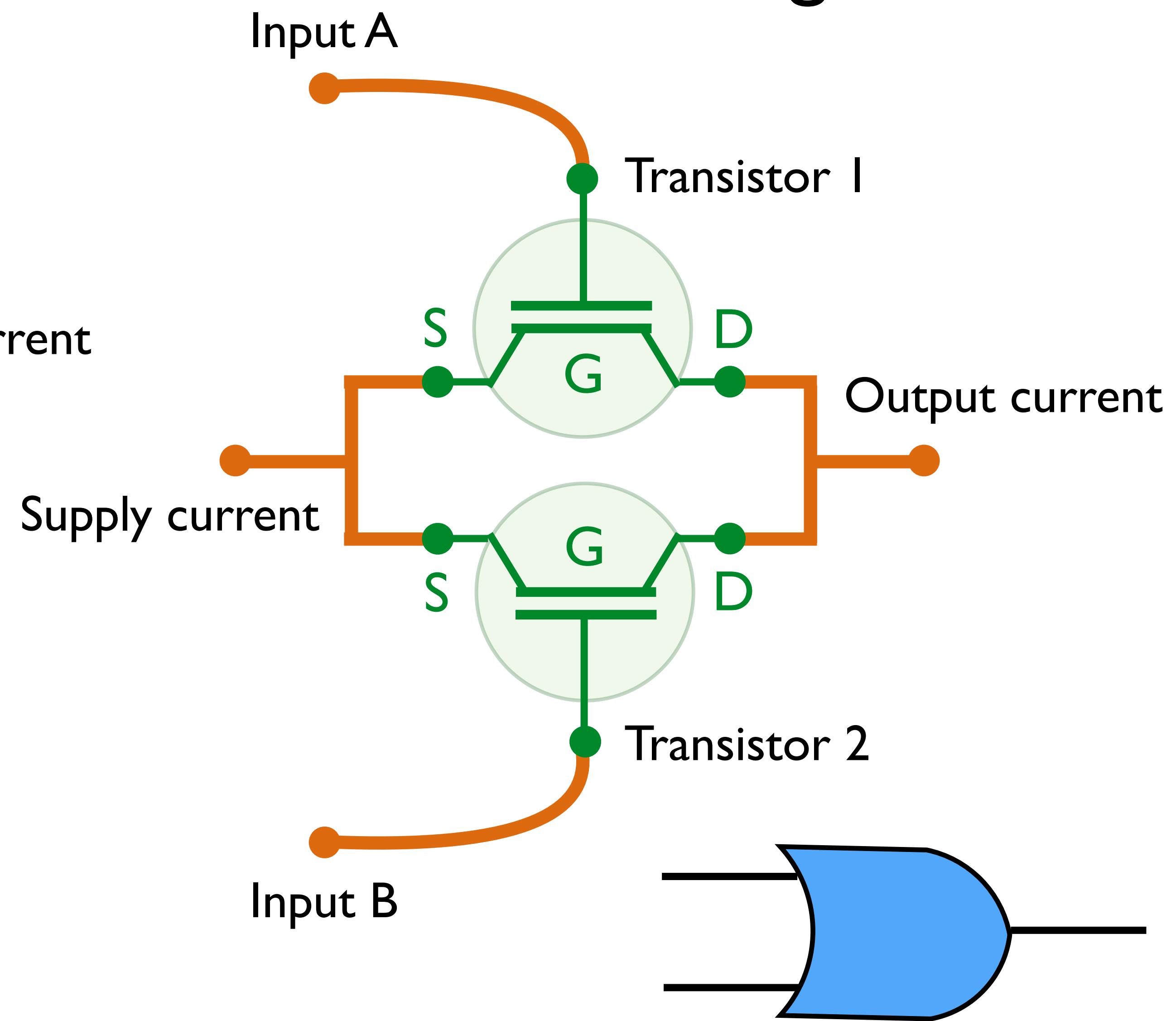




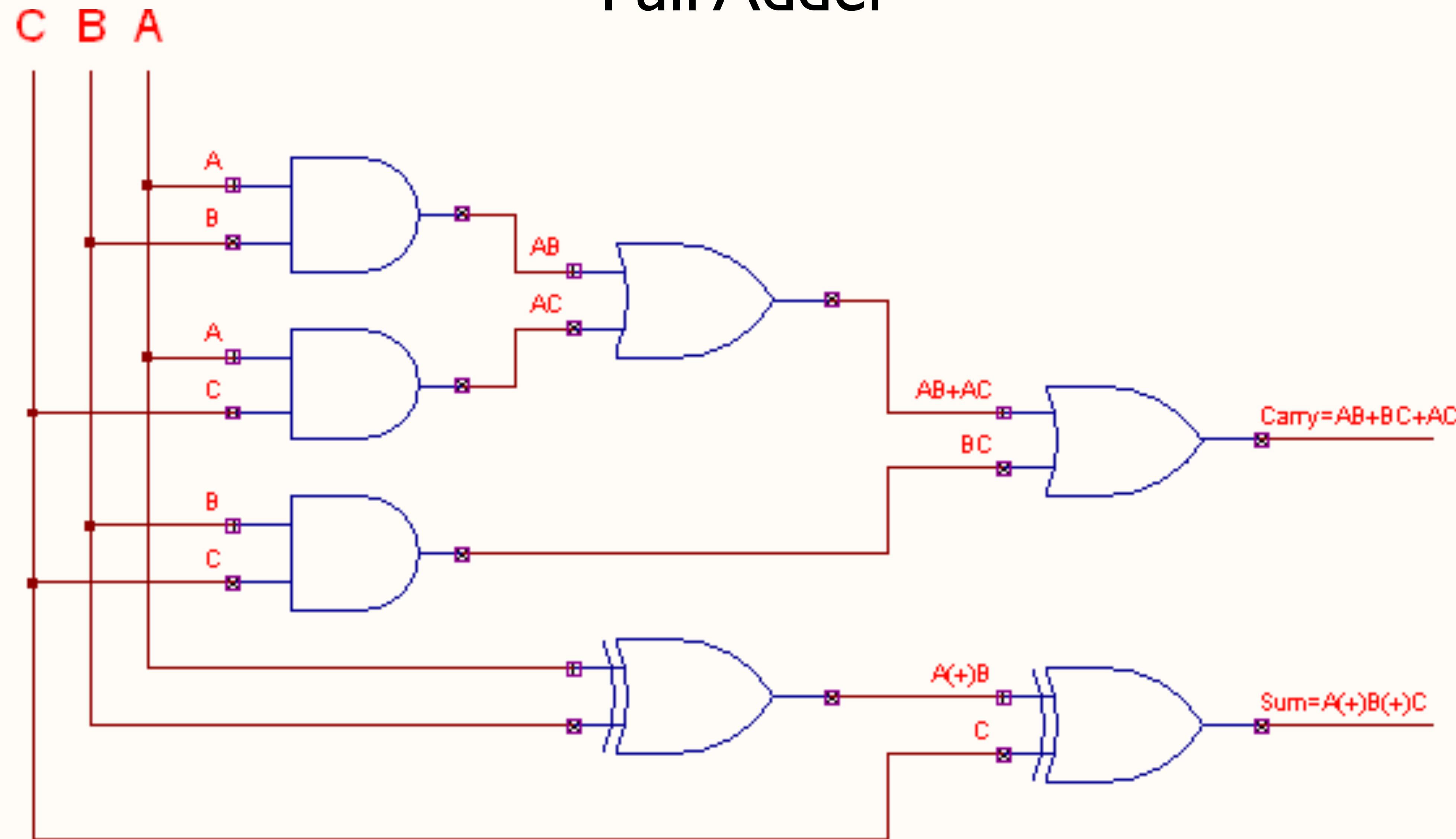
AND gate

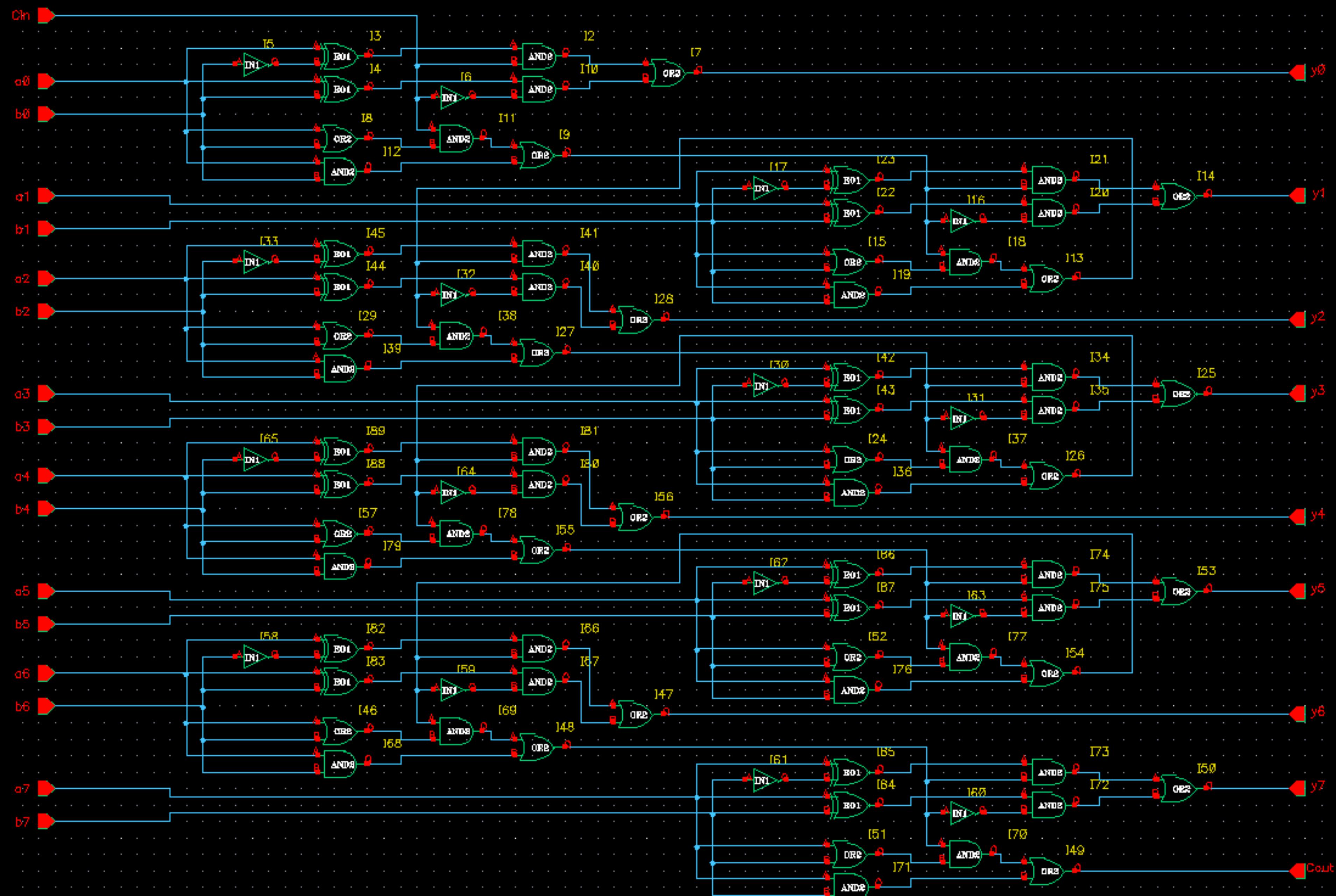


OR gate



Full Adder



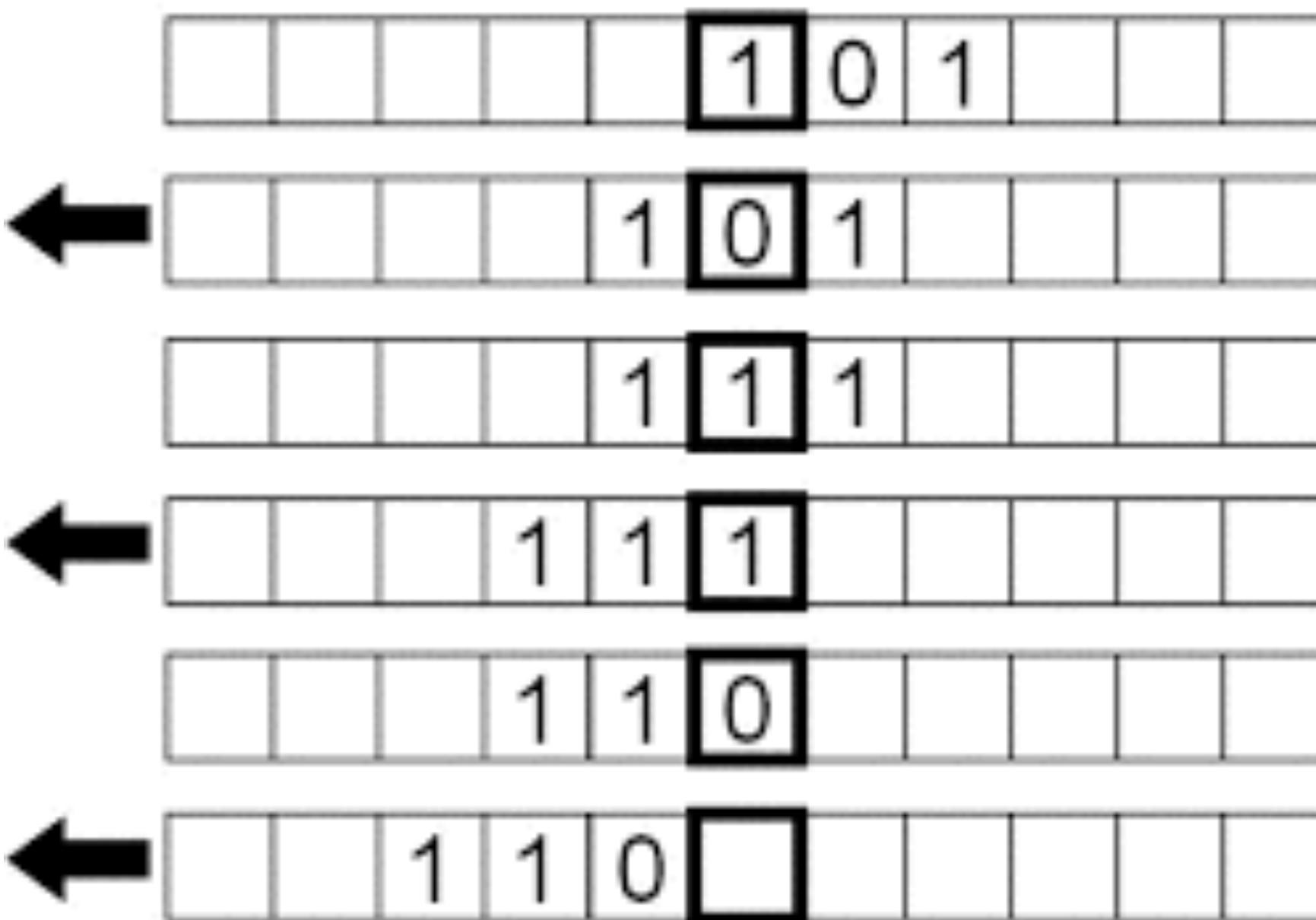


Give me an infinite piece of tape and I'll compute the universe

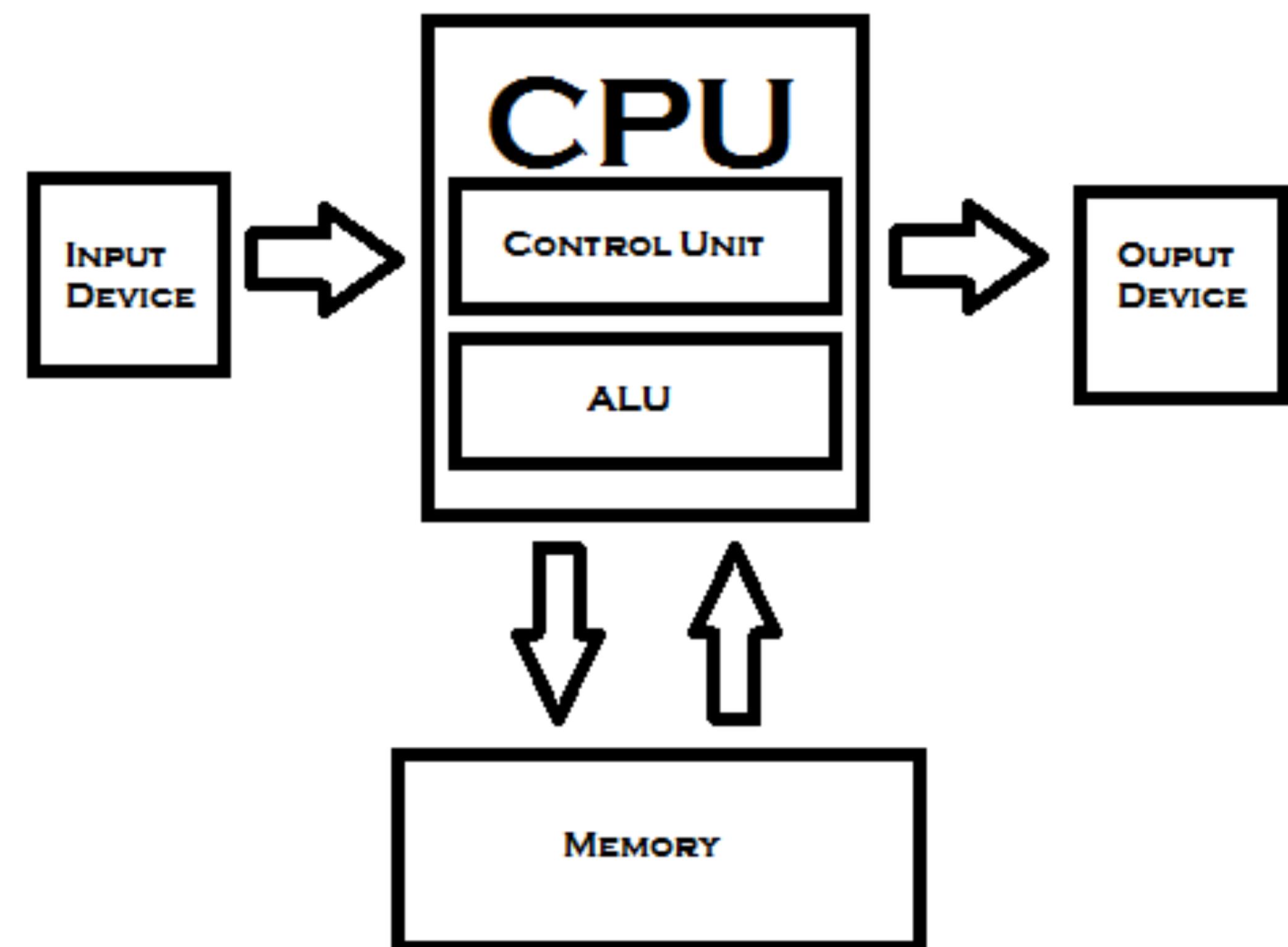


Add 1

- ❖ Move HEAD Right/Left
- ❖ Read value 0/1/blank
- ❖ Write value 0/1/blank



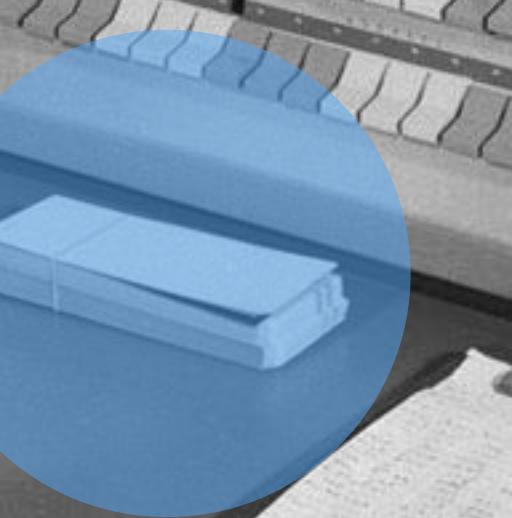
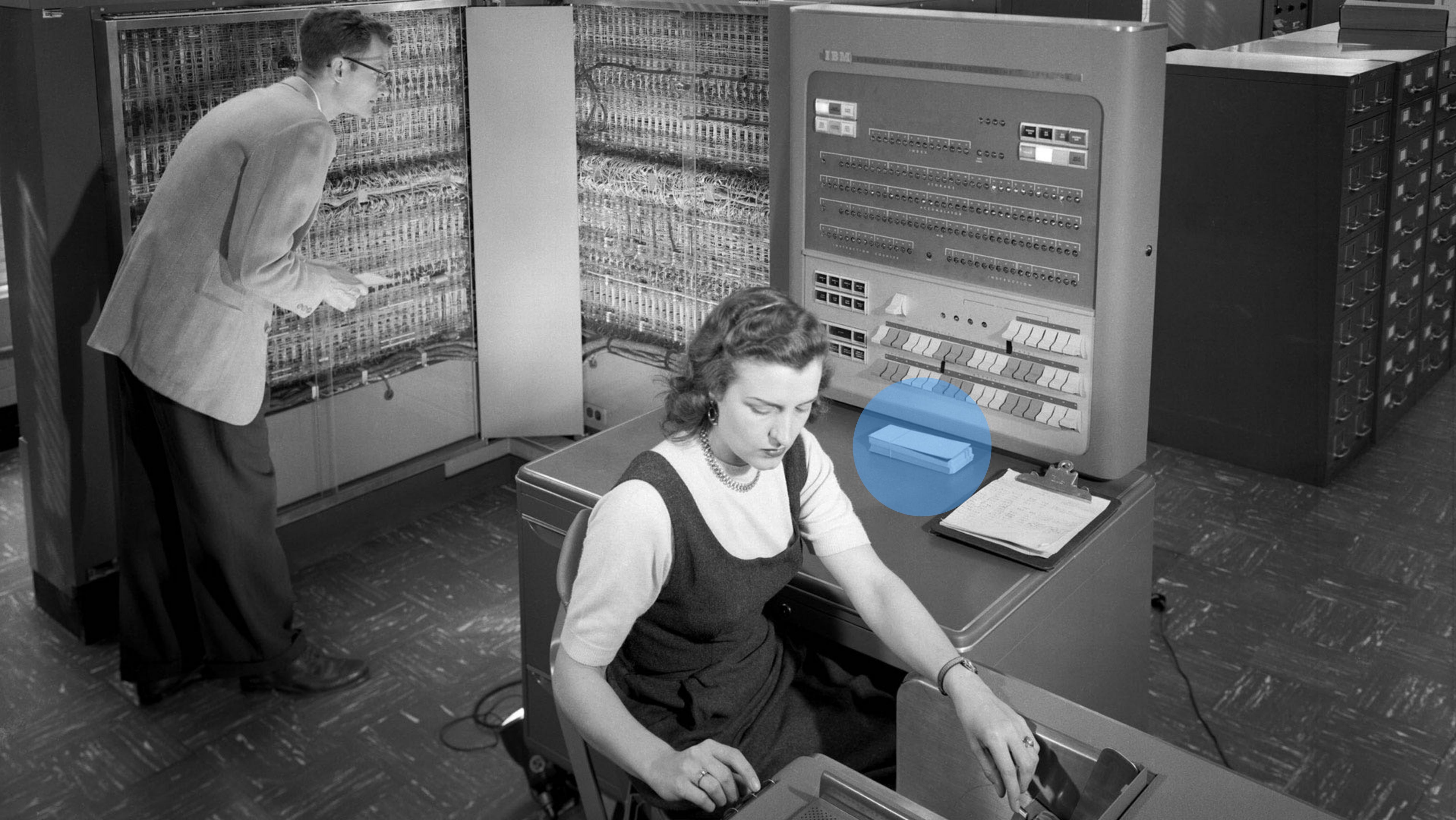
I built the first computer!



STORAGE









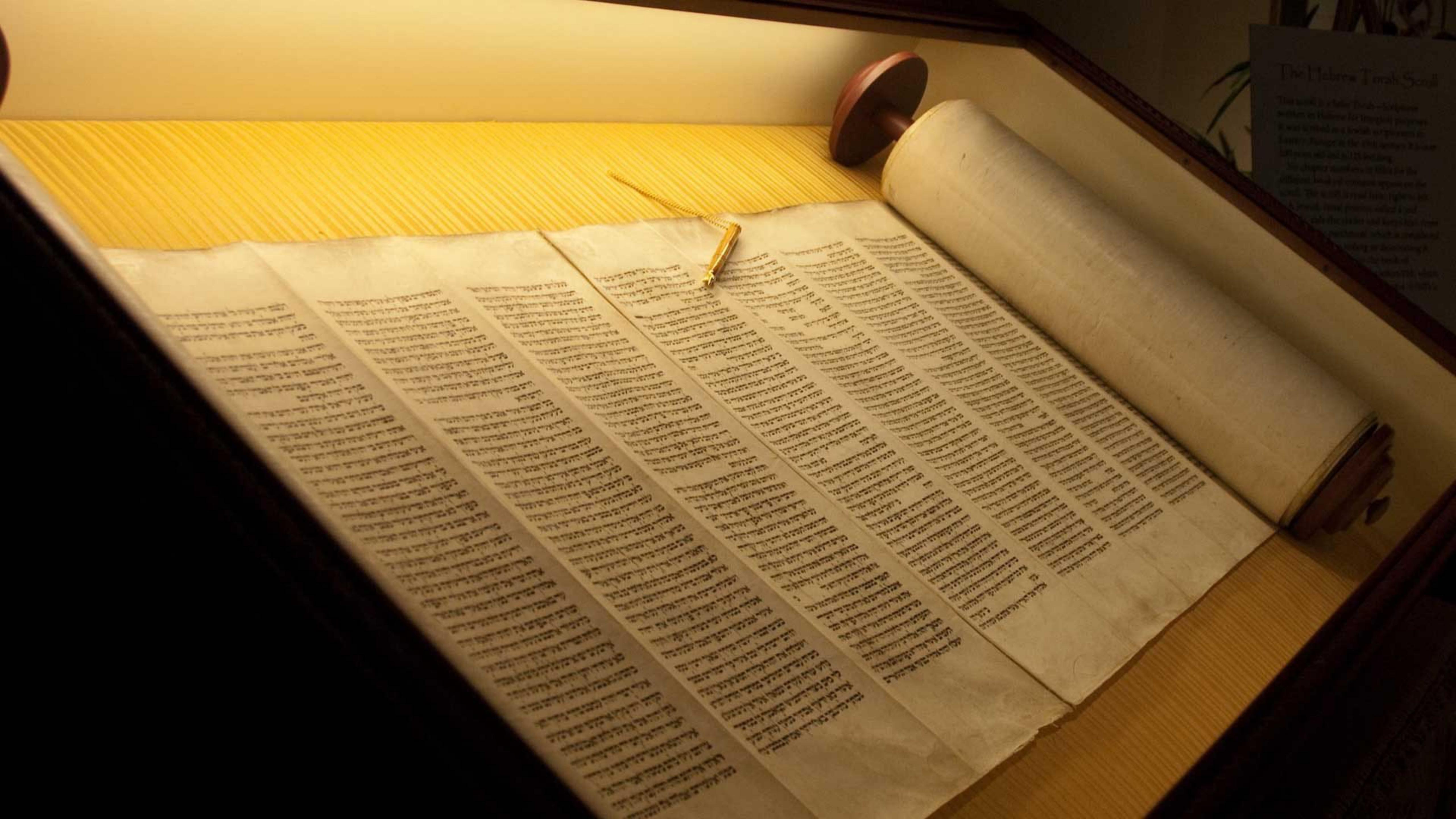


STORAGETEK

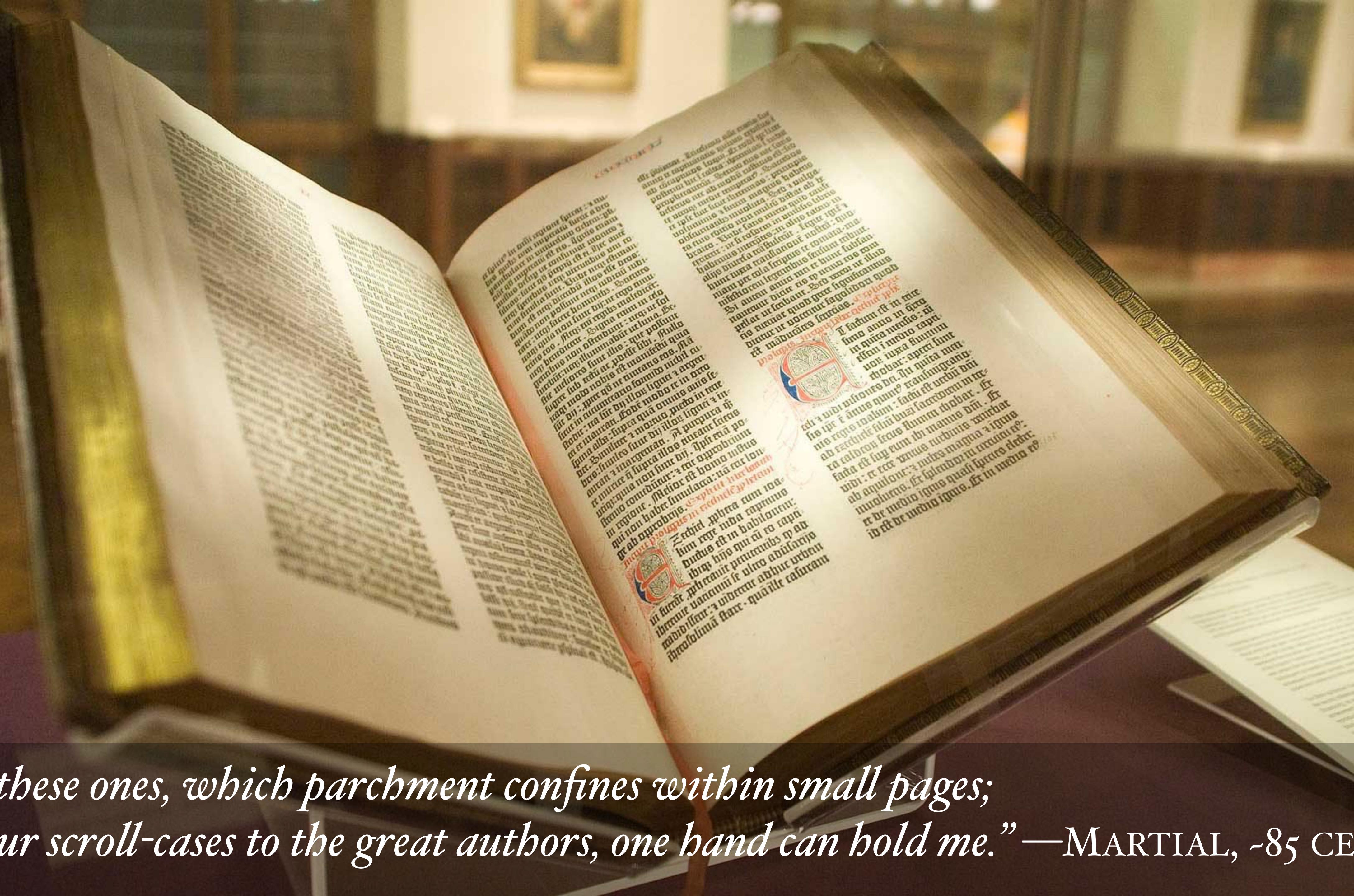
The Hebrew Torah Scroll

This scroll is written in Hebrew script on parchment. It was copied in a Jewish scriptorium in Yemen during the 18th century. It is one of many related to the building.

The original scroll of the Torah appears on the left. The scroll is kept in a wooden case.



*“...buy these ones, which parchment confines within small pages;
give your scroll-cases to the great authors, one hand can hold me.”* —MARTIAL, ~85 CE

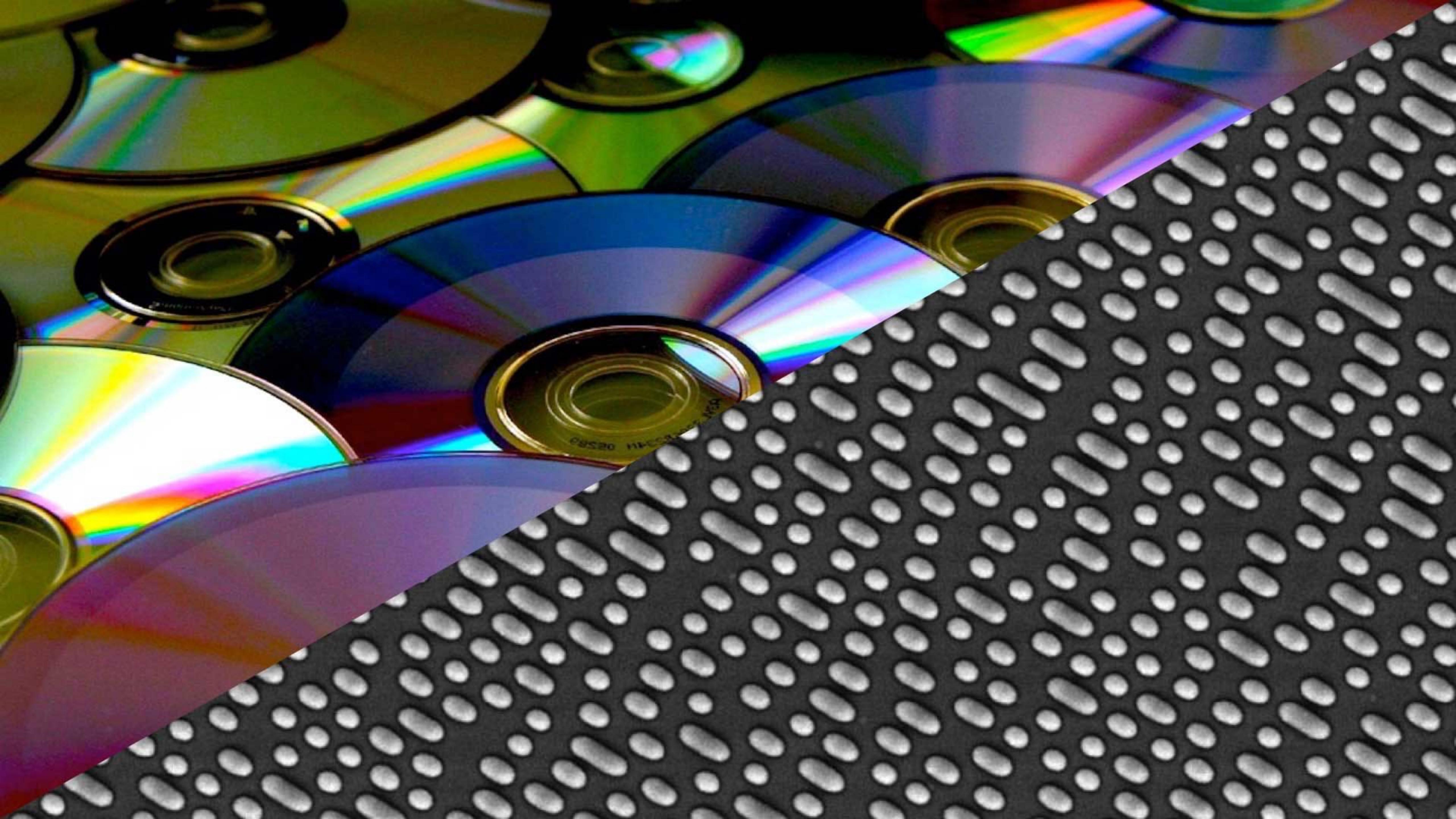


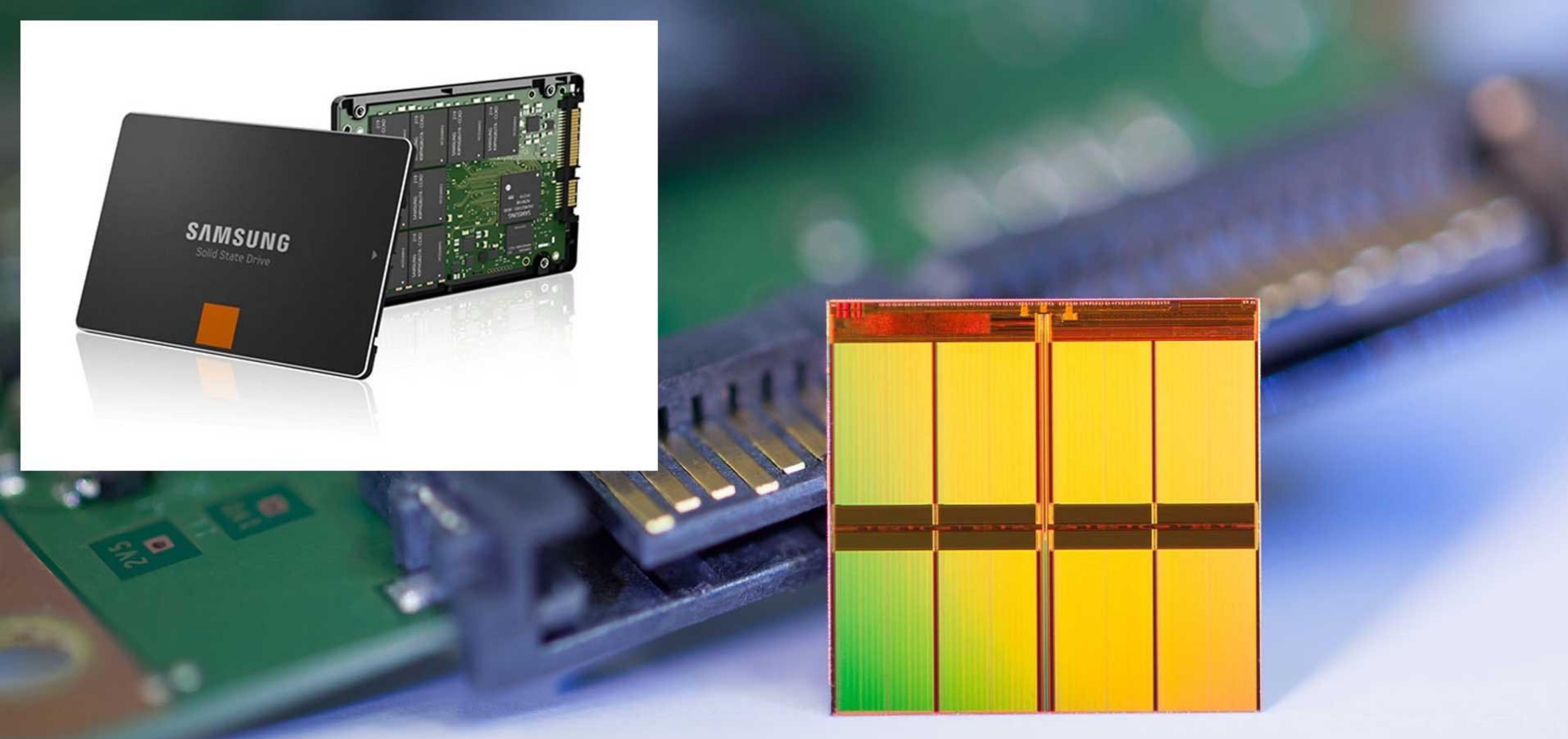


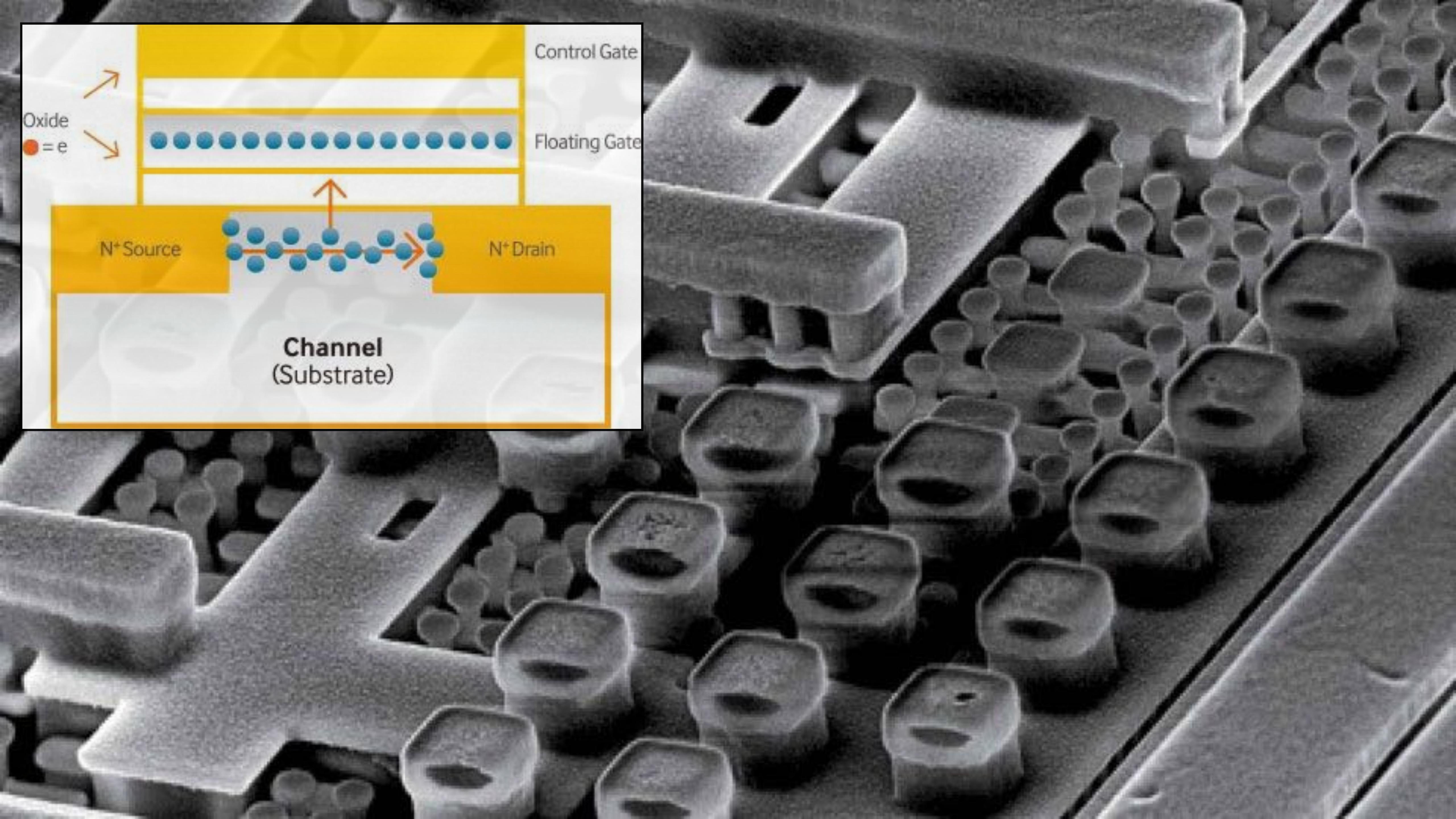
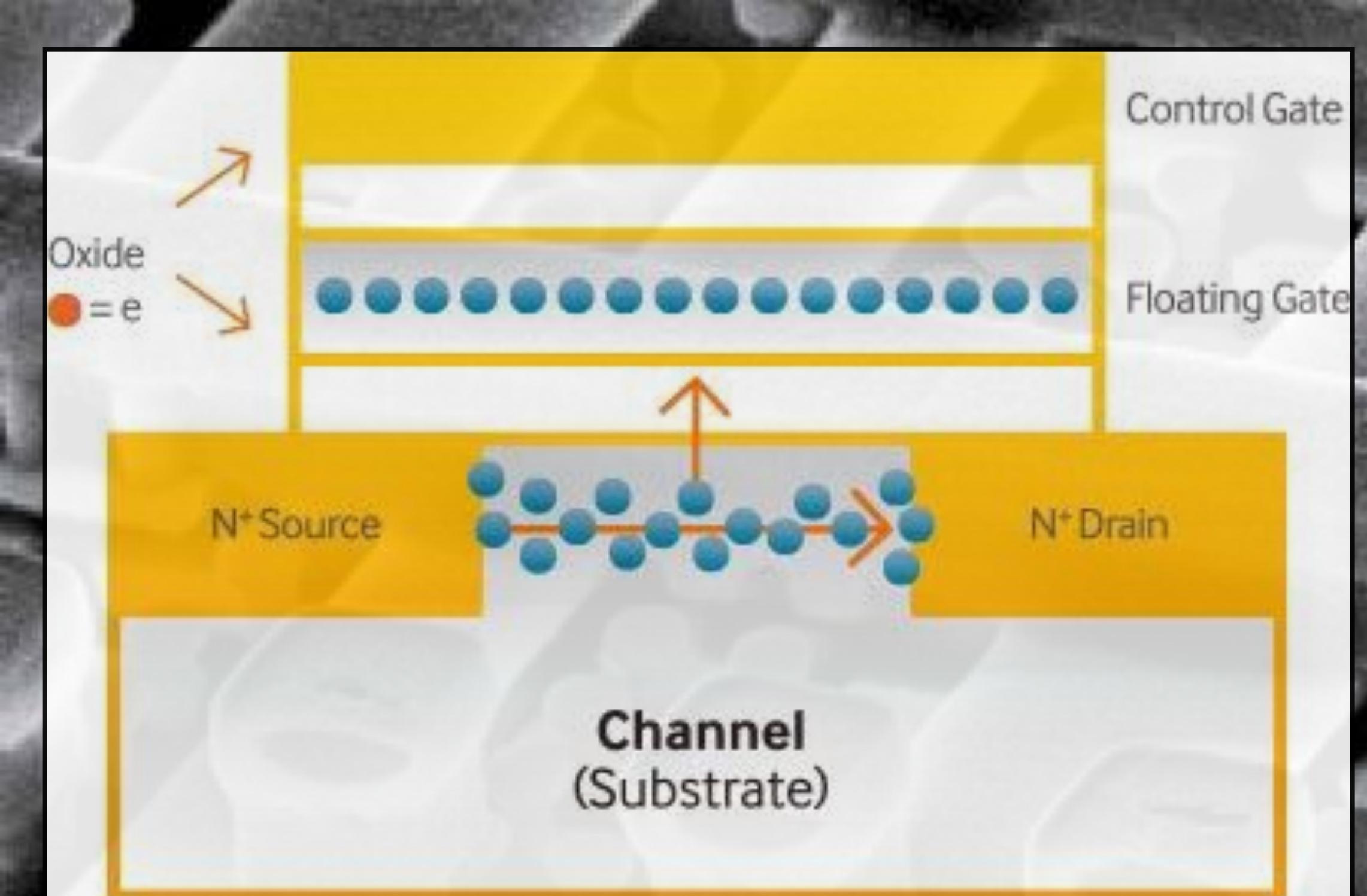
VIDEO LINK

4 SS/SD
boedem
о в БОЛГАРИИ







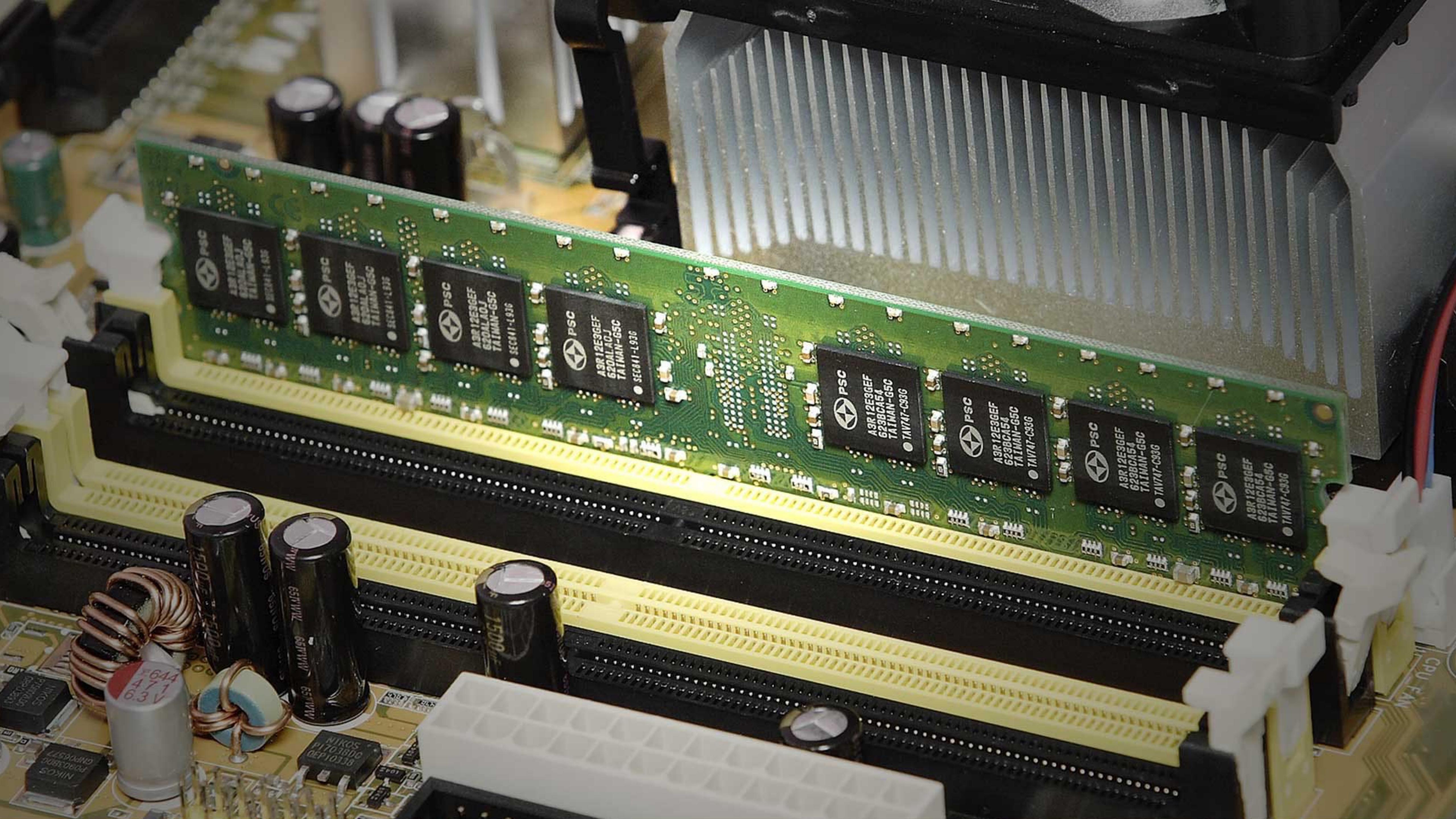


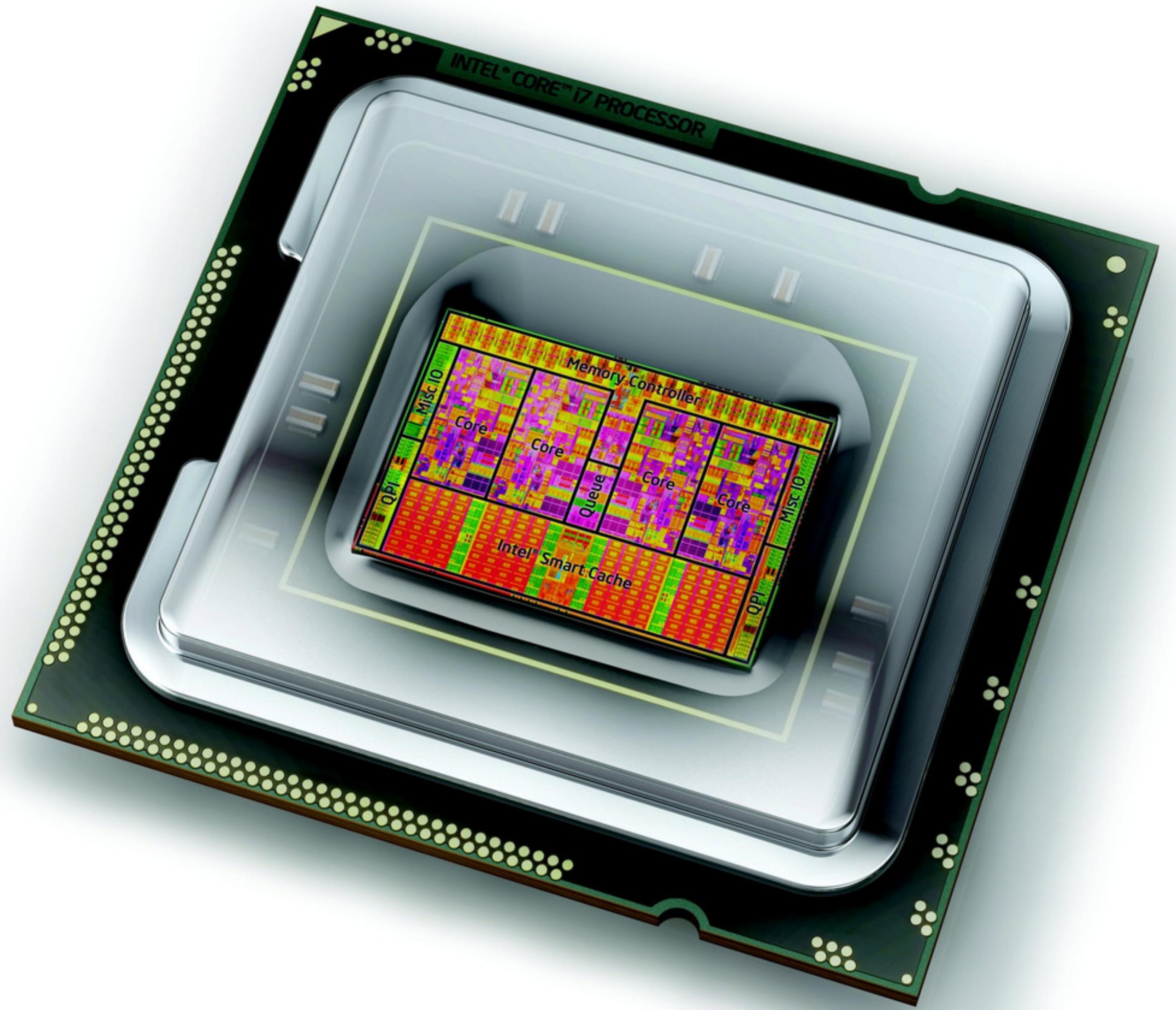


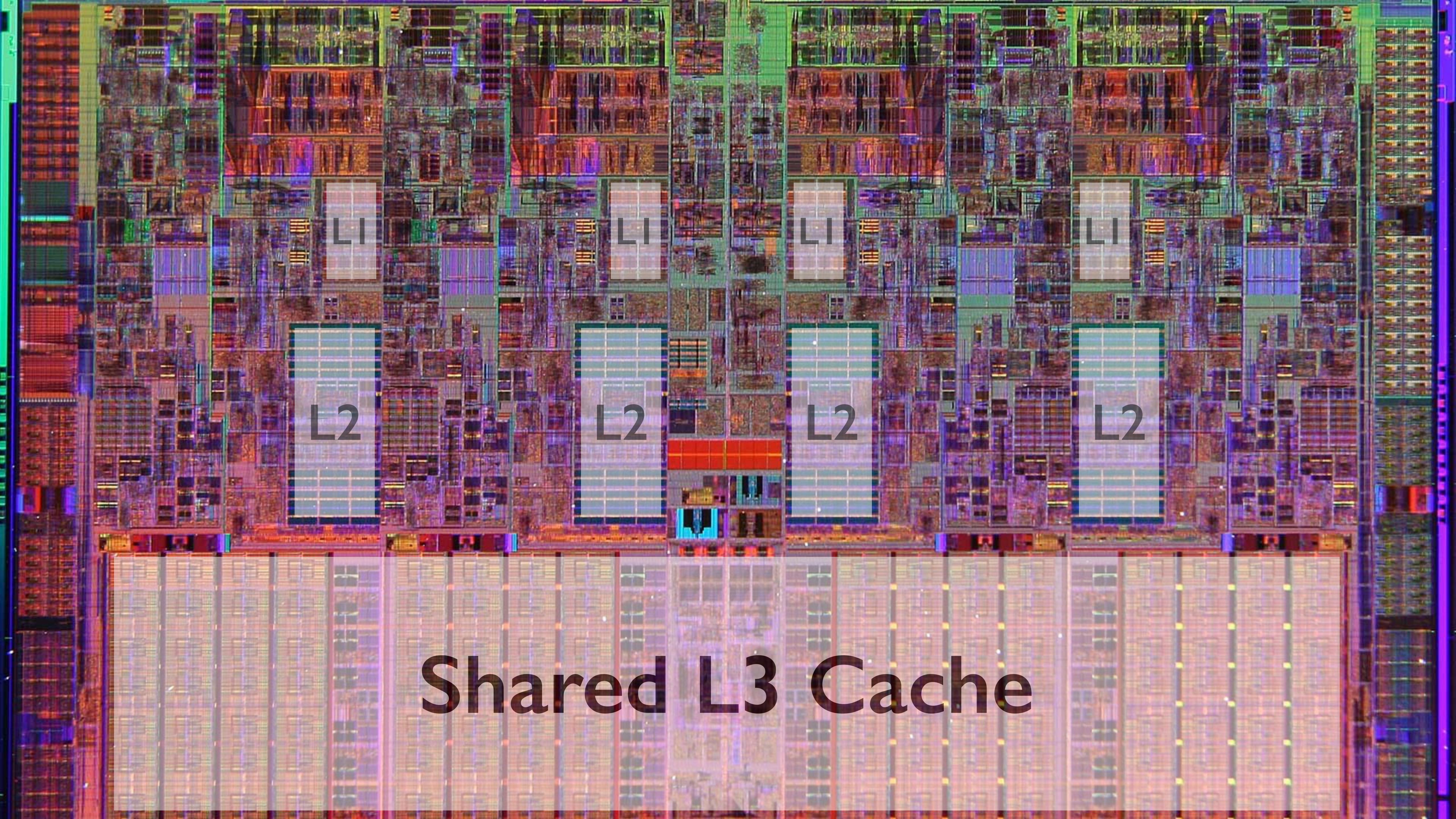
STORAGE



MEMORY

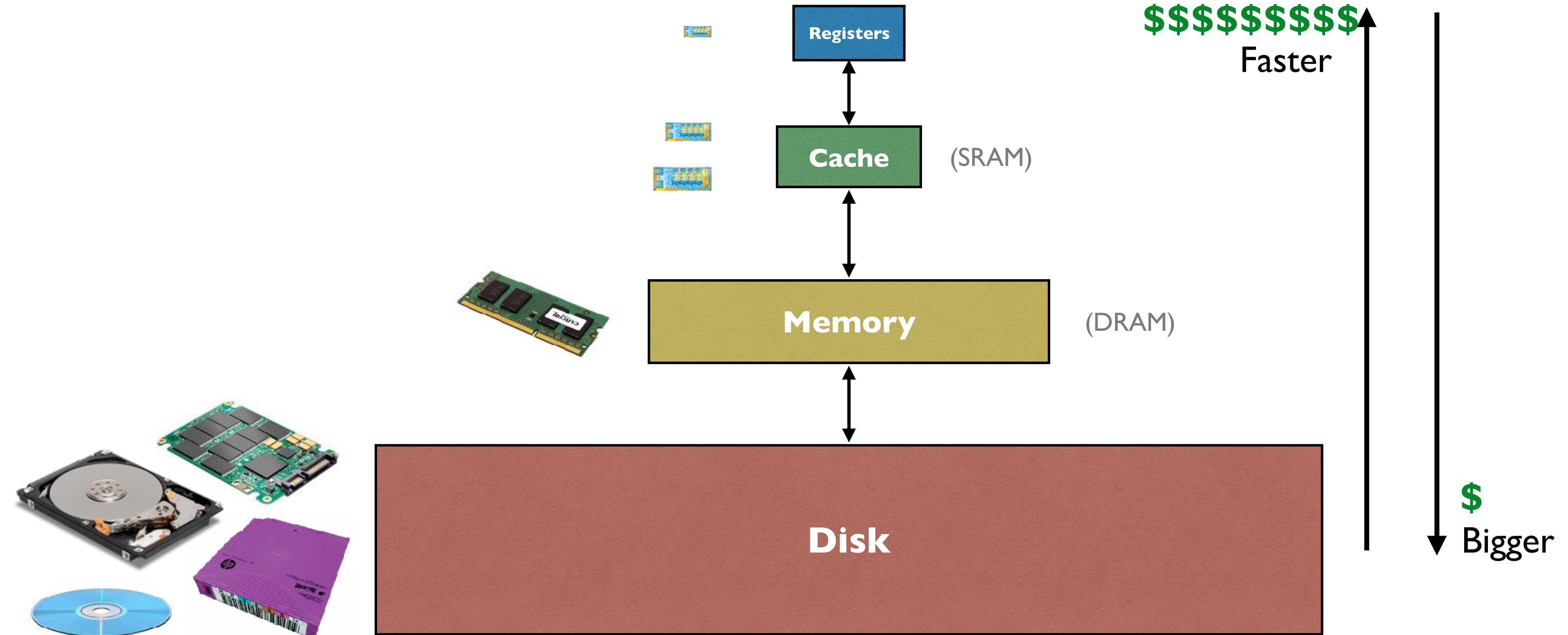






Shared L3 Cache

Size vs. Speed vs. Cost



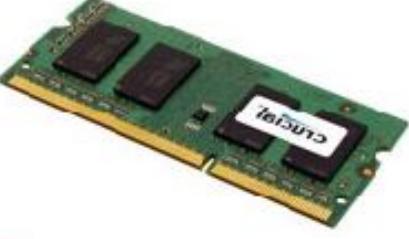


"Must Go Faster"

Medium	Typical Size (bytes)	Approx. Access Time	
CPU Register	64 bits = 8	one cycle < 1 ns	"Memory" primary storage ("non-blocking") volatile (goes away if power off)
L1 Cache	64 000	4–5 cycles ≈ 2 ns	
L2 Cache	256 000	~12 cycles ≈ 5 ns	
RAM	8 000 000 000	70 ns	
Solid State Drive	256 000 000 000	100 000 ns	"Storage" secondary storage ("blocking") non-volatile (persists even without power)
Hard Disk Drive	1 000 000 000 000	12 000 000 ns	
Optical Drive	650 000 000	150 000 000 ns	
Tape Drive	8 000 000 000 000	60 000 000 000 ns	
Network	a big truck?	6e7 – inf ∞ ns	



If 1 byte = 1 mL and 1 clock cycle = 1s

Medium	Typical Size (bytes)	Approx. Access Time	
	CPU Register	8 mL (1.5 tsp)	1 s (on page)
	L1 Cache	64 L (17 gallons)	2 s (on desk)
	L2 Cache	256 L (2 barrels)	5 s (in a pile)
	RAM	8k m³ (3 pools)	1 min (downstairs)
	Solid State Drive	256k m³ (Hindenburg)	1 day (other city)
	Hard Disk Drive	2m m³ (Pyramid)	4 months (Mars)
	Optical Drive	650 L (5 barrels)	4.8 yrs (Pluto)
	Tape Drive	8 m³ (Chagan Lake)	2 millennia (stars)
	Network	planet?	maybe Alpha C., never?

"Memory"
primary storage
("non-blocking")
volatile
(goes away if power off)

"Storage"
secondary storage
("blocking")
non-volatile
(persists even without power)

Part II: Representations & Encodings

11101000 00011110 11010100 10010110 01000010
10101111 11000100 10001010 11011101 10011111
11101111 11011111
01101101 There are only 10 types of 00000100
00100000 people in the world: those 10001111
00110010 who understand binary, and 11111111
01110010 those who do not. 01011100
00110111 00110001
11000110 10100011 01101010 10010110 11000111
00001000 10010001 00101011 11011101 11100101
01101110 00101011 00011100 10011111 01101001
01010111 00100111 1111010 11111000 10111011
01111000 11000010 01000110 00100000 01111101

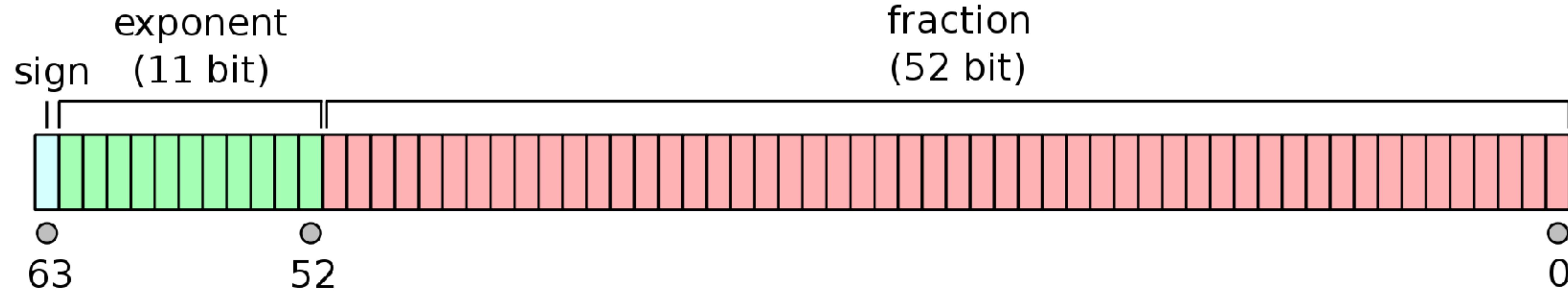


Using {0, 1} to Represent [0, 255]

Physical State	OFF	ON	ON	OFF	OFF	ON	ON	OFF
Binary Notation	0	1	1	0	0	1	1	0
Order of Magnitude	2^7	2^6	2^5	2^4	2^3	2^2	2^1	2^0
Decimal Value	128	64	32	16	8	4	2	1
Applicable Value	0	64	32	0	0	4	2	0
Total Decimal Value	$102 = 64 + 32 + 4 + 2$							

! ?

IEEE 754: Floating-Point Signed Double



- 64 bits total — "double" the previous 32-bit word size
- 52 bits for the *fraction of the significand* (with an implicit “1” bit)
 - Decimal example: in 1.5204×10^4 , the *fraction* is 5204
- 11 bits for the *exponent* — where the *bicimal point* should *float to* (order of mag.)
 - Many special rules – encoding patterns for ± 0 , $\pm \infty$, NaN, etc.
- 1 bit for *sign* (0 positive, 1 negative)

Hexadecimal Notation

Hex. digit	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
Dec. notation	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Bin. notation	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111

- Base-16: uses sixteen different digits per "place" (order)
- To avoid ambiguity: prefaced $0x$ or $U+$ or $\#$, or subscript $_{16}$
- Much easier to convert b2 to/from b16 than to/from b10
- Example: what is $0x2a$ (i.e. $2a_{16}$, $U+2a$) in b2? 10111001 in hex?

BUNPŌ SANNEN SANGATSU HI
KUNIMITSU

According to the writings of the *Unchimyō Collection*, the Bunpō Sannen Kunimitsu at the right became the third generation.

KUNIMITSU UDA
[OEI 1362 ETCHŪ] CHŪKOTŌ JŌSAKU

The early Kunimitsu that moved his residence from Yamato to Kuni Uda to Etchū and entered the priesthood was said to be of around Bunpō, but the existing Kunimitsu works are of around the Yoshinochō period. This smith is probably the father of Oei Kunifusa and Kunimune nado. He signed with a small signature, hamon is sugi.

UDA KUNIMITSU

KUNIMITSU TANSHŪ JŪ
[OEI 1362 TAJIMA]

He is the founder of the Hōjō-ji Ha, and is said to be one of the three disciples of Sōshū Sadamune, but along with the two disciples of Masamune, this is a story that is not within the scope of the actual work.



PAGE K337

KUNIMITSU

PLATE I:

centered around Shintōgo Nakura, they were probably disengaged. The family of Rai Kunitoshi of Kyoto,mitsu and Kunihiro were also both called Hasebe, and Hasebe Kunishige of Yamashiro was probably someone who came after this.

of Shōchū, and the center of that is being Shōwa. In regard to it signed Kunimitsu, there prob-

ably. In the Shōwa Hon (Book

the son of Bizen Saburō

period, he is made out to be

en he was 88 years old,

from Kunimune, there

time of Kunitsuna,

iro Den seems to

ōwa and Genkō

of suguba, and

ths. If Kuni-

smith as a

that was

or son.

nt in

are

the one kanji of the name was the usual. I can think of the

MITSU since Osafune Mitsutada and Nagamitsu, the KUNI

of the Rai Mon, and the KUNI in the Sōshū smiths passed

on to Kunihiro, the son of Kunimitsu. After Hiromitsu, the

names of Hiromasa, Sukehiro,

into the Muromachi period.

The names in the columns, top to bottom, starting with the

right hand column, are as follows.

KUNIMUNE, KUNIMITSU, KUNIHIRO, KUNISHI-

(YAMASHIRO HASEBE)

KUNITSUNA, YUKIMITSU, HIROMITSU

SAMUNE, SADAMUNE, AKIHIRO

line is a conjectural

..... - . - - - . - - - - - - - - - -

HELLO WORLD





ASCII

- American Standard Code for Information Interchange (1960s)
- 7-bit unsigned integers (stored in 8 bits) = 128 chars... +?

Binary	Decimal	Glyph	Binary	Decimal	Glyph
0010 1110	46	.	0011 1010	58	:
0010 1111	47	/	0011 1011	59	;
0011 0000	48	o	0011 1100	60	<
0011 0001	49	I	0011 1101	61	=
0011 0010	50	2	0011 1110	62	>
0011 0011	51	3	0011 1111	63	?
0011 0100	52	4	0100 0000	64	@
0011 0101	53	5	0100 0001	65	A
0011 0110	54	6	0100 0010	66	B
0011 0111	55	7	0100 0011	67	C
0011 1000	56	8	0100 0100	68	D
0011 1001	57	9	0100 0101	69	E

UTF-8

- ◎ **Universal Coded Character Set + Transformation Format – 8-bit**
- ◎ **Handles every code *point* of Unicode (1.1M+; ~260K assigned)**
- ◎ **Variable-width: one to four 8-bit unsigned integers (code *units*)**
- ◎ **Superset of ASCII — backwards-compatible (best for web)**

Glyph	Unicode Code Point	Code Unit 1: <i>singleton or lead</i>	Code Unit 2: <i>trail 1</i>	Code Unit 3: <i>trail 2</i>	Code Unit 4: <i>trail 3</i>
I	U+0049	0100 1001			
♥	U+2764	1110 0010	1001 1101	1010 0100	
J	U+004A	0100 1010			
S	U+0053	0101 0011			
😊	U+1F604	1111 0000	1001 1111	1001 1000	1000 0100

UTF-16

- Variable-width: one or two 16-bit unsigned integers
- Incompatible with ASCII (no 8-bit blocks)
- byte vs. word stream issues
- byte order ambiguity
- space inefficiency for most languages, even C/J html
- (Sort of) predicated UTF-8, which is why stuff inherits it



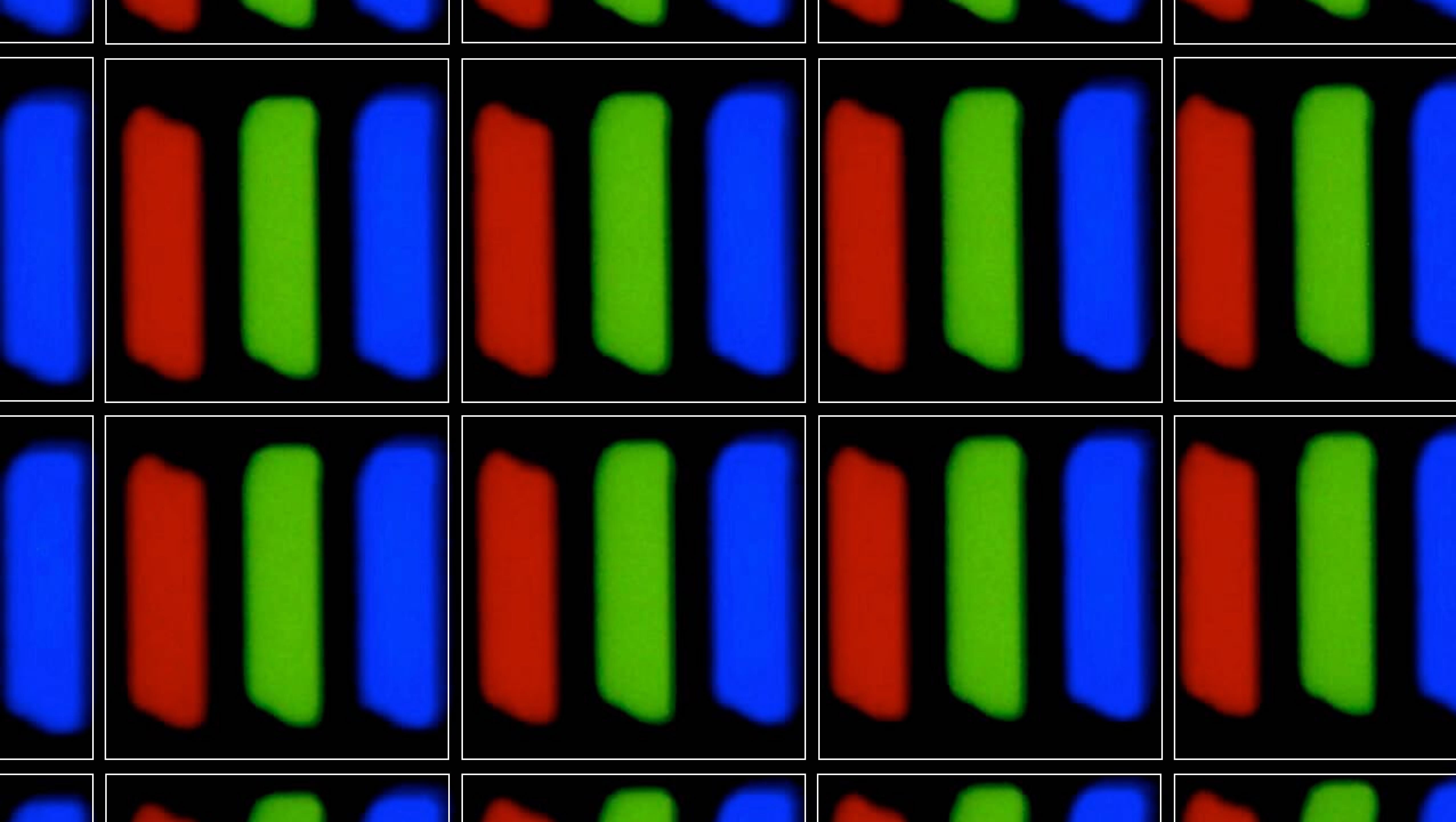
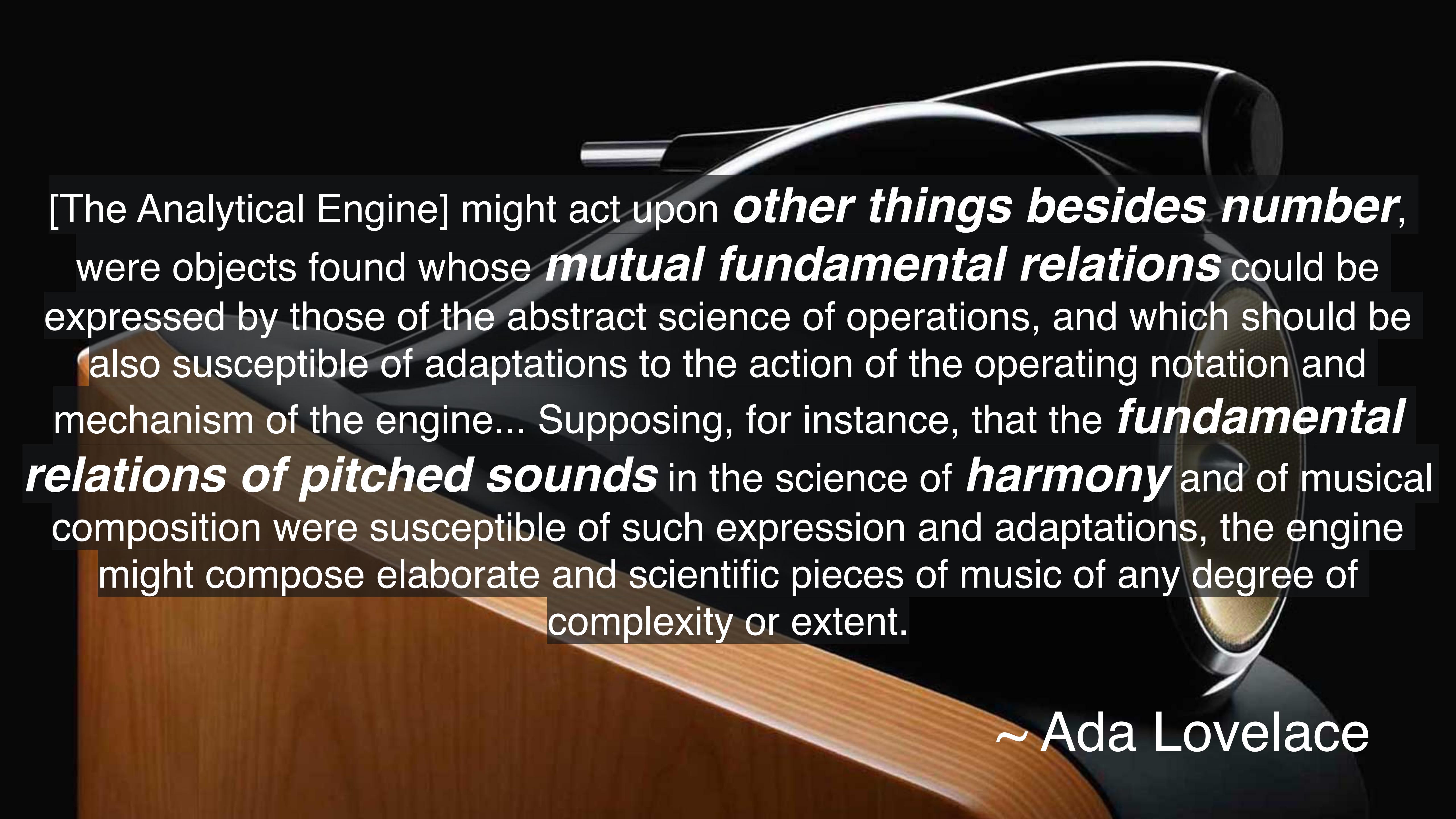


Image Encoding

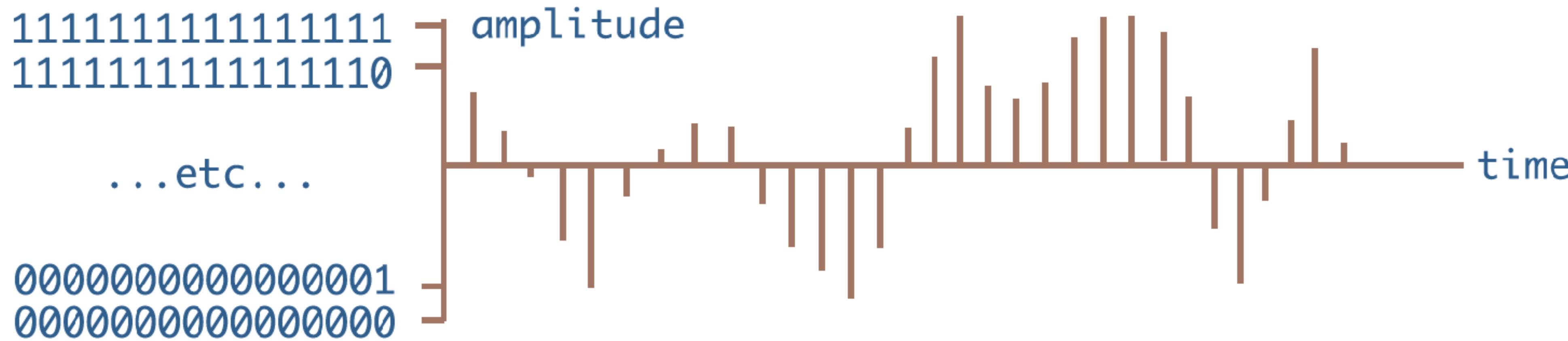
- Simple *bitmaps* are triads of 8-bit unsigned ints for RGB values
- 8 bits makes 256 possible brightnesses per *channel*
- "24-bit" ($8 + 8 + 8$) monitors have $256^3 = \sim 16.8M$ RGB distinct channel combinations ("colors").
 - Since grayscale means RGB channels have to be the same, that's still only 256 possible B&W values.



[The Analytical Engine] might act upon ***other things besides number***, were objects found whose ***mutual fundamental relations*** could be expressed by those of the abstract science of operations, and which should be also susceptible of adaptations to the action of the operating notation and mechanism of the engine... Supposing, for instance, that the ***fundamental relations of pitched sounds*** in the science of ***harmony*** and of musical composition were susceptible of such expression and adaptations, the engine might compose elaborate and scientific pieces of music of any degree of complexity or extent.

~ Ada Lovelace

Audio Encoding



- Simplest is raw PCM (pulse-code modulation)
- 44,100 samples per second; each sample 16-bit *amplitude*
- Different amplitudes over time models an audio wave
- DAC converts values to speaker cone analog signal

Part III:

Abstractions & Languages

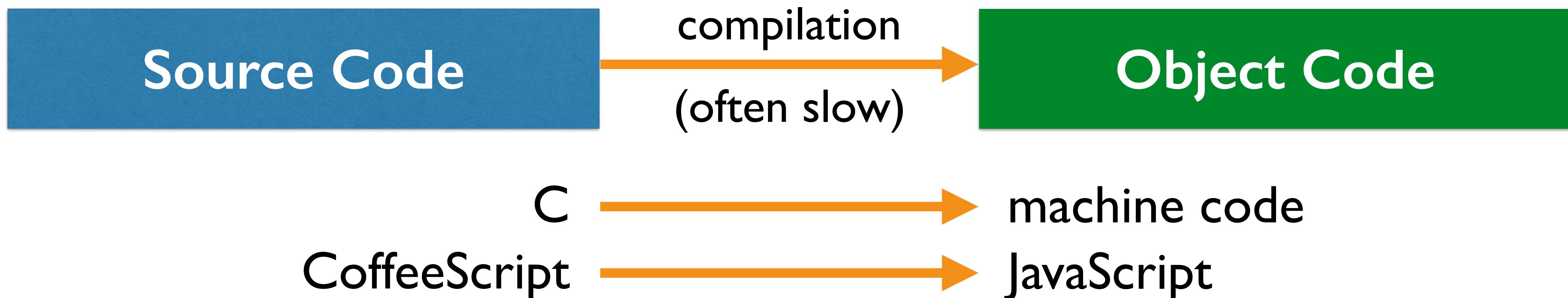
Machine Code & Assembly

- Every CPU has its own *instruction set* — binary codes that trigger the CPU to perform operations on registers.

	op. code	source register	target reg.	destination reg.	shift amount	function type
instruction	000000	00001	00010	00110	00000	100000
hex	0x0	0x1	0x2	0x6	0x0	0x20
decimal	0	1	2	6	0	32
meaning	arithmetic	register 1	register 2	register 6	no offset	addition
English	"take the value in register 1, add the value in register 2, place the result in register 6"					
assembly	add \$t6, \$t1, \$t2					

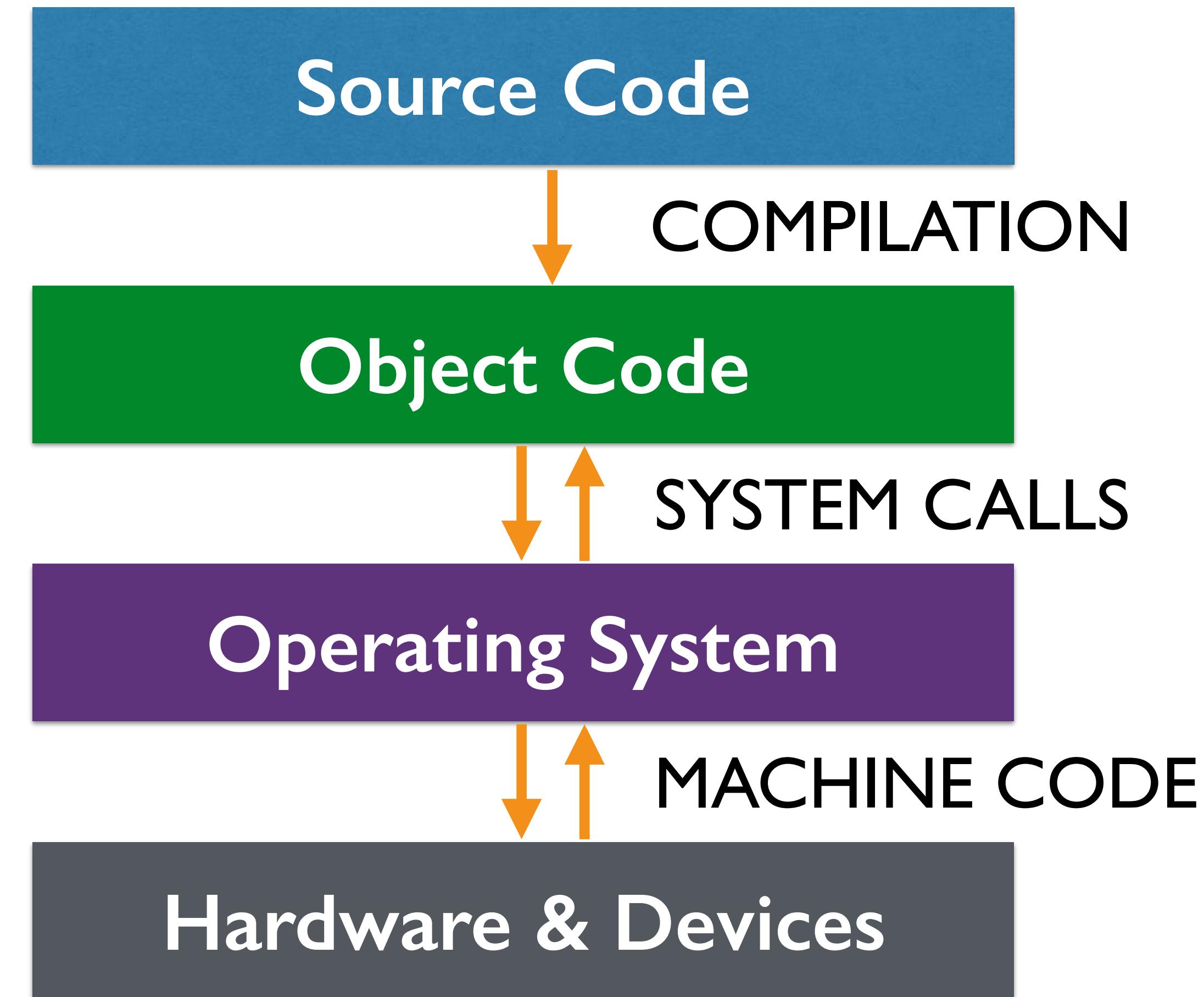
Compilers & Interpreters

- First compiler written in 1952 by Grace Hopper, for A-0.
- “[She] helped teach the machines a language, stopped them from speaking in undecipherable numbers.” — 60 minutes
- Followed by Mark I, FORTRAN, COBOL, etc.



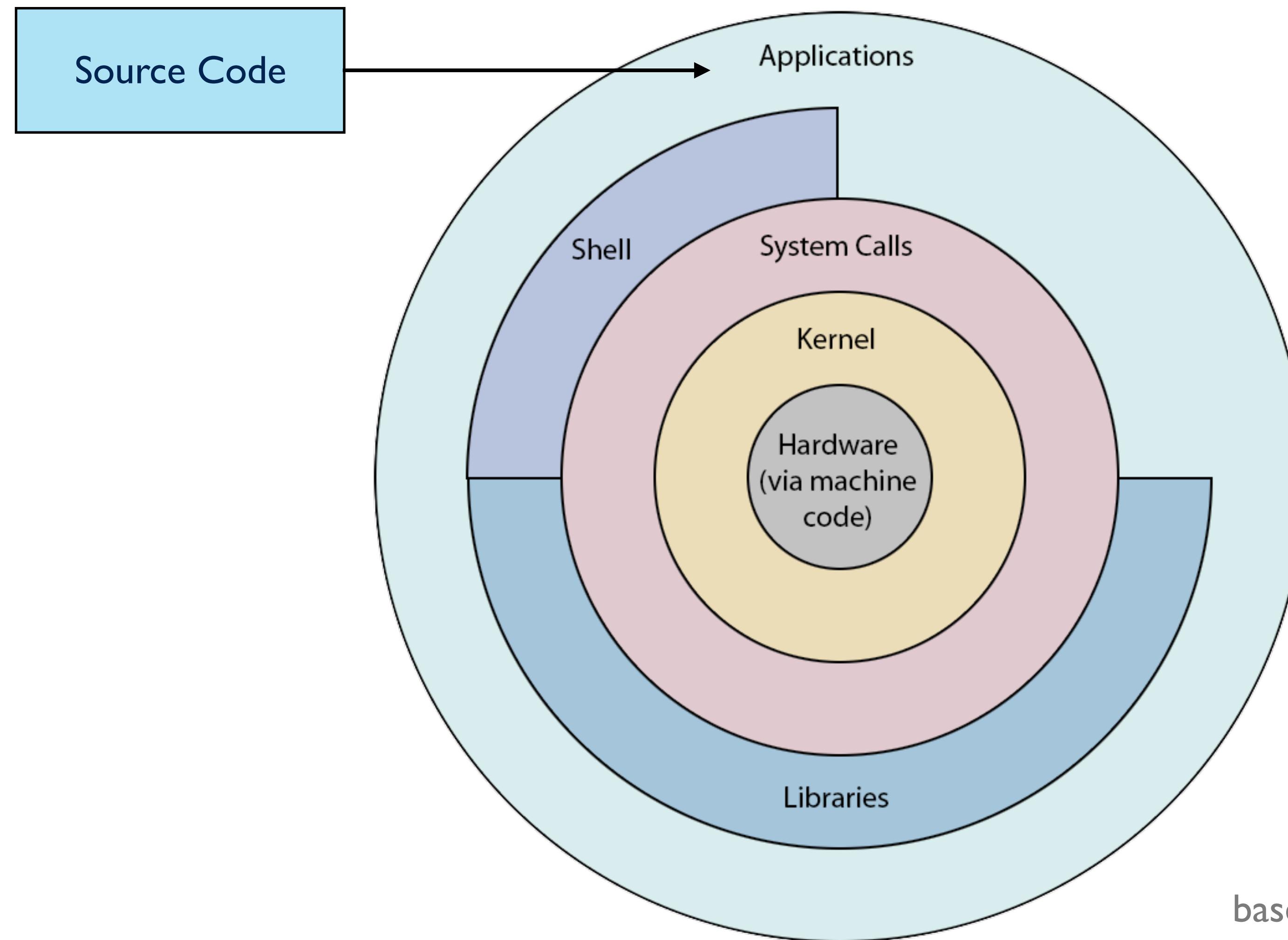


Operating Systems & System Calls





More nuanced / complex...



based on *Advanced Linux Programming*

Languages & Memory Management

- Languages are a *specification*
- Compilers generate the real instructions to alter registers
- Some languages let you instruct the compiler to attempt to alter memory (C)
- Others only provide high-level *data types*, and it is up to the compiler/interpreter to figure out what to do (JS)

```
char ch = 'c';
char t;
char *chptr = &ch;
t = *chptr;
```

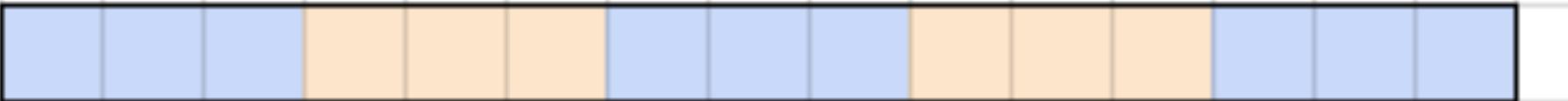
```
var ch = 'c';
var t = ch;
```

Part IV:

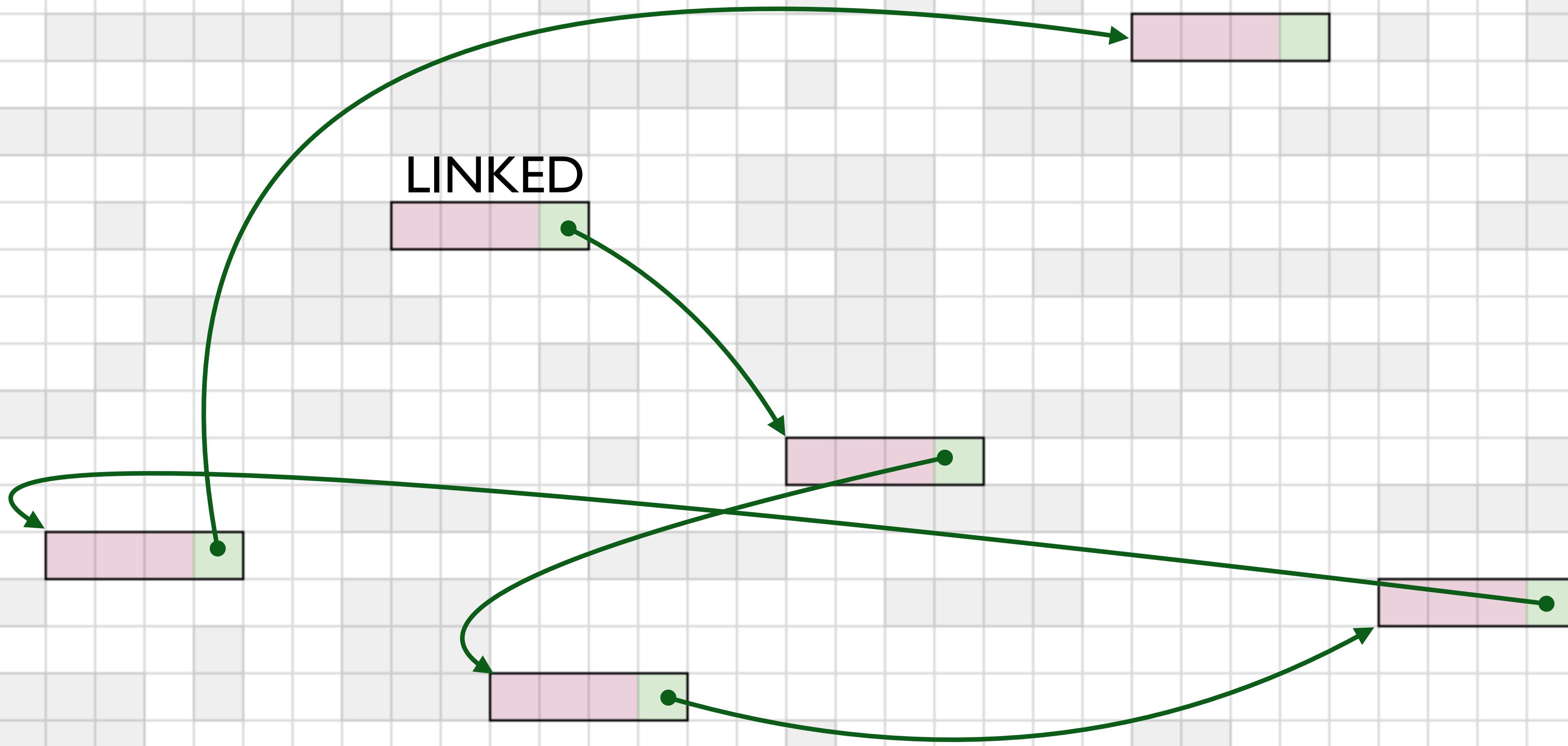
Abstract Data Types

& Data Structures

CONTIGUOUS



MEMORY





The Array Data Structure (non-JS*)

Pseudocode	Compiler/Interpreter	Memory
<code>vals = int8 Array(5)</code>	`vals` is 5 bytes at <code>0x3A6</code>	- - - X X X X X - - - -
<code>vals[0] = 9</code>	put `9` at <code>0x3A6 + 0 = 0x3A6</code>	- - - 9 X X X X - - - -
<code>vals[3] = 4</code>	put `4` at <code>0x3A6 + 3 = 0x3A9</code>	- - - 9 X X 4 X - - - -
<code>vals[2] // undef.</code>	what is at <code>0x3A6 + 2 = 0x3A8</code>	- - - 9 X X 4 X - - - -
<code>vals[3] // 4</code>	what is at <code>0x3A6 + 3 = 0x3A9</code>	- - - 9 X X 4 X - - - -

The Stack ADT

- Collection of elements
- Ordered
- Elements can repeat (not a set)
- Some example operations:
 - Make a new stack
 - Add an element to the stack ("push")
 - Retrieve an element from the list ("pop") - *must be LIFO (Last In, First Out)*
 - Check if stack is empty
 - Look at the top element without removing it ("peek")
 - Clear the stack



The Stack ADT & Array DS

Stack Feature / Operation	Array Implementation with `top`
Collection of elements	Store values at memory addresses
Ordered	Sequential addresses maintain ordering
Create new stack	Initialize a new array
Push onto stack	Insert value at `top` var (next index to use)
Pop off of stack (LIFO)	Use `top` index to return latest value
Check if stack is empty	Return whether `top` variable is 0

ADTs vs DSs

Common Abstract Data Types	(Some) Data Structures
Set	List, Linked Tree, Trie, Hash Table, etc.
List	Linked List, Array
Stack	Array, Linked List
Queue	Linked List, Deque
Map (Associative Array / Dictionary / etc.)	Hash Table, Association List, Red-Black Tree
Graph	Adjacency List, Adjacency Matrix
Tree	Linked Tree, Heap

WHAT ABOUT JS ?

Sorta-new concept: Built-In Types

- **ADT or Abstract Data Type:** describes the behavior we want
- **DS or Data Structure:** how to actually implement an ADT
- **Built-In Type:** the building blocks provided by a given language
 - language *might* specify an ADT: compiler authors decide what DS to use
 - language *might* specify a particular DS: compiler should (in theory) use it
 - or even something in between, like "the foo ADT but operation X must be constant time" (which strongly hints at a particular DS)

JavaScript Primitive (Immutable) Data Types

- **Undefined** · default for unassigned vars / nonexistent props
- **Null** · `typeof` is wrong; Null is a primitive, not "object"
- **Boolean** · could be 1 bit, but may not be *
- **String** · ES: engines use UTF-16 †
- **Number** · ES: 64-bit signed double float ‡
- **Symbol** · ES6: a unique token, can be key for objects

JS

The JavaScript Non-Primitive Data Type

○ Object

- Mutable (can change)
- Collection of *properties* – key-value pairs ("map")
- Variable assignment copies reference, not value; it "points to" the object
- Many other types are actually objects. Examples:
 - **Function**
 - **Array**
 - **Typed Array** (ES6-only)
 - **Regular Expression, Date, others**
 - Constructed primitives (**String, Number, Boolean**, etc.)





pass by value (primitives)

```
var x = 5
```

```
var y = x
```

```
x = 8
```

```
y // 5
```

⋮

```
x → 8
```

```
y → 5
```



pass by reference (Objects)

```
var x = { age: 5 }      |  
var y = x                |  
x.age = 8                |  
y.age // 8
```

x → { age: 8 }
y ↑



pass by reference (Objects)

```
var x = { age: 5 }      |  
var y = x                |  
x.age = 8                |  
y.age // 8                |  
y = {}                  |  
x.age // 8                |
```

x → { age: 8 }
y → {}

A photograph of a large crowd of people waiting in a long queue at a service counter, likely a fast-food restaurant. The queue extends from the foreground down a series of stairs. The people are diverse in age and attire, suggesting a casual setting. The building has a modern design with large glass windows and a white interior.

QUEUES & LINKED LISTS

The Queue ADT

- Like Stack, except **FIFO (First In, First Out)**
- Collection of elements
- Ordered / sequential
- Operations:
 - Enqueue (add)
 - Dequeue (remove)
 - Peek
 - Clear
 - IsEmpty... etc.



The Linked List DS

- Data structure used for *list, stack, queue, deque* ADTs etc.
- Uses **nodes** which encapsulate a **value** and pointer(s)
- Main entity holds reference(s) to just a head and/or tail node
 - the "**handle(s)**"
- Each node then *points to the next and/or previous node*
 - "**singly-linked**" (unidirectional) vs. "**doubly-linked**" (bidirectional)



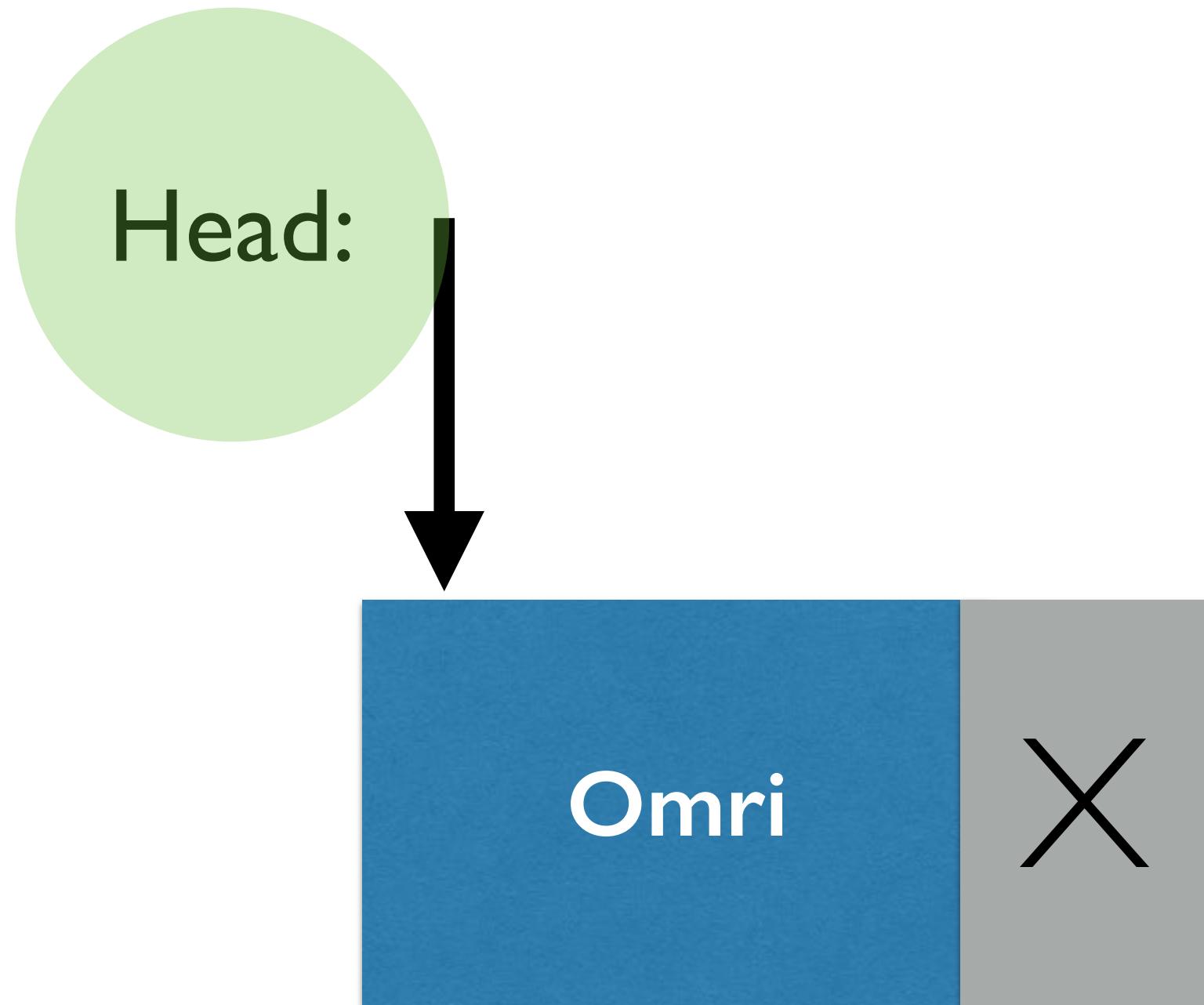


Linked List

Head:



Linked List



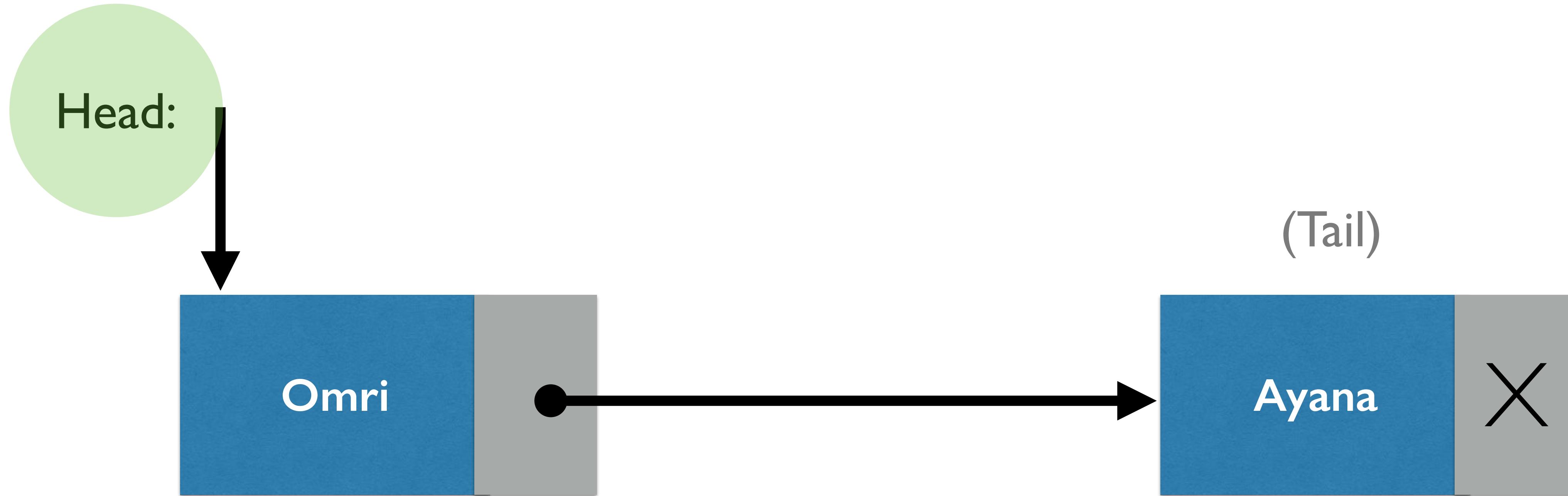


Linked List



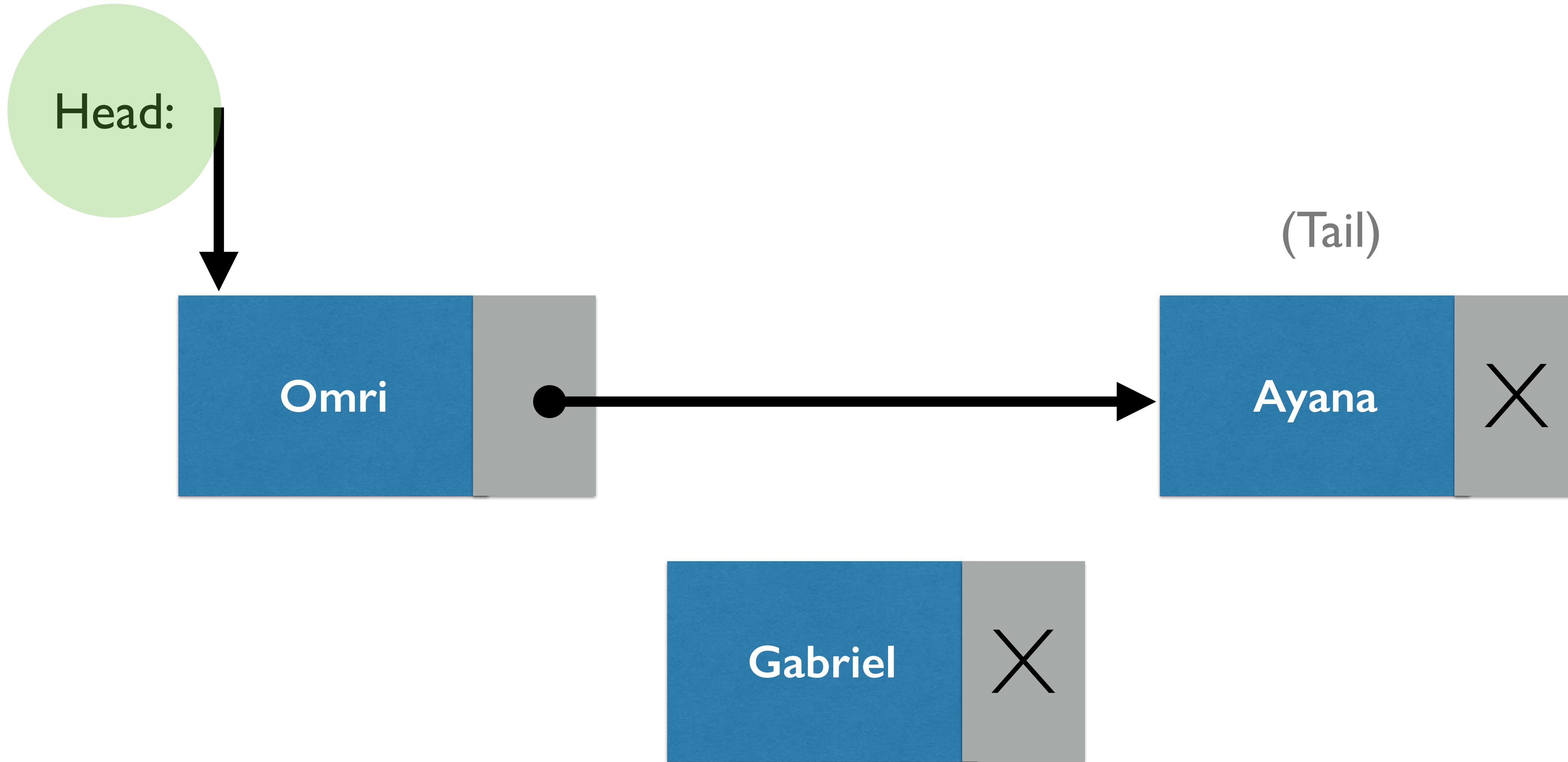


Linked List



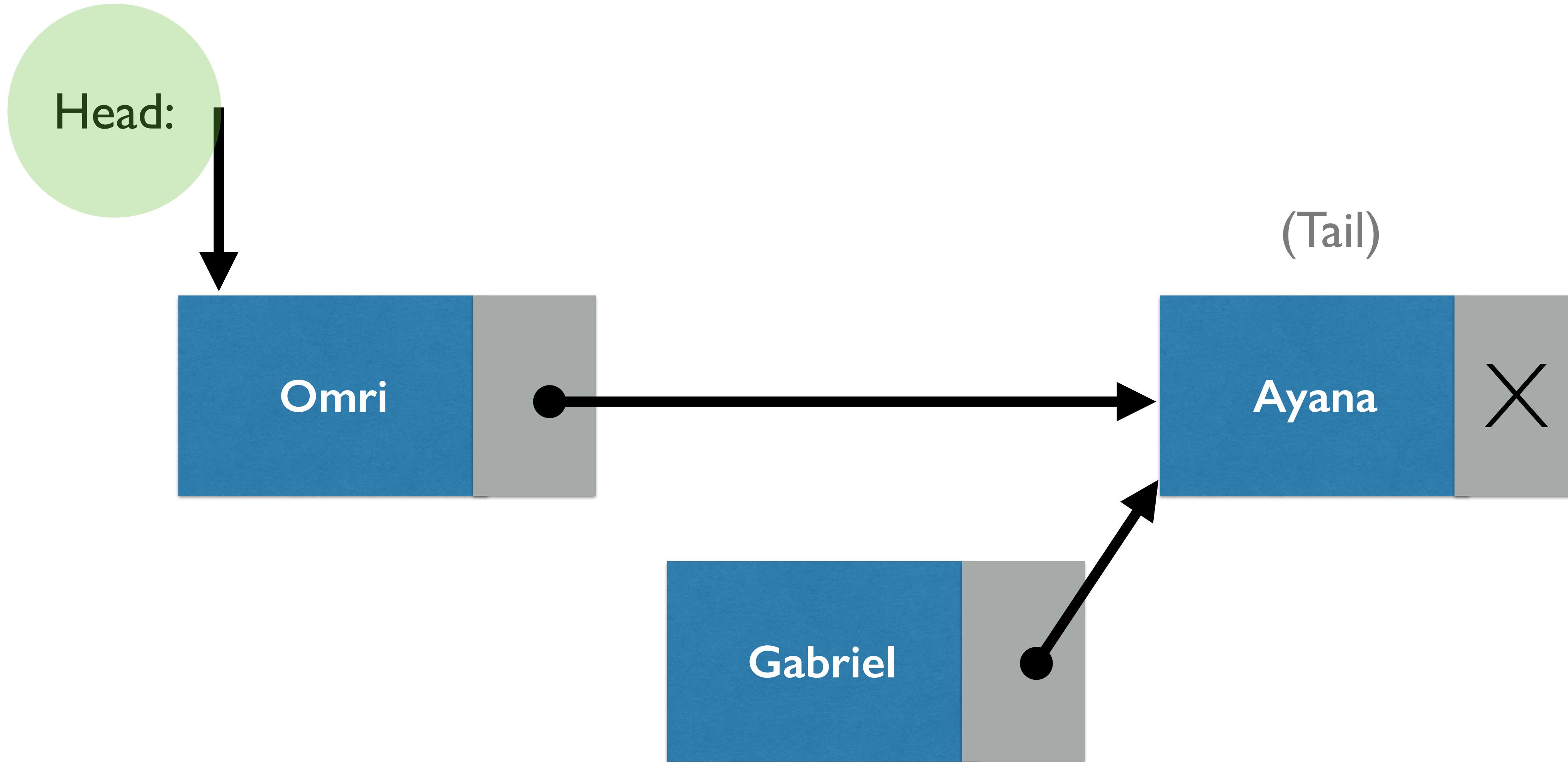


Linked List



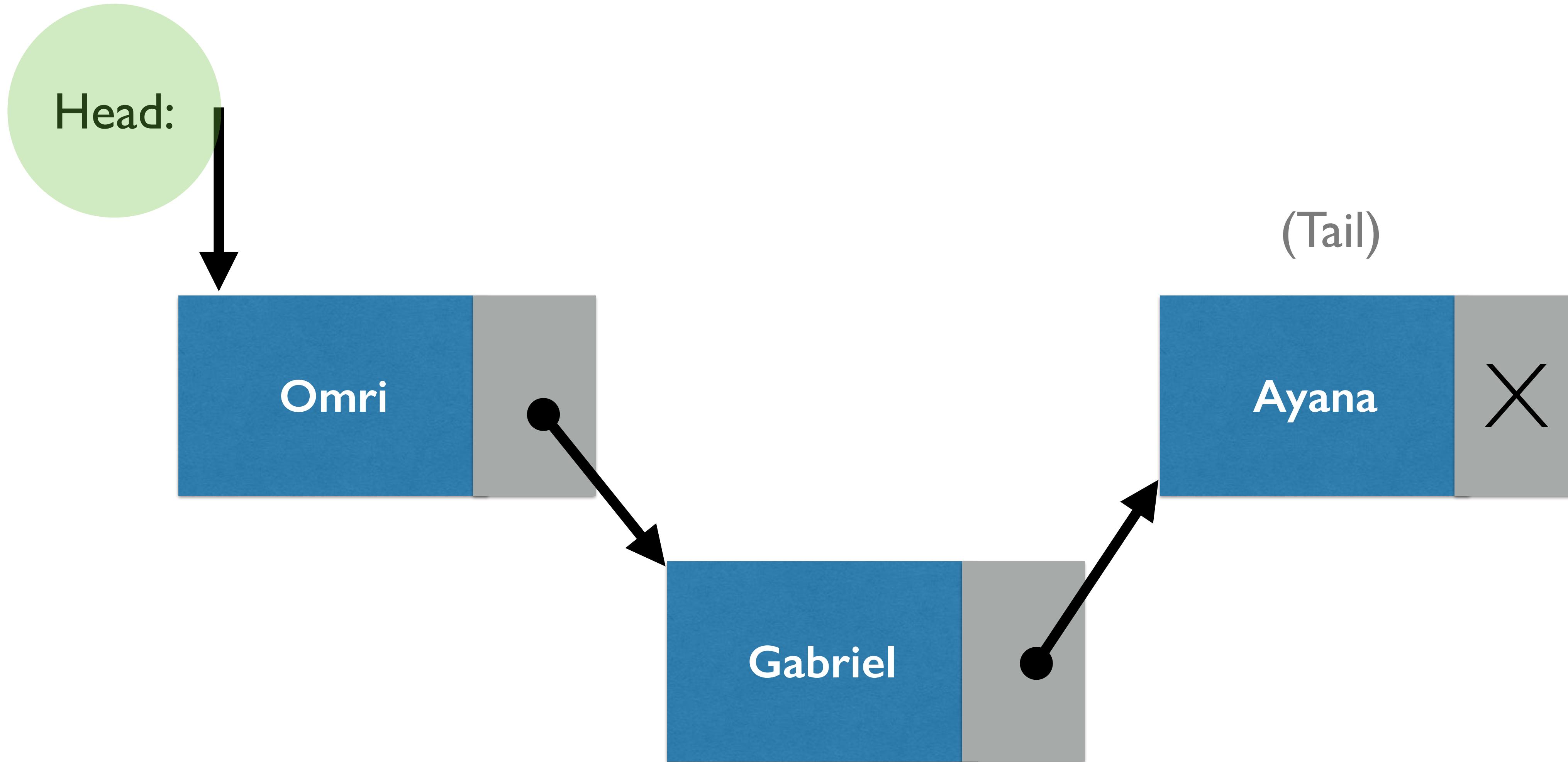


Linked List



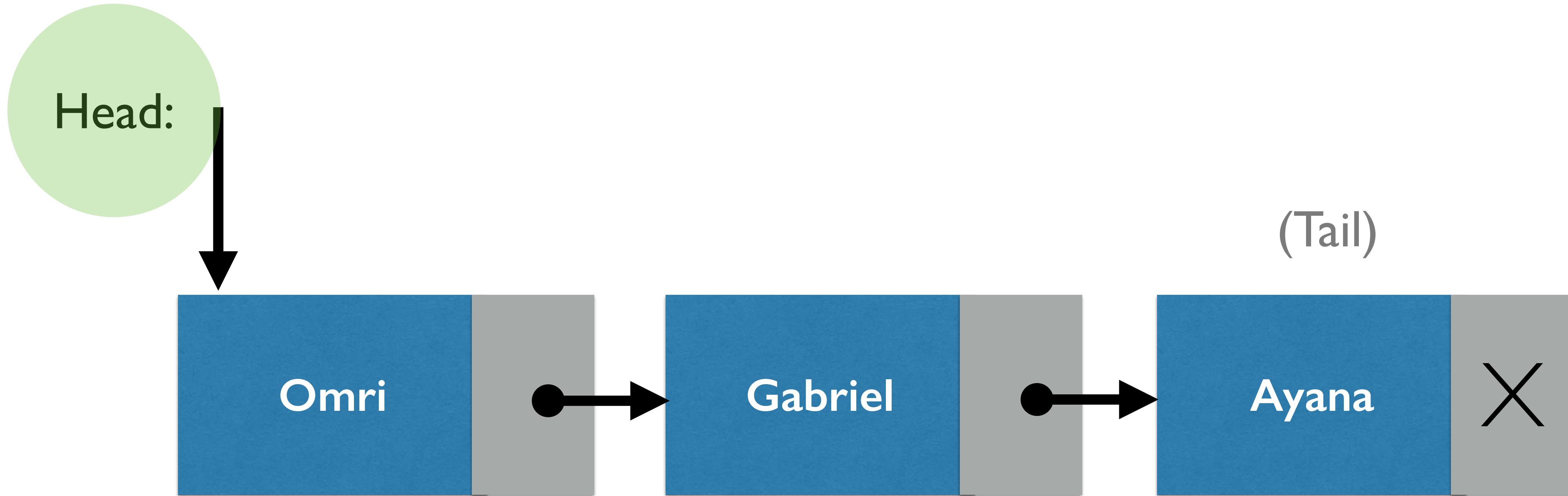


Linked List



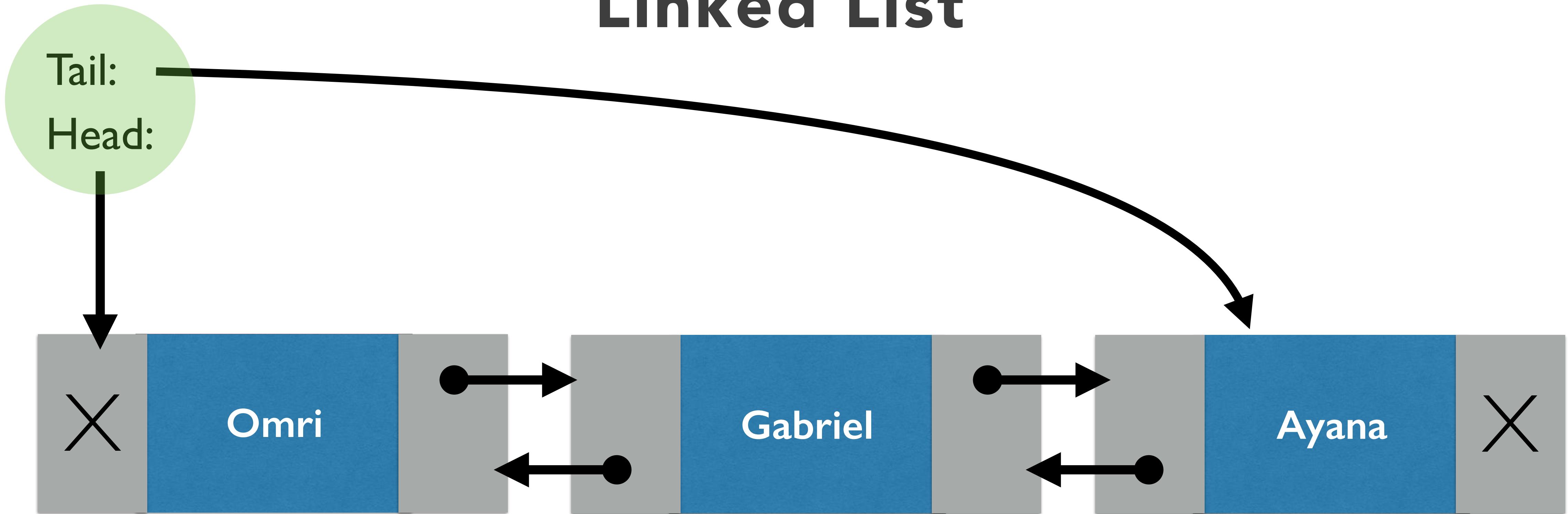


Linked List





Linked List





(some) pros/cons: Linked Lists vs Arrays

Operation	Linked List	Typed Array
Reach element in middle	Must crawl though nodes	Constant time
Insert in middle or start	Constant time (if we have ref). With handle, constant time	Must move all following elements
Add element to end	With handle, constant time	Constant time
Space per element	Container + element + pointer(s)	Just element!
Total space	Grows as needed	Pre-reserved & limited*
Physical locality	Not likely	Best possible

WORKSHOP

