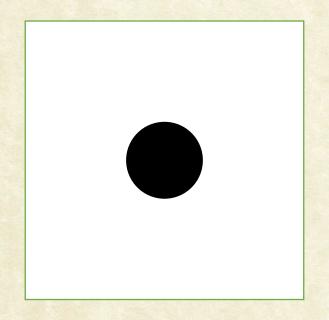
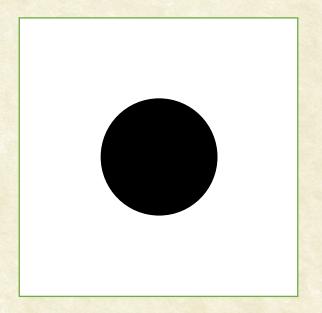




Monsoon 2023: Morphological Image Processing 2

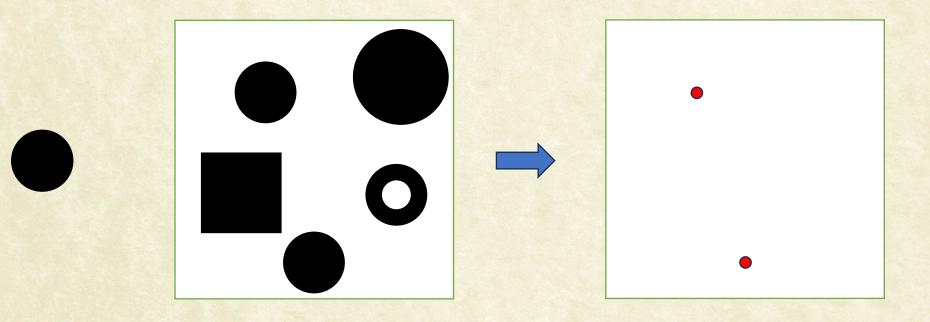








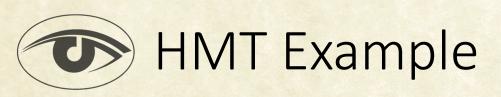
Monsoon 2023: Hit or Miss Transform (HMT)



HMT: Finding Exact Matches

- · Goal:
 - Detect objects of a particular shape in the image (exact matches)
- · Approach:
 - Find locations in the image where:
 - 1. The shape (B_1) fits inside the foreground
 - 2. The boundary of the shape (B_2) fits in the background
 - Take the intersection of the two to find object locations
- Definition:

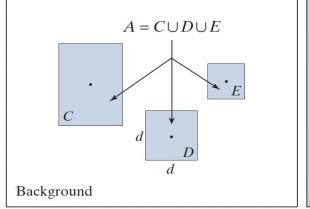
$$I \circledast B_{1,2} = \{z | (B_1)_z \subseteq A \ and (B_2)_z \subseteq A^c \}$$
$$= (A \ominus B_1) \cap (A^c \ominus B_2)$$

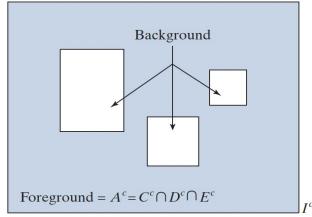


Row1: Original Image and its complement

Row 2:

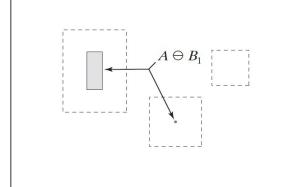
- The structuring elements
- Hits with B₁.
- Row 3:
 - Hits with B₂.
 - Intersection of the hits

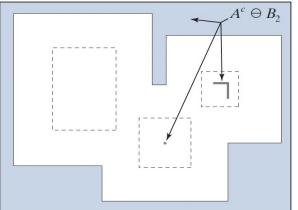




Image, I

pixels





 B_2

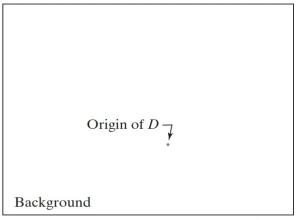
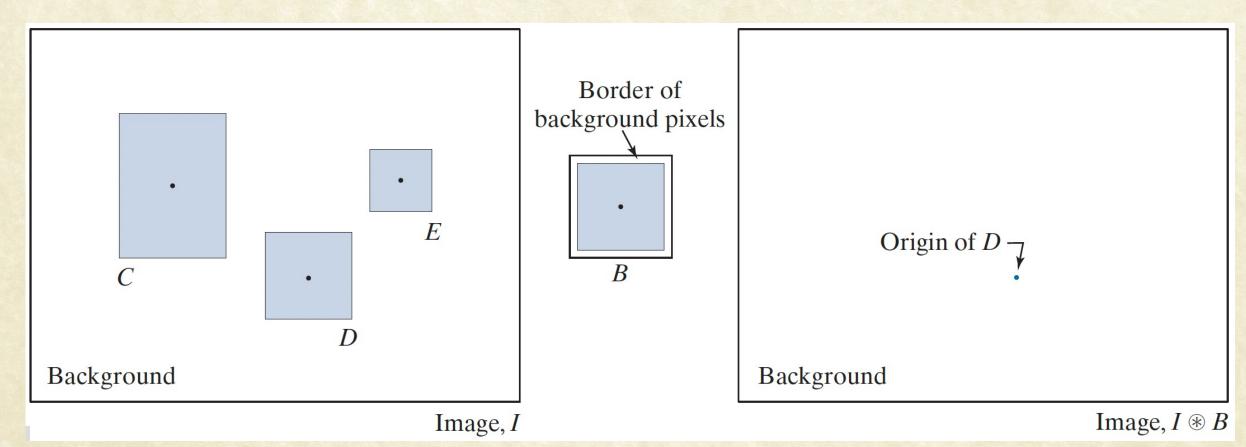


Image: $I \circledast B_{1,2} = A \ominus B_1 \cap A^c \ominus B_2$



HMT with single structuring element



We match backgrounds as well

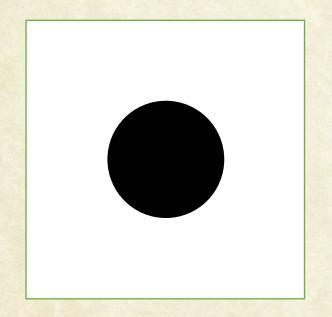


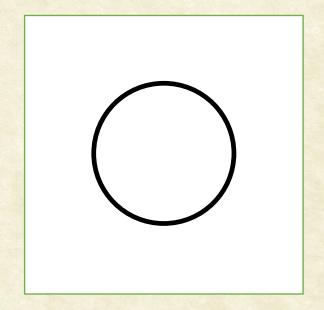
Questions?





Monsoon 2023: Boundary Detection

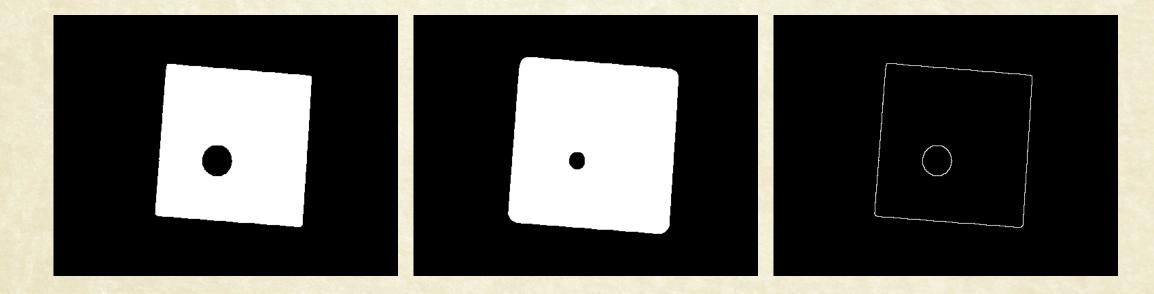






Boundary Detection

- 1. Dilate input image
- 2. Subtract input image from dilated image
- 3. Boundaries remain!





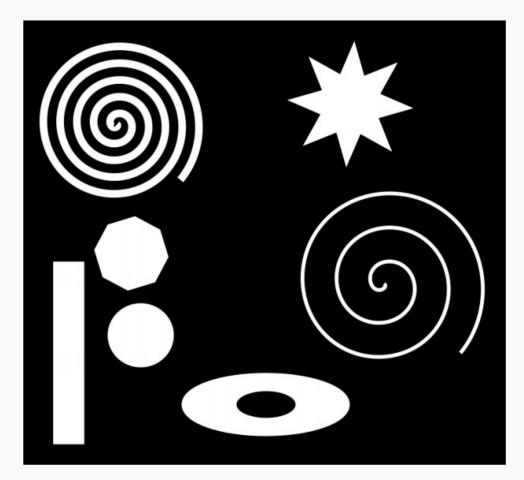
Can use erosion also ..



Fig 3: (a) Original Image (linkon.tif) (B) After erosion operation (C) Boundary Extraction with the help of Erosion.



Boundary Detection: Effect of STREL



1	1	1
1	1	1
1	1	1



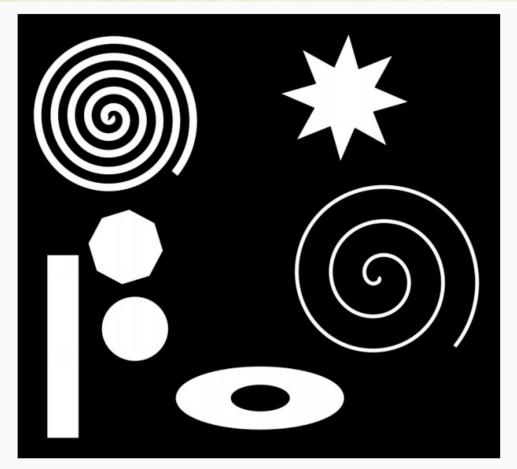
(a) f

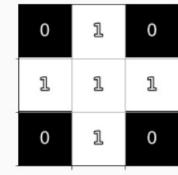
(b) s

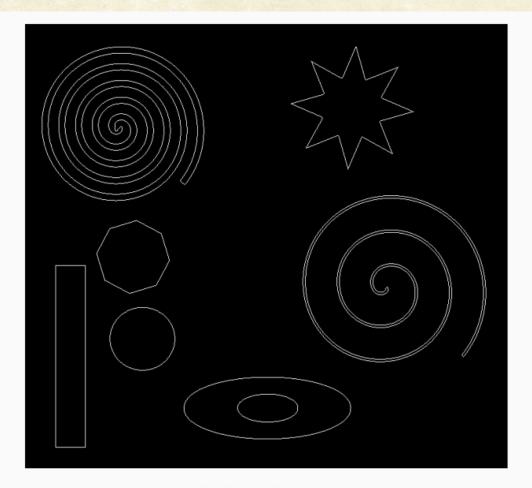
(c) $f-(f\ominus s)$



Boundary Detection: Effect of STREL







(a) f

(b) s

(c) $f-(f\ominus s)$

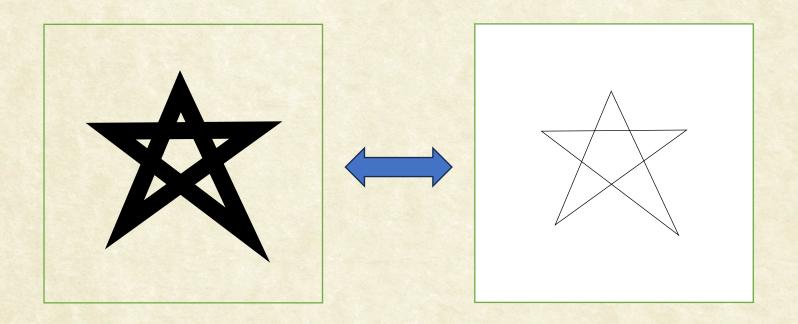


Questions?





Monsoon 2023: Thinning and Thickening





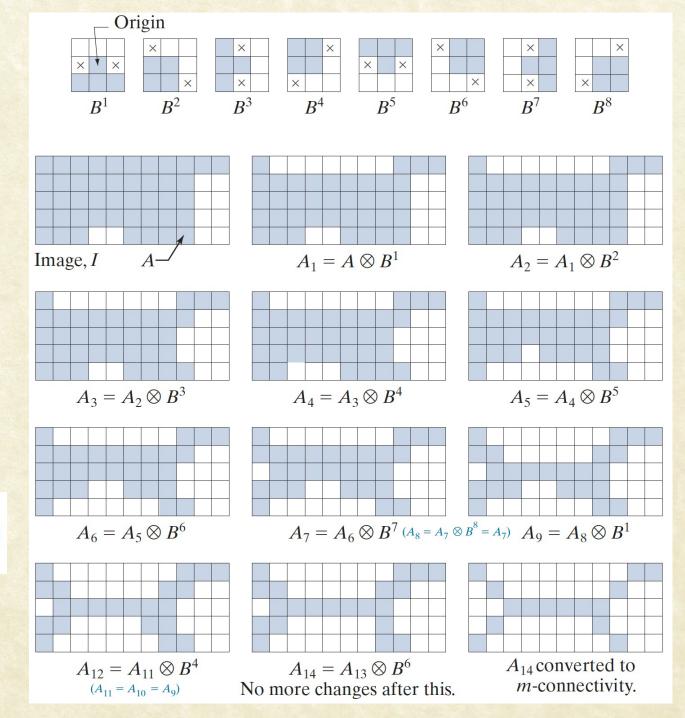
• In terms of HMT:

$$A \otimes B = A - (A \circledast B)$$
$$= A \cap (A \circledast B)^{c}$$

 Repeat with a set of specific structuring elements

$$A \otimes \{B\} = \left(\left(\dots \left(\left(A \otimes B^1 \right) \otimes B^2 \right) \dots \right) \otimes B^n \right)$$

until no more changes

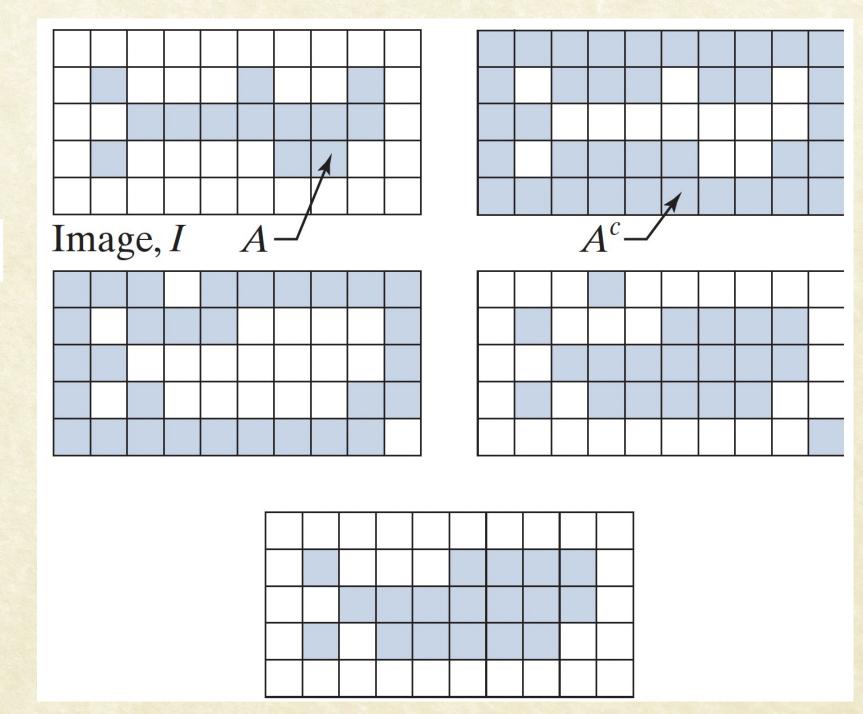




Thickening

Dual of Thinning

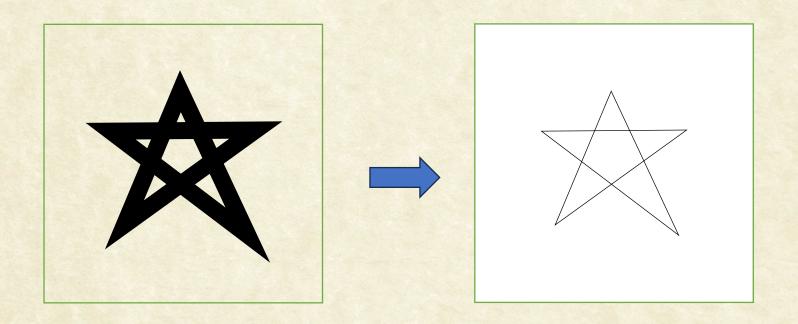
$$A \odot B = A \cup (A \circledast B)$$





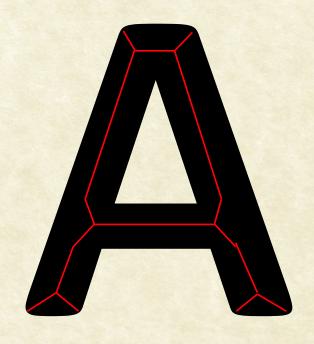


Monsoon 2023: Skeletonization





- The skeleton of a shape is defined as the set of all points in the shape that are equidistant from the two nearest boundary points.
 - Burning the boundary
- The skeleton of a shape is the locus of the center of maximum disks of the shape





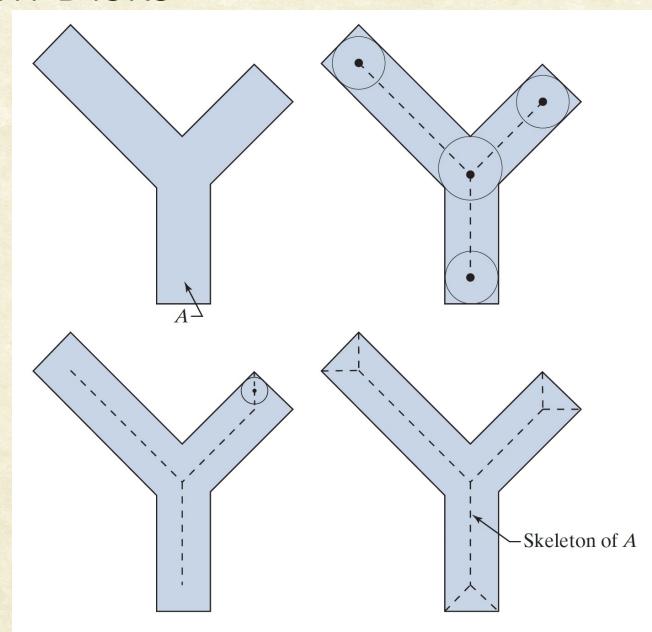
Skeleton as Maximum Disks

Maximum Disks

- A disc d that fits in A, such that no larger disk exists that fits inside A and contains d.
- A maximum disk will touch the boundary of A at two or more points
- Definition:

$$S(A) = \bigcup_{k=0}^{K} S_k(A)$$

$$S_k(A) = (A \ominus kB) - (A \ominus kB) \circ B$$





Other Morphological Algorithms

- Hole Filling
- Connected Component Extraction
- Convex Hull



Questions?