

Experiment 5

Fun with RNNs

实验题目：在这次作业中，我们使用Shakespeare数据集来扩展 `min-char-rnn.py`

实验目标和学习任务：

- 实现RNN前向计算
- 实现RNN的反向传播
- 实现softmax激活函数+ 基于 `tempreature` 的模拟退火算法
- 解释参数

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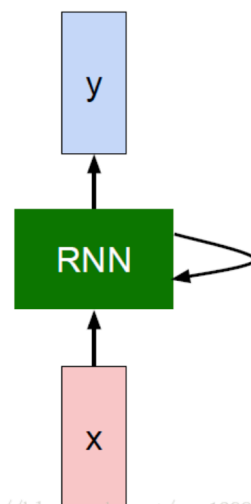
Part 1

RNN前向计算原理

We can process a sequence of vectors \mathbf{x} by applying a **recurrence formula** at every time step:

$$\boxed{h_t} = \boxed{f_W}(\boxed{h_{t-1}}, \boxed{x_t})$$

new state some function with parameters W old state input vector at some time step



<https://blog.csdn.net/sun1398>

并且我们定义输入是一个one-hot向量代表一个词的表示 $x \in R^{vocabsize \times 1}$

$$z = W_{xh} * X_t + W_{hh} * h_{t-1} + b_h \quad (1)$$

$$h_t = \tanh(z) \quad (2)$$

$$y_t = W_{hy} * h_t + b_y \quad (3)$$

$$p_t = \frac{e^{y_t - \max(y_t)}}{\sum_i^{inputsize} e^{y_t^i - \max(y_t)}} \quad (4)$$

上面就是整个前项计算的过程，最终使用的 softmax 进行输出 target。

我们使用实验提供的权重参数文件 `char-rnn-snapshot.npz` ,以 `'shakespeare_train.txt'` 作为整体模型的数据输入

根据上述公式，从模型中采样一个整数序列，使用不同的alpha值来检验模拟退火算法（simulated annealing algorithm）的效果

`sample` 函数的代码展示如下，我们在temp函数中调用

```
def sample(h, seed_ix, n, alpha):
    """
    sample a sequence of integers from the model
    h is memory state, seed_ix is seed letter for first time step
    """

    # Start Your code
    x = np.zeros((vocab_size, 1)) # init input vector with zero of size vocab_size
    x[seed_ix] = 1
    ixes = []
    for t in range(n):
        h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
        y = np.dot(Why, h) + by
        p = np.exp(alpha * y) / np.sum(np.exp(alpha * y))

        ix = np.random.choice(range(vocab_size), p=p.ravel())
        x = np.zeros((vocab_size, 1))
        x[ix] = 1
        ixes.append(ix)
    return ixes
    # End your code
```

不同alpha值的最终文本生成的效果：

`temp(length=200, alpha=1)`

irst Senath the the the the the the the the the the come the the con the the so
have the come the the with the the the the the the the the see the the the the the t
he the shall the the the the the

`temp(length=200, alpha=5)`

irnave prees shall but he one-the not out-iber gothar pray hose's will thou fan to i

```
n so
A bue uncityer!
Thou to deqheor it;
Noth camt sees, whes.
```

```
First Sengee make ving-poldidst seans poon she wisg
```

```
temp(length=200, alpha=0.1)
```

```
ipm??V?AYpD,sgem',?WHYLRy-j;b.
mnN;-
Rm L&&ABeVuEYnnMI: pqmra, &nD!zD!AyOTqCp't::'rpDI
h;:&MEemNy.'Hrw,,
waBC'sg&f.pu
jro'
b IslEtfxub.
KD'SPyY,utgGlVutf.sleksfuWBrcd C,;rttkelDu;h!Z
uQOiMi fo.Ochhq,.ML
```

Part2

我们 `Loss` 使用 `交叉熵 loss`，定义如下:

$$Loss = y_t^{real} * \log(P_t) \quad (5)$$

RNN反向传播原理

RNN反向传播要考虑到上一次的隐状态输出 h_{t-1}

重要的公式推导:

$$\frac{dLoss}{dy_t^i} = p_t^i, if \quad i \neq target \quad (6)$$

$$\frac{dLoss}{dy_t^i} = p_t^i - 1, if \quad i = target \quad (7)$$

$$\frac{dy_t}{dW_{hy}} = h_t \quad (8)$$

$$\frac{dy_t}{db_y} = 1 \quad (9)$$

$$\frac{dLoss}{dh_t} = \frac{dLoss}{dy_t} \frac{dy_t}{dh_t} + \frac{dh_{t+1}}{dh_t} = W_{hy}^T * dy + dh_{t+1} \quad (10)$$

hs[t]是t时刻的hidden state，我们将本时刻输入层+上一时刻的隐藏层作为参数传入tanh函数

```
# encode inputs to 1-hot embedding, size(xs)=(len(input), vocab_size)
xs[t] = np.zeros((vocab_size, 1)) # # encode in 1-of-k representation 1-hot-encoding
xs[t][inputs[t]] = 1
hs[t] = np.tanh(np.dot(Wxh, xs[t]) + np.dot(Whh, hs[t-1]) + bh) # hidden state
ys[t] = np.dot(Why, hs[t]) + by # unnormalized log probabilities for next chars
```

```
#softmax(ys)
ps[t] = np.exp(ys[t] - np.max(ys[t]))/np.sum(np.exp(ys[t] - np.max(ys[t]))) #your code# # probabilities for next chars
```

我们如公式所叙进行loss计算：

```
#计算loss = cross_entropy ()
loss += - np.log(ps[t][targets[t]]) #your code# # softmax (cross-entropy loss)
```

dy 是 softmax层 求导, cross_entropy softmax 求导 $a_j - y_i, y_i$ 为 one-hot 标签, a_j 为 softmax 之后第 j 个神经元输出

```
dy = ps[t] #your code#
dy[targets[t]] -= 1 #your code# # backprop into y.
#反向传播, 求Why与by的导数
dWhy += dy.dot(hs[t].T) #your code#
dby += dy #your code#
```

反向传播到 hidden state

(其中 dh 处反向传播的 梯度外需加上 dhnext):

```
dh = Why.T.dot(dy) + dhnext #your code# # backprop into h
dhraw = dh * (1 - hs[t]**2) #your code# # backprop through tanh nonlinearity
dbh += dhraw #your code#
dWxh += dhraw .dot(xs[t].T) #your code#
dWhh += dhraw .dot(hs[t-1].T) #your code#
dhnext = Whh.dot(dhraw) #your code#
```

生成：

我们使用comp(m, n)函数，从Shakespeare文本文件中的一个随机位置开始，使用一个长度为m的上下文字符串，并生成一个长度为n的字符串来完成上下文字符串。

这里有一些有趣的例子，当我们有不同长度为m的输入上下文字符串时。我们也改变延续的长度n。

sample1 : comp(780, 200)

Context:

se to market:

Clarence still breathes; Edward still lives and reigns:
When they are gone, then must I count my gains.

LADY ANNE:

Set down, set down your honourable load,
If honour may be shrouded in a hearse,
Whilst I awhile obsequiously lament
The untimely fall of virtuous Lancaster.
Poor key-cold figure of a holy king!
Pale ashes of the house of Lancaster!
Thou bloodless remnant of that royal blood!
Be it lawful that I invoke thy ghost,
To hear the lamentations of Poor Anne,
Wife to thy Edward, to thy slaughter'd son,
Stabb'd by the selfsame hand that made these wounds!
Lo, in these windows that let forth thy life,
I pour the helpless balm of my poor eyes.
Cursed be the hand that made these fatal holes!
Cursed be the heart that had the heart to do it!
Cursed the blo

Continuation:

tTiittllee hhaasstt uulltteedd pprroo''ss bbeeaatteenn oo'' tthhyy mmee tthh
ee ddeeiinngg ooff ccaann aass rraaccll''dd.. CCiittiiggeess nnoott nnoott
aa ssuucchh soonn yyoouurr kknnoowss
TToo pprree lleett aa ccaauueess llibby nnoott tthhaann CCeerrlee
AAnnweerr,, nnoo,, tthhiiss aass lleewwooull II''llll::
SSiivvee ffuuee
AAnndd wwiitth yyoouu
II

sample2 : `comp(50,500)`

Context:

ith all my heart.

PRINCE EDWARD:

A beggar, brother

Continuation:

..

VVOOLLUUMNNIIAA::

II ttuussttiinneenn..

VVOOLLUUMMNIIAA::
NNaayy??
VVOOLLUUMMNIIAA::
EEnccuussstt uuss
AAssffoouugghhtt::
AAnndd hhaadd,, mmoommoo aanndd yyouurr ppaannsseerr tthheeaarr..
VVOOLLUUMMNIIAA::
WWhaattinngg ddiidd yyoouu mmee ssiivvee ssaattcchh tthheeaann!!tt CChheeyy
ttiidd??
II hhiimm knnaavvee wwhaatt
TThheennaammpp
II'' aallll bbleepp::
MMy sshhouulldd wwghy cchhaass ggoo..
BBRUUTTUUSS::
TThee tthee tthee aannccoouutt--bbuullee
MMy mmy II ccaainngg ppaayy Clleesstthhy,,
Llooy,, wee ccaaddnnicce
nnoopp
TTuulloovvy,,
II wwiillll lliillll..
SSTThee cceeyy!! AAnnvvee sshhaarrkk II ddeeaarrss!!
WWheerree oorr nnoo;; tthee uunnddiitthh wwaass,, pprreeaanntt aa ccaann
ppooottss ddoonnggee,,
AAnndd yyouurr nnoobblee,, iiss ppoorree yyoouu wwaayyss tthhiissgg--hhooss
ee hhiimm wee ddaarrtt hheeaarr:: bboonddss weeaaccooppaann eeaarr ss

sample3 :

Context:

bov

Continuation:

eedd

TThheeaakkaabbaacceess ssou!! ffoorr weellll:: yyoouu tthee ppeeaarrdd!! tt
oo hhaavvee tthhaatt ssou wwiitthh ssuucchh..

BBRUUTTUUSS::

II hhaavvee ooff aanndd ffaauurr bbee ccoouulldd yyoouu yyoouulldd..

LLAARREECCIINNIIUUSS::

HHee wwoorrggtt..

HHee ccoorrrraamm::

MMe aann rreeweerree bbrreeddee tthhiiss mmiinngg,,

AAnndd ppeeaakkiirrss hheelloo::

WWhhoomm..

SSIICCIINNIIUUSS::

OOvveess wwiillll hheeaarr,, II''llll iiff,, II pprraarree vveennttaaiinniicc
ee ffoorr unneess,,

OOnee hhiiss inn hhiinngg bbeelliiuss hhee too ttaakkee

tthhee ccoonnsssttiuuuss..
VVOOLLUUMMNN EELLIIZZAAIIEESS::
PPaarrsseedd!,,
TThhaann ppooot oonn hhee hhee kkoo II tthhee RRoommee;; ooff yyoouu ss
hhaallllss.. TToollccyy..
CCOORRIIOOLLAANNUUSS::
BBllaabbeeinn::
CCaattww ttiillll ttoo hhaavvee bbeeeennieess ddeeaaddee ggeeaarrffoorr::
SSoo hheaattiilldd
TThhee ooff tthhee ttrruueess II nnooppaa

sample 4: comp(300,300)

Context:

on, upon your approbation.

CORIO LANUS:

Where? at the senate-house?

SICINIUS:

There, Coriolanus.

CORIO LANUS:

May I change these garments?

SICINIUS:

You may, sir.

CORIO LANUS:

That I'll straight do; and, knowing myself again,

Repair to the senate-house.

MENENIUS:

I'll keep you company. Will you al

Continuation:

aaddoo bbrraarrggee vveerrssllyy hhee bbrllee cchhiilldd RRoommee ccoon''tt

SSoorrttyy ffoorr ggoofft ssoommeess::
Llee hhee bbee mmiisshh sseeaavll een,, mmaarree bbee tthhee MMuurrddee??

CCAAUUMMNNIIHH::
NNoo hhaallllliccee.. FFouurr ssoon,, ssoouucciizzeenn::
WWheemmbboorr wwiillll ffaatt,,
TThheeaanngg hhaavvee!!
MMEENNEENNIIUUSS::
aaiivveess tthhoouggghh
TThhaatt mmyy aa tooougghht hhooww plleeaatthh sseeess bbee sshhaallooo
dd mmaayy doonnggeenntthheesseenn aa ppraarree hhee lloorrd ttoo ffoorr,,
wwhiicchh iiss

sample 5: comp(100,500)

Context:

in sunder, that my pent heart
May have some scope to beat, or else I swoon
With this dead-killing new

Continuation:

aanntt aatt mmiissee llllaadd ssttaatt,,
TThheeo,,
II ddaavvee II wwiilllll wweeaarr mmuunn
DDllyy ffiillkk ddiiddee,, mme''ss hh
MMEENNEENNIINNIIZZAANNGGIIRRIIOOUUSS::
CCaallll''tthheess ttiimmee mme,, ssggeeee uudd iitt wwiilllll ooff wwahaatt
lleevveess tthhee hhee hhiiss tthhee ssttoollaann::
MMoorrk,, mmuusstt hhaadd iiss yye aanndd aanndd hhaaggcchh CCuull ccoomm
rroodd hhiiss CCoorriiigglee wweellll,,
AACCiissss!!
VVIIRGGIILLIIAA::
PPaattuullee oonnee sshhee,, CCaannoouurr tthhy ooff ppeeaatthh iitthss tt
hee iiss tthhee tthhee ccaamnee yyouurr llooookkdd
II''
SShaallldd eenppaabbeemm,, wwahaatt,,
,, BBuiinnppoossttee..
SSIICCIINNIIUUSS::
TTrruueenn noott tthhoou,, bbee iitt lloovviecee
ssttree tthhaatt II sseeebbeess aalllll ooff cchhiillee,, wweellll,,
Ooff tthhee aanndd mmiinngg oonn ccoon''tt..
'ss aass wwahaatt yyouu!!
FFoorr aanndd hhaaffcchhiitteess

以下是comp函数的部分内容：

我们从 `shakespeare_train.txt` 中随机采样文本
并存储hidden value


```

for t in range(m):

    # Start Your code
    h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
    # x is one of k encoding of which index is 1 in the char
    x = np.zeros((vocab_size, 1))
    ix = inputs[word_index + 1]
    word_index += 1
    x[ix] = 1
    ixes.append(ix)
    # End your code

```

计算softmax概率，从样本中采样，使用输出作为下一阶段输入：

```

# Start Your code
y = np.dot(Why, h) + by
p = np.exp(y) / np.sum(np.exp(y))
ix = np.random.choice(range(vocab_size), p=p.ravel())
x = np.zeros((vocab_size, 1))
x[ix] = 1
# End your code

```

计算最终的输出结果：

```

# Start Your code
h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
y = np.dot(Why, h) + by
p = np.exp(y) / np.sum(np.exp(y))
ix = np.random.choice(range(vocab_size), p=p.ravel())
x = np.zeros((vocab_size, 1))
x[ix] = 1
ixes.append(ix)
# End your code

```

Part3

char-rnn-snapshot.npz 是训练后的RNN权重

sample.txt 是从RNN中按照不同的 temperature 采样得到的

任务：在RNN生成的样本中，在冒号后面通常会有一个换行符或空格(即冒号)。“:”)字符。在

提供的权重数据中，确定RNN负责这种行为的具体权重。

结论： $W_{xh}[100][9]$, $W_{hy}[0][100]$, $W_{hy}[2][100]$ 是对于行为最重要的具体权重

当字符“:”作为 one-of-K 编码传递进来时，其中输入x中的第9项为1, W_{xh} 的第9列 $W_{xh}[:, 9]$ 被选出。

然后，我们发现hidden单元h的第100个单位是最活跃的，值是0.9999，非常大。注意，h是一个tanh单位，渐近于1。这使得 W_{hh} 和之前的隐藏状态不重要。[9]是造成h[100]非常大的主要原因。

在输出阶段，隐藏单位乘以矩阵 W_{hy} 。结果是 $y[0]$ (换行字符) 和 $y[2]$ (空格字符) 具有较大的值。这是由于当隐藏单元在第100个位置激活时(即输入为“:”)，为什么在 $W_{hy}[:, 100]$ 栏中[0][100]和[2][100]值最大。

较大的 $y[0]$ 和 $y[2]$ 使得在 softmax 函数将输出向量转化为概率向量后，换行字符和空格字符很可能被采样。

这就是为什么换行符和空格符总是跟在冒号后面的原因

结论和分析：

1. RNN 是自然语言处理中的基本神经网络框架，现在的很多问题都是基于这样一个框架完成的。
2. 不同于计算机视觉中 CNN 框架的是：RNN 中拥有非常多的变种神经元，并且需要考虑时序按照 BPTT 展开。
3. RNN 中不像 CNN，RNN 会丢失很多输入中的信息。