

## 1) Magnetic field straight current

The magnitude of the magnetic field in distance  $r$  of a long straight wire with current  $I$  is

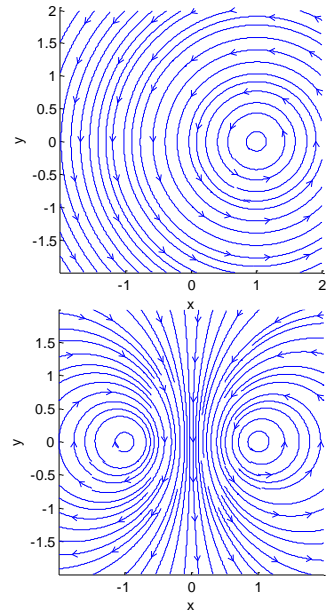
$$H = \frac{I}{2\pi r}$$

The field direction can be described with a vector

$$\begin{pmatrix} H_x \\ H_y \end{pmatrix} = \frac{I}{2\pi r^2} \begin{pmatrix} -y \\ x \end{pmatrix}$$

a) Use `streamslice()` to plot the field lines in the  $xy$ -plane, if the current intersects the  $xy$ -plane at the point  $P$  ( $x=1$ ,  $y=0$ ).

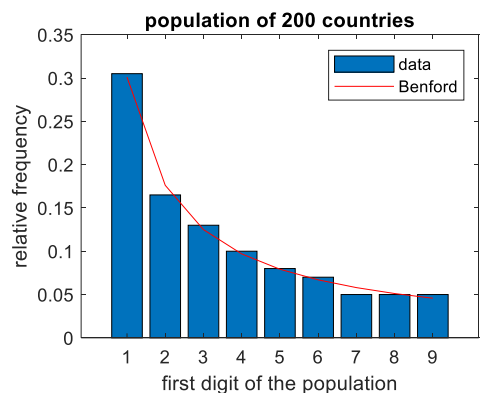
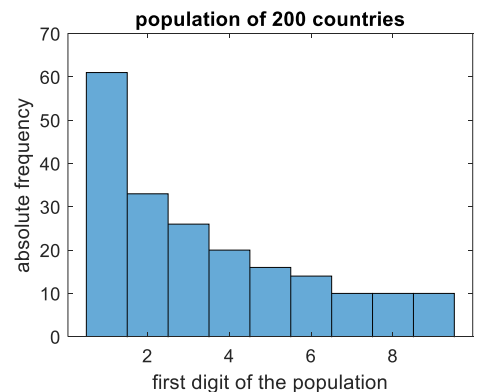
b) Superimpose the magnetic fields of two conductors at points  $P_1$  ( $x_1=1$ ,  $y_1=0$ ) and  $P_2$  ( $x_2=-1$ ,  $y_2=0$ ) whose currents are antiparallel.



## Aufgabe 2: Benford's law

[https://de.wikipedia.org/wiki/Benford'sches\\_Gesetz](https://de.wikipedia.org/wiki/Benford'sches_Gesetz)

- Read in the data set `hw04_population.xlsx`. Column 3 contains the population of the 200 largest countries in the world. Create a histogram of the first digit of the population data.
- Compare the relative frequency of the digits with Benford's analytical formula  
 $p(d) = \log_{10}(1+1/x)$



[Application](#) (in German)

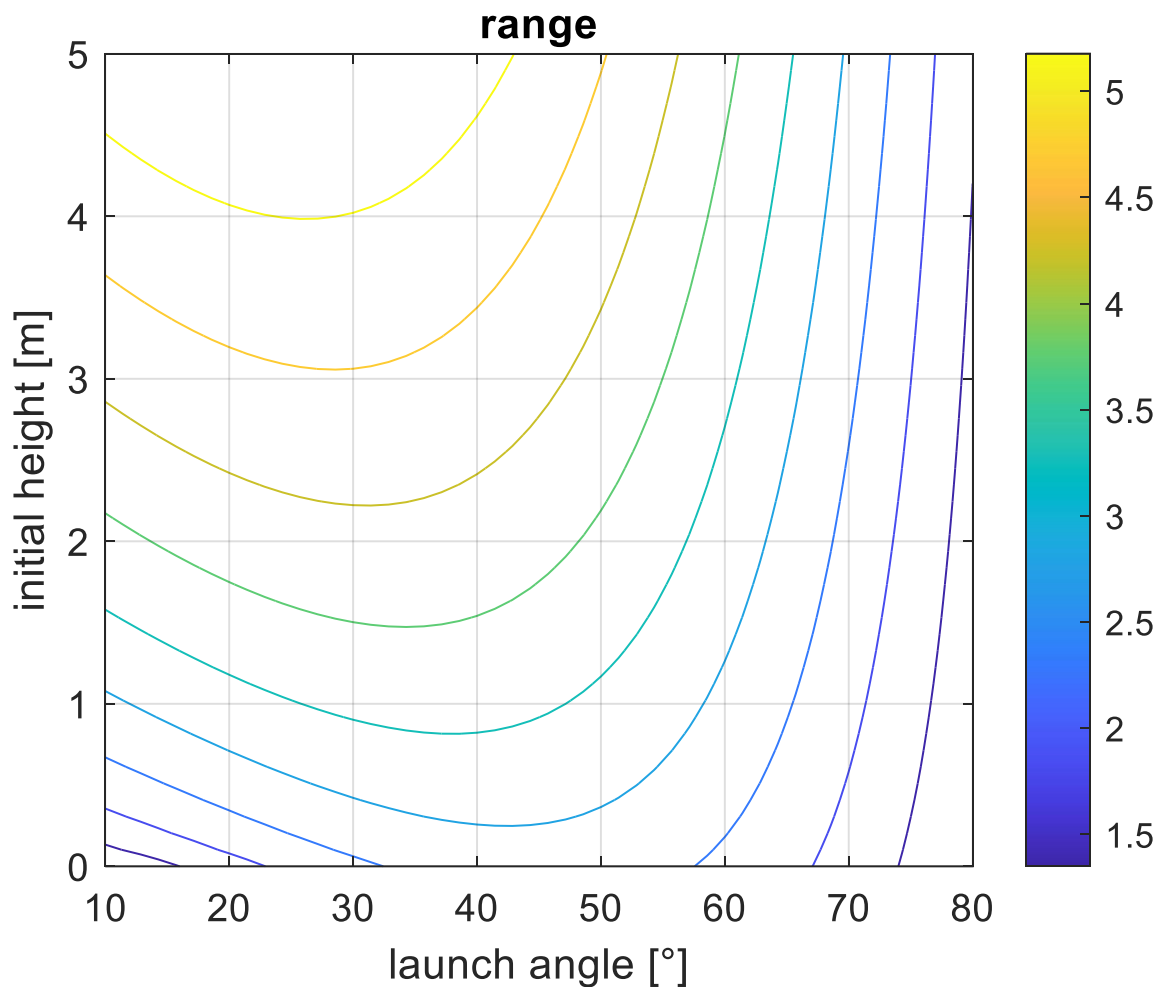
## 3) Furthest throw

The range  $R$  for a throw without friction as a function of the initial height  $h_0$  and the launch angle can be found e.g. on Wikipedia <https://de.wikipedia.org/wiki/Wurfparabel>.

$$R = \frac{v_0^2}{2g} \sin(2\beta) \left[ 1 + \left( 1 + \frac{2gh_0}{v_0^2 \sin^2 \beta} \right)^{1/2} \right] = \frac{v_0 \cos \beta}{g} \left( v_0 \sin \beta + \sqrt{(v_0 \sin \beta)^2 + 2gh_0} \right)$$

Define the function `range(launch angle, initial height)`.

Generate a contourplot of the range as a function of the launch angle ( $10^\circ$ - $80^\circ$ ) and the initial height (0-5m) for the launch velocity  $v_0=5\text{m/s}$ .



**without** Matlab: Do you understand the plot? Read from the plot the optimal launch angle from an initial height of 2.5m to achieve maximum range.