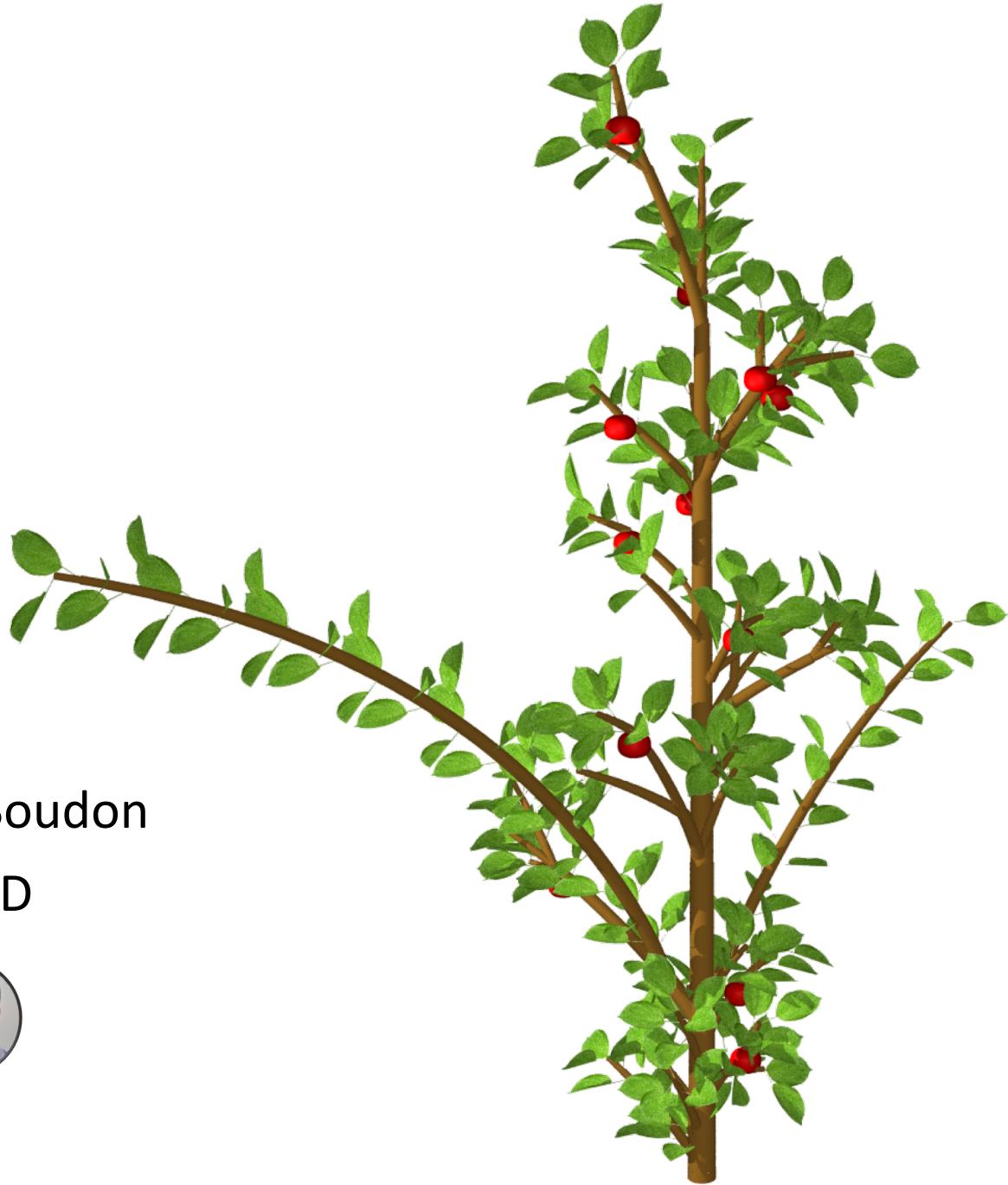


Modelling fruit tree architecture with L-systems

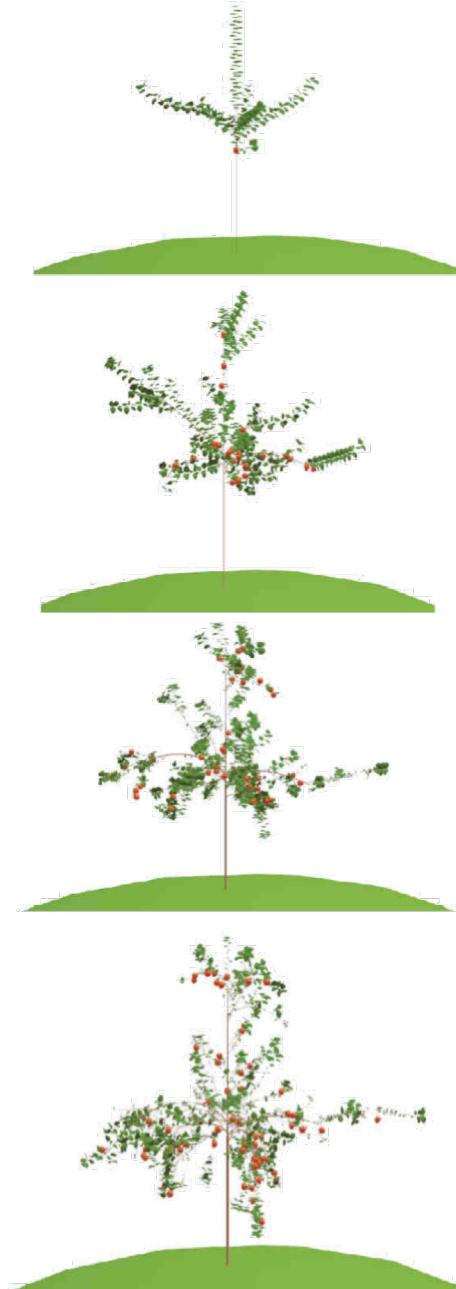
Frédéric Boudon

CIRAD



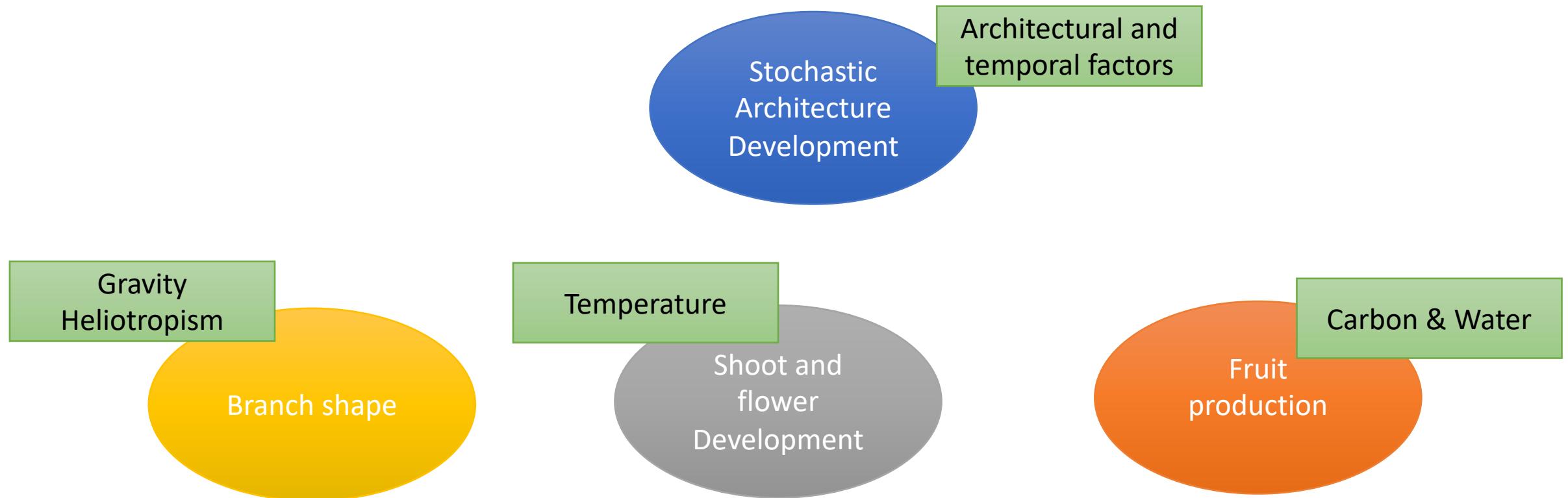
Motivation for a model

- To integrate an **integrative view**.
- Based on existing models of fruit trees
 - Apple tree (Costes et al. 2008),
 - Peach tree (Lopez et al., 2010).
 - Almond tree (De Jong et al., 2017).



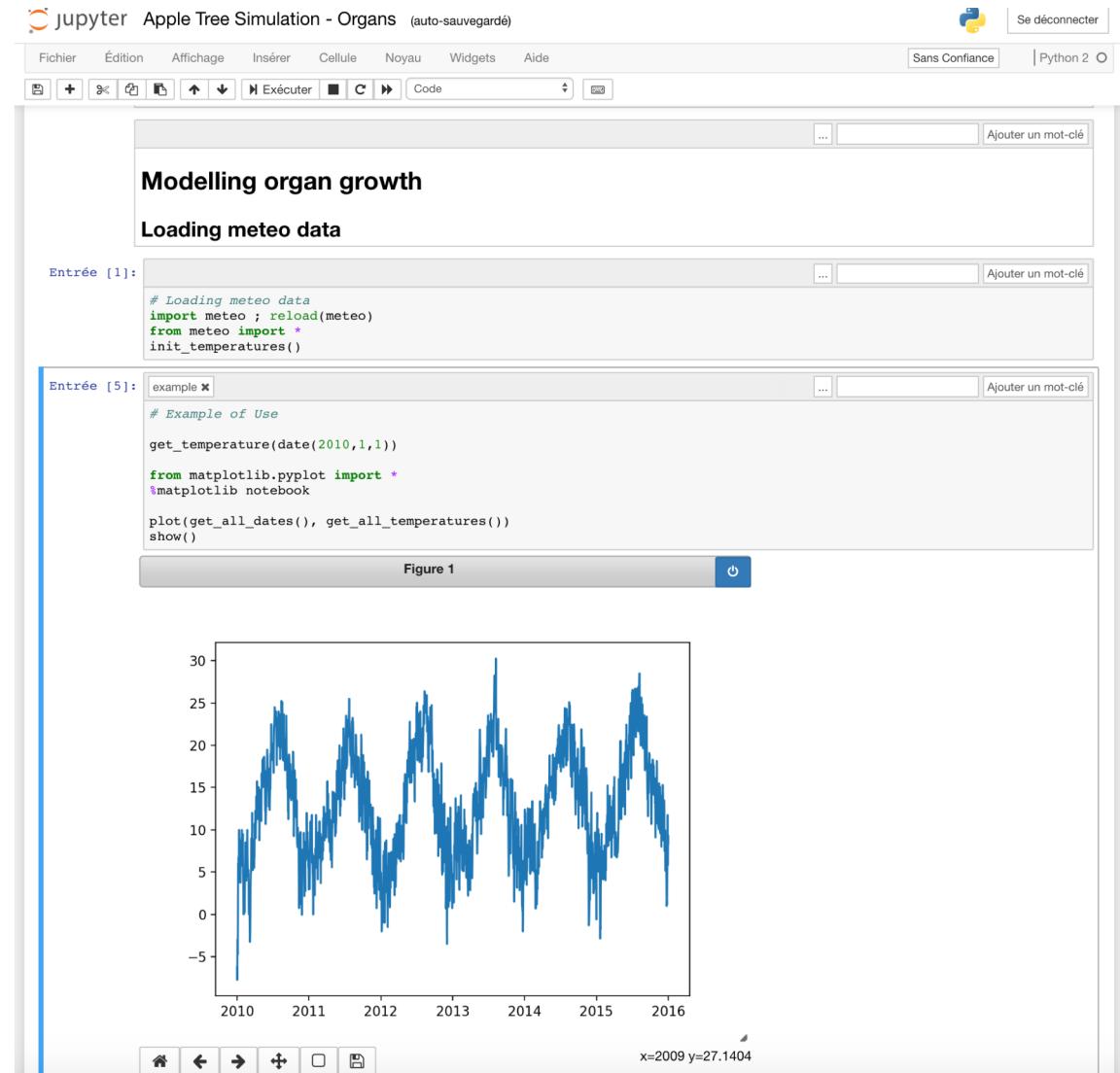
A functional-structural model of fruit tree growth and development

- Creation of an FSPM model that simulates development of architecture, phenology of organs, and production of fruits.



Exercices

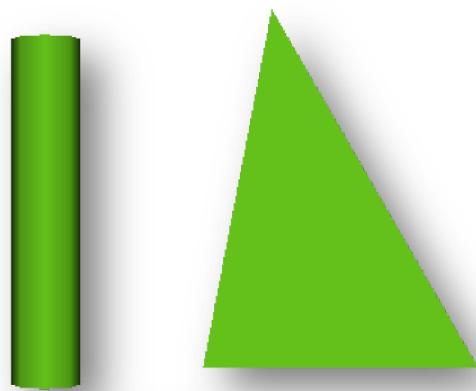
- More details on ...
 - ‘ArchiModelling.ipynb’
 - ‘Apple Tree Simulation - Organs.ipynb’
 - ‘Apple Tree Simulation - Architecture.ipynb’
in the directory ‘archimodelling’



Modelling organ shape

Primitives

- Set of predefined shapes (Cylinder, Sphere, Quad, etc.)



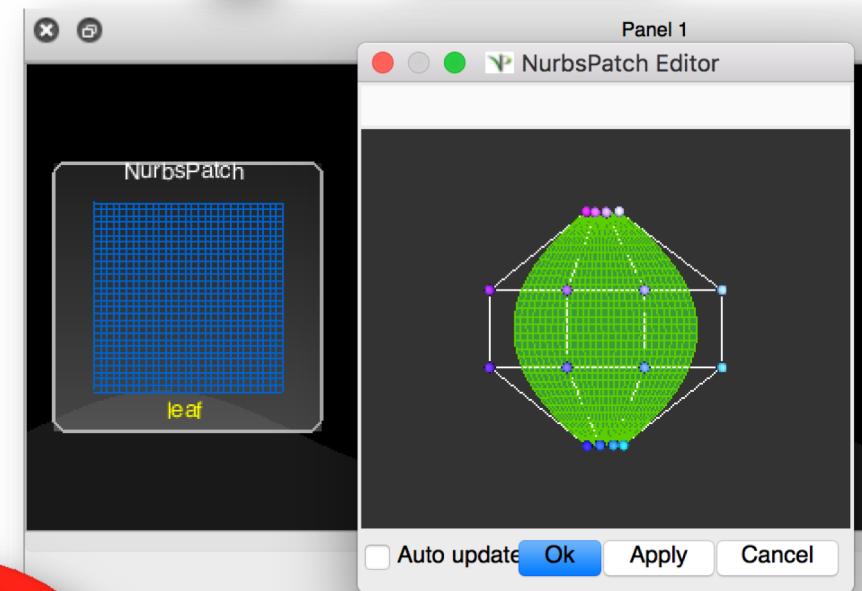
- Define polygon

```
{ . f . + (120) f (1.5) . } (concave)
```

- Display specific shape

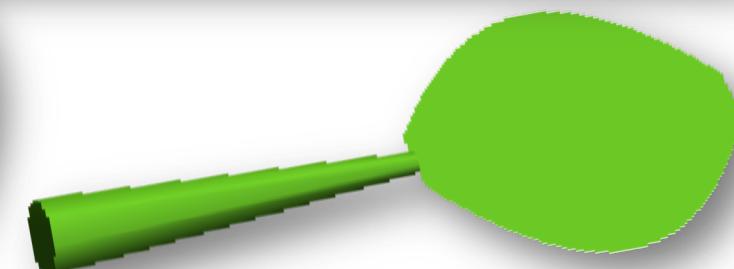
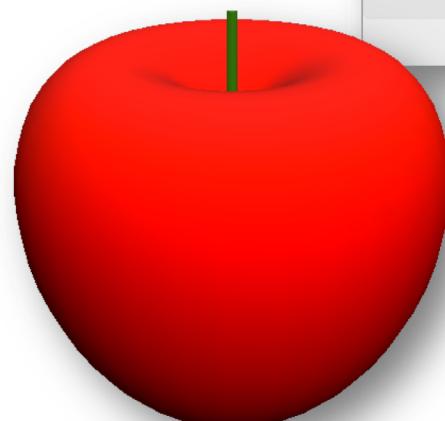
- @g (obj)

- Define graphically with editor

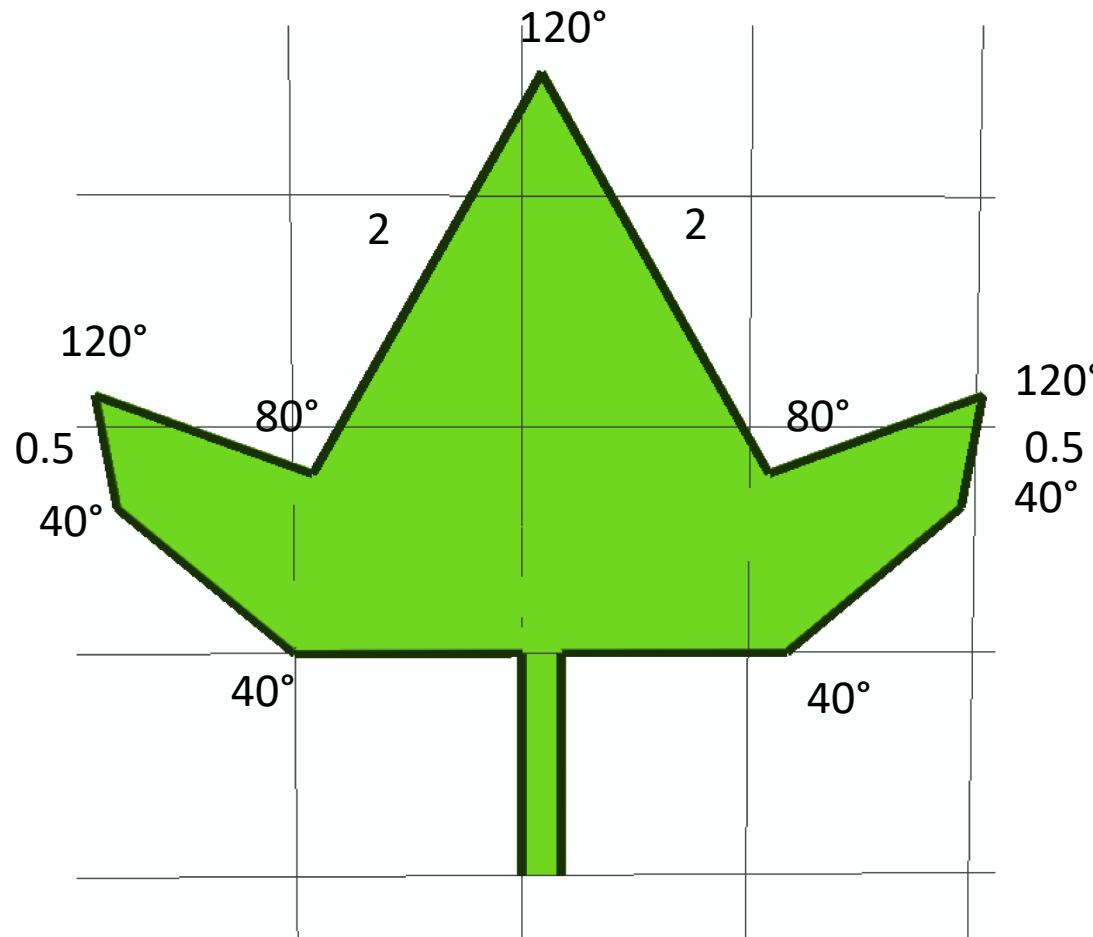


- Define procedurally

```
@g (SOR ( [sectioncurve] ))
```



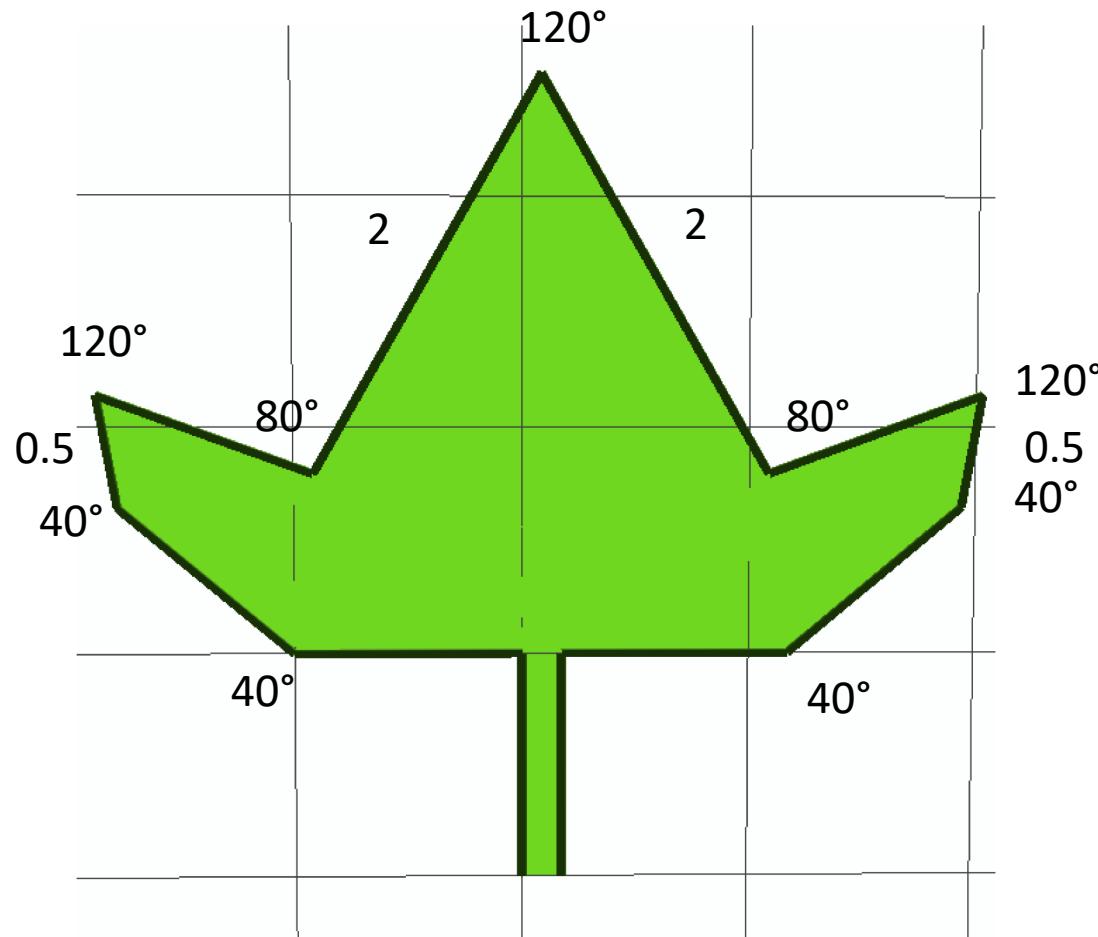
Exercise



Axiom: ,(2) _(0.02) { . F } (True)

F	Move forward, drawing a line
+(<i>a</i>)	Turn left <i>a</i> degrees
-(<i>a</i>)	Turn right <i>a</i> degrees

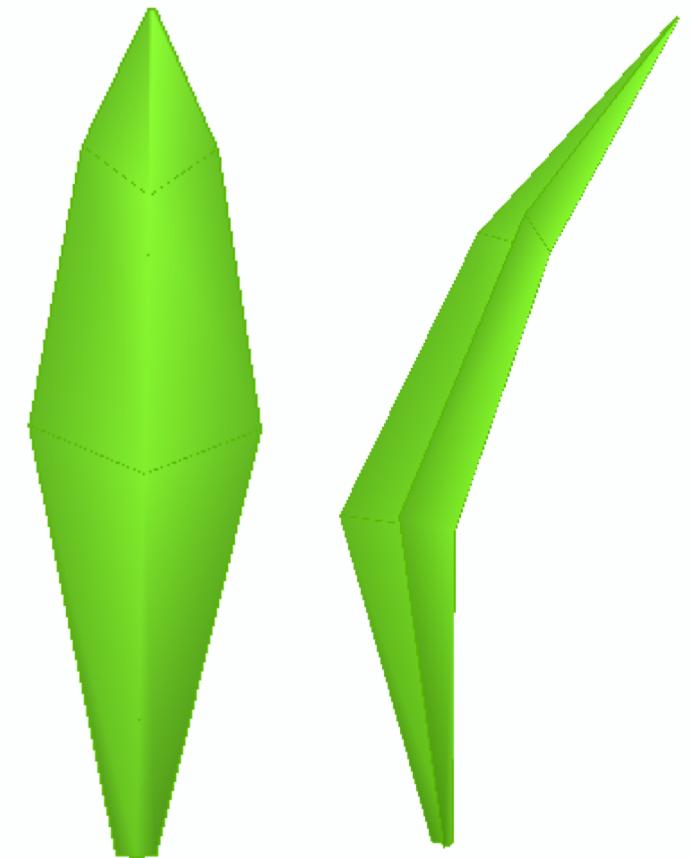
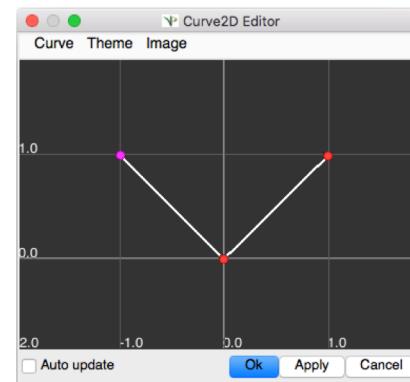
Exercise



Axiom: ,(2)_(0.02) { . F +(90) F -(40) F -(40) F(0.5) -(120) F +(80) F(2) -(120) F(2) +(80) F -(120) F(0.5) -(40) F -(40) F(1) +(90) F } (True)

Sweep surfaces

- Definition of the section of turtle tracing
 - SetContour (section)
- Concatenation of sections
 - @Gc

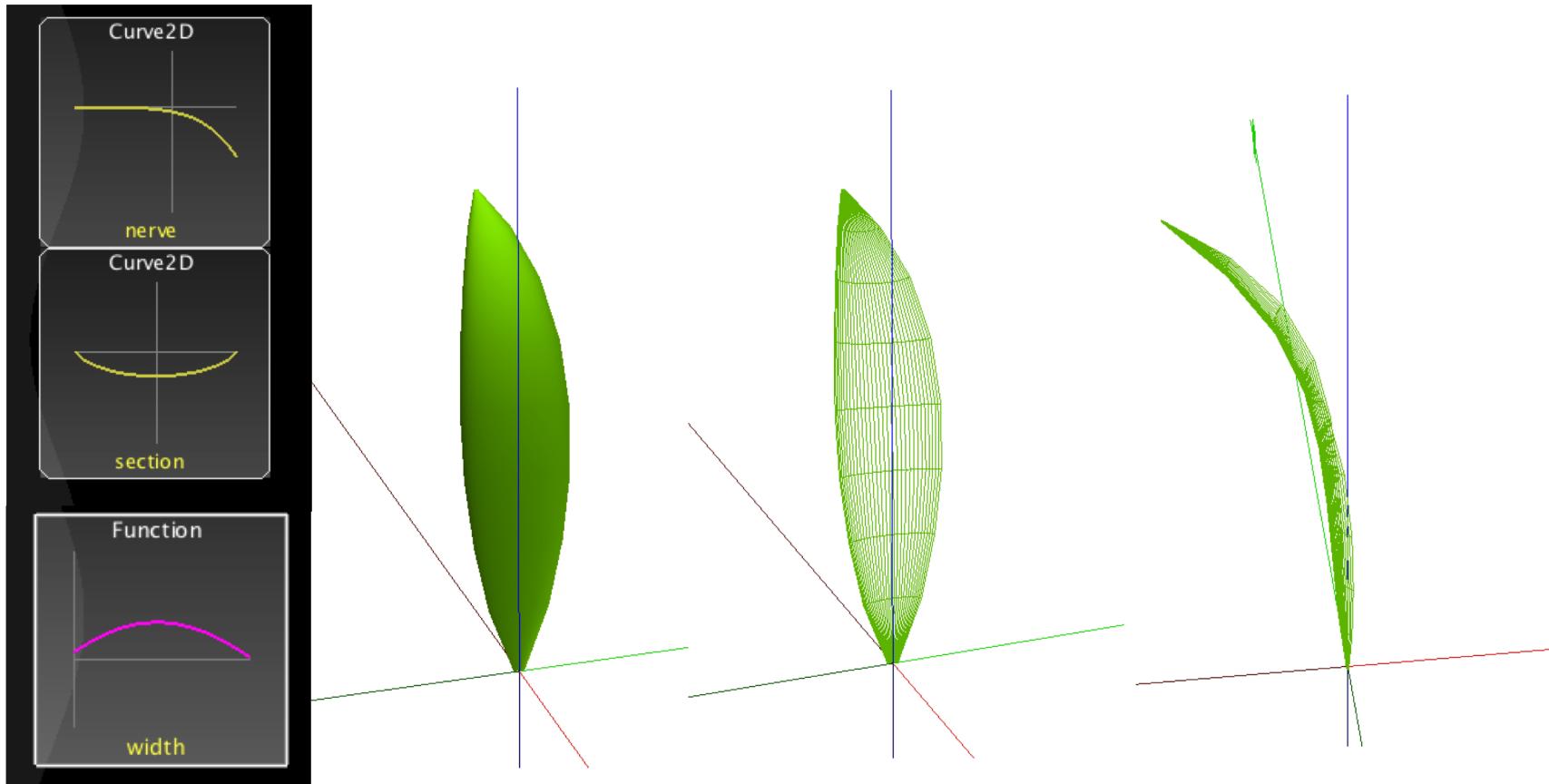


Axiom: @Gc _ (0.05) , (2) **SetContour**(section)
F(1, 0.3) & (20) **F**(1, 0.2) & (10) **F**(1, 0.01)

Sweep surfaces

- Generalization with section and path of the tracing

`Sweep(nerve_curve, section_curve,length, segsize, width,width_func)`



Interpolating profiles

```
axisSet = [axis1, ..., axisN]
times = [0, t1, ..., 1.0]
interpol = ProfileInterpolation(axisSet,times,
                                degree =3)
```

Axiom: **BG(0)** Branch(length)

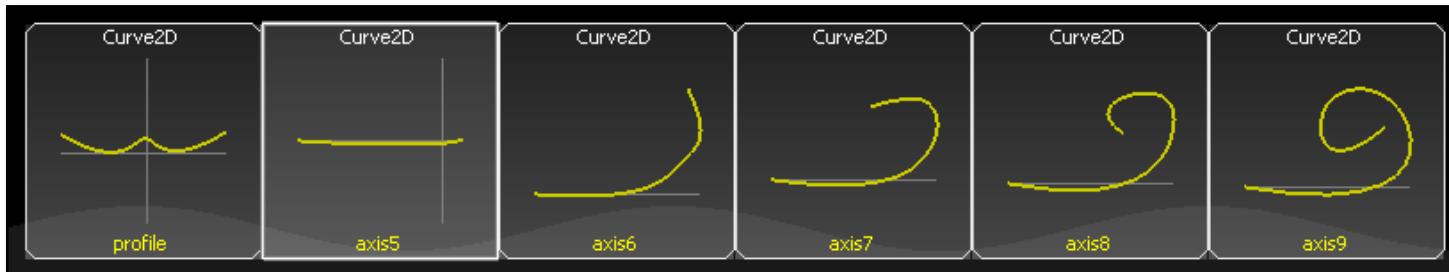
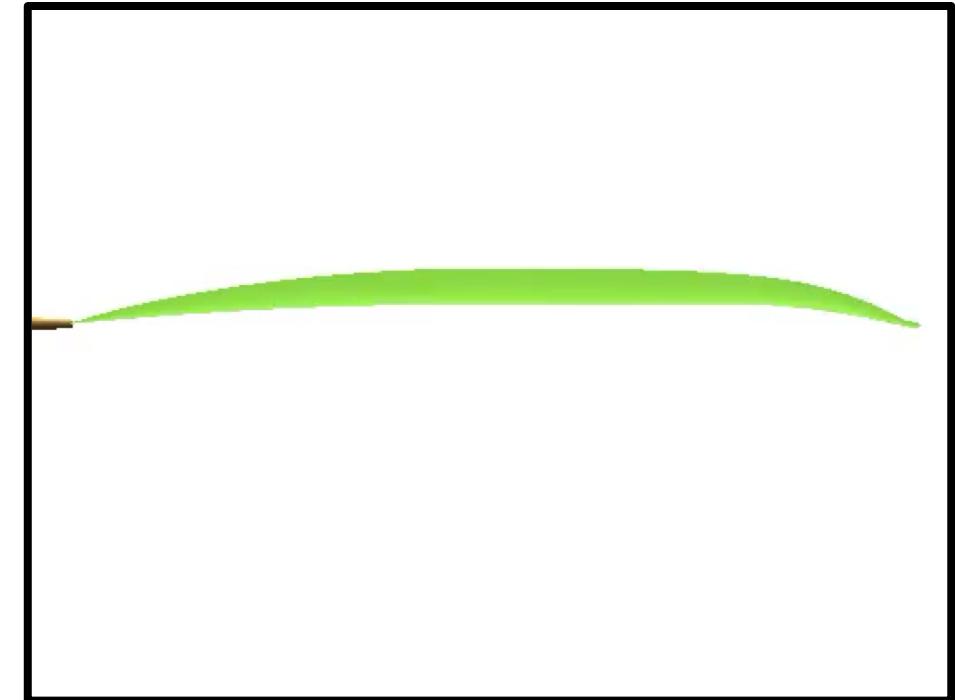
production:

BG(t) --> BG(t+dt)

interpretation:

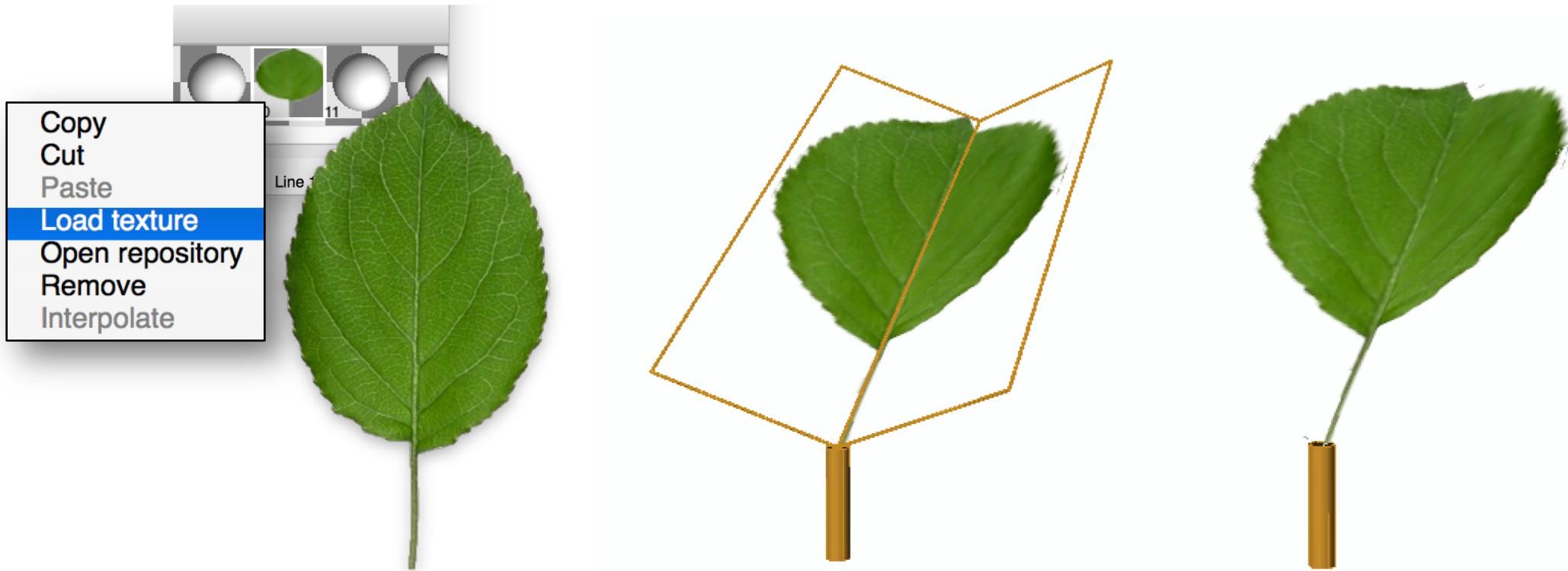
BG(t) --> SetGuide(interpol(t),length)

endsystem



Texturing

- Applying a picture onto a polygon



Exercise : Creating an apple tree leaf

- Open model 'organshape.ipynb' or the notebook
 - Use of ParameterSet to name attributes

```
Apex(p) --> Internode(ParameterSet(length = 2,  
width=0.1))  
Internode(p) --> F(p.length)
```

- Creation of a model
 - In the graphical editor, create a patch, name it 'leafshape'. Edit it to have the shape of a leaf. (In the notebook it is made programmatically)
 - Complete the interpretation rule Leaf(p) so that it use your symbol with command @g
- Creation of a textured model
 - Import image 'apple-leaf.png' as texture in position 10.
 - Complete the interpretation rule Leaf(p)
 - Apply color 10
 - Set up the stretching of the texture on the leaf using TextureVScale



Modelling organ growth and
development

Modelling growth

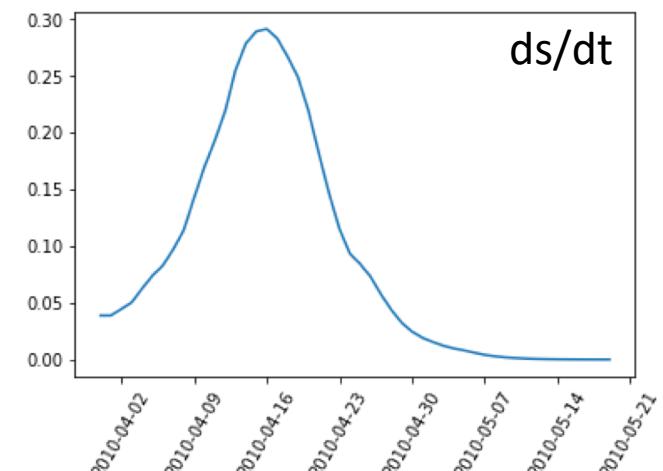
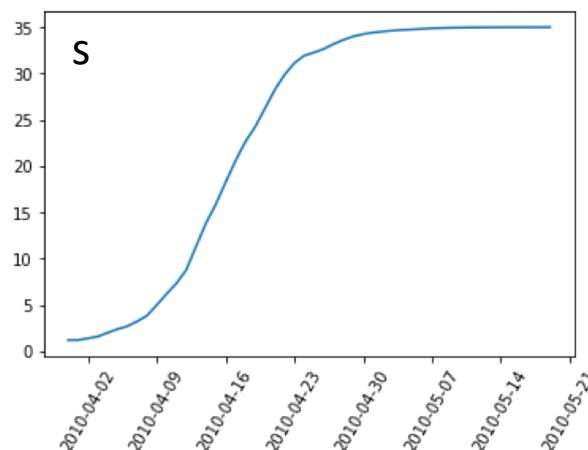
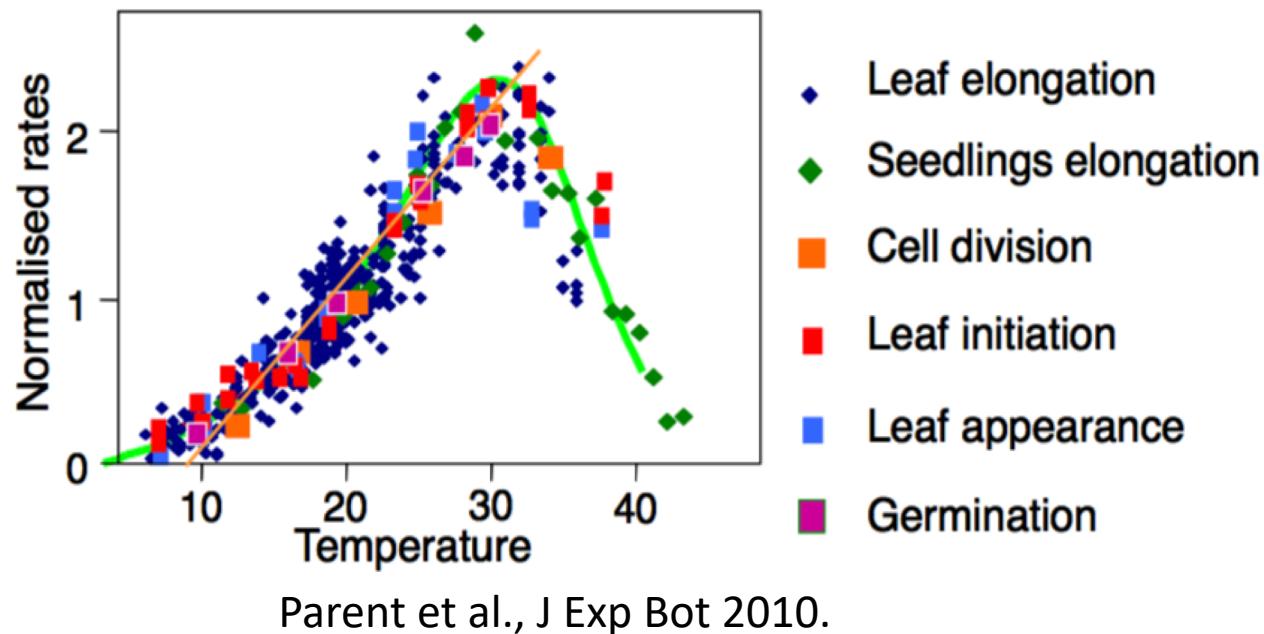
- Growth rate depends on temperature.

$$TTS = \sum_{i=1}^n (t_{mi} - \theta) \cdot \delta \quad \delta = \begin{cases} 0, & t_{mi} \leq \theta \\ 1, & t_{mi} > \theta \end{cases}$$

- Modelling growth with a logistic

$$s(t) = \frac{A}{1 + \exp^{-\frac{t-t_{ip}}{b}}}$$

$$\frac{ds}{dt} = \frac{A \cdot \exp^{-\frac{t-t_{ip}}{b}}}{b \cdot (1 + \exp^{-\frac{t-t_{ip}}{b}})^2}$$



Calendar and environmental information

- Each rewriting step correspond to a time step.
- Need to update global variables of the simulation such as
 - Date of the day
 - Current temperature, environmental conditions, etc.

Calendar and environmental information

- Each rewriting step correspond to a time step.
- Need to update global variables of the simulation such as
 - Date of the day
 - Current temperature, environmental conditions, etc.

```
cdate = None
ctemperature = None

def Start():
    global cdate, ctemperature
    cdate = firstday
    ctemperature = meteo.get_temperature(cdate)

def EndEach():
    global cdate, ctemperature
    cdate += timedelta(days=1)
    ctemperature = meteo.get_temperature(cdate)
```

Exercices

- Complete the notebook and encode.
 - A thermal time model (`ThermalTime.get_effective_temperature`)

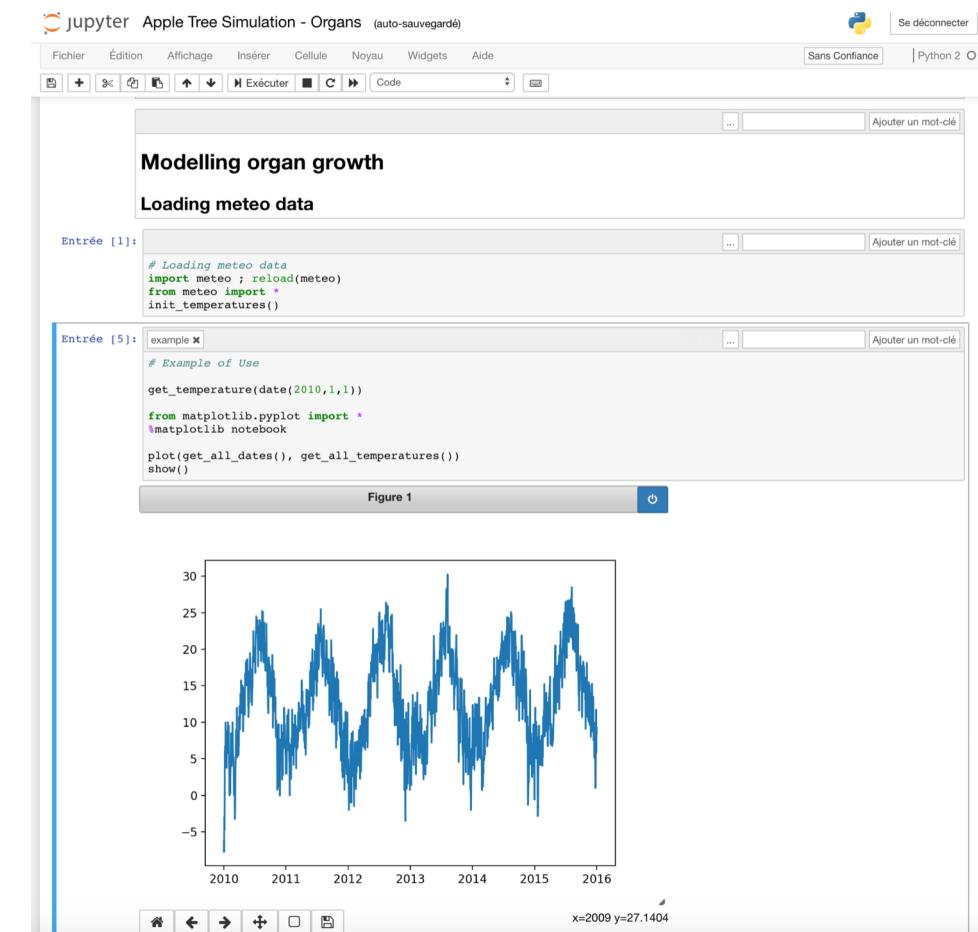
$$TTS = \sum_{i=1}^n (t_{mi} - \theta) \cdot \delta \quad \delta = \begin{cases} 0, & t_{mi} \leq \theta \\ 1, & t_{mi} > \theta \end{cases}$$

- a growth logistic function (`growth_logistic`)

$$s(t) = \frac{A}{1 + \exp^{-\frac{t-t_{ip}}{b}}}$$

- a growth rate function (`growth_rate`)

$$\frac{ds}{dt} = \frac{A \cdot \exp^{-\frac{t-t_{ip}}{b}}}{b \cdot (1 + \exp^{-\frac{t-t_{ip}}{b}})^2}$$



Exercices

- Complete the notebook and encode.

- A thermal time model

$$TTS = \sum_{i=1}^n (t_{mi} - \theta) \cdot \delta \quad \delta = \begin{cases} 0, & t_{mi} \leq \theta \\ 1, & t_{mi} > \theta \end{cases}$$

- a growth logistic function

$$s(t) = \frac{A}{1 + \exp^{-\frac{t-t_{ip}}{b}}}$$

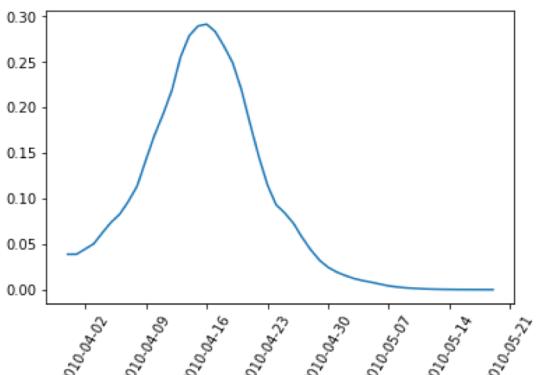
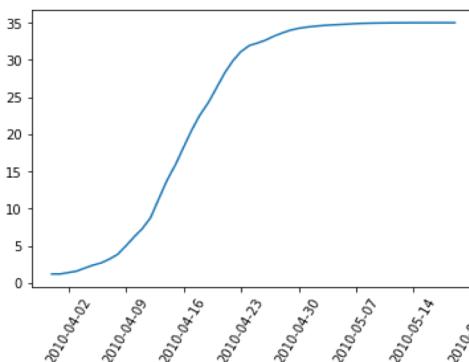
- a growth rate function

$$\frac{ds}{dt} = \frac{A \cdot \exp^{-\frac{t-t_{ip}}{b}}}{b \cdot (1 + \exp^{-\frac{t-t_{ip}}{b}})^2}$$

```
class ThermalTime:
    ...
    def get_effective_temperature(self, cdate):
        ctemp = get_temperature(cdate)
        return max(0, ctemp-self.base_temperature)
```

```
def growth_logistic(ttime, finalsize, tip, b):
    return finalsize / (1 + exp(-(ttime-tip)/b))
```

```
def growth_rate(ttime, finalsize, tip, b):
    g = exp(-(ttime-tip)/b)
    return (finalsize * g) / (b * pow((1+g), 2))
```



Exercise : Modelling apple tree metamer development.

- Open the notebook '*Apple Tree Simulation - Organs.ipynb*' or the organdevolp.ipynb model
- Complete the rule Internode and Leaf

Internode(p) :

```
# Use mthermaltime to get the effective temperature of the day
# and store it in variable ctime.
cttime = mthermaltime.get_effective_temperature(cdate)
# Compute length increment with growth_rate function.
# Parameterize it with p.finallength, tip_internode and b_internode.
# Integrate grow rate on ctime to have length increase.
# Add it to p.length variable
# p.length += ... to complete
# Do the same on the width variable
# p.width += ... to complete
# Accumulate thermal time into variable p.ttime.
p.ttime += cttime
produce Internode(p)
```

Exercise : Modelling apple tree metamer development.

- Internode rules

Internode(p) :

```
cttime = mthermaltime.get_effective_temperature(cdate)

    p.length += growth_rate(p.ttime, p.finallength, tip_internode,
b_internode)*cttime

    p.width += growth_rate(p.ttime, p.finalwidth, tip_internode,
b_internode)*cttime

    p.ttime += cttime
```

produce **Internode**(p)

Exercise : Modelling apple tree metamer development.

- Internode rules

Internode(p) :

```
cttime = mthermaltime.get_effective_time(p.ttime, p.biomass)

    p.length += growth_rate(p.ttime, p.biomass)*cttime

    p.width += growth_rate(p.ttime, p.biomass)*cttime

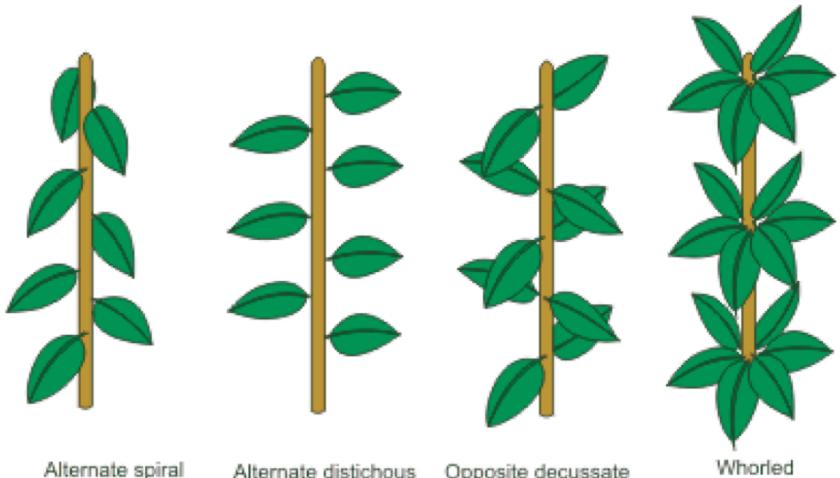
    p.ttime += cttime

produce Internode(p)
```

Modelling Growth Unit
development

Phyllotaxy

- Organisation of leaves along an axis

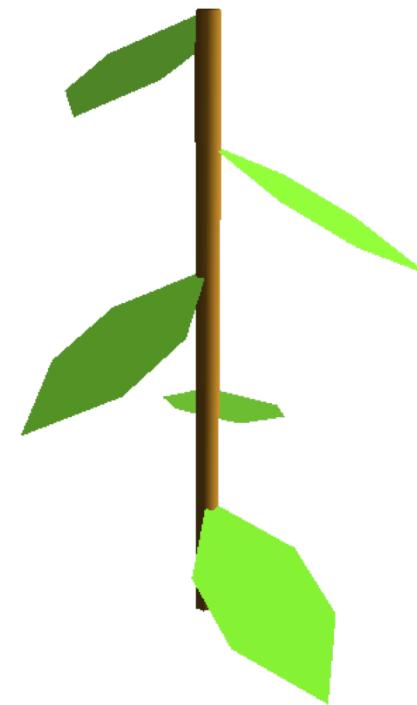


- Exercise: reproduce these organisations



Phyllotaxy

- Alternate phyllotaxy (spiral of 137.5°)

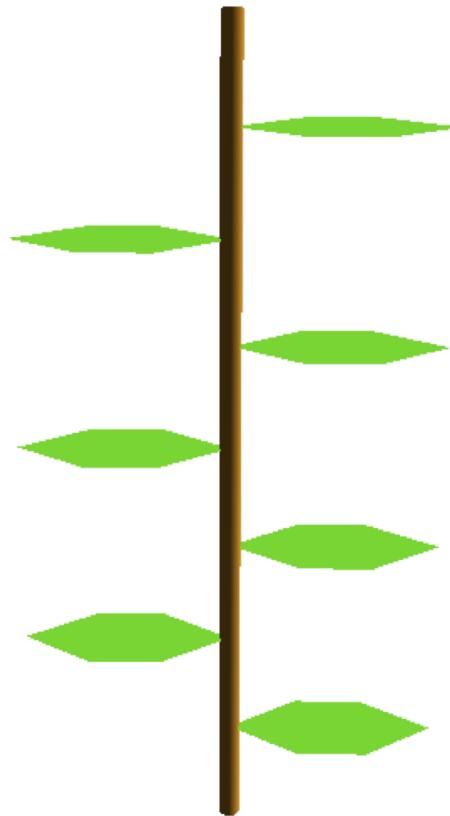
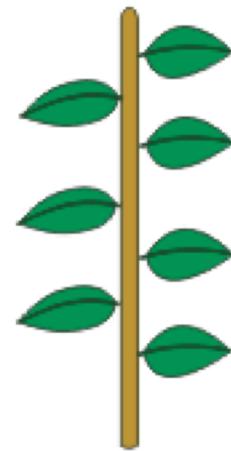


Axiom:

```
for i in range(5) :  
    nproduce F(1) / (137.5) [ &(120) , (2) ~l(2) ]
```

Phyllotaxy

- Alternate phyllotaxy

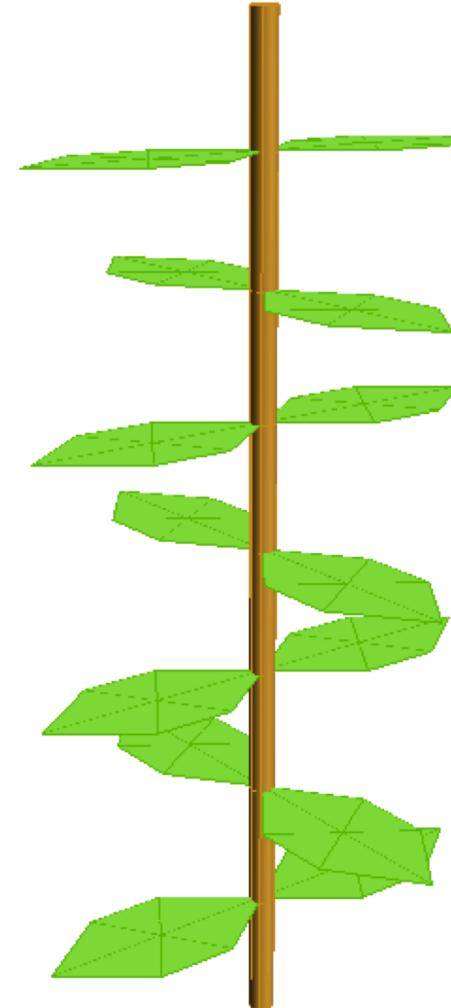
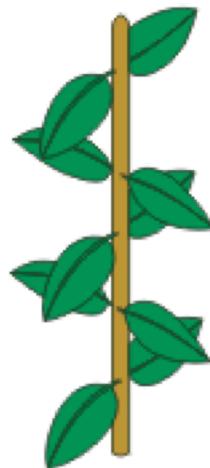


Axiom:

```
for i in range(7):  
    nproduce F(1) / (180) [ &(90) , (2) ~1(2) ]
```

Phyllotaxy

- Opposite decussate phyllotaxy



Axiom:

```
for i in range(7):  
    nproduce F(1) / (90) [ &(90) , (2) ~l(2) ]  
    nproduce [ / (180) &(90) , (2) ~l(2) ]
```

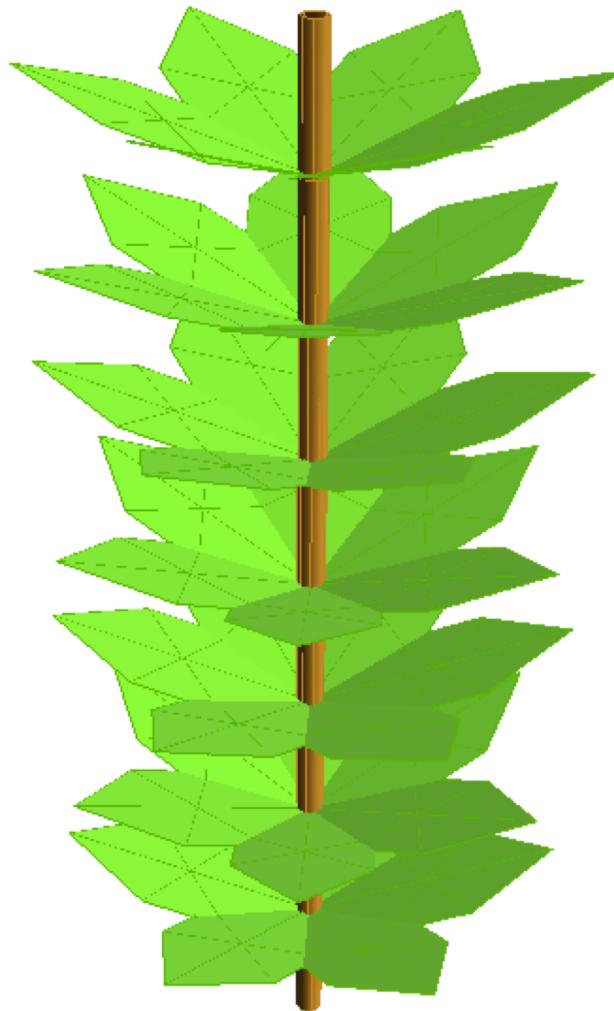
Phyllotaxy

- Whorled phyllotaxy



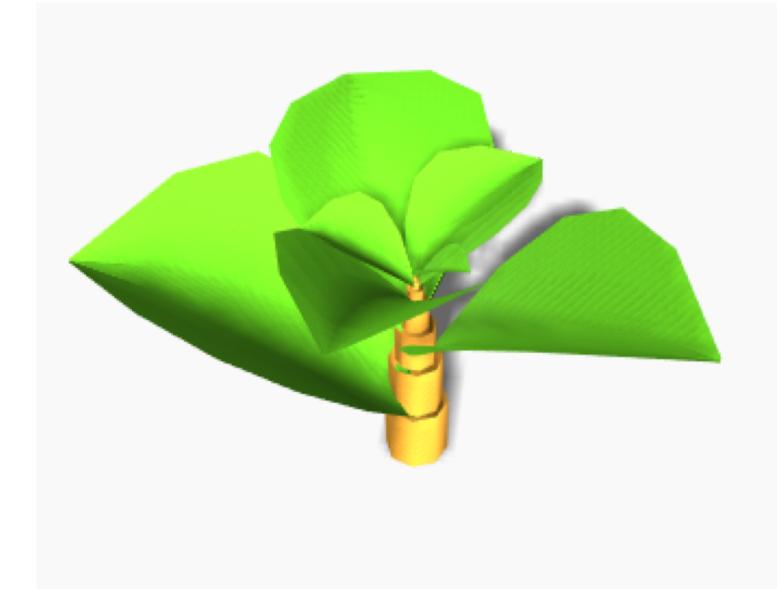
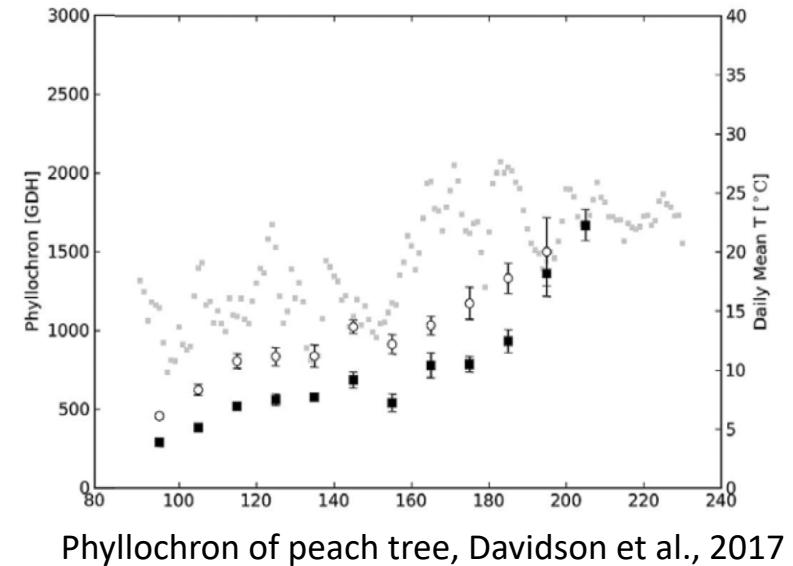
Axiom:

```
for i in range(7):  
    nproduce F(1) / (30)  
    for i in range(6):  
        nproduce / (60) [&(70), (2) ~1(2)]
```



Exercise : Generating the development of an apple tree shoot

- Apple trees have alternate distichous phyllotaxy 2/5 meaning an angle of 144°
- Phyllochron:
 - Preformed metamers : burst with the shoot
 - Neoformed metamers : depend on the temperature
- Modelling Phyllochron with thermal time
 - Study the **MetamerProduction** structure defined in the notebook '*Apple Tree Simulation - Organs.ipynb*'.
 - The function *accumulate* is used to compute the sum of thermal time and return the number of metamer to produce



Exercise : Generating the development of an appletree axis

- Edit the notebook 'Apple Tree Simulation - Organs.ipynb' or open model axis.ipynb
- Complete the rule for meristem.

Meristem(p) :

```
# Retrieve current nb of metamers produce by the meristem (p.metamer)
# accumulate the temperature and retrieve the nb of new metamers to produce
previousnbmetamer = p.nbmetamer
nbnewmetamer = p.accumulate(cdate)
for i in range(nbnewmetamer):
    # produce an Internode whose finallength is given by the internode_length function,
    length and width and ttime set to 0
    # produce symbol for phyllotaxy (144 for the apple tree)
    # produce lateraly (with a branching angle of 60) a leaf whose finalarea is given by
    function leaf_area, and area and width and ttime set to 0
    pass
produce Meristem(p)
```

Exercise : Generating the development of an appletree axis

Meristem(p) :

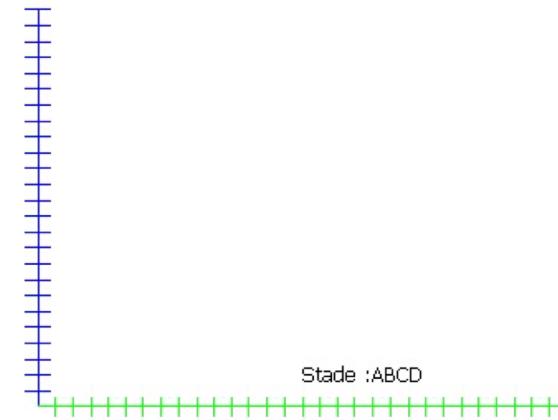
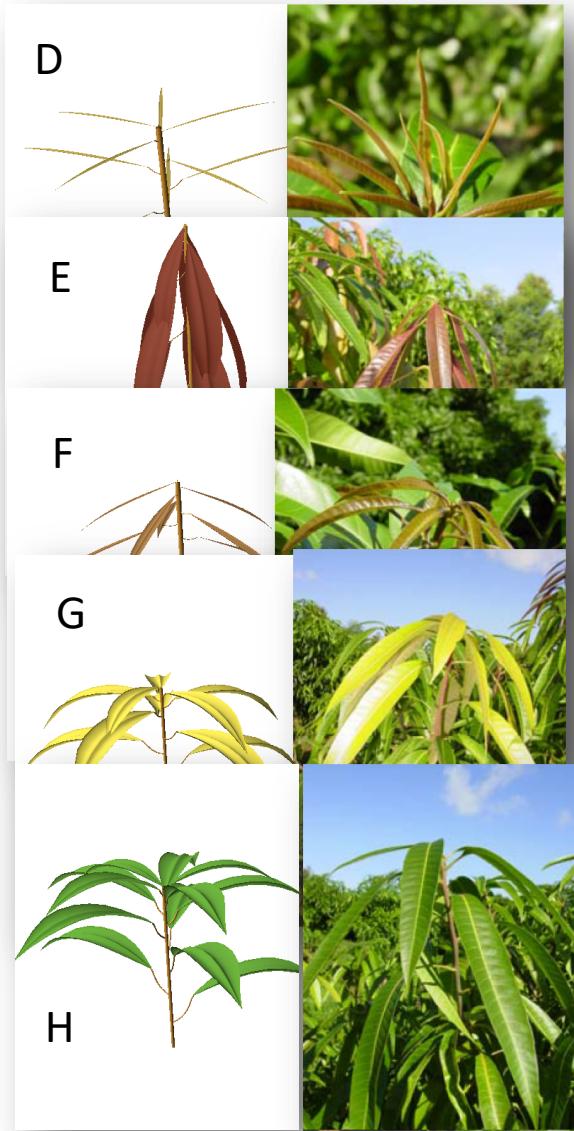
```
# Retrieve current nb of metamers produce by the meristem (p.metamer)
# accumulate the temperature and retrieve the nb of new metamers to produce
previousnbmetamer = p.nbmetamer
nbnewmetamer = p.accumulate(cdate)
for i in range(nbnewmetamer):
    # produce an Internode whose finallength is given by the internode_length function,
    length and width and ttime set to 0
    nproduce Internode(ParameterSet(length=0.01, finallength = internode_length(rank =
previousnbmetamer+i), width=0.01, ttime = 0))
    # produce symbol for phyllotaxy (144 for the apple tree)
    # produce lateraly (with a branching angle of 60) a leaf whose finalarea is given by
    # function leaf_area, and area and ttime set to 0
    nproduce /(144) [&(60) Leaf(ParameterSet(area=0, finalarea = leaf_area(rank =
previousnbmetamer+i), area = 0, ttime = 0)) ]
produce Meristem(p)
```

Exercise : Generating the development of an appletree axis

Meristem(p) :

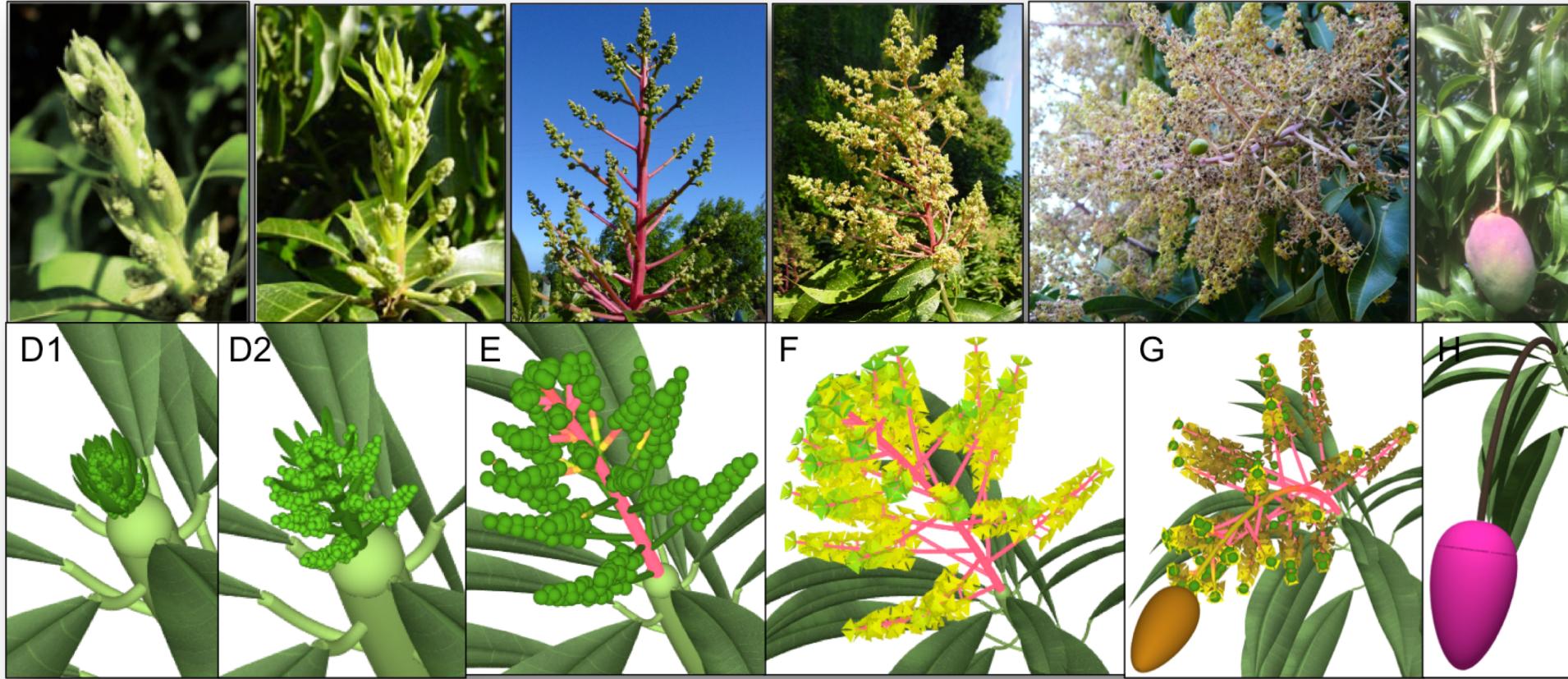
```
# Retrieve current nb of metamer
# accumulate the temperature and
previousnbmetamer = p.nbmetamer
nbnewmetamer = p.accumulate(cda)
for i in range(nbnewmetamer):
    # produce an Internode whose
    # length and width and ttime set to
    nproduce Internode(Parameter(
previousnbmetamer+i), width=0.01,
    # produce symbol for phyllot
    # produce lateraly (with a b
function leaf_area, and area and
    nproduce /(144) [&(60) Leaf(
previousnbmetamer+i), area = 0, t
produce Meristem(p)
```

Mango Growth Unit development



2003-07-02 00:00:00

Mango Inflorescence development



Modelling branch shape

Branch Geometry

- Geometrical embedding of a branch may be complex

```
length = 10
Axiom: Branch(length)
derivation length: 1
production:

interpretation:
Branch(1) :
    for i in range(l):
        nproduce f(0.1) F(1)
endsystem
```



Branch Geometry

- Use of tropism to change orientation of branch

```
length = 10  
Axiom: Elasticity(0.02) @Tp(0,0,1) Branch(length)
```

```
derivation length: 1
```

```
production:
```

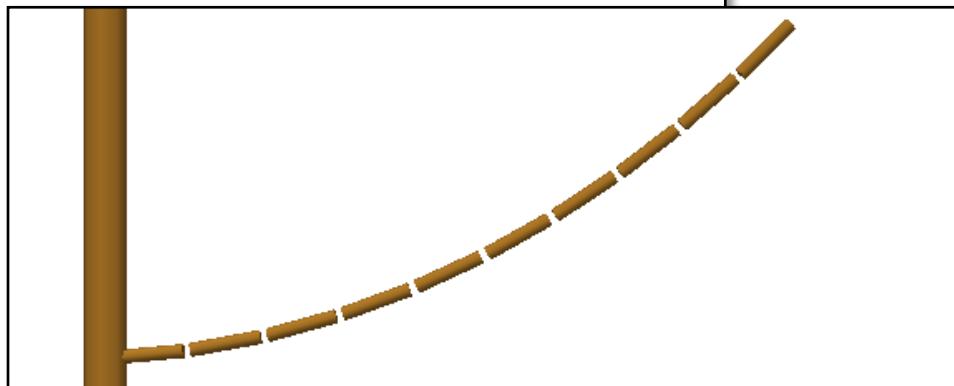
```
interpretation:
```

```
Branch(l) :
```

```
    for i in range(l):
```

```
        nproduce f(0.1) F(1)
```

```
endsystem
```



Branch Geometry

- Use of predefined geometrical embedding

```
length = 10
Axiom: SetGuide(path,length) Branch(length)
```

```
derivation length: 1
```

```
production:
```

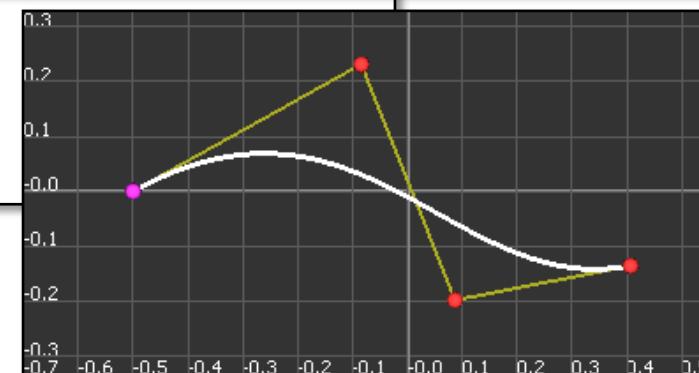
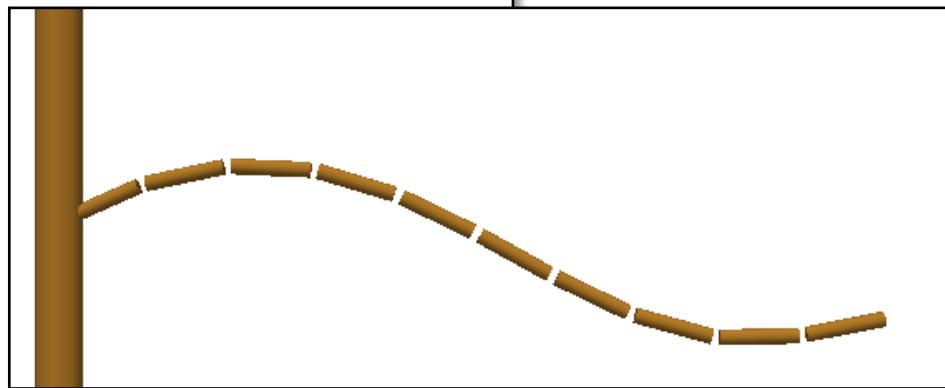
```
interpretation:
```

```
Branch(1) :
```

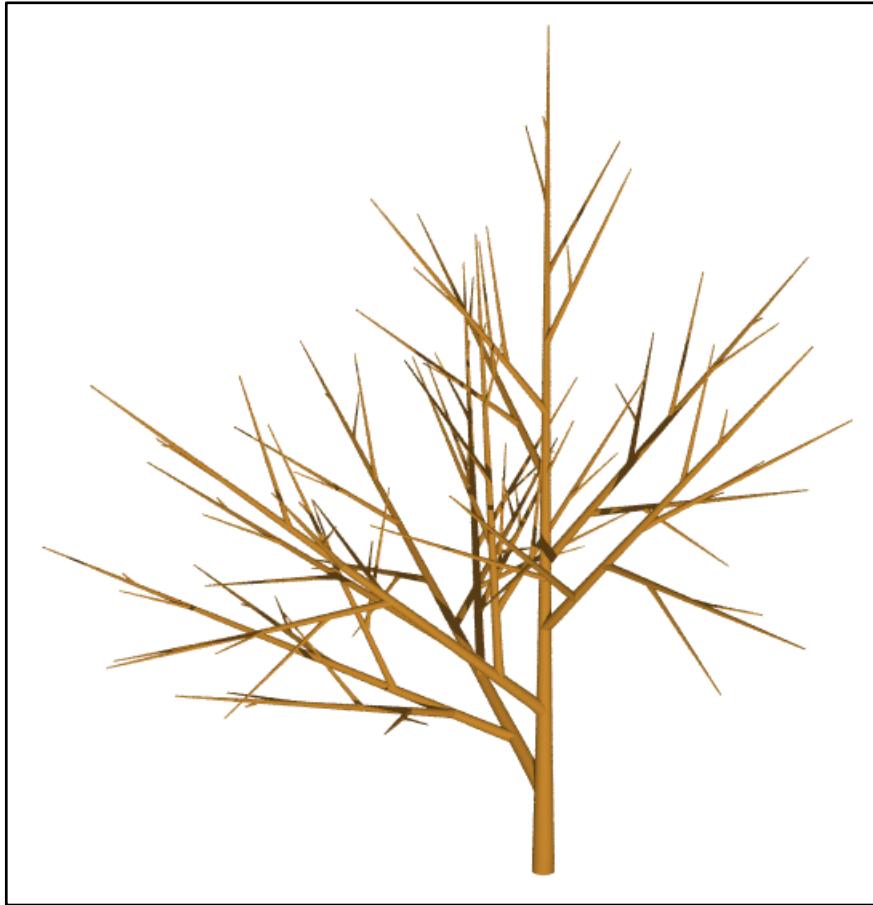
```
    for i in range(l):
```

```
        nproduce f(0.1) F(1)
```

```
endsystem
```

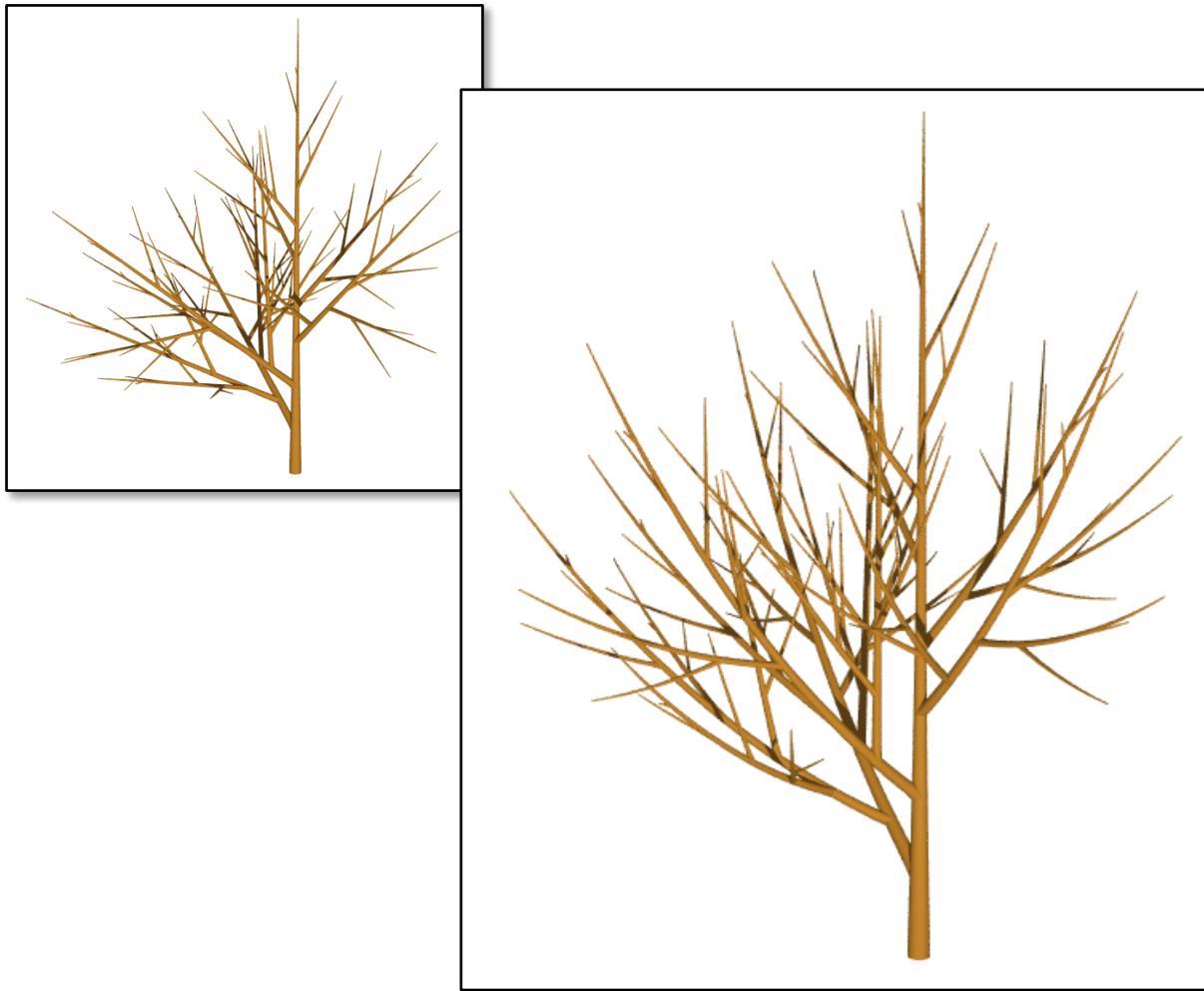


Example on a simple tree structure



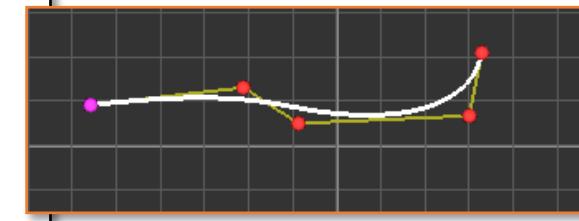
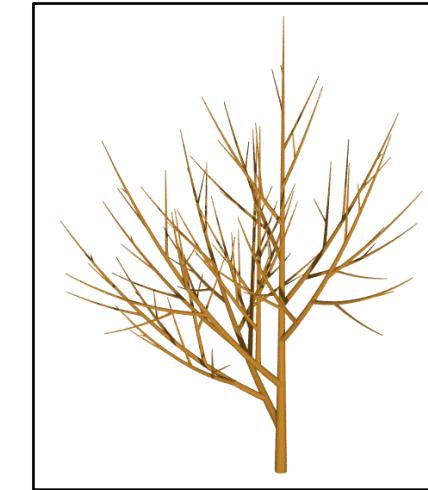
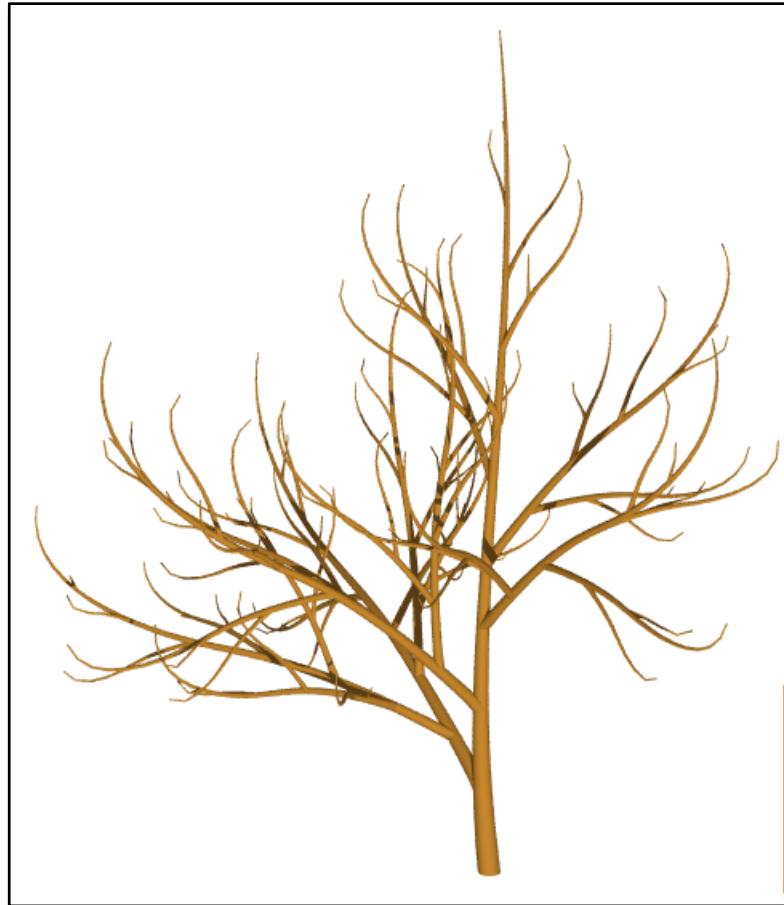
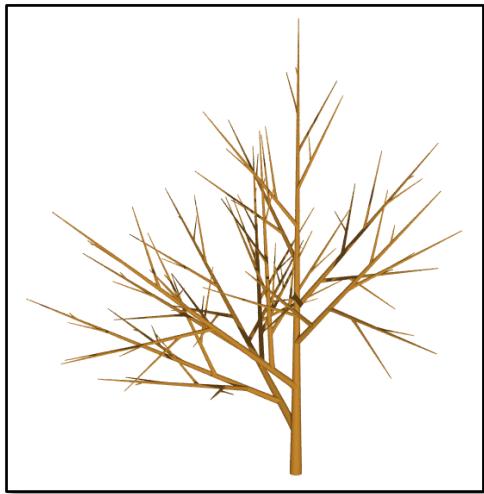
Simple recursive structure

Example on a simple tree structure



Using tropism

Example on a simple tree structure



Using a predefined branch path

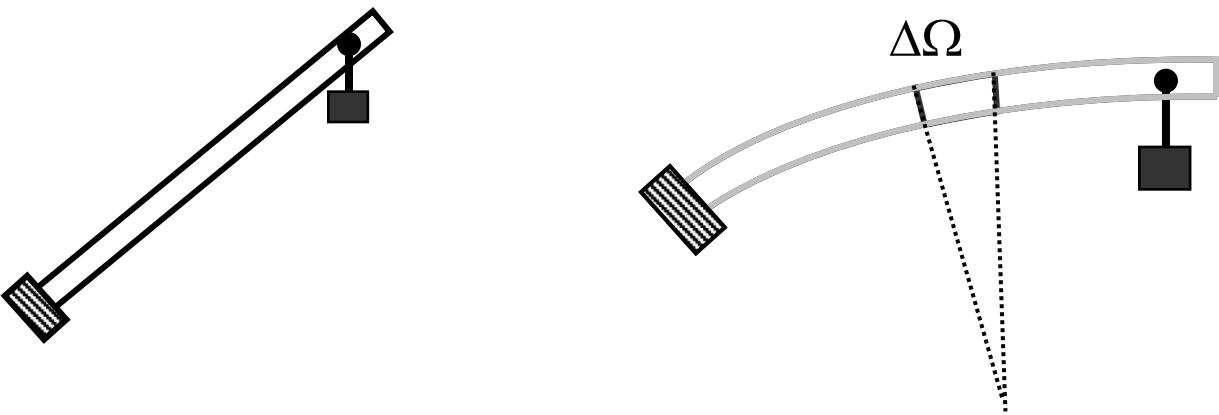
Exercise

- Test on this simple recursive structure
 - To insert an helio-tropism into the axiom. Test different values of the elasticity. For this use modules **@Tp** and **@Ts**
 - To remove tropism and insert a guide at the beginning of each branch using command **SetGuide**. Edit the guide to achieve curved architecture.



Biomechanical approach

- Consider shoot as a loaded beam



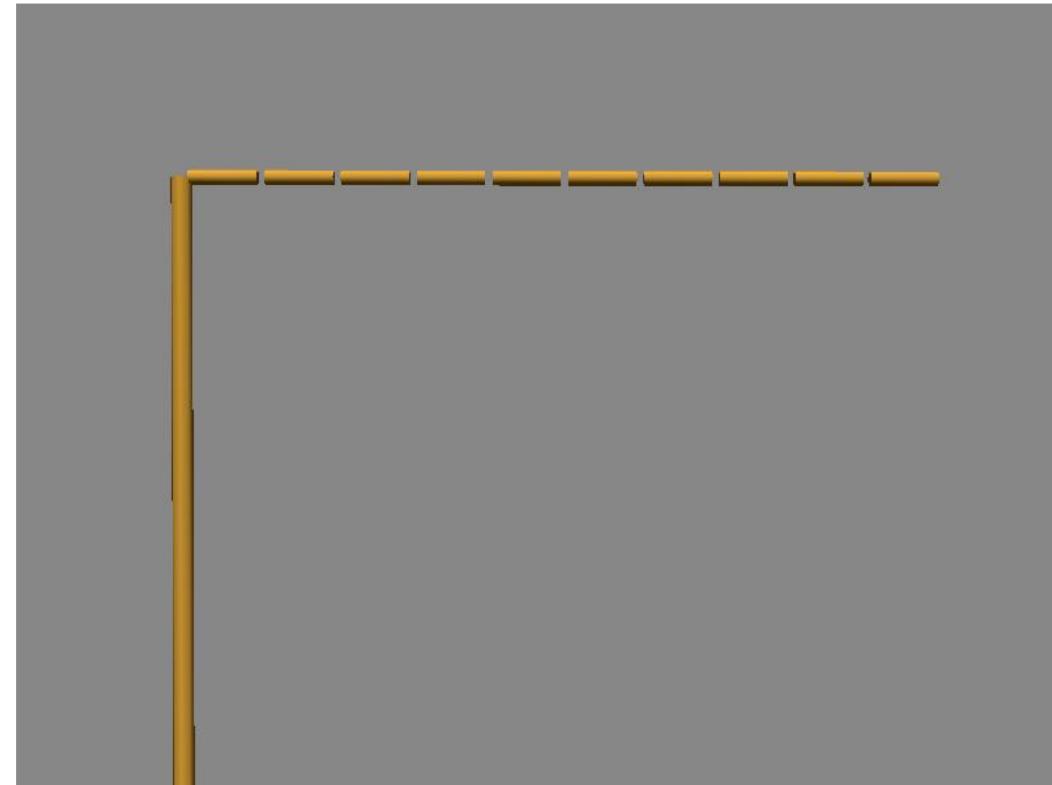
The total torque τ is the sum of the torque due to gravity and the torque due to tropism

$$\tau = \tau_g + \tau_t$$

The rate of rotation Ω is

with
$$\Omega_\tau = \frac{\tau}{R}$$

where $R = EI$
E : wood elasticity
I : section inertia



Require convergence

Modelling tree architecture

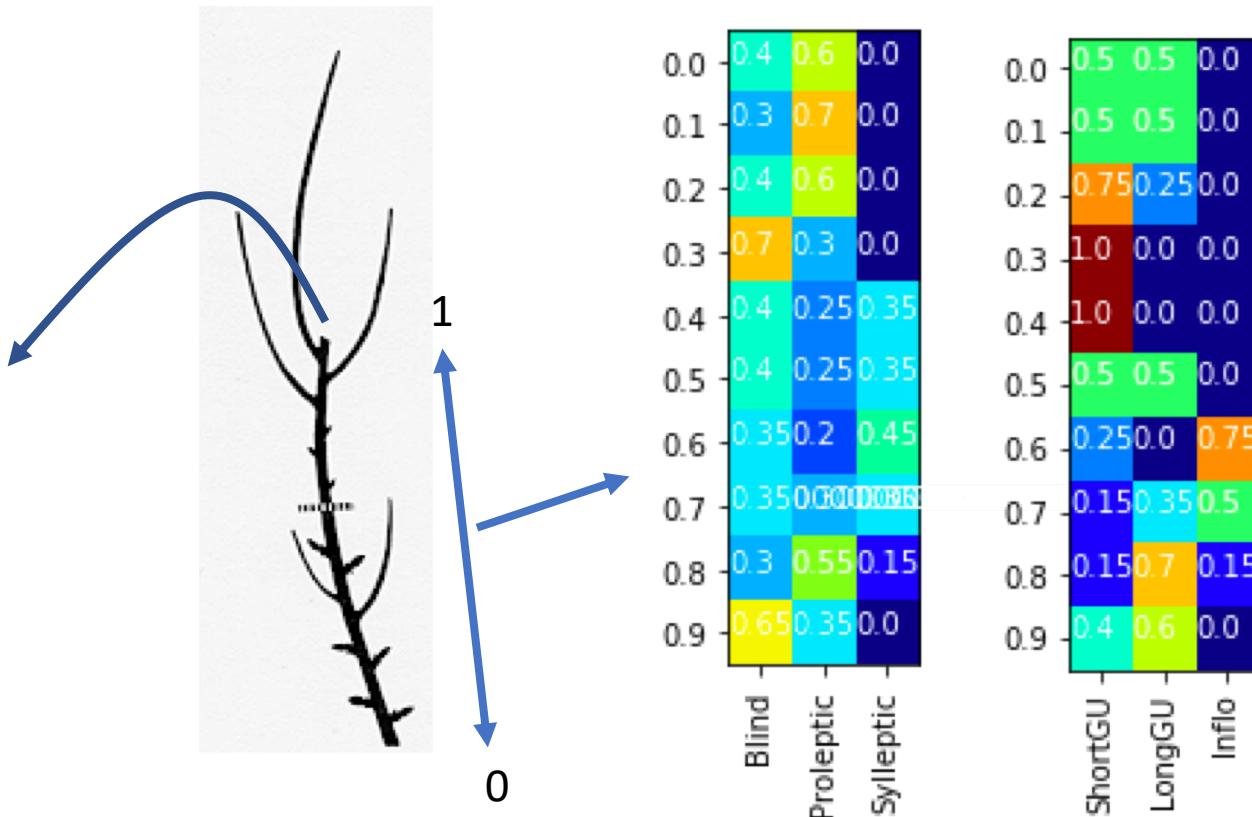
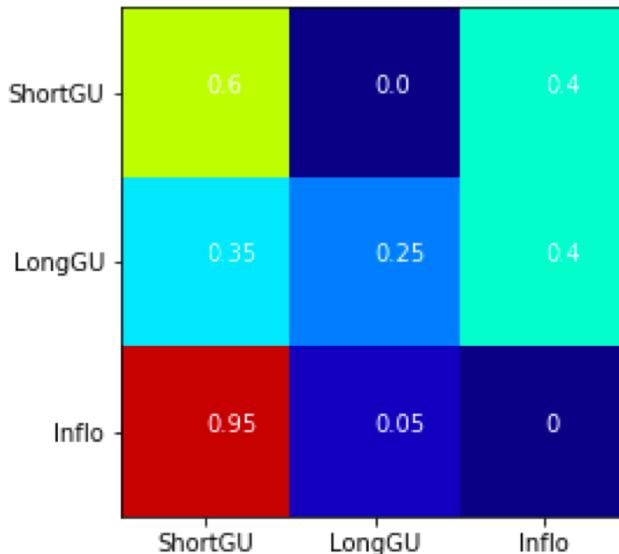
Simulation of apple tree architecture

- Modelling succession and branching of growth units in apple tree.
- Production is decomposed into fate and type.
- Different fates:
 - Proleptic
 - Sylleptic
 - Blind
- Different types :
 - Short GU,
 - Long GU
 - Flowering GU.

Simulation of apple tree architecture

- Probability of branching are defined according to normalized position along GU

- Succession:



Exercise :

More details on 'Apple Tree Simulation - Architecture.ipynb'

- Edit notebook 'Apple Tree Simulation – Architecture' or open model 'architecture.ipynb'
- Change Probabilities of succession and branching

Meristem(p) :

```
...
for i in range(nbnewmetamer):
    rank = previousnbmetamer+i
    normalizedrank = rank / p.mp.nbfinalmetamer
    nproduce Internode(...)
    nproduce / (144) [ &(60) Leaf(...) ]
    ramiffate, ramiftype = branching(p.gutype,
                                         normalizedrank)
    if ramiffate != Blind:
        nproduce [ ... Meristem(init_meristem(ramiffate, ramiftype, ... ) ] ...
else:
    produce Meristem(init_meristem(Proleptic, succession(p.gutype),
...))
```

Exercise :

More details on 'Apple Tree Simulation - Architecture.ipynb'

- Edit notebook 'Apple Tree Simulation – Architecture' or open model 'architecture.ipynb'
- Add rule for flowering GU that always create a lateral short GU and a Flower in terminal position.

Meristem(p) :

```
...
if p.mp.nbmetamer < p.mp.nbfinalmetamer:
    # meristem need to still generate metamer
    nproduce Meristem(p)
else:
    # succession
    if p.gutype == Inflo:
        # to be completed
        # generate a lateral sylleptic GU
        # generate a flower
    else:
        if p.gutype == TrunkGU: nproduce @Tp(0,0,-1) @Ts(0.005)
        produce Meristem(init_meristem(Proleptic, succession(p.gutype), p.init_date,
p.mp.nbfinalmetamer))
```

Exercise :

More details on ‘Apple Tree Simulation - Architecture.ipynb’

- Edit notebook ‘Apple Tree Simulation – Architecture’ or open model ‘architecture.ipynb’

Meristem (p) :

Exercise :

More details on 'Apple Tree Simulation - Architecture.ipynb'

- Edit notebook 'Apple Tree Simulation – Architecture' or open model 'architecture.ipynb'

Meristem(p) :

...

succession

if p.gutype == Inflo:

generate a lateral sylleptic GU

generate a flower

nproduce [& (15) Meristem(init_meristem(Sy...)

succession(p.gutype),

p.initdate,

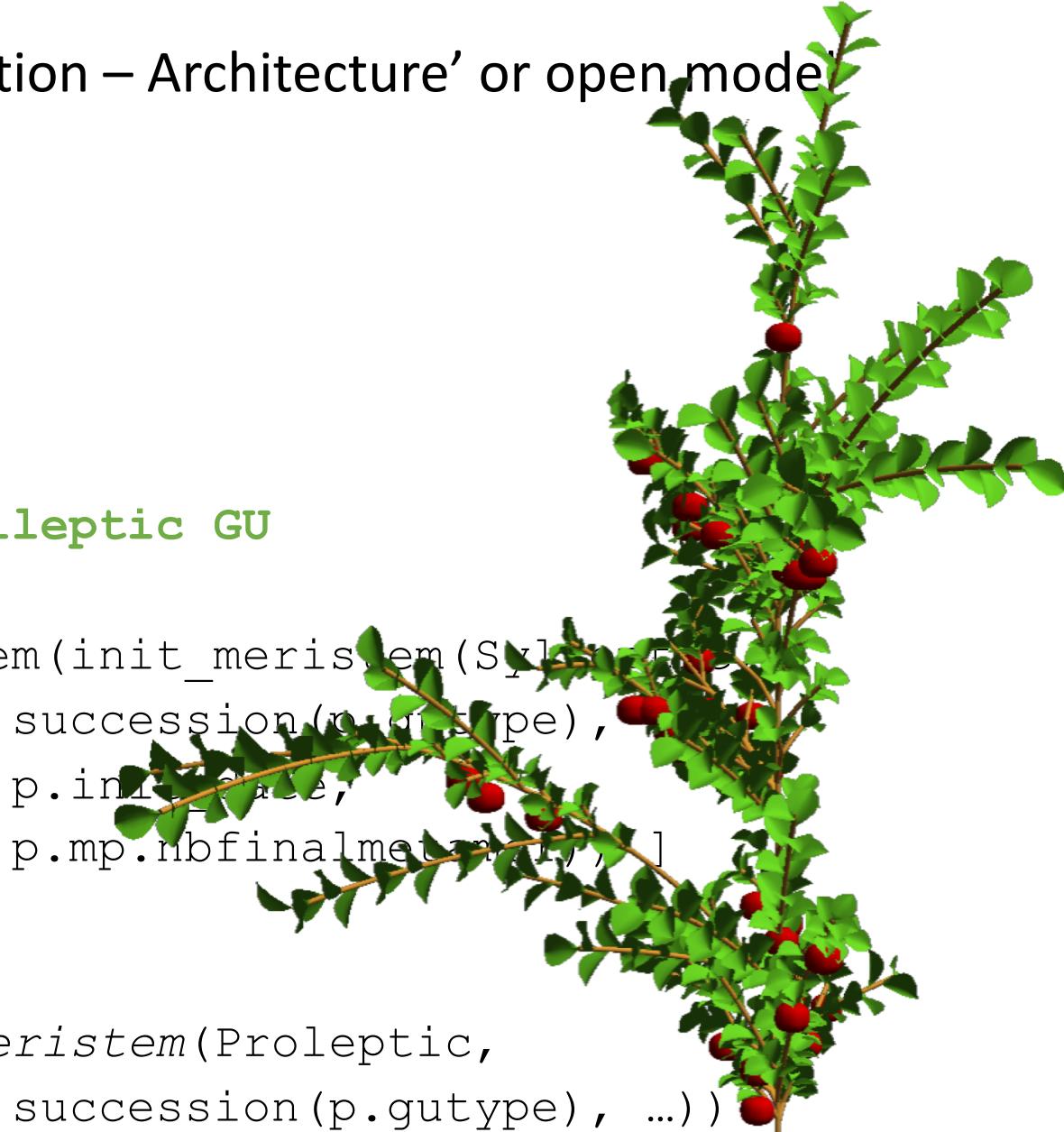
p.mp.nbfinalmeristem(1),]

produce Flower(0)

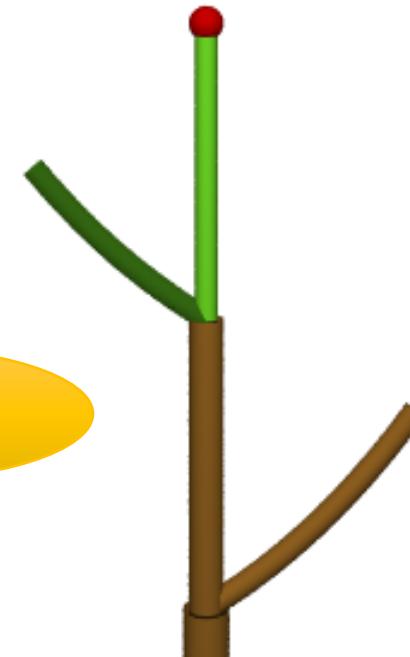
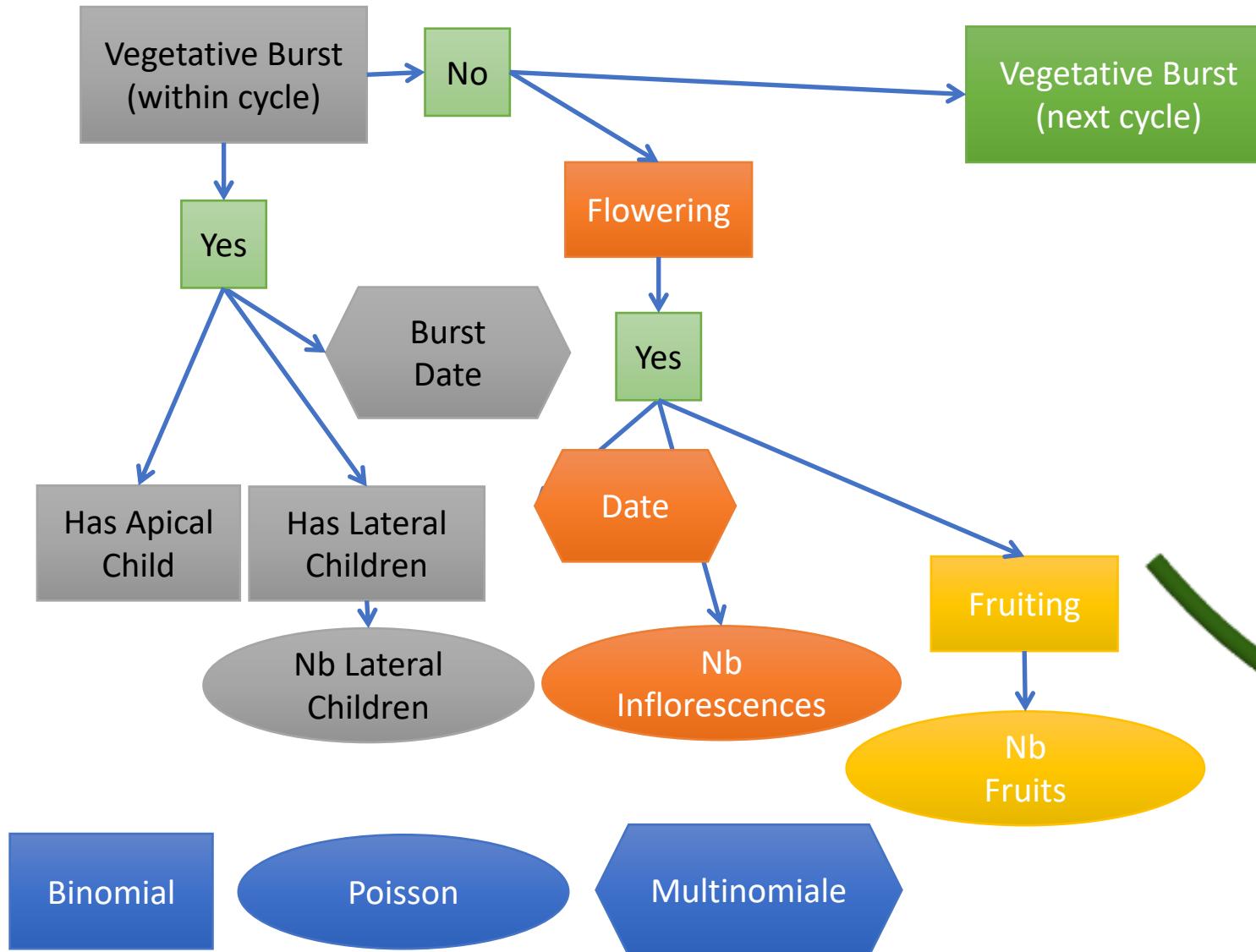
else:

produce **Meristem**(init_meristem(Proleptic,

succession(p.gutype), ...))



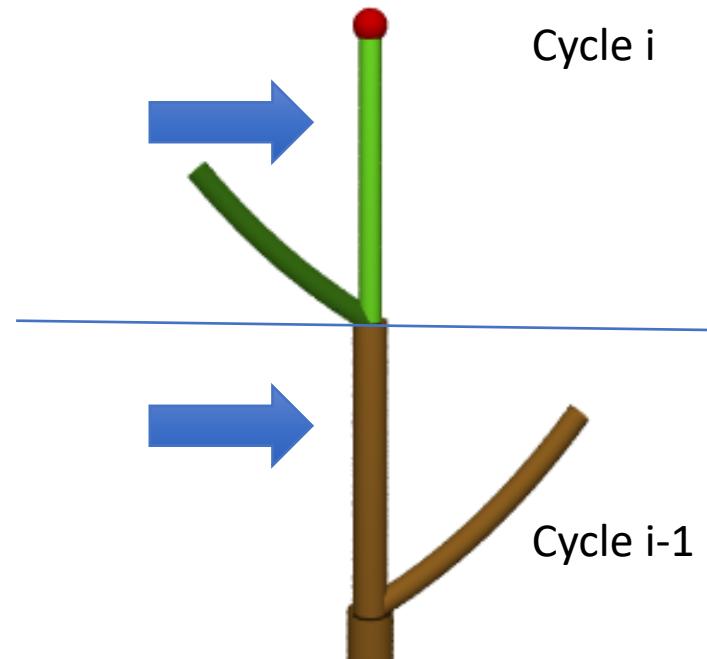
Simulation of mango architecture



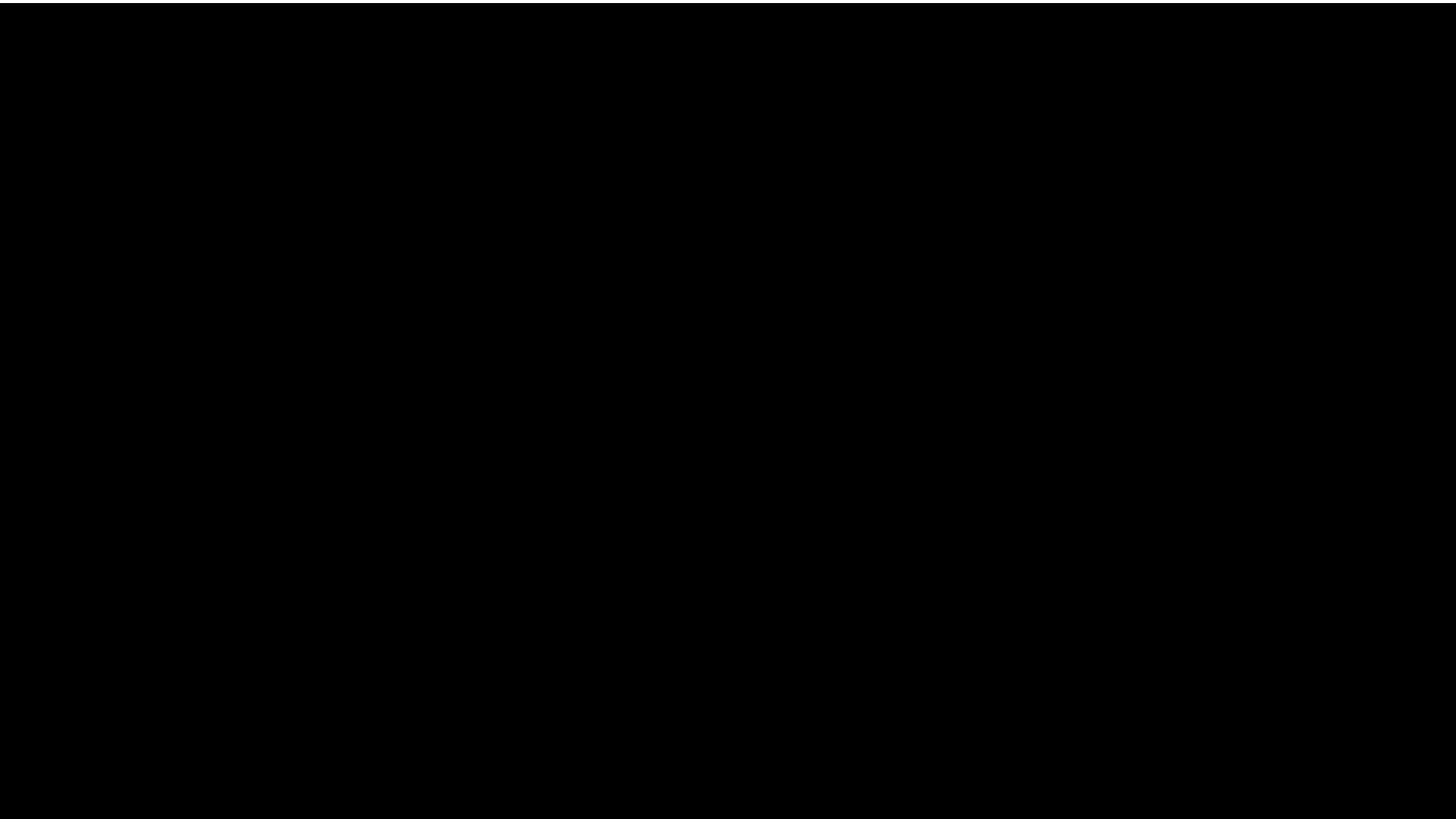
Structural and temporal factors

- ◆ Mother Position : Apical / Lateral
- ◆ Mother Burst Date : Month of vegetative cycle
- ◆ Ancestor Position : Apical / Lateral
- ◆ Ancestor Fate : Vegetative / Flowering

(Dambreville et al., J. Ex.Bot., 2013)



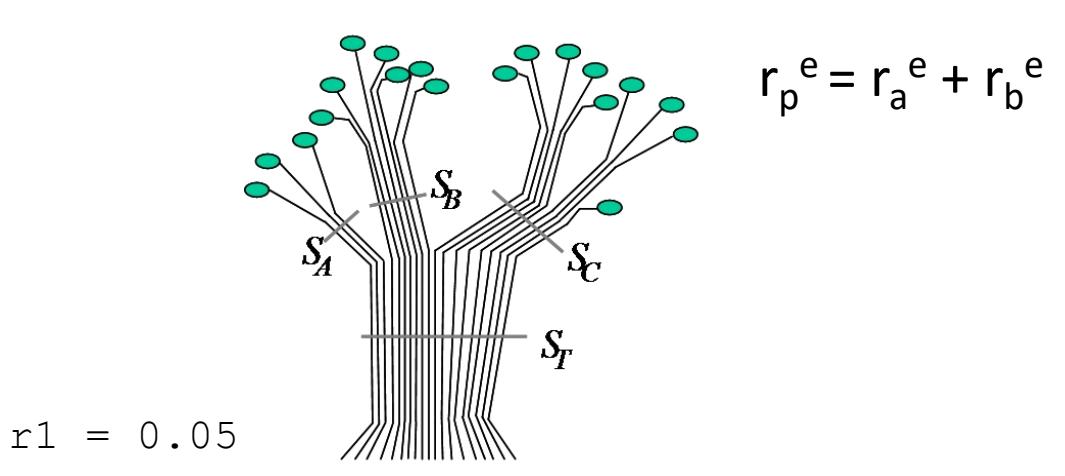
Visual result



Modelling secondary growth

Diameter of branches

- Da Vinci formula

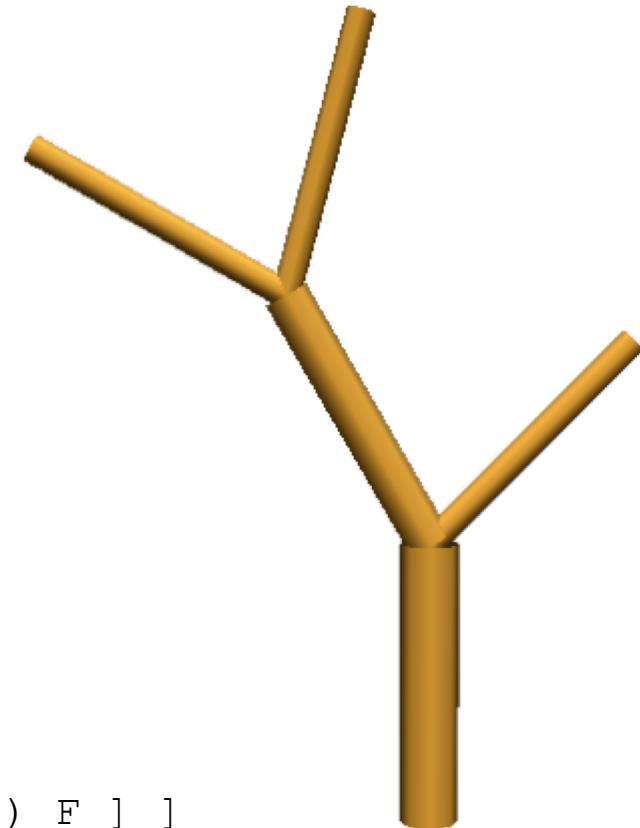


$$r_p^e = r_a^e + r_b^e$$

```
rp1 = pow(2 * pow(r1,e) + pow(r1,e), 1./e)
rp0 = pow(pow(rp1,e) + pow(r1,e), 1./e)
```

Axiom: $_{}(rp0) \ F$

```
[ +(30)  $_{}(rp1) \ F$  [ +(30)  $_{}(r1) \ F$  ] [ -(45)  $_{}(r1) \ F$  ] ]
[ -(45)  $_{}(r1) \ F$  ]
```



Diameter of branches

- Using contextual rules

`r1 = 0.05`

`e = 1.5`

backward()

```
def piperadius(ris):
    return pow(sum([pow(ri,e) for ri in ris]),1./e)
```

Axiom: $\underline{I}(r1) \ I(r1) \ [+(30)I(r1) \ [+(30)I(r1) \] \ [-(45)I(r1) \] \ [-(45)I(r1) \]$

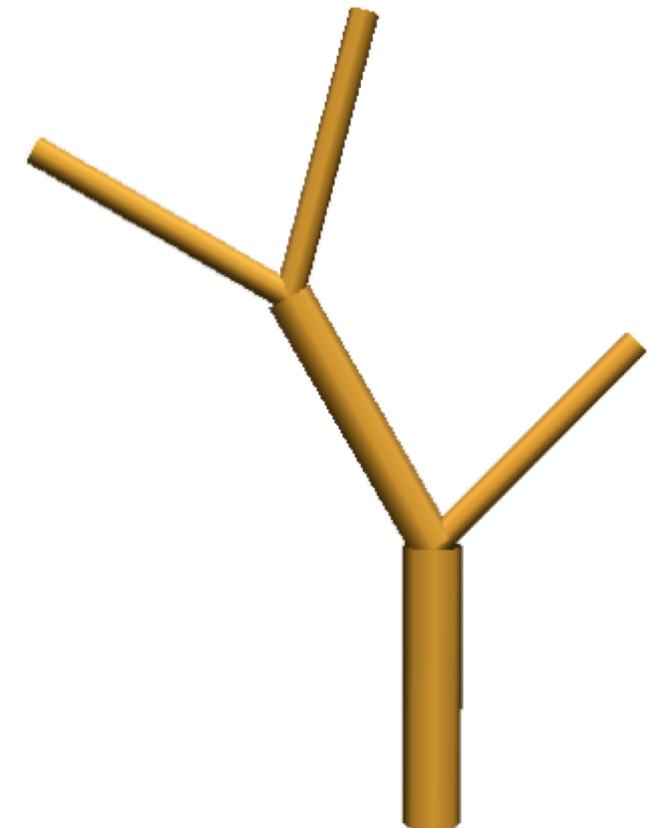
production:

ignore: +-

$I(r) \gg [I(r1) \] \ [I(r2) \] \ --> I(piperadius([r1,r2]))$

interpretation:

$I(r) \ --> \underline{I}(r) \ F$



Test the pipe model on the apple tree

- Radius is estimated directly on the number of descendants.

$$r_i = r_0 \cdot n_i^p$$

With n_i the number of descendants of internode i , r_0 the radius of the extremities and p the pipe exponent.

Exercice: Play with exponent and terminal radius on the model.

Modelling Mortality

Deletion of modules

- Rule of deletion should be explicit:

$A(t) \rightarrow *$
 $A(t) : \text{produce}$

- For an entire branching system, one can use %

$a[b\%[cd]e[\%f]]g[h[\%i]j]k \implies a[b]g[h[]j]k$

Deletion of modules

- Example

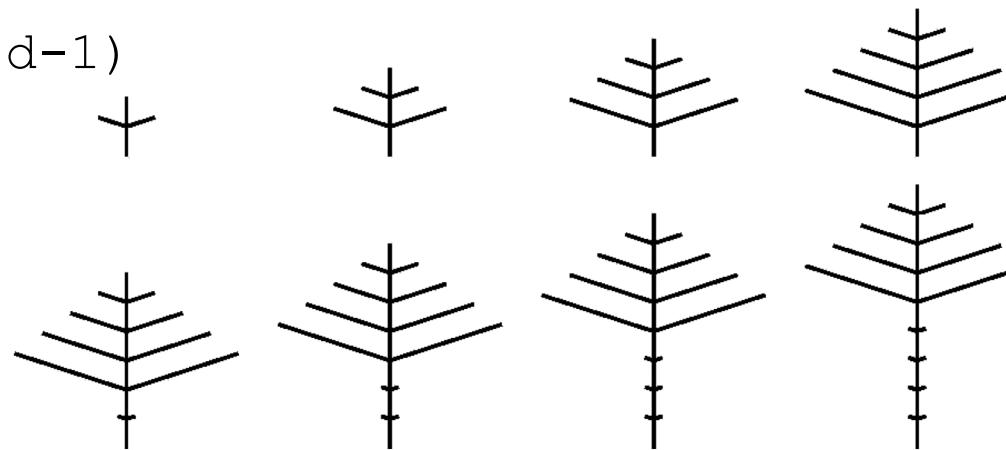
Axiom : A

A \dashrightarrow F(1) [-X(3)B] [+X(3)B] A

B \dashrightarrow F(1) B

X(0) \dashrightarrow F(0.3)%

X(d) \dashrightarrow X(d-1)



Basitonic structure with shedding



Exercise

- Into model on apple tree architecture, discuss group 3.

```
def StartEach():  
    global cdate  
    if cdate.month == 12:  
        useGroup(3)  
    else:  
        useGroup(0)
```

```
group 3:  
Leaf(p) --> %  
Fruit --> %
```

Conclusion

- Example of a step by step build of a apple tree models
 - Dependent of various processes and environmental factors
 - See next classes for more details
 - Can be adapted to other fruit trees
 - Project assignment

