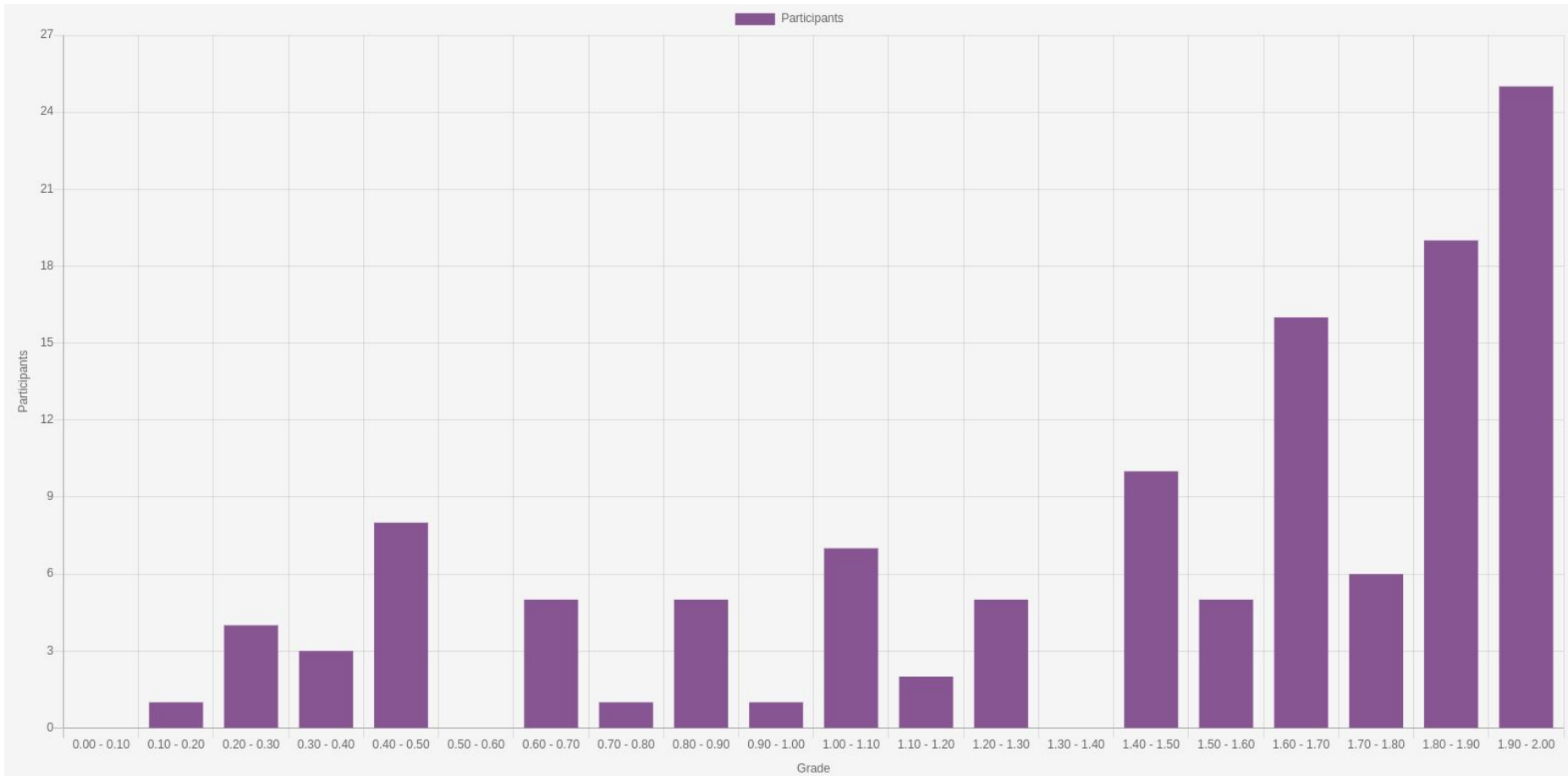


Database Technology

Exercise 7: Review



Q1: Which of the following is a valid condition rule in the grammar for simple subset of SQL?

Select all that apply. Wrong answers subtract partial points. The minimum grade is 0.

- ☐ A. `<Condition> ::= <Attribute> AVAILABLE <Pattern>`
- ☒ B. `<Condition> ::= <Condition> AND <Condition>`
- ☒ C. `<Condition> ::= <Attribute> IN (<Query>)`
- ☐ D. `<Condition> ::= <Attribute> NOT FOUND IN <Pattern>`

Q2: Is the following a valid algebraic law?

$$\sigma_{C1 \text{ AND } C2}(R) = \sigma_{C2}(\sigma_{C1}(R))$$

Assume that the relation R is a set.

True

Q3: How many tuples are selected by the selection $\sigma_{a \neq 75 \text{ AND } b=20}(R)$?

Given is the table $R(a, b)$ with the following tuple and attribute domain cardinalities:

- $T(R) = 172800$
- $V(R, a) = 80$
- $V(R, b) = 40$

Assume that:

- $1 / (3 * V(R, f))$ tuples satisfy the comparison when an attribute is equated to a constant (e.g., $\sigma_{f=15}$)
- Inequality (e.g., $\sigma_{f < 90}$) tends to retrieve one-fourth of the tuples
- For not equals (e.g., $\sigma_{f \neq 90}$), a fraction of $4 / V(R, f)$ number of the tuples will fail to meet the condition

$$\begin{aligned} \text{Total tuples} &= \text{Ceil}(T(R) * (1 - 4/V(R, \sigma_{a \neq 75})) * (1/3 * V(R, \sigma_{b=20}))) \\ &= \text{Ceil}(172800 * (1 - (4/80)) * (1/(3 * 40))) = 1368 \end{aligned}$$

Q4: How many tuples are selected by the selection $\sigma_{a \neq 19 \text{ OR } b=28}(R)$?

Given is the table $R(a, b)$ with the following tuple and attribute domain cardinalities:

- $T(R) = 37800$
- $V(R, a) = 70$
- $V(R, b) = 30$

Assume that:

- $1 / V(R, f)$ tuples satisfy the comparison when an attribute is equated to a constant (e.g., $\sigma_{f=15}$)
- Inequality (e.g., $\sigma_{f < 90}$) tends to retrieve half of the tuples
- For not equals (e.g., $\sigma_{f \neq 90}$), a fraction of $6 / V(R, f)$ number of the tuples will fail to meet the condition
- The conditions are independent

$$m1(\sigma_{a \neq 19}) = \text{Ceil}(37800 * (1 - 6/70)) = 34560$$

$$m2(\sigma_{b=28}) = \text{Ceil}(37800 * 1/30) = 1260$$

$$\begin{aligned} \text{Total tuples} &= \text{Ceil}(n * (1 - (1 - m1/n) * (1 - m2/n))) \\ &= \text{Ceil}(37800 * (1 - (1 - 34560/37800) * (1 - 1260/37800))) \\ &= 34668 \end{aligned}$$

Q5: How many tuples are selected by the join $R \bowtie_{\sigma_{s_2=51}}(S)$?

Given are the tables $R(\underline{r_1}, s_1)$ and $S(\underline{s_1}, s_2)$. $R.s_1$ is a foreign key to $S.s_1$. The tables have the following tuple and attribute domain cardinalities:

- $T(R) = 600$
- $T(S) = 400$
- $V(S, s_2) = 30$

Assume that $1 / V(R, f)$ tuples satisfy the comparison when an attribute is equated to a constant (e.g., $\sigma_{f=15}$)

R Join S = T(R) = 600 due to foreign key relationship

$$T(R) * 1 / V(S, \sigma_{s_2=51}) = 600 * 1 / 30 = 20$$

Q6: What is the estimated size of the natural join?

Consider the natural join $R(a, d) \bowtie S(d, e) \bowtie U(a, c, e)$, and the following important statistics:

$R(a, d)$	$S(d, e)$	$U(a, c, e)$
$T(R) = 1200$	$T(S) = 2400$	$T(U) = 18000$
$V(R, a) = 20$		$V(U, a) = 450$
		$V(U, c) = 450$
$V(R, d) = 40$	$V(S, d) = 20$	
	$V(S, e) = 80$	$V(U, e) = 450$

Size of $R(a, d) \bowtie S(d, e) = T(R) \cdot T(S) / \max[V(R, d), V(S, d)]$ as d is the join key
 $= 1200 \cdot 2400 / 40 = 7200$

Size of $(R(a, d) \bowtie S(d, e)) \bowtie U(a, c, e) = T(R \bowtie S) \cdot T(U) / ((\max[V(R \bowtie S, a), V(U, a)]) \cdot (\max[V(R \bowtie S, e), V(U, e)]))$
as “ a ” and “ e ” are the join keys
 $= 7200 \cdot 18000 / (450 \cdot 450) = 6400$

Q7: What is the cost of the following join order $((T \bowtie U) \bowtie R) \bowtie S$?

Consider four relations $R(c, d)$, $S(a, d)$, $T(b, c)$, and $U(a, b)$. Each relation has 1000 tuples. The relations have the following attribute domain cardinalities:

$R(c, d)$	$S(a, d)$	$T(b, c)$	$U(a, b)$
	$V(S, a) = 20$		$V(U, a) = 500$
		$V(T, b) = 40$	$V(U, b) = 20$
$V(R, c) = 50$		$V(T, c) = 100$	
$V(R, d) = 10$	$V(S, d) = 50$		

$$\begin{aligned}
 \text{Cost of } (((T(b,c) \bowtie U(a,b)) \bowtie R(c,d)) \bowtie S(a,d)) &= \text{Cost of } ((T \bowtie U) \bowtie R) + \text{Cost of } (S) \\
 &= \text{Cost of } ((T \bowtie U) \bowtie R) + 0 \\
 &= \text{Cost of intermediate } (T \bowtie U) + \text{Size of } ((T \bowtie U) \bowtie R) \\
 &= \text{Size of } (T \bowtie U) + \text{Cost}(T) + \text{Cost}(U) + \text{Size of } ((T \bowtie U) \bowtie R) \\
 &= 25000 + 0 + 0 + 250000 = 275000
 \end{aligned}$$

Size of $T(b,c) \bowtie U(a,b)$ = $1000 * 1000 / \max[V(T,b), V(U,b)]$ as b is the join key = $1000 * 1000 / 40 = 25000$

Size of $(T(b,c) \bowtie U(a,b)) \bowtie R(c,d)$ = $T(T \bowtie U) * T(R) / \max[V(T \bowtie U, c), V(R, c)]$ as " c " is the join key
 = $25000 * 1000 / 100 = 250000$

Q8: What is the size of the following join order $((S \bowtie R) \bowtie U)$?

Consider four relations $R(c, d)$, $S(a, b)$, $T(a, d)$, and $U(b, c)$. Each relation has 1000 tuples. The relations have the following attribute domain cardinalities:

$R(c, d)$	$S(a, b)$	$T(a, d)$	$U(b, c)$
	$V(S, a) = 10$	$V(T, a) = 50$	
	$V(S, b) = 250$		$V(U, b) = 50$
$V(R, c) = 100$			$V(U, c) = 200$
$V(R, d) = 100$		$V(T, d) = 10$	

Size of $S(a, b) \bowtie R(c, d) = T(S) * T(R)$ as no join key
 $= 1000000$

Size of $(S(a, b) \bowtie R(c, d)) \bowtie U(b, c) = T(S \bowtie R) * T(U) / ((\max[V(R \bowtie S, b), V(U, b)]) * (\max[V(R \bowtie S, c), V(U, c)]))$
as “a” and “c” are the join keys
 $= 1000000 * 1000 / (250 * 200) = 20000$

Q9: When determining the optimal join order, which join orders can be ignored because they contain a cross product?

Consider four relations $R(c, d)$, $S(a, b)$, $T(b, c)$, and $U(a, d)$. Each relation has 1000 tuples. The relations have the following attribute domain cardinalities:

$R(c, d)$	$S(a, b)$	$T(b, c)$	$U(a, d)$
	$V(S, a) = 250$		$V(U, a) = 20$
	$V(S, b) = 250$	$V(T, b) = 250$	
$V(R, c) = 400$		$V(T, c) = 40$	
$V(R, d) = 50$			$V(U, d) = 200$

☐ A. $(R \bowtie S) \bowtie U$

☐ B. $(R \bowtie S) \bowtie T$

☐ C. $(R \bowtie T) \bowtie S$

☐ D. $(R \bowtie U) \bowtie S$

☐ E. $(R \bowtie T) \bowtie U$

☐ F. $(S \bowtie R) \bowtie T$

Q10: From the options below, select the best join order (i.e., the one with the lowest cost):

Consider four relations $R(a, d)$, $S(b, c)$, $T(a, b)$, and $U(c, d)$. Each relation has 1000 tuples. The relations have the following attribute domain cardinalities:

$R(a, d)$	$S(b, c)$	$T(a, b)$	$U(c, d)$
$V(R, a) = 1000$		$V(T, a) = 10$	
	$V(S, b) = 200$	$V(T, b) = 200$	
	$V(S, c) = 40$		$V(U, c) = 200$
$V(R, d) = 100$			$V(U, d) = 250$

- ☐ a. $((S \bowtie U) \bowtie T) \bowtie R$
- ☐ b. $((U \bowtie T) \bowtie S) \bowtie R$
- ☐ c. $((R \bowtie U) \bowtie S) \bowtie T$
- ☒ d. $((T \bowtie R) \bowtie U) \bowtie S$

Cost of Cost of $((T \bowtie R) \bowtie U) \bowtie S$ = Cost of $((T \bowtie R) \bowtie U)$ + Cost of (S)
 = Cost of $((T \bowtie R) \bowtie U)$ + 0
 = Cost of intermediate $(T \bowtie R)$ + Size of $((T \bowtie R) \bowtie U)$
 = Size of $(T \bowtie R)$ + Cost(T) + Cost(R) + Size of $((T \bowtie R) \bowtie U)$
 = $1000 + 0 + 0 + 4000 = 5000$

Size of $T(a, b) \bowtie R(a, d) = 1000 * 1000 / \max[V(T, a), V(R, a)]$ as a is the join key
 = $1000 * 1000 / 1000 = 1000$

Size of $(T(a, b) \bowtie R(a, d)) \bowtie U(c, d) = T(T \bowtie R) * T(U) / \max[V(T \bowtie R, d), V(U, d)]$ as " d " is the join key
 = $1000 * 1000 / 250 = 4000$

Similarly,

Cost of $((S \bowtie U) \bowtie T) \bowtie R = 30000$

Cost of $((U \bowtie T) \bowtie S) \bowtie R = 1050000$

Cost of $((R \bowtie U) \bowtie S) \bowtie T = 24000$