

StateMint: A Set of Tools for Determining Symbolic Dynamic System Models Using Linear Graph Methods

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Software

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Abstract

StateMint is a set of software tools that reduce sets of dynamic equations and their constraints to a state-space model and related dynamic system model formulations. These tools are especially useful for the student of system dynamics, many of whom can become lost in this algebraic reduction. StateMint includes a Mathematica package, a Python package, and a web interface that is built as a layer on top of the Python package.

Introduction

When deriving a system's state-space model—that is, the vector state (differential) equation and the vector output (algebraic) equation—one begins by forming scalar equations for each element describing its dynamics. The next step is to form a set of N constraint equations that describe the topology of the system defined by the interconnection of the N elements. A set of $2N$ differential and algebraic equations and $2N$ unknown variables result. If properly constructed (e.g. with the linear graph technique), N of the unknown variables can be immediately eliminated through direct substitution. Finally, the set of equations can be reduced to a system of first-order differential equations in state and input variables and their time-derivatives, alone. It is in these last two steps, especially the very last, that a student, manually reducing the set of equations, will often make some minor mistake. This is typically of a “book keeping” variety that, if it teaches the student anything, it is not system dynamics. Instead, the student can be easily discouraged and confused about where they have made their mistake. Fortunately, the software tools presented here will automate the algebraic reduction. These will allow students to focus on understanding the process of dynamic system modeling.

Utilizing the advanced symbolic mathematics capabilities of Mathematica, a package was written to determine the dynamic system model. However, this requires students to install and learn (at least) the basics of Mathematica. To mitigate this problem, a web interface was designed to allow students to use this tool without any knowledge of programming by allowing equations to be input with notation similar to that of many scientific calculators. To support this interface, a Python package was written with the same functionality as the Mathematica package and is deployed as an Amazon AWS Lambda function for use by the web interface. This interface can be accessed by any device with an internet connection and a web browser.

Web Interface

The web interface (statemint.stmartin.edu) has text boxes for entering equations and variables. A special form of the constraint equations is required, as described in the [tutorial](#), based on the text of Rowell and Wormley (Rowell & Wormley, 1997). Once entered, the equations are sent to the Lambda function and the dynamic system model is returned. The results are then displayed as rendered math or source code in any of the following languages: \LaTeX , Matlab, Python, and Mathematica. Examples and documentation are built-in, allowing the user to learn the interface as they use it. The user input can be shared, downloaded, and saved for later use or modification. Because this interface utilizes Amazon AWS serverless resources, required maintenance and costs are minimized. An automated installer for independent deployment of the website is also [included](#) in the StateMint repository.

Python Package

The Python package uses the SymPy library (Meurer et al., 2017) to symbolically reduce the set of elemental and constraint equations to the state and output equations. The main function, `StateMint.Solve`, accepts the input variables, state variable elemental equations, other elemental equations, constraint equations, and output variables. This function returns an object which includes the resulting system as a state-space model and (when applicable) a transfer function. Auxiliary functions, `StateMint.to_numpy.array` and `StateMint.to_numpy.matrix` are included to convert the SymPy symbolic matrices to NumPy (Oliphant, 2015) arrays or matrices respectively. These functions accept a symbolic matrix and a dictionary mapping system parameters to numeric values. The StateMint package is documented at statemint.readthedocs.io and works for both linear and nonlinear systems.

A detailed example of how to use the Python StateMint package is [included](#) in the StateMint repository.

Mathematica Package

The Mathematica package `StateMint` can be installed as described in the [documentation](#). The central function of the package is `stateEquations`, which uses an algorithm similar to that of the Python package, above, to derive the state equations. It takes as arguments lists of elemental equations, constraint equations, primary variables, and input variables and returns the vector state equation, state variables, and the time-derivative of the state variables.

The `outputEquations` function derives the output equations given output expressions in terms of primary and secondary variables (including inputs). The function accepts lists of input variables, state variables, elemental and constraint equations, and output expressions.

The functions `stateEquations` and `outputEquations` yield what are in general *nonlinear* state and output equations. Linear state and output equations are typically written in a standard vector form described by matrices A , B , C , and D (and sometimes E and F). The `linearizeState` function accepts lists of input variables, state variables, and the time-derivatives of the state vector (from `stateEquations`) and returns the A , B , and E matrices. Similarly, `linearizeOutput` returns the C , D , and F matrices.

A detailed example of how to use the Mathematica StateMint package is [included](#) in the StateMint repository. This package is best used by those who are already familiar with Mathematica, or for more complex problems where Mathematica may perform better than SymPy.

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