

¹ MARBLES: Multi-scale Adaptively Refined Boltzmann LatticE Solver

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7 Summary

8 MARBLES is a computational fluid dynamics solver that leverages the lattice Boltzmann
9 method (LBM) and block-structured adaptive mesh refinement (AMR) to simulate flows in
10 complex media. The solver leverages the AMReX ([Zhang et al., 2019](#)) library, a library that
11 provides underlying data structures, parallel paradigms, grids, domain decomposition, and
12 portability programming models to run on massively parallel computing architectures. All major
13 GPU architectures (e.g., NVIDIA, AMD, Intel) are supported through the use of performance
14 portability functionalities implemented in AMReX. The MARBLES software is released in
15 NREL Software Record SWR-23-37 “MARBLES (Multi-scale Adaptively Refined Boltzmann
16 LatticE Solver)” ([Henry de Frahan et al., 2023](#)).

17 MARBLES implements LBM, a mesoscopic approach to computational fluid dynamics in which
18 the computation of the Boltzmann transport equation by advection and collision of fictitious
19 particles results into a solution of the Navier Stokes equation at the macroscale. The evolution
20 equation of LBM proceeds in two parts: a “streaming” step akin to space discretization in which
21 particles representing probability distribution functions at grid cells transfer information about
22 their current state to their nearest neighbors and a “collision” step akin to time discretization in
23 which these advected quantities give rise to new state variables by subsequently relaxing toward
24 their equilibrium distributions over some characteristic time. Macroscopic state variables such
25 as density, momentum and total energy are obtained by locally computing moments of the
26 probability distribution functions. In MARBLES, these steps are carried out on parallelized
27 AMReX blocks in which the phase space is discretized using 27 grid neighbors in 3D (D3Q27)
28 which provides high accuracy and slightly increased memory consumption compared to other
29 LBM stencils. An equivalent stencil is implemented for 2D simulations. The stencil can be
30 sub-divided and applied locally in a region with half the grid spacing using an implementation
31 of the explode and coalesce algorithm ([Chen et al., 2006](#)), where refined cells process two
32 time steps per every step of the parent grid assuming a factor of two grid refinement ratio.
33 This cycling between refinement levels and interpolation between grids is managed by AMReX
34 functionality and minimizes communication between parallel blocks to enable excellent scaling
35 performance.

36 MARBLES uses the Embedded Boundary (EB) formulation in AMReX to represent complex
37 geometries. In this approach, an arbitrary surface is defined by the user, using either composi-
38 tions of simple shapes or an STL file. This is used to intersect the Cartesian mesh and define
39 cells that are covered by the geometry (i.e., inside the body). Bounce back conditions are
40 imposed on these surfaces as part of the streaming step to capture the effect of the geometry
41 on the fluid flow. This leads to a very robust handling of very complex geometry, including
42 flow through porous media.

43 MARBLES is written in C++ and uses an MPI+X approach: the AMR grid patches are

⁴⁴ distributed on different CPU ranks using MPI. Each grid can be either (i) logically tiled and
⁴⁵ solved on different threads on a multi-core CPU machine using OpenMP, or (ii) solved on
⁴⁶ GPU threads on GPU nodes using CUDA, HIP, and SYCL.

⁴⁷ Statement of Need

⁴⁸ Several software tools that implement the Lattice Boltzmann method can found online, including
⁴⁹ a PyTorch based solver, Lettuce ([Bedrunka et al., n.d.](#)), the commonly used OpenLB ([Krause](#)
⁵⁰ [et al., 2021](#)), Palabos ([Latt et al., 2021](#)), waLBerla ([Bauer et al., 2021; Godenschwager et al.,](#)
⁵¹ [2013](#)), and others ([Mora et al., 2020; Pastewka & Greiner, 2019; Schmieschek et al., 2017](#)).

⁵² In contrast with these solvers, MARBLES is the only code to the authors' knowledge to be built
⁵³ on AMReX data structures which allows us to tackle exascale problems and take advantage
⁵⁴ of both CPU and GPU hardware with little change to the underlying code. Because of this,
⁵⁵ MARBLES is easily extensible to other capabilities and has the potential to perform well on
⁵⁶ emerging architectures. MARBLES, through its use of vendor-agnostic programming models
⁵⁷ implemented in AMReX, achieves high performance from a small desktop station to the world's
⁵⁸ largest supercomputer. Additionally, AMReX provides tools to naturally track regions of the
⁵⁹ fluid in need of refinement (e.g., around an evolving fluid-vapor interface or near the surface
⁶⁰ of a deforming solid obstacle) and communicate variables between grid refinement levels in a
⁶¹ highly performant manner.

⁶² MARBLE's unique features consist in implementing the two-population compressible thermal
⁶³ LBM ([Sawant et al., 2022](#)) in a highly scalable and performance portable framework. The LBM
⁶⁴ formulation implemented in MARBLES uses one lattice for mass and momentum equations and
⁶⁵ another lattice for the energy equation, keeping the whole solver within the lattice Boltzmann
⁶⁶ framework without the need for a hybrid discretization approach. A fully lattice Boltzmann
⁶⁷ framework combines exact conservation as in finite volume solvers with the flexibility of a
⁶⁸ structured grid like in immersed boundary finite difference solvers, without their respective
⁶⁹ drawbacks of grid generation and conservation errors, respectively. Using a nearest-neighbor
⁷⁰ based correction to equilibrium pressure, the model maintains Galilean invariance up to third
⁷¹ order in velocity space, sufficient to faithfully simulate the correct viscosity and thermal
⁷² diffusivity over a wide range of temperatures, while still using the standard D3Q27 lattice.

⁷³ MARBLES is intended for students, researchers and engineers interested in simulating mesoscale
⁷⁴ and macroscale flows with the Lattice Boltzmann method on modern high performance
⁷⁵ computing hardware. With performance portability and being vendor agnostic foremost
⁷⁶ considerations in the design of the code, MARBLES can leverage the computational resources
⁷⁷ available on the latest heterogeneous exascale platforms, including GPUs. In this context,
⁷⁸ MARBLES is a valuable tool for studying fluid dynamics and heat transfer scientific and
⁷⁹ engineering problems involving complex geometries. Its applications include flows in porous
⁸⁰ media such as electrodes and geological microstructures, aerodynamic calculations such as
⁸¹ forces on turbines blades and structures subject to external flows, and non-equilibrium flows
⁸² such as those involved in semiconductor manufacturing.

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