

k-diagram: Rethinking Forecasting Uncertainty via

- ² Polar-based Visualization
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Summary

k-diagram is an open-source Python package designed for the in-depth interpretation and diagnosis of probabilistic forecasts. Moving beyond traditional aggregate metrics, the package provides a suite of novel visualization tools, primarily based on polar coordinate systems, to dissect the complex spatiotemporal structure of forecast uncertainty and errors. By mapping statistical properties such as sharpness, reliability, and temporal stability onto intuitive geometric representations, k-diagram enables researchers and practitioners to identify model biases, understand forecast degradation over time, and communicate uncertainty characteristics more effectively. The package is designed to be a practical extension to the standard forecasting workflow, providing the visual evidence needed for more robust model evaluation and trustworthy, context-aware decision-making.

Statement of Need

The evaluation of probabilistic forecasts has a rigorous theoretical foundation based on concepts of calibration and sharpness, which are jointly assessed using proper scoring rules (Gneiting et al., 2007). However, these scores are typically aggregated into a single value, which can obscure vital information about a model's performance in heterogeneous spatiotemporal settings. This is a critical limitation, as modern machine learning models, such as Temporal Fusion Transformers (Lim et al., 2021), are increasingly applied to complex, high-dimensional problems where understanding the local and temporal behavior of uncertainty is paramount. A growing body of applied research highlights this challenge in fields as diverse as predictive policing (Rummens & Hardyns, 2021), energy forecasting (Y. Liu et al., 2021), chaotic market dynamics (Caulk et al., 2022), climatology (Baillie & Chung, 2002) and geohazard (J. Liu et al., 2024).

While an ecosystem of open-source forecasting tools exists, many focus on specific modeling or post-processing tasks, such as forecast reconciliation (Biswas et al., 2025), or provide verification suites for specific domains like climate science (Brady & Spring, 2021). General-purpose libraries like matplotlib (Hunter, 2007) and seaborn (Waskom, 2021) provide the building blocks but lack dedicated functions for the specialized diagnostics needed for high-dimensional uncertainty. Even established visualizations like fan charts, which have seen recent innovations (Sokol, 2025), are primarily designed for single time series and do not scale well to problems involving thousands of simultaneous forecasts (Hong et al., 2025). This creates a critical gap between the generation of complex probabilistic forecasts and the ability to interpret them effectively.

40 k-diagram addresses this gap by providing a scalable and intuitive toolkit designed specifically
41 for the visual diagnosis of spatiotemporal probabilistic forecasts (Kouadio, 2025; J. Liu et al.,



2024). The package's novelty lies in its use of polar coordinates to map different dimensions of forecast performance, such as uncertainty magnitude, reliability, and temporal stability, onto angle and radius. This approach provides compact overviews that reveal patterns obscured in traditional Cartesian plots. By providing clear visual answers to key diagnostic questions (e.g., "Where is a forecast least certain?", "How is its uncertainty evolving?"), k-diagram serves as an essential tool for any researcher or practitioner seeking to move beyond aggregate metrics and gain a deeper, more actionable understanding of their forecasting models.

Functionality

k-diagram is implemented in Python (Python Software Foundation, 2008; Van Rossum & Drake, 2009), leveraging core scientific libraries including numpy (Harris et al., 2020), pandas (McKinney, 2010; Reback et al., 2020), matplotlib (Hunter, 2007), scipy (Virtanen et al., 2020), and scikit-learn (Pedregosa et al., 2011). The core functionality is organized around a cohesive API designed to diagnose key aspects of forecast quality through four primary pillars of analysis (see Figure 1).

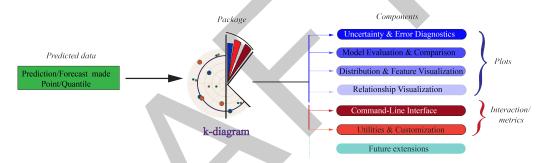


Figure 1: Structure of the k-diagram, illustrating the identification of global components.

The first and primary contribution of k-diagram is a suite of novel polar visualizations for Uncertainty and Error Diagnostics (Kouadio, 2025). The kdiagram.plot.uncertainty, kdiagram.plot.errors, and kdiagram.plot.probabilistic modules provide a comprehensive toolkit for dissecting forecast performance. This includes functions to evaluate prediction interval performance by visualizing coverage, the magnitude of anomalous failures, and the temporal consistency of interval widths. Furthermore, the library introduces innovative methods for visualizing error distributions, such as polar error bands to separate systemic bias from random error, and polar violins, a novel adaptation of the traditional violin plot (Hintze & Nelson, 1998), to compare the full error profiles of multiple models. For a complete assessment of the predictive distribution, a dedicated suite of probabilistic diagnostics offers Polar PIT Histograms for calibration, Sharpness Diagrams for precision, and Continuous Ranked Probability Score (CRPS) plots for overall skill, based on the foundational concepts of probabilistic forecasting (Gneiting et al., 2007).

Building on this, the second pillar focuses on established methods for **Model Evaluation and**Comparison. The package implements well-regarded evaluation techniques, adapting them for
enhanced clarity. Functions in kdiagram.plot.evaluation generate **Taylor Diagrams**, based
on the original formulation by (Taylor, 2001), to holistically compare models on correlation,
standard deviation, and RMSD. Complementing this, the kdiagram.plot.comparison module
provides standard **Reliability Diagrams** for assessing probability calibration, a cornerstone of
forecast verification (Jolliffe & Stephenson, 2012).

The third pillar of functionality addresses **Distribution and Feature Visualization**. k-diagram provides utilities for plotting 1D distributions and Kernel Density Estimates (KDEs) (Silverman, 1986) in both Cartesian and innovative polar ring formats. To facilitate model interpretability,



- the kdiagram.plot.feature_based module offers radar charts to visualize and compare feature importance profiles, creating unique model "fingerprints".
- Finally, the package provides tools for **Relationship Visualization**, where polar plots in kdiagram.plot.relationship offer a novel perspective on the correlation between true and predicted values by mapping them to angle and radius. All functionalities are supported by a set of helper utilities and a command-line interface (CLI) for generating key plots directly from data files. The entire package is designed for ease of use, allowing users to control plot aesthetics, angular coverage (acov), and color mapping to tailor the visualizations for their specific domain.

Illustrative Diagnostics and Application

- The practical utility of k-diagram is best demonstrated through its key diagnostic plots, which are grounded in clear statistical concepts and reveal model behaviors often hidden by aggregate metrics (see Figure 2).
- For instance, the **Coverage Evaluation** plot in Figure 2a provides a point-wise diagnostic of interval performance. For each observation y_i and its corresponding prediction interval $[L_i, U_i]$, a binary coverage value c_i is determined as:

$$c_i = \mathbf{1}(L_i \le y_i \le U_i)$$

- where $\mathbf{1}(\cdot)$ is the indicator function. The plot visualizes each c_i , allowing for a granular analysis of where interval failures occur. The average of these outcomes provides the overall empirical coverage, which at 81.1% is close to the nominal 80% for the Q10-Q90 interval shown.
- The Model Error Distributions diagram (Figure 2b) offers a comparative view by visualizing the full error distribution for multiple models. It uses polar violins, where the shape of each violin is determined by the Kernel Density Estimate (KDE) of the model's errors (Silverman, 1986). The resulting diagram clearly distinguishes a "Good Model" (unbiased and narrow) from a "Biased Model" (shifted from the zero-error line) and an "Inconsistent Model" (wide and dispersed), revealing performance trade-offs that a single error score would miss.
- Finally, the **Forecast Horizon Drift** diagram (Figure 2c) visualizes how uncertainty evolves over time. For each forecast horizon j, it calculates the mean interval width, \bar{w}_j , across all N spatial locations as:

$$\bar{w}_j = \frac{1}{N} \sum_{i=1}^{N} \left(U_{i,j} - L_{i,j} \right)$$

The increasing height of the bars from 2023 to 2026 provides an immediate and intuitive confirmation that the model's uncertainty grows as it forecasts further into the future.



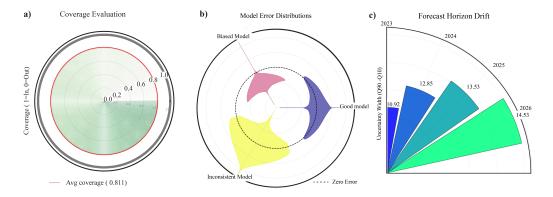


Figure 2: Model performance evaluation. (a) Coverage Evaluation: radial plot comparing empirical coverage against nominal quantile levels (average coverage = 0.811). (b) Model Error Distributions: The radial axis represents the error value, with the dashed circle indicating zero error. The width of each violin shows the density of errors, revealing that the "Good Model" is unbiased and consistent, the "Biased Model" consistently under-predicts, and the "Inconsistent Model" has high variance. (c) Forecast Horizon Drift: radial bar chart of uncertainty width (Q90–Q10) for forecast years 2023–2026, illustrating increasing prediction uncertainty.

These visualization methods were developed alongside research applying advanced deep learning models, such as physics-informed deep learning, to complex environmental forecasting challenges. Specifically, these polar diagnostics were utilized to analyze and interpret the uncertainty associated with land subsidence predictions using an Extreme Temporal Fusion Transformer model (Kouadio et al., 2025) in Nansha city, China.

Full usage examples and a gallery of all plot types are available in the official documentation's gallery section. For a deeper understanding of the mathematical concepts and interpretation guides, please refer to the detailed User Guide. The complete mathematical foundations and derivations for all visualizations are provided in the official Technical Report (Kouadio, 2025).

118 Availability and Community

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The latest stable release of k-diagram is available on the Python Package Index (PyPI) and can be installed via pip install k-diagram. The package is distributed under the OSI-approved Apache License 2.0. Comprehensive documentation, including a user guide, an example gallery, and a detailed API reference, is hosted at https://k-diagram.readthedocs.io/. I welcome contributions from the community; bug reports, feature requests, and development discussions occur on the GitHub repository. Detailed guidelines for contributors can be found in the documentation.

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¹For an overview of the concepts behind Physics-Informed Neural Networks (PINNs), see: https://fusion-lab.readthedocs.io/en/latest/user_guide/models/pinn/index.html



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