

PyWavelets: A Python package for wavelet analysis

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DOI: [10.21105/joss.01134](https://doi.org/10.21105/joss.01134)

Software

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Submitted: 18 December 2018

Published: 18 December 2018

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Summary

Wavelets are a popular tool for computational harmonic analysis. They provide localization in both the temporal (or spatial) domain as well as in the frequency domain. A prominent feature is the ability to perform a multiresolution analysis. The wavelet transforms of natural signals and images tends to have most of their energy concentrated in a small fraction of the coefficients. This sparse representation property is key to the good performance of wavelets in applications such as data compression and denoising. For example, the wavelet transform is a key component of the JPEG 2000 image compression standard.

PyWavelets is a Python package implementing a number of n -dimensional discrete wavelet transforms as well as the 1D continuous wavelet transform. A wide variety of predefined wavelets are provided and it is possible for users to specify custom wavelet filter banks. All discrete wavelet transforms are implemented by convolution with finite impulse response filters. The required up/downsampling convolutions are implemented in C for good performance. Cython (Behnel et al., 2011) is used to wrap the C code and implement axis-specific 1D transformations based on the low-level C routines. All multi-dimensional transforms are implemented in Python via separable application of the 1D transforms. The API for **PyWavelets** was designed to be similar to Matlab’s wavelet toolbox and functions such as the 1D, 2D and 3D discrete wavelet transforms are tested for accuracy vs. their Matlab counterparts. **PyWavelets** has additional functionality not common in other wavelet toolboxes such as support for dimension $n > 3$ and support for both real and complex-valued data in either single or double precision. It is also possible to transform only a subset of axes and to vary the wavelet and signal boundary extension mode on a per-axis basis.

PyWavelets was designed for use by scientists working within a range of applications including time-series analysis, signal processing, image processing and medical imaging. It has already been adopted as a required or optional dependency by a number of other software projects. For example, it has enabled wavelet-based image denoising in scikit-image (Walt et al., 2014). The Operator Discretization Library (ODL) (Adler et al., 2018) uses **PyWavelets** to enable wavelet-based regularization in iterative inverse problems such as computed tomography image reconstruction. A number of common 1D demo signals used in the literature and in the manuscript by Stephan Mallat (???) are provided for use in teaching and for purposes of reproducible research. The source code for **PyWavelets** has been archived to Zenodo with the linked DOI: (Lee et al., 2018).

Acknowledgements

We would to acknowledge the various PyWavelets contributors for their contributions to the library, and specifically Holger Nahrstaedt for contributing a continuous wavelet transform.

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