pyBEMT: An implementation of the Blade Element Momentum Theory in Python

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Summary

The use of rotating blades to generate thrust in the form of propellers or torque in the form of turbines is of great significance for transportation and energy generation. This has led to extensive research and development of mathematical models to better understand, predict and optimize the performance of these machines. The blade element momentum theory (BEMT) is one such method with a long history dating back to Glauert (1935).

Despite the development of more sophisticated methods, such as vortex methods (Gohard, 1978), the blade element momentum theory is still considered relevant for the study of rotor design. Its simple formulation lends itself to use in education and to quickly analyse new ideas. As examples of recent uses of BEMT, it was used by Herniczek, Jee, Sanders, & Feszty (2019) to compare airfoils and blade shapes for an unmanned rotorcraft and by Borg, Xiao, Allsop, Incecik, & Peyrard (2020), together with computational fluid dynamics, to analyze the performance of a high-solidity tidal turbine design. Several open-source packages include an implementation of BEMT, for instance the `AeroDyn` (Moriarty & Hansen, 2005) solver used in the whole-turbine simulation software `OpenFAST`("OpenFAST," 2020), and the `QBlade` (Marten, Wendler, Pechlivanoglou, Nayeri, & Paschereit, 2013) software for wind turbine blade design. `QBlade` has later been forked to develop `JBLADE` (Silvestre, Morgado, & Pascoa, 2013), a software focusing on propeller design.

`pyBEMT` is unique in that it offers a unified implementation of the blade element momentum theory, supporting both propellers and turbines. This is of particular interest in education, to demonstrate the similarities between these two domains. The software is designed as a stand-alone Python implementation with emphasis on readability and extensibility. Its modular design and permissive license also makes it suitable for integration into other simulation tools. Other notable features of the package are a model for coaxial rotors and optimization of rotor parameters using the differential evolution algorithm in `SciPy`. The use of coaxial rotor systems has recently seen renewed interest with the growth in unmanned aerial vehicles and autonomous systems.

Figure 1 shows two examples of predictions from the model for a tidal stream turbine (Bahaj, Molland, Chaplin, & Batten, 2007) and an airplane propeller (Theodorsen, Stickle, & Brevoort, 1937), respectively. `pyBEMT` is currently applied in research projects on rotor design for unmanned aerial vehicles and turbine design for tidal stream turbines, as well as used in education within fluid dynamics and computational engineering.
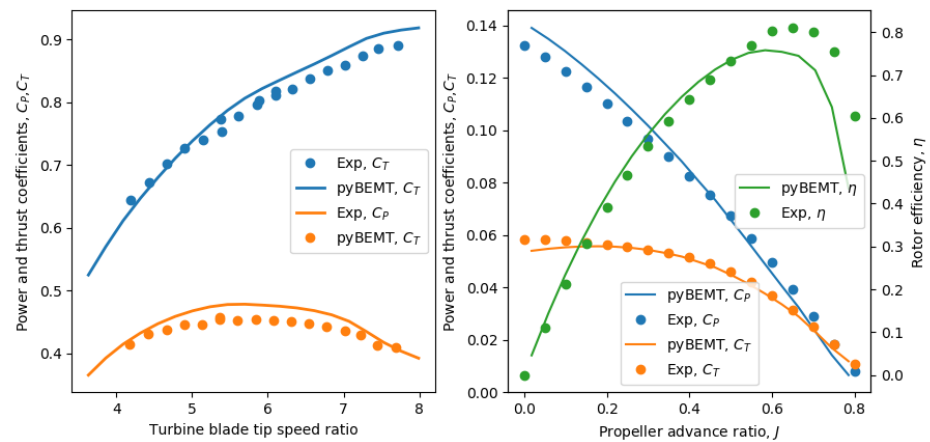
Figure 1: `pyBEMT` applied to a tidal stream turbine (left) and an airplane propeller (right).

Acknowledgements

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