

¹ dynLattice: A finite element environment for dynamic simulation of beam networks and lattice metamaterials

³ **Til Gärtner**  ^{1,2,3} and **Frans P. van der Meer**  ¹

⁴ 1 Delft University of Technology, The Netherlands  ² Netherlands Organisation for Applied Scientific Research, The Netherlands  ⁵ 3 Leibniz University Hannover, Germany 

DOI: [10.xxxxxx/draft](https://doi.org/10.xxxxxx/draft)

Software

- [Review](#) 
- [Repository](#) 
- [Archive](#) 

Editor: Mojtaba Barzegari  ¹⁰

Submitted: 15 September 2025 ¹²

Published: unpublished ¹³

License

Authors of papers retain copyright and release the work under a Creative Commons Attribution 4.0 International License ([CC BY 4.0](#)). ¹⁵ ¹⁶ ¹⁷ ¹⁸

⁶ Summary

Beams and beam structures undergoing fast deformation often experience large strains and inelastic material behaviour. Understanding this behaviour enables engineers and designers to design beam networks resulting in so-called mechanical metamaterials. Metamaterials offer unique properties not found in naturally occurring materials. Harnessing these properties presents new possibilities for a wide range of fields (Davies et al., 2025; Jiao et al., 2023). In order to enable engineers to design mechanical metamaterials, the relation between the geometry of the beam network and the resulting properties needs to be understood. For large deformations at high rates, this usually requires destructive testing, limiting the speed of developments. This limitation can be overcome using efficient numerical tools, allowing for both the accurate and fast description of the inelastic deformation at high rates (Bonfanti et al., 2024).

¹⁸ Background

¹⁹ The following is a short description of the beam kinematics and cross-sectional kinetics implemented in this software, with a more detailed description given in (Gärtner, 2025). ²⁰

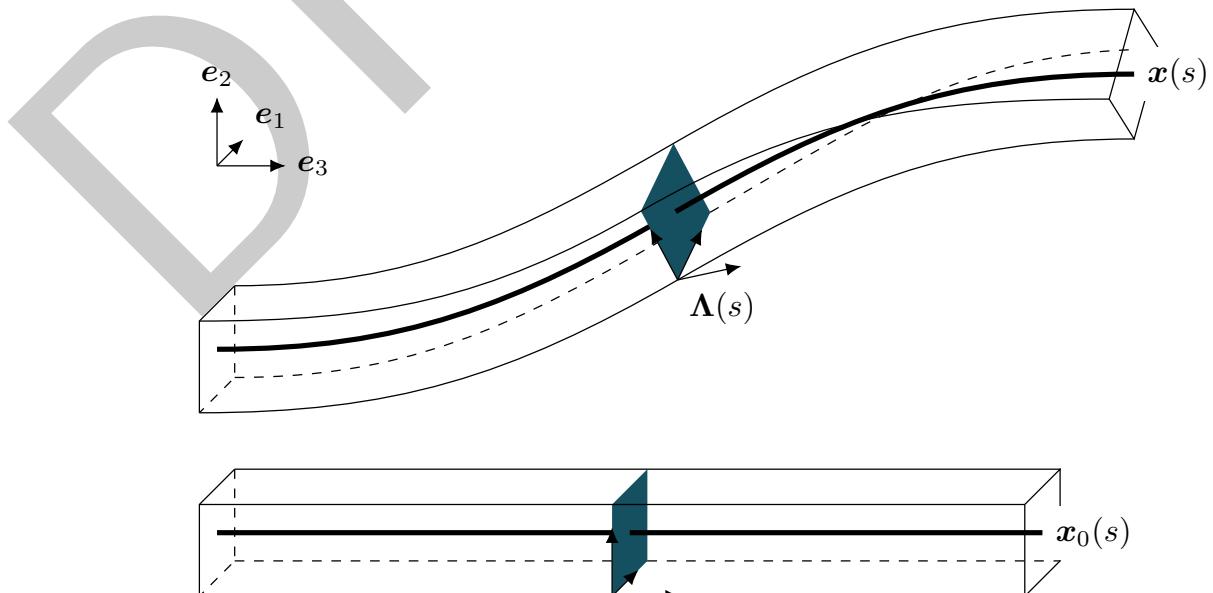


Figure 1: A beam undergoing large deformation.

21 In [Figure 1](#), a beam undergoing large deformation is shown. A beam is described with the
 22 centerline $\mathbf{x}(s)$, where $s \in [s_0, s_1]$ is the measure along the length of the beam, with two
 23 orthonormal directors attached to it $\mathbf{d}_1(s), \mathbf{d}_2(s)$. Together with a third orthonormal director
 24 $\mathbf{d}_3(s) = \mathbf{d}_1(s) \times \mathbf{d}_2(s)$, these are the column vectors of the rotation matrix between the global
 25 reference frame and the local coordinate frame of the beam:

$$\Lambda(s) = \mathbf{d}_i(s) \otimes \mathbf{e}_i = [\mathbf{d}_1(s) \quad \mathbf{d}_2(s) \quad \mathbf{d}_3(s)].$$

26 From these measures, strain prescriptors, describing stretching, shearing, bending, and twisting
 27 of the beam can be derived. These strain prescriptors are then used together with the material
 28 model of the beam, be it elastic (cf. ([Eugster, 2015](#); [Simo & Vu-Quoc, 1986](#))) or elasto-plastic
 29 (cf. ([Gärtner, van den Boom, et al., 2025a](#); [Herrnböck et al., 2022](#); [Smriti et al., 2021](#))), to
 30 assemble the global force vector and—in the static, implicit case—the tangent stiffness matrix
 31 using standard finite element procedures.

32 Statement of need

33 Research on the dynamic behaviour of mechanical metamaterials, especially beam lattices,
 34 relies on numerical tools that can capture large deformations, inelastic behaviour, and contact
 35 while remaining efficient and flexible enough for parameter studies ([Bonfanti et al., 2024](#)).
 36 General-purpose finite element frameworks, e.g. ([Dadvand et al., 2010](#); [Ferrández et al., 2025](#);
 37 [Richart et al., 2024](#)), provide broad capabilities but often lack a complete combination of
 38 non-linear Timoshenko-Ehrenfest beam formulations, robust explicit time integration, and
 39 inelastic constitutive behaviour. Here, a specialized lattice framework, e.g. ([McDonnell & Ning,](#)
 40 [2022](#)), typically delivers high-fidelity beam kinematics but only focuses on elastic deformations
 41 or omits contact between the constituting beams of the lattice. Resulting from this, many
 42 researchers rely on their own implementation of Simo-Reissner beams, which are usually not
 43 available to the community and only consider a subset of the requirements needed for a general
 44 toolkit. An open and extensible environment that unifies geometrically exact beams, explicit
 45 dynamics, inelasticity, and contact is therefore central to advancing simulation-driven design
 46 of lattice metamaterials for high-rate and large deformation applications. Here, dynLattice
 47 takes a first step by building upon the JIVE framework ([Dynaflow Research Group, 2021](#);
 48 [Nguyen-Thanh et al., 2020](#)), keeping the extensible object-oriented design philosophy, and
 49 providing extensive documentation in the style of the underlying framework.

50 State of the field

51 There is a wide plethora of existing finite element toolkits available in the market, such as
 52 MOOSE ([Lindsay et al., 2022](#)), FEniCS ([Baratta et al., 2023](#)), or deal.II ([Arndt et al., 2023](#)),
 53 to name several prominent ones. The usage of these libraries for explicit dynamics with inelastic
 54 beams however, would require substantial alteration of their code, as for example in FEniCS
 55 explicit dynamics is only available using lumped mass matrices, which would be non-physical for
 56 the rotational inertia contributions of the beams, in deal.II neither beam elements nor explicit
 57 solves are available and in MOOSE only a limited Timoshenko-Ehrenfest beam is implemented
 58 with only elastic behaviour. Other finite element toolkits having built in beam-elements and
 59 explicit dynamics include Kratos ([Dadvand et al., 2010](#); [Ferrández et al., 2025](#)) and Akantu
 60 ([Richart et al., 2024](#)). For Kratos similar problems as for MOOSE can be seen in only a
 61 limited set of beam elements being available and none supporting inelastic behaviour in the
 62 cross-sectional strain measures. Akantu, focusing on fracture mechanics and providing a solid
 63 representation of contact, on the other hand only provides Euler-Bernoulli beam elements,
 64 neglecting all shear deformation within the elements. Next to general finite element toolkits,
 65 there are specialized beam toolkits, most prominently for shear-deformable beams, GXBeam
 66 ([McDonnell & Ning, 2022](#)). Here, the same beam theory employed in this contribution is used,
 67 however due to its focus on composite beams, it is limited to (anisotropic) elastic material
 68 behaviour and does not model contact.

69 Software design

70 In order to design metamaterials undergoing large deformations at high rates, dynLattice
71 provides both researchers and engineers in the field a toolkit for numerical experiments.
72 dynLattice is built on top of the openly available C++ JIVE finite element toolkit ([Dynaflow](#)
73 [Research Group, 2021](#); [Nguyen-Thanh et al., 2020](#)) and follows in its design the object-
74 oriented framework of JIVE to describe the partial differential equations and corresponding
75 solution procedures. The toolkit allows for the implementation of original methods through the
76 development of custom *modules*, for parts of the program flow in the simulation framework,
77 and of custom *models*, for anything related to the numerical representation of the system
78 of partial differential equations. In the present addition to the JIVE framework, the *models*
79 further contain a separate *materials* class, representing the constitutive models considered in
80 the problem, separating geometric from material considerations. This separation allows both
81 the easy and user-friendly extension of the frameworks by simple inheritance of the provided
82 classes as well as usability by structuring the inputs needed for the program flow and the
83 problem description. dynLattice additionally uses GMSH ([Geuzaine & Remacle, 2009](#)) to mesh
84 the imported geometries efficiently.

85 Research impact statement

86 dynLattice has enabled a series of research efforts investigating lattice metamaterials Gärtner
87 ([2025](#)). In addition to investigating lattice materials, it has been used to study the behaviour
88 of beams as a multi-scale problem ([Gärtner, van den Boom, et al., 2025a](#)) and has undergone
89 a thorough comparison with experimental data and results from commercial tools ([Gärtner,](#)
90 [Dekker, et al., 2025](#)). Collaborating researchers could easily install and run the software using
91 the provided documentation and apptainer.

92 In addition to external collaboration, dynLattice was also used as a ready-made software
93 package by multiple student theses ([IJzendoorn, 2024](#); [Niessen, 2022](#); [Smit, 2024](#)). During
94 these projects, dynLattice was used on a large cluster ([\(DHPC\), 2024](#)) and on various local
95 machines using the provided apptainer. This demonstrates its availability and usability as
96 stand-alone software without the need for further modifications.

97 Changes to the source code that enable further research are made possible by the object-oriented
98 philosophy inherited from the JIVE package and the clear structure of the code into *modules*,
99 *models* and *materials*, as described in [Software design](#). The provided documentation, available
100 in the source and on the [project website](#), facilitates quick and straightforward adoption by
101 third parties. The included benchmarks serve as a verification tool for the correctness of the
102 implementation and as a guide for creating and extending simple problems.

103 AI Usage Disclosure

104 During the creation of this software, GitHub Copilot (using different versions of Claude Sonnet)
105 was used to enhance the documentation of the source code. In particular, it helped streamline
106 all documentation efforts into Doxygen compatible comments. All generated documentation
107 strings were read and approved by the author.

108 Acknowledgements

109 The research of Til Gärtner is financed by TNO through the PhD program of the Dutch
110 Ministry of Defence.

111 References

- 112 Arndt, D., Bangerth, W., Bergbauer, M., Feder, M., Fehling, M., Heinz, J., Heister, T., Heltai,
 113 L., Kronbichler, M., Maier, M., Munch, P., Pelteret, J.-P., Turcksin, B., Wells, D., &
 114 Zampini, S. (2023). The deal.II library, version 9.5. *J. Numer. Math.*, 31(3), 231–246.
 115 <https://doi.org/10.1515/jnma-2023-0089>
- 116 Baratta, I. A., Dean, J. P., Dokken, J. S., Habera, M., Hale, J. S., Richardson, C. N., Rognes,
 117 M. E., Scroggs, M. W., Sime, N., & Wells, G. N. (2023). *DOLFINx: The next generation
 118 FEniCS problem solving environment*. Zenodo. <https://doi.org/10.5281/zenodo.10447666>
- 119 Bonfanti, S., Hiemer, S., Zulkarnain, R., Guerra, R., Zaizer, M., & Zapperi, S. (2024).
 120 Computational design of mechanical metamaterials. *Nat. Comput. Sci.*, 4(8), 574–583.
 121 <https://doi.org/10.1038/s43588-024-00672-x>
- 122 Dadvand, P., Rossi, R., & Oñate, E. (2010). An object-oriented environment for developing
 123 finite element codes for multi-disciplinary applications. *Arch. Comput. Methods Eng.*,
 124 17(3), 253–297. <https://doi.org/10.1007/s11831-010-9045-2>
- 125 Davies, B., Szyniszewski, S., Dias, M. A., Waal, L. de, Kisil, A., P Smyshlyaev, V., Cooper, S.,
 126 Kamotski, I. V., Touboul, M., Craster, R. V., Capers, J. R., Horsley, S. A. R., Hewson, R.
 127 W., Santer, M., Murphy, R., Thillaithovan, D., Berry, S. J., Conduit, G. J., Earnshaw, J.,
 128 ... Zadpoor, A. (2025). Roadmap on metamaterial theory, modelling and design. *J. Phys.
 129 D: Appl. Phys.*, 58(20). <https://doi.org/10.1088/1361-6463/adc271>
- 130 (DHPC), Delft High Performance Computing Centre. (2024). *DelftBlue Supercomputer (Phase
 131 2)*. <https://www.tudelft.nl/dhpc/ark:/44463/DelftBluePhase2>.
- 132 Dynaflow Research Group. (2021). *JIVE* (Version 3.0). <https://dynaflow.com/software/jive/>
- 133 Eugster, S. R. (2015). *Geometric continuum mechanics and induced beam theories*. Springer.
 134 <https://doi.org/10.1007/978-3-319-16495-3>
- 135 Ferrández, V. M., Bucher, P., Zorrilla, R., Warnakulasuriya, S., Cornejo, A., Rossi, R., Roig,
 136 C., jcotela, Maria, J., tteschemacher, Masó, M., Casas, G., Núñez, M., Dadvand, P.,
 137 Latorre, S., Pouplana, I. D., González, J. I., Afranci, Arrufat, F., ... jgonzalezusua. (2025).
 138 *KratosMultiphysics/kratos: v10.2.3* (Version v10.2.3). Zenodo. <https://doi.org/10.5281/zenodo.15687676>
- 139
- 140 Gärtner, T. (2025). *Are auxetics better for protection? On the behaviour of architected
 141 metamaterials under high-rate loading conditions* [PhD Thesis, Technische Universiteit
 142 Delft]. <https://doi.org/10.4233/uuid:9d0b230e-1008-46a2-a193-b9dd3f8c472f>
- 143 Gärtner, T., Dekker, R., van Veen, D., van den Boom, S. J., & Amaral, L. (2025). (In)efficacy
 144 of auxetic metamaterials for impact mitigation. *Int. J. Impact Eng.*, 206. <https://doi.org/10.1016/j.ijimpeng.2025.105402>
- 145
- 146 Gärtner, T., van den Boom, S. J., Weerheijm, J., & Sluys, L. J. (2024). Geometric effects
 147 on impact mitigation in architected auxetic metamaterials. *Mech. Mater.*, 191. <https://doi.org/10.1016/j.mechmat.2024.104952>
- 148
- 149 Gärtner, T., van den Boom, S. J., Weerheijm, J., & Sluys, L. J. (2025a). A strategy for scaling
 150 the hardening behavior in finite element modelling of geometrically exact beams. *Comput.
 151 Mech.*, 75, 1471–1482. <https://doi.org/10.1007/s00466-024-02572-3>
- 152
- 153 Gärtner, T., van den Boom, S. J., Weerheijm, J., & Sluys, L. J. (2025b). Force transmission
 154 and dissipation in dynamic compression of architected metamaterials. *Materials Today
 155 Advances*, 28. <https://doi.org/10.1016/j.mtadv.2025.100656>
- 156
- 157 Geuzaine, C., & Remacle, J.-F. (2009). Gmsh: A 3-D finite element mesh generator with built-in
 158 pre- and post-processing facilities. *Int. J. Numer. Methods Eng.*, 79(11), 1309–1331.
<https://doi.org/10.1002/nme.2579>

- 158 Herrnböck, L., Kumar, A., & Steinmann, P. (2022). Two-scale off-and online approaches to
159 geometrically exact elastoplastic rods. *Comput. Mech.*, 71(1), 1–24. <https://doi.org/10.1007/s00466-022-02204-8>
- 160
- 161 IJzendoorn, P. van. (2024). *Multiscale modelling of lattice materials: A novel approach using*
162 *beam neural networks* [MSc Thesis, Technische Universiteit Delft]. <http://resolver.tudelft.nl/uuid:682795a0-108e-4f8f-a084-884445081d38>
- 163
- 164 Jiao, P., Mueller, J., Raney, J. R., Zheng, X. R., & Alavi, A. H. (2023). Mechanical
165 metamaterials and beyond. *Nat. Commun.*, 14(1). <https://doi.org/10.1038/s41467-023-41679-8>
- 166
- 167 Lindsay, A. D., Gaston, D. R., Permann, C. J., Miller, J. M., Andrš, D., Slaughter, A. E.,
168 Kong, F., Hansel, J., Carlsen, R. W., Icenhour, C., Harbour, L., Giudicelli, G. L., Stogner,
169 R. H., German, P., Badger, J., Biswas, S., Chapuis, L., Green, C., Hales, J., ... Wong, C.
170 (2022). 2.0 - MOOSE: Enabling massively parallel multiphysics simulation. *SoftwareX*, 20.
171 <https://doi.org/10.1016/j.softx.2022.101202>
- 172 McDonnell, T., & Ning, A. (2022). GXBeam: A pure julia implementation of geometrically
173 exact beam theory. *Journal of Open Source Software*, 7(73), 3997. <https://doi.org/10.21105/joss.03997>
- 174
- 175 Nguyen-Thanh, C., Nguyen, V. P., de Vaucorbeil, A., Kanti Mandal, T., & Wu, J.-Y. (2020).
176 Jive: An open source, research-oriented C++ library for solving partial differential equations.
177 *Adv. Eng. Softw.*, 150. <https://doi.org/10.1016/j.advengsoft.2020.102925>
- 178
- 179 Niessen, A. (2022). *GNNs and beam dynamics: Investigation into the application of graph*
180 *neural networks to predict the dynamic behaviour of lattice beams* [MSc Thesis, Technische
Universiteit Delft]. <http://resolver.tudelft.nl/uuid:b1cad9d4-48e9-4e6e-8760-5aabc3d8bd9f>
- 181
- 182 Richart, N., Anciaux, G., Gallyamov, E., Frérot, L., Kammer, D., Pundir, M., Vocialta, M.,
183 Ramos, A. C., Corrado, M., Müller, P., Barras, F., Zhang, S., Ferry, R., Durussel, S., &
184 Molinari, J.-F. (2024). Akantu: An HPC finite-element library for contact and dynamic
fracture simulations. *J. Open Source Softw.*, 9(94). <https://doi.org/10.21105/joss.05253>
- 185
- 186 Simo, J. C., & Vu-Quoc, L. (1986). A three-dimensional finite-strain rod model. Part II:
187 Computational aspects. *Comput. Methods Appl. Mech. Eng.*, 58(1), 79–116. [https://doi.org/10.1016/0045-7825\(86\)90079-4](https://doi.org/10.1016/0045-7825(86)90079-4)
- 188
- 189 Smit, J. (2024). *Stiffness of architected materials* [BSc Thesis]. Technische Universiteit Delft.
- 190
- 191 Smriti, Kumar, A., & Steinmann, P. (2021). A finite element formulation for a direct approach
to elastoplasticity in special cosserat rods. *Int. J. Numer. Methods Eng.*, 122(3), 657–692.
<https://doi.org/10.1002/nme.6566>