# survPen: an **R** package for hazard and excess hazard modelling with multidimensional penalized splines

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Background

In survival and net survival analysis, in addition to modelling the effect of time (via the baseline hazard), one has often to deal with several continuous covariates and model their functional forms, their time-dependent effects, and their interactions. Model specification becomes therefore a complex problem and penalized regression splines (Ruppert, Wand, & Carroll, 2003; Wood, 2017) represent an appealing solution to that problem as splines offer the required flexibility while penalization limits overfitting issues.

Current implementations of penalized survival models can be slow or unstable and sometimes lack some key features like taking into account expected mortality to provide net survival and excess hazard estimates. In contrast, based on the framework and algorithms developed by Wood, survPen provides an automated, fast, and stable implementation (thanks to explicit calculation of the derivatives of the likelihood) and offers a unified framework for multidimensional penalized hazard and excess hazard models.

In epidemiology, as patients may die from their disease or from other causes, it is relevant to study the mortality due to their disease; also called "excess mortality". This excess mortality is useful to make comparisons between different countries and time periods (Allemani et al., 2018; Uhry et al., 2017) and is directly linked to the concept of net survival which is another important indicator in epidemiology (Perme, Stare, & Estève, 2012).

Summary

survPen is an implementation of multidimensional penalized hazard and excess hazard models for time-to-event data in **R** (R Core Team, 2018). It implements the method detailed in Fauvernier et al. (2019) which is itself included in the framework for general smooth models proposed by Wood, Pya, & Säfken (2016). Other **R** packages propose to fit flexible survival models via penalized regression splines (rstpm2, bamlss, R2BayesX, etc). However, the way they estimate the smoothing parameters is not optimal as they rely on either derivative-free optimization (rstpm2) or MCMC (bamlss, R2BayesX), leading to possibly unstable or time-consuming analyses. The main objective of the survPen package is to offer a fully automatic, fast, stable and convergent procedure in order to model simultaneously non-proportional, non-linear effects of covariates and interactions between them. A second objective is to extend the approach to excess hazard modelling (J. Estève, Benhamou, Croasdale, & Raymond, 1990; L. Remontet, Bossard, Belot, Estève, & French Network of Cancer Registries, 2007). survPen is a free and open-source **R** package, available via GitHub at https:

//github.com/fauvernierma/survPen or via the CRAN repository at https://CRAN.R-project.
org/package=survPen. The major features of `survPen` are documented in a walkthrough
vignette that is included with the package (https://htmlpreview.github.io/?https://github.
com/fauvernierma/survPen/blob/master/inst/doc/survival_analysis_with_survPen.html)

Those features include:

- Univariate penalized splines for the baseline hazard as well as any other continuous covariate.
- Penalized tensor product splines for time-dependent effects and interactions between several continuous covariates.
- Interactions between penalized splines and unpenalized continuous or categorical variables.
- Automatic smoothing parameter estimation by either optimizing the Laplace approximate marginal likelihood (LAML (Wood et al., 2016)) or likelihood cross-validation criterion (LCV (O'Sullivan, 1988)).
- Excess hazard modelling by specifying expected mortality rates.

`survPen` may be of interest to those who 1) analyse any kind of time-to-event data: mortality, disease relapse, machinery breakdown, unemployment, etc 2) wish to describe the associated hazard and to understand which predictors impact its dynamics.

Using the `survPen` package for time-to-event data analyses will help choose the appropriate degree of complexity in survival and net survival contexts while simplifying the model building process.

Multidimensional splines with `survPen` are currently being used in three major ongoing projects:

- Modelling the effects of time since diagnosis, age at diagnosis and year of diagnosis on the mortality due to cancer using French cancer registries data (FRANCIM network, around 1,200,000 tumours diagnosed between 1989 and 2015). This study will provide the new national estimates of cancer survival in France and its results will be used in the evaluation of the French "Plan Cancer" at the end of 2019.
- Modelling the effect of the European Deprivation Index (EDI) on the mortality due to cancer in France, using data from the FRANCIM network; this is the first time that EDI is available in all FRANCIM registries (around 210,000 tumours, diagnosed between 2006 and 2009 in 18 registries).
- For the first time modelling the effects of time since onset, age at onset, current age, year of onset and sex on the mortality due to multiple sclerosis in the biggest cohort of multiple sclerosis patients in France (37,524 patients diagnosed over the period 1960-2014 in 18 OFSEP centres).

Acknowledgements

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