

Odisseo: A Differentiable N-body Code for Gradient-Informed Galactic Dynamics

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Software

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Background

N-body simulations, which model the interactions within a system of particles, are a fundamental tool in computational physics with widespread applications [e.g. planetary science, stellar cluster dynamics, cosmology, molecular dynamics]. While Odisseo (Optimized Differentiable Integrator for Stellar Systems Evolution of Orbits) can be used in any context where an N-body simulation is useful, a key motivating application in galactic astrophysics is the study of stellar streams. Stellar streams are the fossilized remnants of dwarf galaxies and globular clusters that have been tidally disrupted by the gravitational potential of their host galaxy. These structures, observed as coherent filaments of stars in the Milky Way and other nearby galaxies, are powerful probes of astrophysics. Their morphology and kinematics encode detailed information about the host galaxy's gravitational field, making them ideal for mapping its shape. Furthermore, studying the properties of streams and their progenitors is key to unraveling the hierarchical assembly history of galaxies.

The standard workflow has involved running computationally expensive simulations, comparing their projected outputs to observational data via summary statistics, and then using statistical methods like MCMC to explore the vast parameter spaces. While successful, this approaches looses information by compressing rich datasets into simple statistics, and struggles with the high-dimensional parameter spaces required by increasingly complex models. With Odisseo we aim to explore how the new paradigm of differentiable simulations and automatic-differentiation can be adopted to challenge many-body problems.

5 Statement of Need

Inspired by the work of (Alvey et al., 2024) and (Nibauer et al., 2024) on stellar stream differentiable simulators, with Odisseo we intend to offer a general purpose, highly modular, direct N-body simulator package that can be used for detail inference pipeline by taking advantage of the full information present in the phase-space. The main goal is to explore the joint posterior distribution of progenitor and external potential parameters in the context of galactic dynamics. As demonstrated by recent developments, a promising path for inverse modeling techniques lies in leveraging differentiable programming and modern simulation-based inference (SBI) techniques (Holzschuh & Thuerey, 2024).

- By providing a fully differentiable N-body simulator built on JAX (Bradbury et al., 2018),
 Odisseo directly addresses the key bottlenecks of the standard inference pipeline (MCMC). Its
 differentiability allows for the direct use of simulation gradients to guide parameter inference,
 enabling a move from inefficient parameter searches to highly efficient, gradient-informed
 methods.
- 41 Odisseo is designed with open-source, community-driven development in mind, providing a



- robust and accessible foundation that can be extended with new physics models and numerical methods.
- 4 Odisseo Overview

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- Odisseo is a Python package written in a purely functional style to integrate seamlessly with the JAX ecosystem. Its design philosophy is to provide a simple, flexible, and powerful tool for inference-focused N-body simulations. Key features include:
 - End-to-End Differentiable: The entire simulation pipeline is differentiable. The final state
 of the particles is differentiable with respect to the initial parameters, including initial
 conditions, total time of integration, particle masses, and parameters of the external
 potentials.
 - Modularity and Extensibility: The code is highly modular. The functional design allows for individual components —such as integrators, external potentials, or initial condition generators— to be easily swapped or extended by the user. This facilitates rapid prototyping and model testing.
 - JAX Native and Cross-Platform: Built entirely on JAX, Odisseo enables end-to-end Just In Time (JIT) compilation for high performance (jax.jit), automatic vectorization (jax.vmap) for trivial parallelization, and automatic differentiation (jax.grad). This ensures high performance across diverse hardware, including CPUs, GPUs, and TPUs.
 - External Potentials: Odisseo allows for the inclusion of arbitrary external potentials.
 This is essential for realistically modeling the tidal disruption of satellite systems in a Milky Way-like environment. It can be trivially generalized to physical settings where external potentials are important (e.g. molecular dynamics).
 - Direct acceleration: The pairwise particle forces are exact, down to a softening length that is used to avoid numerical errors.
 - Unit Conversion: The conversion between physical and simulation units is handled with a simple CodeUnits class that wraps around astropy functionality (Astropy Collaboration et al., 2022).

Running a simulation

- Four main components are needed to run a simulation :
 - Configuration: it handles the shapes of the arrays in the simulations (e.g. number of particles, number of time steps) and all the components for which recompilation would be required if changed.
- Parameters: it contains the physical parameters with respect to which we can differentiate through the time stepping.
- Initial conditions: the initial state of the simulation, it contains the positions and velocities of all the particles. The masses are a separate array with the same length of initial conditions.
- Time integration: the main function that perform the evolution of the particles state.
- Examples on how to set up different problems are presented in the documentation.

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