

# mpi4py-fft: Parallel Fast Fourier Transforms with MPI for Python

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#### **Software**

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## Summary

The fast Fourier transform (FFT) is an algorithm that efficiently computes the discrete Fourier transform. Since the dawn of our digital society, the FFT has permeated to the heart of everyday life applications involving audio, image, and video processing. The importance of the FFT extends beyond signal processing into scientific computing because it diagonalizes the Poisson operator, which is ubiquitous in descriptions of electromagnetism, gravitation, acoustic and elastic waves, potential flow in fluids, stress in solids, Hamiltonians of the Schroedinger's equation for probability distribution of electrons in quantum mechanics, and diffusion of internal energy, chemical species, and momentum. The FFT has been named the most important numerical algorithm of our time by Professor Gilbert Strang (Strang, 1994).

mpi4py-fft (https://bitbucket.org/mpi4py/mpi4py-fft) is an open-source Python package for computing (in parallel) FFTs of possibly very large and distributed multidimensional arrays. A multidimensional FFT is computed in sequence, over all axes, one axis at the time. In order to fit in the memory of multiple processors, multidimensional arrays have to be distributed along some, but not all, of its axes. Consequently, parallel FFTs are computed with successive sequential (serial) transforms over undivided axes, combined with global array redistributions (using interprocess communication) that realign the arrays for further serial transforms.

For global redistributions, mpi4py-fft makes use of a new and completely generic algorithm (Dalcin, Mortensen, & Keyes, 2019) based on advanced MPI features that allows for any index sets of a multidimensional array to be distributed. It can distribute a single index set (slab decomposition), two index sets (pencil decomposition), or even more for higher-dimensional arrays. The required MPI communications are always handled under the hood by MPI for Python (Dalcin, Paz, Storti, & D'Elia, 2008). For serial FFT transforms, mpi4py-fft uses Cython (Behnel et al., 2011) to wrap most of the FFTW library (Frigo & Johnson, 2005) and provide support for complex-to-complex, real-to-complex, complex-to-real and real-to-real transforms.

mpi4py-fft is highly configurable in how it distributes and redistributes arrays. Large arrays may be globally redistributed for alignment along any given axis, whenever needed by the user. This flexibility has enabled the development of shenfun (Mortensen, 2018, Mortensen (2017)), which is a Python framework for solving partial differential equations (PDEs) by the spectral Galerkin method. shenfun is able to solve PDEs of any given dimensionality by creating tensor product bases as outer products of one-dimensional bases. This leads to large multidimensional arrays that are distributed effortlessly through mpi4py-fft. Throughout the spectralDNS (https://github.com/



spectralDNS/spectralDNS) project shenfun is being used extensively for Direct Numerical Simulations (DNS) of turbulent flows (Mortensen & Langtangen, 2016, Mortensen (2016), Ketcheson, Mortensen, Parsani, & Schilling (2019)), using arrays with billions of unknowns.

mpi4py-fft provides a flexible distributed NumPy array interface, which allows for further reuse in applications beyond the FFT. The distribution requires at least one undivided axis, but apart from that there are no restrictions nor limitations. The interface can simply be used to boost performance of global array operations through MPI.

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