




svFSI: A Multiphysics Package for Integrated Cardiac Modeling

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Summary

Heart disease is the number one cause of death in the US ([Xu et al., 2020](#)). Many efforts have been devoted to studying its progression, diagnosis, and treatment. During the past decade, computational modeling has made significant inroads into the research of heart disease. The heart is inherently a multiphysics system that includes electrophysiology, tissue mechanics, and blood dynamics. Its normal function starts with the propagation of electrical signals that trigger the active contraction of the heart muscle to pump blood into the circulatory system. Rooted in fundamental laws of physics such as the balance of mass, momentum, and energy, computational modeling has been instrumental in studying cardiac physiology such as left ventricular function ([Mittal et al., 2015](#)), cardiac arrhythmia ([Trayanova, 2011](#)), and blood flow in the cardiovascular system ([Arzani & Shadden, 2018](#); [Grande Gutiérrez et al., 2021](#)). svFSI is the first open source software that specializes in enabling coupled electro-mechano-hemodynamic simulations of the heart.

Statement of need

Accompanying the growing popularity of studying cardiac physiology with computational modeling, many open source software tools that specialize in modeling one or two aspects of the multiphysics process in the heart have been developed. For example, SimVascular ([Updegrave et al., 2017](#)) enables patient-specific blood flow modeling by providing a complete pipeline from medical image segmentation to simulation results. FEBio ([Maas et al., 2012](#)) specializes in modeling large-deformation structure mechanics in biophysics with fluid-structure interaction (FSI) capability as well. openCARP ([Plank et al., 2021](#)) focuses on modeling cardiac electrophysiology. There are other general-purpose open source software such as LifeV ([Bertagna et al., 2017](#)) and FEniCS ([Logg et al., 2012](#)), that can be flexibly adapted to simulate different physics in the heart, but significant development effort may be required for this purpose. Recently, Quarteroni et al. have also been developing an open source simulator for the cardiac function, and the fiber generation module ([Africa et al., 2022](#)) and electromechanics ([Fedele et al., 2022](#)) have been announced so far.

svFSI is a new multiphysics finite element solver designed specifically for computational modeling of integrative heart dynamics. As the next generation finite element solver for the SimVascular software, svFSI is capable of modeling hemodynamics, performing large-deformation FSI to capture the motion of cardiac chambers and their interaction with the blood flow, and simulating the complex excitation-contraction coupling between the intracellular ion-exchange processes and tissue contraction. To suit the diverse needs of users, our team

has implemented non-Newtonian blood viscosity models, fiber-reinforced nonlinear hyperelastic material models, and both phenomenological and biophysics-based cellular activation models. svFSI is also capable of resolving the inherent multi-scale phenomena in cardiac physiology such as the interaction between Purkinje fibers and cardiac muscle, and setting up closed-loop multi-scale hemodynamic simulations with physiological boundary conditions. Moreover, it is worth emphasizing that svFSI is fully compatible with SimVascular, and thus can take advantage of the existing pipeline for medical image segmentation, anatomic model construction, meshing, boundary condition prescription, etc. svFSI is written in Fortran, taking advantage of the object-oriented programming features of Fortran 2003. It is capable of parallel simulation using MPI. It also provides several built-in iterative linear solvers and preconditioners, along with many other options through Trilinos (Heroux et al., 2005). The code is highly modularized for ease of interoperability and extension. We acknowledge the limited open source compiler support for Fortran on Windows systems, and there is an ongoing effort to convert svFSI into pure C++ software.

Software architecture

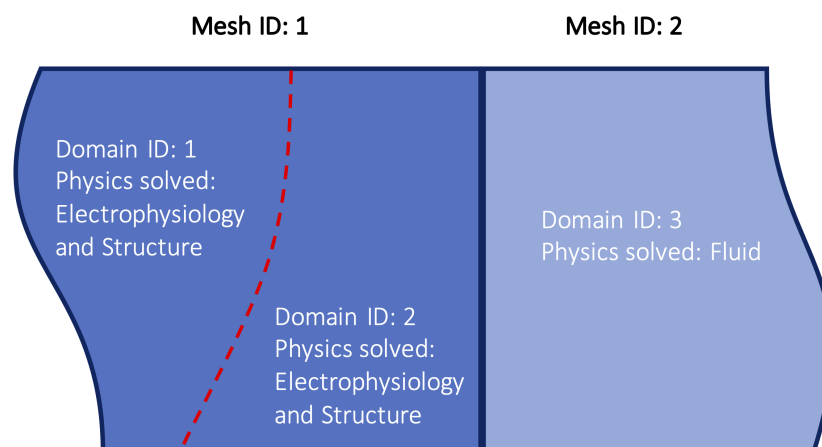


Figure 1: Illustration of a multi-mesh, multi-domain simulation configuration.

The svFSI solver defines a modeling task through three key components (objects): mesh, domain, and equation. A mesh defines a spatial discretization of the physical regions such as the Purkinje network, myocardium, or the blood volume. It can be divided into non-overlapping domains through unique domain IDs. Different physical equations, such as the Navier-Stokes (fluid) equation and the structural mechanics (struct) equation are solved on each domain with domain-specific material properties. Figure 1 illustrates how these three objects are utilized in the multiphysics modeling of cardiac mechanics. The whole computational model is composed of two meshes. Mesh 1 represents the ventricular myocardium, where both electrophysiology and nonlinear solid mechanics equations are solved. Given the material heterogeneity of the myocardium, mesh 1 can be further divided into multiple domains so that domain-specific material properties, such as electrical conductivity and material elasticity, can be assigned. Mesh 2 is the fluid region where only the Navier-Stokes equations are solved.

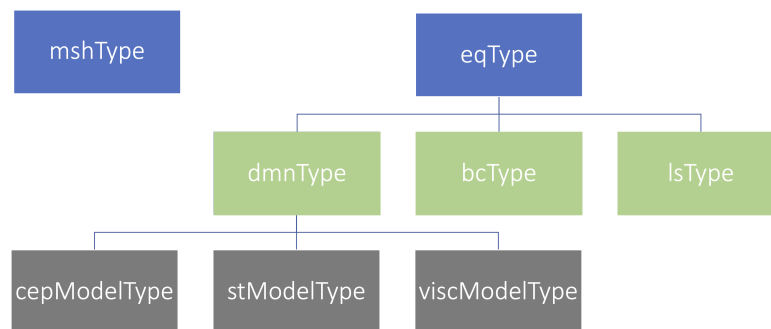


Figure 2: Class hierarchy that constitutes a simulation. Description of each class is provided in [Table 1](#).

This highly flexible, multi-mesh, and multi-domain modeling capability is realized in svFSI through the class hierarchy depicted in [Figure 2](#). The three key components, i.e. mesh, domain, and equation, correspond to classes `mshType`, `dmnType` and `eqType`, respectively. The material heterogeneity for electrophysiology, tissue mechanics or hemodynamics within each domain is defined through `cepModelType`, `stModelType` or `viscModelType` (see [Table 1](#)). Two other important classes, `bcType` and `lsType`, are also shown in [Figure 2](#). They define the boundary conditions and settings for the linear solver that are essential to generating a well-posed simulation configuration.

Class name	Description
<code>mshType</code>	Defines properties of the mesh, such as the element type, number of nodes per element, and coordinates.
<code>eqType</code>	Defines properties of the equation, such as the physics (fluid/struct/electrophysiology), domains, linear solvers, and boundary conditions.
<code>dmnType</code>	Defines properties of the domain, such as the physics (fluid/structure/electrophysiology), material properties, stabilization parameters, etc.
<code>bcType</code>	Defines properties of the boundary conditions, such as Dirichlet or Neumann, time dependence, spatial profile, etc.
<code>lsType</code>	Defines properties of linear solvers.
<code>cepModelType</code>	Defines properties of the electrophysiology model
<code>stModelType</code>	Defines properties of the structure material model
<code>viscModelType</code>	Defines properties of the viscosity model for fluids

Table 1: Main classes defined in svFSI.

Full documentation for svFSI functionality is available from the SimVascular website at <http://simvascular.github.io>.

Conclusion

svFSI is a multiphysics finite-element solver focusing on whole heart modeling and consists of modules that can efficiently simulate hemodynamics, cardiac mechanics, cardiac electrophysiology as well as the multiphysical interactions among them. svFSI has been used to generate several publications ([Bäumler et al., 2020](#); [Kong & Shadden, 2020](#); [Seo, Schiavazzi, et al., 2020](#); [Seo, Fleeter, et al., 2020](#); [Vedula et al., 2017](#)) and is employed in several active projects. We will continue to support and develop the software. New features such as methods to

simulate heart valves, vascular growth and remodeling are currently under development. The software is envisioned to be applicable to a wide range of research questions in both pediatric and adult cardiovascular disease.

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