

Fortuna.jl: Structural and System Reliability Analysis in Julia

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Summary

In any field of engineering, addressing uncertainties is crucial to ensure the adequate reliability - the ability to function without failure – of structures and systems, such as residential and commercial buildings, bridges, nuclear power plants, energy distribution networks, transportation networks, and even electric circuits. In these systems, uncertainties are ubiquitous and present in their geometric and material properties, the demands acting on them, and the measurements used to assess their condition. Moreover, uncertainties can also be present in the probabilistic models used to quantify them. As a result of the irreducibility of some of these uncertainties, it is impossible to guarantee the absolute reliability and serviceability of a system at any given point in time with certainty. However, it is possible to define and quantify measures of reliability, such as the failure probability of a system under given demands, using probabilistic methods developed within the field of structural and system reliability.

Fortuna.jl is an open-source general-purpose package for structural and system reliability analysis purely written in the Julia programming language (Bezanson et al., 2017). It implements a wide suite of commonly used reliability analysis methods to solve reliability, inverse reliability, and sensitivity problems. Fortuna.jl leverages Julia's high-performance capabilities to efficiently solve even the most challenging reliability problems. At the same time, Fortuna.jl is designed to be user-friendly and flexible, making it suitable for both research and teaching settings. It is intended that Fortuna.jl can serve as a platform for the development and implementation of new rapidly emerging reliability analysis methods.

Statement of Need

Due to the largely numerical nature of almost all reliability analysis methods, which often require computation of gradient vectors and Hessian matrices, the use of computational resources is necessary for all but the most trivial problems. As a result, a large number of both open-source and commercial software packages have been developed in different programming languages over the past 30 years, such as UQpy (Python) (Olivier et al., 2020), Pystra (Python), FERUM (MATLAB) (Bourinet et al., 2009), and Calrel (FORTRAN) (Der Kiureghian et al., 2006).

The development of Fortuna.jl was mainly motivated by the absence of packages for structural and system reliability analysis written in Julia. Additionally, it aimed to achieve an improved balance between user experience, ease of implementing new reliability analysis methods, computational efficiency, and interoperability with external finite element (FE) modeling software not directly available through Julia.

A key distinguishing feature of Fortuna.jl is that it is capable of performing differentiation of the limit state function, which defines the failure criterion for a given reliability problem, required by most reliability analysis methods using automatic differentiation techniques provided



by ForwardDiff.jl package (Revels et al., 2016), significantly speeding up the analysis process. This contrasts with other software packages for structural and system reliability analysis, which typically rely on variants of finite difference approximations. As it was mentioned before, Fortuna.jl also allows users to easily define limit state functions using external FE modeling software, such as Abaqus, OpenSees (McKenna et al., 2010), and SAFIR (Franssen & Gernay, 2017). Fortuna.jl can also easily work with surrogate models of limit state functions that are computationally expensive to evaluate, such as when a limit state function is defined in terms of a complex FE model, using the functionality provided by Surrogates.jl package (Bessi et al., 2024). Lastly, Fortuna.jl's ability to work with random variables is based on a widely adopted Distributions.jl package (Besançon et al., 2021), enabling seamless integration with other software packages for probabilistic analysis written in Julia, such as Copulas.jl (Laverny & Jimenez, 2024), RxInter.jl (Bagaev et al., 2023), and Turing.jl (Ge et al., 2018), which provide all the functionality needed for the development and implementation of more modern reliability analysis methods based on Bayesian inference.

Fortuna.jl has already been successfully used to compare the levels of safety achieved by the Allowable Strength Design (ASD) and Load and Resistance Factor Design (LRFD) methods, two design frameworks used to design individual component in structures (Akchurin et al., 2024; Sabelli et al., 2024). Fortuna.jl is also being actively used to develop and implement a next-generation design framework that can account for and optimize system behavior in the design of steel structures, which cannot be achieved using the current methods such as the ASD and LRFD.

Example

Consider a simple reliability problem from Echard et al. (2013) with the limit state function given by

$$g(U_1,U_2) = \frac{1}{2}(U_1-2)^2 - \frac{3}{2}(U_2-5)^3 - 3, \tag{1}$$

where U_1 and U_2 are two independent standard normal random variables. The failure domain defined by this limit state function is shown in Figure 1. The reference geometric reliability index β and failure probability P_f obtained using the first-order reliability method (FORM) are 3.93 and 4.21×10^{-5} , respectively. These results can be easily recreated using Fortuna.jl:

```
# Preamble:
using Fortuna
```

As shown in the code above, the results obtained using Fortuna.jl are consistent with the reference values.



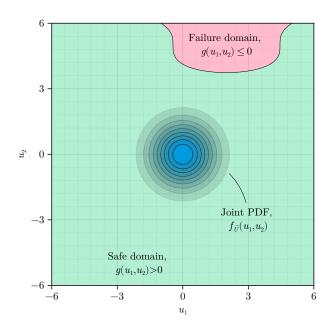


Figure 1: Failure domain defined by the limit state function in Equation 1^1 .

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¹The figure is created using Makie.jl package (Danisch & Krumbiegel, 2021).



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