catwoman: A transit modelling Python package for asymmetric light curves

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Summary

When exoplanets pass in front of their stars from our point of view on Earth, they imprint a transit signature on the stellar light curve which, to date, has been assumed to be symmetric in time, owing to the planet being modelled as a circular area occulting the stellar surface (Kreidberg, 2015; Luger et al., 2019; see, e.g., Mandel & Agol, 2002). However this signature might be asymmetric due to several possible effects, one of which is the different temperature/pressure and/or chemical compositions the different terminator regions a transiting planet could have (see, e.g., Powell et al., 2019). Being able to model these asymmetric signatures directly from transit light curves could give us an unprecedented glimpse into planetary 3-dimensional structure, helping constrain models of atmospheric evolution, structure and composition.

`catwoman` is a Python package that models these asymmetric transit light curves, calculating light curves for any radially symmetric stellar limb darkening law and where planets are modelled as two semi-circles, of different radii, using the integration algorithm developed in (Kreidberg, 2015) and implemented in the `batman` library, from which `catwoman` builds upon. It is fast and efficient and open source with full documentation available to view at https://catwoman.readthedocs.io .

The light curves are modelled as follows: The decrease in flux, δ, as a planet transits its star can be approximated by the sum

$$\delta = \sum_{i=1}^{N} I\left(x_m\right) \Delta A(x_m, R_{p,1}, R_{p,2}, \varphi, d), \tag{1}$$

splitting the semi-circles into iso-intensity bands centred on the star and for each intersectional segment (see Figure 1) you multiply its area, ΔA, by the intensity of the star and then sum these strips to generate the full δ for a specific separation between the centre of the star and planet, d. The code then increments d by a small pre-determined amount (based on the time array given by the user) and recalculates δ.
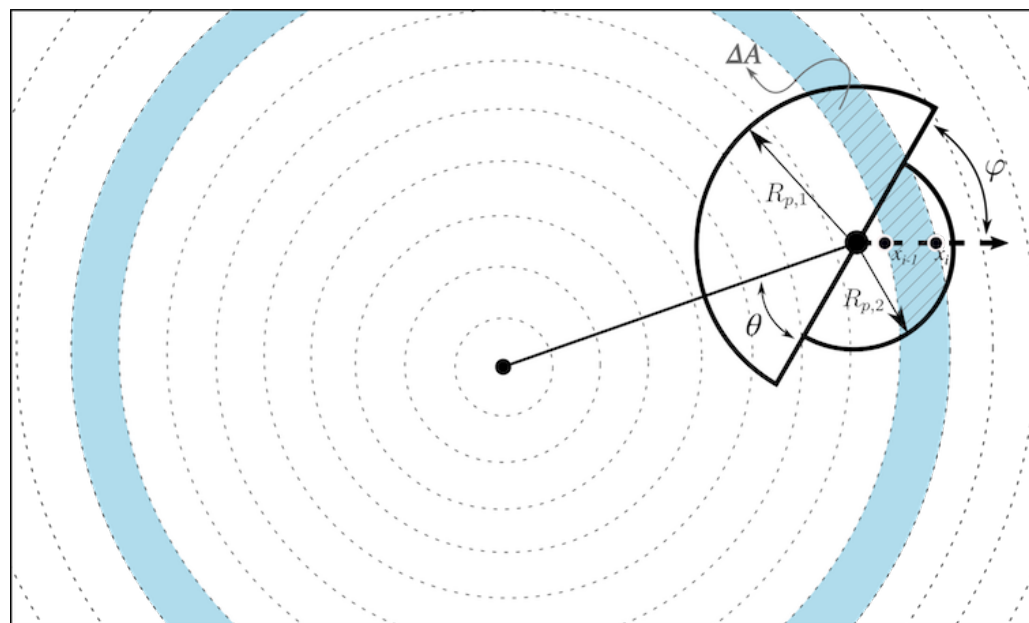
Figure 1: Diagram of the geometric configuration during transit of two stacked semi-circles (one of radius $R_{p,1}$, and another of radius $R_{p,2}$) that model the different limbs of an exoplanet transiting in front of a star. The area of the star has been divided in different sections of radius x_i (dashed circles) — between each subsequent section, the star is assumed to have a radially symmetric intensity profile (e.g., blue band between x_{i-1} and x_i above). In order to obtain the light curve, the challenge is to calculate the sum of the intersectional areas between a given iso-intensity band and the semi-circles, ΔA (blue band with dashed grey lines). Note the stacked semi-circles are inclined by an angle φ with respect to the planetary orbital motion.

The width of the iso-intensity bands determines the truncation error of the model. The model is first initialised with parameters including a maximum truncation error either set by the user or taken as the pre-set value as 1ppm. As in `batman`, `catwoman` first calculates many models, with varying widths and geometrically searches for a width that produces an error less than 1% away (and always less than) the specified level. The model then uses this width value to calculate the desired light curves. A lower specified error, and therefore thinner iso-intensity bands, produces more accurate light curves, however more steps are needed to calculate δ which takes more time.

`catwoman` also allows for φ, the angle of rotation of the semi-circles, to vary as a free parameter, which is something no other model has tried to implement, accounting for the possibility of spin-orbit misalignments of the planet. The two semi-circle radii, $R_{p,1}$ and $R_{p,2}$, and other orbital variables are also completely free parameters.

`catwoman` was designed to be used by astronomical researchers. For a realistic light curve with 100 in-transit data points, `catwoman` takes around 340 seconds to produce 1 million quadratic-limb-darkened light curves on a single 1.3 GHz Intel Core i5 processor. It is used in Espinoza & Jones (in prep.).

Acknowledgements

References

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