

# <sup>1</sup> mfpml: Multi-fidelity probabilistic machine learning toolkit

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## Software

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## <sup>6</sup> Summary

<sup>7</sup> The `mfpml` (multi-fidelity probabilistic machine learning) package provides a Python platform for implementing classic single- and multi-fidelity Bayesian machine learning surrogates and applying them to Bayesian optimization. Although numerous methods have been developed in the domain of multi-fidelity machine learning ([Giselle Fernández-Godino, 2023](#)), no open-source software offers a comprehensive suite of tools for this purpose. This package addresses this gap by providing a platform to replicate existing single- and multi-fidelity Bayesian methods based on Gaussian process regression. Furthermore, it serves as a handy tool for developing new methods in the field of multi-fidelity probabilistic machine learning.



Figure 1: Logo of `mfpml`.

## <sup>15</sup> Statement of Need

<sup>16</sup> `mfpml` is written in Python and depends on a few third-party packages, such as NumPy  
<sup>17</sup> ([Harris et al., 2020](#)) and SciPy ([Virtanen et al., 2020](#)). It includes detailed notebooks and  
<sup>18</sup> autogenerated Sphinx documentation, allowing users to replicate existing methods and develop  
<sup>19</sup> new ones with ease. Specifically, it provides essential modules for building machine learning  
<sup>20</sup> models, including design of experiments, benchmark problems, models, and optimization.

<sup>21</sup> Key features of `mfpml` include:

- <sup>22</sup> 1. **Basic Methods:** Fundamental implementations of popular methods, such as Gaussian  
process regression ([Rasmussen & Williams, 2005](#)), Co-Kriging ([Forrester et al., 2007](#)),  
and corresponding extensions ([Han & Görtz, 2012](#)).
- <sup>25</sup> 2. **Advanced Methods:** Advanced techniques for Bayesian optimization ([Jones et al., 1998](#)),  
including single-fidelity and multi-fidelity optimization.
- <sup>27</sup> 3. **Future Development:** Ongoing work includes adding constrained optimization and  
multi-objective optimization methods, which will be included in future versions.

<sup>29</sup> In a similar scope, several Python packages provide Gaussian process or Bayesian optimization  
<sup>30</sup> functionality—such as GPyTorch ([Gardner et al., 2021](#)) and BoTorch ([Balandat et al., 2020](#)).

31 However, these frameworks primarily target single-fidelity modeling or deep Gaussian processes  
32 and are often coupled with large software dependencies. The SMT toolbox ([Saves et al., 2024](#))  
33 offers various surrogate models with limited capability to integrate multi-fidelity data, yet it  
34 lacks support for multi-fidelity Bayesian optimization. By contrast, `mfpml` is designed as a  
35 lightweight and standalone toolkit that focuses explicitly on multi-fidelity Gaussian process  
36 regression and the corresponding Bayesian optimization framework. It serves both as a platform  
37 for developing and benchmarking novel multi-fidelity Gaussian process methods and as an easily  
38 deployable tool for real-world applications such as aerodynamic shape optimization, materials  
39 design, and other simulation-driven engineering problems.

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