

HiMAP: Hidden Markov for Advanced Prognostics

¹ Thanos Kontogiannis  ^{1*}, Mariana Salinas-Camus  ^{1*}, and Nick Eleftheroglou¹ 

¹ Intelligent Sustainable Prognostics Group, Aerospace Structures and Materials Department, Faculty of Aerospace Engineering, Delft University of Technology, Kluyverweg 1, 2629HS Delft, the Netherlands 
⁶ Corresponding author * These authors contributed equally.

DOI: [10.xxxxxx/draft](https://doi.org/10.xxxxxx/draft)

Software

- [Review](#) 
- [Repository](#) 
- [Archive](#) 

Editor: [Pierre de Buyl](#)  

Reviewers:

- [@AnnikaStein](#)
- [@robmoss](#)

Submitted: 17 February 2025

Published: unpublished

License

Authors of papers retain copyright and release the work under a Creative Commons Attribution 4.0 International License ([CC BY 4.0](#))

Summary

Prognostics, the science of predicting systems' future health, performance, and remaining useful life (RUL), is critical across various fields, including aerospace, energy, manufacturing, and transportation. These industries require advanced tools to model complex and often hidden degradation processes under real-world conditions, where physical models are unavailable or incomplete. Hidden Markov Models (HMMs) and Hidden Semi-Markov Models (HSMMs) effectively address these challenges by providing an unsupervised stochastic framework capable of modeling a system's degradation process without relying on labeled data. By probabilistically representing transitions between hidden states over time, these models effectively capture the stochastic nature of degradation, making them particularly well-suited to handle the complexities of prognostics tasks.

Statement of need

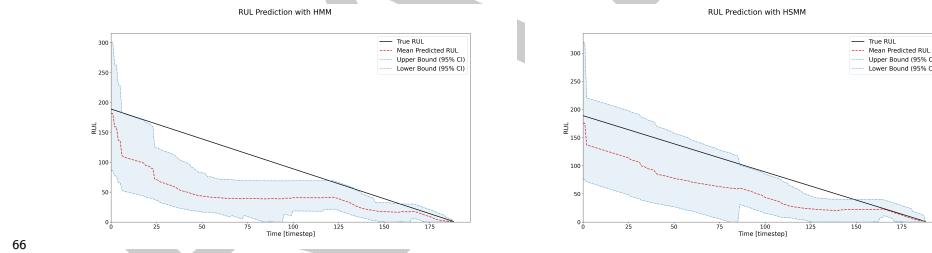
Modern systems in critical industries, such as aerospace and energy, are often used under different operational conditions, with limited or no labeled data available for training. These systems frequently lack comprehensive physical models to accurately describe degradation processes, making it challenging to predict future failures ([Guo et al., 2019](#)). Therefore, advanced prognostics, which are defined here as providing reliable RUL predictions under such conditions, are essential for optimizing maintenance schedules, reducing downtime, and improving system reliability. For example, in aerospace, advanced prognostics assist in predicting component failures in aircraft, thereby reducing in-flight risks and preventing costly delays ([Fu & Avdelidis, 2023](#)). In the energy sector, these methods enable the continuous monitoring of wind turbines ([Novaes Pires Leite et al., 2018](#)) and battery health ([Hu et al., 2020](#)), optimizing efficiency and extending operational lifespans.

While state-of-the-art Deep Learning (DL) models, such as Long Short-Term Memory (LSTM) networks and Convolutional Neural Networks (CNNs), have shown results with high accuracy, they require large labeled datasets, are sensitive to environmental uncertainties, and struggle to generalize when operational conditions deviate from training scenarios ([Vollert & Theissler, 2021](#)), ([Costa et al., 2020](#)), ([Li et al., 2020](#)).

Stochastic models like HMMs ([Rabiner, 1989](#)) and HSMMs ([Yu, 2010](#)) offer a robust alternative for advanced prognostics. By treating RUL as a random variable, these models inherently address the uncertainties in degradation processes and adapt to changes in operational conditions. Their probabilistic foundation makes them particularly suited for real-world applications where labeled failure data is sparse or unavailable. Moreover, their ability to model the stochastic nature of degradation processes ensures reliable predictions, even under varying and unpredictable conditions.

42 HiMAP is a repository that implements HMMs and HSMMs specifically designed for prognostics
 43 applications. To the best of the authors' knowledge, it is the first package to provide such
 44 models explicitly tailored to prognostics rather than to generic time-series analysis. For example,
 45 the packages `hmmlearn` and `hmms` implement continuous and discrete HMMs that can be used
 46 for a wide variety of applications, but they are not targeted to a specific discipline. As a result,
 47 they do not include the assumptions typically required for prognostics, and it is left to the user
 48 to determine how to use the estimated hidden states to compute the RUL. In a similar way,
 49 the package `PyMC` offers a wide and well-documented variety of stochastic and Bayesian models
 50 that can be applied to time-series analysis and survival analysis (a discipline closely related to
 51 prognostics), but none of these models are specifically designed for the prognostic task.

52 In HiMAP, each model is implemented as a dedicated Python class, designed for seamless
 53 integration into diverse workflows. These classes provide essential methods such as `decode`, for
 54 inferring the most likely sequence of hidden states; `fit`, for parameter learning; `bic_fit`, for
 55 jointly selecting the optimal number of hidden states and estimating model parameters; and
 56 `sample`, for generating synthetic sequences. Beyond these core functionalities, the repository
 57 introduces advanced features for calculating RUL using a novel prognostic measure ([Salinas-Camus & Eleftheroglou, 2024](#)). This measure can be easily implemented by the user through
 58 the `prognostics` method and only requires the test dataset as input. By leveraging Viterbi-
 59 decoded state sequences ([Rabiner, 1989](#)), it produces a probability density function (pdf)
 60 of the RUL, enabling reliable and uncertainty-aware predictions. These RUL predictions are
 61 illustrated in the images below, which correspond to the same example trajectory but highlight
 62 the differences in results obtained with each model. Although the HMM can be trained more
 63 quickly, its predictions are less optimal than those of the HSMM, which, as shown in the
 64 figures, yields narrower confidence intervals at the expense of a higher computational cost.
 65



66 References

- 67
- 68 Costa, P. R. de O. da, Akçay, A., Zhang, Y., & Kaymak, U. (2020). Remaining useful lifetime
 69 prediction via deep domain adaptation. *Reliability Engineering & System Safety*, 195,
 70 106682. <https://doi.org/10.1016/j.ress.2019.106682>
- 71 Fu, S., & Avdelidis, N. P. (2023). Prognostic and health management of critical aircraft systems
 72 and components: An overview. *Sensors*, 23(19). <https://doi.org/10.3390/s23198124>
- 73 Guo, J., Li, Z., & Li, M. (2019). A review on prognostics methods for engineering systems. *IEEE
 74 Transactions on Reliability*, 69(3), 1110–1129. <https://doi.org/10.1109/TR.2019.2957965>
- 75 Hu, X., Xu, L., Lin, X., & Pecht, M. (2020). Battery lifetime prognostics. *Joule*, 4(2), 310–346.
 76 <https://doi.org/10.1016/j.joule.2019.11.018>
- 77 Li, X., Zhang, W., Ma, H., Luo, Z., & Li, X. (2020). Data alignments in machinery remaining
 78 useful life prediction using deep adversarial neural networks. *Knowledge-Based Systems*,
 79 197, 105843. <https://doi.org/10.1016/j.knosys.2020.105843>
- 80 Novaes Pires Leite, G. de, Araújo, A. M., & Rosas, P. A. C. (2018). Prognostic techniques
 81 applied to maintenance of wind turbines: A concise and specific review. *Renewable and
 82 Sustainable Energy Reviews*, 81, 1917–1925. <https://doi.org/10.1016/j.rser.2017.06.002>

- 83 Rabiner, L. R. (1989). A tutorial on hidden markov models and selected applications in speech
84 recognition. *Proceedings of the IEEE*, 77, 257–286. <https://doi.org/10.1109/5.18626>
- 85 Salinas-Camus, M., & Eleftheroglou, N. (2024). Uncertainty in aircraft turbofan engine
86 prognostics on the c-MAPSS dataset. *PHM Society European Conference*, 8, 10–10.
87 <https://doi.org/10.36001/phme.2024.v8i1.4007>
- 88 Vollert, S., & Theissler, A. (2021). Challenges of machine learning-based RUL prognosis:
89 A review on NASA's c-MAPSS data set. *2021 26th IEEE International Conference on
90 Emerging Technologies and Factory Automation (ETFA)*, 1–8. <https://doi.org/10.1109/ETFA45728.2021.9613682>
- 92 Yu, S.-Z. (2010). Hidden semi-markov models. *Artificial Intelligence*, 174, 215–243. <https://doi.org/10.1016/j.artint.2009.11.011>
- 93

DRAFT