

Computer-Aided Generation of N-shift RWS

Benjamin Edward Bolling 10 1

1 European Spallation Source ERIC

DOI: 10.21105/joss.03431

Software

- Review 🗗
- Repository 🗗
- Archive ♂

Editor: Mark A. Jensen 🗗 📵

Reviewers:

- @ShantanuDash
- @magedhelmy1

Submitted: 03 May 2021 **Published:** 08 February 2023

License

Authors of papers retain copyright and release the work under a Creative Commons Attribution 4.0 International License (CC BY 4.0).

Statement of Need

All around the world, research institutes and industrial complexes make use of workforces working multiple shifts per day in order to utilise maximum efficiency and profitability of the facility. Creating shift work schedules has, however, always been a challenging task, especially such that are equal for all workers and at the same time distributes the shifts evenly and properly to prevent staff burnout (Becker, 2020).

The purpose and aim of this package is to support research institutes and industrial complexes at which non-standard working hours are applicable with a computational tool to create rotational workforce schedules by providing the user (schedule-maker) with all possible schedules for a set of input constraints/conditions (such as shift lengths, weekly working hours and -resting time) by constructing and utilising a Combinatoric Generator and a Cartesian Product calculator.

Comparing to already available software that (by the developer/author) could be found, this method uses a computational semi-automatic approach rather than the more traditional manual creation of schedules. This computational approach is also able to check and identify every combination that could satisfy the required rotational workforce schedule, if there are any that fully satisfy the requirements. Hence, this application can be used as an aid for schedule-makers by being either supplied with ready schedules or by schedules working as good starting points. It can therefore also be considered as an attempt to implement a slightly different method, which e.g. together with other shift scheduling methods may be combined to find more strategic methods for building rotational shift workforce schedules.

Another approach and need of the application is to serve as a support function for creating rotational shift workforce schedules for large-scale scientific research facilities such as particle accelerators, at which the workforce size is many time very constrained. In those situations, the creation of schedules can be very complex and difficult, making a tool such as this useful. In other cases, it can be used to prove that the constraints are too tight and that these cannot be fulfilled by any schedule, saving time for shift schedulers and hence also for the research facility.

This package provides a graphical user interface (based on PyQt5 (Riverbank Computing Limited, 2016)) tool for generating and constructing acceptable shift arrays if there are any possible arrays following all user-defined constraints. These can be exported to the file formats ODS, CSV, and txt, with the arrays ready to be used as they are or as templates for further modifications (e.g. swapping shifts between workers and hence taking into account individual workers' needs).



Introduction

In order to achieve schedules for the workers that treats everyone equally, the focus of this package is on so-called rotational workforce schedules (RWSs). Rotational workforce schedules means that the schedule rotates after time, and hence, the other option would be static shift schedules. In this project, the term 'shift arrays' is defined to represent all possible schedules following a list of constraints, originating from e.g. country laws, organisational needs, and/or workforce requests.

Computational Approach and Results

In this approach, each worker has the same schedule shifted by one week, resulting in that all workers follow the same schedule. The project has been divided into two phases, *Boolean Shift Arrays* (in which boolean shift arrays are generated) and *From Boolean Shift Arrays to a RWS* (in which a selected boolean shift array is shaped into its final RWS layout). The high-level software architecture flow and a user flowchart can be seen in Figure 4 and Figure 5, respectively.

Boolean Shift Arrays (phase 1)

A boolean shift array is defined such that 1 means that the worker is working and 0 that the worker is not. The input species (also known as constraints) and their respective values used are shown in Table 1 below.

T 11 4	C					. 1					
Table I.	Constraints,	101	the	variables	and	their	meanings	and	some	example	values
Tubic 1.	Construints,	1.0.		Variables	unu	CIICII	micumings,	unu	301110	CAUTTIPIC	values.

Variable	Meaning	Value
\overline{N}	number of shifts per days	2
n_{cf}	number of days off clustered	_
n_S	number of shifts per shift cycle	18
n_W^-	number of weeks to cycle over	4
n_{wd}	number of working days per week	7
n_{wS}	Number of workers per shift (minimum)	1
t_d	daily minimum continuous resting time	11
t_r	weekly minimum single continuous resting time	36
t_s	shift lengths	8.33
t_W	weekly working hours per worker	36.00

Since each week also resembles a worker, the shift array can be set up as a matrix with 7 columns (each representing the days of a week) and $n_W/7$ rows (each representing a worker). The columns can then be summed to achieve the shift occupancy (or how many people are working each shift). Thus, the phase1 algorithm only allows shift arrays to pass for which all shifts are occupied by at least one worker, with a shift represented by the first n_{wd} days for each week. In order to extend to not only use single shifts but also 2- or 3-shifts, a logical condition was added into the algorithm: For N shifts per day, each day has to be filled with at least N workers.

In order to avoid all working days from being clustered together, the constraint for weekly minimum single continuous resting time is added (t_r) . The algorithm ensures that all passed shift arrays have at least t_r hours of free-time over any given 7-day period.

The number of shifts per shift array is, in this algorithm, calculated by

$$n_S = \text{ceil}(t_W/t_s) \tag{1}$$



to have the reason for using ceiling function (and not the floor function) being the argument that it is better with a couple of more hours than fewer. In order to cluster days off (n_{cf}) , the algorithm's GUI has an optional additional constraint that serves this purpose and simply does not allow shift arrays with zeroes in clusters less than this through.

By using the input $n_W \times n_{wd}$ as the iterable and n_S as the length of subsequences of elements from the iterable, the same methodology as the *combinations* function of the *itertools* module in Python (Python Software Foundation, 2020) (a combinatoric generator) is used for creating each shift array. It can be simply described as creating an array of combinations (in this case, zeroes and ones corresponding to a day off or shift work, respectively) with a specific length (number of days in a cycle). By imposing the other inputs as constraints on whether a shift array should be appended to accepted shift arrays, the reason for not using the built-in Python module becomes clear: Python's built-in module returns all array combinations that are possible without any imposed constraints, which quickly escalates to becoming too large for a personal computer's internal memory to handle.

With this, the final result is an array of shift arrays in which each shift array is filled with $7n_S$ ones and $n_W(7-n_S)$ zeroes whilst obeying the above mentioned constraints.

As there are $\binom{n}{r}$ ways to choose r elements from a set of n elements, the number of possible combinations (C) can be expressed by using the factorial of the binomial coefficient:

$$C = \frac{n!}{r! \times (n-r)!}.$$
(2)

with n being the number of days in total in a shift cycle and r being the number of working days per worker in the shift cycle.

Translating this into the variables defined in Table 1 yields the total number of combinations (without constraints), which is hence also the maximum number of accepted combinations:

$$C = \frac{n_W \times n_{wd}!}{n_S!(n_W \times n_{wd} - n_S!)}.$$
(3)

From Boolean Shift Arrays to RWS (phase 2)

In this phase, a new list of combinations with free days clustered in pairs has been generated and a combination selected to proceed with (combination 212 as it has two out of four weekends off (note the zeroes in the bottom table in Figure 2 to the right).

Pressing the Find solutions results in what is shown in Figure 3 (right figure). A schedule can also be constructed completely by hand, but note that the algorithm will find all possible combinations that obey the given constraints. The algorithm is a Cartesian Product calculator, in which each set is a list of shifts (1 = Day, 2 = Evening, etc.) with one set per working day:

$$\text{combinations} = \begin{pmatrix} 1 \\ 2 \\ \vdots \end{pmatrix} \times \begin{pmatrix} 1 \\ 2 \\ \vdots \end{pmatrix} \times \dots \times \begin{pmatrix} 1 \\ 2 \\ \vdots \end{pmatrix} = \prod_{i=1}^{n_{wd}} \begin{pmatrix} 1 \\ 2 \\ \vdots \end{pmatrix}_i = \begin{cases} \begin{bmatrix} 1 & 1 & \dots & 1 \\ 1 & 1 & \dots & 2 \\ \vdots & 1 & \dots & 2 \\ \vdots & 1 & \dots & 1 \\ \vdots & 2 & \dots & 1 \\ \vdots & 2 & \dots & 2 \end{bmatrix}$$
 (4)

where each array in the resulting product is considered as a possible shift schedule matrix. Imposing constraints (resting time between shifts and ensuring all shifts are filled) on each combinations results in solutions from which the user can choose between.



Since all combinations are stored in a matrix form before different combinations are removed from the final solutions matrix, large datasets require severe amount of internal memory for the Cartesian Product method to work. For this, a controlling script has been implemented which calculates a pre-estimate of required internal memory. Approximating that each character in the shiftarray takes up 8 byte of memory yields

$$IM \approx N_{size} = N^{n_S} \times n_S,$$
 (5)

where N_{size} is the total number of zeroes and ones in the full matrix. If the estimated size of the resulting matrix from the operation exceeds 1Gb, the user is prompted whether to continue with the default Cartesian Product method or to use a less internal memory demanding recursive method.

Comparison to similar softwares

Different commercial softwares are available for shift scheduling using computational methods. In 2004, Burke (2004) made a comprehensive literature review of a wide range of approaches, including optimising approaches (mathematical programming), multi-criteria approaches (goal programming), artificial intelligence methods, heuristic approaches, and metaheuristic approaches. Common for these approaches is that they use the constraints by the user and are able to provide more-or-less ready schedule(s), with the limitations for the mathematical approaches not being appropriate and requiring post-generation work. Goal programming defines a target for each criterion and their relative priorities Burke (2004) by applying mathematical programming or by tackling metaheuristics within a multi-objective framework. The complexities from goal programming arise from that real world problems are difficult to solve without some optimisation from a planner.

Many approaches utilising artificial intelligence imitate human reasoning and may hence produce reasonable schedules, such as Petrovic & Berghe (2002) which takes into account parameters such as the appropriate skill mix and staff-to-patient ratios.

Laporte & Pesant (2004) developed a constraint programming algorithm for the construction of rotating shift schedules with the algorithm building the schedules per column (per day), looking for allowed shift stretches (including days off). The pros of their method over this project is that the required computing power is lower than in this project as the shift patterns. However, the method populates the shift schedules with the shift species and does not allow the user to perform the middle step from this project, which is selecting the shift- and rest-day-patterns (referred to as a combination). Therefore, the cons of their algorithm in comparison to this would be that the number of solutions could be very high and require a large amount of computer storage. Moreover, their method had difficulties to obtain evenly spaced full weekends off, which the shift pattern scroll tool in this project can be utilised for finding (see bottom of Figure 2).



Conclusions

In this project, an algorithm has been constructed which generate schedules for different number of weeks to cycle over. The current issue is that the computational complexity (and hence the required computation time) increases with the number of weeks per cycle (see Table 2 and in Figure 1 in benchmarking). This means that for a higher amount of weeks in a shift cycle, this application will need further development in order to have more efficient ways of finding the solutions and/or deployment of the application onto super-computers for generating the Boolean Arrays.

For up to 5 weeks in a shift cycle it is possible to use a general-purpose computer such as the benchmarking Apple MacBook Pro with specifications defined in Table 1 in [benchmarking](https://github.com/benjaminbolling/RSW/blob/master/docs/benchmarking.md. It has thus been demonstrated that the application can be used to generate 1, 2 and 3-shift schedules. The software in this project has also been compared to a few existing methods via a short literature study, showing that it offers both benefits and disadvantages.

Future development plans include adding functionalities in phase 1 such as filtering on number of free weekends and taking into account competences of the shift workers (to ensure full coverage of potential shift competence requirements). An important future development needed is restructuring part of the algorithm to lower the required processing power and hence time needed. Another future development plan includes importing an existing schedule with labels as a CSV-file directly into phase 2 such that modifications and/or checks can be done to assure the schedule is compliant with local rules for the workers. These improvements would further strengthen the usability of this application.

Figures



Figure 1: The RWSing Application's launcher.



● ● • RSW algorithm phase 1									
RSW Algo									
Phase 1: Generate combinations and select combination to solve									
Define the parameters below									
Shift type:									
Define the shift labels	(e.a. D / E		D						
	W	7			٥				
	Number o	f weeks to cycle over:	4	0					
Shift occupancy: 1									
Shift Lengths [h]: 8,33									
Weel		0							
		uous resting time [h]:	36,00 36			0			
		daily resting time [h]:	11			0			
		er free days?	2 18			⊌			
		per person per cycle:							
Load combos	5	save all combos	Generate Combinations						
		constraints found: 13	123110	Fast	generation				
Number of combinations with constraints found: 230									
Time for completion: 239.375303 s									
		Post table generation s	chedule wor	 k					
Browse through the c	ombination	s' indices until you find	one to work	with:					
			212			0			
0 0				0	0				
1 1	1	1	1	0	0				
1 1	0 1	0	1	1	1				
		_ `							
Test For Solu	tions	Save combo	Proceed	with this	combo to next	phase			
Coder: Benjamin Bolling (benjaminbolling@icloud.com)									

 $\textbf{Figure 2:} \ \ \textbf{The RWSing Application's algorithm's "phase 1 GUI", in which the combinations have been generated.$



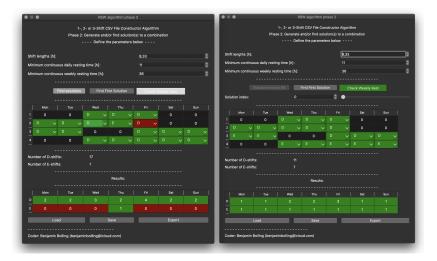


Figure 3: The RWSing Application's algorithm's "phase 2 GUI" as launched from the "phase 1 GUI" and with the second Thursday's shift changed to an evening shift (left) and after finding solutions, showing the first solution (right).

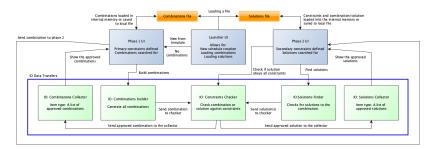


Figure 4: The RWSing Application's high-level software architecture flow.

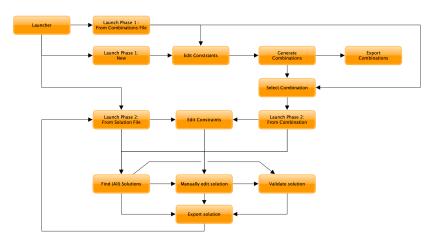


Figure 5: The RWSing Application's high-level user flowchart.



Acknowledgements

The author wants to thank his direct line-manager at European Spallation Source for asking the question if it would be possible to create a software for generating shift schedules, which lead to the idea of creating this project and after a while lead to this final state. The author also wants to thank the reviewers for taking their time reviewing this project.

References

- Becker, T. (2020). A decomposition heuristic for rotational workforce scheduling. *Journal of Scheduling*, 23, 539–554. https://doi.org/10.1007/s10951-020-00659-2
- Burke, D. C., E. (2004). The state of the art of nurse rostering. *Journal of Scheduling*, 7(6), 441-499. https://doi.org/10.1023/B:JOSH.0000046076.75950.0b
- Laporte, G., & Pesant, G. (2004). A general multi-shift scheduling system. *The Journal of the Operational Research Society*, *55*, 1208–1217. https://doi.org/10.1057/palgrave.jors. 2601789
- Petrovic, G. B., S., & Berghe, G. V. (2002). Storing and adapting repair experiences in personnel rostering. *Practice and Theory of Automated Timetabling, Fourth International Conference*, 185–186.
- Python Software Foundation. (2020). *Python Language Reference* (Version 3.8.2). http://www.python.org
- Riverbank Computing Limited. (2016). *PyQt5: Python bindings for the Qt cross platform UI and application toolkit.* https://www.riverbankcomputing.com/software/pyqt/