




# WEdiff: A Python and C++ package for automatic differentiation

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## Software

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## Summary

The need to calculate derivatives occurs frequently in the development of codes that do numerical computations. A common example is codes that solve ordinary or partial differential equations, where differentiation may be required for linearization or for determining the sensitivity of the solution to input parameters. There are a wide variety of methods available to calculate numerical derivatives, including finite differences. Although finite differences can be useful, they are prone to various errors including truncation error (when the difference between the function values is too large) and cancellation error (when the difference between the function values is too small) (Griewank & Walther, 2008). Automatic differentiation is a technique that is able to calculate derivatives with machine accuracy by systematically propagating derivatives through the code using the chain rule of calculus. Essentially, the algorithm is viewed simply as a large number of differentiable operations on data, i.e., the composition of the functions  $f_0, f_1, \dots, f_n$ , for which the derivative with respect to the first function value (which may be a constant) is:

$$\frac{\partial f_n}{\partial f_0} = \frac{\partial f_n}{\partial f_{n-1}} \frac{\partial f_{n-1}}{\partial f_{n-2}} \dots \frac{\partial f_2}{\partial f_1} \frac{\partial f_1}{\partial f_0}$$

The chain rule, expressed in the equation above, can be evaluated in either forward or backwards order. One method for propagating derivatives is source code transformation, where the base code is parsed and a secondary code is produced (Bischof, Khademi, Mauer, & Carle, 1996; Giering & Kaminski, 1998; Hascoet & Pascual, 2013). This method, however, is mainly suitable for procedural programming languages. Another method is based on operator overloading where a class is implemented to hold both the computed value and the accumulated derivative, and implements overloaded operators to propagate the derivatives forwards through the code (Griewank & Walther, 2008; Jemcov, 2009; Jemcov & Mathur, 2004). This method is suitable for object-oriented languages, and just requires that classes and functions be templated to accept the new data type. It is also able to compute derivatives with respect to arbitrary variables, requiring minimal code changes to implement derivative calculations within an existing code.

WEdiff implements forward-mode automatic differentiation using a class called `FwdDiff` which stores both the numerical value and accumulated derivative. All standard mathematical operators and functions are implemented for this type. The code is implemented in C++ and can be used in a straightforward manner in the development of other C++ codes. It also includes Python wrappers generated using SWIG (“SWIG (Simplified Wrapper and Interface Generator),” 2018), enabling it to be used in the development of Python scripts as well.

WEdiff has been designed to be used by researchers in any area of study that involves numerical computations where derivatives are required. As an example, it has recently been

used to determine the sensitivity of temperature fields to the thermophysical properties of solids using a finite-volume-based numerical code (C. DeGroot, 2018). This work can easily be extended to include finite-volume-based solutions of more complex fluid mechanics problems. WEdiff could also be used in many other areas, such as solutions of ordinary differential equations, where the derivative of the solution could be obtained with respect to any input parameters. This would enable both optimization and uncertainty analysis to be conducted. The source code for WEdiff, along with test cases, examples, and documentation, can be found on BitBucket (C. T. DeGroot, 2018).

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