DataAssimilationBenchmarks.jl: a data assimilation research framework.

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Summary

Data assimilation (DA) refers to techniques used to combine the data from physics-based, numerical models and real-world observations to produce an estimate for the state of a time-evolving random process and the parameters that govern its evolution (Asch et al., 2016). Owing to their history in numerical weather prediction, full-scale DA systems are designed to operate in an extremely large dimension of model variables and observations, often with sequential-in-time observational data (Carrassi et al., 2018). As a long-studied "big-data" problem, DA has benefited from the fusion of a variety of techniques, including methods from Bayesian inference, dynamical systems, numerical analysis, optimization, control theory, and machine learning. DA techniques are widely used in many areas of geosciences, neurosciences, biology, autonomous vehicle guidance, and various engineering applications requiring dynamic state estimation and control.

The purpose of this package is to provide a research framework for the theoretical development and empirical validation of novel data assimilation techniques. While analytical proofs can be derived for classical methods, such as the Kalman filter in linear-Gaussian dynamics (Jazwinski, 2007), most currently developed DA techniques are designed for estimation in nonlinear, non-Gaussian models where no analytical solution may exist. DA methods, therefore, must be studied with rigorous numerical simulation in standard test-cases to demonstrate the effectiveness and computational performance of novel algorithms. Pursuant to proposing a novel DA method, one should likewise compare the performance of a proposed scheme with other standard methods within the same class of estimators.

This package implements a variety of standard data assimilation algorithms, including some of the widely used performance modifications that are used in practice to tune these estimators. This software framework was written originally to support the development and intercomparison of methods studied in C. Grudzien & Bocquet (2022). Details of the studied ensemble DA schemes, including pseudo-code detailing their implementation and DA experiment benchmark configurations, can be found in the above principal reference. Additional details on numerical integration schemes utilized in this package can be found in the secondary reference (Grudzien C. et al., 2020).

Statement of need

Standard libraries exist for full-scale DA system research and development, e.g., the Data Assimilation Research Testbed (DART) (Anderson et al., 2009), but there are fewer standard options for theoretical research and algorithm development in simple test systems. Many basic research frameworks, furthermore, do not include standard operational techniques developed

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from classical variational methods, due to the difficulty in constructing tangent linear and adjoint codes (Kalnay et al., 2007). DataAssimilationBenchmarks.jl provides one framework for studying sequential filters and smoothers that are commonly used in online, geoscientific prediction settings, including both ensemble methods and variational schemes, with hybrid methods planned for future development.

Comparison with similar projects

Similar projects to DataAssimilationBenchmarks.jl include the DAPPER Python library (Raanes & others, 2022), DataAssim.jl used by Vetra-Carvalho et al. (2018), and EnsembleKalman-Processes.jl of the Climate Modeling Alliance (Dunbar & others, 2022). These alternatives are differentiated primarily in that:

- DAPPER is a Python-based library which is well-established, and includes many of the same estimators and models. However, numerical simulations in Python run notably slower than simulations in Julia when numerical routines cannot be vectorized in Numpy (Bezanson et al., 2017). Particularly, this can make the wide hyper-parameter search intended above computationally challenging without utilizing additional packages such as Numba (Lam et al., 2015) for code acceleration.

- DataAssim.jl is another established Julia library, but notably lacks an implementation of variational and ensemble-variational techniques.

- EnsembleKalmanProcesses.jl is another established Julia library, but specifically lacks traditional geoscientific DA approaches such as 3D-VAR and the ETKF/S.

Future development

The future development of the DataAssimilationBenchmarks.jl package is intended to expand upon the existing, variational and ensemble-variational filters and sequential smoothers for robust intercomparison of novel schemes. Additional process models and observation models for the DA system are also in development.

Acknowledgements

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