# TriP: A Python package for the kinematic modeling of serial-parallel hybrid robots

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Summary

Robots can be classified according to their mechanical structure. Serial mechanisms like robotic arms are mechanisms where each moving part (called a link) is connected to only the one before and the one after it. They are often used when a large workspace is required, meaning the robot needs a long reach. In parallel mechanisms, the links of the robot form loops causing them to be structurally stronger and stiffer.

If both a large workspace and structural strength are required, hybrids that contain both serial and parallel mechanisms are used. While hybrid mechanisms combine the mechanical advantages of both parallel and serial mechanisms, they also combine their modeling disadvantages:

- Finding an explicit solution for either forward or inverse kinematics is often impossible. Using numerical approaches instead leads to complicated constrained optimization problems for both forward and inverse kinematics.

- While serial mechanisms are very well supported by current robotic frameworks, parallel mechanisms and hybrid mechanisms especially are often not supported at all. A great overview of the supported robot types for different robotic frameworks was compiled by Kumar (2019).

TriP is a python package designed to close this gap using a modular modeling framework akin to the one described by Kumar et al. (2020). It allows the modeling of arbitrary hybrid mechanisms and is capable of calculating forward and inverse kinematics.

The calculations are performed using a symbolic framework. This makes it easy for users to implement custom case-dependent mathematical solvers.

Statement of Need

While a huge number of researchers, such as Pisla et al. (2013), Kanaan et al. (2009), and Zoss et al. (2006), use hybrid serial parallel systems, most modern kinematics frameworks still lack support for such systems. Examples include OpenRAVE (Diankov & Kuffner, 2008), used in the MoveIt! stack (Chitta et al., 2012), the MATLAB robotics toolbox (Corke, 2017), Klampt (Hauser, 2021), and the inverse kinematics Python library (Manceron, 2021). While all these frameworks and libraries offer fast computation of forward and inverse kinematics, they only support branching serial mechanisms. This lack of support often leaves developers with essentially two choices:

Either shoehorn their hybrid robots into a framework not designed to handle them or be left to implement their own kinematic solvers.

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TriP is a lightweight and easy-to-use package for directly modeling hybrid mechanisms and calculating their kinematics. Although TriP is fast for a Python package, it is not built for robust hard-real time control applications. Instead, it is aimed at researchers and engineers who quickly want to build kinematic models to test their mechanical designs. For this reason it also exposes a interface to the nonlinear optimization and algorithmic differentiation tool CasADi (Andersson et al., 2019). This allows researchers to investigate the kinematic properties of their robots, for example, by using CasADi to find singular configurations or to compute manipulability ellipsoides. Similar to MoveIt!, TriP also enables researchers to build their own inverse kinematic solvers.

Overview

TriP models robots using its *Robot* class. A *Robot* object is made up of *Transformation* and *KinematicGroup* objects. The *KinematicGroup* objects are used to model parallel mechanisms while the *Transformation* objects model serial mechanisms. See Figure 1 for reference, where the links of each robot are colored according to the *KinematicGroup* or *Transformation* it belongs to, while joints are either light green or orange, depending on whether they are actuated or not.
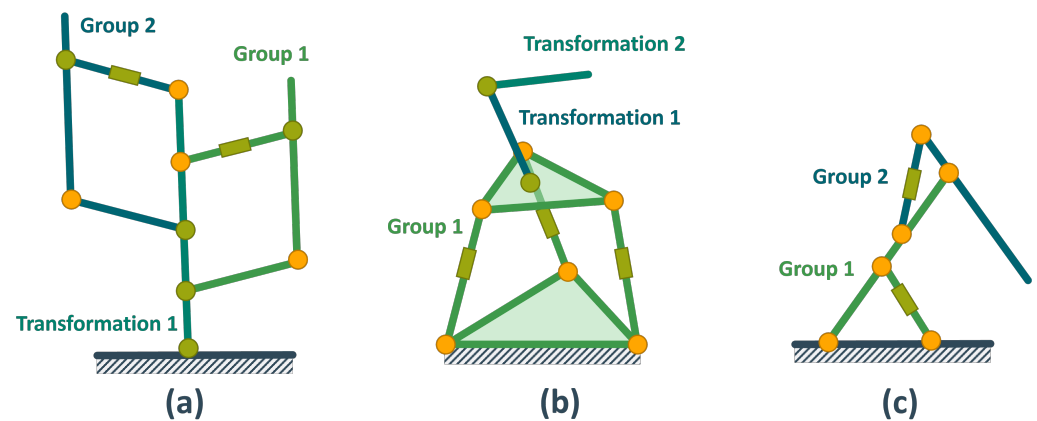

Figure 1: Different Hybrid Robot types and their object structure

Both *KinematicGroups* and *Transformations* can be connected to form branching mechanisms as indicated in Figure 1.

Transformation objects implement homogeneous coordinate transformations between coordinate frames. These can be either dynamic or static with dynamic transformations implementing joints. A few example joints can be seen in Figure 2.
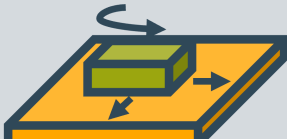

	Transformation(name = 'Revolute Joint',
	          values = { 'rz': 0},
	          state_variables = ['rz'])

	Transformation(name = 'Spherical Joint',
	          values = {'rx': 0, 'ry': 0, 'rz': 0},
	          state_variables = ['rx', 'ry', 'rz'])

	Transformation(name = 'Prismatic Joint',
	          values = { 'tz': 0},
	          state_variables = ['tz'])

	Transformation(name = 'Planar Slider Joint',
	          values = {'tx': 0, 'ty': 0, 'rz': 0},
	          state_variables = ['tx', 'ty', 'rz'])

Figure 2: Sample Joints using the Transformation class

While all example joints use Euler angles in roll pitch yaw convention to describe rotation, quaternions are also supported.

KinematicGroups model parallel mechanisms using the abstraction approach described by Kumar et al. (2020). This approach models a parallel manipulator as a virtual serial manipulator and a mapping that maps the virtual joint state to the true actuated joint state of the parallel manipulator.

An illustrative example of this model is an excavator with two hydraulic cylinders. Each cylinder is part of a parallel mechanism resulting in two *KinematicGroups*. Both can be seen in Figure 3, where one is green and the other one is blue.
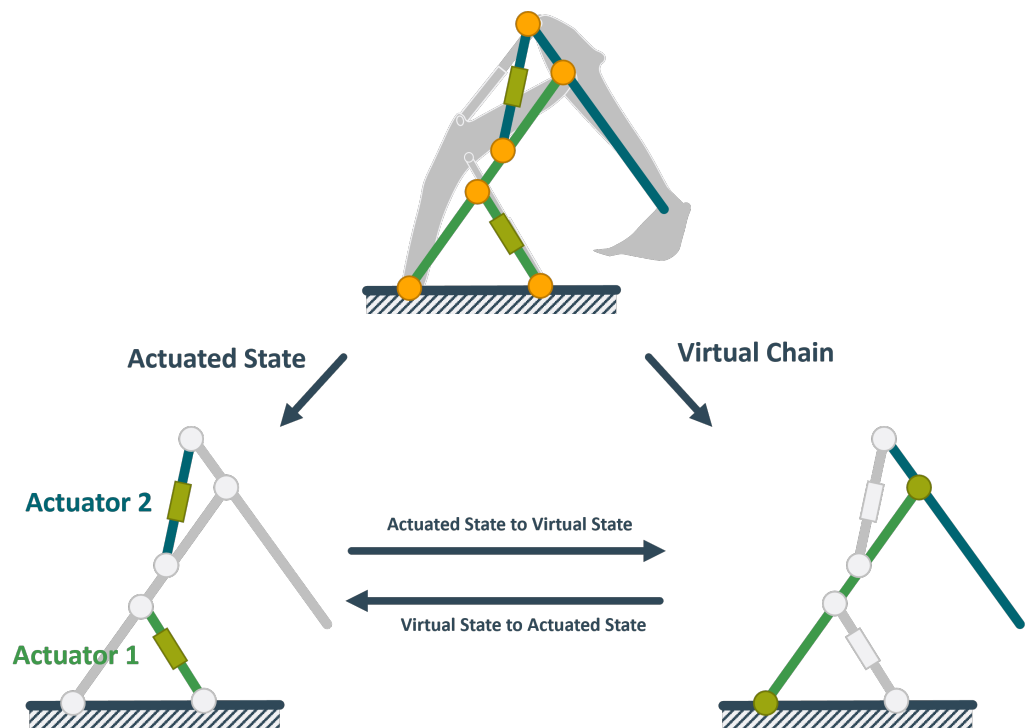
Figure 3: Excavator Arm build from two Groups (green and blue)

The abstraction approach models the excavator as a serial manipulator where the joints are directly actuated. Using two mappings to convert the state of the hydraulic cylinders to the state of the joints and vice versa, it is possible to calculate both forward and inverse kinematics. In this example, the mapping between cylinders and joints can be expressed using trigonometry. Since an explicit formulation of the mappings might not always be possible, TriP can also compute the mapping by solving the closure equation of the parallel manipulator.

TriP can generate symbolic representations of robots using CasADi (Andersson et al., 2019). This symbolic representation can be used to set up a solver object that then solves the inverse kinematics. While the library already implements a simple inverse kinematics solver, the symbolic representation makes it easy to implement custom solvers.

All features of TriP are thoroughly documented with tutorials and examples to help people get started.

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