




# BiGSTARS.jl: A Julia package for bi-global stability analysis for rotating stratified flows

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## Summary

BiGSTARS.jl is a software package written in the Julia programming language ([Bezanson et al., 2017](#)) for investigating the stability of fluid flows relevant to the atmosphere and ocean. It performs linear stability analysis, a technique that determines whether small disturbances introduced into a flow will grow or decay over time. Unlike simpler one-dimensional approaches, bi-global analysis can handle flows whose properties vary in two spatial directions, enabling the study of realistic features such as fronts, jets, and vortices. The package is specifically designed for rotating and stratified fluids, capturing the physical processes essential to geophysical fluid dynamics.

## Statement of need

Linear stability analysis investigates the growth or decay of small perturbations about a basic state by linearizing the governing equations and solving the resulting eigenvalue problem ([Drazin & Reid, 2004](#)). In geophysical fluid dynamics, the interplay between rotation (the Coriolis force) and stratification (the buoyancy force) gives rise to multiple instability mechanisms, including baroclinic instability driven by buoyancy flux and barotropic instability driven by horizontal shear ([Pedlosky, 1987](#)). Such analyses are fundamental for understanding the onset of turbulence, the formation of eddies, and the associated energy transfer across scales in both oceanic and atmospheric systems.

The complexity and dimensionality of stability analyses has evolved substantially, giving rise to distinct methodological approaches with varying computational requirements ([Theofilis, 2011](#)). The classical one-dimensional (1D) stability analysis assumes that the basic state varies along only a single spatial direction. While computationally efficient, this approach presumes spatial homogeneity in the remaining directions and therefore often fails to capture the full dynamics of realistic geophysical flows. At the opposite extreme, the tri-global (3D global) stability analysis allows variations in all three spatial directions, providing the most complete representation of the underlying physics. However, this generality requires substantial computational resources, often beyond the reach of standard research computing infrastructures.

Bridging these two extremes, bi-global (2D global) linear stability analysis occupies an optimal middle ground between 1D and tri-global frameworks ([Theofilis, 2011](#)). In this approach, the basic state varies in two spatial directions while remaining homogeneous in the third, striking a balance between computational tractability and physical realism. Many geophysical flows naturally exhibit this structure, including atmospheric and oceanic jets ([Pedlosky, 1987](#)) as well as submesoscale oceanic fronts and filaments ([McWilliams, 2016](#)), where classical 1D analyses omit key dynamics and fully 3D approaches remain computationally prohibitive.

To address this need, we present BiGSTARS.jl, a Julia-based bi-global stability solver designed to integrate seamlessly with the broader Julia scientific computing ecosystem. The package

is distributed with validated benchmark examples and is intended to be readily accessible to the geophysical fluid dynamics community. BiGSTARS.jl implements a spectral–collocation framework in which the governing equations are discretized using Chebyshev polynomials in the vertical direction and Fourier modes in the horizontal direction, applied to a two-dimensional basic state defined over a rectangular domain.

## State of the field

Although several open-source packages exist for one-dimensional stability analyses (e.g., `pyqg` (Abernathey et al., 2022), `eigntools` (Oishi et al., 2021)), to the best of our knowledge, no fully documented open-source software currently offers a comprehensive bi-global eigenvalue solver capable of treating the linearized rotating Boussinesq equations of motion under the  $f$ -plane approximation (Vallis, 2017).

## Key features

BiGSTARS.jl leverages Chebyshev–Fourier discretization to handle vertically bounded and horizontally periodic domains — an optimal configuration for linear stability analyses of geophysical flows. The Chebyshev operators are constructed using Chebyshev–Gauss–Lobatto nodes, which are the extrema of first-kind Chebyshev polynomials (Trefethen, 2000). Additionally, the framework offers flexible boundary condition handling, enabling the use of different types of mathematical boundary conditions (e.g., Dirichlet, Neumann) for each variable.

The package is based on the shift-and-invert technique, which enables the efficient computation of eigenvalues in targeted regions of the complex plane, crucial for obtaining the most unstable modes. Users can seamlessly switch between multiple Julia eigensolver backends — `ArnoldiMethod.jl` (Stoppels & Nyman, 2024), `Arpack.jl` (Shah, 2018), and `KrylovKit.jl` (Haegeman, 2025) — with built-in performance benchmarking tools. To address convergence challenges in large problems, BiGSTARS.jl employs adaptive convergence strategies, including automatic shift adjustments and retry logic, reducing the need for manual parameter tuning.

The package documentation includes a collection of validated examples that illustrate the key functionalities of the solver, such as setting up a basic state, specifying boundary conditions, and visualizing the results. These examples not only provide an accessible starting point for new users unfamiliar with bi-global stability analysis but also serve as reference cases for developing customized modules.

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