

# <sup>1</sup> BayCauRETM: R package for Bayesian Causal Inference for Recurrent Event Outcomes

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## Software

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## <sup>5</sup> Summary

<sup>6</sup> Observational studies are often conducted to estimate the causal effect of medical treatments on the average rate of a recurrent event outcome within a specific follow-up window in a defined target population. Recurrent events ( e.g. hospitalizations, relapses, and infections) may occur multiple times during follow-up. Causal estimation is challenging with such outcomes because: 1) Recurrent events are typically jointly observed with a terminal event (e.g., death), which precludes future recurrences. 2) Both event count process and the terminal process are unobserved after possible dropout - leading to right censored total event counts and survival time. 3) Patients may initiate the treatment of interest at different times, yielding as many strategies as possible initiation times. Finally, 4) patients are not assigned to treatment strategies randomly, so formal causal methods are required to adjust for observed confounders - i.e. drivers of both treatment patterns and either the recurrent event or death processes.

<sup>17</sup> This paper presents BayCauRETM, an R package for Bayesian estimation of causal effects of different treatment initiation strategies on a recurrent event outcome in the presence of death and censoring. It does so by implementing the methodology developed by Oganisian et al. (2024) which uses Bayesian statistical methods within the potential outcomes causal inference framework. Users specify an initiation time and supply a data.frame containing confounders and columns for censoring, death, and interval-specific recurrent counts, then define terminal and recurrent models via standard R formula syntax. Given these inputs, BayCauRETM performs causal adjustment and outputs adjusted expected event rates over follow-up under the specified initiation time. The package also provides diagnostic and visualization utilities.

<sup>26</sup> Intended users include statisticians, epidemiologists, and health-services researchers analyzing observational data.

## <sup>28</sup> Statement of need

<sup>29</sup> The usual methods (Andersen & Keiding, 2002; Cowling et al., 2006; Ghosh & Lin, 2002) for time-to-event outcomes, recurrent-event outcomes, and multi-state outcomes remain useful for descriptive or associational analysis of death and event rates. Many of these methods can be implemented in R via base functions such as `glm()`, GEE functions in the `geepack` package, or survival functions in the `survival` package. Some specialized R packages such as `msm` (Jackson, 2011) and `reReg` (Chiou et al., 2023) can implement these methods directly. However, while descriptively useful, these methods generally do not target causal effects.

<sup>36</sup> Recent methods targeting causal effects have used inverse-weighted approaches (Schaubel & Zhang, 2010), outcome modeling approaches (Janvin et al., 2024), and doubly-robust approaches (Su et al., 2020). In terms of software, no dedicated R packages are available for these papers beyond implementation code made available as accompanying supplementary information. Moreover, these do not accommodate complexities (1)-(4) listed in the previous

<sup>41</sup> section simultaneously.

<sup>42</sup> Organisian et al. (2024) developed statistical methods that handle complexities (1)-(4) and  
<sup>43</sup> conducted a thorough simulation-based validation of these methods. However, the focus  
<sup>44</sup> was on methodological development and validation, and so development of a user-friendly,  
<sup>45</sup> off-the-shelf R package with readable help files was out of scope. BayCauRETM fills this gap  
<sup>46</sup> by operationalizing the methods of Organisian et al. (2024). Its syntax seeks to maximize  
<sup>47</sup> familiarity to base R users by mirroring standard regression functions such as `lm()` and `glm()`.  
<sup>48</sup> It also has extensive help pages accessible via `help()` or the `?`  command. Thus, BayCauRETM  
<sup>49</sup> provides the first user-friendly software for analyzing complex recurrent-event data while  
<sup>50</sup> handling complexities (1)-(4) described in the Summary section above.

## <sup>51</sup> Data structure, model, and outputs

<sup>52</sup> In this section, we provide an overview of the expected input data structure, models that are  
<sup>53</sup> run under-the-hood, and expected outputs. We refer readers to Organisian et al. (2024) for  
<sup>54</sup> methodological details.

### <sup>55</sup> Data structure and preprocessing

<sup>56</sup> The package expects longitudinal data in long, person-interval format. For follow-up time  $\tau$ ,  
<sup>57</sup> the window  $[0, \tau]$  is partitioned into  $K$  equal-length intervals  $I_k = [\tau_{k-1}, \tau_k)$  for  $k = 1, \dots, K$   
<sup>58</sup> with  $\tau_0 = 0$  and  $\tau_K = \tau$ . Each row represents a patient-interval; a subject has one row per  
<sup>59</sup> interval at risk.

<sup>60</sup> Required data.frame variables are: subject ID, interval index  $k$ , treatment indicator (0 until  
<sup>61</sup> the initiation interval, then 1), interval-specific count of recurrent events, and a terminal-event  
<sup>62</sup> indicator (0 up to death, 1 thereafter). Optional variables include baseline covariates and  
<sup>63</sup> lagged history (e.g., one-interval lag of the event count).

<sup>64</sup> Each row contains a monotone death indicator at the start of interval  $k$ ,  $T_k$ , a monotone  
<sup>65</sup> treatment indicator by the end of interval  $k$ ,  $A_k$ , the interval count  $Y_k$  and baseline covariates  
<sup>66</sup>  $L \in \mathcal{L}$ .

### <sup>67</sup> Causal estimand and potential outcomes

<sup>68</sup> Let  $a(s) = (\underbrace{0, \dots, 0}_{s-1}, 1, \dots, 1)$  be the strategy that initiates treatment at interval  $s \in$   
<sup>69</sup>  $\{1, 2, \dots, K+1\}$ . Let  $T_k^{a(s)}$  and  $Y_k^{a(s)}$  denote, respectively, the death indicator and number  
<sup>70</sup> of recurrent events that would have been observed in interval  $k$  under strategy  $a(s)$ . Formally,  
<sup>71</sup>  $T_k^{a(s)}$  is the potential death indicator following sequence  $a(s)$  up to interval  $k$ , and  $Y_k^{a(s)}$  is  
<sup>72</sup> the corresponding potential number of events.

<sup>73</sup> The target is the difference in average potential incidence rates over follow-up under two  
<sup>74</sup> initiation times:

$$\Delta(s, s') = \mathbb{E} \left[ \frac{\sum_{k=1}^K Y_k^{a(s)}}{K - \sum_{k=1}^K T_k^{a(s)}} \right] - \mathbb{E} \left[ \frac{\sum_{k=1}^K Y_k^{a(s')}}{K - \sum_{k=1}^K T_k^{a(s')}} \right].$$

### <sup>75</sup> Model specification

<sup>76</sup> The package runs a pair of discrete-time models conditional on shared treatment and covariate  
<sup>77</sup> terms.

<sup>78</sup> Here and throughout, we use overbar notation to denote the full history of the recurrent event  
<sup>79</sup> process up to the previous interval, i.e.,  $\bar{Y}_{k-1} = (Y_1, Y_2, \dots, Y_{k-1})$ .

- 80     1. Discrete-time hazard model for the terminal event that models death at a given interval  
 81       conditional on survival up to that interval:

$$\lambda_k(a_k, \bar{Y}_{k-1}, l) = \Pr(T_k = 1 \mid T_{k-1} = 0, a_k, \bar{Y}_{k-1}, l).$$

- 82     2. Distribution for the number of event occurrences in a given interval conditional on  
 83       survival through that interval:

$$f(y_k \mid a_k, \bar{Y}_{k-1}, l) = \Pr(Y_k = y_k \mid T_k = 0, a_k, \bar{Y}_{k-1}, l).$$

84     Here,  $f(y_k \mid a_k, \bar{Y}_{k-1}, l)$  denotes the Poisson probability mass function with conditional mean  
 85       (intensity)  $\mu_k(a_k, \bar{Y}_{k-1}, l) = \mathbb{E}[Y_k \mid A_k, \bar{Y}_{k-1}, L]$ . Together, these two models multiply to form  
 86       a joint model for the terminal and recurrent event occurrence at a given interval.

87     The functions in BayCauRETM implement the following models for the hazard and intensity,  
 88       respectively:

$$\begin{aligned} \text{logit } \lambda_k(a_k, \bar{Y}_{k-1}, l) &= \beta_{0k} + l^\top \beta_L \\ &\quad + y_{k-1} \beta_Y + \beta_A a_k, \\ \log \mu_k(a_k, \bar{Y}_{k-1}, l) &= \theta_{0k} + l^\top \theta_L + y_{k-1} \theta_Y + \theta_A a_k. \end{aligned}$$

89     The time-varying intercepts  $\{\beta_{0k}\}$  and  $\{\theta_{0k}\}$  parameterize the baseline hazard and event  
 90       intensity, respectively. They are assigned a first-order autoregressive (AR1) smoothing prior.  
 91       See Oganisian et al. (2024) for more details.

## 92     Posterior inference and g-computation

93     BayCauRETM conducts full posterior inference for the joint models using Stan (Carpenter et al.,  
 94       2017) through the rstan interface, since the posterior distribution is not available in closed  
 95       form. Stan is a probabilistic programming language that implements Hamiltonian Monte Carlo  
 96       to generate posterior draws.

97     For each parameter draw obtained from Stan, BayCauRETM simulates the joint death-recurrent  
 98       process under  $a(s)$  and  $a(s')$  to obtain a posterior draw of  $\Delta(s, s')$ . Reporting over many  
 99       draws yields posterior samples of  $\Delta(s, s')$ , as described by Oganisian et al. (2024). The  
 100       posterior mean and the 95% credible interval (2.5th and 97.5th percentiles) are reported.

## 101    Quickstart

102     Below we provide a minimal, copy-pastable example illustrating the core functionality of  
 103       BayCauRETM: fitting a joint recurrent-event and terminal-event model and estimating causal  
 104       effects under alternative treatment initiation strategies. A small example dataset is shipped  
 105       with the package, allowing users to run the example without any external data dependencies.

## 106    Installation and setup

107     We first install the development version of the package from GitHub and load the required  
 108       libraries. For reproducibility, we also set a random seed.

```
# install.packages("pak")
pak::pak("LnnnnYW/BayCauRETM")

library(BayCauRETM)
library(dplyr)
library(tidyr)

set.seed(123)
```

109    **Data loading**

110    The package ships with a small example dataset used in the demonstration code. The dataset  
 111    is stored in the package directory and can be loaded using `system.file()`. Loading this file  
 112    creates a data frame named `df` in the workspace.

```
# Load the example dataset shipped with the package
rdata_path <- system.file("demo_code", "data.Rdata", package = "BayCauRETM")
stopifnot(file.exists(rdata_path))
load(rdata_path) # loads an object named `df`
```

113    **Minimal preprocessing**

114    The data are assumed to be in long, person-interval format. For a fast illustrative run, we  
 115    subset the data to a small number of subjects and perform minimal preprocessing. This includes  
 116    ordering observations by subject and time, constructing a discrete time index, creating a lagged  
 117    event-count variable, removing incomplete cases, and standardizing continuous covariates.  
 118    These steps mirror the preprocessing required for real applications but are kept intentionally  
 119    simple here.

```
# Minimal preprocessing
df_fit <- df %>%
  filter(id %in% 1:50) %>% # subset for quickstart
  arrange(id, k) %>%
  mutate(k_fac = as.integer(factor(k, levels = sort(unique(k))))) %>%
  group_by(id) %>%
  mutate(lagYk = if ("lagYk" %in% names(.)) replace_na(lagYk, 0) else lag(Yk, default =
  ungroup()) %>%
  drop_na(Tk, Yk, Ak, L.1, L.2) %>%
  mutate(
    L.1 = as.numeric(scale(L.1)),
    L.2 = as.numeric(scale(L.2))
  )
  K <- length(unique(df_fit$k_fac))
```

120    **Model fitting**

121    We next fit the joint Bayesian model for the recurrent-event and terminal-event processes  
 122    using the main function `fit_causal_recur()`. The user specifies the outcome models through  
 123    standard R formula syntax, along with the relevant column names for subject ID, time index,  
 124    treatment, and lagged history. Here we use a single core and suppress verbose output for  
 125    speed.

```
# Fit the joint recurrent + terminal event model (small settings for illustration)
fit <- fit_causal_recur(
  data      = df_fit,
  K         = K,
  id_col    = "id",
  time_col  = "k_fac",
  treat_col = "Ak",
  lag_col   = "lagYk",
  formula_T = Tk ~ Ak + I(lagYk^2) + L.1 + L.2,
  formula_Y = Yk ~ Ak + I(lagYk^2) + L.1 + L.2,
  cores     = 1,
  verbose   = FALSE
)
```

<sup>126</sup> **Causal effect estimation via g-computation**

<sup>127</sup> Finally, we estimate causal effects corresponding to different treatment initiation strategies using  
<sup>128</sup> Bayesian g-computation. In this example, we compare initiation at two different time points.  
<sup>129</sup> The output summarizes posterior draws of the causal estimand, including point estimates and  
<sup>130</sup> uncertainty intervals.

```
# Bayesian g-computation for two treatment-start strategies
gcomp <- g_computation(
  fit_out = fit,
  s_vec   = c(3, 6),    # start at time 3 vs 6
  B       = 20,
  cores   = 1
)
print(gcomp)
```

<sup>131</sup> This quickstart demonstrates the full workflow of BayCauRETM, from data preparation and  
<sup>132</sup> model fitting to causal effect estimation. Detailed usage and example results are available on  
<sup>133</sup> [GitHub](#) (see the [demo PDF](#)).

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