

geospaNN: A Python package for geospatial neural

- ₂ networks
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Software

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Summary

Geostatistical models are widely used to analyse datasets with spatial information encountered frequently in the geosciences (climate, ecology, forestry, environmental sciences, and other

8 research fields). In geostatistics, the spatial linear mixed effects model (SPLMM)

$$Y = X\beta + \epsilon(s)$$

has long been the standard approach to model such data. SPLMM accounts for the fixed effects between observations Y and covariates X via the linear regression part, while accounting for the correlation across spatial locations s via the spatial error process $\epsilon(s)$. Typically, the spatial dependency embedded in $\epsilon(s)$ is modeled using a Gaussian Process, which provides a parsimonious and flexible solution to modeling spatial correlations and provide spatial predictions at new locations via kriging.

Recently, machine learning techniques like Neural Networks (NNs) have been increasingly incorporated into geostatistics to address complex and non-linear interactions among variables. In this paper, we introduce geospaNN, a Python software for analysis of geospatial data. geospaNN implements a novel adaptation of NN and simultaneously performs non-linear mean function estimation using a NN and spatial predictions (including prediction intervals) using Gaussian processes. For computational efficiency, geospaNN leverages the widely popular Nearest Neighbor Gaussian Process (NNGP) approximation Finley et al. (2019). It is also, to our knowledge, the first Python package to implement scalable covariance matrix computations in geostatistical models.

Statement of Need

geospaNN is a Python package for geospatial analysis that uses NN-GLS (Zhan & Datta, 2024), a novel and scalable class of NNs explicitly designed to account for spatial correlation in the data. The package is effectively represented as a geographically-informed Graph Neural Network (GNN) by using NNGP covariance matrices. It is embedded within the PyG framework, which is designed for scalable execution of GNNs on irregular data structures like graphs. geospaNN is primarily intended for researchers and scientists in machine learning and geostatistics, but can also be applied more generally to estimation and prediction tasks involving other data with dependency structures, like time-series. geospaNN provides lightweight, user-friendly wrappers for data simulation, preprocessing, and model training, which significantly simplify the analytical pipeline. A portion of geospaNN has already been used in articles such as Zhan & Datta (2024) and Heaton et al. (2024). In the future, we anticipate that geospaNN will play a significant role at the interface of machine learning and spatial statistics, serving as a foundation for both scientific and methodological explorations.

The implementation of NNGP models within geospann is of independent importance. NNGP enables scalable covariance matrix inversions, which features extensively in geospatial models.

There exist two widely used R-packages spNNGP (Finley et al., 2019) and BRISC (Saha & Datta,



- 2018) for implementations of NNGP, but to our knowledge there is no Python implementation
- of NNGP. We thus offer an avenue to efficiently analyze massive geospatial datasets in Python.

4 State of the field

45 In Python, to integrate geospatial data with deep learning, several specialized tools have

been developed. Notably, TorchGeo (Stewart et al., 2022) extends PyTorch (Paszke et al.,

2019) for tasks such as land cover classification, object detection, and geospatial segmentation.

Independently, the R package good (Maxwell et al., 2024) was recently introduced for analyzing

49 geospatial and spatiotemporal data. However, these tools primarily supports raster and vector

data, such as satellite imagery, which limits their general applications.

51 GNNs are the most common approaches for data with irregular geometry. It efficiently processes

52 graph-structured data by learning graph-level representations through message passing and

aggregation. For GNNs implementation, the PyTorch Geometric (PyG) library, provides a

highly customizable framework for defining graph convolutional layers (Fey & Lenssen, 2019).

55 GNNs have been widely applied in geospatial analysis, including crop yield prediction (Fan

et al., 2022), and traffic flow modeling (Wang et al., 2020). However, despite their growing

adoption, there is still no systematic analytical software tailored for broad use within the

58 statistical community.

59 The geospaNN Package

 $_{60}$ This section provides an overview of the geospaNN package, including the NN-GLS architecture

ond several technical details. For practical examples and detailed documentation, visit the

62 geospaNN website. A vignette is also available for detailed illustration of the package.

63 NN-GLS Overview

NNGLS considers a simple model for spatial data:

$$Y(s) = m(X(s)) + \epsilon(s)$$

where Y(s) and X(s) are respectively the outcome and covariates observed at location $s,\,m$ is

a non-linear function relating X(s) to Y(s), to be estimated using a NN. The key distinction

from the standard non-linear regression setup is that here the errors $\epsilon(s)$ is a dependent process

that models spatial correlation.

 $_{69}$ Let Σ be a model for the spatial error ϵ , then the well-known theory (Gauss-Markov theorem)

70 of OLS and GLS from the statistical literature motivates the introduction of a GLS-style loss

in NNs:

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$$L\big(m(\cdot)\big) = \frac{1}{n}\big(Y - m(X)\big)^{\top} \Sigma^{-1}\big(Y - m(X)\big).$$

However, minimizing this GLS-style loss in practice presents several challenges:

- 1. The covariance matrix Σ is based on a parametric covariance function, and the parameters are typically unknown.
- 2. Even if Σ is well-estimated, inverting Σ becomes computationally infeasible as the sample size n grows large.
- 3. Since the GLS loss is not additive across observations, mini-batching—an essential technique used in implementation of modern NNs—cannot be applied directly.

NN-GLS addresses these issues by introducing the NNGP to approximate Σ^{-1} , and it naturally equates to a specialized GNN. In brief, NNGP is a nearest-neighbor-based approximation to a full Gaussian Process with a specific covariance structure (Datta, 2022). NNGP sparsifies



the covariance matrix, thus simplifying both likelihood computation and the GLS-style loss, addressing the three issues mentioned above. Specifically, for the GLS loss function:

$$L\big(m(\cdot)\big) = \frac{1}{n}\big(Y - m(X)\big)^{\top} \Sigma^{-1}\big(Y - m(X)\big) = \frac{1}{n}\big(Y^* - m^*(X)\big)^{\top}\big(Y^* - m^*(X)\big) = \frac{1}{n}\sum_{i=1}^n (Y_i^* - m^*(X_i)) = \frac{1$$

where $Y^* = Q^{1/2}Y$ and $m^*(X) = Q^{1/2}m(X)$ can be obtained easily using aggregation over the nearest-neighbot directed acyclic graph specifying the NNGP approximation. The GLS loss returns to an additive form, allowing for mini-batching instead of full-batch training. In NN-GLS, the spatial parameters θ and the weights and biases parameters of the NN used to model m are estimated iteratively, and training proceeds until the validation loss converges. Once estimation is complete, nearest-neighbor-based kriging is used to generate spatial predictions at new locations. The whole procedure embeds the three core features of geospann,

- 1. estimate the non-linear mean function by \hat{m}_i
- $\hat{ heta}$ 2. estimate the spatial parameters by $\hat{ heta}$.
- 3. predict the outcome at new locations by \hat{Y} .

94 NNGP and Other Features

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In addition to estimation and prediction for spatial mixed models using NN-GLS, geospann offers a suite of additional features that support a wide range of geospatial analyses. geospann provides simulation module allowing users to customize the spatial parameters and mean functions to generate Y, X, and s. Users are allowed to customize the spatial coordinates to simulate under different context. geospann implements nearest neighbor kriging, an alternate to full kriging, which has been shown in Zhan & Datta (2024) to guarantee accurate prediction interval under various settings. For essential machine learning tasks, geospann offers modules including NN architecture design, training log report, and result visualization. geospann also implements SPLMM solution as a special case of NN-GLS. It should be an optimal choice for the Python users if efficient SPLMM solution is wanted for large geospatial datasets.

All these functions are included explicitly in the package and can be called independently (see vignette).

Discussion

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The geospaNN package offers an efficient implementation of NN-GLS approach proposed in Zhan & Datta (2024). NN-GLS embeds NN with the spatial mixed model, accounting for spatial correlation by replacing the original loss function with a GLS-style version. geospaNN is 110 capable of performing various statistical tasks, including non-linear mean-function estimation, 111 covariance parameter estimation, spatial prediction with uncertainty quantification. Due to the sparsity of the NNGP approximation, geospaNN is seamlessly integrated into the framework 113 of GNNs, opening up new possibilities for a wide range of advanced neural architectures. A promising future direction for geospaNN is to evolve into a general framework for geospatially-115 informed deep learning, where graph-based message-passing (convolution) can occur multiple times, with weights determined by spatial processes to maintain statistical interpretability. We are also planning to explore the extension of geospaNN towards other data types and 118 distributions in the future. 119

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