

- 1 rmcmc: Robust Markov chain Monte Carlo methods in
- $_{2}$  R
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#### Software

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23

# Summary

Generating samples from a probability distribution is a common requirement in many disciplines. In Bayesian inference, for example, the distribution of interest is the posterior over parameters of a model, given data assumed to be generated from the model. Expectations with respect to the posterior can be estimated using samples, allowing computation of posterior means, variances and other quantities of interest. *Markov chain Monte Carlo* (MCMC) methods are a general class of algorithms for approximately sampling from probability distributions.

rmcmc is an R package providing implementations of MCMC methods for sampling from distributions on  $\mathbb{R}^d$  for  $d \geq 1$ . It provides a general purpose implementation of the Barker proposal (Livingstone & Zanella, 2022), a gradient-based MCMC algorithm inspired by the Barker accept-reject rule (Barker, 1965). rmcmc also provides implementations of other MCMC algorithms based on random walk, Langevin and Hamiltonian dynamics. It has a flexible interface for performing adaptive MCMC so that algorithmic tuning parameters can be learned in a bespoke manner (Andrieu & Thoms, 2008; Haario et al., 2001). The key function provided by the package is sample\_chain, which samples a Markov chain with a user-specified stationary distribution. The chain is sampled by generating proposals and accepting or rejecting them using the Metropolis—Hastings (Hastings, 1970; Metropolis et al., 1953) algorithm. During an initial warm-up stage, the parameters of the proposal distribution can be adapted. Schemes are available to both tune:

- the scale of the proposals by coercing the average acceptance rate to a target value,
- the shape of the proposals to match covariance estimates under the target distribution.

## Statement of need

For target distributions with smooth density functions, gradient-based MCMC methods can provide improved sampling efficiency over simpler schemes such as *random-walk Metropolis* (RWM) in high-dimensional settings (Beskos et al., 2013; Roberts & Rosenthal, 1998; Roberts & Tweedie, 1996). For methods such as *Metropolis adjusted Langevin algorithm* (MALA) (Besag, 1994; Rossky et al., 1978) and *Hamiltonian Monte Carlo* (HMC) (Duane et al., 1987; Neal, 2011), this improved efficiency comes with a cost. Specifically these methods exhibit decreased robustness to tuning of the algorithm's parameters, compared to non-gradient based methods such as RWM (Livingstone & Zanella, 2022).

The Barker proposal provides a middle road. It offers similar efficiency in high-dimensional settings as other gradient-based methods such as MALA (Vogrinc et al., 2023), while allowing easier adaptive tuning of the algorithm's parameters. It also provides improved robustness to certain forms of irregularity, such as skewness, in the target distribution (Hird et al., 2020).

rmcmc fills a niche in the R statistical computing ecosystem, providing general purpose implementations of the Barker proposal, as well as RWM, MALA, and HMC. The package



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also supports several schemes for adapting the proposal parameters. Significant flexibility is available in specifying the log density of the target distribution, and its gradient. Users can:

- directly define functions to compute the log density and its gradient;
- specify a formula for the log density which will then be symbolically differentiated using the deriv function in the base R stats package (R Core Team, 2024);
- or define a model using Stan's modelling syntax via the R interface of BridgeStan (Carpenter et al., 2017; Roualdes et al., 2023).

The package has a modular design, allowing users to easily try out different algorithmic components and options, and to extend the package with new algorithms. This is exemplified in the Barker proposal implementation, which supports customizing the distribution over the auxiliary variables used in generating the proposal. As discussed in Vogrinc et al. (2023) and illustrated in a package vignette, this can significantly improve sampling efficiency in some cases.

rmcmc has a pure R codebase with minimal required dependencies, making it a lightweight addition to other projects. The package also interfaces with several others in addition to BridgeStan. For instance, a wrapper around the *robust adaptive Metropolis* (RAM) (Vihola, 2012) adaptation scheme in the ramcmc package is provided (Helske, 2021). The sampled chain traces can also be directly passed to functions for computing summary statistics and convergence diagnostics in the posterior or coda packages (Bürkner et al., 2024; Plummer et al., 2006).

## Related software

Several other R packages provide implementations of MCMC methods. mcmc (Geyer & Johnson, 2023) provides a general purpose implementation of RWM, along with a 'morphometric' variant (Johnson & Geyer, 2012), which reparametrizes the target distribution to improve efficiency.

MCMCpack (Martin et al., 2011) focuses on providing customized MCMC methods for specific classes of statistical model that exploit the structure of the model, though it does also provide a general purpose RWM implementation. fmcmc (Yon & Marjoram, 2019) is similar in design to rmcmc. It provides a modular framework with a variety of pre-defined proposals such as Gaussian and uniform RWM, and adaptive methods such as RAM and adaptive Metropolis (Haario et al., 2001). None of mcmc, MCMCpack or fmcmc provide gradient-based MCMC methods, which can significantly improve sampling efficiency, as discussed above.

The GitHub repository gzanella/barker (Zanella, 2019) contains code to recreate the numerical experiments in Livingstone & Zanella (2022), and provides a basic implementation of the Barker proposal. The R scripts in the repository are not, however, structured into a package, complicating reuse in other projects. The implementation also only provides support for sampling from the proposal and evaluating its log density ratio.

Stan and NIMBLE (de Valpine et al., 2017), with associated R interfaces rstan (Stan Development Team, 2024) and nimble (de Valpine et al., 2024), are probabilistic programming languages (PPLs), domain specific languages for the specification of probabilistic models. Both Stan and NIMBLE also provide implementations of a variety algorithms to perform inference in models defined via their PPLs, and in particular both offer gradient-based MCMC methods.

Stan's default MCMC implementation is a HMC method, which dynamically sets the trajectory lengths when simulating Hamiltonian dynamics to generate proposals (Betancourt, 2017; Hoffman & Gelman, 2014). Stan also includes schemes for adapting an algorithm's scale (step-size) and shape (metric) parameters, but with limited user-flexibility. Stan also does not currently provide an implementation of the Barker proposal. rmcmc does also offer a basic HMC implementation, but currently only supports HMC with static or randomized trajectory lengths. One of the proposal scale adaptation schemes implemented in rmcmc, is a dual-averaging



- algorithm (Hoffman & Gelman, 2014; Nesterov, 2009). This matches the corresponding scheme in Stan, but in contrast to Stan alternative schemes are available in rmcmc.
- 91 NIMBLE supports defining both models and statistical algorithms in its PPL. It provides
- implementations of a variety of MCMC methods including, RWM, HMC (Turek et al., 2024),
- 93 and the Barker proposal. Compared to rmcmc, NIMBLE's Barker proposal implementation
- <sub>94</sub> is tightly integrated into the broader NIMBLE framework. This means it can only easily be
- <sub>95</sub> applied to models specified in NIMBLE. NIMBLE's Barker proposal implementation provides
- <sub>96</sub> support for adapting the proposal scale and shape parameters. However, unlike <code>rmcmc</code>, the
- <sub>97</sub> adaptation scheme provided is fixed, without an ability to swap in alternative adaptation
- 98 schemes.

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179

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