




FR0STIE: A Python Package for Analysis of Reflectance Spectroscopy of Airless Planetary Surfaces

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Software

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Summary

Reflectance spectroscopy is one of the most powerful remote sensing tools in planetary science. By measuring how sunlight reflects off an airless planetary surface across different wavelengths, scientists can identify surface compositions, constrain physical properties such as grain size and porosity, and investigate processes like radiation weathering. However, the extraction of quantitative information from reflectance spectra is complicated by the presence of strong degeneracies between these parameters (see [Figure 1](#)).

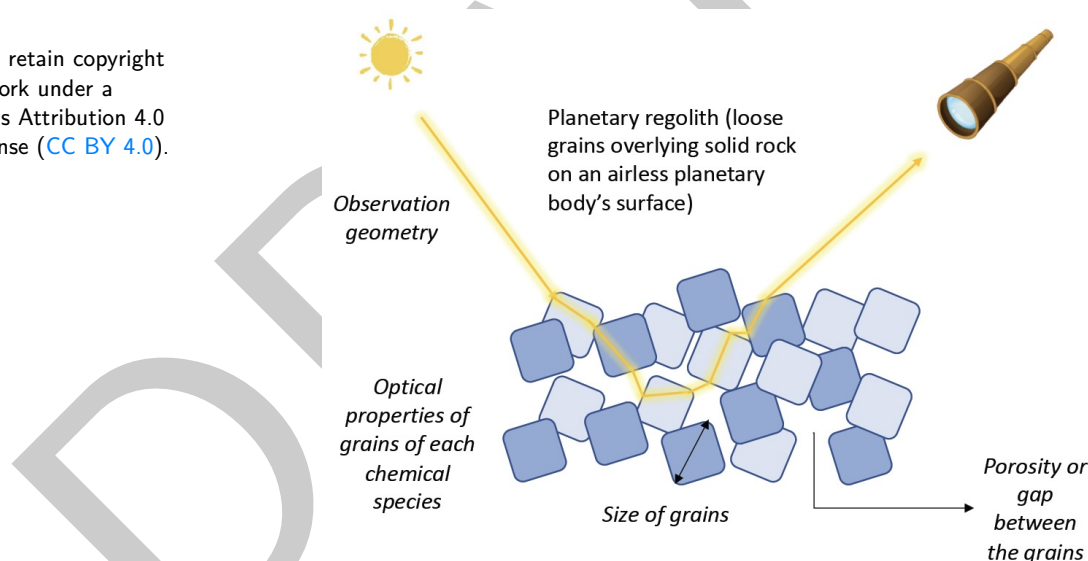


Figure 1: A schematic diagram showing some of the key parameters affecting reflectance from a planetary surface.

FR0STIE is an open-source Python package designed to address this challenge. It combines analytical radiative transfer modeling with modern Bayesian inference techniques, enabling robust and reproducible analysis of reflectance spectra. Specifically, FR0STIE provides tools to (1) forward model the reflectance spectrum of planetary regoliths using Hapke theory, and (2) perform statistical retrievals to infer best-fit parameters and their uncertainties. This approach is particularly useful in dealing with picking out weak signals in spectroscopic data, such as of trace molecules like organics.

FR0STIE is written in Python, with a modular design and comprehensive documentation to make it accessible for students and researchers alike. By adopting a Bayesian framework,

22 FROSTIE facilitates parameter estimation, model comparison, and exploration of degeneracies,
23 offering an intuitive and rigorous way to interpret spectral data.

24 Statement of Need

25 The Hapke model (Hapke, 1981, 2012) is a widely used analytical framework for simulating
26 reflectance from particulate surfaces, and has been applied in planetary science for decades
27 (Ciarniello et al., 2011; Fernando et al., 2016; Fornasier et al., 2024; Helfenstein & Veverka,
28 1987; McEwen, 1991; Mishra, Lewis, Lunine, Helfenstein, et al., 2021; Mishra, Lewis, Lunine,
29 Hand, et al., 2021; Poulet et al., 2002; Protopapa et al., 2017). However, due its complicated
30 nature and numerous parameters, most published studies have used simplified approaches to
31 extract its parameters from data—often relying on grid searches or manual tuning to find
32 best-fit solutions. These methods explore a limited volume of the model’s parameter space and
33 do not easily provide uncertainty estimates, or evaluate the statistical significance of detected
34 components.

35 Bayesian methods offer a natural solution to this problem and have a long-standing history
36 in planetary science subfields such as geophysics and atmospheric remote sensing. Despite
37 this, their application to surface reflectance spectroscopy has been limited. Recent studies
38 (e.g., Belgacem et al., 2020; Lapotre et al., 2017; Mishra, Lewis, Lunine, Helfenstein, et al.,
39 2021; Mishra, Lewis, Lunine, Hand, et al., 2021) have begun to demonstrate the advantages of
40 probabilistic approaches for reflectance analysis, but no widely adopted, open-source software
41 package has existed to implement these techniques—until now.

42 FROSTIE fills this gap by integrating Hapke forward modeling with nested sampling using the
43 dynesty package (Speagle, 2020), enabling rigorous parameter estimation and model comparison.
44 This makes it uniquely suited for analyzing complex surface mixtures, and especially helpful
45 when working with limited or noisy data.

46 While legacy tools like Tetracorder (Clark et al., 2024) offer comprehensive spectral mod-
47 eling capabilities, they are written in C and Fortran and lack a built-in retrieval framework.
48 FROSTIE aims to provide a lightweight, flexible, and Pythonic alternative for modern planetary
49 spectroscopy research.

50 Reflectance spectroscopic modelling and retrieval using FROSTIE

51 At its core, FROSTIE simulates reflectance spectra based on user-specified surface parameters
52 (e.g., abundances, grain sizes, porosity) and a set of optical constants. The model spectrum is
53 convolved with instrumental response functions, allowing for direct comparison to observed
54 data. The retrieval module employs a nested sampling algorithm to explore parameter space
55 (Speagle, 2020), construct posterior distributions, and compute the Bayesian evidence. A
56 schematic of the architecture of FROSTIE is presented in Figure 2.

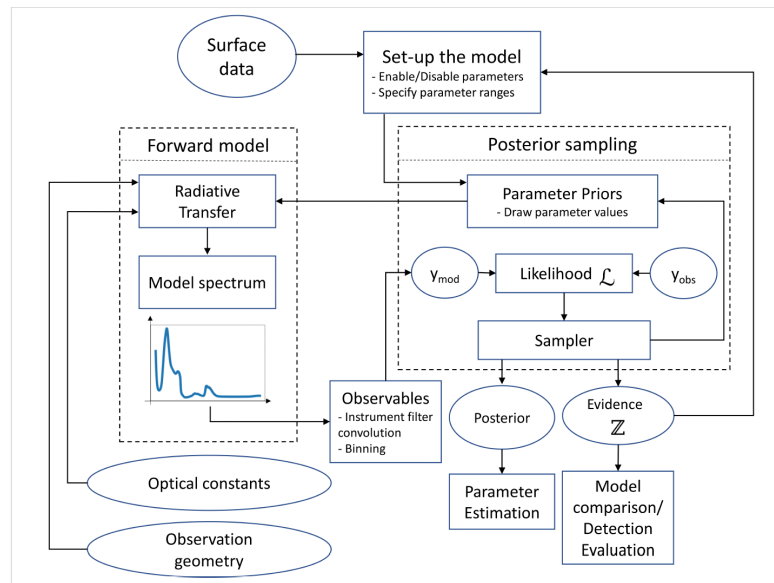


Figure 2: The architecture of FROSTIE. This schematic is inspired from POSEIDON (MacDonald, 2023; MacDonald & Madhusudhan, 2017)

Bayesian evidence is a particularly powerful feature that enables users to test the necessity of including specific components in a spectral model (MacDonald & Madhusudhan, 2017; Mishra, Lewis, Lunine, Helfenstein, et al., 2021). For instance, if adding a candidate species improves the Bayesian evidence, this can be interpreted as quantitative support for its detection. This statistical rigor surpasses traditional methods that rely on reduced chi-squared or arbitrary thresholds.

FROSTIE has been described in detail in published works, which also validate the framework using synthetic and laboratory spectra (Mishra, Lewis, Lunine, Helfenstein, et al., 2021; Mishra, Lewis, Lunine, Hand, et al., 2021). These studies applied FROSTIE to near-infrared datasets of Europa from the Galileo and Juno missions, modeling mixtures of water ice, sulfuric acid hydrates, CO₂, and SO₂. The Bayesian framework enabled quantitative constraints on surface composition, physical parameters like porosity, and statistical confidence in the presence of each species. More recently, FROSTIE has been used to simulate Europa Clipper observations and assess its ability to detect trace organic compounds via Bayesian model comparison (Mishra et al., 2025). These examples highlight FROSTIE's flexibility and scientific utility for planetary surface spectroscopy.

Future Developments

Future developments for FROSTIE aim to expand both its modeling capabilities and accessibility. Planned features include a graphical interface for interactive spectral fitting, support for photometric studies and thermal emission spectroscopy, and implementation of alternative reflectance models (e.g., Douté & Schmitt, 1998; Stamnes et al., 2017). A new module is under development to invert optical constants from reflectance spectra—addressing a major bottleneck in surface modeling due to the limited availability of laboratory data. Additionally, computational efficiency improvements such as JIT compilation and GPU support will be explored, along with cloud-hosted environments to allow users to run analyses without requiring local installation.

Documentation

Documentation for FROSTIE, with step-by-step tutorials illustrating research applications, is available at <https://frostie.readthedocs.io/en/latest/index.html>.

Acknowledgements

FROSTIE depends on many open-source Python tools, including NumPy (Harris et al., 2020), SciPy (Jones et al., 2001--), matplotlib (Hunter, 2007), Jupyter (Kluyver et al., 2016), dynesty (Speagle, 2020), and corner (Foreman-Mackey, 2016).

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