




# 1 Pywaterflood: Well connectivity analysis through 2 capacitance-resistance modeling

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## Software

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## 5 Summary



6 Well connectivity analysis has many applications for subsurface energy, from waterfloods to  
7 CO<sub>2</sub> floods to geothermal. Capacitance Resistance Modeling is useful for performing well  
8 connectivity analysis with limited information about the geology of the reservoirs involved.  
9 They are so-called because the equations describing well influence mimic a network of capacitors  
10 and resistors.

11 Pywaterflood is a Python package that uses Capacitance Resistance Modeling to estimate well  
12 connectivity. The CRM submodule forms the bulk of this package. It can perform capacitance  
13 resistance modeling with differing levels of complexity, from assuming that producing and  
14 injecting wells share one universal time constant, to each producer has the same time constant  
15 with all injectors, to each producer-injector pair has an its own time constant. CRM was  
16 developed by Yousef et al. (2006). The MPI submodule uses a geometrical model of well  
17 influence (Valko et al., 2000), extended and applied to reservoirs with both injecting and  
18 producing wells (Kaviani & Valko, 2010).

## 19 Statement of need

20 Interwell connectivity analysis is important for understanding the geology of subsurface systems.  
21 This can be used to improve oil recovery efficiency (Albertoni & Lake, 2003), better sequester  
22 CO<sub>2</sub> (Tao & Bryant, 2015), and optimize geothermal fields (Akin, 2014).

23 Pywaterflood uses a reduced-physics model to match connections between injecting and  
24 producing wells. As explained in Holanda et al. (2018), capacitance-resistance modeling  
25 provides a method for connectivity analysis more sophisticated than empirical decline analysis,  
26 but more approachable than full reservoir simulation.

27 There is another publicly available tool for capacitance resistance modeling reservoirs like  
28 pywaterflood (Sayarpour, 2008). However, that tool comes in the form of an Excel workbook  
29 and no associated license. This python package provides more extensibility and better performance  
30 than an Excel file. There are other programs for performing waterflood analysis with  
31  in the industry, but they are not open sourced  available for researchers to use.

32 The pywaterflood library can perform the following tasks:

- 33 1. Estimate connectivity between wells in fluid or pressure communication
- 34 2. History-match and forecast the production of wells in waterfloods, CO<sub>2</sub> floods, or  
35 geothermal fields
- 36 3. Provide purely geometric estimates of well connectivity before production data is available

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46 This project relies on the following open-source Python packages: NumPy (Harris et al., 2020;  
47 Walt et al., 2011), SciPy (Virtanen et al., 2020), and pandas (McKinney, 2010). It also uses  
48 the Rust crates ndarray, numpy, and pyo3.

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