

Hyperelastics.jl: A Julia package for hyperelastic material modelling with a large collection of models

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Hyperelastics.jl is a Julia (Bezanson et al. 2017) implementation for the largest (70+) collection of hyperelastic material models in existence. The package provides a set of analytical and data-driven strain energy density functions (SEDF) and the tools required to calibrate the models to material tests. The package is designed to leverage multiple-dispatch to define a common set of functions for calculating the SEDF, Second Piola Kirchoff stress tensor, and the Cauchy stress tensor. The package provides: 1) a material model library that is AD compatible and 2) a set of extensible methods for easily defining and testing new material models. The package leverages the ContinuumMechanicsBase.jl pacakge for defining the continuum scale quantities and their corresponding relationships.

Statement of Need

The development of Hyperelastics. jl began as a study of the accuracy for a variety of material models for a set of experimental data. Often, researchers rely on custom implementations of material models and the data fitting process to find material parameters that match their experimental data. Hyperelastic models can well represent the nonlinear stress-deformation behavior of many biological tissues (Wex et al., 2015) as well as engineering polymeric materials (Beda, 2014). Such material models find applications in developing new materials (Zhu et al., 2024), understanding biological tissue mechanical response (Agarwal & Pelegri, 2024), and soft robotics (Dalklint et al., 2024).

The SEDFs included in this package cover most (if not all) of the available analytical models 24 from the literature to date, from constitutive to phenomelogical models. Furthermore, a 25 selection of data-driven models are incldued as a starting point for the development of new 26 methods. 27

Hyperelastics.jl is part of a spinoff Multi-Scale Material Modelling (M^3) Suite being 28 developed by Vagus LLC (www.vagusllc.com), as a byproduct result of ongoing multi-functional 29 material research being carried out in the Translational Robotics and Controls Engineering Research (TRACER) Lab at Liberty University. A pure Julia implementation allows for the 31 use of automatic differentiation (AD) packages to calculate the partial derivatives of the 32 SEDF. Hyperelastics.jl is designed to leverage multiple-dispatch to define a common set of 33

functions for calculating the SED, Second Piola Kirchoff Stress Tensor, and the Cauchy Stress 34 Tensor. The package provides a set of hyperelastic models and an interface to Optimization.jl 35

(Dixit & Rackauckas, 2023) for fitting model parameters. 36

- Currently, most commercial finite element codes only offer a limited number, often less than 37
- 10, of hyperelastic models which limits the extent to which researchers are able to accurately 38
- model a given material. The closest project to Hyperelastics.jl is the matADi project by 39
- Andreas Dutzler (Dutzler, 2023) which has AD support for 18 material models. 40

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⁴¹ Comparison with Similar Packages

 $_{\tt 42}$ $\,$ Similar to the matADi project by Andreas Dutzler, Hyperelastics.jl provides AD compatible $\,$

- implementations of hyperelastic models. However, Hyperelastics.jl provides a significantly
- ⁴⁴ larger set of material models and offers the potential for including different compressible ⁴⁵ material model terms. matADi does include models for anisotropic hyperelastic materials which
- material model terms. matADi does include models for anisotropic hyperelastic materials which is not support in the current version of Hyperelastics.jl. matADi is focused on python based
- is not support in the current version of Hyperelastics.jl. matADi is focused on python bas
 implementations while Hyperelastics.jl is a pure Julia implementation.
- For using material models in a simulation, the leading commercial finite element analysis (FEA) programs, such as Abagus, Ansys, and LS-DYNA, provide a significantly smaller set
- of hyperelastic models (often less than 10). Implementing a new model in the commercial
- programs is often a complex and time-consuming process requiring explicit definition of different
- 52 partial derivative terms. Furthermore, the model implementations are not compatible between
- ⁵³ commercial programs. To fill the commercial gap, PolymerFEM link provides a slightly larger
- set of models for implementation with a focus on visco-elastic and visco-plastic models. From
- the initial work done with Hyperelastics.jl, it is expected that the AD compatibility will allow
 for a significant improvement in terms of model construction for visco-hyperelastic models.
- 56 for a significant improvement in terms of model construction for visco-hyperelastic models. 57 More recently, Wan et al. (Wan et al., 2024) implemented over 70 hyperelastic material
- models as Abaqus subroutines. The implementation is not AD compatible and is limited to
- ⁵⁹ the Abaqus FEA software.
- The Hyperelastics.jl package aims to fill the gap of providing an open-source and AD compatible implementation of the largest set of Hyperelatic material models available. ADcompatibility reduces the time from model selection to implementation when compared to implementing a new model in a commercial program. Furthermore, the open-source nature allows for the models to be accesible to researchers for further study.

⁶⁵ Use Case: Fitting a Hyperelastic Model to Experimental Data

The common workflow for modelling a new hyperelastic material is shown in figure Figure 1. 66 The package is available for Julia 1.9 and above on all support operating systems. The process 67 commonly begins with the user proving a set of stress-stretch data for a set of uniaxial and/or 68 biaxial tension/compression experiments. The data is loaded into HyperelasticUniaxialTest 69 or HyperelasticBiaxialTest depending on the nature of the experiment. If the material is as-70 sumed to be incompressible, the data for the other principal stretches is calculated. The selection 71 of hyperelastic models is based on multiple dispatch. The primary functions for computations 72 are: StrainEnergyDensity, SecondPiolaKirchoffStressTensor, and CauchyStressTensor. 73 The Second Piola-Kirchoff and Cauchy Stress Tensors are computed by using the partial 74 derivatives of the strain energy density function. By using AD, the implementation of partial 75 derivatives for the majority of the models can be skipped. Furthmore, extensions are provided 76 to load compatible AD functions based on the AD-backend selected. Material models are 77 considered as structs and multiple dispatch is used to select the correct equation for the given model. The model parameters are similarly stored in either structs, NamedTuples, or 79 other field-based data-types such as those in ComponentArrays.jl and LabelledArrays.jl. 80

Once a user has their experimental data, model, and model parameters, an extension is loaded when Optimization.jl is used to load a function for calibrating the material model to the experimental data. The HyperelasticProblem function take the experimental data, model, model parameters, and AD-backend and creates an OptimizationProblem for use with the solvers from Optimization.jl. Once the model is calibrated, the predict function is used to predict the response of the model to the experimental data. The results are can then be plotted to compare the experimental data to the model prediction.

- 88 Additionally, by leveraging multiple dispatch, a selection of data-driven hyperelastic material
- ⁸⁹ models have been implemented for use with the same interface as the analytical models. This



- allows for rapid development of new models and the inclusion of new data-driven models as they become available.
- ⁹² Lastly, with the optimized model parameters, the material model is able to be implemented
- ⁹³ into a larger simulation or analysis. Some examples would include performing a finite element
- ⁹⁴ simulation with Gridap.jl or Ferrite.jl or interpreting the model parameters in the context
- ⁹⁵ of the material microstructure. The package is designed to be extensible and to allow for the
- ⁹⁶ rapid development of new models and the inclusion of new data-driven models as they become
- 97 available.

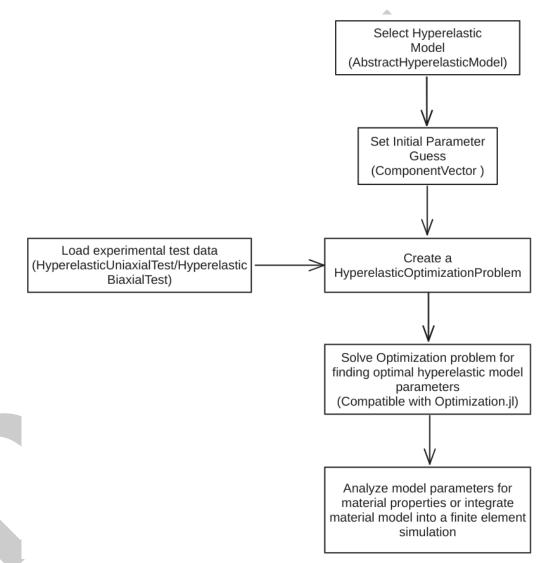


Figure 1: The most common use case for Hyperelastics.jl is to go from experimental or *ab initio* stress-stretch data for uniaxial or biaxial test(s) and proceed to fit and implement the model into a larger simulation or analysis. The respective data types used throughout the process are shown in the figure.

Example Usage

⁹⁹ For an example of going from experimental data to fitting a model, refer to the package documentation.



Availability

¹⁰² Hyperelastics.jl can be found on github.

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