

Flint: a simulator for biological and physiological models in ordinary and stochastic differential equations

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Introduction

Understanding dynamics of living organisms often requires a rigorous mathematical model that describes the hypotheses to be tested. It is widely recognized that the class of ordinary differential equations (ODE) is suitable for describing the time course of variables in a deterministic system, stemming from a simple assumption about the rate of their change. One of such examples is the chemical reaction accelerated by an enzyme following the Michaelis-Menten kinetics; another is the action potential of cardiac cells driven by modulation of ion channels. By a virtue of differential equations, these cellular models can be integrated into the one of tissue or organ level. In fact, the way to integrate a computational model of the physiological functions of the whole individual has been explored since the end of the last century, under the name physiome (Leem, 2016).

It is, however, technically challenging for practitioners in the field of biology or physiology to express their hypotheses on biological organisms in a precise system of ODEs. In order to make it easier to edit a model in problem that implicitly specify the ODEs, several domain-specific languages have been proposed and standardized, including CellML (Lloyd, Halstead, & Nielsen, 2004), the Physiological Hierarchy Markup Language (PHML) (Asai et al., 2015), and the Systems Biology Markup Language (SBML) reported by (Hucka et al., 2003). Although the design principle of each modeling language varies, computational analysis of any model in these languages comprises the shared set of procedures based on the theory of differential equations and dynamical systems.

In this work we introduce *Flint*, a simulator software for models written in the above languages. The simulator allows users to transform a given model into a system of ODEs and solve it in a numerical manner. It also supports stochastic differential equations (SDE), a non-deterministic extension of ODEs, which makes it possible to involve random elements, e.g. noises, in the dynamics.

The development of *Flint* has been tied in with the *physiome.jp* project (Nomura, 2010), which aims to establish a computational platform for multiscale in silico studies on physiome. As part of the platform, *Flint* complements the features of an authoring software *PhysioDesigner* for PHML (Asai et al., 2012), while they are deliberately separated programs. Driven by demands from the project's collaborators, we have enhanced *Flint* to support different modeling standards. For example, in order to leverage a published SBML model of subcellular signaling to build tissue or higher-level physiological ones, there is a technical proposal embedding it in PHML (Asai et al., 2014). Simulating such models is a reason for adopting *Flint* even when other state-of-the-art tools are publicly available, e.g. *COPASI* (Hoops et al., 2006), focusing on its own format. ~~It is~~ *Flint's* main contribution to provide an open, language-agnostic resource for reproducible simulation studies.

↳ that focuses on?

↳ is

↳ not sure what constitutes rigorous in math modelling

Implementation

User interface

Flint is a standalone program that runs on consumer desktop environments such as Microsoft Windows, Apple's macOS, and Linux with GTK. For the simplest usage, its graphical user interface runs a simulation of a given model with only two steps; open the model file, and select the Run button. Running simulations at the command line is also supported, although only a limited number of the functions are available in the command line interface. The simulator delegate the task of displaying the output to gnuplot (Williams, Kelley, & many others, 2017).

Numerical algorithms to solve a system of differential equations

Flint compiles a model written in a supported XML language into bytecode of simulation, and then evaluates it with particular initial values. Our current implementation provides three algorithms for solving initial-value problems for ODEs numerically: the forward Euler method, the Runge-Kutta 4th-order method, and the additive Runge-Kutta scheme implemented in the SUNDIALS library (Hindmarsh et al., 2005). The Euler-Maruyama method is the one for solving SDEs (Higham, 2001).

not quite sure what is meant by this
byte code for a virtual machine?
used
byte code for simulation?

adaptive

Multithreading for parallel simulation

Solving an initial-value problem numerically is only the preliminary step to analyze the dynamics of the model. Further investigation often asks for the different values of initial values or parameters. For instance, hypotheses on biological switches has been stated in terms of bifurcation and demonstrated by a series of simulations changing the values of parameters, in both deterministic (Fussmann, Ellner, Shertzer, & Jr, 2000) and stochastic (Samoilov, Plyasunov, & Arkin, 2005) paradigms. Flint employs multithreading to increase the number of simulations running in parallel. The parallelization is automatically performed when the user assigns multiple values to some parameter of a model for simulation, and honors the number of available CPU cores, which can be adjusted in the preference.

Grid search algorithm for parameter fitting

The larger the number of variables and parameters in a given model are, the more resource-consuming its simulation becomes. It is also the case for estimating plausible values of parameters consistent with the prior knowledge on the behavior of the underlying system. Taking residual sum of squares (RSS) as a measure of the goodness of fit, estimation of parameter values for ODEs turns into a non-linear least-squares problem (Madsen, Nielsen, & Tingleff, 2004). Flint deals with the challenge the modeler faces when fitting the value of parameters via the least-squares method, taking advantage of multithreading if available. Given grid points in the parameter space as an input set, Flint performs the following branch-and-bound algorithm to reduce the number of simultaneously running jobs for the grid search:

```

Input : A set  $S$  of parameter values; timeseries data  $D$  of target
state variables
Output: An element of  $S$  with which simulated timeseries has the
least RSS against  $D$  in  $S$ 
 $m \leftarrow \infty$ ;
foreach  $e \in S$  do // in parallel
   $s \leftarrow 0$ ;
  start simulation with parameters  $e$  from  $t = 0$ ;
  foreach  $t$  found in  $D$  do // in the ascending order of time
    simulate until  $t$ ;
    increment  $s$  by the squared error at  $t$ ;
    if  $s \geq m$  then break;
  end
  if  $s = 0$  then
    | return  $e$ 
  else if  $s < m$  then
    |  $x \leftarrow e$ ;
    |  $m \leftarrow s$ ;
  end
end
return  $x$ 

```

Figure 1: An algorithm for grid search to fit parameter values.

This makes the algorithm sound novel when it isn't.

Unlike existing heuristics for solving non-linear least-squares, the above algorithm can find one of global minima, provided that the input grid contains it. It is also easy to benefit from parallel computing to reduce processing time. Users can define the range of each parameter as well as the way to enumerate grid points, e.g. by a pseudo random number generator. The feature will help researchers gain insight about a subset of parameter values of biological/physiological interest at an early stage of modeling.

of course, it's an exhaustive search!

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