

# Introduction to weather radar

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Pyrad course

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- The weather radar equation
- Polarimetry
- Doppler measurements
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# 1. Introduction

# Definition

RADAR = **RA**dio **D**etection **A**nd **R**anging



**Cambridge Dictionary** : a device or system for finding the position or speed of objects, such as aircraft, that cannot be seen, by measuring the direction and timing of short radio waves that are sent out and reflect back from the objects

# Purpose of a weather radar

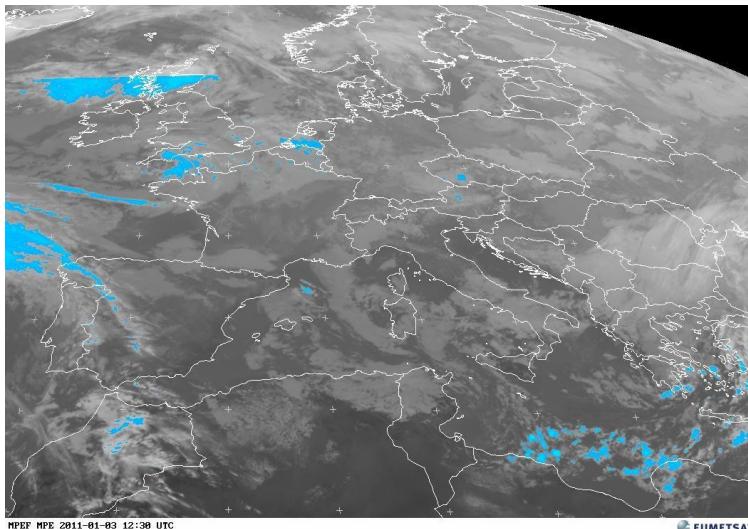
The main purpose of a weather radar is to locate precipitation, calculate its motion and intensity and estimate its type



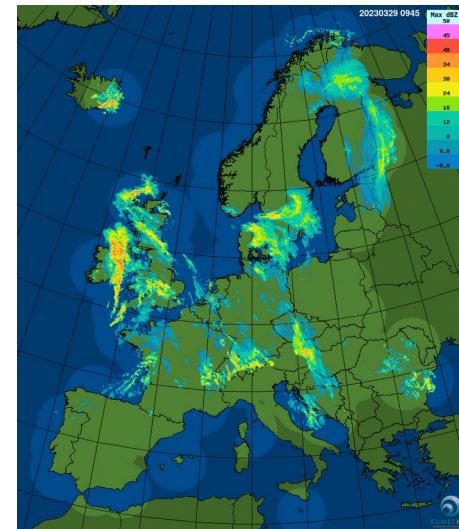
But other objects are also detected



# Instruments for precipitation detection



**MSG : Multi-Sensor  
Precipitation Estimate (MPE)**  
Continental scale  
15 min, 5 km  
Indirect measurement  
Better at low latitudes and for  
convective precipitation



**Radar networks:**  
Range up to 400 km  
~5 min, ~1 km  
Indirect measurement  
e.g. 33 radars in France



**Rain gauges networks :**  
0.1m scale  
~10 min, 1h, 24h  
Direct measurement  
e.g. 551 real time RG in  
France

# Why weather radar ?

Weather radar only instrument that provides :

- Real time measurements
- 3D images of precipitation
- High temporal and spatial resolution
- For a wide range of precipitation intensity (from drizzle to hail)
- At a long range (up to 400 km)

## BUT

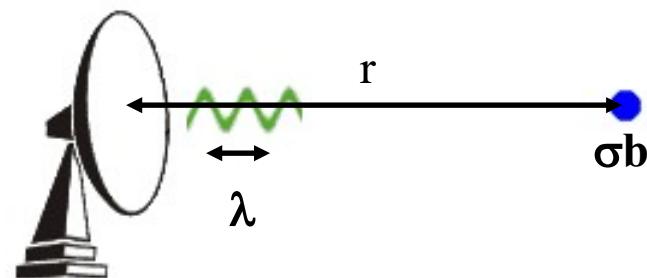
**It is an indirect measurement and a lot of effort is required to go from measured voltage to mm/h**

## 2. Principles of weather radar

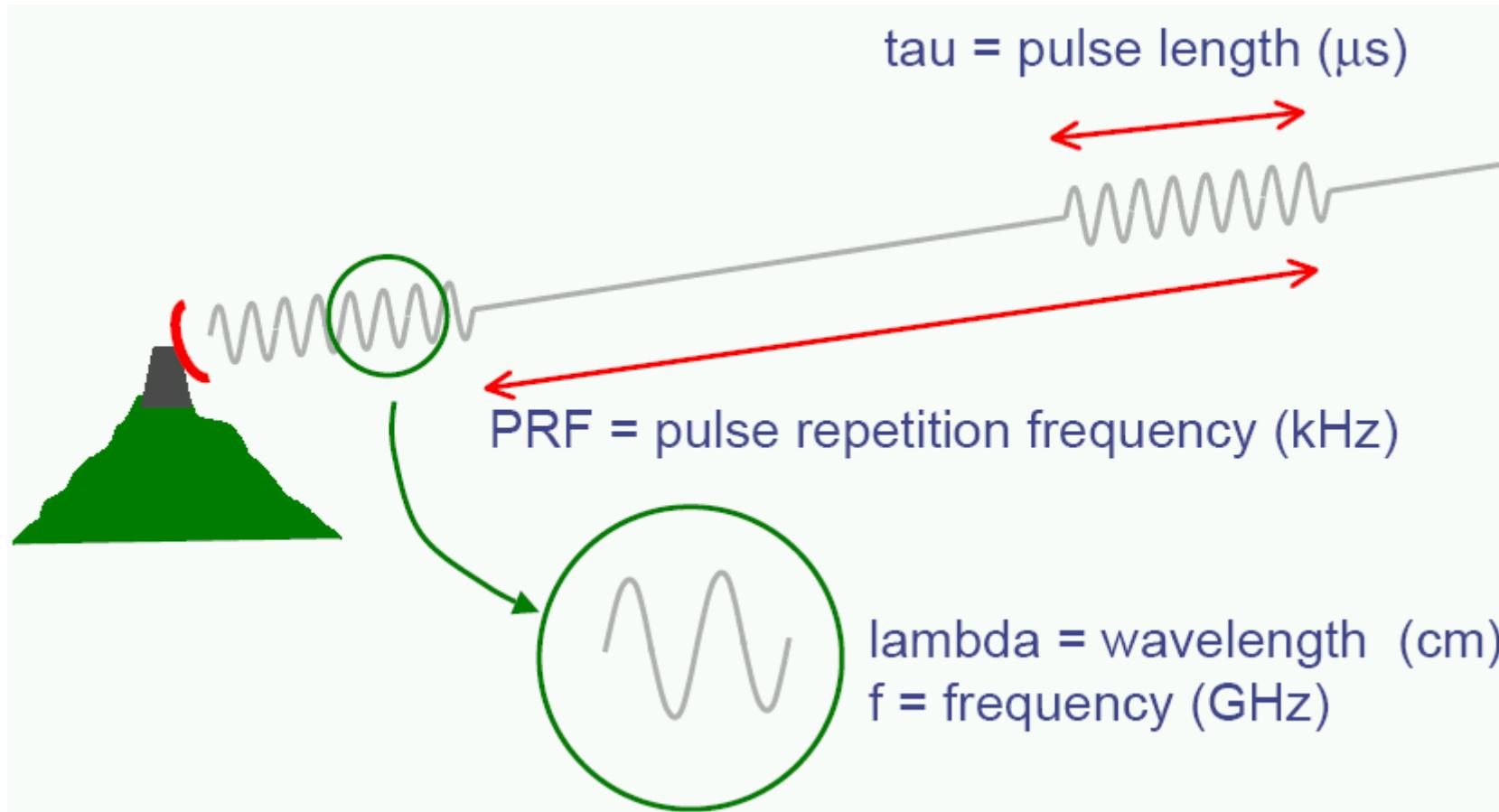
## How it works (pulsed radar)

Emission to the atmosphere at regular intervals (PRT) of a pulse of energy of short duration ( $\tau$ ) and high power  $P_t$  and frequency ( $f$ ,  $\lambda$ ). The pulse is emitted by a directive antenna observing at a certain elevation ( $\alpha$ ) and azimuth ( $\beta$ ) angles through a beam of angular size  $\theta$ .

The scatterers at a particular range ( $r$ ) absorb part of the energy and radiate in all directions. A small fraction of power ( $P_r$ ) is sent back to the radar.



# How it works



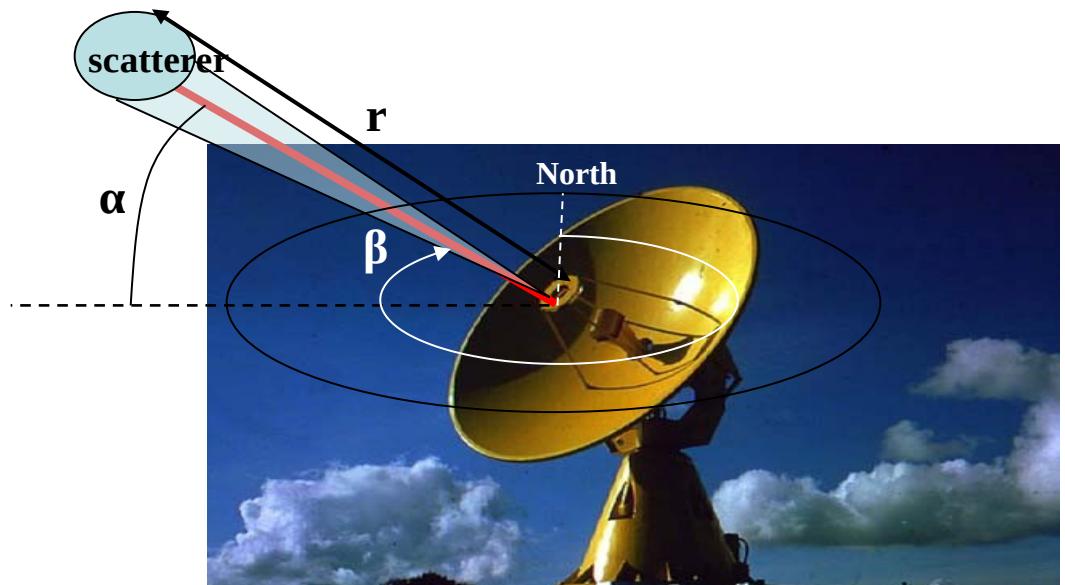
# How it works

Geographical location

Radial distance :  $r = \frac{c \Delta t}{2}$

Azimuth :  $\beta$

Elevation :  $\alpha$

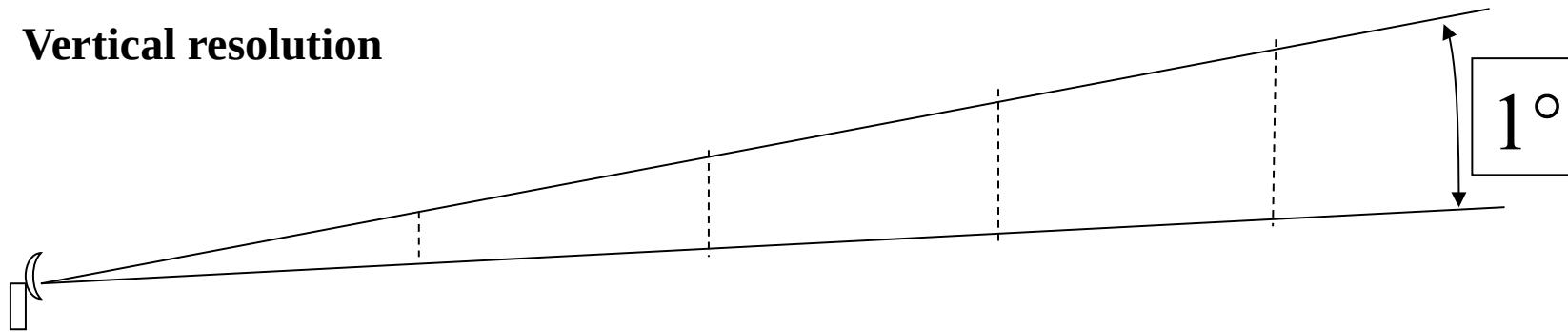


Physical properties

Received signal with respect to the distance of the scatterer

# Resolution

## Vertical resolution



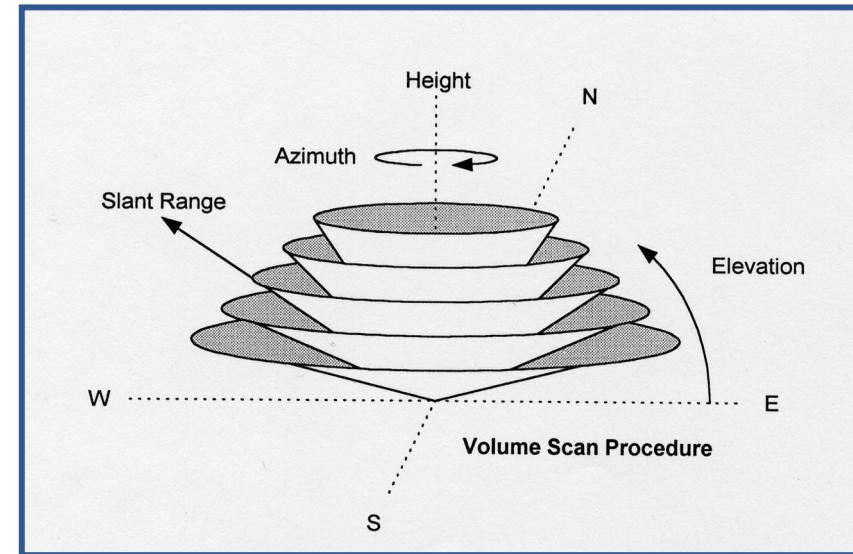
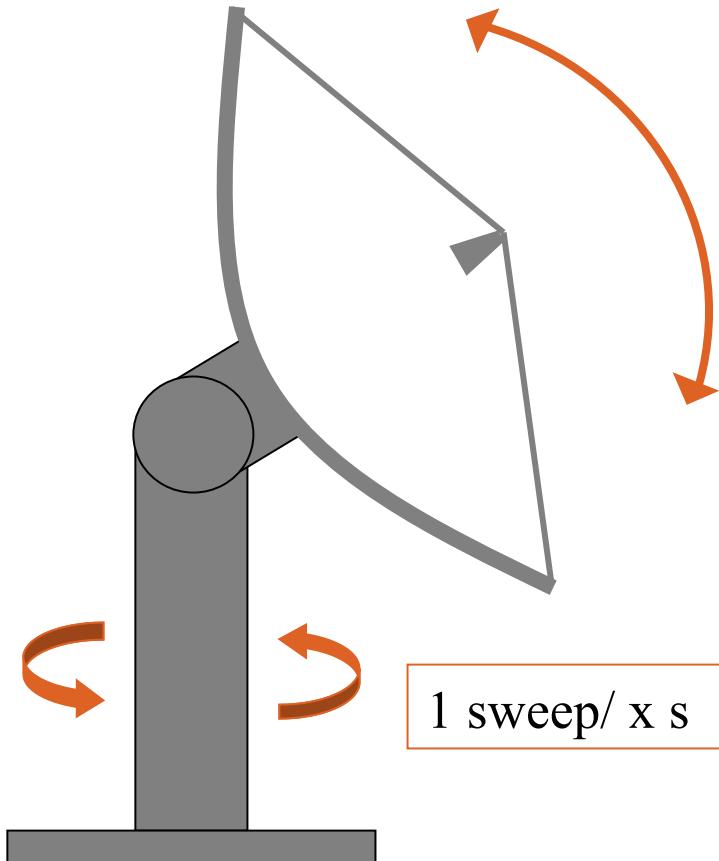
Range :	50 km	100 km	150 km	200 km
Vertical resolution :	0.9 km	1.8 km	2.6 km	3.5 km

**Horizontal resolution** in azimuth = vertical resolution

**Horizontal resolution** in distance: Depends on the speed of light and the pulse duration

$$\Delta r = \frac{c \tau}{2}$$

# Scanning strategy



# Radar wavelength

The choice of the radar wavelength is determined by the size of the scatterer that has to be observed.

The wavelength should be an order of magnitude larger than the scatterer

Larger wavelength require larger antennas to obtain the same beamwidth

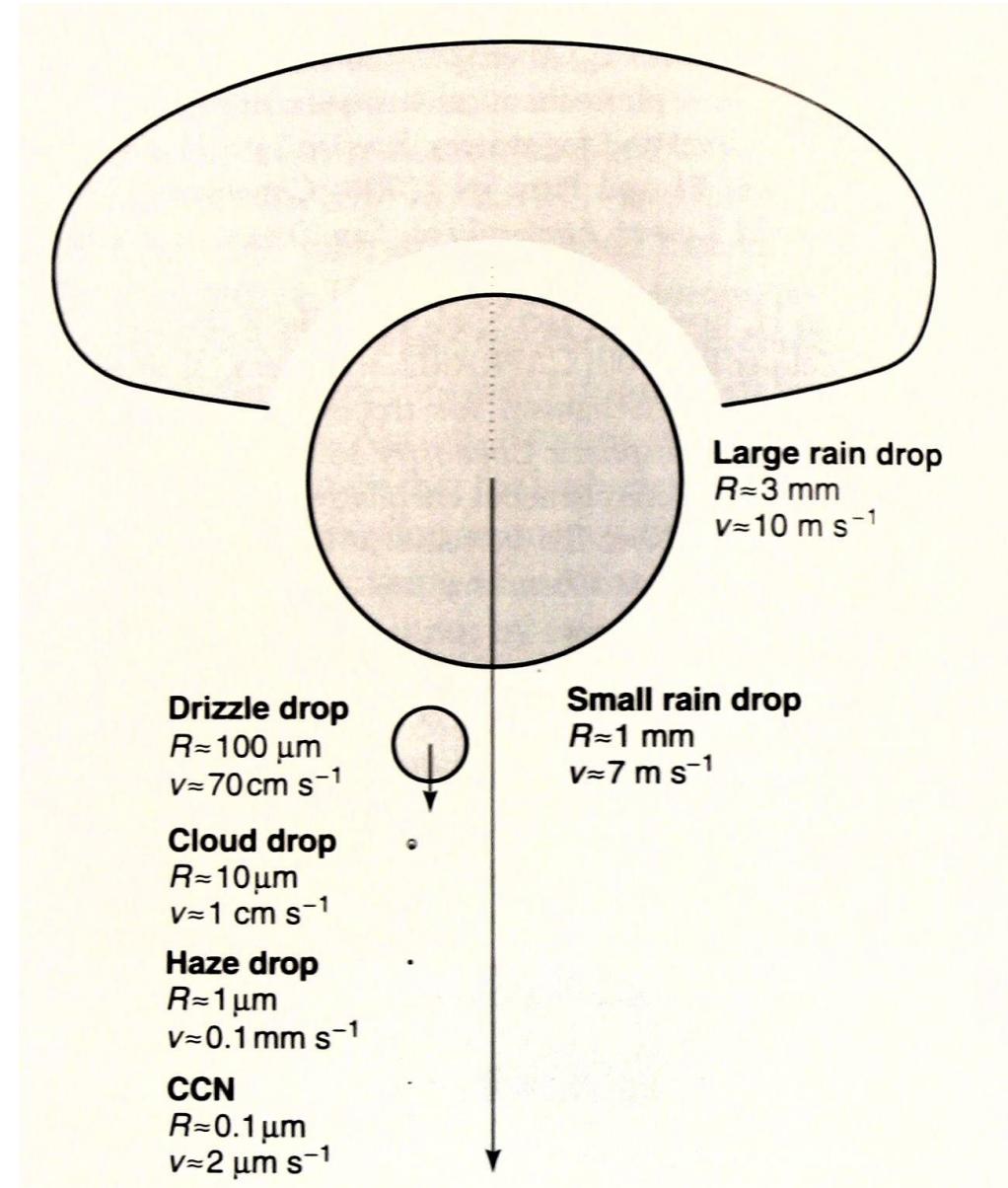
Typical hydrometeor sizes :

Drizzle drop : 0.1 to 0.5 mm

Rain drop : 0.5 to 5 mm

Snowflake : 2 to 5 mm

Hailstone : 5 to 50 mm



# Radar wavelength

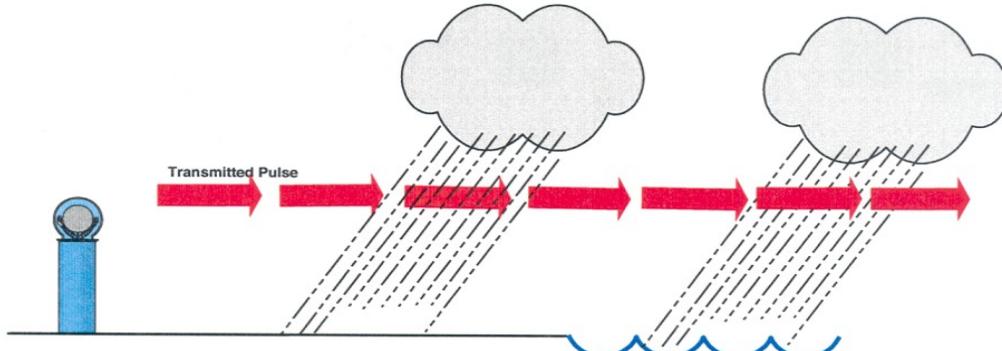


Figure 3a- Long Wavelengths Pass Through Precipitation And Produce No Useful Reflections

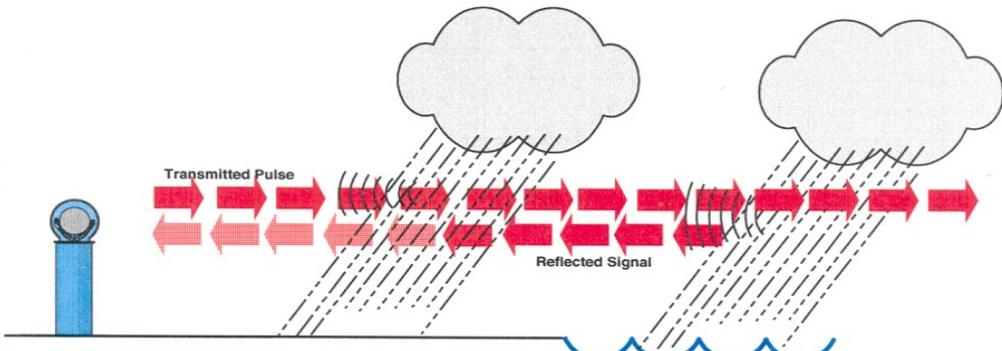


Figure 3b- Proper Wavelengths Pass Through Precipitation And Produce Useful Reflections

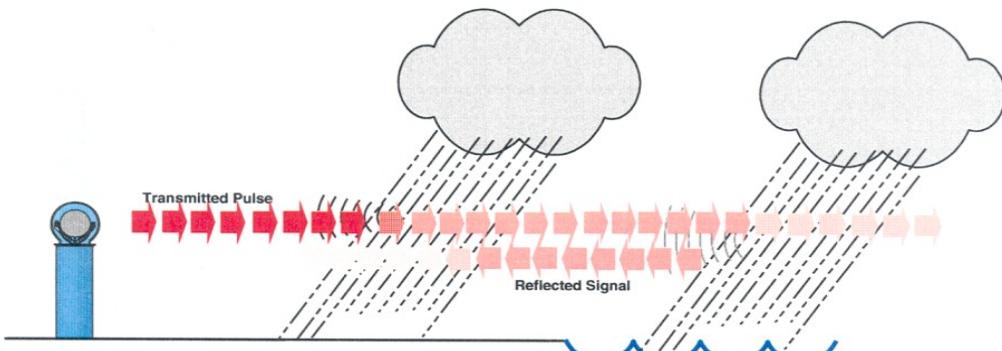


Figure 3c- Short Wavelengths Are Absorbed By Precipitation And Produce No Useful Reflections

# Radar wavelength

wavelength (cm)	1	3	5	10	20
frequency (GHz)	30	10	6	3	1.5
Band	K	X	C	S	L
usage	clouds	precipitation	precipitation	precipitation	aeronautical

### 3. The weather radar equation

# Radar equation for weather radar

Power density incident on target

$$P_r(r) = \underbrace{\frac{P_t}{4\pi r^2} G_t}_{\text{Power density at Rx antenna}} \underbrace{\frac{1}{4\pi r^2} \sigma(r)}_{\text{Rx antenna aperture}} \underbrace{\frac{G_r \lambda^2}{4\pi}}_{\text{Power density at Rx antenna aperture}}$$

Uniform beam filling  
Gaussian antenna pattern

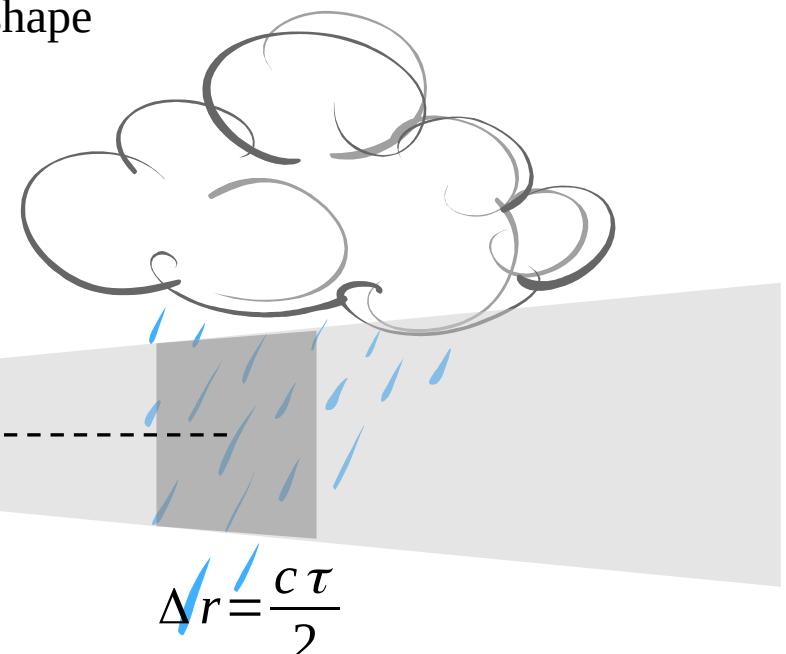
$$\sigma(r) = V(r) \sum_{\forall i} \sigma_i(r) = \pi r^2 \frac{\theta^2}{4} \frac{c\tau}{2 \ln 2} \sum_{\forall i \in V_{unit}} \sigma_i(r)$$

$$\sum_{\forall i \in V_{unit}} \sigma_i(r) = \sum_{\forall i \in V_{unit}} \frac{\pi^5 |K_w|^2 D_i^6(r)}{\lambda^4}$$

↑  
Rayleigh scattering  
Spherical shape

$$S_t = A_t e^{j\Phi_t}$$

$$S_r = A_r e^{j\Phi_r}$$



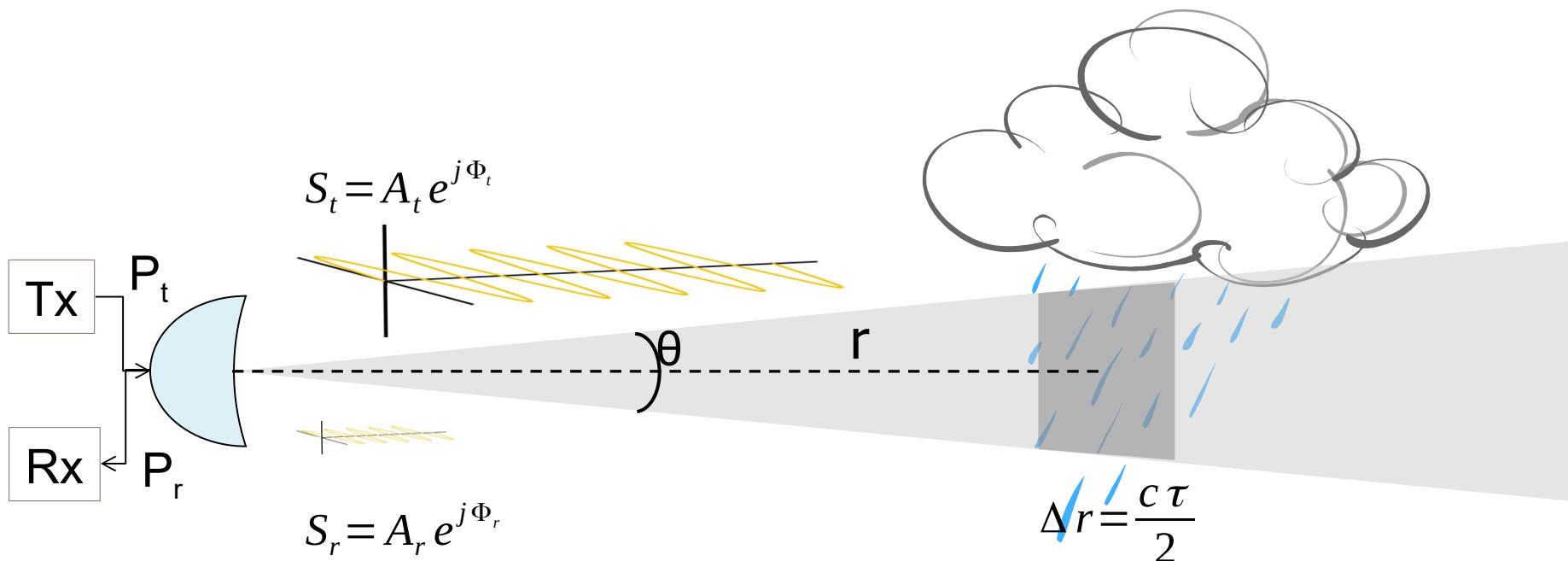
# Radar equation for weather radar

$$P_r(r) = \frac{P_t}{4\pi r^2} G_t \frac{1}{4\pi r^2} \sigma(r) \frac{G_r \lambda^2}{4\pi} = \frac{\pi^3 P_t G_t G_r \theta^2 \tau c}{1024 \ln 2 \lambda^2} \frac{1}{r^2} |K_w|^2 z(r) = \frac{|K_w|^2}{Cr^2} z(r); [W]$$

$$z(r) = \sum_{\forall i \in V_{unit}} D_i^6 = \int_0^\infty N(D, r) D^6 dD; \left[ \frac{mm^6}{m^3} \right]$$

$$LWC(r) = \int_0^\infty N(D, r) V_d(D) dD; \left[ \frac{mm^3}{m^3} \right]$$

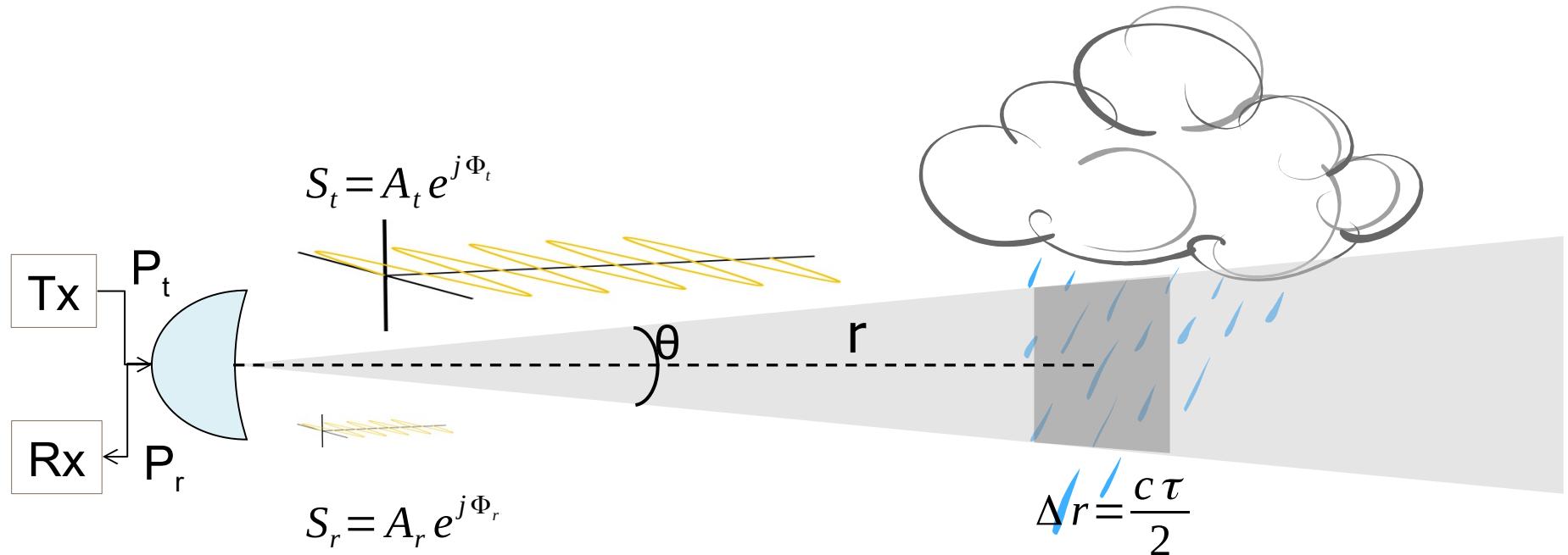
$$R(r) = \int_0^\infty N(D, r) V_d(D) v_t(D) dD; \left[ \frac{mm}{h} \right]$$



# Radar equation for weather radar

$$P_r(r) = \frac{|K_w|^2}{Cr^2} z(r) \quad P_r^{obs}(r) = P_r(r) + P_n$$

$$z(r) = C(P_r^{obs}(r) - P_n) \frac{|L_{atm}|^2(r)}{|K_w|^2} r^2$$



# Relationship reflectivity - rainfall rate

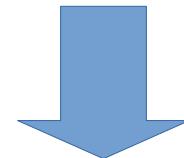
$$z(r) = \int_0^{\infty} N(D, r) D^6 dD = a \left( \int_0^{\infty} \underbrace{N(D, r)}_{\text{Depends on type of precip}} V_d(D) \underbrace{v_t(D)}_{\text{Empirically derived}} dD \right)^b = a R^b$$

Depends on type of precip      Empirically derived

Parameters a and b depend on knowledge of Particle Size Distribution PSD  $N(D, r)$

Most likely a and b can be derived statistically using long-term observations

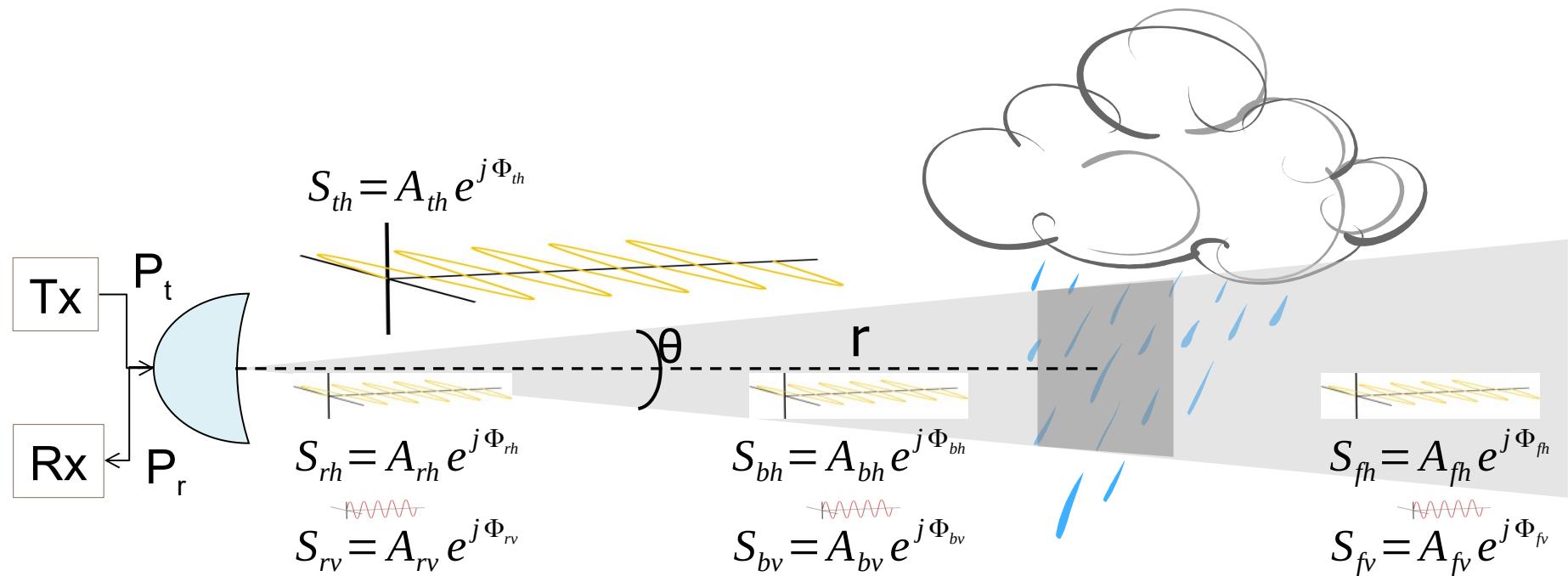
However, individual precipitation events may deviate significantly from the average relationship



Use of auxiliary information to better characterize the PSD

## 4. Polarimetry

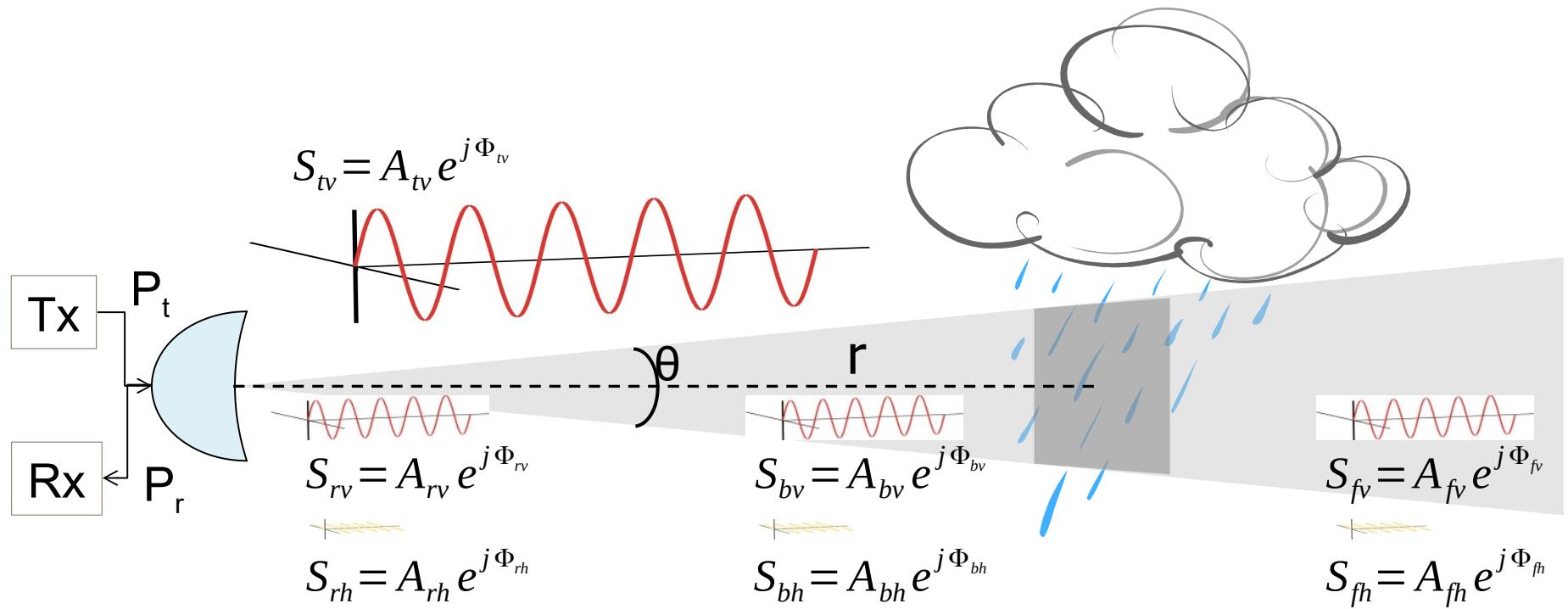
# Polarimetry



# Polarimetry

$$S_b = \begin{pmatrix} S_{b_{vv}} & S_{b_{vh}} \\ S_{b_{hv}} & S_{b_{hh}} \end{pmatrix} \quad \sigma_{b_{xx}} = 4\pi |S_{b_{xx}}|^2$$

$$S_f = \begin{pmatrix} S_{f_{vv}} & S_{f_{vh}} \\ S_{f_{hv}} & S_{f_{hh}} \end{pmatrix} \quad \sigma_{e_{xx}} = 2 \cdot 10^{-3} \Im\{S_{f_{xx}}\}$$



# Polarimetric variables

$$Z_{e_{xx}} = \frac{\lambda^4}{\pi^5} \frac{1}{|K_w|^2} 10^6 \int_0^\infty N(D) \sigma_{b_{xx}}(D) dD \rightarrow Z_{dr} = 10 \log \left( \frac{Z_{hh}}{Z_{vv}} \right)$$

$$LDR_h = 10 \log \left( \frac{\int_0^\infty N(D) |S_{b_{hv}}(D)|^2 dD}{\int_0^\infty N(D) |S_{b_{hh}}(D)|^2 dD} \right)$$

$$\rho_{hv} = \frac{4 \lambda^4}{\pi^4} \frac{1}{|K_w|^2} 10^6 \frac{\left| \int_0^\infty N(D) S_{b_{hh}}(D) S_{b_{vv}}^*(D) dD \right|}{\sqrt{Z_{hh} Z_{vv}}}$$

$$\delta_{co} = \frac{180}{\pi} \arg \left[ \int_0^\infty N(D) S_{b_{hh}}(D) S_{b_{vv}}^*(D) dD \right]$$

Backward scattering

$$A_{xx} = 4.34 \cdot 10^3 \int_0^\infty N(D) \sigma_{e_{xx}}(D) dD$$

$$KDP = \frac{180}{\pi} \lambda \int_0^\infty N(D) \Re \{ S_{f_{hh}}(D) - S_{f_{vv}}(D) \} dD$$

Forward scattering

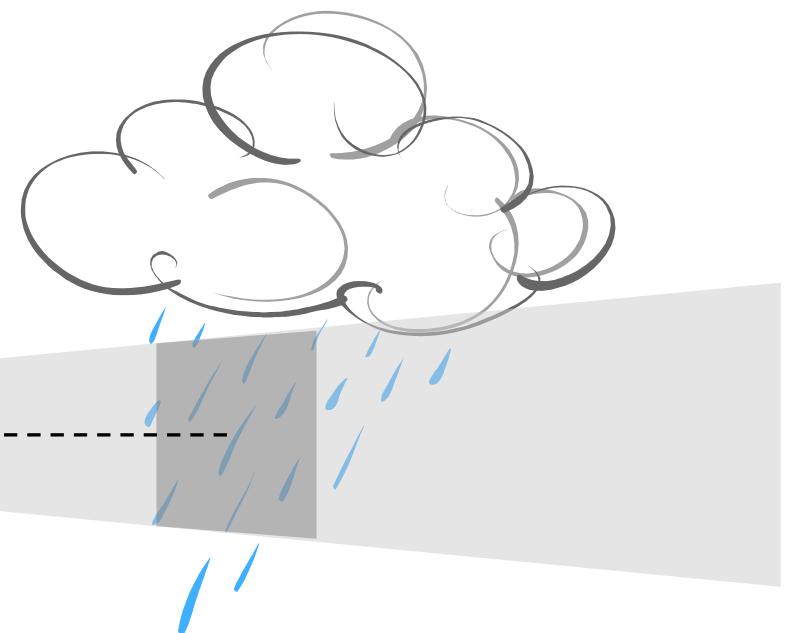
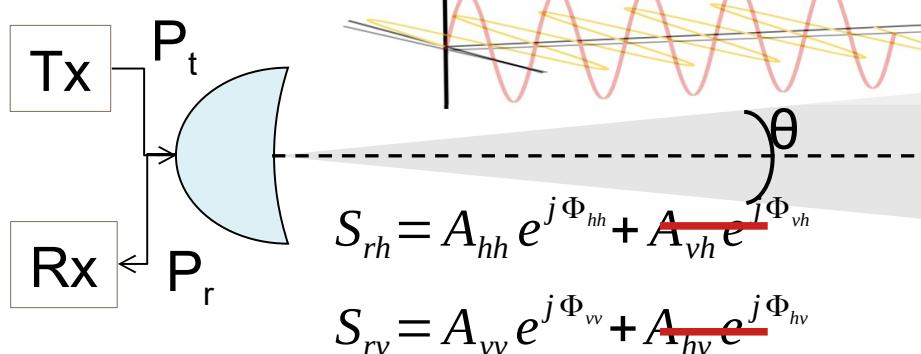
# STAR polarimetric measurements

$$\left. \begin{aligned} z_{ehh}(r) &= C_{hh}(P_{r_{hh}}(r) - P_{n_{hh}}) \frac{L_{atm_{hh}}^2(r)}{|K_w|^2} r^2 \\ z_{evv}(r) &= C_{vv}(P_{r_{vv}}(r) - P_{n_{vv}}) \frac{L_{atm_{vv}}^2(r)}{|K_w|^2} r^2 \end{aligned} \right\} \quad Z_{dr} = 10 \log \left( \frac{z_{hh}}{z_{vv}} \right)$$

$$\Phi_{dp}(r) = \Phi_{hh}(r) - \Phi_{vv}(r) \quad \xrightarrow{\text{blue arrow}} \quad K_{dp}(r) = \frac{1}{2} \frac{d \Phi_{dp}(r)}{dr} = \frac{\Phi_{dp}(r_2) - \Phi_{dp}(r_1)}{2 \Delta r}$$

$$\rho_{hv}(r) = \frac{\langle |S_{rh} S_{rv}^*| \rangle}{P_{rh} P_{rv}}$$

$$S_t = A_{th} e^{j\Phi_{th}} + A_{tv} e^{j\Phi_{tv}}$$



# Polarimetric radar observations

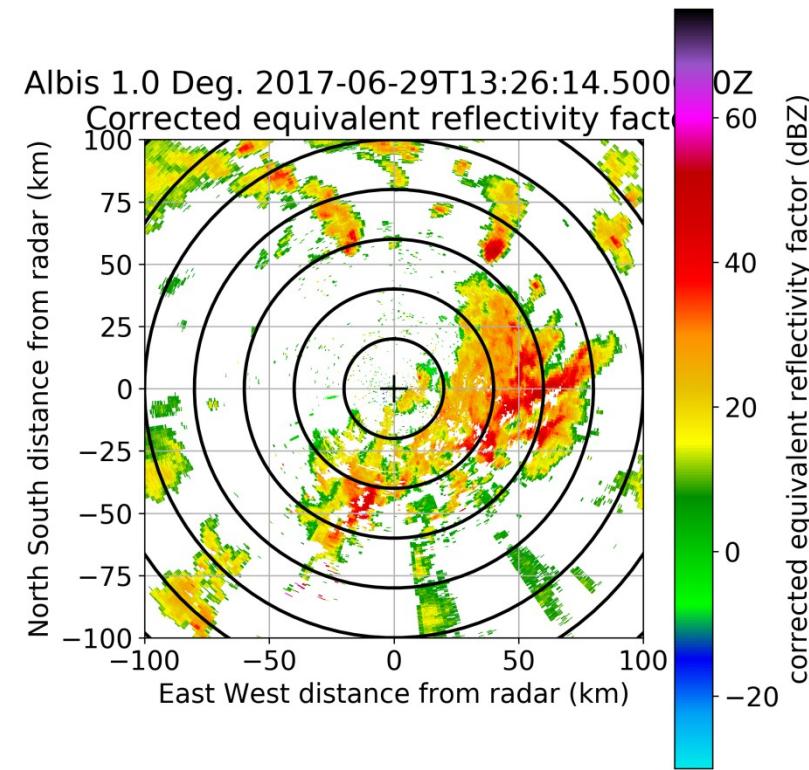
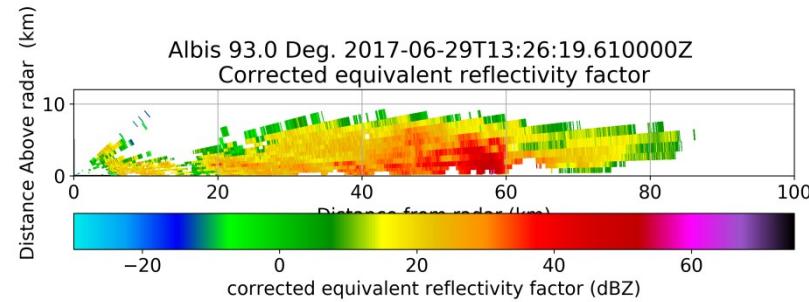
$$z_{hh}^{obs}(r) = z_{hh}(r) - 2 \int_0^r a_h(r) dr - 2 a_h^{radome} + \Delta Z_{hh} + \sigma_{z_{hh}}$$

$$z_{dr}^{obs}(r) = z_{dr}(r) - 2 \int_0^r a_{dp}(r) dr - 2 a_{dp}^{radome} + \Delta Z_{dr} + \sigma_{z_{dr}}$$

$$\Psi_{dp}^{obs}(r) = 2 \int_0^r K_{dp}(r) dr + \delta_{co}(r) + \Phi_{dp_0} + \sigma_{\Phi_{dp}}$$

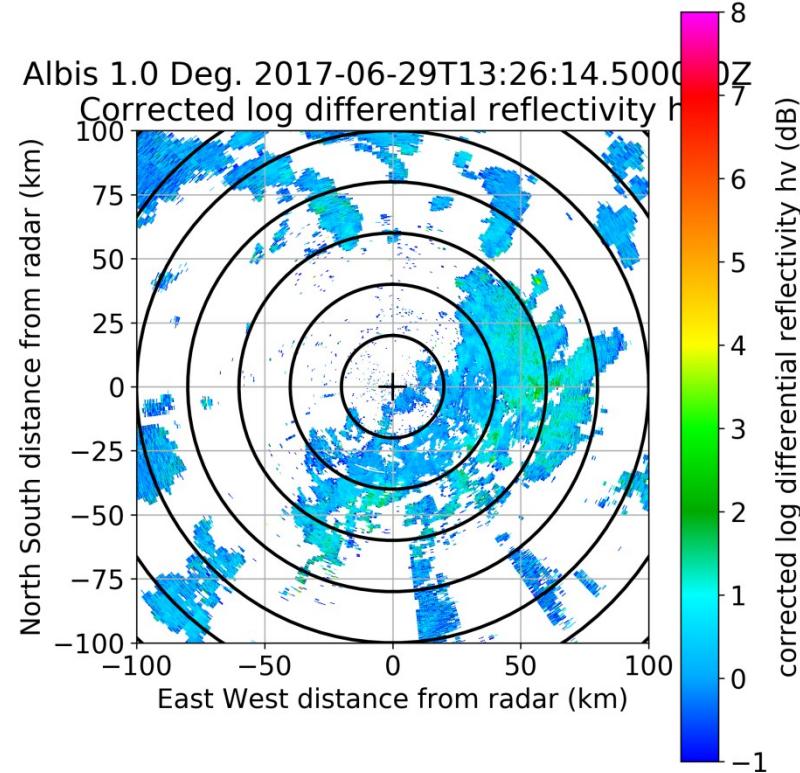
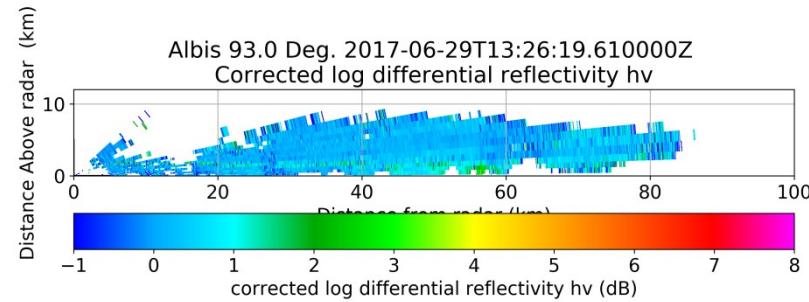
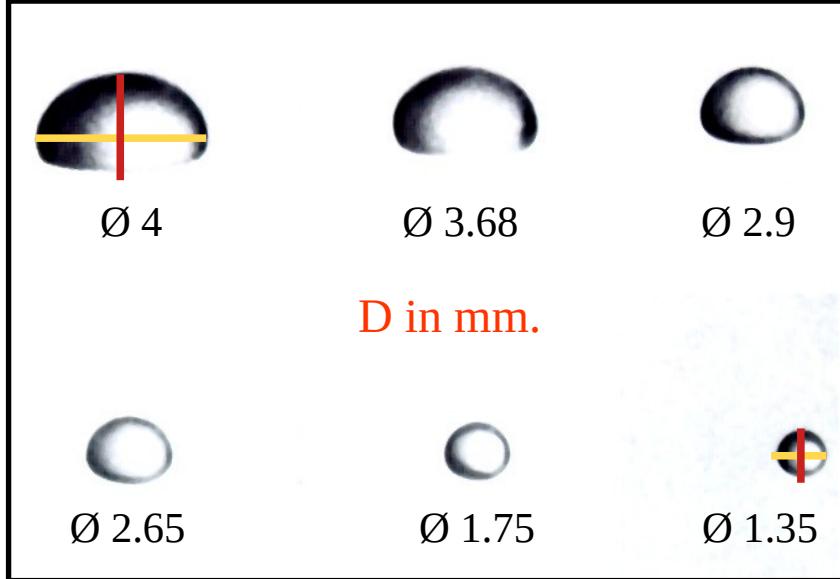
$$\rho_{hv}^{obs}(r) = \rho_{hv}(r) + \sigma_{\rho_{hv}}$$

# reflectivity



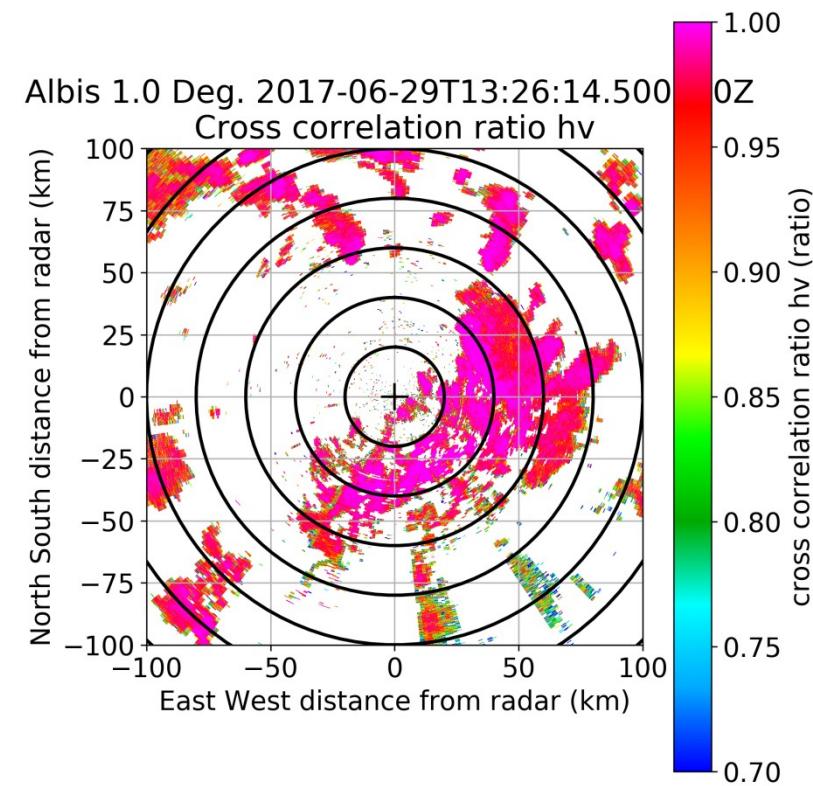
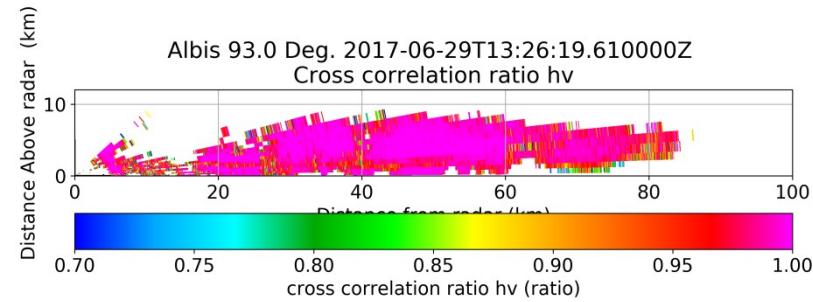
# Differential reflectivity

Linked to hydrometeor shape  
Raindrop size

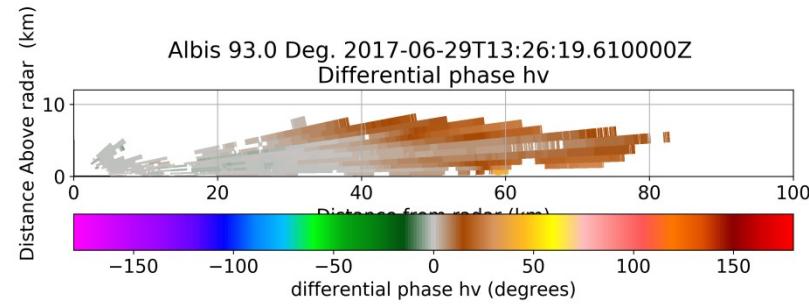


# Co-polar correlation coefficient

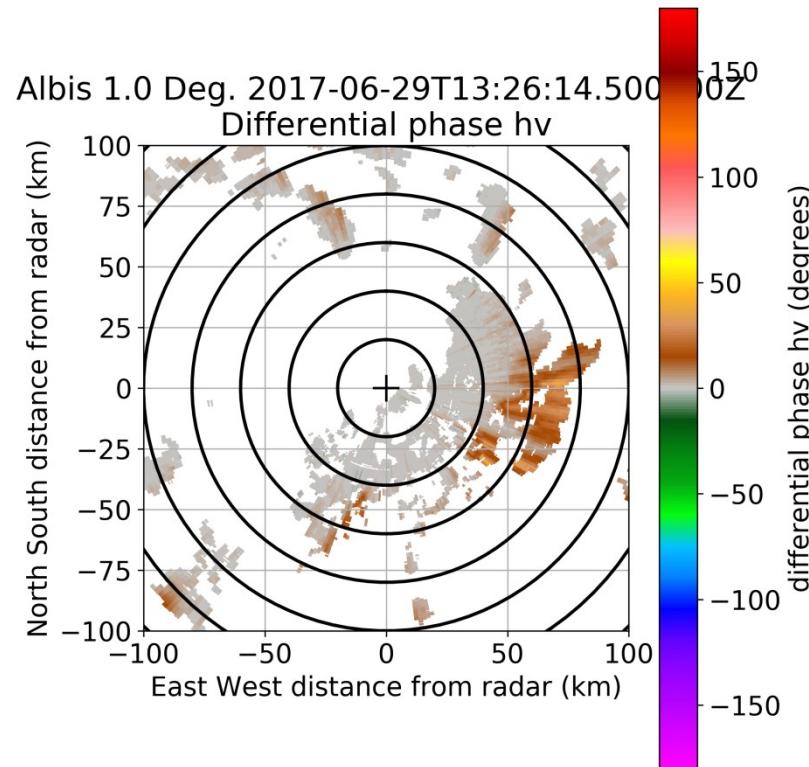
Linked to heterogeneity of the scatterers  
 Hydrometeor phase  
 Antenna quality



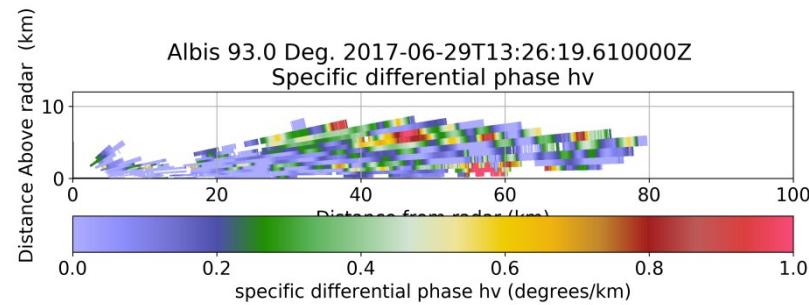
# Differential phase



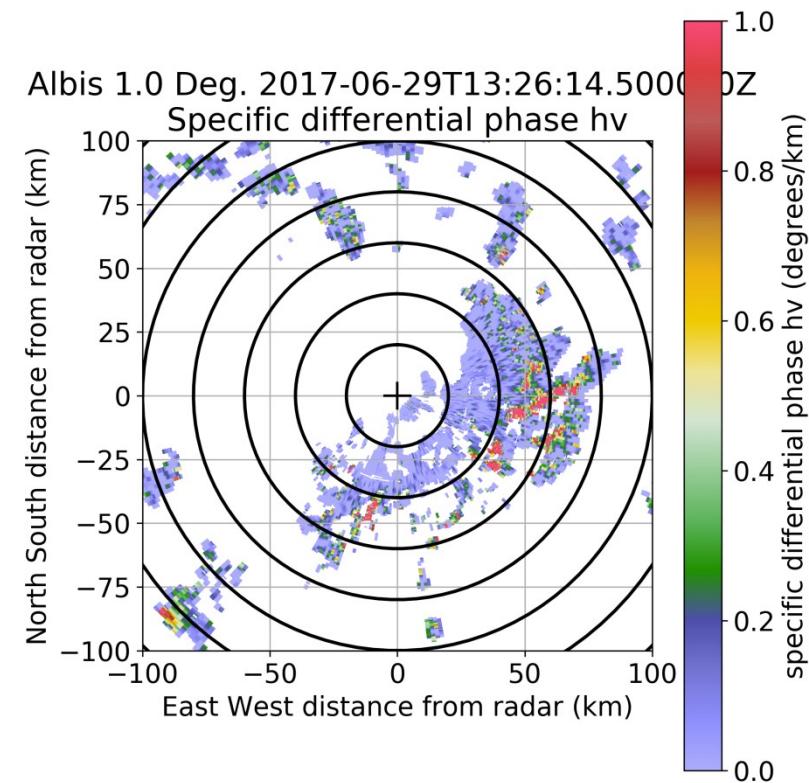
Linked to attenuation



# Specific differential phase



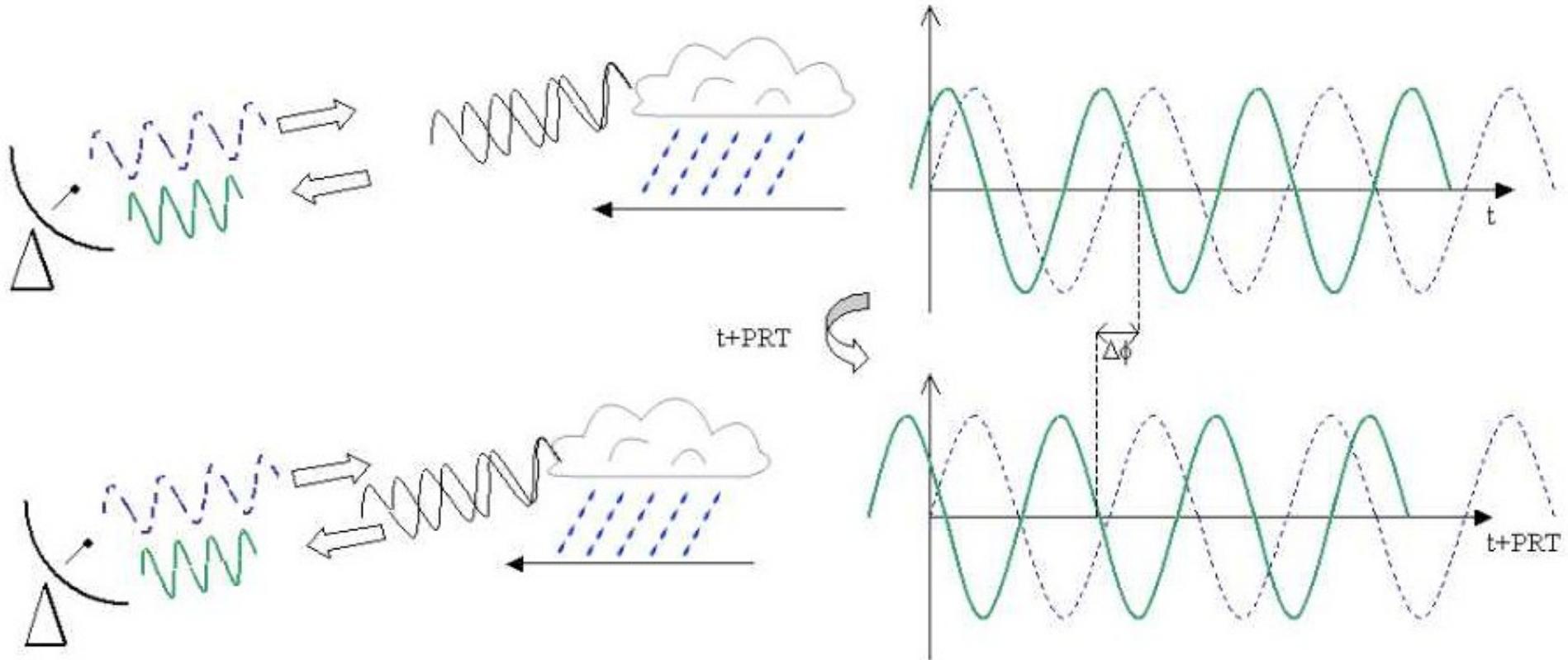
Linked to liquid water content



## 5. Doppler moments

# The Doppler effect

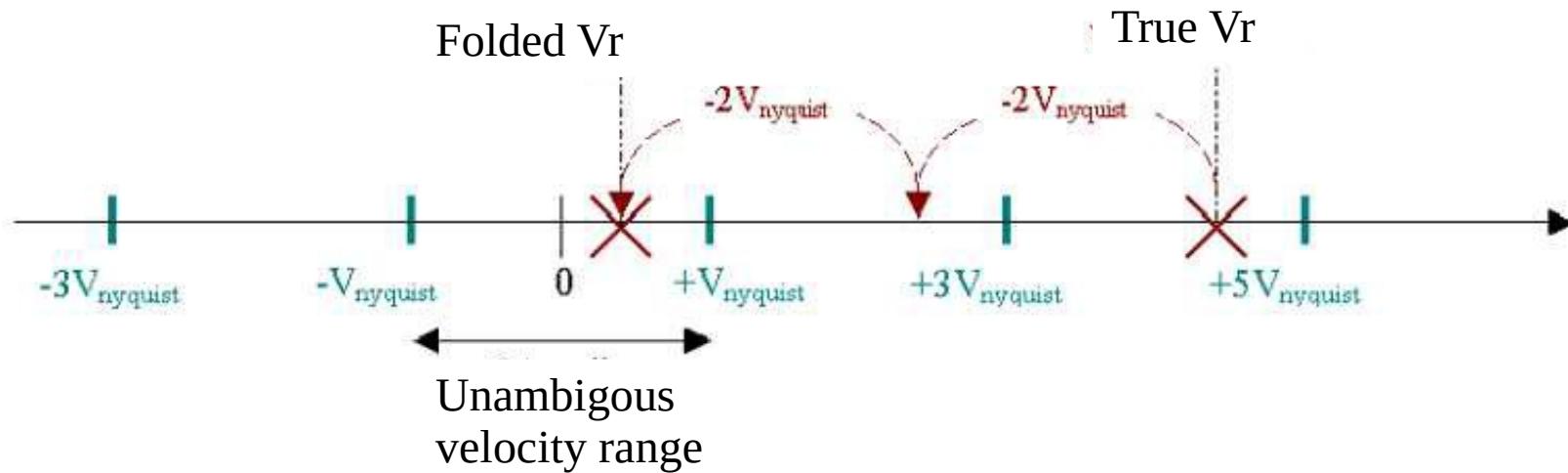
Discovered by Christian Doppler in 1842



$$V_r = \frac{\lambda}{4\pi PRT} \Delta\Phi$$

# Nyquist velocity

$$\Delta \Phi \in ]-\pi, \pi] \rightarrow V_r \in ]-V_{Nyquist}, +V_{Nyquist}]; V_{Nyquist} = \frac{\lambda}{4 P R T}$$



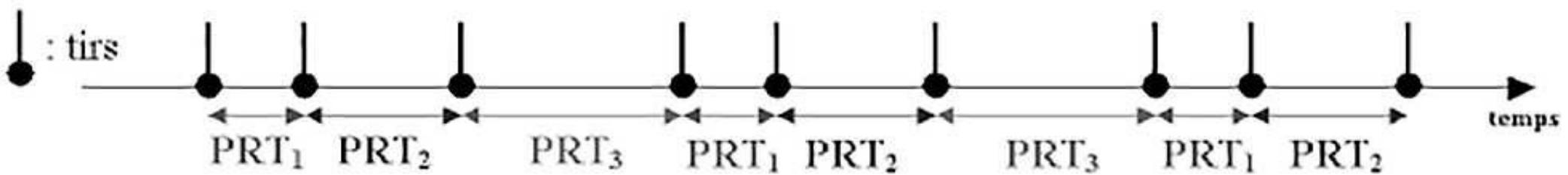
$$V_r^{true} = V_r^{obs} + 2kV_{Nyquist}$$

# Doppler dilemma

$$\left. \begin{aligned} V_{Nyquist} &= \frac{\lambda PRF}{4} \\ r_{max} &= \frac{c}{PRF} \end{aligned} \right\} \uparrow PRF \Rightarrow \uparrow V_{Nyquist} \text{ BUT } \downarrow r_{max}$$

Solution : MULTIPLE PRF

Méthode triple PRT :



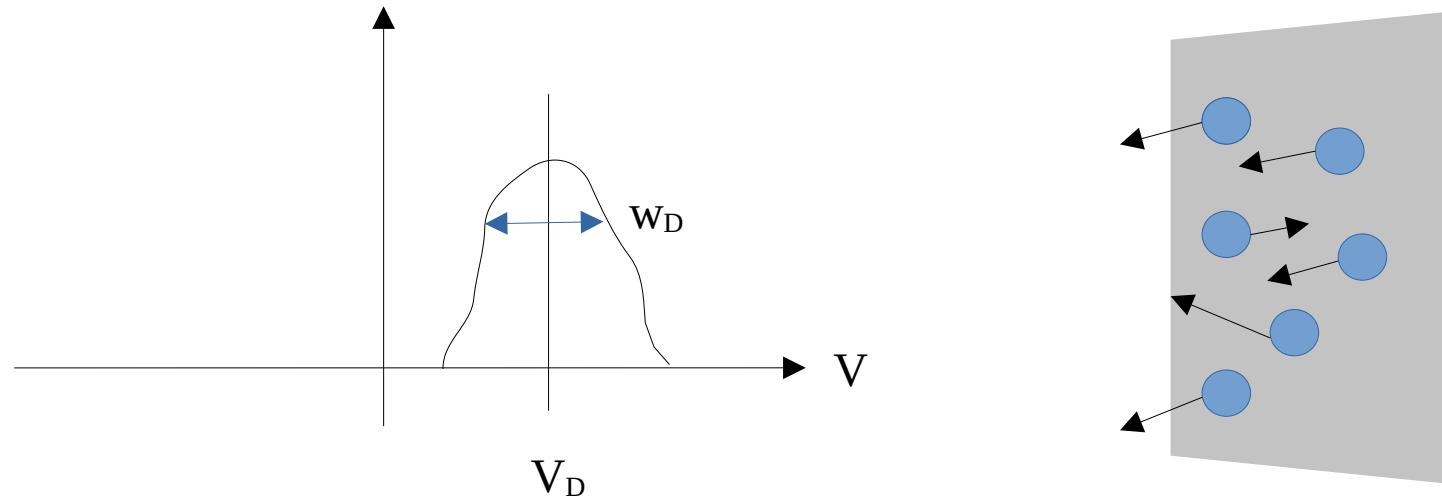
We get 2 or more  $V_r$  potentially folded in 2 or more  $\pm V_{Nyquist}$   
Combining them properly we can extend the Nyquist interval

# Doppler spectrum

The received signal phase will be a combination of multiple single scatterer returns  
Combining several pulses we can obtain the **Doppler spectrum**

The averaged velocity is the Doppler velocity representative of the global displacement (with respect to the radar) within the radar volume

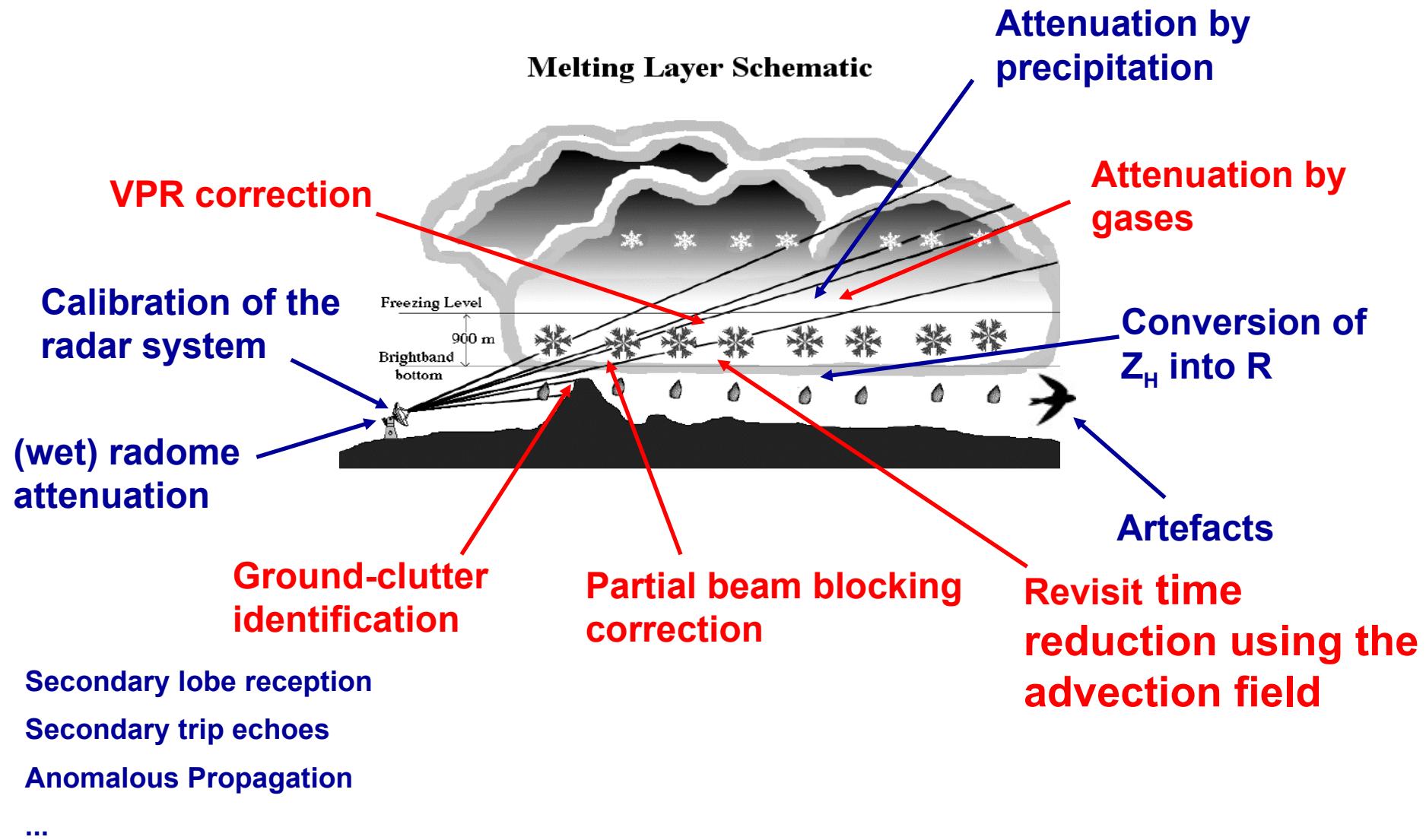
We can compute higher order moments such as the **Doppler spectrum width  $W_D$**   
 $W_D$  is related to the turbulence within the radar volume



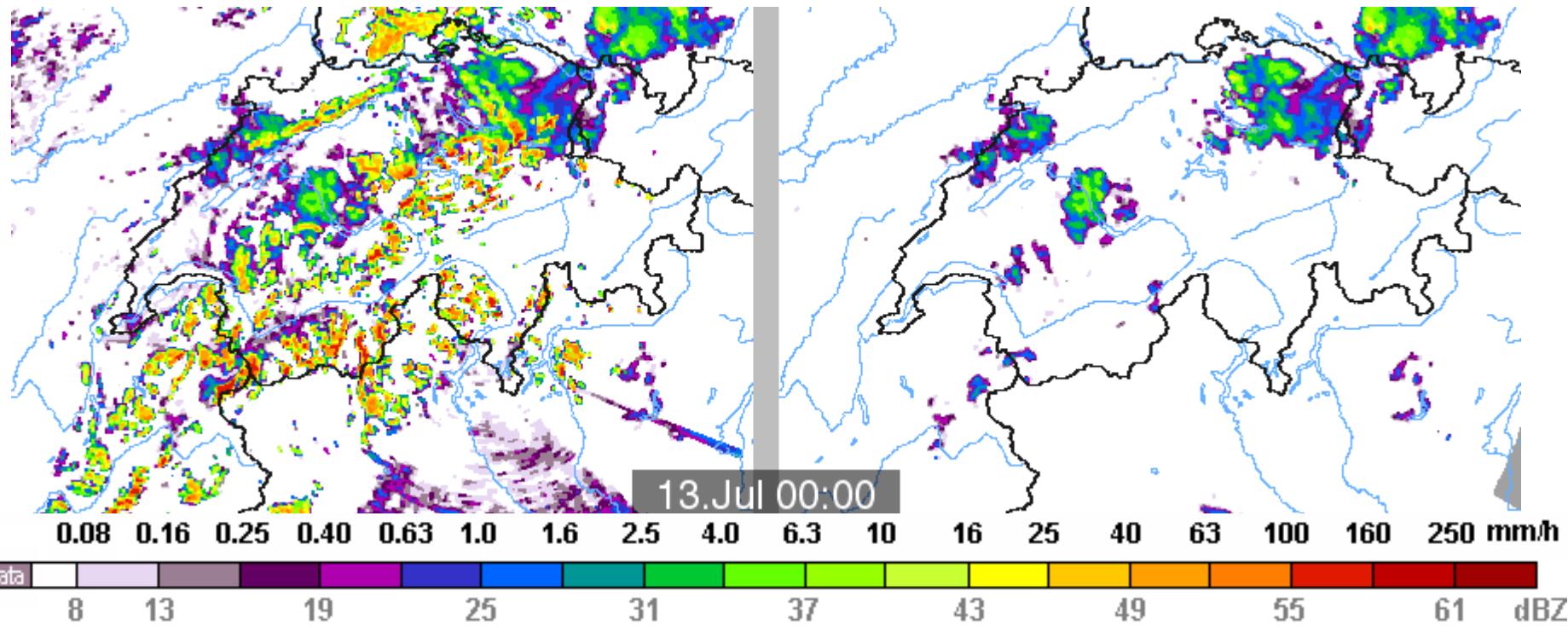
**Ground clutter is centered around 0 m/s**

## 6. Sources of uncertainty

# Sources of uncertainty



# Clutter identification



# Calibration

Calibration: In measurement technology and Metrology is the comparison of measurement values delivered by a device under test with those of a **calibration standard of known accuracy (reference)**. Such a standard could be another measurement device of known accuracy, a device generating the quantity to be measured, etc.

References: internal signal generator, metallic sphere, sun, light rain, precipitation when pointing at the vertical, ground clutter, etc.

**Thank you!  
Grazie mille!  
Moltes Gràcies!  
Merci!**

