

OPENRSP Developer Manual

Version 1.0.0

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OPENRSP : open-ended library for response theory

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Contents

1	Preface	5
1.1	Version Numbering Scheme	5
2	Analysis	7
2.1	Introduction	7
2.1.1	Purpose	7
2.1.2	Scope	8
2.1.3	Product Overview	8
2.1.4	Definitions	8
2.2	References	8
2.3	Specific Requirements	8
2.3.1	External Interfaces	8
2.3.2	Functions	8
2.3.3	Usability Requirements	8
2.3.4	Performance Requirements	8
2.3.5	Logical Database Requirements	8
2.3.6	Design Constraints	8
2.3.7	Software System Attributes	8
2.3.8	Supporting Information	8
2.4	Verification	8
2.5	Appendices	8
2.5.1	Assumptions and Dependencies	8
2.5.2	Acronyms and Abbreviations	8
2.5.3	Theoretical Background	8
2.5.4	Open-Ended Response Theory	8
2.5.5	OPENRSP Framework	9
2.5.6	Perturbations	10
3	Implementation	13
3.1	Header File for Users	13
3.2	Four Basic APIs for the OPENRSP Context	17
3.3	Perturbations	22
3.3.1	Internal Perturbation Labels	22
3.3.2	Callback Functions for Perturbations	24
3.3.3	Perturbation Context and Its Basic APIs	24
3.3.4	Conversion of Perturbation Tuples and Labels	32
3.4	Overlap Operator	42
3.5	One-Electron Operators	56
3.6	Two-Electron Operators	69
3.7	XC Functionals	83
3.8	Zero-Electron Operators	98
3.9	Linear Response Equation Solver	109

3.10	Response Functions	114
3.11	Residues	116
3.12	Fortran APIs	119
3.13	Unit Testing	190
3.13.1	Numerical reference data	190
3.13.2	Testing C APIs	196
3.13.3	Testing Fortran APIs	223
4	Maintenance	225
4.1	Support and Citation	225
4.2	List of Chunks	225

Chapter 1

Preface

1.1 Version Numbering Scheme

The version numbering scheme used for OPENRSP is **Major.Minor.Patch**, where **Major** generally represents new release containing important changes, and it may not be compatible with previous versions.

Minor is changed when a few new features introduced, and it should be compatible with those of the same **Major** number.

Patch usually includes bug fixes, and should be compatible with those of the same **Major.Minor** number.

Chapter 2

Analysis

This chapter presents the “Software Requirements Specification” (SRS) largely based on ISO/IEC/IEEE 29148:2011(E) “Systems and software engineering – Life cycle processes – Requirements engineering”.

2.1 Introduction

This section gives a scope description and overview of everything needed to design and implement OPENRSP (library) by taking the requirements listed in this section into account.

2.1.1 Purpose

The SRS analyses the problem—molecular integral evaluation—that OPENRSP aims to solve, and lays out the requirements that OPENRSP should supply or should not supply.

The SRS is primarily intended to prepare a reference for developing OPENRSP (Version 1.0.0). It can also be proposed to OPENRSP users for their suggestions and comments.

2.1.2 Scope

2.1.3 Product Overview

Product Perspective

Product Functions

User Characteristics

Limitations

2.1.4 Definitions

2.2 References

2.3 Specific Requirements

2.3.1 External Interfaces

2.3.2 Functions

2.3.3 Usability Requirements

2.3.4 Performance Requirements

2.3.5 Logical Database Requirements

2.3.6 Design Constraints

2.3.7 Software System Attributes

2.3.8 Supporting Information

2.4 Verification

2.5 Appendices

2.5.1 Assumptions and Dependencies

2.5.2 Acronyms and Abbreviations

2.5.3 Theoretical Background

For the time being, OPENRSP has implemented the density matrix-based quasienergy formulation of the Kohn–Sham density functional response theory using perturbation- and time-dependent basis sets [1, 2].

The density matrix-based quasienergy formulation actually works for different levels of theory, i.e., one-, two- and four-component levels. A relativistic implementation can be found in Ref. [3].

OPENRSP uses the recursive programming techniques [4] to compute different molecular properties order by order. The recursive programming techniques can also be used for calculations of residues, the implementation of the first order residues can be found in Ref. [5].

2.5.4 Open-Ended Response Theory

The name OPENRSP stands for **open-ended response theory**, that is, the library is:

1. open-ended for different levels of theory, i.e., one-, two- and four-component levels;
2. open-ended for different wave functions, e.g., atomic-orbital (AO) based density matrix, molecular orbital (MO) coefficients and coupled cluster (CC);
3. open-ended for different kinds of perturbations; and
4. open-ended for different host programs.

As aforementioned, OPENRSP has for the time being implemented the AO based density matrix response theory (source codes in `src/ao_dens`)¹, and it works for one-, two- and four-component levels by simply setting the appropriate Hamiltonian. We are now planning to implement the MO and CC based response theories.

To make OPENRSP work for any perturbation, we will implement the so called **perturbation free scheme**, see Section 2.5.6.

In order to make it easy for implementing OPENRSP into different host programs (written in different programming languages), we agree to use the **callback function scheme** in OPENRSP in the 2015 Skibotn meeting. The callback functions are specified by host programs by calling the OPENRSP application program interface (APIs, both C and Fortran implemented) during run time, and will be used by OPENRSP during calculations, to get contributions from electronic and nuclear Hamiltonian, and to get response parameters from solving the linear response equation.

Another important issue affects the implementation of OPENRSP into different host programs is the matrix and its different operations that OPENRSP extensively depends on. Different host programs can have different types of matrices (dense and sparse, sequential and parallel) and written by different programming languages (e.g. C and Fortran).

To best utilize the host program's developed matrix routines (if there is), and also to remove this complexity of matrix problem from OPENRSP, we also agree to build OPENRSP on top of the **QcMatrix library** in the 2015 Skibotn meeting. This matrix library works as an adapter between OPENRSP and different matrix routines (implemented in different host programs) that can be written in C and Fortran².

2.5.5 OpenRSP Framework

Therefore, a full picture of OPENRSP used in a C host program can be (the description of OPENRSP Fortran APIs can be found in Section 3.12):

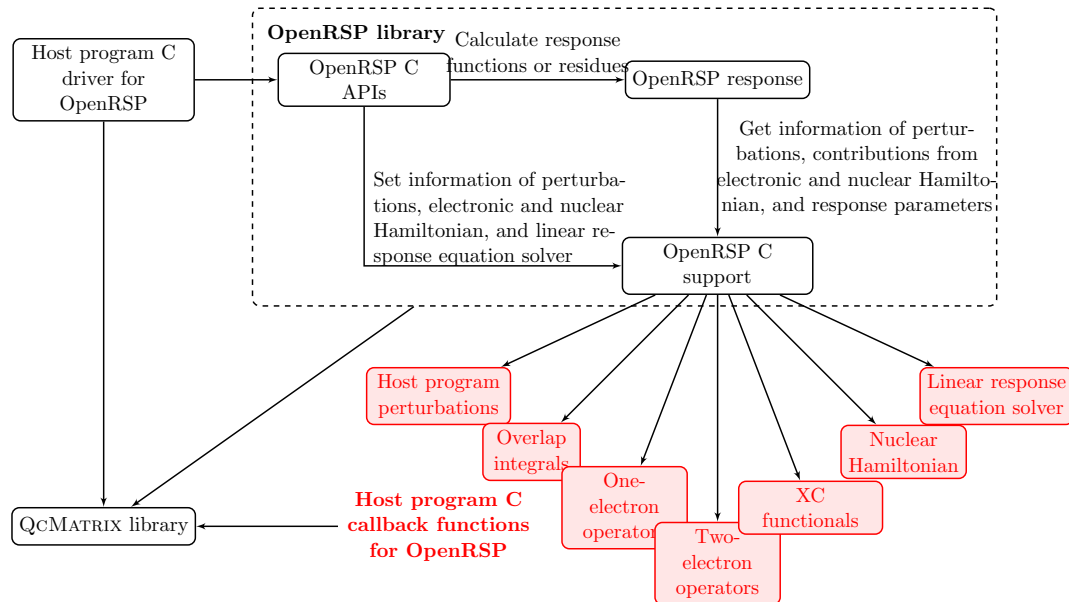


Figure 2.1: OPENRSP used in a C host program.

As shown in Figure 2.1, the OPENRSP library is divided into three parts:

¹The codes in `src/ao_dens` are written in Fortran, but OPENRSP APIs are implemented using C language. Therefore, adapter codes between them are implemented in `src/ao_dens/adapter`, for OPENRSP APIs calling the codes of AO based density matrix response theory, also for the AO based density matrix response theory codes calling the callback functions (as function pointers saved by OPENRSP APIs).

²If there is no matrix routines implemented in a host program, it can fully use the QcMatrix library that will invoke BLAS and LAPACK libraries for matrix operations.

1. The “OPENRSP C APIs” work mostly between the host program driver routine and other parts of the OPENRSP library, that all the information saved in the “OPENRSP C support” will be set up by calling the corresponding OPENRSP C API;
2. The “OPENRSP response” is the core part in which the performance of response theory will be done;
3. The “OPENRSP C support” saves the information of perturbations, electronic and nuclear Hamiltonian and linear response equation solver, and will be used by the “OPENRSP response” part during calculating response functions and residues.

The “OPENRSP response” was already implemented using Fortran for the AO based density matrix response theory (source codes in `src/ao_dens`) that will not be covered here.

2.5.6 Perturbations

For perturbations in OPENRSP, we introduce the following notations and convention:

Perturbation is described by a label (a), a complex frequency (ω) and its order (n), and written as a_{ω}^n . Any two perturbations are different if they have different labels, and/or frequencies, and/or orders.

Perturbation label is an integer distinguishing one perturbation from others; all *different* perturbation labels involved in the calculations should be given by calling the application programming interface (API) `OpenRSPSetPerturbations()`; OPENRSP will stop if there is any unspecified perturbation label given afterwards when calling the APIs `OpenRSPGetRSPFun()` or `OpenRSPGetResidue()`.

Perturbation order Each perturbation can acting on molecules once or many times, that is the order of the perturbation.

Perturbation components and their ranks Each perturbation may have different numbers of components for their different orders, the position of each component is called its rank.

For instance, there will usually be x, y, z components for the electric dipole perturbation, and their ranks are $\{0, 1, 2\}$ in zero-based numbering, or $\{1, 2, 3\}$ in one-based numbering.

Perturbation tuple An ordered list of perturbation labels, and in which we further require that *identical perturbation labels should be consecutive*. That means the tuple (a, b, b, c) is allowed, but (a, b, c, b) is illegal because the identical labels b are not consecutive.

As a tuple:

1. Multiple instances of the same labels are allowed so that $(a, b, b, c) \neq (a, b, c)$, and
2. The perturbation labels are ordered so that $(a, b, c) \neq (a, c, b)$ (because their corresponding response functions or residues are in different shapes).

We will sometimes use an abbreviated form of perturbation tuple as, for instance $abc \equiv (a, b, c)$.

Obviously, a perturbation tuple + its corresponding complex frequencies for each perturbation label can be viewed as a set of perturbations, in which the number of times a label (with the same frequency) appears is the order of the corresponding perturbation.

For example, a tuple (a, b, b, c) + its complex frequencies $(\omega_a, \omega_b, \omega_b, \omega_c)$ define perturbations $a_{\omega_a}^1$, $b_{\omega_b}^2$ and $c_{\omega_c}^1$; another tuple (a, b, b, c) + different complex frequencies for labels b — $(\omega_a, \omega_{b_1}, \omega_{b_2}, \omega_c)$ define different perturbations $a_{\omega_a}^1$, $b_{\omega_{b_1}}^1$, $b_{\omega_{b_2}}^1$ and $c_{\omega_c}^1$.

Category of perturbation frequencies We use different integers for distinguishing different values of frequencies within a frequency configuration. The category array is determined by:

1. For each frequency configuration, we start at the first perturbation and let its frequency value be designated number 1, then
2. For the next perturbation,
 - (a) If its frequency value corresponds to a frequency value encountered previously in this frequency, then use the same designation as for that previously encountered frequency value, or
 - (b) If its frequency value has not been encountered before, then let that frequency value

be designated with the first unused number;

3. Continue like this until the end of the perturbation tuple;
4. Start the numbering over again at the next frequency configuration.

Canonical order

1. In OPENRSP, all perturbation tuples are canonically ordered according to the argument `pert_tuple` in the `OpenRSPGetRSPFun()` or `OpenRSPGetResidue()`. For instance, when a perturbation tuple (a, b, c) given as `pert_tuple` in the API `OpenRSPGetRSPFun()`, OPENRSP will use such order ($a > b > c$) to arrange all perturbation tuples inside and sent to the callback functions.
2. Moreover, a collection of several perturbation tuples will also follow the canonical order. For instance, a collection of all possible perturbation tuples of labels a, b, c, d are $(0, a, b, ab, c, ac, bc, abc, d, ad, bd, abd, cd, acd, bcd, abcd)$, where 0 means unperturbed quantities that is always the first one in the collection.

Perturbation a The first perturbation label in the tuple sent to OPENRSP APIs `OpenRSPGetRSPFun()` or `OpenRSPGetResidue()`, are the perturbation a [1].

Perturbation addressing

1. The addressing of perturbation labels in a tuple, as mentioned in the term **Canonical order**, is decided by
 - (a) the argument `pert_tuple` sent to the API `OpenRSPGetRSPFun()` or `OpenRSPGetResidue()`, and
 - (b) the canonical order that OPENRSP uses.
2. The addressing of components per perturbation (several consecutive identical labels with the same complex frequency) are decided by the host program, as will be discussed in the following **perturbation free scheme**.
3. The addressing of a collection of perturbation tuples follows the canonical order as aforementioned.

Therefore, the shape of response functions or residues is mostly decided by the host program. Take \mathcal{E}^{abc} for example, its shape is (N_a, N_{bb}, N_c) , where N_a and N_c are respectively the numbers of components of the first order of the perturbations a and c , and N_{bb} is the number of components of the second order of the perturbation b , and

1. In OPENRSP, we will use notation `[a][bb][c]` for \mathcal{E}^{abc} , where the leftmost index (`a`) runs slowest in memory and the rightmost index (`c`) runs fastest. However, one should be aware that the results are still in a one-dimensional array.
2. If there two different frequencies for the perturbation label b , OPENRSP will return `[a][b1][b2][c]`, where `b1` and `b2` stand for the components of the first order of the perturbation b .
3. The notation for a collection of perturbation tuples (still in a one-dimensional array) is `{1, [a], [b], [a][b], [c], [a][c], [b][c], [a][b][c]}` for $(0, a, b, ab, c, ac, bc, abc)$, where as aforementioned the first one is the unperturbed quantities.

Perturbation Free Scheme

Now, let us discuss our **perturbation free scheme**. As aforementioned, there could be **different numbers of components** for different perturbations. In different host programs, these components could be arranged in different ways.

For instance, there are 9 components for the second order magnetic derivatives in a redundant way $xx, xy, xz, yx, yy, yz, zx, zy, zz$, but 6 components in a non-redundant way xx, xy, xz, yy, yz, zz . There are at most four centers in different integrals, non-zero high order (≥ 5) geometric derivatives are only those with at most four differentiated centers.

To take all the above information into account in OPENRSP will make it so complicated and not necessary, because response theory actually does not care about the detailed knowledge of different perturbations. In particular, when all the (perturbed) integrals and expectation values are computed by the host program's callback functions, the detailed information of perturbations:

1. the number of components, and
 2. how they are arranged in memory
- can be hidden from OPENRSP .

The former can be easily solved by sending the numbers of components of different perturbation labels (up to their maximum orders) to the OPENRSP API `OpenRSPSetPerturbations()`.

The latter can be important for OPENRSP to construct higher-order derivatives from lower-order ones. We have two cases:

1. Higher-order derivatives are taken with respect to different perturbations, for instance, $\frac{\partial^3}{\partial a \partial b \partial c}$ are simply the direct product of components of lower-order derivatives with respect to each perturbation $\frac{\partial}{\partial a}$, $\frac{\partial}{\partial b}$ and $\frac{\partial}{\partial c}$.
2. Higher-order derivatives are taken with respect to **one perturbation**. Take the second order-derivatives (in the redundant format) for example, they can be constructed from the first-order ones as,

$$\begin{aligned}
 x + x &\rightarrow xx, & 0 + 0 &\rightarrow 0, \\
 x + y &\rightarrow xy, & 0 + 1 &\rightarrow 1, \\
 x + z &\rightarrow xz, & 0 + 2 &\rightarrow 2, \\
 y + x &\rightarrow yx, & 1 + 0 &\rightarrow 3, \\
 y + y &\rightarrow yy, & 1 + 1 &\rightarrow 4, \\
 y + z &\rightarrow yz, & 1 + 2 &\rightarrow 5, \\
 z + x &\rightarrow zx, & 2 + 0 &\rightarrow 6, \\
 z + y &\rightarrow zy, & 2 + 1 &\rightarrow 7, \\
 z + z &\rightarrow zz, & 2 + 2 &\rightarrow 8,
 \end{aligned}$$

where we have ranked different components in zero-based numbering (numbers on the right). Because the ranks can be different in different host programs, also the above mapping relationship between lower- and higher-order derivatives (with respect to **one perturbation**) can be different in different host programs.

We therefore ask for a callback function `get_pert_concatenation()` from host programs. This callback function will, from given components of a **concatenated perturbation tuple** (i.e. higher-order derivatives with respect to one perturbation), get the ranks of components of the **sub-perturbation tuples with the same perturbation label** (i.e. lower-order derivatives with respect to one perturbation).

As such, the numbers of different components of perturbations and their ranks are totally decided by the host program—that is the **perturbation free scheme**.

Chapter 3

Implementation

3.1 Header File for Users

To use OPENRSP, C users need to include the following header file into their codes:

```
13  <OpenRSP.h 13>≡
    /*
      <OpenRSPLicense 14a>

      <header name='OpenRSP.h' author='Bin Gao' date='2014-01-27'>
        The header file of OpenRSP library for users
      </header>
    */

    #if !defined(OPENRSP_H)
    #define OPENRSP_H

    /* host program perturbations */
    #include "RSPPerturbation.h"
    /* type of electronic wave function */
    /*#include "RSPWaveFunction.h"*/
    /* overlap integrals */
    #include "RSPOverlap.h"
    /* one-electron operators */
    #include "RSPOneOper.h"
    /* two-electron operators */
    #include "RSPTwoOper.h"
    /* exchange-correlation (XC) functionals */
    #include "RSPXCFun.h"
    /* zero-electron operators */
    #include "RSPZeroOper.h"
    /* linear response equation solver */
    #include "RSPSolver.h"

    <OpenRSPStruct 14b>

    <OpenRSPAPIs 14c>

    #endif
```

Here, the directives `#if !defined(OPENRSP_H)` and `#define OPENRSP_H` (**include guard**) to-

gether prevent the header file from being compiled more than once.

We plan to release OPENRSP under the GNU Lesser General Public License:

```
14a <OpenRSPLicense 14a>≡
OpenRSP: open-ended library for response theory
Copyright 2015 Radovan Bast,
        Daniel H. Friese,
        Bin Gao,
        Dan J. Jonsson,
        Magnus Ringholm,
        Kenneth Ruud,
        Andreas Thorvaldsen
```

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In the following sections, we will describe how to implement each component of the “OPENRSP C support” (red blocks in Figure 2.1 under the “OPENRSP C support”) and the corresponding “OPENRSP C API”. Each component will have its header file, implemented C struct and corresponding functions that can be called inside OPENRSP.

The OPENRSP context `OpenRSPStruct` will encapsulate all the implemented C struct’s of the “OPENRSP C support” components into another C struct:

```
14b <OpenRSPStruct 14b>≡
typedef struct {
    QBool assembled;                /* indicates if the OpenRSP context assembled */
    RSPPert *rsp_pert;              /* host program perturbations */
    /*ElecWav *elec_wav;*/          /* implementation-specific data of (electronic) wave f
    /*ElecWavType elec_wav_type;*/
    RSPOverlap *overlap;            /* overlap integrals */
    RSPOneOper *one_oper;           /* one-electron operators */
    RSPTwoOper *two_oper;          /* two-electron operators */
    RSPXCFun *xc_fun;              /* XC functionals */
    RSPZeroOper *zero_oper;         /* zero-electron operators */
    RSPSolver *rsp_solver;          /* linear response equation solver */
    /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
    QInt num_atoms;
} OpenRSP;
```

where we have used types, macros and APIs implemented in the QCMATRIX library and one should be familiar with them first.

Users should use the OPENRSP context and the following APIs to access the functionalities of OPENRSP:

```
14c <OpenRSPAPIs 14c>≡
extern QErrorCode OpenRSPCreate(OpenRSP*,const QInt);
```

```

extern QErrorCode OpenRSPSetPerturbations(OpenRSP*,
                                           const QInt,
                                           const QcPertInt*,
                                           const QInt*,
                                           const QInt*,
                                           void*,
                                           const GetPertCat);
/*extern QErrorCode OpenRSPSetWaveFunction(OpenRSP*,const ElecWavType);*/
extern QErrorCode OpenRSPSetOverlap(OpenRSP*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt*,
                                     void*,
                                     const GetOverlapMat,
                                     const GetOverlapExp);
extern QErrorCode OpenRSPAddOneOper(OpenRSP*,
                                    const QInt,
                                    const QcPertInt*,
                                    const QInt*,
                                    void*,
                                    const GetOneOperMat,
                                    const GetOneOperExp);
extern QErrorCode OpenRSPAddTwoOper(OpenRSP*,
                                    const QInt,
                                    const QcPertInt*,
                                    const QInt*,
                                    void*,
                                    const GetTwoOperMat,
                                    const GetTwoOperExp);
extern QErrorCode OpenRSPAddXCFun(OpenRSP*,
                                  const QInt,
                                  const QcPertInt*,
                                  const QInt*,
                                  void*,
                                  const GetXCFunMat,
                                  const GetXCFunExp);
extern QErrorCode OpenRSPAddZeroOper(OpenRSP*,
                                      const QInt,
                                      const QcPertInt*,
                                      const QInt*,
                                      void*,

```

```

#endif

                                const GetZeroOperContrib);
extern QErrorCode OpenRSPSetLinearRSPSolver(OpenRSP*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                void*,
#endif
                                const GetLinearRSPSolution);
extern QErrorCode OpenRSPAssemble(OpenRSP*);
extern QErrorCode OpenRSPWrite(const OpenRSP*,FILE*);
extern QErrorCode OpenRSPGetRSPFun(OpenRSP*,
                                const QcMat*,
                                const QcMat*,
                                const QcMat*,
                                const QInt,
                                const QInt*,
                                const QcPertInt*,
                                const QInt*,
                                const QReal*,
                                const QInt*,
                                const QInt,
                                QReal*);
extern QErrorCode OpenRSPGetResidue(OpenRSP*,
                                const QcMat*,
                                const QcMat*,
                                const QcMat*,
                                const QInt,
                                const QInt,
                                const QReal*,
                                QcMat*[],
                                const QInt,
                                const QInt*,
                                const QcPertInt*,
                                const QInt*,
                                const QInt*,
                                const QInt*,
                                const QReal*,
                                const QInt*,
                                const QInt,
                                QReal*);
extern QErrorCode OpenRSPDestroy(OpenRSP*);

```

Here, we have also introduced the type of electronic wave function, but which has not been implemented.

Last but not least, the directive

```

#if defined(OPENRSP_C_USER_CONTEXT)
                                void*,
#endif

```

in most OPENRSP APIs enables users to provide their necessary setting for the callback functions that OPENRSP will send it back when invoking the callback functions. For instance, users can provide the information of basis sets to OPENRSP and use it inside the callback functions for different integral calculations.

3.2 Four Basic APIs for the OpenRSP Context

In this section, we will implement four basic APIs `OpenRSPCreate()`, `OpenRSPAssemble()`, `OpenRSPWrite()` and `OpenRSPDestroy()`, while other APIs will be implemented in the following sections. These four APIs respectively create, assemble, write and destroy the OPENRSP context.

The API `OpenRSPCreate()` is very simple as it only initializes the pointers of the context:

```
17a <OpenRSP.c 17a>≡
/*
  <OpenRSPLicense 14a>
*/

#include "OpenRSP.h"

/* <function name='OpenRSPCreate' author='Bin Gao' date='2014-01-28'>
  Creates the OpenRSP context
  <param name='open_rsp' direction='inout'>The OpenRSP context</param>
  <param name='num_atoms' direction='in'>
    Number of atoms
  </param>
  <return>Error information</return>
</function> */
QErrorCode OpenRSPCreate(OpenRSP *open_rsp, const QInt num_atoms)
{
  open_rsp->assembled = QFALSE;
  open_rsp->rsp_pert = NULL;
  /*open_rsp->elec_wav = NULL;*/
  /*open_rsp->elec_wav_type = ELEC_AO_D_MATRIX;*/
  open_rsp->overlap = NULL;
  open_rsp->one_oper = NULL;
  open_rsp->two_oper = NULL;
  open_rsp->xc_fun = NULL;
  open_rsp->zero_oper = NULL;
  open_rsp->rsp_solver = NULL;
  /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
  open_rsp->num_atoms = num_atoms;
  return QSUCCESS;
}
```

The other three APIs are also easy to implement, as they only invoke functions of the “OPENRSP C support” part to respectively assemble, write and destroy the corresponding C struct’s:

```
17b <OpenRSP.c 17a>+≡
/* <function name='OpenRSPAssemble' author='Bin Gao' date='2014-07-30'>
  Assembles the OpenRSP context
  <param name='open_rsp' direction='inout'>The OpenRSP context</param>
  <return>Error information</return>
</function> */
QErrorCode OpenRSPAssemble(OpenRSP *open_rsp)
{
  QErrorCode ierr; /* error information */
  open_rsp->assembled = QFALSE;
  /* assembles host program perturbations */
  if (open_rsp->rsp_pert!=NULL) {
```

```

        ierr = RSPPertAssemble(open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertAssemble()");
    }
    else {
        QErrorExit(FILE_AND_LINE, "perturbations not set by OpenRSPSetPerturbations()");
    }
/*FIXME: to implement ierr = xxAssemble(open_rsp->elec_eom); */
/* assembles overlap integrals */
if (open_rsp->overlap!=NULL) {
    ierr = RSPOverlapAssemble(open_rsp->overlap,
                              open_rsp->rsp_pert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapAssemble()");
}
/* assembles one-electron operators */
if (open_rsp->one_oper!=NULL) {
    ierr = RSPOneOperAssemble(open_rsp->one_oper,
                              open_rsp->rsp_pert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperAssemble()");
}
/* assembles two-electron operators */
if (open_rsp->two_oper!=NULL) {
    ierr = RSPTwoOperAssemble(open_rsp->two_oper,
                              open_rsp->rsp_pert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperAssemble()");
}
/* assembles XC functionals */
if (open_rsp->xc_fun!=NULL) {
    ierr = RSPXCFunAssemble(open_rsp->xc_fun,
                            open_rsp->rsp_pert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunAssemble()");
}
/* assembles nuclear Hamiltonian */
if (open_rsp->zero_oper!=NULL) {
    ierr = RSPZeroOperAssemble(open_rsp->zero_oper,
                              open_rsp->rsp_pert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperAssemble()");
}
/* assembles linear response equation solver */
if (open_rsp->rsp_solver!=NULL) {
    ierr = RSPSolverAssemble(open_rsp->rsp_solver);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverAssemble()");
}
else {
    QErrorExit(FILE_AND_LINE, "solver not set by OpenRSPSetSolver()");
}
open_rsp->assembled = QTRUE;
return QSUCCESS;
}

/* <function name='OpenRSPWrite' author='Bin Gao' date='2014-07-30'>
    Writes the OpenRSP context
    <param name='open_rsp' direction='in'>The OpenRSP context</param>

```

```

    <param name='fp_rsp' direction='inout'>File pointer</param>
    <return>Error information</return>
</function> */
QErrorCode OpenRSPWrite(const OpenRSP *open_rsp, FILE *fp_rsp)
{
    QErrorCode ierr; /* error information */
    fprintf(fp_rsp,
            "\nOpenRSP library compiled at %s, %s\n",
            __TIME__,
            __DATE__);
    /* context of the (electronic) wave function */
    /*FIXME: ierr = xxWrite(open_rsp->elec_eom); */
    if (open_rsp->rsp_pert!=NULL) {
        ierr = RSPPertWrite(open_rsp->rsp_pert, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertWrite()");
    }
    if (open_rsp->overlap!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> overlap integrals\n");
        ierr = RSPOverlapWrite(open_rsp->overlap, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapWrite()");
    }
    if (open_rsp->one_oper!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of one-electron operators\n");
        ierr = RSPOneOperWrite(open_rsp->one_oper, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperWrite()");
    }
    if (open_rsp->two_oper!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of two-electron operators\n");
        ierr = RSPTwoOperWrite(open_rsp->two_oper, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperWrite()");
    }
    if (open_rsp->xc_fun!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of XC functionals\n");
        ierr = RSPXCFunWrite(open_rsp->xc_fun, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunWrite()");
    }
    if (open_rsp->zero_oper!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> nuclear Hamiltonian\n");
        ierr = RSPZeroOperWrite(open_rsp->zero_oper, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperWrite()");
    }
    if (open_rsp->rsp_solver!=NULL) {
        ierr = RSPSolverWrite(open_rsp->rsp_solver, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverWrite()");
    }
    /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
    fprintf(fp_rsp,
            "OpenRSPWrite>> number of atoms %"QINT_FMT"\n",
            open_rsp->num_atoms);
    return QSUCCESS;
}

```

```

/* <function name='OpenRSPDestroy' author='Bin Gao' date='2014-01-28'>
    Destroys the OpenRSP context
    <param name='open_rsp' direction='inout'>The OpenRSP context</param>
    <return>Error information</return>
</function> */
QErrorCode OpenRSPDestroy(OpenRSP *open_rsp)
{
    QErrorCode ierr; /* error information */
    open_rsp->assembled = QFALSE;
    // if (open_rsp->elec_eom!=NULL) {
    ///*FIXME: to implement ierr = xxDestroy(open_rsp->elec_eom); */
    //     free(open_rsp->elec_eom);
    //     open_rsp->elec_eom = NULL;
    // }
    /* destroys the context of all perturbations involved in calculations */
    if (open_rsp->rsp_pert!=NULL) {
        ierr = RSPPertDestroy(open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertDestroy()");
        free(open_rsp->rsp_pert);
        open_rsp->rsp_pert = NULL;
    }
    /* destroys the context of overlap integrals */
    if (open_rsp->overlap!=NULL) {
        ierr = RSPOverlapDestroy(open_rsp->overlap);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapDestroy()");
        free(open_rsp->overlap);
        open_rsp->overlap = NULL;
    }
    /* destroys the linked list of one-electron operators */
    if (open_rsp->one_oper!=NULL) {
        ierr = RSPOneOperDestroy(&open_rsp->one_oper);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperDestroy()");
    }
    /* destroys the linked list of two-electron operators */
    if (open_rsp->two_oper!=NULL) {
        ierr = RSPTwoOperDestroy(&open_rsp->two_oper);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperDestroy()");
    }
    /* destroys the linked list of exchange-correlation functionals */
    if (open_rsp->xc_fun!=NULL) {
        ierr = RSPXCFunDestroy(&open_rsp->xc_fun);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunDestroy()");
    }
    /* destroys the context of nuclear Hamiltonian */
    if (open_rsp->zero_oper!=NULL) {
        ierr = RSPZeroOperDestroy(open_rsp->zero_oper);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperDestroy()");
        free(open_rsp->zero_oper);
        open_rsp->zero_oper = NULL;
    }
    /* destroys the context of linear response equation solver */
    if (open_rsp->rsp_solver!=NULL) {

```

```
        ierr = RSPSolverDestroy(open_rsp->rsp_solver);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverDestroy()");
        free(open_rsp->rsp_solver);
        open_rsp->rsp_solver = NULL;
    }
    return QSUCCESS;
}
```

3.3 Perturbations

The header file of perturbations is organized as:

```
22a <RSPPerturbation.h 22a>≡
/*
  <OpenRSPLicense 14a>

  <header name='RSPPerturbation.h' author='Bin Gao' date='2015-06-23'>
    The header file of perturbations used inside OpenRSP
  </header>
*/

#if !defined(RSP_PERTURBATION_H)
#define RSP_PERTURBATION_H

/* QcMatrix library */
#include "qcmatrix.h"

<RSPPertBasicTypes 22b>

<RSPPertCallback 24a>

<RSPPertStruct 24b>

<RSPPertAPIs 26a>

#endif
```

3.3.1 Internal Perturbation Labels

Perturbation labels are represented by integers. Each different label is marked by an internal identifier for calculating reponse functions and residues, so OPENRSP can sort these labels in ascending order by their identifiers. For instance, identifiers for a perturbation tuple *acbadbc* are 0120321.

To avoid using extra arrays for identifiers, we combine each host programs' label with its identifier into a QcPertInt type integer:

$$\text{QcPertInt} = \text{identifier} \ll \text{OPENRSP_PERT_LABEL_BIT} + \text{label},$$

where OPENRSP_PERT_LABEL_BIT is the number of bits in an object of QcPertInt for representing the host programs' perturbation labels:

```
22b <RSPPertBasicTypes 22b>≡
/* <macrodef name='OPENRSP_PERT_LABEL_BIT'>
  Set <OPENRSP_PERT_LABEL_BIT>
</macrodef>
<constant name='OPENRSP_PERT_LABEL_BIT'>
  Number of bits in an object of <QcPertInt> type for a perturbation label
</constant> */
#if !defined(OPENRSP_PERT_LABEL_BIT)
#define OPENRSP_PERT_LABEL_BIT 10
#endif
```

The type `QcPertInt` is defined as:

23a `<RSPPertBasicTypes 22b>+≡`

```

/* <datatype name='QcPertInt'>
    Data type of integers to represent perturbation labels
</datatype>
<constant name='QCPERTINT_MAX'>
    Maximal value of an object of the <QcPertInt> type
</constant>
<constant name='QCPERTINT_FMT'>
    Format string of <QcPertInt> type
</constant> */
//typedef unsigned long QcPertInt;
//#define QCPERTINT_MAX ULONG_MAX
//#define QCPERTINT_FMT "lu"
typedef unsigned int QcPertInt;
#define QCPERTINT_MAX UINT_MAX
#define QCPERTINT_FMT "u"

```

Here we also define a constant `QCPERTINT_MAX` for the maximal value of an object of the `QcPertInt` type, and a format string (`QCPERTINT_FMT`) of the `QcPertInt` type.

From `OPENRSP_PERT_LABEL_BIT` and `QCPERTINT_MAX` we can compute `OPENRSP_PERT_LABEL_MAX` and `OPENRSP_PERT_ID_MAX`, which are the maximal values of host programs' perturbation labels and internal perturbation identifiers:

23b `<RSPPertBasicTypes 22b>+≡`

```

/* <constant name='OPENRSP_PERT_LABEL_MAX'>
    Maximal value for perturbation labels
</constant>
<constant name='OPENRSP_PERT_ID_MAX'>
    Maximal value for internal perturbation identifier
</constant> */
extern const QcPertInt OPENRSP_PERT_LABEL_MAX;
extern const QcPertInt OPENRSP_PERT_ID_MAX;

```

Here, to avoid multiple inclusions of the header file that will lead to multiple definitions, we have the following implementation file for the `OPENRSP_PERT_LABEL_MAX` and `OPENRSP_PERT_ID_MAX`:

23c `<RSPPerturbation.c 23c>≡`

```

/*
    <OpenRSPLicense 14a>
*/

#include "RSPPerturbation.h"

const QcPertInt OPENRSP_PERT_LABEL_MAX = (1<<OPENRSP_PERT_LABEL_BIT)-1;
const QcPertInt OPENRSP_PERT_ID_MAX = (QCPERTINT_MAX-(1<<OPENRSP_PERT_LABEL_BIT)+1)
    >> OPENRSP_PERT_LABEL_BIT;

/* see https://scaryreasoner.wordpress.com/2009/02/28/checking-sizeof-at-compile-time
    accessing date Oct. 6, 2015 */
#define QC_BUILD_BUG_ON(condition) ((void)sizeof(char[1 - 2*!!(condition)]))
void RSPPertCheckLabelBit()
{
    QC_BUILD_BUG_ON(sizeof(QcPertInt)*CHAR_BIT<=OPENRSP_PERT_LABEL_BIT);
    QC_BUILD_BUG_ON(QINT_MAX<OPENRSP_PERT_LABEL_MAX);
}

```

The function `RSPPertCheckLabelBit()` ensures that (i) `OPENRSP_PERT_LABEL_BIT` is not too large and there are still bits left for the identifiers, and (ii) the number of different perturbation labels is not greater than the maximal value of an object of the `QInt` type so that we can still use `QInt` type integers for the number of (different) perturbation labels and the length of perturbation tuples. Note that the number of internal identifiers is less than or equal to the number of different perturbation labels involved in calculations, so it automatically satisfies the condition (ii).

One will have building error when compiling the function `RSPPertCheckLabelBit()` if the constant `OPENRSP_PERT_LABEL_BIT` is too large. However, the function `RSPPertCheckLabelBit()` can not guarantee the above setting (`QcPertInt` type and `OPENRSP_PERT_LABEL_BIT`) is enough for holding the host programs' perturbation labels and the internal identifiers. This will be checked against `OPENRSP_PERT_LABEL_MAX` and `OPENRSP_PERT_ID_MAX` by `OPENRSP` when (i) setting the host programs' perturbations, and (ii) calculating response functions or residues.

3.3.2 Callback Functions for Perturbations

As discussed in Section 2.5.6, we will need a callback function `get_pert_concatenation()` to get the ranks of components of sub-perturbation tuples (with the same perturbation label) for given components of the corresponding concatenated perturbation tuple. The type of this callback function is defined as follows:

24a $\langle RSPPertCallback \text{ 24a} \rangle \equiv$

```
typedef void (*GetPertCat)(const QInt,
                           const QcPertInt,
                           const QInt,
                           const QInt,
                           const QInt*,
                           #if defined(OPENRSP_C_USER_CONTEXT)
                           void*,
                           #endif
                           QInt*);
```

We will discuss how to use this callback function in Section 3.3.4.

3.3.3 Perturbation Context and Its Basic APIs

Also as mentioned in Section 2.5.6, `OPENRSP` needs to know the numbers of components of host programs' perturbations. Because the number of components of a higher-order perturbation is simply the product of numbers of components of lower-order perturbations with different labels. For instance, the number of components of a perturbation $a_{\omega_a}^{n_a} b_{\omega_b}^{n_b}$ is simply the product of numbers of components of perturbations $a_{\omega_a}^{n_a}$ and $b_{\omega_b}^{n_b}$.

Therefore, if there are in total p different perturbation labels a_1, a_2, \dots, a_p involved in calculations, `OPENRSP` needs to know

1. allowed maximal order of a perturbation described by exactly **one** of these different labels a_1, a_2, \dots, a_p ; let us mark these allowed maximal orders as n_1, n_2, \dots, n_p , which means we will have $k_j \leq n_j$ ($1 \leq j \leq p$) for any perturbation $a_{1,\omega_1}^{k_1} a_{2,\omega_2}^{k_2} \dots a_{p,\omega_p}^{k_p}$;
2. numbers of components of perturbations $a_{j,\omega_j}^{k_j}$, where $1 \leq k_j \leq n_j$ and $1 \leq j \leq p$; let us mark these numbers of components as $[N_j^{k_j}]$.

The above information is saved into the following `struct`:

24b $\langle RSPPertStruct \text{ 24b} \rangle \equiv$

```
typedef struct {
    QInt num_pert_lab;                /* number of different perturbation
                                     labels $$$ */
    QInt *pert_max_orders;            /* $n_{1},n_{2},\cdots,n_{p}$ */
    QInt *ptr_ncomp;                 /* pointers to  $[N_{\{j\}}^{k_{\{j\}}}]$  */
};
```



```

        for each  $a_{\{j\}}$  $ */
    QInt *pert_num_comps;          /*  $[N_{\{j\}}^{k_{\{j\}}}]$ , where
                                    $1 \leq k_{\{j\}} \leq n_{\{j\}}$  and  $1 \leq j \leq p$  $ */
    QcPertInt *pert_labels;       /*  $a_{\{1\}}, a_{\{2\}}, \dots, a_{\{p\}}$  $ */
    #if defined(OPENRSP_C_USER_CONTEXT)
        void *user_ctx;          /* user-defined callback function context */
    #endif
    GetPertCat get_pert_concatenation; /* user-specified function for getting
                                       the ranks of components of sub-perturbation
                                       tuples (with the same perturbation label)
                                       for given components of the corresponding
                                       concatenated perturbation tuple */
} RSPPert;

```

and users can set the above information by the following API:

```

25  <OpenRSP.c 17a> +=
    /* <function name='OpenRSPSetPerturbations' author='Bin Gao' date='2015-06-29'>
       Sets all perturbations involved in response theory calculations
       <param name='open_rsp' direction='inout'>The OpenRSP context</param>
       <param name='num_pert_lab' direction='in'>
          Number of all different perturbation labels involved in calculations
       </param>
       <param name='pert_labels' direction='in'>
          All the different perturbation labels involved
       </param>
       <param name='pert_max_orders' direction='in'>
          Allowed maximal order of a perturbation described by exactly one of
          the above different labels
       </param>
       <param name='pert_num_comps' direction='in'>
          Number of components of a perturbation described by exactly one of
          the above different labels, up to the allowed maximal order, size
          is therefore the sum of <param_max_orders>
       </param>
       <param name='user_ctx' direction='in'>
          User-defined callback function context
       </param>
       <param name='get_pert_concatenation' direction='in'>
          User specified function for getting the ranks of components of
          sub-perturbation tuples (with the same perturbation label) for given
          components of the corresponding concatenated perturbation tuple
       </param>
       <return>Error information</return>
    </function> */
    QErrorCode OpenRSPSetPerturbations(OpenRSP *open_rsp,
                                       const QInt num_pert_lab,
                                       const QcPertInt *pert_labels,
                                       const QInt *pert_max_orders,
                                       const QInt *pert_num_comps,
    #if defined(OPENRSP_C_USER_CONTEXT)
                                       void *user_ctx,
    #endif
                                       const GetPertCat get_pert_concatenation)

```

```

{
    QErrorCode ierr; /* error information */
    /* creates the context of all perturbations involved in calculations */
    if (open_rsp->rsp_pert!=NULL) {
        ierr = RSPPertDestroy(open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertDestroy()");
    }
    else {
        open_rsp->rsp_pert = (RSPPert *)malloc(sizeof(RSPPert));
        if (open_rsp->rsp_pert==NULL) {
            QErrorExit(FILE_AND_LINE, "allocates memory for perturbations");
        }
    }
    ierr = RSPPertCreate(open_rsp->rsp_pert,
                        num_pert_lab,
                        pert_labels,
                        pert_max_orders,
                        pert_num_comps,
#ifdef OPENRSP_C_USER_CONTEXT
                        user_ctx,
#endif
                        get_pert_concatenation);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertCreate()");
    return QSUCCESS;
}

```

The APIs `RSPPertCreate()` and `RSPPertDestroy()` will respectively create and destroy the content of the struct `RSPPert`. We also need APIs to assemble and to write the struct `RSPPert`:

26a $\langle RSPPertAPIs \text{ 26a} \rangle \equiv$

```

extern QErrorCode RSPPertCreate(RSPPert*,
                                const QInt,
                                const QcPertInt*,
                                const QInt*,
                                const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
                                void*,
#endif
                                const GetPertCat);
extern QErrorCode RSPPertAssemble(RSPPert*);
extern QErrorCode RSPPertWrite(const RSPPert*,FILE*);
extern QErrorCode RSPPertDestroy(RSPPert*);

```

which are respectively implemented as follows:

26b $\langle RSPPerturbation.c \text{ 23c} \rangle + \equiv$

```

/* <function name='RSPPertCreate'
   attr='private'
   author='Bin Gao'
   date='2015-06-28'>
    Sets all perturbations involved in response theory calculations, should be
    called at first
    <param name='rsp_pert' direction='inout'>
        The context of perturbations
    </param>

```

```

    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels involved in calculations
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels involved
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
    </param>
    <param name='pert_num_comps' direction='in'>
        Number of components of a perturbation described by exactly one of
        the above different labels, up to the allowed maximal order, size
        is therefore the sum of <pert_max_orders>
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback function context
    </param>
    <param name='get_pert_concatenation' direction='in'>
        User-specified function for getting the ranks of components of
        sub-perturbation tuples (with the same perturbation label) for given
        components of the corresponding concatenated perturbation tuple
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPPertCreate(RSPPert *rsp_pert,
                        const QInt num_pert_lab,
                        const QcPertInt *pert_labels,
                        const QInt *pert_max_orders,
                        const QInt *pert_num_comps,
#ifdef OPENRSP_C_USER_CONTEXT
                        void *user_ctx,
#endif
                        const GetPertCat get_pert_concatenation)
{
    QInt ilab;    /* incremental recorders over perturbation labels */
    QInt jlab;
    QInt iorder; /* incremental recorder over orders */
    QInt icomp;  /* incremental recorder over components */
    if (num_pert_lab < 1) {
        printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab > OPENRSP_PERT_LABEL_MAX) {
        printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPPertCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
    }
    rsp_pert->num_pert_lab = num_pert_lab;

```

```

rsp_pert->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
if (rsp_pert->pert_labels==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
}
rsp_pert->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
if (rsp_pert->pert_max_orders==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
}
rsp_pert->ptr_ncomp = (QInt *)malloc((num_pert_lab+1)*sizeof(QInt));
if (rsp_pert->ptr_ncomp==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for pointers to components");
}
rsp_pert->ptr_ncomp[0] = 0;
for (ilab=0; ilab<num_pert_lab; ilab++) {
    if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPPertCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "invalid perturbation label");
    }
    /* each element of <pert_labels> should be unique */
    for (jlab=0; jlab<ilab; jlab++) {
        if (pert_labels[jlab]==pert_labels[ilab]) {
            printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   jlab,
                   pert_labels[jlab]);
            printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
        }
    }
    rsp_pert->pert_labels[ilab] = pert_labels[ilab];
    if (pert_max_orders[ilab]<1) {
        printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPPertCreate>> allowed maximal order is %"QINT_FMT"\n",
               pert_max_orders[ilab]);
        QErrorExit(FILE_AND_LINE, "only positive order allowed");
    }
    rsp_pert->pert_max_orders[ilab] = pert_max_orders[ilab];
    /* <c>rsp_pert->ptr_ncomp[ilab]</c> points to the number of components
       of <c>rsp_pert->pert_labels[ilab]</c> */
}

```

```

    rsp_pert->ptr_ncomp[ilab+1] = rsp_pert->ptr_ncomp[ilab]+pert_max_orders[ilab];
}
/* <c>rsp_pert->ptr_ncomp[num_pert_lab]</c> equals to the size of
   <c>rsp_pert->pert_num_comps</c> */
rsp_pert->pert_num_comps = (QInt *)malloc(rsp_pert->ptr_ncomp[num_pert_lab]
                                           *sizeof(QInt));
if (rsp_pert->pert_num_comps==NULL) {
    printf("RSPPertCreate>> size of numbers of components %"QINT_FMT"\n",
           rsp_pert->ptr_ncomp[num_pert_lab]);
    QErrorExit(FILE_AND_LINE, "allocates memory for numbers of components");
}
for (ilab=0, icoomp=0; ilab<num_pert_lab; ilab++) {
    for (iorder=1; iorder<=rsp_pert->pert_max_orders[ilab]; iorder++, icoomp++) {
        if (pert_num_comps[icoomp]<1) {
            printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            printf("RSPPertCreate>> allowed maximal order is %"QINT_FMT"\n",
                   pert_max_orders[ilab]);
            printf("RSPPertCreate>> %"QINT_FMT"-th No. of comps. is %"QINT_FMT"\n",
                   iorder,
                   pert_num_comps[icoomp]);
            QErrorExit(FILE_AND_LINE, "incorrect number of components");
        }
        rsp_pert->pert_num_comps[icoomp] = pert_num_comps[icoomp];
    }
}
}
#endif defined(OPENRSP_C_USER_CONTEXT)
    rsp_pert->user_ctx = user_ctx;
#endif
    rsp_pert->get_pert_concatenation = get_pert_concatenation;
    return QSUCCESS;
}

```

Here we check the number of perturbation labels and each label against OPENRSP_PERT_LABEL_MAX.

```

29  <RSPPerturbation.c 23c>+≡
    /* <function name='RSPPertAssemble'
       attr='private'
       author='Bin Gao'
       date='2015-06-28'>
       Assembles the context of perturbations involved in calculations
       <param name='rsp_pert' direction='inout'>
           The context of perturbations
       </param>
       <return>Error information</return>
    </function> */
    QErrorCode RSPPertAssemble(RSPPert *rsp_pert)
    {
        if (rsp_pert->pert_labels==NULL ||
            rsp_pert->pert_max_orders==NULL ||
            rsp_pert->ptr_ncomp==NULL ||
            rsp_pert->pert_num_comps==NULL ||

```

```

    rsp_pert->get_pert_concatenation==NULL) {
        QErrorExit(FILE_AND_LINE, "perturbations are not correctly set");
    }
    return QSUCCESS;
}

/* <function name='RSPPertWrite'
    attr='private'
    author='Bin Gao'
    date='2015-06-28'>
    Writes the context of perturbations involved in calculations
    <param name='rsp_pert' direction='in'>
        The context of perturbations
    </param>
    <param name='fp_pert' direction='inout'>File pointer</param>
    <return>Error information</return>
</function> */
QErrorCode RSPPertWrite(const RSPPert *rsp_pert, FILE *fp_pert)
{
    QInt ilab; /* incremental recorder over perturbation labels */
    QInt icomp; /* incremental recorder over components */
    fprintf(fp_pert,
        "RSPPertWrite>> number of all perturbation labels %"QINT_FMT"\n",
        rsp_pert->num_pert_lab);
    fprintf(fp_pert,
        "RSPPertWrite>> label          maximum-order      numbers-of-components\n");
    for (ilab=0; ilab<rsp_pert->num_pert_lab; ilab++) {
        fprintf(fp_pert,
            "RSPPertWrite>>  %"QCPERTINT_FMT"          %"QINT_FMT"          "
            rsp_pert->pert_labels[ilab],
            rsp_pert->pert_max_orders[ilab]);
        for (icomp=rsp_pert->ptr_ncomp[ilab]; icomp<rsp_pert->ptr_ncomp[ilab+1]; icomp++) {
            fprintf(fp_pert, " %"QINT_FMT",", rsp_pert->pert_num_comps[icomp]);
        }
        fprintf(fp_pert, "\n");
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        if (rsp_pert->user_ctx!=NULL) {
            fprintf(fp_pert, "RSPPertWrite>> user-defined function context given\n");
        }
    #endif
    return QSUCCESS;
}

/* <function name='RSPPertDestroy'
    attr='private'
    author='Bin Gao'
    date='2015-06-28'>
    Destroys the context of perturbations involved in calculations, should be
    called at the end
    <param name='rsp_pert' direction='inout'>
        The context of perturbations

```

```

    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPPertDestroy(RSPPert *rsp_pert)
{
    rsp_pert->num_pert_lab = 0;
    free(rsp_pert->pert_labels);
    rsp_pert->pert_labels = NULL;
    free(rsp_pert->pert_max_orders);
    rsp_pert->pert_max_orders = NULL;
    free(rsp_pert->ptr_ncomp);
    rsp_pert->ptr_ncomp = NULL;
    free(rsp_pert->pert_num_comps);
    rsp_pert->pert_num_comps = NULL;
#ifdef OPENRSP_C_USER_CONTEXT
    rsp_pert->user_ctx = NULL;
#endif
    rsp_pert->get_pert_concatenation = NULL;
    return QSUCCESS;
}

```

When users set different contributions to the Hamiltonian, there are also perturbations acting on the corresponding contributions. We need to check if these perturbations are valid:

31a $\langle RSPertAPIs\ 26a \rangle + \equiv$

```

extern QErrorCode RSPPertValidateLabelOrder(const RSPPert*,
                                             const QInt,
                                             const QcPertInt*,
                                             const QInt*);

```

31b $\langle RSPPerturbation.c\ 23c \rangle + \equiv$

```

/* <function name='RSPPertValidateLabelOrder'
   attr='private'
   author='Bin Gao'
   date='2015-10-15'>

Check the validity of given perturbation labels and corresponding allowed
maximal orders
<param name='rsp_pert' direction='in'>
    The context of perturbations
</param>
<param name='num_pert_lab' direction='in'>
    Number of all different perturbation labels
</param>
<param name='pert_labels' direction='in'>
    Different perturbation labels that will be checked
</param>
<param name='pert_max_orders' direction='in'>
    Allowed maximal order of a perturbation described by exactly one of
    the above different labels
</param>
<return>
    <QSUCCESS> if perturbation labels and orders are valid,
    <QFAILURE> otherwise
</return>

```

```

</function> */
QErrorCode RSPPertValidateLabelOrder(const RSPPert *rsp_pert,
                                     const QInt num_pert_lab,
                                     const QcPertInt *pert_labels,
                                     const QInt *pert_max_orders)
{
    QInt ilab;          /* incremental recorders over perturbation labels */
    QInt jlab;
    QBool pert_valid; /* validity of the perturbations */
    for (ilab=0; ilab<num_pert_lab; ilab++) {
        pert_valid = QFALSE;
        for (jlab=0; jlab<rsp_pert->num_pert_lab; jlab++) {
            /* valid perturbation label, checks its allowed maximal order */
            if (pert_labels[ilab]==rsp_pert->pert_labels[jlab]) {
                if (pert_max_orders[ilab]<=rsp_pert->pert_max_orders[jlab]) {
                    pert_valid = QTRUE;
                }
                break;
            }
        }
        if (pert_valid==QFALSE) return QFAILURE;
    }
    return QSUCCESS;
}

```

One should note that we here assume all the elements of `pert_labels` are different.

3.3.4 Conversion of Perturbation Tuples and Labels

As discussed in Section 3.3.1, we will use internal perturbation labels (identifier and host program's perturbation label) inside OPENRSP. As such, we need to implement functions for the conversion of internal perturbation labels and host programs' ones.

First, when calculating response functions and residues, we need to convert the users' given perturbation tuple $abc\dots$ into our internal one. We also need to sort the perturbation tuple $abc\dots$ and the corresponding complex frequencies $[\omega_a\omega_b\omega_c\dots, \dots]$. The sorting is carried out in two steps:

1. We take the first label of the perturbation tuple as the perturbation a (see definition in Section 2.5.6). We fix the first label of the tuple, and rearrange the tuple by collecting identical labels together after their first entity.

For example, the sorted perturbation tuple of $acbadbc$ becomes $aaccbbd$.

2. We next sort frequencies of the same perturbation labels in ascending order, and the frequency of the first label of the tuple is the negative sum of frequencies of other labels.

For example, if users give two frequency configurations for a perturbation tuple $aaccbbd$, the sorted frequencies will satisfy:

$$\begin{aligned}
 -\sum_i \omega_i &\leq \omega_1 \leq \omega_2 \leq \omega_3 \leq \omega_4 \leq \omega_5 \leq \omega_6, \\
 -\sum_i \omega'_i &\leq \omega'_1 \leq \omega'_2 \leq \omega'_3 \leq \omega'_4 \leq \omega'_5 \leq \omega'_6.
 \end{aligned}$$

The following function will perform the above converting and sorting procedure, and also check if the perturbation labels have been given by the API `OpenRSPSetPerturbations()`:


```

// QcPertInt id_pert; /* identifiers of different perturbation labels */
// QBool lab_valid; /* validity of the perturbation labels */
//
// QInt ipert,jpert; /* incremental recorders */
// QInt first_id; /* first identical pertubation label in the tuple */
// QInt last_id; /* last identical pertubation label in the tuple */
// QBool non_id; /* indicates if non-identical label found */
//
// id_pert = 0;
//
// for (ipert=0,jpert=0; ipert<len_tuple; ) {
//
// /* checks the current perturbation label against all known
// perturbation labels */
// lab_valid = QFALSE;
// for (ilab=0; ilab<rsp_pert->num_pert_lab; ilab++) {
// if (pert_tuple[ipert]==rsp_pert->pert_labels[ilab]) {
// lab_valid = QTRUE;
// break;
// }
// }
// if (lab_valid==QTRUE) {
// /* converts the current perturbation label to internal one */
// intern_pert_tuple[jpert] = (id_pert<<OPENRSP_PERT_LABEL_BIT)
// + pert_tuple[ipert];
// /* finds the other same perturbation labels */
//
// /* updates the identifier */
// id_pert++;
// else {
// printf("RSPPertCreate>> %"QINT_FMT"-th perturbation %"QCPERTINT_FMT"\n",
// ipert,
// pert_tuple[ipert]);
// QErrorExit(FILE_AND_LINE, "invalid perturbation label");
// }
//
// }
//
// /* we first try to find consecutive identical pertubation labels */
// first_id = 0;
// non_id = QFALSE;
// for (ipert=first_id; ipert<len_tuple-1; ipert++) {
// if (pert_tuple[ipert]!=pert_tuple[ipert+1]) {
// last_id = ipert;
// non_id = QTRUE;
// break;
// }
// }
// if (non_id==QTRUE) {
// }

```

```

//     else {
//     }

    return QSUCCESS;
}

```

where we have also checked the number of different identifiers against `OPENRSP_PERT_ID_MAX`.

Inside `OPENRSP`, we mostly use the internal perturbation labels/tuples. But when we use callback functions to get integrals and/or expectation values of overlap, one- and two-electron operators as well as contributions from nuclear Hamiltonian, only the host programs' perturbation labels and orders are meaningful for these callback functions; when we want the integrals and/or expectation values of XC functionals¹, we need to convert our internal perturbation tuples to the host programs' ones.

We first consider the former task—a function that converts an internal perturbation tuple into host program's perturbation labels and orders:

35a `<RSPertAPIs 26a>+≡`

```

extern QErrorCode RSPPertInternTupleToHostLabelOrder(const QInt,
                                                    const QcPertInt*,
                                                    const QInt,
                                                    const QcPertInt*,
                                                    const QInt*,
                                                    QInt*,
                                                    QcPertInt*,
                                                    QInt*);

```

This function also checks if the resulted perturbation labels and orders are allowed (or non-zero perturbed quantities) by checking against allowed host program's perturbation labels and orders:

35b `<RSPPerturbation.c 23c>+≡`

```

/* <function name='RSPPertInternTupleToHostLabelOrder'
   attr='private'
   author='Bin Gao'
   date='2015-10-08'>

    Convert an internal perturbation tuple to host program's perturbation
    labels and the corresponding orders
    <param name='len_intern_tuple' direction='in'>
        Length of the internal perturbation tuple
    </param>
    <param name='intern_pert_tuple' direction='in'>
        The internal perturbation tuple
    </param>
    <param name='num_allowed_labels' direction='in'>
        Number of allowed different host program's perturbation labels
    </param>
    <param name='allowed_pert_labels' direction='in'>
        All the allowed different host program's perturbation labels
    </param>
    <param name='allowed_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different host program's labels
    </param>

```

¹XC functionals need all density matrices and are calculated differently from other operators, we therefore choose to send the perturbation tuple to XC-functional callback functions

```

    <param name='num_pert' direction='out'>
        Number of different perturbations from the internal perturbation tuple,
        $-1$ indicates there are perturbation labels/orders not allowed
    </param>
    <param name='pert_labels' direction='out'>
        Host program's perturbation labels of the resulted perturbations
    </param>
    <param name='pert_orders' direction='out'>
        Orders of the resulted perturbations
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPPertInternTupleToHostLabelOrder(const QInt len_intern_tuple,
                                                const QcPertInt *intern_pert_tuple,
                                                const QInt num_allowed_labels,
                                                const QcPertInt *allowed_pert_labels,
                                                const QInt *allowed_max_orders,
                                                QInt *num_pert,
                                                QcPertInt *pert_labels,
                                                QInt *pert_orders)
{
    QcPertInt host_pert_label; /* host program's perturbation label */
    QBool pert_allowed;        /* resulted perturbations allowed or not */
    QInt ipert;                /* incremental recorder for different perturbations */
    QInt ilab;                 /* incremental recorder over perturbation labels */
    QInt idx_allowed;          /* index of the allowed perturbation label */
    ipert = 0;
    for (ilab=0; ilab<len_intern_tuple; ) {
        /* converts to the host program's label */
        host_pert_label = intern_pert_tuple[ilab] & OPENRSP_PERT_LABEL_MAX;
        /* checks if the label is allowed */
        pert_allowed = QFALSE;
        for (idx_allowed=0; idx_allowed<num_allowed_labels; idx_allowed++) {
            if (host_pert_label==allowed_pert_labels[idx_allowed]) {
                pert_allowed = QTRUE;
                break;
            }
        }
        /* returns a negative number if the label is not allowed */
        if (pert_allowed==QFALSE) {
            *num_pert = -1;
            return QSUCCESS;
        }
        /* finds consecutive identical internal perturbation labels */
        pert_labels[ipert] = intern_pert_tuple[ilab];
        pert_orders[ipert] = 1;
        ilab++;
        for (; ilab<len_intern_tuple; ) {
            if (pert_labels[ipert]==intern_pert_tuple[ilab]) {
                pert_orders[ipert]++;
            }
            else {

```

```

        break;
    }
    ilab++;
}
/* checks if the order is allowed */
if (pert_orders[ipert]>allowed_max_orders[idx_allowed]) {
    *num_pert = -1;
    return QSUCCESS;
}
/* saves the host program's label */
pert_labels[ipert] = host_pert_label;
ipert++;
}
*num_pert = ipert;
return QSUCCESS;
}

```

where the conversion of the internal label to the host program's label is simply done by the bitwise AND operation (`&=`) with `OPENRSP_PERT_LABEL_MAX`.

As such, the latter task—converting our internal perturbation tuples to the host programs' ones is also quite easy:

37a `<RSPertAPIs 26a>+≡`

```

extern QErrorCode RSPPertInternTupleToHostTuple(const QInt,
                                                const QcPertInt*,
                                                const QInt,
                                                const QcPertInt*,
                                                const QInt*,
                                                QInt*,
                                                QcPertInt*);

```

37b `<RSPPerturbation.c 23c>+≡`

```

/* <function name='RSPPertInternTupleToHostTuple'
   attr='private'
   author='Bin Gao'
   date='2015-10-12'>

Convert an internal perturbation tuple to the corresponding host
program's one
<param name='len_intern_tuple' direction='in'>
    Length of the internal perturbation tuple
</param>
<param name='intern_pert_tuple' direction='in'>
    The internal perturbation tuple
</param>
<param name='num_allowed_labels' direction='in'>
    Number of allowed different host program's perturbation labels
</param>
<param name='allowed_pert_labels' direction='in'>
    All the allowed different host program's perturbation labels
</param>
<param name='allowed_max_orders' direction='in'>
    Allowed maximal order of a perturbation described by exactly one of
    the above different host program's labels
</param>

```

```

    <param name='len_tuple' direction='out'>
        Length of the resulted host program's perturbation tuple,
        $-1$ indicates there are perturbation labels/orders not allowed
    </param>
    <param name='pert_tuple' direction='out'>
        The resulted host program's perturbation tuple
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPPertInternTupleToHostTuple(const QInt len_intern_tuple,
                                          const QcPertInt *intern_pert_tuple,
                                          const QInt num_allowed_labels,
                                          const QcPertInt *allowed_pert_labels,
                                          const QInt *allowed_max_orders,
                                          QInt *len_tuple,
                                          QcPertInt *pert_tuple)
{
    QcPertInt host_pert_label; /* host program's perturbation label */
    QInt host_pert_order;      /* order of host program's perturbation */
    QBool pert_allowed;        /* resulted perturbations allowed or not */
    QInt ipert;                /* incremental recorder for different perturbations */
    QInt ilab;                 /* incremental recorder over perturbation labels */
    QInt idx_allowed;          /* index of the allowed perturbation label */
    ipert = 0;
    for (ilab=0; ilab<len_intern_tuple; ) {
        /* converts to the host program's label */
        host_pert_label = intern_pert_tuple[ilab] & OPENRSP_PERT_LABEL_MAX;
        /* checks if the label is allowed */
        pert_allowed = QFALSE;
        for (idx_allowed=0; idx_allowed<num_allowed_labels; idx_allowed++) {
            if (host_pert_label==allowed_pert_labels[idx_allowed]) {
                pert_allowed = QTRUE;
                break;
            }
        }
        /* returns a negative number if the label is not allowed */
        if (pert_allowed==QFALSE) {
            *len_tuple = -1;
            return QSUCCESS;
        }
        /* finds consecutive identical internal perturbation labels */
        pert_tuple[ipert] = intern_pert_tuple[ilab];
        host_pert_order = 1;
        ilab++;
        for (; ilab<len_intern_tuple; ) {
            if (pert_tuple[ipert]==intern_pert_tuple[ilab]) {
                host_pert_order++;
            }
            else {
                break;
            }
            ilab++;
        }
    }
}

```

```

    }
    /* checks if the order is allowed */
    if (host_pert_order>allowed_max_orders[idx_allowed]) {
        *len_tuple = -1;
        return QSUCCESS;
    }
    /* saves the host program's labels */
    for (; host_pert_order>0; host_pert_order--) {
        pert_tuple[ipert] = host_pert_label;
        ipert++;
    }
}
*len_tuple = ipert;
return QSUCCESS;
}

```

We will also use the callback function declared in Section 3.3.2 for OPENRSP to construct higher-order derivatives from lower-order ones:

39a $\langle RSPertAPIs\ 26a \rangle + \equiv$

```

extern QErrorCode RSPPertGetConcatenation(const RSPPert*,
                                           const QcPertInt,
                                           const QInt,
                                           const QInt,
                                           const QInt,
                                           const QInt*,
                                           QInt*);

```

This function actually uses the callback function `get_pert_concatenation()` to get ranks of components of sub-perturbation tuples (with the same perturbation label) for given components of the corresponding concatenated perturbation tuple:

39b $\langle RSPPerturbation.c\ 23c \rangle + \equiv$

```

/* <function name='RSPPertGetConcatenation'
   attr='private'
   author='Bin Gao'
   date='2015-06-28'>

Gets the ranks of components of sub-perturbation tuples
<param name='rsp_pert' direction='inout'>
    The context of perturbations
</param>
<param name='intern_pert_label' direction='in'>
    The internal perturbation label
</param>
<param name='first_cat_comp' direction='in'>
    Rank of the first component of the concatenated perturbation tuple
</param>
<param name='num_cat_comps' direction='in'>
    Number of components of the concatenated perturbation tuple
</param>
<param name='num_sub_tuples' direction='in'>
    Number of sub-perturbation tuples to construct the concatenated
    perturbation tuple
</param>
<param name='len_sub_tuples' direction='in'>

```

```

    Length of each sub-perturbation tuple, size is <num_sub_tuples> so
    that the length of the concatenated perturbation tuple is the sum
    of <len_sub_tuples>
</param>
<param name='rank_sub_comps' direction='out'>
    Ranks of components of sub-perturbation tuples for the corresponding
    component of the concatenated perturbation tuple, i.e. <num_cat_comps>
    components starting from the one with the rank <first_cat_comp>; size
    is therefore the product of <num_sub_tuples> and <num_cat_comps>, and
    is arranged as <c>[num_cat_comps][num_sub_tuples]</c> in memory
</param>
<return>Error information</return>
</function> */
QErrorCode RSPPertGetConcatenation(const RSPPert *rsp_pert,
                                   const QcPertInt intern_pert_label,
                                   const QInt first_cat_comp,
                                   const QInt num_cat_comps,
                                   const QInt num_sub_tuples,
                                   const QInt *len_sub_tuples,
                                   QInt *rank_sub_comps)
{
    QcPertInt pert_label;
    /* converts to host program's perturbation label */
    pert_label = intern_pert_label & OPENRSP_PERT_LABEL_MAX;
    #if defined(OPENRSP_ZERO_BASED)
        rsp_pert->get_pert_concatenation(pert_label,
                                         first_cat_comp,
                                         num_cat_comps,
                                         num_sub_tuples,
                                         len_sub_tuples,
                                         #if defined(OPENRSP_C_USER_CONTEXT)
                                         rsp_pert->user_ctx,
                                         #endif
                                         rank_sub_comps);
    #else
        QInt icomp; /* incremental recorder over ranks of components */
        rsp_pert->get_pert_concatenation(pert_label,
                                         first_cat_comp+1,
                                         num_cat_comps,
                                         num_sub_tuples,
                                         len_sub_tuples,
                                         #if defined(OPENRSP_C_USER_CONTEXT)
                                         rsp_pert->user_ctx,
                                         #endif
                                         rank_sub_comps);
        for (icomp=0; icomp<num_cat_comps*num_sub_tuples; icomp++) {
            rank_sub_comps[icomp]--;
        }
    #endif
    return QSUCCESS;
}

```


July 12, 2018/Users/bga006/Work/XKjem/gitlab/lldalton-openrsp/external/openrsp/web/RSPPerturbat

Here except for the conversion to host program's perturbation label, we also need to convert ranks to zero-based numbering if users have chosen the one-based numbering.

3.4 Overlap Operator

OPENRSP needs to invoke host program's callback functions to calculate the integral matrices or expectation values of overlap operator as well as its derivatives with respect to different perturbations. Users can use the following API to tell OPENRSP the information of the overlap operator:

```
42  <OpenRSP.c 17a>+≡
    /* <function name='OpenRSPSetOverlap' author='Bin Gao' date='2014-07-30'>
        Set the overlap operator
        <param name='open_rsp' direction='inout'>
            The context of response theory calculations
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act on the
            overlap operator
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels involved
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback function context
        </param>
        <param name='get_overlap_mat' direction='in'>
            User-specified callback function to calculate integral matrices of
            overlap operator as well as its derivatives with respect to different
            perturbations
        </param>
        <param name='get_overlap_exp' direction='in'>
            User-specified callback function to calculate expectation values of
            overlap operator as well as its derivatives with respect to different
            perturbations
        </param>
        <return>Error information</return>
    </function> */
QErrorCode OpenRSPSetOverlap(OpenRSP *open_rsp,
                             const QInt num_pert_lab,
                             const QcPertInt *pert_labels,
                             const QInt *pert_max_orders,
#ifdef (OPENRSP_C_USER_CONTEXT)
                             void *user_ctx,
#endif
                             const GetOverlapMat get_overlap_mat,
                             const GetOverlapExp get_overlap_exp)
{
    QErrorCode ierr; /* error information */
    /* creates the context of overlap operator */
    if (open_rsp->overlap!=NULL) {
        ierr = RSPOverlapDestroy(open_rsp->overlap);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapDestroy()");
    }
}
```

```

    }
    else {
        open_rsp->overlap = (RSPOverlap *)malloc(sizeof(RSPOverlap));
        if (open_rsp->overlap==NULL) {
            QErrorExit(FILE_AND_LINE, "allocates memory for overlap");
        }
    }
    ierr = RSPOverlapCreate(open_rsp->overlap,
                            num_pert_lab,
                            pert_labels,
                            pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                            user_ctx,

                            get_overlap_mat,
                            get_overlap_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapCreate()");
    return QSUCCESS;
}

```

The following header file defines all quantities we need for the overlap operator. Types `GetOverlapMat` and `GetOverlapExp` define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of overlap operator and its derivatives.

```

43  <RSPOverlap.h 43>≡
    /*
    <OpenRSPLicense 14a>

    <header name='RSPOneOper.h' author='Bin Gao' date='2014-08-05'>
        The header file of overlap operator used inside OpenRSP
    </header>
    */

    #if !defined(RSP_OVERLAP_H)
    #define RSP_OVERLAP_H

    #include "qcmatrix.h"
    #include "RSPPerturbation.h"

    typedef void (*GetOverlapMat)(const QInt,
                                   const QcPertInt*,
                                   const QInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt*,
    #if defined(OPENRSP_C_USER_CONTEXT)
                                   void*,
    #endif
                                   const QInt,

```

```

                                QcMat*[]);
typedef void (*GetOverlapExp)(const QInt,
                                const QcPertInt*,
                                const QInt*,
                                const QInt,
                                const QcPertInt*,
                                const QInt*,
                                const QInt,
                                const QcPertInt*,
                                const QInt*,
                                const QInt,
                                QcMat*[],
                                void*,
                                const QInt,
                                QReal*);

```

⟨*RSPOverlapStruct* 44⟩

⟨*RSPOverlapAPIs* 45a⟩

#endif

The context of overlap operator is:

```

44  ⟨RSPOverlapStruct 44⟩≡
    typedef struct {
        QInt num_pert_lab;           /* number of different perturbation labels
                                      that can act as perturbations on the
                                      overlap operator */
        QInt bra_num_pert;          /* number of perturbations on the bra center,
                                      only used for callback functions */
        QInt ket_num_pert;          /* number of perturbations on the ket center,
                                      only used for callback functions */
        QInt oper_num_pert;         /* number of perturbations on the overlap operator,
                                      only used for callback functions */
        QInt *pert_max_orders;      /* allowed maximal order of a perturbation
                                      described by exactly one of these
                                      different labels */
        QInt *bra_pert_orders;      /* orders of perturbations on the bra center,
                                      only used for callback functions */
        QInt *ket_pert_orders;      /* orders of perturbations on the ket center,
                                      only used for callback functions */
        QInt *oper_pert_orders;     /* orders of perturbations on the overlap operator,
                                      only used for callback functions */
        QcPertInt *pert_labels;     /* all the different perturbation labels */
        QcPertInt *bra_pert_labels; /* labels of perturbations on the bra center,
                                      only used for callback functions */
        QcPertInt *ket_pert_labels; /* labels of perturbations on the ket center,
                                      only used for callback functions */
        QcPertInt *oper_pert_labels; /* labels of perturbations on the overlap operator,
                                      only used for callback functions */
    };
    #if defined(OPENRSP_C_USER_CONTEXT)

```

```

    void *user_ctx;                /* user-defined callback-function context */
#endif
    GetOverlapMat get_overlap_mat; /* user-specified function for calculating
                                   integral matrices */
    GetOverlapExp get_overlap_exp; /* user-specified function for calculating
                                   expectation values */
} RSPOverlap;

```

Here perturbations on the overlap operator represent those acting on the whole integral of the overlap operator, i.e. they can act on either the bra center or the ket center by applying the rule of derivatives of a product.

Functions related to the overlap operator are as follows:

```

45a  <RSPOverlapAPIs 45a>≡
extern QErrorCode RSPOverlapCreate(RSPOverlap*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt*,
                                   #if defined(OPENRSP_C_USER_CONTEXT)
                                   void*,
                                   #endif
                                   const GetOverlapMat,
                                   const GetOverlapExp);
extern QErrorCode RSPOverlapAssemble(RSPOverlap*,const RSPPert*);
extern QErrorCode RSPOverlapWrite(const RSPOverlap*,FILE*);
extern QErrorCode RSPOverlapGetMat(RSPOverlap*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   QcMat*[]);
extern QErrorCode RSPOverlapGetExp(RSPOverlap*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt,
                                   QcMat*[],
                                   const QInt,
                                   QReal*);
extern QErrorCode RSPOverlapDestroy(RSPOverlap*);

```

Let us now implement all the functions declared:

```

45b  <RSPOverlap.c 45b>≡
/*
   <OpenRSPLicense 14a>
*/

#include "RSPOverlap.h"

```

```

/* <function name='RSPOverlapCreate'
    attr='private'
    author='Bin Gao'
    date='2014-08-05'>
    Create the context of overlap operator, should be called at first
    <param name='overlap' direction='inout'>
        The context of overlap operator
    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the overlap operator
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback-function context
    </param>
    <param name='get_overlap_mat' direction='in'>
        User-specified function for calculating integral matrices of the
        overlap operator and its derivatives
    </param>
    <param name='get_overlap_exp' direction='in'>
        User-specified function for calculating expectation values of the
        overlap operator and its derivatives
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPOverlapCreate(RSPOverlap *overlap,
                            const QInt num_pert_lab,
                            const QcPertInt *pert_labels,
                            const QInt *pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                            void *user_ctx,
#endif
                            const GetOverlapMat get_overlap_mat,
                            const GetOverlapExp get_overlap_exp)
{
    QInt ilab; /* incremental recorders over perturbation labels */
    QInt jlab;
    if (num_pert_lab < 0) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab > OPENRSP_PERT_LABEL_MAX) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
    }
}

```

```

    printf("RSPOverlapCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
           OPENRSP_PERT_LABEL_MAX);
    QErrorExit(FILE_AND_LINE, "too many perturbation labels");
}
overlap->num_pert_lab = num_pert_lab;
if (overlap->num_pert_lab>0) {
    overlap->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->pert_max_orders==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    overlap->bra_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->bra_pert_orders==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on bra center");
    }
    overlap->ket_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->ket_pert_orders==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on ket center");
    }
    overlap->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->oper_pert_orders==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on overlap operator");
    }
    overlap->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->pert_labels==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    overlap->bra_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->bra_pert_labels==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on bra center");
    }
    overlap->ket_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->ket_pert_labels==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on ket center");
    }
    overlap->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->oper_pert_labels==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
    }
}

```

```

        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on overlap operato
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                ilab,
                pert_labels[ilab]);
            printf("RSPOverlapCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
                OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {
            if (pert_labels[jlab]==pert_labels[ilab]) {
                printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                    jlab,
                    pert_labels[jlab]);
                printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                    ilab,
                    pert_labels[ilab]);
                QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
            }
        }
        overlap->pert_labels[ilab] = pert_labels[ilab];
        if (pert_max_orders[ilab]<1) {
            printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                ilab,
                pert_labels[ilab]);
            printf("RSPOverlapCreate>> allowed maximal order is %"QINT_FMT"\n",
                pert_max_orders[ilab]);
            QErrorExit(FILE_AND_LINE, "only positive order allowed");
        }
        overlap->pert_max_orders[ilab] = pert_max_orders[ilab];
    }
}
else {
    overlap->pert_max_orders = NULL;
    overlap->bra_pert_orders = NULL;
    overlap->ket_pert_orders = NULL;
    overlap->oper_pert_orders = NULL;
    overlap->pert_labels = NULL;
    overlap->bra_pert_labels = NULL;
    overlap->ket_pert_labels = NULL;
    overlap->oper_pert_labels = NULL;
}
#if defined(OPENRSP_C_USER_CONTEXT)
    overlap->user_ctx = user_ctx;
#endif
overlap->get_overlap_mat = get_overlap_mat;
overlap->get_overlap_exp = get_overlap_exp;
return QSUCCESS;
}

```


As shown here, we allow for an overlap operator that does not depend on any perturbation—`num_pert_lab==0`, i.e. any perturbed integral matrix and expectation value of this overlap operator is zero.

```

49  <RSPOverlap.c 45b>+≡
    /* <function name='RSPOverlapAssemble'
        attr='private'
        author='Bin Gao'
        date='2014-08-05'>
        Assembles the context of overlap operator
        <param name='overlap' direction='inout'>
            The context of overlap operator
        </param>
        <param name='rsp_pert' direction='in'>
            The context of perturbations
        </param>
        <return>Error information</return>
    </function> */
    QErrorCode RSPOverlapAssemble(RSPOverlap *overlap, const RSPPert *rsp_pert)
    {
        QErrorCode ierr; /* error information */
        if (overlap->num_pert_lab>0 &&
            (overlap->pert_labels==NULL || overlap->pert_max_orders==NULL)) {
            QErrorExit(FILE_AND_LINE, "perturbations of overlap operator not set");
        }
        if (overlap->get_overlap_mat==NULL || overlap->get_overlap_exp==NULL) {
            QErrorExit(FILE_AND_LINE, "callback functions of overlap operator not set");
        }
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                         overlap->num_pert_lab,
                                         overlap->pert_labels,
                                         overlap->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        return QSUCCESS;
    }

    /* <function name='RSPOverlapWrite'
        attr='private'
        author='Bin Gao'
        date='2014-08-05'>
        Writes the context of overlap operator
        <param name='overlap' direction='in'>
            The context of overlap operator
        </param>
        <param name='fp_overlap' direction='inout'>File pointer</param>
        <return>Error information</return>
    </function> */
    QErrorCode RSPOverlapWrite(const RSPOverlap *overlap, FILE *fp_overlap)
    {
        QInt ilab; /* incremental recorder over perturbation labels */

```

```

fprintf(fp_overlap,
        "RSPOverlapWrite>> number of pert. labels that overlap operator depends on %"QI
        overlap->num_pert_lab);
fprintf(fp_overlap, "RSPOverlapWrite>> label                maximum-order\n");
for (ilab=0; ilab<overlap->num_pert_lab; ilab++) {
    fprintf(fp_overlap,
            "RSPOverlapWrite>>          %"QCPERTINT_FMT"          %"QINT_FMT"\n",
            overlap->pert_labels[ilab],
            overlap->pert_max_orders[ilab]);
}
#ifdef OPENRSP_C_USER_CONTEXT
    if (overlap->user_ctx!=NULL) {
        fprintf(fp_overlap, "RSPOverlapWrite>> user-defined function context given\n");
    }
#endif
    return QSUCCESS;
}

/* <function name='RSPOverlapGetMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates integral matrices of the overlap operator
    <param name='overlap' direction='inout'>
        The context of overlap operator
    </param>
    <param name='bra_len_tuple' direction='in'>
        Length of the perturbation tuple on the bra center
    </param>
    <param name='bra_pert_tuple' direction='in'>
        Perturbation tuple on the bra center
    </param>
    <param name='ket_len_tuple' direction='in'>
        Length of the perturbation tuple on the ket center
    </param>
    <param name='ket_pert_tuple' direction='in'>
        Perturbation tuple on the ket center
    </param>
    <param name='oper_len_tuple' direction='in'>
        Length of the perturbation tuple on the overlap operator
    </param>
    <param name='oper_pert_tuple' direction='in'>
        Perturbation tuple on the overlap operator
    </param>
    <param name='num_int' direction='in'>
        Number of the integral matrices
    </param>
    <param name='val_int' direction='inout'>
        The integral matrices
    </param>
    <return>Error information</return>
</function> */

```



```

        overlap->ket_pert_orders,
        overlap->oper_num_pert,
        overlap->oper_pert_labels,
        overlap->oper_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
        overlap->user_ctx,
#endif

        num_int,
        val_int);

    return QSUCCESS;
}

/* <function name='RSPOverlapGetExp'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates expectation values of the overlap operator
    <param name='overlap' direction='inout'>
        The context of overlap operator
    </param>
    <param name='bra_len_tuple' direction='in'>
        Length of the perturbation tuple on the bra center
    </param>
    <param name='bra_pert_tuple' direction='in'>
        Perturbation tuple on the bra center
    </param>
    <param name='ket_len_tuple' direction='in'>
        Length of the perturbation tuple on the ket center
    </param>
    <param name='ket_pert_tuple' direction='in'>
        Perturbation tuple on the ket center
    </param>
    <param name='oper_len_tuple' direction='in'>
        Length of the perturbation tuple on the overlap operator
    </param>
    <param name='oper_pert_tuple' direction='in'>
        Perturbation tuple on the overlap operator
    </param>
    <param name='num_dmat' direction='in'>
        Number of atomic orbital (AO) based density matrices
    </param>
    <param name='dens_mat' direction='in'>
        The AO based density matrices
    </param>
    <param name='num_exp' direction='in'>
        Number of the expectation values
    </param>
    <param name='val_exp' direction='inout'>
        The expectation values
    </param>
    <return>Error information</return>
</function> */

```



```

        overlap->ket_num_pert,
        overlap->ket_pert_labels,
        overlap->ket_pert_orders,
        overlap->oper_num_pert,
        overlap->oper_pert_labels,
        overlap->oper_pert_orders,
        num_dmat,
        dens_mat,
#ifdef OPENRSP_C_USER_CONTEXT
        overlap->user_ctx,
#endif

        num_exp,
        val_exp);

    return QSUCCESS;
}

/* <function name='RSPOverlapDestroy'
   attr='private'
   author='Bin Gao'
   date='2014-08-05'>
   Destroys the context of overlap operator, should be called at the end
   <param name='overlap' direction='inout'>
       The context of overlap operator
   </param>
   <return>Error information</return>
</function> */
QErrorCode RSPOverlapDestroy(RSPOverlap *overlap)
{
    if (overlap->pert_max_orders!=NULL) {
        free(overlap->pert_max_orders);
        overlap->pert_max_orders = NULL;
    }
    if (overlap->bra_pert_orders!=NULL) {
        free(overlap->bra_pert_orders);
        overlap->bra_pert_orders = NULL;
    }
    if (overlap->ket_pert_orders!=NULL) {
        free(overlap->ket_pert_orders);
        overlap->ket_pert_orders = NULL;
    }
    if (overlap->oper_pert_orders!=NULL) {
        free(overlap->oper_pert_orders);
        overlap->oper_pert_orders = NULL;
    }
    if (overlap->pert_labels!=NULL) {
        free(overlap->pert_labels);
        overlap->pert_labels = NULL;
    }
    if (overlap->bra_pert_labels!=NULL) {
        free(overlap->bra_pert_labels);
        overlap->bra_pert_labels = NULL;
    }
}

```

```
    if (overlap->ket_pert_labels!=NULL) {
        free(overlap->ket_pert_labels);
        overlap->ket_pert_labels = NULL;
    }
    if (overlap->oper_pert_labels!=NULL) {
        free(overlap->oper_pert_labels);
        overlap->oper_pert_labels = NULL;
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        overlap->user_ctx = NULL;
    #endif
    overlap->get_overlap_mat = NULL;
    overlap->get_overlap_exp = NULL;
    return QSUCCESS;
}
```

3.5 One-Electron Operators

Users can use the following API to add different one-electron operators:

```

56  <OpenRSP.c 17a>+≡
    /* <function name='OpenRSPAddOneOper' author='Bin Gao' date='2014-07-30'>
        Add a one-electron operator to the Hamiltonian
        <param name='open_rsp' direction='inout'>
            The context of response theory calculations
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act on the
            one-electron operator
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels involved
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback function context
        </param>
        <param name='get_one_oper_mat' direction='in'>
            User-specified callback function to calculate integral matrices of
            one-electron operator as well as its derivatives with respect to
            different perturbations
        </param>
        <param name='get_one_oper_exp' direction='in'>
            User-specified callback function to calculate expectation values of
            one-electron operator as well as its derivatives with respect to
            different perturbations
        </param>
        <return>Error information</return>
    </function> */
    QErrorCode OpenRSPAddOneOper(OpenRSP *open_rsp,
                                const QInt num_pert_lab,
                                const QcPertInt *pert_labels,
                                const QInt *pert_max_orders,
    #if defined(OPENRSP_C_USER_CONTEXT)
                                void *user_ctx,
    #endif
                                const GetOneOperMat get_one_oper_mat,
                                const GetOneOperExp get_one_oper_exp)
    {
        QErrorCode ierr; /* error information */
        /* creates the linked list of one-electron operators */
        if (open_rsp->one_oper==NULL) {
            ierr = RSPOneOperCreate(&open_rsp->one_oper,
                                    num_pert_lab,
                                    pert_labels,
                                    pert_max_orders,

```



```

    #if defined(OPENRSP_C_USER_CONTEXT)
        user_ctx,
    #endif

    get_one_oper_mat,
    get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperCreate()");
}
/* adds the one-electron operator to the linked list */
else {
    ierr = RSPOneOperAdd(open_rsp->one_oper,
        num_pert_lab,
        pert_labels,
        pert_max_orders,
    #if defined(OPENRSP_C_USER_CONTEXT)
        user_ctx,
    #endif

    get_one_oper_mat,
    get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperAdd()");
}
return QSUCCESS;
}

```

The following header file defines all quantities we need for one-electron operators. Types `GetOneOperMat` and `GetOneOperpExp` define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of a one-electron operator and its derivatives.

```

57 <RSPOneOper.h 57>≡
    /*
        <OpenRSPLicense 14a>

        <header name='RSPOneOper.h' author='Bin Gao' date='2014-07-30'>
            The header file of one-electron operators used inside OpenRSP
        </header>
    */

    #if !defined(RSP_ONEOPER_H)
    #define RSP_ONEOPER_H

    #include "qcmatrix.h"
    #include "RSPPerturbation.h"

    typedef void (*GetOneOperMat)(const QInt,
        const QcPertInt*,
        const QInt*,
    #if defined(OPENRSP_C_USER_CONTEXT)
        void*,
    #endif

        const QInt,
        QcMat*[]);
    typedef void (*GetOneOperExp)(const QInt,
        const QcPertInt*,

```

```

        const QInt*,
        const QInt,
        QcMat*[],
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif

        const QInt,
        QReal*);

```

⟨RSPOneOperStruct 58a⟩

⟨RSPOneOperAPIs 58b⟩

```

#endif

```

Here we use a linked list for the context of one-electron operators:

```

58a  ⟨RSPOneOperStruct 58a⟩≡
    typedef struct RSPOneOper RSPOneOper;
    struct RSPOneOper {
        QInt num_pert_lab;           /* number of different perturbation labels
                                     that can act as perturbations on the
                                     one-electron operator */
        QInt oper_num_pert;         /* number of perturbations on the
                                     one-electron operator, only used for
                                     callback functions */
        QInt *pert_max_orders;      /* allowed maximal order of a perturbation
                                     described by exactly one of these
                                     different labels */
        QInt *oper_pert_orders;     /* orders of perturbations on the
                                     one-electron operator, only used for
                                     callback functions */
        QcPertInt *pert_labels;     /* all the different perturbation labels */
        QcPertInt *oper_pert_labels; /* labels of perturbations on the
                                     one-electron operator, only used for
                                     callback functions */

#ifdef OPENRSP_C_USER_CONTEXT
        void *user_ctx;             /* user-defined callback-function context */
#endif
        GetOneOperMat get_one_oper_mat; /* user-specified function for calculating
                                     integral matrices */
        GetOneOperExp get_one_oper_exp; /* user-specified function for calculating
                                     expectation values */
        RSPOneOper *next_oper;       /* pointer to the next one-electron operator */
    };

```

and the functions related to the one-electron operators:

```

58b  ⟨RSPOneOperAPIs 58b⟩≡
    extern QErrorCode RSPOneOperCreate(RSPOneOper**,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt*,

#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif

    );

```

```

        const GetOneOperMat,
        const GetOneOperExp);
extern QErrorCode RSPOneOperAdd(RSPOneOper*,
        const QInt,
        const QcPertInt*,
        const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
        void*,
#endif
        const GetOneOperMat,
        const GetOneOperExp);
extern QErrorCode RSPOneOperAssemble(RSPOneOper*,const RSPPert*);
extern QErrorCode RSPOneOperWrite(RSPOneOper*,FILE*);
extern QErrorCode RSPOneOperGetMat(RSPOneOper*,
        const QInt,
        const QcPertInt*,
        const QInt,
        QcMat*[]);
extern QErrorCode RSPOneOperGetExp(RSPOneOper*,
        const QInt,
        const QcPertInt*,
        const QInt,
        QcMat*[],
        const QInt,
        QReal*);
extern QErrorCode RSPOneOperDestroy(RSPOneOper**);

```

The functions are implemented as follows:

```

59  <RSPOneOper.c 59>≡
    /*
    <OpenRSPLicense 14a>
    */

#include "RSPOneOper.h"

/* <function name='RSPOneOperCreate'
    attr='private'
    author='Bin Gao'
    date='2014-07-30'>
    Create a node of a linked list for a given one-electron operator, should
    be called at first
    <param name='one_oper' direction='inout'>
        The linked list of one-electron operators
    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the one-electron operator
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of

```

```

    the above different labels
</param>
<param name='user_ctx' direction='in'>
    User-defined callback-function context
</param>
<param name='get_one_oper_mat' direction='in'>
    User-specified function for calculating integral matrices of the
    one-electron operator and its derivatives
</param>
<param name='get_one_oper_exp' direction='in'>
    User-specified function for calculating expectation values of the
    one-electron operator and its derivatives
</param>
<return>Error information</return>
</function> */
QErrorCode RSPOneOperCreate(RSPOneOper **one_oper,
                           const QInt num_pert_lab,
                           const QcPertInt *pert_labels,
                           const QInt *pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                           void *user_ctx,
#endif
                           const GetOneOperMat get_one_oper_mat,
                           const GetOneOperExp get_one_oper_exp)
{
    RSPOneOper *new_oper; /* new operator */
    QInt ilab;             /* incremental recorders over perturbation labels */
    QInt jlab;
    new_oper = (RSPOneOper *)malloc(sizeof(RSPOneOper));
    if (new_oper==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for one-electron operator");
    }
    if (num_pert_lab<0) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPOneOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
    }
    new_oper->num_pert_lab = num_pert_lab;
    if (new_oper->num_pert_lab>0) {
        new_oper->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
        if (new_oper->pert_max_orders==NULL) {
            printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
                   num_pert_lab);
            QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
        }
    }
}

```

```

new_oper->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
if (new_oper->oper_pert_orders==NULL) {
    printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on 1el operator");
}
new_oper->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
if (new_oper->pert_labels==NULL) {
    printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
}
new_oper->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
if (new_oper->oper_pert_labels==NULL) {
    printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on 1el operator");
}
for (ilab=0; ilab<num_pert_lab; ilab++) {
    if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPOneOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "invalid perturbation label");
    }
    /* each element of <pert_labels> should be unique */
    for (jlab=0; jlab<ilab; jlab++) {
        if (pert_labels[jlab]==pert_labels[ilab]) {
            printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   jlab,
                   pert_labels[jlab]);
            printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
        }
    }
    new_oper->pert_labels[ilab] = pert_labels[ilab];
    if (pert_max_orders[ilab]<1) {
        printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPOneOperCreate>> allowed maximal order is %"QINT_FMT"\n",
               pert_max_orders[ilab]);
        QErrorExit(FILE_AND_LINE, "only positive order allowed");
    }
    new_oper->pert_max_orders[ilab] = pert_max_orders[ilab];
}
}
else {

```

```

        new_oper->pert_max_orders = NULL;
        new_oper->oper_pert_orders = NULL;
        new_oper->pert_labels = NULL;
        new_oper->oper_pert_labels = NULL;
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        new_oper->user_ctx = user_ctx;
    #endif
    new_oper->get_one_oper_mat = get_one_oper_mat;
    new_oper->get_one_oper_exp = get_one_oper_exp;
    new_oper->next_oper = NULL;
    *one_oper = new_oper;
    return QSUCCESS;
}

```

As shown here, we allow for a one-electron operator that does not depend on any perturbation—`num_pert_lab==0`, i.e. any perturbed integral matrix and expectation value of this one-electron operator is zero.

```

62  <RSPOneOper.c 59>+≡
    /* <function name='RSPOneOperAdd'
        attr='private'
        author='Bin Gao'
        date='2014-07-30'>

        Add a given one-electron operator to the linked list
        <param name='one_oper' direction='inout'>
            The linked list of one-electron operators
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act as
            perturbations on the one-electron operator
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback-function context
        </param>
        <param name='get_one_oper_mat' direction='in'>
            User-specified function for calculating integral matrices of the
            one-electron operator and its derivatives
        </param>
        <param name='get_one_oper_exp' direction='in'>
            User-specified function for calculating expectation values of the
            one-electron operator and its derivatives
        </param>
        <return>Error information</return>
    </function> */
    QErrorCode RSPOneOperAdd(RSPOneOper *one_oper,

```

```

        const QInt num_pert_lab,
        const QcPertInt *pert_labels,
        const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
        void *user_ctx,
#endif

        const GetOneOperMat get_one_oper_mat,
        const GetOneOperExp get_one_oper_exp)
{
    RSPOneOper *new_oper; /* new operator */
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    /* creates the new operator */
    ierr = RSPOneOperCreate(&new_oper,
                           num_pert_lab,
                           pert_labels,
                           pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                           user_ctx,
#endif

                           get_one_oper_mat,
                           get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperCreate()");
    /* walks to the last operator */
    cur_oper = one_oper;
    while (cur_oper->next_oper!=NULL) {
        cur_oper = cur_oper->next_oper;
    }
    /* inserts the new operator to the tail of the linked list */
    cur_oper->next_oper = new_oper;
    return QSUCCESS;
}

/* <function name='RSPOneOperAssemble'
    attr='private'
    author='Bin Gao'
    date='2014-07-30'>
    Assembles the linked list of one-electron operators
    <param name='one_oper' direction='inout'>
        The linked list of one-electron operators
    </param>
    <param name='rsp_pert' direction='in'>
        The context of perturbations
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPOneOperAssemble(RSPOneOper *one_oper, const RSPPert *rsp_pert)
{
    QInt ioper;          /* incremental recorder over operators */
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    ioper = 0;

```

```

cur_oper = one_oper;
do {
    if (cur_oper->num_pert_lab>0 &&
        (cur_oper->pert_labels==NULL || cur_oper->pert_max_orders==NULL)) {
        printf("RSPOneOperAssemble>> %"QINT_FMT"-th one-electron operator\n",
            ioper);
        QErrorExit(FILE_AND_LINE, "perturbations of one-electron operator not set");
    }
    if (cur_oper->get_one_oper_mat==NULL || cur_oper->get_one_oper_exp==NULL) {
        printf("RSPOneOperAssemble>> %"QINT_FMT"-th one-electron operator\n",
            ioper);
        QErrorExit(FILE_AND_LINE, "callback functions of one-electron operator not set");
    }
    /* checks perturbation labels and allowed maximal orders against
       all known perturbations */
    ierr = RSPPertValidateLabelOrder(rsp_pert,
                                    cur_oper->num_pert_lab,
                                    cur_oper->pert_labels,
                                    cur_oper->pert_max_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
    /* moves to the next operator */
    ioper++;
    cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPOneOperWrite'
   attr='private'
   author='Bin Gao'
   date='2014-07-30'>
Writes the linked list of one-electron operators
<param name='one_oper' direction='in'>
    The linked list of one-electron operators
</param>
<param name='fp_oper' direction='inout'>File pointer</param>
<return>Error information</return>
</function> */
QErrorCode RSPOneOperWrite(RSPOneOper *one_oper, FILE *fp_oper)
{
    QInt ioper;          /* incremental recorder over operators */
    RSPOneOper *cur_oper; /* current operator */
    QInt ilab;           /* incremental recorder over perturbation labels */
    ioper = 0;
    cur_oper = one_oper;
    do {
        fprintf(fp_oper, "RSPOneOperWrite>> operator %"QINT_FMT"\n", ioper);
        fprintf(fp_oper,
            "RSPOneOperWrite>> number of pert. labels that one-electron operator depend
            cur_oper->num_pert_lab);
        fprintf(fp_oper, "RSPOneOperWrite>> label          maximum-order\n");
        for (ilab=0; ilab<cur_oper->num_pert_lab; ilab++) {

```



```

        fprintf(fp_oper,
                "RSPOneOperWrite>>          %"QCPERTINT_FMT"          %"QINT_FMT"\n",
                cur_oper->pert_labels[ilab],
                cur_oper->pert_max_orders[ilab]);
    }
#ifdef OPENRSP_C_USER_CONTEXT
    if (cur_oper->user_ctx!=NULL) {
        fprintf(fp_oper, "RSPOneOperWrite>> user-defined function context given\n");
    }
#endif
    /* moves to the next operator */
    ioper++;
    cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPOneOperGetMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates integral matrices of the linked list of one-electron operators
    <param name='one_oper' direction='inout'>
        The linked list of one-electron operators
    </param>
    <param name='oper_len_tuple' direction='in'>
        Length of the perturbation tuple on the linked list of one-electron
        operators
    </param>
    <param name='oper_pert_tuple' direction='in'>
        Perturbation tuple on the linked list of one-electron operators
    </param>
    <param name='num_int' direction='in'>
        Number of the integral matrices
    </param>
    <param name='val_int' direction='inout'>
        The integral matrices
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPOneOperGetMat(RSPOneOper *one_oper,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt num_int,
                            QcMat *val_int[])
{
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;       /* error information */
    cur_oper = one_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the one-electron operator */

```

```

ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                           oper_pert_tuple,
                                           cur_oper->num_pert_lab,
                                           cur_oper->pert_labels,
                                           cur_oper->pert_max_orders,
                                           &cur_oper->oper_num_pert,
                                           cur_oper->oper_pert_labels,
                                           cur_oper->oper_pert_orders);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()")
/* checks if the perturbations on the one-electron operator
   result in zero values */
if (cur_oper->oper_num_pert>=0) {
    /* calculates integral matrices using the callback function */
    cur_oper->get_one_oper_mat(cur_oper->oper_num_pert,
                              cur_oper->oper_pert_labels,
                              cur_oper->oper_pert_orders,
                              cur_oper->user_ctx,
                              num_int,
                              val_int);
}
/* moves to the next operator */
cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPOneOperGetExp'
   attr='private'
   author='Bin Gao'
   date='2015-10-15'>
Calculates expectation values of the linked list of one-electron operators
<param name='one_oper' direction='inout'>
    The linked list of one-electron operators
</param>
<param name='oper_len_tuple' direction='in'>
    Length of the perturbation tuple on the linked list of one-electron
    operators
</param>
<param name='oper_pert_tuple' direction='in'>
    Perturbation tuple on the linked list of one-electron operators
</param>
<param name='num_dmat' direction='in'>
    Number of atomic orbital (AO) based density matrices
</param>
<param name='dens_mat' direction='in'>
    The AO based density matrices
</param>
<param name='num_exp' direction='in'>
    Number of the expectation values
</param>

```

```

    <param name='val_exp' direction='inout'>
        The expectation values
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPOneOperGetExp(RSPOneOper *one_oper,
                           const QInt oper_len_tuple,
                           const QcPertInt *oper_pert_tuple,
                           const QInt num_dmat,
                           QcMat *dens_mat[],
                           const QInt num_exp,
                           QReal *val_exp)
{
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    cur_oper = one_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the one-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                    oper_pert_tuple,
                                                    cur_oper->num_pert_lab,
                                                    cur_oper->pert_labels,
                                                    cur_oper->pert_max_orders,
                                                    &cur_oper->oper_num_pert,
                                                    cur_oper->oper_pert_labels,
                                                    cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()")
        /* checks if the perturbations on the one-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert>=0) {
            /* calculates expectation values using the callback function */
            cur_oper->get_one_oper_exp(cur_oper->oper_num_pert,
                                       cur_oper->oper_pert_labels,
                                       cur_oper->oper_pert_orders,
                                       num_dmat,
                                       dens_mat,
                                       cur_oper->user_ctx,
                                       num_exp,
                                       val_exp);
        }
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}

/* <function name='RSPOneOperDestroy'
   attr='private'
   author='Bin Gao'

```

```

        date='2014-07-30'>
Destroys the linked list of one-electron operators, should be called
at the end
<param name='one_oper' direction='inout'>
    The linked list of one-electron operators
</param>
<return>Error information</return>
</function> */
QErrorCode RSPOneOperDestroy(RSPOneOper **one_oper)
{
    RSPOneOper *cur_oper; /* current operator */
    RSPOneOper *next_oper; /* next operator */
    /* walks to the last operator */
    cur_oper = *one_oper;
    while (cur_oper!=NULL) {
        if (cur_oper->pert_max_orders!=NULL) {
            free(cur_oper->pert_max_orders);
            cur_oper->pert_max_orders = NULL;
        }
        if (cur_oper->oper_pert_orders!=NULL) {
            free(cur_oper->oper_pert_orders);
            cur_oper->oper_pert_orders = NULL;
        }
        if (cur_oper->pert_labels!=NULL) {
            free(cur_oper->pert_labels);
            cur_oper->pert_labels = NULL;
        }
        if (cur_oper->oper_pert_labels!=NULL) {
            free(cur_oper->oper_pert_labels);
            cur_oper->oper_pert_labels = NULL;
        }
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        cur_oper->user_ctx = NULL;
    #endif
    cur_oper->get_one_oper_mat = NULL;
    cur_oper->get_one_oper_exp = NULL;
    next_oper = cur_oper->next_oper;
    free(cur_oper);
    cur_oper = NULL;
    cur_oper = next_oper;
}
return QSUCCESS;
}

```

3.6 Two-Electron Operators

Users can use the following API to add different two-electron operators:

```
69  <OpenRSP.c 17a>+≡
    /* <function name='OpenRSPAddTwoOper' author='Bin Gao' date='2014-08-05'>
        Add a two-electron operator to the Hamiltonian
        <param name='open_rsp' direction='inout'>
            The context of response theory calculations
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act on the
            two-electron operator
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels involved
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback function context
        </param>
        <param name='get_two_oper_mat' direction='in'>
            User-specified callback function to calculate integral matrices of
            two-electron operator as well as its derivatives with respect to
            different perturbations
        </param>
        <param name='get_two_oper_exp' direction='in'>
            User-specified callback function to calculate expectation values of
            two-electron operator as well as its derivatives with respect to
            different perturbations
        </param>
        <return>Error information</return>
    </function> */
    QErrorCode OpenRSPAddTwoOper(OpenRSP *open_rsp,
                                const QInt num_pert_lab,
                                const QcPertInt *pert_labels,
                                const QInt *pert_max_orders,
    #if defined(OPENRSP_C_USER_CONTEXT)
                                void *user_ctx,
    #endif
                                const GetTwoOperMat get_two_oper_mat,
                                const GetTwoOperExp get_two_oper_exp)
    {
        QErrorCode ierr; /* error information */
        /* creates the linked list of two-electron operators */
        if (open_rsp->two_oper==NULL) {
            ierr = RSPTwoOperCreate(&open_rsp->two_oper,
                                    num_pert_lab,
                                    pert_labels,
                                    pert_max_orders,
```

```

    #if defined(OPENRSP_C_USER_CONTEXT)
        user_ctx,
    #endif

    get_two_oper_mat,
    get_two_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperCreate()");
}
/* adds the two-electron operator to the linked list */
else {
    ierr = RSPTwoOperAdd(open_rsp->two_oper,
        num_pert_lab,
        pert_labels,
        pert_max_orders,
    #if defined(OPENRSP_C_USER_CONTEXT)
        user_ctx,
    #endif

    get_two_oper_mat,
    get_two_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperAdd()");
}
return QSUCCESS;
}

```

The following header file defines all quantities we need for two-electron operators. Types `GetTwoOperMat` and `GetTwoOperpExp` define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of a two-electron operator and its derivatives.

```

70 <RSPTwoOper.h 70>≡
    /*
        <OpenRSPLicense 14a>

        <header name='RSPTwoOper.h' author='Bin Gao' date='2014-08-05'>
            The header file of two-electron operators used inside OpenRSP
        </header>
    */

    #if !defined(RSP_TWOOOPER_H)
    #define RSP_TWOOOPER_H

    #include "qcmatrix.h"
    #include "RSPPerturbation.h"

    typedef void (*GetTwoOperMat)(const QInt,
        const QcPertInt*,
        const QInt*,
        const QInt,
        QcMat*[],
    #if defined(OPENRSP_C_USER_CONTEXT)
        void*,
    #endif

        const QInt,
        QcMat*[]);

```

```

typedef void (*GetTwoOperExp)(const QInt,
                               const QcPertInt*,
                               const QInt*,
                               const QInt,
                               const QInt*,
                               QcMat*[],
                               const QInt*,
                               QcMat*[],
                               void*,
                               const QInt,
                               QReal*);

```

⟨*RSPTwoOperStruct* 71a⟩

⟨*RSPTwoOperAPIs* 71b⟩

```
#endif
```

Here we use a linked list for the context of two-electron operators:

```

71a  ⟨RSPTwoOperStruct 71a⟩≡
    typedef struct RSPTwoOper RSPTwoOper;
    struct RSPTwoOper {
        QInt num_pert_lab;           /* number of different perturbation labels
                                     that can act as perturbations on the
                                     two-electron operator */
        QInt oper_num_pert;         /* number of perturbations on the
                                     two-electron operator, only used for
                                     callback functions */
        QInt *pert_max_orders;      /* allowed maximal order of a perturbation
                                     described by exactly one of these
                                     different labels */
        QInt *oper_pert_orders;     /* orders of perturbations on the
                                     two-electron operator, only used for
                                     callback functions */
        QcPertInt *pert_labels;     /* all the different perturbation labels */
        QcPertInt *oper_pert_labels; /* labels of perturbations on the
                                     two-electron operator, only used for
                                     callback functions */
        #if defined(OPENRSP_C_USER_CONTEXT)
            void *user_ctx;          /* user-defined callback-function context */
        #endif
        GetTwoOperMat get_two_oper_mat; /* user-specified function for calculating
                                     integral matrices */
        GetTwoOperExp get_two_oper_exp; /* user-specified function for calculating
                                     expectation values */
        RSPTwoOper *next_oper;       /* pointer to the next two-electron operator */
    };

```

and the functions related to the two-electron operators:

```

71b  ⟨RSPTwoOperAPIs 71b⟩≡
    extern QErrorCode RSPTwoOperCreate(RSPTwoOper**,
                                       const QInt,

```

```

        const QcPertInt*,
        const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif
        const GetTwoOperMat,
        const GetTwoOperExp);
extern QErrorCode RSPTwoOperAdd(RSPTwoOper*,
        const QInt,
        const QcPertInt*,
        const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif
        const GetTwoOperMat,
        const GetTwoOperExp);
extern QErrorCode RSPTwoOperAssemble(RSPTwoOper*, const RSPPert*);
extern QErrorCode RSPTwoOperWrite(RSPTwoOper*, FILE*);
extern QErrorCode RSPTwoOperGetMat(RSPTwoOper*,
        const QInt,
        const QcPertInt*,
        const QInt,
        QcMat*[],
        const QInt,
        QcMat*[]);
extern QErrorCode RSPTwoOperGetExp(RSPTwoOper*,
        const QInt,
        const QcPertInt*,
        const QInt,
        const QInt*,
        QcMat*[],
        const QInt*,
        QcMat*[],
        const QInt,
        QReal*);
extern QErrorCode RSPTwoOperDestroy(RSPTwoOper**);

```

The functions are implemented as follows:

```

72  <RSPTwoOper.c 72>≡
    /*
    <OpenRSPLicense 14a>
    */

#include "RSPTwoOper.h"

/* <function name='RSPTwoOperCreate'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Create a node of a linked list for a given two-electron operator, should
    be called at first
    <param name='two_oper' direction='inout'>
    The linked list of two-electron operators

```



```

    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the two-electron operator
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback-function context
    </param>
    <param name='get_two_oper_mat' direction='in'>
        User-specified function for calculating integral matrices of the
        two-electron operator and its derivatives
    </param>
    <param name='get_two_oper_exp' direction='in'>
        User-specified function for calculating expectation values of the
        two-electron operator and its derivatives
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPTwoOperCreate(RSPTwoOper **two_oper,
                           const QInt num_pert_lab,
                           const QcPertInt *pert_labels,
                           const QInt *pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                           void *user_ctx,
#endif
                           const GetTwoOperMat get_two_oper_mat,
                           const GetTwoOperExp get_two_oper_exp)
{
    RSPTwoOper *new_oper; /* new operator */
    QInt ilab;             /* incremental recorders over perturbation labels */
    QInt jlab;
    new_oper = (RSPTwoOper *)malloc(sizeof(RSPTwoOper));
    if (new_oper==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for two-electron operator");
    }
    if (num_pert_lab<0) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPTwoOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
    }
}

```

```

    QErrorExit(FILE_AND_LINE, "too many perturbation labels");
}
new_oper->num_pert_lab = num_pert_lab;
if (new_oper->num_pert_lab>0) {
    new_oper->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->pert_max_orders==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
            num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    new_oper->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->oper_pert_orders==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
            num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on 2el operator");
    }
    new_oper->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->pert_labels==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
            num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    new_oper->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->oper_pert_labels==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
            num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on 2el operator");
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                ilab,
                pert_labels[ilab]);
            printf("RSPTwoOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
                OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {
            if (pert_labels[jlab]==pert_labels[ilab]) {
                printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                    jlab,
                    pert_labels[jlab]);
                printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                    ilab,
                    pert_labels[ilab]);
                QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
            }
        }
        new_oper->pert_labels[ilab] = pert_labels[ilab];
        if (pert_max_orders[ilab]<1) {
            printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",

```

```

        ilab,
        pert_labels[ilab]);
    printf("RSPTwoOperCreate>> allowed maximal order is %"QINT_FMT"\n",
        pert_max_orders[ilab]);
    QErrorExit(FILE_AND_LINE, "only positive order allowed");
}
new_oper->pert_max_orders[ilab] = pert_max_orders[ilab];
}
}
else {
    new_oper->pert_max_orders = NULL;
    new_oper->oper_pert_orders = NULL;
    new_oper->pert_labels = NULL;
    new_oper->oper_pert_labels = NULL;
}
#if defined(OPENRSP_C_USER_CONTEXT)
    new_oper->user_ctx = user_ctx;
#endif
    new_oper->get_two_oper_mat = get_two_oper_mat;
    new_oper->get_two_oper_exp = get_two_oper_exp;
    new_oper->next_oper = NULL;
    *two_oper = new_oper;
    return QSUCCESS;
}

```

As shown here, we allow for a two-electron operator that does not depend on any perturbation—`num_pert_lab==0`, i.e. any perturbed integral matrix and expectation value of this two-electron operator is zero.

75 $\langle RSPTwoOper.c \ 72 \rangle + \equiv$

```

/* <function name='RSPTwoOperAdd'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>

Add a given two-electron operator to the linked list
<param name='two_oper' direction='inout'>
    The linked list of two-electron operators
</param>
<param name='num_pert_lab' direction='in'>
    Number of all different perturbation labels that can act as
    perturbations on the two-electron operator
</param>
<param name='pert_labels' direction='in'>
    All the different perturbation labels
</param>
<param name='pert_max_orders' direction='in'>
    Allowed maximal order of a perturbation described by exactly one of
    the above different labels
</param>
<param name='user_ctx' direction='in'>
    User-defined callback-function context
</param>
<param name='get_two_oper_mat' direction='in'>

```

```

    User-specified function for calculating integral matrices of the
    two-electron operator and its derivatives
</param>
<param name='get_two_oper_exp' direction='in'>
    User-specified function for calculating expectation values of the
    two-electron operator and its derivatives
</param>
<return>Error information</return>
</function> */
QErrorCode RSPTwoOperAdd(RSPTwoOper *two_oper,
                        const QInt num_pert_lab,
                        const QcPertInt *pert_labels,
                        const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                        void *user_ctx,
#endif
                        const GetTwoOperMat get_two_oper_mat,
                        const GetTwoOperExp get_two_oper_exp)
{
    RSPTwoOper *new_oper; /* new operator */
    RSPTwoOper *cur_oper; /* current operator */
    QErrorCode ierr;       /* error information */
    /* creates the new operator */
    ierr = RSPTwoOperCreate(&new_oper,
                           num_pert_lab,
                           pert_labels,
                           pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                           user_ctx,
#endif
                           get_two_oper_mat,
                           get_two_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperCreate()");
    /* walks to the last operator */
    cur_oper = two_oper;
    while (cur_oper->next_oper!=NULL) {
        cur_oper = cur_oper->next_oper;
    }
    /* inserts the new operator to the tail of the linked list */
    cur_oper->next_oper = new_oper;
    return QSUCCESS;
}

/* <function name='RSPTwoOperAssemble'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Assembles the linked list of two-electron operators
    <param name='two_oper' direction='inout'>
        The linked list of two-electron operators
    </param>
    <param name='rsp_pert' direction='in'>

```

```

    The context of perturbations
</param>
<return>Error information</return>
</function> */
QErrorCode RSPTwoOperAssemble(RSPTwoOper *two_oper, const RSPPert *rsp_pert)
{
    QInt ioper;          /* incremental recorder over operators */
    RSPTwoOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    ioper = 0;
    cur_oper = two_oper;
    do {
        if (cur_oper->num_pert_lab>0 &&
            (cur_oper->pert_labels==NULL || cur_oper->pert_max_orders==NULL)) {
            printf("RSPTwoOperAssemble>> %"QINT_FMT"-th two-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "perturbations of two-electron operator not set");
        }
        if (cur_oper->get_two_oper_mat==NULL || cur_oper->get_two_oper_exp==NULL) {
            printf("RSPTwoOperAssemble>> %"QINT_FMT"-th two-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "callback functions of two-electron operator not set");
        }
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                         cur_oper->num_pert_lab,
                                         cur_oper->pert_labels,
                                         cur_oper->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}

/* <function name='RSPTwoOperWrite'
   attr='private'
   author='Bin Gao'
   date='2014-08-06'>
   Writes the linked list of two-electron operators
   <param name='two_oper' direction='in'>
       The linked list of two-electron operators
   </param>
   <param name='fp_oper' direction='inout'>File pointer</param>
   <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperWrite(RSPTwoOper *two_oper, FILE *fp_oper)
{
    QInt ioper;          /* incremental recorder over operators */
    RSPTwoOper *cur_oper; /* current operator */

```

```

QInt ilab;          /* incremental recorder over perturbation labels */
ioper = 0;
cur_oper = two_oper;
do {
    fprintf(fp_oper, "RSPTwoOperWrite>> operator %"QINT_FMT"\n", ioper);
    fprintf(fp_oper,
        "RSPTwoOperWrite>> number of pert. labels that two-electron operator depend
        cur_oper->num_pert_lab);
    fprintf(fp_oper, "RSPTwoOperWrite>> label          maximum-order\n");
    for (ilab=0; ilab<cur_oper->num_pert_lab; ilab++) {
        fprintf(fp_oper,
            "RSPTwoOperWrite>>          %"QCPERTINT_FMT"          %"QINT_FMT"\n",
            cur_oper->pert_labels[ilab],
            cur_oper->pert_max_orders[ilab]);
    }
}
#ifdef OPENRSP_C_USER_CONTEXT
    if (cur_oper->user_ctx!=NULL) {
        fprintf(fp_oper, "RSPTwoOperWrite>> user-defined function context given\n");
    }
#endif
    /* moves to the next operator */
    ioper++;
    cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPTwoOperGetMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates integral matrices of the linked list of two-electron operators
    <param name='two_oper' direction='inout'>
        The linked list of two-electron operators
    </param>
    <param name='oper_len_tuple' direction='in'>
        Length of the perturbation tuple on the linked list of two-electron
        operators
    </param>
    <param name='oper_pert_tuple' direction='in'>
        Perturbation tuple on the linked list of two-electron operators
    </param>
    <param name='num_int' direction='in'>
        Number of the integral matrices
    </param>
    <param name='val_int' direction='inout'>
        The integral matrices
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPTwoOperGetMat(RSPTwoOper *two_oper,
    const QInt oper_len_tuple,

```

```

        const QcPertInt *oper_pert_tuple,
        const QInt num_dmat,
        QcMat *dens_mat[],
        const QInt num_int,
        QcMat *val_int[])
{
    RSPTwoOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    cur_oper = two_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the two-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                    oper_pert_tuple,
                                                    cur_oper->num_pert_lab,
                                                    cur_oper->pert_labels,
                                                    cur_oper->pert_max_orders,
                                                    &cur_oper->oper_num_pert,
                                                    cur_oper->oper_pert_labels,
                                                    cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()")
        /* checks if the perturbations on the two-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert>=0) {
            /* calculates integral matrices using the callback function */
            cur_oper->get_two_oper_mat(cur_oper->oper_num_pert,
                                       cur_oper->oper_pert_labels,
                                       cur_oper->oper_pert_orders,
                                       num_dmat,
                                       dens_mat,
                                       cur_oper->user_ctx,
                                       num_int,
                                       val_int);
        }
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}

/* <function name='RSPTwoOperGetExp'
   attr='private'
   author='Bin Gao'
   date='2015-10-15'>
Calculates expectation values of the linked list of two-electron operators
<param name='two_oper' direction='inout'>
    The linked list of two-electron operators
</param>
<param name='oper_len_tuple' direction='in'>
    Length of the perturbation tuple on the linked list of two-electron

```



```

        cur_oper->pert_max_orders,
        &cur_oper->oper_num_pert,
        cur_oper->oper_pert_labels,
        cur_oper->oper_pert_orders);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()")
/* checks if the perturbations on the two-electron operator
   result in zero values */
if (cur_oper->oper_num_pert>=0) {
    /* calculates expectation values using the callback function */
    cur_oper->get_two_oper_exp(cur_oper->oper_num_pert,
                              cur_oper->oper_pert_labels,
                              cur_oper->oper_pert_orders,
                              dmat_len_tuple,
                              num_LHS_dmat,
                              LHS_dens_mat,
                              num_RHS_dmat,
                              RHS_dens_mat,

#ifdef OPENRSP_C_USER_CONTEXT
                              cur_oper->user_ctx,

                              num_exp,
                              val_exp);
}
/* moves to the next operator */
cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPTwoOperDestroy'
   attr='private'
   author='Bin Gao'
   date='2014-08-06'>
Destroys the linked list of two-electron operators, should be called
at the end
<param name='two_oper' direction='inout'>
    The linked list of two-electron operators
</param>
<return>Error information</return>
</function> */
QErrorCode RSPTwoOperDestroy(RSPTwoOper **two_oper)
{
    RSPTwoOper *cur_oper; /* current operator */
    RSPTwoOper *next_oper; /* next operator */
    /* walks to the last operator */
    cur_oper = *two_oper;
    while (cur_oper!=NULL) {
        if (cur_oper->pert_max_orders!=NULL) {
            free(cur_oper->pert_max_orders);
            cur_oper->pert_max_orders = NULL;
        }
        if (cur_oper->oper_pert_orders!=NULL) {

```

```
        free(cur_oper->oper_pert_orders);
        cur_oper->oper_pert_orders = NULL;
    }
    if (cur_oper->pert_labels!=NULL) {
        free(cur_oper->pert_labels);
        cur_oper->pert_labels = NULL;
    }
    if (cur_oper->oper_pert_labels!=NULL) {
        free(cur_oper->oper_pert_labels);
        cur_oper->oper_pert_labels = NULL;
    }
#ifdef OPENRSP_C_USER_CONTEXT
    cur_oper->user_ctx = NULL;
#endif
    cur_oper->get_two_oper_mat = NULL;
    cur_oper->get_two_oper_exp = NULL;
    next_oper = cur_oper->next_oper;
    free(cur_oper);
    cur_oper = NULL;
    cur_oper = next_oper;
}
return QSUCCESS;
}
```

3.7 XC Functionals

Users can use the following API to add different XC functionals:

```

83  <OpenRSP.c 17a>+≡
    /* <function name='OpenRSPAddXCFun' author='Bin Gao' date='2015-06-23'>
        Add an XC functional to the Hamiltonian
        <param name='open_rsp' direction='inout'>
            The context of response theory calculations
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act on the
            XC functional
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels involved
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback function context
        </param>
        <param name='get_xc_fun_mat' direction='in'>
            User-specified callback function to calculate integral matrices of
            XC functional as well as its derivatives with respect to
            different perturbations
        </param>
        <param name='get_xc_fun_exp' direction='in'>
            User-specified callback function to calculate expectation values of
            XC functional as well as its derivatives with respect to
            different perturbations
        </param>
        <return>Error information</return>
    </function> */
    QErrorCode OpenRSPAddXCFun(OpenRSP *open_rsp,
                               const QInt num_pert_lab,
                               const QcPertInt *pert_labels,
                               const QInt *pert_max_orders,
    #if defined(OPENRSP_C_USER_CONTEXT)
                               void *user_ctx,
    #endif
                               const GetXCFunMat get_xc_fun_mat,
                               const GetXCFunExp get_xc_fun_exp)
    {
        QErrorCode ierr; /* error information */
        /* creates the linked list of XC functionals */
        if (open_rsp->xc_fun==NULL) {
            ierr = RSPXCFunCreate(&open_rsp->xc_fun,
                                   num_pert_lab,
                                   pert_labels,
                                   pert_max_orders,

```

```

#if defined(OPENRSP_C_USER_CONTEXT)
    user_ctx,
#endif

    get_xc_fun_mat,
    get_xc_fun_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunCreate()");
}
/* adds the XC functional to the linked list */
else {
    ierr = RSPXCFunAdd(open_rsp->xc_fun,
        num_pert_lab,
        pert_labels,
        pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
        user_ctx,
#endif
        get_xc_fun_mat,
        get_xc_fun_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunAdd()");
}
return QSUCCESS;
}

```

The following header file defines all quantities we need for XC functionals. Types `GetXCFunMat` and `GetXCFunExp` define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of an XC functional and its derivatives.

```

84 <RSPXCFun.h 84>≡
    /*
        <OpenRSPLicense 14a>

        <header name='RSPXCFun.h' author='Bin Gao' date='2014-08-06'>
            The header file of XC functionals used inside OpenRSP
        </header>
    */

    #if !defined(RSP_XCFUN_H)
    #define RSP_XCFUN_H

    #include "qcmatrix.h"
    #include "RSPPerturbation.h"

    typedef void (*GetXCFunMat)(const QInt,
        const QcPertInt*,
        const QInt,
        const QInt*,
        const QInt,
        const QInt*,
        const QInt,
        QcMat* [],
    #if defined(OPENRSP_C_USER_CONTEXT)
        void*,
    #endif

```

```

        const QInt,
        QcMat*[]);
typedef void (*GetXCFunExp)(const QInt,
        const QcPertInt*,
        const QInt,
        const QInt*,
        const QInt,
        const QInt*,
        const QInt,
        QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
        void*,
#endif
        const QInt,
        QReal*);

<RSPXCFunStruct 86a>

<RSPXCFunAPIs 86b>

#endif

```

The complete density matrix perturbation tuples (canonically ordered) for a property \mathcal{E}^{abc} (i.e. the perturbation tuple `xc_pert_tuple` is `abc`) are

$$(D, D^a, D^b, D^{ab}, D^c, D^{ac}, D^{bc}), \quad (3.1)$$

and with the (0,2) rule, the relevant density matrix perturbation tuples become

$$(D, D^b, D^c, D^{bc}), \quad (3.2)$$

which gives the `dmatrix_num_tuple` as 4.

How about identical abc?

We then need to give the indices of the density matrix perturbation tuples passed (canonically ordered), whose size is `dmatrix_num_tuple`. Sticking with the above example, the density matrix perturbation tuples passed as Eq. (3.2) have their associated indices `dmatrix_idx_tuple` as {1,3,5,7}, because these numbers correspond to the positions of the “(k,n)-surviving” perturbation tuples in the canonically ordered complete density matrix perturbation tuples (3.1).

The number of collected AO based density matrices for the passed density matrix perturbation tuples (specified by `dmatrix_idx_tuple`) and all frequency configurations, that is

$$\text{num_freq_configs} \times \sum_{i=0}^{\text{dmatrix_idx_tuple}-1} N_i, \quad (3.3)$$

where N_i is the number of density matrices for the density matrix perturbation tuple `dmatrix_idx_tuple[i]` for a frequency configuration.

The collected AO based density matrices are in `dens_mat`, and size is `num_dmat`, and arranged as `[num_freq_configs][dmatrix_idx_tuple]`.

The number of output integral matrices and expectation values equals to the product of the size of perturbations on the XC functional (specified by the perturbation tuple `xc_pert_tuple`) and the number of different frequency configurations `num_freq_configs`, and arranged as `[num_freq_configs][xc_pert_tuple]` and `[num_freq_configs][xc_pert_tuple][2]`.

We agree to add an extra argument—integer—to tell which kind of differentiation will be performed: (1) on AO density matrices only, (2) on XC functional only, and (3) on both.

A linked list is also used for the context of XC functionals:

```
86a <RSPXCFunStruct 86a>≡
typedef struct RSPXCFun RSPXCFun;
struct RSPXCFun {
    QInt num_pert_lab;          /* number of different perturbation labels
                                that can act as perturbations on the
                                XC functional */
    QInt xc_len_tuple;          /* length of perturbation tuple on the
                                XC functional, only used for
                                callback functions */
    QInt *pert_max_orders;      /* allowed maximal order of a perturbation
                                described by exactly one of these
                                different labels */
    QcPertInt *pert_labels;     /* all the different perturbation labels */
    QcPertInt *xc_pert_tuple;   /* perturbation tuple on the XC functional,
                                only used for callback functions */
#ifdef OPENRSP_C_USER_CONTEXT
    void *user_ctx;             /* user-defined callbac-kfunction context */
#endif
    GetXCFunMat get_xc_fun_mat; /* user-specified function for calculating
                                integral matrices */
    GetXCFunExp get_xc_fun_exp; /* user-specified function for calculating
                                expectation values */
    RSPXCFun *next_xc;          /* pointer to the next XC functional */
};
```

and the functions related to the XC functionals:

```
86b <RSPXCFunAPIs 86b>≡
extern QErrorCode RSPXCFunCreate(RSPXCFun**,
                                const QInt,
                                const QcPertInt*,
                                const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
                                void*,
#endif
                                const GetXCFunMat,
                                const GetXCFunExp);
extern QErrorCode RSPXCFunAdd(RSPXCFun*,
                              const QInt,
                              const QcPertInt*,
                              const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
                              void*,
#endif
                              const GetXCFunMat,
                              const GetXCFunExp);
extern QErrorCode RSPXCFunAssemble(RSPXCFun*,const RSPPert*);
extern QErrorCode RSPXCFunWrite(RSPXCFun*,FILE*);
extern QErrorCode RSPXCFunGetMat(RSPXCFun*,
                                const QInt,
                                const QcPertInt*,
                                const QInt,
                                const QInt*,
```

```

        const QInt,
        const QInt*,
        const QInt,
        QcMat*[],
        const QInt,
        QcMat*[]);
extern QErrorCode RSPXCFunGetExp(RSPXCFun*,
        const QInt,
        const QcPertInt*,
        const QInt,
        const QInt*,
        const QInt,
        const QInt*,
        const QInt,
        QcMat*[],
        const QInt,
        QReal*);
extern QErrorCode RSPXCFunDestroy(RSPXCFun**);

```

The functions are implemented as follows:

```

87  <RSPXCFun.c 87>≡
    /*
      <OpenRSPLicense 14a>
    */

#include "RSPXCFun.h"

/* <function name='RSPXCFunCreate'
   attr='private'
   author='Bin Gao'
   date='2015-06-23'>
  Create a node of a linked list for a given XC functional, should
  be called at first
  <param name='xc_fun' direction='inout'>
    The linked list of XC functionals
  </param>
  <param name='num_pert_lab' direction='in'>
    Number of all different perturbation labels that can act as
    perturbations on the XC functional
  </param>
  <param name='pert_labels' direction='in'>
    All the different perturbation labels
  </param>
  <param name='pert_max_orders' direction='in'>
    Allowed maximal order of a perturbation described by exactly one of
    the above different labels
  </param>
  <param name='user_ctx' direction='in'>
    User-defined callback-function context
  </param>
  <param name='get_xc_fun_mat' direction='in'>
    User-specified function for calculating integral matrices of the
    XC functional and its derivatives

```

```

    </param>
    <param name='get_xc_fun_exp' direction='in'>
        User-specified function for calculating expectation values of the
        XC functional and its derivatives
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPXCFunCreate(RSPXCFun **xc_fun,
                        const QInt num_pert_lab,
                        const QcPertInt *pert_labels,
                        const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                        void *user_ctx,
#endif
                        const GetXCFunMat get_xc_fun_mat,
                        const GetXCFunExp get_xc_fun_exp)
{
    RSPXCFun *new_xc; /* new XC functional */
    QInt ilab;         /* incremental recorders over perturbation labels */
    QInt jlab;
    new_xc = (RSPXCFun *)malloc(sizeof(RSPXCFun));
    if (new_xc==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for XC functional");
    }
    if (num_pert_lab<0) {
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPXCFunCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
    }
    new_xc->num_pert_lab = num_pert_lab;
    if (new_xc->num_pert_lab>0) {
        new_xc->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
        if (new_xc->pert_max_orders==NULL) {
            printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
                   num_pert_lab);
            QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
        }
        new_xc->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
        if (new_xc->pert_labels==NULL) {
            printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
                   num_pert_lab);
            QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
        }
        new_xc->xc_len_tuple = 0;
        for (ilab=0; ilab<num_pert_lab; ilab++) {

```



```

    if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
            ilab,
            pert_labels[ilab]);
        printf("RSPXCFunCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n"
            OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "invalid perturbation label");
    }
    /* each element of <pert_labels> should be unique */
    for (jlab=0; jlab<ilab; jlab++) {
        if (pert_labels[jlab]==pert_labels[ilab]) {
            printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n"
                jlab,
                pert_labels[jlab]);
            printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n"
                ilab,
                pert_labels[ilab]);
            QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
        }
    }
    new_xc->pert_labels[ilab] = pert_labels[ilab];
    if (pert_max_orders[ilab]<1) {
        printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
            ilab,
            pert_labels[ilab]);
        printf("RSPXCFunCreate>> allowed maximal order is %"QINT_FMT"\n",
            pert_max_orders[ilab]);
        QErrorExit(FILE_AND_LINE, "only positive order allowed");
    }
    new_xc->pert_max_orders[ilab] = pert_max_orders[ilab];
    new_xc->xc_len_tuple += pert_max_orders[ilab];
}
new_xc->xc_pert_tuple = (QcPertInt *)malloc(new_xc->xc_len_tuple*sizeof(QcPertInt))
if (new_xc->xc_pert_tuple==NULL) {
    printf("RSPXCFunCreate>> length of perturbation tuple %"QINT_FMT"\n",
        new_xc->xc_len_tuple);
    QErrorExit(FILE_AND_LINE, "allocates memory for pert. tuple on XC functional");
}
}
else {
    new_xc->pert_max_orders = NULL;
    new_xc->pert_labels = NULL;
    new_xc->xc_pert_tuple = NULL;
}
#endif
new_xc->get_xc_fun_mat = get_xc_fun_mat;
new_xc->get_xc_fun_exp = get_xc_fun_exp;
new_xc->next_xc = NULL;
*xc_fun = new_xc;
return QSUCCESS;

```

```
}
```

As shown here, we allow for an XC functional that does not depend on any peraturbation—`num_pert_lab==0`, i.e. any perturbed integral matrix and expectation value of this XC functional is zero.

```
90  <RSPXCFun.c 87>+≡
    /* <function name='RSPXCFunAdd'
        attr='private'
        author='Bin Gao'
        date='2015-06-23'>
    Add a given XC functional to the linked list
    <param name='xc_fun' direction='inout'>
        The linked list of XC functionals
    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the XC functional
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback-function context
    </param>
    <param name='get_xc_fun_mat' direction='in'>
        User-specified function for calculating integral matrices of the
        XC functional and its derivatives
    </param>
    <param name='get_xc_fun_exp' direction='in'>
        User-specified function for calculating expectation values of the
        XC functional and its derivatives
    </param>
    <return>Error information</return>
    </function> */
QErrorCode RSPXCFunAdd(RSPXCFun *xc_fun,
                      const QInt num_pert_lab,
                      const QcPertInt *pert_labels,
                      const QInt *pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                      void *user_ctx,
#endif
                      const GetXCFunMat get_xc_fun_mat,
                      const GetXCFunExp get_xc_fun_exp)
{
    RSPXCFun *new_xc; /* new XC functional */
    RSPXCFun *cur_xc; /* current XC functional */
    QErrorCode ierr; /* error information */
    /* creates the new XC functional */
```

```

ierr = RSPXCFunCreate(&new_xc,
                    num_pert_lab,
                    pert_labels,
                    pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                    user_ctx,
#endif
                    get_xc_fun_mat,
                    get_xc_fun_exp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunCreate()");
/* walks to the last XC functional */
cur_xc = xc_fun;
while (cur_xc->next_xc!=NULL) {
    cur_xc = cur_xc->next_xc;
}
/* inserts the new XC functional to the tail of the linked list */
cur_xc->next_xc = new_xc;
return QSUCCESS;
}

/* <function name='RSPXCFunAssemble'
    attr='private'
    author='Bin Gao'
    date='2015-06-23'>
    Assembles the linked list of XC functionals
    <param name='xc_fun' direction='inout'>
        The linked list of XC functionals
    </param>
    <param name='rsp_pert' direction='in'>
        The context of perturbations
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPXCFunAssemble(RSPXCFun *xc_fun, const RSPPert *rsp_pert)
{
    QInt ixc;          /* incremental recorder over XC functionals */
    RSPXCFun *cur_xc;  /* current XC functional */
    QErrorCode ierr;   /* error information */
    ixc = 0;
    cur_xc = xc_fun;
    do {
        if (cur_xc->num_pert_lab>0 &&
            (cur_xc->pert_labels==NULL || cur_xc->pert_max_orders==NULL)) {
            printf("RSPXCFunAssemble>> %"QINT_FMT"-th XC functional\n",
                   ixc);
            QErrorExit(FILE_AND_LINE, "perturbations of XC functional not set");
        }
        if (cur_xc->get_xc_fun_mat==NULL || cur_xc->get_xc_fun_exp==NULL) {
            printf("RSPXCFunAssemble>> %"QINT_FMT"-th XC functional\n",
                   ixc);
            QErrorExit(FILE_AND_LINE, "callback functions of XC functional not set");
        }
    }
}

```

```

    /* checks perturbation labels and allowed maximal orders against
       all known perturbations */
    ierr = RSPPertValidateLabelOrder(rsp_pert,
                                     cur_xc->num_pert_lab,
                                     cur_xc->pert_labels,
                                     cur_xc->pert_max_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
    /* moves to the next XC functional */
    ixc++;
    cur_xc = cur_xc->next_xc;
} while (cur_xc!=NULL);
return QSUCCESS;
}

/* <function name='RSPXCFunWrite'
   attr='private'
   author='Bin Gao'
   date='2015-06-23'>
Writes the linked list of XC functionals
<param name='xc_fun' direction='in'>
  The linked list of XC functionals
</param>
<param name='fp_xc' direction='inout'>File pointer</param>
<return>Error information</return>
</function> */
QErrorCode RSPXCFunWrite(RSPXCFun *xc_fun, FILE *fp_xc)
{
    QInt ixc;          /* incremental recorder over XC functionals */
    RSPXCFun *cur_xc; /* current XC functional */
    QInt ilab;         /* incremental recorder over perturbation labels */
    ixc = 0;
    cur_xc = xc_fun;
    do {
        fprintf(fp_xc, "RSPXCFunWrite>> XC functional %"QINT_FMT"\n", ixc);
        fprintf(fp_xc,
                "RSPXCFunWrite>> number of pert. labels that XC functional depends on %"QINT_FMT"\n",
                cur_xc->num_pert_lab);
        fprintf(fp_xc, "RSPXCFunWrite>> label          maximum-order\n");
        for (ilab=0; ilab<cur_xc->num_pert_lab; ilab++) {
            fprintf(fp_xc,
                    "RSPXCFunWrite>>          %"QCPERTINT_FMT"          %"QINT_FMT"\n",
                    cur_xc->pert_labels[ilab],
                    cur_xc->pert_max_orders[ilab]);
        }
    }
#ifdef OPENRSP_C_USER_CONTEXT
    if (cur_xc->user_ctx!=NULL) {
        fprintf(fp_xc, "RSPXCFunWrite>> user-defined function context given\n");
    }
#endif
    /* moves to the next XC functional */
    ixc++;
    cur_xc = cur_xc->next_xc;
}

```

```

    } while (cur_xc!=NULL);
    return QSUCCESS;
}

/* <function name='RSPXCFunGetMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates integral matrices of the linked list of XC functionals
    <param name='xc_fun' direction='inout'>
        The linked list of XC functionals
    </param>
    <param name='xc_len_tuple' direction='in'>
        Length of the perturbation tuple on the linked list of XC functionals
    </param>
    <param name='xc_pert_tuple' direction='in'>
        Perturbation tuple on the linked list of XC functionals
    </param>
    <param name='num_freq_configs' direction='in'>
        The number of different frequency configurations to be considered for
        the perturbation tuple
    </param>
    <param name='pert_freq_category' direction='in'>
        Category of perturbation frequencies
    </param>
    <param name='dmat_num_tuple' direction='in'>
        The number of different perturbation tuples of the atomic orbital (AO)
        based density matrices passed
    </param>
    <param name='dmat_idx_tuple' direction='in'>
        Indices of the density matrix perturbation tuples passed (canonically
        ordered)
    </param>
    <param name='num_dmat' direction='in'>
        Number of collected AO based density matrices for the passed density
        matrix perturbation tuples and all frequency configurations
    </param>
    <param name='dens_mat' direction='in'>
        The collected AO based density matrices
    </param>
    <param name='num_int' direction='in'>
        Number of the integral matrices
    </param>
    <param name='val_int' direction='inout'>
        The integral matrices
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPXCFunGetMat(RSPXCFun *xc_fun,
    const QInt xc_len_tuple,
    const QcPertInt *xc_pert_tuple,
    const QInt num_freq_configs,

```

```

        const QInt *pert_freq_category,
        const QInt dmat_num_tuple,
        const QInt *dmat_idx_tuple,
        const QInt num_dmat,
        QcMat *dens_mat[],
        const QInt num_int,
        QcMat *val_int[])
{
    RSPXCFun *cur_xc; /* current XC functional */
    QErrorCode ierr; /* error information */
    cur_xc = xc_fun;
    do {
        /* gets the host program's perturbation tuple on the XC functional */
        ierr = RSPPertInternTupleToHostTuple(xc_len_tuple,
                                              xc_pert_tuple,
                                              cur_xc->num_pert_lab,
                                              cur_xc->pert_labels,
                                              cur_xc->pert_max_orders,
                                              &cur_xc->xc_len_tuple,
                                              cur_xc->xc_pert_tuple);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostTuple()");
        /* checks if the perturbations on the XC functional result in
           zero values */
        if (cur_xc->xc_len_tuple>=0) {
            /* calculates integral matrices using the callback function */
            cur_xc->get_xc_fun_mat(cur_xc->xc_len_tuple,
                                   cur_xc->xc_pert_tuple,
                                   num_freq_configs,
                                   pert_freq_category,
                                   dmat_num_tuple,
                                   dmat_idx_tuple,
                                   num_dmat,
                                   dens_mat,
#ifdef OPENRSP_C_USER_CONTEXT
                                   cur_xc->user_ctx,
#endif
                                   num_int,
                                   val_int);
        }
        /* moves to the next XC functional */
        cur_xc = cur_xc->next_xc;
    } while (cur_xc!=NULL);
    return QSUCCESS;
}

/* <function name='RSPXCFunGetExp'
   attr='private'
   author='Bin Gao'
   date='2015-10-15'>
Calculates expectation values of the linked list of XC functionals
<param name='xc_fun' direction='inout'>
The linked list of XC functionals

```

```

    </param>
    <param name='xc_len_tuple' direction='in'>
        Length of the perturbation tuple on the linked list of XC functionals
    </param>
    <param name='xc_pert_tuple' direction='in'>
        Perturbation tuple on the linked list of XC functionals
    </param>
    <param name='num_freq_configs' direction='in'>
        The number of different frequency configurations to be considered for
        the perturbation tuple
    </param>
    <param name='pert_freq_category' direction='in'>
        Category of perturbation frequencies
    </param>
    <param name='dmat_num_tuple' direction='in'>
        The number of different perturbation tuples of the atomic orbital (AO)
        based density matrices passed
    </param>
    <param name='dmat_idx_tuple' direction='in'>
        Indices of the density matrix perturbation tuples passed (canonically
        ordered)
    </param>
    <param name='num_dmat' direction='in'>
        Number of collected AO based density matrices for the passed density
        matrix perturbation tuples and all frequency configurations
    </param>
    <param name='dens_mat' direction='in'>
        The collected AO based density matrices
    </param>
    <param name='num_exp' direction='in'>
        Number of the expectation values
    </param>
    <param name='val_exp' direction='inout'>
        The expectation values
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPXCFunGetExp(RSPXCFun *xc_fun,
                        const QInt xc_len_tuple,
                        const QcPertInt *xc_pert_tuple,
                        const QInt num_freq_configs,
                        const QInt *pert_freq_category,
                        const QInt dmat_num_tuple,
                        const QInt *dmat_idx_tuple,
                        const QInt num_dmat,
                        QcMat *dens_mat[],
                        const QInt num_exp,
                        QReal *val_exp)
{
    RSPXCFun *cur_xc; /* current XC functional */
    QErrorCode ierr; /* error information */
    cur_xc = xc_fun;

```

```

do {
    /* gets the host program's perturbation tuple on the XC functional */
    ierr = RSPPertInternTupleToHostTuple(xc_len_tuple,
                                          xc_pert_tuple,
                                          cur_xc->num_pert_lab,
                                          cur_xc->pert_labels,
                                          cur_xc->pert_max_orders,
                                          &cur_xc->xc_len_tuple,
                                          cur_xc->xc_pert_tuple);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostTuple()");
    /* checks if the perturbations on the XC functional result in
       zero values */
    if (cur_xc->xc_len_tuple>=0) {
        /* calculates expectation values using the callback function */
        cur_xc->get_xc_fun_exp(cur_xc->xc_len_tuple,
                              cur_xc->xc_pert_tuple,
                              num_freq_configs,
                              pert_freq_category,
                              dmat_num_tuple,
                              dmat_idx_tuple,
                              num_dmat,
                              dens_mat,
                              cur_xc->user_ctx,
                              num_exp,
                              val_exp);
    }
    /* moves to the next XC functional */
    cur_xc = cur_xc->next_xc;
} while (cur_xc!=NULL);
return QSUCCESS;
}

/* <function name='RSPXCFunDestroy'
   attr='private'
   author='Bin Gao'
   date='2015-06-23'>
   Destroys the linked list of XC functionals, should be called at the end
   <param name='xc_fun' direction='inout'>
       The linked list of XC functionals
   </param>
   <return>Error information</return>
</function> */
QErrorCode RSPXCFunDestroy(RSPXCFun **xc_fun)
{
    RSPXCFun *cur_xc;    /* current XC functional */
    RSPXCFun *next_xc;   /* next XC functional */
    /* walks to the last XC functional */
    cur_xc = *xc_fun;
    while (cur_xc!=NULL) {
        if (cur_xc->pert_max_orders!=NULL) {

```



```
        free(cur_xc->pert_max_orders);
        cur_xc->pert_max_orders = NULL;
    }
    if (cur_xc->pert_labels!=NULL) {
        free(cur_xc->pert_labels);
        cur_xc->pert_labels = NULL;
    }
    if (cur_xc->xc_pert_tuple!=NULL) {
        free(cur_xc->xc_pert_tuple);
        cur_xc->xc_pert_tuple = NULL;
    }
#ifdef OPENRSP_C_USER_CONTEXT
    cur_xc->user_ctx = NULL;
#endif
    cur_xc->get_xc_fun_mat = NULL;
    cur_xc->get_xc_fun_exp = NULL;
    next_xc = cur_xc->next_xc;
    free(cur_xc);
    cur_xc = NULL;
    cur_xc = next_xc;
}
return QSUCCESS;
}
```

3.8 Zero-Electron Operators

Users can use the following API to add different zero-electron operators (such as nuclear repulsion and nuclei-field interaction):

```

98  (OpenRSP.c 17a)+≡
    /* <function name='OpenRSPAddZeroOper' author='Bin Gao' date='2015-02-12'>
        Add a zero-electron operator to the Hamiltonian
        <param name='open_rsp' direction='inout'>
            The context of response theory calculations
        </param>
        <param name='num_pert_lab' direction='in'>
            Number of all different perturbation labels that can act on the
            zero-electron operator
        </param>
        <param name='pert_labels' direction='in'>
            All the different perturbation labels involved
        </param>
        <param name='pert_max_orders' direction='in'>
            Allowed maximal order of a perturbation described by exactly one of
            the above different labels
        </param>
        <param name='user_ctx' direction='in'>
            User-defined callback function context
        </param>
        <param name='get_zero_oper_contrib' direction='in'>
            User-specified callback function to calculate contributions from the
            zero-electron operator
        </param>
        <return>Error information</return>
    </function> */
QErrorCode OpenRSPAddZeroOper(OpenRSP *open_rsp,
                              const QInt num_pert_lab,
                              const QcPertInt *pert_labels,
                              const QInt *pert_max_orders,
                              #if defined(OPENRSP_C_USER_CONTEXT)
                              void *user_ctx,
                              #endif

                              const GetZeroOperContrib get_zero_oper_contrib)
{
    QErrorCode ierr; /* error information */
    /* creates the linked list of zero-electron operators */
    if (open_rsp->zero_oper==NULL) {
        ierr = RSPZeroOperCreate(&open_rsp->zero_oper,
                                num_pert_lab,
                                pert_labels,
                                pert_max_orders,
                                #if defined(OPENRSP_C_USER_CONTEXT)
                                user_ctx,
                                #endif

                                get_zero_oper_contrib);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperCreate()");
    }
}

```

```

    }
    /* adds the zero-electron operator to the linked list */
    else {
        ierr = RSPZeroOperAdd(open_rsp->zero_oper,
                               num_pert_lab,
                               pert_labels,
                               pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                               user_ctx,
#endif
                               get_zero_oper_contrib);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperAdd()");
    }
    return QSUCCESS;
}

```

The following header file defines all quantities we need for the zero-electron operator. Type `GetZeroOperContrib` defines the requirements of the host-program's callback function to calculate the contribution of zero-electron operator and its derivatives.

99a $\langle RSPZeroOper.h$ 99a \equiv

```

/*
   $\langle OpenRSPLicense$  14a  $\rangle$ 

  <header name='RSPZeroOper.h' author='Bin Gao' date='2014-12-11'>
    The header file of zero-electron operator used inside OpenRSP
  </header>
*/

#ifdef !defined(RSP_ELEC_FREE_OPER_H)
#define RSP_ELEC_FREE_OPER_H

#include "qcmatrix.h"
#include "RSPPerturbation.h"

typedef void (*GetZeroOperContrib)(const QInt,
                                   const QcPertInt*,
                                   const QInt*,
#ifdef OPENRSP_C_USER_CONTEXT
                                   void*,
#endif
                                   const QInt,
                                   QReal*);

 $\langle RSPZeroOperStruct$  99b  $\rangle$ 

 $\langle RSPZeroOperAPIs$  100  $\rangle$ 

#endif

```

The context of zero-electron operator is:

99b $\langle RSPZeroOperStruct$ 99b \equiv

```

typedef struct RSPZeroOper RSPZeroOper;
struct RSPZeroOper {

```

```

    QInt num_pert_lab;          /* number of different perturbation labels
                                that can act as perturbations on the
                                zero-electron operator */
    QInt oper_num_pert;         /* number of perturbations on the
                                zero-electron operator, only used for
                                callback functions */
    QInt *pert_max_orders;      /* allowed maximal order of a perturbation
                                described by exactly one of these
                                different labels */
    QInt *oper_pert_orders;     /* orders of perturbations on the
                                zero-electron operator, only used for
                                callback functions */
    QcPertInt *pert_labels;     /* all the different perturbation labels */
    QcPertInt *oper_pert_labels; /* labels of perturbations on the
                                zero-electron operator, only used for
                                callback functions */

    #if defined(OPENRSP_C_USER_CONTEXT)
        void *user_ctx;         /* user-defined callback-function context */
    #endif
    GetZeroOperContrib get_zero_oper_contrib; /* user-specified function for calculating
                                                contribution from the zero-electron operator */
    RSPZeroOper *next_oper;     /* pointer to the next zero-electron operator */
};

```

and the functions related to the zero-electron operators:

100 $\langle RSPZeroOperAPIs \ 100 \rangle \equiv$

```

extern QErrorCode RSPZeroOperCreate(RSPZeroOper**,
                                    const QInt,
                                    const QcPertInt*,
                                    const QInt*,

    #if defined(OPENRSP_C_USER_CONTEXT)
                                    void*,
    #endif
                                    const GetZeroOperContrib);
extern QErrorCode RSPZeroOperAdd(RSPZeroOper*,
                                 const QInt,
                                 const QcPertInt*,
                                 const QInt*,

    #if defined(OPENRSP_C_USER_CONTEXT)
                                 void*,
    #endif
                                 const GetZeroOperContrib);
extern QErrorCode RSPZeroOperAssemble(RSPZeroOper*, const RSPPert*);
extern QErrorCode RSPZeroOperWrite(const RSPZeroOper*, FILE*);
extern QErrorCode RSPZeroOperGetContribution(RSPZeroOper*,
                                              const QInt,
                                              const QcPertInt*,
                                              const QInt,
                                              QReal*);

extern QErrorCode RSPZeroOperDestroy(RSPZeroOper**);
/*FIXME: RSPZeroOperGetNumAtoms() to be removed after perturbation free scheme implemented*/
extern QErrorCode RSPZeroOperGetNumAtoms(const RSPZeroOper*, QInt*);

```

The functions are implemented as follows:

```

101  <RSPZeroOper.c 101>≡
    /*
      <OpenRSPLicense 14a>
    */

#include "RSPZeroOper.h"

/* <function name='RSPZeroOperCreate'
    attr='private'
    author='Bin Gao'
    date='2015-02-12'>
    Create a node of a linked list for a given zero-electron operator, should
    be called at first
    <param name='zero_oper' direction='inout'>
        The linked list of zero-electron operators
    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the zero-electron operator
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>
    <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback-function context
    </param>
    <param name='get_zero_oper_contrib' direction='in'>
        User-specified function for calculating contribution of the
        zero-electron operator and its derivatives
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPZeroOperCreate(RSPZeroOper **zero_oper,
                             const QInt num_pert_lab,
                             const QcPertInt *pert_labels,
                             const QInt *pert_max_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                             void *user_ctx,
#endif
                             const GetZeroOperContrib get_zero_oper_contrib)
{
    RSPZeroOper *new_oper; /* new operator */
    QInt ilab; /* incremental recorders over perturbation labels */
    QInt jlab;
    new_oper = (RSPZeroOper *)malloc(sizeof(RSPZeroOper));
    if (new_oper==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for zero-electron operator");
    }
}

```

```

if (num_pert_lab<0) {
    printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
}
else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
    printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    printf("RSPZeroOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
           OPENRSP_PERT_LABEL_MAX);
    QErrorExit(FILE_AND_LINE, "too many perturbation labels");
}
new_oper->num_pert_lab = num_pert_lab;
if (new_oper->num_pert_lab>0) {
    new_oper->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->pert_max_orders==NULL) {
        printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    new_oper->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->oper_pert_orders==NULL) {
        printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on zero-electron o
    }
    new_oper->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->pert_labels==NULL) {
        printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    new_oper->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->oper_pert_labels==NULL) {
        printf("RSPZeroOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on zero-electron o
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPZeroOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            printf("RSPZeroOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"
                   OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {
            if (pert_labels[jlab]==pert_labels[ilab]) {
                printf("RSPZeroOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"
                       jlab,

```

```

        pert_labels[jlab]);
    printf("RSPZeroOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"
        ilab,
        pert_labels[ilab]);
    QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
}
}
new_oper->pert_labels[ilab] = pert_labels[ilab];
if (pert_max_orders[ilab]<1) {
    printf("RSPZeroOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
        ilab,
        pert_labels[ilab]);
    printf("RSPZeroOperCreate>> allowed maximal order is %"QINT_FMT"\n",
        pert_max_orders[ilab]);
    QErrorExit(FILE_AND_LINE, "only positive order allowed");
}
new_oper->pert_max_orders[ilab] = pert_max_orders[ilab];
}
}
else {
    new_oper->pert_max_orders = NULL;
    new_oper->oper_pert_orders = NULL;
    new_oper->pert_labels = NULL;
    new_oper->oper_pert_labels = NULL;
}
#ifdef OPENRSP_C_USER_CONTEXT
    new_oper->user_ctx = user_ctx;
#endif
new_oper->get_zero_oper_contrib = get_zero_oper_contrib;
new_oper->next_oper = NULL;
*zero_oper = new_oper;
return QSUCCESS;
}

```

As shown here, we allow for a zero-electron operator that does not depend on any perturbation— $\text{num_pert_lab}=0$, i.e. any perturbed contribution of this zero-electron operator is zero.

103 $\langle RSPZeroOper.c \text{ 101} \rangle + \equiv$

```

/* <function name='RSPZeroOperAdd'
    attr='private'
    author='Bin Gao'
    date='2015-02-12'>
    Add a given zero-electron operator to the linked list
    <param name='zero_oper' direction='inout'>
        The linked list of zero-electron operators
    </param>
    <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act as
        perturbations on the zero-electron operator
    </param>
    <param name='pert_labels' direction='in'>
        All the different perturbation labels
    </param>

```

```

<param name='pert_max_orders' direction='in'>
    Allowed maximal order of a perturbation described by exactly one of
    the above different labels
</param>
<param name='user_ctx' direction='in'>
    User-defined callback-function context
</param>
<param name='get_zero_oper_contrib' direction='in'>
    User-specified function for calculating contribution of the
    zero-electron operator and its derivatives
</param>
<return>Error information</return>
</function> */
QErrorCode RSPZeroOperAdd(RSPZeroOper *zero_oper,
                        const QInt num_pert_lab,
                        const QcPertInt *pert_labels,
                        const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                        void *user_ctx,
#endif
                        const GetZeroOperContrib get_zero_oper_contrib)
{
    RSPZeroOper *new_oper; /* new operator */
    RSPZeroOper *cur_oper; /* current operator */
    QErrorCode ierr;        /* error information */
    /* creates the new operator */
    ierr = RSPZeroOperCreate(&new_oper,
                            num_pert_lab,
                            pert_labels,
                            pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_zero_oper_contrib);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPZeroOperCreate()");
    /* walks to the last operator */
    cur_oper = zero_oper;
    while (cur_oper->next_oper!=NULL) {
        cur_oper = cur_oper->next_oper;
    }
    /* inserts the new operator to the tail of the linked list */
    cur_oper->next_oper = new_oper;
    return QSUCCESS;
}

/* <function name='RSPZeroOperAssemble'
    attr='private'
    author='Bin Gao'
    date='2015-02-12'>
    Assembles the context of zero-electron operator
    <param name='zero_oper' direction='inout'>
        The context of zero-electron operator

```



```

    </param>
    <param name='rsp_pert' direction='in'>
        The context of perturbations
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPZeroOperAssemble(RSPZeroOper *zero_oper,
                               const RSPPert *rsp_pert)
{
    QInt ioper;          /* incremental recorder over operators */
    RSPZeroOper *cur_oper; /* current operator */
    QErrorCode ierr;      /* error information */
    ioper = 0;
    cur_oper = zero_oper;
    do {
        if (cur_oper->num_pert_lab>0 &&
            (cur_oper->pert_labels==NULL || cur_oper->pert_max_orders==NULL)) {
            printf("RSPZeroOperAssemble>> %"QINT_FMT"-th zero-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "perturbations of zero-electron operator not set");
        }
        if (zero_oper->get_zero_oper_contrib==NULL) {
            printf("RSPZeroOperAssemble>> %"QINT_FMT"-th zero-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "callback function of zero-electron operator not set");
        }
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                          cur_oper->num_pert_lab,
                                          cur_oper->pert_labels,
                                          cur_oper->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}

/* <function name='RSPZeroOperWrite'
   attr='private'
   author='Bin Gao'
   date='2015-02-12'>
Writes the linked list of zero-electron operators
<param name='zero_oper' direction='in'>
    The linked list of zero-electron operators
</param>
<param name='fp_oper' direction='inout'>File pointer</param>
<return>Error information</return>
</function> */
QErrorCode RSPZeroOperWrite(const RSPZeroOper *zero_oper, FILE *fp_oper)

```

```

{
    QInt ioper;          /* incremental recorder over operators */
    RSPZeroOper *cur_oper; /* current operator */
    QInt ilab;           /* incremental recorder over perturbation labels */
    ioper = 0;
    cur_oper = zero_oper;
    do {
        fprintf(fp_oper, "RSPZeroOperWrite>> operator %"QINT_FMT"\n", ioper);
        fprintf(fp_oper,
            "RSPZeroOperWrite>> number of pert. labels that zero-electron operator depends on\n",
            cur_oper->num_pert_lab);
        fprintf(fp_oper, "RSPZeroOperWrite>> label          maximum-order\n");
        for (ilab=0; ilab<cur_oper->num_pert_lab; ilab++) {
            fprintf(fp_oper,
                "RSPZeroOperWrite>>          %"QCPERTINT_FMT"          %"QINT_FMT"\n",
                cur_oper->pert_labels[ilab],
                cur_oper->pert_max_orders[ilab]);
        }
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        if (cur_oper->user_ctx!=NULL) {
            fprintf(fp_oper, "RSPZeroOperWrite>> user-defined function context given\n");
        }
    #endif
    /* moves to the next operator */
    ioper++;
    cur_oper = cur_oper->next_oper;
} while (cur_oper!=NULL);
return QSUCCESS;
}

/* <function name='RSPZeroOperGetContribution'
    attr='private'
    author='Bin Gao'
    date='2015-10-15'>
    Calculates contribution of the linked list of zero-electron operators
    <param name='zero_oper' direction='inout'>
        The linked list of zero-electron operators
    </param>
    <param name='oper_len_tuple' direction='in'>
        Length of the perturbation tuple on the linked list of zero-electron
        operators
    </param>
    <param name='oper_pert_tuple' direction='in'>
        Perturbation tuple on the linked list of zero-electron operators
    </param>
    <param name='size_pert' direction='in'>
        Size of the perturbations on the linked list of zero-electron operators
    </param>
    <param name='val_oper' direction='inout'>
        The contribution of the linked list of zero-electron operators
    </param>
    <return>Error information</return>

```

```

</function> */
QErrorCode RSPZeroOperGetContribution(RSPZeroOper *zero_oper,
                                     const QInt oper_len_tuple,
                                     const QcPertInt *oper_pert_tuple,
                                     const QInt size_pert,
                                     QReal *val_oper)
{
    RSPZeroOper *cur_oper; /* current operator */
    QErrorCode ierr;       /* error information */
    cur_oper = zero_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the zero-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                    oper_pert_tuple,
                                                    cur_oper->num_pert_lab,
                                                    cur_oper->pert_labels,
                                                    cur_oper->pert_max_orders,
                                                    &cur_oper->oper_num_pert,
                                                    cur_oper->oper_pert_labels,
                                                    cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()")
        /* checks if the perturbations on the zero-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert>=0) {
            /* calculates contribution of zero-electron operator using the
               callback function */
            cur_oper->get_zero_oper_contrib(cur_oper->oper_num_pert,
                                            cur_oper->oper_pert_labels,
                                            cur_oper->oper_pert_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                                            cur_oper->user_ctx,
#endif
                                            size_pert,
                                            val_oper);
        }
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}

/* <function name='RSPZeroOperDestroy'
   attr='private'
   author='Bin Gao'
   date='2015-02-12'>
Destroys the linked list of zero-electron operators, should be called
at the end
<param name='zero_oper' direction='inout'>
    The linked list of zero-electron operators
</param>
<return>Error information</return>

```

```

    </function> */
QErrorCode RSPZeroOperDestroy(RSPZeroOper **zero_oper)
{
    RSPZeroOper *cur_oper; /* current operator */
    RSPZeroOper *next_oper; /* next operator */
    /* walks to the last operator */
    cur_oper = *zero_oper;
    while (cur_oper!=NULL) {
        if (cur_oper->pert_max_orders!=NULL) {
            free(cur_oper->pert_max_orders);
            cur_oper->pert_max_orders = NULL;
        }
        if (cur_oper->oper_pert_orders!=NULL) {
            free(cur_oper->oper_pert_orders);
            cur_oper->oper_pert_orders = NULL;
        }
        if (cur_oper->pert_labels!=NULL) {
            free(cur_oper->pert_labels);
            cur_oper->pert_labels = NULL;
        }
        if (cur_oper->oper_pert_labels!=NULL) {
            free(cur_oper->oper_pert_labels);
            cur_oper->oper_pert_labels = NULL;
        }
    }
    #if defined(OPENRSP_C_USER_CONTEXT)
        cur_oper->user_ctx = NULL;
    #endif
    cur_oper->get_zero_oper_contrib = NULL;
    next_oper = cur_oper->next_oper;
    free(cur_oper);
    cur_oper = NULL;
    cur_oper = next_oper;
}
return QSUCCESS;
}

```

3.9 Linear Response Equation Solver

Users can use the following API to set the linear response equation solver:

```
109a  <OpenRSP.c 17a>+=
/* <function name='OpenRSPSetLinearRSPSolver' author='Bin Gao' date='2014-08-06'>
    Set the context of linear response equation solver
    <param name='open_rsp' direction='inout'>
        The context of response theory calculations
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback function context
    </param>
    <param name='get_linear_rsp_solution' direction='in'>
        User-specified callback function of linear response equation solver
    </param>
    <return>Error information</return>
</function> */
QErrorCode OpenRSPSetLinearRSPSolver(OpenRSP *open_rsp,
#if defined(OPENRSP_C_USER_CONTEXT)
                                void *user_ctx,
#endif
                                const GetLinearRSPSolution get_linear_rsp_solution)
{
    QErrorCode ierr; /* error information */
    /* creates the context of response equation solver */
    if (open_rsp->rsp_solver!=NULL) {
        ierr = RSPSolverDestroy(open_rsp->rsp_solver);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverDestroy()");
    }
    else {
        open_rsp->rsp_solver = (RSPSolver *)malloc(sizeof(RSPSolver));
        if (open_rsp->rsp_solver==NULL) {
            QErrorExit(FILE_AND_LINE, "allocates memory for solver");
        }
    }
    ierr = RSPSolverCreate(open_rsp->rsp_solver,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_linear_rsp_solution);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverCreate()");
    return QSUCCESS;
}
```

The following header file defines all quantities we need for the linear response equation solver. Type `GetLinearRSPSolution` defines the requirements of the callback function of the linear response equation solver.

```
109b  <RSPSolver.h 109b>≡
/*
    <OpenRSPLicense 14a>

    <header name='RSPSolver.h' author='Bin Gao' date='2014-08-06'>
```

The header file of linear response equation solver used inside OpenRSP

</header>

*/

#if !defined(RSP_SOLVER_H)

#define RSP_SOLVER_H

#include "qcmatrix.h"

```
typedef void (*GetLinearRSPSolution)(const QInt,
                                     const QInt*,
                                     const QInt*,
                                     const QReal*,
                                     QcMat*[],
```

#if defined(OPENRSP_C_USER_CONTEXT)

void*,

#endif

QcMat*[]);

<RSPSolverStruct 110a>

<RSPSolverAPIs 110b>

#endif

The context of linear response equation solver is:

110a

<RSPSolverStruct 110a>≡

```
typedef struct {
```

#if defined(OPENRSP_C_USER_CONTEXT)

void *user_ctx;

/* user-defined callback-function
context */

#endif

GetLinearRSPSolution get_linear_rsp_solution; /* user-specified function of
linear response equation solver */

} RSPSolver;

and the related functions are:

110b

<RSPSolverAPIs 110b>≡

extern QErrorCode RSPSolverCreate(RSPSolver*,

#if defined(OPENRSP_C_USER_CONTEXT)

void*,

#endif

const GetLinearRSPSolution);

extern QErrorCode RSPSolverAssemble(RSPSolver*);

extern QErrorCode RSPSolverWrite(const RSPSolver*,FILE*);

```
extern QErrorCode RSPSolverGetLinearRSPSolution(const RSPSolver*,
                                                const QInt,
                                                const QInt*,
                                                const QInt*,
                                                const QReal*,
                                                QcMat*[],
                                                QcMat*[]);
```

extern QErrorCode RSPSolverDestroy(RSPSolver*);

These functions are implemented as follows:

```

111 <RSPSolver.c 111>≡
/*
  <OpenRSPLicense 14a>
*/

#include "RSPSolver.h"

/* <function name='RSPSolverCreate'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Create the context of response equation solver, should be called at first
    <param name='rsp_solver' direction='inout'>
        The context of response equation solver
    </param>
    <param name='user_ctx' direction='in'>
        User-defined callback function context
    </param>
    <param name='get_linear_rsp_solution' direction='in'>
        User-specified callback function of linear response equation solver
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPSolverCreate(RSPSolver *rsp_solver,
#if defined(OPENRSP_C_USER_CONTEXT)
    void *user_ctx,
#endif
    const GetLinearRSPSolution get_linear_rsp_solution)
{
#if defined(OPENRSP_C_USER_CONTEXT)
    rsp_solver->user_ctx = user_ctx;
#endif
    rsp_solver->get_linear_rsp_solution = get_linear_rsp_solution;
    return QSUCCESS;
}

/* <function name='RSPSolverAssemble'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Assembles the context of response equation solver
    <param name='rsp_solver' direction='inout'>
        The context of response equation solver
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPSolverAssemble(RSPSolver *rsp_solver)
{
/*FIXME: to implement? */
    return QSUCCESS;
}

```

```

/* <function name='RSPSolverWrite'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Writes the context of response equation solver
    <param name='rsp_solver' direction='in'>
        The context of response equation solver
    </param>
    <param name='fp_solver' direction='inout'>File pointer</param>
    <return>Error information</return>
</function> */
QErrorCode RSPSolverWrite(const RSPSolver *rsp_solver, FILE *fp_solver)
{
#ifdef OPENRSP_C_USER_CONTEXT
    if (rsp_solver->user_ctx!=NULL) {
        fprintf(fp_solver, "RSPSolverWrite>> user-defined function context given\n");
    }
#endif
    return QSUCCESS;
}

/* <function name='RSPSolverGetLinearRSPSolution'
    attr='private'
    author='Bin Gao'
    date='2014-08-06'>
    Solve the linear response equation
    <param name='rsp_solver' direction='in'>
        The context of response equation solver
    </param>
    <param name='num_pert' direction='in'>
        Number of different perturbations on the right hand side of the linear
        response equation
    </param>
    <param name='num_comps' direction='in'>
        Number of components of each perturbation, size is <num_pert>
    </param>
    <param name='num_freq_sums' direction='in'>
        For each perturbation, number of complex frequency sums on the left hand
        side of the linear response equation, size is <num_pert>
    </param>
    <param name='freq_sums' direction='in'>
        The complex frequency sums on the left hand side of the linear response
        equation, size is twice of the sum of <num_freq_sums>
    </param>
    <param name='RHS_mat' direction='in'>
        Right-hand-side (RHS) matrices, size is the dot product of <num_comps>
        and <num_freq_sums>, and index of <num_freq_sums> runs faster in memory
    <param name='rsp_param' direction='inout'>
        Solved response parameters, size is the dot product of <num_comps> and
        <num_freq_sums>, and index of <num_freq_sums> runs faster in memory
    </param>

```



```

        <return>Error information</return>
    </function> */
QErrorCode RSPSolverGetLinearRSPSolution(const RSPSolver *rsp_solver,
                                         const QInt num_pert,
                                         const QInt *num_comps,
                                         const QInt *num_freq_sums,
                                         const QReal *freq_sums,
                                         QcMat *RHS_mat[],
                                         QcMat *rsp_param[])
{
    rsp_solver->get_linear_rsp_solution(num_pert,
                                         num_comps,
                                         num_freq_sums,
                                         freq_sums,
                                         RHS_mat,
                                         #if defined(OPENRSP_C_USER_CONTEXT)
                                         rsp_solver->user_ctx,
                                         #endif
                                         rsp_param);

    return QSUCCESS;
}

/* <function name='RSPSolverDestroy'
    attr='private'
    author='Bin Gao'
    date='2014-08-05'>
    Destroys the context of response equation solver, should be called at the end
    <param name='rsp_solver' direction='inout'>
        The context of response equation solver
    </param>
    <return>Error information</return>
</function> */
QErrorCode RSPSolverDestroy(RSPSolver *rsp_solver)
{
    #if defined(OPENRSP_C_USER_CONTEXT)
        rsp_solver->user_ctx = NULL;
    #endif
    rsp_solver->get_linear_rsp_solution = NULL;
    return QSUCCESS;
}

```



```

        const QReal *pert_freqs,
        const QInt *kn_rules,
        const QInt size_rsp_funs,
        QReal *rsp_funs)
{
    //QErrorCode ierr; /* error information */
    if (open_rsp->assembled==QFALSE) {
        QErrorExit(FILE_AND_LINE, "OpenRSPAssemble() should be called before calculations")
    }
    //switch (open_rsp->elec_wav_type) {
    /** density matrix-based response theory */
    //case ELEC_AO_D_MATRIX:
        OpenRSPGetRSPFun_f(open_rsp->num_atoms,
                            num_props,
                            len_tuple,
                            pert_tuple,
                            num_freq_configs,
                            pert_freqs,
                            kn_rules,
                            ref_ham,
                            ref_overlap,
                            ref_state,
                            open_rsp->rsp_solver,
                            open_rsp->zero_oper,
                            open_rsp->overlap,
                            open_rsp->one_oper,
                            open_rsp->two_oper,
                            open_rsp->xc_fun,
                            //id_outp,
                            size_rsp_funs,
                            rsp_funs);

        // break;
    /** molecular orbital (MO) coefficient matrix-based response theory */
    //case ELEC_MO_C_MATRIX:
        // break;
    /** couple cluster-based response theory */
    //case ELEC_COUPLED_CLUSTER:
        // break;
    //default:
        // printf("OpenRSPGetRSPFun>> type of (electronic) wave function %d\n",
        //         open_rsp->elec_wav_type);
        // QErrorExit(FILE_AND_LINE, "invalid type of (electronic) wave function");
    //}
    return QSUCCESS;
}

```

3.11 Residues

Users can use the following API to get the residues:

```
116 <OpenRSP.c 17a>+≡
/*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
void OpenRSPGetResidue_f(const QInt num_atoms,
                        const QInt num_props,
                        const QInt *len_tuple,
                        const QcPertInt *pert_tuple,
                        const QInt *residue_num_pert,
                        const QInt *residue_idx_pert,
                        const QInt *num_freq_configs,
                        const QReal *pert_freqs,
                        const QInt *kn_rules,
                        const QcMat *ref_ham,
                        const QcMat *ref_overlap,
                        const QcMat *ref_state,
                        const QInt order_residue,
                        const QInt num_excit,
                        const QReal *excit_energy,
                        QcMat *eigen_vector[],
                        RSPSolver *rsp_solver,
                        //RSPZeroOper *zero_oper,
                        RSPOverlap *overlap,
                        RSPOneOper *one_oper,
                        RSPTwoOper *two_oper,
                        RSPXCFun *xc_fun,
                        const QInt size_residues,
                        QReal *residues);

/*@% \brief gets the residues for given perturbations
\author Bin Gao
\date 2014-07-31
\param[OpenRSP:struct]{inout} open_rsp the context of response theory calculations
\param[QcMat:struct]{in} ref_ham Hamiltonian of referenced state
\param[QcMat:struct]{in} ref_state electronic state of referenced state
\param[QcMat:struct]{in} ref_overlap overlap integral matrix of referenced state
\param[QInt:int]{in} order_residue order of residues, that is also the length of
each excitation tuple
\param[QInt:int]{in} num_excit number of excitation tuples that will be used for
residue calculations
\param[QReal:real]{in} excit_energy excitation energies of all tuples, size is
‘‘order_residue’’ :math:\times ‘‘num_excit’’, and arranged
as ‘‘[num_excit][order_residue]’’; that is, there will be
‘‘order_residue’’ frequencies of perturbation labels (or sums
of frequencies of perturbation labels) respectively equal to
the ‘‘order_residue’’ excitation energies per tuple
‘‘excit_energy[i][:]’’ (‘‘i’’ runs from ‘‘0’’ to ‘‘num_excit-1’’)
\param[QcMat:struct]{in} eigen_vector eigenvectors (obtained from the generalized
eigenvalue problem) of all excitation tuples, size is ‘‘order_residue’’
:math:\times ‘‘num_excit’’, and also arranged in memory
as ‘‘[num_excit][order_residue]’’ so that each eigenvector has
```

```

        its corresponding excitation energy in ‘‘excit_energy’’
\param[QInt:int]{in} num_props number of properties to calculate
\param[QInt:int]{in} len_tuple length of perturbation tuple for each property
\param[QInt:int]{in} pert_tuple ordered list of perturbation labels
    for each property
\param[QInt:int]{in} residue_num_pert for each property and each excitation energy
    in the tuple, the number of perturbation labels whose sum of
    frequencies equals to that excitation energy, size is ‘‘order_residue’’
    :math:\backslashtimes ‘‘num_props’’, and arranged as ‘‘[num_props][order_residue]’’;
    a negative ‘‘residue_num_pert[i][j]’’ (‘‘i’’ runs from ‘‘0’’ to
    ‘‘num_props-1’’) means that the sum of frequencies of perturbation
    labels equals to ‘‘-excit_energy[:]][j]’’
\param[QInt:int]{in} residue_idx_pert for each property and each excitation energy
    in the tuple, the indices of perturbation labels whose sum of
    frequencies equals to that excitation energy, size is
    ‘‘sum(residue_num_pert)’’, and arranged as ‘‘[residue_num_pert]’’
\param[QInt:int]{in} num_freq_configs number of different frequency
    configurations for each property
\param[QReal:real]{in} pert_freqs complex frequencies of each perturbation
    label (except for the perturbation a) over all frequency configurations
    and excitation tuples
\param[QInt:int]{in} kn_rules number k for the kn rule for each property
\param[QInt:int]{in} size_residues size of the residues
\param[QReal:real]{out} residues the residues
\return[QErrorCode:int] error information
*/
QErrorCode OpenRSPGetResidue(OpenRSP *open_rsp,
                            const QcMat *ref_ham,
                            const QcMat *ref_state,
                            const QcMat *ref_overlap,
                            const QInt order_residue,
                            const QInt num_excit,
                            const QReal *excit_energy,
                            QcMat *eigen_vector[],
                            const QInt num_props,
                            const QInt *len_tuple,
                            const QcPertInt *pert_tuple,
                            const QInt *residue_num_pert,
                            const QInt *residue_idx_pert,
                            const QInt *num_freq_configs,
                            const QReal *pert_freqs,
                            const QInt *kn_rules,
                            const QInt size_residues,
                            QReal *residues)
{
    //QErrorCode ierr; /* error information */
    if (open_rsp->assembled==QFALSE) {
        QErrorExit(FILE_AND_LINE, "OpenRSPAssemble() should be invoked before any calculati
    }
    //switch (open_rsp->elec_wav_type) {
    ///* density matrix-based response theory */
    //case ELEC_AO_D_MATRIX:

```

```

    OpenRSPGetResidue_f(open_rsp->num_atoms,
                        num_props,
                        len_tuple,
                        pert_tuple,
                        residue_num_pert,
                        residue_idx_pert,
                        num_freq_configs,
                        pert_freqs,
                        kn_rules,
                        ref_ham,
                        ref_overlap,
                        ref_state,
                        order_residue,
                        num_excit,
                        excit_energy,
                        eigen_vector,
                        open_rsp->rsp_solver,
                        //open_rsp->zero_oper,
                        open_rsp->overlap,
                        open_rsp->one_oper,
                        open_rsp->two_oper,
                        open_rsp->xc_fun,
                        //id_outp,
                        size_residues,
                        residues);

//    break;
////* molecular orbital (MO) coefficient matrix-based response theory */
//case ELEC_MO_C_MATRIX:
//    break;
////* couple cluster-based response theory */
//case ELEC_COUPLED_CLUSTER:
//    break;
//default:
//    printf("OpenRSPGetResidue>> type of (electronic) wave function %d\n",
//           open_rsp->elec_wav_type);
//    QErrorExit(FILE_AND_LINE, "invalid type of (electronic) wave function");
//}
return QSUCCESS;
}

```

3.12 Fortran APIs

This section will implement APIs for Fortran users by using the Fortran ISO_C_BINDING.

We also plan to release this part of the OPENRSP under the GNU Lesser General Public License:

```
119a <OpenRSPLicenseFortran 119a>≡
!! OpenRSP: open-ended library for response theory
!! Copyright 2015 Radovan Bast,
!!           Daniel H. Friese,
!!           Bin Gao,
!!           Dan J. Jonsson,
!!           Magnus Ringholm,
!!           Kenneth Ruud,
!!           Andreas Thorvaldsen
!!
!! OpenRSP is free software: you can redistribute it and/or modify
!! it under the terms of the GNU Lesser General Public License as
!! published by the Free Software Foundation, either version 3 of
!! the License, or (at your option) any later version.
!!
!! OpenRSP is distributed in the hope that it will be useful,
!! but WITHOUT ANY WARRANTY; without even the implied warranty of
!! MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
!! GNU Lesser General Public License for more details.
!!
!! You should have received a copy of the GNU Lesser General Public
!! License along with OpenRSP. If not, see <http://www.gnu.org/licenses/>.
```

Here is the organization of the module file:

```
119b <OpenRSP.F90 119b>≡
!!
!! <QCLANG='Fortran'>
!! <para>
!!   Fortran users should use the module <OpenRSP_f> in their codes to access
!!   the functionalities of OpenRSP. We have used the same name for Fortran
!!   data types and constants, for instance <OpenRSP>; macro definitions are
!!   also controlled by the same names, such as <OPENRSP_USER_CONTEXT>; however
!!   all Fortran modules and functions are appended by <c>_f</c>.
!! </para>
!!
<OpenRSPLicenseFortran 119a>
!! <module name='OpenRSP_f' author='Bin Gao' date='2014-07-12'>
!!   The module file of OpenRSP library for Fortran users
!! </module>

! basic data types
#include "api/qcmatrix_c_type.h"

module OpenRSP_f

    use, intrinsic :: iso_c_binding
    use qcmatrix_f, only: QINT,      &
                        QREAL,      &
```

```

        QFAILURE, &
        QcMat, &
        QcMat_C_LOC
use RSPSolver_f, only: SolverFun_f, &
                      RSPSolverCreate_f, &
                      RSPSolverDestroy_f
use RSPPerturbation_f, only: QcPertInt, &
                             PertFun_f, &
                             RSPPertCreate_f, &
                             RSPPertDestroy_f
use RSPOverlap_f, only: OverlapFun_f, &
                       RSPOverlapCreate_f, &
                       RSPOverlapDestroy_f
use RSPOneOper_f, only: OneOperFun_f, &
                      RSPOneOperCreate_f, &
                      RSPOneOperDestroy_f
use RSPTwoOper_f, only: TwoOperFun_f, &
                      RSPTwoOperCreate_f, &
                      RSPTwoOperDestroy_f
use RSPXCFun_f, only: XCFunFun_f, &
                    RSPXCFunCreate_f, &
                    RSPXCFunDestroy_f
use RSPZeroOper_f, only: ZeroOperFun_f, &
                      RSPZeroOperCreate_f, &
                      RSPZeroOperDestroy_f

implicit none

! type of equation of motion (EOM) of electrons
integer(kind=QINT), parameter, public :: ELEC_AO_D_MATRIX = 0
integer(kind=QINT), parameter, public :: ELEC_MO_C_MATRIX = 1
integer(kind=QINT), parameter, public :: ELEC_COUPLED_CLUSTER = 2

! linked list of context of callback subroutines of zero-electron operators
type, private :: ZeroOperList_f
    type(ZeroOperFun_f), pointer :: zero_oper_fun => null()
    type(ZeroOperList_f), pointer :: next_zero_oper => null()
end type ZeroOperList_f

! linked list of context of callback subroutines of one-electron operators
type, private :: OneOperList_f
    type(OneOperFun_f), pointer :: one_oper_fun => null()
    type(OneOperList_f), pointer :: next_one_oper => null()
end type OneOperList_f

! linked list of context of callback subroutines of two-electron operators
type, private :: TwoOperList_f
    type(TwoOperFun_f), pointer :: two_oper_fun => null()
    type(TwoOperList_f), pointer :: next_two_oper => null()
end type TwoOperList_f

! linked list of context of callback subroutines of XC functionals

```



```

type, private :: XCFunList_f
  type(XCFunFun_f), pointer :: xcfun_fun => null()
  type(XCFunList_f), pointer :: next_xc_fun => null()
end type XCFunList_f

! OpenRSP type (inspired by http://wiki.rac.manchester.ac.uk/community/GPU/GpuFaq/FortranAPIs)
type, public :: OpenRSP
  private
    type(C_PTR) :: c_rsp = C_NULL_PTR
    type(SolverFun_f), pointer :: solver_fun => null()
    type(PertFun_f), pointer :: pert_fun => null()
    type(OverlapFun_f), pointer :: overlap_fun => null()
    type(OneOperList_f), pointer :: list_one_oper => null()
    type(TwoOperList_f), pointer :: list_two_oper => null()
    type(XCFunList_f), pointer :: list_xc_fun => null()
    type(ZeroOperList_f), pointer :: list_zero_oper => null()
  end type OpenRSP

! functions provided by the Fortran APIs
public :: OpenRSPCreate_f
!public :: OpenRSPSetElecEOM_f
public :: OpenRSPSetLinearRSPSolver_f
public :: OpenRSPSetPerturbations_f
public :: OpenRSPSetOverlap_f
public :: OpenRSPAddOneOper_f
public :: OpenRSPAddTwoOper_f
public :: OpenRSPAddXCFun_f
public :: OpenRSPAddZeroOper_f
public :: OpenRSPAssemble_f
public :: OpenRSPWrite_f
public :: OpenRSPGetRSPFun_f
public :: OpenRSPGetResidue_f
public :: OpenRSPDestroy_f

interface OpenRSPWrite_f
  module procedure OpenRSPWritebyFileName_f
  module procedure OpenRSPWritebyUnit_f
end interface OpenRSPWrite_f

interface
  integer(C_INT) function OpenRSPCreateFortranAdapter(open_rsp, &
                                                        num_atoms) &
    bind(C, name="OpenRSPCreateFortranAdapter")
    use, intrinsic :: iso_c_binding
    type(C_PTR), intent(inout) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_atoms
  end function OpenRSPCreateFortranAdapter
!integer(C_INT) function f_api_OpenRSPSetElecEOM(open_rsp, &
!                                                elec_EOM_type) &
!  bind(C, name="f_api_OpenRSPSetElecEOM")
!  use, intrinsic :: iso_c_binding
!  type(C_PTR), intent(inout) :: open_rsp

```

[illegible]

[illegible]

```

                                pert_max_orders,      &
                                user_ctx,              &
                                get_zero_oper_contrib) &

    bind(C, name="OpenRSPAddZeroOper")
    use, intrinsic :: iso_c_binding
    use RSPPertBasicTypes_f, only: C_QCPERTINT
    type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
    type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_zero_oper_contrib
end function OpenRSPAddZeroOper
integer(C_INT) function OpenRSPAssemble(open_rsp) &
    bind(C, name="OpenRSPAssemble")
    use, intrinsic :: iso_c_binding
    type(C_PTR), value, intent(in) :: open_rsp
end function OpenRSPAssemble
integer(C_INT) function OpenRSPWriteFortranAdapter(open_rsp, &
                                                    file_name) &
    bind(C, name="OpenRSPWriteFortranAdapter")
    use, intrinsic :: iso_c_binding
    type(C_PTR), value, intent(in) :: open_rsp
    character(C_CHAR), intent(in) :: file_name(*)
end function OpenRSPWriteFortranAdapter
integer(C_INT) function OpenRSPWriteStdOutFortranAdapter(open_rsp) &
    bind(C, name="OpenRSPWriteStdOutFortranAdapter")
    use, intrinsic :: iso_c_binding
    type(C_PTR), value, intent(in) :: open_rsp
end function OpenRSPWriteStdOutFortranAdapter
integer(C_INT) function OpenRSPGetRSPFun(open_rsp,      &
                                         ref_ham,      &
                                         ref_state,    &
                                         ref_overlap,   &
                                         num_props,     &
                                         len_tuple,     &
                                         pert_tuple,    &
                                         num_freq_configs, &
                                         pert_freqs,    &
                                         kn_rules,      &
                                         size_rsp_funs, &
                                         rsp_funs)      &
    bind(C, name="OpenRSPGetRSPFun")
    use, intrinsic :: iso_c_binding
    use RSPPertBasicTypes_f, only: C_QCPERTINT
    type(C_PTR), value, intent(in) :: open_rsp
    type(C_PTR), value, intent(in) :: ref_ham
    type(C_PTR), value, intent(in) :: ref_state
    type(C_PTR), value, intent(in) :: ref_overlap
    integer(kind=C_QINT), value, intent(in) :: num_props
    integer(kind=C_QINT), intent(in) :: len_tuple(num_props)
    integer(kind=C_QCPERTINT), intent(in) :: pert_tuple(sum(len_tuple))

```

```

integer(kind=C_QINT), intent(in) :: num_freq_configs(num_props)
real(kind=C_QREAL), intent(in) :: &
    pert_freqs(2*dot_product(len_tuple,num_freq_configs))
integer(kind=C_QINT), intent(in) :: kn_rules(num_props)
integer(kind=C_QINT), value, intent(in) :: size_rsp_funs
real(kind=C_QREAL), intent(out) :: rsp_funs(2*size_rsp_funs)
end function OpenRSPGetRSPFun
integer(C_INT) function OpenRSPGetResidue(open_rsp,      &
                                          ref_ham,      &
                                          ref_state,    &
                                          ref_overlap,   &
                                          order_residue, &
                                          num_excit,     &
                                          excit_energy,  &
                                          eigen_vector,  &
                                          num_props,     &
                                          len_tuple,     &
                                          pert_tuple,    &
                                          residue_num_pert, &
                                          residue_idx_pert, &
                                          num_freq_configs, &
                                          pert_freqs,    &
                                          kn_rules,      &
                                          size_residues,  &
                                          residues)      &

bind(C, name="OpenRSPGetResidue")
use, intrinsic :: iso_c_binding
use RSPPertBasicTypes_f, only: C_QCPERTINT
type(C_PTR), value, intent(in) :: open_rsp
type(C_PTR), value, intent(in) :: ref_ham
type(C_PTR), value, intent(in) :: ref_state
type(C_PTR), value, intent(in) :: ref_overlap
integer(kind=C_QINT), value, intent(in) :: order_residue
integer(kind=C_QINT), value, intent(in) :: num_excit
real(kind=C_QREAL), intent(in) :: excit_energy(order_residue*num_excit)
type(C_PTR), intent(in) :: eigen_vector(order_residue*num_excit)
integer(kind=C_QINT), value, intent(in) :: num_props
integer(kind=C_QINT), intent(in) :: len_tuple(num_props)
integer(kind=C_QCPERTINT), intent(in) :: pert_tuple(sum(len_tuple))
integer(kind=C_QINT), intent(in) :: residue_num_pert(order_residue*num_props)
integer(kind=C_QINT), intent(in) :: residue_idx_pert(sum(residue_num_pert))
integer(kind=C_QINT), intent(in) :: num_freq_configs(num_props)
real(kind=C_QREAL), intent(in) :: &
    pert_freqs(2*dot_product(len_tuple,num_freq_configs)*num_excit)
integer(kind=C_QINT), intent(in) :: kn_rules(num_props)
integer(kind=C_QINT), value, intent(in) :: size_residues
real(kind=C_QREAL), intent(out) :: residues(2*size_residues)
end function OpenRSPGetResidue
integer(C_INT) function OpenRSPDestroyFortranAdapter(open_rsp) &
bind(C, name="OpenRSPDestroyFortranAdapter")
use, intrinsic :: iso_c_binding
type(C_PTR), intent(inout) :: open_rsp

```

```

        end function OpenRSPDestroyFortranAdapter
    end interface

contains

function OpenRSPCreate_f(open_rsp, num_atoms) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    integer(kind=QINT), intent(in) :: num_atoms
    ierr = OpenRSPCreateFortranAdapter(open_rsp%c_rsp, num_atoms)
    nullify(open_rsp%solver_fun)
    nullify(open_rsp%pert_fun)
    nullify(open_rsp%overlap_fun)
    nullify(open_rsp%list_one_oper)
    nullify(open_rsp%list_two_oper)
    nullify(open_rsp%list_xc_fun)
    nullify(open_rsp%list_zero_oper)
end function OpenRSPCreate_f

!function OpenRSPSetElecEOM_f(open_rsp, elec_EOM_type) result(ierr)
!    integer(kind=4) :: ierr
!    type(OpenRSP), intent(inout) :: open_rsp
!    integer(kind=QINT), intent(in) :: elec_EOM_type
!    ierr = f_api_OpenRSPSetElecEOM(open_rsp%c_rsp, elec_EOM_type)
!end function OpenRSPSetElecEOM_f

function OpenRSPSetLinearRSPSolver_f(open_rsp,      &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,      &
#endif
                                get_linear_rsp_solution) result(ierr)

    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_linear_rsp_solution(num_pert,      &
                                            num_comps,      &
                                            num_freq_sums, &
                                            freq_sums,      &
                                            RHS_mat,      &
#if defined(OPENRSP_F_USER_CONTEXT)
                                            len_ctx,      &
                                            user_ctx,      &
#endif
                                            rsp_param)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            integer(kind=QINT), intent(in) :: num_pert
            integer(kind=QINT), intent(in) :: num_comps(num_pert)
            integer(kind=QINT), intent(in) :: num_freq_sums(num_pert)
            real(kind=QREAL), intent(in) :: freq_sums(2*sum(num_freq_sums))

```

```

        type(QcMat), intent(in) :: RHS_mat(dot_product(num_comps,num_freq_sums))
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        type(QcMat), intent(inout) :: rsp_param(dot_product(num_comps,num_freq_sums))
end subroutine get_linear_rsp_solution
subroutine RSPSolverGetLinearRSPSolution_f(num_pert,      &
                                           num_comps,    &
                                           num_freq_sums, &
                                           freq_sums,     &
                                           RHS_mat,       &
                                           user_ctx,      &
                                           rsp_param)     &

    bind(C, name="RSPSolverGetLinearRSPSolution_f")
    use, intrinsic :: iso_c_binding
    integer(kind=C_QINT), value, intent(in) :: num_pert
    integer(kind=C_QINT), intent(in) :: num_comps(num_pert)
    integer(kind=C_QINT), intent(in) :: num_freq_sums(num_pert)
    real(kind=C_QREAL), intent(in) :: freq_sums(2*sum(num_freq_sums))
    type(C_PTR), intent(in) :: RHS_mat(dot_product(num_comps,num_freq_sums))
    type(C_PTR), value, intent(in) :: user_ctx
    type(C_PTR), intent(in) :: rsp_param(dot_product(num_comps,num_freq_sums))
end subroutine RSPSolverGetLinearRSPSolution_f
end interface
if (associated(open_rsp%solver_fun)) then
    call RSPSolverDestroy_f(open_rsp%solver_fun)
else
    allocate(open_rsp%solver_fun)
end if
! adds context of callback function of response equation solver
call RSPSolverCreate_f(open_rsp%solver_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx,      &
#endif
    get_linear_rsp_solution)
ierr = OpenRSPSetLinearRSPSolver(open_rsp%c_rsp,      &
                                c_loc(open_rsp%solver_fun), &
                                c_funloc(RSPSolverGetLinearRSPSolution_f))
end function OpenRSPSetLinearRSPSolver_f

function OpenRSPSetPerturbations_f(open_rsp,      &
                                    num_pert_lab,  &
                                    pert_labels,   &
                                    pert_max_orders, &
                                    pert_num_comps, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx,      &
#endif
    get_pert_concatenation) result(ierr)

    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp

```

```

integer(kind=QINT), intent(in) :: num_pert_lab
integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
integer(kind=QINT), intent(in) :: pert_num_comps(:)
#if defined(OPENRSP_F_USER_CONTEXT)
character(len=1), intent(in) :: user_ctx(:)
#endif

interface
  subroutine get_pert_concatenation(pert_label,      &
                                   first_cat_comp, &
                                   num_cat_comps,   &
                                   num_sub_tuples, &
                                   len_sub_tuples, &

#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx,        &
                                   user_ctx,       &

#endif
                                   rank_sub_comps)

    use qcmatrix_f, only: QINT
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QcPertInt), intent(in) :: pert_label
    integer(kind=QINT), intent(in) :: first_cat_comp
    integer(kind=QINT), intent(in) :: num_cat_comps
    integer(kind=QINT), intent(in) :: num_sub_tuples
    integer(kind=QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

    integer(kind=QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_co
end subroutine get_pert_concatenation
subroutine RSPPertGetConcatenation_f(pert_label,      &
                                   first_cat_comp, &
                                   num_cat_comps,   &
                                   num_sub_tuples, &
                                   len_sub_tuples, &
                                   user_ctx,       &
                                   rank_sub_comps) &

  bind(C, name="RSPPertGetConcatenation_f")
  use, intrinsic :: iso_c_binding
  use RSPPertBasicTypes_f, only: C_QCPERTINT
  integer(kind=C_QCPERTINT), value, intent(in) :: pert_label
  integer(kind=C_QINT), value, intent(in) :: first_cat_comp
  integer(kind=C_QINT), value, intent(in) :: num_cat_comps
  integer(kind=C_QINT), value, intent(in) :: num_sub_tuples
  integer(kind=C_QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
  type(C_PTR), value, intent(in) :: user_ctx
  integer(kind=C_QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_
end subroutine RSPPertGetConcatenation_f
end interface
if (associated(open_rsp%pert_fun)) then
  call RSPPertDestroy_f(open_rsp%pert_fun)

```



```

    else
        allocate(open_rsp%pert_fun)
    end if
    ! adds context of callback functions of perturbations
    call RSPPertCreate_f(open_rsp%pert_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
        user_ctx,          &
#endif
        get_pert_concatenation)
    ierr = OpenRSPSetPerturbations(open_rsp%c_rsp,      &
        num_pert_lab,      &
        pert_labels,      &
        pert_max_orders,  &
        pert_num_comps,   &
        c_loc(open_rsp%pert_fun), &
        c_funloc(RSPPertGetConcatenation_f))
end function OpenRSPSetPerturbations_f

function OpenRSPSetOverlap_f(open_rsp,      &
    num_pert_lab,      &
    pert_labels,      &
    pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx,          &
#endif
    get_overlap_mat, &
    get_overlap_exp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    integer(kind=QINT), intent(in) :: num_pert_lab
    integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_overlap_mat(bra_num_pert,      &
            bra_pert_labels,      &
            bra_pert_orders,      &
            ket_num_pert,          &
            ket_pert_labels,      &
            ket_pert_orders,      &
            oper_num_pert,        &
            oper_pert_labels,      &
            oper_pert_orders,      &
#if defined(OPENRSP_F_USER_CONTEXT)
            len_ctx,              &
            user_ctx,            &
#endif
            num_int,              &
            val_int)
        use qcmatrix_f, only: QINT,QREAL,QcMat
    end subroutine
end function

```

```

        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: bra_num_pert
        integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
        integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
        integer(kind=QINT), intent(in) :: ket_num_pert
        integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
        integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    #if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
    #endif

        integer(kind=QINT), intent(in) :: num_int
        type(QcMat), intent(inout) :: val_int(num_int)
    end subroutine get_overlap_mat
    subroutine get_overlap_exp(bra_num_pert,      &
                               bra_pert_labels,  &
                               bra_pert_orders,  &
                               ket_num_pert,     &
                               ket_pert_labels,  &
                               ket_pert_orders,  &
                               oper_num_pert,    &
                               oper_pert_labels, &
                               oper_pert_orders, &
                               num_dmat,         &
                               dens_mat,         &
    #if defined(OPENRSP_F_USER_CONTEXT)
                               len_ctx,          &
                               user_ctx,         &
    #endif
                               num_exp,          &
                               val_exp)

    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: bra_num_pert
    integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
    integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
    integer(kind=QINT), intent(in) :: ket_num_pert
    integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
    integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    integer(kind=QINT), intent(in) :: num_dmat
    type(QcMat), intent(in) :: dens_mat(num_dmat)
    #if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
    #endif

    integer(kind=QINT), intent(in) :: num_exp

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```

      real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine get_overlap_exp
subroutine RSPOverlapGetMat_f(bra_num_pert,      &
                             bra_pert_labels,  &
                             bra_pert_orders,  &
                             ket_num_pert,      &
                             ket_pert_labels,  &
                             ket_pert_orders,  &
                             oper_num_pert,    &
                             oper_pert_labels, &
                             oper_pert_orders, &
                             user_ctx,         &
                             num_int,          &
                             val_int)         &
  bind(C, name="RSPOverlapGetMat_f")
  use, intrinsic :: iso_c_binding
  use RSPPertBasicTypes_f, only: C_QCPERTINT
  integer(kind=C_QINT), value, intent(in) :: bra_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
  integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
  integer(kind=C_QINT), value, intent(in) :: ket_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
  integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
  integer(kind=C_QINT), value, intent(in) :: oper_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
  integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
  type(C_PTR), value, intent(in) :: user_ctx
  integer(kind=C_QINT), value, intent(in) :: num_int
  type(C_PTR), intent(inout) :: val_int(num_int)
end subroutine RSPOverlapGetMat_f
subroutine RSPOverlapGetExp_f(bra_num_pert,      &
                              bra_pert_labels,  &
                              bra_pert_orders,  &
                              ket_num_pert,      &
                              ket_pert_labels,  &
                              ket_pert_orders,  &
                              oper_num_pert,    &
                              oper_pert_labels, &
                              oper_pert_orders, &
                              num_dmat,         &
                              dens_mat,         &
                              user_ctx,         &
                              num_exp,          &
                              val_exp)         &
  bind(C, name="RSPOverlapGetExp_f")
  use, intrinsic :: iso_c_binding
  use RSPPertBasicTypes_f, only: C_QCPERTINT
  integer(kind=C_QINT), value, intent(in) :: bra_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
  integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
  integer(kind=C_QINT), value, intent(in) :: ket_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)

```

```

        integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine RSPOverlapGetExp_f
end interface
if (associated(open_rsp%overlap_fun)) then
    call RSPOverlapDestroy_f(open_rsp%overlap_fun)
else
    allocate(open_rsp%overlap_fun)
end if
! adds context of callback functions of the overlap integrals
call RSPOverlapCreate_f(open_rsp%overlap_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_overlap_mat, &
    get_overlap_exp)
ierr = OpenRSPSetOverlap(open_rsp%c_rsp, &
    num_pert_lab, &
    pert_labels, &
    pert_max_orders, &
    c_loc(open_rsp%overlap_fun), &
    c_funloc(RSPOverlapGetMat_f), &
    c_funloc(RSPOverlapGetExp_f))
end function OpenRSPSetOverlap_f

function OpenRSPAddOneOper_f(open_rsp, &
    num_pert_lab, &
    pert_labels, &
    pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_one_oper_mat, &
    get_one_oper_exp) result(ierr)
integer(kind=4) :: ierr
type(OpenRSP), intent(inout) :: open_rsp
integer(kind=QINT), intent(in) :: num_pert_lab
integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
character(len=1), intent(in) :: user_ctx(:)
#endif
interface
    subroutine get_one_oper_mat(oper_num_pert, &
        oper_pert_labels, &

```

```

                                oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                len_ctx,          &
                                user_ctx,          &
#endif
                                num_int,          &
                                val_int)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
    integer(kind=QINT), intent(in) :: num_int
    type(QcMat), intent(inout) :: val_int(num_int)
end subroutine get_one_oper_mat
subroutine get_one_oper_exp(oper_num_pert,      &
                            oper_pert_labels, &
                            oper_pert_orders, &
                            num_dmat,         &
                            dens_mat,         &
#if defined(OPENRSP_F_USER_CONTEXT)
                            len_ctx,          &
                            user_ctx,          &
#endif
                            num_exp,          &
                            val_exp)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    integer(kind=QINT), intent(in) :: num_dmat
    type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
    integer(kind=QINT), intent(in) :: num_exp
    real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine get_one_oper_exp
subroutine RSPOneOperGetMat_f(oper_num_pert,      &
                              oper_pert_labels, &
                              oper_pert_orders, &
                              user_ctx,          &
                              num_int,          &
                              val_int)          &
    bind(C, name="RSPOneOperGetMat_f")
    use, intrinsic :: iso_c_binding

```

```

        use RSPPertBasicTypes_f, only: C_QCPERTINT
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_int
        type(C_PTR), intent(inout) :: val_int(num_int)
    end subroutine RSPOneOperGetMat_f
    subroutine RSPOneOperGetExp_f(oper_num_pert,      &
                                oper_pert_labels, &
                                oper_pert_orders, &
                                num_dmat,         &
                                dens_mat,         &
                                user_ctx,         &
                                num_exp,          &
                                val_exp)          &
        bind(C, name="RSPOneOperGetExp_f")
        use, intrinsic :: iso_c_binding
        use RSPPertBasicTypes_f, only: C_QCPERTINT
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine RSPOneOperGetExp_f
end interface
type(OneOperList_f), pointer :: cur_one_oper !current one-electron operator
! inserts the context of callback functions to the tail of the linked list
if (associated(open_rsp%list_one_oper)) then
    cur_one_oper => open_rsp%list_one_oper
    do while (associated(cur_one_oper%next_one_oper))
        cur_one_oper => cur_one_oper%next_one_oper
    end do
    allocate(cur_one_oper%next_one_oper)
    cur_one_oper => cur_one_oper%next_one_oper
else
    allocate(open_rsp%list_one_oper)
    cur_one_oper => open_rsp%list_one_oper
end if
allocate(cur_one_oper%one_oper_fun)
nullify(cur_one_oper%next_one_oper)
! adds context of callback functions of the new one-electron operator
call RSPOneOperCreate_f(cur_one_oper%one_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,          &
#endif
                                get_one_oper_mat,    &
                                get_one_oper_exp)
ierr = OpenRSPAddOneOper(open_rsp%c_rsp,          &

```

```

        num_pert_lab,          &
        pert_labels,          &
        pert_max_orders,      &
        c_loc(cur_one_oper%one_oper_fun), &
        c_funloc(RSPOneOperGetMat_f),    &
        c_funloc(RSPOneOperGetExp_f))
end function OpenRSPAddOneOper_f

function OpenRSPAddTwoOper_f(open_rsp,      &
                             num_pert_lab,  &
                             pert_labels,   &
                             pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                             user_ctx,      &
#endif
                             get_two_oper_mat, &
                             get_two_oper_exp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    integer(kind=QINT), intent(in) :: num_pert_lab
    integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_two_oper_mat(oper_num_pert,      &
                                    oper_pert_labels, &
                                    oper_pert_orders, &
                                    num_dmat,          &
                                    dens_mat,          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                    len_ctx,          &
                                    user_ctx,          &
#endif
                                    num_int,          &
                                    val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int
            type(QcMat), intent(inout) :: val_int(num_int)
        end subroutine get_two_oper_mat
        subroutine get_two_oper_exp(oper_num_pert,      &

```



```

                                oper_pert_orders, &
                                dmat_len_tuple,   &
                                num_LHS_dmat,     &
                                LHS_dens_mat,     &
                                num_RHS_dmat,     &
                                RHS_dens_mat,     &
                                user_ctx,        &
                                num_exp,         &
                                val_exp)         &
    bind(C, name="RSPTwoOperGetExp_f")
    use, intrinsic :: iso_c_binding
    use RSPPertBasicTypes_f, only: C_QCPERTINT
    integer(kind=C_QINT), value, intent(in) :: oper_num_pert
    integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    integer(kind=C_QINT), value, intent(in) :: dmat_len_tuple
    integer(kind=C_QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
    type(C_PTR), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
    integer(kind=C_QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
    type(C_PTR), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
    type(C_PTR), value, intent(in) :: user_ctx
    integer(kind=C_QINT), value, intent(in) :: num_exp
    real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine RSPTwoOperGetExp_f
end interface
type(TwoOperList_f), pointer :: cur_two_oper !current two-electron operator
! inserts the context of callback functions to the tail of the linked list
if (associated(open_rsp%list_two_oper)) then
    cur_two_oper => open_rsp%list_two_oper
    do while (associated(cur_two_oper%next_two_oper))
        cur_two_oper => cur_two_oper%next_two_oper
    end do
    allocate(cur_two_oper%next_two_oper)
    cur_two_oper => cur_two_oper%next_two_oper
else
    allocate(open_rsp%list_two_oper)
    cur_two_oper => open_rsp%list_two_oper
end if
allocate(cur_two_oper%two_oper_fun)
nullify(cur_two_oper%next_two_oper)
! adds context of callback functions of the new two-electron operator
call RSPTwoOperCreate_f(cur_two_oper%two_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,        &
#endif
                                get_two_oper_mat,   &
                                get_two_oper_exp)
ierr = OpenRSPAddTwoOper(open_rsp%c_rsp, &
                                num_pert_lab,      &
                                pert_labels,       &
                                pert_max_orders,   &
                                c_loc(cur_two_oper%two_oper_fun), &

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        c_funloc(RSPTwoOperGetMat_f),      &
        c_funloc(RSPTwoOperGetExp_f))
end function OpenRSPAddTwoOper_f

function OpenRSPAddXCFun_f(open_rsp,      &
                           num_pert_lab,  &
                           pert_labels,   &
                           pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                           user_ctx,      &
#endif
                           get_xc_fun_mat, &
                           get_xc_fun_exp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    integer(kind=QINT), intent(in) :: num_pert_lab
    integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_xc_fun_mat(xc_len_tuple,      &
                                   xc_pert_tuple,     &
                                   num_freq_configs,  &
                                   pert_freq_category, &
                                   dmat_num_tuple,    &
                                   dmat_idx_tuple,    &
                                   num_dmat,          &
                                   dens_mat,          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx,           &
                                   user_ctx,          &
#endif
                                   num_int,           &
                                   val_int)
            use qcmatrix_f, only: QINT, QREAL, QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: xc_len_tuple
            integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
            integer(kind=QINT), intent(in) :: num_freq_configs
            integer(kind=QINT), intent(in) :: &
                pert_freq_category(num_freq_configs*xc_len_tuple)
            integer(kind=QINT), intent(in) :: dmat_num_tuple
            integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int

```

```

        type(QcMat), intent(inout) :: val_int(num_int)
    end subroutine get_xc_fun_mat
    subroutine get_xc_fun_exp(xc_len_tuple,      &
                             xc_pert_tuple,     &
                             num_freq_configs,  &
                             pert_freq_category, &
                             dmat_num_tuple,    &
                             dmat_idx_tuple,    &
                             num_dmat,         &
                             dens_mat,         &
    #if defined(OPENRSP_F_USER_CONTEXT)
                             len_ctx,          &
                             user_ctx,         &
    #endif
                             num_exp,          &
                             val_exp)
        use qcmatrix_f, only: QINT,QREAL,QcMat
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: xc_len_tuple
        integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
        integer(kind=QINT), intent(in) :: num_freq_configs
        integer(kind=QINT), intent(in) :: &
            pert_freq_category(num_freq_configs*xc_len_tuple)
        integer(kind=QINT), intent(in) :: dmat_num_tuple
        integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=QINT), intent(in) :: num_dmat
        type(QcMat), intent(in) :: dens_mat(num_dmat)
    #if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
    #endif

        integer(kind=QINT), intent(in) :: num_exp
        real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine get_xc_fun_exp
    subroutine RSPXCFunGetMat_f(xc_len_tuple,      &
                                xc_pert_tuple,     &
                                num_freq_configs,  &
                                pert_freq_category, &
                                dmat_num_tuple,    &
                                dmat_idx_tuple,    &
                                num_dmat,         &
                                dens_mat,         &
                                user_ctx,         &
                                num_int,          &
                                val_int)         &
        bind(C, name="RSPXCFunGetMat_f")
        use, intrinsic :: iso_c_binding
        use RSPPertBasicTypes_f, only: C_QCPERTINT
        integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
        integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_freq_configs
        integer(kind=C_QINT), intent(in) :: &

```

```

        pert_freq_category(num_freq_configs*xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
        integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_int
        type(C_PTR), intent(inout) :: val_int(num_int)
    end subroutine RSPXCFunGetMat_f
    subroutine RSPXCFunGetExp_f(xc_len_tuple,      &
                                xc_pert_tuple,      &
                                num_freq_configs,    &
                                pert_freq_category,  &
                                dmat_num_tuple,      &
                                dmat_idx_tuple,      &
                                num_dmat,            &
                                dens_mat,            &
                                user_ctx,            &
                                num_exp,            &
                                val_exp)            &
        bind(C, name="RSPXCFunGetExp_f")
        use, intrinsic :: iso_c_binding
        use RSPPertBasicTypes_f, only: C_QCPERTINT
        integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
        integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_freq_configs
        integer(kind=C_QINT), intent(in) :: &
            pert_freq_category(num_freq_configs*xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
        integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine RSPXCFunGetExp_f
end interface
type(XCFunList_f), pointer :: cur_xc_fun !current XC functional
! inserts the context of callback functions to the tail of the linked list
if (associated(open_rsp%list_xc_fun)) then
    cur_xc_fun => open_rsp%list_xc_fun
    do while (associated(cur_xc_fun%next_xc_fun))
        cur_xc_fun => cur_xc_fun%next_xc_fun
    end do
    allocate(cur_xc_fun%next_xc_fun)
    cur_xc_fun => cur_xc_fun%next_xc_fun
else
    allocate(open_rsp%list_xc_fun)
    cur_xc_fun => open_rsp%list_xc_fun
end if
allocate(cur_xc_fun%xcfun_fun)
nullify(cur_xc_fun%next_xc_fun)

```

```

! adds context of callback functions of the new XC functional
call RSPXCFunCreate_f(cur_xc_fun%xcfun_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_xc_fun_mat, &
    get_xc_fun_exp)
ierr = OpenRSPAddXCFun(open_rsp%c_rsp, &
    num_pert_lab, &
    pert_labels, &
    pert_max_orders, &
    c_loc(cur_xc_fun%xcfun_fun), &
    c_funloc(RSPXCFunGetMat_f), &
    c_funloc(RSPXCFunGetExp_f))
end function OpenRSPAddXCFun_f

function OpenRSPAddZeroOper_f(open_rsp, &
    num_pert_lab, &
    pert_labels, &
    pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_zero_oper_contrib) result(ierr)
integer(kind=4) :: ierr
type(OpenRSP), intent(inout) :: open_rsp
integer(kind=QINT), intent(in) :: num_pert_lab
integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
character(len=1), intent(in) :: user_ctx(:)
#endif
interface
    subroutine get_zero_oper_contrib(oper_num_pert, &
        oper_pert_labels, &
        oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
        len_ctx, &
        user_ctx, &
#endif
        size_pert, &
        val_oper)
        use qcmatrix_f, only: QINT,QREAL
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    end subroutine
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
    integer(kind=QINT), intent(in) :: size_pert

```

```

        real(kind=QREAL), intent(inout) :: val_oper(2*size_pert)
    end subroutine get_zero_oper_contrib
    subroutine RSPZeroOperGetContribution_f(oper_num_pert,      &
                                           oper_pert_labels, &
                                           oper_pert_orders, &
                                           user_ctx,          &
                                           size_pert,          &
                                           val_oper)           &

        bind(C, name="RSPZeroOperGetContribution_f")
        use, intrinsic :: iso_c_binding
        use RSPPertBasicTypes_f, only: C_QCPERTINT
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: size_pert
        real(kind=C_QREAL), intent(inout) :: val_oper(2*size_pert)
    end subroutine RSPZeroOperGetContribution_f
end interface
type(ZeroOperList_f), pointer :: cur_zero_oper !current zero-electron operator
! inserts the context of callback functions to the tail of the linked list
if (associated(open_rsp%list_zero_oper)) then
    cur_zero_oper => open_rsp%list_zero_oper
    do while (associated(cur_zero_oper%next_zero_oper))
        cur_zero_oper => cur_zero_oper%next_zero_oper
    end do
    allocate(cur_zero_oper%next_zero_oper)
    cur_zero_oper => cur_zero_oper%next_zero_oper
else
    allocate(open_rsp%list_zero_oper)
    cur_zero_oper => open_rsp%list_zero_oper
end if
allocate(cur_zero_oper%zero_oper_fun)
nullify(cur_zero_oper%next_zero_oper)
! adds context of callback function of the new zero-electron operator
call RSPZeroOperCreate_f(cur_zero_oper%zero_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_zero_oper_contrib)
ierr = OpenRSPAddZeroOper(open_rsp%c_rsp, &
    num_pert_lab, &
    pert_labels, &
    pert_max_orders, &
    c_loc(cur_zero_oper%zero_oper_fun), &
    c_funloc(RSPZeroOperGetContribution_f))
end function OpenRSPAddZeroOper_f

function OpenRSPAssemble_f(open_rsp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    ierr = OpenRSPAssemble(open_rsp%c_rsp)

```

```

end function OpenRSPAssemble_f

function OpenRSPWritebyFileName_f(open_rsp, file_name) result(ierr)
  integer(kind=4) :: ierr
  type(OpenRSP), intent(in) :: open_rsp
  character(*), intent(in) :: file_name
  ierr = OpenRSPWriteFortranAdapter(open_rsp%c_rsp, &
                                     file_name//C_NULL_CHAR)
end function OpenRSPWritebyFileName_f

function OpenRSPWritebyUnit_f(open_rsp, io_unit) result(ierr)
  integer(kind=4) :: ierr
  type(OpenRSP), intent(in) :: open_rsp
  integer(kind=4), intent(in) :: io_unit
integer(kind=4), parameter :: MAX_LEN_QCCHAR = 256
integer(kind=4), parameter :: QCSTDOUT = 6
  logical(kind=4) is_opened
  logical(kind=4) is_named
  character(MAX_LEN_QCCHAR) file_name
  if (io_unit==QCSTDOUT) then
    ierr = OpenRSPWriteStdOutFortranAdapter(open_rsp%c_rsp)
  else
    ! gets the file name from its associated logical unit
    inquire(unit=io_unit,      &
            opened=is_opened, &
            named=is_named,   &
            name=file_name)
    if (is_opened .and. is_named) then
      if (len_trim(file_name)==MAX_LEN_QCCHAR) then
        write(QCSTDOUT,100) "file name too long, increase MAX_LEN_QCCHAR", &
                           MAX_LEN_QCCHAR
        call QErrorExit(QCSTDOUT, __LINE__, "OpenRSP.F90")
      else
        ! writes by file name
        ierr = OpenRSPWriteFortranAdapter(open_rsp%c_rsp, &
                                           trim(file_name)//C_NULL_CHAR)
      end if
    else
      write(QCSTDOUT,100) "logical unit is not named and/or opened", &
                        io_unit
      call QErrorExit(QCSTDOUT, __LINE__, "OpenRSP.F90")
    end if
  end if
100  format("OpenRSPWritebyUnit_f>> ",A,I6)
end function OpenRSPWritebyUnit_f

function OpenRSPGetRSPFun_f(open_rsp,      &
                             ref_ham,      &
                             ref_state,    &
                             ref_overlap,  &
                             num_props,    &
                             len_tuple,    &

```

```

        pert_tuple,      &
        num_freq_configs, &
        pert_freqs,      &
        kn_rules,         &
        size_rsp_funs,    &
        rsp_funs) result(ierr)

integer(kind=4) :: ierr
type(OpenRSP), intent(in) :: open_rsp
type(QcMat), target, intent(in) :: ref_ham
type(QcMat), target, intent(in) :: ref_state
type(QcMat), target, intent(in) :: ref_overlap
integer(kind=QINT), intent(in) :: num_props
integer(kind=QINT), intent(in) :: len_tuple(num_props)
integer(kind=QcPertInt), intent(in) :: pert_tuple(sum(len_tuple))
integer(kind=QINT), intent(in) :: num_freq_configs(num_props)
real(kind=QREAL), intent(in) :: &
    pert_freqs(2*dot_product(len_tuple,num_freq_configs))
integer(kind=QINT), intent(in) :: kn_rules(num_props)
integer(kind=QINT), intent(in) :: size_rsp_funs
real(kind=QREAL), intent(out) :: rsp_funs(2*size_rsp_funs)
type(C_PTR) c_ref_ham(1)
type(C_PTR) c_ref_state(1)
type(C_PTR) c_ref_overlap(1)
ierr = QcMat_C_LOC((/ref_ham/), c_ref_ham)
if (ierr==QFAILURE) return
ierr = QcMat_C_LOC((/ref_state/), c_ref_state)
if (ierr==QFAILURE) return
ierr = QcMat_C_LOC((/ref_overlap/), c_ref_overlap)
if (ierr==QFAILURE) return
ierr = OpenRSPGetRSPFun(open_rsp%c_rsp,      &
    c_ref_ham(1),      &
    c_ref_state(1),    &
    c_ref_overlap(1),  &
    num_props,         &
    len_tuple,         &
    pert_tuple,        &
    num_freq_configs,  &
    pert_freqs,        &
    kn_rules,          &
    size_rsp_funs,     &
    rsp_funs)

c_ref_ham(1) = C_NULL_PTR
c_ref_state(1) = C_NULL_PTR
c_ref_overlap(1) = C_NULL_PTR
end function OpenRSPGetRSPFun_f

function OpenRSPGetResidue_f(open_rsp,      &
    ref_ham,      &
    ref_state,    &
    ref_overlap,  &
    order_residue, &
    num_excit,    &

```



```

        excit_energy,      &
        eigen_vector,      &
        num_props,         &
        len_tuple,         &
        pert_tuple,        &
        residue_num_pert,  &
        residue_idx_pert,  &
        num_freq_configs,  &
        pert_freqs,        &
        kn_rules,          &
        size_residues,     &
        residues) result(ierr)

integer(kind=4) :: ierr
type(OpenRSP), intent(in) :: open_rsp
type(QcMat), target, intent(in) :: ref_ham
type(QcMat), target, intent(in) :: ref_state
type(QcMat), target, intent(in) :: ref_overlap
integer(kind=QINT), intent(in) :: order_residue
integer(kind=QINT), intent(in) :: num_excit
real(kind=QREAL), intent(in) :: excit_energy(order_residue*num_excit)
type(QcMat), intent(in) :: eigen_vector(order_residue*num_excit)
integer(kind=QINT), intent(in) :: num_props
integer(kind=QINT), intent(in) :: len_tuple(num_props)
integer(kind=QcPertInt), intent(in) :: pert_tuple(sum(len_tuple))
integer(kind=QINT), intent(in) :: residue_num_pert(order_residue*num_props)
integer(kind=QINT), intent(in) :: residue_idx_pert(sum(residue_num_pert))
integer(kind=QINT), intent(in) :: num_freq_configs(num_props)
real(kind=QREAL), intent(in) :: &
    pert_freqs(2*dot_product(len_tuple,num_freq_configs)*num_excit)
integer(kind=QINT), intent(in) :: kn_rules(num_props)
integer(kind=QINT), intent(in) :: size_residues
real(kind=QREAL), intent(out) :: residues(2*size_residues)
type(C_PTR) c_ref_ham(1)
type(C_PTR) c_ref_state(1)
type(C_PTR) c_ref_overlap(1)
type(C_PTR), allocatable :: c_eigen_vector(:)
integer(kind=QINT) iext
ierr = QcMat_C_LOC((/ref_ham/), c_ref_ham)
if (ierr==QFAILURE) return
ierr = QcMat_C_LOC((/ref_state/), c_ref_state)
if (ierr==QFAILURE) return
ierr = QcMat_C_LOC((/ref_overlap/), c_ref_overlap)
if (ierr==QFAILURE) return
allocate(c_eigen_vector(order_residue*num_excit), stat=ierr)
if (ierr/=0) return
ierr = QcMat_C_LOC(eigen_vector, c_eigen_vector)
if (ierr==QFAILURE) return
ierr = OpenRSPGetResidue(open_rsp%c_rsp,      &
    c_ref_ham(1),      &
    c_ref_state(1),    &
    c_ref_overlap(1),  &
    order_residue,     &

```

```

        num_excit,      &
        excit_energy,   &
        c_eigen_vector, &
        num_props,      &
        len_tuple,      &
        pert_tuple,     &
        residue_num_pert, &
        residue_idx_pert, &
        num_freq_configs, &
        pert_freqs,     &
        kn_rules,       &
        size_residues,  &
        residues)

c_ref_ham(1) = C_NULL_PTR
c_ref_state(1) = C_NULL_PTR
c_ref_overlap(1) = C_NULL_PTR
do iext = 1, order_residue*num_excit
    c_eigen_vector(iext) = C_NULL_PTR
end do
deallocate(c_eigen_vector)
end function OpenRSPGetResidue_f

function OpenRSPDestroy_f(open_rsp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    type(OneOperList_f), pointer :: cur_one_oper      !current one-electron operator
    type(OneOperList_f), pointer :: next_one_oper     !next one-electron operator
    type(TwoOperList_f), pointer :: cur_two_oper      !current two-electron operator
    type(TwoOperList_f), pointer :: next_two_oper     !next two-electron operator
    type(XCFunList_f), pointer :: cur_xc_fun          !current XC functional
    type(XCFunList_f), pointer :: next_xc_fun         !next XC functional
    type(ZeroOperList_f), pointer :: cur_zero_oper    !current zero-electron operator
    type(ZeroOperList_f), pointer :: next_zero_oper   !next zero-electron operator
    ierr = OpenRSPDestroyFortranAdapter(open_rsp%c_rsp)
    ! cleans up callback subroutine of response equation solver
    if (associated(open_rsp%solver_fun)) then
        call RSPSolverDestroy_f(open_rsp%solver_fun)
        deallocate(open_rsp%solver_fun)
        nullify(open_rsp%solver_fun)
    end if
    ! cleans up callback subroutines of perturbations
    if (associated(open_rsp%pert_fun)) then
        call RSPPertDestroy_f(open_rsp%pert_fun)
        deallocate(open_rsp%pert_fun)
        nullify(open_rsp%pert_fun)
    end if
    ! cleans up callback subroutines of overlap integrals
    if (associated(open_rsp%overlap_fun)) then
        call RSPOverlapDestroy_f(open_rsp%overlap_fun)
        deallocate(open_rsp%overlap_fun)
        nullify(open_rsp%overlap_fun)
    end if
end function

```

```

! cleans up the linked list of context of callback subroutines of one-electron oper
cur_one_oper => open_rsp%list_one_oper
do while (associated(cur_one_oper))
  next_one_oper => cur_one_oper%next_one_oper
  if (associated(cur_one_oper%one_oper_fun)) then
    call RSPOneOperDestroy_f(cur_one_oper%one_oper_fun)
    deallocate(cur_one_oper%one_oper_fun)
    nullify(cur_one_oper%one_oper_fun)
  end if
  deallocate(cur_one_oper)
  nullify(cur_one_oper)
  cur_one_oper => next_one_oper
end do

! cleans up the linked list of context of callback subroutines of two-electron oper
cur_two_oper => open_rsp%list_two_oper
do while (associated(cur_two_oper))
  next_two_oper => cur_two_oper%next_two_oper
  if (associated(cur_two_oper%two_oper_fun)) then
    call RSPTwoOperDestroy_f(cur_two_oper%two_oper_fun)
    deallocate(cur_two_oper%two_oper_fun)
    nullify(cur_two_oper%two_oper_fun)
  end if
  deallocate(cur_two_oper)
  nullify(cur_two_oper)
  cur_two_oper => next_two_oper
end do

! cleans up the linked list of context of callback subroutines of XC functionals
cur_xc_fun => open_rsp%list_xc_fun
do while (associated(cur_xc_fun))
  next_xc_fun => cur_xc_fun%next_xc_fun
  if (associated(cur_xc_fun%xcfun_fun)) then
    call RSPXCFunDestroy_f(cur_xc_fun%xcfun_fun)
    deallocate(cur_xc_fun%xcfun_fun)
    nullify(cur_xc_fun%xcfun_fun)
  end if
  deallocate(cur_xc_fun)
  nullify(cur_xc_fun)
  cur_xc_fun => next_xc_fun
end do

! cleans up the linked list of context of callback subroutines of zero-electron oper
cur_zero_oper => open_rsp%list_zero_oper
do while (associated(cur_zero_oper))
  next_zero_oper => cur_zero_oper%next_zero_oper
  if (associated(cur_zero_oper%zero_oper_fun)) then
    call RSPZeroOperDestroy_f(cur_zero_oper%zero_oper_fun)
    deallocate(cur_zero_oper%zero_oper_fun)
    nullify(cur_zero_oper%zero_oper_fun)
  end if
  deallocate(cur_zero_oper)
  nullify(cur_zero_oper)
  cur_zero_oper => next_zero_oper
end do

```



```

#if defined(OPENRSP_F_USER_CONTEXT)
                                len_ctx,          &
                                user_ctx,          &
#endif

                                rank_sub_comps)

    use qcmatrix_f, only: QINT
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QcPertInt), intent(in) :: pert_label
    integer(kind=QINT), intent(in) :: first_cat_comp
    integer(kind=QINT), intent(in) :: num_cat_comps
    integer(kind=QINT), intent(in) :: num_sub_tuples
    integer(kind=QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
    integer(kind=QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_comps)
end subroutine GetPertConcatenation_f
end interface

! context of callback subroutine of response equation solver
type, public :: PertFun_f
    private
#if defined(OPENRSP_F_USER_CONTEXT)
    ! user-defined callback function context
    integer(kind=QINT) :: len_ctx = 0
    character(len=1), allocatable :: user_ctx(:)
#endif
! callback functions
    procedure(GetPertConcatenation_f), nopass, pointer :: get_pert_concatenation
end type PertFun_f

public :: RSPPertCreate_f
public :: RSPPertGetConcatenation_f
public :: RSPPertDestroy_f

contains

!% \brief creates the context of callback subroutines of perturbations
! \author Bin Gao
! \date 2014-08-18
! \param[PertFun_f:type]{inout} pert_fun the context of callback subroutines
! \param[character]{in} user_ctx user-defined callback function context
! \param[subroutine]{in} get_pert_concatenation user specified function for
!% getting rank of a perturbation
subroutine RSPPertCreate_f(pert_fun,          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,          &
#endif
                                get_pert_concatenation)
    type(PertFun_f), intent(inout) :: pert_fun
#if defined(OPENRSP_F_USER_CONTEXT)

```



```

                                num_cat_comps, &
                                num_sub_tuples, &
                                len_sub_tuples, &
                                user_ctx, &
                                rank_sub_comps) &
bind(C, name="RSPPertGetConcatenation_f")
integer(kind=C_QINT), value, intent(in) :: pert_label
integer(kind=C_QINT), value, intent(in) :: first_cat_comp
integer(kind=C_QINT), value, intent(in) :: num_cat_comps
integer(kind=C_QINT), value, intent(in) :: num_sub_tuples
integer(kind=C_QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
type(C_PTR), value, intent(in) :: user_ctx
integer(kind=C_QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_comps)
type(PertFun_f), pointer :: pert_fun !context of callback subroutines
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, pert_fun)
! invokes Fortran callback subroutine to get the rank of the perturbation
call pert_fun%get_pert_concatenation(pert_label, &
                                first_cat_comp, &
                                num_cat_comps, &
                                num_sub_tuples, &
                                len_sub_tuples, &

                                pert_fun%len_ctx, &
                                pert_fun%user_ctx, &

                                rank_sub_comps)

! cleans up
nullify(pert_fun)
return
end subroutine RSPPertGetConcatenation_f

!% \brief cleans the context of callback subroutines of perturbations
! \author Bin Gao
! \date 2014-08-18
!% \param[PertFun_f:type]{inout} pert_fun the context of callback subroutines
subroutine RSPPertDestroy_f(pert_fun)
    type(PertFun_f), intent(inout) :: pert_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    pert_fun%len_ctx = 0
    deallocate(pert_fun%user_ctx)
#endif
    nullify(pert_fun%get_pert_concatenation)
end subroutine RSPPertDestroy_f

end module RSPPerturbation_f

```

151 $\langle RSPOverlap.F90$ 151 $\rangle \equiv$
 $\langle OpenRSPLicenseFortran$ 119a \rangle

!! 2014-08-05, Bin Gao
!! * first version

```

! basic data types
#include "api/qcmatrix_c_type.h"

#define OPENRSP_API_SRC "src/fortran/RSPOverlap.F90"

module RSPOverlap_f

  use, intrinsic :: iso_c_binding
  use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
  use RSPPertBasicTypes_f, only: QcPertInt, &
                                C_QCPERTINT

  implicit none

  integer(kind=4), private, parameter :: STDOUT = 6

  ! user specified callback subroutines
  abstract interface
    subroutine OverlapGetMat_f(bra_num_pert,      &
                              bra_pert_labels,    &
                              bra_pert_orders,    &
                              ket_num_pert,       &
                              ket_pert_labels,    &
                              ket_pert_orders,    &
                              oper_num_pert,     &
                              oper_pert_labels,   &
                              oper_pert_orders,   &
                              &
                              len_ctx,           &
                              user_ctx,         &
                              &
                              num_int,          &
                              val_int)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: bra_num_pert
    integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
    integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
    integer(kind=QINT), intent(in) :: ket_num_pert
    integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
    integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
  end interface

  #if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
  #endif

  integer(kind=QINT), intent(in) :: num_int
  type(QcMat), intent(inout) :: val_int(num_int)
end subroutine OverlapGetMat_f

```



```

subroutine OverlapGetExp_f(bra_num_pert,      &
                          bra_pert_labels,  &
                          bra_pert_orders,  &
                          ket_num_pert,     &
                          ket_pert_labels,  &
                          ket_pert_orders,  &
                          oper_num_pert,    &
                          oper_pert_labels, &
                          oper_pert_orders, &
                          num_dmat,         &
                          dens_mat,         &
#if defined(OPENRSP_F_USER_CONTEXT)
                          len_ctx,          &
                          user_ctx,         &
#endif
                          num_exp,          &
                          val_exp)
  use qcmatrix_f, only: QINT,QREAL,QcMat
  use RSPPertBasicTypes_f, only: QcPertInt
  integer(kind=QINT), intent(in) :: bra_num_pert
  integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
  integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
  integer(kind=QINT), intent(in) :: ket_num_pert
  integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
  integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
  integer(kind=QINT), intent(in) :: oper_num_pert
  integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
  integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
  integer(kind=QINT), intent(in) :: num_dmat
  type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
  integer(kind=QINT), intent(in) :: len_ctx
  character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
  integer(kind=QINT), intent(in) :: num_exp
  real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine OverlapGetExp_f
end interface

! context of callback subroutines of overlap integrals
type, public :: OverlapFun_f
  private
#if defined(OPENRSP_F_USER_CONTEXT)
  ! user-defined callback function context
  integer(kind=QINT) :: len_ctx = 0
  character(len=1), allocatable :: user_ctx(:)
#endif
! callback functions
  procedure(OverlapGetMat_f), nopass, pointer :: get_overlap_mat
  procedure(OverlapGetExp_f), nopass, pointer :: get_overlap_exp
end type OverlapFun_f

```

```

public :: RSPOverlapCreate_f
public :: RSPOverlapGetMat_f
public :: RSPOverlapGetExp_f
public :: RSPOverlapDestroy_f

contains

!% \brief creates the context of callback subroutines of overlap integrals
! \author Bin Gao
! \date 2014-08-05
! \param[OverlapFun_f:type]{inout} overlap_fun the context of callback subroutines
! \param[character]{in} user_ctx user-defined callback function context
! \param[subroutine]{in} get_overlap_mat user specified function for
!     getting integral matrices
! \param[subroutine]{in} get_overlap_exp user specified function for
!%     getting expectation values
subroutine RSPOverlapCreate_f(overlap_fun,      &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,      &
#endif
                                get_overlap_mat, &
                                get_overlap_exp)
    type(OverlapFun_f), intent(inout) :: overlap_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_overlap_mat(bra_num_pert,      &
                                    bra_pert_labels,  &
                                    bra_pert_orders,  &
                                    ket_num_pert,      &
                                    ket_pert_labels,   &
                                    ket_pert_orders,   &
                                    oper_num_pert,     &
                                    oper_pert_labels,  &
                                    oper_pert_orders,  &
#if defined(OPENRSP_F_USER_CONTEXT)
                                    len_ctx,          &
                                    user_ctx,         &
#endif
                                    num_int,          &
                                    val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: bra_num_pert
            integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
            integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
            integer(kind=QINT), intent(in) :: ket_num_pert
            integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
            integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)

```

```

        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_int
        type(QcMat), intent(inout) :: val_int(num_int)
end subroutine get_overlap_mat
subroutine get_overlap_exp(bra_num_pert,      &
                          bra_pert_labels, &
                          bra_pert_orders, &
                          ket_num_pert,    &
                          ket_pert_labels, &
                          ket_pert_orders, &
                          oper_num_pert,   &
                          oper_pert_labels, &
                          oper_pert_orders, &
                          num_dmat,        &
                          dens_mat,        &
#if defined(OPENRSP_F_USER_CONTEXT)
                          len_ctx,         &
                          user_ctx,        &
#endif
                          num_exp,         &
                          val_exp)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: bra_num_pert
    integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
    integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
    integer(kind=QINT), intent(in) :: ket_num_pert
    integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
    integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    integer(kind=QINT), intent(in) :: num_dmat
    type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

    integer(kind=QINT), intent(in) :: num_exp
    real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine get_overlap_exp
end interface
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=4) ierr !error information
    overlap_fun%len_ctx = size(user_ctx)
    allocate(overlap_fun%user_ctx(overlap_fun%len_ctx), stat=ierr)
    if (ierr/=0) then
        write(STDOUT,"(A,I8)") "RSPOverlapCreate_f>> length", overlap_fun%len_ctx
    end if
#endif

```

```

        stop "RSPOverlapCreate_f>> failed to allocate memory for user_ctx"
    end if
    overlap_fun%user_ctx = user_ctx
#endif

    overlap_fun%get_overlap_mat => get_overlap_mat
    overlap_fun%get_overlap_exp => get_overlap_exp
end subroutine RSPOverlapCreate_f

!% \brief calls Fortran callback subroutine to get integral matrices of overlap integrals
! \author Bin Gao
! \date 2014-08-05
! \param[integer]{in} bra_len_tuple length of the perturbation tuple on the bra
! \param[integer]{in} bra_pert_tuple perturbation tuple on the bra
! \param[integer]{in} ket_len_tuple length of the perturbation tuple on the ket
! \param[integer]{in} ket_pert_tuple perturbation tuple on the ket
! \param[integer]{in} len_tuple length of perturbation tuple on the overlap integrals
! \param[integer]{in} pert_tuple perturbation tuple on the overlap integrals
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_int number of the integral matrices
!% \param[C_PTR:type]{inout} val_int the integral matrices
subroutine RSPOverlapGetMat_f(bra_num_pert,      &
                             bra_pert_labels,  &
                             bra_pert_orders,  &
                             ket_num_pert,     &
                             ket_pert_labels,  &
                             ket_pert_orders,  &
                             oper_num_pert,    &
                             oper_pert_labels, &
                             oper_pert_orders, &
                             user_ctx,         &
                             num_int,          &
                             val_int)         &

    bind(C, name="RSPOverlapGetMat_f")
    integer(kind=C_QINT), value, intent(in) :: bra_num_pert
    integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
    integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
    integer(kind=C_QINT), value, intent(in) :: ket_num_pert
    integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
    integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
    integer(kind=C_QINT), value, intent(in) :: oper_num_pert
    integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    type(C_PTR), value, intent(in) :: user_ctx
    integer(kind=C_QINT), value, intent(in) :: num_int
    type(C_PTR), intent(inout) :: val_int(num_int)
    type(OverlapFun_f), pointer :: overlap_fun !context of callback subroutines
    type(QcMat), allocatable :: f_val_int(:)   !integral matrices
    integer(kind=4) ierr                       !error information
    ! converts C pointer to Fortran QcMat type
    allocate(f_val_int(num_int), stat=ierr)
    if (ierr/=0) then
        write(STDOUT,"(A,I8)") "RSPOverlapGetMat_f>> num_int", num_int
    end if
end subroutine RSPOverlapGetMat_f

```

```

        stop "RSPOverlapGetMat_f>> failed to allocate memory for f_val_int"
    end if
    ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
    call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
    ! gets the Fortran callback subroutine
    call c_f_pointer(user_ctx, overlap_fun)
    ! invokes Fortran callback subroutine to calculate the integral matrices
    call overlap_fun%get_overlap_mat(bra_num_pert,      &
                                     bra_pert_labels,   &
                                     bra_pert_orders,   &
                                     ket_num_pert,       &
                                     ket_pert_labels,    &
                                     ket_pert_orders,    &
                                     oper_num_pert,      &
                                     oper_pert_labels,   &
                                     oper_pert_orders,   &
                                     overlap_fun%len_ctx, &
                                     overlap_fun%user_ctx, &
                                     num_int,            &
                                     f_val_int)

    ! cleans up
    nullify(overlap_fun)
    ierr = QcMat_C_NULL_PTR(A=f_val_int)
    call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
    deallocate(f_val_int)
end subroutine RSPOverlapGetMat_f

```

```

!% \brief calls Fortran callback subroutine to get expectation values of overlap integrals
! \author Bin Gao
! \date 2014-08-05
! \param[integer]{in} bra_len_tuple length of the perturbation tuple on the bra
! \param[integer]{in} bra_pert_tuple perturbation tuple on the bra
! \param[integer]{in} ket_len_tuple length of the perturbation tuple on the ket
! \param[integer]{in} ket_pert_tuple perturbation tuple on the ket
! \param[integer]{in} len_tuple length of perturbation tuple on the overlap integrals
! \param[integer]{in} pert_tuple perturbation tuple on the overlap integrals
! \param[integer]{in} num_dmat number of atomic orbital (AO) based density matrices
! \param[C_PTR:type]{inout} dens_mat the AO based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_exp number of expectation values
!% \param[real]{out} val_exp the expectation values
subroutine RSPOverlapGetExp_f(bra_num_pert,      &
                             bra_pert_labels,   &
                             bra_pert_orders,   &
                             ket_num_pert,      &
                             ket_pert_labels,   &
                             ket_pert_orders,   &
                             oper_num_pert,     &
                             oper_pert_labels,  &
                             oper_pert_orders,  &

```



```

#if defined(OPENRSP_F_USER_CONTEXT)
        len_ctx,          &
        user_ctx,         &
#endif

        num_int,          &
        val_int)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

    integer(kind=QINT), intent(in) :: num_int
    type(QcMat), intent(inout) :: val_int(num_int)
end subroutine OneOperGetMat_f
subroutine OneOperGetExp_f(oper_num_pert, &
                           oper_pert_labels, &
                           oper_pert_orders, &
                           num_dmat, &
                           dens_mat, &
#if defined(OPENRSP_F_USER_CONTEXT)
                           len_ctx, &
                           user_ctx, &
#endif
                           num_exp, &
                           val_exp)
    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: oper_num_pert
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
    integer(kind=QINT), intent(in) :: num_dmat
    type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

    integer(kind=QINT), intent(in) :: num_exp
    real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine OneOperGetExp_f
end interface

! context of callback subroutines of one-electron operator
type, public :: OneOperFun_f
private
#if defined(OPENRSP_F_USER_CONTEXT)
    ! user-defined callback function context
    integer(kind=QINT) :: len_ctx = 0
    character(len=1), allocatable :: user_ctx(:)

```



```

#endif

! callback functions
procedure(OneOperGetMat_f), nopass, pointer :: get_one_oper_mat
procedure(OneOperGetExp_f), nopass, pointer :: get_one_oper_exp
end type OneOperFun_f

public :: RSPOneOperCreate_f
public :: RSPOneOperGetMat_f
public :: RSPOneOperGetExp_f
public :: RSPOneOperDestroy_f

contains

!% \brief creates the context of callback subroutines of one-electron operator
! \author Bin Gao
! \date 2014-08-03
! \param[OneOperFun_f:type]{inout} one_oper_fun the context of callback subroutines
! \param[character]{in} user_ctx user-defined callback function context
! \param[subroutine]{in} get_one_oper_mat user specified function for
! getting integral matrices
! \param[subroutine]{in} get_one_oper_exp user specified function for
!% getting expectation values
subroutine RSPOneOperCreate_f(one_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx, &
#endif
                                get_one_oper_mat, &
                                get_one_oper_exp)
    type(OneOperFun_f), intent(inout) :: one_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_one_oper_mat(oper_num_pert, &
                                    oper_pert_labels, &
                                    oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                    len_ctx, &
                                    user_ctx, &
#endif
                                    num_int, &
                                    val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int

```

```

        type(QcMat), intent(inout) :: val_int(num_int)
    end subroutine get_one_oper_mat
    subroutine get_one_oper_exp(oper_num_pert,      &
                               oper_pert_labels, &
                               oper_pert_orders, &
                               num_dmat,         &
                               dens_mat,         &
    #if defined(OPENRSP_F_USER_CONTEXT)
                               len_ctx,          &
                               user_ctx,         &
    #endif
                               num_exp,          &
                               val_exp)

        use qcmatrix_f, only: QINT,QREAL,QcMat
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=QINT), intent(in) :: num_dmat
        type(QcMat), intent(in) :: dens_mat(num_dmat)
    #if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
    #endif

        integer(kind=QINT), intent(in) :: num_exp
        real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine get_one_oper_exp
end interface
    #if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        one_oper_fun%len_ctx = size(user_ctx)
        allocate(one_oper_fun%user_ctx(one_oper_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPOneOperCreate_f>> length", one_oper_fun%len_ctx
            stop "RSPOneOperCreate_f>> failed to allocate memory for user_ctx"
        end if
        one_oper_fun%user_ctx = user_ctx
    #endif

    one_oper_fun%get_one_oper_mat => get_one_oper_mat
    one_oper_fun%get_one_oper_exp => get_one_oper_exp
end subroutine RSPOneOperCreate_f

!% \brief calls Fortran callback subroutine to get integral matrices of
!     a one-electron operator
! \author Bin Gao
! \date 2014-08-02
! \param[integer]{in} len_tuple length of perturbation tuple on the one-electron opera
! \param[integer]{in} pert_tuple perturbation tuple on the one-electron operator
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_int number of the integral matrices
!% \param[C_PTR:type]{inout} val_int the integral matrices
subroutine RSPOneOperGetMat_f(oper_num_pert,      &

```

```

                                oper_pert_labels, &
                                oper_pert_orders, &
                                user_ctx,          &
                                num_int,          &
                                val_int)          &
bind(C, name="RSPOneOperGetMat_f")
integer(kind=C_QINT), value, intent(in) :: oper_num_pert
integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
type(C_PTR), value, intent(in) :: user_ctx
integer(kind=C_QINT), value, intent(in) :: num_int
type(C_PTR), intent(inout) :: val_int(num_int)
type(OneOperFun_f), pointer :: one_oper_fun !context of callback subroutines
type(QcMat), allocatable :: f_val_int(:)    !integral matrices
integer(kind=4) ierr                        !error information
! converts C pointer to Fortran QcMat type
allocate(f_val_int(num_int), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPOneOperGetMat_f>> num_int", num_int
    stop "RSPOneOperGetMat_f>> failed to allocate memory for f_val_int"
end if
ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, one_oper_fun)
! invokes Fortran callback subroutine to calculate the integral matrices
call one_oper_fun%get_one_oper_mat(oper_num_pert,
                                   &
                                   oper_pert_labels, &
                                   oper_pert_orders, &
                                   &
                                   one_oper_fun%len_ctx, &
                                   one_oper_fun%user_ctx, &
                                   &
                                   num_int,          &
                                   f_val_int)

! cleans up
nullify(one_oper_fun)
ierr = QcMat_C_NULL_PTR(A=f_val_int)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
deallocate(f_val_int)
end subroutine RSPOneOperGetMat_f

!% \brief calls Fortran callback subroutine to get expectation values of
!     a one-electron operator
! \author Bin Gao
! \date 2014-08-02
! \param[integer]{in} len_tuple length of perturbation tuple on the one-electron opera
! \param[integer]{in} pert_tuple perturbation tuple on the one-electron operator
! \param[integer]{in} num_dmat number of atomic orbital (AO) based density matrices
! \param[C_PTR:type]{inout} dens_mat the AO based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_exp number of expectation values

```

```

!% \param[real]{out} val_exp the expectation values
subroutine RSPOneOperGetExp_f(oper_num_pert,      &
                             oper_pert_labels, &
                             oper_pert_orders, &
                             num_dmat,         &
                             dens_mat,         &
                             user_ctx,         &
                             num_exp,          &
                             val_exp)          &
  bind(C, name="RSPOneOperGetExp_f")
  integer(kind=C_QINT), value, intent(in) :: oper_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
  integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
  integer(kind=C_QINT), value, intent(in) :: num_dmat
  type(C_PTR), intent(in) :: dens_mat(num_dmat)
  type(C_PTR), value, intent(in) :: user_ctx
  integer(kind=C_QINT), value, intent(in) :: num_exp
  real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
  type(OneOperFun_f), pointer :: one_oper_fun !context of callback subroutines
  type(QcMat), allocatable :: f_dens_mat(:)   !AO based density matrices
  integer(kind=4) ierr                       !error information
  ! converts C pointer to Fortran QcMat type
  allocate(f_dens_mat(num_dmat), stat=ierr)
  if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPOneOperGetExp_f>> num_dmat", num_dmat
    stop "RSPOneOperGetExp_f>> failed to allocate memory for f_dens_mat"
  end if
  ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
  call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
  ! gets the Fortran callback subroutine
  call c_f_pointer(user_ctx, one_oper_fun)
  ! invokes Fortran callback subroutine to calculate the expectation values
  call one_oper_fun%get_one_oper_exp(oper_num_pert,      &
                                     oper_pert_labels,   &
                                     oper_pert_orders,   &
                                     num_dmat,           &
                                     f_dens_mat,         &
                                     one_oper_fun%len_ctx, &
                                     one_oper_fun%user_ctx, &
                                     num_exp,            &
                                     val_exp)

  ! cleans up
  nullify(one_oper_fun)
  ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
  call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
  deallocate(f_dens_mat)
  return
end subroutine RSPOneOperGetExp_f

!% \brief cleans the context of callback subroutines of one-electron operator

```

```

! \author Bin Gao
! \date 2014-08-03
!% \param[OneOperFun_f:type]{inout} one_oper_fun the context of callback subroutines
subroutine RSPOneOperDestroy_f(one_oper_fun)
    type(OneOperFun_f), intent(inout) :: one_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    one_oper_fun%len_ctx = 0
    deallocate(one_oper_fun%user_ctx)
#endif
    nullify(one_oper_fun%get_one_oper_mat)
    nullify(one_oper_fun%get_one_oper_exp)
end subroutine RSPOneOperDestroy_f

end module RSPOneOper_f

#undef OPENRSP_API_SRC

```

165 $\langle RSPTwoOper.F90$ 165 \equiv
 $\langle OpenRSPLicenseFortran$ 119a \rangle

```

!! 2014-08-06, Bin Gao
!! * first version

! basic data types
#include "api/qcmatrix_c_type.h"

#define OPENRSP_API_SRC "src/fortran/RSPTwoOper.F90"

module RSPTwoOper_f

    use, intrinsic :: iso_c_binding
    use qcmatrix_f, only: QINT, QREAL, QcMat, QcMat_C_F_POINTER, QcMat_C_NULL_PTR
    use RSPPertBasicTypes_f, only: QcPertInt, &
        C_QCPERTINT

    implicit none

    integer(kind=4), private, parameter :: STDOUT = 6

    ! user specified callback subroutines
    abstract interface
        subroutine TwoOperGetMat_f(oper_num_pert, &
                                   oper_pert_labels, &
                                   oper_pert_orders, &
                                   num_dmat, &
                                   dens_mat, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx, &
                                   user_ctx, &
#endif
                                   num_int, &
                                   val_int)

```

```

        use qcmatrix_f, only: QINT,QREAL,QcMat
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=QINT), intent(in) :: num_dmat
        type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_int
        type(QcMat), intent(inout) :: val_int(num_int)
end subroutine TwoOperGetMat_f
subroutine TwoOperGetExp_f(oper_num_pert,      &
                           oper_pert_labels, &
                           oper_pert_orders, &
                           dmat_len_tuple,   &
                           num_LHS_dmat,     &
                           LHS_dens_mat,     &
                           num_RHS_dmat,     &
                           RHS_dens_mat,     &
                           len_ctx,          &
                           user_ctx,         &
                           num_exp,          &
                           val_exp)
        use qcmatrix_f, only: QINT,QREAL,QcMat
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=QINT), intent(in) :: dmat_len_tuple
        integer(kind=QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
        type(QcMat), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
        integer(kind=QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
        type(QcMat), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_exp
        real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine TwoOperGetExp_f
end interface

! context of callback subroutines of two-electron operator
type, public :: TwoOperFun_f
    private
#if defined(OPENRSP_F_USER_CONTEXT)
    ! user-defined callback function context

```

```

        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif

        ! callback functions
        procedure(TwoOperGetMat_f), nopass, pointer :: get_two_oper_mat
        procedure(TwoOperGetExp_f), nopass, pointer :: get_two_oper_exp
    end type TwoOperFun_f

    public :: RSPTwoOperCreate_f
    public :: RSPTwoOperGetMat_f
    public :: RSPTwoOperGetExp_f
    public :: RSPTwoOperDestroy_f

    contains

    !% \brief creates the context of callback subroutines of two-electron operator
    ! \author Bin Gao
    ! \date 2014-08-06
    ! \param[TwoOperFun_f:type]{inout} two_oper_fun the context of callback subroutines
    ! \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine]{in} get_two_oper_mat user specified function for
    !     getting integral matrices
    ! \param[subroutine]{in} get_two_oper_exp user specified function for
    !%     getting expectation values
    subroutine RSPTwoOperCreate_f(two_oper_fun,      &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,          &
#endif
                                get_two_oper_mat, &
                                get_two_oper_exp)
        type(TwoOperFun_f), intent(inout) :: two_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
    interface
        subroutine get_two_oper_mat(oper_num_pert,      &
                                    oper_pert_labels, &
                                    oper_pert_orders, &
                                    num_dmat,          &
                                    dens_mat,          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                    len_ctx,          &
                                    user_ctx,          &
#endif
                                    num_int,          &
                                    val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
            integer(kind=QINT), intent(in) :: num_dmat

```

```

        type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_int
        type(QcMat), intent(inout) :: val_int(num_int)
end subroutine get_two_oper_mat
subroutine get_two_oper_exp(oper_num_pert,      &
                           oper_pert_labels, &
                           oper_pert_orders, &
                           dmat_len_tuple,   &
                           num_LHS_dmat,     &
                           LHS_dens_mat,     &
                           num_RHS_dmat,     &
                           RHS_dens_mat,     &
                           len_ctx,          &
                           user_ctx,         &
                           num_exp,          &
                           val_exp)
#if defined(OPENRSP_F_USER_CONTEXT)
        len_ctx,          &
        user_ctx,         &
        num_exp,          &
        val_exp)
        use qcmatrix_f, only: QINT,QREAL,QcMat
        use RSPPertBasicTypes_f, only: QcPertInt
        integer(kind=QINT), intent(in) :: oper_num_pert
        integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=QINT), intent(in) :: dmat_len_tuple
        integer(kind=QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
        type(QcMat), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
        integer(kind=QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
        type(QcMat), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
#endif
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_exp
        real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
end subroutine get_two_oper_exp
end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        two_oper_fun%len_ctx = size(user_ctx)
        allocate(two_oper_fun%user_ctx(two_oper_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPTwoOperCreate_f>> length", two_oper_fun%len_ctx
            stop "RSPTwoOperCreate_f>> failed to allocate memory for user_ctx"
        end if
        two_oper_fun%user_ctx = user_ctx
#endif
        two_oper_fun%get_two_oper_mat => get_two_oper_mat
        two_oper_fun%get_two_oper_exp => get_two_oper_exp

```



```
end subroutine RSPTwoOperCreate_f
```

```
!% \brief calls Fortran callback subroutine to get integral matrices of
!      a two-electron operator
! \author Bin Gao
! \date 2014-08-06
! \param[integer]{in} len_tuple length of perturbation tuple on the two-electron opera
! \param[integer]{in} pert_tuple perturbation tuple on the two-electron operator
! \param[integer]{in} num_dmat number of AO based density matrices
! \param[C_PTR:type]{in} dens_mat the AO based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_int number of the integral matrices
!% \param[C_PTR:type]{inout} val_int the integral matrices
subroutine RSPTwoOperGetMat_f(oper_num_pert,      &
                             oper_pert_labels, &
                             oper_pert_orders, &
                             num_dmat,         &
                             dens_mat,         &
                             user_ctx,         &
                             num_int,         &
                             val_int)         &
  bind(C, name="RSPTwoOperGetMat_f")
  integer(kind=C_QINT), value, intent(in) :: oper_num_pert
  integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
  integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
  integer(kind=C_QINT), value, intent(in) :: num_dmat
  type(C_PTR), intent(in) :: dens_mat(num_dmat)
  type(C_PTR), value, intent(in) :: user_ctx
  integer(kind=C_QINT), value, intent(in) :: num_int
  type(C_PTR), intent(inout) :: val_int(num_int)
  type(TwoOperFun_f), pointer :: two_oper_fun !context of callback subroutines
  type(QcMat), allocatable :: f_dens_mat(:)   !AO based density matrices
  type(QcMat), allocatable :: f_val_int(:)    !integral matrices
  integer(kind=4) ierr                       !error information
  ! converts C pointer to Fortran QcMat type
  allocate(f_dens_mat(num_dmat), stat=ierr)
  if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPTwoOperGetMat_f>> num_dmat", num_dmat
    stop "RSPTwoOperGetMat_f>> failed to allocate memory for f_dens_mat"
  end if
  ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
  call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
  allocate(f_val_int(num_int), stat=ierr)
  if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPTwoOperGetMat_f>> num_int", num_int
    stop "RSPTwoOperGetMat_f>> failed to allocate memory for f_val_int"
  end if
  ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
  call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
  ! gets the Fortran callback subroutine
  call c_f_pointer(user_ctx, two_oper_fun)
  ! invokes Fortran callback subroutine to calculate the integral matrices
```

```

      call two_oper_fun%get_two_oper_mat(oper_num_pert,      &
                                         oper_pert_labels,  &
                                         oper_pert_orders,  &
                                         num_dmat,          &
                                         f_dens_mat,        &

#if defined(OPENRSP_F_USER_CONTEXT)
                                         two_oper_fun%len_ctx, &
                                         two_oper_fun%user_ctx, &

#endif
                                         num_int,           &
                                         f_val_int)

```

```

      ! cleans up
      nullify(two_oper_fun)
      ierr = QcMat_C_NULL_PTR(A=f_val_int)
      call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
      ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
      call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
      deallocate(f_val_int)
      deallocate(f_dens_mat)
end subroutine RSPTwoOperGetMat_f

```

```

!% \brief calls Fortran callback subroutine to get expectation values of
!      a two-electron operator

```

```

! \author Bin Gao
! \date 2014-08-06

```

```

! \param[integer]{in} len_tuple length of perturbation tuple on the two-electron opera
! \param[integer]{in} pert_tuple perturbation tuple on the two-electron operator
! \param[integer]{in} dmat_len_tuple length of different perturbation tuples
!      of the left-hand-side (LHS) and right-hand-side (RHS) AO based density
!      matrices passed
! \param[integer]{in} num_LHS_dmat number of LHS AO based density matrices
!      passed for each LHS density matrix perturbation tuple
! \param[C_PTR:type]{in} LHS_dens_mat the LHS AO based density matrices
! \param[integer]{in} num_RHS_dmat number of RHS AO based density matrices
!      passed for each RHS density matrix perturbation tuple
! \param[C_PTR:type]{in} RHS_dens_mat the RHS AO based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_exp number of expectation values

```

```

!% \param[real]{out} val_exp the expectation values

```

```

subroutine RSPTwoOperGetExp_f(oper_num_pert,      &
                              oper_pert_labels, &
                              oper_pert_orders, &
                              dmat_len_tuple,    &
                              num_LHS_dmat,      &
                              LHS_dens_mat,       &
                              num_RHS_dmat,      &
                              RHS_dens_mat,       &
                              user_ctx,          &
                              num_exp,           &
                              val_exp)           &

```

```

      bind(C, name="RSPTwoOperGetExp_f")
      integer(kind=C_QINT), value, intent(in) :: oper_num_pert

```

```

integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
integer(kind=C_QINT), value, intent(in) :: dmat_len_tuple
integer(kind=C_QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
type(C_PTR), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
integer(kind=C_QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
type(C_PTR), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
type(C_PTR), value, intent(in) :: user_ctx
integer(kind=C_QINT), value, intent(in) :: num_exp
real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
type(TwoOperFun_f), pointer :: two_oper_fun      !context of callback subroutines
type(QcMat), allocatable :: f_LHS_dens_mat(:)    !LHS AO based density matrices
type(QcMat), allocatable :: f_RHS_dens_mat(:)    !RHS AO based density matrices
integer(kind=4) ierr                             !error information
! converts C pointer to Fortran QcMat type
allocate(f_LHS_dens_mat(sum(num_LHS_dmat)), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPTwoOperGetExp_f>> sum(num_LHS_dmat)", &
        sum(num_LHS_dmat)
    stop "RSPTwoOperGetExp_f>> failed to allocate memory for f_LHS_dens_mat"
end if
ierr = QcMat_C_F_POINTER(A=f_LHS_dens_mat, c_A=LHS_dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
allocate(f_RHS_dens_mat(sum(num_RHS_dmat)), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPTwoOperGetExp_f>> sum(num_RHS_dmat)", &
        sum(num_RHS_dmat)
    stop "RSPTwoOperGetExp_f>> failed to allocate memory for f_RHS_dens_mat"
end if
ierr = QcMat_C_F_POINTER(A=f_RHS_dens_mat, c_A=RHS_dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, two_oper_fun)
! invokes Fortran callback subroutine to calculate the expectation values
call two_oper_fun%get_two_oper_exp(oper_num_pert,
                                     &
                                     oper_pert_labels,
                                     &
                                     oper_pert_orders,
                                     &
                                     dmat_len_tuple,
                                     &
                                     num_LHS_dmat,
                                     &
                                     f_LHS_dens_mat,
                                     &
                                     num_RHS_dmat,
                                     &
                                     f_RHS_dens_mat,
                                     &
                                     two_oper_fun%len_ctx, &
                                     two_oper_fun%user_ctx, &
                                     num_exp,
                                     &
                                     val_exp)

! cleans up
nullify(two_oper_fun)
ierr = QcMat_C_NULL_PTR(A=f_RHS_dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)

```



```

                                pert_freq_category, &
                                dmat_num_tuple,      &
                                dmat_idx_tuple,      &
                                num_dmat,            &
                                dens_mat,            &
#if defined(OPENRSP_F_USER_CONTEXT)
                                len_ctx,             &
                                user_ctx,            &
#endif
                                num_int,              &
                                val_int)

    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: xc_len_tuple
    integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
    integer(kind=QINT), intent(in) :: num_freq_configs
    integer(kind=QINT), intent(in) :: &
        pert_freq_category(num_freq_configs*xc_len_tuple)
    integer(kind=QINT), intent(in) :: dmat_num_tuple
    integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
    integer(kind=QINT), intent(in) :: num_dmat
    type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
    integer(kind=QINT), intent(in) :: len_ctx
    character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
    integer(kind=QINT), intent(in) :: num_int
    type(QcMat), intent(inout) :: val_int(num_int)
end subroutine XCFunGetMat_f
subroutine XCFunGetExp_f(xc_len_tuple,      &
                        xc_pert_tuple,      &
                        num_freq_configs,    &
                        pert_freq_category, &
                        dmat_num_tuple,      &
                        dmat_idx_tuple,      &
                        num_dmat,            &
                        dens_mat,            &
#if defined(OPENRSP_F_USER_CONTEXT)
                        len_ctx,             &
                        user_ctx,            &
#endif
                        num_exp,              &
                        val_exp)

    use qcmatrix_f, only: QINT,QREAL,QcMat
    use RSPPertBasicTypes_f, only: QcPertInt
    integer(kind=QINT), intent(in) :: xc_len_tuple
    integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
    integer(kind=QINT), intent(in) :: num_freq_configs
    integer(kind=QINT), intent(in) :: &
        pert_freq_category(num_freq_configs*xc_len_tuple)
    integer(kind=QINT), intent(in) :: dmat_num_tuple

```

```

        integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=QINT), intent(in) :: num_dmat
        type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=QINT), intent(in) :: len_ctx
        character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

        integer(kind=QINT), intent(in) :: num_exp
        real(kind=QREAL), intent(inout) :: val_exp(2*num_exp)
    end subroutine XCFunGetExp_f
end interface

! context of callback subroutines of XC functional
type, public :: XCFunFun_f
    private
#if defined(OPENRSP_F_USER_CONTEXT)
    ! user-defined callback function context
    integer(kind=QINT) :: len_ctx = 0
    character(len=1), allocatable :: user_ctx(:)
#endif

! callback functions
    procedure(XCFunGetMat_f), nopass, pointer :: get_xc_fun_mat
    procedure(XCFunGetExp_f), nopass, pointer :: get_xc_fun_exp
end type XCFunFun_f

public :: RSPXCFunCreate_f
public :: RSPXCFunGetMat_f
public :: RSPXCFunGetExp_f
public :: RSPXCFunDestroy_f

contains

!% \brief creates the context of callback subroutines of XC functional
! \author Bin Gao
! \date 2015-06-23
! \param[XCFunFun_f:type]{inout} xcfun_fun the context of callback subroutines
! \param[character]{in} user_ctx user-defined callback function context
! \param[subroutine]{in} get_xc_fun_mat user specified function for
!     getting integral matrices
! \param[subroutine]{in} get_xc_fun_exp user specified function for
!     getting expectation values
subroutine RSPXCFunCreate_f(xcfun_fun,      &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,  &
#endif
                                get_xc_fun_mat, &
                                get_xc_fun_exp)
    type(XCFunFun_f), intent(inout) :: xcfun_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
    interface

```

```

subroutine get_xc_fun_mat(xc_len_tuple,      &
                        xc_pert_tuple,      &
                        num_freq_configs,   &
                        pert_freq_category, &
                        dmat_num_tuple,     &
                        dmat_idx_tuple,     &
                        num_dmat,           &
                        dens_mat,           &
#if defined(OPENRSP_F_USER_CONTEXT)
                        len_ctx,            &
                        user_ctx,           &
#endif
                        num_int,            &
                        val_int)
  use qcmatrix_f, only: QINT,QREAL,QcMat
  use RSPPertBasicTypes_f, only: QcPertInt
  integer(kind=QINT), intent(in) :: xc_len_tuple
  integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
  integer(kind=QINT), intent(in) :: num_freq_configs
  integer(kind=QINT), intent(in) :: &
    pert_freq_category(num_freq_configs*xc_len_tuple)
  integer(kind=QINT), intent(in) :: dmat_num_tuple
  integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
  integer(kind=QINT), intent(in) :: num_dmat
  type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
  integer(kind=QINT), intent(in) :: len_ctx
  character(len=1), intent(in) :: user_ctx(len_ctx)
#endif

  integer(kind=QINT), intent(in) :: num_int
  type(QcMat), intent(inout) :: val_int(num_int)
end subroutine get_xc_fun_mat
subroutine get_xc_fun_exp(xc_len_tuple,      &
                        xc_pert_tuple,      &
                        num_freq_configs,   &
                        pert_freq_category, &
                        dmat_num_tuple,     &
                        dmat_idx_tuple,     &
                        num_dmat,           &
                        dens_mat,           &
#if defined(OPENRSP_F_USER_CONTEXT)
                        len_ctx,            &
                        user_ctx,           &
#endif
                        num_exp,            &
                        val_exp)
  use qcmatrix_f, only: QINT,QREAL,QcMat
  use RSPPertBasicTypes_f, only: QcPertInt
  integer(kind=QINT), intent(in) :: xc_len_tuple
  integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
  integer(kind=QINT), intent(in) :: num_freq_configs
  integer(kind=QINT), intent(in) :: &

```



```

        num_dmat,          &
        dens_mat,         &
        user_ctx,         &
        num_int,          &
        val_int)          &

bind(C, name="RSPXCFunGetMat_f")
integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
integer(kind=C_QINT), value, intent(in) :: num_freq_configs
integer(kind=C_QINT), intent(in) :: &
    pert_freq_category(num_freq_configs*xc_len_tuple)
integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
integer(kind=C_QINT), value, intent(in) :: num_dmat
type(C_PTR), intent(in) :: dens_mat(num_dmat)
type(C_PTR), value, intent(in) :: user_ctx
integer(kind=C_QINT), value, intent(in) :: num_int
type(C_PTR), intent(inout) :: val_int(num_int)
type(XCFunFun_f), pointer :: xcfun_fun      !context of callback subroutines
type(QcMat), allocatable :: f_dens_mat(:)  !AO based density matrices
type(QcMat), allocatable :: f_val_int(:)   !integral matrices
integer(kind=4) ierr                      !error information
! converts C pointer to Fortran QcMat type
allocate(f_dens_mat(num_dmat), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPXCFunGetMat_f>> num_dmat", num_dmat
    stop "RSPXCFunGetMat_f>> failed to allocate memory for f_dens_mat"
end if
ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
allocate(f_val_int(num_int), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPXCFunGetMat_f>> num_int", num_int
    stop "RSPXCFunGetMat_f>> failed to allocate memory for f_val_int"
end if
ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, xcfun_fun)
! invokes Fortran callback subroutine to calculate the integral matrices
call xcfun_fun%get_xc_fun_mat(xc_len_tuple,      &
                             xc_pert_tuple,      &
                             num_freq_configs,    &
                             pert_freq_category,  &
                             dmat_num_tuple,      &
                             dmat_idx_tuple,      &
                             num_dmat,            &
                             f_dens_mat,          &

#ifdef OPENRSP_F_USER_CONTEXT
                             xcfun_fun%len_ctx,    &
                             xcfun_fun%user_ctx,   &
#endif

#endif

```

```

                                num_int,          &
                                f_val_int)

! cleans up
nullify(xcfun_fun)
ierr = QcMat_C_NULL_PTR(A=f_val_int)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
deallocate(f_val_int)
deallocate(f_dens_mat)
end subroutine RSPXCFunGetMat_f

!% \brief calls Fortran callback subroutine to get expectation values of
!      an XC functional
! \author Bin Gao
! \date 2015-06-23
! \param[integer]{in} len_tuple length of perturbation tuple on the XC functional
! \param[integer]{in} pert_tuple perturbation tuple on the XC functional
! \param[integer]{in} num_freq_configs the number of different frequency
!      configurations to be considered for the perturbation tuple
! \param[integer]{in} pert_freq_category category of perturbation frequencies
! \param[integer]{in} dmat_len_tuple the number of different perturbation
!      tuples of the A0 based density matrices passed
! \param[integer]{in} dmat_idx_tuple indices of the density matrix
!      perturbation tuples passed (canonically ordered)
! \param[integer]{in} num_dmat number of collected A0 based density matrices for
!      the passed density matrix perturbation tuples and all frequency configurations
! \param[C_PTR:type]{in} dens_mat the collected A0 based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_exp number of expectation values
!% \param[real]{out} val_exp the expectation values
subroutine RSPXCFunGetExp_f(xc_len_tuple,          &
                           xc_pert_tuple,          &
                           num_freq_configs,        &
                           pert_freq_category,      &
                           dmat_num_tuple,          &
                           dmat_idx_tuple,          &
                           num_dmat,                &
                           dens_mat,                &
                           user_ctx,                &
                           num_exp,                 &
                           val_exp)                 &

bind(C, name="RSPXCFunGetExp_f")
integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
integer(kind=C_QINT), value, intent(in) :: num_freq_configs
integer(kind=C_QINT), intent(in) :: &
    pert_freq_category(num_freq_configs*xc_len_tuple)
integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
integer(kind=C_QINT), value, intent(in) :: num_dmat
type(C_PTR), intent(in) :: dens_mat(num_dmat)

```

```

type(C_PTR), value, intent(in) :: user_ctx
integer(kind=C_QINT), value, intent(in) :: num_exp
real(kind=C_QREAL), intent(inout) :: val_exp(2*num_exp)
type(XCFunFun_f), pointer :: xcfun_fun      !context of callback subroutines
type(QcMat), allocatable :: f_dens_mat(:)  !AO based density matrices
integer(kind=4) ierr                      !error information
! converts C pointer to Fortran QcMat type
allocate(f_dens_mat(num_dmat), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPXCFunGetExp_f>> num_dmat", num_dmat
    stop "RSPXCFunGetExp_f>> failed to allocate memory for f_dens_mat"
end if
ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, xcfun_fun)
! invokes Fortran callback subroutine to calculate the expectation values
call xcfun_fun%get_xc_fun_exp(xc_len_tuple,      &
                             xc_pert_tuple,      &
                             num_freq_configs,    &
                             pert_freq_category,  &
                             dmat_num_tuple,      &
                             dmat_idx_tuple,      &
                             num_dmat,           &
                             f_dens_mat,          &
                             &
                             xcfun_fun%len_ctx,    &
                             xcfun_fun%user_ctx,  &
                             &
                             num_exp,             &
                             val_exp)

! cleans up
nullify(xcfun_fun)
ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
deallocate(f_dens_mat)
return
end subroutine RSPXCFunGetExp_f

!% \brief cleans the context of callback subroutines of XC functional
! \author Bin Gao
! \date 2015-06-23
!% \param[XCFunFun_f:type]{inout} xcfun_fun the context of callback subroutines
subroutine RSPXCFunDestroy_f(xcfun_fun)
    type(XCFunFun_f), intent(inout) :: xcfun_fun
    if defined(OPENRSP_F_USER_CONTEXT)
        xcfun_fun%len_ctx = 0
        deallocate(xcfun_fun%user_ctx)
    endif
    nullify(xcfun_fun%get_xc_fun_mat)
    nullify(xcfun_fun%get_xc_fun_exp)
end subroutine RSPXCFunDestroy_f

```

```
end module RSPXCFun_f
```

```
#undef OPENRSP_API_SRC
```

```
180  <RSPZeroOper.F90 180>≡
    <OpenRSPLicenseFortran 119a>
```

```
!! 2015-06-23, Bin Gao
```

```
!! * first version
```

```
! basic data types
```

```
#include "api/qcmatrix_c_type.h"
```

```
#define OPENRSP_API_SRC "src/fortran/RSPZeroOper.F90"
```

```
module RSPZeroOper_f
```

```
    use, intrinsic :: iso_c_binding
```

```
    use qcmatrix_f, only: QINT,QREAL
```

```
    use RSPPertBasicTypes_f, only: QcPertInt, &
                                   C_QCPERTINT
```

```
    implicit none
```

```
    integer(kind=4), private, parameter :: STDOUT = 6
```

```
    ! user specified callback subroutine
```

```
    abstract interface
```

```
        subroutine ZeroOperGetContrib_f(oper_num_pert,    &
                                         oper_pert_labels, &
                                         oper_pert_orders, &
```

```
#if defined(OPENRSP_F_USER_CONTEXT)
```

```
        len_ctx,          &
        user_ctx,         &
```

```
#endif
```

```
        size_pert,        &
        val_oper)
```

```
    use qcmatrix_f, only: QINT,QREAL
```

```
    use RSPPertBasicTypes_f, only: QcPertInt
```

```
    integer(kind=QINT), intent(in) :: oper_num_pert
```

```
    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
```

```
    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
```

```
#if defined(OPENRSP_F_USER_CONTEXT)
```

```
    integer(kind=QINT), intent(in) :: len_ctx
```

```
    character(len=1), intent(in) :: user_ctx(len_ctx)
```

```
#endif
```

```
    integer(kind=QINT), intent(in) :: size_pert
```

```
    real(kind=QREAL), intent(inout) :: val_oper(2*size_pert)
```

```
    end subroutine ZeroOperGetContrib_f
```

```
end interface
```

```

! context of callback subroutine of zero-electron operator
type, public :: ZeroOperFun_f
  private
#if defined(OPENRSP_F_USER_CONTEXT)
  ! user-defined callback function context
  integer(kind=QINT) :: len_ctx = 0
  character(len=1), allocatable :: user_ctx(:)
#endif

! callback function
  procedure(ZeroOperGetContrib_f), nopass, pointer :: get_zero_oper_contrib
end type ZeroOperFun_f

public :: RSPZeroOperCreate_f
public :: RSPZeroOperGetContribution_f
public :: RSPZeroOperDestroy_f

contains

!% \brief creates the context of callback subroutine of zero-electron operator
! \author Bin Gao
! \date 2015-06-23
! \param[ZeroOperFun_f:type]{inout} zero_oper_fun the context of callback subroutine
! \param[character]{in} user_ctx user-defined callback function context
! \param[subroutine]{in} get_zero_oper_contrib user specified function for
!% getting zero-electron operator contributions
subroutine RSPZeroOperCreate_f(zero_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,      &
#endif
                                get_zero_oper_contrib)
  type(ZeroOperFun_f), intent(inout) :: zero_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
  character(len=1), intent(in) :: user_ctx(:)
#endif
  interface
    subroutine get_zero_oper_contrib(oper_num_pert, &
                                     oper_pert_labels, &
                                     oper_pert_orders, &
                                     len_ctx,      &
                                     user_ctx,      &
                                     size_pert,    &
                                     val_oper)
      use qcmatrix_f, only: QINT,QREAL
      use RSPPertBasicTypes_f, only: QcPertInt
      integer(kind=QINT), intent(in) :: oper_num_pert
      integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
      integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
      integer(kind=QINT), intent(in) :: len_ctx
      character(len=1), intent(in) :: user_ctx(len_ctx)

```



```

        ! cleans up
        nullify(zero_oper_fun)
        return
    end subroutine RSPZeroOperGetContribution_f

    !% \brief cleans the context of callback subroutine of zero-electron operator
    ! \author Bin Gao
    ! \date 2015-06-23
    !% \param[ZeroOperFun_f:type]{inout} zero_oper_fun the context of callback subroutine
    subroutine RSPZeroOperDestroy_f(zero_oper_fun)
        type(ZeroOperFun_f), intent(inout) :: zero_oper_fun
    #if defined(OPENRSP_F_USER_CONTEXT)
        zero_oper_fun%len_ctx = 0
        deallocate(zero_oper_fun%user_ctx)
    #endif
        nullify(zero_oper_fun%get_zero_oper_contrib)
    end subroutine RSPZeroOperDestroy_f

end module RSPZeroOper_f

#undef OPENRSP_API_SRC

```

183 $\langle RSPSolver.F90$ 183 $\rangle \equiv$
 $\langle OpenRSPLicenseFortran$ 119a \rangle

```

!! 2014-08-06, Bin Gao
!! * first version

! basic data types
#include "api/qcmatrix_c_type.h"

#define OPENRSP_API_SRC "src/fortran/RSPSolver.F90"

module RSPSolver_f

    use, intrinsic :: iso_c_binding
    use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR

    implicit none

    integer(kind=4), private, parameter :: STDOUT = 6

    ! user specified callback subroutine
    abstract interface
        subroutine SolverRun_f(num_pert,      &
                               num_comps,     &
                               num_freq_sums, &
                               freq_sums,     &
                               RHS_mat,       &
    #if defined(OPENRSP_F_USER_CONTEXT)
                               len_ctx,       &
                               user_ctx,      &

```

```

#endif

      rsp_param)
      use qcmatrix_f, only: QINT,QREAL,QcMat
      integer(kind=QINT), intent(in) :: num_pert
      integer(kind=QINT), intent(in) :: num_comps(num_pert)
      integer(kind=QINT), intent(in) :: num_freq_sums(num_pert)
      real(kind=QREAL), intent(in) :: freq_sums(2*sum(num_freq_sums))
      type(QcMat), intent(in) :: RHS_mat(dot_product(num_comps,num_freq_sums))
#if defined(OPENRSP_F_USER_CONTEXT)
      integer(kind=QINT), intent(in) :: len_ctx
      character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
      type(QcMat), intent(inout) :: rsp_param(dot_product(num_comps,num_freq_sums))
    end subroutine SolverRun_f
  end interface

  ! context of callback subroutine of response equation solver
  type, public :: SolverFun_f
    private
#if defined(OPENRSP_F_USER_CONTEXT)
    ! user-defined callback function context
    integer(kind=QINT) :: len_ctx = 0
    character(len=1), allocatable :: user_ctx(:)
#endif
    ! callback function
    procedure(SolverRun_f), nopass, pointer :: get_linear_rsp_solution
  end type SolverFun_f

  public :: RSPSolverCreate_f
  public :: RSPSolverGetLinearRSPSolution_f
  public :: RSPSolverDestroy_f

  contains

  !% \brief creates the context of callback subroutine of response equation solver
  ! \author Bin Gao
  ! \date 2014-08-06
  ! \param[SolverFun_f:type]{inout} solver_fun the context of callback subroutine
  ! \param[character]{in} user_ctx user-defined callback function context
  ! \param[subroutine]{in} get_linear_rsp_solution user specified function of
  !% response equation solver
  subroutine RSPSolverCreate_f(solver_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
    user_ctx, &
#endif
    get_linear_rsp_solution)
    type(SolverFun_f), intent(inout) :: solver_fun
#if defined(OPENRSP_F_USER_CONTEXT)
    character(len=1), intent(in) :: user_ctx(:)
#endif
  end subroutine

  interface
    subroutine get_linear_rsp_solution(num_pert, &

```



```

                                user_ctx,      &
                                rsp_param)     &
bind(C, name="RSPSolverGetLinearRSPSolution_f")
integer(kind=C_QINT), value, intent(in) :: num_pert
integer(kind=C_QINT), intent(in) :: num_comps(num_pert)
integer(kind=C_QINT), intent(in) :: num_freq_sums(num_pert)
real(kind=C_QREAL), intent(in) :: freq_sums(2*sum(num_freq_sums))
type(C_PTR), intent(in) :: RHS_mat(dot_product(num_comps,num_freq_sums))
type(C_PTR), value, intent(in) :: user_ctx
type(C_PTR), intent(in) :: rsp_param(dot_product(num_comps,num_freq_sums))
type(SolverFun_f), pointer :: solver_fun      !context of callback subroutine
integer(kind=QINT) size_solution              !size of solution of response equation
type(QcMat), allocatable :: f_RHS_mat(:)      !RHS matrices
type(QcMat), allocatable :: f_rsp_param(:)    !response parameters
integer(kind=4) ierr                          !error information
! converts C pointer to Fortran QcMat type
size_solution = dot_product(num_comps,num_freq_sums)
allocate(f_RHS_mat(size_solution), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPSolverGetLinearRSPSolution_f>> size_solution", &
                           size_solution
    stop "RSPSolverGetLinearRSPSolution_f>> failed to allocate memory for f_RHS_mat"
end if
ierr = QcMat_C_F_POINTER(A=f_RHS_mat, c_A=RHS_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
allocate(f_rsp_param(size_solution), stat=ierr)
if (ierr/=0) then
    write(STDOUT,"(A,I8)") "RSPSolverGetLinearRSPSolution_f>> size_solution", &
                           size_solution
    stop "RSPSolverGetLinearRSPSolution_f>> failed to allocate memory for f_rsp_param"
end if
ierr = QcMat_C_F_POINTER(A=f_rsp_param, c_A=rsp_param)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
! gets the Fortran callback subroutine
call c_f_pointer(user_ctx, solver_fun)
! invokes Fortran callback subroutine to solve the response equation
call solver_fun%get_linear_rsp_solution(num_pert,
                                &
                                num_comps,
                                &
                                num_freq_sums,
                                &
                                freq_sums,
                                &
                                f_RHS_mat,
                                &

#if defined(OPENRSP_F_USER_CONTEXT)
                                solver_fun%len_ctx, &
                                solver_fun%user_ctx, &

#endif

                                f_rsp_param)

! cleans up
nullify(solver_fun)
ierr = QcMat_C_NULL_PTR(A=f_rsp_param)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
ierr = QcMat_C_NULL_PTR(A=f_RHS_mat)
call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)

```

```

        deallocate(f_rsp_param)
        deallocate(f_RHS_mat)
        return
    end subroutine RSPSolverGetLinearRSPSolution_f

    !% \brief cleans the context of callback subroutine of response equation solver
    ! \author Bin Gao
    ! \date 2014-08-06
    !% \param[SolverFun_f:type]{inout} solver_fun the context of callback subroutine
    subroutine RSPSolverDestroy_f(solver_fun)
        type(SolverFun_f), intent(inout) :: solver_fun
    #if defined(OPENRSP_F_USER_CONTEXT)
        solver_fun%len_ctx = 0
        deallocate(solver_fun%user_ctx)
    #endif
        nullify(solver_fun%get_linear_rsp_solution)
    end subroutine RSPSolverDestroy_f

end module RSPSolver_f

```

```
#undef OPENRSP_API_SRC
```

Furthermoe, we implement the following Fortran adapters:

```

187 <OpenRSPFortranAdapter.c 187>≡
    /*
    <OpenRSPLicense 14a>

    2014-07-31, Bin Gao
    * first version
    */

#include "OpenRSP.h"

QErrorCode OpenRSPCreateFortranAdapter(void **open_rsp, const QInt num_atoms)
{
    OpenRSP *c_open_rsp;
    QErrorCode ierr;
    c_open_rsp = (OpenRSP *)malloc(sizeof(OpenRSP));
    if (c_open_rsp==NULL) {
        QErrorExit(FILE_AND_LINE, "failed to allocate memory for c_open_rsp");
    }
    ierr = OpenRSPCreate(c_open_rsp, num_atoms);
    *open_rsp = (void *) (c_open_rsp);
    return ierr;
}

//QErrorCode f_api_OpenRSPSetElecEOM(void **open_rsp,
//                                  const QInt elec_EOM_type)
//{
//    OpenRSP *c_open_rsp;
//    ElecEOMType c_elec_EOM_type;
//    QErrorCode ierr;
//    /* should be consistent with what defined in src/f03/openrsp_f.F90 */

```

```

//      switch (elec_EOM_type) {
//      case 0:
//          c_elec_EOM_type = ELEC_AO_D_MATRIX;
//          break;
//      case 1:
//          c_elec_EOM_type = ELEC_MO_C_MATRIX;
//          break;
//      case 2:
//          c_elec_EOM_type = ELEC_COUPLED_CLUSTER;
//          break;
//      default:
//          return QFAILURE;
//      }
//      c_open_rsp = (OpenRSP *)(*open_rsp);
//      ierr = OpenRSPSetElecEOM(c_open_rsp, c_elec_EOM_type);
//      return ierr;
//}

```

```

QErrorCode OpenRSPWriteFortranAdapter(const void *open_rsp,
                                     const char *file_name)
{
    FILE *fp_rsp;
    OpenRSP *c_open_rsp;
    QErrorCode ierr;
    fp_rsp = fopen(file_name, "a");
    if (fp_rsp==NULL) {
        printf("OpenRSPWriteFortranAdapter>> file name %s\n", file_name);
        QErrorExit(FILE_AND_LINE, "failed to open the file");
    }
    c_open_rsp = (OpenRSP *)open_rsp;
    ierr = OpenRSPWrite(c_open_rsp, fp_rsp);
    fprintf(fp_rsp, "\n");
    fclose(fp_rsp);
    return ierr;
}

```

```

QErrorCode OpenRSPWriteStdOutFortranAdapter(const void *open_rsp)
{
    OpenRSP *c_open_rsp;
    QErrorCode ierr;
    c_open_rsp = (OpenRSP *)open_rsp;
    ierr = OpenRSPWrite(c_open_rsp, stdout);
    fprintf(stdout, "\n");
    return ierr;
}

```

```

QErrorCode OpenRSPDestroyFortranAdapter(void **open_rsp)
{
    OpenRSP *c_open_rsp;
    QErrorCode ierr;
    c_open_rsp = (OpenRSP *)(*open_rsp);
    ierr = OpenRSPDestroy(c_open_rsp);
}

```

```
    *open_rsp = NULL;  
    open_rsp = NULL;  
    return ierr;  
}
```

3.13 Unit Testing

3.13.1 Numerical reference data

To test OPENRSP, we mimic callback functions by reading different data files *.dat. These files were obtained from calculations using Dalton program for the following twisted hydrogen peroxide with STO-3G:

```
H  1.6701141465  -0.1122989688  1.8068721870
H -0.7421983272 -1.5025093539 -1.8068589821
O  0.0475007085  0.0952594669 -1.3682817885
O -0.1137549810  0.0064888625  1.3682805836
```

For the time being, we have the following reference data at Hartree-Fock level as shown in Table 3.1.

Table 3.1: Numerical reference data of the twisted hydrogen peroxide from Dalton program, calculated at Hartree-Fock level with STO-3G basis sets.

Property(frequencies)	k	Files
$\mathcal{L}_{k,0-k}^g(0)$	0	tests/DMathF/E1g
$\mathcal{L}_{k,1-k}^{gg}(0,0)$	0	tests/DMathF/E2g
$\mathcal{L}_{k,2-k}^{ggg}(0,0,0)$	0	tests/DMathF/E3gk0
$\mathcal{L}_{k,2-k}^{ggg}(0,0,0)$	1	tests/DMathF/E3gk1
$\mathcal{L}_{k,3-k}^{gggg}(0,0,0,0)$	1	tests/DMathF/E4g
$\mathcal{L}_{k,0-k}^f(0)$	0	tests/DMathF/E1f
$\mathcal{L}_{k,2-k}^{fff}(0,0,0)$	1	tests/DMathF/E3f
$\mathcal{L}_{k,2-k}^{fff}(-2\omega, \omega, \omega)$	1	tests/DMathF/E3fww
$\mathcal{L}_{k,2-k}^{fff}(-3\omega, \omega, 2\omega)$	1	tests/DMathF/E3fw2w
$\mathcal{L}_{k,4-k}^{ffff}(-2\omega, -\omega, 0, \omega, 2\omega)$	2	tests/DMathF/E5f
$\mathcal{L}_{k,1-k}^{gf}(0,0)$	0	tests/DMathF/E1g1f
$\mathcal{L}_{k,2-k}^{gff}(0,0,0)$	0	tests/DMathF/E1g2f
$\mathcal{L}_{k,4-k}^{gffff}(0, -3\omega, \omega, \omega, \omega)$	0	tests/DMathF/E1g4fk0
$\mathcal{L}_{k,4-k}^{gffff}(0, -3\omega, \omega, \omega, \omega)$	1	tests/DMathF/E1g4fk1
$\mathcal{L}_{k,4-k}^{gggff}(0,0,0, -\omega, \omega)$	2	tests/DMathF/E3g2f
$\mathcal{L}_{k,5-k}^{ggffff}(0,0, -\omega, -\omega, 0, 2\omega)$	1	tests/DMathF/E2g4f

During building, the following CMake file will generate lists of filenames containing the above data files:

```
190 <OpenRSPTestData.cmake 190>≡
# Generated by notangle -ROpenRSPTestData.cmake web/UnitTesting.nw > cmake/OpenRSPTestData.
include_directories(${PROJECT_BINARY_DIR})
set(OPENRSP_TEST_DATA ${PROJECT_BINARY_DIR}/OpenRSPTestData.h)
file(WRITE ${OPENRSP_TEST_DATA} "#if !defined(OPENRSP_TEST_DATA_H)\n")
file(APPEND ${OPENRSP_TEST_DATA} "#define OPENRSP_TEST_DATA_H\n\n")
file(APPEND ${OPENRSP_TEST_DATA} "#include \"qcmatrix.h\"\n\n")
# function of reading matrices from a dat file
file(APPEND ${OPENRSP_TEST_DATA} "extern QErrorCode OpenRSPTestReadMat(const char*,\n")
file(APPEND ${OPENRSP_TEST_DATA} "                                const QInt,\n")
file(APPEND ${OPENRSP_TEST_DATA} "                                const QInt,\n")
file(APPEND ${OPENRSP_TEST_DATA} "                                QcMat*[]);\n\n")
# function of zeroing matrices
```

```

file(APPEND ${OPENRSP_TEST_DATA} "extern QErrorCode OpenRSPTestZeroMat(const QInt,\n")
file(APPEND ${OPENRSP_TEST_DATA} "                                QcMat*[]);\n\n")
# atomic-orbital (AO) density matrix-based response theory
#
# unperturbed AO-based Fock matrix
get_filename_component(DMAT_HF_FOCK
                        ${LIB_OPENRSP_PATH}/tests/DMatHF/FOCK.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define DMAT_HF_FOCK \"${DMAT_HF_FOCK}\"\\n\\n")
# unperturbed AO-based density matrix
get_filename_component(DMAT_HF_DENSITY
                        ${LIB_OPENRSP_PATH}/tests/DMatHF/DENSITY.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define DMAT_HF_DENSITY \"${DMAT_HF_DENSITY}\"\\n\\n")
# unperturbed AO-based overlap integral matrix
get_filename_component(DMAT_OVERLAP
                        ${LIB_OPENRSP_PATH}/tests/DMatHF/OVERLAP.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define DMAT_OVERLAP \"${DMAT_OVERLAP}\"\\n\\n")
# unperturbed AO-based dipole length integral matrices
get_filename_component(DMAT_DIPLIN
                        ${LIB_OPENRSP_PATH}/tests/DMatHF/DIPLIN.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define DMAT_DIPLIN \"${DMAT_DIPLIN}\"\\n\\n")
# two-electron integrals contracted with perturbed AO-based density matrices
# for solving polarizability at frequency as 0.072
get_filename_component(ALPHA_GMAT_AO_HF
                        ${LIB_OPENRSP_PATH}/tests/AlphaGMatAOHF.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define ALPHA_GMAT_AO_HF \"${ALPHA_GMAT_AO_HF}\"\\n\\n")
# response parameters for solving polarizability at frequency as 0.072
get_filename_component(ALPHA_RSPARAM_AO_HF
                        ${LIB_OPENRSP_PATH}/tests/AlphaRSPParamAOHF.dat
                        ABSOLUTE)

file(APPEND
      ${OPENRSP_TEST_DATA}
      "#define ALPHA_RSPARAM_AO_HF \"${ALPHA_RSPARAM_AO_HF}\"\\n\\n")
file(APPEND ${OPENRSP_TEST_DATA} "\n#endif\n")

```

The following file will read a *.dat file and put the data into matrices:

```

191 <OpenRSPTestData.c 191>≡
/*
    <OpenRSPLicense 14a>

```

```

*/

#ifdef QCMATRIX_SINGLE_PRECISION
#define QCREAL_FMT "f"
#else
#define QCREAL_FMT "lf"
#endif

#include "OpenRSPTTestData.h"

/* <function name='OpenRSPTTestReadMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-18'>
    Reads a dat file and puts the data into matrices
    <param name='file_mat' direction='in'>
        Name of the dat file
    </param>
    <param name='num_skip_mat' direction='in'>
        Number of the first few matrices to skip
    </param>
    <param name='num_read_mat' direction='in'>
        Number of matrices to read
    </param>
    <param name='mat_read' direction='inout'>
        Matrices read
    </param>
    <return>Error information</return>
</function> */
QErrorCode OpenRSPTTestReadMat(const char *file_mat,
                                const QInt num_skip_mat,
                                const QInt num_read_mat,
                                QcMat *mat_read[])
{
    FILE *fp_dat;          /* file pointer */
    QInt dat_num_read;      /* number of arguments read from the dat file */
    QInt dat_num_mat;       /* number of matrices in the dat file */
    QInt dat_num_row;       /* number of rows of matrices */
    QInt dat_num_col;       /* number of columns of matrices */
    QInt dat_num_val;       /* number of values of matrices */
    QReal *dat_real_elms;   /* elements of real part */
    QReal *dat_imag_elms;   /* elements of imaginary part */
    QInt imat;              /* incremental recorder over matrices */
    QInt ival;              /* incremental recorder over values */
    QErrorCode ierr;        /* error information */
    /* parameters for setting matrices */
    const QInt NUM_BLOCKS=1;
#ifdef ZERO_BASED_NUMBERING
    const QInt IDX_BLOCK_ROW[]={0};
    const QInt IDX_BLOCK_COL[]={0};
    const QInt IDX_FIRST_ROW=0;
    const QInt IDX_FIRST_COL=0;

```



```

#else
    const QInt IDX_BLOCK_ROW[]={1};
    const QInt IDX_BLOCK_COL[]={1};
    const QInt IDX_FIRST_ROW=1;
    const QInt IDX_FIRST_COL=1;
#endif

    QcSymType sym_type;
    QcDataType data_type[1];
    fp_dat = fopen(file_mat, "r");
    if (fp_dat==NULL) {
        printf("OpenRSPTTestReadMat>> file: %s\n", file_mat);
        QErrorExit(FILE_AND_LINE, "open the dat file");
    }
    /* reads the number of matrices */
    if (fscanf(fp_dat, "%QINT_FMT", &dat_num_mat)!=1) {
        QErrorExit(FILE_AND_LINE, "read number of matrices");
    }
    /* checks the number of matrices to read */
    if (num_skip_mat+num_read_mat>dat_num_mat) {
        printf("OpenRSPTTestReadMat>> number of skipping matrices %QINT_FMT\n",
            num_skip_mat);
        printf("OpenRSPTTestReadMat>> number of reading matrices %QINT_FMT\n",
            num_read_mat);
        printf("OpenRSPTTestReadMat>> number of matrices on the file %QINT_FMT\n",
            dat_num_mat);
        QErrorExit(FILE_AND_LINE, "not enough matrices on the file");
    }
    /* skips the first few matrices, including the '\n' of the first line */
    dat_num_read = fgetc(fp_dat);
    for (imat=0; imat<num_skip_mat; imat++) {
        /*fscanf(fp_dat, "%*[^\\n]\\n", NULL);*/
        /* reads the information of matrix */
        dat_num_read = fscanf(fp_dat,
            "%d %d %QINT_FMT %QINT_FMT",
            &sym_type, &data_type[0], &dat_num_row, &dat_num_col);
        if (dat_num_read!=4) {
            printf("OpenRSPTTestReadMat>> number of arguments read %QINT_FMT\n",
                dat_num_read);
            QErrorExit(FILE_AND_LINE, "read information of matrix");
        }
        dat_num_read = fgetc(fp_dat);
        do {
            dat_num_read = fgetc(fp_dat);
        } while (dat_num_read!='\\n');
        /* skips imaginary part */
        if (data_type[0]!=QREALMAT) {
            do {
                dat_num_read = fgetc(fp_dat);
            } while (dat_num_read!='\\n');
        }
    }
    /* initializes the elements of imaginary part */

```

```

dat_imag_elms = NULL;
for (imat=0; imat<num_read_mat; imat++) {
    /* reads the information of matrix */
    dat_num_read = fscanf(fp_dat,
                          "%d %d %"QINT_FMT" %"QINT_FMT"",
                          &sym_type, &data_type[0], &dat_num_row, &dat_num_col);
    if (dat_num_read!=4) {
        printf("OpenRSPTTestReadMat>> number of arguments read %"QINT_FMT"\n",
              dat_num_read);
        QErrorExit(FILE_AND_LINE, "read information of matrix");
    }
    /* allocates memory for elements of real part */
    dat_num_val = dat_num_row*dat_num_col;
    dat_real_elms = (QReal *)malloc(dat_num_val*sizeof(QReal));
    if (dat_real_elms==NULL) {
        printf("OpenRSPTTestReadMat>> matrix %"QINT_FMT"\n",
              imat+num_skip_mat);
        printf("OpenRSPTTestReadMat>> number of elements %"QINT_FMT"\n",
              dat_num_val);
        QErrorExit(FILE_AND_LINE, "allocates memory for elements of real part");
    }
    /* reads elements of real part */
    for (ival=0; ival<dat_num_val; ival++) {
        if (fscanf(fp_dat, %"QCREAL_FMT"", &dat_real_elms[ival])!=1) {
            printf("OpenRSPTTestReadMat>> %"QINT_FMT"-th element\n", ival);
            QErrorExit(FILE_AND_LINE, "read elements of real part");
        }
    }
    if (data_type[0]!=QREALMAT) {
        /* allocates memory for elements of imaginary part */
        dat_imag_elms = (QReal *)malloc(dat_num_val*sizeof(QReal));
        if (dat_imag_elms==NULL) {
            printf("OpenRSPTTestReadMat>> matrix %"QINT_FMT"\n",
                  imat+num_skip_mat);
            printf("OpenRSPTTestReadMat>> number of elements %"QINT_FMT"\n",
                  dat_num_val);
            QErrorExit(FILE_AND_LINE, "allocates memory for elements of imaginary part");
        }
        /* reads elements of imaginary part */
        for (ival=0; ival<dat_num_val; ival++) {
            if (fscanf(fp_dat, %"QCREAL_FMT"", &dat_imag_elms[ival])!=1) {
                printf("OpenRSPTTestReadMat>> %"QINT_FMT"-th element\n", ival);
                QErrorExit(FILE_AND_LINE, "read elements of imaginary part");
            }
        }
    }
    /* creates the matrix */
    ierr = QcMatCreate(mat_read[imat]);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatCreate()");
    ierr = QcMatBlockCreate(mat_read[imat], NUM_BLOCKS);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatBlockCreate()");
    ierr = QcMatSetSymType(mat_read[imat], sym_type);

```

```

QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetSymType()");
ierr = QcMatSetDataType(mat_read[imat],
                        NUM_BLOCKS,
                        IDX_BLOCK_ROW,
                        IDX_BLOCK_COL,
                        data_type);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDataType()");
ierr = QcMatSetDimMat(mat_read[imat], dat_num_row, dat_num_col);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDimMat()");
ierr = QcMatAssemble(mat_read[imat]);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatAssemble()");
/* saves the values into the matrix */
ierr = QcMatSetValues(mat_read[imat],
                    IDX_BLOCK_ROW[0],
                    IDX_BLOCK_COL[0],
                    IDX_FIRST_ROW,
                    dat_num_row,
                    IDX_FIRST_COL,
                    dat_num_col,
                    dat_real_elms,
                    dat_imag_elms);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetValues()");
free(dat_real_elms);
dat_real_elms = NULL;
if (dat_imag_elms!=NULL) {
    free(dat_imag_elms);
    dat_imag_elms = NULL;
}
}
fclose(fp_dat);
return QSUCCESS;
}

```

The following function will zero out a few matrices:

```

195  <OpenRSPTTestData.c 191>+≡
/* <function name='OpenRSPTTestZeroMat'
    attr='private'
    author='Bin Gao'
    date='2015-10-18'>
Zero out a few matrices
<param name='num_mat' direction='in'>
    Number of matrices to be zeroed out
</param>
<param name='mat_zero' direction='inout'>
    Matrices to be zeroed out
</param>
<return>Error information</return>
</function> */
QErrorCode OpenRSPTTestZeroMat(const QInt num_mat, QcMat *mat_zero[])
{
    QInt imat;          /* incremental recorder over matrices */
    QErrorCode ierr;    /* error information */
    /* parameters for setting matrices */

```

```

    const QInt NUM_BLOCKS=1;
#if defined(ZERO_BASED_NUMBERING)
    const QInt IDX_BLOCK_ROW[]={0};
    const QInt IDX_BLOCK_COL[]={0};
#else
    const QInt IDX_BLOCK_ROW[]={1};
    const QInt IDX_BLOCK_COL[]={1};
#endif
    QcDataType DATA_TYPE[1]={QREALMAT};
    const QInt DAT_NUM_ROW=32;
    const QInt DAT_NUM_COL=32;
    for (imat=0; imat<num_mat; imat++) {
        ierr = QcMatCreate(mat_zero[imat]);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatCreate()");
        ierr = QcMatBlockCreate(mat_zero[imat], NUM_BLOCKS);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatBlockCreate()");
        ierr = QcMatSetSymType(mat_zero[imat], QSYMMAT);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetSymType()");
        ierr = QcMatSetDataType(mat_zero[imat],
                                NUM_BLOCKS,
                                IDX_BLOCK_ROW,
                                IDX_BLOCK_COL,
                                DATA_TYPE);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDataType()");
        ierr = QcMatSetDimMat(mat_zero[imat], DAT_NUM_ROW, DAT_NUM_COL);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDimMat()");
        ierr = QcMatAssemble(mat_zero[imat]);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatAssemble()");
        ierr = QcMatZeroEntries(mat_zero[imat]);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatZeroEntries()");
    }
    return QSUCCESS;
}

```

3.13.2 Testing C APIs

We first implement perturbations and its callback function for unit testing:

```

196 <OpenRSPTestPerturbations.h 196>≡
    /*
        <OpenRSPLicense 14a>

```

This is the header file of perturbations.

```

    2014-07-31, Bin Gao:
    * first version
    */

```

```

#include "OpenRSP.h"

```

```

#define NUM_ALL_PERT 3
#define PERT_GEOMETRIC 1

```

```

#define PERT_DIPOLE 2
#define PERT_MAGNETIC 5
#define MAX_ORDER_GEOMETRIC 7
#define MAX_ORDER_DIPOLE 1
#define MAX_ORDER_MAGNETIC 7

extern const QcPertInt ALL_PERT_LABELS[NUM_ALL_PERT];
extern const QInt ALL_PERT_MAX_ORDERS[NUM_ALL_PERT];
extern const QInt ALL_PERT_SIZES[15];
extern const QInt NUM_ATOMS;

```

197a $\langle \text{OpenRSPTestPerturbations.c } 197a \rangle \equiv$

```

/*
  \langle \text{OpenRSPLicense } 14a \rangle
*/

#include "OpenRSPTestPerturbations.h"

/* labels of all perturbations */
const QcPertInt ALL_PERT_LABELS[]={PERT_GEOMETRIC,
                                   PERT_DIPOLE,
                                   PERT_MAGNETIC};
/* allowed maximal orders of all perturbations */
const QInt ALL_PERT_MAX_ORDERS[]={MAX_ORDER_GEOMETRIC,
                                   MAX_ORDER_DIPOLE,
                                   MAX_ORDER_MAGNETIC};
/* sizes of all perturbations up to their maximal orders */
const QInt ALL_PERT_SIZES[]={
    12,78,364,1365,4368,12376,31824, /* geometric derivatives (4 atoms) */
    3,                               /* electric dipole */
    3,6,10,15,21,28,36};           /* magnetic derivatives */
const QInt NUM_ATOMS=4;

```

Here we have used three different perturbation labels for geometric, dipole length and magnetic perturbations.

197b $\langle \text{OpenRSPPertCallback.h } 197b \rangle \equiv$

```

/*
  \langle \text{OpenRSPLicense } 14a \rangle

  This is the header file of perturbations' callback function.

  2014-07-31, Bin Gao:
  * first version
*/

#if !defined(OPENRSP_PERT_CALLBACK_H)
#define OPENRSP_PERT_CALLBACK_H

#include "OpenRSP.h"

#if defined(OPENRSP_C_USER_CONTEXT)
#define PERT_CONTEXT "NRNZGEO"
#endif

```

```

extern void get_pert_concatenation(const QInt,
                                   const QcPertInt,
                                   const QInt,
                                   const QInt,
                                   const QInt*,
                                   void*,
                                   QInt*);

```

```

#endif

```

198a $\langle \text{OpenRSPPertCallback.c } 198a \rangle \equiv$

```

/*
   $\langle \text{OpenRSPLicense } 14a \rangle$ 
*/

```

```

#include "OpenRSPPertCallback.h"

```

```

void get_pert_concatenation(const QInt pert_label,
                            const QcPertInt first_cat_comp,
                            const QInt num_cat_comps,
                            const QInt num_sub_tuples,
                            const QInt *len_sub_tuples,
                            void *user_ctx,
                            QInt *rank_sub_comps)
{
  /*FIXME: to implement*/
}

```

The following header and C files implement the callback function for zero-electron operator (nuclear Hamiltonian):

198b $\langle \text{OpenRSPZeroOperCallback.h } 198b \rangle \equiv$

```

/*
   $\langle \text{OpenRSPLicense } 14a \rangle$ 

```

This header file contains callback function for zero-electron operator (nuclear Hamiltonian).

```

2015-10-16, Bin Gao:
* first version
*/

```

```

#if !defined(OPENRSP_ZERO_OPER_CALLBACK_H)
#define OPENRSP_ZERO_OPER_CALLBACK_H

```

```

#include "OpenRSP.h"

```

```

#if defined(OPENRSP_C_USER_CONTEXT)
#define ZERO_OPER_CONTEXT "ZERO_OPER"
#endif

```

```

extern void get_zero_oper_contrib(const QInt,
                                  const QcPertInt*,
                                  const QInt*,
                                  void*,
                                  const QInt,
                                  QReal*);

#endif

```

199a $\langle \text{OpenRSPZeroOperCallback.c } 199a \rangle \equiv$
 /*
 $\langle \text{OpenRSPLicense } 14a \rangle$
 */

```
#include "OpenRSPZeroOperCallback.h"
```

```

void get_zero_oper_contrib(const QInt oper_num_pert,
                          const QcPertInt *oper_pert_labels,
                          const QInt *oper_pert_orders,
                          void *user_ctx,
                          const QInt size_pert,
                          QReal *val_oper)
{
  /*FIXME: to implement*/
}

```

We next implement callback functions for AO-based response theory calculations:

199b $\langle \text{OpenRSPDMatCallback.h } 199b \rangle \equiv$
 /*
 $\langle \text{OpenRSPLicense } 14a \rangle$

This header file contains callback functions for AO-based response theory calculations.

```

2015-10-16, Bin Gao:
* first version
*/

```

```

#if !defined(OPENRSP_DMAT_CALLBACK_H)
#define OPENRSP_DMAT_CALLBACK_H

```

```

#include "OpenRSP.h"
#include "OpenRSPTestData.h"

```

```

#if defined(OPENRSP_C_USER_CONTEXT)
#define OVERLAP_CONTEXT "OVERLAP"
#define ONEHAM_CONTEXT "ONEHAM"
#define EXT_FIELD_CONTEXT "EXT_FIELD"
#define TWO_OPER_CONTEXT "NONLAO"
#define SOLVER_CONTEXT "SOLVER"

```

```
#endif
```

```
extern void get_overlap_mat(const QInt,
                           const QcPertInt*,
                           const QInt*,
                           const QInt,
                           const QcPertInt*,
                           const QInt*,
                           const QInt,
                           const QcPertInt*,
                           const QInt*,
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
    void*,
```

```
#endif
```

```
    const QInt,
    QcMat*[]);
extern void get_overlap_exp(const QInt,
                           const QcPertInt*,
                           const QInt*,
                           const QInt,
                           const QcPertInt*,
                           const QInt*,
                           const QInt,
                           const QcPertInt*,
                           const QInt*,
                           const QInt,
                           QcMat*[],
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
    void*,
```

```
#endif
```

```
    const QInt,
    QReal*);
extern void get_one_oper_mat(const QInt,
                             const QcPertInt*,
                             const QInt*,
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
    void*,
```

```
#endif
```

```
    const QInt,
    QcMat*[]);
extern void get_one_oper_exp(const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             QcMat*[],
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
    void*,
```

```
#endif
```

```
    const QInt,
    QReal*);
extern void get_two_oper_mat(const QInt,
                             const QcPertInt*,
```



```

        const QInt*,
        const QInt,
        QcMat*[],
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif

        const QInt,
        QcMat*[]);
extern void get_two_oper_exp(const QInt,
        const QcPertInt*,
        const QInt*,
        const QInt,
        const QInt*,
        QcMat*[],
        const QInt*,
        QcMat*[],
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif

        const QInt,
        QReal*);
extern void get_linear_rsp_solution(const QInt,
        const QInt*,
        const QInt*,
        const QReal*,
        QcMat*[],
#ifdef OPENRSP_C_USER_CONTEXT
        void*,
#endif

        QcMat*[]);

#endif

```

By using the functions developed in Subsection 3.13.1, we can implement the following file callback functions to read matrices from *.dat files for the AO-based response theory calculations:

201 *⟨OpenRSPDMatCallback.c 201⟩*≡

```

/*
  ⟨OpenRSPLicense 14a⟩
*/

#include "OpenRSPDMatCallback.h"

void get_overlap_mat(const QInt bra_num_pert,
        const QcPertInt *bra_pert_labels,
        const QInt *bra_pert_orders,
        const QInt ket_num_pert,
        const QcPertInt *ket_pert_labels,
        const QInt *ket_pert_orders,
        const QInt oper_num_pert,
        const QcPertInt *oper_pert_labels,
        const QInt *oper_pert_orders,
#ifdef OPENRSP_C_USER_CONTEXT
        void *user_ctx,

```

```

#endif

        const QInt num_int,
        QcMat *val_int[])

{
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *overlap_context;
#endif
    QcMat **tmp_int;
    const QReal NUMBER_ONE[]={1.0,0.0};
    QBool zero_int;
    QErrorCode ierr;
    QInt ilab;
#if defined(OPENRSP_C_USER_CONTEXT)
    overlap_context = (char *)user_ctx;
    if (strcmp(overlap_context, OVERLAP_CONTEXT)!=0) {
        printf("get_overlap_mat>> incorrect operator at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
    switch (oper_num_pert) {
    case 0:
        switch (bra_num_pert) {
        case 0:
            switch (ket_num_pert) {
            case 0:
                /* unperturbed AO-based overlap integral matrix */
                tmp_int = (QcMat **)malloc(sizeof(QcMat *));
                if (tmp_int==NULL) {
                    printf("get_overlap_mat>> error happened at %s: %s\n",
                        FILE_AND_LINE,
                        "allocates memory for temporary matrix array");
                    exit(QFAILURE);
                }
                tmp_int[0] = (QcMat *)malloc(sizeof(QcMat));
                if (tmp_int[0]==NULL) {
                    printf("get_overlap_mat>> error happened at %s: %s\n",
                        FILE_AND_LINE,
                        "allocates memory for temporary matrices");
                    exit(QFAILURE);
                }
                ierr = OpenRSPTestReadMat(DMAT_OVERLAP, 0, 1, tmp_int);
                if (ierr!=QSUCCESS) {
                    printf("get_overlap_mat>> error happened at %s: %s\n",
                        FILE_AND_LINE,
                        "calling OpenRSPTestReadMat()");
                    exit(ierr);
                }
                ierr = QcMatAXPY(NUMBER_ONE, tmp_int[0], val_int[0]);
                if (ierr!=QSUCCESS) {
                    printf("get_overlap_mat>> error happened at %s: %s\n",

```

```

        FILE_AND_LINE,
        "calling QcMatAXPY()");
    exit(ierr);
}
ierr = QcMatDestroy(tmp_int[0]);
if (ierr!=QSUCCESS) {
    printf("get_overlap_mat>> error happened at %s: %s\n",
        FILE_AND_LINE,
        "calling QcMatDestroy()");
    exit(ierr);
}
free(tmp_int[0]);
tmp_int[0] = NULL;
free(tmp_int);
tmp_int = NULL;
break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<ket_num_pert; ilab++) {
        if (ket_pert_labels[ilab]!=PERT_GEOMETRIC &&
            ket_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_overlap_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}
break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<bra_num_pert; ilab++) {
        if (bra_pert_labels[ilab]!=PERT_GEOMETRIC &&
            bra_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_overlap_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}
break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<oper_num_pert; ilab++) {
        if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&

```

```

        oper_pert_labels[ilab] != PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int == QFALSE) {
        printf("get_overlap_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}

void get_overlap_exp(const QInt bra_num_pert,
                    const QcPertInt *bra_pert_labels,
                    const QInt *bra_pert_orders,
                    const QInt ket_num_pert,
                    const QcPertInt *ket_pert_labels,
                    const QInt *ket_pert_orders,
                    const QInt oper_num_pert,
                    const QcPertInt *oper_pert_labels,
                    const QInt *oper_pert_orders,
                    const QInt num_dens,
                    QcMat *ao_dens[],
#ifdef OPENRSP_C_USER_CONTEXT
                    void *user_ctx,
#endif
                    const QInt num_exp,
                    QReal *val_exp)
{
#include "OpenRSPTestPerturbations.h"
#ifdef OPENRSP_C_USER_CONTEXT
    char *overlap_context;
#endif
    QcMat *val_int[1];
    QInt idens;
    QBool zero_int;
    QErrorCode ierr;
    QInt ilab;
#ifdef OPENRSP_C_USER_CONTEXT
    overlap_context = (char *)user_ctx;
    if (strcmp(overlap_context, OVERLAP_CONTEXT) != 0) {
        printf("get_overlap_mat>> incorrect operator at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
    switch (oper_num_pert) {
    case 0:
        switch (bra_num_pert) {
        case 0:
            switch (ket_num_pert) {

```

```

case 0:
    /* unperturbed AO-based overlap integral matrix */
    val_int[0] = (QcMat *)malloc(sizeof(QcMat));
    if (val_int[0]==NULL) {
        printf("get_overlap_exp>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "allocats memory for matrix");
        exit(QFAILURE);
    }
    ierr = OpenRSPTTestReadMat(DMAT_OVERLAP, 0, 1, val_int);
    if (ierr!=QSUCCESS) {
        printf("get_overlap_mat>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling OpenRSPTTestReadMat()");
        exit(ierr);
    }
    for (idens=0; idens<num_dens; idens++) {
        ierr = QcMatGetMatProdTrace(val_int[0],
            ao_dens[idens],
            MAT_NO_OPERATION,
            1,
            &val_exp[2*idens]);

        if (ierr!=QSUCCESS) {
            printf("get_overlap_exp>> error happened at %s: %s\n",
                FILE_AND_LINE,
                "calling QcMatGetMatProdTrace");
            exit(ierr);
        }
    }
    ierr = QcMatDestroy(val_int[0]);
    if (ierr!=QSUCCESS) {
        printf("get_overlap_exp>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling QcMatDestroy()");
        exit(ierr);
    }
    free(val_int[0]);
    val_int[0] = NULL;
    break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<ket_num_pert; ilab++) {
        if (ket_pert_labels[ilab]!=PERT_GEOMETRIC &&
            ket_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_overlap_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }

```

```

        }
    }
    break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<bra_num_pert; ilab++) {
        if (bra_pert_labels[ilab]!=PERT_GEOMETRIC &&
            bra_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_overlap_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}
break;
default:
    zero_int = QFALSE;
    for (ilab=0; ilab<oper_num_pert; ilab++) {
        if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
            oper_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_overlap_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}
}

void get_one_oper_mat(const QInt oper_num_pert,
                    const QcPertInt *oper_pert_labels,
                    const QInt *oper_pert_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                    void *user_ctx,
#endif
                    const QInt num_int,
                    QcMat *val_int[])
{
#include "OpenRSPTestPerturbations.h"
#ifdef OPENRSP_C_USER_CONTEXT
    char *one_oper_context;
#endif
    QcMat **tmp_int;
    const QReal NUMBER_ONE[]={1.0,0.0};
    QBool zero_int;

```

```

    QErrorCode ierr;
    QInt ilab;
#ifdef OPENRSP_C_USER_CONTEXT
    one_oper_context = (char *)user_ctx;
    if (strcmp(one_oper_context, ONEHAM_CONTEXT)==0) {
        zero_int = QFALSE;
        for (ilab=0; ilab<oper_num_pert; ilab++) {
            if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
                oper_pert_labels[ilab]!=PERT_MAGNETIC) {
                zero_int = QTRUE;
                break;
            }
        }
        if (zero_int==QFALSE) {
            printf("get_one_oper_mat>> not implemented at %s\n",
                FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else if (strcmp(one_oper_context, EXT_FIELD_CONTEXT)==0) {
        zero_int = QFALSE;
        for (ilab=0; ilab<oper_num_pert; ilab++) {
            if ((oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
                oper_pert_labels[ilab]!=PERT_MAGNETIC &&
                oper_pert_labels[ilab]!=PERT_DIPOLE) ||
                (oper_pert_labels[ilab]==PERT_DIPOLE &&
                oper_pert_orders[0]>1)) {
                zero_int = QTRUE;
                break;
            }
        }
        if (zero_int==QFALSE) {
            switch (oper_num_pert) {
            case 1:
                /* unperturbed AO-based dipole length integral matrices */
                if (oper_pert_labels[0]==PERT_DIPOLE && oper_pert_orders[0]==1) {
                    tmp_int = (QcMat **)malloc(3*sizeof(QcMat *));
                    if (tmp_int==NULL) {
                        printf("get_one_oper_mat>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "allocates memory for temporary matrix array");
                        exit(QFAILURE);
                    }
                    for (ilab=0; ilab<3; ilab++) {
                        tmp_int[ilab] = (QcMat *)malloc(sizeof(QcMat));
                        if (tmp_int[ilab]==NULL) {
                            printf("get_one_oper_mat>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "allocates memory for temporary matrices");
                            exit(QFAILURE);
                        }
                    }
                }
            }
        }
    }

```

```

        ierr = OpenRSPTestReadMat(DMAT_DIPLN, 0, 3, tmp_int);
        if (ierr!=QSUCCESS) {
            printf("get_one_oper_mat>> error happened at %s: %s\n",
                FILE_AND_LINE,
                "calling OpenRSPTestReadMat()");
            exit(ierr);
        }
        for (ilab=0; ilab<3; ilab++) {
            ierr = QcMatAXPY(NUMBER_ONE, tmp_int[ilab], val_int[ilab]);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                    FILE_AND_LINE,
                    "calling QcMatAXPY()");
                exit(ierr);
            }
            ierr = QcMatDestroy(tmp_int[ilab]);
            if (ierr!=QSUCCESS) {
                printf("get_overlap_mat>> error happened at %s: %s\n",
                    FILE_AND_LINE,
                    "calling QcMatDestroy()");
                exit(ierr);
            }
            free(tmp_int[ilab]);
            tmp_int[ilab] = NULL;
        }
        free(tmp_int);
        tmp_int = NULL;
    }
    else {
        printf("get_one_oper_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
    break;
default:
    printf("get_one_oper_mat>> not implemented at %s\n",
        FILE_AND_LINE);
    exit(QFAILURE);
}
}
}
else {
    printf("get_one_oper_mat>> unknown one-electron operator at %s\n",
        FILE_AND_LINE);
    exit(QFAILURE);
}
}
#else
zero_int = QFALSE;
for (ilab=0; ilab<oper_num_pert; ilab++) {
    if ((oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
        oper_pert_labels[ilab]!=PERT_MAGNETIC &&
        oper_pert_labels[ilab]!=PERT_DIPOLE) ||

```



```

        (oper_pert_labels[ilab]==PERT_DIPOLE &&
         oper_pert_orders[0]>1)) {
        zero_int = QTRUE;
        break;
    }
}
if (zero_int==QFALSE) {
    switch (oper_num_pert) {
    case 1:
        /* unperturbed AO-based dipole length integral matrices */
        if (oper_pert_labels[0]==PERT_DIPOLE && oper_pert_orders[0]==1) {
            tmp_int = (QcMat **)malloc(3*sizeof(QcMat *));
            if (tmp_int==NULL) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "allocates memory for temporary matrix array");
                exit(QFAILURE);
            }
            for (ilab=0; ilab<3; ilab++) {
                tmp_int[ilab] = (QcMat *)malloc(sizeof(QcMat));
                if (tmp_int[ilab]==NULL) {
                    printf("get_one_oper_mat>> error happened at %s: %s\n",
                           FILE_AND_LINE,
                           "allocates memory for temporary matrices");
                    exit(QFAILURE);
                }
            }
            ierr = OpenRSPTTestReadMat(DMAT_DIPLN, 0, 3, tmp_int);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTTestReadMat()");
                exit(ierr);
            }
            for (ilab=0; ilab<3; ilab++) {
                ierr = QcMatAXPY(NUMBER_ONE, tmp_int[ilab], val_int[ilab]);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_mat>> error happened at %s: %s\n",
                           FILE_AND_LINE,
                           "calling QcMatAXPY()");
                    exit(ierr);
                }
                ierr = QcMatDestroy(tmp_int[ilab]);
                if (ierr!=QSUCCESS) {
                    printf("get_overlap_mat>> error happened at %s: %s\n",
                           FILE_AND_LINE,
                           "calling QcMatDestroy()");
                    exit(ierr);
                }
                free(tmp_int[ilab]);
                tmp_int[ilab] = NULL;
            }
        }
    }
}

```

```

        free(tmp_int);
        tmp_int = NULL;
    }
    else {
        printf("get_one_oper_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
    break;
default:
    printf("get_one_oper_mat>> not implemented at %s\n",
        FILE_AND_LINE);
    exit(QFAILURE);
}
}
#endif
}

void get_one_oper_exp(const QInt oper_num_pert,
                    const QcPertInt *oper_pert_labels,
                    const QInt *oper_pert_orders,
                    const QInt num_dmat,
                    QcMat *dens_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
                    void *user_ctx,
#endif
                    const QInt num_exp,
                    QReal *val_exp)
{
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *one_oper_context;
#endif
    QcMat *val_int[1];
    QBool zero_int;
    QInt offset_exp;
    QInt ilab;
    QInt idens;
    QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    one_oper_context = (char *)user_ctx;
    if (strcmp(one_oper_context, ONEHAM_CONTEXT)==0) {
        zero_int = QFALSE;
        for (ilab=0; ilab<oper_num_pert; ilab++) {
            if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
                oper_pert_labels[ilab]!=PERT_MAGNETIC) {
                zero_int = QTRUE;
                break;
            }
        }
    }
    if (zero_int==QFALSE) {
        printf("get_one_oper_exp>> not implemented at %s\n",

```

```

        FILE_AND_LINE);
    exit(QFAILURE);
}
}
else if (strcmp(one_oper_context, EXT_FIELD_CONTEXT)==0) {
    zero_int = QFALSE;
    for (ilab=0; ilab<oper_num_pert; ilab++) {
        if ((oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
            oper_pert_labels[ilab]!=PERT_MAGNETIC &&
            oper_pert_labels[ilab]!=PERT_DIPOLE) ||
            (oper_pert_labels[ilab]==PERT_DIPOLE &&
            oper_pert_orders[0]>1)) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        switch (oper_num_pert) {
            case 1:
                /* unperturbed AO-based dipole length integral matrices */
                if (oper_pert_labels[0]==PERT_DIPOLE && oper_pert_orders[0]==1) {
                    val_int[0] = (QcMat *)malloc(sizeof(QcMat));
                    if (val_int[0]==NULL) {
                        printf("get_one_oper_exp>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "allocats memory for matrix");
                        exit(QFAILURE);
                    }
                    offset_exp = 0;
                    for (ilab=0; ilab<3; ilab++) {
                        ierr = OpenRSPTTestReadMat(DMAT_DIPLIN, ilab, 1, val_int);
                        if (ierr!=QSUCCESS) {
                            printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling OpenRSPTTestReadMat()");
                            exit(ierr);
                        }
                    }
                    for (idens=0; idens<num_dmat; idens++) {
                        ierr = QcMatGetMatProdTrace(val_int[0],
                                                    dens_mat[idens],
                                                    MAT_NO_OPERATION,
                                                    1,
                                                    &val_exp[offset_exp+2*idens]);

                        if (ierr!=QSUCCESS) {
                            printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling QcMatGetMatProdTrace()");
                            exit(ierr);
                        }
                    }
                    ierr = QcMatDestroy(val_int[0]);
                    if (ierr!=QSUCCESS) {

```

```

        printf("get_one_oper_exp>> error happened at %s: %s\n",
               FILE_AND_LINE,
               "calling QcMatDestroy()");
        exit(ierr);
    }
    offset_exp += 2*num_dmat;
}
free(val_int[0]);
val_int[0] = NULL;
}
else {
    printf("get_one_oper_exp>> not implemented at %s\n",
           FILE_AND_LINE);
    exit(QFAILURE);
}
break;
default:
    printf("get_one_oper_exp>> not implemented at %s\n",
           FILE_AND_LINE);
    exit(QFAILURE);
}
}
}
else {
    printf("get_one_oper_exp>> unknown one-electron operator at %s\n",
           FILE_AND_LINE);
    exit(QFAILURE);
}
#else
zero_int = QFALSE;
for (ilab=0; ilab<oper_num_pert; ilab++) {
    if ((oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
        oper_pert_labels[ilab]!=PERT_MAGNETIC &&
        oper_pert_labels[ilab]!=PERT_DIPOLE) ||
        (oper_pert_labels[ilab]==PERT_DIPOLE &&
        oper_pert_orders[0]>1)) {
        zero_int = QTRUE;
        break;
    }
}
if (zero_int==QFALSE) {
    switch (oper_num_pert) {
    case 1:
        /* unperturbed A0-based dipole length integral matrices */
        if (oper_pert_labels[0]==PERT_DIPOLE && oper_pert_orders[0]==1) {
            val_int[0] = (QcMat *)malloc(sizeof(QcMat));
            if (val_int[0]==NULL) {
                printf("get_one_oper_exp>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "allocats memory for matrix");
                exit(QFAILURE);
            }

```

```

        offset_exp = 0;
        for (ilab=0; ilab<3; ilab++) {
            ierr = OpenRSPTTestReadMat(DMAT_DIPLN, ilab, 1, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_exp>> error happened at %s: %s\n",
                    FILE_AND_LINE,
                    "calling OpenRSPTTestReadMat()");
                exit(ierr);
            }
            for (idens=0; idens<num_dmat; idens++) {
                ierr = QcMatGetMatProdTrace(val_int[0],
                    dens_mat[idens],
                    MAT_NO_OPERATION,
                    1,
                    &val_exp[offset_exp+2*idens]);

                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_exp>> error happened at %s: %s\n",
                        FILE_AND_LINE,
                        "calling QcMatGetMatProdTrace()");
                    exit(ierr);
                }
            }
            ierr = QcMatDestroy(val_int[0]);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_exp>> error happened at %s: %s\n",
                    FILE_AND_LINE,
                    "calling QcMatDestroy()");
                exit(ierr);
            }
            offset_exp += 2*num_dmat;
        }
        free(val_int[0]);
        val_int[0] = NULL;
    }
    else {
        printf("get_one_oper_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
    break;
default:
    printf("get_one_oper_exp>> not implemented at %s\n",
        FILE_AND_LINE);
    exit(QFAILURE);
}

}
#endif
}

void get_two_oper_mat(const QInt oper_num_pert,
    const QcPertInt *oper_pert_labels,
    const QInt *oper_pert_orders,

```

```

        const QInt num_dmat,
        QcMat *dens_mat[],
#ifdef OPENRSP_C_USER_CONTEXT
        void *user_ctx,
#endif

        const QInt num_int,
        QcMat *val_int[])

{
#include "OpenRSPTestPerturbations.h"
#ifdef OPENRSP_C_USER_CONTEXT
    char *two_oper_context;
#endif
    QcMat **tmp_int;
    const QReal NUMBER_ONE[]={1.0,0.0};
    QBool zero_int;
    QErrorCode ierr;
    QInt ilab;
    static QInt id_gmat = -1;
#ifdef OPENRSP_C_USER_CONTEXT
    two_oper_context = (char *)user_ctx;
    if (strcmp(two_oper_context, TWO_OPER_CONTEXT)!=0) {
        printf("get_two_oper_mat>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
    zero_int = QFALSE;
    for (ilab=0; ilab<oper_num_pert; ilab++) {
        if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
            oper_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        /* two-electron integrals contracted with perturbed AO-based density
           matrices for solving polarizability at frequency as 0.072 */
        if (oper_num_pert==0){
            id_gmat++;
            if (id_gmat>5) {
                printf("get_two_oper_mat>> not implemented at %s\n",
                    FILE_AND_LINE);
                exit(QFAILURE);
            }
            tmp_int = (QcMat **)malloc(sizeof(QcMat *));
            if (tmp_int==NULL) {
                printf("get_two_oper_mat>> error happened at %s: %s\n",
                    FILE_AND_LINE,
                    "allocates memory for temporary matrix array");
                exit(QFAILURE);
            }
            tmp_int[0] = (QcMat *)malloc(sizeof(QcMat));

```

```

    if (tmp_int[0]==NULL) {
        printf("get_two_oper_mat>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "allocates memory for temporary matrices");
        exit(QFAILURE);
    }
    ierr = OpenRSPTTestReadMat(ALPHA_GMAT_AO_HF, id_gmat, 1, tmp_int);
    if (ierr!=QSUCCESS) {
        printf("get_two_oper_mat>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling OpenRSPTTestReadMat()");
        exit(ierr);
    }
    ierr = QcMatAXPY(NUMBER_ONE, tmp_int[0], val_int[0]);
    if (ierr!=QSUCCESS) {
        printf("get_two_oper_mat>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling QcMatAXPY()");
        exit(ierr);
    }
    ierr = QcMatDestroy(tmp_int[0]);
    if (ierr!=QSUCCESS) {
        printf("get_two_oper_mat>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling QcMatDestroy()");
        exit(ierr);
    }
    free(tmp_int[0]);
    tmp_int[0] = NULL;
    free(tmp_int);
    tmp_int = NULL;
}
else {
    printf("get_two_oper_mat>> not implemented at %s\n",
        FILE_AND_LINE);
    exit(QFAILURE);
}
}
}

void get_two_oper_exp(const QInt oper_num_pert,
    const QcPertInt *oper_pert_labels,
    const QInt *oper_pert_orders,
    const QInt dmat_len_tuple,
    const QInt *num_LHS_dmat,
    QcMat *LHS_dens_mat[],
    const QInt *num_RHS_dmat,
    QcMat *RHS_dens_mat[],
#ifdef OPENRSP_C_USER_CONTEXT
    void *user_ctx,
#endif
    const QInt num_exp,

```

```

        QReal *val_exp)
{
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *two_oper_context;
#endif
    QBool zero_int;
    QErrorCode ierr;
    QInt ilab;
#if defined(OPENRSP_C_USER_CONTEXT)
    two_oper_context = (char *)user_ctx;
    if (strcmp(two_oper_context, TWO_OPER_CONTEXT)!=0) {
        printf("get_two_oper_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
    zero_int = QFALSE;
    for (ilab=0; ilab<oper_num_pert; ilab++) {
        if (oper_pert_labels[ilab]!=PERT_GEOMETRIC &&
            oper_pert_labels[ilab]!=PERT_MAGNETIC) {
            zero_int = QTRUE;
            break;
        }
    }
    if (zero_int==QFALSE) {
        printf("get_two_oper_exp>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
}

void get_linear_rsp_solution(const QInt num_pert,
                            const QInt *num_comps,
                            const QInt *num_freq_sums,
                            const QReal *freq_sums,
                            QcMat *RHS_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
                            void *user_ctx,
#endif
                            QcMat *rsp_param[])
{
#if defined(OPENRSP_C_USER_CONTEXT)
    char *solver_context;
#endif
    static QInt id_rsparam = -1;
    QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    solver_context = (char *)user_ctx;
    if (strcmp(solver_context, SOLVER_CONTEXT)!=0) {
        printf("get_linear_rsp_solution>> invalid context at %s\n",
            FILE_AND_LINE);
    }
}

```



```

        exit(QFAILURE);
    }
#endif
    id_rsparam++;
    if (id_rsparam>2) {
        printf("get_linear_rsp_solution>> not implemented at %s\n",
            FILE_AND_LINE);
        exit(QFAILURE);
    }
    ierr = OpenRSPTTestReadMat(ALPHA_RSPARAM_AO_HF, id_rsparam, 1, rsp_param);
    if (ierr!=QSUCCESS) {
        printf("get_linear_rsp_solution>> error happened at %s: %s\n",
            FILE_AND_LINE,
            "calling OpenRSPTTestReadMat()");
        exit(ierr);
    }
}

```

The atomic-orbital density matrix-based response theory is tested by:

217a $\langle \text{OpenRSPDmatTest.h } 217a \rangle \equiv$

```

/*
  \langle \text{OpenRSPLicense } 14a \rangle

  This is the header file of unit testing of the AO density matrix-based
  response theory.

  2014-07-31, Bin Gao
  * first version
*/
#if !defined(OPENRSP_DMAT_TEST_H)
#define OPENRSP_DMAT_TEST_H

#include "OpenRSPPertCallback.h"
#include "OpenRSPDmatCallback.h"

extern QErrorCode OpenRSPDmatTest(OpenRSP*,FILE*);

#endif

```

217b $\langle \text{OpenRSPDmatTest.c } 217b \rangle \equiv$

```

/*
  \langle \text{OpenRSPLicense } 14a \rangle

  This file tests the AO density matrix-based response theory.

  2014-07-31, Bin Gao
  * first version
*/

#include "OpenRSPDmatTest.h"

#if defined(QCMATRIX_SINGLE_PRECISION)
#define QCREAL_FMT "f"

```

```

#else
#define QCREAL_FMT "lf"
#endif

QErrorCode OpenRSPDMatTest(OpenRSP *open_rsp, FILE *fp_log)
{
#include "OpenRSPTestPerturbations.h"
    /* overlap operator */
    QInt overlap_num_pert=2;
    QcPertInt overlap_pert_labels[]={PERT_GEOMETRIC,
                                     PERT_MAGNETIC};
    QInt overlap_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                MAX_ORDER_MAGNETIC};

    /* one-electron Hamiltonian */
    QInt oneham_num_pert=2;
    QcPertInt oneham_pert_labels[]={PERT_GEOMETRIC,
                                    PERT_MAGNETIC};
    QInt oneham_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                MAX_ORDER_MAGNETIC};

    /* external field */
    QInt ext_field_num_pert=3;
    QcPertInt ext_field_pert_labels[]={PERT_GEOMETRIC,
                                       PERT_DIPOLE,
                                       PERT_MAGNETIC};
    QInt ext_field_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                   MAX_ORDER_DIPOLE,
                                   MAX_ORDER_MAGNETIC};

    /* two-electron operator */
    QInt two_oper_num_pert=2;
    QcPertInt two_oper_pert_labels[]={PERT_GEOMETRIC,
                                       PERT_MAGNETIC};
    QInt two_oper_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                   MAX_ORDER_MAGNETIC};

    /* referenced state */
    QcMat *F_unpert[1];
    QcMat *D_unpert[1];
    QcMat *S_unpert[1];
    /* polarizability */
    QInt ALPHA_NUM_PROPS=1;
    QInt ALPHA_LEN_TUPLE[]={2};
    QcPertInt ALPHA_PERT_TUPLE[]={PERT_DIPOLE,PERT_DIPOLE};
    QInt ALPHA_NUM_FREQ_CONFIGS[]={1};
    QReal ALPHA_PERT_FREQS[]={-0.072,0.0,0.072,0.0};
    QInt ALPHA_KN_RULES[]={0};
    /* response functions */
    QInt size_rsp_funs;
    QReal rsp_funs[18];
    QInt ipert,jpert,ival;
    /* error information */
    QErrorCode ierr;

    /**/ sets the equation of motion of electrons */

```

```

//ierr = OpenRSPSetElecEOM(open_rsp, ELEC_AO_D_MATRIX);
//QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetElecEOM");
//fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPSetElecEOM() passed\n");

/* sets the context of linear response equation solver */
ierr = OpenRSPSetLinearRSPSolver(open_rsp,
#if defined(OPENRSP_C_USER_CONTEXT)
    (void *)SOLVER_CONTEXT,
#endif
    &get_linear_rsp_solution);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetLinearRSPSolver()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPSetLinearRSPSolver() passed\n");

/* sets the context of overlap operator */
ierr = OpenRSPSetOverlap(open_rsp,
    overlap_num_pert,
    overlap_pert_labels,
    overlap_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
    (void *)OVERLAP_CONTEXT,
#endif
    &get_overlap_mat,
    &get_overlap_exp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetOverlap()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPSetOverlap() passed\n");

/* adds one-electron Hamiltonian */
ierr = OpenRSPAddOneOper(open_rsp,
    oneham_num_pert,
    oneham_pert_labels,
    oneham_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
    (void *)ONEHAM_CONTEXT,
#endif
    &get_one_oper_mat,
    &get_one_oper_exp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddOneOper(h)");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPAddOneOper(h) passed\n");

/* adds external field */
ierr = OpenRSPAddOneOper(open_rsp,
    ext_field_num_pert,
    ext_field_pert_labels,
    ext_field_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
    (void *)EXT_FIELD_CONTEXT,
#endif
    &get_one_oper_mat,
    &get_one_oper_exp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddOneOper(V)");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPAddOneOper(V) passed\n");

```

```

/* adds two-electron operator */
ierr = OpenRSPAddTwoOper(open_rsp,
                        two_oper_num_pert,
                        two_oper_pert_labels,
                        two_oper_pert_orders,
#ifdef OPENRSP_C_USER_CONTEXT
                        (void *)TWO_OPER_CONTEXT,
#endif
                        &get_two_oper_mat,
                        &get_two_oper_exp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddTwoOper()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPAddTwoOper() passed\n");

/* assembles the context of response theory calculations */
ierr = OpenRSPAssemble(open_rsp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAssemble()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPAssemble() passed\n");

/* writes the context of response theory calculations */
ierr = OpenRSPWrite(open_rsp, fp_log);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPWrite()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPWrite() passed\n");

/* sets the unperturbed AO-based Fock matrix */
F_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
if (F_unpert[0]==NULL) {
    QErrorExit(FILE_AND_LINE, "allocates memory for Fock matrix");
}
ierr = OpenRSPTestReadMat(DMAT_HF_FOCK, 0, 1, F_unpert);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(F)");
/* sets the unperturbed AO-based density matrix */
D_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
if (D_unpert[0]==NULL) {
    QErrorExit(FILE_AND_LINE, "allocates memory for density matrix");
}
ierr = OpenRSPTestReadMat(DMAT_HF_DENSITY, 0, 1, D_unpert);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(D)");
/* sets the unperturbed AO-based overlap integral matrix */
S_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
if (S_unpert[0]==NULL) {
    QErrorExit(FILE_AND_LINE, "allocates memory for overlap integral matrix");
}
ierr = OpenRSPTestReadMat(DMAT_OVERLAP, 0, 1, S_unpert);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(S)");

/* gets the polarizability */
size_rsp_funs = 9;
ierr = OpenRSPGetRSPFun(open_rsp,
                        F_unpert[0],
                        D_unpert[0],
                        S_unpert[0],
                        ALPHA_NUM_PROPS,

```

```

        ALPHA_LEN_TUPLE,
        ALPHA_PERT_TUPLE,
        ALPHA_NUM_FREQ_CONFIGS,
        ALPHA_PERT_FREQS,
        ALPHA_KN_RULES,
        size_rsp_funs,
        rsp_funs);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPGetRSPFun()");
fprintf(fp_log, "OpenRSPDmatTest>> OpenRSPGetRSPFun() passed\n");
for (ipert=0,ival=0; ipert<3; ipert++) {
    for (jpert=0; jpert<3; jpert++) {
        fprintf(fp_log,
            " (%"QCREAL_FMT","QCREAL_FMT")",
            rsp_funs[ival], rsp_funs[ival+1]);
        ival += 2;
    }
    fprintf(fp_log, "\n");
}

/* cleans */
ierr = QcMatDestroy(F_unpert[0]);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(F)");
free(F_unpert[0]);
F_unpert[0] = NULL;
ierr = QcMatDestroy(D_unpert[0]);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(D)");
free(D_unpert[0]);
D_unpert[0] = NULL;
ierr = QcMatDestroy(S_unpert[0]);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(S)");
free(S_unpert[0]);
S_unpert[0] = NULL;

return QSUCCESS;
}

```

221 $\langle \text{OpenRSPTest.h } 221 \rangle \equiv$

```

/*
 $\langle \text{OpenRSPLicense } 14a \rangle$ 

```

This is the header file of OpenRSP unit testing.

```

2014-07-31, Bin Gao:
* first version
*/

```

```

#if !defined(OPENRSP_TEST_H)
#define OPENRSP_TEST_H

```

```

#include <string.h>
#include "OpenRSP.h"

```

```

#include "OpenRSPTestPerturbations.h"
#include "OpenRSPPertCallback.h"
#include "OpenRSPZeroOperCallback.h"
#include "OpenRSPDMatTest.h"

#if !defined(OPENRSP_TEST_EXECUTABLE)
extern QErrorCode OpenRSPTest(FILE *fp_log);
#endif

#endif

```

222 *<OpenRSPTest.c 222>*≡

```

/*
  <OpenRSPLicense 14a>

  This file tests the APIs of OpenRSP library.

  2014-07-31, Bin Gao
  * first version
  */

#include "OpenRSPTest.h"

/* <macrodef name='OPENRSP_TEST_EXECUTABLE'>
  Build test suite as excutables.
</macrodef> */
#if defined(OPENRSP_TEST_EXECUTABLE)
QErrorCode main()
{
  FILE *fp_log=stdout; /* file pointer */
#else
QErrorCode OpenRSPTest(FILE *fp_log)
{
#endif
#include "OpenRSPTestPerturbations.h"
  OpenRSP open_rsp; /* context of response theory calculations */
  QErrorCode ierr; /* error information */

  /* creates the context of response theory calculations */
  ierr = OpenRSPCreate(&open_rsp, NUM_ATOMS);
  QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPCreate()");
  fprintf(fp_log, "OpenRSPTest>> OpenRSPCreate() passed\n");

  /* sets information of all perturbations */
  ierr = OpenRSPSetPerturbations(&open_rsp,
                                NUM_ALL_PERT,
                                ALL_PERT_LABELS,
                                ALL_PERT_MAX_ORDERS,
                                ALL_PERT_SIZES,
#if defined(OPENRSP_C_USER_CONTEXT)
                                (void *)PERT_CONTEXT,
#endif
  )
#endif

```

```

                                &get_pert_concatenation);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetPerturbations()");
fprintf(fp_log, "OpenRSPTest>> OpenRSPSetPerturbations() passed\n");

/* adds the nuclear Hamiltonian */
ierr = OpenRSPAddZeroOper(&open_rsp,
                          NUM_ALL_PERT,
                          ALL_PERT_LABELS,
                          ALL_PERT_MAX_ORDERS,
#ifdef OPENRSP_C_USER_CONTEXT
                          (void *)ZERO_OPER_CONTEXT,
#endif
                          &get_zero_oper_contrib);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddZeroOper()");
fprintf(fp_log, "OpenRSPTest>> OpenRSPAddZeroOper() passed\n");

/* tests the density matrix-based response theory */
ierr = OpenRSPDmatTest(&open_rsp, fp_log);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPDmatTest()");
fprintf(fp_log, "OpenRSPTest>> density matrix-based response theory passed\n");

/* destroys the context of response theory calculations */
ierr = OpenRSPDestroy(&open_rsp);
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPDestroy()");
fprintf(fp_log, "OpenRSPTest>> OpenRSPDestroy() passed\n");

return QSUCCESS;
}

```

3.13.3 Testing Fortran APIs

```

223 <OpenRSPTest.F90 223>≡
    !! <QcLang='Fortran'>
    <OpenRSPLicenseFortran 119a>
    !!
    !! This file tests the Fortran APIs of OpenRSP library.
    !!
    !! 2014-08-03, Bin Gao
    !! * first version

```


Chapter 4

Maintenance

4.1 Support and Citation

If there is any question regarding the use of OPENRSP, please contact the authors as given in the file `AUTHORS.rst`.

If you have used OPENRSP and found it is useful, please consider to cite OPENRSP as described in the file `openrsp.bib`.

4.2 List of Chunks

<OpenRSPAPIs 14c>
<OpenRSPDMatCallback.c 201>
<OpenRSPDMatCallback.h 199b>
<OpenRSPDMatTest.c 217b>
<OpenRSPDMatTest.h 217a>
<OpenRSP.F90 119b>
<OpenRSPFortranAdapter.c 187>
<OpenRSPLicense 14a>
<OpenRSPLicenseFortran 119a>
<OpenRSPPertCallback.c 198a>
<OpenRSPPertCallback.h 197b>
<OpenRSPStruct 14b>
<OpenRSPTestData.c 191>
<OpenRSPTestData.cmake 190>
<OpenRSPTest.F90 223>
<OpenRSPTestPerturbations.c 197a>
<OpenRSPTestPerturbations.h 196>
<OpenRSPTest.c 222>
<OpenRSPTest.h 221>
<OpenRSPZeroOperCallback.c 199a>
<OpenRSPZeroOperCallback.h 198b>
<OpenRSP.c 17a>
<OpenRSP.h 13>
<RSPOneOperAPIs 58b>
<RSPOneOper.F90 159>
<RSPOneOperStruct 58a>
<RSPOneOper.c 59>
<RSPOneOper.h 57>
<RSPOverlapAPIs 45a>
<RSPOverlap.F90 151>

[⟨RSPOverlapStruct 44⟩](#)
[⟨RSPOverlap.c 45b⟩](#)
[⟨RSPOverlap.h 43⟩](#)
[⟨RSPPertBasicTypes 22b⟩](#)
[⟨RSPPertBasicTypes.F90 148a⟩](#)
[⟨RSPPertCallback 24a⟩](#)
[⟨RSPPertStruct 24b⟩](#)
[⟨RSPPerturbation.F90 148b⟩](#)
[⟨RSPPerturbation.c 23c⟩](#)
[⟨RSPPerturbation.h 22a⟩](#)
[⟨RSPSolverAPIs 110b⟩](#)
[⟨RSPSolver.F90 183⟩](#)
[⟨RSPSolverStruct 110a⟩](#)
[⟨RSPSolver.c 111⟩](#)
[⟨RSPSolver.h 109b⟩](#)
[⟨RSPTwoOperAPIs 71b⟩](#)
[⟨RSPTwoOperStruct 71a⟩](#)
[⟨RSPTwoOper.c 72⟩](#)
[⟨RSPTwoOper.h 70⟩](#)
[⟨RSPTwooper.F90 165⟩](#)
[⟨RSPXCFunAPIs 86b⟩](#)
[⟨RSPXCFun.F90 172⟩](#)
[⟨RSPXCFunStruct 86a⟩](#)
[⟨RSPXCFun.c 87⟩](#)
[⟨RSPXCFun.h 84⟩](#)
[⟨RSPZeroOperAPIs 100⟩](#)
[⟨RSPZeroOper.F90 180⟩](#)
[⟨RSPZeroOperStruct 99b⟩](#)
[⟨RSPZeroOper.c 101⟩](#)
[⟨RSPZeroOper.h 99a⟩](#)
[⟨RSPertAPIs 26a⟩](#)

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Index

OPENRSP Fortran APIs, [9](#)
OPENRSP License, [14](#), [119](#)
OPENRSP Fortran APIs, [119](#)
OPENRSP framework, [9](#)
QCMATRIX library, [9](#)
OpenRSP.h, [13](#)
OPENRSP_PERT_ID_MAX, [23](#)
OPENRSP_PERT_LABEL_BIT, [22](#)
OPENRSP_PERT_LABEL_MAX, [23](#)
OpenRSPAssemble(), [17](#)
OpenRSPCreate(), [17](#)
OpenRSPDestroy(), [17](#)
OpenRSPSetPerturbations(), [25](#)
OpenRSPWrite(), [17](#)
QCPERTINT_FMT, [23](#)
QCPERTINT_MAX, [23](#)
QcPertInt, [23](#)
struct OpenRSP, [14](#)

Callback function scheme, [9](#)

Include guard, [13](#)

Open-ended response theory, [8](#)

Support and citation, [225](#)

Theoretical background, [8](#)

Unit testing, [190](#)

User-defined context, [16](#)

Version numbering scheme, [5](#)