OpenRSP Developer Manual Version 1.0.0

Radovan Bast
Daniel H. Friese
Bin Gao
Dan J. Jonsson
Magnus Ringholm
Kenneth Ruud
Andreas Thorvaldsen

Centre for Theoretical and Computational Chemistry (CTCC)

Department of Chemistry

University of Tromsø—The Arctic University of Norway
N-9037, Tromsø, Norway

OpenRSP: open-ended library for response theory

© 2015

Radovan Bast

Daniel H. Friese

Bin Gao

Dan J. Jonsson

Magnus Ringholm

Kenneth Ruud

Andreas Thorvaldsen

OPENRSP is free software: you can redistribute it and/or modify it under the terms of the GNU Lesser General Public License as published by the Free Software Foundation, either version 3 of the License, or (at your option) any later version.

OPENRSP is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU Lesser General Public License for more details.

You should have received a copy of the GNU Lesser General Public License along with OPENRSP . If not, see http://www.gnu.org/licenses/>.

HOWEVER, YOU CANNOT USE IDEAS, DATA, OR WORDING OF THIS DOCUMENT WITHOUT AN APPROPRIATE CITATION.

Contents

1	\mathbf{Pre}		5
	1.1	Version Numbering Scheme	5
2	Ana	lysis	7
	2.1	Introduction	7
		2.1.1 Purpose	7
		2.1.2 Scope	8
		2.1.3 Product Overview	8
		2.1.4 Definitions	8
	2.2	References	8
	2.3	Specific Requirements	8
		2.3.1 External Interfaces	8
		2.3.2 Functions	8
		2.3.3 Usability Requirements	8
		2.3.4 Performance Requirements	8
		2.3.5 Logical Database Requirements	8
		2.3.6 Design Constraints	
		2.3.7 Software System Attributes	8
		2.3.8 Supporting Information	8
	2.4	Verification	
	2.5	Appendices	
		2.5.1 Assumptions and Dependencies	8
		2.5.2 Acronyms and Abbreviations	
		2.5.3 Theoretical Background	
		2.5.4 Open-Ended Response Theory	
		2.5.5 OPENRSP Framework	
		2.5.6 Perturbations	10
3	Imp	lementation	13
	3.1	Header File for Users	13
	3.2	Four Basic APIs for the OpenRSP Context	17
	3.3	Perturbations	21
		3.3.1 Internal Perturbation Labels	21
		3.3.2 Callback Functions for Perturbations	23
		3.3.3 Perturbation Context and Its Basic APIs	23
		3.3.4 Conversion of Perturbation Tuples and Labels	31
	3.4	Overlap Operator	41
	3.5	One-Electron Operators	55
	3.6	Two-Electron Operators	68
	3.7	XC Functionals	82
	3.8	Nuclear Hamiltonian	96
	3.9	Linear Response Equation Solver	106

4	web/Preface.tex October 18, 20)15
	3.10 Response Functions 1 3.11 Residues 1 3.12 Fortran APIs 1 3.13 Unit Testing 1 3.13.1 Testing C APIs 1 3.13.2 Testing Fortran APIs 2	113 115 182 182
4	Maintenance 2 4.1 Support and Citation 2 4.2 List of Chunks 2	

Chapter 1

Preface

1.1 Version Numbering Scheme

The version numbering scheme used for OpenRSP is Major.Minor.Patch, where

Major generally represents new release containing important changes, and it may not be compatible with previous versions.

Minor is changed when a few new features introduced, and it should be compatible with those of the same **Major** number.

Patch usually includes bug fixes, and should be compatible with those of the same Major.Minor number.

Chapter 2

Analysis

This chapter presents the "Software Requirements Specification" (SRS) largely based on ISO/IEC/IEEE 29148:2011(E) "Systems and software engineering – Life cycle processes – Requirements engineering".

2.1 Introduction

This section gives a scope description and overview of everything needed to design and implement OPENRSP (library) by taking the requirements listed in this section into account.

2.1.1 Purpose

The SRS analyses the problem—molecular integral evaluation—that OPENRSP aims to solve, and lays out the requirements that OPENRSP should supply or should not supply.

The SRS is primarily intended to prepare a reference for developing OpenRSP (Version 1.0.0). It can also be proposed to OpenRSP users for their suggestions and comments.

8 web/Analysis.tex October 18, 2015

2.1.2 Scope

2.1.3 Product Overview

Product Perspective

Product Functions

User Characteristics

Limitations

- 2.1.4 Definitions
- 2.2 References

2.3 Specific Requirements

- 2.3.1 External Interfaces
- 2.3.2 Functions
- 2.3.3 Usability Requirements
- 2.3.4 Performance Requirements
- 2.3.5 Logical Database Requirements
- 2.3.6 Design Constraints
- 2.3.7 Software System Attributes
- 2.3.8 Supporting Information
- 2.4 Verification

2.5 Appendices

- 2.5.1 Assumptions and Dependencies
- 2.5.2 Acronyms and Abbreviations

2.5.3 Theoretical Background

For the time being, OPENRSP has implemented the density matrix-based quasienergy formulation of the Kohn-Sham density functional response theory using perturbation- and time-dependent basis sets [1, 2].

The density matrix-based quasienergy formulation actually works for different levels of theory, i.e., one-, two- and four-component levels. A relativistic implementation can be found in Ref. [3].

OPENRSP uses the recursive programming techniques [4] to compute different molecular properties order by order. The recursive programming techniques can also be used for calculations of residues, the implementation of the first order residues can be found in Ref. [5].

2.5.4 Open-Ended Response Theory

The name OpenRSP stands for open-ended response theory, that is, the library is:

- 1. open-ended for different levels of theory, i.e., one-, two- and four-component levels;
- 2. open-ended for different wave functions, e.g., atomic-orbital (AO) based density matrix, molecular orbital (MO) cofficients and coupled cluster (CC);
- 3. open-ended for different kinds of perturbations; and
- 4. open-ended for different host programs.

October 18, 2015 web/Analysis.tex 9

As aformentioned, OPENRSP has for the time being implemented the AO based density matrix response theory (source codes in src/ao_dens)¹, and it works for one-, two- and four-component levels by simply setting the appropriate Hamiltonian. We are now planning to implement the MO and CC based response theories.

To make OpenRSP work for any perturbation, we will implement the so called **perturbation** free scheme, see Section 2.5.6.

In order to make it easy for implementing OPENRSP into different host programs (written in different programming languages), we agree to use the **callback function scheme** in OPENRSP in the 2015 Skibotn meeting. The callback functions are specified by host programs by calling the OPENRSP application program interface (APIs, both C and Fortran implemented) during run time, and will be used by OPENRSP during calculations, to get contributions from electronic and nuclear Hamiltonian, and to get response parameters from solving the linear response equation.

Another important issue affects the implementation of OPENRSP into different host programs is the matrix and its different operations that OPENRSP extensively depends on. Different host programs can have different types of matrices (dense and sparse, sequential and parallel) and written by different programming languages (e.g. C and Fortran).

To best utilize the host program's developed matrix routines (if there is), and also to remove this complexity of matrix problem from OpenRSP, we also agree to build OpenRSP on top of the **QcMatrix library** in the 2015 Skibotn meeting. This matrix library works as an adapter between OpenRSP and different matrix routines (implemented in different host programs) that can be written in C and Fortran².

2.5.5 OpenRSP Framework

Therefore, a full picture of OPENRSP used in a C host program can be (the description of OPENRSP Fortran APIs can be found in Section 3.12):

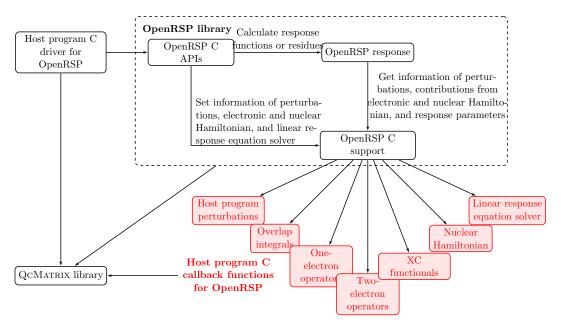


Figure 2.1: OpenRSP used in a C host program.

As shown in Figure 2.1, the OPENRSP library is divided into three parts:

¹The codes in src/ao_dens are written in Fortran, but OPENRSP APIs are implemented using C language. Therefore, adapter codes between them are implemented in src/ao_dens/adapter, for OPENRSP APIs calling the codes of AO based density matrix response theory, also for the AO based density matrix response theory codes calling the callback functions (as function pointers saved by OPENRSP APIs).

²If there is no matrix routines implemented in a host program, it can fully use the QcMatrix library that will invoke BLAS and LAPACK libraries for matrix operations.

10 web/Analysis.tex October 18, 2015

1. The "OPENRSP C APIs" work mostly between the host program driver routine and other parts of the OPENRSP library, that all the information saved in the "OPENRSP C support" will be set up by calling the corresponding OPENRSP C API;

- 2. The "OPENRSP response" is the core part in which the performance of response theory will be done;
- 3. The "OPENRSP C support" saves the information of perturbations, electronic and nuclear Hamiltonian and linear response equation solver, and will be used by the "OPENRSP response" part during calculating response functions and residues.

The "OPENRSP response" was already implemented using Fortran for the AO based density matrix response theory (source codes in src/ao_dens) that will not be covered here.

2.5.6 Perturbations

For perturbations in OpenRSP, we introduce the following notations and convention:

Perturbation is described by a label (a), a complex frequency (ω) and its order (n), and written as a_{ω}^{n} Any two perturbations are different if they have different labels, and/or frequencies, and/or orders.

Perturbation label is an integer distinguishing one perturbation from others; all different perturbation labels involved in the calculations should be given by calling the application programming interface (API) OpenRSPSetPerturbations(); OPENRSP will stop if there is any unspecified perturbation label given afterwards when calling the APIs OpenRSPGetRSPFun() or OpenRSPGetResidue().

Perturbation order Each perturbation can acting on molecules once or many times, that is the order of the perturbation.

Perturbation components and their ranks Each perturbation may have different numbers of components for their different orders, the position of each component is called its rank. For instance, there will usually be x, y, z components for the electric dipole perturbation, and their ranks are $\{0,1,2\}$ in zero-based numbering, or $\{1,2,3\}$ in one-based numbering.

Perturbation tuple An ordered list of perturbation labels, and in which we further require that identical perturbation labels should be consecutive. That means the tuple (a, b, b, c) is allowed, but (a, b, c, b) is illegal because the identical labels b are not consecutive. As a tuple:

- 1. Multiple instances of the same labels are allowed so that $(a, b, b, c) \neq (a, b, c)$, and
- 2. The perturbation labels are ordered so that $(a, b, c) \neq (a, c, b)$ (because their corresponding response functions or residues are in different shapes).

We will sometimes use an abbreviated form of perturbation tuple as, for instance $abc \equiv (a, b, c)$.

Obviously, a perturbation tuple + its corresponding complex frequencies for each perturbation label can be viewed as a set of perturbations, in which the number of times a label (with the same frequency) appears is the order of the corresponding perturbation.

For example, a tuple (a,b,b,c) + its complex frequencies $(\omega_a,\omega_b,\omega_b,\omega_c)$ define perturbations $a^1_{\omega_a},\ b^2_{\omega_b}$ and $c^1_{\omega_c}$; another tuple (a,b,b,c) + different complex frequencies for labels b— $(\omega_a,\omega_{b_1},\omega_{b_2},\omega_c)$ define different perturbations $a^1_{\omega_a},\ b^1_{\omega_{b_1}},\ b^1_{\omega_{b_2}}$ and $c^1_{\omega_c}$.

Canonical order

- 1. In OPENRSP, all perturbation tuples are canonically orderd according to the argument pert_tuple in the OpenRSPGetRSPFun() or OpenRSPGetResidue(). For instance, when a perturbation tuple (a,b,c) given as pert_tuple in the API OpenRSPGetRSPFun(), OPENRSP will use such order (a > b > c) to arrange all perturbation tuples inside and sent to the callback functions.
- 2. Moreover, a collection of several perturbation tuples will also follow the canonical order. For instance, a collection of all possible perturbation tuples of labels a, b, c are (0, a, b, c, ab, ac, bc, abc), where 0 means unperturbed quantities that is always the first one in the collection.

October 18, 2015 web/Analysis.tex 11

Perturbation a The first perturbation label in the tuple sent to OPENRSP APIs OpenRSPGetRSPFun() or OpenRSPGetResidue(), are the perturbation a [1].

Perturbation addressing

- 1. The addressing of perturbation labels in a tuple, as mentioned in the term **Canonical** order, is decided by
 - (a) the argument pert_tuple sent to the API OpenRSPGetRSPFun() or OpenRSPGetResidue(), and
 - (b) the canonical order that OpenRSP uses.
- 2. The addressing of components per perturbation (several consecutive identical labels with the same complex frequency) are decided by the host program, as will be discussed in the following **perturbation free scheme**.
- 3. The addressing of a collection of perturbation tuples follows the canonical order as aforementioned.

Therefore, the shape of response functions or residues is mostly decided by the host program. Take \mathcal{E}^{abbc} for example, its shape is (N_a, N_{bb}, N_c) , where N_a and N_c are respectively the numbers of components of the first order of the perturbations a and c, and N_{bb} is the number of components of the second order of the perturbation b, and

- 1. In OpenRSP, we will use notation [a] [bb] [c] for \mathcal{E}^{abbc} , where the leftmost index (a) runs slowest in memory and the rightmost index (c) runs fastest. However, one should be aware that the results are still in a one-dimensional array.
- 2. If there two different frequencies for the perturbation label b, OPENRSP will return [a] [b1] [b2] [c], where b1 and b2 stand for the components of the first order of the perturbation b.
- 3. The notation for a collection of perturbation tuples (still in a one-dimensional array) is {1,[a],[b],[c],[a][b],[a][c],[b][c],[a][b][c]} for (0, a, b, c, ab, ac, bc, abc), where as aforementioned the first one is the unperturbed quantities.

Perturbation Free Scheme

Now, let us discuss our **perturbation free scheme**. As aforementioned, there could be **different numbers of components** for different perturbations. In different host programs, these components could **be arranged in different ways**.

For instance, there are 9 components for the second order magnetic derivatives in a redundant way xx, xy, xz, yx, yy, yz, zx, zy, zz, but 6 components in a non-redundant way xx, xy, xz, yy, yz, zz. There are at most four centers in different integrals, non-zero high order (≥ 5) geometric derivatives are only those with at most four differentiated centers.

To take all the above information into account in OPENRSP will make it so complicated and not necessary, because response theory actually does not care about the detailed knowledge of different perturbations. In particular, when all the (perturbed) integrals and expectation values are computed by the host program's callback functions, the detailed information of perturbations:

- 1. the number of components, and
- 2. how they are arranged in memory can be hidden from OpenRSP.

The former can be easily solved by sending the numbers of components of different perturbation labels (up to their maximum orders) to the OPENRSPAPI OpenRSPSetPerturbations().

The latter can be important for OpenRSP to construct higher-order derivatives from lower-order ones. We have two cases:

- 1. Higher-order derivatives are taken with respect to different perturbations, for instance, $\frac{\partial^3}{\partial a\partial b\partial c}$ are simply the direct product of components of lower-order derivatives with respect to each perturbation $\frac{\partial}{\partial a}$, $\frac{\partial}{\partial b}$ and $\frac{\partial}{\partial c}$.
- 2. Higher-order derivatives are taken with respect to **one perturbation**. Take the second order-derivatives (in the redundant format) for example, they can be constructed from the

first-order ones as,

$$x + x \to xx, 0 + 0 \to 0,$$

 $x + y \to xy, 0 + 1 \to 1,$
 $x + z \to xz, 0 + 2 \to 2,$
 $y + x \to yx, 1 + 0 \to 3,$
 $y + y \to yy, 1 + 1 \to 4,$
 $y + z \to yz, 1 + 2 \to 5,$
 $z + x \to zx, 2 + 0 \to 6,$
 $z + y \to zy, 2 + 1 \to 7,$
 $z + z \to zz, 2 + 2 \to 8,$

where we have ranked different components in zero-based numbering (numbers on the right). Because the ranks can be different in different host programs, also the above mapping relationship between lower- and higher-order derivatives (with respect to **one perturbation**) can be different in different host programs.

We therefore ask for a callback function <code>get_pert_concatenation()</code> from host programs. This callback function will, from given components of a **concatenated perturbation tuple** (i.e. higher-order derivatives with respect to one perturbation), get the ranks of components of the **sub-perturbation tuples with the same perturbation label** (i.e. lower-order derivatives with respect to one perturbation).

As such, the numbers of different components of perturbations and their ranks are totally decided by the host program—that is the **perturbation free scheme**.

Chapter 3

#endif

Implementation

3.1 Header File for Users

```
To use OpenRSP, C users need to include the following header file into their codes:
      \langle OpenRSP.h \ 13 \rangle \equiv
13
          ⟨OpenRSPLicense 14a⟩
          <header name='OpenRSP.h' author='Bin Gao' date='2014-01-27'>
            The header file of OpenRSP library for users
          </header>
        #if !defined(OPENRSP_H)
        #define OPENRSP_H
        /* host program perturbations */
        #include "RSPPerturbation.h"
        /* type of electronic wave function */
        /*#include "RSPWaveFunction.h"*/
        /* overlap integrals */
        #include "RSPOverlap.h"
        /* one-electron operators */
        #include "RSPOneOper.h"
        /* two-electron operators */
        #include "RSPTwoOper.h"
        /* exchange-correlation (XC) functionals */
        #include "RSPXCFun.h"
        /* nuclear Hamiltonian */
        #include "RSPNucHamilton.h"
        /* linear response equation solver */
        #include "RSPSolver.h"
        \langle \mathit{OpenRSPStruct~14b} \rangle
        \langle OpenRSPAPIs 14c \rangle
```

Here, the directives #if !defined(OPENRSP_H) and #define OPENRSP_H (include guard) to-

gether prevent the header file from being compiled more than once.

We plan to release OPENRSP under the GNU Lesser General Public License:

```
14a \langle OpenRSPLicense \ 14a \rangle \equiv
```

```
OpenRSP: open-ended library for response theory
Copyright 2015 Radovan Bast,
Daniel H. Friese,
Bin Gao,
Dan J. Jonsson,
Magnus Ringholm,
Kenneth Ruud,
Andreas Thorvaldsen
```

OpenRSP is free software: you can redistribute it and/or modify it under the terms of the GNU Lesser General Public License as published by the Free Software Foundation, either version 3 of the License, or (at your option) any later version.

OpenRSP is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU Lesser General Public License for more details.

You should have received a copy of the GNU Lesser General Public License along with OpenRSP. If not, see http://www.gnu.org/licenses/>.

In the following sections, we will describe how to implement each component of the "OPENRSP C support" (red blocks in Figure 2.1 under the "OPENRSP C support") and the corresponding "OPENRSP C API". Each component will have its header file, implemented C struct and corresponding functions that can be called inside OPENRSP.

The OPENRSP context OpenRSPStruct will encapsulate all the implemented C struct's of the "OPENRSP C support" components into another C struct:

```
14b \langle OpenRSPStruct \ 14b \rangle \equiv
```

```
typedef struct {
   QBool assembled;
                                  /* indicates if the OpenRSP context assembled */
   RSPPert *rsp_pert;
                                  /* host program perturbations */
   /*ElecWav *elec_wav;*/
                                    /* implementation-specific data of (electronic) wave f
   /*ElecWavType elec_wav_type;*/
   RSPOverlap *overlap;
                                 /* overlap integrals */
   RSPOneOper *one_oper;
                                  /* one-electron operators */
   RSPTwoOper *two_oper;
                                 /* two-electron operators */
                                  /* XC functionals */
   RSPXCFun *xc_fun;
   RSPNucHamilton *nuc_hamilton; /* nuclear Hamiltonian */
   RSPSolver *rsp_solver;
                                  /* linear response equation solver */
} OpenRSP;
```

where we have used types, macros and APIs implemented in the QCMATRIX library and one should be familiar with them first.

Users should use the OpenRSP context and the following APIs to access the functionalities of OpenRSP:

```
14c \langle OpenRSPAPIs \ 14c \rangle \equiv
```

```
const QcPertInt*,
                                           const QInt*,
                                           const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                           void*,
#endif
                                           const GetPertCat);
/*extern QErrorCode OpenRSPSetWaveFunction(OpenRSP*,const ElecWavType);*/
extern QErrorCode OpenRSPSetOverlap(OpenRSP*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     void*,
#endif
                                     const GetOverlapMat,
                                     const GetOverlapExp);
extern QErrorCode OpenRSPAddOneOper(OpenRSP*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     void*,
#endif
                                     const GetOneOperMat,
                                     const GetOneOperExp);
extern QErrorCode OpenRSPAddTwoOper(OpenRSP*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     void*,
#endif
                                     const GetTwoOperMat,
                                     const GetTwoOperExp);
extern QErrorCode OpenRSPAddXCFun(OpenRSP*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                   void*,
#endif
                                   const GetXCFunMat,
                                   const GetXCFunExp);
extern QErrorCode OpenRSPSetNucHamilton(OpenRSP*,
                                         const QInt,
                                         const QcPertInt*,
                                         const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                         void*,
#endif
                                         const GetNucContrib,
```

```
/*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
                                         const QInt);
extern QErrorCode OpenRSPSetLinearRSPSolver(OpenRSP*,
#if defined(OPENRSP_C_USER_CONTEXT)
                                              void*,
#endif
                                              const GetLinearRSPSolution);
extern QErrorCode OpenRSPAssemble(OpenRSP*);
extern QErrorCode OpenRSPWrite(const OpenRSP*,FILE*);
extern QErrorCode OpenRSPGetRSPFun(OpenRSP*,
                                    const QcMat*,
                                    const QcMat*,
                                    const QcMat*,
                                    const QInt,
                                    const QInt*,
                                    const QcPertInt*,
                                    const QInt*,
                                    const QReal*,
                                    const QInt*,
                                    const QInt,
                                    QReal*);
extern QErrorCode OpenRSPGetResidue(OpenRSP*,
                                     const QcMat*,
                                     const QcMat*,
                                     const QcMat*,
                                     const QInt,
                                     const QInt,
                                     const QReal*,
                                     QcMat*[],
                                     const QInt,
                                     const QInt*,
                                     const QcPertInt*,
                                     const QInt*,
                                     const QInt*,
                                     const QInt*,
                                     const QReal*,
                                     const QInt*,
                                     const QInt,
                                     QReal*);
extern QErrorCode OpenRSPDestroy(OpenRSP*);
```

Here, we have also introduced the type of electronic wave function, but which has not been implemented.

Last but not least, the directive

#endif

in most OpenRSP APIs enables users to provide their necessary setting for the callback functions that OpenRSP will send it back when invoking the callback functions. For instance, users can provide the information of basis sets to OpenRSP and use it inside the callback functions for different integral calculations.

3.2 Four Basic APIs for the OpenRSP Context

17a

17b

In this section, we will implement four basic APIs OpenRSPCreate(), OpenRSPAssemble(), OpenRSPWrite() and OpenRSPDestroy(), while other APIs will be implemented in the following sections. These four APIs respectively create, assemble, write and destroy the OpenRSP context.

The API OpenRSPCreate() is very simple as it only initializes the pointers of the context:

```
\langle OpenRSP.c \ 17a \rangle \equiv
 /*
    ⟨OpenRSPLicense 14a⟩
 #include "OpenRSP.h"
 /* <function name='OpenRSPCreate' author='Bin Gao' date='2014-01-28'>
       Creates the OpenRSP context
       <param name='open_rsp' direction='inout'>The OpenRSP context</param>
       <return>Error information</return>
     </function> */
 QErrorCode OpenRSPCreate(OpenRSP *open_rsp)
      open_rsp->assembled = QFALSE;
      open_rsp->rsp_pert = NULL;
      /*open_rsp->elec_wav = NULL;*/
      /*open_rsp->elec_wav_type = ELEC_AO_D_MATRIX;*/
      open_rsp->overlap = NULL;
      open_rsp->one_oper = NULL;
      open_rsp->two_oper = NULL;
      open_rsp->xc_fun = NULL;
      open_rsp->nuc_hamilton = NULL;
      open_rsp->rsp_solver = NULL;
      return QSUCCESS;
 }
The other three APIs are also easy to implement, as they only invoke functions of the "OpenRSP C
support" part to respectively assemble, write and destroy the corresponding C struct's:
\langle OpenRSP.c \ 17a \rangle + \equiv
 /* <function name='OpenRSPAssemble' author='Bin Gao' date='2014-07-30'>
       Assembles the OpenRSP context
       <param name='open_rsp' direction='inout'>The OpenRSP context</param>
```

```
}
/*FIXME: to implement ierr = xxAssemble(open_rsp->elec_eom); */
    /* assembles overlap integrals */
    if (open_rsp->overlap!=NULL) {
        ierr = RSPOverlapAssemble(open_rsp->overlap,
                                  open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapAssemble()");
   }
    /* assembles one-electron operators */
    if (open_rsp->one_oper!=NULL) {
        ierr = RSPOneOperAssemble(open_rsp->one_oper,
                                  open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperAssemble()");
    }
    /* assembles two-electron operators */
    if (open_rsp->two_oper!=NULL) {
        ierr = RSPTwoOperAssemble(open_rsp->two_oper,
                                  open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperAssemble()");
    }
    /* assembles XC functionals */
    if (open_rsp->xc_fun!=NULL) {
        ierr = RSPXCFunAssemble(open_rsp->xc_fun,
                                open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunAssemble()");
    }
    /* assembles nuclear Hamiltonian */
    if (open_rsp->nuc_hamilton!=NULL) {
        ierr = RSPNucHamiltonAssemble(open_rsp->nuc_hamilton,
                                      open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPNucHamiltonAssemble()");
    }
    /* assembles linear response equation solver */
    if (open_rsp->rsp_solver!=NULL) {
        ierr = RSPSolverAssemble(open_rsp->rsp_solver);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverAssemble()");
    }
    else {
        QErrorExit(FILE_AND_LINE, "solver not set by OpenRSPSetSolver()");
    open_rsp->assembled = QTRUE;
   return QSUCCESS;
}
/* <function name='OpenRSPWrite' author='Bin Gao' date='2014-07-30'>
    Writes the OpenRSP context
     <param name='open_rsp' direction='in'>The OpenRSP context</param>
     <param name='fp_rsp' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode OpenRSPWrite(const OpenRSP *open_rsp, FILE *fp_rsp)
```

```
QErrorCode ierr; /* error information */
   fprintf(fp_rsp,
            "\nOpenRSP library compiled at %s, %s\n",
            __TIME__,
            __DATE__);
   /* context of the (electronic) wave function */
   /*FIXME: ierr = xxWrite(open_rsp->elec_eom); */
    if (open_rsp->rsp_pert!=NULL) {
        ierr = RSPPertWrite(open_rsp->rsp_pert, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertWrite()");
   }
    if (open_rsp->overlap!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> overlap integrals\n");
        ierr = RSPOverlapWrite(open_rsp->overlap, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapWrite()");
    if (open_rsp->one_oper!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of one-electron operators\n");
        ierr = RSPOneOperWrite(open_rsp->one_oper, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperWrite()");
    if (open_rsp->two_oper!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of two-electron operators\n");
        ierr = RSPTwoOperWrite(open_rsp->two_oper, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperWrite()");
   }
    if (open_rsp->xc_fun!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> linked list of XC functionals\n");
        ierr = RSPXCFunWrite(open_rsp->xc_fun, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunWrite()");
   }
    if (open_rsp->nuc_hamilton!=NULL) {
        fprintf(fp_rsp, "OpenRSPWrite>> nuclear Hamiltonian\n");
        ierr = RSPNucHamiltonWrite(open_rsp->nuc_hamilton, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPNucHamiltonWrite()");
   }
   if (open_rsp->rsp_solver!=NULL) {
        ierr = RSPSolverWrite(open_rsp->rsp_solver, fp_rsp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverWrite()");
   }
   return QSUCCESS;
}
/* <function name='OpenRSPDestroy' author='Bin Gao' date='2014-01-28'>
    Destroys the OpenRSP context
    <param name='open_rsp' direction='inout'>The OpenRSP context</param>
    <return>Error information</return>
   </function> */
QErrorCode OpenRSPDestroy(OpenRSP *open_rsp)
   QErrorCode ierr; /* error information */
   open_rsp->assembled = QFALSE;
```

```
if (open_rsp->elec_eom!=NULL) {
//
///*FIXME: to implement ierr = xxDestroy(open_rsp->elec_eom); */
          free(open_rsp->elec_eom);
//
//
          open_rsp->elec_eom = NULL;
//
      }
    /* destroys the context of all perturbations involved in calculations */
    if (open_rsp->rsp_pert!=NULL) {
        ierr = RSPPertDestroy(open_rsp->rsp_pert);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertDestroy()");
        free(open_rsp->rsp_pert);
        open_rsp->rsp_pert = NULL;
    }
    /* destroys the context of overlap integrals */
    if (open_rsp->overlap!=NULL) {
        ierr = RSPOverlapDestroy(open_rsp->overlap);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapDestroy()");
        free(open_rsp->overlap);
        open_rsp->overlap = NULL;
    }
    /* destroys the linked list of one-electron operators */
    if (open_rsp->one_oper!=NULL) {
        ierr = RSPOneOperDestroy(&open_rsp->one_oper);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperDestroy()");
    }
    /* destroys the linked list of two-electron operators */
    if (open_rsp->two_oper!=NULL) {
        ierr = RSPTwoOperDestroy(&open_rsp->two_oper);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperDestroy()");
    }
    /* destroys the linked list of exchange-correlation functionals */
    if (open_rsp->xc_fun!=NULL) {
        ierr = RSPXCFunDestroy(&open_rsp->xc_fun);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunDestroy()");
    }
    /* destroys the context of nuclear Hamiltonian */
    if (open_rsp->nuc_hamilton!=NULL) {
        ierr = RSPNucHamiltonDestroy(open_rsp->nuc_hamilton);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPNucHamiltonDestroy()");
        free(open_rsp->nuc_hamilton);
        open_rsp->nuc_hamilton = NULL;
    }
    /* destroys the context of linear response equation sovler */
    if (open_rsp->rsp_solver!=NULL) {
        ierr = RSPSolverDestroy(open_rsp->rsp_solver);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverDestroy()");
        free(open_rsp->rsp_solver);
        open_rsp->rsp_solver = NULL;
    }
    return QSUCCESS;
}
```

3.3 Perturbations

21a

The header file of perturbations is organized as:

3.3.1 Internal Perturbation Labels

Perturbation labels are represented by integers. Each different label is marked by an internal identifier for calculating reponse functions and residues, so OpenRSP can sort these labels in ascending order by their identifiers. For instance, identifiers for a perturbation tuple *acbadbc* are 0120321.

To avoid using extra arrays for identifiers, we combine each host programs' label with its identifier into a QcPertInt type integer:

```
QcPertInt = identifier < OPENRSP_PERT_LABEL_BIT + label,
```

where OPENRSP_PERT_LABEL_BIT is the number of bits in an object of QcPertInt for representing the host programs' perturbation labels:

```
The type QcPertInt is defined as:
      \langle RSPPertBasicTypes \ 21b \rangle + \equiv
22a
        /* <datatype name='QcPertInt'>
              Data type of integers to represent perturbation labels
            <constant name='QCPERTINT_MAX'>
              Maximal value of an object of the <QcPertInt> type
            </constant>
            <constant name='QCPERTINT_FMT'>
              Format string of <QcPertInt> type
            </constant> */
        //typedef unsigned long QcPertInt;
        //#define QCPERTINT_MAX ULONG_MAX
        //#define QCPERTINT_FMT "lu"
        typedef unsigned int QcPertInt;
        #define QCPERTINT_MAX UINT_MAX
        #define QCPERTINT_FMT "u"
      Here we also define a constant QCPERTINT_MAX for the maximal value of an object of the QcPertInt
      type, and a format string (QCPERTINT_FMT) of the QcPertInt type.
          From OPENRSP_PERT_LABEL_BIT and QCPERTINT_MAX we can compute OPENRSP_PERT_LABEL_MAX
      and OPENRSP_PERT_ID_MAX, which are the maximal values of host programs' perturbation labels
      and internal perturbation identifiers:
22b
      \langle RSPPertBasicTypes \ 21b \rangle + \equiv
        /* <constant name='OPENRSP_PERT_LABEL_MAX'>
              Maximal value for perturbation labels
            <constant name='OPENRSP_PERT_ID_MAX'>
              Maximal value for internal perturbation identifier
            </constant> */
        extern const QcPertInt OPENRSP_PERT_LABEL_MAX;
        extern const QcPertInt OPENRSP_PERT_ID_MAX;
      Here, to avoid multiple inclusions of the header file that will lead to multiple definitions, we have
      the following implementation file for the OPENRSP_PERT_LABEL_MAX and OPENRSP_PERT_ID_MAX:
22c
      \langle RSPPerturbation.c \ 22c \rangle \equiv
        /*
           \langle OpenRSPLicense 14a \rangle
        #include "RSPPerturbation.h"
        const QcPertInt OPENRSP_PERT_LABEL_MAX = (1<<OPENRSP_PERT_LABEL_BIT)-1;</pre>
        const QcPertInt OPENRSP_PERT_ID_MAX =
                          (QCPERTINT_MAX-OPENRSP_PERT_LABEL_MAX)>>OPENRSP_PERT_LABEL_BIT;
        /* see https://scaryreasoner.wordpress.com/2009/02/28/checking-sizeof-at-compile-time
            accessing date Oct. 6, 2015 */
        #define QC_BUILD_BUG_ON(condition) ((void)sizeof(char[1 - 2*!!(condition)]))
        void RSPPertCheckLabelBit()
             QC_BUILD_BUG_ON(sizeof(QcPertInt)*CHAR_BIT<=OPENRSP_PERT_LABEL_BIT);
             QC_BUILD_BUG_ON(QINT_MAX<OPENRSP_PERT_LABEL_MAX);
```

The function RSPPertCheckLabelBit() ensures that (i) OPENRSP_PERT_LABEL_BIT is not too large and there are still bits left for the identifiers, and (ii) the number of different perturbation labels is not greater than the maximal value of an object of the QInt type so that we can still use QInt type integers for the number of (different) perturbation labels and the length of perturbation tuples. Note that the number of internal identifiers is less than or equal to the number of different perturbation labels involved in calculations, so it automatically satisfies the condition (ii).

One will have building error when compiling the function RSPPertCheckLabelBit() if the constant OPENRSP_PERT_LABEL_BIT is too large. However, the function RSPPertCheckLabelBit() can not guarantee the above setting (QcPertInt type and OPENRSP_PERT_LABEL_BIT) is enough for holding the host programs' perturbation labels and the internal identifiers. This will be checked against OPENRSP_PERT_LABEL_MAX and OPENRSP_PERT_ID_MAX by OPENRSP when (i) setting the host programs' perturbations, and (ii) calculating response functions or residues.

3.3.2 Callback Functions for Perturbations

As discussed in Section 2.5.6, we will need a callback function get_pert_concatenation() to get the ranks of components of sub-perturbation tuples (with the same perturbation label) for given components of the corresponding concatenated perturbation tuple. The type of this callback function is defined as follows:

We will discuss how to use this callback function in Section 3.3.4.

3.3.3 Perturbation Context and Its Basic APIs

Also as mentioned in Section 2.5.6, OPENRSP needs to know the numbers of components of host programs' perturbations. Because the number of components of a higher-order perturbation is simply the product of numbers of components of lower-order perturbations with different labels. For instance, the number of components of a perturbation $a^{n_a}_{\omega_a}b^{n_b}_{\omega_b}$ is simply the product of numbers of components of perturbations $a^{n_a}_{\omega_a}$ and $b^{n_b}_{\omega_b}$.

Therefore, if there are in total p different perturbation labels a_1, a_2, \dots, a_p involved in calculations, OpenRSP needs to know

- 1. allowed maximal order of a perturbation described by exactly **one** of these different labels a_1, a_2, \dots, a_p ; let us mark these allowed maximal orders as n_1, n_2, \dots, n_p , which means we will have $k_j \leq n_j$ $(1 \leq j \leq p)$ for any perturbation $a_{1,\omega_1}^{k_1} a_{2,\omega_2}^{k_2} \cdots a_{p,\omega_p}^{k_p}$;
- 2. numbers of components of perturbations $a_{j,\omega_j}^{k_j}$, where $1 \le k_j \le n_j$ and $1 \le j \le p$; let us mark these numbers of components as $[N_i^{k_j}]$.

The above information is saved into the following struct:

```
 \begin{array}{lll} & \langle RSPPertStruct\ 23b\rangle \equiv \\ & \text{typedef struct}\ \{\\ & & \text{QInt num\_pert\_lab;} & /*\ number\ of\ different\ perturbation} \\ & & & \text{labels}\ \$p\$\ */\\ & & & \text{QInt}\ *pert\_max\_orders; & /*\ \$n_{1},n_{2},\cdot dots,n_{p} \$\ */\\ & & & \text{QInt}\ *ptr\_ncomp; & /*\ pointers\ to\ \$[N_{j}^{k_{j}}]\$  \end{array}
```

24

```
for each $a_{j}$ */
                                          * [N_{j}^{k_{j}}], where
     QInt *pert_num_comps;
                                              1\le k_{j}\le n_{j}\ and 1\le j\le p*/
     QcPertInt *pert_labels;
                                          /* $a_{1},a_{2},\cdots,a_{p}$ */
 #if defined(OPENRSP_C_USER_CONTEXT)
                                          /* user-defined callback function context */
     void *user_ctx;
 #endif
     GetPertCat get_pert_concatenation;
                                          /* user-specified function for getting
                                              the ranks of components of sub-perturbation
                                              tuples (with the same perturbation label)
                                              for given components of the corresponding
                                              concatenated perturbation tuple */
 } RSPPert;
and users can set the above information by the following API:
\langle OpenRSP.c \ 17a \rangle + \equiv
 /* <function name='OpenRSPSetPerturbations' author='Bin Gao' date='2015-06-29'>
      Sets all perturbations involved in response theory calculations
      <param name='open_rsp' direction='inout'>The OpenRSP context</param>
       <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels involved in calculations
      </param>
       <param name='pert_labels' direction='in'>
        All the different perturbation labels involved
       </param>
       <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
       </param>
       <param name='pert_num_comps' direction='in'>
        Number of components of a perturbation described by exactly one of
        the above different labels, up to the allowed maximal order, size
        is therefore the sum of <pert_max_orders>
      </param>
       <param name='user_ctx' direction='in'>
        User-defined callback function context
      </param>
       <param name='get_pert_concatenation' direction='in'>
        User specified function for getting the ranks of components of
        sub-perturbation tuples (with the same perturbation label) for given
        components of the corresponding concatenated perturbation tuple
      </param>
       <return>Error information</return>
    </function> */
 QErrorCode OpenRSPSetPerturbations(OpenRSP *open_rsp,
                                     const QInt num_pert_lab,
                                     const QcPertInt *pert_labels,
                                     const QInt *pert_max_orders,
                                     const QInt *pert_num_comps,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                     void *user_ctx,
 #endif
                                     const GetPertCat get_pert_concatenation)
```

```
{
             QErrorCode ierr; /* error information */
             /* creates the context of all perturbations involved in calculations */
             if (open_rsp->rsp_pert!=NULL) {
                 ierr = RSPPertDestroy(open_rsp->rsp_pert);
                 QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertDestroy()");
             }
             else {
                 open_rsp->rsp_pert = (RSPPert *)malloc(sizeof(RSPPert));
                 if (open_rsp->rsp_pert==NULL) {
                     QErrorExit(FILE_AND_LINE, "allocates memory for perturbations");
                 }
             }
             ierr = RSPPertCreate(open_rsp->rsp_pert,
                                   num_pert_lab,
                                   pert_labels,
                                   pert_max_orders,
                                   pert_num_comps,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                   user_ctx,
        #endif
                                   get_pert_concatenation);
             QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertCreate()");
             return QSUCCESS;
        }
      The APIs RSPPertCreate() and RSPPertDestroy() will respectively create and destroy the con-
      tent of the struct RSPPert. We also need APIs to assemble and to write the struct RSPPert:
      \langle RSPertAPIs \ 25a \rangle \equiv
25a
        extern QErrorCode RSPPertCreate(RSPPert*,
                                           const QInt,
                                           const QcPertInt*,
                                           const QInt*,
                                           const QInt*,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                           void*,
        #endif
                                           const GetPertCat);
        extern QErrorCode RSPPertAssemble(RSPPert*);
        extern QErrorCode RSPPertWrite(const RSPPert*,FILE*);
        extern QErrorCode RSPPertDestroy(RSPPert*);
      which are respectively implemented as follows:
25b
      \langle RSPPerturbation.c \ 22c \rangle + \equiv
        /* <function name='RSPPertCreate'</pre>
                      attr='private'
                      author='Bin Gao'
                      date='2015-06-28'>
              Sets all perturbations involved in response theory calculations, should be
              called at first
              <param name='rsp_pert' direction='inout'>
                The context of perturbations
              </param>
```

```
<param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels involved in calculations
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels involved
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='pert_num_comps' direction='in'>
       Number of components of a perturbation described by exactly one of
       the above different labels, up to the allowed maximal order, size
       is therefore the sum of <pert_max_orders>
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback function context
     </param>
     <param name='get_pert_concatenation' direction='in'>
       User-specified function for getting the ranks of components of
       sub-perturbation tuples (with the same perturbation label) for given
       components of the corresponding concatenated perturbation tuple
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPPertCreate(RSPPert *rsp_pert,
                         const QInt num_pert_lab,
                         const QcPertInt *pert_labels,
                         const QInt *pert_max_orders,
                         const QInt *pert_num_comps,
#if defined(OPENRSP_C_USER_CONTEXT)
                         void *user_ctx,
#endif
                         const GetPertCat get_pert_concatenation)
{
                 /* incremental recorders over perturbation labels */
    QInt ilab;
    QInt jlab;
    QInt iorder; /* incremental recorder over orders */
   QInt icomp;
                 /* incremental recorder over components */
    if (num_pert_lab<1) {</pre>
        printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPPertCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
    }
    rsp_pert->num_pert_lab = num_pert_lab;
```

```
rsp_pert->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
if (rsp_pert->pert_labels==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
}
rsp_pert->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
if (rsp_pert->pert_max_orders==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
}
rsp_pert->ptr_ncomp = (QInt *)malloc((num_pert_lab+1)*sizeof(QInt));
if (rsp_pert->ptr_ncomp==NULL) {
    printf("RSPPertCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    QErrorExit(FILE_AND_LINE, "allocates memory for pointers to components");
}
rsp_pert->ptr_ncomp[0] = 0;
for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
    if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPPertCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "invalid perturbation label");
    }
    /* each element of <pert_labels> should be unique */
    for (jlab=0; jlab<ilab; jlab++) {</pre>
        if (pert_labels[jlab] == pert_labels[ilab]) {
            printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   pert_labels[jlab]);
            printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   pert_labels[ilab]);
            QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
        }
    }
    rsp_pert->pert_labels[ilab] = pert_labels[ilab];
    if (pert_max_orders[ilab]<1) {</pre>
        printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
               ilab,
               pert_labels[ilab]);
        printf("RSPPertCreate>> allowed maximal order is %"QINT_FMT"\n",
               pert_max_orders[ilab]);
        QErrorExit(FILE_AND_LINE, "only positive order allowed");
    rsp_pert->pert_max_orders[ilab] = pert_max_orders[ilab];
    /* <c>rsp_pert->ptr_ncomp[ilab]</c> points to the number of components
       of <c>rsp_pert->pert_labels[ilab]</c> */
```

```
rsp_pert->ptr_ncomp[ilab+1] = rsp_pert->ptr_ncomp[ilab]+pert_max_orders[ilab];
                        }
                        \label{lem:comp_num_pert_lab} $$ \ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensuremath{^{<}}\ensu
                              <c>rsp_pert->pert_num_comps</c> */
                       rsp_pert->pert_num_comps = (QInt *)malloc(rsp_pert->ptr_ncomp[num_pert_lab]
                                                                                                                  *sizeof(QInt));
                        if (rsp_pert->pert_num_comps==NULL) {
                                rsp_pert->ptr_ncomp[num_pert_lab]);
                                QErrorExit(FILE_AND_LINE, "allocates memory for numbers of components");
                        for (ilab=0,icomp=0; ilab<num_pert_lab; ilab++) {</pre>
                                for (iorder=1; iorder<=rsp_pert->pert_max_orders[ilab]; iorder++,icomp++) {
                                         if (pert_num_comps[icomp]<1) {</pre>
                                                 printf("RSPPertCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                                                                 ilab,
                                                                pert_labels[ilab]);
                                                 printf("RSPPertCreate>> allowed maximal order is %"QINT_FMT"\n",
                                                                pert_max_orders[ilab]);
                                                 printf("RSPPertCreate>> %"QINT_FMT"-th No. of comps. is %"QINT_FMT"\n",
                                                                iorder,
                                                                pert_num_comps[icomp]);
                                                 QErrorExit(FILE_AND_LINE, "incorrect number of components");
                                         }
                                        rsp_pert->pert_num_comps[icomp] = pert_num_comps[icomp];
                                }
               #if defined(OPENRSP_C_USER_CONTEXT)
                        rsp_pert->user_ctx = user_ctx;
               #endif
                       rsp_pert->get_pert_concatenation = get_pert_concatenation;
                       return QSUCCESS;
               }
            Here we check the number of perturbation labels and each label against OPENRSP_PERT_LABEL_MAX.
            \langle RSPPerturbation.c \ 22c \rangle + \equiv
28
               /* <function name='RSPPertAssemble'</pre>
                                           attr='private'
                                           author='Bin Gao'
                                           date='2015-06-28'>
                          Assembles the context of perturbations involved in calculations
                          <param name='rsp_pert' direction='inout'>
                              The context of perturbations
                          </param>
                          <return>Error information</return>
                      </function> */
               QErrorCode RSPPertAssemble(RSPPert *rsp_pert)
               {
                        if (rsp_pert->pert_labels==NULL ||
                                rsp_pert->pert_max_orders==NULL ||
                                rsp_pert->ptr_ncomp==NULL ||
                                rsp_pert->pert_num_comps==NULL ||
```

```
rsp_pert->get_pert_concatenation==NULL) {
        QErrorExit(FILE_AND_LINE, "perturbations are not correctly set");
    }
   return QSUCCESS;
}
/* <function name='RSPPertWrite'</pre>
            attr='private'
             author='Bin Gao'
             date='2015-06-28'>
    Writes the context of perturbations involved in calculations
     <param name='rsp_pert' direction='in'>
      The context of perturbations
    </param>
     <param name='fp_pert' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPPertWrite(const RSPPert *rsp_pert, FILE *fp_pert)
{
    QInt ilab; /* incremental recorder over perturbation labels */
    QInt icomp; /* incremental recorder over components */
    fprintf(fp_pert,
            "RSPPertWrite>> number of all perturbation labels %"QINT_FMT"\n",
            rsp_pert->num_pert_lab);
    fprintf(fp_pert,
                                                              numbers-of-components\n");
            "RSPPertWrite>> label
                                            maximum-order
    for (ilab=0; ilab<rsp_pert->num_pert_lab; ilab++) {
        fprintf(fp_pert,
                "RSPPertWrite>> %"QCPERTINT_FMT"
                                                                 %"QINT_FMT"
                rsp_pert->pert_labels[ilab],
                rsp_pert->pert_max_orders[ilab]);
        for (icomp=rsp_pert->ptr_ncomp[ilab]; icomp<rsp_pert->ptr_ncomp[ilab+1]; icomp++) {
            fprintf(fp_pert, " %"QINT_FMT"", rsp_pert->pert_num_comps[icomp]);
        fprintf(fp_pert, "\n");
#if defined(OPENRSP_C_USER_CONTEXT)
    if (rsp_pert->user_ctx!=NULL) {
        fprintf(fp_pert, "RSPPertWrite>> user-defined function context given\n");
    }
#endif
   return QSUCCESS;
}
/* <function name='RSPPertDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-06-28'>
    Destroys the context of perturbations involved in calculations, should be
    called at the end
     <param name='rsp_pert' direction='inout'>
       The context of perturbations
```

</param>

<return>Error information</return>

```
</function> */
        QErrorCode RSPPertDestroy(RSPPert *rsp_pert)
            rsp_pert->num_pert_lab = 0;
             free(rsp_pert->pert_labels);
            rsp_pert->pert_labels = NULL;
             free(rsp_pert->pert_max_orders);
            rsp_pert->pert_max_orders = NULL;
             free(rsp_pert->ptr_ncomp);
             rsp_pert->ptr_ncomp = NULL;
             free(rsp_pert->pert_num_comps);
             rsp_pert->pert_num_comps = NULL;
        #if defined(OPENRSP_C_USER_CONTEXT)
             rsp_pert->user_ctx = NULL;
        #endif
             rsp_pert->get_pert_concatenation = NULL;
            return QSUCCESS;
        }
         When users set different contributions to the Hamiltonian, there are also perturbations acting
      on the corresponding contributions. We need to check if these perturbations are valid:
      \langle RSPertAPIs \ 25a \rangle + \equiv
30a
        extern QErrorCode RSPPertValidateLabelOrder(const RSPPert*,
                                                        const QInt,
                                                        const QcPertInt*,
                                                        const QInt*);
30b
      \langle RSPPerturbation.c \ 22c \rangle + \equiv
        /* <function name='RSPPertValidateLabelOrder'
                      attr='private'
                      author='Bin Gao'
                      date='2015-10-15'>
              Check the validity of given perturbation labels and corresponding allowed
              maximal orders
              <param name='rsp_pert' direction='in'>
                The context of perturbations
              </param>
              <param name='num_pert_lab' direction='in'>
                Number of all different perturbation labels
              </param>
              <param name='pert_labels' direction='in'>
                Different perturbation labels that will be checked
              </param>
              <param name='pert_max_orders' direction='in'>
                Allowed maximal order of a perturbation described by exactly one of
                the above different labels
              </param>
              <return>
                <QSUCCESS> if perturbation labels and orders are valid,
                <QFAILURE> otherwise
              </return>
```

```
</function> */
QErrorCode RSPPertValidateLabelOrder(const RSPPert *rsp_pert,
                                      const QInt num_pert_lab,
                                      const QcPertInt *pert_labels,
                                      const QInt *pert_max_orders)
{
    QInt ilab;
                       /* incremental recorders over perturbation labels */
   QInt jlab;
    QBool pert_valid; /* validity of the perturbations */
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
        pert_valid = QFALSE;
        for (jlab=0; jlab<rsp_pert->num_pert_lab; jlab++) {
            /* valid perturbation label, checks its allowed maximal order */
            if (pert_labels[ilab] == rsp_pert->pert_labels[jlab]) {
                if (pert_max_orders[ilab]<=rsp_pert->pert_max_orders[jlab]) {
                    pert_valid = QTRUE;
                }
                break;
            }
        }
        if (pert_valid==QFALSE) return QFAILURE;
    }
    return QSUCCESS;
}
```

One should note that we here assume all the elements of pert_labels are different.

3.3.4 Conversion of Perturbation Tuples and Labels

As discussed in Section 3.3.1, we will use internal perturbation labels (identifier and host program's perturbation label) inside OpenRSP. As such, we need to implement functions for the conversion of internal perturbation labels and host programs' ones.

First, when calculating response functions and residues, we need to convert the users' given perturbation tuple $abc\cdots$ into our internal one. We also need to sort the perturbation tuple $abc\cdots$ and the corresponding complex frequencies $[\omega_a\omega_b\omega_c\cdots,\cdots]$. The sorting is carried out in two steps:

- 1. We take the first label of the perturbation tuple as the perturbation a (see definition in Section 2.5.6). We fix the first label of the tuple, and rearrange the tuple by collecting identical labels together after their first entity.
 - For example, the sorted perturbation tuple of acbadbc becomes aaccbbd.
- 2. We next sort frequencies of the same perturbation labels in ascending order, and the frequency of the first label of the tuple is the negative sum of frequencies of other labels. For example, if users give two frequency configurations for a perturbation tuple *aaccbbd*, the sorted frequencies will satisfy:

$$-\sum_{i} \omega_{i} \leq \omega_{1} \leq \omega_{2} \leq \omega_{3} \leq \omega_{4} \leq \omega_{5} \leq \omega_{6},$$
$$-\sum_{i} \omega'_{i} \leq \omega'_{1} \leq \omega'_{2} \leq \omega'_{3} \leq \omega'_{4} \leq \omega'_{5} \leq \omega'_{6}.$$

The following function will perform the above converting and sorting procedure, and also check if the perturbation labels have been given by the API OpenRSPSetPerturbations():

```
extern QErrorCode RSPPertHostToInternal(const RSPPert*,
                                                 const QInt,
                                                 QcPertInt*,
                                                 const QInt,
                                                 QReal*);
32
     \langle RSPPerturbation.c \ 22c \rangle + \equiv
       /* <function name='RSPPertHostToInternal'</pre>
                    attr='private'
                    author='Bin Gao'
                    date='2015-10-08'>
            Check, convert and sort a host program's perturbation tuple and
            corresponding frequencies
            <param name='rsp_pert' direction='in'>
              The context of perturbations
            </param>
            <param name='len_tuple' direction='in'>
              Length of the host program's and the internal perturbation tuples
            <param name='pert_tuple' direction='in'>
              The host program's perturbation tuple, in which the first label
              is the perturbation $a$
            </param>
            <param name='num_freq_configs' direction='in'>
              Number of different frequency configurations
            </param>
            <param name='pert_freqs' direction='in'>
              Complex frequencies of each perturbation label (except for the
              perturbation $a$) over all frequency configurations, size is therefore
              $2\times[(<len_tuple>-1)\times<num_freq_configs>]$, and arranged as
              <c>[num_freq_configs] [len_tuple-1] [2] </c> in memory (that is, the real
              and imaginary parts of each frequency are consecutive in memory)
            </param>
            <param name='intern_pert_tuple' direction='out'>
              The internal perturbation tuple, in which identical perturbation labels
              are consecutive, and the first one is the perturbation $a$
            </param>
            <param name='intern_pert_freqs' direction='out'>
              Internal complex frequencies (in ascending order among identical
              perturbation labels) of each perturbation label (including the
              perturbation $a$) over all frequency configurations, size is therefore
              $2\times<len_tuple>\times<num_freq_configs>$, and arranged as
              <c>[num_freq_configs][len_tuple][2]</c> in memory (that is, the real and
              imaginary parts of each frequency are consecutive in memory)
            </param>
            <return>Error information</return>
          </function> */
       QErrorCode RSPPertHostToInternal(const RSPPert *rsp_pert,
                                         const QInt len_tuple,
                                         QcPertInt *pert_tuple,
                                         const QInt num_freq_configs,
                                         QReal *pert_freqs)
       {
```

```
//
      QcPertInt id_pert; /* identifiers of different perturbation labels */
//
                          /* validity of the perturbation labels */
      QBool lab_valid;
//
      QInt ipert, jpert; /* incremental recorders */
//
//
      QInt first_id;
                         /* first identical pertubation label in the tuple */
//
      QInt last_id;
                         /* last identical pertubation label in the tuple */
                         /* indicates if non-identical label found */
//
      QBool non_id;
//
//
      id_pert = 0;
//
//
      for (ipert=0,jpert=0; ipert<len_tuple; ) {</pre>
//
//
        /* checks the current perturbation label against all known
//
             perturbation labels */
//
          lab_valid = QFALSE;
//
          for (ilab=0; ilab<rsp_pert->num_pert_lab; ilab++) {
//
              if (pert_tuple[ipert] == rsp_pert->pert_labels[ilab]) {
//
                  lab_valid = QTRUE;
//
                  break;
//
              }
//
          }
//
          if (lab_valid==QTRUE) {
//
              /* converts the current perturbation label to internal one */
              intern_pert_tuple[jpert] = (id_pert<<OPENRSP_PERT_LABEL_BIT)</pre>
//
//
                                        + pert_tuple[ipert];
//
              /* finds the other same perturbation labels */
//
//
//
              /* updates the identifier */
//
              id_pert++;
//
          else {
//
              printf("RSPPertCreate>> %"QINT_FMT"-th perturbation %"QCPERTINT_FMT"\n",
//
                     ipert,
//
                     pert_tuple[ipert]);
//
              QErrorExit(FILE_AND_LINE, "invalid perturbation label");
//
          }
//
//
//
      }
//
//
      /* we first try to find consecutive identical pertubation labels */
//
      first_id = 0;
//
      non_id = QFALSE;
//
      for (ipert=first_id; ipert<len_tuple-1; ipert++) {</pre>
//
          if (pert_tuple[ipert]!=pert_tuple[ipert+1]) {
//
              last_id = ipert;
//
              non_id = QTRUE;
//
              break;
//
          }
//
      if (non_id=QTRUE) {
//
//
      }
```

```
// else {
// }

return QSUCCESS;
}
```

where we have also checked the number of different identifiers against OPENRSP_PERT_ID_MAX.

Inside OpenRSP, we mostly use the internal perturbation labels/tuples. But when we use callback functions to get integrals and/or expectation values of overlap, one- and two-electron operators as well as contributions from nuclear Hamiltonian, only the host programs' perturbation labels and orders are meaningful for these callback functions; when we want the integrals and/or expectation values of XC functionals¹, we need to convert our internal perturbation tuples to the host programs' ones.

We first consider the former taks—a function that converts an internal pertubration tuple into host program's perturbation labels and orders:

```
\langle RSPertAPIs \ 25a \rangle + \equiv
```

This function also checks if the resulted perturbation labels and orders are allowed (or non-zero perturbed quantities) by checkeing against allowed host program's perturbation labels and orders:

```
\langle RSPPerturbation.c \ 22c \rangle + \equiv
```

```
/* <function name='RSPPertInternTupleToHostLabelOrder'
             attr='private'
             author='Bin Gao'
             date='2015-10-08'>
    Convert an internal perturbation tuple to host program's pertubation
    labels and the corresponding orders
     <param name='len_intern_tuple' direction='in'>
       Length of the internal perturbation tuple
     </param>
     <param name='intern_pert_tuple' direction='in'>
       The internal perturbation tuple
     <param name='num_allowed_labels' direction='in'>
       Number of allowed different host program's perturbation labels
     <param name='allowed_pert_labels' direction='in'>
       All the allowed different host program's perturbation labels
     </param>
     <param name='allowed_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different host program's labels
     </param>
```

¹XC functionals need all density matrices and are calculated differently from other operators, we therefore choose to send the perturbation tuple to XC-functional callback functions

```
<param name='num_pert' direction='out'>
       Number of different perturbations from the internal perturbation tuple,
       $-1$ indicates there are perturbation labels/orders not allowed
     </param>
     <param name='pert_labels' direction='out'>
       Host program's pertubation labels of the resulted perturbations
     <param name='pert_orders' direction='out'>
       Orders of the resulted perturbations
     <return>Error information</return>
   </function> */
QErrorCode RSPPertInternTupleToHostLabelOrder(const QInt len_intern_tuple,
                                               const QcPertInt *intern_pert_tuple,
                                               const QInt num_allowed_labels,
                                               const QcPertInt *allowed_pert_labels,
                                               const QInt *allowed_max_orders,
                                              QInt *num_pert,
                                               QcPertInt *pert_labels,
                                              QInt *pert_orders)
{
    QcPertInt host_pert_label; /* host program's perturbation label */
                                /* resulted perturbations allowed or not */
    QBool pert_allowed;
                                /* incremental recorder for different perturbations */
    QInt ipert;
    QInt ilab;
                                /* incremental recorder over perturbation labels */
    QInt idx_allowed;
                                /* index of the allowed perturbation label */
    ipert = 0;
    for (ilab=0; ilab<len_intern_tuple; ) {</pre>
        /* converts to the host program's label */
        host_pert_label = intern_pert_tuple[ilab] & OPENRSP_PERT_LABEL_MAX;
        /* checks if the label is allowed */
        pert_allowed = QFALSE;
        for (idx_allowed=0; idx_allowed<num_allowed_labels; idx_allowed++) {
            if (host_pert_label==allowed_pert_labels[idx_allowed]) {
                pert_allowed = QTRUE;
                break;
            }
        }
        /* returns a negative number if the label is not allowed */
        if (pert_allowed==QFALSE) {
            *num_pert = -1;
            return QSUCCESS;
        /* finds consecutive identical internal perturbation labels */
        pert_labels[ipert] = intern_pert_tuple[ilab];
        pert_orders[ipert] = 1;
        ilab++;
        for (; ilab<len_intern_tuple; ) {</pre>
            if (pert_labels[ipert] == intern_pert_tuple[ilab]) {
                pert_orders[ipert]++;
            }
            else {
```

```
break;
}
ilab++;
}
/* checks if the order is allowed */
if (pert_orders[ipert]>allowed_max_orders[idx_allowed]) {
    *num_pert = -1;
    return QSUCCESS;
}
/* saves the host program's label */
    pert_labels[ipert] = host_pert_label;
    ipert++;
}
*num_pert = ipert;
return QSUCCESS;
}
```

where the conversion of the internal label to the host program's label is simply done by the bitwise AND operation (&=) with OPENRSP_PERT_LABEL_MAX.

As such, the latter task—converting our internal perturbation tuples to the host programs' ones is also quite easy:

```
\langle RSPertAPIs \ 25a \rangle + \equiv
36a
        extern QErrorCode RSPPertInternTupleToHostTuple(const QInt,
                                                            const QcPertInt*,
                                                            const QInt,
                                                            const QcPertInt*,
                                                            const QInt*,
                                                            QInt*,
                                                            QcPertInt*);
36b
      \langle RSPPerturbation.c \ 22c \rangle + \equiv
        /* <function name='RSPPertInternTupleToHostTuple'</pre>
                      attr='private'
                      author='Bin Gao'
                      date='2015-10-12'>
             Convert an internal perturbation tuple to the corresponding host
             program's one
              <param name='len_intern_tuple' direction='in'>
                Length of the internal perturbation tuple
              <param name='intern_pert_tuple' direction='in'>
                The internal perturbation tuple
              </param>
              <param name='num_allowed_labels' direction='in'>
                Number of allowed different host program's perturbation labels
              </param>
              <param name='allowed_pert_labels' direction='in'>
                All the allowed different host program's perturbation labels
              </param>
              <param name='allowed_max_orders' direction='in'>
                Allowed maximal order of a perturbation described by exactly one of
                the above different host program's labels
              </param>
```

```
<param name='len_tuple' direction='out'>
       Length of the resulted host program's perturbation tuple,
       $-1$ indicates there are perturbation labels/orders not allowed
     </param>
     <param name='pert_tuple' direction='out'>
       The resulted host program's perturbation tuple
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPPertInternTupleToHostTuple(const QInt len_intern_tuple,
                                         const QcPertInt *intern_pert_tuple,
                                         const QInt num_allowed_labels,
                                         const QcPertInt *allowed_pert_labels,
                                         const QInt *allowed_max_orders,
                                         QInt *len_tuple,
                                         QcPertInt *pert_tuple)
{
    QcPertInt host_pert_label; /* host program's perturbation label */
    QInt host_pert_order;
                                /* order of host program's perturbation */
                               /* resulted perturbations allowed or not */
    QBool pert_allowed;
    QInt ipert;
                                /* incremental recorder for different perturbations */
                               /* incremental recorder over perturbation labels */
    QInt ilab;
    QInt idx_allowed;
                                /* index of the allowed perturbation label */
    ipert = 0;
    for (ilab=0; ilab<len_intern_tuple; ) {</pre>
        /* converts to the host program's label */
        host_pert_label = intern_pert_tuple[ilab] & OPENRSP_PERT_LABEL_MAX;
        /* checks if the label is allowed */
        pert_allowed = QFALSE;
        for (idx_allowed=0; idx_allowed<num_allowed_labels; idx_allowed++) {</pre>
            if (host_pert_label==allowed_pert_labels[idx_allowed]) {
                pert_allowed = QTRUE;
                break;
            }
        }
        /* returns a negative number if the label is not allowed */
        if (pert_allowed==QFALSE) {
            *len_tuple = -1;
            return QSUCCESS;
        /* finds consecutive identical internal perturbation labels */
        pert_tuple[ipert] = intern_pert_tuple[ilab];
        host_pert_order = 1;
        ilab++;
        for (; ilab<len_intern_tuple; ) {</pre>
            if (pert_tuple[ipert] == intern_pert_tuple[ilab]) {
                host_pert_order++;
            }
            else {
                break;
            }
            ilab++;
```

```
/* checks if the order is allowed */
if (host_pert_order>allowed_max_orders[idx_allowed]) {
     *len_tuple = -1;
     return QSUCCESS;
}

/* saves the host program's labels */
for (; host_pert_order>0; host_pert_order--) {
     pert_tuple[ipert] = host_pert_label;
     ipert++;
}

*len_tuple = ipert;
return QSUCCESS;
}
```

We will also use the callback function declared in Section 3.3.2 for OpenRSP to construct higher-order derivatives from lower-order ones:

```
38a \langle RSPertAPIs \ 25a \rangle + \equiv
extern QErrorCode RSPPertGetConcatenation(const RSPPert*,
const QcPertInt,
const QInt,
const QInt,
const QInt,
const QInt,
QInt*);
```

This function actually uses the callback function get_pert_concatenation() to get ranks of components of sub-perturbation tuples (with the same perturbation label) for given components of the corresponding concatenated perturbation tuple:

```
38b
      \langle RSPPerturbation.c \ 22c \rangle + \equiv
        /* <function name='RSPPertGetConcatenation'</pre>
                      attr='private'
                      author='Bin Gao'
                      date='2015-06-28'>
             Gets the ranks of components of sub-perturbation tuples
              <param name='rsp_pert' direction='inout'>
               The context of perturbations
             </param>
              <param name='intern_pert_label' direction='in'>
               The internal perturbation label
             </param>
              <param name='first_cat_comp' direction='in'>
               Rank of the first component of the concatenated perturbation tuple
              <param name='num_cat_comps' direction='in'>
               Number of components of the concatenated perturbation tuple
             </param>
              <param name='num_sub_tuples' direction='in'>
               Number of sub-perturbation tuples to construct the concatenated
               perturbation tuple
              </param>
```

<param name='len_sub_tuples' direction='in'>

```
Length of each sub-perturbation tuple, size is <num_sub_tuples> so
       that the length of the concatenated perturbation tuple is the sum
       of <len_sub_tuples>
     </param>
     <param name='rank_sub_comps' direction='out'>
       Ranks of components of sub-perturbation tuples for the corresponding
       component of the concatenated perturbation tuple, i.e. <num_cat_comps>
       components starting from the one with the rank <first_cat_comp>; size
       is therefore the product of <num_sub_tuples> and <num_cat_comps>, and
       is arranged as <c>[num_cat_comps][num_sub_tuples]</c> in memory
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPPertGetConcatenation(const RSPPert *rsp_pert,
                                   const QcPertInt intern_pert_label,
                                   const QInt first_cat_comp,
                                   const QInt num_cat_comps,
                                   const QInt num_sub_tuples,
                                   const QInt *len_sub_tuples,
                                   QInt *rank_sub_comps)
{
    QcPertInt pert_label;
    /* converts to host program's perturbation label */
   pert_label = intern_pert_label & OPENRSP_PERT_LABEL_MAX;
#if defined(OPENRSP_ZERO_BASED)
   rsp_pert->get_pert_concatenation(pert_label,
                                     first_cat_comp,
                                     num_cat_comps,
                                     num_sub_tuples,
                                     len_sub_tuples,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     rsp_pert->user_ctx,
#endif
                                     rank_sub_comps);
#else
    QInt icomp; /* incremental recorder over ranks of components */
   rsp_pert->get_pert_concatenation(pert_label,
                                     first_cat_comp+1,
                                     num_cat_comps,
                                     num_sub_tuples,
                                     len_sub_tuples,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     rsp_pert->user_ctx,
#endif
                                     rank_sub_comps);
    for (icomp=0; icomp<num_cat_comps*num_sub_tuples; icomp++) {</pre>
        rank_sub_comps[icomp]--;
   }
#endif
   return QSUCCESS;
}
```

Here except for the conversion to host program's perturbation label, we also need to convert ranks to zero-based numbering if users have chosen the one-based numbering.

3.4 Overlap Operator

OPENRSP needs to invoke host program's callback functions to calculate the integral matrices or expectation values of overlap operator as well as its derivatives with respect to different perturbations. Users can use the following API to tell OpenRSP the information of the overlap operator:

```
\langle OpenRSP.c \ 17a \rangle + \equiv
41
       /* <function name='OpenRSPSetOverlap' author='Bin Gao' date='2014-07-30'>
            Set the overlap operator
            <param name='open_rsp' direction='inout'>
              The context of response theory calculations
            </param>
            <param name='num_pert_lab' direction='in'>
              Number of all different perturbation labels that can act on the
              overlap operator
            </param>
            <param name='pert_labels' direction='in'>
              All the different perturbation labels involved
            </param>
            <param name='pert_max_orders' direction='in'>
              Allowed maximal order of a perturbation described by exactly one of
              the above different labels
            </param>
            <param name='user_ctx' direction='in'>
              User-defined callback function context
            </param>
            <param name='get_overlap_mat' direction='in'>
              User-specified callback function to calculate integral matrices of
              overlap operator as well as its derivatives with respect to different
              perturbations
            </param>
            <param name='get_overlap_exp' direction='in'>
              User-specified callback function to calculate expectation values of
              overlap operator as well as its derivatives with respect to different
              perturbations
            </param>
            <return>Error information</return>
          </function> */
       QErrorCode OpenRSPSetOverlap(OpenRSP *open_rsp,
                                     const QInt num_pert_lab,
                                     const QcPertInt *pert_labels,
                                     const QInt *pert_max_orders,
       #if defined(OPENRSP_C_USER_CONTEXT)
                                     void *user_ctx,
       #endif
                                     const GetOverlapMat get_overlap_mat,
                                     const GetOverlapExp get_overlap_exp)
       {
           QErrorCode ierr; /* error information */
           /* creates the context of overlap operator */
           if (open_rsp->overlap!=NULL) {
               ierr = RSPOverlapDestroy(open_rsp->overlap);
               QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapDestroy()");
```

```
}
    else {
        open_rsp->overlap = (RSPOverlap *)malloc(sizeof(RSPOverlap));
        if (open_rsp->overlap==NULL) {
            QErrorExit(FILE_AND_LINE, "allocates memory for overlap");
        }
    }
    ierr = RSPOverlapCreate(open_rsp->overlap,
                            num_pert_lab,
                            pert_labels,
                            pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_overlap_mat,
                            get_overlap_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOverlapCreate()");
    return QSUCCESS;
}
```

The following header file defines all quantities we need for the overlap operator. Types GetOverlapMat and GetOverlapExp define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of overlap operator and its derivatives.

```
\langle RSPOverlap.h \ 42 \rangle \equiv
    ⟨OpenRSPLicense 14a⟩
    <header name='RSPOneOper.h' author='Bin Gao' date='2014-08-05'>
      The header file of overlap operator used inside OpenRSP
    </header>
 */
 #if !defined(RSP_OVERLAP_H)
 #define RSP_OVERLAP_H
 #include "qcmatrix.h"
 #include "RSPPerturbation.h"
 typedef void (*GetOverlapMat)(const QInt,
                                  const QcPertInt*,
                                  const QInt*,
                                  const QInt,
                                  const QcPertInt*,
                                  const QInt*,
                                  const QInt,
                                  const QcPertInt*,
                                  const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                  void*,
 #endif
                                  const QInt,
```

```
QcMat*[]);
 typedef void (*GetOverlapExp)(const QInt,
                                 const QcPertInt*,
                                 const QInt*,
                                 const QInt,
                                 const QcPertInt*,
                                 const QInt*,
                                 const QInt,
                                 const QcPertInt*,
                                 const QInt*,
                                 const QInt,
                                 QcMat*[],
 #if defined(OPENRSP_C_USER_CONTEXT)
                                 void*,
 #endif
                                 const QInt,
                                 QReal*);
 \langle RSPOverlapStruct 43 \rangle
 \langle RSPOverlapAPIs \ 44a \rangle
 #endif
The context of overlap operator is:
\langle RSPOverlapStruct \ 43 \rangle \equiv
 typedef struct {
     QInt num_pert_lab;
                                       /* number of different perturbation labels
                                           that can act as perturbations on the
                                           overlap operator */
                                       /* number of perturbations on the bra center,
     QInt bra_num_pert;
                                           only used for callback functions */
     QInt ket_num_pert;
                                       /* number of perturbations on the ket center,
                                           only used for callback functions */
     QInt oper_num_pert;
                                       /* number of perturbations on the overlap operator,
                                           only used for callback functions */
                                       /* allowed maximal order of a perturbation
     QInt *pert_max_orders;
                                           described by exactly one of these
                                           different labels */
     QInt *bra_pert_orders;
                                       /* orders of perturbations on the bra center,
                                           only used for callback functions */
     QInt *ket_pert_orders;
                                        /* orders of perturbations on the ket center,
                                           only used for callback functions */
     QInt *oper_pert_orders;
                                        /* orders of perturbations on the overlap operator,
                                           only used for callback functions */
     QcPertInt *pert_labels;
                                        /* all the different perturbation labels */
                                        /* labels of perturbations on the bra center,
     QcPertInt *bra_pert_labels;
                                           only used for callback functions */
                                       /* labels of perturbations on the ket center,
     QcPertInt *ket_pert_labels;
                                           only used for callback functions */
                                       /* labels of perturbations on the overlap operator,
     QcPertInt *oper_pert_labels;
                                           only used for callback functions */
 #if defined(OPENRSP_C_USER_CONTEXT)
```

```
void *user_ctx;
                                                /* user-defined callback-function context */
        #endif
             GetOverlapMat get_overlap_mat; /* user-specified function for calculating
                                                    integral matrices */
             GetOverlapExp get_overlap_exp;
                                                /* user-specified function for calculating
                                                    expectation values */
        } RSPOverlap;
       and the functions related to the overlap operator:
       \langle RSPOverlapAPIs \ 44a \rangle \equiv
44a
        extern QErrorCode RSPOverlapCreate(RSPOverlap*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt*,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                               void*,
        #endif
                                               const GetOverlapMat,
                                               const GetOverlapExp);
        extern QErrorCode RSPOverlapAssemble(RSPOverlap*,const RSPPert*);
        extern QErrorCode RSPOverlapWrite(const RSPOverlap*,FILE*);
        extern QErrorCode RSPOverlapGetMat(RSPOverlap*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               QcMat*[]);
        extern QErrorCode RSPOverlapGetExp(RSPOverlap*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               const QcPertInt*,
                                               const QInt,
                                               QcMat*[],
                                               const QInt,
                                               QReal*);
        extern QErrorCode RSPOverlapDestroy(RSPOverlap*);
          Let us now implement all the functions declared:
44b
       \langle RSPOverlap.c \ 44b \rangle \equiv
           \langle OpenRSPLicense 14a \rangle
        #include "RSPOverlap.h"
        /* <function name='RSPOverlapCreate'</pre>
                       attr='private'
                       author='Bin Gao'
```

```
date='2014-08-05'>
    Create the context of overlap operator, should be called at first
     <param name='overlap' direction='inout'>
       The context of overlap operator
     </param>
     <param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels that can act as
      perturbations on the overlap operator
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback-function context
     </param>
     <param name='get_overlap_mat' direction='in'>
       User-specified function for calculating integral matrices of the
       overlap operator and its derivatives
     </param>
     <param name='get_overlap_exp' direction='in'>
       User-specified function for calculating expectation values of the
       overlap operator and its derivatives
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOverlapCreate(RSPOverlap *overlap,
                            const QInt num_pert_lab,
                            const QcPertInt *pert_labels,
                            const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            void *user_ctx,
#endif
                            const GetOverlapMat get_overlap_mat,
                            const GetOverlapExp get_overlap_exp)
{
    QInt ilab; /* incremental recorders over perturbation labels */
    QInt jlab;
    if (num_pert_lab<0) {</pre>
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPOverlapCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
```

```
}
overlap->num_pert_lab = num_pert_lab;
if (overlap->num_pert_lab>0) {
    overlap->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->pert_max_orders==NULL) {
        printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    overlap->bra_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->bra_pert_orders==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on bra center");
    }
    overlap->ket_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->ket_pert_orders==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on ket center");
    overlap->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (overlap->oper_pert_orders==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on overlap operato
    }
    overlap->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->pert_labels==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    overlap->bra_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->bra_pert_labels==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on bra center");
    }
    overlap->ket_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->ket_pert_labels==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on ket center");
    overlap->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (overlap->oper_pert_labels==NULL) {
       printf("RSPOverlapCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on overlap operato
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
```

```
if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
                printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                       ilab,
                       pert_labels[ilab]);
                printf("RSPOverlapCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\
                       OPENRSP_PERT_LABEL_MAX);
                QErrorExit(FILE_AND_LINE, "invalid perturbation label");
            }
            /* each element of <pert_labels> should be unique */
            for (jlab=0; jlab<ilab; jlab++) {</pre>
                if (pert_labels[jlab] == pert_labels[ilab]) {
                    printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                           jlab,
                           pert_labels[jlab]);
                    printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                           ilab,
                           pert_labels[ilab]);
                    QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
                }
            }
            overlap->pert_labels[ilab] = pert_labels[ilab];
            if (pert_max_orders[ilab]<1) {</pre>
                printf("RSPOverlapCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                       ilab,
                       pert_labels[ilab]);
                printf("RSPOverlapCreate>> allowed maximal order is %"QINT_FMT"\n",
                       pert_max_orders[ilab]);
                QErrorExit(FILE_AND_LINE, "only positive order allowed");
            }
            overlap->pert_max_orders[ilab] = pert_max_orders[ilab];
        }
    }
    else {
        overlap->pert_max_orders = NULL;
        overlap->bra_pert_orders = NULL;
        overlap->ket_pert_orders = NULL;
        overlap->oper_pert_orders = NULL;
        overlap->pert_labels = NULL;
        overlap->bra_pert_labels = NULL;
        overlap->ket_pert_labels = NULL;
        overlap->oper_pert_labels = NULL;
    }
#if defined(OPENRSP_C_USER_CONTEXT)
    overlap->user_ctx = user_ctx;
#endif
    overlap->get_overlap_mat = get_overlap_mat;
    overlap->get_overlap_exp = get_overlap_exp;
    return QSUCCESS;
}
```

As shown here, we allow for an overlap operator that does not depend on any peraturbation—num_pert_lab==0, i.e. any perturbed integral matrix and expectation value of this overlap operator

```
is zero.
```

```
\langle RSPOverlap.c \ 44b \rangle + \equiv
48
       /* <function name='RSPOverlapAssemble'</pre>
                    attr='private'
                    author='Bin Gao'
                    date='2014-08-05'>
            Assembles the context of overlap operator
            <param name='overlap' direction='inout'>
              The context of overlap operator
            </param>
            <param name='rsp_pert' direction='in'>
              The context of perturbations
            </param>
            <return>Error information</return>
          </function> */
       QErrorCode RSPOverlapAssemble(RSPOverlap *overlap, const RSPPert *rsp_pert)
           QErrorCode ierr; /* error information */
           if (overlap->num_pert_lab>0 &&
               (overlap->pert_labels==NULL || overlap->pert_max_orders==NULL)) {
               QErrorExit(FILE_AND_LINE, "perturbations of overlap operator not set");
           }
           if (overlap->get_overlap_mat==NULL || overlap->get_overlap_exp==NULL) {
               QErrorExit(FILE_AND_LINE, "callback functions of overlap operator not set");
           }
           /* checks perturbation labels and allowed maximal orders against
              all known perturbations */
           ierr = RSPPertValidateLabelOrder(rsp_pert,
                                             overlap->num_pert_lab,
                                              overlap->pert_labels,
                                             overlap->pert_max_orders);
           QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
           return QSUCCESS;
       }
       /* <function name='RSPOverlapWrite'</pre>
                    attr='private'
                    author='Bin Gao'
                    date='2014-08-05'>
            Writes the context of overlap operator
            <param name='overlap' direction='in'>
              The context of overlap operator
            <param name='fp_overlap' direction='inout'>File pointer</param>
            <return>Error information</return>
          </function> */
       QErrorCode RSPOverlapWrite(const RSPOverlap *overlap, FILE *fp_overlap)
       {
           QInt ilab; /* incremental recorder over perturbation labels */
           fprintf(fp_overlap,
                    "RSPOverlapWrite>> number of pert. labels that overlap operator depends on %"QI
                    overlap->num_pert_lab);
```

```
fprintf(fp_overlap, "RSPOverlapWrite>> label
                                                            maximum-order\n");
    for (ilab=0; ilab<overlap->num_pert_lab; ilab++) {
        fprintf(fp_overlap,
                "RSPOverlapWrite>>
                                          %"QCPERTINT_FMT"
                                                                            %"QINT_FMT"\n",
                overlap->pert_labels[ilab],
                overlap->pert_max_orders[ilab]);
    }
#if defined(OPENRSP_C_USER_CONTEXT)
    if (overlap->user_ctx!=NULL) {
        fprintf(fp_overlap, "RSPOverlapWrite>> user-defined function context given\n");
    }
#endif
   return QSUCCESS;
}
/* <function name='RSPOverlapGetMat'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates integral matrices of the overlap operator
     <param name='overlap' direction='inout'>
       The context of overlap operator
     </param>
     <param name='bra_len_tuple' direction='in'>
       Length of the perturbation tuple on the bra center
     </param>
     <param name='bra_pert_tuple' direction='in'>
       Perturbation tuple on the bra center
     </param>
     <param name='ket_len_tuple' direction='in'>
       Length of the perturbation tuple on the ket center
     </param>
     <param name='ket_pert_tuple' direction='in'>
       Perturbation tuple on the ket center
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the overlap operator
     </param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the overlap operator
     </param>
     <param name='num_int' direction='in'>
       Number of the integral matrices
     </param>
     <param name='val_int' direction='inout'>
       The integral matrices
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOverlapGetMat(RSPOverlap *overlap,
                            const QInt bra_len_tuple,
                            const QcPertInt *bra_pert_tuple,
```

```
const QInt ket_len_tuple,
                            const QcPertInt *ket_pert_tuple,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt num_int,
                            QcMat *val_int[])
{
    QErrorCode ierr; /* error information */
    /* gets perturbation labels and corresponding orders out of the internal
       perturbation tuple on the bra center */
    ierr = RSPPertInternTupleToHostLabelOrder(bra_len_tuple,
                                               bra_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->bra_num_pert,
                                               overlap->bra_pert_labels,
                                               overlap->bra_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    /* checks if the perturbations on the bra center result in zero values */
    if (overlap->bra_num_pert<0) return QSUCCESS;</pre>
    /* performs the same procedure for the perturbations on the ket center */
    ierr = RSPPertInternTupleToHostLabelOrder(ket_len_tuple,
                                               ket_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->ket_num_pert,
                                               overlap->ket_pert_labels,
                                               overlap->ket_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    if (overlap->ket_num_pert<0) return QSUCCESS;</pre>
    /* performs the same procedure for the perturbations on the overlap operator */
    ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                               oper_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->oper_num_pert,
                                               overlap->oper_pert_labels,
                                               overlap->oper_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    if (overlap->oper_num_pert<0) return QSUCCESS;</pre>
    /* calculates integral matrices using the callback function */
    overlap->get_overlap_mat(overlap->bra_num_pert,
                             overlap->bra_pert_labels,
                             overlap->bra_pert_orders,
                             overlap->ket_num_pert,
                             overlap->ket_pert_labels,
                              overlap->ket_pert_orders,
                              overlap->oper_num_pert,
                              overlap->oper_pert_labels,
```

```
overlap->oper_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             overlap->user_ctx,
#endif
                             num_int,
                             val_int);
   return QSUCCESS;
}
/* <function name='RSPOverlapGetExp'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates expectation values of the overlap operator
     <param name='overlap' direction='inout'>
       The context of overlap operator
     <param name='bra_len_tuple' direction='in'>
       Length of the perturbation tuple on the bra center
     <param name='bra_pert_tuple' direction='in'>
       Perturbation tuple on the bra center
     </param>
     <param name='ket_len_tuple' direction='in'>
       Length of the perturbation tuple on the ket center
     </param>
     <param name='ket_pert_tuple' direction='in'>
       Perturbation tuple on the ket center
     </param>
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the overlap operator
     </param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the overlap operator
     <param name='num_dmat' direction='in'>
       Number of atomic orbital (AO) based density matrices
     </param>
     <param name='dens_mat' direction='in'>
       The AO based density matrices
     </param>
     <param name='num_exp' direction='in'>
       Number of the expectation values
     </param>
     <param name='val_exp' direction='inout'>
       The expectation values
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOverlapGetExp(RSPOverlap *overlap,
                            const QInt bra_len_tuple,
                            const QcPertInt *bra_pert_tuple,
```

```
const QInt ket_len_tuple,
                            const QcPertInt *ket_pert_tuple,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt num_dmat,
                            QcMat *dens_mat[],
                            const QInt num_exp,
                            QReal *val_exp)
{
    QErrorCode ierr; /* error information */
    /* gets perturbation labels and corresponding orders out of the internal
       perturbation tuple on the bra center */
    ierr = RSPPertInternTupleToHostLabelOrder(bra_len_tuple,
                                               bra_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->bra_num_pert,
                                               overlap->bra_pert_labels,
                                               overlap->bra_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    /* checks if the perturbations on the bra center result in zero values */
    if (overlap->bra_num_pert<0) return QSUCCESS;</pre>
    /* performs the same procedure for the perturbations on the ket center */
    ierr = RSPPertInternTupleToHostLabelOrder(ket_len_tuple,
                                               ket_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->ket_num_pert,
                                               overlap->ket_pert_labels,
                                               overlap->ket_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    if (overlap->ket_num_pert<0) return QSUCCESS;</pre>
    /* performs the same procedure for the perturbations on the overlap operator */
    ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                               oper_pert_tuple,
                                               overlap->num_pert_lab,
                                               overlap->pert_labels,
                                               overlap->pert_max_orders,
                                               &overlap->oper_num_pert,
                                               overlap->oper_pert_labels,
                                               overlap->oper_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    if (overlap->oper_num_pert<0) return QSUCCESS;</pre>
    /* calculates expectation values using the callback function */
    overlap->get_overlap_exp(overlap->bra_num_pert,
                             overlap->bra_pert_labels,
                             overlap->bra_pert_orders,
                              overlap->ket_num_pert,
                              overlap->ket_pert_labels,
                              overlap->ket_pert_orders,
```

```
overlap->oper_num_pert,
                             overlap->oper_pert_labels,
                             overlap->oper_pert_orders,
                             num_dmat,
                             dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                             overlap->user_ctx,
#endif
                             num_exp,
                             val_exp);
    return QSUCCESS;
}
/* <function name='RSPOverlapDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-05'>
     Destroys the context of overlap operator, should be called at the end
     <param name='overlap' direction='inout'>
       The context of overlap operator
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOverlapDestroy(RSPOverlap *overlap)
    if (overlap->pert_max_orders!=NULL) {
        free(overlap->pert_max_orders);
        overlap->pert_max_orders = NULL;
    }
    if (overlap->bra_pert_orders!=NULL) {
        free(overlap->bra_pert_orders);
        overlap->bra_pert_orders = NULL;
    }
    if (overlap->ket_pert_orders!=NULL) {
        free(overlap->ket_pert_orders);
        overlap->ket_pert_orders = NULL;
    }
    if (overlap->oper_pert_orders!=NULL) {
        free(overlap->oper_pert_orders);
        overlap->oper_pert_orders = NULL;
    }
    if (overlap->pert_labels!=NULL) {
        free(overlap->pert_labels);
        overlap->pert_labels = NULL;
    if (overlap->bra_pert_labels!=NULL) {
        free(overlap->bra_pert_labels);
        overlap->bra_pert_labels = NULL;
    }
    if (overlap->ket_pert_labels!=NULL) {
        free(overlap->ket_pert_labels);
        overlap->ket_pert_labels = NULL;
```

```
}
if (overlap->oper_pert_labels!=NULL) {
    free(overlap->oper_pert_labels);
    overlap->oper_pert_labels = NULL;
}
#if defined(OPENRSP_C_USER_CONTEXT)
    overlap->user_ctx = NULL;
#endif
    overlap->get_overlap_mat = NULL;
    overlap->get_overlap_exp = NULL;
    return QSUCCESS;
}
```

3.5 One-Electron Operators

Users can use the following API to add different one-electron operators: $\langle OpenRSP.c~17a \rangle + \equiv$ /* <function name='OpenRSPAddOneOper' author='Bin Gao' date

```
/* <function name='OpenRSPAddOneOper' author='Bin Gao' date='2014-07-30'>
     Add a one-electron operator to the Hamiltonian
     <param name='open_rsp' direction='inout'>
       The context of response theory calculations
     </param>
     <param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels that can act on the
       one-electron operator
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels involved
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback function context
     </param>
     <param name='get_one_oper_mat' direction='in'>
       User-specified callback function to calculate integral matrices of
       one-electron operator as well as its derivatives with respect to
       different perturbations
     </param>
     <param name='get_one_oper_exp' direction='in'>
       User-specified callback function to calculate expectation values of
       one-electron operator as well as its derivatives with respect to
       different perturbations
     </param>
     <return>Error information</return>
   </function> */
QErrorCode OpenRSPAddOneOper(OpenRSP *open_rsp,
                             const QInt num_pert_lab,
                             const QcPertInt *pert_labels,
                             const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             void *user_ctx,
#endif
                             const GetOneOperMat get_one_oper_mat,
                             const GetOneOperExp get_one_oper_exp)
{
    QErrorCode ierr; /* error information */
    /* creates the linked list of one-electron operators */
    if (open_rsp->one_oper==NULL) {
        ierr = RSPOneOperCreate(&open_rsp->one_oper,
                                num_pert_lab,
                                pert_labels,
                                pert_max_orders,
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
                                 user_ctx,
#endif
                                 get_one_oper_mat,
                                 get_one_oper_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperCreate()");
    }
    /* adds the one-electron operator to the linked list */
    else {
        ierr = RSPOneOperAdd(open_rsp->one_oper,
                              num_pert_lab,
                              pert_labels,
                              pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                              user_ctx,
#endif
                              get_one_oper_mat,
                              get_one_oper_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperAdd()");
    }
    return QSUCCESS;
}
```

The following header file defines all quantities we need for one-electron operators. Types GetOneOperMat and GetOneOperpExp define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of a one-electron operator and its derivatives.

```
\langle RSPOneOper.h \ 56 \rangle \equiv
    ⟨OpenRSPLicense 14a⟩
   <header name='RSPOneOper.h' author='Bin Gao' date='2014-07-30'>
      The header file of one-electron operators used inside OpenRSP
    </header>
 */
 #if !defined(RSP_ONEOPER_H)
 #define RSP_ONEOPER_H
 #include "qcmatrix.h"
 #include "RSPPerturbation.h"
 typedef void (*GetOneOperMat)(const QInt,
                                  const QcPertInt*,
                                  const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                  void*,
 #endif
                                  const QInt,
                                  QcMat*[]);
 typedef void (*GetOneOperExp)(const QInt,
                                  const QcPertInt*,
```

```
const QInt*,
                                         const QInt,
                                         QcMat*[],
        #if defined(OPENRSP_C_USER_CONTEXT)
                                         void*,
        #endif
                                         const QInt,
                                         QReal*);
        \langle RSPOneOperStruct 57a \rangle
        \langle RSPOneOperAPIs \ 57b \rangle
        #endif
      Here we use a linked list for the context of one-electron operators:
57a
      \langle RSPOneOperStruct 57a \rangle \equiv
        typedef struct RSPOneOper RSPOneOper;
        struct RSPOneOper {
             QInt num_pert_lab;
                                                 /* number of different perturbation labels
                                                    that can act as perturbations on the
                                                    one-electron operator */
             QInt oper_num_pert;
                                                 /* number of perturbations on the
                                                    one-electron operator, only used for
                                                    callback functions */
                                                 /* allowed maximal order of a perturbation
             QInt *pert_max_orders;
                                                    described by exactly one of these
                                                    different labels */
                                                 /* orders of perturbations on the
             QInt *oper_pert_orders;
                                                    one-electron operator, only used for
                                                    callback functions */
             QcPertInt *pert_labels;
                                                 /* all the different perturbation labels */
             QcPertInt *oper_pert_labels;
                                                 /* labels of perturbations on the
                                                    one-electron operator, only used for
                                                    callback functions */
        #if defined(OPENRSP_C_USER_CONTEXT)
             void *user_ctx;
                                                 /* user-defined callback-function context */
        #endif
             GetOneOperMat get_one_oper_mat;
                                                 /* user-specified function for calculating
                                                    integral matrices */
             GetOneOperExp get_one_oper_exp;
                                                /* user-specified function for calculating
                                                    expectation values */
             RSPOneOper *next_oper;
                                                 /* pointer to the next one-electron operator */
        };
      and the functions related to the one-electron operators:
      \langle RSPOneOperAPIs \ 57b \rangle \equiv
57b
        extern QErrorCode RSPOneOperCreate(RSPOneOper**,
                                              const QInt,
                                              const QcPertInt*,
                                              const QInt*,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                              void*,
        #endif
```

const GetOneOperMat,

58

```
const GetOneOperExp);
 extern QErrorCode RSPOneOperAdd(RSPOneOper*,
                                   const QInt,
                                   const QcPertInt*,
                                   const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                   void*,
 #endif
                                   const GetOneOperMat,
                                    const GetOneOperExp);
 extern QErrorCode RSPOneOperAssemble(RSPOneOper*,const RSPPert*);
 extern QErrorCode RSPOneOperWrite(RSPOneOper*,FILE*);
 extern QErrorCode RSPOneOperGetMat(RSPOneOper*,
                                       const QInt,
                                       const QcPertInt*,
                                       const QInt,
                                       QcMat*[]);
 extern QErrorCode RSPOneOperGetExp(RSPOneOper*,
                                       const QInt,
                                       const QcPertInt*,
                                       const QInt,
                                       QcMat*[],
                                       const QInt,
                                       QReal*);
 extern QErrorCode RSPOneOperDestroy(RSPOneOper**);
   The functions are implemented as follows:
\langle RSPOneOper.c \ 58 \rangle \equiv
    \langle OpenRSPLicense 14a \rangle
 #include "RSPOneOper.h"
 /* <function name='RSPOneOperCreate'</pre>
               attr='private'
               author='Bin Gao'
               date='2014-07-30'>
       Create a node of a linked list for a given one-electron operator, should
       be called at first
       <param name='one_oper' direction='inout'>
         The linked list of one-electron operators
       </param>
       <param name='num_pert_lab' direction='in'>
         Number of all different perturbation labels that can act as
         perturbations on the one-electron operator
       </param>
       <param name='pert_labels' direction='in'>
         All the different perturbation labels
       </param>
       <param name='pert_max_orders' direction='in'>
         Allowed maximal order of a perturbation described by exactly one of
```

```
the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback-function context
     <param name='get_one_oper_mat' direction='in'>
       User-specified function for calculating integral matrices of the
       one-electron operator and its derivatives
     </param>
     <param name='get_one_oper_exp' direction='in'>
       User-specified function for calculating expectation values of the
       one-electron operator and its derivatives
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOneOperCreate(RSPOneOper **one_oper,
                            const QInt num_pert_lab,
                            const QcPertInt *pert_labels,
                            const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            void *user_ctx,
#endif
                            const GetOneOperMat get_one_oper_mat,
                            const GetOneOperExp get_one_oper_exp)
{
   RSPOneOper *new_oper; /* new operator */
    QInt ilab;
                           /* incremental recorders over perturbation labels */
    QInt jlab;
    new_oper = (RSPOneOper *)malloc(sizeof(RSPOneOper));
    if (new_oper==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for one-electron operator");
    }
    if (num_pert_lab<0) {</pre>
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPOneOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
    }
   new_oper->num_pert_lab = num_pert_lab;
    if (new_oper->num_pert_lab>0) {
        new_oper->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
        if (new_oper->pert_max_orders==NULL) {
            printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
                   num_pert_lab);
            QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
        }
```

```
new_oper->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->oper_pert_orders==NULL) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on 1el operator");
    }
    new_oper->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->pert_labels==NULL) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    new_oper->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->oper_pert_labels==NULL) {
        printf("RSPOneOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on 1el operator");
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            printf("RSPOneOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\
                   OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {</pre>
            if (pert_labels[jlab] == pert_labels[ilab]) {
                printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                       jlab,
                       pert_labels[jlab]);
                printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                       pert_labels[ilab]);
                QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
            }
        }
        new_oper->pert_labels[ilab] = pert_labels[ilab];
        if (pert_max_orders[ilab]<1) {</pre>
            printf("RSPOneOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            printf("RSPOneOperCreate>> allowed maximal order is %"QINT_FMT"\n",
                   pert_max_orders[ilab]);
            QErrorExit(FILE_AND_LINE, "only positive order allowed");
        }
        new_oper->pert_max_orders[ilab] = pert_max_orders[ilab];
    }
}
else {
```

```
new_oper->pert_max_orders = NULL;
new_oper->oper_pert_orders = NULL;
new_oper->pert_labels = NULL;
new_oper->oper_pert_labels = NULL;
}
#if defined(OPENRSP_C_USER_CONTEXT)
new_oper->user_ctx = user_ctx;
#endif
new_oper->get_one_oper_mat = get_one_oper_mat;
new_oper->get_one_oper_exp = get_one_oper_exp;
new_oper->next_oper = NULL;
*one_oper = new_oper;
return QSUCCESS;
}
```

As shown here, we allow for a one-electron operator that does not depend on any peraturbation—num_pert_lab==0, i.e. any perturbed integral matrix and expectation value of this one-electron operator is zero.

```
\langle RSPOneOper.c 58 \rangle + \equiv
61
       /* <function name='RSPOneOperAdd'</pre>
                     attr='private'
                     author='Bin Gao'
                     date='2014-07-30'>
            Add a given one-electron operator to the linked list
             <param name='one_oper' direction='inout'>
              The linked list of one-electron operators
             </param>
             <param name='num_pert_lab' direction='in'>
              Number of all different perturbation labels that can act as
              perturbations on the one-electron operator
            </param>
             <param name='pert_labels' direction='in'>
              All the different perturbation labels
            </param>
             <param name='pert_max_orders' direction='in'>
              Allowed maximal order of a perturbation described by exactly one of
              the above different labels
             </param>
             <param name='user_ctx' direction='in'>
              User-defined callback-function context
             </param>
             <param name='get_one_oper_mat' direction='in'>
              User-specified function for calculating integral matrices of the
              one-electron operator and its derivatives
            </param>
             <param name='get_one_oper_exp' direction='in'>
              User-specified function for calculating expectation values of the
              one-electron operator and its derivatives
            </param>
             <return>Error information</return>
          </function> */
       QErrorCode RSPOneOperAdd(RSPOneOper *one_oper,
```

```
const QInt num_pert_lab,
                         const QcPertInt *pert_labels,
                         const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                         void *user_ctx,
#endif
                         const GetOneOperMat get_one_oper_mat,
                         const GetOneOperExp get_one_oper_exp)
{
    RSPOneOper *new_oper; /* new operator */
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;
                          /* error information */
    /* creates the new operator */
    ierr = RSPOneOperCreate(&new_oper,
                            num_pert_lab,
                            pert_labels,
                            pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_one_oper_mat,
                            get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPOneOperCreate()");
    /* walks to the last operator */
    cur_oper = one_oper;
    while (cur_oper->next_oper!=NULL) {
        cur_oper = cur_oper->next_oper;
    }
    /* inserts the new operator to the tail of the linked list */
    cur_oper->next_oper = new_oper;
   return QSUCCESS;
}
/* <function name='RSPOneOperAssemble'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-07-30'>
     Assembles the linked list of one-electron operators
     <param name='one_oper' direction='inout'>
       The linked list of one-electron operators
     </param>
     <param name='rsp_pert' direction='in'>
       The context of perturbations
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOneOperAssemble(RSPOneOper *one_oper, const RSPPert *rsp_pert)
    QInt ioper;
                           /* incremental recorder over operators */
    RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr; /* error information */
    ioper = 0;
```

```
cur_oper = one_oper;
    do {
        if (cur_oper->num_pert_lab>0 &&
            (cur_oper->pert_labels==NULL || cur_oper->pert_max_orders==NULL)) {
            printf("RSPOneOperAssemble>> %"QINT_FMT"-th one-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "perturbations of one-electron operator not set");
        }
        if (cur_oper->get_one_oper_mat==NULL || cur_oper->get_one_oper_exp==NULL) {
            printf("RSPOneOperAssemble>> %"QINT_FMT"-th one-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "callback functions of one-electron operator not set"
        }
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                         cur_oper->num_pert_lab,
                                         cur_oper->pert_labels,
                                         cur_oper->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPOneOperWrite'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-07-30'>
    Writes the linked list of one-electron operators
    <param name='one_oper' direction='in'>
       The linked list of one-electron operators
     <param name='fp_oper' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOneOperWrite(RSPOneOper *one_oper, FILE *fp_oper)
                           /* incremental recorder over operators */
    QInt ioper;
   RSPOneOper *cur_oper; /* current operator */
                          /* incremental recorder over perturbation labels */
    QInt ilab;
    ioper = 0;
    cur_oper = one_oper;
    do {
        fprintf(fp_oper, "RSPOneOperWrite>> operator %"QINT_FMT"\n", ioper);
        fprintf(fp_oper,
                "RSPOneOperWrite>> number of pert. labels that one-electron operator depend
                cur_oper->num_pert_lab);
        fprintf(fp_oper, "RSPOneOperWrite>> label
                                                            maximum-order\n");
        for (ilab=0; ilab<cur_oper->num_pert_lab; ilab++) {
```

```
fprintf(fp_oper,
                    "RSPOneOperWrite>>
                                              %"QCPERTINT_FMT"
                                                                                %"QINT_FMT"\
                    cur_oper->pert_labels[ilab],
                    cur_oper->pert_max_orders[ilab]);
        }
#if defined(OPENRSP_C_USER_CONTEXT)
        if (cur_oper->user_ctx!=NULL) {
            fprintf(fp_oper, "RSPOneOperWrite>> user-defined function context given\n");
#endif
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPOneOperGetMat'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates integral matrices of the linked list of one-electron operators
     <param name='one_oper' direction='inout'>
       The linked list of one-electron operators
     </param>
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of one-electron
       operators
     </param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of one-electron operators
     <param name='num_int' direction='in'>
       Number of the integral matrices
     <param name='val_int' direction='inout'>
       The integral matrices
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOneOperGetMat(RSPOneOper *one_oper,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt num_int,
                            QcMat *val_int[])
{
   RSPOneOper *cur_oper; /* current operator */
   QErrorCode ierr;
                           /* error information */
    cur_oper = one_oper;
   do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the one-electron operator */
```

```
ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                   oper_pert_tuple,
                                                   cur_oper->num_pert_lab,
                                                   cur_oper->pert_labels,
                                                   cur_oper->pert_max_orders,
                                                   &cur_oper->oper_num_pert,
                                                   cur_oper->oper_pert_labels,
                                                   cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()"
        /* checks if the perturbations on the one-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert<0) continue;</pre>
        /* calculates integral matrices using the callback function */
        cur_oper->get_one_oper_mat(cur_oper->oper_num_pert,
                                    cur_oper->oper_pert_labels,
                                    cur_oper->oper_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                                    cur_oper->user_ctx,
#endif
                                   num_int,
                                    val_int);
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPOneOperGetExp'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
     Calculates expectation values of the linked list of one-electron operators
     <param name='one_oper' direction='inout'>
       The linked list of one-electron operators
     </param>
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of one-electron
       operators
     </param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of one-electron operators
     </param>
     <param name='num_dmat' direction='in'>
       Number of atomic orbital (AO) based density matrices
     <param name='dens_mat' direction='in'>
       The AO based density matrices
     </param>
     <param name='num_exp' direction='in'>
       Number of the expectation values
     </param>
     <param name='val_exp' direction='inout'>
```

```
The expectation values
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPOneOperGetExp(RSPOneOper *one_oper,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt num_dmat,
                            QcMat *dens_mat[],
                            const QInt num_exp,
                            QReal *val_exp)
{
   RSPOneOper *cur_oper; /* current operator */
    QErrorCode ierr;
                           /* error information */
    cur_oper = one_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the one-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                   oper_pert_tuple,
                                                   cur_oper->num_pert_lab,
                                                   cur_oper->pert_labels,
                                                   cur_oper->pert_max_orders,
                                                   &cur_oper->oper_num_pert,
                                                   cur_oper->oper_pert_labels,
                                                   cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()"
        /* checks if the perturbations on the one-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert<0) continue;</pre>
        /* calculates expectation values using the callback function */
        cur_oper->get_one_oper_exp(cur_oper->oper_num_pert,
                                    cur_oper->oper_pert_labels,
                                    cur_oper->oper_pert_orders,
                                    num_dmat,
                                    dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                    cur_oper->user_ctx,
#endif
                                    num_exp,
                                    val_exp);
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPOneOperDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-07-30'>
     Destroys the linked list of one-electron operators, should be called
```

```
at the end
    <param name='one_oper' direction='inout'>
       The linked list of one-electron operators
    </param>
    <return>Error information</return>
   </function> */
QErrorCode RSPOneOperDestroy(RSPOneOper **one_oper)
{
    RSPOneOper *cur_oper; /* current operator */
    RSPOneOper *next_oper; /* next operator */
    /* walks to the last operator */
    cur_oper = *one_oper;
   while (cur_oper!=NULL) {
        if (cur_oper->pert_max_orders!=NULL) {
            free(cur_oper->pert_max_orders);
            cur_oper->pert_max_orders = NULL;
        }
        if (cur_oper->oper_pert_orders!=NULL) {
            free(cur_oper->oper_pert_orders);
            cur_oper->oper_pert_orders = NULL;
        }
        if (cur_oper->pert_labels!=NULL) {
            free(cur_oper->pert_labels);
            cur_oper->pert_labels = NULL;
        }
        if (cur_oper->oper_pert_labels!=NULL) {
            free(cur_oper->oper_pert_labels);
            cur_oper->oper_pert_labels = NULL;
        }
#if defined(OPENRSP_C_USER_CONTEXT)
        cur_oper->user_ctx = NULL;
#endif
        cur_oper->get_one_oper_mat = NULL;
        cur_oper->get_one_oper_exp = NULL;
        next_oper = cur_oper->next_oper;
        free(cur_oper);
        cur_oper = NULL;
        cur_oper = next_oper;
    }
   return QSUCCESS;
}
```

3.6 Two-Electron Operators

Users can use the following API to add different two-electron operators:

```
\langle OpenRSP.c \ 17a \rangle + \equiv
 /* <function name='OpenRSPAddTwoOper' author='Bin Gao' date='2014-08-05'>
       Add a two-electron operator to the Hamiltonian
       <param name='open_rsp' direction='inout'>
        The context of response theory calculations
       </param>
       <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act on the
        two-electron operator
      </param>
      <param name='pert_labels' direction='in'>
        All the different perturbation labels involved
       </param>
       <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
      </param>
       <param name='user_ctx' direction='in'>
        User-defined callback function context
       </param>
       <param name='get_two_oper_mat' direction='in'>
        User-specified callback function to calculate integral matrices of
        two-electron operator as well as its derivatives with respect to
        different perturbations
       </param>
       <param name='get_two_oper_exp' direction='in'>
        User-specified callback function to calculate expectation values of
        two-electron operator as well as its derivatives with respect to
        different perturbations
      </param>
       <return>Error information</return>
     </function> */
 QErrorCode OpenRSPAddTwoOper(OpenRSP *open_rsp,
                               const QInt num_pert_lab,
                               const QcPertInt *pert_labels,
                               const QInt *pert_max_orders,
 #if defined(OPENRSP_C_USER_CONTEXT)
                               void *user_ctx,
 #endif
                               const GetTwoOperMat get_two_oper_mat,
                               const GetTwoOperExp get_two_oper_exp)
 {
     QErrorCode ierr; /* error information */
     /* creates the linked list of two-electron operators */
     if (open_rsp->two_oper==NULL) {
          ierr = RSPTwoOperCreate(&open_rsp->two_oper,
                                  num_pert_lab,
                                  pert_labels,
                                  pert_max_orders,
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
                                 user_ctx,
#endif
                                 get_two_oper_mat,
                                 get_two_oper_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperCreate()");
    }
    /* adds the two-electron operator to the linked list */
    else {
        ierr = RSPTwoOperAdd(open_rsp->two_oper,
                              num_pert_lab,
                              pert_labels,
                              pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                              user_ctx,
#endif
                              get_two_oper_mat,
                              get_two_oper_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperAdd()");
    }
    return QSUCCESS;
}
```

The following header file defines all quantities we need for two-electron operators. Types GetTwoOperMat and GetTwoOperpExp define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of a two-electron operator and its derivatives.

```
\langle RSPTwoOper.h \ 69 \rangle \equiv
    ⟨OpenRSPLicense 14a⟩
    <header name='RSPTwoOper.h' author='Bin Gao' date='2014-08-05'>
      The header file of two-electron operators used inside OpenRSP
    </header>
 */
 #if !defined(RSP_TWOOPER_H)
 #define RSP_TWOOPER_H
 #include "qcmatrix.h"
 #include "RSPPerturbation.h"
 typedef void (*GetTwoOperMat)(const QInt,
                                  const QcPertInt*,
                                  const QInt*,
                                  const QInt,
                                  QcMat*[],
 #if defined(OPENRSP_C_USER_CONTEXT)
                                  void*,
 #endif
                                  const QInt,
                                  QcMat*[]);
```

```
typedef void (*GetTwoOperExp)(const QInt,
                                         const QcPertInt*,
                                         const QInt*,
                                         const QInt,
                                         const QInt*,
                                         QcMat*[],
                                         const QInt*,
                                         QcMat*[],
        #if defined(OPENRSP_C_USER_CONTEXT)
                                         void*,
        #endif
                                         const QInt,
                                         QReal*);
        \langle RSPTwoOperStruct 70a \rangle
        \langle RSPTwoOperAPIs \ 70b \rangle
        #endif
      Here we use a linked list for the context of two-electron operators:
70a
      \langle RSPTwoOperStruct 70a \rangle \equiv
        typedef struct RSPTwoOper RSPTwoOper;
        struct RSPTwoOper {
                                                 /* number of different perturbation labels
            QInt num_pert_lab;
                                                    that can act as perturbations on the
                                                    two-electron operator */
            QInt oper_num_pert;
                                                /* number of perturbations on the
                                                    two-electron operator, only used for
                                                    callback functions */
                                                /* allowed maximal order of a perturbation
            QInt *pert_max_orders;
                                                    described by exactly one of these
                                                    different labels */
            QInt *oper_pert_orders;
                                                 /* orders of perturbations on the
                                                    two-electron operator, only used for
                                                    callback functions */
            QcPertInt *pert_labels;
                                                 /* all the different perturbation labels */
            QcPertInt *oper_pert_labels;
                                                 /* labels of perturbations on the
                                                    two-electron operator, only used for
                                                    callback functions */
        #if defined(OPENRSP_C_USER_CONTEXT)
                                                 /* user-defined callback-function context */
            void *user_ctx;
        #endif
            GetTwoOperMat get_two_oper_mat;
                                                /* user-specified function for calculating
                                                    integral matrices */
            GetTwoOperExp get_two_oper_exp;
                                                /* user-specified function for calculating
                                                    expectation values */
            RSPTwoOper *next_oper;
                                                /* pointer to the next two-electron operator */
        };
      and the functions related to the two-electron operators:
      \langle RSPTwoOperAPIs \ 70b \rangle \equiv
70b
        extern QErrorCode RSPTwoOperCreate(RSPTwoOper**,
                                              const QInt,
```

```
const QcPertInt*,
                                       const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                       void*,
 #endif
                                       const GetTwoOperMat,
                                       const GetTwoOperExp);
 extern QErrorCode RSPTwoOperAdd(RSPTwoOper*,
                                    const QInt,
                                    const QcPertInt*,
                                    const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                    void*,
 #endif
                                    const GetTwoOperMat,
                                    const GetTwoOperExp);
 extern QErrorCode RSPTwoOperAssemble(RSPTwoOper*,const RSPPert*);
 extern QErrorCode RSPTwoOperWrite(RSPTwoOper*,FILE*);
 extern QErrorCode RSPTwoOperGetMat(RSPTwoOper*,
                                       const QInt,
                                       const QcPertInt*,
                                       const QInt,
                                       QcMat*[],
                                       const QInt,
                                       QcMat*[]);
 extern QErrorCode RSPTwoOperGetExp(RSPTwoOper*,
                                       const QInt,
                                       const QcPertInt*,
                                       const QInt,
                                       const QInt*,
                                       QcMat*[],
                                       const QInt*,
                                       QcMat*[],
                                       const QInt,
                                       QReal*);
 extern QErrorCode RSPTwoOperDestroy(RSPTwoOper**);
  The functions are implemented as follows:
\langle RSPTwoOper.c \ 71 \rangle \equiv
    \langle OpenRSPLicense 14a \rangle
 #include "RSPTwoOper.h"
 /* <function name='RSPTwoOperCreate'</pre>
               attr='private'
               author='Bin Gao'
               date='2014-08-06'>
       Create a node of a linked list for a given two-electron operator, should
       be called at first
       <param name='two_oper' direction='inout'>
         The linked list of two-electron operators
```

```
</param>
     <param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels that can act as
       perturbations on the two-electron operator
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback-function context
     <param name='get_two_oper_mat' direction='in'>
       User-specified function for calculating integral matrices of the
       two-electron operator and its derivatives
     </param>
     <param name='get_two_oper_exp' direction='in'>
       User-specified function for calculating expectation values of the
       two-electron operator and its derivatives
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperCreate(RSPTwoOper **two_oper,
                            const QInt num_pert_lab,
                            const QcPertInt *pert_labels,
                            const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            void *user_ctx,
#endif
                            const GetTwoOperMat get_two_oper_mat,
                            const GetTwoOperExp get_two_oper_exp)
{
   RSPTwoOper *new_oper; /* new operator */
                           /* incremental recorders over perturbation labels */
    QInt ilab;
    QInt jlab;
   new_oper = (RSPTwoOper *)malloc(sizeof(RSPTwoOper));
    if (new_oper==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for two-electron operator");
    }
    if (num_pert_lab<0) {</pre>
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        \label{lem:labels printf("RSPTwoOperCreate">> number of perturbation labels "QINT_FMT" \n",
               num_pert_lab);
        printf("RSPTwoOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
```

QErrorExit(FILE_AND_LINE, "too many perturbation labels");

```
}
new_oper->num_pert_lab = num_pert_lab;
if (new_oper->num_pert_lab>0) {
    new_oper->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->pert_max_orders==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    new_oper->oper_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_oper->oper_pert_orders==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on 2el operator");
    new_oper->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->pert_labels==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    new_oper->oper_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_oper->oper_pert_labels==NULL) {
        printf("RSPTwoOperCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on 2el operator");
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   ilab,
                   pert_labels[ilab]);
            printf("RSPTwoOperCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\
                   OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {</pre>
            if (pert_labels[jlab] == pert_labels[ilab]) {
                printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                       jlab,
                       pert_labels[jlab]);
                printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                       ilab,
                       pert_labels[ilab]);
                QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
            }
        }
        new_oper->pert_labels[ilab] = pert_labels[ilab];
        if (pert_max_orders[ilab]<1) {</pre>
            printf("RSPTwoOperCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
```

```
ilab,
                       pert_labels[ilab]);
                printf("RSPTwoOperCreate>> allowed maximal order is %"QINT_FMT"\n",
                       pert_max_orders[ilab]);
                QErrorExit(FILE_AND_LINE, "only positive order allowed");
            }
            new_oper->pert_max_orders[ilab] = pert_max_orders[ilab];
        }
    }
    else {
        new_oper->pert_max_orders = NULL;
       new_oper->oper_pert_orders = NULL;
       new_oper->pert_labels = NULL;
       new_oper->oper_pert_labels = NULL;
    }
#if defined(OPENRSP_C_USER_CONTEXT)
   new_oper->user_ctx = user_ctx;
#endif
   new_oper->get_two_oper_mat = get_two_oper_mat;
   new_oper->get_two_oper_exp = get_two_oper_exp;
   new_oper->next_oper = NULL;
    *two_oper = new_oper;
   return QSUCCESS;
}
```

As shown here, we allow for a two-electron operator that does not depend on any peraturbation—num_pert_lab==0, i.e. any perturbed integral matrix and expectation value of this two-electron operator is zero.

```
\langle RSPTwoOper.c 71 \rangle + \equiv
74
       /* <function name='RSPTwoOperAdd'</pre>
                     attr='private'
                     author='Bin Gao'
                     date='2014-08-06'>
            Add a given two-electron operator to the linked list
            <param name='two_oper' direction='inout'>
              The linked list of two-electron operators
             </param>
             <param name='num_pert_lab' direction='in'>
              Number of all different perturbation labels that can act as
              perturbations on the two-electron operator
             <param name='pert_labels' direction='in'>
              All the different perturbation labels
            </param>
            <param name='pert_max_orders' direction='in'>
              Allowed maximal order of a perturbation described by exactly one of
              the above different labels
            </param>
             <param name='user_ctx' direction='in'>
              User-defined callback-function context
             </param>
             <param name='get_two_oper_mat' direction='in'>
```

```
User-specified function for calculating integral matrices of the
       two-electron operator and its derivatives
     </param>
     <param name='get_two_oper_exp' direction='in'>
       User-specified function for calculating expectation values of the
       two-electron operator and its derivatives
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperAdd(RSPTwoOper *two_oper,
                         const QInt num_pert_lab,
                         const QcPertInt *pert_labels,
                         const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                         void *user_ctx,
#endif
                         const GetTwoOperMat get_two_oper_mat,
                         const GetTwoOperExp get_two_oper_exp)
{
   RSPTwoOper *new_oper; /* new operator */
   RSPTwoOper *cur_oper; /* current operator */
    QErrorCode ierr;
                           /* error information */
    /* creates the new operator */
    ierr = RSPTwoOperCreate(&new_oper,
                            num_pert_lab,
                            pert_labels,
                            pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_two_oper_mat,
                            get_two_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPTwoOperCreate()");
    /* walks to the last operator */
    cur_oper = two_oper;
    while (cur_oper->next_oper!=NULL) {
        cur_oper = cur_oper->next_oper;
    }
    /* inserts the new operator to the tail of the linked list */
    cur_oper->next_oper = new_oper;
   return QSUCCESS;
}
/* <function name='RSPTwoOperAssemble'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
    Assembles the linked list of two-electron operators
     <param name='two_oper' direction='inout'>
       The linked list of two-electron operators
     </param>
     <param name='rsp_pert' direction='in'>
```

```
The context of perturbations
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperAssemble(RSPTwoOper *two_oper, const RSPPert *rsp_pert)
                          /* incremental recorder over operators */
   QInt ioper;
   RSPTwoOper *cur_oper; /* current operator */
   QErrorCode ierr; /* error information */
   ioper = 0;
   cur_oper = two_oper;
   do {
        if (cur_oper->num_pert_lab>0 &&
            (cur_oper->pert_labels==NULL || cur_oper->pert_max_orders==NULL)) {
           printf("RSPTwoOperAssemble>> %"QINT_FMT"-th two-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "perturbations of two-electron operator not set");
        }
        if (cur_oper->get_two_oper_mat==NULL || cur_oper->get_two_oper_exp==NULL) {
           printf("RSPTwoOperAssemble>> %"QINT_FMT"-th two-electron operator\n",
                   ioper);
            QErrorExit(FILE_AND_LINE, "callback functions of two-electron operator not set"
        }
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                         cur_oper->num_pert_lab,
                                         cur_oper->pert_labels,
                                         cur_oper->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
   } while (cur_oper!=NULL);
   return QSUCCESS;
}
/* <function name='RSPTwoOperWrite'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
    Writes the linked list of two-electron operators
    <param name='two_oper' direction='in'>
       The linked list of two-electron operators
     <param name='fp_oper' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperWrite(RSPTwoOper *two_oper, FILE *fp_oper)
{
   QInt ioper;
                          /* incremental recorder over operators */
   RSPTwoOper *cur_oper; /* current operator */
```

```
QInt ilab;
                           /* incremental recorder over perturbation labels */
    ioper = 0;
    cur_oper = two_oper;
    do {
        fprintf(fp_oper, "RSPTwoOperWrite>> operator %"QINT_FMT"\n", ioper);
        fprintf(fp_oper,
                "RSPTwoOperWrite>> number of pert. labels that two-electron operator depend
                cur_oper->num_pert_lab);
        fprintf(fp_oper, "RSPTwoOperWrite>> label
                                                            maximum-order\n");
        for (ilab=0; ilab<cur_oper->num_pert_lab; ilab++) {
            fprintf(fp_oper,
                                              %"QCPERTINT_FMT"
                                                                                %"QINT_FMT"\
                    "RSPTwoOperWrite>>
                    cur_oper->pert_labels[ilab],
                    cur_oper->pert_max_orders[ilab]);
        }
#if defined(OPENRSP_C_USER_CONTEXT)
        if (cur_oper->user_ctx!=NULL) {
            fprintf(fp_oper, "RSPTwoOperWrite>> user-defined function context given\n");
        }
#endif
        /* moves to the next operator */
        ioper++;
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPTwoOperGetMat'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates integral matrices of the linked list of two-electron operators
     <param name='two_oper' direction='inout'>
       The linked list of two-electron operators
     </param>
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of two-electron
       operators
     </param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of two-electron operators
     </param>
     <param name='num_int' direction='in'>
       Number of the integral matrices
     <param name='val_int' direction='inout'>
      The integral matrices
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperGetMat(RSPTwoOper *two_oper,
                            const QInt oper_len_tuple,
```

```
const QcPertInt *oper_pert_tuple,
                            const QInt num_dmat,
                            QcMat *dens_mat[],
                            const QInt num_int,
                            QcMat *val_int[])
{
   RSPTwoOper *cur_oper; /* current operator */
                          /* error information */
    QErrorCode ierr;
    cur_oper = two_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the two-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                   oper_pert_tuple,
                                                   cur_oper->num_pert_lab,
                                                   cur_oper->pert_labels,
                                                   cur_oper->pert_max_orders,
                                                   &cur_oper->oper_num_pert,
                                                   cur_oper->oper_pert_labels,
                                                   cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()"
        /* checks if the perturbations on the two-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert<0) continue;</pre>
        /* calculates integral matrices using the callback function */
        cur_oper->get_two_oper_mat(cur_oper->oper_num_pert,
                                   cur_oper->oper_pert_labels,
                                   cur_oper->oper_pert_orders,
                                   num_dmat,
                                   dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                   cur_oper->user_ctx,
#endif
                                   num_int,
                                   val_int);
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
   return QSUCCESS;
}
/* <function name='RSPTwoOperGetExp'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates expectation values of the linked list of two-electron operators
     <param name='two_oper' direction='inout'>
       The linked list of two-electron operators
     </param>
     <param name='oper_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of two-electron
       operators
```

```
</param>
     <param name='oper_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of two-electron operators
     </param>
     <param name='dmat_len_tuple' direction='in'>
       Length of different perturbation tuples of the left-hand-side (LHS) and
       right-hand-side (RHS) atomic orbital (AO) based density matrices passed
     </param>
     <param name='num_LHS_dmat' direction='in'>
       Number of LHS AO based density matrices passed for each LHS density
       matrix perturbation tuple
     </param>
     <param name='LHS_dens_mat' direction='in'>
       The LHS AO based density matrices
     <param name='num_RHS_dmat' direction='in'>
       Number of RHS AO based density matrices passed for each RHS density
      matrix perturbation tuple
     </param>
     <param name='RHS_dens_mat' direction='in'>
       The RHS AO based density matrices
     <param name='num_exp' direction='in'>
       Number of the expectation values
     </param>
     <param name='val_exp' direction='inout'>
       The expectation values
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperGetExp(RSPTwoOper *two_oper,
                            const QInt oper_len_tuple,
                            const QcPertInt *oper_pert_tuple,
                            const QInt dmat_len_tuple,
                            const QInt *num_LHS_dmat,
                            QcMat *LHS_dens_mat[],
                            const QInt *num_RHS_dmat,
                            QcMat *RHS_dens_mat[],
                            const QInt num_exp,
                            QReal *val_exp)
{
   RSPTwoOper *cur_oper; /* current operator */
    QErrorCode ierr;
                           /* error information */
    cur_oper = two_oper;
    do {
        /* gets perturbation labels and corresponding orders out of the internal
           perturbation tuple on the two-electron operator */
        ierr = RSPPertInternTupleToHostLabelOrder(oper_len_tuple,
                                                  oper_pert_tuple,
                                                  cur_oper->num_pert_lab,
                                                  cur_oper->pert_labels,
                                                   cur_oper->pert_max_orders,
```

```
&cur_oper->oper_num_pert,
                                                   cur_oper->oper_pert_labels,
                                                   cur_oper->oper_pert_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()"
        /* checks if the perturbations on the two-electron operator
           result in zero values */
        if (cur_oper->oper_num_pert<0) continue;</pre>
        /* calculates expectation values using the callback function */
        cur_oper->get_two_oper_exp(cur_oper->oper_num_pert,
                                    cur_oper->oper_pert_labels,
                                    cur_oper->oper_pert_orders,
                                    dmat_len_tuple,
                                   num_LHS_dmat,
                                    LHS_dens_mat,
                                   num_RHS_dmat,
                                   RHS_dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                    cur_oper->user_ctx,
#endif
                                   num_exp,
                                   val_exp);
        /* moves to the next operator */
        cur_oper = cur_oper->next_oper;
    } while (cur_oper!=NULL);
    return QSUCCESS;
}
/* <function name='RSPTwoOperDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
     Destroys the linked list of two-electron operators, should be called
     at the end
     <param name='two_oper' direction='inout'>
       The linked list of two-electron operators
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPTwoOperDestroy(RSPTwoOper **two_oper)
    RSPTwoOper *cur_oper; /* current operator */
    RSPTwoOper *next_oper; /* next operator */
    /* walks to the last operator */
    cur_oper = *two_oper;
    while (cur_oper!=NULL) {
        if (cur_oper->pert_max_orders!=NULL) {
            free(cur_oper->pert_max_orders);
            cur_oper->pert_max_orders = NULL;
        }
        if (cur_oper->oper_pert_orders!=NULL) {
            free(cur_oper->oper_pert_orders);
            cur_oper->oper_pert_orders = NULL;
```

```
}
        if (cur_oper->pert_labels!=NULL) {
            free(cur_oper->pert_labels);
            cur_oper->pert_labels = NULL;
        }
        if (cur_oper->oper_pert_labels!=NULL) {
            free(cur_oper->oper_pert_labels);
            cur_oper->oper_pert_labels = NULL;
#if defined(OPENRSP_C_USER_CONTEXT)
        cur_oper->user_ctx = NULL;
#endif
        cur_oper->get_two_oper_mat = NULL;
        cur_oper->get_two_oper_exp = NULL;
        next_oper = cur_oper->next_oper;
        free(cur_oper);
        cur_oper = NULL;
        cur_oper = next_oper;
    }
    return QSUCCESS;
}
```

3.7 XC Functionals

```
Users can use the following API to add different XC functionals:
```

```
\langle OpenRSP.c \ 17a \rangle + \equiv
 /* <function name='OpenRSPAddXCFun' author='Bin Gao' date='2015-06-23'>
      Add an XC functional to the Hamiltonian
       <param name='open_rsp' direction='inout'>
        The context of response theory calculations
       </param>
       <param name='num_pert_lab' direction='in'>
        Number of all different perturbation labels that can act on the
        XC functional
      </param>
      <param name='pert_labels' direction='in'>
        All the different perturbation labels involved
       </param>
       <param name='pert_max_orders' direction='in'>
        Allowed maximal order of a perturbation described by exactly one of
        the above different labels
      </param>
       <param name='user_ctx' direction='in'>
        User-defined callback function context
       </param>
       <param name='get_xc_fun_mat' direction='in'>
        User-specified callback function to calculate integral matrices of
        XC functional as well as its derivatives with respect to
        different perturbations
      </param>
       <param name='get_xc_fun_exp' direction='in'>
        User-specified callback function to calculate expectation values of
        XC functional as well as its derivatives with respect to
        different perturbations
      </param>
       <return>Error information</return>
     </function> */
 QErrorCode OpenRSPAddXCFun(OpenRSP *open_rsp,
                             const QInt num_pert_lab,
                             const QcPertInt *pert_labels,
                             const QInt *pert_max_orders,
 #if defined(OPENRSP_C_USER_CONTEXT)
                             void *user_ctx,
 #endif
                             const GetXCFunMat get_xc_fun_mat,
                             const GetXCFunExp get_xc_fun_exp)
 {
     QErrorCode ierr; /* error information */
     /* creates the linked list of XC functionals */
     if (open_rsp->xc_fun==NULL) {
          ierr = RSPXCFunCreate(&open_rsp->xc_fun,
                                num_pert_lab,
                                pert_labels,
                                pert_max_orders,
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
                               user_ctx,
#endif
                               get_xc_fun_mat,
                               get_xc_fun_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunCreate()");
    }
    /* adds the XC functional to the linked list */
    else {
        ierr = RSPXCFunAdd(open_rsp->xc_fun,
                            num_pert_lab,
                            pert_labels,
                           pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                            user_ctx,
#endif
                            get_xc_fun_mat,
                            get_xc_fun_exp);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunAdd()");
    }
    return QSUCCESS;
}
```

The following header file defines all quantities we need for XC functionals. Types GetXCFunMat and GetXCFunpExp define the requirements of two callback functions from the host program to calculate respectively the integral matrices and expectation values of an XC functional and its derivatives.

```
\langle RSPXCFun.h \ 83 \rangle \equiv
    ⟨OpenRSPLicense 14a⟩
    <header name='RSPXCFun.h' author='Bin Gao' date='2014-08-06'>
      The header file of XC functionals used inside OpenRSP
    </header>
 #if !defined(RSP_XCFUN_H)
 #define RSP_XCFUN_H
 #include "qcmatrix.h"
 #include "RSPPerturbation.h"
 typedef void (*GetXCFunMat)(const QInt,
                                const QcPertInt*,
                                const QInt,
                                const QInt,
                                const QInt*,
                                const QInt,
                                QcMat*[],
 #if defined(OPENRSP_C_USER_CONTEXT)
                                void*,
 #endif
                                const QInt,
```

```
QcMat*[]);
        typedef void (*GetXCFunExp)(const QInt,
                                       const QcPertInt*,
                                       const QInt,
                                       const QInt,
                                       const QInt*,
                                       const QInt,
                                       QcMat*[],
        #if defined(OPENRSP_C_USER_CONTEXT)
                                       void*,
        #endif
                                       const QInt,
                                       QReal*);
        \langle RSPXCFunStruct 84a \rangle
        \langle RSPXCFunAPIs 84b \rangle
        #endif
       Here we use a linked list for the context of XC functionals:
84a
       \langle RSPXCFunStruct 84a \rangle \equiv
        typedef struct RSPXCFun RSPXCFun;
        struct RSPXCFun {
                                            /* number of different perturbation labels
             QInt num_pert_lab;
                                                that can act as perturbations on the
                                                XC functional */
             QInt xc_len_tuple;
                                            /* length of perturbation tuple on the
                                                XC functional, only used for
                                                callback functions */
                                            /* allowed maximal order of a perturbation
             QInt *pert_max_orders;
                                                described by exactly one of these
                                                different labels */
             QcPertInt *pert_labels;
                                            /* all the different perturbation labels */
                                            /* perturbation tuple on the XC functional,
             QcPertInt *xc_pert_tuple;
                                                only used for callback functions */
        #if defined(OPENRSP_C_USER_CONTEXT)
                                            /* user-defined callbac-kfunction context */
             void *user_ctx;
        #endif
                                            /* user-specified function for calculating
             GetXCFunMat get_xc_fun_mat;
                                                integral matrices */
             GetXCFunExp get_xc_fun_exp;
                                            /* user-specified function for calculating
                                                expectation values */
             RSPXCFun *next_xc;
                                            /* pointer to the next XC functional */
        };
       and the functions related to the XC functionals:
84b
       \langle RSPXCFunAPIs 84b \rangle \equiv
        extern QErrorCode RSPXCFunCreate(RSPXCFun**,
                                            const QInt,
                                            const QcPertInt*,
                                            const QInt*,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                            void*,
```

```
#endif
                                     const GetXCFunMat,
                                     const GetXCFunExp);
 extern QErrorCode RSPXCFunAdd(RSPXCFun*,
                                  const QInt,
                                  const QcPertInt*,
                                  const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                  void*,
 #endif
                                  const GetXCFunMat,
                                  const GetXCFunExp);
 extern QErrorCode RSPXCFunAssemble(RSPXCFun*,const RSPPert*);
 extern QErrorCode RSPXCFunWrite(RSPXCFun*,FILE*);
 extern QErrorCode RSPXCFunGetMat(RSPXCFun*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt,
                                     const QInt,
                                     const QInt*,
                                     const QInt,
                                     QcMat*[],
                                     const QInt,
                                     QcMat*[]);
 extern QErrorCode RSPXCFunGetExp(RSPXCFun*,
                                     const QInt,
                                     const QcPertInt*,
                                     const QInt,
                                     const QInt,
                                     const QInt*,
                                     const QInt,
                                     QcMat*[],
                                     const QInt,
                                     QReal*);
 extern QErrorCode RSPXCFunDestroy(RSPXCFun**);
  The functions are implemented as follows:
\langle RSPXCFun.c \ 85 \rangle \equiv
    \langle OpenRSPLicense 14a \rangle
 #include "RSPXCFun.h"
 /* <function name='RSPXCFunCreate'</pre>
               attr='private'
               author='Bin Gao'
               date='2015-06-23'>
       Create a node of a linked list for a given XC functional, should
       be called at first
       <param name='xc_fun' direction='inout'>
         The linked list of XC functionals
       </param>
```

```
<param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels that can act as
      perturbations on the XC functional
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback-function context
     </param>
     <param name='get_xc_fun_mat' direction='in'>
       User-specified function for calculating integral matrices of the
       XC functional and its derivatives
     </param>
     <param name='get_xc_fun_exp' direction='in'>
       User-specified function for calculating expectation values of the
       XC functional and its derivatives
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunCreate(RSPXCFun **xc_fun,
                          const QInt num_pert_lab,
                          const QcPertInt *pert_labels,
                          const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                          void *user_ctx,
#endif
                          const GetXCFunMat get_xc_fun_mat,
                          const GetXCFunExp get_xc_fun_exp)
{
   RSPXCFun *new_xc; /* new XC functional */
    QInt ilab;
                       /* incremental recorders over perturbation labels */
    QInt jlab;
   new_xc = (RSPXCFun *)malloc(sizeof(RSPXCFun));
    if (new_xc==NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for XC functional");
    }
    if (num_pert_lab<0) {</pre>
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
    }
    else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        printf("RSPXCFunCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
               OPENRSP_PERT_LABEL_MAX);
        QErrorExit(FILE_AND_LINE, "too many perturbation labels");
```

```
}
new_xc->num_pert_lab = num_pert_lab;
if (new_xc->num_pert_lab>0) {
    new_xc->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (new_xc->pert_max_orders==NULL) {
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    }
    new_xc->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (new_xc->pert_labels==NULL) {
        printf("RSPXCFunCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    new_xc->xc_len_tuple = 0;
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   pert_labels[ilab]);
            printf("RSPXCFunCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n"
                   OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {</pre>
            if (pert_labels[jlab] == pert_labels[ilab]) {
                printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n"
                       pert_labels[jlab]);
                printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n"
                       pert_labels[ilab]);
                QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");
            }
        }
        new_xc->pert_labels[ilab] = pert_labels[ilab];
        if (pert_max_orders[ilab]<1) {</pre>
            printf("RSPXCFunCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\n",
                   pert_labels[ilab]);
            printf("RSPXCFunCreate>> allowed maximal order is %"QINT_FMT"\n",
                   pert_max_orders[ilab]);
            QErrorExit(FILE_AND_LINE, "only positive order allowed");
        }
        new_xc->pert_max_orders[ilab] = pert_max_orders[ilab];
        new_xc->xc_len_tuple += pert_max_orders[ilab];
    }
    new_xc->xc_pert_tuple = (QcPertInt *)malloc(new_xc->xc_len_tuple*sizeof(QcPertInt))
    if (new_xc->xc_pert_tuple==NULL) {
        printf("RSPXCFunCreate>> length of perturbation tuple %"QINT_FMT"\n",
```

```
new_xc->xc_len_tuple);
              QErrorExit(FILE_AND_LINE, "allocates memory for pert. tuple on XC functional");
          }
      }
      else {
          new_xc->pert_max_orders = NULL;
          new_xc->pert_labels = NULL;
          new_xc->xc_pert_tuple = NULL;
      }
 #if defined(OPENRSP_C_USER_CONTEXT)
      new_xc->user_ctx = user_ctx;
 #endif
     new_xc->get_xc_fun_mat = get_xc_fun_mat;
     new_xc->get_xc_fun_exp = get_xc_fun_exp;
     new_xc->next_xc = NULL;
      *xc_fun = new_xc;
     return QSUCCESS;
 }
As shown here, we allow for an XC functional that does not depend on any peraturbation—
num_pert_lab==0, i.e. any perturbed integral matrix and expectation value of this XC functional
is zero.
\langle RSPXCFun.c \ 85 \rangle + \equiv
 /* <function name='RSPXCFunAdd'
               attr='private'
               author='Bin Gao'
               date='2015-06-23'>
       Add a given XC functional to the linked list
       <param name='xc_fun' direction='inout'>
         The linked list of XC functionals
       </param>
       <param name='num_pert_lab' direction='in'>
         Number of all different perturbation labels that can act as
         perturbations on the XC functional
       </param>
       <param name='pert_labels' direction='in'>
         All the different perturbation labels
       </param>
       <param name='pert_max_orders' direction='in'>
         Allowed maximal order of a perturbation described by exactly one of
         the above different labels
       </param>
       <param name='user_ctx' direction='in'>
         User-defined callback-function context
       </param>
```

<param name='get_xc_fun_mat' direction='in'>

<param name='get_xc_fun_exp' direction='in'>

XC functional and its derivatives

XC functional and its derivatives

</param>

User-specified function for calculating integral matrices of the

User-specified function for calculating expectation values of the

```
</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunAdd(RSPXCFun *xc_fun,
                       const QInt num_pert_lab,
                       const QcPertInt *pert_labels,
                       const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                       void *user_ctx,
#endif
                       const GetXCFunMat get_xc_fun_mat,
                       const GetXCFunExp get_xc_fun_exp)
{
   RSPXCFun *new_xc; /* new XC functional */
   RSPXCFun *cur_xc; /* current XC functional */
                       /* error information */
    QErrorCode ierr;
    /* creates the new XC functional */
    ierr = RSPXCFunCreate(&new_xc,
                          num_pert_lab,
                          pert_labels,
                          pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                          user_ctx,
#endif
                          get_xc_fun_mat,
                          get_xc_fun_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPXCFunCreate()");
    /* walks to the last XC functional */
    cur_xc = xc_fun;
    while (cur_xc->next_xc!=NULL) {
        cur_xc = cur_xc->next_xc;
    /* inserts the new XC functional to the tail of the linked list */
    cur_xc->next_xc = new_xc;
    return QSUCCESS;
}
/* <function name='RSPXCFunAssemble'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-06-23'>
    Assembles the linked list of XC functionals
     <param name='xc_fun' direction='inout'>
       The linked list of XC functionals
     </param>
     <param name='rsp_pert' direction='in'>
       The context of perturbations
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunAssemble(RSPXCFun *xc_fun, const RSPPert *rsp_pert)
{
```

```
QInt ixc;
                       /* incremental recorder over XC functionals */
   RSPXCFun *cur_xc; /* current XC functional */
    QErrorCode ierr; /* error information */
    ixc = 0;
    cur_xc = xc_fun;
    do {
        if (cur_xc->num_pert_lab>0 &&
            (cur_xc->pert_labels==NULL || cur_xc->pert_max_orders==NULL)) {
            printf("RSPXCFunAssemble>> %"QINT_FMT"-th XC functional\n",
            QErrorExit(FILE_AND_LINE, "perturbations of XC functional not set");
        }
        if (cur_xc->get_xc_fun_mat==NULL || cur_xc->get_xc_fun_exp==NULL) {
            printf("RSPXCFunAssemble>> %"QINT_FMT"-th XC functional\n",
            QErrorExit(FILE_AND_LINE, "callback functions of XC functional not set");
        /* checks perturbation labels and allowed maximal orders against
           all known perturbations */
        ierr = RSPPertValidateLabelOrder(rsp_pert,
                                         cur_xc->num_pert_lab,
                                         cur_xc->pert_labels,
                                         cur_xc->pert_max_orders);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
        /* moves to the next XC functional */
        ixc++;
        cur_xc = cur_xc->next_xc;
    } while (cur_xc!=NULL);
   return QSUCCESS;
}
/* <function name='RSPXCFunWrite'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-06-23'>
    Writes the linked list of XC functionals
     <param name='xc_fun' direction='in'>
       The linked list of XC functionals
     </param>
     <param name='fp_xc' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunWrite(RSPXCFun *xc_fun, FILE *fp_xc)
{
                       /* incremental recorder over XC functionals */
   RSPXCFun *cur_xc; /* current XC functional */
                      /* incremental recorder over perturbation labels */
    QInt ilab;
    ixc = 0;
    cur_xc = xc_fun;
        fprintf(fp_xc, "RSPXCFunWrite>> XC functional %"QINT_FMT"\n", ixc);
        fprintf(fp_xc,
```

```
"RSPXCFunWrite>> number of pert. labels that XC functional depends on %"QIN
                cur_xc->num_pert_lab);
        fprintf(fp_xc, "RSPXCFunWrite>> label
                                                         maximum-order\n");
        for (ilab=0; ilab<cur_xc->num_pert_lab; ilab++) {
            fprintf(fp_xc,
                    "RSPXCFunWrite>>
                                           %"QCPERTINT_FMT"
                                                                              %"QINT_FMT"\n"
                    cur_xc->pert_labels[ilab],
                    cur_xc->pert_max_orders[ilab]);
        }
#if defined(OPENRSP_C_USER_CONTEXT)
        if (cur_xc->user_ctx!=NULL) {
            fprintf(fp_xc, "RSPXCFunWrite>> user-defined function context given\n");
        }
#endif
        /* moves to the next XC functional */
        ixc++;
        cur_xc = cur_xc->next_xc;
    } while (cur_xc!=NULL);
   return QSUCCESS;
}
/* <function name='RSPXCFunGetMat'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates integral matrices of the linked list of XC functionals
     <param name='xc_fun' direction='inout'>
       The linked list of XC functionals
     </param>
     <param name='xc_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of XC functionals
     </param>
     <param name='xc_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of XC functionals
     <param name='num_freq_configs' direction='in'>
       The number of different frequency configurations to be considered for
       the perturbation tuple
     </param>
     <param name='dmat_num_tuple' direction='in'>
       The number of different perturbation tuples of the atomic orbital (AO)
       based density matrices passed
     </param>
     <param name='dmat_idx_tuple' direction='in'>
       Indices of the density matrix perturbation tuples passed (canonically
       ordered)
     </param>
     <param name='num_dmat' direction='in'>
       Number of collected AO based density matrices for the passed density
       matrix perturbation tuples and all frequency configurations
     </param>
     <param name='dens_mat' direction='in'>
```

```
The collected AO based density matrices
     </param>
     <param name='num_int' direction='in'>
       Number of the integral matrices
     </param>
     <param name='val_int' direction='inout'>
       The integral matrices
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunGetMat(RSPXCFun *xc_fun,
                          const QInt xc_len_tuple,
                          const QcPertInt *xc_pert_tuple,
                          const QInt num_freq_configs,
                          const QInt dmat_num_tuple,
                          const QInt *dmat_idx_tuple,
                          const QInt num_dmat,
                          QcMat *dens_mat[],
                          const QInt num_int,
                          QcMat *val_int[])
{
   RSPXCFun *cur_xc; /* current XC functional */
                       /* error information */
    QErrorCode ierr;
    cur_xc = xc_fun;
    do {
        /* gets the host program's perturbation tuple on the XC functional */
        ierr = RSPPertInternTupleToHostTuple(xc_len_tuple,
                                              xc_pert_tuple,
                                              cur_xc->num_pert_lab,
                                              cur_xc->pert_labels,
                                              cur_xc->pert_max_orders,
                                              &cur_xc->xc_len_tuple,
                                              cur_xc->xc_pert_tuple);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostTuple()");
        /* checks if the perturbations on the XC functional result in
           zero values */
        if (cur_xc->xc_len_tuple<0) continue;</pre>
        /* calculates integral matrices using the callback function */
        cur_xc->get_xc_fun_mat(cur_xc->xc_len_tuple,
                               cur_xc->xc_pert_tuple,
                               num_freq_configs,
                               dmat_num_tuple,
                               dmat_idx_tuple,
                               num_dmat,
                               dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                cur_xc->user_ctx,
#endif
                               num_int,
                               val_int);
        /* moves to the next XC functional */
        cur_xc = cur_xc->next_xc;
```

```
} while (cur_xc!=NULL);
   return QSUCCESS;
}
/* <function name='RSPXCFunGetExp'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates expectation values of the linked list of XC functionals
     <param name='xc_fun' direction='inout'>
       The linked list of XC functionals
     </param>
     <param name='xc_len_tuple' direction='in'>
       Length of the perturbation tuple on the linked list of XC functionals
     <param name='xc_pert_tuple' direction='in'>
       Perturbation tuple on the linked list of XC functionals
     </param>
     <param name='num_freq_configs' direction='in'>
       The number of different frequency configurations to be considered for
       the perturbation tuple
     </param>
     <param name='dmat_num_tuple' direction='in'>
       The number of different perturbation tuples of the atomic orbital (AO)
       based density matrices passed
     </param>
     <param name='dmat_idx_tuple' direction='in'>
       Indices of the density matrix perturbation tuples passed (canonically
       ordered)
     </param>
     <param name='num_dmat' direction='in'>
       Number of collected AO based density matrices for the passed density
       matrix perturbation tuples and all frequency configurations
     </param>
     <param name='dens_mat' direction='in'>
       The collected AO based density matrices
     </param>
     <param name='num_exp' direction='in'>
       Number of the expectation values
     <param name='val_exp' direction='inout'>
       The expectation values
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunGetExp(RSPXCFun *xc_fun,
                          const QInt xc_len_tuple,
                          const QcPertInt *xc_pert_tuple,
                          const QInt num_freq_configs,
                          const QInt dmat_num_tuple,
                          const QInt *dmat_idx_tuple,
                          const QInt num_dmat,
```

```
QcMat *dens_mat[],
                          const QInt num_exp,
                          QReal *val_exp)
{
   RSPXCFun *cur_xc; /* current XC functional */
    QErrorCode ierr;
                      /* error information */
    cur_xc = xc_fun;
    do {
        /* gets the host program's perturbation tuple on the XC functional */
        ierr = RSPPertInternTupleToHostTuple(xc_len_tuple,
                                              xc_pert_tuple,
                                              cur_xc->num_pert_lab,
                                              cur_xc->pert_labels,
                                              cur_xc->pert_max_orders,
                                              &cur_xc->xc_len_tuple,
                                              cur_xc->xc_pert_tuple);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostTuple()");
        /* checks if the perturbations on the XC functional result in
           zero values */
        if (cur_xc->xc_len_tuple<0) continue;</pre>
        /* calculates expectation values using the callback function */
        cur_xc->get_xc_fun_exp(cur_xc->xc_len_tuple,
                               cur_xc->xc_pert_tuple,
                               num_freq_configs,
                               dmat_num_tuple,
                               dmat_idx_tuple,
                               num_dmat,
                               dens_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                cur_xc->user_ctx,
#endif
                               num_exp,
                               val_exp);
        /* moves to the next XC functional */
        cur_xc = cur_xc->next_xc;
    } while (cur_xc!=NULL);
   return QSUCCESS;
}
/* <function name='RSPXCFunDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-06-23'>
     Destroys the linked list of XC functionals, should be called at the end
     <param name='xc_fun' direction='inout'>
       The linked list of XC functionals
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPXCFunDestroy(RSPXCFun **xc_fun)
    RSPXCFun *cur_xc; /* current XC functional */
```

```
RSPXCFun *next_xc; /* next XC functional */
    /* walks to the last XC functional */
    cur_xc = *xc_fun;
    while (cur_xc!=NULL) {
        if (cur_xc->pert_max_orders!=NULL) {
            free(cur_xc->pert_max_orders);
            cur_xc->pert_max_orders = NULL;
        }
        if (cur_xc->pert_labels!=NULL) {
            free(cur_xc->pert_labels);
            cur_xc->pert_labels = NULL;
        }
        if (cur_xc->xc_pert_tuple!=NULL) {
            free(cur_xc->xc_pert_tuple);
            cur_xc->xc_pert_tuple = NULL;
#if defined(OPENRSP_C_USER_CONTEXT)
        cur_xc->user_ctx = NULL;
#endif
        cur_xc->get_xc_fun_mat = NULL;
        cur_xc->get_xc_fun_exp = NULL;
        next_xc = cur_xc->next_xc;
        free(cur_xc);
        cur_xc = NULL;
        cur_xc = next_xc;
    }
    return QSUCCESS;
}
```

3.8 Nuclear Hamiltonian

Users can use the following API to set nuclear Hamiltonian (nuclear repulsion and nuclei-field interaction):

```
96
     \langle OpenRSP.c \ 17a \rangle + \equiv
       /* <function name='OpenRSPSetNucHamilton' author='Bin Gao' date='2015-02-12'>
            Set the context of nuclear Hamiltonian
            <param name='open_rsp' direction='inout'>
              The context of response theory calculations
            </param>
            <param name='num_pert_lab' direction='in'>
              Number of all different perturbation labels that can act on the
              nuclear Hamiltonian
            </param>
            <param name='pert_labels' direction='in'>
              All the different perturbation labels involved
            <param name='pert_max_orders' direction='in'>
              Allowed maximal order of a perturbation described by exactly one of
              the above different labels
            </param>
            <param name='user_ctx' direction='in'>
              User-defined callback function context
            </param>
            <param name='get_nuc_contrib' direction='in'>
              User-specified callback function to calculate nuclear contributions
            <param name='num_atoms' direction='in'>
              Number of atoms
            </param>
            <return>Error information</return>
          </function> */
       QErrorCode OpenRSPSetNucHamilton(OpenRSP *open_rsp,
                                         const QInt num_pert_lab,
                                         const QcPertInt *pert_labels,
                                         const QInt *pert_max_orders,
       #if defined(OPENRSP_C_USER_CONTEXT)
                                         void *user_ctx,
       #endif
                                         const GetNucContrib get_nuc_contrib,
       /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
                                         const QInt num_atoms)
       {
           QErrorCode ierr; /* error information */
           /* creates the context of nuclear Hamiltonian */
           if (open_rsp->nuc_hamilton!=NULL) {
               ierr = RSPNucHamiltonDestroy(open_rsp->nuc_hamilton);
               QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPNucHamiltonDestroy()");
           else {
               open_rsp->nuc_hamilton = (RSPNucHamilton *)malloc(sizeof(RSPNucHamilton));
```

```
if (open_rsp->nuc_hamilton==NULL) {
            QErrorExit(FILE_AND_LINE, "allocates memory for nuclear Hamiltonian");
        }
    }
    ierr = RSPNucHamiltonCreate(open_rsp->nuc_hamilton,
                                num_pert_lab,
                                pert_labels,
                                pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                                user_ctx,
#endif
                                get_nuc_contrib,
/*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
                                num_atoms);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPNucHamiltonCreate()");
    return QSUCCESS;
}
```

The header file of the nuclear Hamiltonian is:

97

The following header file defines all quantities we need for the nuclear Hamiltonian. Type GetNucContrib defines the requirements of the host-program's callback function to calculate the contribution of nuclear Hamiltonian and its derivatives.

```
\langle RSPNucHamilton.h \ 97 \rangle \equiv
 /*
    ⟨OpenRSPLicense 14a⟩
    <header name='RSPNucHamilton.h' author='Bin Gao' date='2014-12-11'>
      The header file of nuclear Hamiltonian used inside OpenRSP
    </header>
 */
 #if !defined(RSP_NUCHAMILTON_H)
 #define RSP_NUCHAMILTON_H
 #include "qcmatrix.h"
 #include "RSPPerturbation.h"
 typedef void (*GetNucContrib)(const QInt,
                                    const QcPertInt*,
                                    const QInt*,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                    void*,
 #endif
                                    const QInt,
                                    QReal*);
 \langle RSNucHamiltonStruct 98a \rangle
 \langle RSPNucHamiltonAPIs 98b \rangle
 #endif
```

The context of nuclear Hamiltonian is:

 $\langle OpenRSPLicense 14a \rangle$

```
98a
      \langle RSNucHamiltonStruct\ 98a \rangle \equiv
        typedef struct {
            QInt num_pert_lab;
                                              /* number of different perturbation labels
                                                  that can act as perturbations on the
                                                 nuclear Hamiltonian */
                                              /* number of perturbations on the
            QInt nuc_num_pert;
                                                  nuclear Hamiltonian, only used for
                                                  callback functions */
            QInt *pert_max_orders;
                                              /* allowed maximal order of a perturbation
                                                  described by exactly one of these
                                                  different labels */
            QInt *nuc_pert_orders;
                                              /* orders of perturbations on the
                                                 nuclear Hamiltonian, only used for
                                                  callback functions */
            QcPertInt *pert_labels;
                                              /* all the different perturbation labels */
            QcPertInt *nuc_pert_labels;
                                              /* labels of perturbations on the
                                                  nuclear Hamiltonian, only used for
                                                  callback functions */
        #if defined(OPENRSP_C_USER_CONTEXT)
                                              /* user-defined callback-function context */
            void *user_ctx;
        #endif
            GetNucContrib get_nuc_contrib; /* user-specified function for calculating
                                                  contribution from the nuclear Hamiltonian */
        /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
            QInt num_atoms;
        } RSPNucHamilton;
      and the functions related to the nuclear Hamiltonian:
      \langle RSPNucHamiltonAPIs \ 98b \rangle \equiv
98b
        extern QErrorCode RSPNucHamiltonCreate(RSPNucHamilton*,
                                                  const QInt,
                                                  const QcPertInt*,
                                                  const QInt*,
        #if defined(OPENRSP_C_USER_CONTEXT)
                                                  void*,
        #endif
                                                  const GetNucContrib,
        /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
                                                  const QInt);
        extern QErrorCode RSPNucHamiltonAssemble(RSPNucHamilton*,const RSPPert*);
        extern QErrorCode RSPNucHamiltonWrite(const RSPNucHamilton*,FILE*);
        extern QErrorCode RSPNucHamiltonGetContributions(RSPNucHamilton*,
                                                            const QInt,
                                                            const QcPertInt*,
                                                            const QInt,
                                                            QReal*);
        extern QErrorCode RSPNucHamiltonDestroy(RSPNucHamilton*);
        /*FIXME: RSPNucHamiltonGetNumAtoms() to be removed after perturbation free scheme implement
        extern QErrorCode RSPNucHamiltonGetNumAtoms(const RSPNucHamilton*,QInt*);
         The functions are implemented as follows:
98c
      \langle RSPNucHamilton.c \ 98c \rangle \equiv
```

```
*/
#include "RSPNucHamilton.h"
/* <function name='RSPNucHamiltonCreate'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-02-12'>
    Create the context of nuclear Hamiltonian, should be called at first
     <param name='nuc_hamilton' direction='inout'>
       The context of nuclear Hamiltonian
     </param>
     <param name='num_pert_lab' direction='in'>
       Number of all different perturbation labels that can act as
       perturbations on the nuclear Hamiltonian
     </param>
     <param name='pert_labels' direction='in'>
       All the different perturbation labels
     </param>
     <param name='pert_max_orders' direction='in'>
       Allowed maximal order of a perturbation described by exactly one of
       the above different labels
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback-function context
     </param>
     <param name='get_nuc_contrib' direction='in'>
       User-specified function for calculating contribution of the
       nuclear Hamiltonian and its derivatives
     </param>
     <param name='num_atoms' direction='in'>
       Number of atoms
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPNucHamiltonCreate(RSPNucHamilton *nuc_hamilton,
                                const QInt num_pert_lab,
                                const QcPertInt *pert_labels,
                                const QInt *pert_max_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                                void *user_ctx,
#endif
                                const GetNucContrib get_nuc_contrib,
/*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
                                const QInt num_atoms)
{
    QInt ilab; /* incremental recorders over perturbation labels */
    QInt jlab;
    if (num_pert_lab<0) {</pre>
        printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "invalid number of perturbation labels");
```

```
}
else if (num_pert_lab>OPENRSP_PERT_LABEL_MAX) {
    printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
           num_pert_lab);
    printf("RSPNucHamiltonCreate>> maximal value for pert. labels %"QCPERTINT_FMT"\n",
           OPENRSP_PERT_LABEL_MAX);
    QErrorExit(FILE_AND_LINE, "too many perturbation labels");
}
nuc_hamilton->num_pert_lab = num_pert_lab;
if (nuc_hamilton->num_pert_lab>0) {
    nuc_hamilton->pert_max_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (nuc_hamilton->pert_max_orders==NULL) {
        printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for allowed maximal orders");
    nuc_hamilton->nuc_pert_orders = (QInt *)malloc(num_pert_lab*sizeof(QInt));
    if (nuc_hamilton->nuc_pert_orders==NULL) {
        printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. orders on nuclear Hamilto
    }
    nuc_hamilton->pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt));
    if (nuc_hamilton->pert_labels==NULL) {
        printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for perturbation labels");
    }
    nuc_hamilton->nuc_pert_labels = (QcPertInt *)malloc(num_pert_lab*sizeof(QcPertInt))
    if (nuc_hamilton->nuc_pert_labels==NULL) {
        printf("RSPNucHamiltonCreate>> number of perturbation labels %"QINT_FMT"\n",
               num_pert_lab);
        QErrorExit(FILE_AND_LINE, "allocates memory for pert. labels on nuclear Hamilto
    }
    for (ilab=0; ilab<num_pert_lab; ilab++) {</pre>
        if (pert_labels[ilab]>OPENRSP_PERT_LABEL_MAX) {
            printf("RSPNucHamiltonCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                   pert_labels[ilab]);
            printf("RSPNucHamiltonCreate>> maximal value for pert. labels %"QCPERTINT_F
                   OPENRSP_PERT_LABEL_MAX);
            QErrorExit(FILE_AND_LINE, "invalid perturbation label");
        }
        /* each element of <pert_labels> should be unique */
        for (jlab=0; jlab<ilab; jlab++) {</pre>
            if (pert_labels[jlab] == pert_labels[ilab]) {
                printf("RSPNucHamiltonCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_F
                       pert_labels[jlab]);
                printf("RSPNucHamiltonCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_F
                       pert_labels[ilab]);
```

QErrorExit(FILE_AND_LINE, "repeated perturbation labels not allowed");

```
}
                     }
                     nuc_hamilton->pert_labels[ilab] = pert_labels[ilab];
                     if (pert_max_orders[ilab]<1) {</pre>
                         printf("RSPNucHamiltonCreate>> %"QINT_FMT"-th pert. label %"QCPERTINT_FMT"\
                                 ilab,
                                pert_labels[ilab]);
                         printf("RSPNucHamiltonCreate">> allowed maximal order is \cite{Continuous}"QINT_FMT"\n",
                                pert_max_orders[ilab]);
                         QErrorExit(FILE_AND_LINE, "only positive order allowed");
                     }
                     nuc_hamilton->pert_max_orders[ilab] = pert_max_orders[ilab];
                }
            }
            else {
                nuc_hamilton->pert_max_orders = NULL;
                nuc_hamilton->nuc_pert_orders = NULL;
                nuc_hamilton->pert_labels = NULL;
                nuc_hamilton->nuc_pert_labels = NULL;
        #if defined(OPENRSP_C_USER_CONTEXT)
            nuc_hamilton->user_ctx = user_ctx;
        #endif
            nuc_hamilton->get_nuc_contrib = get_nuc_contrib;
        /*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
            nuc_hamilton->num_atoms = num_atoms;
            return QSUCCESS;
        }
      As shown here, we allow for an nuclear Hamiltonian that does not depend on any peraturbation—
      num_pert_lab==0, i.e. any perturbed contribution of this nuclear Hamiltonian is zero.
      \langle RSPNucHamilton.c \ 98c \rangle + \equiv
101
        /* <function name='RSPNucHamiltonAssemble'</pre>
                      attr='private'
                      author='Bin Gao'
                      date='2015-02-12'>
             Assembles the context of nuclear Hamiltonian
              <param name='nuc_hamilton' direction='inout'>
               The context of nuclear Hamiltonian
              <param name='rsp_pert' direction='in'>
               The context of perturbations
             </param>
              <return>Error information</return>
           </function> */
        QErrorCode RSPNucHamiltonAssemble(RSPNucHamilton *nuc_hamilton,
                                            const RSPPert *rsp_pert)
        {
            QErrorCode ierr; /* error information */
            if (nuc_hamilton->num_pert_lab>0 &&
                 (nuc_hamilton->pert_labels==NULL || nuc_hamilton->pert_max_orders==NULL)) {
```

```
QErrorExit(FILE_AND_LINE, "perturbations of nuclear Hamiltonian not set");
    }
    if (nuc_hamilton->get_nuc_contrib==NULL) {
        QErrorExit(FILE_AND_LINE, "callback function of nuclear Hamiltonian not set");
    /* checks perturbation labels and allowed maximal orders against
       all known perturbations */
    ierr = RSPPertValidateLabelOrder(rsp_pert,
                                     nuc_hamilton->num_pert_lab,
                                     nuc_hamilton->pert_labels,
                                     nuc_hamilton->pert_max_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertValidateLabelOrder()");
   return QSUCCESS;
}
/* <function name='RSPNucHamiltonWrite'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-02-12'>
    Writes the context of nuclear Hamiltonian
     <param name='nuc_hamilton' direction='in'>
       The context of nuclear Hamiltonian
     </param>
     <param name='fp_nuc' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPNucHamiltonWrite(const RSPNucHamilton *nuc_hamilton,
                               FILE *fp_nuc)
{
    QInt ilab; /* incremental recorder over perturbation labels */
    fprintf(fp_nuc,
            "RSPNucHamiltonWrite>> number of pert. labels that nuclear Hamiltonian depends
            nuc_hamilton->num_pert_lab);
    fprintf(fp_nuc, "RSPNucHamiltonWrite>> label
                                                           maximum-order\n");
    for (ilab=0; ilab<nuc_hamilton->num_pert_lab; ilab++) {
        fprintf(fp_nuc,
                                                                                %"QINT_FMT"\
                "RSPNucHamiltonWrite>>
                                             %"QCPERTINT_FMT"
                nuc_hamilton->pert_labels[ilab],
                nuc_hamilton->pert_max_orders[ilab]);
    }
#if defined(OPENRSP_C_USER_CONTEXT)
    if (nuc_hamilton->user_ctx!=NULL) {
        fprintf(fp_nuc, "RSPNucHamiltonWrite>> user-defined function context given\n");
    }
#endif
/*FIXME: num_atoms to be removed after perturbation free scheme implemented*/
    fprintf(fp_nuc,
            "RSPNucHamiltonWrite>> number of atoms %"QINT_FMT"\n",
            nuc_hamilton->num_atoms);
   return QSUCCESS;
}
```

```
/* <function name='RSPNucHamiltonGetContributions'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-10-15'>
    Calculates contribution of the nuclear Hamiltonian
     <param name='nuc_hamilton' direction='inout'>
       The context of nuclear Hamiltonian
     </param>
     <param name='nuc_len_tuple' direction='in'>
       Length of the perturbation tuple on the nuclear Hamiltonian
     </param>
     <param name='nuc_pert_tuple' direction='in'>
       Perturbation tuple on the nuclear Hamiltonian
     </param>
     <param name='size_pert' direction='in'>
       Size of the perturbations on the nuclear Hamiltonian
     <param name='val_nuc' direction='inout'>
       The contribution of the nuclear Hamiltonian
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPNucHamiltonGetContributions(RSPNucHamilton *nuc_hamilton,
                                           const QInt nuc_len_tuple,
                                           const QcPertInt *nuc_pert_tuple,
                                           const QInt size_pert,
                                           QReal *val_nuc)
{
    QErrorCode ierr; /* error information */
    /* gets perturbation labels and corresponding orders out of the internal
       perturbation tuple on the nuclear Hamiltonian */
    ierr = RSPPertInternTupleToHostLabelOrder(nuc_len_tuple,
                                               nuc_pert_tuple,
                                               nuc_hamilton->num_pert_lab,
                                               nuc_hamilton->pert_labels,
                                               nuc_hamilton->pert_max_orders,
                                               &nuc_hamilton->nuc_num_pert,
                                               nuc_hamilton->nuc_pert_labels,
                                               nuc_hamilton->nuc_pert_orders);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPPertInternTupleToHostLabelOrder()");
    /* checks if the perturbations on the nuclear Hamiltonian
       result in zero values */
    if (nuc_hamilton->nuc_num_pert<0) return QSUCCESS;</pre>
    /* calculates contribution of nuclear Hamiltonian using the
       callback function */
   nuc_hamilton->get_nuc_contrib(nuc_hamilton->nuc_num_pert,
                                  nuc_hamilton->nuc_pert_labels,
                                  nuc_hamilton->nuc_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                                  nuc_hamilton->user_ctx,
#endif
                                  size_pert,
```

```
val_nuc);
   return QSUCCESS;
}
/*% \brief gets the number of atoms
    \author Bin Gao
    \date 2015-02-12
    \param[RSPNucHamilton:struct]{in} nuc_hamilton the context of nuclear Hamiltonian
    \param[QInt:int]{out} num_atoms number of atoms
    \return[QErrorCode:int] error information
*/
QErrorCode RSPNucHamiltonGetNumAtoms(const RSPNucHamilton *nuc_hamilton,
                                      QInt *num_atoms)
{
    *num_atoms = nuc_hamilton->num_atoms;
   return QSUCCESS;
}
/* <function name='RSPNucHamiltonDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2015-02-12'>
    Destroys the context of nuclear Hamiltonian, should be called at the end
     <param name='nuc_hamilton' direction='inout'>
       The context of nuclear Hamiltonian
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPNucHamiltonDestroy(RSPNucHamilton *nuc_hamilton)
    if (nuc_hamilton->pert_max_orders!=NULL) {
        free(nuc_hamilton->pert_max_orders);
        nuc_hamilton->pert_max_orders = NULL;
    }
    if (nuc_hamilton->nuc_pert_orders!=NULL) {
        free(nuc_hamilton->nuc_pert_orders);
        nuc_hamilton->nuc_pert_orders = NULL;
    }
    if (nuc_hamilton->pert_labels!=NULL) {
        free(nuc_hamilton->pert_labels);
        nuc_hamilton->pert_labels = NULL;
    }
    if (nuc_hamilton->nuc_pert_labels!=NULL) {
        free(nuc_hamilton->nuc_pert_labels);
        nuc_hamilton->nuc_pert_labels = NULL;
    }
#if defined(OPENRSP_C_USER_CONTEXT)
   nuc_hamilton->user_ctx = NULL;
#endif
   nuc_hamilton->get_nuc_contrib = NULL;
    return QSUCCESS;
}
```

3.9 Linear Response Equation Solver

```
Users can use the following API to set the linear response equation solver:
       \langle OpenRSP.c \ 17a \rangle + \equiv
106a
         /* <function name='OpenRSPSetLinearRSPSolver' author='Bin Gao' date='2014-08-06'>
              Set the context of linear response equation solver
               <param name='open_rsp' direction='inout'>
                 The context of response theory calculations
               </param>
               <param name='user_ctx' direction='in'>
                 User-defined callback function context
               <param name='get_linear_rsp_solution' direction='in'>
                 User-specified callback function of linear response equation solver
               <return>Error information</return>
            </function> */
         QErrorCode OpenRSPSetLinearRSPSolver(OpenRSP *open_rsp,
         #if defined(OPENRSP_C_USER_CONTEXT)
                                                 void *user_ctx,
         #endif
                                                 const GetLinearRSPSolution get_linear_rsp_solution)
         {
             QErrorCode ierr; /* error information */
             /* creates the context of response equation solver */
             if (open_rsp->rsp_solver!=NULL) {
                  ierr = RSPSolverDestroy(open_rsp->rsp_solver);
                  QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverDestroy()");
             }
             else {
                  open_rsp->rsp_solver = (RSPSolver *)malloc(sizeof(RSPSolver));
                  if (open_rsp->rsp_solver==NULL) {
                      QErrorExit(FILE_AND_LINE, "allocates memory for solver");
                  }
             }
             ierr = RSPSolverCreate(open_rsp->rsp_solver,
         #if defined(OPENRSP_C_USER_CONTEXT)
                                      user_ctx,
         #endif
                                      get_linear_rsp_solution);
             QErrorCheckCode(ierr, FILE_AND_LINE, "calling RSPSolverCreate()");
             return QSUCCESS;
         }
       The following header file defines all quantities we need for the linear response equation solver. Type
       GetLinearRSPSolution defines the requirements of the callback function of the linear response
       equation solver.
       \langle RSPSolver.h \ 106b \rangle \equiv
106b
           ⟨OpenRSPLicense 14a⟩
```

<header name='RSPSolver.h' author='Bin Gao' date='2014-08-06'>

```
The header file of linear response equation solver used inside OpenRSP
            </header>
          */
          #if !defined(RSP_SOLVER_H)
          #define RSP_SOLVER_H
          #include "qcmatrix.h"
          typedef void (*GetLinearRSPSolution)(const QInt,
                                                    const QReal*,
                                                    const QInt,
                                                    QcMat*[],
          #if defined(OPENRSP_C_USER_CONTEXT)
                                                    void*,
          #endif
                                                    QcMat*[]);
          \langle RSPSolverStruct 107a \rangle
          \langle RSPSolverAPIs 107b \rangle
          #endif
        The context of linear response equation solver is:
        \langle RSPSolverStruct 107a \rangle \equiv
107a
          typedef struct {
          #if defined(OPENRSP_C_USER_CONTEXT)
              void *user_ctx;
                                                                    /* user-defined callback-function
                                                                       context */
          #endif
                                                                   /* user-specified function of
              GetLinearRSPSolution get_linear_rsp_solution;
                                                                       linear response equation solver */
          } RSPSolver:
        and the related functions are:
        \langle RSPSolverAPIs \ 107b \rangle \equiv
107b
          extern QErrorCode RSPSolverCreate(RSPSolver*,
          #if defined(OPENRSP_C_USER_CONTEXT)
                                                void*,
          #endif
                                                const GetLinearRSPSolution);
          extern QErrorCode RSPSolverAssemble(RSPSolver*);
          extern QErrorCode RSPSolverWrite(const RSPSolver*,FILE*);
          extern QErrorCode RSPSolverGetLinearRSPSolution(const RSPSolver*,
                                                                const QInt,
                                                                 const QReal*,
                                                                 const QInt,
                                                                QcMat*[],
                                                                 QcMat*[]);
          extern QErrorCode RSPSolverDestroy(RSPSolver*);
           These functions are implemented as follows:
        \langle RSPSolver.c \ 107c \rangle \equiv
107c
```

```
/*
  ⟨OpenRSPLicense 14a⟩
#include "RSPSolver.h"
/* <function name='RSPSolverCreate'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
     Create the context of response equation solver, should be called at first
     <param name='rsp_solver' direction='inout'>
       The context of response equation solver
     </param>
     <param name='user_ctx' direction='in'>
       User-defined callback function context
     <param name='get_linear_rsp_solution' direction='in'>
       User-specified callback function of linear response equation solver
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPSolverCreate(RSPSolver *rsp_solver,
#if defined(OPENRSP_C_USER_CONTEXT)
                            void *user_ctx,
#endif
                            const GetLinearRSPSolution get_linear_rsp_solution)
#if defined(OPENRSP_C_USER_CONTEXT)
    rsp_solver->user_ctx = user_ctx;
#endif
    rsp_solver->get_linear_rsp_solution = get_linear_rsp_solution;
    return QSUCCESS;
}
/* <function name='RSPSolverAssemble'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
     Assembles the context of response equation solver
     <param name='rsp_solver' direction='inout'>
       The context of response equation solver
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPSolverAssemble(RSPSolver *rsp_solver)
/*FIXME: to implement? */
    return QSUCCESS;
/* <function name='RSPSolverWrite'</pre>
```

```
attr='private'
             author='Bin Gao'
             date='2014-08-06'>
    Writes the context of response equation solver
    <param name='rsp_solver' direction='in'>
       The context of response equation solver
     </param>
     <param name='fp_solver' direction='inout'>File pointer</param>
     <return>Error information</return>
   </function> */
QErrorCode RSPSolverWrite(const RSPSolver *rsp_solver, FILE *fp_solver)
#if defined(OPENRSP_C_USER_CONTEXT)
    if (rsp_solver->user_ctx!=NULL) {
        fprintf(fp_solver, "RSPSolverWrite>> user-defined function context given\n");
    }
#endif
   return QSUCCESS;
}
/* <function name='RSPSolverGetLinearRSPSolution'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-06'>
    Solve the linear response equation
     <param name='rsp_solver' direction='in'>
       The context of response equation solver
     </param>
     <param name='num_freq_sums' direction='in'>
       Number of complex frequency sums on the left hand side of the linear
       response equation
     </param>
     <param name='freq_sums' direction='in'>
       The complex frequency sums on the left hand side
     </param>
     <param name='size_pert' direction='in'>
       Size of perturbations acting on the time-dependent
       self-consistent-field (TDSCF) equation
     </param>
     <param name='RHS_mat' direction='in'>
       Right-hand-side (RHS) matrices, size is the product of <size_pert>
       and <num_freq_sums>
     <param name='rsp_param' direction='inout'>
       Solved response parameters, size is the product of <size_pert>
       and <num_freq_sums>
     </param>
     <return>Error information</return>
   </function> */
QErrorCode RSPSolverGetLinearRSPSolution(const RSPSolver *rsp_solver,
                                         const QInt num_freq_sums,
                                          const QReal *freq_sums,
                                          const QInt size_pert,
```

```
QcMat *RHS_mat[],
                                          QcMat *rsp_param[])
{
    rsp_solver->get_linear_rsp_solution(num_freq_sums,
                                         freq_sums,
                                         size_pert,
                                         RHS_mat,
#if defined(OPENRSP_C_USER_CONTEXT)
                                         rsp_solver->user_ctx,
#endif
                                         rsp_param);
    return QSUCCESS;
}
/* <function name='RSPSolverDestroy'</pre>
             attr='private'
             author='Bin Gao'
             date='2014-08-05'>
     Destroys the context of response equation solver, should be called at the end
     <param name='rsp_solver' direction='inout'>
       The context of response equation solver
     <return>Error information</return>
   </function> */
QErrorCode RSPSolverDestroy(RSPSolver *rsp_solver)
{
#if defined(OPENRSP_C_USER_CONTEXT)
    rsp_solver->user_ctx = NULL;
#endif
    rsp_solver->get_linear_rsp_solution = NULL;
    return QSUCCESS;
}
```

3.10 Response Functions

```
Users can use the following API to get the response functions:
111
      \langle OpenRSP.c \ 17a \rangle + \equiv
        void OpenRSPGetRSPFun_f(const QInt num_props,
                                 const QInt *len_tuple,
                                 const QcPertInt *pert_tuple,
                                 const QInt *num_freq_configs,
                                 const QReal *pert_freqs,
                                 const QInt *kn_rules,
                                 const QcMat *ref_ham,
                                 const QcMat *ref_overlap,
                                 const QcMat *ref_state,
                                 RSPSolver *rsp_solver,
                                 RSPNucHamilton *nuc_hamilton,
                                 RSPOverlap *overlap,
                                 RSPOneOper *one_oper,
                                 RSPTwoOper *two_oper,
                                 RSPXCFun *xc_fun,
                                 const QInt size_rsp_funs,
                                 QReal *rsp_funs);
        /*@% \brief gets the response functions for given perturbations
             \author Bin Gao
             \date 2014-07-31
             \param[OpenRSP:struct]{inout} open_rsp the context of response theory calculations
             \param[QcMat:struct]{in} ref_ham Hamiltonian of referenced state
             \param[QcMat:struct]{in} ref_state electronic state of referenced state
             \param[QcMat:struct]{in} ref_overlap overlap integral matrix of referenced state
             \param[QInt:int]{in} num_props number of properties to calculate
             \param[QInt:int]{in} len_tuple length of perturbation tuple for each property
             \param[QInt:int]{in} pert_tuple ordered list of perturbation labels
                 for each property
             \param[QInt:int]{in} num_freq_configs number of different frequency
                 configurations for each property
             \param[QReal:real]{in} pert_freqs complex frequencies of each perturbation label
                 (except for the perturbation a) over all frequency configurations
             \param[QInt:int]{in} kn_rules number k for the kn rule for each property
             \param[QInt:int]{in} size_rsp_funs size of the response functions
             \param[QReal:real]{out} rsp_funs the response functions
             \return[QErrorCode:int] error information
        */
        QErrorCode OpenRSPGetRSPFun(OpenRSP *open_rsp,
                                     const QcMat *ref_ham,
                                     const QcMat *ref_state,
                                     const QcMat *ref_overlap,
                                     const QInt num_props,
                                     const QInt *len_tuple,
                                     const QcPertInt *pert_tuple,
                                     const QInt *num_freq_configs,
                                     const QReal *pert_freqs,
```

const QInt *kn_rules,

```
const QInt size_rsp_funs,
                            QReal *rsp_funs)
{
    //QErrorCode ierr; /* error information */
    if (open_rsp->assembled==QFALSE) {
        QErrorExit(FILE_AND_LINE, "OpenRSPAssemble() should be called before calculations")
    //switch (open_rsp->elec_wav_type) {
    ///* density matrix-based response theory */
    //case ELEC_AO_D_MATRIX:
        OpenRSPGetRSPFun_f(num_props,
                           len_tuple,
                           pert_tuple,
                           num_freq_configs,
                           pert_freqs,
                           kn_rules,
                           ref_ham,
                           ref_overlap,
                           ref_state,
                           open_rsp->rsp_solver,
                           open_rsp->nuc_hamilton,
                           open_rsp->overlap,
                           open_rsp->one_oper,
                           open_rsp->two_oper,
                           open_rsp->xc_fun,
                           //id_outp,
                           size_rsp_funs,
                           rsp_funs);
    //
          break;
    ///* molecular orbital (MO) coefficient matrix-based response theory */
    //case ELEC_MO_C_MATRIX:
         break;
    ///* couple cluster-based response theory */
    //case ELEC_COUPLED_CLUSTER:
    //
          break;
    //default:
          printf("OpenRSPGetRSPFun>> type of (electronic) wave function %d\n",
    //
    //
                 open_rsp->elec_wav_type);
          QErrorExit(FILE_AND_LINE, "invalid type of (electronic) wave function");
    //
    //}
    return QSUCCESS;
}
```

3.11 Residues

```
Users can use the following API to get the residues:
      \langle \mathit{OpenRSP.c} \ 17a \rangle + \equiv
113
        /*0% \brief gets the residues for given perturbations
             \author Bin Gao
             \date 2014-07-31
             \param[OpenRSP:struct]{inout} open_rsp the context of response theory calculations
             \param[QcMat:struct]{in} ref_ham Hamiltonian of referenced state
             \param[QcMat:struct]{in} ref_state electronic state of referenced state
             \param[QcMat:struct]{in} ref_overlap overlap integral matrix of referenced state
             \param[QInt:int]{in} order_residue order of residues, that is also the length of
                 each excitation tuple
             \param[QInt:int]{in} num_excit number of excitation tuples that will be used for
                 residue calculations
             \param[QReal:real]{in} excit_energy excitation energies of all tuples, size is
                 ''order_residue'' :math:'\times' ''num_excit'', and arranged
                 as ''[num_excit][order_residue]'; that is, there will be
                 "order_residue" frequencies of perturbation labels (or sums
                 of frequencies of perturbation labels) respectively equal to
                 the "order_residue" excitation energies per tuple
                 ''excit_energy[i][:]'' (''i'' runs from ''0'' to ''num_excit-1'')
             \param[QcMat:struct]{in} eigen_vector eigenvectors (obtained from the generalized
                 eigenvalue problem) of all excitation tuples, size is "order_residue"
                 :math:'\times' ''num_excit'', and also arranged in memory
                 as ''[num_excit][order_residue]'' so that each eigenvector has
                 its corresponding excitation energy in "excit_energy"
             \param[QInt:int]{in} num_props number of properties to calculate
             \param[QInt:int]{in} len_tuple length of perturbation tuple for each property
             \param[QInt:int]{in} pert_tuple ordered list of perturbation labels
                 for each property
             \param[QInt:int]{in} residue_num_pert for each property and each excitation energy
                 in the tuple, the number of perturbation labels whose sum of
                 frequencies equals to that excitation energy, size is "order_residue"
                 :math:'\times' ''num_props'', and arragned as ''[num_props][order_residue]';
                 a negative ''residue_num_pert[i][j]'' (''i'' runs from ''0'' to
                 ''num_props-1'') means that the sum of frequencies of perturbation
                 labels equals to ''-excit_energy[:][j]''
             \param[QInt:int]{in} residue_idx_pert for each property and each excitation energy
                 in the tuple, the indices of perturbation labels whose sum of
                 frequencies equals to that excitation energy, size is
                 "sum(residue_num_pert)", and arranged as "[residue_num_pert]"
             \param[QInt:int]{in} num_freq_configs number of different frequency
                 configurations for each property
             \param[QReal:real]{in} pert_freqs complex frequencies of each perturbation
                 label (except for the perturbation a) over all frequency configurations
                 and excitation tuples
             \param[QInt:int]{in} kn_rules number k for the kn rule for each property
             \param[QInt:int]{in} size_residues size of the residues
             \param[QReal:real]{out} residues the residues
```

\return[QErrorCode:int] error information

```
QErrorCode OpenRSPGetResidue(OpenRSP *open_rsp,
                             const QcMat *ref_ham,
                             const QcMat *ref_state,
                             const QcMat *ref_overlap,
                             const QInt order_residue,
                             const QInt num_excit,
                             const QReal *excit_energy,
                             QcMat *eigen_vector[],
                             const QInt num_props,
                             const QInt *len_tuple,
                             const QcPertInt *pert_tuple,
                             const QInt *residue_num_pert,
                             const QInt *residue_idx_pert,
                             const QInt *num_freq_configs,
                             const QReal *pert_freqs,
                             const QInt *kn_rules,
                             const QInt size_residues,
                             QReal *residues)
{
    //QErrorCode ierr; /* error information */
    if (open_rsp->assembled==QFALSE) {
        QErrorExit(FILE_AND_LINE, "OpenRSPAssemble() should be invoked before any calculati
    }
    //switch (open_rsp->elec_wav_type) {
    ///* density matrix-based response theory */
    //case ELEC_AO_D_MATRIX:
    ///* molecular orbital (MO) coefficient matrix-based response theory */
    //case ELEC_MO_C_MATRIX:
         break;
    ///* couple cluster-based response theory */
    //case ELEC_COUPLED_CLUSTER:
         break;
    //default:
    //
          printf("OpenRSPGetResidue>> type of (electronic) wave function %d\n",
    //
                 open_rsp->elec_wav_type);
          QErrorExit(FILE_AND_LINE, "invalid type of (electronic) wave function");
    //
    //}
   return QSUCCESS;
}
```

3.12 Fortran APIs

This section will implement APIs for Fortran users by using the Fortran ISO_C_BINDING.

We also plan to release this part of the OpenRSP under the GNU Lesser General Public License:

```
\langle OpenRSPLicenseFortran \ 115a \rangle \equiv
115a
         !! OpenRSP: open-ended library for response theory
         !! Copyright 2015 Radovan Bast,
         !!
                            Daniel H. Friese,
         !!
                             Bin Gao,
         !!
                             Dan J. Jonsson,
                            Magnus Ringholm,
         !!
         !!
                            Kenneth Ruud,
         !!
                             Andreas Thorvaldsen
         !!
         !! OpenRSP is free software: you can redistribute it and/or modify
         !! it under the terms of the GNU Lesser General Public License as
         !! published by the Free Software Foundation, either version 3 of
         !! the License, or (at your option) any later version.
         !!
         !! OpenRSP is distributed in the hope that it will be useful,
         !! but WITHOUT ANY WARRANTY; without even the implied warranty of
         !! MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
         !! GNU Lesser General Public License for more details.
         !!
         !! You should have received a copy of the GNU Lesser General Public
         !! License along with OpenRSP. If not, see <a href="http://www.gnu.org/licenses/">http://www.gnu.org/licenses/>.
       Here is the organization of the module file:
       \langle OpenRSP.F90 \ 115b \rangle \equiv
115b
         !!
         !! <QCLANG='Fortran'>
         !! <para>
              Fortran users should use the module <OpenRSP_f> in their codes to access
         !!
              the functionalities of OpenRSP. We have used the same name for Fortran
              data types and constants, for instance <OpenRSP>; macro definitions are
         !!
              also controlled by the same names, such as <OPENRSP_USER_CONTEXT>; however
         !!
               all Fortran modules and functions are appended by <c>_f</c>.
         !! </para>
         !!
         ⟨OpenRSPLicenseFortran 115a⟩
         !! <module name='OpenRSP_f' author='Bin Gao' date='2014-07-12'>
               The module file of OpenRSP library for Fortran users
         !! </module>
         ! basic data types
         #include "api/qcmatrix_c_type.h"
         module OpenRSP_f
             use, intrinsic :: iso_c_binding
             use qcmatrix_f, only: QINT,
```

QREAL,

```
QFAILURE, &
                      QcMat,
                      QcMat_C_LOC
use RSPSolver_f, only: SolverFun_f,
                       RSPSolverCreate_f, &
                       RSPSolverDestroy_f
use RSPPerturbation_f, only: QcPertInt,
                                              &
                             PertFun_f,
                                              &
                             RSPPertCreate_f, &
                             RSPPertDestrov_f
use RSPOverlap_f, only: OverlapFun_f,
                        RSPOverlapCreate_f, &
                        RSPOverlapDestroy_f
use RSPOneOper_f, only: OneOperFun_f,
                        RSPOneOperCreate_f, &
                        RSPOneOperDestroy_f
use RSPTwoOper_f, only: TwoOperFun_f,
                        RSPTwoOperCreate_f, &
                        RSPTwoOperDestroy_f
use RSPXCFun_f, only: XCFunFun_f,
                      RSPXCFunCreate_f, &
                      RSPXCFunDestroy_f
use RSPNucHamilton_f, only: NucHamiltonFun_f,
                            RSPNucHamiltonCreate_f, &
                            RSPNucHamiltonDestroy_f
implicit none
! type of equation of motion (EOM) of electrons
integer(kind=QINT), parameter, public :: ELEC_AO_D_MATRIX = 0
integer(kind=QINT), parameter, public :: ELEC_MO_C_MATRIX = 1
integer(kind=QINT), parameter, public :: ELEC_COUPLED_CLUSTER = 2
! linked list of context of callback subroutines of one-electron operators
type, private :: OneOperList_f
    type(OneOperFun_f), pointer :: one_oper_fun => null()
    type(OneOperList_f), pointer :: next_one_oper => null()
end type OneOperList_f
! linked list of context of callback subroutines of two-electron operators
type, private :: TwoOperList_f
    type(TwoOperFun_f), pointer :: two_oper_fun => null()
    type(TwoOperList_f), pointer :: next_two_oper => null()
end type TwoOperList_f
! linked list of context of callback subroutines of XC functionals
type, private :: XCFunList_f
   type(XCFunFun_f), pointer :: xcfun_fun => null()
    type(XCFunList_f), pointer :: next_xc_fun => null()
end type XCFunList_f
! OpenRSP type (inspired by http://wiki.rac.manchester.ac.uk/community/GPU/GpuFaq/Fortr
```

```
type, public :: OpenRSP
    private
    type(C_PTR) :: c_rsp = C_NULL_PTR
    type(SolverFun_f), pointer :: solver_fun => null()
    type(PertFun_f), pointer :: pert_fun => null()
    type(OverlapFun_f), pointer :: overlap_fun => null()
    type(OneOperList_f), pointer :: list_one_oper => null()
    type(TwoOperList_f), pointer :: list_two_oper => null()
    type(XCFunList_f), pointer :: list_xc_fun => null()
    type(NucHamiltonFun_f), pointer :: nuc_hamilton_fun => null()
end type OpenRSP
! functions provided by the Fortran APIs
public :: OpenRSPCreate_f
!public :: OpenRSPSetElecEOM_f
public :: OpenRSPSetLinearRSPSolver_f
public :: OpenRSPSetPerturbations_f
public :: OpenRSPSetOverlap_f
public :: OpenRSPAddOneOper_f
public :: OpenRSPAddTwoOper_f
public :: OpenRSPAddXCFun_f
public :: OpenRSPSetNucHamilton_f
public :: OpenRSPAssemble_f
public :: OpenRSPWrite_f
public :: OpenRSPGetRSPFun_f
!public :: OpenRSPGetResidue_f
public :: OpenRSPDestroy_f
interface OpenRSPWrite_f
    module procedure OpenRSPWritebyFileName_f
    module procedure OpenRSPWritebyUnit_f
end interface OpenRSPWrite_f
interface
    integer(C_INT) function OpenRSPCreateFortranAdapter(open_rsp) &
        bind(C, name="OpenRSPCreateFortranAdapter")
        use, intrinsic :: iso_c_binding
        type(C_PTR), intent(inout) :: open_rsp
    end function OpenRSPCreateFortranAdapter
    !integer(C_INT) function f_api_OpenRSPSetElecEOM(open_rsp,
    ļ
                                                      elec_EOM_type) &
    !
         bind(C, name="f_api_OpenRSPSetElecEOM")
    !
         use, intrinsic :: iso_c_binding
         type(C_PTR), intent(inout) :: open_rsp
         integer(kind=C_QINT), value, intent(in) :: elec_EOM_type
    !end function f_api_OpenRSPSetElecEOM
    integer(C_INT) function OpenRSPSetLinearRSPSolver(open_rsp,
                                                                         &
                                                       user_ctx,
                                                                         &
                                                       get_linear_rsp_solution) &
        bind(C, name="OpenRSPSetLinearRSPSolver")
        use, intrinsic :: iso_c_binding
        type(C_PTR), value, intent(in) :: open_rsp
```

```
type(C_PTR), value, intent(in) :: user_ctx
   type(C_FUNPTR), value, intent(in) :: get_linear_rsp_solution
end function OpenRSPSetLinearRSPSolver
integer(C_INT) function OpenRSPSetPerturbations(open_rsp,
                                                num_pert_lab,
                                                                        &
                                                pert_labels,
                                                                        &
                                                pert_max_orders,
                                                                        &
                                                                        &
                                                pert_num_comps,
                                                user_ctx,
                                                get_pert_concatenation) &
   bind(C, name="OpenRSPSetPerturbations")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_num_comps(sum(pert_max_orders))
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_pert_concatenation
end function OpenRSPSetPerturbations
integer(C_INT) function OpenRSPSetOverlap(open_rsp,
                                          num_pert_lab,
                                                           &
                                          pert_labels,
                                          pert_max_orders, &
                                          user_ctx,
                                          get_overlap_mat, &
                                          get_overlap_exp) &
   bind(C, name="OpenRSPSetOverlap")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_overlap_mat
    type(C_FUNPTR), value, intent(in) :: get_overlap_exp
end function OpenRSPSetOverlap
integer(C_INT) function OpenRSPAddOneOper(open_rsp,
                                          num_pert_lab,
                                          pert_labels,
                                          pert_max_orders, &
                                          user_ctx,
                                          get_one_oper_mat, &
                                          get_one_oper_exp) &
   bind(C, name="OpenRSPAddOneOper")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
    type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
```

```
integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_one_oper_mat
    type(C_FUNPTR), value, intent(in) :: get_one_oper_exp
end function OpenRSPAddOneOper
integer(C_INT) function OpenRSPAddTwoOper(open_rsp,
                                          num_pert_lab,
                                         pert_labels,
                                                           Хr.
                                          pert_max_orders, &
                                          user_ctx,
                                          get_two_oper_mat, &
                                          get_two_oper_exp) &
   bind(C, name="OpenRSPAddTwoOper")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_two_oper_mat
    type(C_FUNPTR), value, intent(in) :: get_two_oper_exp
end function OpenRSPAddTwoOper
integer(C_INT) function OpenRSPAddXCFun(open_rsp,
                                       num_pert_lab,
                                       pert_labels,
                                       pert_max_orders, &
                                        user_ctx,
                                        get_xc_fun_mat, &
                                        get_xc_fun_exp) &
   bind(C, name="OpenRSPAddXCFun")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
    integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_xc_fun_mat
    type(C_FUNPTR), value, intent(in) :: get_xc_fun_exp
end function OpenRSPAddXCFun
integer(C_INT) function OpenRSPSetNucHamilton(open_rsp,
                                              num_pert_lab,
                                              pert_labels,
                                              pert_max_orders, &
                                              user_ctx,
                                              get_nuc_contrib, &
                                              num_atoms)
   bind(C, name="OpenRSPSetNucHamilton")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
```

```
integer(kind=C_QINT), value, intent(in) :: num_pert_lab
    integer(kind=C_QCPERTINT), intent(in) :: pert_labels(num_pert_lab)
    integer(kind=C_QINT), intent(in) :: pert_max_orders(num_pert_lab)
   type(C_PTR), value, intent(in) :: user_ctx
    type(C_FUNPTR), value, intent(in) :: get_nuc_contrib
    integer(kind=C_QINT), value, intent(in) :: num_atoms
end function OpenRSPSetNucHamilton
integer(C_INT) function OpenRSPAssemble(open_rsp) &
   bind(C, name="OpenRSPAssemble")
   use, intrinsic :: iso_c_binding
   type(C_PTR), value, intent(in) :: open_rsp
end function OpenRSPAssemble
integer(C_INT) function OpenRSPWriteFortranAdapter(open_rsp, &
                                                   file_name) &
   bind(C, name="OpenRSPWriteFortranAdapter")
   use, intrinsic :: iso_c_binding
   type(C_PTR), value, intent(in) :: open_rsp
    character(C_CHAR), intent(in) :: file_name(*)
end function OpenRSPWriteFortranAdapter
integer(C_INT) function OpenRSPWriteStdOutFortranAdapter(open_rsp) &
   bind(C, name="OpenRSPWriteStdOutFortranAdapter")
   use, intrinsic :: iso_c_binding
   type(C_PTR), value, intent(in) :: open_rsp
end function OpenRSPWriteStdOutFortranAdapter
integer(C_INT) function OpenRSPGetRSPFun(open_rsp,
                                                           &
                                         ref_ham,
                                                           &
                                         ref_state,
                                         ref_overlap,
                                                           &
                                         num_props,
                                                           &
                                         len_tuple,
                                                           &
                                         pert_tuple,
                                                           &
                                         num_freq_configs, &
                                         pert_freqs,
                                                           &
                                         kn_rules,
                                                           &
                                         size_rsp_funs,
                                                           &
                                         rsp_funs)
                                                           &
   bind(C, name="OpenRSPGetRSPFun")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   type(C_PTR), value, intent(in) :: open_rsp
    type(C_PTR), value, intent(in) :: ref_ham
   type(C_PTR), value, intent(in) :: ref_state
   type(C_PTR), value, intent(in) :: ref_overlap
    integer(kind=C_QINT), value, intent(in) :: num_props
    integer(kind=C_QINT), intent(in) :: len_tuple(num_props)
    integer(kind=C_QCPERTINT), intent(in) :: pert_tuple(sum(len_tuple))
    integer(kind=C_QINT), intent(in) :: num_freq_configs(num_props)
   real(kind=C_QREAL), intent(in) :: pert_freqs(2*dot_product(len_tuple,num_freq_c
    integer(kind=C_QINT), intent(in) :: kn_rules(num_props)
    integer(kind=C_QINT), value, intent(in) :: size_rsp_funs
   real(kind=C_QREAL), intent(out) :: rsp_funs(2*size_rsp_funs)
end function OpenRSPGetRSPFun
```

```
integer(C_INT) function OpenRSPDestroyFortranAdapter(open_rsp) &
           bind(C, name="OpenRSPDestroyFortranAdapter")
           use, intrinsic :: iso_c_binding
            type(C_PTR), intent(inout) :: open_rsp
        end function OpenRSPDestroyFortranAdapter
   end interface
    contains
   function OpenRSPCreate_f(open_rsp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        ierr = OpenRSPCreateFortranAdapter(open_rsp%c_rsp)
       nullify(open_rsp%solver_fun)
       nullify(open_rsp%pert_fun)
       nullify(open_rsp%overlap_fun)
       nullify(open_rsp%list_one_oper)
       nullify(open_rsp%list_two_oper)
       nullify(open_rsp%list_xc_fun)
       nullify(open_rsp%nuc_hamilton_fun)
    end function OpenRSPCreate_f
    !function OpenRSPSetElecEOM_f(open_rsp, elec_EOM_type) result(ierr)
         integer(kind=4) :: ierr
         type(OpenRSP), intent(inout) :: open_rsp
         integer(kind=QINT), intent(in) :: elec_EOM_type
         ierr = f_api_OpenRSPSetElecEOM(open_rsp%c_rsp, elec_EOM_type)
    !end function OpenRSPSetElecEOM_f
   function OpenRSPSetLinearRSPSolver_f(open_rsp,
#if defined(OPENRSP_F_USER_CONTEXT)
                                         user_ctx,
#endif
                                         get_linear_rsp_solution) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
#if defined(OPENRSP_F_USER_CONTEXT)
       character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_linear_rsp_solution(num_freq_sums, &
                                               freq_sums,
                                               size_pert,
                                                              &
                                               RHS_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                               len_ctx,
                                                              &
                                               user_ctx,
                                                              &
#endif
                                               rsp_param)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                integer(kind=QINT), intent(in) :: num_freq_sums
                real(kind=QREAL), intent(in) :: freq_sums(2*num_freq_sums)
```

```
integer(kind=QINT), intent(in) :: size_pert
                type(QcMat), intent(in) :: RHS_mat(num_freq_sums*size_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                type(QcMat), intent(inout) :: rsp_param(num_freq_sums*size_pert)
            end subroutine get_linear_rsp_solution
            subroutine RSPSolverGetLinearRSPSolution_f(num_freq_sums, &
                                                       freq_sums,
                                                       size_pert,
                                                       RHS_mat,
                                                                       &
                                                       user_ctx,
                                                                      &
                                                       rsp_param)
                                                                       &
                bind(C, name="RSPSolverGetLinearRSPSolution_f")
                use, intrinsic :: iso_c_binding
                integer(kind=C_QINT), value, intent(in) :: num_freq_sums
                real(kind=C_QREAL), intent(in) :: freq_sums(2*num_freq_sums)
                integer(kind=C_QINT), value, intent(in) :: size_pert
                type(C_PTR), intent(in) :: RHS_mat(num_freq_sums*size_pert)
                type(C_PTR), value, intent(in) :: user_ctx
                type(C_PTR), intent(inout) :: rsp_param(num_freq_sums*size_pert)
            end subroutine RSPSolverGetLinearRSPSolution_f
        end interface
        if (associated(open_rsp%solver_fun)) then
            call RSPSolverDestroy_f(open_rsp%solver_fun)
            allocate(open_rsp%solver_fun)
        end if
        ! adds context of callback function of response equation solver
        call RSPSolverCreate_f(open_rsp%solver_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                               user_ctx,
#endif
                               get_linear_rsp_solution)
        ierr = OpenRSPSetLinearRSPSolver(open_rsp%c_rsp,
                                         c_loc(open_rsp%solver_fun), &
                                         c_funloc(RSPSolverGetLinearRSPSolution_f))
   end function OpenRSPSetLinearRSPSolver_f
   function OpenRSPSetPerturbations_f(open_rsp,
                                                        &
                                       num_pert_lab,
                                                        &
                                       pert_labels,
                                       pert_max_orders, &
                                       pert_num_comps,
#if defined(OPENRSP_F_USER_CONTEXT)
                                       user_ctx,
#endif
                                       get_pert_concatenation) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
```

```
integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_num_comps(:)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_pert_concatenation(pert_label,
                                              first_cat_comp, &
                                              num_cat_comps, &
                                              num_sub_tuples, &
                                              len_sub_tuples, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                                              &
                                              len_ctx,
                                              user_ctx,
#endif
                                              rank_sub_comps)
                use qcmatrix_f, only: QINT
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QcPertInt), intent(in) :: pert_label
                integer(kind=QINT), intent(in) :: first_cat_comp
                integer(kind=QINT), intent(in) :: num_cat_comps
                integer(kind=QINT), intent(in) :: num_sub_tuples
                integer(kind=QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_co
            end subroutine get_pert_concatenation
            subroutine RSPPertGetConcatenation_f(pert_label,
                                                 first_cat_comp, &
                                                 num_cat_comps, &
                                                 num_sub_tuples, &
                                                 len_sub_tuples, &
                                                 user_ctx,
                                                 rank_sub_comps) &
                bind(C, name="RSPPertGetConcatenation_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QCPERTINT), value, intent(in) :: pert_label
                integer(kind=C_QINT), value, intent(in) :: first_cat_comp
                integer(kind=C_QINT), value, intent(in) :: num_cat_comps
                integer(kind=C_QINT), value, intent(in) :: num_sub_tuples
                integer(kind=C_QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_
            end subroutine RSPPertGetConcatenation_f
        end interface
        if (associated(open_rsp%pert_fun)) then
            call RSPPertDestroy_f(open_rsp%pert_fun)
        else
```

```
allocate(open_rsp%pert_fun)
        end if
        ! adds context of callback functions of perturbations
        call RSPPertCreate_f(open_rsp%pert_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                             user_ctx,
                                                &
#endif
                             get_pert_concatenation)
        ierr = OpenRSPSetPerturbations(open_rsp%c_rsp,
                                                                    &
                                       num_pert_lab,
                                       pert_labels,
                                                                    &
                                       pert_max_orders,
                                                                    &
                                       pert_num_comps,
                                                                    &
                                       c_loc(open_rsp%pert_fun),
                                                                    &
                                       c_funloc(RSPPertGetConcatenation_f))
    end function OpenRSPSetPerturbations_f
                                                  &
    function OpenRSPSetOverlap_f(open_rsp,
                                                  &
                                 num_pert_lab,
                                 pert_labels,
                                                  &
                                 pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                 user_ctx,
                                                  &
#endif
                                 get_overlap_mat, &
                                 get_overlap_exp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
        integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_overlap_mat(bra_num_pert,
                                       bra_pert_labels,
                                       bra_pert_orders,
                                       ket_num_pert,
                                       ket_pert_labels,
                                       ket_pert_orders,
                                       oper_num_pert,
                                       oper_pert_labels, &
                                       oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                                         &
                                       user_ctx,
                                                         &
#endif
                                       num_int,
                                                         &
                                       val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
```

```
integer(kind=QINT), intent(in) :: bra_num_pert
                integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
                integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
                integer(kind=QINT), intent(in) :: ket_num_pert
                integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
                integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_overlap_mat
            subroutine get_overlap_exp(bra_num_pert,
                                       bra_pert_labels,
                                       bra_pert_orders, &
                                       ket_num_pert,
                                       ket_pert_labels, &
                                       ket_pert_orders, &
                                       oper_num_pert,
                                       oper_pert_labels, &
                                       oper_pert_orders, &
                                       num_dmat,
                                       dens_mat,
                                                         &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                                         &
                                       user_ctx,
#endif
                                                         &
                                       num_exp,
                                       val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: bra_num_pert
                integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
                integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
                integer(kind=QINT), intent(in) :: ket_num_pert
                integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
                integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
```

```
end subroutine get_overlap_exp
subroutine RSPOverlapGetMat_f(bra_num_pert,
                             bra_pert_labels,
                              bra_pert_orders,
                              ket_num_pert,
                              ket_pert_labels, &
                              ket_pert_orders, &
                              oper_num_pert,
                              oper_pert_labels, &
                              oper_pert_orders, &
                              user_ctx,
                              num_int,
                              val_int)
                                                &
   bind(C, name="RSPOverlapGetMat_f")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   integer(kind=C_QINT), value, intent(in) :: bra_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
   integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
   integer(kind=C_QINT), value, intent(in) :: ket_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
   integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
   integer(kind=C_QINT), value, intent(in) :: oper_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
   integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
   type(C_PTR), value, intent(in) :: user_ctx
   integer(kind=C_QINT), value, intent(in) :: num_int
   type(C_PTR), intent(inout) :: val_int(num_int)
end subroutine RSPOverlapGetMat_f
subroutine RSPOverlapGetExp_f(bra_num_pert,
                             bra_pert_labels,
                              bra_pert_orders, &
                              ket_num_pert,
                              ket_pert_labels, &
                              ket_pert_orders,
                              oper_num_pert,
                              oper_pert_labels, &
                              oper_pert_orders, &
                              num_dmat,
                              dens_mat,
                              user_ctx,
                                               &
                              num_exp,
                                                &
                              val_exp)
   bind(C, name="RSPOverlapGetExp_f")
   use, intrinsic :: iso_c_binding
   use RSPPertBasicTypes_f, only: C_QCPERTINT
   integer(kind=C_QINT), value, intent(in) :: bra_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
   integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
   integer(kind=C_QINT), value, intent(in) :: ket_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
   integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
```

```
integer(kind=C_QINT), value, intent(in) :: oper_num_pert
                integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=C_QINT), value, intent(in) :: num_dmat
                type(C_PTR), intent(in) :: dens_mat(num_dmat)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_exp
                real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine RSPOverlapGetExp_f
        end interface
        if (associated(open_rsp%overlap_fun)) then
            call RSPOverlapDestroy_f(open_rsp%overlap_fun)
        else
            allocate(open_rsp%overlap_fun)
        end if
        ! adds context of callback functions of the overlap integrals
        call RSPOverlapCreate_f(open_rsp%overlap_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,
                                                      Źг
#endif
                                get_overlap_mat,
                                get_overlap_exp)
        ierr = OpenRSPSetOverlap(open_rsp%c_rsp,
                                 num_pert_lab,
                                                                &
                                 pert_labels,
                                                                &
                                 pert_max_orders,
                                 c_loc(open_rsp%overlap_fun), &
                                 c_funloc(RSPOverlapGetMat_f), &
                                 c_funloc(RSPOverlapGetExp_f))
   end function OpenRSPSetOverlap_f
   function OpenRSPAddOneOper_f(open_rsp,
                                                   &
                                 num_pert_lab,
                                 pert_labels,
                                 pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                                   &
                                 user_ctx,
#endif
                                 get_one_oper_mat, &
                                 get_one_oper_exp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
        integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_one_oper_mat(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
```

```
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                           &
                                        user_ctx,
#endif
                                        num_int,
                                                           &₹.
                                        val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_one_oper_mat
            subroutine get_one_oper_exp(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
                                        num_dmat,
                                        dens_mat,
                                                           &
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                           &
                                        user_ctx,
#endif
                                        num_exp,
                                                           &
                                        val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_one_oper_exp
            subroutine RSPOneOperGetMat_f(oper_num_pert,
                                          oper_pert_labels, &
                                          oper_pert_orders, &
                                          user_ctx,
                                          num_int,
                                                            Źг
                                          val_int)
                bind(C, name="RSPOneOperGetMat_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
```

integer(kind=C_QINT), value, intent(in) :: oper_num_pert

```
integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_int
                type(C_PTR), intent(inout) :: val_int(num_int)
            end subroutine RSPOneOperGetMat_f
            subroutine RSPOneOperGetExp_f(oper_num_pert,
                                          oper_pert_labels, &
                                          oper_pert_orders, &
                                          num_dmat,
                                          dens_mat,
                                                           &
                                          user_ctx,
                                                            &
                                          num_exp,
                                          val_exp)
                bind(C, name="RSPOneOperGetExp_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QINT), value, intent(in) :: oper_num_pert
                integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=C_QINT), value, intent(in) :: num_dmat
                type(C_PTR), intent(in) :: dens_mat(num_dmat)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_exp
                real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine RSPOneOperGetExp_f
        end interface
        type(OneOperList_f), pointer :: cur_one_oper !current one-electron operator
        ! inserts the context of callback functions to the tail of the linked list
        if (associated(open_rsp%list_one_oper)) then
            cur_one_oper => open_rsp%list_one_oper
            do while (associated(cur_one_oper%next_one_oper))
                cur_one_oper => cur_one_oper%next_one_oper
            end do
            allocate(cur_one_oper%next_one_oper)
            cur_one_oper => cur_one_oper%next_one_oper
        else
            allocate(open_rsp%list_one_oper)
            cur_one_oper => open_rsp%list_one_oper
        end if
        allocate(cur_one_oper%one_oper_fun)
        nullify(cur_one_oper%next_one_oper)
        ! adds context of callback functions of the new one-electron operator
        call RSPOneOperCreate_f(cur_one_oper%one_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                                           &
                                user_ctx,
#endif
                                get_one_oper_mat,
                                                           &
                                get_one_oper_exp)
        ierr = OpenRSPAddOneOper(open_rsp%c_rsp,
                                                                    &
                                 num_pert_lab,
```

```
pert_labels,
                                                                    &
                                                                    &₹.
                                 pert_max_orders,
                                 c_loc(cur_one_oper%one_oper_fun), &
                                 c_funloc(RSPOneOperGetMat_f),
                                 c_funloc(RSPOneOperGetExp_f))
    end function OpenRSPAddOneOper_f
    function OpenRSPAddTwoOper_f(open_rsp,
                                                   &
                                 num_pert_lab,
                                                   &
                                 pert_labels,
                                 pert_max_orders,
#if defined(OPENRSP_F_USER_CONTEXT)
                                 user_ctx,
                                                   &
#endif
                                 get_two_oper_mat, &
                                 get_two_oper_exp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
        integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_two_oper_mat(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
                                        num_dmat,
                                        dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                          &
                                        user_ctx,
#endif
                                        num_int,
                                        val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_two_oper_mat
            subroutine get_two_oper_exp(oper_num_pert,
                                        oper_pert_labels, &
```

```
oper_pert_orders, &
                                        dmat_len_tuple,
                                        num_LHS_dmat,
                                                          &
                                        LHS_dens_mat,
                                        num_RHS_dmat,
                                        RHS_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                          &
                                        user_ctx,
                                                          &
#endif
                                        num_exp,
                                                          &
                                        val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: dmat_len_tuple
                integer(kind=QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
                type(QcMat), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
                integer(kind=QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
                type(QcMat), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_two_oper_exp
            subroutine RSPTwoOperGetMat_f(oper_num_pert,
                                          oper_pert_labels, &
                                          oper_pert_orders, &
                                          num_dmat,
                                          dens_mat,
                                                            &
                                          user_ctx,
                                          num_int,
                                                            Хr.
                                          val_int)
                                                            &
                bind(C, name="RSPTwoOperGetMat_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QINT), value, intent(in) :: oper_num_pert
                integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=C_QINT), value, intent(in) :: num_dmat
                type(C_PTR), intent(in) :: dens_mat(num_dmat)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_int
                type(C_PTR), intent(inout) :: val_int(num_int)
            end subroutine RSPTwoOperGetMat_f
            subroutine RSPTwoOperGetExp_f(oper_num_pert,
                                          oper_pert_labels, &
                                          oper_pert_orders, &
```

```
dmat_len_tuple,
                                          num_LHS_dmat,
                                                             &
                                          LHS_dens_mat,
                                                             &
                                          num_RHS_dmat,
                                                             &₹.
                                          RHS_dens_mat,
                                          user_ctx,
                                          num_exp,
                                                             lг
                                          val_exp)
                                                             &
                bind(C, name="RSPTwoOperGetExp_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QINT), value, intent(in) :: oper_num_pert
                integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=C_QINT), value, intent(in) :: dmat_len_tuple
                integer(kind=C_QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
                type(C_PTR), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
                integer(kind=C_QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
                type(C_PTR), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_exp
                real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine RSPTwoOperGetExp_f
        end interface
        type(TwoOperList_f), pointer :: cur_two_oper !current two-electron operator
        ! inserts the context of callback functions to the tail of the linked list
        if (associated(open_rsp%list_two_oper)) then
            cur_two_oper => open_rsp%list_two_oper
            do while (associated(cur_two_oper%next_two_oper))
                cur_two_oper => cur_two_oper%next_two_oper
            end do
            allocate(cur_two_oper%next_two_oper)
            cur_two_oper => cur_two_oper%next_two_oper
        else
            allocate(open_rsp%list_two_oper)
            cur_two_oper => open_rsp%list_two_oper
        end if
        allocate(cur_two_oper%two_oper_fun)
        nullify(cur_two_oper%next_two_oper)
        ! adds context of callback functions of the new two-electron operator
        call RSPTwoOperCreate_f(cur_two_oper%two_oper_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,
                                                            Хr.
#endif
                                get_two_oper_mat,
                                get_two_oper_exp)
        ierr = OpenRSPAddTwoOper(open_rsp%c_rsp,
                                                                    Хr.
                                 num_pert_lab,
                                                                    &₹.
                                 pert_labels,
                                                                    &
                                 pert_max_orders,
                                                                    &
                                 c_loc(cur_two_oper%two_oper_fun), &
                                 c_funloc(RSPTwoOperGetMat_f),
```

```
c_funloc(RSPTwoOperGetExp_f))
    end function OpenRSPAddTwoOper_f
    function OpenRSPAddXCFun_f(open_rsp,
                               num_pert_lab,
                                                &
                               pert_labels,
                                                &
                               pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                               user_ctx,
                                                &
#endif
                               get_xc_fun_mat, &
                               get_xc_fun_exp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
        integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_xc_fun_mat(xc_len_tuple,
                                      xc_pert_tuple,
                                      num_freq_configs, &
                                      dmat_num_tuple,
                                      dmat_idx_tuple,
                                                        &
                                      num_dmat,
                                      dens_mat,
                                                        &
#if defined(OPENRSP_F_USER_CONTEXT)
                                                        &
                                      len_ctx,
                                      user_ctx,
                                                        &
#endif
                                      num_int,
                                                        &
                                      val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: xc_len_tuple
                integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=QINT), intent(in) :: num_freq_configs
                integer(kind=QINT), intent(in) :: dmat_num_tuple
                integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_xc_fun_mat
            subroutine get_xc_fun_exp(xc_len_tuple,
                                      xc_pert_tuple,
```

```
num_freq_configs, &
                                      dmat_num_tuple,
                                      dmat_idx_tuple,
                                                        &
                                      num_dmat,
                                                        &
                                      dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                      len_ctx,
                                                        lг
                                      user_ctx,
                                                        &
#endif
                                                        &
                                      num_exp,
                                      val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: xc_len_tuple
                integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=QINT), intent(in) :: num_freq_configs
                integer(kind=QINT), intent(in) :: dmat_num_tuple
                integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_xc_fun_exp
            subroutine RSPXCFunGetMat_f(xc_len_tuple,
                                                          &
                                        xc_pert_tuple,
                                                          &
                                        num_freq_configs, &
                                        dmat_num_tuple,
                                        dmat_idx_tuple,
                                                          &₹.
                                        num_dmat,
                                        dens_mat,
                                                          &
                                                         &
                                        user_ctx,
                                                          &
                                        num_int,
                                        val_int)
                bind(C, name="RSPXCFunGetMat_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
                integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=C_QINT), value, intent(in) :: num_freq_configs
                integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
                integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=C_QINT), value, intent(in) :: num_dmat
                type(C_PTR), intent(in) :: dens_mat(num_dmat)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_int
                type(C_PTR), intent(inout) :: val_int(num_int)
            end subroutine RSPXCFunGetMat_f
            subroutine RSPXCFunGetExp_f(xc_len_tuple,
                                                          &
```

xc_pert_tuple,

&

```
num_freq_configs, &
                                        dmat_num_tuple,
                                        dmat_idx_tuple,
                                        num_dmat,
                                        dens_mat,
                                                         &
                                                         &
                                        user_ctx,
                                                         &
                                        num_exp,
                                        val_exp)
                                                          &
                bind(C, name="RSPXCFunGetExp_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
                integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
                integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=C_QINT), value, intent(in) :: num_freq_configs
                integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
                integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=C_QINT), value, intent(in) :: num_dmat
                type(C_PTR), intent(in) :: dens_mat(num_dmat)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: num_exp
                real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine RSPXCFunGetExp_f
        end interface
        type(XCFunList_f), pointer :: cur_xc_fun !current XC functional
        ! inserts the context of callback functions to the tail of the linked list
        if (associated(open_rsp%list_xc_fun)) then
            cur_xc_fun => open_rsp%list_xc_fun
            do while (associated(cur_xc_fun%next_xc_fun))
                cur_xc_fun => cur_xc_fun%next_xc_fun
            end do
            allocate(cur_xc_fun%next_xc_fun)
            cur_xc_fun => cur_xc_fun%next_xc_fun
        else
            allocate(open_rsp%list_xc_fun)
            cur_xc_fun => open_rsp%list_xc_fun
        end if
        allocate(cur_xc_fun%xcfun_fun)
        nullify(cur_xc_fun%next_xc_fun)
        ! adds context of callback functions of the new XC functional
        call RSPXCFunCreate_f(cur_xc_fun%xcfun_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                              user_ctx,
#endif
                              get_xc_fun_mat,
                              get_xc_fun_exp)
        ierr = OpenRSPAddXCFun(open_rsp%c_rsp,
                               num_pert_lab,
                                                            lг
                               pert_labels,
                                                            &
                               pert_max_orders,
                               c_loc(cur_xc_fun%xcfun_fun), &
                               c_funloc(RSPXCFunGetMat_f),
```

```
c_funloc(RSPXCFunGetExp_f))
    end function OpenRSPAddXCFun_f
    function OpenRSPSetNucHamilton_f(open_rsp,
                                     num_pert_lab,
                                                       &
                                     pert_labels,
                                     pert_max_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                                       &
                                     user_ctx,
#endif
                                     get_nuc_contrib, &
                                     num_atoms) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        integer(kind=QINT), intent(in) :: num_pert_lab
        integer(kind=QcPertInt), intent(in) :: pert_labels(num_pert_lab)
        integer(kind=QINT), intent(in) :: pert_max_orders(num_pert_lab)
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        integer(kind=QINT), intent(in) :: num_atoms
        interface
            subroutine get_nuc_contrib(nuc_num_pert,
                                       nuc_pert_labels, &
                                       nuc_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                       user_ctx,
#endif
                                       size_pert,
                                                         Хr.
                                       val_nuc)
                use qcmatrix_f, only: QINT,QREAL
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: nuc_num_pert
                integer(kind=QcPertInt), intent(in) :: nuc_pert_labels(nuc_num_pert)
                integer(kind=QINT), intent(in) :: nuc_pert_orders(nuc_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: size_pert
                real(kind=QREAL), intent(inout) :: val_nuc(size_pert)
            end subroutine get_nuc_contrib
            subroutine RSPNucHamiltonGetContributions_f(nuc_num_pert,
                                                         nuc_pert_labels, &
                                                         nuc_pert_orders, &
                                                         user_ctx,
                                                         size_pert,
                                                                          &
                                                         val_nuc)
                                                                          &
                bind(C, name="RSPNucHamiltonGetContributions_f")
                use, intrinsic :: iso_c_binding
                use RSPPertBasicTypes_f, only: C_QCPERTINT
```

```
integer(kind=C_QINT), value, intent(in) :: nuc_num_pert
                integer(kind=C_QCPERTINT), intent(in) :: nuc_pert_labels(nuc_num_pert)
                integer(kind=C_QINT), intent(in) :: nuc_pert_orders(nuc_num_pert)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), value, intent(in) :: size_pert
                real(kind=C_QREAL), intent(inout) :: val_nuc(size_pert)
            end subroutine RSPNucHamiltonGetContributions_f
        end interface
        if (associated(open_rsp%nuc_hamilton_fun)) then
            call RSPNucHamiltonDestroy_f(open_rsp%nuc_hamilton_fun)
        else
            allocate(open_rsp%nuc_hamilton_fun)
        end if
        ! adds context of callback function of the nuclear Hamiltonian
        call RSPNucHamiltonCreate_f(open_rsp%nuc_hamilton_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                    user_ctx,
                                                                &
#endif
                                    get_nuc_contrib)
        ierr = OpenRSPSetNucHamilton(open_rsp%c_rsp,
                                                                                  &
                                     num_pert_lab,
                                     pert_labels,
                                                                                  &
                                     pert_max_orders,
                                                                                  &
                                     c_loc(open_rsp%nuc_hamilton_fun),
                                                                                  &
                                     c_funloc(RSPNucHamiltonGetContributions_f), &
                                     num_atoms)
    end function OpenRSPSetNucHamilton_f
    function OpenRSPAssemble_f(open_rsp) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(inout) :: open_rsp
        ierr = OpenRSPAssemble(open_rsp%c_rsp)
    end function OpenRSPAssemble_f
    function OpenRSPWritebyFileName_f(open_rsp, file_name) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(in) :: open_rsp
        character*(*), intent(in) :: file_name
        ierr = OpenRSPWriteFortranAdapter(open_rsp%c_rsp, &
                                          file_name//C_NULL_CHAR)
    end function OpenRSPWritebyFileName_f
    function OpenRSPWritebyUnit_f(open_rsp, io_unit) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(in) :: open_rsp
        integer(kind=4), intent(in) :: io_unit
integer(kind=4), parameter :: MAX_LEN_QCCHAR = 256
integer(kind=4), parameter :: QCSTDOUT = 6
        logical(kind=4) is_opened
        logical(kind=4) is_named
        character(MAX_LEN_QCCHAR) file_name
        if (io_unit==QCSTDOUT) then
```

```
ierr = OpenRSPWriteStdOutFortranAdapter(open_rsp%c_rsp)
        else
            ! gets the file name from its associated logical unit
            inquire(unit=io_unit,
                    opened=is_opened, &
                    named=is_named,
                    name=file_name)
            if (is_opened .and. is_named) then
                if (len_trim(file_name) == MAX_LEN_QCCHAR) then
                    write(QCSTDOUT, 100) "file name too long, increase MAX_LEN_QCCHAR", &
                                        MAX_LEN_QCCHAR
                    call QErrorExit(QCSTDOUT, __LINE__, "OpenRSP.F90")
                else
                    ! writes by file name
                    ierr = OpenRSPWriteFortranAdapter(open_rsp%c_rsp, &
                                                      trim(file_name)//C_NULL_CHAR)
                end if
            else
                write(QCSTDOUT,100) "logical unit is not named and/or opened", &
                                    io_unit
                call QErrorExit(QCSTDOUT, __LINE__, "OpenRSP.F90")
            end if
        end if
        format("OpenRSPWritebyUnit_f>> ",A,I6)
100
    end function OpenRSPWritebyUnit_f
    function OpenRSPGetRSPFun_f(open_rsp,
                                ref_ham,
                                                  &
                                ref_state,
                                                  &
                                ref_overlap,
                                                  &
                                                  &
                                num_props,
                                len_tuple,
                                                  &
                                pert_tuple,
                                num_freq_configs, &
                                pert_freqs,
                                                  &
                                kn_rules,
                                                  &
                                size_rsp_funs,
                                rsp_funs) result(ierr)
        integer(kind=4) :: ierr
        type(OpenRSP), intent(in) :: open_rsp
        type(QcMat), target, intent(in) :: ref_ham
        type(QcMat), target, intent(in) :: ref_state
        type(QcMat), target, intent(in) :: ref_overlap
        integer(kind=QINT), intent(in) :: num_props
        integer(kind=QINT), intent(in) :: len_tuple(num_props)
        integer(kind=QcPertInt), intent(in) :: pert_tuple(sum(len_tuple))
        integer(kind=QINT), intent(in) :: num_freq_configs(num_props)
        real(kind=QREAL), intent(in) :: pert_freqs(2*dot_product(len_tuple,num_freq_configs
        integer(kind=QINT), intent(in) :: kn_rules(num_props)
        integer(kind=QINT), intent(in) :: size_rsp_funs
        real(kind=QREAL), intent(out) :: rsp_funs(2*size_rsp_funs)
        type(C_PTR) c_ref_ham(1)
```

```
type(C_PTR) c_ref_state(1)
    type(C_PTR) c_ref_overlap(1)
    ierr = QcMat_C_LOC((/ref_ham/), c_ref_ham)
    if (ierr==QFAILURE) return
    ierr = QcMat_C_LOC((/ref_state/), c_ref_state)
    if (ierr==QFAILURE) return
    ierr = QcMat_C_LOC((/ref_overlap/), c_ref_overlap)
    if (ierr==QFAILURE) return
    ierr = OpenRSPGetRSPFun(open_rsp%c_rsp,
                                               &
                            c_ref_ham(1),
                            c_ref_state(1),
                            c_ref_overlap(1), &
                            num_props,
                            len_tuple,
                                               &
                            pert_tuple,
                            num_freq_configs,
                            pert_freqs,
                                               &
                            kn_rules,
                            size_rsp_funs,
                                               Źг
                            rsp_funs)
    c_ref_ham(1) = C_NULL_PTR
    c_ref_state(1) = C_NULL_PTR
    c_ref_overlap(1) = C_NULL_PTR
end function OpenRSPGetRSPFun_f
function OpenRSPDestroy_f(open_rsp) result(ierr)
    integer(kind=4) :: ierr
    type(OpenRSP), intent(inout) :: open_rsp
    type(OneOperList_f), pointer :: cur_one_oper
                                                   !current one-electron operator
    type(OneOperList_f), pointer :: next_one_oper !next one-electron operator
    type(TwoOperList_f), pointer :: cur_two_oper
                                                   !current two-electron operator
    type(TwoOperList_f), pointer :: next_two_oper !next two-electron operator
    type(XCFunList_f), pointer :: cur_xc_fun
                                                   !current XC functional
    type(XCFunList_f), pointer :: next_xc_fun
                                                   !next XC functional
    ierr = OpenRSPDestroyFortranAdapter(open_rsp%c_rsp)
    ! cleans up callback subroutine of response equation solver
    if (associated(open_rsp%solver_fun)) then
        call RSPSolverDestroy_f(open_rsp%solver_fun)
        deallocate(open_rsp%solver_fun)
        nullify(open_rsp%solver_fun)
    end if
    ! cleans up callback subroutines of perturbations
    if (associated(open_rsp%pert_fun)) then
        call RSPPertDestroy_f(open_rsp%pert_fun)
        deallocate(open_rsp%pert_fun)
       nullify(open_rsp%pert_fun)
    end if
    ! cleans up callback subroutines of overlap integrals
    if (associated(open_rsp%overlap_fun)) then
        call RSPOverlapDestroy_f(open_rsp%overlap_fun)
        deallocate(open_rsp%overlap_fun)
       nullify(open_rsp%overlap_fun)
```

```
end if
                ! cleans up the linked list of context of callback subroutines of one-electron oper
                cur_one_oper => open_rsp%list_one_oper
                do while (associated(cur_one_oper))
                    next_one_oper => cur_one_oper%next_one_oper
                    if (associated(cur_one_oper%one_oper_fun)) then
                        call RSPOneOperDestroy_f(cur_one_oper%one_oper_fun)
                        deallocate(cur_one_oper%one_oper_fun)
                        nullify(cur_one_oper%one_oper_fun)
                    deallocate(cur_one_oper)
                    nullify(cur_one_oper)
                    cur_one_oper => next_one_oper
                end do
                ! cleans up the linked list of context of callback subroutines of two-electron oper
                cur_two_oper => open_rsp%list_two_oper
                do while (associated(cur_two_oper))
                    next_two_oper => cur_two_oper%next_two_oper
                    if (associated(cur_two_oper%two_oper_fun)) then
                        call RSPTwoOperDestroy_f(cur_two_oper%two_oper_fun)
                        deallocate(cur_two_oper%two_oper_fun)
                        nullify(cur_two_oper%two_oper_fun)
                    end if
                    deallocate(cur_two_oper)
                    nullify(cur_two_oper)
                    cur_two_oper => next_two_oper
                end do
                ! cleans up the linked list of context of callback subroutines of XC functionals
                cur_xc_fun => open_rsp%list_xc_fun
                do while (associated(cur_xc_fun))
                    next_xc_fun => cur_xc_fun%next_xc_fun
                    if (associated(cur_xc_fun%xcfun_fun)) then
                        call RSPXCFunDestroy_f(cur_xc_fun%xcfun_fun)
                        deallocate(cur_xc_fun%xcfun_fun)
                        nullify(cur_xc_fun%xcfun_fun)
                    end if
                    deallocate(cur_xc_fun)
                    nullify(cur_xc_fun)
                    cur_xc_fun => next_xc_fun
                ! cleans up callback subroutine of nuclear Hamiltonian
                if (associated(open_rsp%nuc_hamilton_fun)) then
                    call RSPNucHamiltonDestroy_f(open_rsp%nuc_hamilton_fun)
                    deallocate(open_rsp%nuc_hamilton_fun)
                    nullify(open_rsp%nuc_hamilton_fun)
                end if
            end function OpenRSPDestroy_f
        end module OpenRSP_f
      \langle RSPPertBasicTypes.F90 \ 140 \rangle \equiv
140
        module RSPPertBasicTypes_f
```

```
use, intrinsic :: iso_c_binding
            implicit none
            ! <datatype name='QcPertInt'>
                Data type of integers to represent perturbation labels
            ! </datatype>
            ! <datatype name='C_QCPERTINT'>
                Integers of perturbation labels to interoperates with C code
            ! </datatype>
            ! <constant name='QCPERTINT_MAX'>
                Maximal value of an object of the <QcPertInt> type
            ! </constant>
            !integer(kind=4), parameter, public :: QcPertInt = 8
            !integer, parameter, public :: C_QCPERTINT = C_LONG
            integer(kind=4), parameter, public :: QcPertInt = 4
            integer, parameter, public :: C_QCPERTINT = C_INT
        end module RSPPertBasicTypes_f
141
      \langle RSPPerturbation.F90 \ 141 \rangle \equiv
        ⟨OpenRSPLicenseFortran 115a⟩
        !! 2014-08-18, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        module RSPPerturbation_f
            use, intrinsic :: iso_c_binding
            use qcmatrix_f, only: QINT
            use RSPPertBasicTypes_f, only: QcPertInt, &
                                            C_QCPERTINT
            implicit none
            integer(kind=4), private, parameter :: STDOUT = 6
            ! user specified callback subroutines
            abstract interface
                subroutine GetPertConcatenation_f(pert_label,
                                                   first_cat_comp, &
                                                   num_cat_comps, &
                                                   num_sub_tuples, &
                                                   len_sub_tuples, &
        #if defined(OPENRSP_F_USER_CONTEXT)
                                                   len_ctx,
                                                                    &
                                                   user_ctx,
        #endif
                                                   rank_sub_comps)
                    use qcmatrix_f, only: QINT
```

```
use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QcPertInt), intent(in) :: pert_label
            integer(kind=QINT), intent(in) :: first_cat_comp
            integer(kind=QINT), intent(in) :: num_cat_comps
            integer(kind=QINT), intent(in) :: num_sub_tuples
            integer(kind=QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_comps)
        end subroutine GetPertConcatenation_f
    end interface
    ! context of callback subroutine of response equation solver
   type, public :: PertFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback functions
        procedure(GetPertConcatenation_f), nopass, pointer :: get_pert_concatenation
   end type PertFun_f
   public :: RSPPertCreate_f
   public :: RSPPertGetConcatenation_f
   public :: RSPPertDestroy_f
   contains
    !% \brief creates the context of callback subroutines of perturbations
    ! \author Bin Gao
    ! \date 2014-08-18
    ! \param[PertFun_f:type]{inout} pert_fun the context of callback subroutines
    ! \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine]{in} get_pert_concatenation user specified function for
    ! %
           getting rank of a perturbation
    subroutine RSPPertCreate_f(pert_fun,
#if defined(OPENRSP_F_USER_CONTEXT)
                               user_ctx,
#endif
                               get_pert_concatenation)
        type(PertFun_f), intent(inout) :: pert_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_pert_concatenation(pert_label,
                                              first_cat_comp, &
                                              num_cat_comps, &
```

```
num_sub_tuples, &
                                              len_sub_tuples, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                              len_ctx,
                                              user_ctx,
                                                              &
#endif
                                              rank_sub_comps)
                use qcmatrix_f, only: QINT
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QcPertInt), intent(in) :: pert_label
                integer(kind=QINT), intent(in) :: first_cat_comp
                integer(kind=QINT), intent(in) :: num_cat_comps
                integer(kind=QINT), intent(in) :: num_sub_tuples
                integer(kind=QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_co
            end subroutine get_pert_concatenation
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        pert_fun%len_ctx = size(user_ctx)
        allocate(pert_fun%user_ctx(pert_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A, I8)") "RSPPertCreate_f>> length", pert_fun%len_ctx
            stop "RSPPertCreate_f>> failed to allocate memory for user_ctx"
        end if
        pert_fun%user_ctx = user_ctx
#endif
       pert_fun%get_pert_concatenation => get_pert_concatenation
    end subroutine RSPPertCreate_f
    !% \brief calls Fortran callback subroutine to get the rank of
    !
           a perturbation with its components
    ! \author Bin Gao
    ! \date 2014-08-18
    ! \param[integer]{in} pert_label lable of the perturbation
      \param[integer]{in} pert_num_comp number of components of the perturbation
      \param[integer]{in} pert_components components of the perturbation
      \param[integer]{in} pert_comp_orders orders of the components
    ! \param[C_PTR:type]{in} user_ctx user-defined callback function context
    !% \param[integer]{out} pert_rank the rank of the perturbation
    subroutine RSPPertGetConcatenation_f(pert_label,
                                         first_cat_comp, &
                                         num_cat_comps, &
                                         num_sub_tuples, &
                                         len_sub_tuples, &
                                         user_ctx,
                                         rank_sub_comps) &
        bind(C, name="RSPPertGetConcatenation_f")
```

```
integer(kind=C_QCPERTINT), value, intent(in) :: pert_label
                integer(kind=C_QINT), value, intent(in) :: first_cat_comp
                integer(kind=C_QINT), value, intent(in) :: num_cat_comps
                integer(kind=C_QINT), value, intent(in) :: num_sub_tuples
                integer(kind=C_QINT), intent(in) :: len_sub_tuples(num_sub_tuples)
                type(C_PTR), value, intent(in) :: user_ctx
                integer(kind=C_QINT), intent(out) :: rank_sub_comps(num_sub_tuples*num_cat_comps)
                type(PertFun_f), pointer :: pert_fun !context of callback subroutines
                ! gets the Fortran callback subroutine
                call c_f_pointer(user_ctx, pert_fun)
                ! invokes Fortran callback subroutine to get the rank of the perturbation
                call pert_fun%get_pert_concatenation(pert_label,
                                                                           &
                                                       first_cat_comp,
                                                                           &
                                                       num_cat_comps,
                                                                           &
                                                       num_sub_tuples,
                                                       len_sub_tuples,
        #if defined(OPENRSP_F_USER_CONTEXT)
                                                       pert_fun%len_ctx, &
                                                       pert_fun%user_ctx, &
        #endif
                                                       rank_sub_comps)
                ! cleans up
                nullify(pert_fun)
                return
            \verb"end subroutine RSPPertGetConcatenation_f"
            !% \brief cleans the context of callback subroutines of perturbations
            ! \author Bin Gao
            ! \date 2014-08-18
            !% \param[PertFun_f:type]{inout} pert_fun the context of callback subroutines
            subroutine RSPPertDestroy_f(pert_fun)
                type(PertFun_f), intent(inout) :: pert_fun
        #if defined(OPENRSP_F_USER_CONTEXT)
                pert_fun%len_ctx = 0
                deallocate(pert_fun%user_ctx)
        #endif
                nullify(pert_fun%get_pert_concatenation)
            end subroutine RSPPertDestroy_f
        end module RSPPerturbation_f
      \langle RSPOverlap.F90 \ 144 \rangle \equiv
144
        \langle OpenRSPLicenseFortran\ 115a \rangle
        !! 2014-08-05, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        #define OPENRSP_API_SRC "src/fortran/RSPOverlap.F90"
```

module RSPOverlap_f

```
use, intrinsic :: iso_c_binding
   use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
   use RSPPertBasicTypes_f, only: QcPertInt, &
                                   C_QCPERTINT
   implicit none
   integer(kind=4), private, parameter :: STDOUT = 6
    ! user specified callback subroutines
   abstract interface
        subroutine OverlapGetMat_f(bra_num_pert,
                                                     &
                                   bra_pert_labels,
                                                     &
                                   bra_pert_orders,
                                   ket_num_pert,
                                   ket_pert_labels, &
                                   ket_pert_orders, &
                                   oper_num_pert,
                                   oper_pert_labels, &
                                   oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx,
                                                     &
                                   user_ctx,
                                                     &
#endif
                                   num_int,
                                   val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: bra_num_pert
            integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
            integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
            integer(kind=QINT), intent(in) :: ket_num_pert
            integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
            integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int
            type(QcMat), intent(inout) :: val_int(num_int)
        end subroutine OverlapGetMat_f
        subroutine OverlapGetExp_f(bra_num_pert,
                                                     &
                                   bra_pert_labels, &
                                   bra_pert_orders, &
                                   ket_num_pert,
                                                     &
                                   ket_pert_labels, &
                                   ket_pert_orders, &
```

```
oper_num_pert,
                                   oper_pert_labels, &
                                   oper_pert_orders, &
                                   num_dmat,
                                   dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx,
                                                     &
                                   user_ctx,
#endif
                                                     &
                                   num_exp,
                                   val_exp)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: bra_num_pert
            integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
            integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
            integer(kind=QINT), intent(in) :: ket_num_pert
            integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
            integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_exp
           real(kind=QREAL), intent(inout) :: val_exp(num_exp)
        end subroutine OverlapGetExp_f
   end interface
    ! context of callback subroutines of overlap integrals
   type, public :: OverlapFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback functions
       procedure(OverlapGetMat_f), nopass, pointer :: get_overlap_mat
        procedure(OverlapGetExp_f), nopass, pointer :: get_overlap_exp
    end type OverlapFun_f
   public :: RSPOverlapCreate_f
   public :: RSPOverlapGetMat_f
   public :: RSPOverlapGetExp_f
   public :: RSPOverlapDestroy_f
    contains
```

```
!% \brief creates the context of callback subroutines of overlap integrals
    ! \author Bin Gao
    ! \date 2014-08-05
    ! \param[OverlapFun_f:type]{inout} overlap_fun the context of callback subroutines
    ! \param[character]{in} user_ctx user-defined callback function context
     \param[subroutine]{in} get_overlap_mat user specified function for
           getting integral matrices
    ! \param[subroutine]{in} get_overlap_exp user specified function for
           getting expectation values
    subroutine RSPOverlapCreate_f(overlap_fun,
#if defined(OPENRSP_F_USER_CONTEXT)
                                                   &
                                  user_ctx,
#endif
                                  get_overlap_mat, &
                                  get_overlap_exp)
        type(OverlapFun_f), intent(inout) :: overlap_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_overlap_mat(bra_num_pert,
                                       bra_pert_labels,
                                       bra_pert_orders,
                                       ket_num_pert,
                                       ket_pert_labels, &
                                       ket_pert_orders,
                                       oper_num_pert,
                                       oper_pert_labels, &
                                       oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                                         &
                                       user_ctx,
#endif
                                       num_int,
                                                         &
                                       val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: bra_num_pert
                integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
                integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
                integer(kind=QINT), intent(in) :: ket_num_pert
                integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
                integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
```

```
type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_overlap_mat
            subroutine get_overlap_exp(bra_num_pert,
                                                         &
                                       bra_pert_labels, &
                                       bra_pert_orders, &
                                       ket_num_pert,
                                       ket_pert_labels, &
                                       ket_pert_orders, &
                                       oper_num_pert,
                                       oper_pert_labels, &
                                       oper_pert_orders, &
                                       num_dmat,
                                       dens_mat,
                                                         &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                       user_ctx,
#endif
                                                         &
                                       num_exp,
                                       val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: bra_num_pert
                integer(kind=QcPertInt), intent(in) :: bra_pert_labels(bra_num_pert)
                integer(kind=QINT), intent(in) :: bra_pert_orders(bra_num_pert)
                integer(kind=QINT), intent(in) :: ket_num_pert
                integer(kind=QcPertInt), intent(in) :: ket_pert_labels(ket_num_pert)
                integer(kind=QINT), intent(in) :: ket_pert_orders(ket_num_pert)
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_overlap_exp
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        overlap_fun%len_ctx = size(user_ctx)
        allocate(overlap_fun%user_ctx(overlap_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A, I8)") "RSPOverlapCreate_f>> length", overlap_fun%len_ctx
            stop "RSPOverlapCreate_f>> failed to allocate memory for user_ctx"
        overlap_fun%user_ctx = user_ctx
#endif
        overlap_fun%get_overlap_mat => get_overlap_mat
        overlap_fun%get_overlap_exp => get_overlap_exp
```

$\verb"end subroutine RSPOverlapCreate_f"$

```
!% \brief calls Fortran callback subroutine to get integral matrices of overlap integra
! \author Bin Gao
! \date 2014-08-05
 \param[integer]{in} bra_len_tuple length of the perturbation tuple on the bra
  \param[integer]{in} bra_pert_tuple perturbation tuple on the bra
  \param[integer]{in} ket_len_tuple length of the perturbation tuple on the ket
  \param[integer]{in} ket_pert_tuple perturbation tuple on the ket
! \param[integer]{in} len_tuple length of perturbation tuple on the overlap integrals
  \param[integer]{in} pert_tuple perturbation tuple on the overlap integrals
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
  \param[integer]{in} num_int number of the integral matrices
!% \param[C_PTR:type]{inout} val_int the integral matrices
subroutine RSPOverlapGetMat_f(bra_num_pert,
                             bra_pert_labels,
                             bra_pert_orders, &
                             ket_num_pert,
                             ket_pert_labels, &
                             ket_pert_orders,
                             oper_num_pert,
                             oper_pert_labels, &
                             oper_pert_orders, &
                             user_ctx,
                                               &
                             num_int,
                             val_int)
                                               &
   bind(C, name="RSPOverlapGetMat_f")
   integer(kind=C_QINT), value, intent(in) :: bra_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
   integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
   integer(kind=C_QINT), value, intent(in) :: ket_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
   integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
   integer(kind=C_QINT), value, intent(in) :: oper_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
   integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
   type(C_PTR), value, intent(in) :: user_ctx
   integer(kind=C_QINT), value, intent(in) :: num_int
   type(C_PTR), intent(inout) :: val_int(num_int)
   type(OverlapFun_f), pointer :: overlap_fun !context of callback subroutines
   type(QcMat), allocatable :: f_val_int(:) !integral matrices
   integer(kind=4) ierr
                                                !error information
   ! converts C pointer to Fortran QcMat type
   allocate(f_val_int(num_int), stat=ierr)
   if (ierr/=0) then
       write(STDOUT,"(A,I8)") "RSPOverlapGetMat_f>> num_int", num_int
       stop "RSPOverlapGetMat_f>> failed to allocate memory for f_val_int"
   ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
   call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
   ! gets the Fortran callback subroutine
   call c_f_pointer(user_ctx, overlap_fun)
```

```
! invokes Fortran callback subroutine to calculate the integral matrices
        call overlap_fun%get_overlap_mat(bra_num_pert,
                                                               Źг
                                        bra_pert_labels,
                                                               &
                                        bra_pert_orders,
                                                              &
                                        ket_num_pert,
                                        ket_pert_labels,
                                                              &
                                        ket_pert_orders,
                                                              &
                                        oper_num_pert,
                                        oper_pert_labels,
                                                               &
                                        oper_pert_orders,
#if defined(OPENRSP_F_USER_CONTEXT)
                                        overlap_fun%len_ctx,
                                        overlap_fun%user_ctx, &
#endif
                                        num_int,
                                        f_val_int)
        ! cleans up
       nullify(overlap_fun)
        ierr = QcMat_C_NULL_PTR(A=f_val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_val_int)
    end subroutine RSPOverlapGetMat_f
    !% \brief calls Fortran callback subroutine to get expectation values of overlap integr
    ! \author Bin Gao
      \date 2014-08-05
    ! \param[integer]{in} bra_len_tuple length of the perturbation tuple on the bra
      \param[integer]{in} bra_pert_tuple perturbation tuple on the bra
      \param[integer]{in} ket_len_tuple length of the perturbation tuple on the ket
      \param[integer]{in} ket_pert_tuple perturbation tuple on the ket
      \param[integer]{in} len_tuple length of perturbation tuple on the overlap integrals
    ! \param[integer]{in} pert_tuple perturbation tuple on the overlap integrals
    ! \param[integer]{in} num_dmat number of atomic orbital (AO) based density matrices
    ! \param[C_PTR:type]{inout} dens_mat the AO based density matrices
      \param[C_PTR:type]{in} user_ctx user-defined callback function context
      \param[integer]{in} num_exp number of expectation values
    !% \param[real]{out} val_exp the expectation values
    subroutine RSPOverlapGetExp_f(bra_num_pert,
                                  bra_pert_labels,
                                  bra_pert_orders,
                                  ket_num_pert,
                                  ket_pert_labels, &
                                 ket_pert_orders, &
                                  oper_num_pert,
                                  oper_pert_labels, &
                                  oper_pert_orders, &
                                  num_dmat,
                                  dens_mat,
                                                   &
                                                   &
                                  user_ctx,
                                  num_exp,
                                                    &
                                  val_exp)
        bind(C, name="RSPOverlapGetExp_f")
```

```
integer(kind=C_QINT), value, intent(in) :: bra_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: bra_pert_labels(bra_num_pert)
        integer(kind=C_QINT), intent(in) :: bra_pert_orders(bra_num_pert)
        integer(kind=C_QINT), value, intent(in) :: ket_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: ket_pert_labels(ket_num_pert)
        integer(kind=C_QINT), intent(in) :: ket_pert_orders(ket_num_pert)
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(C_QREAL), intent(inout) :: val_exp(num_exp)
        type(OverlapFun_f), pointer :: overlap_fun !context of callback subroutines
        type(QcMat), allocatable :: f_dens_mat(:)    !AO based density matrices
        integer(kind=4) ierr
                                                    !error information
        ! converts C pointer to Fortran QcMat type
        allocate(f_dens_mat(num_dmat), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPOverlapGetExp_f>> num_dmat", num_dmat
            stop "RSPOverlapGetExp_f>> failed to allocate memory for f_dens_mat"
        ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, overlap_fun)
        ! invokes Fortran callback subroutine to calculate the expectation values
        call overlap_fun%get_overlap_exp(bra_num_pert,
                                                               &
                                         bra_pert_labels,
                                                               &
                                                               &
                                         bra_pert_orders,
                                         ket_num_pert,
                                         ket_pert_labels,
                                         ket_pert_orders,
                                                               &
                                         oper_num_pert,
                                         oper_pert_labels,
                                         oper_pert_orders,
                                                               &
                                         num_dmat,
                                                               &
                                         f_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                         overlap_fun%len_ctx,
                                         overlap_fun%user_ctx, &
#endif
                                         num_exp,
                                         val_exp)
        ! cleans up
        nullify(overlap_fun)
        ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_dens_mat)
        return
    end subroutine RSPOverlapGetExp_f
```

```
!% \brief cleans the context of callback subroutines of overlap integrals
            ! \author Bin Gao
            ! \date 2014-08-05
            !% \param[OverlapFun_f:type]{inout} overlap_fun the context of callback subroutines
            subroutine RSPOverlapDestroy_f(overlap_fun)
                type(OverlapFun_f), intent(inout) :: overlap_fun
        #if defined(OPENRSP_F_USER_CONTEXT)
                overlap_fun%len_ctx = 0
                deallocate(overlap_fun%user_ctx)
        #endif
                nullify(overlap_fun%get_overlap_mat)
                nullify(overlap_fun%get_overlap_exp)
            end subroutine RSPOverlapDestroy_f
        end module RSPOverlap_f
        #undef OPENRSP_API_SRC
152
      \langle RSPOneOper.F90 \ 152 \rangle \equiv
        ⟨OpenRSPLicenseFortran 115a⟩
            2014-08-02, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        #define OPENRSP_API_SRC "src/fortran/RSPOneOper.F90"
        module RSPOneOper_f
            use, intrinsic :: iso_c_binding
            use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
            use RSPPertBasicTypes_f, only: QcPertInt, &
                                            C_QCPERTINT
            implicit none
            integer(kind=4), private, parameter :: STDOUT = 6
            ! user specified callback subroutines
            abstract interface
                subroutine OneOperGetMat_f(oper_num_pert,
                                            oper_pert_labels, &
                                            oper_pert_orders, &
        #if defined(OPENRSP_F_USER_CONTEXT)
                                                               &
                                            len_ctx,
                                            user_ctx,
                                                               &
        #endif
                                            num_int,
                                                               &
                                            val_int)
```

```
use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int
            type(QcMat), intent(inout) :: val_int(num_int)
        end subroutine OneOperGetMat_f
        subroutine OneOperGetExp_f(oper_num_pert,
                                   oper_pert_labels, &
                                   oper_pert_orders, &
                                   num_dmat,
                                   dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                   len_ctx,
                                                     &
                                   user_ctx,
                                                     &
#endif
                                   num_exp,
                                                     &
                                   val_exp)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_exp
           real(kind=QREAL), intent(inout) :: val_exp(num_exp)
        end subroutine OneOperGetExp_f
   end interface
    ! context of callback subroutines of one-electron operator
   type, public :: OneOperFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback functions
        procedure(OneOperGetMat_f), nopass, pointer :: get_one_oper_mat
        procedure(OneOperGetExp_f), nopass, pointer :: get_one_oper_exp
    end type OneOperFun_f
```

```
154
```

```
public :: RSPOneOperCreate_f
    public :: RSPOneOperGetMat_f
   public :: RSPOneOperGetExp_f
   public :: RSPOneOperDestroy_f
    contains
    !\% \brief creates the context of callback subroutines of one-electron operator
    ! \author Bin Gao
    ! \date 2014-08-03
      \param[OneOperFun_f:type]{inout} one_oper_fun the context of callback subroutines
      \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine] {in} get_one_oper_mat user specified function for
           getting integral matrices
       \param[subroutine]{in} get_one_oper_exp user specified function for
    ! %
           getting expectation values
    subroutine RSPOneOperCreate_f(one_oper_fun,
#if defined(OPENRSP_F_USER_CONTEXT)
                                                    lг
                                  user_ctx,
#endif
                                  get_one_oper_mat, &
                                  get_one_oper_exp)
        type(OneOperFun_f), intent(inout) :: one_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_one_oper_mat(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                           &
                                        user_ctx,
#endif
                                        num_int,
                                                          &
                                        val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_one_oper_mat
            subroutine get_one_oper_exp(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
                                        num_dmat,
```

```
dens_mat,
                                                          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                          &
                                        user_ctx,
#endif
                                                          &
                                        num_exp,
                                        val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_one_oper_exp
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        one_oper_fun%len_ctx = size(user_ctx)
        allocate(one_oper_fun%user_ctx(one_oper_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A, 18)") "RSPOneOperCreate_f>> length", one_oper_fun%len_ctx
            stop "RSPOneOperCreate_f>> failed to allocate memory for user_ctx"
        end if
        one_oper_fun%user_ctx = user_ctx
#endif
        one_oper_fun%get_one_oper_mat => get_one_oper_mat
        one_oper_fun%get_one_oper_exp => get_one_oper_exp
   end subroutine RSPOneOperCreate_f
    !% \brief calls Fortran callback subroutine to get integral matrices of
           a one-electron operator
    ! \author Bin Gao
      \date 2014-08-02
    ! \param[integer]{in} len_tuple length of perturbation tuple on the one-electron opera
    ! \param[integer]{in} pert_tuple perturbation tuple on the one-electron operator
    ! \param[C_PTR:type]{in} user_ctx user-defined callback function context
      \param[integer]{in} num_int number of the integral matrices
    !% \param[C_PTR:type]{inout} val_int the integral matrices
    subroutine RSPOneOperGetMat_f(oper_num_pert,
                                  oper_pert_labels, &
                                  oper_pert_orders, &
                                  user_ctx,
                                  num_int,
                                                    &
                                  val_int)
        bind(C, name="RSPOneOperGetMat_f")
```

```
integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_int
        type(C_PTR), intent(inout) :: val_int(num_int)
        type(OneOperFun_f), pointer :: one_oper_fun !context of callback subroutines
        type(QcMat), allocatable :: f_val_int(:) !integral matrices
        integer(kind=4) ierr
                                                     !error information
        ! converts C pointer to Fortran QcMat type
        allocate(f_val_int(num_int), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPOneOperGetMat_f>> num_int", num_int
            stop "RSPOneOperGetMat_f>> failed to allocate memory for f_val_int"
        ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, one_oper_fun)
        ! invokes Fortran callback subroutine to calculate the integral matrices
        call one_oper_fun%get_one_oper_mat(oper_num_pert,
                                           oper_pert_labels,
                                           oper_pert_orders,
#if defined(OPENRSP_F_USER_CONTEXT)
                                           one_oper_fun%len_ctx,
                                           one_oper_fun%user_ctx, &
#endif
                                           num_int,
                                                                  &
                                           f_val_int)
        ! cleans up
       nullify(one_oper_fun)
        ierr = QcMat_C_NULL_PTR(A=f_val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_val_int)
   end subroutine RSPOneOperGetMat_f
    !% \brief calls Fortran callback subroutine to get expectation values of
           a one-electron operator
    ! \author Bin Gao
      \date 2014-08-02
      \param[integer]{in} len_tuple length of perturbation tuple on the one-electron opera
      \param[integer]{in} pert_tuple perturbation tuple on the one-electron operator
    ! \param[integer]{in} num_dmat number of atomic orbital (AO) based density matrices
    ! \param[C_PTR:type]{inout} dens_mat the AO based density matrices
      \verb|\param[C_PTR:type]{in}| user\_ctx user-defined callback function context|
    ! \param[integer]{in} num_exp number of expectation values
    !% \param[real]{out} val_exp the expectation values
    subroutine RSPOneOperGetExp_f(oper_num_pert,
                                  oper_pert_labels, &
                                  oper_pert_orders, &
                                  num_dmat,
                                  dens_mat,
                                                    &
```

```
&
                                  user_ctx,
                                  num_exp,
                                                    lг
                                  val_exp)
                                                    Źг
        bind(C, name="RSPOneOperGetExp_f")
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
        type(OneOperFun_f), pointer :: one_oper_fun !context of callback subroutines
        type(QcMat), allocatable :: f_dens_mat(:)
                                                      !AO based density matrices
        integer(kind=4) ierr
                                                     !error information
        ! converts C pointer to Fortran QcMat type
        allocate(f_dens_mat(num_dmat), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPOneOperGetExp_f>> num_dmat", num_dmat
            stop "RSPOneOperGetExp_f>> failed to allocate memory for f_dens_mat"
        end if
        ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, one_oper_fun)
        ! invokes Fortran callback subroutine to calculate the expectation values
        call one_oper_fun%get_one_oper_exp(oper_num_pert,
                                           oper_pert_labels,
                                                                   &
                                           oper_pert_orders,
                                                                   &
                                           num_dmat,
                                           f_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                           one_oper_fun%len_ctx,
                                           one_oper_fun%user_ctx, &
#endif
                                                                   &
                                           num_exp,
                                           val_exp)
        ! cleans up
        nullify(one_oper_fun)
        ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_dens_mat)
        return
   end subroutine RSPOneOperGetExp_f
    !\% \brief cleans the context of callback subroutines of one-electron operator
    ! \author Bin Gao
    ! \date 2014-08-03
    !% \param[OneOperFun_f:type]{inout} one_oper_fun the context of callback subroutines
    subroutine RSPOneOperDestroy_f(one_oper_fun)
        type(OneOperFun_f), intent(inout) :: one_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
```

```
one_oper_fun%len_ctx = 0
                deallocate(one_oper_fun%user_ctx)
        #endif
                nullify(one_oper_fun%get_one_oper_mat)
                nullify(one_oper_fun%get_one_oper_exp)
            end subroutine RSPOneOperDestroy_f
        end module RSPOneOper_f
        #undef OPENRSP_API_SRC
      \langle RSPTwoper.F90 \ 158 \rangle \equiv
158
        ⟨OpenRSPLicenseFortran 115a⟩
        !! 2014-08-06, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        #define OPENRSP_API_SRC "src/fortran/RSPTwoOper.F90"
        module RSPTwoOper_f
            use, intrinsic :: iso_c_binding
            use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
            use RSPPertBasicTypes_f, only: QcPertInt, &
                                            C_QCPERTINT
            implicit none
            integer(kind=4), private, parameter :: STDOUT = 6
            ! user specified callback subroutines
            abstract interface
                subroutine TwoOperGetMat_f(oper_num_pert,
                                            oper_pert_labels, &
                                            oper_pert_orders, &
                                            num_dmat,
                                            dens_mat,
        #if defined(OPENRSP_F_USER_CONTEXT)
                                            len_ctx,
                                            user_ctx,
                                                               &
        #endif
                                                               &
                                            num_int,
                                            val_int)
                    use qcmatrix_f, only: QINT,QREAL,QcMat
                    use RSPPertBasicTypes_f, only: QcPertInt
                    integer(kind=QINT), intent(in) :: oper_num_pert
                    integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                    integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                    integer(kind=QINT), intent(in) :: num_dmat
```

```
type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int
           type(QcMat), intent(inout) :: val_int(num_int)
        end subroutine TwoOperGetMat_f
        subroutine TwoOperGetExp_f(oper_num_pert,
                                   oper_pert_labels, &
                                   oper_pert_orders, &
                                   dmat_len_tuple,
                                   num_LHS_dmat,
                                                     &
                                   LHS_dens_mat,
                                                     &
                                   num_RHS_dmat,
                                   RHS_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                                     &
                                   len_ctx,
                                                     &r.
                                   user_ctx,
#endif
                                   num_exp,
                                   val_exp)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: oper_num_pert
            integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
            integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
            integer(kind=QINT), intent(in) :: dmat_len_tuple
            integer(kind=QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
            type(QcMat), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
            integer(kind=QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
            type(QcMat), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_exp
            real(kind=QREAL), intent(inout) :: val_exp(num_exp)
        end subroutine TwoOperGetExp_f
   end interface
    ! context of callback subroutines of two-electron operator
   type, public :: TwoOperFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback functions
       procedure(TwoOperGetMat_f), nopass, pointer :: get_two_oper_mat
        procedure(TwoOperGetExp_f), nopass, pointer :: get_two_oper_exp
```

```
end type TwoOperFun_f
   public :: RSPTwoOperCreate_f
   public :: RSPTwoOperGetMat_f
   public :: RSPTwoOperGetExp_f
   public :: RSPTwoOperDestroy_f
   contains
    !% \brief creates the context of callback subroutines of two-electron operator
    ! \author Bin Gao
     \date 2014-08-06
    ! \param[TwoOperFun_f:type]{inout} two_oper_fun the context of callback subroutines
    ! \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine] {in} get_two_oper_mat user specified function for
           getting integral matrices
    ! \param[subroutine]{in} get_two_oper_exp user specified function for
           getting expectation values
    ! %
    subroutine RSPTwoOperCreate_f(two_oper_fun,
#if defined(OPENRSP_F_USER_CONTEXT)
                                  user_ctx,
#endif
                                  get_two_oper_mat, &
                                  get_two_oper_exp)
        type(TwoOperFun_f), intent(inout) :: two_oper_fun
#if defined(OPENRSP_F_USER_CONTEXT)
       character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_two_oper_mat(oper_num_pert,
                                        oper_pert_labels, &
                                        oper_pert_orders, &
                                        num_dmat,
                                        dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                          &
                                        user_ctx,
#endif
                                                          &
                                        num_int,
                                        val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
```

```
type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_two_oper_mat
            subroutine get_two_oper_exp(oper_num_pert,
                                                          &
                                        oper_pert_labels, &
                                        oper_pert_orders, &
                                        dmat_len_tuple,
                                        num_LHS_dmat,
                                        LHS_dens_mat,
                                                          &
                                        num_RHS_dmat,
                                                          &
                                        RHS_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                        len_ctx,
                                                          &
                                        user_ctx,
#endif
                                        num_exp,
                                        val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: oper_num_pert
                integer(kind=QcPertInt), intent(in) :: oper_pert_labels(oper_num_pert)
                integer(kind=QINT), intent(in) :: oper_pert_orders(oper_num_pert)
                integer(kind=QINT), intent(in) :: dmat_len_tuple
                integer(kind=QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
                type(QcMat), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
                integer(kind=QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
                type(QcMat), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_two_oper_exp
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        two_oper_fun%len_ctx = size(user_ctx)
        allocate(two_oper_fun%user_ctx(two_oper_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A, I8)") "RSPTwoOperCreate_f>> length", two_oper_fun%len_ctx
            stop "RSPTwoOperCreate_f>> failed to allocate memory for user_ctx"
        end if
        two_oper_fun%user_ctx = user_ctx
#endif
        two_oper_fun%get_two_oper_mat => get_two_oper_mat
        two_oper_fun%get_two_oper_exp => get_two_oper_exp
   end subroutine RSPTwoOperCreate_f
    !% \brief calls Fortran callback subroutine to get integral matrices of
           a two-electron operator
    ! \author Bin Gao
    ! \date 2014-08-06
```

```
! \param[integer]{in} len_tuple length of perturbation tuple on the two-electron opera
! \param[integer]{in} pert_tuple perturbation tuple on the two-electron operator
! \param[integer]{in} num_dmat number of AO based density matrices
! \param[C_PTR:type]{in} dens_mat the AO based density matrices
! \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[integer]{in} num_int number of the integral matrices
!% \param[C_PTR:type]{inout} val_int the integral matrices
subroutine RSPTwoOperGetMat_f(oper_num_pert,
                              oper_pert_labels, &
                              oper_pert_orders, &
                              num_dmat,
                              dens_mat,
                                              &
                              user_ctx,
                                               &
                              num_int,
                              val_int)
   bind(C, name="RSPTwoOperGetMat_f")
   integer(kind=C_QINT), value, intent(in) :: oper_num_pert
   integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
   integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
   integer(kind=C_QINT), value, intent(in) :: num_dmat
   type(C_PTR), intent(in) :: dens_mat(num_dmat)
   type(C_PTR), value, intent(in) :: user_ctx
   integer(kind=C_QINT), value, intent(in) :: num_int
   type(C_PTR), intent(inout) :: val_int(num_int)
   type(TwoOperFun_f), pointer :: two_oper_fun !context of callback subroutines
   type(QcMat), allocatable :: f_dens_mat(:)
                                                !AO based density matrices
   type(QcMat), allocatable :: f_val_int(:)
                                                 !integral matrices
   integer(kind=4) ierr
                                                 !error information
   ! converts C pointer to Fortran QcMat type
   allocate(f_dens_mat(num_dmat), stat=ierr)
   if (ierr/=0) then
       write(STDOUT,"(A,I8)") "RSPTwoOperGetMat_f>> num_dmat", num_dmat
        stop "RSPTwoOperGetMat_f>> failed to allocate memory for f_dens_mat"
   end if
   ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
   call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
   allocate(f_val_int(num_int), stat=ierr)
   if (ierr/=0) then
       write(STDOUT,"(A,I8)") "RSPTwoOperGetMat_f>> num_int", num_int
        stop "RSPTwoOperGetMat_f>> failed to allocate memory for f_val_int"
   end if
   ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
   call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
   ! gets the Fortran callback subroutine
   call c_f_pointer(user_ctx, two_oper_fun)
   ! invokes Fortran callback subroutine to calculate the integral matrices
   call two_oper_fun%get_two_oper_mat(oper_num_pert,
                                      oper_pert_labels,
                                                              &
                                       oper_pert_orders,
                                                             &
                                       num_dmat,
                                                              &
                                       f_dens_mat,
```

```
two_oper_fun%len_ctx,
                                           two_oper_fun%user_ctx, &
#endif
                                           num_int,
                                           f_val_int)
        ! cleans up
       nullify(two_oper_fun)
        ierr = QcMat_C_NULL_PTR(A=f_val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_val_int)
        deallocate(f_dens_mat)
    end subroutine RSPTwoOperGetMat_f
    !% \brief calls Fortran callback subroutine to get expectation values of
           a two-electron operator
      \author Bin Gao
    !
      \date 2014-08-06
      \param[integer]{in} len_tuple length of perturbation tuple on the two-electron opera
      \param[integer]{in} pert_tuple perturbation tuple on the two-electron operator
       \param[integer]{in} dmat_len_tuple length of different perturbation tuples
           of the left-hand-side (LHS) and right-hand-side (RHS) AO based density
    Ţ
           matrices passed
    Ţ
       \param[integer]{in} num_LHS_dmat number of LHS AO based density matrices
           passed for each LHS density matrix perturbation tuple
    ļ
       \param[C_PTR:type]{in} LHS_dens_mat the LHS AO based density matrices
      \param[integer]{in} num_RHS_dmat number of RHS AO based density matrices
           passed for each RHS density matrix perturbation tuple
      \param[C_PTR:type]{in} RHS_dens_mat the RHS AO based density matrices
      \param[C_PTR:type]{in} user_ctx user-defined callback function context
       \param[integer]{in} num_exp number of expectation values
    !% \param[real]{out} val_exp the expectation values
    subroutine RSPTwoOperGetExp_f(oper_num_pert,
                                  oper_pert_labels, &
                                  oper_pert_orders, &
                                  dmat_len_tuple,
                                  num_LHS_dmat,
                                  LHS_dens_mat,
                                  num_RHS_dmat,
                                  RHS_dens_mat,
                                  user_ctx,
                                                    &
                                                    &
                                  num_exp,
                                  val_exp)
                                                    &
        bind(C, name="RSPTwoOperGetExp_f")
        integer(kind=C_QINT), value, intent(in) :: oper_num_pert
        integer(kind=C_QCPERTINT), intent(in) :: oper_pert_labels(oper_num_pert)
        integer(kind=C_QINT), intent(in) :: oper_pert_orders(oper_num_pert)
        integer(kind=C_QINT), value, intent(in) :: dmat_len_tuple
        integer(kind=C_QINT), intent(in) :: num_LHS_dmat(dmat_len_tuple)
        type(C_PTR), intent(in) :: LHS_dens_mat(sum(num_LHS_dmat))
        integer(kind=C_QINT), intent(in) :: num_RHS_dmat(dmat_len_tuple)
```

```
type(C_PTR), intent(in) :: RHS_dens_mat(sum(num_RHS_dmat))
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
        type(TwoOperFun_f), pointer :: two_oper_fun    !context of callback subroutines
        type(QcMat), allocatable :: f_LHS_dens_mat(:) !LHS AO based density matrices
        type(QcMat), allocatable :: f_RHS_dens_mat(:) !RHS AO based density matrices
        integer(kind=4) ierr
                                                       !error information
        ! converts C pointer to Fortran QcMat type
        allocate(f_LHS_dens_mat(sum(num_LHS_dmat)), stat=ierr)
        if (ierr/=0) then
           write(STDOUT,"(A,18)") "RSPTwoOperGetExp_f>> sum(num_LHS_dmat)", &
                                   sum(num_LHS_dmat)
            stop "RSPTwoOperGetExp_f>> failed to allocate memory for f_LHS_dens_mat"
        end if
        ierr = QcMat_C_F_POINTER(A=f_LHS_dens_mat, c_A=LHS_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        allocate(f_RHS_dens_mat(sum(num_RHS_dmat)), stat=ierr)
        if (ierr/=0) then
           write(STDOUT,"(A,18)") "RSPTwoOperGetExp_f>> sum(num_RHS_dmat)", &
                                   sum(num_RHS_dmat)
            stop "RSPTwoOperGetExp_f>> failed to allocate memory for f_RHS_dens_mat"
        end if
        ierr = QcMat_C_F_POINTER(A=f_RHS_dens_mat, c_A=RHS_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, two_oper_fun)
        ! invokes Fortran callback subroutine to calculate the expectation values
        call two_oper_fun%get_two_oper_exp(oper_num_pert,
                                           oper_pert_labels,
                                                                  &
                                           oper_pert_orders,
                                           dmat_len_tuple,
                                                                  &
                                           num_LHS_dmat,
                                           f_LHS_dens_mat,
                                           num_RHS_dmat,
                                           f_RHS_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                           two_oper_fun%len_ctx,
                                           two_oper_fun%user_ctx, &
#endif
                                           num_exp,
                                                                   &
                                           val_exp)
        ! cleans up
        nullify(two_oper_fun)
        ierr = QcMat_C_NULL_PTR(A=f_RHS_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ierr = QcMat_C_NULL_PTR(A=f_LHS_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_RHS_dens_mat)
        deallocate(f_LHS_dens_mat)
    end subroutine RSPTwoOperGetExp_f
```

```
!% \brief cleans the context of callback subroutines of two-electron operator
            ! \author Bin Gao
            ! \date 2014-08-06
            !% \param[TwoOperFun_f:type]{inout} two_oper_fun the context of callback subroutines
            subroutine RSPTwoOperDestroy_f(two_oper_fun)
                type(TwoOperFun_f), intent(inout) :: two_oper_fun
        #if defined(OPENRSP_F_USER_CONTEXT)
                two_oper_fun%len_ctx = 0
                deallocate(two_oper_fun%user_ctx)
        #endif
                nullify(two_oper_fun%get_two_oper_mat)
                nullify(two_oper_fun%get_two_oper_exp)
            end subroutine RSPTwoOperDestroy_f
        end module RSPTwoOper_f
        #undef OPENRSP_API_SRC
165
      \langle RSPXCFun.F90 \ 165 \rangle \equiv
        ⟨OpenRSPLicenseFortran 115a⟩
            2015-06-23, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        #define OPENRSP_API_SRC "src/fortran/RSPXCFun.F90"
        module RSPXCFun_f
            use, intrinsic :: iso_c_binding
            use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
            use RSPPertBasicTypes_f, only: QcPertInt, &
                                            C_QCPERTINT
            implicit none
            integer(kind=4), private, parameter :: STDOUT = 6
            ! user specified callback subroutines
            abstract interface
                subroutine XCFunGetMat_f(xc_len_tuple,
                                                             &
                                          xc_pert_tuple,
                                                             &
                                          num_freq_configs, &
                                          dmat_num_tuple,
                                          dmat_idx_tuple,
                                                             &
                                          num_dmat,
                                                             &
                                          dens_mat,
                                                             &
        #if defined(OPENRSP_F_USER_CONTEXT)
                                          len_ctx,
                                                             &
```

```
&
                                 user_ctx,
#endif
                                 num_int,
                                                   &
                                 val_int)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: xc_len_tuple
            integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
            integer(kind=QINT), intent(in) :: num_freq_configs
            integer(kind=QINT), intent(in) :: dmat_num_tuple
            integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_int
            type(QcMat), intent(inout) :: val_int(num_int)
        end subroutine XCFunGetMat_f
        subroutine XCFunGetExp_f(xc_len_tuple,
                                                   &
                                 xc_pert_tuple,
                                 num_freq_configs, &
                                 dmat_num_tuple,
                                 dmat_idx_tuple,
                                                   &
                                 num_dmat,
                                                   Хr.
                                 dens_mat,
                                                   &
#if defined(OPENRSP_F_USER_CONTEXT)
                                 len_ctx,
                                                   &
                                 user_ctx,
                                                   &₹.
#endif
                                 num_exp,
                                                    &
                                 val_exp)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: xc_len_tuple
            integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
            integer(kind=QINT), intent(in) :: num_freq_configs
            integer(kind=QINT), intent(in) :: dmat_num_tuple
            integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
            integer(kind=QINT), intent(in) :: num_dmat
            type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: num_exp
            real(kind=QREAL), intent(inout) :: val_exp(num_exp)
        end subroutine XCFunGetExp_f
    end interface
```

```
! context of callback subroutines of XC functional
    type, public :: XCFunFun_f
        private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback functions
        procedure(XCFunGetMat_f), nopass, pointer :: get_xc_fun_mat
        procedure(XCFunGetExp_f), nopass, pointer :: get_xc_fun_exp
    end type XCFunFun_f
   public :: RSPXCFunCreate_f
   public :: RSPXCFunGetMat_f
   public :: RSPXCFunGetExp_f
   public :: RSPXCFunDestroy_f
    contains
    !% \brief creates the context of callback subroutines of XC functional
    ! \author Bin Gao
    ! \date 2015-06-23
      \param[XCFunFun_f:type]{inout} xcfun_fun the context of callback subroutines
      \param[character]{in} user_ctx user-defined callback function context
      \param[subroutine]{in} get_xc_fun_mat user specified function for
           getting integral matrices
      \param[subroutine]{in} get_xc_fun_exp user specified function for
    ! %
           getting expectation values
    subroutine RSPXCFunCreate_f(xcfun_fun,
#if defined(OPENRSP_F_USER_CONTEXT)
                                user_ctx,
                                                &
#endif
                                get_xc_fun_mat, &
                                get_xc_fun_exp)
        type(XCFunFun_f), intent(inout) :: xcfun_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_xc_fun_mat(xc_len_tuple,
                                                         &
                                      xc_pert_tuple,
                                                         &
                                      num_freq_configs, &
                                      dmat_num_tuple,
                                      dmat_idx_tuple,
                                                         &
                                      num_dmat,
                                                         &
                                      dens_mat,
                                                        &
#if defined(OPENRSP_F_USER_CONTEXT)
                                      len_ctx,
                                                         &
                                      user_ctx,
                                                         &
#endif
                                                         &
                                      num_int,
```

```
val_int)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: xc_len_tuple
                integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=QINT), intent(in) :: num_freq_configs
                integer(kind=QINT), intent(in) :: dmat_num_tuple
                integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_int
                type(QcMat), intent(inout) :: val_int(num_int)
            end subroutine get_xc_fun_mat
            subroutine get_xc_fun_exp(xc_len_tuple,
                                                        &
                                      xc_pert_tuple,
                                      num_freq_configs, &
                                      dmat_num_tuple,
                                      dmat_idx_tuple,
                                      num_dmat,
                                                        &
                                      dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                      len_ctx,
                                                        &
                                      user_ctx,
#endif
                                                        &
                                      num_exp,
                                      val_exp)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: xc_len_tuple
                integer(kind=QcPertInt), intent(in) :: xc_pert_tuple(xc_len_tuple)
                integer(kind=QINT), intent(in) :: num_freq_configs
                integer(kind=QINT), intent(in) :: dmat_num_tuple
                integer(kind=QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
                integer(kind=QINT), intent(in) :: num_dmat
                type(QcMat), intent(in) :: dens_mat(num_dmat)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: num_exp
                real(kind=QREAL), intent(inout) :: val_exp(num_exp)
            end subroutine get_xc_fun_exp
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        xcfun_fun%len_ctx = size(user_ctx)
        allocate(xcfun_fun%user_ctx(xcfun_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
```

```
write(STDOUT,"(A,I8)") "RSPXCFunCreate_f>> length", xcfun_fun%len_ctx
            stop "RSPXCFunCreate_f>> failed to allocate memory for user_ctx"
        end if
        xcfun_fun%user_ctx = user_ctx
#endif
        xcfun_fun%get_xc_fun_mat => get_xc_fun_mat
        xcfun_fun%get_xc_fun_exp => get_xc_fun_exp
    end subroutine RSPXCFunCreate_f
    !% \brief calls Fortran callback subroutine to get integral matrices of
           an XC functional
      \author Bin Gao
      \date 2015-06-23
      \param[integer]{in} len_tuple length of perturbation tuple on the XC functional
      \param[integer]{in} pert_tuple perturbation tuple on the XC functional
      \param[integer]{in} num_freq_configs the number of different frequency
           configurations to be considered for the perturbation tuple
      \param[integer]{in} dmat_len_tuple the number of different perturbation
           tuples of the AO based density matrices passed
      \param[integer]{in} dmat_idx_tuple indices of the density matrix
           perturbation tuples passed (canonically ordered)
      \param[integer]{in} num_dmat number of collected AO based density matrices for
           the passed density matrix perturbation tuples and all frequency configurations
      \param[C_PTR:type]{in} dens_mat the collected AO based density matrices
      \param[C_PTR:type]{in} user_ctx user-defined callback function context
      \param[integer]{in} num_int number of the integral matrices
    !% \param[C_PTR:type]{inout} val_int the integral matrices
    subroutine RSPXCFunGetMat_f(xc_len_tuple,
                               xc_pert_tuple,
                               num_freq_configs, &
                               dmat_num_tuple,
                               dmat_idx_tuple,
                               num_dmat,
                               dens_mat,
                                                &
                               user_ctx,
                                                &
                                                  &
                               num_int,
                               val_int)
                                                  &
        bind(C, name="RSPXCFunGetMat_f")
        integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
        integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_freq_configs
        integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
        integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_int
        type(C_PTR), intent(inout) :: val_int(num_int)
        type(XCFunFun_f), pointer :: xcfun_fun
                                                   !context of callback subroutines
        type(QcMat), allocatable :: f_dens_mat(:) !AO based density matrices
        type(QcMat), allocatable :: f_val_int(:) !integral matrices
        integer(kind=4) ierr
                                                   !error information
```

```
! converts C pointer to Fortran QcMat type
        allocate(f_dens_mat(num_dmat), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPXCFunGetMat_f>> num_dmat", num_dmat
            stop "RSPXCFunGetMat_f>> failed to allocate memory for f_dens_mat"
        end if
        ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        allocate(f_val_int(num_int), stat=ierr)
        if (ierr/=0) then
            write(STDOUT,"(A,I8)") "RSPXCFunGetMat_f>> num_int", num_int
            stop "RSPXCFunGetMat_f>> failed to allocate memory for f_val_int"
        end if
        ierr = QcMat_C_F_POINTER(A=f_val_int, c_A=val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, xcfun_fun)
        ! invokes Fortran callback subroutine to calculate the integral matrices
        call xcfun_fun%get_xc_fun_mat(xc_len_tuple,
                                                          &
                                      xc_pert_tuple,
                                                          &
                                      num_freq_configs,
                                      dmat_num_tuple,
                                      dmat_idx_tuple,
                                                          &
                                      num_dmat,
                                                          &
                                      f_dens_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                                      xcfun_fun%len_ctx, &
                                      xcfun_fun%user_ctx, &
#endif
                                      num_int,
                                                          &
                                      f_val_int)
        ! cleans up
       nullify(xcfun_fun)
        ierr = QcMat_C_NULL_PTR(A=f_val_int)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        deallocate(f_val_int)
        deallocate(f_dens_mat)
    end subroutine RSPXCFunGetMat_f
    !% \brief calls Fortran callback subroutine to get expectation values of
           an XC functional
    ! \author Bin Gao
      \date 2015-06-23
      \param[integer]{in} len_tuple length of perturbation tuple on the XC functional
      \param[integer]{in} pert_tuple perturbation tuple on the XC functional
      \param[integer]{in} num_freq_configs the number of different frequency
           configurations to be considered for the perturbation tuple
       \param[integer]{in} dmat_len_tuple the number of different perturbation
           tuples of the AO based density matrices passed
       \param[integer]{in} dmat_idx_tuple indices of the density matrix
```

```
ļ
          perturbation tuples passed (canonically ordered)
      \param[integer]{in} num_dmat number of collected AO based density matrices for
    Ţ
           the passed density matrix perturbation tuples and all frequency configurations
    ! \param[C_PTR:type]{in} dens_mat the collected AO based density matrices
    ! \param[C_PTR:type]{in} user_ctx user-defined callback function context
      \param[integer]{in} num_exp number of expectation values
    !% \param[real]{out} val_exp the expectation values
    subroutine RSPXCFunGetExp_f(xc_len_tuple,
                                xc_pert_tuple,
                                num_freq_configs, &
                                dmat_num_tuple,
                                dmat_idx_tuple,
                                num_dmat,
                                                  &
                                dens_mat,
                                                  &
                                                &
                                user_ctx,
                                                  &
                                num_exp,
                                val_exp)
        bind(C, name="RSPXCFunGetExp_f")
        integer(kind=C_QINT), value, intent(in) :: xc_len_tuple
        integer(kind=C_QCPERTINT), intent(in) :: xc_pert_tuple(xc_len_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_freq_configs
        integer(kind=C_QINT), value, intent(in) :: dmat_num_tuple
        integer(kind=C_QINT), intent(in) :: dmat_idx_tuple(dmat_num_tuple)
        integer(kind=C_QINT), value, intent(in) :: num_dmat
        type(C_PTR), intent(in) :: dens_mat(num_dmat)
        type(C_PTR), value, intent(in) :: user_ctx
        integer(kind=C_QINT), value, intent(in) :: num_exp
        real(kind=C_QREAL), intent(inout) :: val_exp(num_exp)
        type(XCFunFun_f), pointer :: xcfun_fun    !context of callback subroutines
        type(QcMat), allocatable :: f_dens_mat(:) !AO based density matrices
        integer(kind=4) ierr
                                                   !error information
        ! converts C pointer to Fortran QcMat type
        allocate(f_dens_mat(num_dmat), stat=ierr)
        if (ierr/=0) then
           write(STDOUT,"(A,I8)") "RSPXCFunGetExp_f>> num_dmat", num_dmat
            stop "RSPXCFunGetExp_f>> failed to allocate memory for f_dens_mat"
        end if
        ierr = QcMat_C_F_POINTER(A=f_dens_mat, c_A=dens_mat)
        call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
        ! gets the Fortran callback subroutine
        call c_f_pointer(user_ctx, xcfun_fun)
        ! invokes Fortran callback subroutine to calculate the expectation values
        call xcfun_fun%get_xc_fun_exp(xc_len_tuple,
                                      xc_pert_tuple,
                                                          &
                                      num_freq_configs,
                                      dmat_num_tuple,
                                                          &
                                      dmat_idx_tuple,
                                                          &
                                      num_dmat,
                                                          &
                                      f_dens_mat,
                                                          &
#if defined(OPENRSP_F_USER_CONTEXT)
                                      xcfun_fun%len_ctx, &
                                      xcfun_fun%user_ctx, &
```

```
172
```

```
#endif
                                                                     &
                                                num_exp,
                                                val_exp)
                ! cleans up
                nullify(xcfun_fun)
                ierr = QcMat_C_NULL_PTR(A=f_dens_mat)
                call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
                deallocate(f_dens_mat)
                return
            end subroutine RSPXCFunGetExp_f
            !% \brief cleans the context of callback subroutines of XC functional
            ! \author Bin Gao
            ! \date 2015-06-23
            !% \param[XCFunFun_f:type] {inout} xcfun_fun the context of callback subroutines
            subroutine RSPXCFunDestroy_f(xcfun_fun)
                type(XCFunFun_f), intent(inout) :: xcfun_fun
        #if defined(OPENRSP_F_USER_CONTEXT)
                xcfun_fun%len_ctx = 0
                deallocate(xcfun_fun%user_ctx)
        #endif
                nullify(xcfun_fun%get_xc_fun_mat)
                nullify(xcfun_fun%get_xc_fun_exp)
            end subroutine RSPXCFunDestroy_f
        end module RSPXCFun_f
        #undef OPENRSP_API_SRC
      \langle RSPNucHamilton.F90 \ 172 \rangle \equiv
172
        \langle OpenRSPLicenseFortran 115a \rangle
        !! 2015-06-23, Bin Gao
        !! * first version
        ! basic data types
        #include "api/qcmatrix_c_type.h"
        #define OPENRSP_API_SRC "src/fortran/RSPNucHamilton.F90"
        module RSPNucHamilton_f
            use, intrinsic :: iso_c_binding
            use qcmatrix_f, only: QINT,QREAL
            use RSPPertBasicTypes_f, only: QcPertInt, &
                                             C_QCPERTINT
            implicit none
            integer(kind=4), private, parameter :: STDOUT = 6
            ! user specified callback subroutine
```

```
abstract interface
        subroutine NucHamiltonGetContrib_f(nuc_num_pert,
                                           nuc_pert_labels, &
                                           nuc_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                           len_ctx,
                                           user_ctx,
                                                            &₹.
#endif
                                           size_pert,
                                                            &
                                           val_nuc)
            use qcmatrix_f, only: QINT,QREAL
            use RSPPertBasicTypes_f, only: QcPertInt
            integer(kind=QINT), intent(in) :: nuc_num_pert
            integer(kind=QcPertInt), intent(in) :: nuc_pert_labels(nuc_num_pert)
            integer(kind=QINT), intent(in) :: nuc_pert_orders(nuc_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            integer(kind=QINT), intent(in) :: size_pert
            real(kind=QREAL), intent(inout) :: val_nuc(size_pert)
        end subroutine NucHamiltonGetContrib_f
    end interface
    ! context of callback subroutine of nuclear Hamiltonian
   type, public :: NucHamiltonFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback function
        procedure(NucHamiltonGetContrib_f), nopass, pointer :: get_nuc_contrib
   end type NucHamiltonFun_f
   public :: RSPNucHamiltonCreate_f
   public :: RSPNucHamiltonGetContributions_f
   public :: RSPNucHamiltonDestroy_f
   contains
    !% \brief creates the context of callback subroutine of nuclear Hamiltonian
    ! \author Bin Gao
    ! \date 2015-06-23
    ! \param[NucHamiltonFun_f:type]{inout} nuc_hamilton_fun the context of callback subrou
    ! \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine] {in} get_nuc_contrib user specified function for
    !%
           getting nuclear contributions
    subroutine RSPNucHamiltonCreate_f(nuc_hamilton_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                      user_ctx,
```

```
#endif
                                      get_nuc_contrib)
        type(NucHamiltonFun_f), intent(inout) :: nuc_hamilton_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_nuc_contrib(nuc_num_pert,
                                       nuc_pert_labels, &
                                       nuc_pert_orders, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                       len_ctx,
                                       user_ctx,
                                                        &
#endif
                                       size_pert,
                                       val_nuc)
                use qcmatrix_f, only: QINT,QREAL
                use RSPPertBasicTypes_f, only: QcPertInt
                integer(kind=QINT), intent(in) :: nuc_num_pert
                integer(kind=QcPertInt), intent(in) :: nuc_pert_labels(nuc_num_pert)
                integer(kind=QINT), intent(in) :: nuc_pert_orders(nuc_num_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                integer(kind=QINT), intent(in) :: size_pert
                real(kind=QREAL), intent(inout) :: val_nuc(size_pert)
            end subroutine get_nuc_contrib
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        nuc_hamilton_fun%len_ctx = size(user_ctx)
        allocate(nuc_hamilton_fun%user_ctx(nuc_hamilton_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A, 18)") "RSPNucHamiltonCreate_f>> length", nuc_hamilton_fun%len_
            stop "RSPNucHamiltonCreate_f>> failed to allocate memory for user_ctx"
        end if
       nuc_hamilton_fun%user_ctx = user_ctx
#endif
        nuc_hamilton_fun%get_nuc_contrib => get_nuc_contrib
   end subroutine RSPNucHamiltonCreate_f
    !% \brief calls Fortran callback subroutine to get nuclear contributions
    ! \author Bin Gao
    ! \date 2015-06-23
    ! \param[integer]{in} len_tuple length of perturbation tuple on the nuclear Hamiltonia
    ! \param[integer]{in} pert_tuple perturbation tuple on the nuclear Hamiltonian
    ! \param[C_PTR:type]{in} user_ctx user-defined callback function context
      \param[integer]{in} size_pert size of the perturbations on the nuclear Hamiltonian
    !% \param[real]{out} val_nuc the nuclear contributions
    subroutine RSPNucHamiltonGetContributions_f(nuc_num_pert,
                                                nuc_pert_labels, &
```

```
nuc_pert_orders, &
                                                   user_ctx,
                                                                     &
                                                   size_pert,
                                                                     &
                                                   val_nuc)
          bind(C, name="RSPNucHamiltonGetContributions_f")
          integer(kind=C_QINT), value, intent(in) :: nuc_num_pert
          integer(kind=C_QCPERTINT), intent(in) :: nuc_pert_labels(nuc_num_pert)
          integer(kind=C_QINT), intent(in) :: nuc_pert_orders(nuc_num_pert)
          type(C_PTR), value, intent(in) :: user_ctx
          integer(kind=C_QINT), value, intent(in) :: size_pert
          real(C_QREAL), intent(inout) :: val_nuc(size_pert)
          type(NucHamiltonFun_f), pointer :: nuc_hamilton_fun !context of callback subroutin
          ! gets the Fortran callback subroutine
          call c_f_pointer(user_ctx, nuc_hamilton_fun)
          ! invokes Fortran callback subroutine to calculate the nuclear contributions
          call nuc_hamilton_fun%get_nuc_contrib(nuc_num_pert,
                                                 nuc_pert_labels,
                                                                             &
                                                 nuc_pert_orders,
                                                                             &
 #if defined(OPENRSP_F_USER_CONTEXT)
                                                 nuc_hamilton_fun%len_ctx,
                                                 nuc_hamilton_fun%user_ctx, &
 #endif
                                                 size_pert,
                                                                             &
                                                 val_nuc)
          ! cleans up
          nullify(nuc_hamilton_fun)
      end subroutine RSPNucHamiltonGetContributions_f
      !% \brief cleans the context of callback subroutine of nuclear Hamiltonian
      ! \author Bin Gao
      ! \date 2015-06-23
      !\% \simeq [NucHamiltonFun_f:type]{inout} nuc_hamilton_fun the context of callback subrou}
      subroutine RSPNucHamiltonDestroy_f(nuc_hamilton_fun)
          type(NucHamiltonFun_f), intent(inout) :: nuc_hamilton_fun
 #if defined(OPENRSP_F_USER_CONTEXT)
         nuc_hamilton_fun%len_ctx = 0
          deallocate(nuc_hamilton_fun%user_ctx)
 #endif
          nullify(nuc_hamilton_fun%get_nuc_contrib)
      end subroutine RSPNucHamiltonDestroy_f
 end module RSPNucHamilton_f
 #undef OPENRSP_API_SRC
\langle RSPSolver.F90 \ 175 \rangle \equiv
 \langle OpenRSPLicenseFortran 115a \rangle
 !! 2014-08-06, Bin Gao
 !! * first version
```

175

```
! basic data types
#include "api/qcmatrix_c_type.h"
#define OPENRSP_API_SRC "src/fortran/RSPSolver.F90"
module RSPSolver_f
    use, intrinsic :: iso_c_binding
    use qcmatrix_f, only: QINT,QREAL,QcMat,QcMat_C_F_POINTER,QcMat_C_NULL_PTR
    implicit none
    integer(kind=4), private, parameter :: STDOUT = 6
    ! user specified callback subroutine
    abstract interface
        subroutine SolverRun_f(num_freq_sums, &
                               freq_sums,
                               size_pert,
                               RHS_mat,
#if defined(OPENRSP_F_USER_CONTEXT)
                               len_ctx,
                                             &
                               user_ctx,
#endif
                               rsp_param)
            use qcmatrix_f, only: QINT,QREAL,QcMat
            integer(kind=QINT), intent(in) :: num_freq_sums
            real(kind=QREAL), intent(in) :: freq_sums(2*num_freq_sums)
            integer(kind=QINT), intent(in) :: size_pert
            type(QcMat), intent(in) :: RHS_mat(num_freq_sums*size_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
            integer(kind=QINT), intent(in) :: len_ctx
            character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
            type(QcMat), intent(inout) :: rsp_param(num_freq_sums*size_pert)
        end subroutine SolverRun_f
    end interface
    ! context of callback subroutine of response equation solver
    type, public :: SolverFun_f
       private
#if defined(OPENRSP_F_USER_CONTEXT)
        ! user-defined callback function context
        integer(kind=QINT) :: len_ctx = 0
        character(len=1), allocatable :: user_ctx(:)
#endif
        ! callback function
        procedure(SolverRun_f), nopass, pointer :: get_linear_rsp_solution
    end type SolverFun_f
   public :: RSPSolverCreate_f
    public :: RSPSolverGetLinearRSPSolution_f
```

```
public :: RSPSolverDestroy_f
   contains
    !% \brief creates the context of callback subroutine of response equation solver
    ! \author Bin Gao
    ! \date 2014-08-06
    ! \param[SolverFun_f:type]{inout} solver_fun the context of callback subroutine
    ! \param[character]{in} user_ctx user-defined callback function context
    ! \param[subroutine] {in} get_linear_rsp_solution user specified function of
    ! %
           response equation solver
    subroutine RSPSolverCreate_f(solver_fun, &
#if defined(OPENRSP_F_USER_CONTEXT)
                                 user_ctx,
#endif
                                 get_linear_rsp_solution)
        type(SolverFun_f), intent(inout) :: solver_fun
#if defined(OPENRSP_F_USER_CONTEXT)
        character(len=1), intent(in) :: user_ctx(:)
#endif
        interface
            subroutine get_linear_rsp_solution(num_freq_sums, &
                                               freq_sums,
                                               size_pert,
                                               RHS_mat,
                                                              &
#if defined(OPENRSP_F_USER_CONTEXT)
                                               len_ctx,
                                               user_ctx,
#endif
                                               rsp_param)
                use qcmatrix_f, only: QINT,QREAL,QcMat
                integer(kind=QINT), intent(in) :: num_freq_sums
                real(kind=QREAL), intent(in) :: freq_sums(2*num_freq_sums)
                integer(kind=QINT), intent(in) :: size_pert
                type(QcMat), intent(in) :: RHS_mat(num_freq_sums*size_pert)
#if defined(OPENRSP_F_USER_CONTEXT)
                integer(kind=QINT), intent(in) :: len_ctx
                character(len=1), intent(in) :: user_ctx(len_ctx)
#endif
                type(QcMat), intent(inout) :: rsp_param(num_freq_sums*size_pert)
            end subroutine get_linear_rsp_solution
        end interface
#if defined(OPENRSP_F_USER_CONTEXT)
        integer(kind=4) ierr !error information
        solver_fun%len_ctx = size(user_ctx)
        allocate(solver_fun%user_ctx(solver_fun%len_ctx), stat=ierr)
        if (ierr/=0) then
            write(STDOUT, "(A,18)") "RSPSolverCreate_f>> length", solver_fun%len_ctx
            stop "RSPSolverCreate_f>> failed to allocate memory for user_ctx"
        solver_fun%user_ctx = user_ctx
#endif
```

solver_fun%get_linear_rsp_solution => get_linear_rsp_solution
end subroutine RSPSolverCreate_f

```
!% \brief calls Fortran callback subroutine to get solution of response equation
! \author Bin Gao
  \date 2014-08-06
  \param[integer]{in} num_freq_sums number of complex frequency sums
       on the left hand side of the linear response equation
  \param[real]{in} freq_sums the complex frequency sums on the left hand side
  \param[integer]{in} size_pert size of perturbations acting on the
       time-dependent self-consistent-field (TDSCF) equation
  \param[C_PTR:type]{in} RHS_mat RHS matrices, size is \var{num_freq_sums}*\var{size_p}
  \param[C_PTR:type]{in} user_ctx user-defined callback function context
! \param[C_PTR:type]{out} rsp_param solved response parameters,
       size is \var{num_freq_sums}*\var{size_pert}
subroutine RSPSolverGetLinearRSPSolution_f(num_freq_sums, &
                                           freq_sums,
                                           size_pert,
                                           RHS_mat,
                                                          Źг
                                           user_ctx,
                                                          &
                                           rsp_param)
   bind(C, name="RSPSolverGetLinearRSPSolution_f")
   integer(kind=C_QINT), value, intent(in) :: num_freq_sums
   real(kind=C_QREAL), intent(in) :: freq_sums(2*num_freq_sums)
   integer(kind=C_QINT), value, intent(in) :: size_pert
   type(C_PTR), intent(in) :: RHS_mat(num_freq_sums*size_pert)
   type(C_PTR), value, intent(in) :: user_ctx
   type(C_PTR), intent(inout) :: rsp_param(num_freq_sums*size_pert)
   type(SolverFun_f), pointer :: solver_fun    !context of callback subroutine
   integer(kind=QINT) size_solution
                                                !size of solution of response equation
                                               !RHS matrices
   type(QcMat), allocatable :: f_RHS_mat(:)
   type(QcMat), allocatable :: f_rsp_param(:) !response parameters
   integer(kind=4) ierr
                                                !error information
   ! converts C pointer to Fortran QcMat type
   size_solution = num_freq_sums*size_pert
   allocate(f_RHS_mat(size_solution), stat=ierr)
   if (ierr/=0) then
       write(STDOUT,"(A,18)") "RSPSolverGetLinearRSPSolution_f>> size_solution", &
                               size_solution
        stop "RSPSolverGetLinearRSPSolution_f>> failed to allocate memory for f_RHS_mat
   end if
   ierr = QcMat_C_F_POINTER(A=f_RHS_mat, c_A=RHS_mat)
   call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
   allocate(f_rsp_param(size_solution), stat=ierr)
   if (ierr/=0) then
       write(STDOUT,"(A,18)") "RSPSolverGetLinearRSPSolution_f>> size_solution", &
                               size_solution
       stop "RSPSolverGetLinearRSPSolution_f>> failed to allocate memory for f_rsp_par
   end if
   ierr = QcMat_C_F_POINTER(A=f_rsp_param, c_A=rsp_param)
   call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
   ! gets the Fortran callback subroutine
```

```
call c_f_pointer(user_ctx, solver_fun)
          ! invokes Fortran callback subroutine to solve the response equation
          call solver_fun%get_linear_rsp_solution(num_freq_sums,
                                                    freq_sums,
                                                    size_pert,
                                                                          &
                                                    f_RHS_mat,
 #if defined(OPENRSP_F_USER_CONTEXT)
                                                    solver_fun%len_ctx, &
                                                    solver_fun%user_ctx, &
 #endif
                                                    f_rsp_param)
          ! cleans up
          nullify(solver_fun)
          ierr = QcMat_C_NULL_PTR(A=f_rsp_param)
          call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
          ierr = QcMat_C_NULL_PTR(A=f_RHS_mat)
          call QErrorCheckCode(STDOUT, ierr, __LINE__, OPENRSP_API_SRC)
          deallocate(f_rsp_param)
          deallocate(f_RHS_mat)
          return
     end subroutine RSPSolverGetLinearRSPSolution_f
      !% \brief cleans the context of callback subroutine of response equation solver
      ! \author Bin Gao
      ! \date 2014-08-06
      !% \param[SolverFun_f:type]{inout} solver_fun the context of callback subroutine
      subroutine RSPSolverDestroy_f(solver_fun)
          type(SolverFun_f), intent(inout) :: solver_fun
 #if defined(OPENRSP_F_USER_CONTEXT)
          solver_fun%len_ctx = 0
          deallocate(solver_fun%user_ctx)
 #endif
          nullify(solver_fun%get_linear_rsp_solution)
      end subroutine RSPSolverDestroy_f
 end module RSPSolver_f
 #undef OPENRSP_API_SRC
  Furthermoe, we implement the following Fortran adapters:
\langle OpenRSPFortranAdapter.c \ 179 \rangle \equiv
    \langle OpenRSPLicense 14a \rangle
    2014-07-31, Bin Gao
     * first version
 #include "OpenRSP.h"
 QErrorCode OpenRSPCreateFortranAdapter(void **open_rsp)
 {
     OpenRSP *c_open_rsp;
```

179

```
QErrorCode ierr;
    c_open_rsp = (OpenRSP *)malloc(sizeof(OpenRSP));
    if (c_open_rsp==NULL) {
        QErrorExit(FILE_AND_LINE, "failed to allocate memory for c_open_rsp");
    }
    ierr = OpenRSPCreate(c_open_rsp);
    *open_rsp = (void *)(c_open_rsp);
    return ierr;
}
//QErrorCode f_api_OpenRSPSetElecEOM(void **open_rsp,
//
                                     const QInt elec_EOM_type)
//{
//
      OpenRSP *c_open_rsp;
//
      ElecEOMType c_elec_EOM_type;
//
      QErrorCode ierr;
//
     /* should be consistent with what defined in src/f03/openrsp_f.F90 */
//
      switch (elec_EOM_type) {
//
      case 0:
         c_elec_EOM_type = ELEC_AO_D_MATRIX;
//
//
         break;
//
//
          c_elec_EOM_type = ELEC_MO_C_MATRIX;
//
         break;
//
      case 2:
//
          c_elec_EOM_type = ELEC_COUPLED_CLUSTER;
//
          break;
//
     default:
//
          return QFAILURE;
//
      c_open_rsp = (OpenRSP *)(*open_rsp);
//
//
      ierr = OpenRSPSetElecEOM(c_open_rsp, c_elec_EOM_type);
//
      return ierr;
//}
QErrorCode OpenRSPWriteFortranAdapter(const void *open_rsp,
                                      const char *file_name)
{
    FILE *fp_rsp;
    OpenRSP *c_open_rsp;
    QErrorCode ierr;
    fp_rsp = fopen(file_name, "a");
    if (fp_rsp==NULL) {
        printf("OpenRSPWriteFortranAdapter>> file name %s\n", file_name);
        QErrorExit(FILE_AND_LINE, "failed to open the file");
    }
    c_open_rsp = (OpenRSP *)open_rsp;
    ierr = OpenRSPWrite(c_open_rsp, fp_rsp);
    fprintf(fp_rsp, "\n");
    fclose(fp_rsp);
    return ierr;
}
```

```
QErrorCode OpenRSPWriteStdOutFortranAdapter(const void *open_rsp)
{
   OpenRSP *c_open_rsp;
   QErrorCode ierr;
    c_open_rsp = (OpenRSP *)open_rsp;
   ierr = OpenRSPWrite(c_open_rsp, stdout);
   fprintf(stdout, "\n");
   return ierr;
}
QErrorCode OpenRSPDestroyFortranAdapter(void **open_rsp)
   OpenRSP *c_open_rsp;
   QErrorCode ierr;
    c_open_rsp = (OpenRSP *)(*open_rsp);
    ierr = OpenRSPDestroy(c_open_rsp);
    *open_rsp = NULL;
   open_rsp = NULL;
   return ierr;
}
```

3.13 Unit Testing

3.13.1 Testing C APIs

```
We first implement perturbations and its callback function for unit testing:
       \langle OpenRSPTestPerturbations.h \ 182a \rangle \equiv
182a
           ⟨OpenRSPLicense 14a⟩
           This is the header file of perturbations.
           2014-07-31, Bin Gao:
           * first version
         #include "OpenRSP.h"
         #define NUM_ALL_PERT 3
         extern const QcPertInt PERT_GEOMETRIC;
         extern const QcPertInt PERT_DIPOLE;
         extern const QcPertInt PERT_MAGNETIC;
         extern const QInt MAX_ORDER_GEOMETRIC;
         extern const QInt MAX_ORDER_DIPOLE;
         extern const QInt MAX_ORDER_MAGNETIC;
         extern const QcPertInt ALL_PERT_LABELS[NUM_ALL_PERT];
         extern const QInt ALL_PERT_MAX_ORDERS[NUM_ALL_PERT];
         extern const QInt ALL_PERT_SIZES[15];
         extern const QInt NUM_ATOMS;
182b
       \langle OpenRSPTestPerturbations.c \ 182b \rangle \equiv
           \langle OpenRSPLicense 14a \rangle
         #include "OpenRSPTestPerturbations.h"
         const QcPertInt PERT_GEOMETRIC = 1;
         const QcPertInt PERT_DIPOLE = 2;
         const QcPertInt PERT_MAGNETIC = 5;
         const QInt MAX_ORDER_GEOMETRIC = 7;
         const QInt MAX_ORDER_DIPOLE = 1;
         const QInt MAX_ORDER_MAGNETIC = 7;
         /* labels of all perturbations */
         const QcPertInt ALL_PERT_LABELS[] = {PERT_GEOMETRIC,
                                               PERT_DIPOLE,
                                               PERT_MAGNETIC);
         /* allowed maximal orders of all perturbations */
         const QInt ALL_PERT_MAX_ORDERS[] = {MAX_ORDER_GEOMETRIC,
                                              MAX_ORDER_DIPOLE,
                                              MAX_ORDER_MAGNETIC};
         /* sizes of all perturbations up to their maximal orders */
         const QInt ALL_PERT_SIZES[]={
             12,78,364,1365,4368,12376,31824, /* geometric derivatives (4 atoms) */
                                                  /* electric dipole */
             3,
```

/* magnetic derivatives */

3,6,10,15,21,28,36};

```
const QInt NUM_ATOMS=4;
        Here we have used three different perturbation labels for geometric, dipole length and magnetic
        perturbations.
        \langle OpenRSPPertCallback.h \ 183a \rangle \equiv
183a
            ⟨OpenRSPLicense 14a⟩
            This is the header file of perturbations' callback function.
            2014-07-31, Bin Gao:
            * first version
          #if !defined(OPENRSP_PERT_CALLBACK_H)
          #define OPENRSP_PERT_CALLBACK_H
          #include "OpenRSP.h"
          #if defined(OPENRSP_C_USER_CONTEXT)
          #define PERT_CONTEXT "NRNZGEO"
          #endif
          extern void get_pert_concatenation(const QInt,
                                                 const QcPertInt,
                                                 const QInt,
                                                 const QInt,
                                                 const QInt*,
          #if defined(OPENRSP_C_USER_CONTEXT)
                                                 void*,
          #endif
                                                 QInt*);
          #endif
183b
        \langle OpenRSPPertCallback.c \ 183b \rangle \equiv
            \langle OpenRSPLicense 14a \rangle
          #include "OpenRSPPertCallback.h"
          void get_pert_concatenation(const QInt pert_label,
                                         const QcPertInt first_cat_comp,
                                         const QInt num_cat_comps,
                                         const QInt num_sub_tuples,
                                         const QInt *len_sub_tuples,
          #if defined(OPENRSP_C_USER_CONTEXT)
                                         void *user_ctx,
          #endif
                                         QInt *rank_sub_comps)
          /*FIXME: to implement*/
```

```
184
```

} The following header and C files implement the callback function for nuclear Hamiltonian: $\langle OpenRSPNucHamiltonCallback.h \ 184a \rangle \equiv$ 184a ⟨OpenRSPLicense 14a⟩ This header file contains callback function for nuclear Hamiltonian. 2015-10-16, Bin Gao: * first version #if !defined(OPENRSP_NUC_HAMILTON_CALLBACK_H) #define OPENRSP_NUC_HAMILTON_CALLBACK_H #include "OpenRSP.h" #if defined(OPENRSP_C_USER_CONTEXT) #define NUC_HAMILTON_CONTEXT "NUC_HAMILTON" #endif extern void get_nuc_contrib(const QInt, const QcPertInt*, const QInt*, #if defined(OPENRSP_C_USER_CONTEXT) void*, #endif const QInt, QReal*); #endif $\langle OpenRSPNucHamiltonCallback.c \ 184b \rangle \equiv$ 184b⟨OpenRSPLicense 14a⟩ #include "OpenRSPNucHamiltonCallback.h" void get_nuc_contrib(const QInt nuc_num_pert, const QcPertInt *nuc_pert_labels, const QInt *nuc_pert_orders, #if defined(OPENRSP_C_USER_CONTEXT) void *user_ctx, #endif const QInt size_pert, QReal *val_nuc) /*FIXME: to implement*/ We next implement callback functions for AO-based response theory calculations: $\langle OpenRSPDensAOCallback.h \ 184c \rangle \equiv$ 184c

```
/*
  ⟨OpenRSPLicense 14a⟩
 This header file contains callback functions for AO-based response theory
  calculations.
 2015-10-16, Bin Gao:
 * first version
*/
#if !defined(OPENRSP_DENS_AO_CALLBACK_H)
#define OPENRSP_DENS_AO_CALLBACK_H
#include "OpenRSP.h"
#include "OpenRSPTestData.h"
#if defined(OPENRSP_C_USER_CONTEXT)
#define OVERLAP_CONTEXT "OVERLAP"
#define ONEHAM_CONTEXT "ONEHAM"
#define EXT_FIELD_CONTEXT "EXT_FIELD"
#define TWO_OPER_CONTEXT "NONLAO"
#define SOLVER_CONTEXT "SOLVER"
#endif
extern void get_overlap_mat(const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             const QcPertInt*,
                             const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                             void*,
#endif
                             const QInt,
                             QcMat*[]);
extern void get_overlap_exp(const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             const QcPertInt*,
                             const QInt*,
                             const QInt,
                             QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
                             void*,
#endif
```

```
const QInt,
                             QReal*);
extern void get_one_oper_mat(const QInt,
                              const QcPertInt*,
                              const QInt*,
#if defined(OPENRSP_C_USER_CONTEXT)
                              void*,
#endif
                              const QInt,
                              QcMat*[]);
extern void get_one_oper_exp(const QInt,
                              const QcPertInt*,
                              const QInt*,
                              const QInt,
                              QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
                              void*,
#endif
                              const QInt,
                              QReal*);
extern void get_two_oper_mat(const QInt,
                              const QcPertInt*,
                              const QInt*,
                              const QInt,
                              QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
                              void*,
#endif
                              const QInt,
                              QcMat*[]);
extern void get_two_oper_exp(const QInt,
                              const QcPertInt*,
                              const QInt*,
                              const QInt,
                              const QInt*,
                              QcMat*[],
                              const QInt*,
                              QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
                              void*,
#endif
                              const QInt,
                              QReal*);
extern void get_linear_rsp_solution(const QInt,
                                      const QReal*,
                                      const QInt,
                                      QcMat*[],
#if defined(OPENRSP_C_USER_CONTEXT)
                                     void*,
#endif
                                      QcMat*[]);
```

#endif

Here we mimic callback functions by reading different AO-based matrices from files *.dat. These matrices were calculated from Dalton program, and saved in the directory tests. During building, the following CMake file will generated list of filenames containing these AO-based matrices:

```
\langle OpenRSPTestData.cmake\ 187 \rangle \equiv
187
        # Generated by notangle -ROpenRSPTestData.cmake web/UnitTesting.nw > cmake/OpenRSPTestData.
        include_directories(${PROJECT_BINARY_DIR})
        # atomic-orbital (AO) density matrix-based response theory
        set(OPENRSP_TEST_DATA ${PROJECT_BINARY_DIR}/OpenRSPTestData.h)
        file(WRITE ${OPENRSP_TEST_DATA} "#if !defined(OPENRSP_TEST_DATA_H)\n")
        file(APPEND ${OPENRSP_TEST_DATA} "#define OPENRSP_TEST_DATA_H\n\n")
        file(APPEND ${OPENRSP_TEST_DATA} "#include \"qcmatrix.h\"\n\n")
        # function of reading matrices from a dat file
        file(APPEND ${OPENRSP_TEST_DATA} "extern QErrorCode OpenRSPTestReadMat(const char*,\n")
        file(APPEND ${OPENRSP_TEST_DATA} "
                                                                                 const QInt,\n")
        file(APPEND ${OPENRSP_TEST_DATA} "
                                                                                 const QInt,\n")
        file(APPEND ${OPENRSP_TEST_DATA} "
                                                                                 QcMat*[]);\n\n")
        # function of zeroing matrices
        file(APPEND ${OPENRSP_TEST_DATA} "extern QErrorCode OpenRSPTestZeroMat(const QInt,\n")
        file(APPEND ${OPENRSP_TEST_DATA} "
                                                                                 QcMat*[]);\n\n")
        # unperturbed AO-based Fock matrix
        get_filename_component(FOCK_AO_HF
                               ${LIB_OPENRSP_PATH}/tests/FockAOHF.dat
                               ABSOLUTE)
        file(APPEND
             ${OPENRSP_TEST_DATA}
             "#define FOCK_AO_HF \"${FOCK_AO_HF}\"\n")
        # unperturbed AO-based density matrix
        get_filename_component(DENS_AO_HF
                               ${LIB_OPENRSP_PATH}/tests/DensAOHF.dat
                               ABSOLUTE)
        file(APPEND
             ${OPENRSP_TEST_DATA}
             "#define DENS_AO_HF \"${DENS_AO_HF}\"\n")
        # unperturbed AO-based overlap integral matrix
        get_filename_component(OVERLAP_AO
                               ${LIB_OPENRSP_PATH}/tests/OverlapAO.dat
                               ABSOLUTE)
        file(APPEND
             ${OPENRSP_TEST_DATA}
             "#define OVERLAP_AO \"${OVERLAP_AO}\"\n")
        # unperturbed AO-based dipole length integral matrices
        get_filename_component(DIPLEN_AO
                               ${LIB_OPENRSP_PATH}/tests/DipLenAO.dat
                               ABSOLUTE)
        file(APPEND
             ${OPENRSP_TEST_DATA}
             "#define DIPLEN_AO \"${DIPLEN_AO}\"\n")
        # two-electron integrals contracted with perturbed AO-based density matrices
        # for solving polarizability at frequency as 0.072
        get_filename_component(ALPHA_GMAT_AO_HF
                               ${LIB_OPENRSP_PATH}/tests/AlphaGMatAOHF.dat
```

₹

FILE *fp_dat;

```
ABSOLUTE)
 file(APPEND
       ${OPENRSP_TEST_DATA}
       "#define ALPHA_GMAT_AO_HF \"${ALPHA_GMAT_AO_HF}\"\n")
 # response parameters for solving polarizability at frequency as 0.072
 get_filename_component(ALPHA_RSPARAM_AO_HF
                          ${LIB_OPENRSP_PATH}/tests/AlphaRSParamAOHF.dat
 file(APPEND
       ${OPENRSP_TEST_DATA}
       "#define ALPHA_RSPARAM_AO_HF \"${ALPHA_RSPARAM_AO_HF}\"\n")
 file(APPEND ${OPENRSP_TEST_DATA} "\n#endif\n")
The following file will read a tests/*.dat file and put the data into matrices:
\langle OpenRSPTestData.c \ 188 \rangle \equiv
    \langle OpenRSPLicense 14a \rangle
 #if defined(QCMATRIX_SINGLE_PRECISION)
 #define QCREAL_FMT "f"
 #else
 #define QCREAL_FMT "lf"
 #endif
 #include "OpenRSPTestData.h"
 /* <function name='OpenRSPTestReadMat'</pre>
               attr='private'
               author='Bin Gao'
               date='2015-10-18'>
       Reads a dat file and puts the data into matrices
       <param name='file_mat' direction='in'>
         Name of the dat file
       </param>
       <param name='num_skip_mat' direction='in'>
         Number of the first few matrices to skip
       </param>
       <param name='num_read_mat' direction='in'>
         Number of matrices to read
       </param>
       <param name='mat_read' direction='inout'>
         Matrices read
       </param>
       <return>Error information</return>
     </function> */
 QErrorCode OpenRSPTestReadMat(const char *file_mat,
                                 const QInt num_skip_mat,
                                  const QInt num_read_mat,
                                 QcMat *mat_read[])
```

/* file pointer */

QInt dat_num_read; /* number of arguments read from the dat file */

```
QInt dat_num_mat;
                      /* number of matrices in the dat file */
   QInt dat_num_row; /* number of rows of matrices */
   QInt dat_num_col; /* number of columns of matrices */
   QInt dat_num_val; /* number of values of matrices */
   QReal *dat_values; /* values of matrices */
   QInt imat;
                      /* incremental recorder over matrices */
                      /* incremental recorder over values */
   QInt ival;
   QBool assembled; /* matrix assembled or not */
                      /* error information */
   QErrorCode ierr;
   /* parameters for setting matrices */
   const QInt NUM_BLOCKS=1;
#if defined(ZERO_BASED_NUMBERING)
   const QInt IDX_BLOCK_ROW[]={0};
    const QInt IDX_BLOCK_COL[]={0};
    const QInt IDX_FIRST_ROW=0;
   const QInt IDX_FIRST_COL=0;
#else
   const QInt IDX_BLOCK_ROW[]={1};
   const QInt IDX_BLOCK_COL[]={1};
   const QInt IDX_FIRST_ROW=1;
    const QInt IDX_FIRST_COL=1;
#endif
   QcDataType DATA_TYPE[1]={QREALMAT};
   fp_dat = fopen(file_mat, "r");
   if (fp_dat==NULL) {
        printf("OpenRSPTestReadMat>> file: %s\n", file_mat);
        QErrorExit(FILE_AND_LINE, "open the dat file");
   }
   dat_num_read = fscanf(fp_dat,
                          "%"QINT_FMT" %"QINT_FMT" %"QINT_FMT"",
                          &dat_num_mat, &dat_num_row, &dat_num_col);
   if (dat_num_read!=3) {
       printf("OpenRSPTestReadMat>> number of arguments read %"QINT_FMT"\n",
               dat_num_read);
        QErrorExit(FILE_AND_LINE, "read information of data");
   }
   /* checks the number of matrices to read */
    if (num_skip_mat+num_read_mat>dat_num_mat) {
       printf("OpenRSPTestReadMat>> number of skipping matrices %"QINT_FMT"\n",
               num_skip_mat);
       printf("OpenRSPTestReadMat>> number of reading matrices %"QINT_FMT"\n",
              num_read_mat);
        printf("OpenRSPTestReadMat>> number of matrices on the file %"QINT_FMT"\n",
               dat_num_mat);
        QErrorExit(FILE_AND_LINE, "not enough matrices on the file");
   }
   dat_num_val = dat_num_row*dat_num_col;
   dat_values = (QReal *)malloc(dat_num_val*sizeof(QReal));
   if (dat_values==NULL) {
       printf("OpenRSPTestReadMat>> number of values %"QINT_FMT"\n",
               dat_num_val);
        QErrorExit(FILE_AND_LINE, "allocates memory for values");
```

```
}
     /* skips the first few lines, including the '\n' of the first line */
     for (imat=0; imat<=num_skip_mat; imat++) {</pre>
          /*fscanf(fp_dat, "%*[^\n]\n", NULL);*/
              dat_num_read = fgetc(fp_dat);
          } while (dat_num_read!='\n');
     }
     for (imat=0; imat<num_read_mat; imat++) {</pre>
          for (ival=0; ival<dat_num_val; ival++) {</pre>
              if (fscanf(fp_dat, "%"QCREAL_FMT"", &dat_values[ival])!=1) {
                  printf("OpenRSPTestReadMat>> %"QINT_FMT"-th element\n", ival);
                  QErrorExit(FILE_AND_LINE, "read values");
              }
          }
          /* checks if the matrix is assembled or not */
          ierr = QcMatIsAssembled(mat_read[imat], &assembled);
          QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatIsAssembled()");
          if (assembled==QFALSE) {
              ierr = QcMatBlockCreate(mat_read[imat], NUM_BLOCKS);
              QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatBlockCreate()");
              ierr = QcMatSetDataType(mat_read[imat],
                                       NUM_BLOCKS,
                                        IDX_BLOCK_ROW,
                                        IDX_BLOCK_COL,
                                        DATA_TYPE);
              QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDataType()");
              ierr = QcMatSetDimMat(mat_read[imat], dat_num_row, dat_num_col);
              QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDimMat()");
              ierr = QcMatAssemble(mat_read[imat]);
              QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatAssemble()");
          }
          /* saves the values into the matrix */
          ierr = QcMatSetValues(mat_read[imat],
                                 IDX_BLOCK_ROW[0],
                                 IDX_BLOCK_COL[0],
                                 IDX_FIRST_ROW,
                                 dat_num_row,
                                 IDX_FIRST_COL,
                                 dat_num_col,
                                 dat_values,
                                 NULL);
          QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetValues()");
     }
     free(dat_values);
     dat_values = NULL;
     fclose(fp_dat);
     return QSUCCESS;
 }
  The following function will zero out a few matrices:
\langle OpenRSPTestData.c \ 188 \rangle + \equiv
 /* <function name='OpenRSPTestZeroMat'</pre>
```

```
attr='private'
             author='Bin Gao'
             date='2015-10-18'>
    Zero out a few matrices
     <param name='num_mat' direction='in'>
       Number of matrices to be zeroed out
     </param>
     <param name='mat_zero' direction='inout'>
       Matrices to be zeroed out
     </param>
     <return>Error information</return>
   </function> */
QErrorCode OpenRSPTestZeroMat(const QInt num_mat, QcMat *mat_zero[])
{
                        /* incremental recorder over matrices */
    QInt imat;
    QBool assembled;
                       /* matrix assembled or not */
    QErrorCode ierr;
                       /* error information */
    /* parameters for setting matrices */
    const QInt NUM_BLOCKS=1;
#if defined(ZERO_BASED_NUMBERING)
    const QInt IDX_BLOCK_ROW[]={0};
    const QInt IDX_BLOCK_COL[]={0};
#else
    const QInt IDX_BLOCK_ROW[]={1};
    const QInt IDX_BLOCK_COL[]={1};
#endif
    QcDataType DATA_TYPE[1]={QREALMAT};
    const QInt DAT_NUM_ROW=32;
    const QInt DAT_NUM_COL=32;
    for (imat=0; imat<num_mat; imat++) {</pre>
        /* checks if the matrix is assembled or not */
        ierr = QcMatIsAssembled(mat_zero[imat], &assembled);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatIsAssembled()");
        if (assembled==QFALSE) {
            ierr = QcMatBlockCreate(mat_zero[imat], NUM_BLOCKS);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatBlockCreate()");
            ierr = QcMatSetSymType(mat_zero[imat], QSYMMAT);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetSymType()");
            ierr = QcMatSetDataType(mat_zero[imat],
                                    NUM_BLOCKS,
                                    IDX_BLOCK_ROW,
                                    IDX_BLOCK_COL,
                                    DATA_TYPE);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDataType()");
            ierr = QcMatSetDimMat(mat_zero[imat], DAT_NUM_ROW, DAT_NUM_COL);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatSetDimMat()");
            ierr = QcMatAssemble(mat_zero[imat]);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatAssemble()");
        }
        /* zeroes out the matrix */
        ierr = QcMatZeroEntries(mat_zero[imat]);
        QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatZeroEntries()");
```

```
}
return QSUCCESS;
}
```

By using the above functions to read matrices for dat files and zero matrices, we can implement the following file callback functions for AO-based response theory calculations:

```
\langle OpenRSPDensAOCallback.c \ 192 \rangle \equiv
 /*
    \langle OpenRSPLicense 14a \rangle
 #include "OpenRSPDensAOCallback.h"
 void get_overlap_mat(const QInt bra_num_pert,
                       const QcPertInt *bra_pert_labels,
                        const QInt *bra_pert_orders,
                        const QInt ket_num_pert,
                        const QcPertInt *ket_pert_labels,
                        const QInt *ket_pert_orders,
                        const QInt oper_num_pert,
                        const QcPertInt *oper_pert_labels,
                        const QInt *oper_pert_orders,
 #if defined(OPENRSP_C_USER_CONTEXT)
                       void *user_ctx,
 #endif
                        const QInt num_int,
                        QcMat *val_int[])
 #include "OpenRSPTestPerturbations.h"
 #if defined(OPENRSP_C_USER_CONTEXT)
      char *overlap_context;
 #endif
     QErrorCode ierr;
 #if defined(OPENRSP_C_USER_CONTEXT)
     overlap_context = (char *)user_ctx;
      if (strcmp(overlap_context, OVERLAP_CONTEXT)!=0) {
          printf("get_overlap_mat>> incorrect operator at %s\n",
                 FILE_AND_LINE);
          exit(QFAILURE);
     }
 #endif
     /* unperturbed AO-based overlap integral matrix */
      if (oper_num_pert==0 && bra_num_pert==0 && ket_num_pert==0) {
          ierr = OpenRSPTestReadMat(OVERLAP_AO, 0, 1, val_int);
          if (ierr!=QSUCCESS) {
              printf("get_overlap_mat>> error happened at %s: %s\n",
                     FILE_AND_LINE,
                     "calling OpenRSPTestReadMat()");
              exit(ierr);
          }
     }
     else if (oper_num_pert==1 && bra_num_pert==0 && ket_num_pert==0) {
```

```
if (oper_pert_labels[0] == PERT_GEOMETRIC) {
        printf("get_overlap_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    /* zero matrices */
    else if (oper_pert_labels[0] == PERT_DIPOLE) {
        ierr = OpenRSPTestZeroMat(num_int, val_int);
        if (ierr!=QSUCCESS) {
            printf("get_overlap_mat>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling OpenRSPTestZeroMat()");
            exit(ierr);
        }
    }
    else if (oper_pert_labels[0] == PERT_MAGNETIC) {
        printf("get_overlap_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        printf("get_overlap_mat>> unknown perturbations at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
}
else if (oper_num_pert==0 && bra_num_pert==1 && ket_num_pert==0) {
    if (bra_pert_labels[0] == PERT_GEOMETRIC) {
        printf("get_overlap_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    /* zero matrices */
    else if (bra_pert_labels[0] == PERT_DIPOLE) {
        ierr = OpenRSPTestZeroMat(num_int, val_int);
        if (ierr!=QSUCCESS) {
            printf("get_overlap_mat>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling OpenRSPTestZeroMat()");
            exit(ierr);
        }
    }
    else if (bra_pert_labels[0] == PERT_MAGNETIC) {
        printf("get_overlap_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        printf("get_overlap_mat>> unknown perturbations at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
```

```
}
    else if (oper_num_pert==0 && bra_num_pert==0 && ket_num_pert==1) {
        if (ket_pert_labels[0] == PERT_GEOMETRIC) {
            printf("get_overlap_mat>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        /* zero matrices */
        else if (ket_pert_labels[0] == PERT_DIPOLE) {
            ierr = OpenRSPTestZeroMat(num_int, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_overlap_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                        "calling OpenRSPTestZeroMat()");
                exit(ierr);
            }
        }
        else if (ket_pert_labels[0] == PERT_MAGNETIC) {
            printf("get_overlap_mat>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
        else {
            printf("get_overlap_mat>> unknown perturbations at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else {
        printf("get_overlap_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
}
void get_overlap_exp(const QInt bra_num_pert,
                     const QcPertInt *bra_pert_labels,
                     const QInt *bra_pert_orders,
                     const QInt ket_num_pert,
                     const QcPertInt *ket_pert_labels,
                     const QInt *ket_pert_orders,
                     const QInt oper_num_pert,
                     const QcPertInt *oper_pert_labels,
                     const QInt *oper_pert_orders,
                     const QInt num_dens,
                     QcMat *ao_dens[],
#if defined(OPENRSP_C_USER_CONTEXT)
                     void *user_ctx,
#endif
                     const QInt num_exp,
                     QReal *val_exp)
{
```

```
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *overlap_context;
#endif
    QcMat *val_int[1];
   QInt idens;
   QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    overlap_context = (char *)user_ctx;
    if (strcmp(overlap_context, OVERLAP_CONTEXT)!=0) {
        printf("get_overlap_mat>> incorrect operator at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
    /* unperturbed AO-based overlap integral matrix */
    if (oper_num_pert==0 && bra_num_pert==0 && ket_num_pert==0) {
        val_int[0] = (QcMat *)malloc(sizeof(QcMat));
        if (val_int[0] == NULL) {
            \label{lem:printf("get_overlap_exp>> error happened at $\%s: $\%s\n"$,}
                   FILE_AND_LINE,
                   "allocats memory for matrix");
            exit(QFAILURE);
        }
        ierr = QcMatCreate(val_int[0]);
        if (ierr!=QSUCCESS) {
            printf("get_overlap_exp>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling QcMatCreate()");
            exit(ierr);
        }
        ierr = OpenRSPTestReadMat(OVERLAP_AO, 0, 1, val_int);
        if (ierr!=QSUCCESS) {
            printf("get_overlap_mat>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling OpenRSPTestReadMat()");
            exit(ierr);
        }
        for (idens=0; idens<num_dens; idens++) {</pre>
            ierr = QcMatGetMatProdTrace(val_int[0],
                                         ao_dens[idens],
                                         MAT_NO_OPERATION,
                                         &val_exp[2*idens]);
            if (ierr!=QSUCCESS) {
                printf("get_overlap_exp>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                        "calling QcMatGetMatProdTrace");
                exit(ierr);
            }
        }
        ierr = QcMatDestroy(val_int[0]);
```

```
if (ierr!=QSUCCESS) {
        printf("get_overlap_exp>> error happened at %s: %s\n",
               FILE_AND_LINE,
               "calling QcMatDestroy()");
        exit(ierr);
    }
    free(val_int[0]);
    val_int[0] = NULL;
else if (oper_num_pert==1 && bra_num_pert==0 && ket_num_pert==0) {
    if (oper_pert_labels[0] == PERT_GEOMETRIC) {
        printf("get_overlap_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    /* zero matrices */
    else if (oper_pert_labels[0] == PERT_DIPOLE) {
        for (idens=0; idens<2*num_exp; idens++) {</pre>
            val_exp[idens] = 0;
        }
    }
    else if (oper_pert_labels[0] == PERT_MAGNETIC) {
        printf("get_overlap_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        printf("get_overlap_exp>> unknown perturbations at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
}
else if (oper_num_pert==0 && bra_num_pert==1 && ket_num_pert==0) {
    if (bra_pert_labels[0] == PERT_GEOMETRIC) {
        printf("get_overlap_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    /* zero matrices */
    else if (bra_pert_labels[0] == PERT_DIPOLE) {
        for (idens=0; idens<2*num_exp; idens++) {</pre>
            val_exp[idens] = 0;
        }
    }
    else if (bra_pert_labels[0] == PERT_MAGNETIC) {
        printf("get_overlap_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        printf("get_overlap_exp>> unknown perturbations at %s\n",
               FILE_AND_LINE);
```

```
exit(QFAILURE);
        }
   }
    else if (oper_num_pert==0 && bra_num_pert==0 && ket_num_pert==1) {
        if (ket_pert_labels[0] == PERT_GEOMETRIC) {
            printf("get_overlap_exp>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
        /* zero matrices */
        else if (ket_pert_labels[0] == PERT_DIPOLE) {
            for (idens=0; idens<2*num_exp; idens++) {</pre>
                val_exp[idens] = 0;
            }
        }
        else if (ket_pert_labels[0] == PERT_MAGNETIC) {
            printf("get_overlap_exp>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
        else {
            printf("get_overlap_exp>> unknown perturbations at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else if (oper_num_pert==0 && bra_num_pert==1 && ket_num_pert==1) {
        /* zero matrices */
        if (bra_pert_labels[0] == PERT_DIPOLE || ket_pert_labels[0] == PERT_DIPOLE) {
            for (idens=0; idens<2*num_exp; idens++) {</pre>
                val_exp[idens] = 0;
            }
        }
        else {
            printf("get_overlap_exp>> unknown perturbations at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else {
         printf("get_overlap_exp>> not implemented at %s\n",
                FILE_AND_LINE);
         exit(QFAILURE);
    }
}
void get_one_oper_mat(const QInt oper_num_pert,
                      const QcPertInt *oper_pert_labels,
                       const QInt *oper_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                      void *user_ctx,
#endif
```

```
const QInt num_int,
                      QcMat *val_int[])
{
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *one_oper_context;
#endif
   QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    one_oper_context = (char *)user_ctx;
    if (strcmp(one_oper_context, ONEHAM_CONTEXT)==0) {
        /* zero matrices */
        if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
            ierr = OpenRSPTestZeroMat(num_int, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTestZeroMat()");
                exit(ierr);
            }
        }
        else {
            printf("get_one_oper_mat>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else if (strcmp(one_oper_context, EXT_FIELD_CONTEXT)==0) {
        if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
            /* unperturbed AO-based dipole length integral matrices */
            if (oper_pert_orders[0]==1) {
                ierr = OpenRSPTestReadMat(DIPLEN_AO, 0, 3, val_int);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_mat>> error happened at %s: %s\n",
                           FILE_AND_LINE,
                           "calling OpenRSPTestReadMat()");
                    exit(ierr);
                }
            }
            /* zero matrices */
            else {
                ierr = OpenRSPTestZeroMat(num_int, val_int);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_mat>> error happened at %s: %s\n",
                           FILE_AND_LINE,
                           "calling OpenRSPTestZeroMat()");
                    exit(ierr);
                }
            }
        }
        else {
            printf("get_one_oper_mat>> not implemented at %s\n",
```

```
FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else {
        printf("get_one_oper_mat>> unknown one-electron operator at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
#else
    if (oper_num_pert==1 && oper_pert_labels[0] == PERT_DIPOLE) {
        /* unperturbed AO-based dipole length integral matrices */
        if (oper_pert_orders[0] == 1) {
            ierr = OpenRSPTestReadMat(DIPLEN_AO, 0, 3, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTestReadMat()");
                exit(ierr);
            }
        /* zero matrices */
        else {
            ierr = OpenRSPTestZeroMat(num_int, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_one_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTestZeroMat()");
                exit(ierr);
            }
        }
   }
    else {
        printf("get_one_oper_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
   }
#endif
}
void get_one_oper_exp(const QInt oper_num_pert,
                      const QcPertInt *oper_pert_labels,
                      const QInt *oper_pert_orders,
                      const QInt num_dmat,
                      QcMat *dens_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
                      void *user_ctx,
#endif
                      const QInt num_exp,
                      QReal *val_exp)
{
#include "OpenRSPTestPerturbations.h"
```

```
#if defined(OPENRSP_C_USER_CONTEXT)
    char *one_oper_context;
#endif
    QcMat *val_int[1];
    QInt imat;
   QInt offset_exp;
   QInt idens;
    QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    one_oper_context = (char *)user_ctx;
    if (strcmp(one_oper_context, ONEHAM_CONTEXT)==0) {
        /* zero matrices */
        if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
            for (idens=0; idens<2*num_exp; idens++) {</pre>
                val_exp[idens] = 0;
        }
        else {
            printf("get_one_oper_exp>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
   }
    else if (strcmp(one_oper_context, EXT_FIELD_CONTEXT)==0) {
        if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
            /* unperturbed AO-based dipole length integral matrices */
            if (oper_pert_orders[0] == 1) {
                val_int[0] = (QcMat *)malloc(sizeof(QcMat));
                if (val_int[0] == NULL) {
                    printf("get_one_oper_exp>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "allocats memory for matrix");
                    exit(QFAILURE);
                }
                offset_exp = 0;
                for (imat=0; imat<3; imat++) {</pre>
                    ierr = QcMatCreate(val_int[0]);
                    if (ierr!=QSUCCESS) {
                        printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling QcMatCreate()");
                        exit(ierr);
                    }
                    ierr = OpenRSPTestReadMat(DIPLEN_AO, imat, 1, val_int);
                    if (ierr!=QSUCCESS) {
                        printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling OpenRSPTestReadMat()");
                        exit(ierr);
                    for (idens=0; idens<num_dmat; idens++) {</pre>
                         ierr = QcMatGetMatProdTrace(val_int[0],
```

dens_mat[idens],

```
MAT_NO_OPERATION,
                                                      &val_exp[offset_exp+2*idens]);
                         if (ierr!=QSUCCESS) {
                             printf("get_one_oper_exp>> error happened at %s: %s\n",
                                    FILE_AND_LINE,
                                    "calling QcMatGetMatProdTrace()");
                             exit(ierr);
                        }
                    }
                    ierr = QcMatDestroy(val_int[0]);
                    if (ierr!=QSUCCESS) {
                        printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling QcMatDestroy()");
                        exit(ierr);
                    }
                    offset_exp += 2*num_dmat;
                }
                free(val_int[0]);
                val_int[0] = NULL;
            }
            /* zero matrices */
            else {
                for (idens=0; idens<2*num_exp; idens++) {</pre>
                    val_exp[idens] = 0;
                }
            }
        }
        else {
            printf("get_one_oper_exp>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
    else {
        printf("get_one_oper_exp>> unknown one-electron operator at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
#else
    if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
        /* unperturbed AO-based dipole length integral matrices */
        if (oper_pert_orders[0]==1) {
            offset_exp = 0;
            for (imat=0; imat<3; imat++) {</pre>
                ierr = QcMatCreate(&val_int[0]);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_exp>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "calling QcMatCreate()");
```

```
exit(ierr);
                }
                ierr = OpenRSPTestReadMat(DIPLEN_AO, imat, 1, val_int);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_exp>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "calling OpenRSPTestReadMat()");
                     exit(ierr);
                }
                for (idens=0; idens<num_dmat; idens++) {</pre>
                     ierr = QcMatGetMatProdTrace(&val_int[0],
                                                  dens_mat[idens],
                                                  MAT_NO_OPERATION,
                                                  1,
                                                  &val_exp[offset_exp+2*idens]);
                     if (ierr!=QSUCCESS) {
                         printf("get_one_oper_exp>> error happened at %s: %s\n",
                                FILE_AND_LINE,
                                "calling QcMatGetMatProdTrace()");
                         exit(ierr);
                    }
                }
                ierr = QcMatDestroy(val_int[0]);
                if (ierr!=QSUCCESS) {
                    printf("get_one_oper_exp>> error happened at %s: %s\n",
                            FILE_AND_LINE,
                            "calling QcMatDestroy()");
                     exit(ierr);
                }
                offset_exp += 2*num_dmat;
            }
        }
        /* zero matrices */
        else {
            for (idens=0; idens<2*num_exp; idens++) {</pre>
                val_exp[idens] = 0;
            }
        }
        printf("get_one_oper_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
}
void get_two_oper_mat(const QInt oper_num_pert,
                       const QcPertInt *oper_pert_labels,
                       const QInt *oper_pert_orders,
                       const QInt num_dmat,
                       QcMat *dens_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
```

```
void *user_ctx,
#endif
                      const QInt num_int,
                      QcMat *val_int[])
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
    char *two_oper_context;
#endif
    QErrorCode ierr;
    static QInt id_gmat = -1;
#if defined(OPENRSP_C_USER_CONTEXT)
    two_oper_context = (char *)user_ctx;
    if (strcmp(two_oper_context, TWO_OPER_CONTEXT)!=0) {
        printf("get_two_oper_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        /* two-electron integrals contracted with perturbed AO-based density
           matrices for solving polarizability at frequency as 0.072 */
        if (oper_num_pert==0) {
            id_gmat++;
            if (id_gmat>5) {
                printf("get_two_oper_mat>> not implemented at %s\n",
                       FILE_AND_LINE);
                exit(QFAILURE);
            }
            ierr = OpenRSPTestReadMat(ALPHA_GMAT_AO_HF, id_gmat, 1, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_two_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTestReadMat()");
                exit(ierr);
            }
        }
        /* zero matrices */
        else if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
            ierr = OpenRSPTestZeroMat(num_int, val_int);
            if (ierr!=QSUCCESS) {
                printf("get_two_oper_mat>> error happened at %s: %s\n",
                       FILE_AND_LINE,
                       "calling OpenRSPTestZeroMat()");
                exit(ierr);
            }
        }
        else {
            printf("get_two_oper_mat>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
   }
```

```
#else
    /* two-electron integrals contracted with perturbed AO-based density
       matrices for solving polarizability at frequency as 0.072 */
    if (oper_num_pert==0) {
        id_gmat++;
        if (id_gmat>5) {
            printf("get_two_oper_mat>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
        ierr = OpenRSPTestReadMat(ALPHA_GMAT_AO_HF, id_gmat, 1, val_int);
        if (ierr!=QSUCCESS) {
            printf("get_two_oper_mat>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling OpenRSPTestReadMat()");
            exit(ierr);
        }
    }
    /* zero matrices */
    else if (oper_num_pert==1 && oper_pert_labels[0] == PERT_DIPOLE) {
        ierr = OpenRSPTestZeroMat(num_int, val_int);
        if (ierr!=QSUCCESS) {
            printf("get_two_oper_mat>> error happened at %s: %s\n",
                   FILE_AND_LINE,
                   "calling OpenRSPTestZeroMat()");
            exit(ierr);
        }
    }
    else {
        printf("get_two_oper_mat>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
#endif
}
void get_two_oper_exp(const QInt oper_num_pert,
                      const QcPertInt *oper_pert_labels,
                      const QInt *oper_pert_orders,
                      const QInt dmat_len_tuple,
                      const QInt *num_LHS_dmat,
                      QcMat *LHS_dens_mat[],
                      const QInt *num_RHS_dmat,
                      QcMat *RHS_dens_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
                      void *user_ctx,
#endif
                      const QInt num_exp,
                      QReal *val_exp)
#include "OpenRSPTestPerturbations.h"
#if defined(OPENRSP_C_USER_CONTEXT)
```

```
char *two_oper_context;
#endif
   QInt ival;
    QErrorCode ierr;
#if defined(OPENRSP_C_USER_CONTEXT)
    two_oper_context = (char *)user_ctx;
    if (strcmp(two_oper_context, TWO_OPER_CONTEXT)!=0) {
        printf("get_two_oper_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
    }
    else {
        /* zero matrices */
        if (oper_num_pert==1 && oper_pert_labels[0] == PERT_DIPOLE) {
            for (ival=0; ival<2*num_exp; ival++) {</pre>
                val_exp[ival] = 0;
            }
        }
        else {
            printf("get_two_oper_exp>> not implemented at %s\n",
                   FILE_AND_LINE);
            exit(QFAILURE);
        }
    }
#else
    /* zero matrices */
    if (oper_num_pert==1 && oper_pert_labels[0]==PERT_DIPOLE) {
        for (ival=0; ival<2*num_exp; ival++) {</pre>
            val_exp[ival] = 0;
        }
    }
    else {
        printf("get_two_oper_exp>> not implemented at %s\n",
               FILE_AND_LINE);
        exit(QFAILURE);
#endif
}
void get_linear_rsp_solution(const QInt size_pert,
                              const QReal *freq_sums,
                              const QInt num_freq_sums,
                              QcMat *RHS_mat[],
#if defined(OPENRSP_C_USER_CONTEXT)
                              void *user_ctx,
#endif
                              QcMat *rsp_param[])
#if defined(OPENRSP_C_USER_CONTEXT)
    char *solver_context;
#endif
    static QInt id_rsparam = -1;
```

```
QErrorCode ierr;
         #if defined(OPENRSP_C_USER_CONTEXT)
             solver_context = (char *)user_ctx;
              if (strcmp(solver_context, SOLVER_CONTEXT)!=0) {
                  printf("get_linear_rsp_solution>> invalid context at %s\n",
                         FILE_AND_LINE);
                  exit(QFAILURE);
             }
         #endif
             id_rsparam++;
             if (id_rsparam>2) {
                  printf("get_linear_rsp_solution>> not implemented at %s\n",
                         FILE_AND_LINE);
                  exit(QFAILURE);
             }
             ierr = OpenRSPTestReadMat(ALPHA_RSPARAM_AO_HF, id_rsparam, 1, rsp_param);
              if (ierr!=QSUCCESS) {
                  printf("get_linear_rsp_solution>> error happened at %s: %s\n",
                         FILE_AND_LINE,
                         "calling OpenRSPTestReadMat()");
                  exit(ierr);
             }
         }
       The atomic-orbital density matrix-based response theory is tested by:
206a
       \langle OpenRSPDensAOTest.h \ 206a \rangle \equiv
         /*
           ⟨OpenRSPLicense 14a⟩
            This is the header file of unit testing of the AO density matrix-based
            response theory.
            2014-07-31, Bin Gao
            * first version
         */
         #if !defined(OPENRSP_DENS_AO_TEST_H)
         #define OPENRSP_DENS_AO_TEST_H
         #include "OpenRSPPertCallback.h"
         #include "OpenRSPDensAOCallback.h"
         extern QErrorCode OpenRSPDensAOTest(OpenRSP*,FILE*);
         #endif
       \langle OpenRSPDensAOTest.c \ 206b \rangle \equiv
206b
           ⟨OpenRSPLicense 14a⟩
            This file tests the AO density matrix-based response theory.
            2014-07-31, Bin Gao
            * first version
```

```
*/
#include "OpenRSPDensAOTest.h"
#if defined(QCMATRIX_SINGLE_PRECISION)
#define QCREAL_FMT "f"
#else
#define QCREAL_FMT "lf"
#endif
QErrorCode OpenRSPDensAOTest(OpenRSP *open_rsp, FILE *fp_log)
#include "OpenRSPTestPerturbations.h"
    /* overlap operator */
    QInt overlap_num_pert=2;
    QcPertInt overlap_pert_labels[]={PERT_GEOMETRIC,
                                     PERT_MAGNETIC};
   QInt overlap_pert_orders[] = {MAX_ORDER_GEOMETRIC,
                                MAX_ORDER_MAGNETIC};
    /* one-electron Hamiltonian */
    QInt oneham_num_pert=2;
    QcPertInt oneham_pert_labels[]={PERT_GEOMETRIC,
                                    PERT_MAGNETIC};
    QInt oneham_pert_orders[]={MAX_ORDER_GEOMETRIC,
                               MAX_ORDER_MAGNETIC};
    /* external field */
    QInt ext_field_num_pert=3;
    QcPertInt ext_field_pert_labels[]={PERT_GEOMETRIC,
                                       PERT_DIPOLE,
                                       PERT_MAGNETIC};
    QInt ext_field_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                  MAX_ORDER_DIPOLE,
                                  MAX_ORDER_MAGNETIC};
    /* two-electron operator */
    QInt two_oper_num_pert=2;
    QcPertInt two_oper_pert_labels[]={PERT_GEOMETRIC,
                                      PERT_MAGNETIC;
    QInt two_oper_pert_orders[]={MAX_ORDER_GEOMETRIC,
                                 MAX_ORDER_MAGNETIC};
    /* referenced state */
    QcMat *F_unpert[1];
    QcMat *D_unpert[1];
    QcMat *S_unpert[1];
    /* polarizability */
    QInt ALPHA_NUM_PROPS=1;
    QInt ALPHA_LEN_TUPLE[]={2};
    QcPertInt ALPHA_PERT_TUPLE[]={PERT_DIPOLE, PERT_DIPOLE};
    QInt ALPHA_NUM_FREQ_CONFIGS[]={1};
    QReal ALPHA_PERT_FREQS[]={-0.072,0.0,0.072,0.0};
    QInt ALPHA_KN_RULES[]={0};
    /* response functions */
    QInt size_rsp_funs;
```

```
QReal rsp_funs[18];
    QInt ipert, jpert, ival;
    /* error information */
    QErrorCode ierr;
    ///* sets the equation of motion of electrons */
    //ierr = OpenRSPSetElecEOM(open_rsp, ELEC_AO_D_MATRIX);
    //QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetElecEOM");
    //fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPSetElecEOM() passed\n");
    /* sets the context of linear response equation solver */
    ierr = OpenRSPSetLinearRSPSolver(open_rsp,
#if defined(OPENRSP_C_USER_CONTEXT)
                                     (void *)SOLVER_CONTEXT,
#endif
                                     &get_linear_rsp_solution);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetLinearRSPSolver()");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPSetLinearRSPSolver() passed\n");
    /* sets the context of overlap operator */
    ierr = OpenRSPSetOverlap(open_rsp,
                             overlap_num_pert,
                             overlap_pert_labels,
                             overlap_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             (void *)OVERLAP_CONTEXT,
#endif
                             &get_overlap_mat,
                             &get_overlap_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetOverlap()");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPSetOverlap() passed\n");
    /* adds one-electron Hamiltonian */
    ierr = OpenRSPAddOneOper(open_rsp,
                             oneham_num_pert,
                             oneham_pert_labels,
                             oneham_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             (void *)ONEHAM_CONTEXT,
#endif
                             &get_one_oper_mat,
                             &get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddOneOper(h)");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPAddOneOper(h) passed\n");
    /* adds external field */
    ierr = OpenRSPAddOneOper(open_rsp,
                             ext_field_num_pert,
                             ext_field_pert_labels,
                             ext_field_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             (void *)EXT_FIELD_CONTEXT,
```

```
#endif
```

```
&get_one_oper_mat,
                             &get_one_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddOneOper(V)");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPAddOneOper(V) passed\n");
    /* adds two-electron operator */
    ierr = OpenRSPAddTwoOper(open_rsp,
                             two_oper_num_pert,
                             two_oper_pert_labels,
                             two_oper_pert_orders,
#if defined(OPENRSP_C_USER_CONTEXT)
                             (void *)TWO_OPER_CONTEXT,
#endif
                             &get_two_oper_mat,
                             &get_two_oper_exp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAddTwoOper()");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPAddTwoOper() passed\n");
    /* assembles the context of response theory calculations */
    ierr = OpenRSPAssemble(open_rsp);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPAssemble()");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPAssemble() passed\n");
    /* writes the context of response theory calculations */
    ierr = OpenRSPWrite(open_rsp, fp_log);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPWrite()");
    fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPWrite() passed\n");
    /* sets the unperturbed AO-based Fock matrix */
   F_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
    if (F_unpert[0] == NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for Fock matrix");
    }
    ierr = QcMatCreate(F_unpert[0]);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatCreate(F)");
    ierr = OpenRSPTestReadMat(FOCK_AO_HF, 0, 1, F_unpert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(F)");
    /* sets the unperturbed AO-based density matrix */
    D_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
    if (D_unpert[0] == NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for density matrix");
    }
    ierr = QcMatCreate(D_unpert[0]);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatCreate(D)");
    ierr = OpenRSPTestReadMat(DENS_AO_HF, 0, 1, D_unpert);
    QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(D)");
    /* sets the unperturbed AO-based overlap integral matrix */
    S_unpert[0] = (QcMat *)malloc(sizeof(QcMat));
    if (S_unpert[0] == NULL) {
        QErrorExit(FILE_AND_LINE, "allocates memory for overlap integral matrix");
    }
```

```
ierr = QcMatCreate(S_unpert[0]);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatCreate(S)");
            ierr = OpenRSPTestReadMat(OVERLAP_AO, 0, 1, S_unpert);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPTestReadMat(S)");
            /* gets the polarizability */
            size_rsp_funs = 9;
            ierr = OpenRSPGetRSPFun(open_rsp,
                                     F_unpert[0],
                                     D_unpert[0],
                                     S_unpert[0],
                                     ALPHA_NUM_PROPS,
                                     ALPHA_LEN_TUPLE,
                                     ALPHA_PERT_TUPLE,
                                     ALPHA_NUM_FREQ_CONFIGS,
                                     ALPHA_PERT_FREQS,
                                     ALPHA_KN_RULES,
                                     size_rsp_funs,
                                     rsp_funs);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPGetRSPFun()");
            fprintf(fp_log, "OpenRSPDensAOTest>> OpenRSPGetRSPFun() passed\n");
            for (ipert=0,ival=0; ipert<3; ipert++) {</pre>
                for (jpert=0; jpert<3; jpert++) {</pre>
                     fprintf(fp_log,
                             " (%"QCREAL_FMT",%"QCREAL_FMT")",
                             rsp_funs[ival], rsp_funs[ival+1]);
                     ival += 2;
                }
                fprintf(fp_log, "\n");
            }
            /* cleans */
            ierr = QcMatDestroy(F_unpert[0]);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(F)");
            free(F_unpert[0]);
            F_unpert[0] = NULL;
            ierr = QcMatDestroy(D_unpert[0]);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(D)");
            free(D_unpert[0]);
            D_unpert[0] = NULL;
            ierr = QcMatDestroy(S_unpert[0]);
            QErrorCheckCode(ierr, FILE_AND_LINE, "calling QcMatDestroy(S)");
            free(S_unpert[0]);
            S_unpert[0] = NULL;
            return QSUCCESS;
        }
210
      \langle OpenRSPTest.h \ 210 \rangle \equiv
          ⟨OpenRSPLicense 14a⟩
```

```
This is the header file of OpenRSP unit testing.
          2014-07-31, Bin Gao:
          * first version
        #if !defined(OPENRSP_TEST_H)
        #define OPENRSP_TEST_H
        #include <string.h>
        #include "OpenRSP.h"
        #include "OpenRSPTestPerturbations.h"
        #include "OpenRSPPertCallback.h"
        #include "OpenRSPNucHamiltonCallback.h"
        #include "OpenRSPDensAOTest.h"
        #if !defined(OPENRSP_TEST_EXECUTABLE)
        extern QErrorCode OpenRSPTest(FILE *fp_log);
        #endif
        #endif
      \langle OpenRSPTest.c \ 211 \rangle \equiv
211
        /*
          \langle OpenRSPLicense 14a \rangle
           This file tests the APIs of OpenRSP library.
           2014-07-31, Bin Gao
           * first version
        */
        #include "OpenRSPTest.h"
        /* <macrodef name='OPENRSP_TEST_EXECUTABLE'>
             Build test suite as excutables.
           </macrodef> */
        #if defined(OPENRSP_TEST_EXECUTABLE)
        QErrorCode main()
            FILE *fp_log=stdout; /* file pointer */
        QErrorCode OpenRSPTest(FILE *fp_log)
        #endif
        #include "OpenRSPTestPerturbations.h"
            OpenRSP open_rsp; /* context of response theory calculations */
            QErrorCode ierr; /* error information */
            /* creates the context of response theory calculations */
            ierr = OpenRSPCreate(&open_rsp);
```

```
QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPCreate()");
     fprintf(fp_log, "OpenRSPTest>> OpenRSPCreate() passed\n");
     /* sets information of all perturbations */
     ierr = OpenRSPSetPerturbations(&open_rsp,
                                     NUM_ALL_PERT,
                                     ALL_PERT_LABELS,
                                     ALL_PERT_MAX_ORDERS,
                                     ALL_PERT_SIZES,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                      (void *)PERT_CONTEXT,
 #endif
                                     &get_pert_concatenation);
     QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetPerturbations()");
     fprintf(fp_log, "OpenRSPTest>> OpenRSPSetPerturbations() passed\n");
     /* sets the nuclear Hamiltonian */
     ierr = OpenRSPSetNucHamilton(&open_rsp,
                                   NUM_ALL_PERT,
                                   ALL_PERT_LABELS,
                                   ALL_PERT_MAX_ORDERS,
 #if defined(OPENRSP_C_USER_CONTEXT)
                                    (void *)NUC_HAMILTON_CONTEXT,
 #endif
                                   &get_nuc_contrib,
                                   NUM_ATOMS);
     QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPSetNucHamilton()");
     fprintf(fp_log, "OpenRSPTest>> OpenRSPSetNucHamilton() passed\n");
     /* tests the density matrix-based response theory */
     ierr = OpenRSPDensAOTest(&open_rsp, fp_log);
     QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPDensAOTest()");
     fprintf(fp_log, "OpenRSPTest>> density matrix-based response theory passed\n");
     /* destroys the context of response theory calculations */
     ierr = OpenRSPDestroy(&open_rsp);
     QErrorCheckCode(ierr, FILE_AND_LINE, "calling OpenRSPDestroy()");
     fprintf(fp_log, "OpenRSPTest>> OpenRSPDestroy() passed\n");
     return QSUCCESS;
 }
3.13.2 Testing Fortran APIs
\langle OpenRSPTest.F90 \ 212 \rangle \equiv
 !! <QcLang='Fortran'>
 ⟨OpenRSPLicenseFortran 115a⟩
 !! This file tests the Fortran APIs of OpenRSP library.
 !!
 !! 2014-08-03, Bin Gao
 !! * first version
```

Chapter 4

Maintenance

4.1 Support and Citation

If there is any question regarding the use of OPENRSP, please contact the authors as given in the file AUTHORS.rst.

If you have used OPENRSP and found it is useful, please consider to cite OPENRSP as described in the file openrsp.bib.

4.2 List of Chunks

```
⟨OpenRSPAPIs 14c⟩
\langle OpenRSPDensAOCallback.c 192 \rangle
\langle OpenRSPDensAOCallback.h \ 184c \rangle
\langle OpenRSPDensAOTest.c \ 206b \rangle
\langle OpenRSPDensAOTest.h \ 206a \rangle
\langle OpenRSP.F90 \ 115b \rangle
\langle OpenRSPFortranAdapter.c 179 \rangle
\langle OpenRSPLicense 14a \rangle
\langle OpenRSPLicenseFortran 115a \rangle
\langle OpenRSPNucHamiltonCallback.c 184b \rangle
\langle OpenRSPNucHamiltonCallback.h \ 184a \rangle
\langle OpenRSPPertCallback.c \ 183b \rangle
\langle OpenRSPPertCallback.h \ 183a \rangle
\langle OpenRSPStruct 14b \rangle
\langle OpenRSPTestData.c \ 188 \rangle
\langle OpenRSPTestData.cmake\ 187 \rangle
\langle OpenRSPTest.F90 \ 212 \rangle
\langle OpenRSPTestPerturbations.c \ 182b \rangle
\langle OpenRSPTestPerturbations.h \ 182a \rangle
\langle OpenRSPTest.c \ 211 \rangle
\langle OpenRSPTest.h \ 210 \rangle
\langle OpenRSP.c \ 17a \rangle
\langle OpenRSP.h \ 13 \rangle
\langle RSNucHamiltonStruct\ 98a \rangle
\langle RSPNucHamiltonAPIs 98b \rangle
\langle RSPNucHamilton.F90 \ 172 \rangle
\langle RSPNucHamilton.c \ 98c \rangle
\langle RSPNucHamilton.h | 97 \rangle
\langle RSPOneOperAPIs \ 57b \rangle
\langle RSPOneOper.F90 \ 152 \rangle
```

214 web/Maintenance.tex October 18, 2015

```
\langle RSPOneOperStruct 57a \rangle
\langle RSPOneOper.c 58 \rangle
\langle RSPOneOper.h \ 56 \rangle
\langle RSPOverlapAPIs \ 44a \rangle
\langle RSPOverlap.F90 \ 144 \rangle
\langle RSPOverlapStruct \ 43 \rangle
\langle RSPOverlap.c \ 44b \rangle
\langle RSPOverlap.h \ 42 \rangle
\langle RSPPertBasicTypes \ 21b \rangle
\langle RSPPertBasicTypes.F90 \ 140 \rangle
\langle RSPPertCallback 23a \rangle
\langle RSPPertStruct \ 23b \rangle
\langle RSPPerturbation. F90 \ 141 \rangle
\langle RSPPerturbation.c \ 22c \rangle
\langle RSPPerturbation.h \ 21a \rangle
\langle RSPSolverAPIs \ 107b \rangle
\langle RSPSolver.F90 \ 175 \rangle
\langle RSPSolverStruct\ 107a \rangle
\langle RSPSolver.c \ 107c \rangle
\langle RSPSolver.h \ 106b \rangle
\langle RSPTwoOperAPIs \ 70b \rangle
\langle RSPTwoOperStruct 70a \rangle
\langle RSPTwoOper.c \ 71 \rangle
\langle RSPTwoOper.h 69 \rangle
\langle RSPTwoper.F90 \ 158 \rangle
\langle RSPXCFunAPIs 84b \rangle
\langle RSPXCFun.F90 \ 165 \rangle
\langle RSPXCFunStruct 84a \rangle
\langle RSPXCFun.c.85 \rangle
\langle RSPXCFun.h \ 83 \rangle
⟨RSPertAPIs 25a⟩
```

Bibliography

- [1] Andreas J. Thorvaldsen, Kenneth Ruud, Kasper Kristensen, Poul Jørgensen, and Sonia Coriani. A density matrix-based quasienergy formulation of the Kohn–Sham density functional response theory using perturbation- and time-dependent basis sets. *J. Chem. Phys.*, 129(21):214108, 2008.
- [2] Radovan Bast, Ulf Ekström, Bin Gao, Trygve Helgaker, Kenneth Ruud, and Andreas J. Thorvaldsen. The ab initio calculation of molecular electric, magnetic and geometric properties. *Phys. Chem. Chem. Phys.*, 13(7):2627–2651, 2011.
- [3] Radovan Bast, Andreas J. Thorvaldsen, Magnus Ringholm, and Kenneth Ruud. Atomic orbital-based cubic response theory for one-, two-, and four-component relativistic self-consistent field models. *Chem. Phys.*, 356(1–3):177–186, 2009.
- [4] Magnus Ringholm, Dan Jonsson, and Kenneth Ruud. A General, Recursive, and Open-Ended Response Code. J. Comput. Chem., 35(8):622–633, 2014.
- [5] Daniel H. Friese, Maarten T. P. Beerepoot, Magnus Ringholm, and Kenneth Ruud. Open-Ended Recursive Approach for the Calculation of Multiphoton Absorption Matrix Elements. *J. Chem. Theory Comput.*, 11(3):1129–1144, 2015.

Index

```
OPENRSP Fortran APIs, 9
OpenRSP License, 14, 115
OPENRSP Fortran APIs, 115
OpenRSP framework, 9
QCMATRIX library, 9
OpenRSP.h, 13
OPENRSP_PERT_ID_MAX, 22
OPENRSP_PERT_LABEL_BIT, 21
OPENRSP_PERT_LABEL_MAX, 22
OpenRSPAssemble(), 17
OpenRSPCreate(), 17
OpenRSPDestroy(), 17
OpenRSPSetPerturbations(), 24
OpenRSPWrite(), 17
QCPERTINT_FMT, 22
QCPERTINT_MAX, 22
QcPertInt, 22
struct OpenRSP, 14
Callback function scheme, 9
Include guard, 13
Open-ended response theory, 8
Support and citation, 213
Theoretical background, 8
Unit testing, 182
User-defined context, 16
Version numbering scheme, 5
```