



INSTITUTE FOR
SUSTAINABLE
AVIATION



CERFACS
CENTRE EUROPÉEN DE RECHERCHE ET DE FORMATION AVANÇÉE EN CALCUL SCIENTIFIQUE

ISAE
Institut Supérieur de l'Aéronautique et de l'Espace
SUPAERO

OpenTURNS User Day #16

23 March 2023

Modeling the impact of atmospheric variables on
the performance of an aircraft during take-off:

*Towards the adaptation of air traffic
operations to global warming*

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Directors: Sophie Ricci⁽¹⁾, Nicolas Gourdain⁽²⁾

⁽²⁾ DAEP, ISAE-SUPAERO,
Univ. of Toulouse

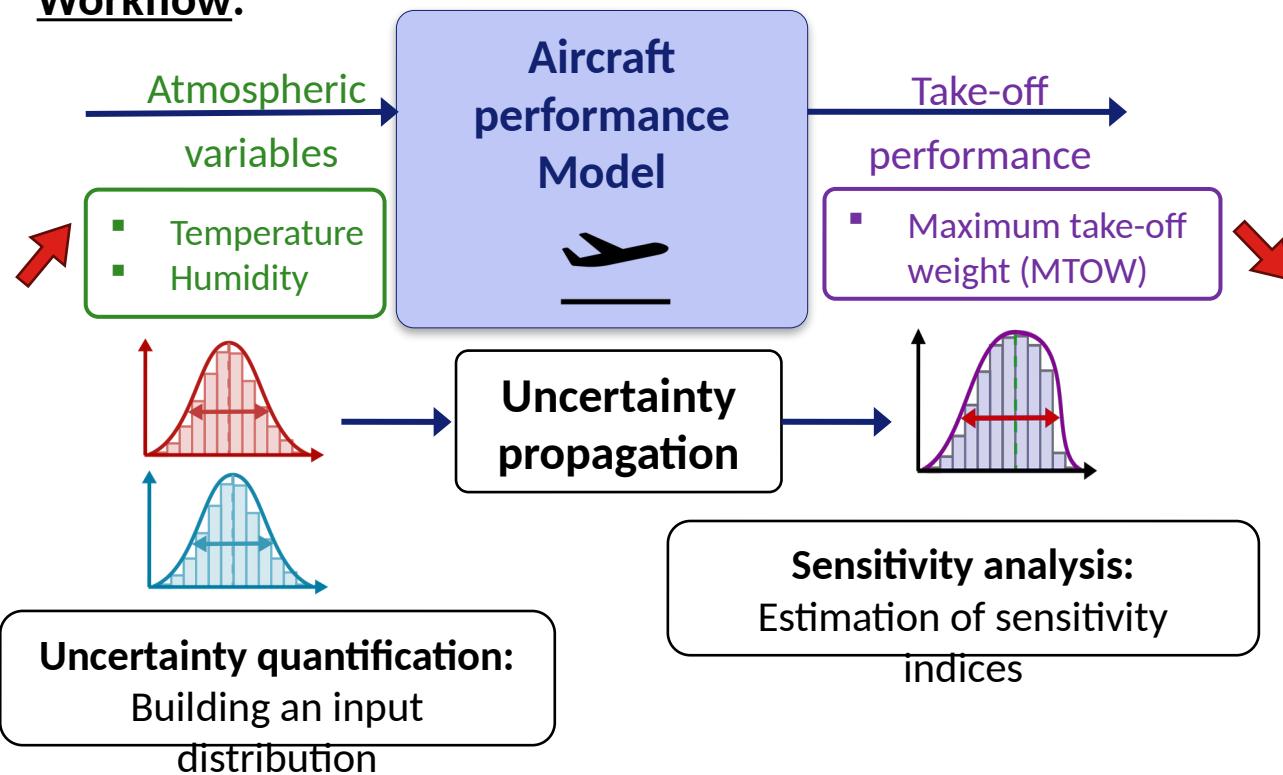
Introduction



Context of the study

How will atmospheric changes due to climate change affect aircraft performance during take-off in the future?

Workflow:



- ✉ Quantify the influence of atmospheric input variables on aircraft performance output
- ✉ Quantify the sensitivity of performance to these variables

Variables

- **Huss:** Daily mean specific humidity
- **Tasmax:** Daily maximum temperature (K)

Specific humidity:

mass of water vapor

total mass of the air parcel

Future period:

- 2015-2100 (In this presentation: 2020-2050)

Localization:

- Database of 13 airports around the world

4 different SSP (Shared Socio-economic Pathways) scenarios:

- SSP1-2.6, SSP2-4.5, SSP3-7.0, and SSP5-8.5

Outputs of climate model: CNRM-CM6-1

- Fully coupled atmosphere-ocean general circulation model
- Developed by the CNRM/CERFACS modelling group for CMIP6 project [4]

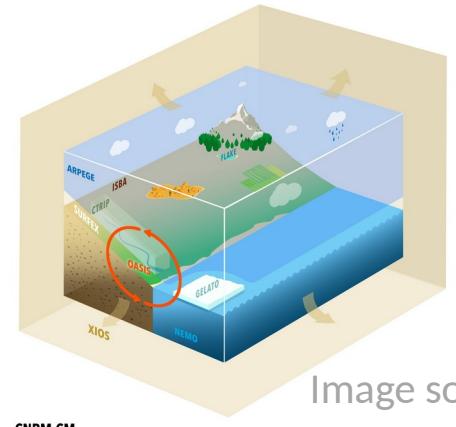
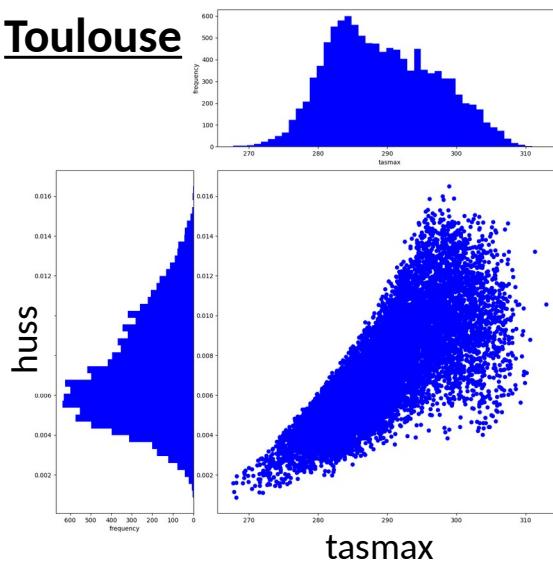


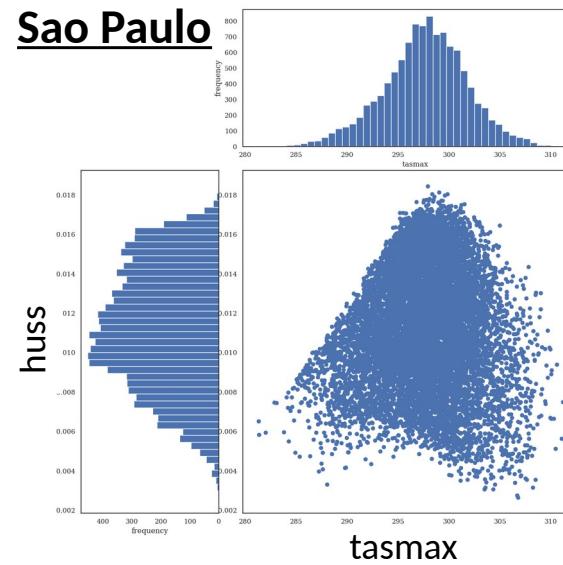
Image source:
umr-cnrm

What the data looks like

Toulouse



Sao Paulo

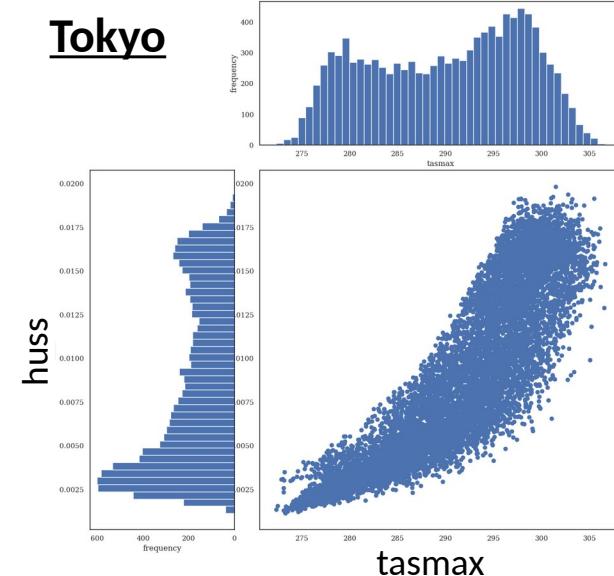


In the values space

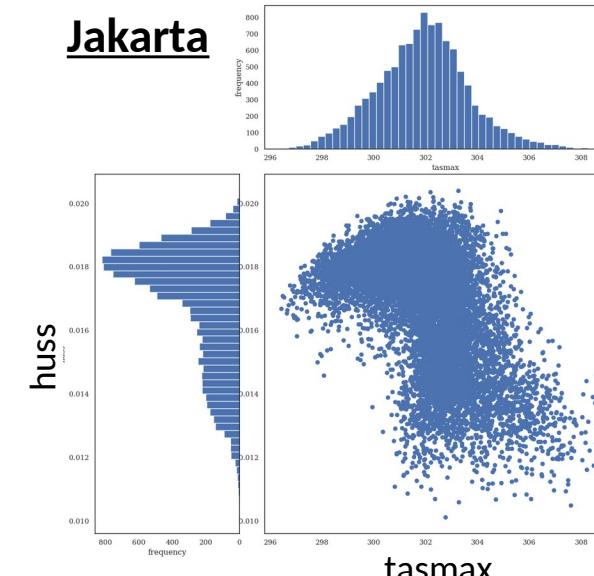
- Daily variables for period 2020-2050
→ 10 956 data points
- Scenario SSP 3.7-0

Tasmax and huss correlated?

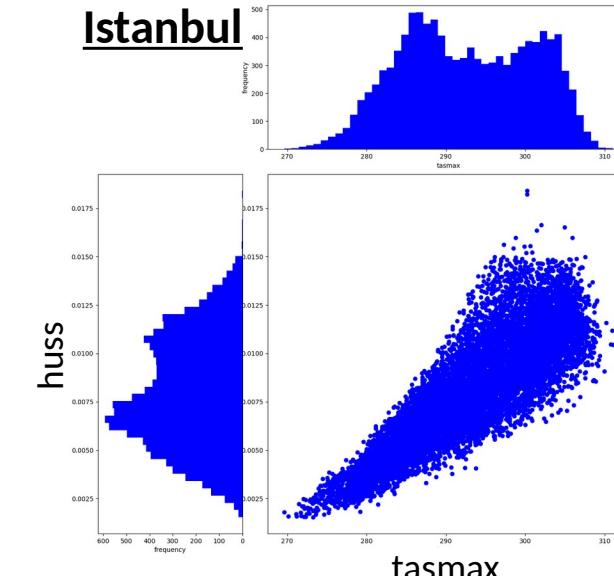
Tokyo



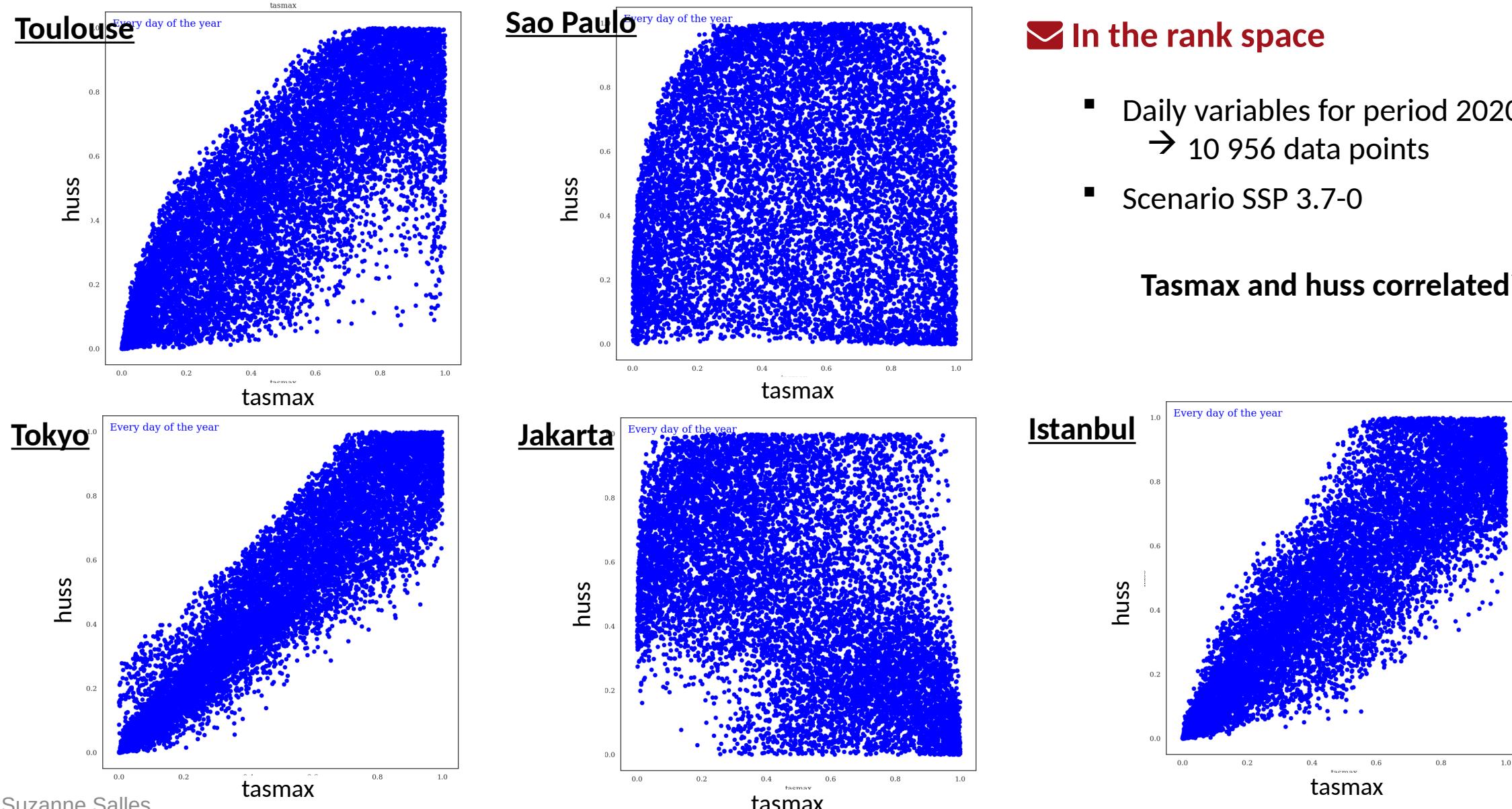
Jakarta



Istanbul



What the data looks like



In the rank space

- Daily variables for period 2020-2050
→ 10 956 data points
- Scenario SSP 3.7-0

Tasmax and huss correlated?

Focusing on extreme values

1. Summer
2. Quantiles
3. Critical threshold

Focusing on extreme values

- 1. Summer
- 2. Quantiles
- 3. Critical threshold

3-month summer restriction

Strict summer definition

North hemisphere:

June, July, August

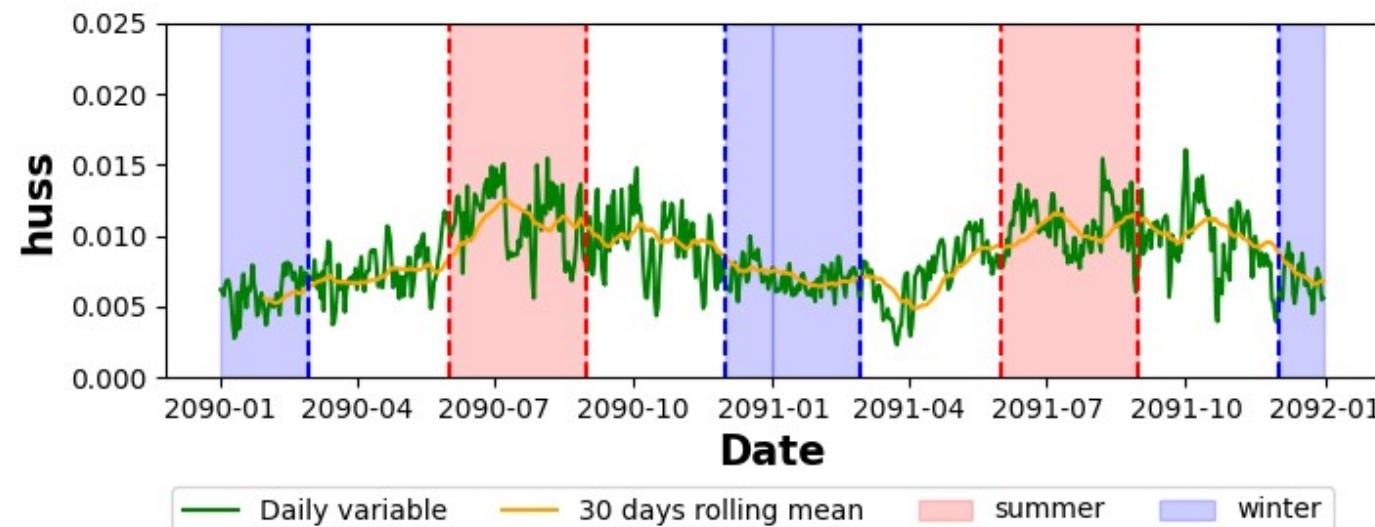
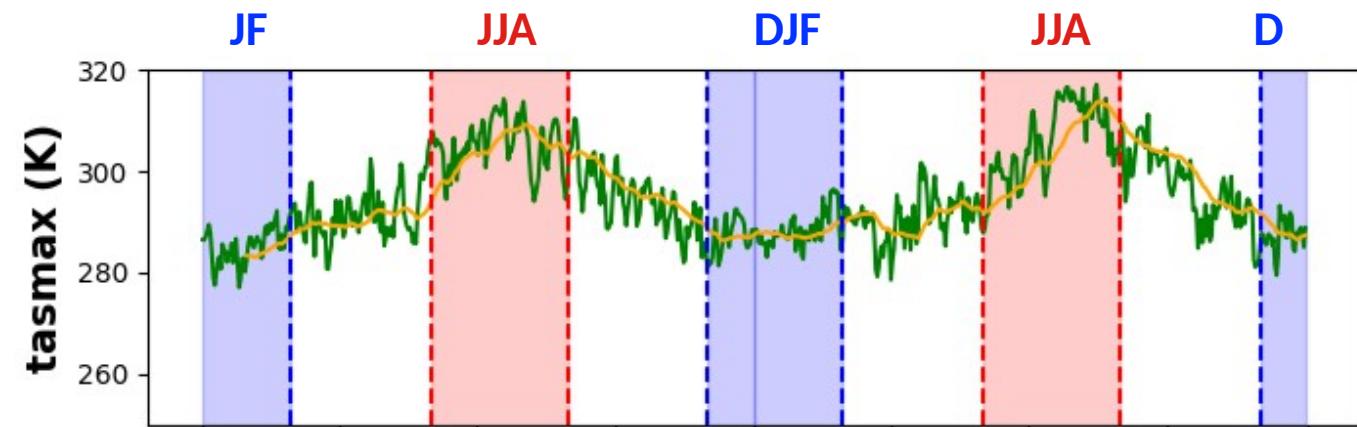
South hemisphere:

December, January, February

- Data fluctuates a lot
- Summer season seems to be when the variables are the highest

Toulouse

Plot of daily data for 2 years



3-month summer restriction

Strict summer definition

North hemisphere:

June, July, August

South hemisphere:

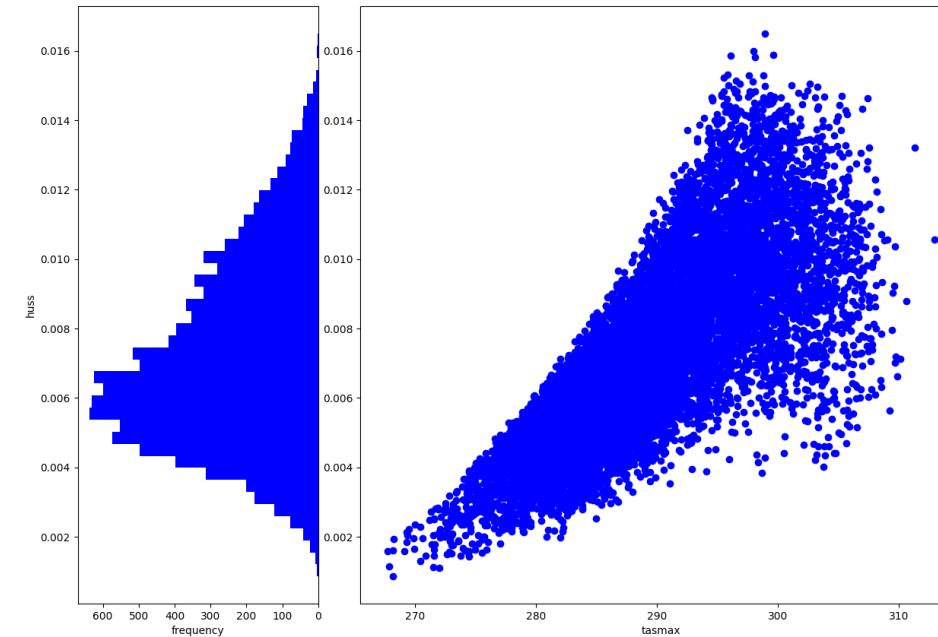
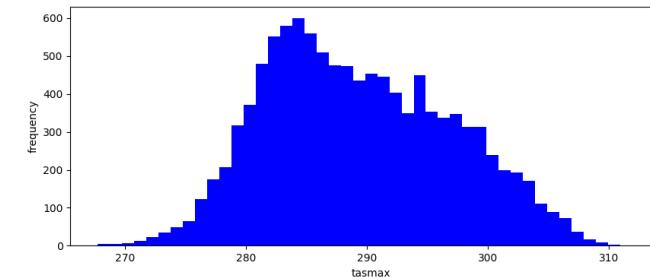
December, January, February

Every day of the year:

10 956 points

Data points for the case of TLS airport, all days, between 2020 and 2050 for scenario ssp370

Toulouse



Correlation coefficients :

Pearson : 0.77

Spearman : 0.81

3-month summer restriction

Strict summer definition

North hemisphere:

June, July, August

South hemisphere:

December, January, February

Every day of the year:

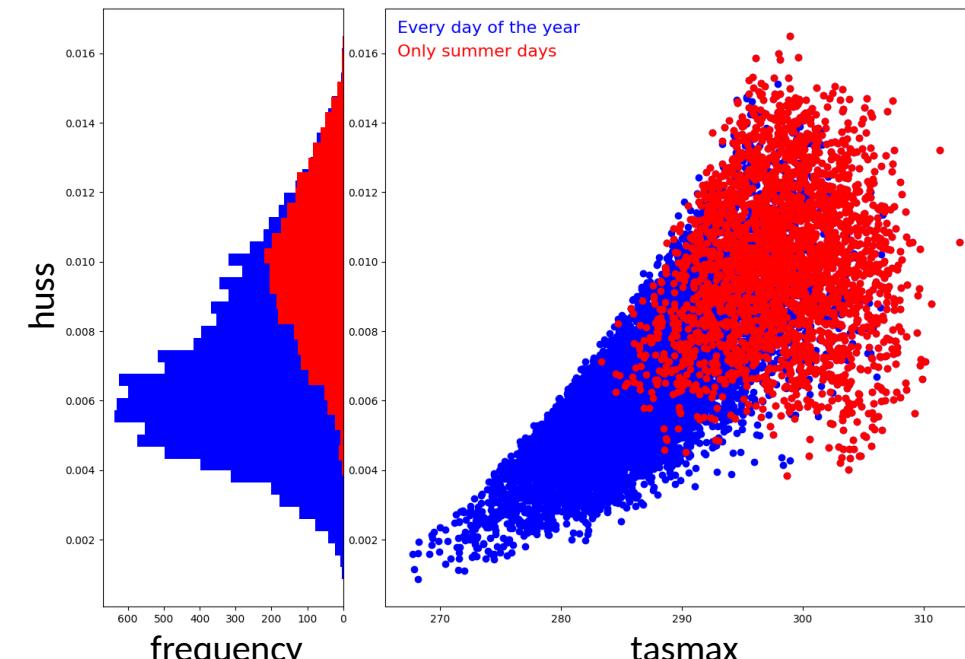
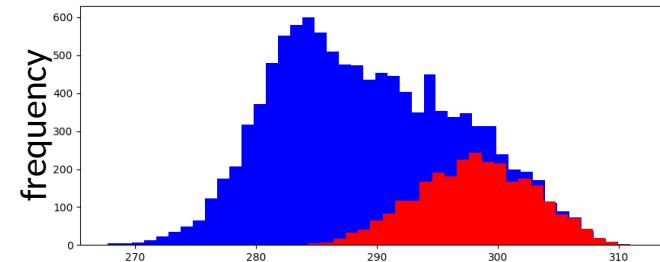
10 956 points

Only summer days:

2 700 points

Data points for the case of TLS airport, all days, between 2020 and 2050 for scenario ssp370

Toulouse



Correlation coefficients :

Pearson : 0.77

Spearman : 0.81

Pearson : 0.10

Spearman : 0.089

Pros: fixed window of 90 days per year for any case

Cons: doesn't necessarily apply to tropical climate

3-month summer restriction

Strict summer definition

North hemisphere:

June, July, August

South hemisphere:

December, January, February

Every day of the year:

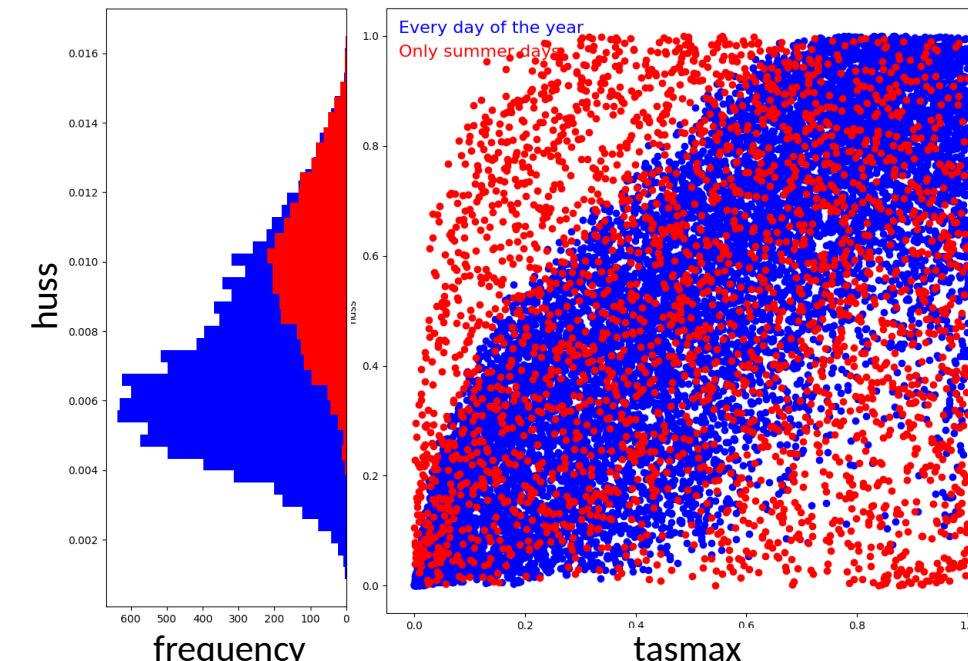
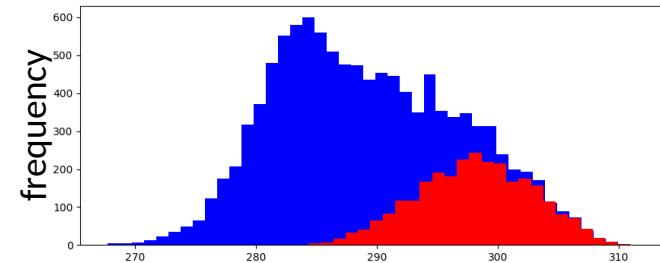
10 956 points

Only summer days:

2 700 points

Data points for the case of TLS airport, all days, between 2020 and 2050 for scenario ssp370

Toulouse



Correlation coefficients :

Pearson : 0.77

Spearman : 0.81

Pearson : 0.10

Spearman : 0.089

✉ In the rank space

Pros: fixed window of 90 days per year for any case

Cons: doesn't necessarily apply to tropical climate

Other distributions for other airports

Strict summer definition

North hemisphere:

June, July, August

South hemisphere:

December, January, February

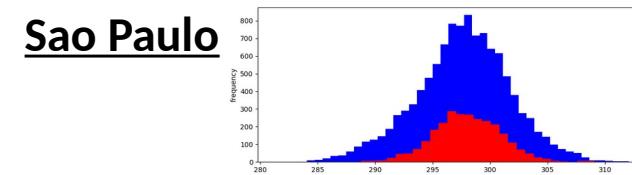
Every day of the year:

10 956 points

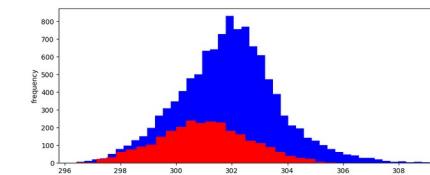
Only summer days:

2 700 points

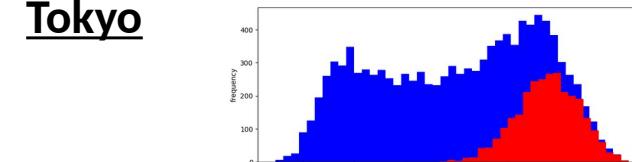
Sao Paulo



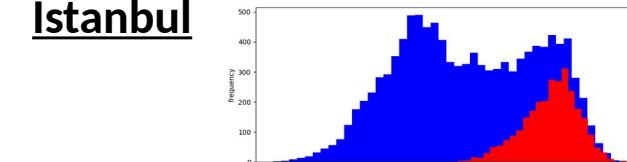
Jakarta



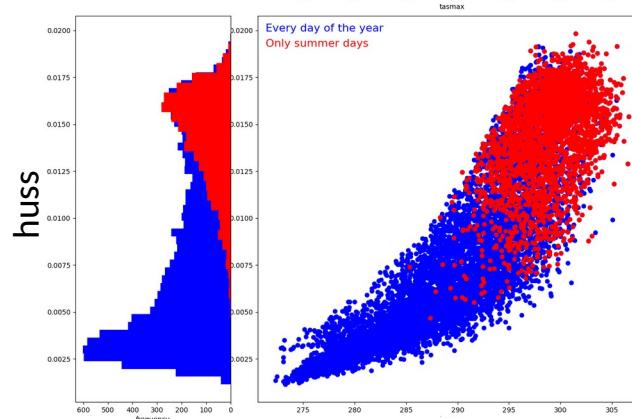
Tokyo



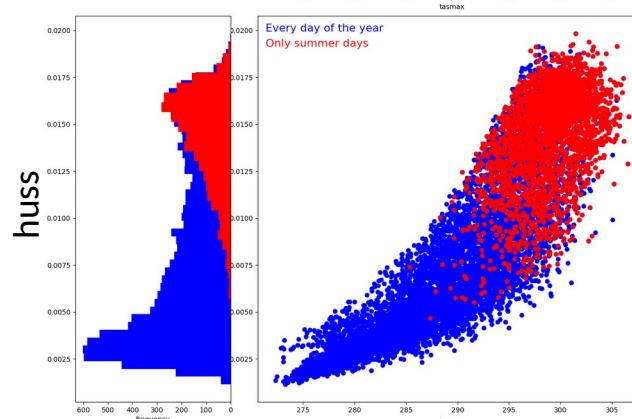
Istanbul



huss



tasmax



tasmax

Other distributions for other airports

Strict summer definition

North hemisphere:

June, July, August

South hemisphere:

December, January, February

Every day of the year:

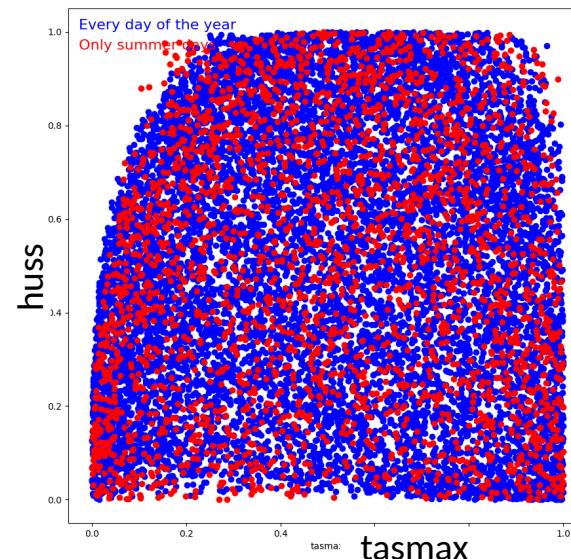
10 956 points

✉ In the rank space

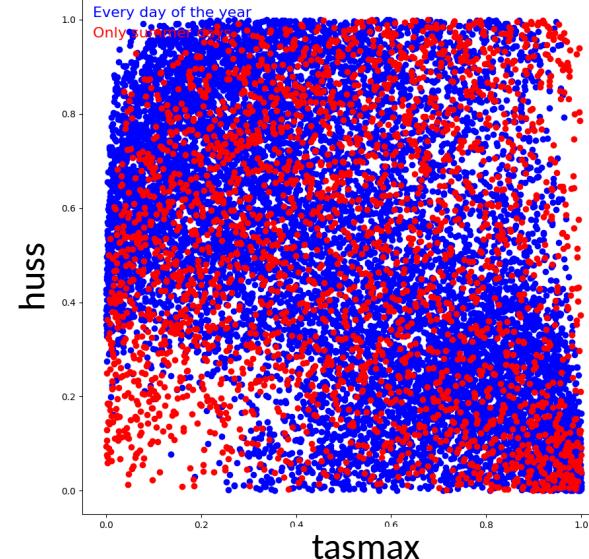
Only summer days:

2 700 points

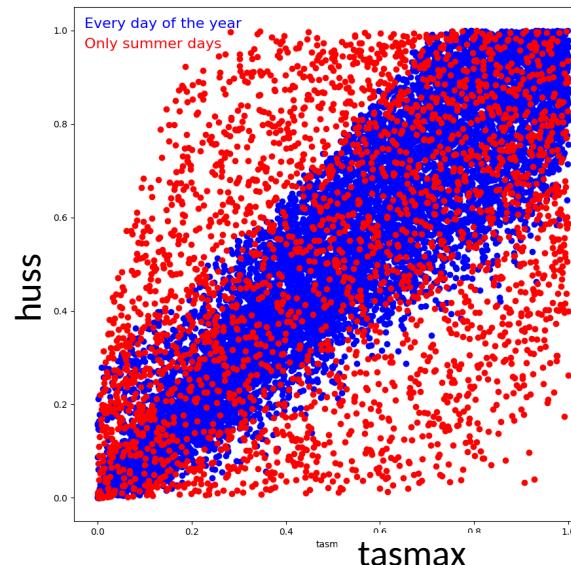
Sao Paulo



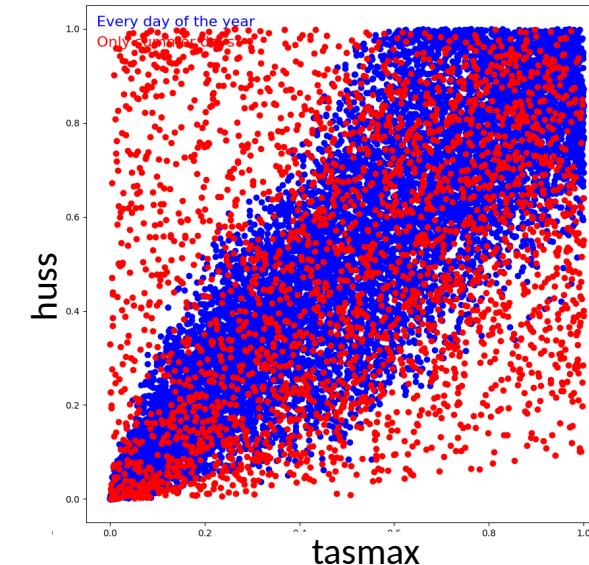
Jakarta



Tokyo



Istanbul



Focusing on extreme values

1. Summer
2. Extreme quantiles
3. Critical threshold

Extreme quantiles

Extreme values

Defines as all values above the 80th percentile

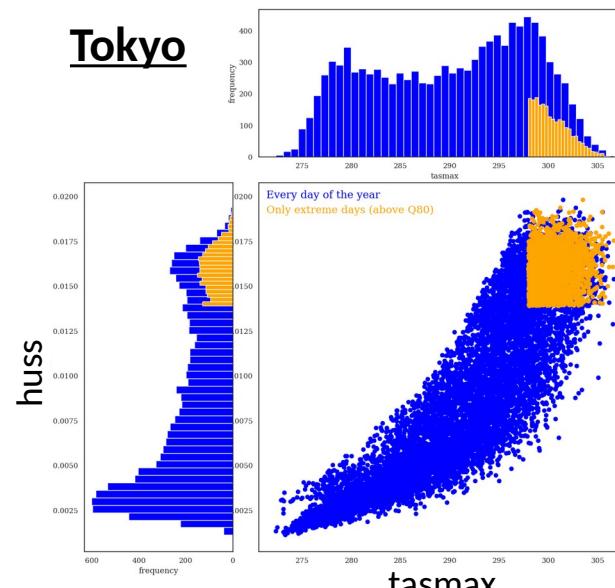
Every day of the year:

10 956 points

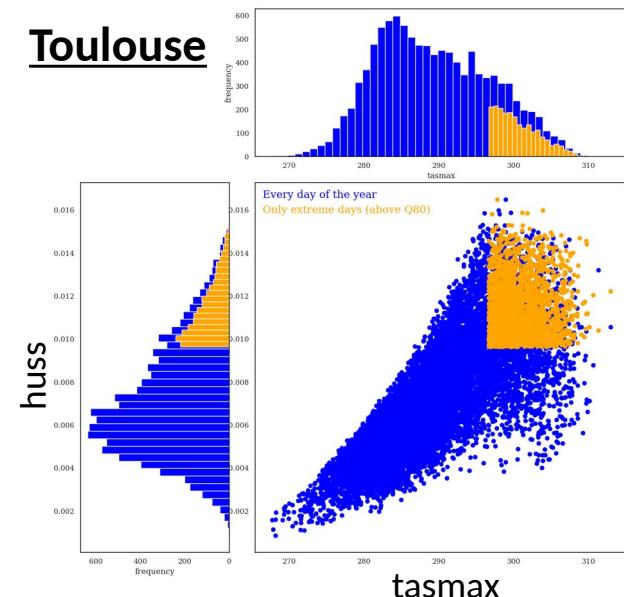
Only extreme Q80 values:

2 192 points

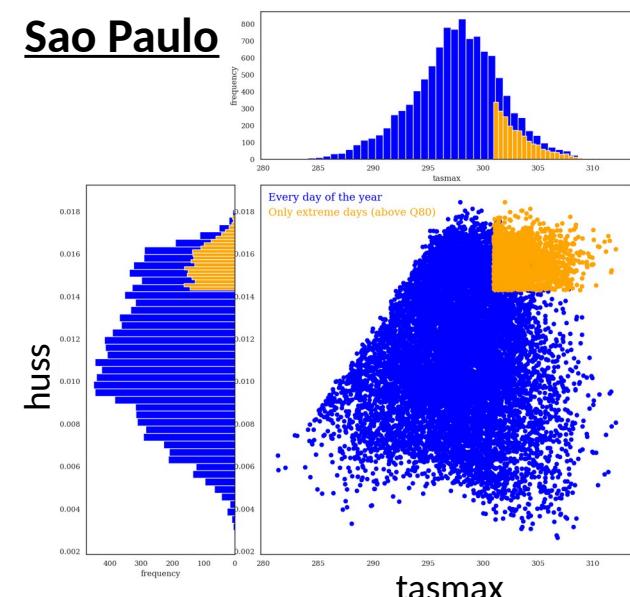
Tokyo



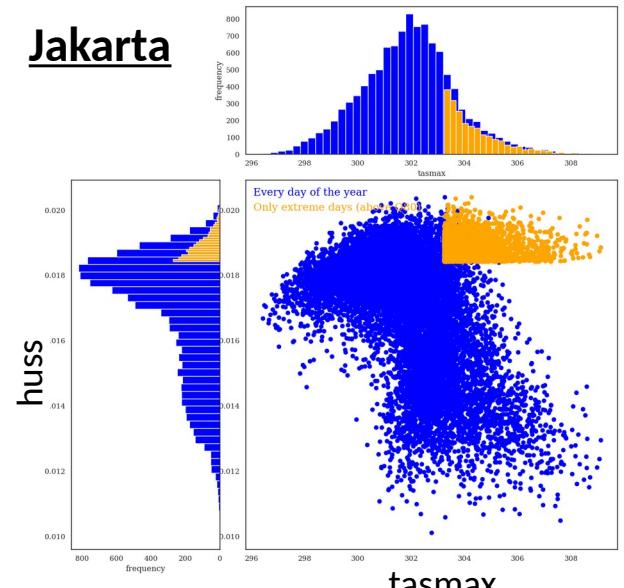
Toulouse



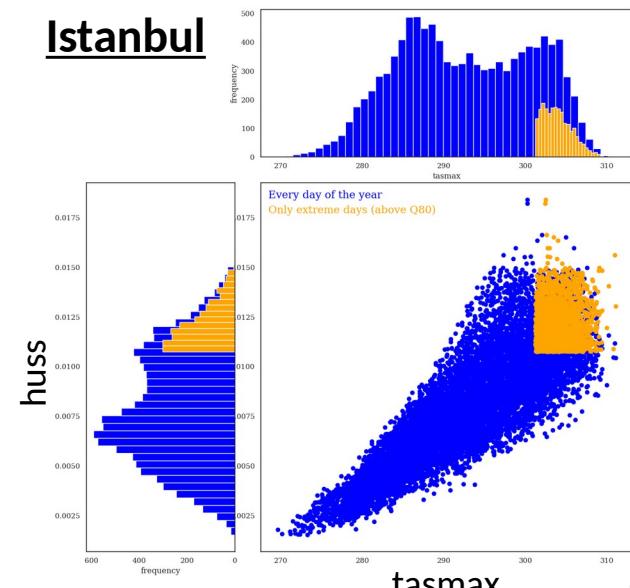
Sao Paulo



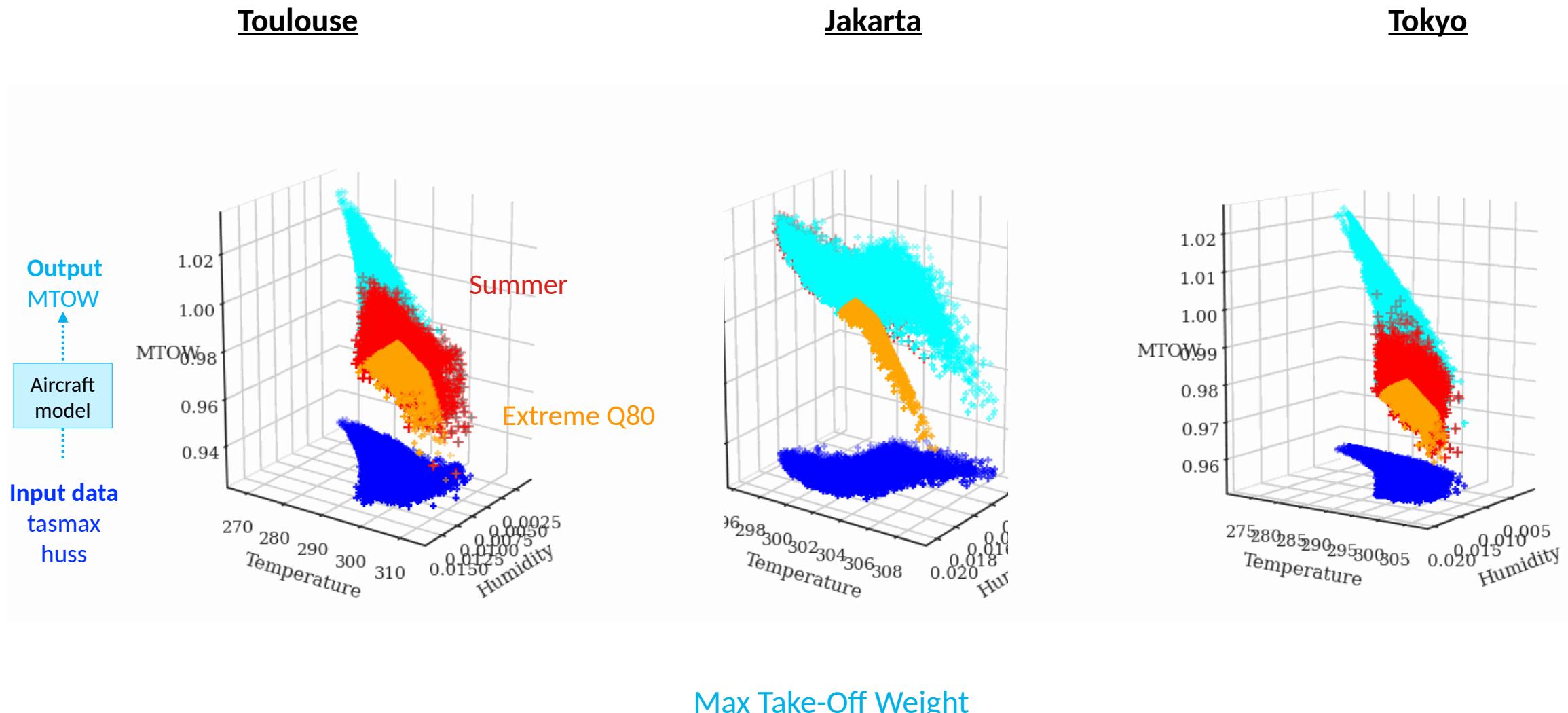
Jakarta



Istanbul



Propagation of extreme values



Focusing on extreme values

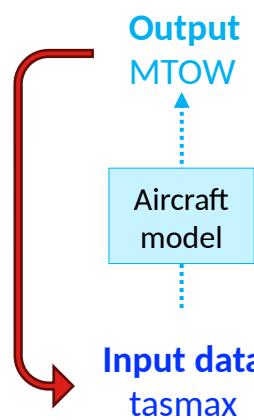
1. Summer
2. Extreme quantiles
- 3. Critical threshold**

Critical MTOW threshold

MTOW threshold

Critical domain defined for

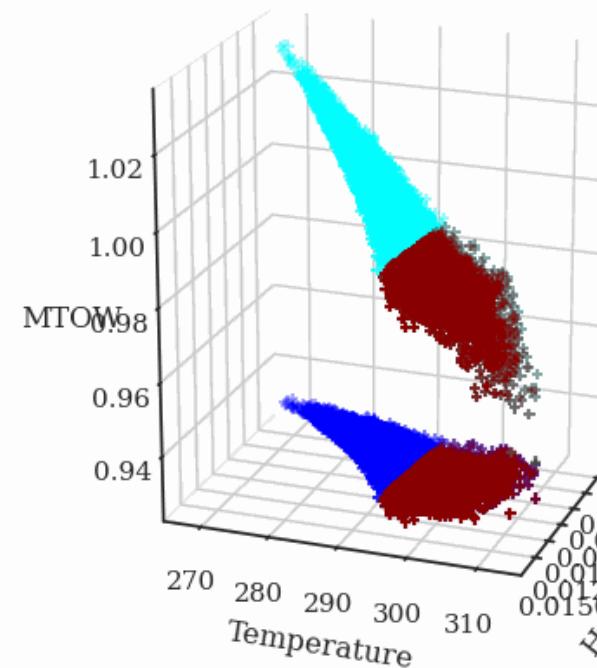
Critical threshold definition



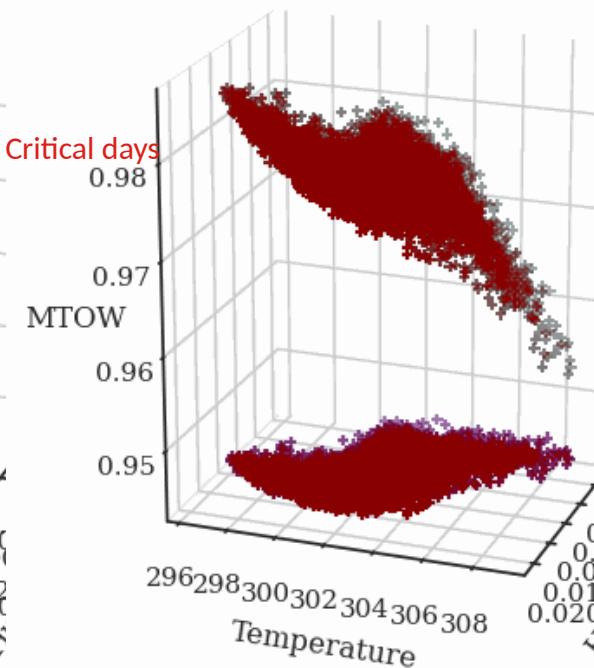
→ Focuses on all input variables that give performance defined as critical

Con: Variable number of critical data

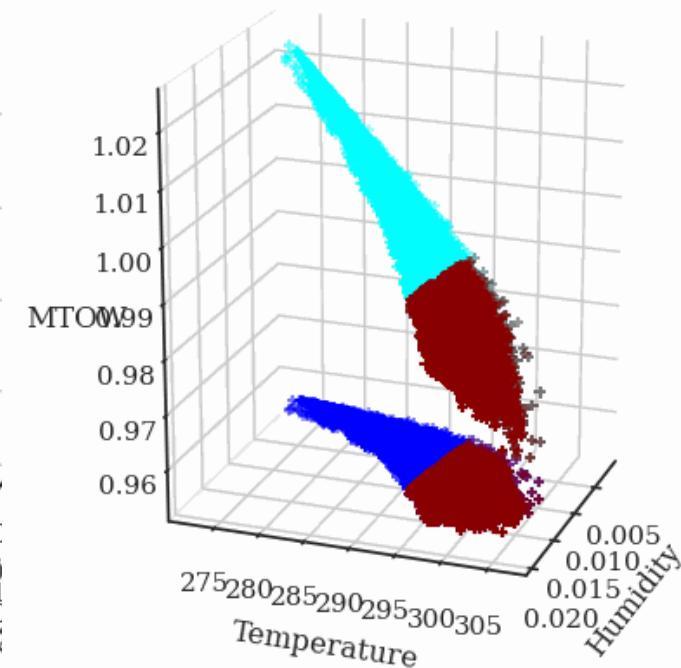
Toulouse



Jakarta



Tokyo



3 240 critical days
(29.6 % of days)

10 958 critical days
(100% of days)

4 400 critical days
(40.2% of days)

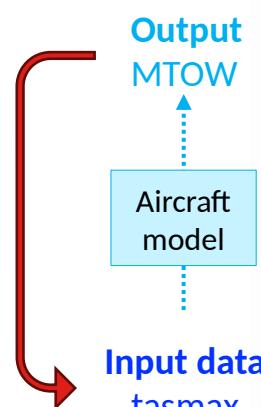
Max Take-Off Weight

Critical MTOW threshold

MTOW threshold

Critical domain defined for

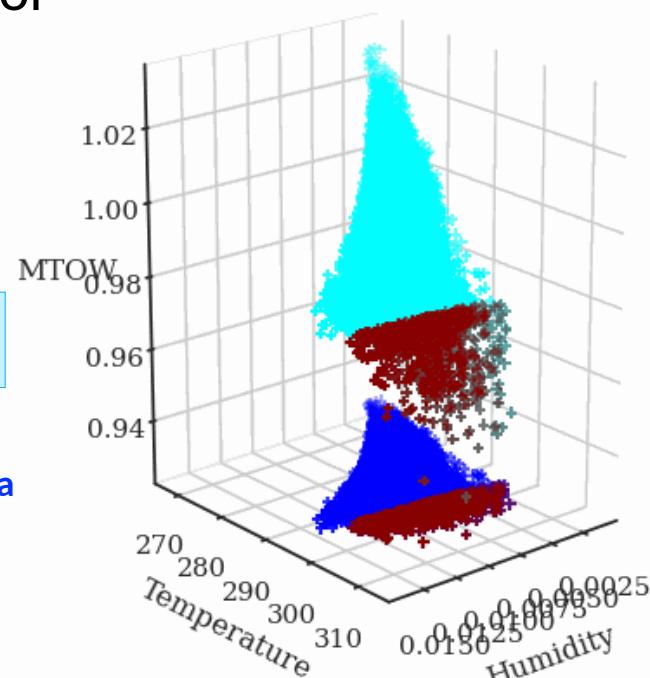
Critical threshold definition



→ Focuses on all input variables that give performance defined as critical

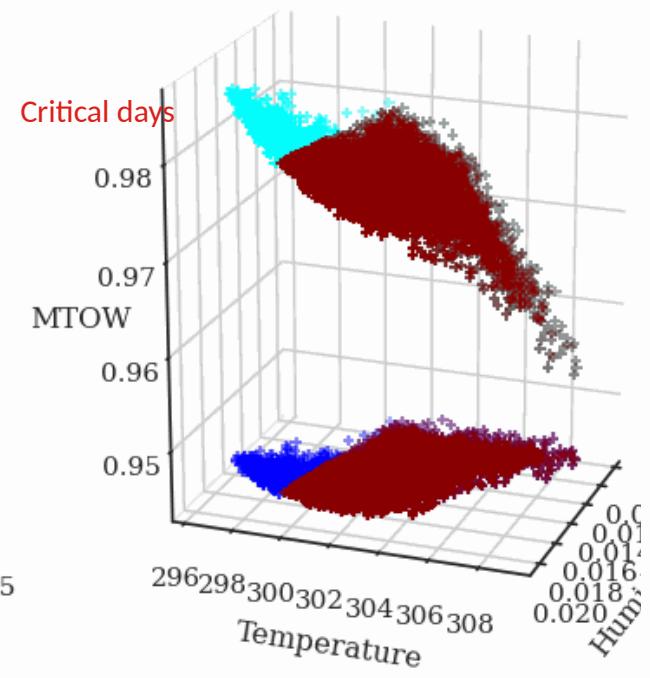
Con: Variable number of critical data

Toulouse



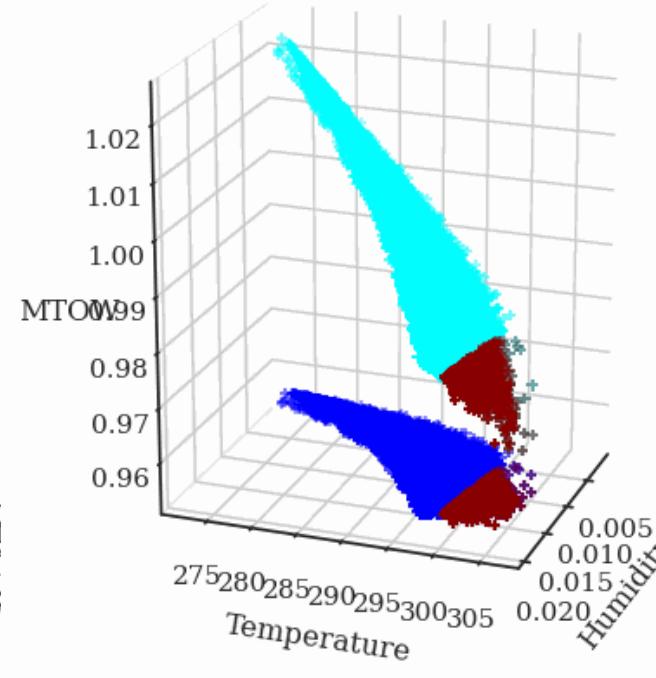
3 240 critical days
(7.7 % of days)

Jakarta



9 669 critical days
(88.2% of days)

Tokyo



993 critical days
(9.0% of days)

Max Take-Off Weight

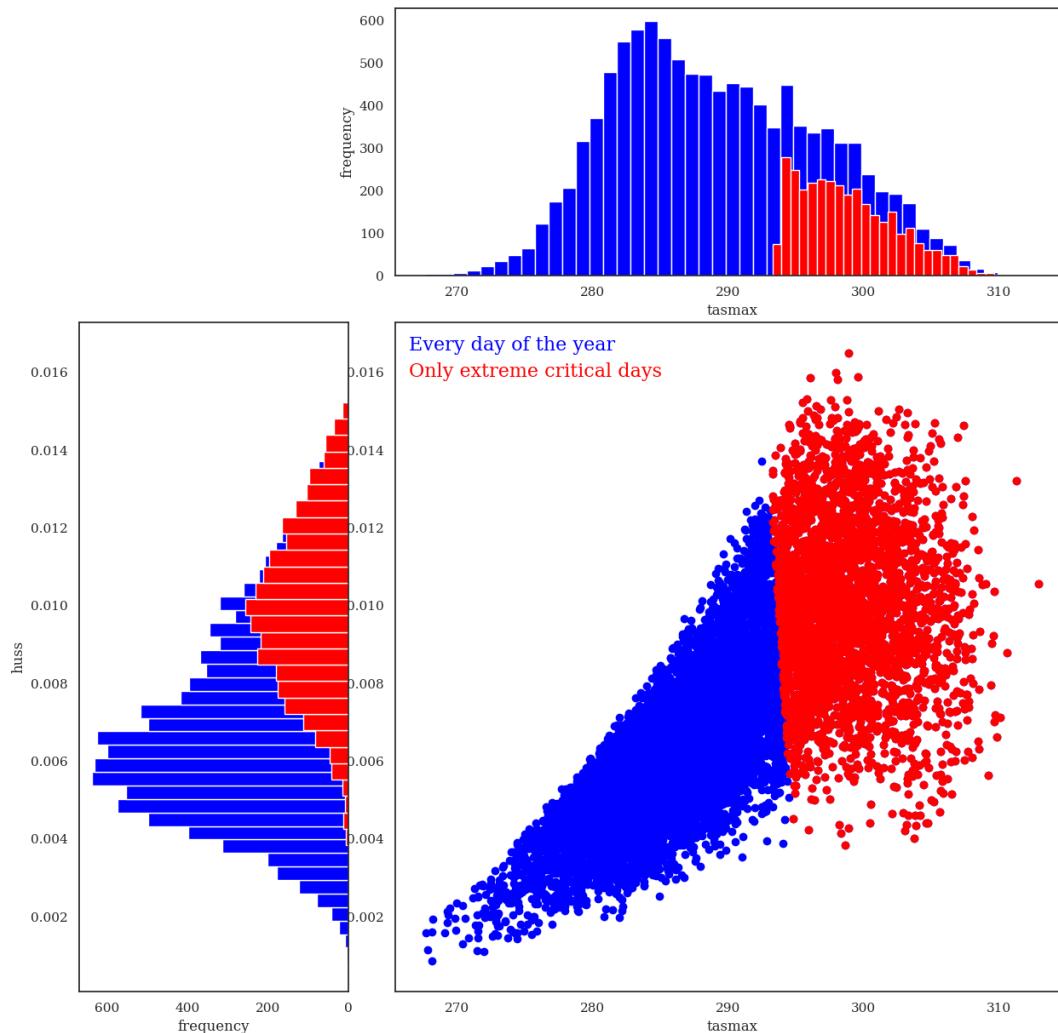
Fitting input distribution and sensitivity analysis

For critical data

Input distribution

Toulouse

Threshold =



Every day of the year:

10 956 points

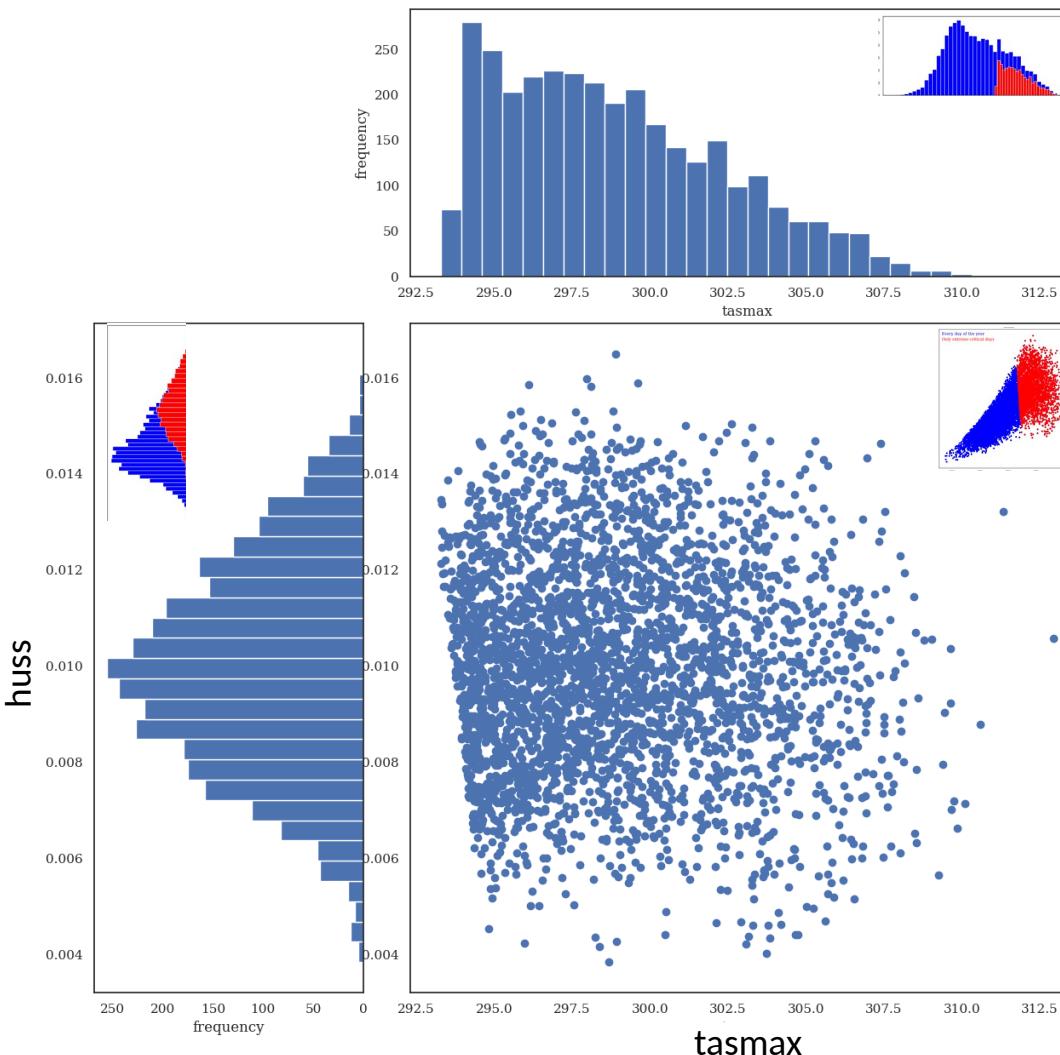
Only critical days:

3 240 points

Critical input distribution

Toulouse

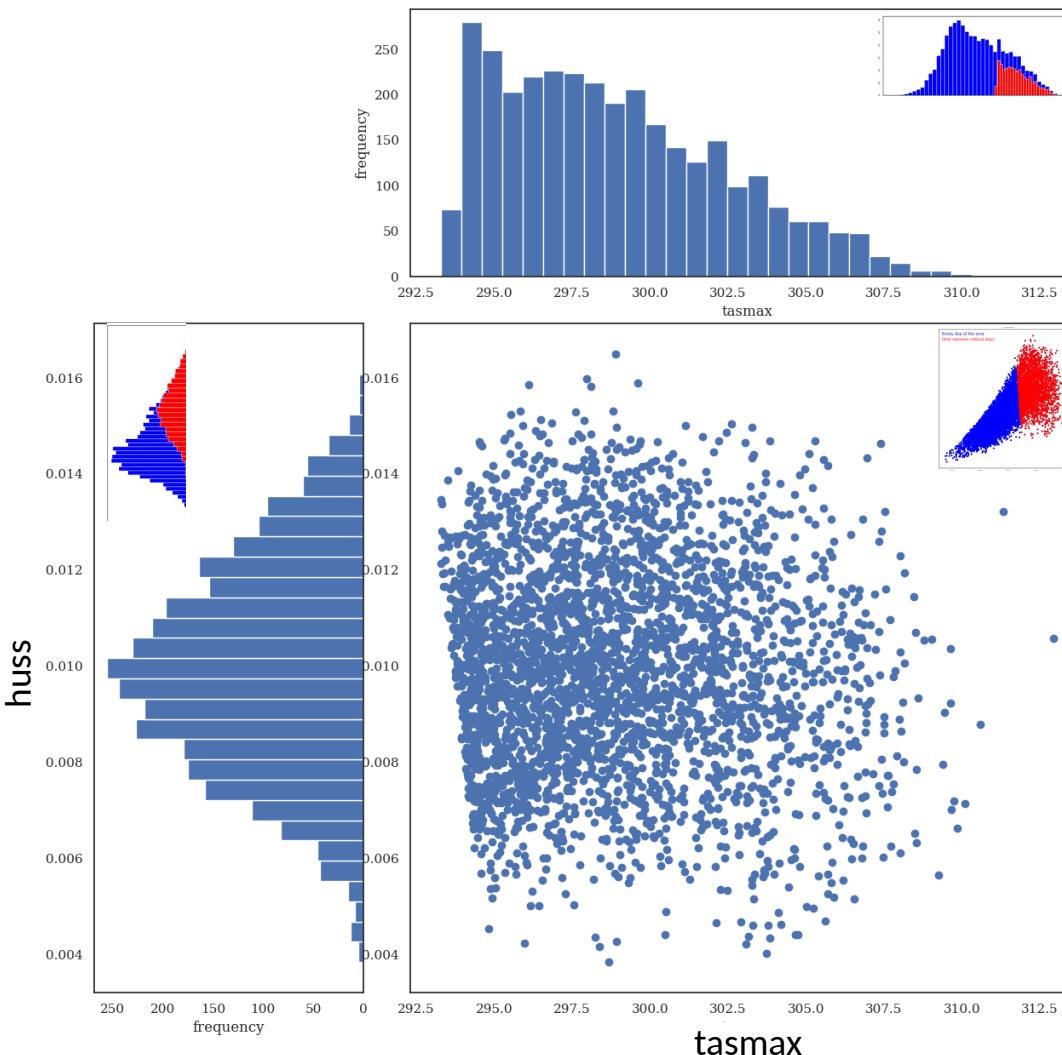
Threshold =



Dependency

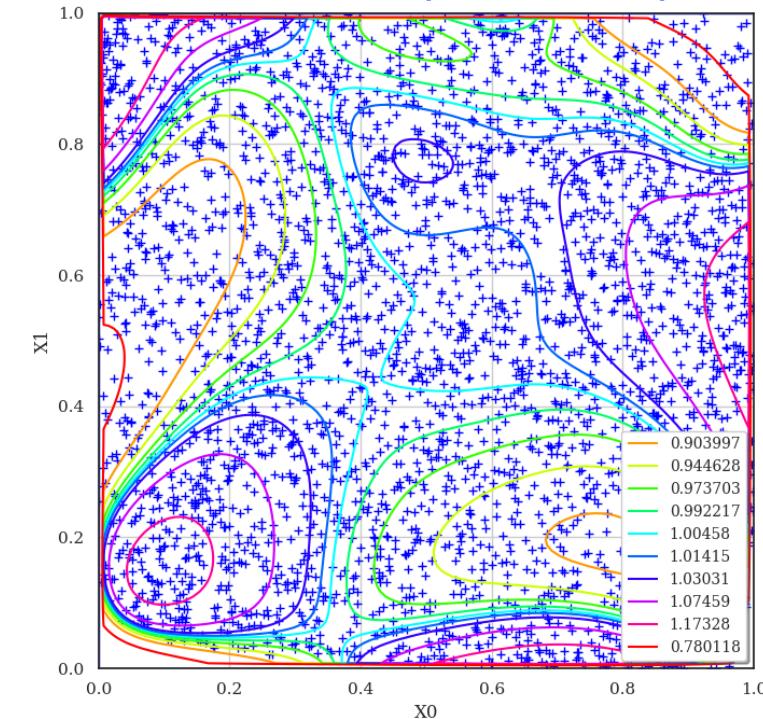
Toulouse

Threshold =



Fitting an Empirical Bernstein Copula

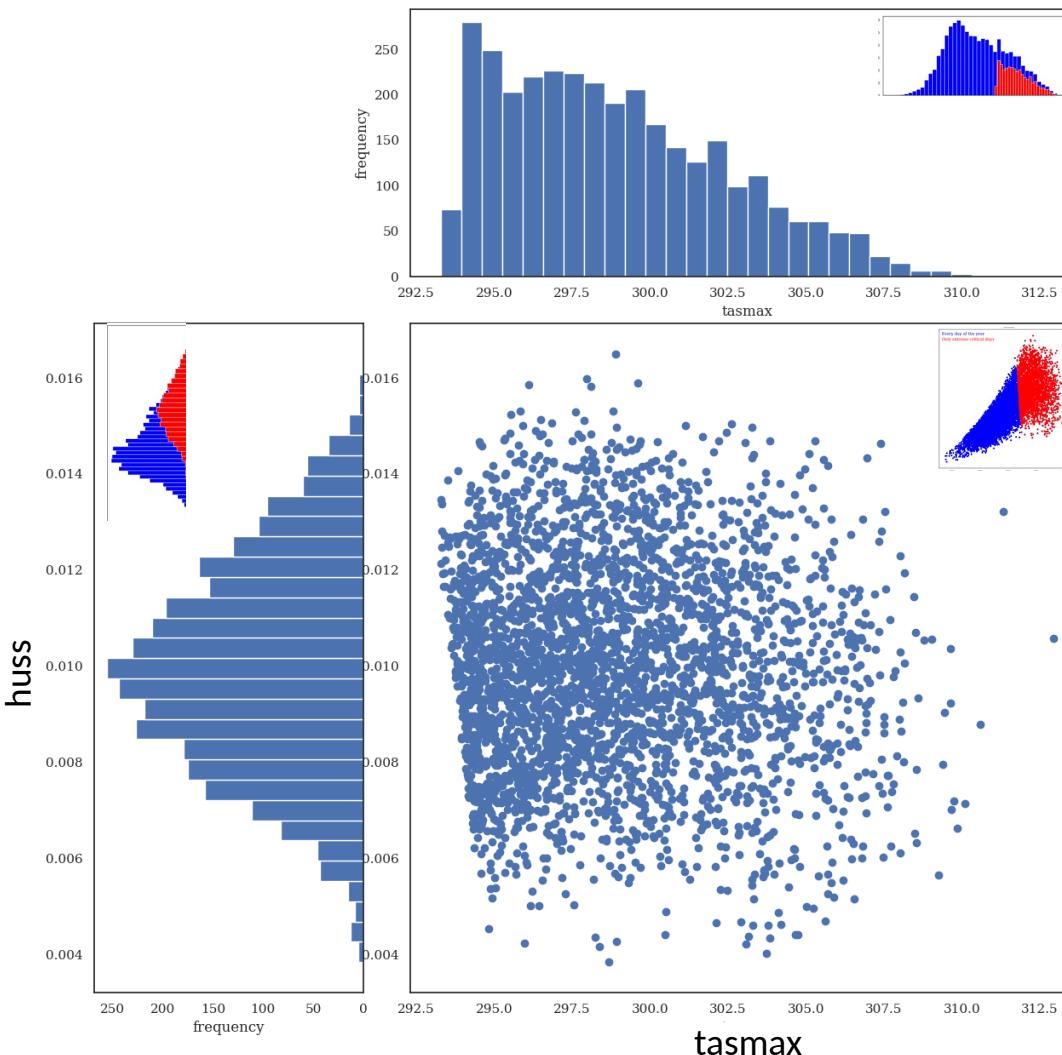
+ Sample in rank space



Dependency

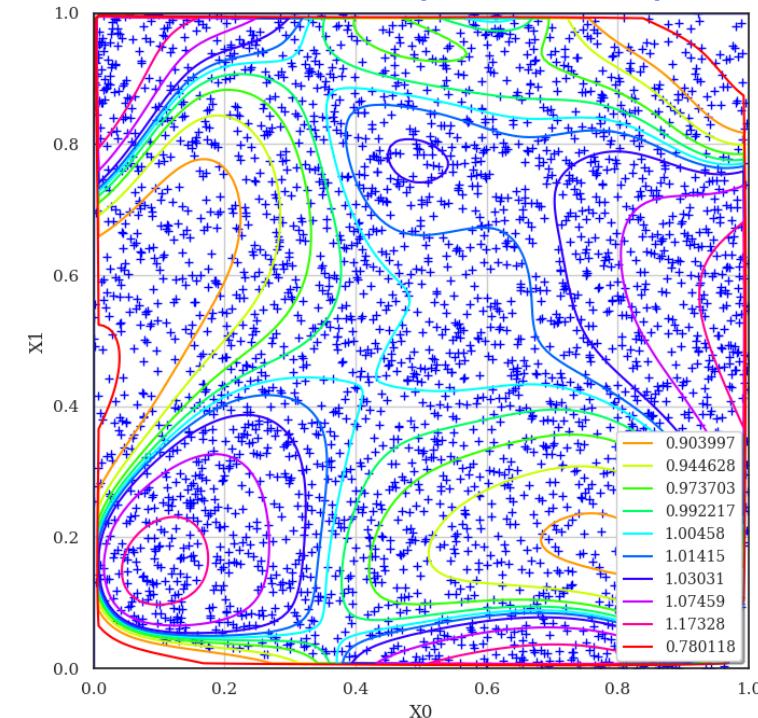
Toulouse

Threshold =



Fitting an Empirical Bernstein Copula

+ Sample in rank space



Copula PDF contours

Difference between lowest and highest density: 0.27

Correlation coefficients

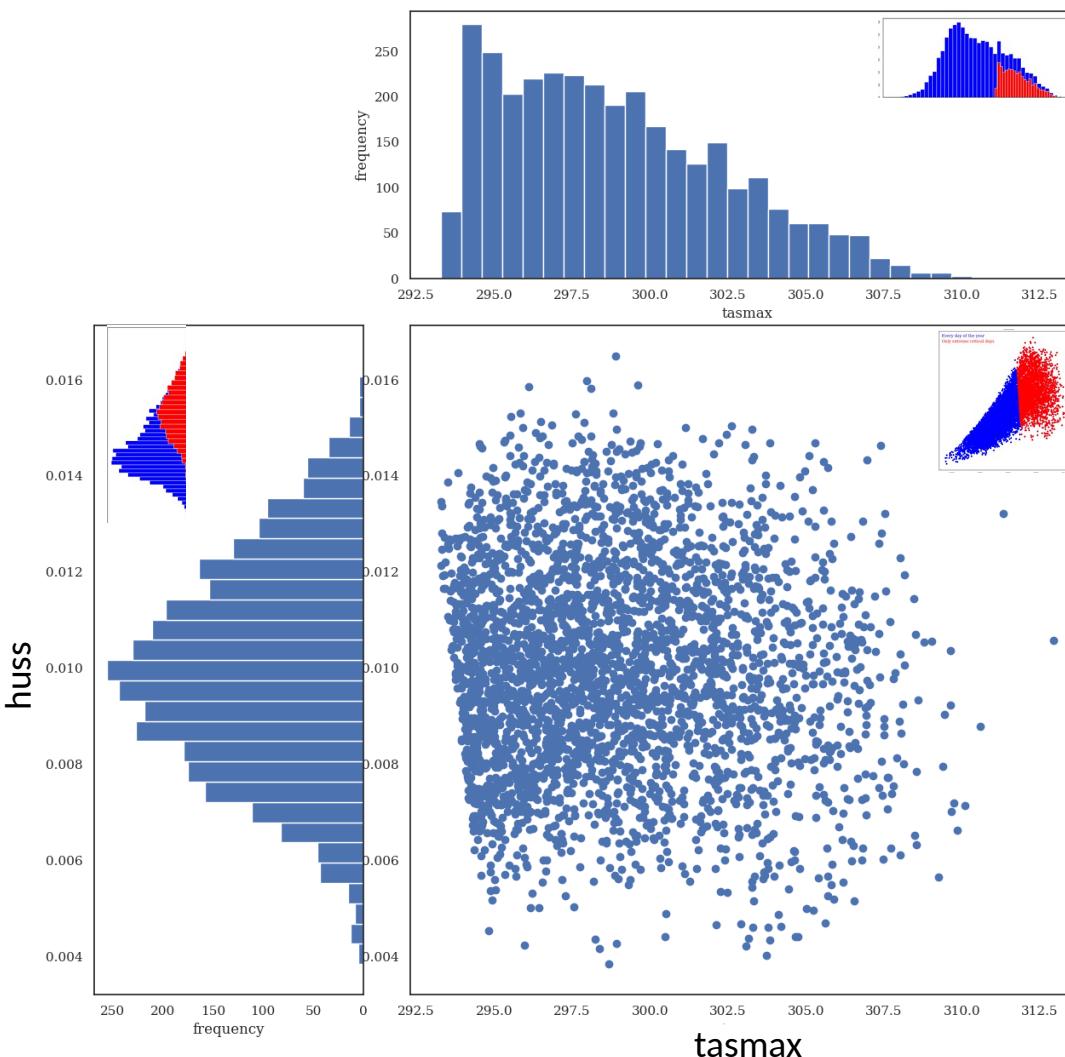
Pearson: -0.048

Spearman: -0.018

Dependency

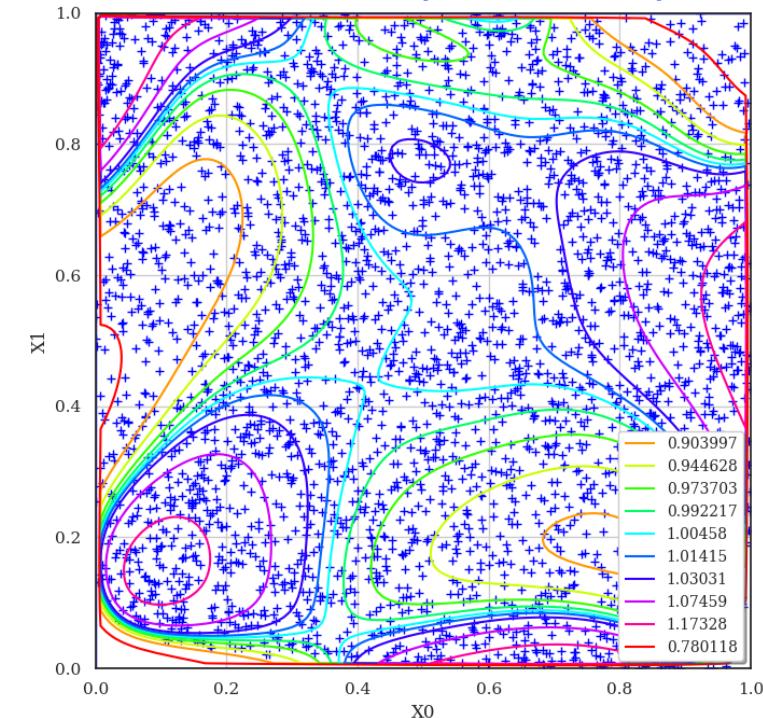
Toulouse

Threshold =



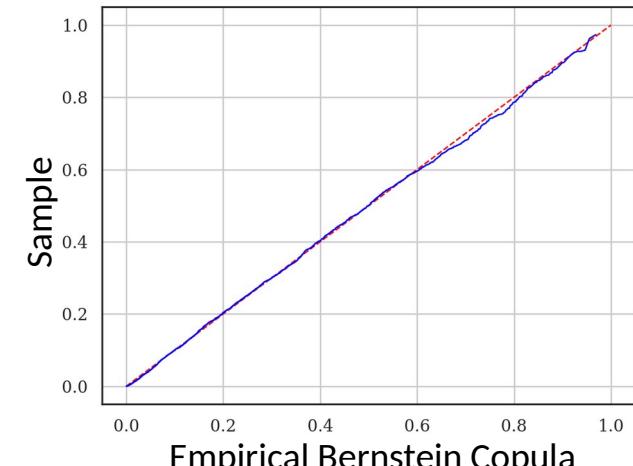
Fitting an Empirical Bernstein Copula

+ Sample in rank space



Difference between lowest and highest density: 0.27

Kendall plot



Copula PDF contours

Correlation coefficients

Pearson: -0.048

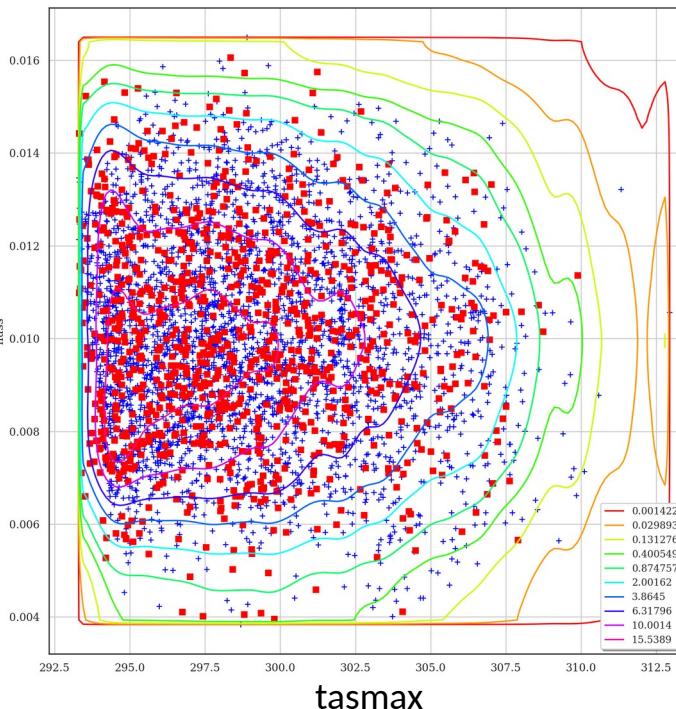
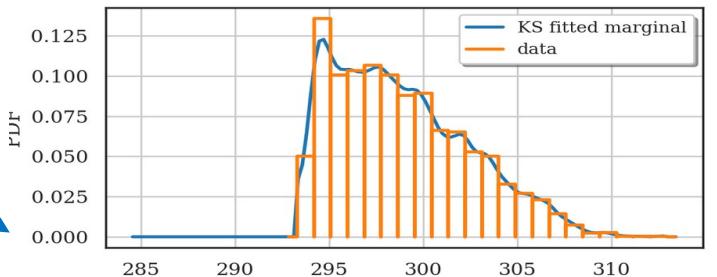
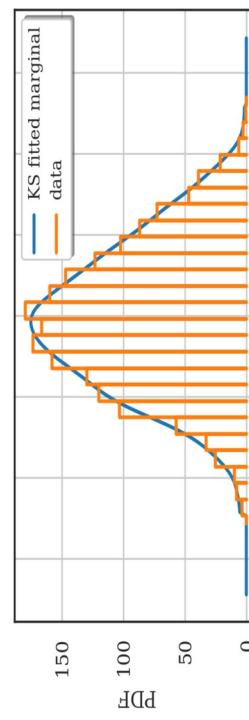
Spearman: -0.018

Joint composed distribution

Toulouse

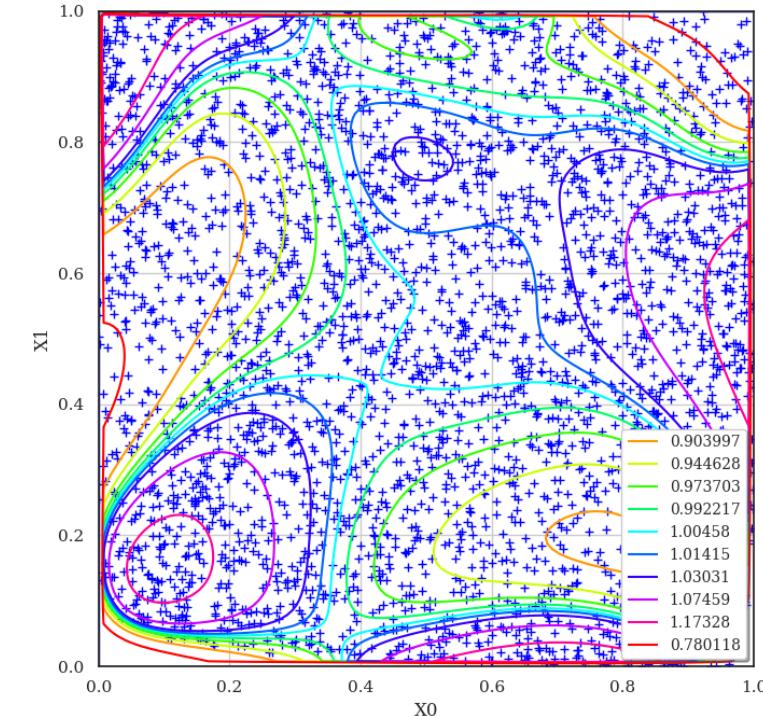
Threshold =

Fitted marginals
with Kernel
Smoothing



Fitting an Empirical Bernstein Copula

+ Sample in rank space

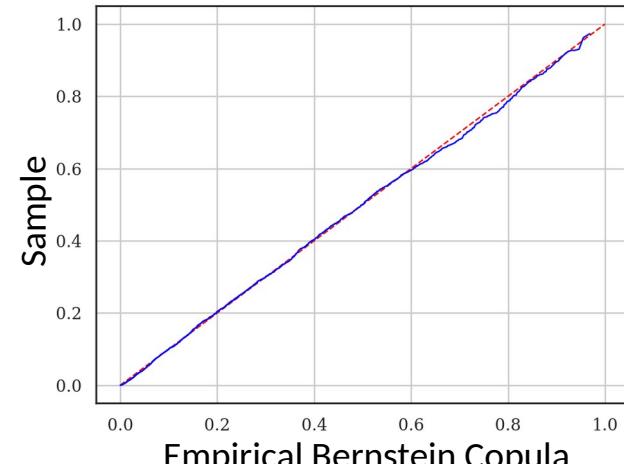


Difference between lowest and highest density: 0.27

Joint distribution contours

- + Data sample
- Sample on fitted PDF

Kendall plot



Copula PDF contours

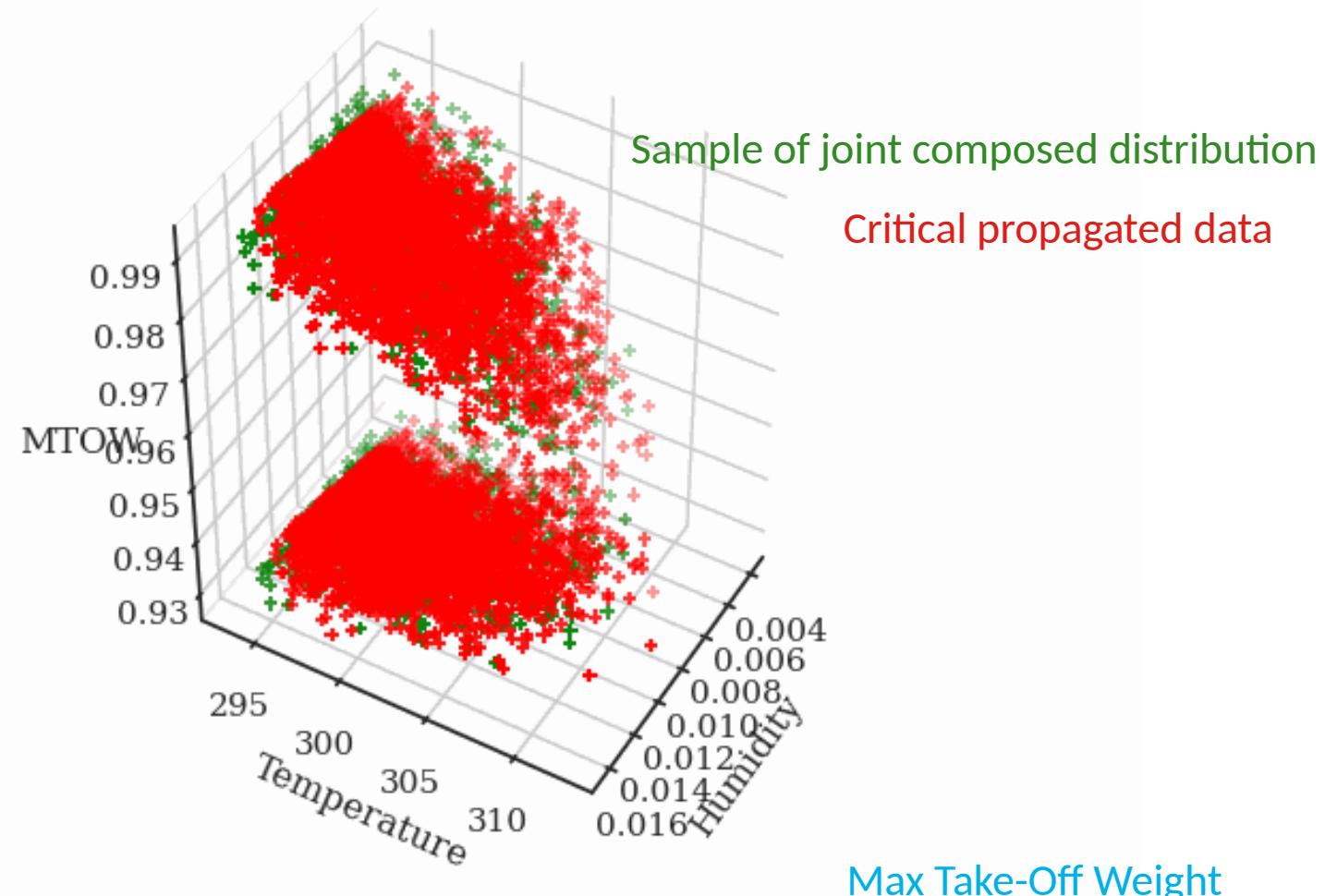
Correlation coefficients

Pearson: -0.048

Spearman: -0.018

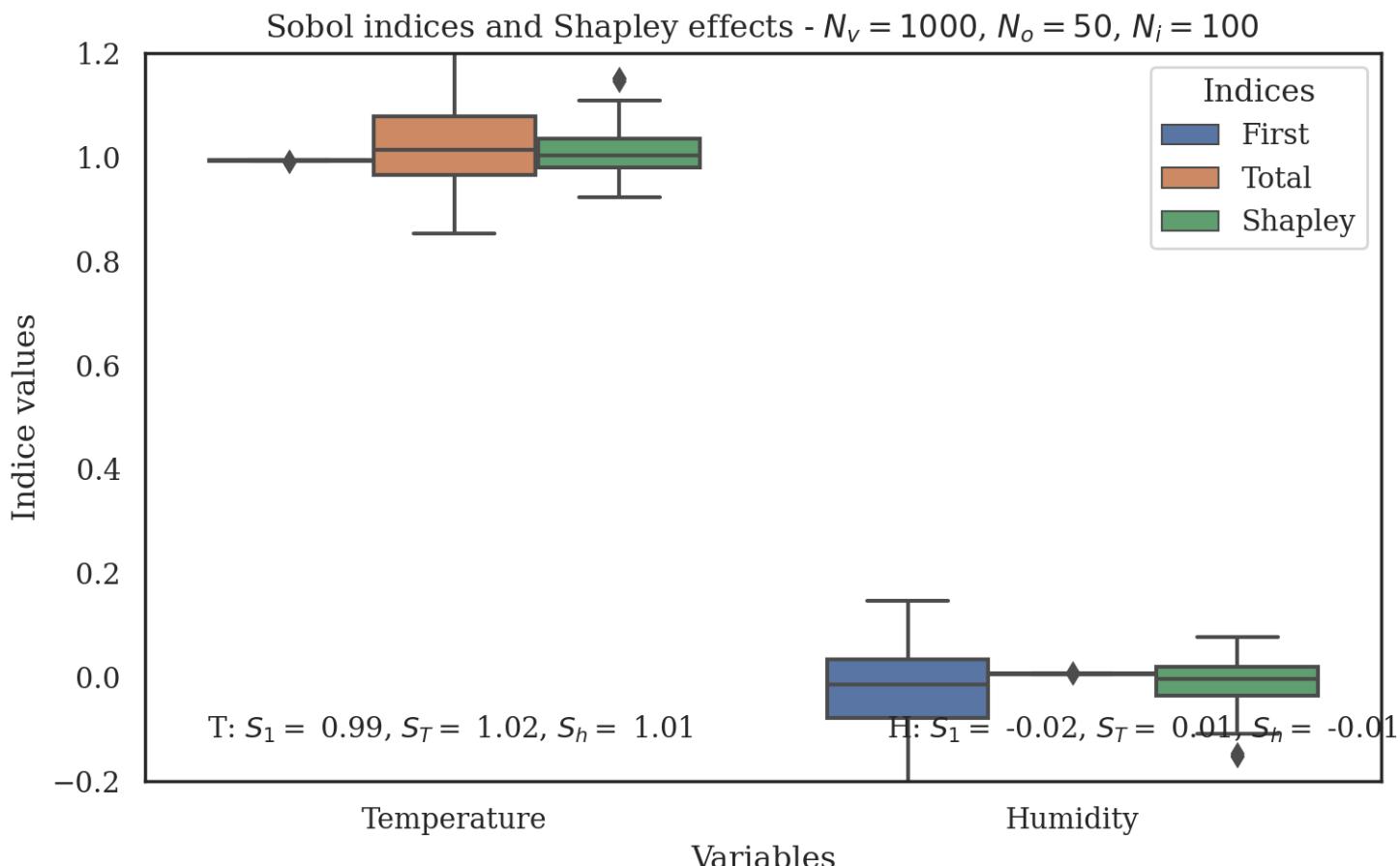
Propagated results

Toulouse



Sensitivity Analysis

Toulouse

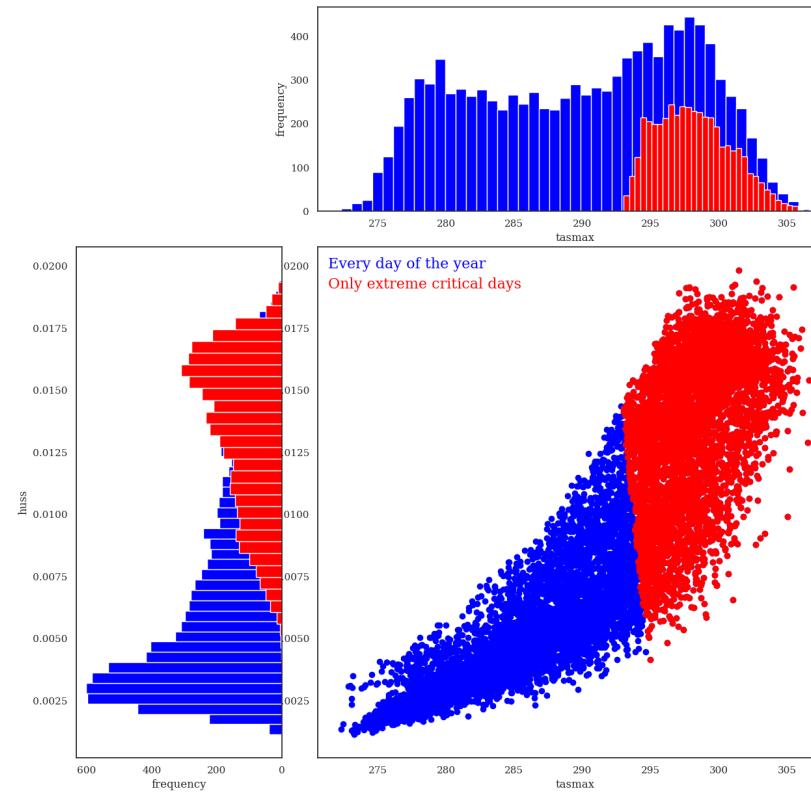


Critical input distribution

Tokyo

Threshold =

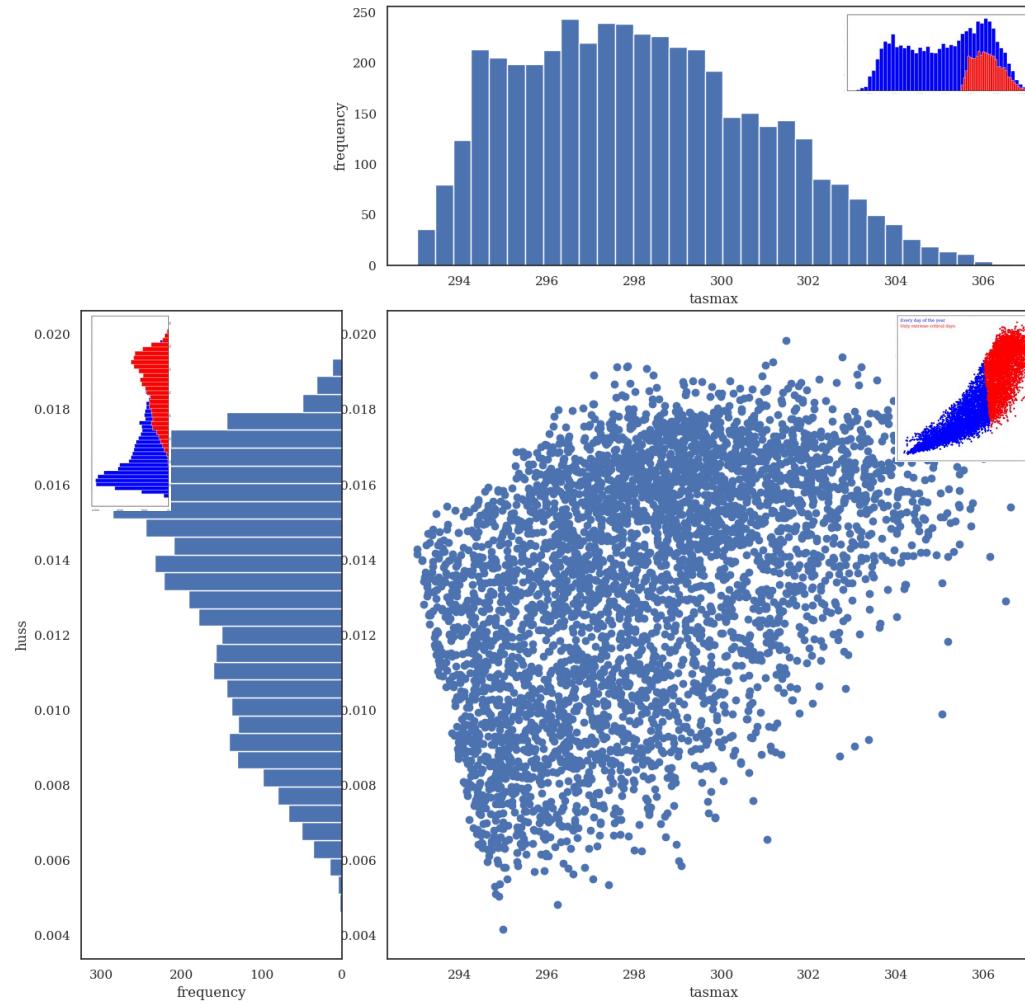
Data points for the case of HND airport, between 2020 and 2050 for scenario ssp370



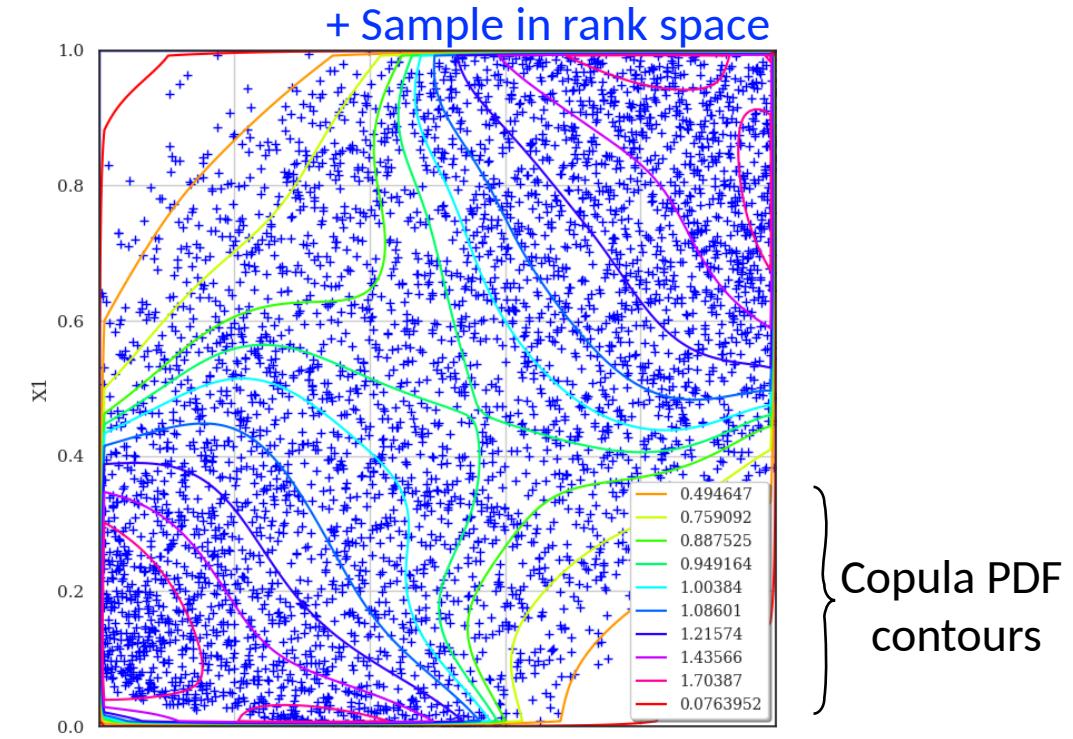
Dependency

Tokyo

Threshold =



Fitting an Empirical Bernstein Copula



Difference between lowest
and highest density: 1.21

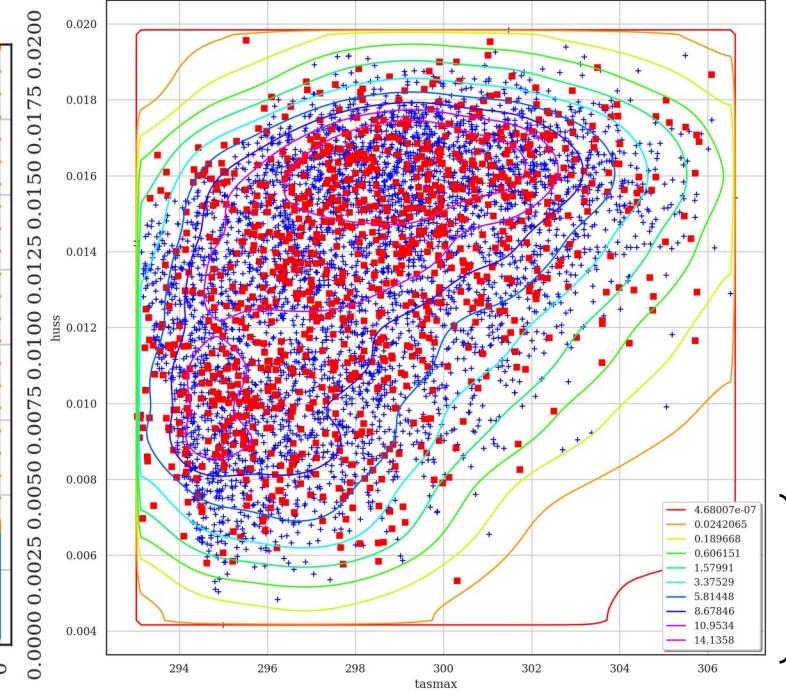
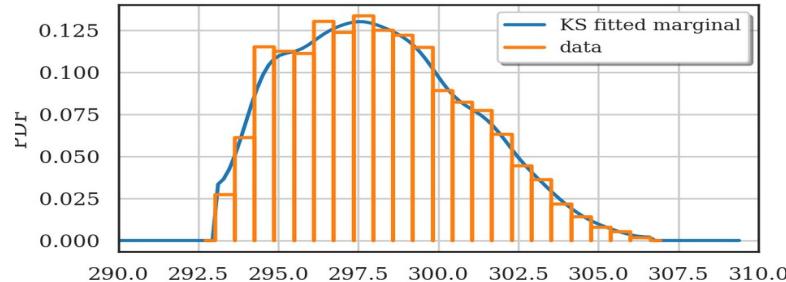
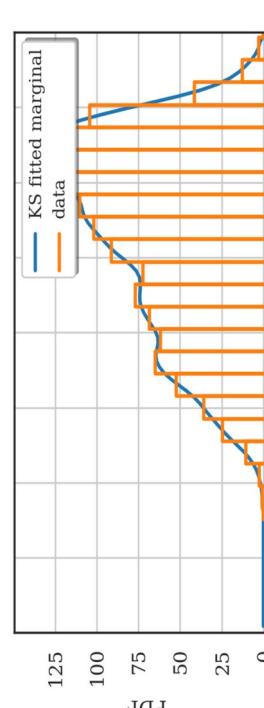
Correlation coefficients
Pearson: 0.45
Spearman: 0.47

Joint composed distribution

Tokyo

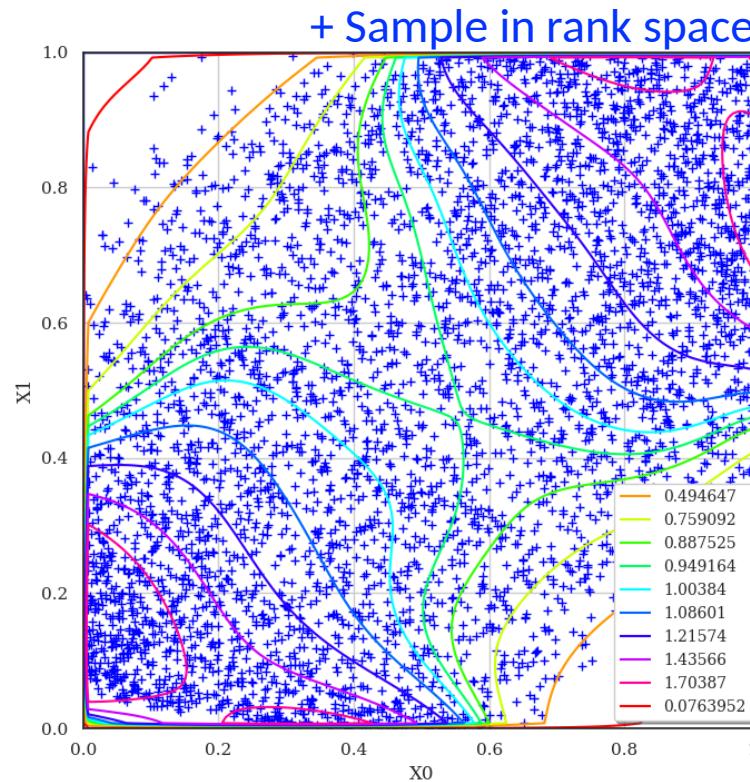
Threshold =

Fitted marginals
with Kernel
Smoothing



} Joint distribution
contours
+ Data sample
■ Sample on fitted PDF

Fitting an Empirical Bernstein Copula



} Copula PDF
contours

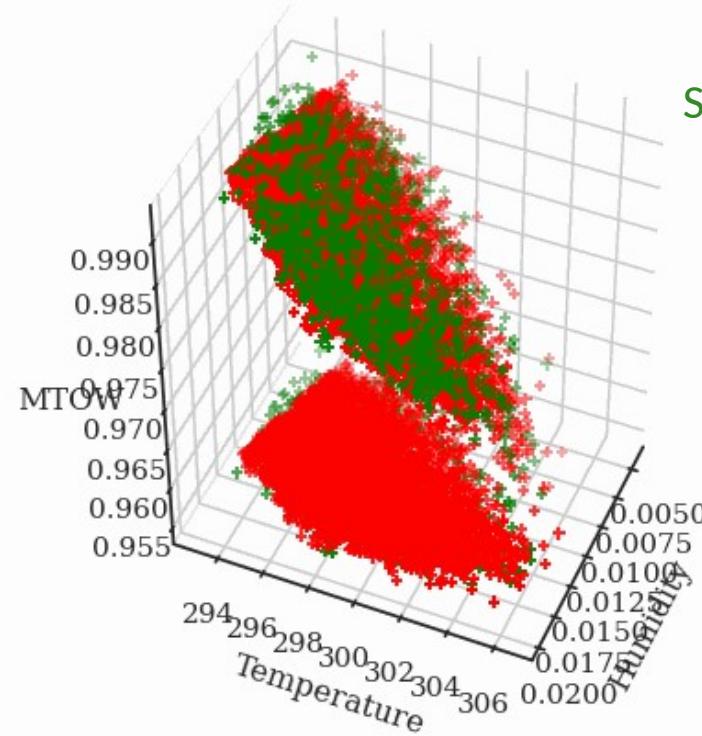
Difference between lowest
and highest density: 1.21

Correlation coefficients
Pearson: 0.45
Spearman: 0.47

Propagated result

Tokyo

Threshold =



Sample of joint composed distribution

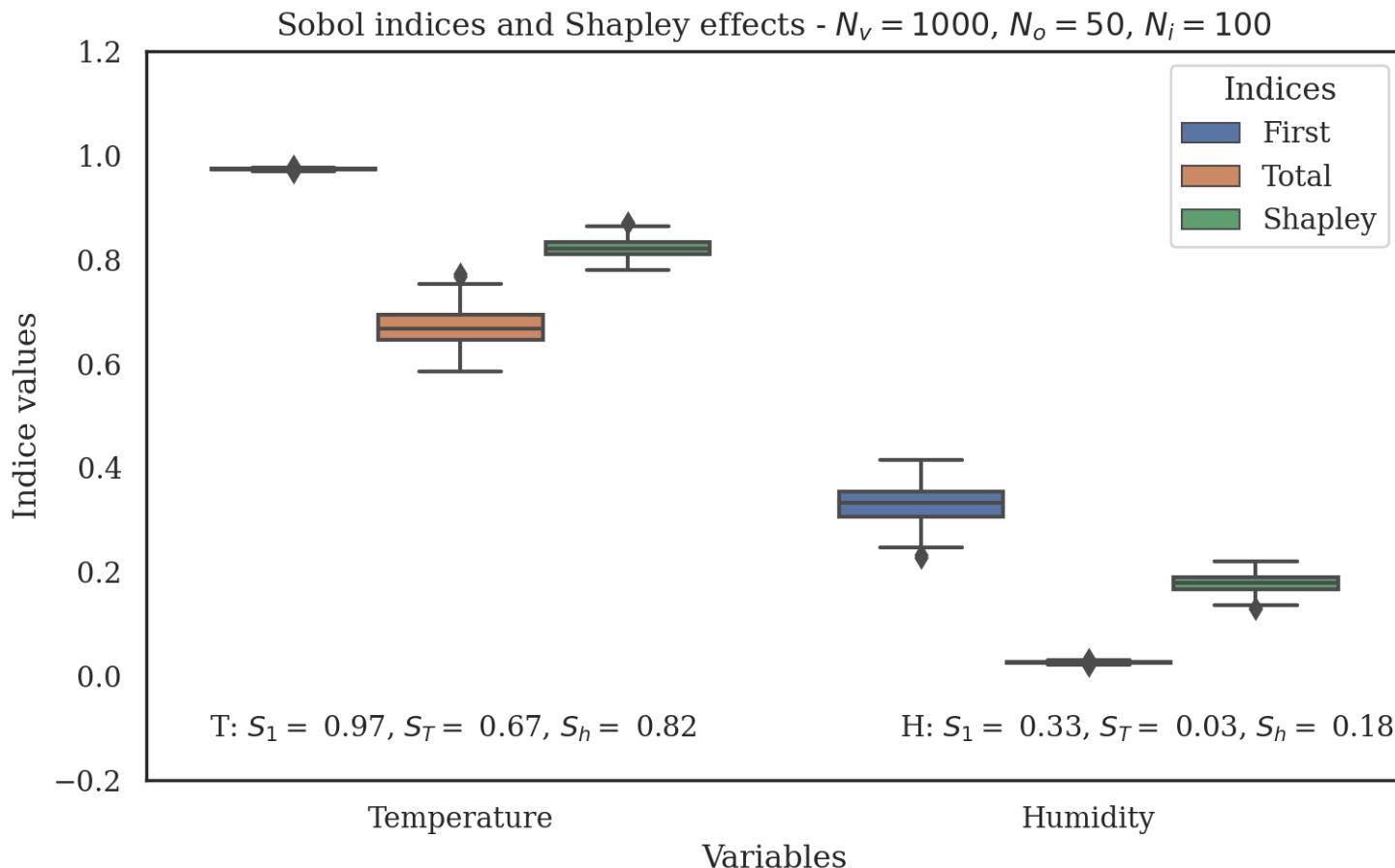
Critical propagated data

Max Take-Off Weight

Sensitivity Analysis

Tokyo

Threshold =

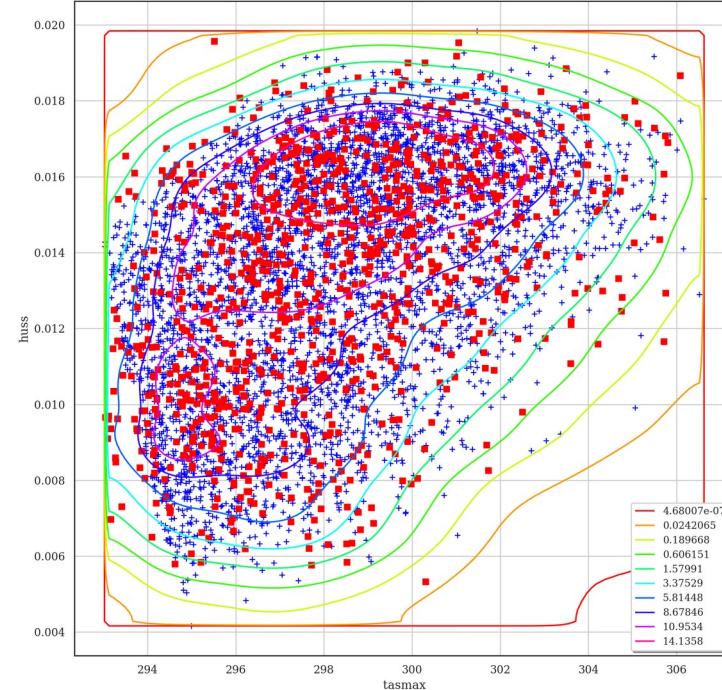


Importance of dependency

Tokyo

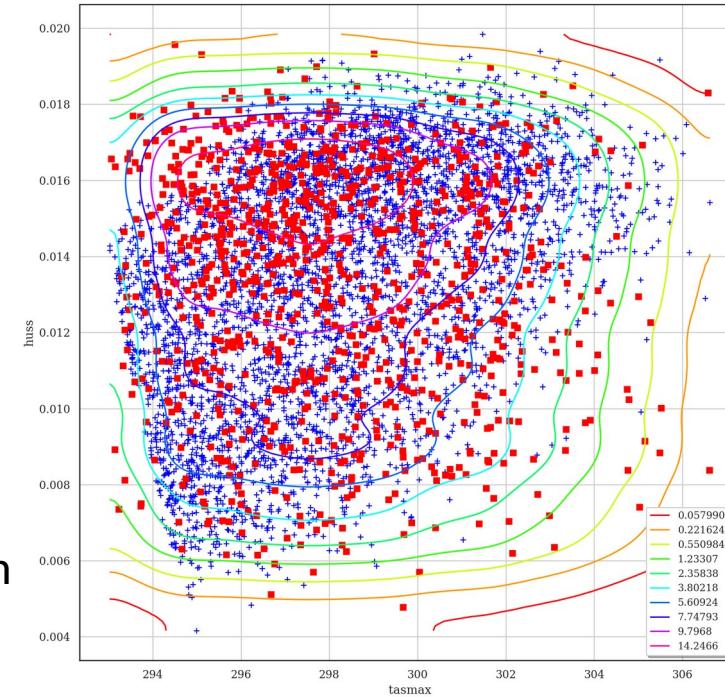
Threshold =

With Empirical Bernstein copula



Joint distribution
contours

With independent copula



Joint distribution
contours

Shapley indices:

Temperature

$$S_h = 0.82$$

$$S_h = 0.94$$

Humidity

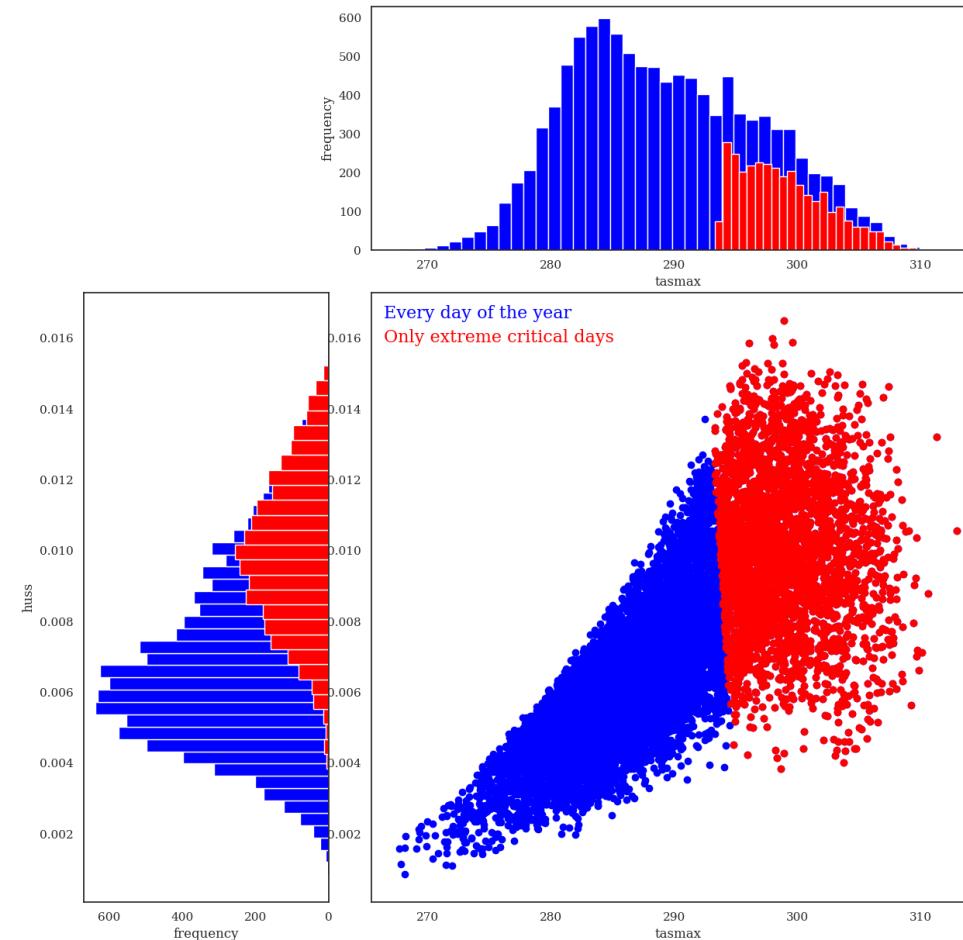
$$S_h = 0.18$$

$$S_h = 0.06$$

Why focus on extreme values?

All days vs. critical days

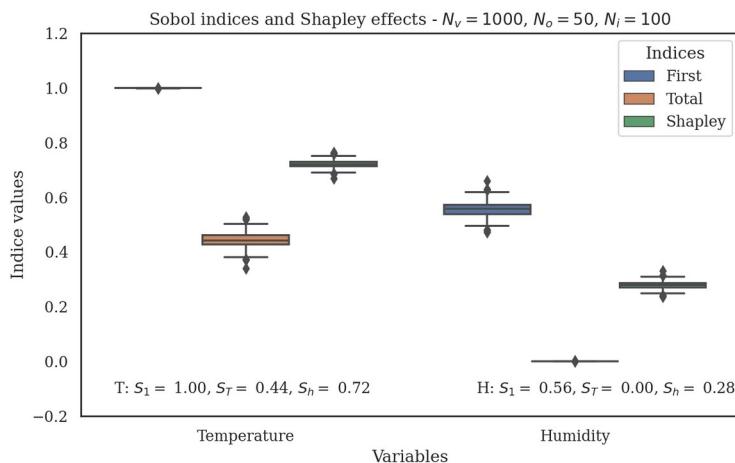
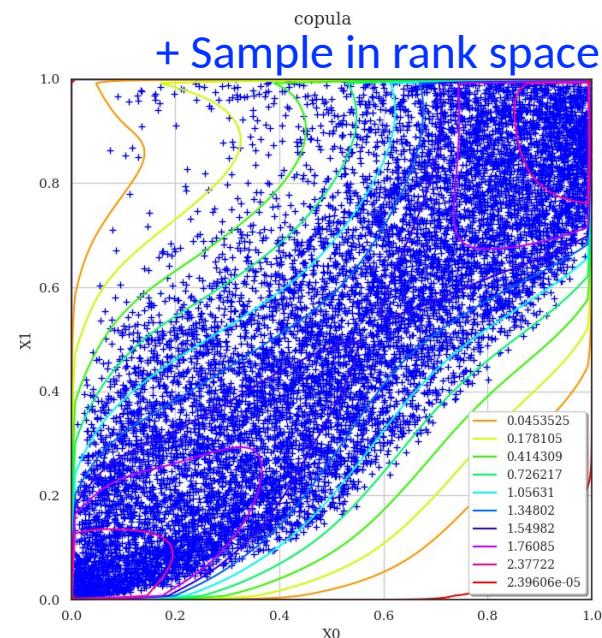
Data points for the case of TLS airport, between 2020 and 2050 for scenario ssp370



All days vs. critical days

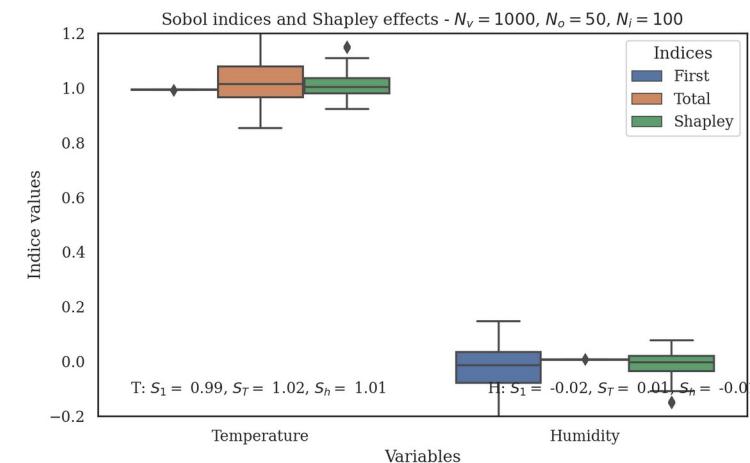
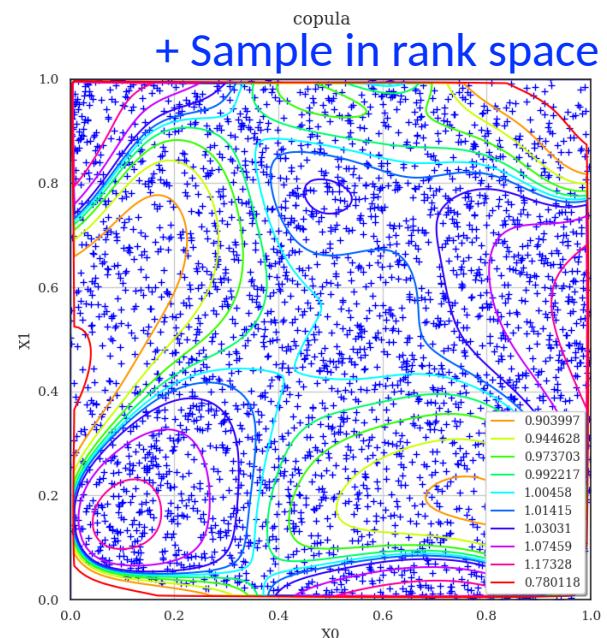
All year

Correlation coefficients
 Pearson: 0.77
 Spearman: 0.81



Critical days

Correlation coefficients:
 Pearson : -0.048
 Spearman : -0.018



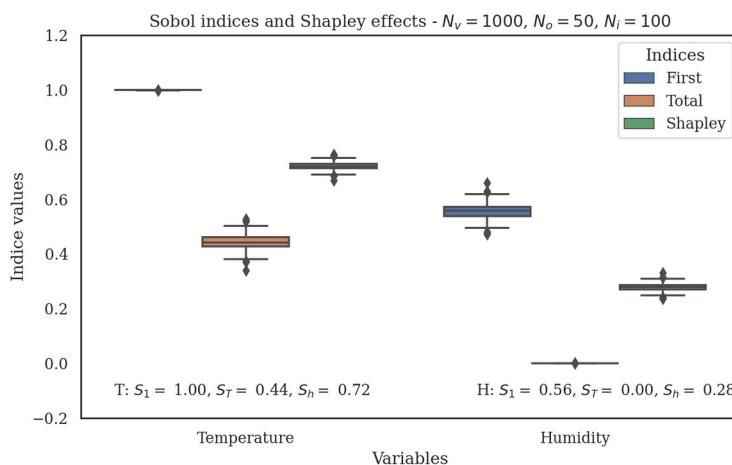
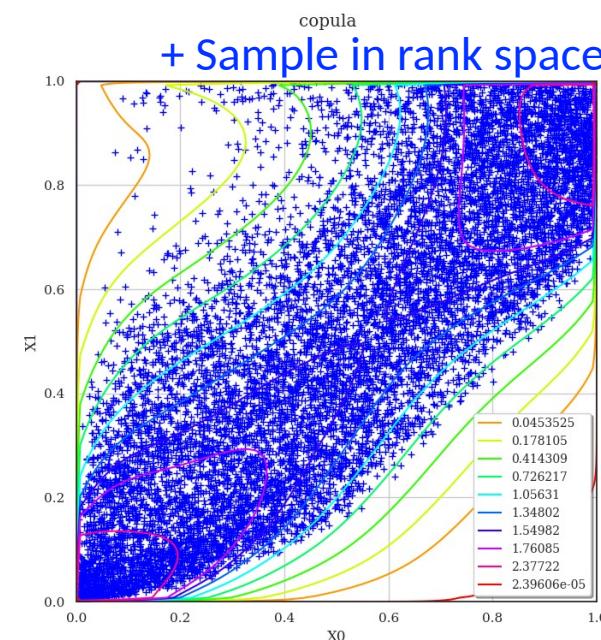
All days vs. critical days

All year

Correlation coefficients

Pearson: 0.77

Spearman: 0.81

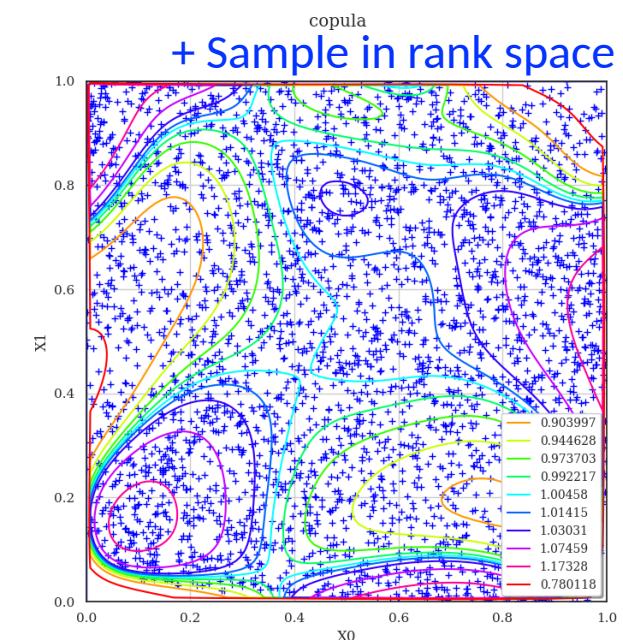


Critical days

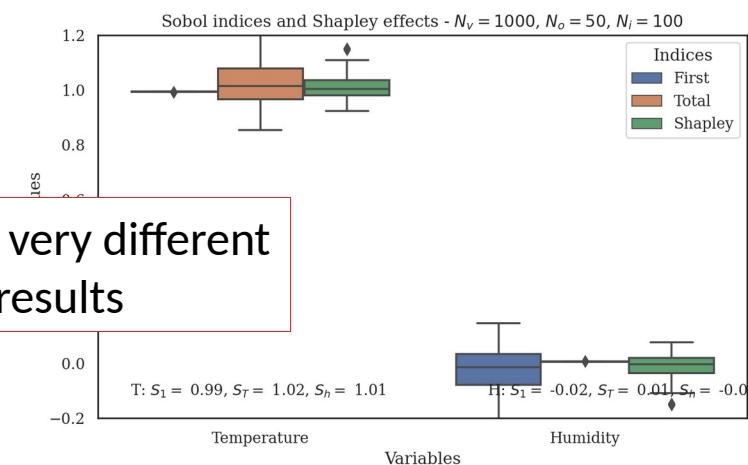
Correlation coefficients:

Pearson : -0.048

Spearman : -0.018



Dependency structure very different
✉ Impacts sensitivity results



Conclusion and perspectives

- High temperature and humidity have a negative effect on performance
- Sensitivity of MTOW: Temperature predominant in its elementary influence but humidity also has a non negligible influence in case of dependency
- Methodology put into place in order to add more input variables and outputs
 - Other atmospheric variables: wind components, precipitation...
 - Parameters of the aircraft: compression ratios, efficiencies in engine...

Thank you for your attention

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Some references

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