

Current situation of Project-Intrinsically

Syouki Tsuyama (Tokyo Tech)

Contents

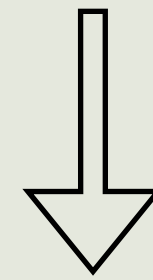
- Research concept & Background
 - One-shot Continuation
 - Multiplicity
 - Dependently-typed Compilers
- Current Condition & Future Work

Contents

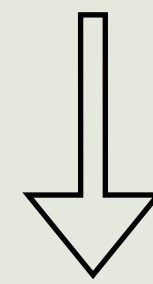
- Research concept & Background
 - One-shot Continuation
 - Multiplicity
 - Dependently-typed Compilers
- Current Condition & Future Work

Research Concept

Effect system + Tracing variable usage



Detect how many times operations use continuations



Make compiler that optimize based on continuation usage
(or optimizer)

One-shot Continuation^[Bruggeman PLDI'96]

Restricted continuations which can be called **at most once**

✓ `shift (fun k -> 0)`

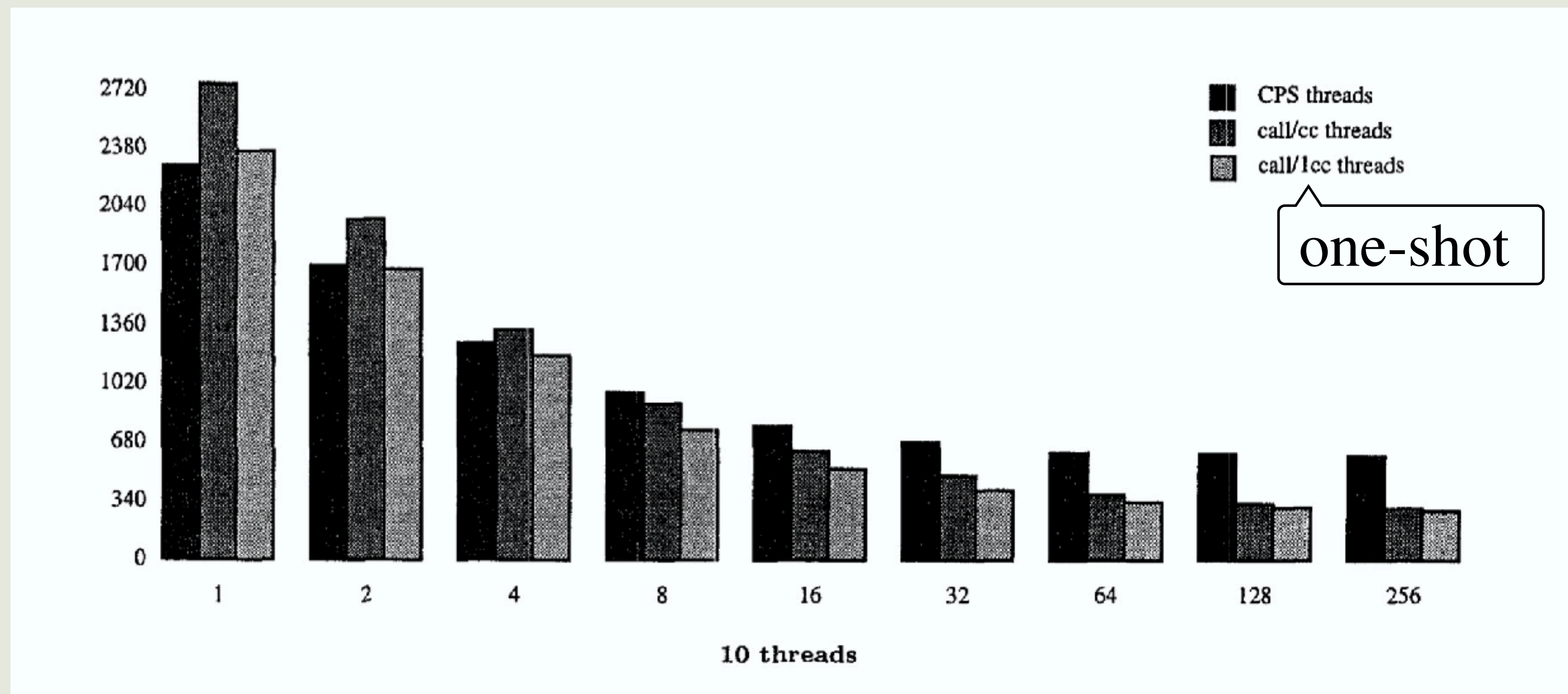
Continuation

✓ `shift (fun k -> k 0)`

✗ `shift (fun k -> (k , k))`

Compilation for One-shot Continuation

More efficient compilation^[Bruggeman PLDI'96]
than unrestricted continuation



Multiplicity

Multiplicity is given to each variable
to indicate how many times the variable is used

e.g.	0	Unused
	1	Used at once
	ω	Unrestricted

Multiplicity Example

$\text{drop} : (\textcolor{red}{0} \ x : \text{Int}) \rightarrow \text{Int}$
 $\text{drop } _ = 0$

$\text{id} : (\textcolor{red}{1} \ x : \text{Int}) \rightarrow \text{Int}$
 $\text{id } x = x$

$\text{copy} : (x : \text{Int}) \rightarrow \text{Int}$
 $\text{copy } x = (x, x)$

Counting Usage of Continuation

Continuation + Multiplicity

can detect whether k is one-shot or not

`shift (fun (\emptyset k) \rightarrow \emptyset)`

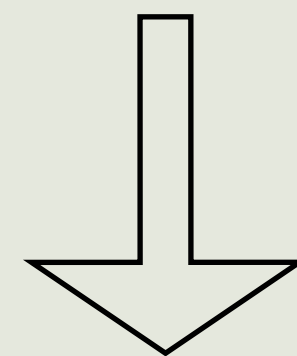
`shift (fun (1 k) \rightarrow k \emptyset)`

One-shot

`shift (fun (ω k) \rightarrow (k , k)) \rightarrow Unrestricted`

Dependently-typed Compiler [Pickard ICFP'21]

Intrinsically-typed AST (IT-AST)



`compile`

Target language

Dependent types help to
derive `compile` which satisfy correctness theorem

Components of Dependently-typed Compiler

Five components.

1. IT-AST

which represents only well-typed expression of source language

```
data Exp : Ty → Set
  num    : ℕ → Expr ℕ
  bool   : ℬ → Expr ℬ
```

2. ITI

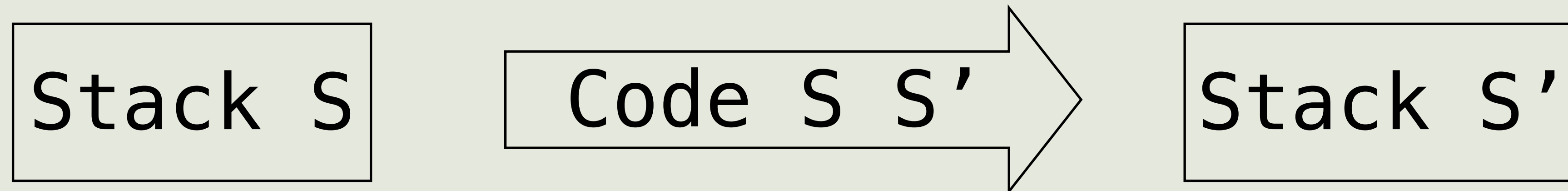
evaluates expressions of type T into values of type T

```
eval : Exp T → T
```

Components of Dependently-typed Compiler

3. Syntax of target language

Here, Code $S \ S'$ represents stack machine code



`data Stack : List Ty → Set`

`data Code : List Ty → List Ty → Set`

Input stack

Output stack

Components of Dependently-typed Compiler

4. Execution function

which determines semantics of target language

$\text{exec} : \text{Code } S \ S' \rightarrow \text{Stack } S \rightarrow \text{Stack } S'$

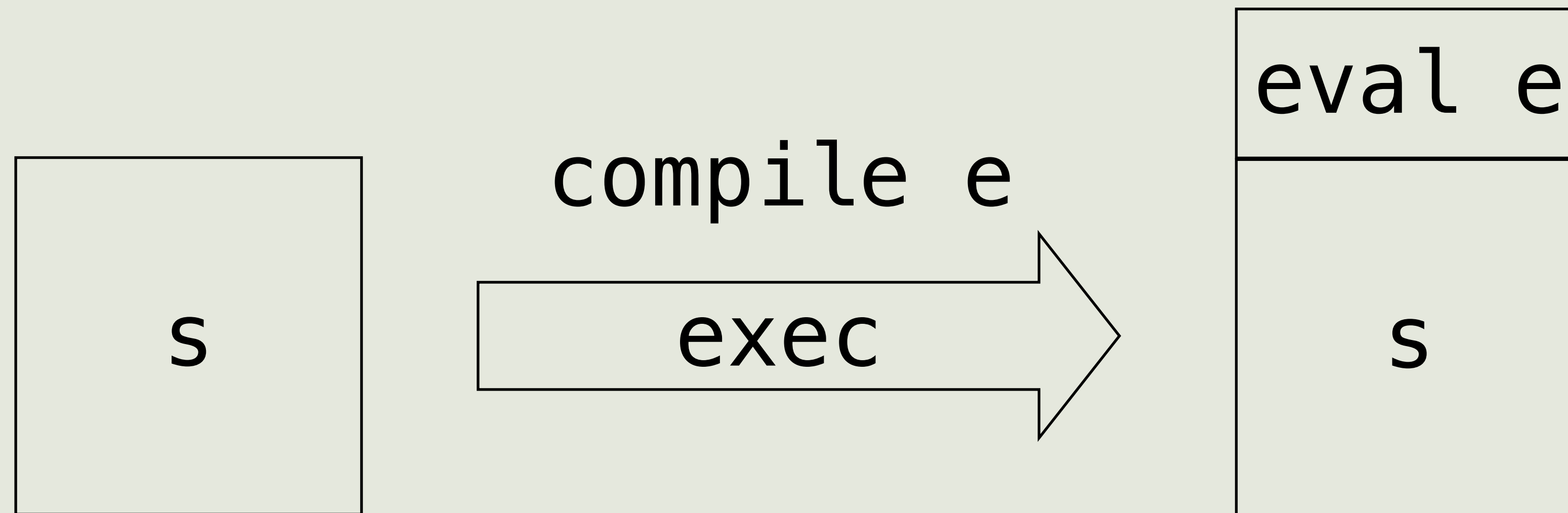
5. Compiler

which transforms IT-AST into target language

$\text{compile} : \text{Exp } T \rightarrow \text{Code } S \ (T :: S)$

Correctness Theorem

$\text{exec } (\text{compile } e) \ s \equiv (\text{eval } e) :: s$



Summerly

Source
program

\emptyset k

1 k

ω k

optimize

One-shot

Unrestricted

dependently-typed

compiler
optimizer

Contents

- Research concept & Background
 - One-shot Continuation
 - Multiplicity
 - Dependently-typed Compilers
- **Current Condition & Future Work**

λe : A language with algebraic effect

- Effect signature / Definition of effect

effect Choose { **choose** : () \rightarrow Bool }

Operation

- Handler / Behavior of the effect operation

handle { if (do **choose**()) then 1 else 0 }
with { **choose** _ k \rightarrow k true }

Adding New Feature / $\lambda e + \text{Multiplicity}$

effect Choose { choose : $() \rightarrow \text{Bool}$; 1 }

Continuation usage

handle { if (do choose()) then 1 else 0 }
with { choose _ k \rightarrow k true }

k can be used 1 times

λe so far

I used PHOAS for variable binding

However, PHOAS cannot extend with multiplicity

```
data Val (Var : VTy → Set) : VTy → Set where
  var : Var T → Val Var T
  fun : (Var A → Cmp Var C) → Val Var (A ⇒ C)
```

e.g. `id = fun (\x → x)`

Changing PHOAS to De Bruijn indice

Rewritten IT-AST using De Bruijn indice

```
data Val (Γ : Ctx) : VTy -> Set where
  var    : T ∈ Γ → Val Γ T
  fun    : Cmp (A :: Γ) C → Val Γ (A ⇒ C)
```

e.g. `id = fun (var 0)`

To give multiplicity, I'm going to rewrite to

```
Ctx = List (Ty × Mul)
```

Future Work

- Complete Intrinsically-typed AST
 - Need to consider composing and separation of Ctx
- learn how to compile continuation manipulation^[masuko PPL'10]
- Goal : Make a compiler or an optimizer