

Homework 2

Question 1:

Generate the coin flipping model for the following observed data:

trials = 4

theta_real = 0.35 # *unknown value in a real experiment*

data = pz.Binomial(n=1, p=theta_real).rvs(trials)

Compare the following priors:

1. $\theta \sim \text{Beta}(20, 20)$
2. $\theta \sim \text{Uniform}(0, 1)$
3. $\theta \sim \text{Uniform}(-1, 2)$

- a. Create graphic models (Kruschke diagrams) for all the options.
- b. Compare with the results of using *pm.model_to_graphviz*.
- c. Are there models that don't run or have errors? Explain.
- d. Compare the posteriors.

Question 2:

- a. Load the chemical shift data you saw in the lecture.
You can use this line to load the chemical shift data:

```
data =  
np.loadtxt("https://github.com/aloctavodia/BAP3/raw/refs/heads/main/code/data/chemical_shifts.csv")
```

- b. We will model the data using a normal distribution.
The prior for σ will be a halfnormal distribution with $\sigma_\sigma = 5$.
The prior for μ will be a normal distribution with $\mu_\mu = \text{mean}(\text{data})$.
We will try a few values for σ_μ (the standard deviation of the prior of μ).
 - Draw the model
 - Write the model equations

- c. Try a few values for σ_μ .
How robust/sensitive are the inferences to these changes? Include posterior predictive checks in your analysis.
- d. What do you think of using a Gaussian, which is an unbounded distribution (goes from $-\infty$ to ∞), to model bounded data (between 0-100) such as this?

Question 3:

Model the data using the Student's t-distribution instead of a normal distribution. Compare the results to those from Question 2.

Question 4:

We will define outliers as any value more than 1.5 IQR (Interquartile range) beyond the IQR.

- a. Compute the mean and standard deviation of the chemical shift with and without the outliers.
- b. Compare those results to the Bayesian estimation using the Gaussian and Student's t-distribution. What do you observe?
- c. Add more outliers to the data and compute new posteriors for the Student's t model and one of your normal models. What do you observe?

Question 5:

In both the tutorial and the lecture, we looked at the Tips dataset.

- a. Load the data and run the model as we did.
- b. Explore the InferenceData object.
 - 1. How many groups does it contain?
 - 2. Inspect the posterior distribution of the parameter μ for a specific day using the sel method.
 - 3. Compute and plot the distribution of the mean differences between Thursday and Sunday. What are the coordinates and dimensions of the resulting DataArray?