And, for the hous is crinkled to and fro, And hath so queinte weyes for to go— For hit is shapen as the mase is wroght— Therto have I a remedie in my thoght, That, by a clewe of twyne, as he hath goon, The same wey he may returne anoon, Folwing alwey the threed, as he hath come.

- Geoffrey Chaucer, The Legend of Good Women (c. 1385)

"Com'è bello il mondo e come sono brutti i labirinti!" dissi sollevato.
"Come sarebbe bello il mondo se ci fosse una regola per girare nei labirinti," rispose il mio maestro.

["How beautiful the world is, and how ugly labyrinths are," I said, relieved.
"How beautiful the world would be if there were a procedure for moving through labyrinths," my master replied.]

— Umberto Eco, Il nome della rosa (1980) English translation (*The Name of the Rose*) by William Weaver (1983)

6

Depth-First Search

In the previous chapter, we considered a generic algorithm—whatever-first search—for traversing arbitrary graphs, both undirected and directed. In this chapter, we focus on a particular instantiation of this algorithm called *depth-first search*, and primarily on the behavior of this algorithm in directed graphs.

Although depth-first search can be accurately described as "whatever-first search with a stack", the algorithm is normally implemented recursively, rather than using an explicit stack:

 $\frac{\text{DFS}(v):}{\text{if } v \text{ is unmarked}}$ $\max k v$ $\text{for each edge } v \rightarrow w$ DFS(w)