Graphical Abstract

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Highlights

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- Dam sites 18, 19, 20, and 28 appear most often in the results, making them reliable choices for Morocco's urgent dam site expansion needs.
- The four GP models (WGP, LGP, CGP, EGP) were extended with Multi-Choice Goal Programming to reflect the reality of multiple targets and choices in decision-making.
- Goal programming was adopted for it's closeness in underlying principles with Collective Intelligence.

Dam Site Selection for Expansion in Morocco using Multi-Criteria Decision Making

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Abstract

Water scarcity poses a critical challenge to Morocco, where dams remain central to national strategies for irrigation, hydropower, and water supply. Selecting suitable sites for dam expansion is a complex decision problem, requiring the balance of technical, economic, social, and environmental objectives. This study applies Multi-Criteria Decision Making (MCDM) through four Goal Programming (GP) variants—Weighted (WGP), Lexicographic (LGP), Chebyshev (CGP), and Extended (EGP)—to the selection of three dams from twenty-eight candidates under a fixed budget constraint. To reflect policy uncertainty, Multi-Choice Goal Programming (MCGP) extensions were incorporated for key socio-environmental targets (population, farmland area, residence distance, farmland distance, and road access). Results identify dams 18, 19, and 20 as a consistently robust core across models and scenarios, while dams 28, 21, and 23 emerge as flexible alternatives when environmental or social criteria are emphasized. Sensitivity analysis on both weights and targets confirms that WGP and LGP provide stable recommendations, whereas CGP and EGP display greater variability. These findings suggest that GP does not yield a single rigid solution but rather a decision space that combines stability with adaptability, allowing policymakers to reconcile competing objectives.Beyond the case of Morocco, the study contributes methodologically by integrating multi-choice goals and systematic sensitivity analysis into GP, and theoretically by framing dam site selection as a problem of compromise and robustness rather than strict optimization. The approach offers a transparent, adaptable, and policy-relevant decision-support tool for sustainable water infrastructure planning under uncertainty.

Keywords: Multi-Criteria Decision Making, Goal Programming, Dam Site Selection, Water Resource Management, Morocco

Acronyms

CGP Chebyshev Goal Programming. 1

CI Collective Intelligence. 1

EGP Extended Goal Programming. 1

GIS Geographic Information System. 1

GP Goal Programming. 1

LGP Lexicographic Goal Programming. 1

MCDM Multi-Criteria Decision Making. 1

MCGP Multi-Choice Goal Programming. 1

SA Sensitivity Analysis. 1

WGP Weighted Goal Programming. 1

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1. Introduction

Water has become one of the most strategically important and contested natural resources of the 21st century. Increasing population growth, accelerating urbanization, and the intensifying effects of climate change are exerting significant pressure on freshwater systems worldwide (American Meteorological Society 2017)[1]. Dams have historically played a critical role in water management, providing storage for irrigation, hydropower generation, domestic supply, and flood control. Globally, they are regarded as cornerstones of national development strategies, yet their design and expansion decisions require careful balancing of social, economic, and environmental considerations [2, 1].

In North Africa, and particularly in Morocco, the challenge of water scarcity is especially pronounced. Morocco is among the most water-stressed countries in the region, with per capita renewable water resources steadily declining over the last decades—from about $2,560m_3$ in 1960 to roughly $620m_3$ in 2020—due to reduced rainfall, rising demand, and sedimentation in existing reservoirs [3]. Dams remain central to Morocco's national water policy, as they underpin agricultural productivity, food security, and energy diversification. The government has therefore invested heavily in dam infrastructure expansion, with over 150 large dams already constructed and several additional projects planned [4]. However, the benefits of such infrastructure are accompanied by substantial trade-offs related to land use, environmental sustainability, and local socio-economic impacts.

Selecting suitable sites for future dams thus constitutes a complex strategic decision problem. Beyond hydrological and engineering feasibility, the siting of dams must also account for population distribution, access to transport networks, farmland protection, and broader ecological constraints. Conventional single-objective approaches often fall short in capturing these competing dimensions. As a result, there has been a shift toward multi-criteria decision making (MCDM) methods, which provide structured frameworks to integrate diverse quantitative and qualitative factors into dam site evaluations [4, 5]. In this study, we position dam site selection for expansion in Morocco within this broader discourse of sustainable and multi-objective water infrastructure planning.

1.1. Problem of Dam Site Selection

While dams are vital for Morocco's long-term water security and economic growth, the process of selecting their sites involves a web of conflicting objectives and constraints. On one hand, governments and planners seek to maximize storage capacity, agricultural productivity, and energy generation. On the other, environmental and social considerations, such as farmland preservation, displacement risks, ecological integrity, and equitable access, place strong constraints on dam siting decisions [6, 7]. These competing goals transform site selection from a straightforward engineering task into a multi-objective decision problem that requires balancing diverse interests under uncertainty.

Traditional approaches to dam site evaluation have often prioritized hydrological suitability or cost efficiency, using single-objective models that emphasize technical feasibility. However, these methods tend to underrepresent the wider social and environmental impacts, leading to decisions that may be technically sound but socially or ecologically unsustainable. To overcome these limitations, researchers and practitioners have increasingly adopted multi-criteria decision making (MCDM) frameworks, which explicitly incorporate heterogeneous factors into decision analysis [6, 8]. MCDM methods enable decision makers to consider trade-offs among economic, environmental, and social criteria, while also accommodating input from multiple stakeholders.

In Morocco, these complexities are heightened by the diversity of candidate dam sites and the country's urgent need for expansion under resource constraints. From the 28 candidate sites considered in this study, three could be selected, making the optimization problem both discrete and sensitive to value judgments about which criteria should dominate. This tension underscores the importance of adopting robust decision-support tools capable of producing transparent, justifiable, and adaptable recommendations. It is in this context that the present work turns to Goal Programming (GP) — a family of MCDM techniques especially suited to structuring and solving problems where multiple, potentially conflicting objectives must be addressed simultaneously.

1.2. Multi-Criteria Decision Making

Decision-making in real-world contexts rarely revolves around a single objective. Governments, businesses, and communities are frequently confronted with situations where they must balance conflicting goals—for example, maximizing economic returns while minimizing environmental damage, or ensuring technical efficiency while promoting social equity. To address such complexities, scholars and practitioners have developed Multi-Criteria Decision-Making (MCDM) as a structured scientific approach that enables systematic evaluation of alternatives when trade-offs are unavoidable [9, 10]. Far from being a purely theoretical construct, MCDM has become a practical decision-support tool that reflects the realities of modern governance and resource management [11].

At its core, Multi-Criteria Decision-Making (MCDM) refers to a family of quantitative and qualitative techniques designed to support decisions that involve multiple, often conflicting, evaluation criteria [9, 10]. Unlike simple optimization models, which concentrate on maximizing or minimizing a single objective, MCDM provides a structured way for decision-makers to balance competing priorities [12, 13]. In practice, this means that MCDM captures the reality that most real-world choices are about trade-offs rather than absolutes. In this sense, it can be seen as a form of collective reasoning: just as a group of individuals brings diverse perspectives to arrive at a shared judgment, MCDM integrates diverse evaluation criteria into a coherent and balanced decision outcome [14, 15].

Over time, Multi-Criteria Decision-Making (MCDM) has developed into an interdisciplinary field, drawing insights from mathematics, economics, computer science, and the social sciences. The rapid growth of computational power has accelerated this evolution, making it possible to design more sophisticated approaches. In particular, fuzzy MCDM methods have been introduced to address uncertainty in decision environments [16, 17], while hybrid approaches now integrate MCDM with artificial intelligence and machine learning to enhance accuracy and adaptability [18]. As a result, MCDM has moved beyond being a theoretical tool to become a cornerstone of modern decision science, widely applied to some of today's most complex real-world challenges.

MCDM techniques have demonstrated remarkable versatility across diverse fields. In engineering and environmental planning, they provide structured frameworks for prioritizing design alternatives and evaluating trade-offs in infrastructure development, environmental impact assessments, and land-use planning [18, 19]. In energy systems, MCDM has been employed to compare renewable energy technologies, identify suitable sites for facilities, and support the transition toward low-carbon strategies [20]. In the realm of business and finance, these methods assist managers in evaluating investment portfolios, assessing operational risks, and formulating strategic policies [21]. Beyond these traditional domains, MCDM has also become increasingly prominent in sustainability research, where decision-makers must balance economic growth, ecological preservation, and social welfare in an integrated manner [22, 17]. Collectively, these applications illustrate how MCDM adapts to the specific needs of each context while maintaining its role as a systematic tool for rational decision-making.

These applications highlight the very nature of the challenges MCDM is designed to address: decisions with multiple stakeholders, competing objectives, incomplete information, and long-term uncertainties. In this sense, MCDM resonates with the philosophy of collective intelligence, where diverse contributions must be synthesized into a coherent solution[15]. Just as collective intelligence seeks to prevent dominance by a single actor in group decision-making, MCDM provides a safeguard against the dominance of a single criterion in technical evaluations. This parallel underscores MCDM's role not only as a computational tool but also as a conceptual bridge between quantitative rigor and inclusive decision-making.

The importance of MCDM has grown in recent decades due to the increasing complexity of global challenges. Climate change, resource scarcity, and sustainable development goals all require decisions that balance competing priorities. For instance, governments must decide how to allocate limited water supplies across agriculture, energy, and domestic use; companies must balance profitability against environmental and social responsibility; and communities must weigh development needs against cultural and ecological preservation [12, 23]. Traditional single-objective decision tools fall short in these contexts, while MCDM offers a structured and transparent process for evaluating trade-offs.

MCDM provides a rigorous yet flexible decision-support framework, particularly well-suited to wicked problems—those with no single optimal solution but multiple competing pathways. This makes it a powerful tool for addressing Morocco's dam site investment challenge, where economic, social, and environmental goals must all be considered simultaneously under conditions of uncertainty.

1.3. MCDM in Water Resource Management and Dam Site Selection

The complexity of water resource management makes it a prominent field for the application of Multi-Criteria Decision-Making (MCDM). Early studies in this domain emphasized technical and economic feasibility, particularly in irrigation planning, watershed management, and hydropower development [20, 24]. However, these approaches often overlooked environmental and social dimensions, limiting their comprehensiveness.

From the mid-2000s onward, the literature reflects a growing integration of Geographic Information Systems (GIS) with MCDM to enable spatially explicit decision frameworks. For example, [24] combined GIS and AHP to identify hydropower locations in Brazil, while [18] applied GIS-based multi-criteria analysis for dam site suitability in Turkey. These studies highlighted how spatial integration of hydrological, geological, and socio-economic data strengthens the robustness of site evaluations.

Uncertainty in hydrological and climate conditions has also driven the development of fuzzy and probabilistic MCDM methods. [16] pioneered fuzzy extensions of MCDM based on ideal and anti-ideal concepts, and subsequent reviews [17] show that fuzzy MCDM techniques have become widely used for handling ambiguity in water resource allocation and dam planning. Recent studies extend this trend by employing hybrid models that combine MCDM with optimization algorithms or artificial intelligence. [25], for instance, integrated hybrid artificial intelligence models with multi-criteria decision analysis to improve flood risk assessment in Vietnam.

The evolution of criteria in dam site selection is another clear trend. While early models emphasized economic and engineering parameters, contemporary studies increasingly incorporate environmental and social concerns such as biodiversity protection, resettlement impacts, and ecosystem trade-offs [19, 18]. Reviews of the literature highlights four broad developments. The widespread adoption of GIS for spatial analysis, a shift toward sustainability criteria alongside engineering and economic factors,expanded use of fuzzy and probabilistic approaches to address uncertainty, and the integration of MCDM with machine learning and optimization for greater accuracy.

Despite these advances, several gaps persist. The selection and weighting of criteria remain highly subjective and context-dependent, creating challenges for replicability [26, 17]. Data scarcity, especially in developing regions, further constrains model precision and reliability [20, 19]. Moreover, most studies emphasize greenfield projects such as new dams or small hydropower, while fewer address the optimization of existing infrastructure, which is equally critical under climate and fiscal constraints [12, 24]. Finally, there is limited application of these frameworks in North African contexts, despite acute water scarcity and reliance on dams in countries such as Morocco [22].

This gap is particularly significant for Morocco, where the central challenge is not simply the identification of new dam sites but the prioritization of existing infrastructure for expansion and rehabilitation under competing economic, environmental, and social pressures. Addressing this gap requires the adoption of systematic, context-specific MCDM frameworks that explicitly integrate sustainability goals with fiscal and climate realities.

1.4. Collective Intelligence in MCDM

Multi-Criteria Decision-Making (MCDM) offers a family of methodologies—ranging from value measurement methods such as the Analytic Hierarchy Process (AHP) and Analytic Network Process (ANP), to outranking methods such as ELECTRE and PROMETHEE, to distance-based techniques like TOPSIS, and to mathematical programming approaches such as Goal Programming (GP) and Multi-Objective Linear Programming (MOLP)[26, 9]. Each methodology provides a different mechanism for balancing conflicting objectives: value measurement methods rely on hierarchical structuring and subjective weights, outranking methods emphasize pairwise comparison and preference thresholds, distance-based approaches compare alternatives to ideal/anti-ideal solutions, and mathematical programming models optimize across multiple objectives under explicit constraints.

Theories of collective intelligence (CI), as discussed by [27], highlight that groups outperform individuals when three conditions are met: diversity of perspectives, independence of judgments, and effective aggregation mechanisms. When viewed through this lens, MCDM methodologies can be understood as formal aggregation mechanisms that operationalize these principles. AHP and ANP capture diversity through structured weighting, outranking methods allow pluralism of thresholds and vetoes, and fuzzy/grey extensions address uncertainty in human judgments [17, 16]. However, most of these methods are either too dependent on subjective weights or lack iterative feedback loops that resemble the adaptive, deliberative, and iterative nature of CI systems [15].

Goal Programming (GP) stands out as the MCDM methodology most aligned with CI theories. Like collective intelligence, GP does not aim for a single optimal solution but rather for a satisficing compromise that balances multiple, often conflicting, goals. Just as groups rarely arrive at unanimous "optimal" outcomes but instead reach negotiated compromises through deliberation, GP models minimize deviations from a set of priority-ranked or weighted goals rather than forcing one criterion to dominate [13]. Moreover, GP frameworks are inherently flexible: they allow the integration of diverse stakeholder goals, adjustment of priorities, and iterative recalibration—mirroring the feedback-driven and inclusive character of collective intelligence processes [14].

While many MCDM methods resonate with elements of CI, Goal Programming is the methodology that most closely embodies its spirit, particularly in contexts where diverse goals must be reconciled rather than hierarchically imposed. For this reason, our study adopts four distinct Goal Programming models—Weighted Goal Programming (WGP), Compromise Goal Programming (CGP), Extended Goal Programming (EGP), and Lexicographic Goal Programming (LGP), to investigate how different compromise structures capture the dynamics of collective decision-making in complex, multi-criteria contexts.

1.5. Goal Programming

Goal Programming (GP) is particularly well suited for addressing complex infrastructure planning problems such as dam site selection, where multiple and often conflicting objectives must be balanced. Unlike single-objective optimization, which collapses diverse concerns into a single aggregate function, GP preserves the multi-dimensional nature of decision making [28]. It does so by minimizing deviations from multiple goals, thereby offering solutions that reflect a compromise among technical, economic, environmental, and social considerations. In recent years, GP models have been applied in contexts with strong stakeholder conflicts and ecological constraints, creating more sustainable decision pathways [29].

A further advantage of GP lies in its flexibility. The method allows for different formulations that align with distinct decision-making philosophies. The Weighted Goal Programming (WGP) model facilitates explicit trade-offs between goals through assigned weights, making it well suited for contexts where objectives can be expressed in relative importance [30]. Lexicographic Goal Programming (LGP), by contrast, imposes a strict hierarchy of priorities, ensuring that higher-order goals are fully satisfied before lower-order ones are considered [13]. Chebyshev Goal Programming (CGP) emphasizes fairness by minimizing the maximum deviation across all goals, producing outcomes that are more equitable among competing objectives [30]. Finally, the Extended Goal Programming (EGP) model generalizes the GP framework by introducing additional parameters that penalize deviations asymmetrically, thereby capturing flexible stakeholder preferences and allowing more nuanced solutions [13]

Taken together, these four formulations enable decision makers to examine the dam site selection problem through multiple lenses: balanced compromise (WGP), priority satisfaction (LGP), fairness (CGP), and flexibility (EGP). In this study, each formulation is mapped to a distinct sub-question concerning how Morocco's dam expansion strategy might weigh competing objectives. By doing so, the analysis not only identifies feasible dam site combinations, but also generates a spectrum of alternatives reflecting different governance and policy orientations. This multi-model approach also strengthens the robustness of final recommendations, as it allows comparisons across frameworks and provides insights into the conditions under which different dam sites emerge as optimal.

2. Methodology

Research Objectives and Sub-Questions

The overarching objective of this research is to support evidence-based dam site selection for Morocco's future water infrastructure expansion, under conditions of competing economic, social, environmental, and technical objectives. Specifically, the study addresses the challenge of selecting three sites from a pool of 28 candidate dams, while ensuring that the solutions remain robust, transparent, and adaptable to shifting policy priorities.

To operationalize this objective, the study applies four Goal Programming (GP) formulations, each addressing a distinct sub-question:

- **Weighted Goal Programming (WGP):** What is the most balanced solution when objectives are explicitly weighted according to their relative ?
- **Lexicographic Goal Programming (LGP):** What solution emerges when objectives are ranked hierarchically and pursued in strict priority order?
- **Chebyshev Goal Programming (CGP):** How can the selection be made fair by minimizing the maximum deviation across all objectives?
- **Extended Goal Programming (EGP):** How do flexible formulations, which penalize deviations asymmetrically, alter site selection when stakeholder preferences are uneven?

In addition to these base models, the research incorporates Multi-Choice Goal Programming (MCGP) extensions, which allow for more realistic goal setting by considering intervals or multiple aspiration levels rather than fixed targets. This extension captures the uncertainty and diversity of stakeholder preferences, broadening the scope of feasible solutions.

Finally, a Sensitivity Analysis (SA) is performed on both weights and targets to evaluate the robustness and reliability of the proposed solutions. The SA addresses questions such as: *How stable are the selected dam* *sites under changing weight assignments?* and *Which dams remain consistently selected across different target scenarios?*

2.1. Criteria Selection

The robustness of any Multi-Criteria Decision-Making (MCDM) model depends fundamentally on the choice of evaluation criteria, since these define the dimensions along which dam sites are assessed. The inclusion or exclusion of particular indicators can significantly influence outcomes, as previous studies on dam planning have demonstrated [31]. In this study, ten criteria were selected to evaluate and prioritize dam sites for investment in Morocco, combining technical, environmental, socio-economic, and infrastructural dimensions to ensure a balanced assessment. Table 1 summarizes these criteria, their units, data sources, and justifications.

Technical indicators such as dam height, storage capacity, and reservoir area were included because they determine the physical potential of a site to store water. These measures are widely used in hydropower site selection literature and remain fundamental in investment decisions [32, 33]. Climatic conditions, represented by temperature and rainfall, provide essential insight into the sustainability of storage and inflows. High temperatures intensify evaporation losses, while rainfall history indicates hydrological reliability, both of which are critical under Morocco's variable climate [34].

Socio-economic dimensions were captured by commune population, proximity to residential centers, farmland area, and farmland distance. Population reflects demand pressure and potential beneficiaries, though normalization was conducted to prevent large communes from skewing results [35, 36]. Likewise, farmland measures account for the agricultural benefits of dam expansion, emphasizing the role of irrigation in Morocco's water strategy [37]. Proximity to settlements ensures accessibility and equity, aligning with social sustainability goals.

Infrastructural connectivity, represented by the distance to the nearest road, was included because access routes directly affect construction costs, operational efficiency, and maintenance feasibility [38]. Together, these ten dimensions ensure that the analysis captures Morocco's triple objective: meeting water demand, ensuring economic returns, and promoting long-term sustainability.

To estimate the targets for each criterion, the model maximizes values under the constraint of selecting three dams with a total budget of 500 million USD. The maximum achievable objective then serves as the benchmark or "target." This approach ensures that the targets are not arbitrary but instead reflect realistic upper bounds within fiscal and operational constraints.

Insights from prior studies further underscore the importance of such criteria design. For instance, Rana and Patel (2020) demonstrated that including population data shifted site rankings compared to purely technical models [33], while [39] showed that incorporating ecological considerations produced different priorities than cost-based evaluations alone . These findings confirm that criteria selection fundamentally shapes decision outcomes.

The ten selected criteria provide a comprehensive and context-appropriate framework for evaluating Morocco's dams. By incorporating physical, climatic, social, and infrastructural factors (see Table 1), the study ensures methodological rigor while reflecting principles of collective intelligence.

2.2. *Data Source*

Hydrological and structural attributes of dams were obtained from the Food and Agriculture Organization (FAO) AQUASTAT database for Morocco [40]. Dam height is reported in meters (m) and refers to the vertical distance from the crest to the lowest foundation point. Storage capacity is measured in million cubic meters (10^6 m^3) and reflects the initial designed volume of the reservoir, not considering reduction due to sedimentation. Reservoir surface area is reported in square kilometers (km^2) and shows the water-covered footprint when the reservoir is at full supply level.

Climatic data were sourced from the NASA POWER database [41], which provides historical rainfall and temperature records. For each dam-site commune, monthly values from 2010 to 2024 were aggregated into annual totals, and the median annual values were taken as representative estimates. Rainfall is expressed in millimeters per year (mm/year), while temperature is measured in degrees Celsius (°C).

Socio-economic and land-use indicators were extracted from shapefiles obtained from SIG-Maroc [42] and processed with QGIS and Python. Commune population provides an estimate of the number of residents living in the same commune as the dam site. Because population values varied widely (range: 1,276–1,494,413; span: 1,493,137) [35], the data were normalized using min–max scaling into a 0–50 range to reduce the influence of extremes [36, 43]. Distance to the nearest road was calculated in kilometers (km) using geographical coordinates of each dam [44], provincial route shapefiles [45], and the Python GeoPandas package [46]. Farmland area was derived from land use/land cover (LULC) shapefiles [47] and estimated in square meters (m^2), while farmland distance was calculated as the shortest distance between the dam-site centroid and the closest farmland polygon [48].

Finally, nearest conglomerate residence — defined as the shortest distance between the dam site and the nearest highly populated settlement — was estimated by visual inspection of Google Earth imagery [49], combined with distance calculations using the Geopy Python package [50].

2.3. *Goal Porgramming Variants*

A generic goal program [13] may be presented as:

Minimize:

$$a = h(n, p) \tag{1}$$

Subject to:

$$f_q(x) + n_q - p_q = b_q \qquad q = 1, ..., Q \tag{2}$$

$$x \varepsilon R \tag{3}$$

$$n_q, p_q \geq 0 \qquad q = 1, ..., Q \tag{4}$$

The generic Goal Programme has Q goals involving n decision variables $x = x_1, x_2, ..., x_n$. Each goal q has a target value b_q and an acheived value $f_q(x)$. Each goal then has a positive or negative deviational varibales p_q

Table 1: Summary of Criteria and Data Sources

Criterion	Data Source	Unit	Processing Notes
Dam height	FAO AQUASTAT [40]	Meters	Direct extraction from national database
Reservoir storage capacity	FAO AQUASTAT [40]	Million m^3	Used as initial reservoir volume
Reservoir surface area	FAO AQUASTAT [40]	km^2	Used to assess spatial footprint
Annual rainfall (median)	NASA POWER [41]	mm/year	Aggregated from monthly data (2010–2024)
Annual temperature (median)	NASA POWER [41]	°C	Aggregated from monthly data (2010–2024)
Commune population	SIG-Maroc [42]	Persons	Derived from shapefiles; normalized via min–max scaling
Distance to nearest road	SIG-Maroc [42]	Kilometers	Calculated using GeoPandas and provincial road shapefiles
Farmland area	LULC Archive [47]	m^2	Extracted from LULC shapefiles via geospatial processing
Distance to farmland	LULC Archive [47]	Kilometers	Spatially computed from dam-site centroid
Distance to nearest conglomerate residence	Google Earth + Geopy [50]	Kilometers	Visual inspection + spatial computation using Python

and n_q respectively. p_q and n_q are non-negative and cannot be non-zero simultaneously. h is a function of the deviational variables representing the penalties associated with non-acheivement of the targets and R is the feasible region of x in decision space.

2.4. *Weighted Goal Programming*

In Weighted Goal Programming (WGP) the objective function is a simple sum of the deviational variables by allocating suitable weigts to each of them (the L_1 metric). [13] recommend normalisation and assuming that $b_q > 0 \qquad q = 1, ..., Q$, the model becomes:

Minimize:

$$a = \sum_{q=1}^{Q} \left(\frac{u_q n_q}{b_q} + \frac{v_q p_q}{b_q} \right) \tag{5}$$

Subject to:

$$f_q(x) + n_q - p_q = b_q \qquad q = 1, ..., Q \tag{6}$$

$$x \varepsilon R \tag{7}$$

$$n_q, p_q \geq 0 \qquad q = 1, ..., Q \tag{8}$$

Where R is the feasible region of x in the decision space.

Dam Site Selection for Expansion, Weighted Goal Program Formulation:

Minimise:

$$\min a = \frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.04}p_3 + \frac{1}{48.74}p_4 + \frac{1}{0.52}n_5 + \frac{1}{22.07}n_6 + \frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9 + \frac{1}{0.68}n_{10} \tag{9}$$

Subject to:

$$\sum_{i=1}^{28} h_i x_i + n_1 - p_1 = 47 \tag{10}$$

$$\sum_{i=1}^{28} c_i x_i + n_2 - p_2 = 3 \tag{11}$$

$$\sum_{i=1}^{28} r_i x_i + n_3 - p_3 = 0.04 \tag{12}$$

$$\sum_{i=1}^{28} t_i x_i + n_4 - p_4 = 48.74 \tag{13}$$

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52 \tag{14}$$

$$\sum_{i=1}^{28} rain_i x_i + n_6 - p_6 = 22.07 \tag{15}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86 \tag{16}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32 \tag{17}$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23 \tag{18}$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68 \tag{19}$$

$$\sum_{i=1}^{28} x_i = 3 \tag{20}$$

$$\sum_{i=1}^{28} b_i x_i \leq 500 \tag{21}$$

2.5. Chebyshev Goal Programming

In Chebyshev Goal Programming (CGP) the objective is to minimize the maximum deviation of the goal. The CGP was first used by Flavell [51] but more recent examples are given in [52, 53]. This minmax criteria uses the L_∞ metric and aims to achieve a balance between the different levels of the statisfaction of each of the goals. The model is defined as:

Minimize:

$$a = D \tag{22}$$

Subject to:

$$f_q(x) + n_q - p_q = b_q \qquad q = 1, ..., Q \tag{23}$$

$$\frac{u_q n_q}{b_q} + \frac{v_q p_q}{b_q} \leq D \qquad q = 1, ..., Q \tag{24}$$

$$x \varepsilon F \tag{25}$$

$$n_q, p_q \geq 0 \qquad q = 1, ..., Q \tag{26}$$

$$D \geq 0 \tag{27}$$

All variables non-negative.

Dam site selection for expansion, Chebyshev Goal Program Formulation:

Minimise:

$$a = D \tag{28}$$

Subject to:

$$\sum_{i=1}^{28} h_i x_i + n_1 - p_1 = 47 \tag{29}$$

$$\sum_{i=1}^{28} c_i x_i + n_2 - p_2 = 3 \tag{30}$$

$$\sum_{i=1}^{28} r_i x_i + n_3 - p_3 = 0.04 \tag{31}$$

$$\sum_{i=1}^{28} t_i x_i + n_4 - p_4 = 48.74 \tag{32}$$

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52 \tag{33}$$

$$\sum_{i=1}^{28} rain_i x_i + n_6 - p_6 = 22.07 \tag{34}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86 \tag{35}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32 \tag{36}$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23 \tag{37}$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68 \tag{38}$$

$$\sum_{i=1}^{28} x_i = 3 \tag{39}$$

$$\sum_{i=1}^{28} b_i x_i \leq 500 \tag{40}$$

$$\frac{1}{47} n_1 \leq D \tag{41}$$

$$\frac{1}{3} n_2 \leq D \tag{42}$$

$$\frac{1}{0.04} p_3 \leq D \tag{43}$$

$$\frac{1}{0.04} p_4 \leq D \tag{44}$$

$$\frac{1}{48.74} n_5 \leq D \tag{45}$$

$$\frac{1}{0.52} n_6 \leq D \tag{46}$$

$$\frac{1}{22.07} p_7 \leq D \tag{47}$$

$$\frac{1}{0.32} p_8 \leq D \tag{48}$$

$$\frac{1}{0.23} p_9 \leq D \tag{49}$$

$$\frac{1}{0.68} n_{10} \leq D \tag{50}$$

2.6. Extended Goal Programming

Extended Goal programming (EGP) was first proposed by Romero [54] in the context of a lexicographic ordering of the goals and was later generalised in [55]. Some recent applications include [56, 57]. It aims to allow both of the above approaches by combining the optimisation given by WGP and the balancing given by CGP. For a nonlexicographic EGP, the general model is:

Minimise:

$$a = \alpha D + (1 - \alpha) \sum_{q=1}^{Q} \left(\frac{u_q n_q}{b_q} + \frac{v_q p_q}{b_q} \right) \tag{51}$$

Subject to:

$$f_q(x) + n_q - p_q = b_q \qquad q = 1, ..., Q \tag{52}$$

$$\frac{u_q n_q}{b_q} + \frac{v_q p_q}{b_q} \leq D \qquad q = 1, ..., Q \tag{53}$$

$$x \varepsilon F \tag{54}$$

$$n_q, p_q \geq 0 \qquad q = 1, ..., Q \tag{55}$$

$$D \geq 0 \tag{56}$$

The parameter α is a constant between 0 and 1 which controls the mix of optimization (L_1)and balance (L_∞) in the acheivement function.

Dam site selection for expansion, Extended Goal Program Formulation:

Minimise:

$$\begin{aligned}\min Z = \alpha D_1 + (1-\alpha)\Bigg(\frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.04}p_3 + \frac{1}{48.74}p_4 + \frac{1}{0.52}n_5 + \frac{1}{22.07}n_6 \\ + \frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9 + \frac{1}{0.68}n_{10}\Bigg)\end{aligned} \tag{57}$$

Subject to:

$$\sum_{i=1}^{28} h_i x_i + n_1 - p_1 = 47 \tag{58}$$

$$\sum_{i=1}^{28} c_i x_i + n_2 - p_2 = 3 \tag{59}$$

$$\sum_{i=1}^{28} r_i x_i + n_3 - p_3 = 0.04 \tag{60}$$

$$\sum_{i=1}^{28} t_i x_i + n_4 - p_4 = 48.74 \tag{61}$$

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52 \tag{62}$$

$$\sum_{i=1}^{28} rain_i x_i + n_6 - p_6 = 22.07 \tag{63}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86 \tag{64}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32 \tag{65}$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23 \tag{66}$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68 \tag{67}$$

$$\sum_{i=1}^{28} x_i = 3 \tag{68}$$

$$\sum_{i=1}^{28} b_i x_i \leq 500 \tag{69}$$

$$\frac{1}{47} n_1 \leq D \tag{70}$$

$$\frac{1}{3} n_2 \leq D \tag{71}$$

$$\frac{1}{0.04} p_3 \leq D \tag{72}$$

$$\frac{1}{0.04} p_4 \leq D \tag{73}$$

$$\frac{1}{48.74} n_5 \leq D \tag{74}$$

$$\frac{1}{0.52} n_6 \leq D \tag{75}$$

$$\frac{1}{22.07} p_7 \leq D \tag{76}$$

$$\frac{1}{0.32} p_8 \leq D \tag{77}$$

$$\frac{1}{0.23} p_9 \leq D \tag{78}$$

$$\frac{1}{0.68} n_{10} \leq D \tag{79}$$

2.7. Lexicographic Goal Programming

To formulate the lexicographic goal program algebraically, we define the number of priority levels as L with corresponding index $l = 1, ..., L$. Each priority level now becomes a function of a set of unwanted deviational variables which we define as $h_1(n, p)$, giving the equation below:

Minimize:

$$a = [h_1(n, p), \qquad h_2(n, p), ..., \qquad h_L(n, p)] \tag{80}$$

Subject to:

$$f_q(x) + n_q - p_q = b_q \qquad q = 1, ..., Q \tag{81}$$

$$x \varepsilon F \tag{82}$$

$$n_q, p_q \geq 0 \qquad q = 1, ..., Q \tag{83}$$

where each $h_1(n, p)$ contains a number of unwanted deviational variables. The exact nature of $h_1(n, p)$ depends on the nature of the goal programme to be formulated, but if we assume that it is linear and separable then it will assume the form

$$h_1(n, p) = \sum_{q=1}^{Q} \left(\frac{u_q^l n_q}{b_q} + \frac{v_q^l p_q}{b_q} \right) \tag{84}$$

Where u_q^l is the preferential weight associated with the minimisation of n_q in the lth priority level. v_q^l is the preferential weight associated with the minimisation of p_q in the lth priority level.

To model our problem using the Lexicographic Goal Programming, we group goals into three priority levels, priority level 1 (Dam Hieght, Dam Capacity, Population, and Farmland Area), priority level 2 (Reservoir Area, Temperature, and Rainfall), and priority level 3 (Residence distance,Farmland distance, and Nearest road distance). In this caterization, we consider the goals in the first priority level as infinitely more important than goal in lower levels. In practice, this means that the optimization first focuses on minimizing deviations for the goals in priority level 1. Only after the best possible achievement of these goals is secured do we consider the goals in priority level 2, and subsequently priority level 3. At each stage, the solution space is restricted so that improvements at lower levels never come at the expense of higher-level goals. This hierarchical structure reflects the decision makers' preferences, ensuring that the most critical objectives dominate the solution process.

Let P_1 and P_2 be the objective function values for Priority 1 and Priority 2, the EqLGPObjectivePriorityThree-ThirtySeven model can be expressed as follows: Priority one (1) Model:

Minimize:

$$\min a = \frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.52}n_5 + \frac{1}{0.68}n_{10} \tag{85}$$

Subject to:

$$\text{Equations (58) to (124)}$$

Priority two (2) Model:

Minimise:

$$\min a = \frac{1}{0.04}p_3 + \frac{1}{48.74}p_4\frac{1}{22.07}n_6 \tag{86}$$

Subject to:

$$Equations\ (58)\text{ to }(124)$$

$$\frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.52}n_5 + \frac{1}{0.68}n_{10} = P_1 \tag{87}$$

Priority three (3) Model:

Minimise:

$$\min a = \frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9 \tag{88}$$

Subject to:

$$Equations\ (58)\text{ to }(124)$$

$$\frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.52}n_5 + \frac{1}{0.68}n_{10} = P_1 \tag{89}$$

$$\frac{1}{0.04}p_3 + \frac{1}{48.74}p_4\frac{1}{22.07}n_6 = P_2 \tag{90}$$

2.8. Multi-Choice Goal Programming

In traditional goal programming, a decision maker specifies a single aspiration level for each goal. For example, a target profit, a desired level or service, or environmental impact. The model then seeks to minimize the difference between what is acheived and this single target.

However, in many real-world problems, it is unrealistic to think that there is only one acceptable target. Decision Makers may instead face a situation where several possible aspiration levels are reasonable. For example, a company might aim for at least \$1M in profit, but would also be satisfied if it reaches \$1.2M or \$1.3M. Similarly, a community might consider different acceptable levels of water storage or pollution reduction.

This is where Multi-Choice Goal Programming (MCGP) comes in. Instead of fixing just one aspiration level per goal, MCGP allows multiple aspiration levels to be set. The model then chooses the most appropriate level during optimization, depending on what is feasible given the constraints. This flexibility better reflects the real uncertainty and negotiation invloved in decision making.

MCGP General Formulation

The general idea of the MCGP can be written as [28]:

Minimise:

$$\min a = \sum_{i=1}^{n} \left(d_i^+ + d_i^-\right) \tag{91}$$

Subject to:

$$f_i(X) - d_i^+ + d_i^- = g_{ij} * z_{ij}, \qquad i = 1, 2, ..., n \tag{92}$$

Where:

- $f_i(X)$ is the achievement of goal i
- $g_i j$ is one of the possible aspiration levels for goal i
- d_i^+ and d_i^- are the over-archievement deviations
- $z_i j$ is a binary variable that selects which aspiration level is chosen for goal i
- X is the set of decision varibales subject to feasiblity constraints.

Under each goal, the model not only minimizes deviations but also chooses which level among the multiple options is best matched under the given conditions.

2.9. Applying Multi-Choice Goal Programming

The concept of Multi-Choice Goal Programming is applied to Weigthed Goal Program model (WGP), Chebyshev Goal Program (CGP), and Extended Goal Program (EGP). For our dam site selection project, 5 of the targets can be could assume multiple values. These are population, residence distance, farmland distance, nearest road, and farmland area. Thus, an extra goal value, which is 10 percent (10%) more than the original goal is created for each.

2.9.1. *Multi-Choice Weighted Goal Program (MCWGP)*

To extend Weighted Goal program to multi-choice goal program, the orginal weigted goal program defined from equations (93) to (124) is maintained. the only change will be in the targets of the constraints corresponding to population, residence distance, farmland distance, nearest road, and farmland area as showed below:

Minimise:

$$\begin{aligned} \min a = \frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.04}p_3 + \frac{1}{48.74}p_4 + \frac{1}{0.52}n_5 + \\ \frac{1}{22.07}n_6 + \frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9 + \frac{1}{0.68}n_{10} \end{aligned} \tag{93}$$

Subject to:

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52z_1 + 0.57(1 - z_1) \tag{94}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86z_2 + 2.05(1 - z_2) \tag{95}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32z_3 + 0.35(1 - z_3) \tag{96}$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23z_3 + 0.25(1 - z_3) \tag{97}$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68z_5 + 0.75(1 - z_5) \tag{98}$$

All other equations from equation (93) to (124) remain unchanged.

Where z_1, z_2, z_3, z_4, and z_5 are binary vairables.

2.9.2. *Multi-Choice Chebyshev Goal Program (MCWGP)*

In a similar approach, we extend the Chebyshev Goal Program with the target flexibility of the multi-choice goal program. To acheive this, we maintain all equations of the the CGP and change the targets for population, residence, farmland, nearest road, and farm area constraints.

Minimize:

$$a = D \tag{99}$$

Subject to:

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52z_1 + 0.57(1 - z_1) \tag{100}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86z_2 + 2.05(1 - z_2) \tag{101}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32z_3 + 0.35(1 - z_3) \quad (102)$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23z_3 + 0.25(1 - z_3) \quad (103)$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68z_5 + 0.75(1 - z_5) \quad (104)$$

All other equations from equation (58) to (124) remain unchanged.

$$\sum_{i=1}^{28} x_i = 3 \quad (105)$$

$$\sum_{i=1}^{28} b_i x_i \leq 500 \quad (106)$$

$$\frac{1}{47} n_1 \leq D \quad (107)$$

$$\frac{1}{3} n_2 \leq D \quad (108)$$

$$\frac{1}{0.04} p_3 \leq D \quad (109)$$

$$\frac{1}{0.04} p_4 \leq D \quad (110)$$

$$\frac{1}{48.74} n_5 \leq D \quad (111)$$

$$\frac{1}{0.52} n_6 \leq D \quad (112)$$

$$\frac{1}{22.07} p_7 \leq D \quad (113)$$

$$\frac{1}{0.32} p_8 \leq D \quad (114)$$

$$\frac{1}{0.23} p_9 \leq D \quad (115)$$

$$\frac{1}{0.68} n_{10} \leq D \quad (116)$$

Where z_1, z_2, z_3, z_4, and z_5 are binary vairables.

2.9.3. Multi-Choice Chebyshev Goal Program (MCWGP)

In a similar way, an Extended Goal Programming version of weighted goal program would be the usual EGP with the targets of the appropriate goals modefied.

Minimise:

$$\min Z = \alpha D_1 + (1-\alpha)\left(\frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.04}p_3 + \frac{1}{48.74}p_4 + \frac{1}{0.52}n_5 + \frac{1}{22.07}n_6 + \frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9 + \frac{1}{0.68}n_{10}\right) \tag{117}$$

Subjec to:

$$\sum_{i=1}^{28} pop_i x_i + n_5 - p_5 = 0.52z_1 + 0.57(1-z_1) \tag{118}$$

$$\sum_{i=1}^{28} res_i x_i + n_7 - p_7 = 1.86z_2 + 2.05(1-z_2) \tag{119}$$

$$\sum_{i=1}^{28} fd_i x_i + n_8 - p_8 = 0.32z_3 + 0.35(1-z_3) \tag{120}$$

$$\sum_{i=1}^{28} road_i x_i + n_9 - p_9 = 0.23z_3 + 0.25(1-z_3) \tag{121}$$

$$\sum_{i=1}^{28} fa_i x_i + n_{10} - p_{10} = 0.68z_5 + 0.75(1-z_5) \tag{122}$$

All other equations from equation (58) to (124) remain unchanged.

$$\sum_{i=1}^{28} x_i = 3 \tag{123}$$

$$\sum_{i=1}^{28} b_i x_i \leq 500 \tag{124}$$

$$\frac{1}{47}n_1 \leq D \tag{125}$$

$$\frac{1}{3}n_2 \leq D \tag{126}$$

$$\frac{1}{0.04}p_3 \leq D \tag{127}$$

$$\frac{1}{0.04}p_4 \leq D \tag{128}$$

$$\frac{1}{48.74}n_5 \leq D \tag{129}$$

$$\frac{1}{0.52}n_6 \leq D \tag{130}$$

$$\frac{1}{22.07}p_7 \leq D \tag{131}$$

$$\frac{1}{0.32}p_8 \leq D \tag{132}$$

$$\frac{1}{0.23}p_9 \leq D \tag{133}$$

$$\frac{1}{0.68}n_{10} \leq D \tag{134}$$

2.10. Sensitivity Analysis

Dam site selection is inherently complex, characterized by multiple criteria whose influences are uncertain. Sensitivity Analysis (SA) accesses how variations in inputs affect model output[58].

The objective of SA in this project is to to answer the question: How stable are the outcomes of the various site selection models?

2.10.1. Sensitivity Analysis test data generation

Two Sensitivity Analysis (SA) test are conducted, weighted analysis and target analysis. Weighted SA determines the effect of slight changes in weight to the outcomes of the models. It is conducted for Weighted GP and Lexicographic GP models. For WGP SA test, each term in the objecive function received a weight (decimal value between 0 and 1). All weight within a test weight set sum up to one(1). The model is ran 10 times with 10 different weight sets and he output recorded. Target analysis verifies how changes in targets affect the original outcome. It is conducted for all four models. Similarly, the models are ran 10 times with 10 different set of targets, each criteria receiving a different target value in each ran. All test are conducted keeping dam site selection number (3) and budget (\$500M) constant. This assumes no uncertainty in the proposed budget for constructing 3 dam sites.

10 weight sets, each for a term in the WGP model were generated using dirichlet sampling[59]. The Dirichlet generator creates a uniformly distributed vector across the goal simplex. The Dirichlet distribution is a statistical tool used when you have several proportions that must add up to one. It's the multi-category version of the Beta distribution and is often used in Bayesian modeling because of it's has convenient mathematical properties[60]. Dirichlet sampling has been effectively used in modeling income-share distributions, portfolio weighting, and objective weighting[61, 62, 63].

In MCDM, a moderate number of iterations is sufficient to capture stability patterns without overburdening computation. For instance, [64] highlight that sensitivity analysis in decision models does not require exhaustive runs; rather, a limited number of systematic variations can reveal whether rankings are robust to weight changes. Similarly, [26] note that a relatively small set of scenarios (often 5–15) is adequate to detect meaningful changes in alternatives' rankings. Therefore, conducting 10 rounds provides a balanced approach—enough to observe whether rankings shift under plausible weight variations, while keeping the analysis efficient.

3. Results

3.1. Weighted Goal Programming Solution

The model selected Dams 18, 19, and 23 with a total cost of \$481.5M. Relative to the ten goals, the solution exceeds several targets (e.g., height, capacity) while minimizing the weighted penalty of deviations, resulting in a weighted deviation score of 14.93. We can observe from Figure 1 that the farmland area criterion was the driving factor in the WGP solution, with dam height and rainfall also exerting a significant influence. These three criteria together shaped the final weighted deviation score of 14.93. Table A.24 lists per-dam attributes; Table 2 summarizes achieved values versus targets and the corresponding deviations. This indicates a balanced compromise solution under the specified weights and budget.

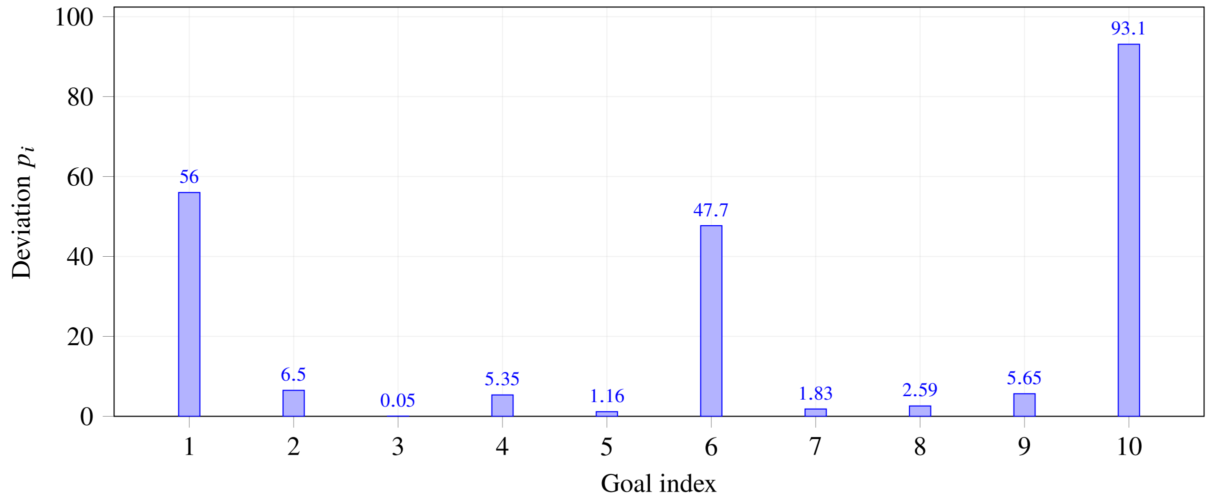

Figure 1: Weighted Goal Programming — deviations above targets (p_i) for each goal.

Table 2: Goal achievement versus targets in the Weighted Goal Programming model

#	Criterion	Target	Achieved	Deviation
1	Dam height (m)	47.00	103.00	$p_1 = 56.00$
2	Capacity (Mm^3)	3.00	9.50	$p_2 = 6.50$
3	Reservoir area (km^2)	0.04	0.09	$p_3 = 0.05$
4	Temperature (°C)	48.74	54.09	$p_4 = 5.35$
5	Population index	0.52	1.68	$p_5 = 1.16$
6	Rainfall	22.07	69.77	$p_6 = 47.70$
7	Residence	1.86	3.69	$p_7 = 1.83$
8	Farmland distance	0.32	2.91	$p_8 = 2.59$
9	Nearest road	0.23	5.88	$p_9 = 5.65$
10	Farmland area	0.68	93.78	$p_{10} = 93.10$

3.2. Chebyshev Goal Programming Solution

In the Chebyshev (min–max) goal programming run, we minimize the maximum normalized, weighted deviation across all ten goals, yielding an optimal scalar deviation of $D^* = 25.2174$. Under the selection and budget constraints (exactly 3 dams, $\sum cost <= \$500$), the model selects dams 19, 20, and 28, with a total estimated cost of \$158.7 + \$166.5 + \$172.1 = \$497.3 million, thereby fully respecting the cap. Relative to the targets, this solution equalizes the worst-off goal (in the sense of the achievement scalarization), so no single criterion dominates the compromise. The binding deviations are those that attain D^* after normalization by their respective scaling factors, while the remaining goals exhibit strictly smaller normalized deviations. The binding criterion is Nearest road (Criterion 9) since it's weighted deviation $p_9/0.23 = 25.2174 = D^*$ (Table 4), all other deviations are strictly smaller. This indicates the worst normalized shortfall at the optimum occurs on the road-proximity goal, with all other goals at or within the Chebyshev bound. Detailed per-criterion achievements and deviations are reported in Table 3, with the selected alternative attributes summarized in Table A.24.

Table 3: CGP: goal achievement vs. targets and deviations (all $n_i = 0$)

#	Criterion	Target	Achieved	Deviation type	Value
1	Dam height (m)	47.00	138.00	p_1	91.00
2	Capacity (Mm^3)	3.00	71.50	p_2	68.50
3	Reservoir area (km^2)	0.04	0.46	p_3	0.42
4	Temperature (°C)	48.74	48.74	p_4	0.00
5	Population index	0.52	2.09	p_5	1.57
6	Rainfall	22.07	63.76	p_6	41.69
7	Residence	1.86	15.74	p_7	13.88
8	Farmland distance	0.32	4.30	p_8	3.98
9	Nearest road	0.23	6.03	p_9	5.80
10	Farmland area	0.68	24.71	p_{10}	24.03

Table 4: Chebyshev GP: weighted deviations and the binding (max) constraint

#	Criterion	Deviation	Weight term in D	Weighted dev.
3	Reservoir area	$p_3 = 0.4200$	$\frac{1}{0.04} p_3$	10.5000
4	Temperature	$p_4 = 0$	$\frac{1}{0.04} p_4$	0.0000
7	Residence	$p_7 = 13.8800$	$\frac{1}{22.07} p_7$	0.6290
8	Farmland distance	$p_8 = 3.9800$	$\frac{1}{0.32} p_8$	12.4375
9	Nearest road	$p_9 = 5.8000$	$\frac{1}{0.23} p_9$	**25.2174**
			Max (i.e., $D^\star$)	**25.2174**

3.3. *Extended Goal Programming Solution*

In the Extended Goal Programming (EGP) run with $\alpha = 0.8$, the model selects Dams 16, 19, and 28 with a total estimated cost of \$154.8 + \$158.7 + \$172.1 = \$485.6 M (within the \$500 M cap). The optimized bound on the Chebyshev-normalized terms is $D^\star = 27.0$, while the composite objective value is $f^\star = \alpha D^\star + (1 - \alpha)\left(\frac{p_3}{0.04} + \frac{p_4}{48.74} + \frac{p_7}{0.35} + \frac{p_8}{0.32} + \frac{p_9}{23}\right) = 32.6816$. The D-binding criterion is *Temperature* (criterion 4) because $\frac{p_4}{0.04} = 27.0$ attains $D^\star$; the weighted-sum part is chiefly driven by *Residence* via $\frac{p_7}{0.35} \approx 48.17$. Tables A.24 and 5 detail the selected alternatives and goal achievements; Fig. 2 visualizes both the D-normalized terms and the $(1 - \alpha)$ weighted-sum terms for each criterion.

Table 5: EGP: goal achievement vs. targets and deviations (here, all $n_i = 0$)

#	Criterion	Target	Achieved	Deviation type	Value
1	Dam height (m)	47.00	98.00	p_1	51.00
2	Capacity (Mm^3)	3.00	11.80	p_2	8.80
3	Reservoir area (km^2)	0.04	0.10	p_3	0.06
4	Temperature (°C)	48.74	49.82	p_4	1.08
5	Population index	0.52	50.82	p_5	50.30
6	Rainfall	22.07	50.10	p_6	28.03
7	Residence	1.86	18.72	p_7	16.86
8	Farmland distance	0.32	2.09	p_8	1.77
9	Nearest road	0.23	4.44	p_9	4.21
10	Farmland area	0.68	45.24	p_{10}	44.56

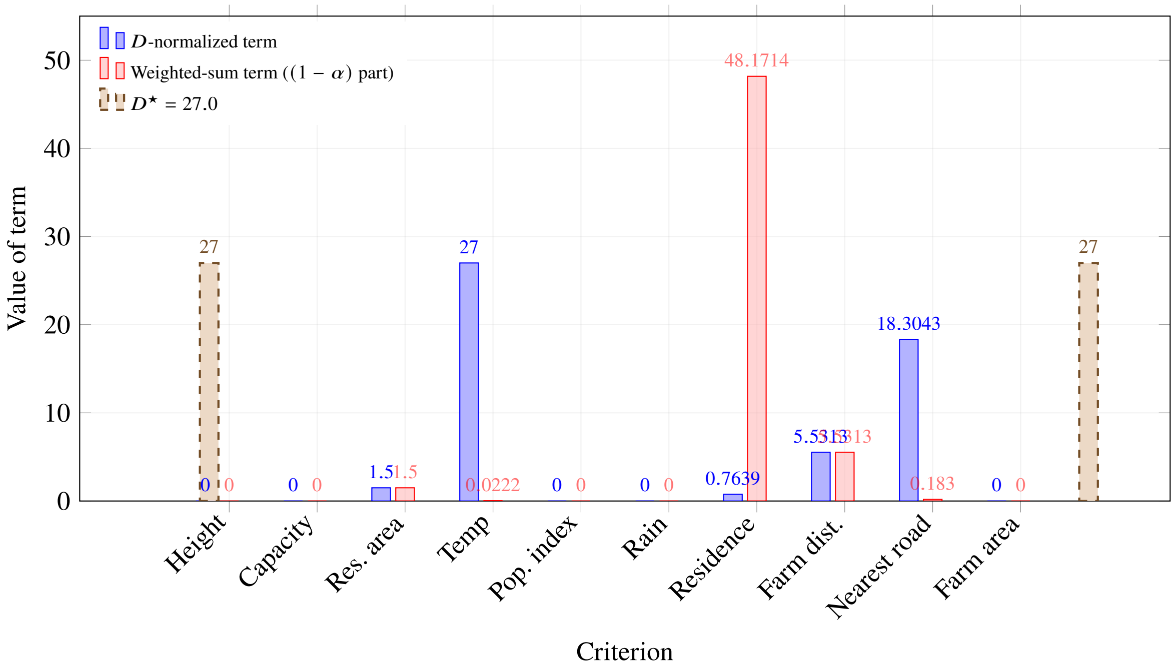

Figure 2: EGP contributions by criterion: comparison of the D-normalized terms (used in the minimax bound) versus the terms entering the $(1-\alpha)$ weighted-sum portion of the objective ($\alpha = 0.8$). The D-binding criterion is *Temperature*; the weighted-sum is dominated by *Residence*.

3.4. Lexicographic Goal Programming Solution

In the Lexicographic Goal Programming (LGP) solution, we optimize three priority levels in sequence. **Priority 1** minimizes $(1/47)n_1 + (1/3)n_2 + (1/0.52)n_5 + (1/0.68)n_{10}$ and attains 0, implying no underachievement on height, capacity, population, or farmland area at the optimum. **Priority 2** then minimizes $(1/0.04)p_3 + (1/48.74)p_4 + (1/22.07)n_6$ subject to Priority 1's optimum, yielding 0.0416 (driven by temperature: $p_4/48.74 \approx 0.0416$). **Priority 3** finally minimizes $(1/0.35)p_7 + (1/0.32)p_8 + (1/23)p_9$ under the earlier priorities, giving 83.4264. The resulting portfolio selects Dams **19, 21, 28** with total cost \$158.7 + \$164.3 + \$172.1 = \$495.1 M (within the \$500 M cap). Table A.24 lists the attributes of the selected dams, and Table 6 reports achieved values versus targets and deviations; notably, temperature and the Priority 3 social–access criteria (residence, farmland distance, road proximity) drive the lexicographic refinement Figure 3.

Table 6: LGP: goal achievement vs. targets and deviations (final portfolio; $n_i = 0$)

#	Criterion	Target	Achieved	Deviation type	Value
1	Dam height (m)	47.00	123.00	p_1	76.00
2	Capacity (Mm^3)	3.00	10.50	p_2	7.50
3	Reservoir area (km^2)	0.04	0.04	p_3	0.00
4	Temperature (°C)	48.74	50.77	p_4	2.03
5	Population index	0.52	1.13	p_5	0.61
6	Rainfall	22.07	55.60	p_6	33.53
7	Residence	1.86	26.02	p_7	24.16
8	Farmland distance	0.32	4.80	p_8	4.48
9	Nearest road	0.23	9.38	p_9	9.15
10	Farmland area	0.68	36.41	p_{10}	35.73

In Fig. 3, a clear pattern emerges. **Dam~19** is selected by all four models, indicating a robust choice insensitive

Table 7: Lexicographic GP: summary of priority objective values (final portfolio)

Priority	Objective minimized	Optimal value
1	$\frac{1}{47}n_1 + \frac{1}{3}n_2 + \frac{1}{0.52}n_5 + \frac{1}{0.68}n_{10}$	0.0000
2	$\frac{1}{0.04}p_3 + \frac{1}{48.74}p_4 + \frac{1}{22.07}n_6$	0.0416
3	$\frac{1}{0.35}p_7 + \frac{1}{0.32}p_8 + \frac{1}{23}p_9$	83.4264

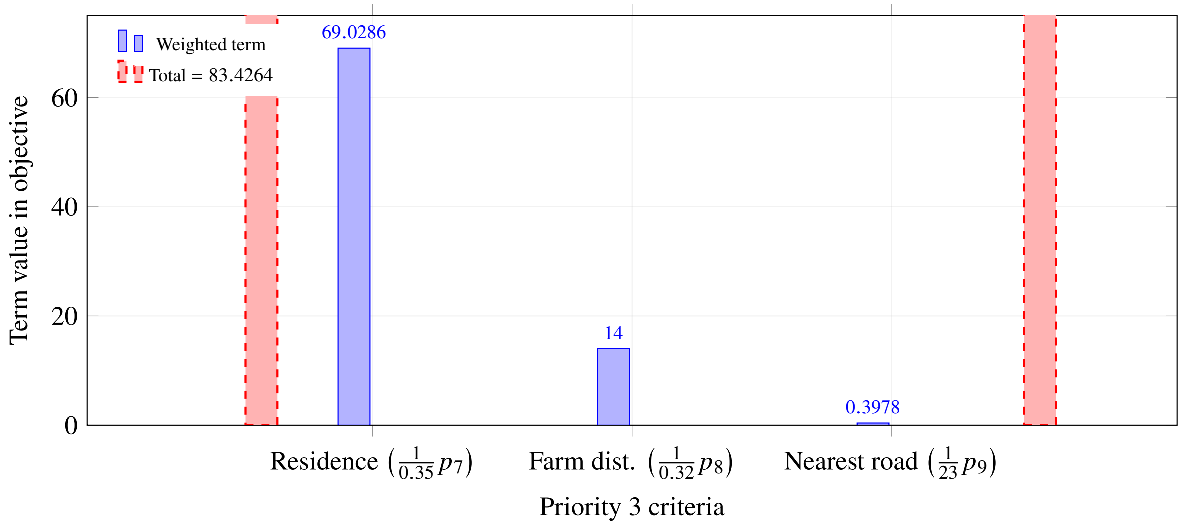

Figure 3: Lexicographic GP, Priority 3 objective components for the final portfolio: $\frac{1}{0.35}p_7 = 69.0286$, $\frac{1}{0.32}p_8 = 14.0000$, and $\frac{1}{23}p_9 = 0.3978$. Their sum equals the Priority 3 value 83.4264.

to the change from weighted-sum (WGP) to Chebyshev (CGP) to extended (EGP) and lexicographic (LGP) formulations. A near-core site, **Dam$\tilde{2}$8**, appears in three models (CGP, EGP, LGP) but not WGP, suggesting that minimax and priority-based emphases favor it. The remaining slot is model-sensitive: WGP picks 18, 23, CGP swaps in 20, EGP prefers 16, and LGP chooses 21. Overall, moving from WGP to CGP/EGP/LGP consolidates consensus around 19, 28 while the third selection pivots according to each model's treatment of deviations (weighted-sum vs. max-deviation vs. lexicographic priorities).

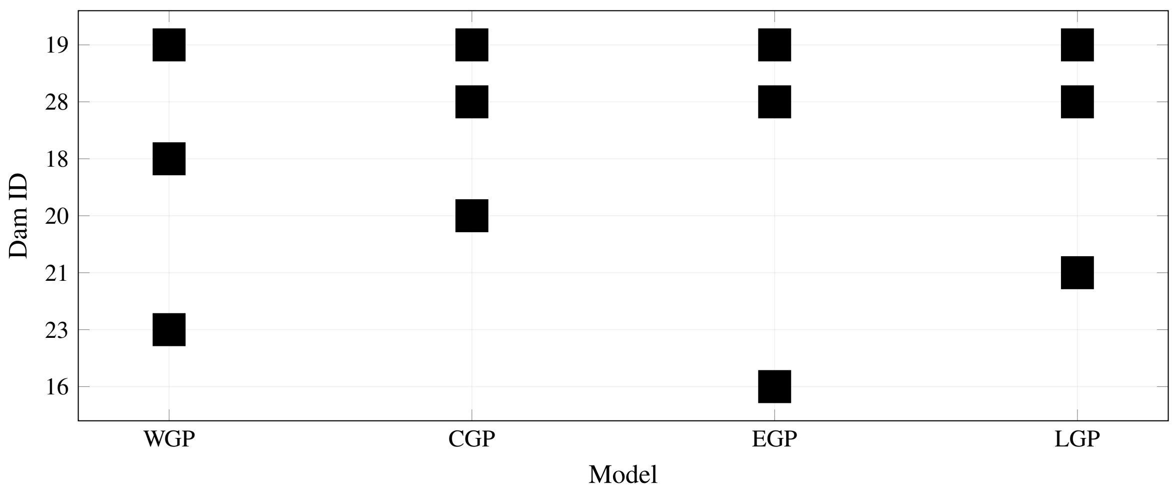

Figure 4: Model–dam selection map for the four GP variants. Dam 19 is chosen by all four; Dam 28 by three (CGP, EGP, LGP); the others are singletons (WGP: 18, 23; CGP: 20; EGP: 16; LGP: 21).

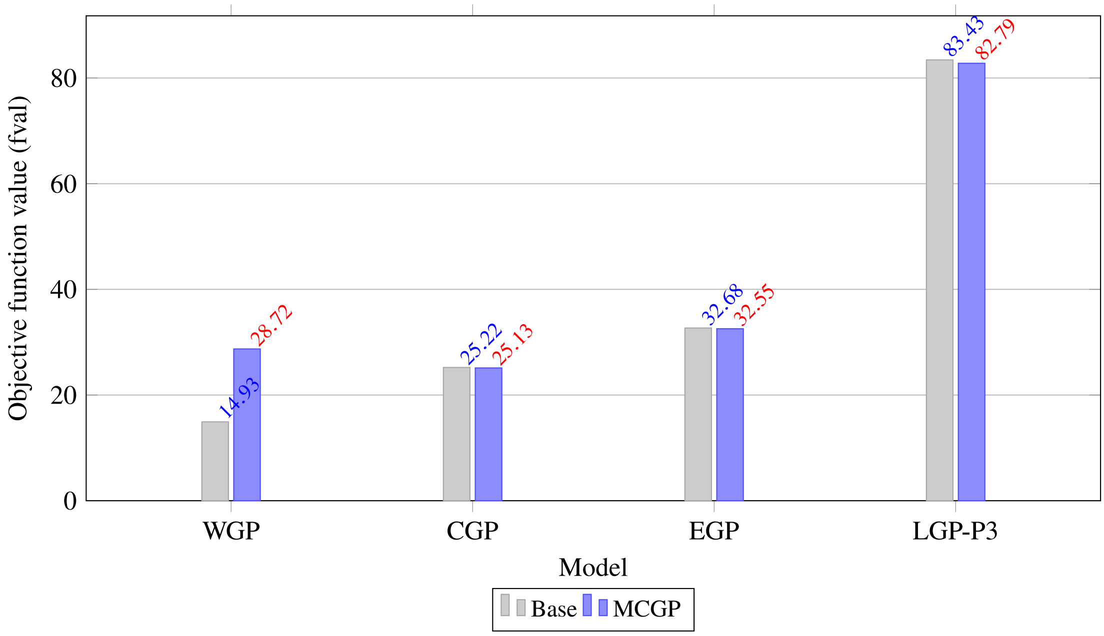

Figure 5: Comparison of *fval* for Base vs. MCGP variants across models.

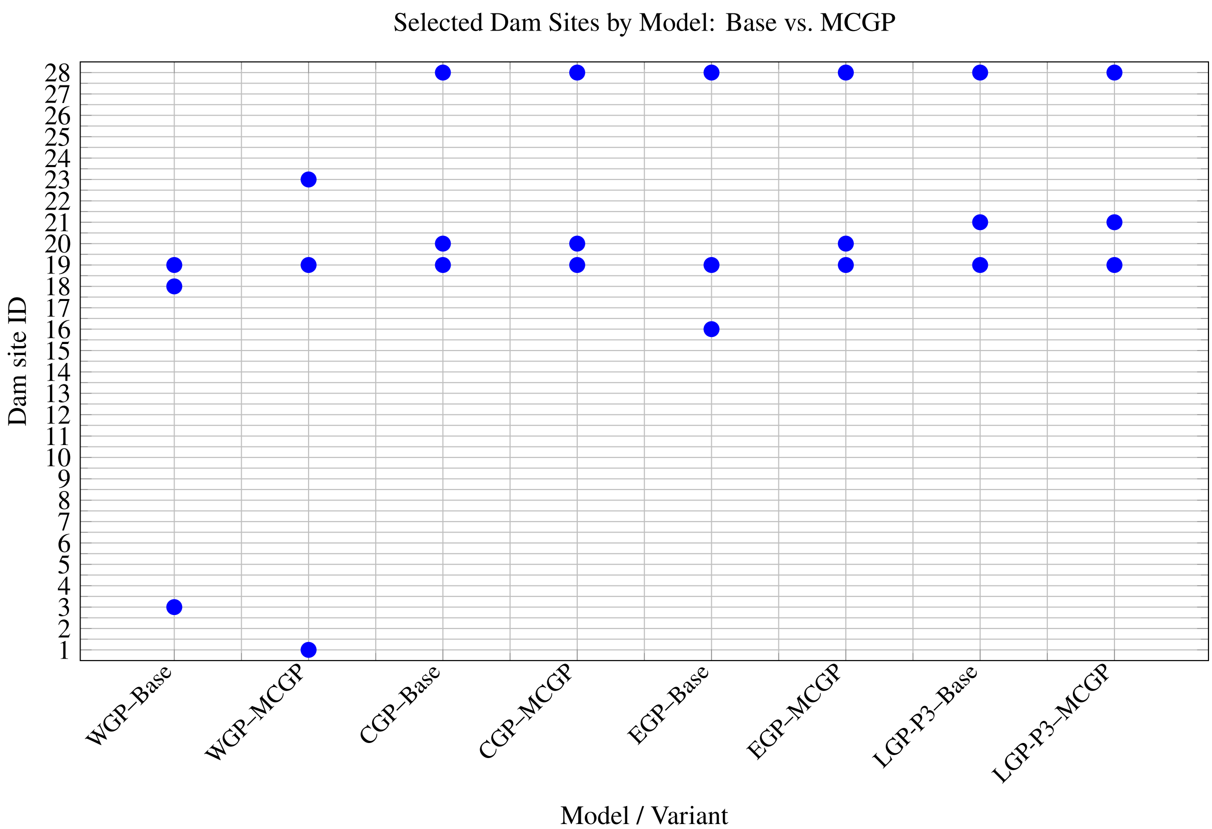

Figure 6: Selected dam sites for each model under Base and MCGP formulations. All markers are blue circles; x-axis labels indicate the model variant.

3.5. *Multi-Choice GP Extension Solutions*

3.5.1. *Weighted GP*

In the multi–choice extension of the weighted goal program (WGP–MCGP), five social/access criteria were allowed target flexibility. The model selected the lower bounds for *Population* (0.52) and *Farmland area* (0.68), while adopting the upper bounds for *Nearest residence* (2.05), *Farmland distance* (0.35), and *Nearest road* (0.25), as shown in Table 8. The resulting weighted deviation objective is 28.7245, which is higher than the fixed–target WGP value (14.9277) by +13.7968 (Figure 9), reflecting the tighter upper–bound targets imposed on three criteria. Fig. 7 visualizes the chosen target levels across the flexible goals and the model output is reported in A.44.

Table 8: WGP–MCGP: flexible criteria, available targets, and chosen level (from z).

Criterion	**Lower target (L)**	**Upper target (U)**	**Chosen**
Population index	0.52	0.57	L (0.52)
Nearest residence	1.86	2.05	U (2.05)
Farmland distance	0.32	0.35	U (0.35)
Nearest road	0.23	0.25	U (0.25)
Farmland area	0.68	0.75	L (0.68)

Table 9: WGP vs. WGP–MCGP summary.

Model	**Portfolio**	**Cost (M$)**	**Objective**	Δ vs. WGP
WGP (fixed targets)	{18,19,23}	481.5	14.9277	–
WGP–MCGP (flexible)	{1,19,23}	487.4	28.7245	+13.7968

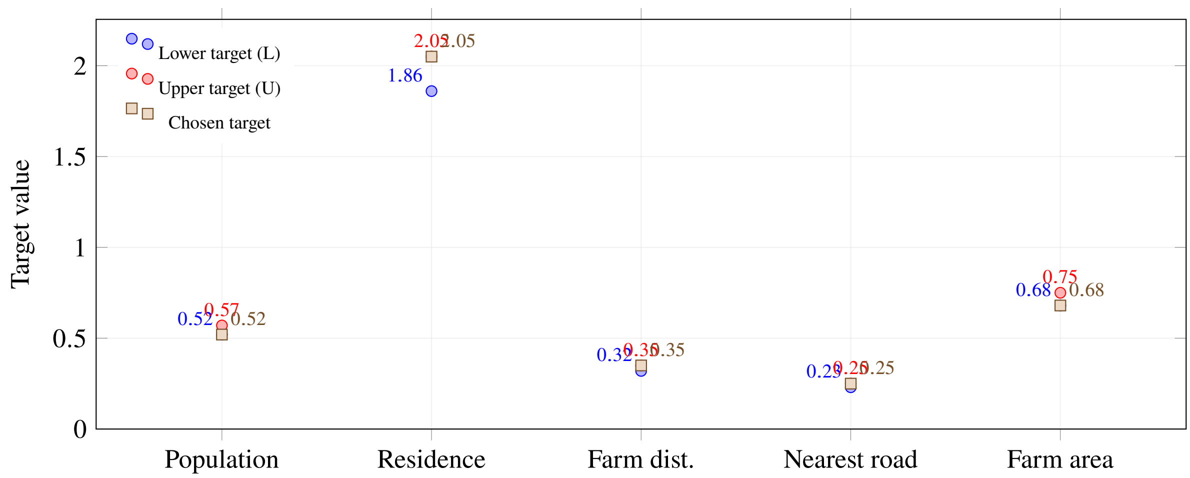

Figure 7: WGP–MCGP target flexibility across five criteria: chosen levels (squares) relative to the available lower/upper targets (dots).

3.5.2. *Chebyshev GP*

Allowing target flexibility on five socio-environmental criteria retains the CGP portfolio $\{19, 20, 28\}$ while slightly improving the minimax objective from $D^\star = 25.2174$ to 25.1304 (Table 10). The model chooses the lower targets for Population and Farmland area, and the upper targets for Nearest residence, Farmland distance, and Nearest road (Table 11). With the selected dams, the worst normalized deviation is still *Nearest road* ($p_9/0.23$), followed by Farmland distance and Reservoir area (Figure 8); all other normalized deviations are zero in the minimax sense. Achieved values relative to the chosen targets are detailed in Table 12 and the model output is reported in A.44

Table 10: Chebyshev GP (CGP) vs. CGP–MCGP with target flexibility on five goals.

Model	Selected dams	Total cost (M$)	$D^\star$	ΔD vs. CGP
CGP (fixed targets)	{19, 20, 28}	497.3	25.2174	–
CGP–MCGP (flexible)	{19, 20, 28}	497.3	25.1304	−0.0870 (–0.345%)

Table 11: CGP–MCGP chosen targets for flexible goals (binary z_k: 1 = lower target, 0 = upper target).

Criterion	Target options	Chosen (z_k)	Target used
Population	0.52 (low) | 0.57 (high)	$z_1 = 1$	0.52
Nearest residence	1.86 (low) | 2.05 (high)	$z_2 = 0$	2.05
Farmland distance	0.32 (low) | 0.35 (high)	$z_3 = 0$	0.35
Nearest road	0.23 (low) | 0.25 (high)	$z_4 = 0$	0.25
Farmland area	0.68 (low) | 0.75 (high)	$z_5 = 1$	0.68

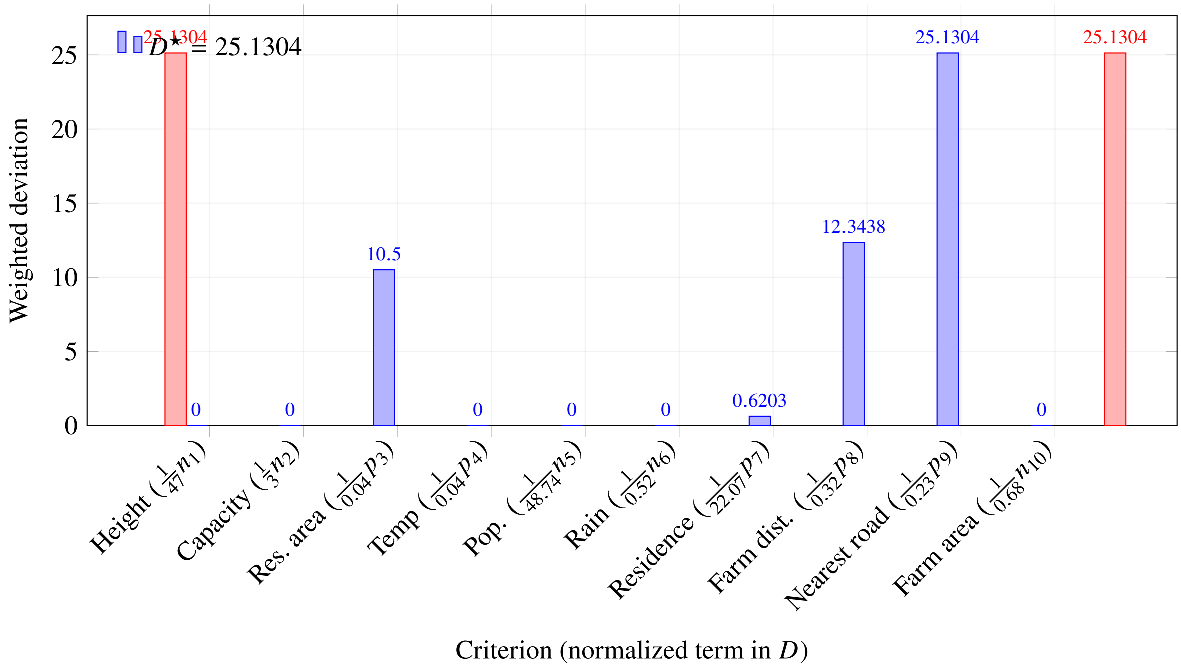

Figure 8: CGP–MCGP normalized deviations in the minimax objective. The binding criterion remains *Nearest road* with $p_9/0.23 = D^\star$; flexibility slightly reduces the worst normalized deviation compared to fixed-target CGP.

3.5.3. Extended GP

With $\alpha = 0.8$, the extended goal program under multi-choice targets selects the same portfolio as the CGP–MCGP case, $\{19, 20, 28\}$, at a total cost of \$497.3 M (Table 13). Target flexibility is exercised by choosing lower bounds for Population and Farmland area and upper bounds for Nearest residence, Farmland distance, and Nearest road (Table 14). The worst normalized deviation remains *Nearest road* ($p_9/0.23 = 25.1304$), defining $D^\star$, followed by Farmland distance and Reservoir area (Figure 9). The composite objective evaluates to $f = 0.8 \times 25.1304 + 0.2 \times 62.2094 = 32.5462$, indicating that the portfolio balances a modest improvement in

Table 12: CGP–MCGP achievements vs. (chosen) targets and deviations for the selected set $\{19, 20, 28\}$.

#	Criterion	Target	Achieved	Deviation
1	Height (m)	47.00	138.00	$p_1 = 91.00$
2	Capacity (Mm^3)	3.00	71.50	$p_2 = 68.50$
3	Reservoir area (km^2)	0.04	0.46	$p_3 = 0.42$
4	Temperature (°C)	48.74	48.74	$p_4 = 0.00$
5	Population (0–50, norm.)	0.52	2.09	$p_5 = 1.57$
6	Rainfall (cm)	22.07	63.76	$p_6 = 41.69$
7	Nearest residence (km)	2.05	15.74	$p_7 = 13.69$
8	Farmland distance (km)	0.35	4.30	$p_8 = 3.95$
9	Nearest road (km)	0.25	6.03	$p_9 = 5.78$
10	Farmland area (km^2)	0.68	24.71	$p_{10} = 24.03$

the minimax term with a larger weighted-sum contribution, consistent with the α-weighted trade-off; per-criterion achievements and deviations are listed in Table 15.

Table 13: Extended Goal Programming with Multi-Choice targets (EGP–MCGP), $\alpha = 0.8$.

Model	Selected dams	Total cost (M$)	$D^\star$	WGP term S	Objective $f = \alpha D + (1 - \alpha)S$
EGP–MCGP	$\{19, 20, 28\}$	497.3	25.1304	62.2094	32.5462

Table 14: EGP–MCGP chosen targets for flexible goals (binary z_k: 1 = lower target, 0 = upper target).

Criterion	Target options	Chosen (z_k)	Target used
Population	0.52 (low) | 0.57 (high)	$z_1 = 1$	0.52
Nearest residence	1.86 (low) | 2.05 (high)	$z_2 = 0$	2.05
Farmland distance	0.32 (low) | 0.35 (high)	$z_3 = 0$	0.35
Nearest road	0.23 (low) | 0.25 (high)	$z_4 = 0$	0.25
Farmland area	0.68 (low) | 0.75 (high)	$z_5 = 1$	0.68

3.5.4. Lexicographic GP

Relative to the baseline LGP, introducing multi-choice targets leaves the Priority 1 and Priority 2 objectives unchanged while delivering a modest improvement at Priority 3 (from 83.4264 to 82.7889; Table 16, Fig. 10). The chosen target pattern is consistent across priorities—lower targets for Population and Farmland area, upper targets for Nearest residence, Farmland distance, and Nearest road (Table 17)—and the P1 portfolio is $\{6,7,18\}$, with the final P3 portfolio shown in Table 18 and Fig. 11.

3.6. Sensitivity Analysis

Sensitivity analysis (SA) is a crucial step in multi-criteria decision-making (MCDM), as it evaluates the robustness of solutions when key model parameters are perturbed. In goal programming applications, where weights, targets, and other constraints guide the optimization, small changes can sometimes lead to disproportionately large shifts in the selected alternatives or in the overall objective performance. Testing models under these conditions therefore helps answer the central question: are the solutions stable enough to be trusted for real-world implementation, or do they fluctuate under modest changes in assumptions?

Table 15: EGP–MCGP achievements vs. (chosen) targets and deviations for the selected set $\{19, 20, 28\}$.

#	Criterion	Target	Achieved	Deviation
1	Height (m)	47.00	138.00	$p_1 = 91.00$
2	Capacity (Mm^3)	3.00	71.50	$p_2 = 68.50$
3	Reservoir area (km^2)	0.04	0.46	$p_3 = 0.42$
4	Temperature (°C)	48.74	48.74	$p_4 = 0.00$
5	Population (0–50, norm.)	0.52	2.09	$p_5 = 1.57$
6	Rainfall (cm)	22.07	63.76	$p_6 = 41.69$
7	Nearest residence (km)	2.05	15.74	$p_7 = 13.69$
8	Farmland distance (km)	0.35	4.30	$p_8 = 3.95$
9	Nearest road (km)	0.25	6.03	$p_9 = 5.78$
10	Farmland area (km^2)	0.68	24.71	$p_{10} = 24.03$

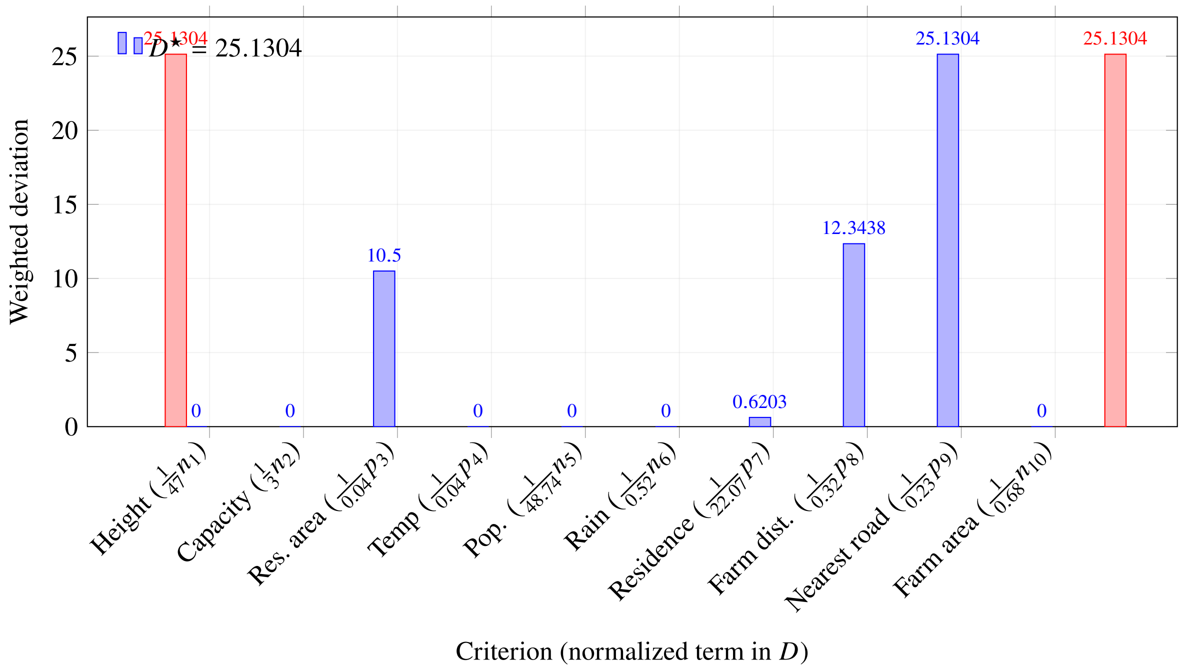

Figure 9: EGP–MCGP normalized deviations in the minimax term D. The binding criterion is *Nearest road* with $p_9/0.23 = D^\star$; next are Farmland distance and Reservoir area.

Table 16: Lexicographic objectives by priority: baseline LGP vs LGP–MCGP.

	Priority 1	Priority 2	Priority 3
LGP (baseline)	0.0000	0.0416	83.4264
LGP–MCGP (this work)	0.0000	0.0416	82.7889
Δ (MCGP − LGP)	0.0000	0.0000	-0.6375

Table 17: LGP–MCGP target flexibility (binary z_k: 1 = lower target, 0 = upper target).

Criterion	Options	z_k	Target used
Population	0.52 (low) | 0.57 (high)	1	0.52
Nearest residence (km)	1.86 (low) | 2.05 (high)	0	2.05
Farmland distance (km)	0.32 (low) | 0.35 (high)	0	0.35
Nearest road (km)	0.23 (low) | 0.25 (high)	0	0.25
Farmland area (km^2)	0.68 (low) | 0.75 (high)	1	0.68

Table 18: Selected dam IDs across priorities.

Case	Priority	Selected dams (IDs)
LGP (baseline)	Final	{20,21,28}
LGP–MCGP	P1	{6,7,18}
LGP–MCGP	P2	{20,21,28}
LGP–MCGP	P3	{20,21,28}

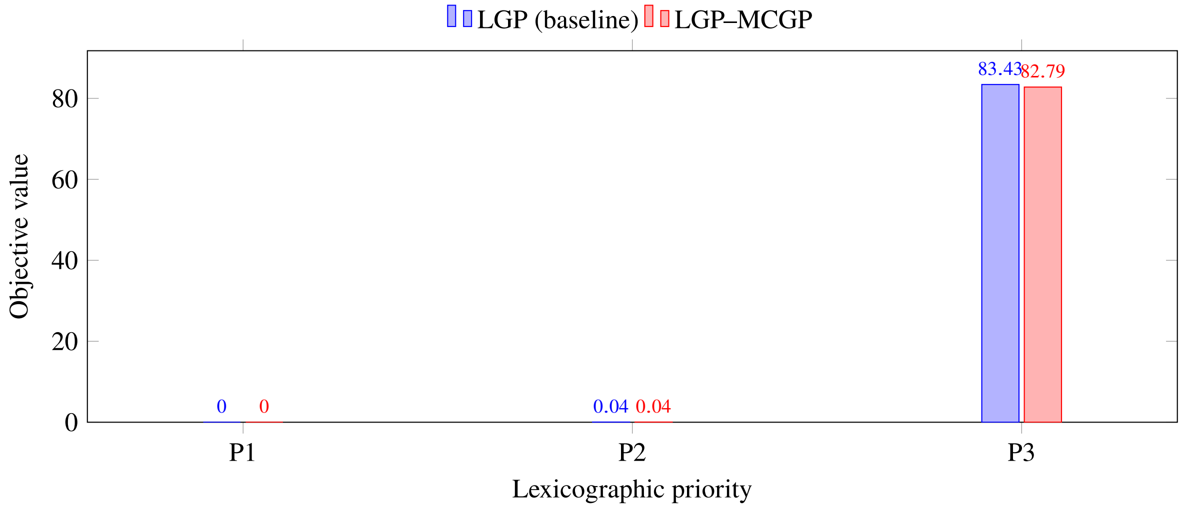

Figure 10: Lexicographic objectives by priority. MCGP matches P1 and P2 and achieves a small improvement at P3 (≈ 0.64).

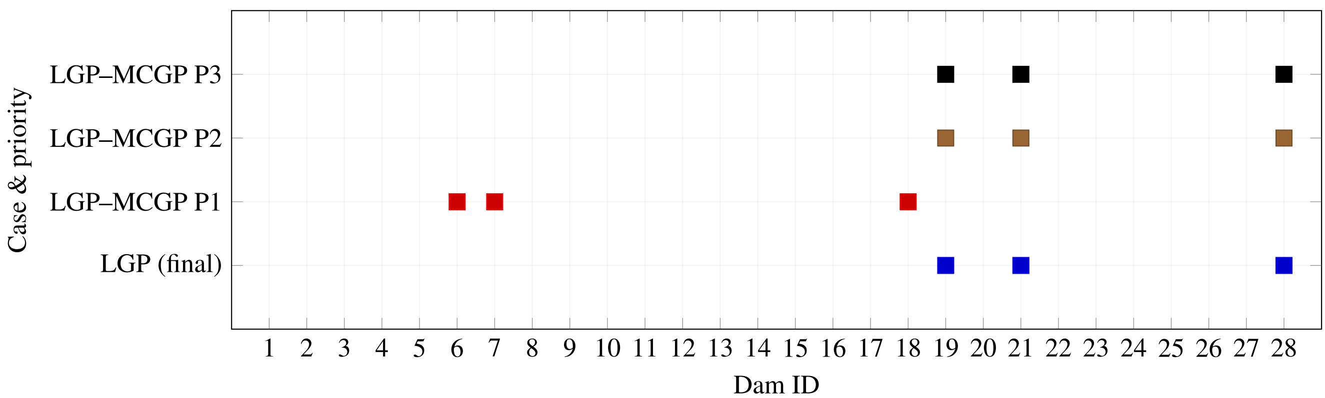

Figure 11: Selected-dam map across LGP baseline and LGP–MCGP priorities. Filled squares mark dams included in each portfolio.

In this study, two types of sensitivity analysis were carried out to systematically investigate robustness across the four goal programming models considered—Weighted Goal Programming (WGP), Lexicographic Goal Programming (LGP), Chebyshev Goal Programming (CGP), and Extended Goal Programming (EGP).

We varied the distribution of weights across objectives using ten randomized test sets and compared the resulting solutions against the base model. The purpose was to determine whether changes in emphasis among objectives significantly alter the selection of dam sites or the associated objective function values. Key questions included: Which dam sites are consistently selected across different weight configurations? Which sites appear only under specific weight emphases? How variable are the objective values under weight perturbations?

Here, the emphasis shifted from weights to the target levels defined for each goal. Ten different target scenarios were generated and applied across all four models, with results compared against their respective base solutions. The objective was to assess: How sensitive is each model to adjustments in target values? Do some models show large swings in objective values while others remain stable? Which dam sites persistently appear across target variations, and which are target-sensitive?

Together, these analyses offer complementary insights. Weight SA reveals the impact of subjective trade-offs among competing objectives, while Target SA shows how solution stability depends on the feasibility and realism of the goals themselves. In the following sections, we first present the results of Weight SA, before moving on to Target SA.

3.6.1. Weight Analysis

The weight sensitivity analysis focused on how variations in the relative importance of objectives influenced the Weighted Goal Programming (WGP) and Lexicographic Goal Programming (LGP) models. Figure 12 maps dam-site selections across ten randomized weight sets compared with the base WGP solution. The heatmap shows that dams 18 and 19 were consistently chosen in nearly all scenarios, while other sites such as 12, 13, and 23 appeared only under specific weight allocations. This highlights the presence of a "core set" of robust sites that are insensitive to weight perturbations, alongside more marginal sites that enter solutions when emphasis shifts to particular objectives.

Objective function values also varied under weight perturbations. The lollipop plot in Figure 13 compares the performance of each test set against the base WGP solution. While the base solution achieved an objective value of 14.93, the sensitivity runs produced substantially lower values ranging between 0.26 and 2.50. This suggests that, although the base configuration is balanced across objectives, certain weight allocations heavily prioritize specific goals at the expense of overall balance, yielding smaller numerical deviations. In other words, the weight distribution strongly shapes model efficiency, but the solutions remain internally consistent across scenarios.

A more direct measure of robustness is shown in the frequency analysis of dam selections (Figure 14). Dam 18 was selected in 70% of runs, dam 19 in 80%, and dam 23 in 60%, while other sites appeared much less frequently. The overlay of the base solution confirms that the sites chosen there align with those most frequently selected under sensitivity runs, reinforcing the interpretation of robustness. Finally, the LGP model illustrates a different dynamic

(Figure 15): while Priority 1 and Priority 2 objectives remain essentially stable across weight sets, Priority 3 shows wide variation, with objective values ranging from 2.5 to 13.1. This reflects the lexicographic structure—higher priorities dominate decision outcomes, leaving lower priorities sensitive to residual trade-offs. Together, these findings show that weight changes mainly affect the inclusion of marginal dam sites and the performance of lower-priority goals, while a stable subset of core sites persists across scenarios.

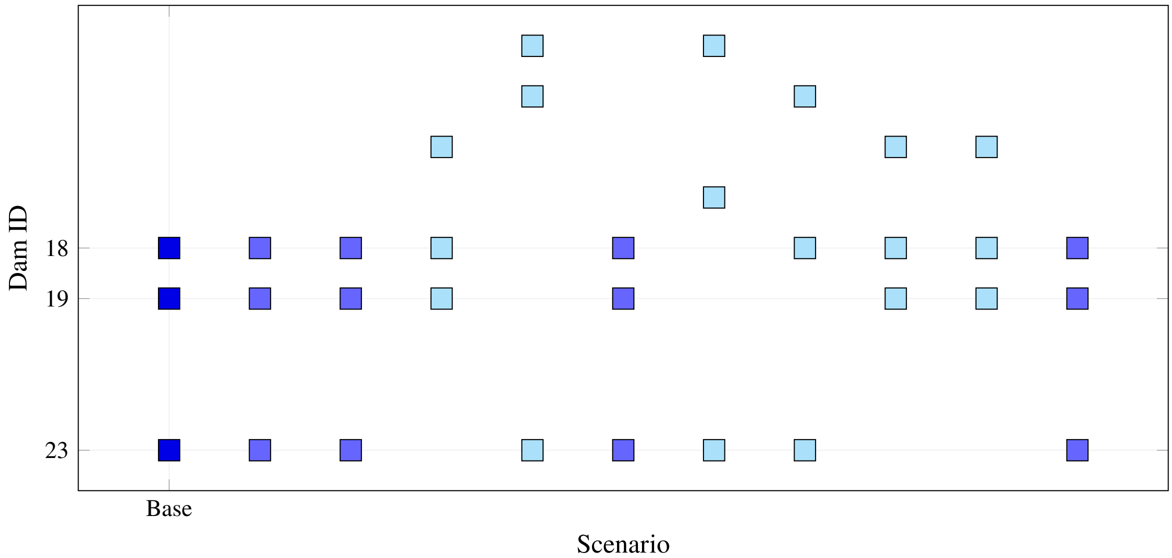

Figure 12: Scenario–dam selection map for the base WGP (first column) and ten test sets. Each filled square marks a selected dam site.

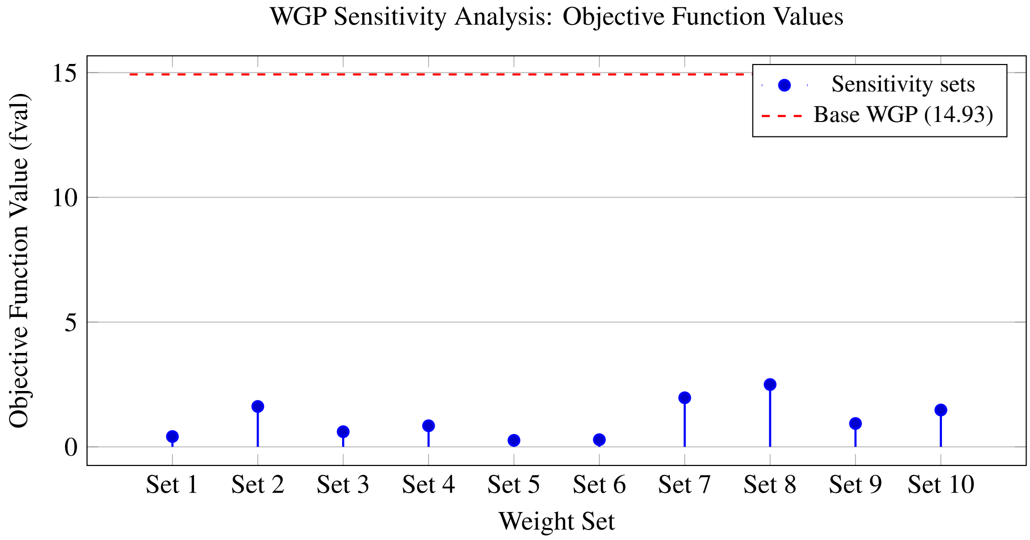

Figure 13: Lollipop plot of *fval* across 10 weight sets (blue dots), compared with the base Weighted Goal Programming solution (red dashed line).

3.6.2. Target Analysis

The target sensitivity analysis investigated how variations in goal target levels affected model outcomes across the four formulations (WGP, CGP, EGP, and LGP). Figure 16 shows the changes in objective values across ten target sets, compared with dashed lines representing the base models. WGP displayed remarkable stability, with values

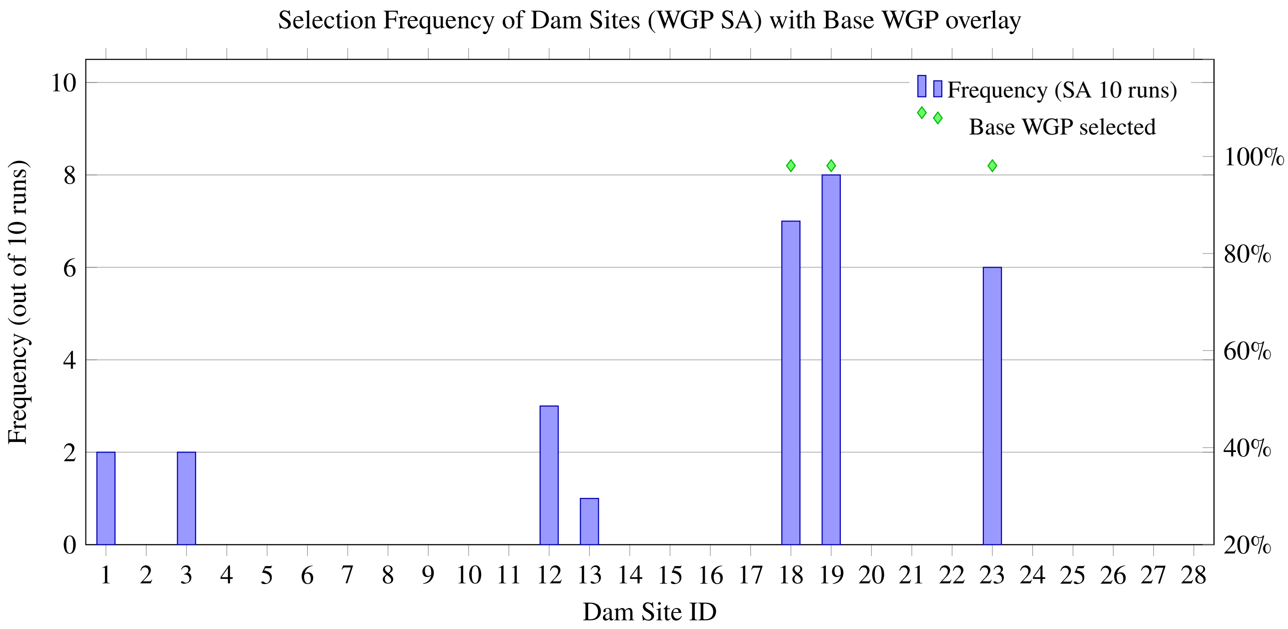

Figure 14: Summary of dam-site selection frequency across 10 WGP sensitivity runs; red diamonds mark sites selected by the Base WGP solution. Right axis shows percent of runs.

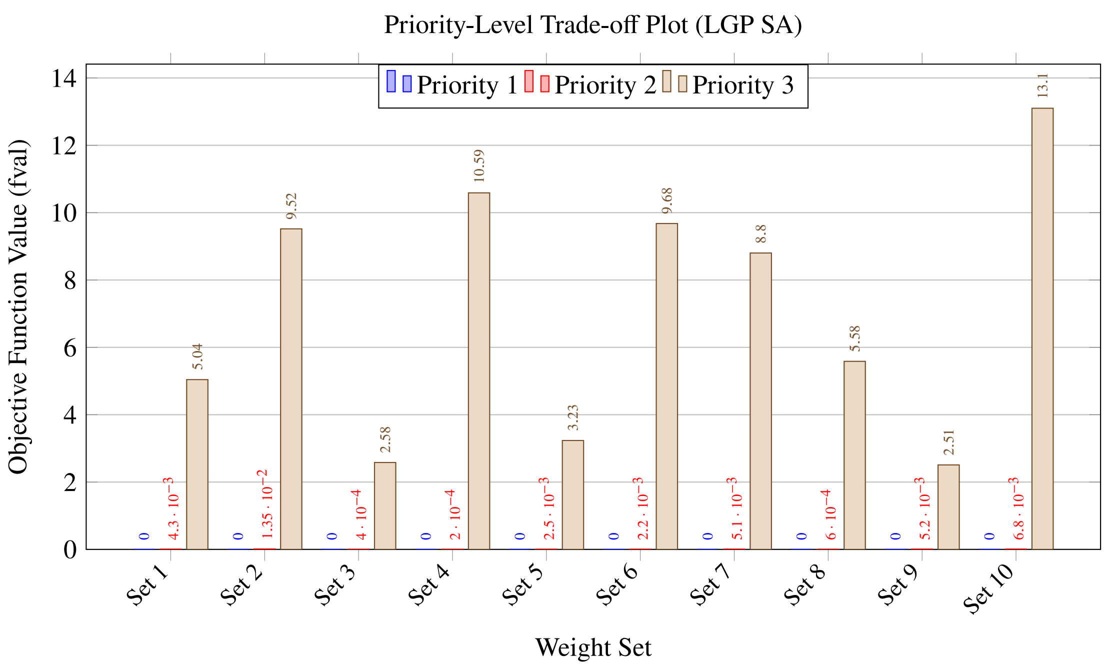

Figure 15: Comparison of objective values (*fval*) at Priority 1, 2, and 3 across weight sets for Lexicographic Goal Programming sensitivity analysis. Numbers above bars show exact values.

clustered tightly around its base of 14.93. LGP was also comparatively stable, with modest variation between 23 and 38. In contrast, CGP and EGP exhibited wide fluctuations: CGP ranged from 0.0 to 238.5, and EGP from 3.0 to 203.4. The logarithmic scale emphasizes these contrasts, highlighting that while WGP and LGP maintain consistent performance, CGP and EGP are highly sensitive to shifts in target definitions.

These variations are further reflected in dam-site selection patterns. Figure 17 compares selected sites across models and target sets, with base solutions included for reference. WGP consistently selected the core set of dams 18, 19, and 20 across all scenarios, reflecting its stability under target perturbations. LGP displayed moderate variability, occasionally switching between site 19, 20, 21, and 28 depending on the target scenario. EGP and CGP were considerably more dynamic, with their selections shifting more frequently across sites such as 1, 16, 19, 20, and 28. This shows that while WGP and LGP preserve a degree of selection robustness, CGP and EGP yield more target-sensitive outcomes that may complicate interpretation and implementation.

Table 19 summarizes the descriptive statistics of objective values across the ten target scenarios for each model. WGP again emerges as the most stable (standard deviation = 0.63), followed by LGP (6.21), while CGP (87.44) and EGP (71.29) show very high variability. Finally, the grouped bar chart in Figure 18 presents the frequency of site selection across target sets. The results reinforce the earlier patterns: dams 18–20 are robustly selected by WGP, dam 28 is highly persistent in LGP and partially in CGP/EGP, while sites such as 1, 15, 16, and 22 appear intermittently in the more sensitive models. Taken together, these findings demonstrate that target variation exerts strong influence on CGP and EGP, while WGP and LGP provide more stable recommendations and a clearer distinction between robust and target-sensitive dam sites.

Table 19: Descriptive statistics of $fval$ across Target Sensitivity Analysis (per model).

Model	Min	Max	Mean	Std Dev
WGP	14.06	16.10	14.93	0.63
CGP	0.00	238.50	65.20	87.44
EGP	3.03	203.35	61.46	71.29
LGP (P3)	23.37	37.85	29.22	6.21

4. Conclusions

This study applied Goal Programming (GP) to the problem of selecting three optimal dam sites from a set of twenty-eight candidates under multiple, and sometimes conflicting, objectives. GP was chosen because of its ability to balance competing economic, social, environmental, and technical concerns in a structured and transparent way. Unlike single-objective optimization, GP offers multiple formulations that allow decision makers to incorporate their preferences through weighting, prioritization, and fairness-driven rules. Moreover, GP aligns closely with principles of collective intelligence, providing a decision framework that accommodates diverse viewpoints and contextual constraints while still generating actionable recommendations.

To fully explore the dam site selection problem, four GP variants were employed, each addressing a distinct sub-question. The Weighted Goal Programming (WGP) model asked: what is the most balanced solution when

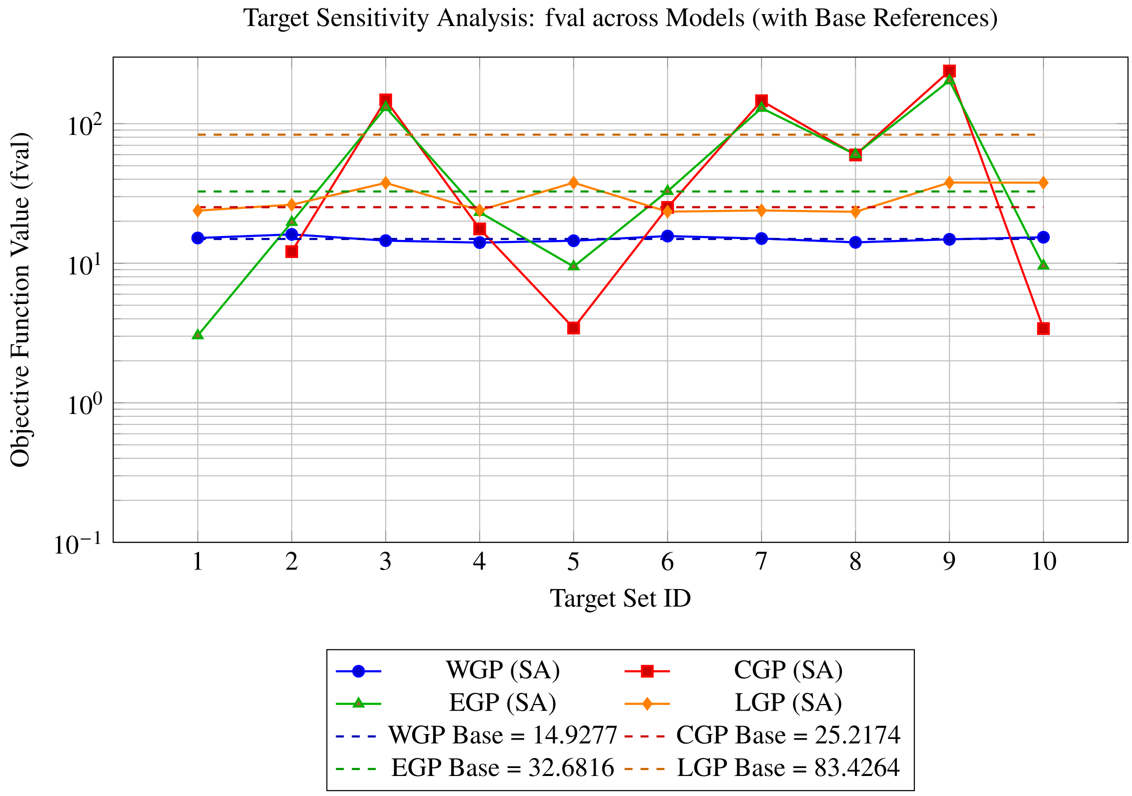

Figure 16: Target Sensitivity Analysis: *fval* across target sets for WGP, CGP, EGP, and LGP with dashed lines showing Base model objective values. Logarithmic scale improves joint visibility across models.

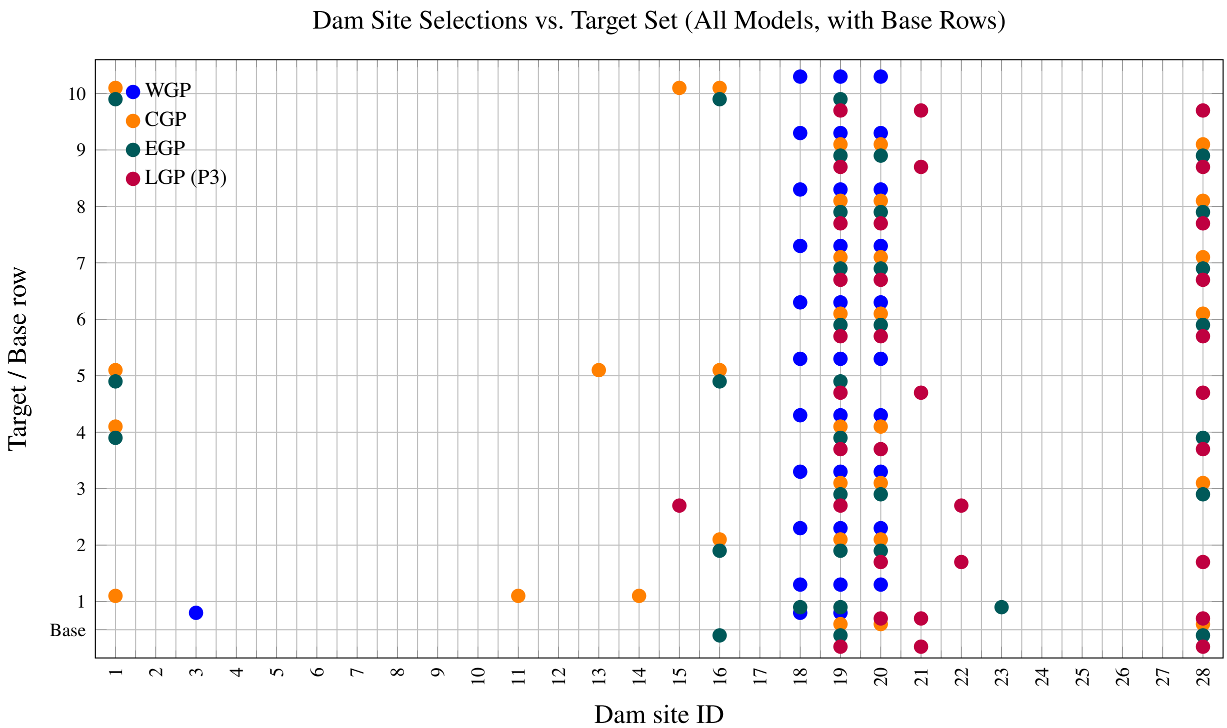

Figure 17: Selected dam sites by model and target set (circles; slight vertical offsets prevent overlap). Base models included on the "Base" row.

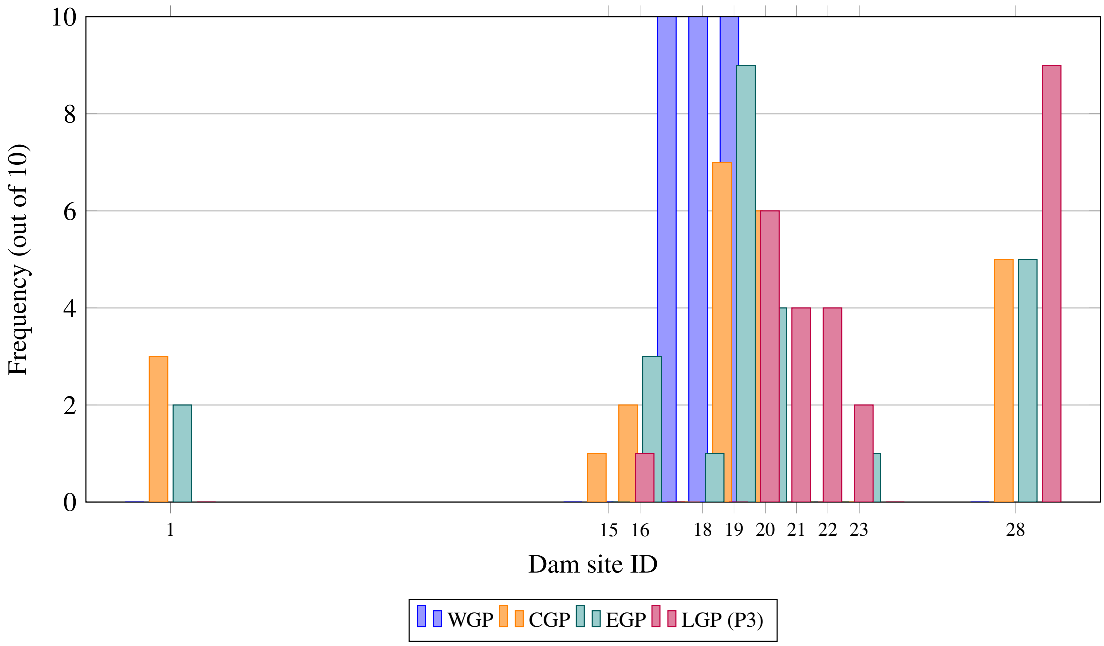

Figure 18: Selection frequency of dam sites across Target Sensitivity Analysis (only sites selected at least once).

all objectives are weighted simultaneously? The Lexicographic Goal Programming (LGP) model investigated: what solution emerges when objectives are ranked by strict priority? The Chebyshev Goal Programming (CGP) model examined: what solution minimizes the maximum deviation, thereby ensuring fairness across objectives? Finally, the Extended Goal Programming (EGP) model explored: how do solutions change when large deviations are penalized more heavily, revealing asymmetric trade-offs? Together, these formulations ensured that the problem was analyzed not from a single viewpoint, but across different logics of compromise, priority, fairness, and flexibility.

Multi-choice decision making (MCDM) was applied specifically to five selected targets: population, residence distance, farmland distance, nearest road, and farmland area. These criteria were identified as the most critical socio-technical and environmental considerations from earlier screening of possible objectives. Focusing on these five allowed for a tractable yet comprehensive representation of the competing goals most relevant to dam placement. The purpose of using MCDM here was not only to reveal the trade-offs between these key targets, but also to compare how different GP models interpret and resolve these trade-offs, thereby supporting more transparent decision making.

Sensitivity analysis was then conducted in two parts to test both the robustness and the reliability of the results. Weight sensitivity analysis examined how solutions shifted when the relative importance of objectives was perturbed, revealing which dam sites were consistently robust (selected across many scenarios) and which were sensitive to weight changes. Target sensitivity analysis, in contrast, evaluated the models under changing target levels, demonstrating that while WGP and LGP were stable, CGP and EGP displayed greater variability. These experiments were designed not only to test model stability, but also to guide decision makers by highlighting which recommendations remain credible even under uncertainty.

The combined findings suggest that dams 18, 19, and 20 form a consistently robust core set, appearing frequently across models and scenarios. However, a more nuanced recommendation emerges from the sensitivity results: while these three sites are highly reliable, site 28 and, to a lesser extent, sites 21 and 23, emerge as meaningful alternatives when particular objectives—especially environmental or social priorities—are given greater weight. Thus, the final recommendation is not a single rigid solution, but a set of robust core dams (18, 19, 20) complemented by flexible alternatives (28, 21, 23) that can be emphasized depending on contextual preferences. This flexibility, supported by GP and sensitivity analysis, strengthens the decision-making process by balancing stability with adaptability to local policy and stakeholder priorities.

Beyond the specific case of dam site selection, this study demonstrates the broader value of Goal Programming in infrastructure planning under competing objectives. By combining multiple GP formulations with systematic sensitivity analysis, the research illustrates how quantitative models can be translated into robust yet flexible recommendations that accommodate diverse stakeholder priorities. This integration of MCDM with sensitivity testing thus strengthens the link between optimization models and practical, policy-relevant decision support.

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Appendix A. Appendix

Appendix A.1. Dam site data for 28 dams

Table A.20: Generated weight sets (Dirichlet distribution, each row sums to 1).

Set	w_1	w_2	w_3	w_4	w_5	w_6	w_7	w_8	w_9	w_{10}
1	0.0227	0.2049	0.0468	0.0386	0.0914	0.1428	0.0317	0.0192	0.1159	0.2860
2	0.0070	0.0021	0.2364	0.2445	0.0683	0.0274	0.0969	0.0971	0.0131	0.2071
3	0.3275	0.0069	0.0260	0.2038	0.0424	0.0671	0.1081	0.0326	0.0850	0.1005
4	0.0105	0.0838	0.0079	0.3567	0.0266	0.2107	0.0415	0.1638	0.0694	0.0289
5	0.0607	0.0295	0.0513	0.3088	0.2222	0.2819	0.0153	0.0097	0.0114	0.0090
6	0.2207	0.1851	0.0263	0.0184	0.0677	0.0660	0.0039	0.0995	0.1187	0.1935
7	0.1901	0.1284	0.0442	0.0541	0.1202	0.0061	0.0897	0.2419	0.0414	0.0839
8	0.0695	0.0101	0.1077	0.1322	0.0502	0.1241	0.2275	0.1591	0.0325	0.0871
9	0.0046	0.0247	0.0449	0.0054	0.0365	0.0569	0.2021	0.0515	0.1027	0.4708
10	0.0033	0.0038	0.1642	0.3134	0.0262	0.1393	0.1262	0.0696	0.0527	0.1012

Table A.21: Generated RHS target sets (±20% variation around base values).

Set	t_1	t_2	t_3	t_4	t_5	t_6	t_7	t_8	t_9	t_{10}
1	48.6331	2.6354	0.0417	53.4186	0.5878	17.7502	1.7689	0.2817	0.2283	0.8106
2	56.0241	3.1042	0.0351	50.8542	0.5699	24.9478	1.4959	0.3043	0.2024	0.6750
3	46.6565	3.5760	0.0414	42.8169	0.5426	24.1885	2.1025	0.2574	0.2187	0.5985
4	41.3687	2.9781	0.0477	50.4336	0.4568	23.0273	2.0385	0.3617	0.1850	0.6467
5	44.6968	2.6406	0.0397	58.0982	0.5381	19.3880	1.9407	0.3507	0.2600	0.5469
6	37.8005	2.8530	0.0352	48.3838	0.6198	22.8369	1.6340	0.3339	0.2521	0.7687
7	53.1286	2.4128	0.0380	42.9002	0.5162	26.3075	1.9246	0.2811	0.2400	0.7453
8	51.5116	3.3912	0.0322	46.3516	0.4577	21.9087	2.2171	0.3311	0.2020	0.7095
9	49.0387	3.2880	0.0452	39.1999	0.4945	19.4257	1.8464	0.3814	0.2380	0.5974
10	41.2884	3.1301	0.0438	55.0954	0.4182	20.9885	1.6371	0.3177	0.2742	0.7036

Table A.22: Generated budget and number-of-sites sets.

Set	Budget	K (sites)
1	432.44	3
2	584.80	2
3	524.80	3
4	563.68	4
5	417.06	3
6	501.52	5
7	488.04	2
8	542.47	2
9	447.02	4
10	470.27	5

Table A.23: Criteria and budget data for 28 dam sites

Dam	Height	Capacity	Res. Area	Temp.	Pop.	Rainfall	Residence	Farm. Dist.	Nearest Road	Farm. Area	Budget
1	29.00	2.00	0.08	18.94	0.24	15.98	3.52	0.10	0.01	226.95	163.40
2	33.00	18.00	0.24	18.75	0.38	17.45	11.65	1.29	0.21	214.26	170.90
3	71.00	96.00	0.60	19.06	0.24	10.80	0.70	0.11	0.25	6.02	158.20
4	50.00	83.00	0.88	19.10	21.80	13.32	3.58	3.63	0.01	36.19	180.90
5	40.00	9.50	0.26	18.94	0.28	15.98	4.08	1.69	0.11	60.24	168.60
6	46.00	13.00	0.07	18.00	0.23	19.57	2.97	5.11	1.12	0.13	174.80
7	18.00	2.00	0.08	18.78	0.13	12.29	2.50	2.75	0.23	0.05	167.30
8	64.00	725.00	20.00	18.98	0.14	17.02	15.76	2.90	0.02	23.57	192.50
9	100.00	197.00	0.50	16.30	0.51	10.47	3.20	6.35	0.01	41.94	191.20
10	85.00	369.00	1.90	17.50	0.57	12.15	7.82	0.16	2.82	21.81	180.30
11	20.00	2.70	0.08	16.38	0.00	11.52	28.64	16.80	5.69	0.01	193.80
12	20.00	1.00	0.29	21.37	0.66	3.73	0.81	0.90	0.86	12.05	152.20
13	26.00	1.30	0.02	18.98	0.20	17.19	3.91	0.33	0.83	16.21	156.80
14	17.00	1.00	0.03	18.42	0.19	19.19	2.60	3.24	0.28	31.09	166.00
15	15.00	1.10	0.03	18.00	50.00	19.57	9.72	0.11	0.83	36.08	153.20
16	15.00	2.30	0.07	18.00	50.00	19.57	6.61	0.26	0.21	36.08	154.80
17	45.00	43.00	0.33	18.00	5.12	19.57	3.58	0.35	4.98	12.80	169.20
18	29.00	1.00	0.02	19.29	0.40	30.36	0.35	1.77	3.49	2.09	157.50
19	57.00	6.50	0.02	16.26	0.45	22.99	0.81	0.90	0.93	0.62	158.70
20	55.00	62.00	0.43	16.92	1.27	33.23	3.63	2.47	1.80	15.55	166.50
21	40.00	1.00	0.01	18.95	0.31	25.07	13.91	2.97	5.15	27.25	164.30
22	36.00	12.00	0.31	14.70	0.23	25.41	9.59	8.20	0.55	8.79	177.40
23	17.00	2.00	0.05	18.54	0.83	16.42	2.53	0.24	1.46	91.07	165.30
24	55.00	55.50	0.34	16.92	0.21	33.23	2.95	5.47	2.31	0.01	169.50
25	70.00	592.00	4.76	16.67	1.53	7.88	14.84	8.13	0.29	21.96	186.70
26	94.00	216.00	0.75	21.27	0.19	9.31	25.23	3.62	0.22	1.13	191.90
27	79.00	110.00	0.51	17.40	0.68	8.07	3.86	0.58	1.26	33.78	190.40
28	26.00	3.00	0.01	15.56	0.37	7.54	11.30	0.93	3.30	8.54	172.10

Table A.24: Model Evaluation Results and Selected Sites

Model	**fval**	p1	p2	p3	p4	p5	p6	p7	p8	p9	p10	n1	n2	n3	n4	n5	n6	n7	n8	n9	n10	**Selected Sites**
WGP	14.9277	0	0	0	0	0	0	0	0	0	0	56.0	6.5	0.05	5.35	1.16	47.70	1.83	2.59	5.65	93.10	17, 18, 22
CGP	25.2174	0	0	0	0	0	0	0	0	0	0	91.0	68.5	0.42	0	1.57	41.69	13.88	3.98	5.80	24.03	19, 20, 28
EGP	32.6816	0	0	0	0	0	0	0	0	0	0	51.0	8.8	0.06	1.08	50.30	28.03	16.86	1.77	4.21	44.56	17, 19, 28
LGP Priority 1	0	0	0	0	0	0	0	0	0	0	0	46.0	13.0	0.13	7.33	0.24	40.15	3.96	9.31	4.61	1.59	6, 7, 18
LGP Priority 2	0.0416	0	0	0	0	0	0	0	0	0	0	76.0	7.5	0	2.03	0.61	33.53	24.16	4.48	9.15	35.73	17, 19, 28
LGP Priority 3	83.4264	0	0	0	0	0	0	0	0	0	0	76.0	7.5	0	2.03	0.61	33.53	24.16	4.48	9.15	35.73	17, 19, 28

Table A.25: WGP Weight Sensitivity Analysis Results (with Selected Sites)

Weight Test Set	**fval**	p1	p2	p3	p4	p5	p6	p7	p8	p9	p10	n1	n2	n3	n4	n5	n6	n7	n8	n9	n10	**Selected Sites**
1	0.4128	0	0	0	0	0	0	0	0	0	0	56.00	6.50	0.05	5.35	1.16	47.70	1.83	2.59	5.65	93.10	18, 19, 23
2	1.6183	0	0	0	0	0	0	0	0	0	0	56.00	6.50	0.05	5.35	1.16	47.70	1.83	2.59	5.65	93.10	18, 19, 23
3	0.6062	0	0	0	0	0	0	0	0	0	0	59.00	5.50	0.29	8.18	0.99	35.01	0.11	3.25	5.05	14.08	12, 18, 19
4	0.8450	0	0	0	0	0	0	0	0	0	0	70.00	97.00	0.69	7.80	0.79	21.13	4.89	0.13	1.49	323.36	1, 3, 23
5	0.2595	0	0	0	0	0	0	0	0	0	0	56.00	6.50	0.05	5.35	1.16	47.70	1.83	2.59	5.65	93.10	18, 19, 23
6	0.2860	0	0	0	0	0	0	0	0	0	0	25.00	2.30	0.11	7.72	0.75	27.52	8.10	0.35	2.07	333.55	1, 13, 23
7	1.9670	0	0	0	0	0	0	0	0	0	0	98.00	101.50	0.63	5.12	1.00	28.14	2.18	0.93	2.41	97.03	3, 19, 23
8	2.4976	0	0	0	0	0	0	0	0	0	0	59.00	5.50	0.29	8.18	0.99	35.01	0.11	3.25	5.05	14.08	12, 18, 19
9	0.9350	0	0	0	0	0	0	0	0	0	0	59.00	5.50	0.29	8.18	0.99	35.01	0.11	3.25	5.05	14.08	12, 18, 19
10	1.4761	0	0	0	0	0	0	0	0	0	0	56.00	6.50	0.05	5.35	1.16	47.70	1.83	2.59	5.65	93.10	18, 19, 23

Table A.26: Full dataset results with extracted selected sites.

Target Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
1	15.1687	0	0	0	0	0	0	0	0	0	0	54.3669	6.8646	0.0483	0.6714	1.0922	52.0198	1.9211	2.6283	5.6517	92.9694	{36, 37, 40}
2	16.0963	0	0	0	0	0	0	0	0	0	0	46.9759	6.3958	0.0549	3.2358	1.1101	44.8222	2.1941	2.6057	5.6776	93.1050	{36, 37, 40}
3	14.5178	0	0	0	0	0	0	0	0	0	0	56.3435	5.9240	0.0486	11.2731	1.1374	45.5815	1.5875	2.6526	5.6613	93.1815	{36, 37, 40}
4	14.0624	0	0	0	0	0	0	0	0	0	0	61.6313	6.5219	0.0423	3.6564	1.2232	46.7427	1.6515	2.5483	5.6950	93.1333	{36, 37, 40}
5	14.4975	0	0	0	4.0082	0	0	0	0	0	0	58.3032	6.8594	0.0503	0	1.1419	50.3820	1.7493	2.5593	5.6200	93.2331	{36, 37, 40}
6	15.6563	0	0	0	0	0	0	0	0	0	0	65.1995	6.6470	0.0548	5.7062	1.0602	46.9331	2.0560	2.5761	5.6279	93.0113	{36, 37, 40}
7	15.0330	0	0	0	0	0	0	0	0	0	0	49.8714	7.0872	0.0520	11.1898	1.1638	43.4625	1.7654	2.6289	5.6400	93.0347	{36, 37, 40}
8	14.1186	0	0	0	0	0	0	0	0	0	0	51.4884	6.1088	0.0578	7.7384	1.2223	47.8613	1.4729	2.5789	5.6780	93.0705	{36, 37, 40}
9	14.8396	0	0	0	0	0	0	0	0	0	0	53.9613	6.2120	0.0448	14.8901	1.1855	50.3443	1.8436	2.5286	5.6420	93.1826	{36, 37, 40}
10	15.3641	0	0	0	1.0054	0	0	0	0	0	0	61.7116	6.3699	0.0462	0	1.2618	48.7815	2.0529	2.5923	5.6058	93.0764	{36, 37, 40}

Table A.27: Results of budget-based sensitivity analysis with extracted selected sites.

Budget	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
432.4411	*No feasible results*																					
584.7991	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
524.7983	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
563.6782	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
417.0606	*No feasible results*																					
501.5193	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
488.0362	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
542.4664	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
447.0190	*No feasible results*																					
470.2650	18.1079	0	0	0	0	0	0	0	0	0.0000	0	59.0000	5.5000	0.2900	8.1800	0.9900	35.0100	0.1100	3.2500	5.0500	14.0800	{31, 36, 37}

Table A.28: Results of site selection analysis with extracted selected site indices.

No. of Sites Selected	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
3	14.9277	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{36, 37, 40}
2	7.5259	0	0	0	13.1900	0	0	0.7000	0	0	0	39.0000	4.5000	0	0	0.3300	31.2800	0	2.3500	4.1900	2.0300	{36, 37}
1	2.0658	0	0	0.0200	32.4800	0.0700	0	1.0500	0	0	0.0600	10.0000	3.5000	0	0	0	0.9200	0	0.5800	0.7000	0	{36}

Table A.29: Results of target analysis showing fval/D, feature values, and extracted selected site indices.

Target Test Set	**fval/D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
1	0	0	0	0	0	0	0	0	0	0	0	15.3669	1.4646	0.3583	4.8914	50.3122	21.5298	12.2811	0.8283	1.4717	274.2694	{1, 31, 34}
2	12.1215	0	0	0	0	0	0	0	0	0	0	70.9759	67.6958	0.4849	0.3258	51.1501	50.8422	9.5541	3.3257	2.7376	51.5750	{35, 38, 39}
3	148.0771	0	0	0	0	0	0	0	0	0	0	91.3435	67.9240	0.4186	5.9231	1.5474	39.5715	13.6375	4.0426	5.8113	24.1115	{37, 38, 45}
4	17.6305	0	0	0	0	0	0	0	0	0	0	70.6313	8.5219	0.0623	0.3264	0.6032	23.4827	13.5915	1.5683	4.0550	235.4633	{1, 37, 45}
5	3.4348	0	0	0	2.1782	0	0	0	0	0	0	25.3032	2.9594	0.1303	0	49.9019	33.3520	12.0993	0.3393	0.7900	278.6931	{1, 31, 34}
6	25.1214	0	0	0	0	0	0	0	0	0	0	100.1995	68.6470	0.4248	0.3562	1.4702	40.9231	14.1060	3.9661	5.7779	23.9413	{37, 38, 45}
7	145.9941	0	0	0	0	0	0	0	0	0	0	84.8714	69.0872	0.4220	5.8398	1.5738	37.4525	13.8154	4.0189	5.7900	23.9647	{37, 38, 45}
8	59.7109	0	0	0	0	0	0	0	0	0	0	86.4884	68.1088	0.4278	2.3884	1.6323	41.8513	13.5229	3.9689	5.8280	24.0005	{37, 38, 45}
9	238.5017	0	0	0	0	0	0	0	0	0	0	88.9613	68.2120	0.4148	9.5401	1.5955	44.3343	13.8936	3.9186	5.7920	24.1126	{37, 38, 45}
10	3.4040	0	0	0	0.2916	0	0	0	0	0.0071	0	17.7116	2.2699	0.1362	0.1362	99.8218	34.1315	18.2129	0.1523	0.7829	298.4064	{1, 32, 33}

Table A.30: CGP Budget Sensitivity Analysis results showing feasible and infeasible solutions with selected site indices.

Budget	**fval/D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
432.4411	*No feasible results*																					
584.7991	0	0	0	0	0	0	0	0	0	0	0	89.0000	599.8000	5.0000	5.8500	1.4900	18.9800	20.9700	9.8300	1.0000	97.7300	{24, 32, 44}
524.7983	0	0	0	0	0	0	0	0	0	0	0	96.0000	216.0000	1.0800	12.8400	0.5700	6.9500	27.7000	4.3000	0.8600	239.4500	{1, 31, 44}
563.6782	0	0	0	0	0.0900	0	0	0	0	0	0	96.0000	217.7000	0.8700	7.8500	0	14.7400	55.5300	20.2000	5.6900	227.4100	{1, 30, 44}
417.0606	*No feasible results*																					
501.5193	0	0	0	0	0	0	0	0	0	0	0	17.0000	1.1000	0.3600	9.5700	50.3800	17.2100	12.1900	0.7900	1.4700	274.4000	{1, 31, 34}
488.0362	0	0	0	0	0	0	0	0	0	0	0	17.0000	1.1000	0.3600	9.5700	50.3800	17.2100	12.1900	0.7900	1.4700	274.4000	{1, 31, 34}
542.4664	0	0	0	0	0	0	0	0	0	0	0	96.0000	216.0000	1.0800	12.8400	0.5700	6.9500	27.7000	4.3000	0.8600	239.4500	{1, 31, 44}
447.0190	*No feasible results*																					
470.2650	0	0	0	0	0	0	0	0	0	0	0	17.0000	1.1000	0.3600	9.5700	50.3800	17.2100	12.1900	0.7900	1.4700	274.4000	{1, 31, 34}

Table A.31: CGP number of selected sites sensitivity snalysis results

Sites Selected	**fval/D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
3	0	0	0	0	0	0	0	0	0	0	0	17.0000	1.1000	0.3600	9.5700	50.3800	17.2100	12.1900	0.7900	1.4700	274.4000	{1, 31, 34}
2	0	0	0	0	8.5300	0.0900	0	0	0	0	0	76.0000	215.0000	0.7900	0	0	3.2200	26.8900	3.4000	0	227.4000	{1, 47}
1	0	27.0000	2.0000	0	27.3700	0	18.3400	1.0500	0	0	0	0	0	0.2500	0	0.1400	0	0	0.5800	0.6300	11.3700	{31}

Table A.32: EGP Sensitivity Analyses results: evaluation of target test sets with feature values and selected site indices.

Target Test Set	**fval**	**D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	3.0337	0	0	0	0	0	0	0	0	0	0	0	54.3669	6.8646	0.0483	0.6714	1.0922	52.0198	1.9211	2.6283	5.6517	92.9694	{38, 39, 43}
2	19.6847	12.1215	0	0	0	0	0	0	0	0	0	0	70.9759	67.6958	0.4849	0.3258	51.1501	50.8422	9.5541	3.3257	2.7376	51.5750	{38, 41, 42}
3	130.949	148.0771	0	0	0	0	0	0	0	0	0	0	91.3435	67.9240	0.4186	5.9231	1.5474	39.5715	13.6375	4.0426	5.8113	24.1115	{39, 40, 48}
4	23.1993	17.6305	0	0	0	0	0	0	0	0	0	0	70.6313	8.5219	0.0623	0.3264	0.6032	23.4827	13.5915	1.5683	4.0550	235.4633	{1, 39, 48}
5	9.4657	3.8696	0	0	0	4.8982	0	0	0	0	0	0	56.3032	8.1594	0.1303	0	50.1519	39.1520	8.9993	0.9093	0.8900	263.1031	{1, 37, 40}
6	32.8122	25.1214	0	0	0	0	0	0	0	0	0	0	100.1995	68.6470	0.4248	0.3562	1.4702	40.9231	14.1060	3.9661	5.7779	23.9413	{39, 40, 48}
7	129.3857	145.9941	0	0	0	0	0	0	0	0	0	0	84.8714	69.0872	0.4220	5.8398	1.5738	37.4525	13.8154	4.0189	5.7900	23.9647	{39, 40, 48}
8	60.1762	59.7109	0	0	0	0	0	0	0	0	0	0	86.4884	68.1088	0.4278	2.3884	1.6323	41.8513	13.5229	3.9689	5.8280	24.0005	{39, 40, 48}
9	203.3531	238.5017	0	0	0	0	0	0	0	0	0	0	88.9613	68.2120	0.4148	9.5401	1.5955	44.3343	13.8936	3.9186	5.7920	24.1126	{39, 40, 48}
10	9.5897	3.808	0	0	0	1.8954	0	0	0	0	0	0	59.7116	7.6699	0.1262	0	50.2718	37.5515	9.3029	0.9423	0.8758	262.9464	{1, 37, 40}

Table A.33: EGP Budget-constrained Sensitivity Analyses: results of target test sets with feature values and selected site indices.

Target Test Set	**Budget**	**fval**	**D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	432.4411	*No feasible results*																						
2	584.7991	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
3	524.7983	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
4	563.6782	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
5	417.0606	*No feasible results*																						
6	501.5193	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
7	488.0362	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
8	542.4664	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{39, 40, 43}
9	447.0190	*No feasible results*																						
10	470.2650	3.6216	0	0	0	0	0	0	0	0	0	0	0	59.0000	5.5000	0.2900	8.1800	0.9900	35.0100	0.1100	3.2500	5.0500	14.0800	{33, 38, 39}

Table A.34: EGP number of selected sites sensitivity snalysis results

Number of Sites Selected	**fval**	**D**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
3	2.9855	0	0	0	0	0	0	0	0	0	0	0	56.0000	6.5000	0.0500	5.3500	1.1600	47.7000	1.8300	2.5900	5.6500	93.1000	{37, 38, 41}
2	1.5052	0	0	0	0	13.1900	0	0	0.7000	0	0	0	39.0000	4.5000	0	0	0.3300	31.2800	0	2.3500	4.1900	2.0300	{37, 38}
1	0.4132	0	0	0	0.0200	32.4800	0.0700	0	1.0500	0	0	0.0600	10.0000	3.5000	0	0	0	0.9200	0	0.5800	0.7000	0	{39}

Table A.35: LGP Target Sensitivity Analysis for Priority 1

Target Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	0	0	0	0	0	0	0	0	0	0	0	45.8166	13.3713	0.1221	12.9312	0.1870	40.4746	3.6656	9.3239	4.5982	1.7038	{26,27,36}
2	0	0	0	0	1.3995	0	0	0	0	0	0	47.8683	0.9883	0.0750	0	0.3798	43.4016	14.9274	7.1193	8.6500	28.6752	{33,36,39}
3	0	0	0	0	0	0	0	0	0	0	0	43.5964	13.5022	0.1298	13.3625	0.1367	42.6863	3.7705	9.3147	4.5736	1.6196	{26,27,36}
4	0	0	0	0	0	0	0	0	0	0	0	42.0429	0.8466	0.0767	8.0898	0.3844	41.2670	15.1138	7.1374	8.6434	28.6024	{33,36,39}
5	0	0	0	0	0	0	0	0	0	0	0	38.5599	13.1304	0.1280	15.4896	0.2380	42.8816	3.5906	9.3468	4.5866	1.6000	{26,27,36}
6	0	0	0	0	0	0	0	0	0	0	0	40.6912	0.5251	0.0717	5.7874	0.4071	45.5639	15.1302	7.1064	8.6664	28.6407	{33,36,39}
7	0	0	0	0	0	0	0	0	0	0	0	41.2119	13.0441	0.1237	9.4485	0.2134	43.8448	3.9527	9.3496	4.5643	1.6681	{26,27,36}
8	0	0	0	0	0	0	0	0	0	0	0	45.4013	0.6944	0.0706	0.5644	0.3426	44.5213	15.2114	7.1688	8.6685	28.5750	{33,36,39}
9	0	0	0	0	0	0	0	0	0	0	0	36.6660	13.3448	0.1259	8.0468	0.1577	41.1093	3.8649	9.3636	4.6091	1.6742	{26,27,36}
10	0	0	0	0	0	0	0	0	0	0	0	45.8171	0.4042	0.0746	3.3146	0.3276	42.1563	14.9808	7.1536	8.6785	28.7073	{33,36,39}

Table A.36: LGP Target Sensitivity Analysis for Priority 2

Target Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	8.8884	0	0	0	0	0	0	0	0	0	0	98.4529	68.0613	0.4188	8.4696	1.5337	39.5781	14.0400	3.9841	5.8098	23.9165	{36,37,46,50}
2	0.0142	0	0	0	0.3973	0	0	0	0	0	0	43.1582	8.0757	0.0142	0	50.3904	26.4912	19.7920	1.6475	4.8330	44.5890	{36,39,42,50}
3	0.0063	0	0	0	2.3767	0	0	0	0	0	0	47.0041	1.7995	0.0063	0	0.3442	31.5651	27.1303	3.8794	9.0698	51.3287	{35,41,47}
4	8.1421	0	0	0	0	0	0	0	0	0	0	91.6040	68.6279	0.4133	7.7288	1.4940	41.0211	14.2032	3.9577	5.7780	24.0885	{36,37,46,50}
5	0.0017	0	0	0	6.1021	0	0	0	0	0	0	80.0436	7.5386	0.0017	0	0.6925	30.3029	24.1036	4.5356	9.1340	35.6649	{36,38,42,47}
6	2.4988	0	0	0	0	0	0	0	0	0	0	86.5026	68.7581	0.4205	2.0783	1.4832	45.1897	13.6080	3.9703	5.8400	23.9826	{36,37,50}
7	1.0498	0	0	0	0	0	0	0	0	0	0	87.7229	68.2129	0.4234	0.6263	1.5922	38.0077	14.1749	3.9332	5.7930	24.1482	{36,37,50}
8	4.6095	0	0	0	0	0	0	0	0	0	0	99.1672	68.2908	0.4162	4.1933	1.5767	42.6311	13.5697	4.0307	5.7664	24.0094	{36,37,50}
9	0	0	0	0.0028	2.6339	0	0	0	0	0	0	74.5754	8.0213	0	0	0.6547	33.8136	24.2393	4.4266	9.1865	35.6306	{36,38,42,47}
10	0.007	0	0	0.0028	2.6339	0	0	0	0	0	0	74.5754	8.0213	0	0	0.6547	33.8136	24.2393	4.4266	9.1865	35.6306	{36,38,42,47}

Table A.37: LGP Target Sensitivity Analysis for Priority 3

Target Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	23.8339	0	0	0	0	0	0	0	0	0	0	90.8166	68.8713	0.4121	5.6012	1.5170	42.0146	13.5856	3.9939	5.7882	24.1438	{36,37,46,50}
2	26.2725	0	0	0	7.6495	0	0	0	0	0	0	83.8683	7.4883	0.0050	0	0.6698	31.2816	24.1874	4.4293	9.1600	35.6952	{36,38,42,47}
3	37.6495	0	0	0	0	0	0	0	0	0	0	63.0429	16.4466	0.3267	0.0298	50.2244	41.5170	18.4738	8.8574	2.0834	44.7024	{35,41,44,47}
4	23.9389	0	0	0	0	0	0	0	0	0	0	83.5599	68.6304	0.4180	8.1596	1.5680	44.4216	13.5106	4.0168	5.7766	24.0400	{36,37,46,50}
5	37.7732	0	0	0	6.1021	0	0	0	0	0	0	80.0436	7.5386	0.0017	0	0.6925	30.3029	24.1036	4.5356	9.1340	35.6649	{36,38,42,47}
6	23.4183	0	0	0	0	0	0	0	0	0	0	86.5026	68.7581	0.4205	2.0783	1.4832	45.1897	13.6080	3.9703	5.8400	23.9826	{36,37,50}
7	23.9012	0	0	0	0	0	0	0	0	0	0	87.7229	68.2129	0.4234	0.6263	1.5922	38.0077	14.1749	3.9332	5.7930	24.1482	{36,37,50}
8	23.3668	0	0	0	0	0	0	0	0	0	0	99.1672	68.2908	0.4162	4.1933	1.5767	42.6311	13.5697	4.0307	5.7664	24.0094	{36,37,50}
9	37.8524	0	0	0.0028	2.6339	0	0	0	0	0	0	74.5754	8.0213	0	0	0.6547	33.8136	24.2393	4.4266	9.1865	35.6306	{36,38,42,47}
10	37.7892	0	0	0	1.3684	0	0	0	0	0	0	69.1277	7.4091	0.0070	0	0.5602	35.4288	24.1839	4.4936	9.1116	35.8378	{36,38,42,47}

Table A.38: LGP Weight Sensitivity Analysis for Priority 1

Weight Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Targets**
1	0	0	0	0	0	0	0	0	0	0	0	15.0000	2.3000	0.1300	7.3300	50.0100	40.1500	7.6000	4.4600	3.7000	37.5400	{31,36,38,41}
2	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
3	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
4	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
5	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
6	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
7	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
8	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
9	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}
10	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.9600	9.3100	4.6100	1.5900	{28,29,36}

Table A.39: LGP Weight Sensitivity Analysis for Priority 2

Weight Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Dams**
1	0.0043	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
2	0.0135	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
3	0.0004	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
4	0.0002	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
5	0.0025	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
6	0.0022	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
7	0.0051	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
8	0.0006	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
9	0.0052	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
10	0.0068	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}

Table A.40: LGP Weight Sensitivity Analysis for Priority 3

Weight Test Set	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Dams**
1	5.0425	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
2	9.5191	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
3	2.5808	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
4	10.5879	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
5	3.2344	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
6	9.6772	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
7	8.8018	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
8	5.5848	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
9	2.5091	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}
10	13.1004	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{3,7,10,28}

Table A.41: LGP Budget Sensitivity Analysis Results for Priority 1, showing feasible and infeasible solutions with selected dam indices.

Budget	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Dams**
432.4411	0	0	0	0	0	0	0	0	0	0	20.0000	2.7000	0.1400	5.7100	0.0100	32.1000	29.6300	21.0000	9.1800	1.4700	{27, 31, 37}	
584.7991	0	0	0	0	0	0	0	0	0	0	20.0000	2.7000	0.1400	5.7100	0.0100	32.1000	29.6300	21.0000	9.1800	1.4700	{27, 31, 37}	
524.7983	0	0	0	0	0	0	0	0	0	0	20.0000	2.7000	0.1400	5.7100	0.0100	32.1000	29.6300	21.0000	9.1800	1.4700	{27, 31, 37}	
563.6782													*No feasible results*									
417.0606	0	0	0	0	0	0	0	0	0	0	54.0000	6.8000	0.0700	4.8100	50.3300	50.8500	5.9100	2.6100	4.4000	38.1100	{36, 38, 39}	
501.5193													*No feasible results*									
488.0362	0	0	0	0	0	0	0	0	0	0	15.0000	2.3000	0.1300	7.3300	50.0100	40.1500	7.6000	4.4600	3.7000	37.5400	{27, 36, 38}	
542.4664	0	0	0	0	0	0	0	0	0	0	57.0000	6.5000	0.0800	5.5900	0.4600	43.5700	1.8000	5.1000	4.4200	2.0800	{27, 38, 39}	
447.0190													*No feasible results*									
470.2650	0	0	0	0	0	0	0	0	0	0	20.0000	2.7000	0.1400	5.7100	0.0100	32.1000	29.6300	21.0000	9.1800	1.4700	{27, 31, 37}	

Table A.42: LGP Budget Sensitivity Analysis Results for Priority 2, showing feasible and infeasible solutions with selected dam indices.

Budget	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Dams**
432.4411	0.0416	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{39, 41, 48}
584.7991	0.0416	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{39, 41, 48}
524.7983	0.0416	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{39, 41, 48}
563.6782	*No feasible results*																					
417.0606	0.6188	0	0	0	0	0	0	0	0	0	0	65.0000	5.8000	0.0200	5.7900	0.5300	48.4700	3.2100	2.6800	5.0200	18.2400	{31, 36, 37}
501.5193	*No feasible results*																					
488.0362	0.0416	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{39, 41, 48}
542.4664	0.3618	0	0	0	0	0	0	0	0	0	0	76.0000	5.8000	0.0100	5.4500	0.4400	43.1800	16.7700	3.8800	6.6800	43.4000	{31, 36, 38}
447.0190	*No feasible results*																					
470.2650	0.0416	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{39, 41, 48}

Table A.43: LGP Budget Sensitivity Analysis Results (Priority 3).

Budget	**fval**	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
432.4411	83.4264	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{19, 21, 28}
584.7991	83.4264													*No feasible results*								
524.7983	83.4264	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	-0.0000	2.0300	0.6100	33.5300	24.1600	4.4800	9.1500	35.7300	{19, 21, 28}
563.6782													*No feasible results*									
417.0606	6.3617	0	0	0	0	0	0	0	0	0	0	101.0000	100.5000	0.8700	7.9500	0.8300	15.4500	0.4600	1.5900	1.8100	18.0100	{3, 11, 19}
501.5193													*No feasible results*									
488.0362	6.3617	0	0	0	0	0	0	0	0	0	0	101.0000	100.5000	0.8700	7.9500	0.8300	15.4500	0.4600	1.5900	1.8100	18.0100	{3, 11, 19}
542.4664	6.3617	0	0	0	0	0	0	0	0	0	0	101.0000	100.5000	0.8700	7.9500	0.8300	15.4500	0.4600	1.5900	1.8100	18.0100	{3, 11, 19}
447.0190													*No feasible results*									
470.2650	6.3617	0	0	0	0	0	0	0	0	0	0	101.0000	100.5000	0.8700	7.9500	0.8300	15.4500	0.4600	1.5900	1.8100	18.0100	{3, 11, 19}

Model	**fval**	**D**	z_1	z_2	z_3	z_4	z_5	p_1	p_2	p_3	p_4	p_5	p_6	p_7	p_8	p_9	p_{10}	n_1	n_2	n_3	n_4	n_5	n_6	n_7	n_8	n_9	n_{10}	**Selected Sites**
WGP	28.7245	–	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	56.0000	7.5000	0.1100	5.0000	1.0000	33.3200	4.8100	0.8900	2.1500	317.9600	{1, 19, 23}
CGP	25.1304	25.1304	1	0	0	0	1	0	0	0	1.0052	0	0	0	0	0	0	91.0000	68.5000	0.4200	1.0052	1.5700	41.6900	13.6900	3.9500	5.7800	24.0300	{19, 20, 28}
EGP	32.5462	25.1304	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	91.0000	68.5000	0.4200	0.0000	1.5700	41.6900	13.6900	3.9500	5.7800	24.0300	{19, 20, 28}
LGP P1	0	–	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	46.0000	13.0000	0.1300	7.3300	0.2400	40.1500	3.7700	9.2800	4.5900	1.5900	{6, 7, 12}
LGP P2	0.0416	–	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	23.9700	4.4500	9.1300	35.7300	{19, 21, 28}
LGP P3	82.7889	–	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	76.0000	7.5000	0	2.0300	0.6100	33.5300	23.9700	4.4500	9.1300	35.7300	{19, 21, 28}

Table A.44: Results for WGP, CGP, EGP, and LGP Multi-Choice Goal Programming Extensions.