

## Day 5 : dsa babua pattern course :- two pointers problem

### Problem 1 : Strobogrammatic Number



#### Definition (Kya hota hai Strobogrammatic Number?)

Aisa number jo  $180^\circ$  rotate karne par same dikhe, usko **Strobogrammatic Number** bolte hain.

→  $180^\circ$  rotation ka matlab:

Top-ultra se ghumane par digits apne valid rotated pair ke equal rehne chahiye.

#### ✓ Valid Strobogrammatic Digits & Their Pairs:

Digit	After $180^\circ$ Rotation	Valid?
0	0	✓
1	1	✓
8	8	✓
6	9	✓
9	6	✓



#### Invalid Digits (kabhi Strobogrammatic nahi hote):

2, 3, 4, 5, 7

Yeh rotate hone ke baad koi valid digit nahi banate.



#### Concept / Intuition (Logic samajhna sabse important)

Aapko ek **string of digits** milta hai.

Aapko check karna hai → kya yeh number **rotate hone ke baad same** ban sakta hai?

#### Two Pointer Approach:

1.  $i = 0$  left se start
2.  $j = n - 1$  right se start
3. Check:

mapping[s[i]] == s[j]

4.

5. Agar kisi point pe match nahi hua → **not strobogrammatic**

#### Mapping:

0 → 0

1 → 1

8 → 8

6 → 9

9 → 6

### Example 1

**Input: "69"**

Left = '6' → rotated = '9'

Right = '9'

✓ match

So "69" is **strobogrammatic**

### Example 2

**Input: "818"**

Indices:

0 → 8

1 → 1

2 → 8

Pairs:

8 ↔ 8 ✓

1 ↔ 1 ✓

Center element always valid (0,1,8) ✓

So → **Yes**

### Example 3

**Input: "12"**

Left = 1 → maps to 1

Right = 2 → but 2 is invalid

✗ Not strobogrammatic

### Algorithm (Step-by-step)

1. Create a **map** of valid strobogrammatic pairs
2. Use two pointers i and j
3. For each pair:
  - Check if s[i] exists in map
  - Check if map[s[i]] == s[j]
4. If koi mismatch → return false
5. Loop end hone par → return true

### Time & Space Complexity

 **Time: O(n)**

Har iteration me i++ aur j--

→ ek hi pass me kaam done

 **Space: O(1)**

Map me sirf 5 entries → constant space

### Final Code (C++ Two Pointer Approach)

```
cpp

class Solution {
public:
    bool isStrobogrammatic(string s) {
        unordered_map<char, char> mp = {
            {'0','0'}, {'1','1'}, {'8','8'},
            {'6','9'}, {'9','6'}
        };

        int i = 0, j = s.size() - 1;

        while(i <= j) {
            char L = s[i];
            char R = s[j];

            if(mp.find(L) == mp.end()) return false; // invalid digit

            if(mp[L] != R) return false; // pair mismatch

            i++;
            j--;
        }
        return true;
    }
};
```

## ✓ Revision Points

- Valid digits: **0,1,8,6,9**
- 6 ↔ 9 pair important
- Invalid digits: **2,3,4,5,7**
- Two pointers + mapping
- Time: O(n), Space: O(1)

## Problem 2: Append Characters to String to Make Subsequence —

### 🎯 Problem Goal

Aapko **two strings S (source)** aur **T (target)** diye gaye hain.

Aapko **minimum characters** batane हैं jo S ke end me append karne padेंगे, tāki T, S ka subsequence ban jaye.



### What is a Subsequence? (Quick Recap)

Subsequence = string created by

→ **Deleting ANY characters**

→ **Without changing the order**

Example:

S = "babuaDS"

Valid subsequences: "bauS", "bbu", "babua"

Order same rahe = subsequence

(positions skip ho sakte hain → delete allowed)



## Core Idea / Intuition (Two Pointer)

Aapko check karna hai ki **T ka kitna part S me match ho sakta hai**

→ **starting se, order maintain** karte हूँ.

**Two Pointers:**

- i → S ke characters traverse karega
- j → T ke characters match karega

**Matching Rules:**

- Agar  $S[i] == T[j] \rightarrow \text{match} \rightarrow j++$
- Warna → S[i] ko ignore (delete) →  $i++$
- Process continue until S exhausts.

Last me:

👉 T ka jitna part match nahi hua = append karna padega

**Formula:**

answer = T×length - j



## Example Explained

S = "coaching"

T = "coding"

Matching step-by-step:

S	T	Match?	j (progress in T)
c	c	✓	1
o	o	✓	2
a	d	✗	2
c	d	✗	2
h	d	✗	2
i	d	✗	2
n	d	✗	2
g	d	✗	2

👉 S me "d" kabhi mila hi nahi

👉 T ke matched part = "co" → (length = 2)

👉 Remaining = "ding" → 4 characters

So answer = **4**

## Algorithm — Clean Steps

1. Two pointers:
  - $i = 0$  (for S)
  - $j = 0$  (for T)
2. While  $i < n$  and  $j < m$ :
  - If characters match  $\rightarrow j++$
  - Always move  $i++$
3. End me  $j$  = number of matched characters.
4. Append needed =  $m - j$   
(jo T ka remaining part bacha hai)

## Time Complexity

$O(n + m)$

$\rightarrow$  Ek pass S par, aur T pointer ek direction me badhta hai.

## Space Complexity

$O(1)$

$\rightarrow$  No extra space.

## Final C++ Code (Clean)

```
cpp

class Solution {
public:
    int appendCharacters(string s, string t) {
        int i = 0, j = 0;

        while(i < s.size() && j < t.size()) {
            if(s[i] == t[j]) j++;
            i++;
        }

        return t.size() - j;
    }
};
```

## ✓ Revision Notes (5-sec scan)

- Subsequence  $\rightarrow$  delete allowed, order not change
- Two pointers  $\rightarrow$  S scan, T match
- Last matched index =  $j$
- Append =  $t \times \text{length} - j$
- Simple linear problem
- Mostly asked in interviews as warm-up

### Problem 3 : 1650 — Lowest Common Ancestor of a Binary Tree III (Tree nodes have parent pointer)

#### Problem Goal

Aapko **binary tree** diya hai jisme har node ke paas

- left
- right
- parent  
pointer diya hua hai.

Aapko do nodes **p** aur **q** diye gaye hain.

👉 **Lowest Common Ancestor (LCA)** return karna hai.

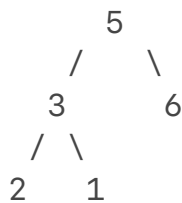
#### What is LCA? (Simple Definition)

For two nodes **p** and **q**:

**LCA = wo lowest (i.e., sabse neeche wala) node jiske subtree me p aur q dono descendant ho.**

Node can be a descendant of itself.

Example:



- $LCA(2,1) = 3$
- $LCA(3,1) = 3$
- $LCA(3,6) = 5$

#### Approach 1 — Using Set (Brute but Good)

**Intuition:**

1. p se **parent chain** upar jao aur sab nodes ek **set** me daal do.
2. Ab q se **upar jao**:
  - jo pehla node **set me mil jaye** → that is LCA.

**Why it works?**

Kyuki dono nodes ka **first common parent** = LCA.

#### ✓ Algorithm Steps (Approach 1)

1. Create a set.
2. Traverse upward from p:
  - Insert p into set.
  - Move  $p = p.parent$
3. Traverse upward from q:
  - If (q in set) → return q
  - Else  $q = q.parent$

## 🕒 Complexity:

Time:  $O(\text{height of tree})$

Space:  $O(\text{height})$  // set me upar jaate nodes store honge

## ✓ Code (Approach 1)

```
class Solution {
public:
    Node* lowestCommonAncestor(Node* p, Node* q) {
        unordered_set<Node*> st;

        while(p != nullptr) {
            st.insert(p);
            p = p->parent;
        }

        while(q != nullptr) {
            if(st.count(q)) return q;
            q = q->parent;
        }

        return nullptr;
    }
};
```

## ★ Approach 2 — Two Pointer Trick (Best Approach)

Same technique as "Intersection of Two Linked Lists".

## 🧠 Beautiful Intuition

Parent pointers → nodes form **linked lists** going upward:

Example:

p → parent → parent → ... → root → null

q → parent → parent → ... → root → null

These two upward chains behave like **two linked lists**.

Like intersection of linked lists:

distance(p to root) = A

distance(q to root) = B

common tail path = C

If you traverse like:

p1 = p

q1 = q

Each step:

p1 = (p1 == NULL ? q : p1.parent)

q1 = (q1 == NULL ? p : q1.parent)

👉 Guaranteed that

**p1 and q1 will meet exactly at LCA.**

Why?

Both pointers travel:

A + C + B + C = same total distance

### ✓ Algorithm Steps (Approach 2)

1. Create pointers p1 = p and q1 = q.
2. Loop until p1 == q1:
  - Move p1 upward:

p1 = p1 == NULL ? q : p1.parent

○

- Move q1 upward:

q1 = q1 == NULL ? p : q1.parent

○

3. When both meet → that's LCA.

### 🔥 Why This Approach Is Amazing?

- No extra space
- Elegant
- Fast
- Works like linked list intersection logic
- Guaranteed meeting point = LCA

### 🕒 Complexity

Time:  $O(\text{height})$

Space:  $O(1)$



## ✓ Final Best Code (Approach 2)

cpp

```
class Solution {
public:
    Node* lowestCommonAncestor(Node* p, Node* q) {
        Node* p1 = p;
        Node* q1 = q;

        while(p1 != q1) {
            p1 = (p1 == nullptr ? q : p1->parent);
            q1 = (q1 == nullptr ? p : q1->parent);
        }

        return p1; // or q1
    }
};
```



## Revision Notes (5-sec scan)

- LCA = lowest node having p & q as descendants
- Approach 1 → store parents of p → walk q upwards
- Approach 2 → two-pointer intersection trick
- Best approach = **Two Pointer**
- Space =  $O(1)$