

# SVM

July 24, 2020

```
[1]: import mglearn
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.svm import LinearSVC
from sklearn.datasets import load_iris
```

```
[2]: iris = load_iris()
```

```
[3]: iris
```

```
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```

Correlation\n      =====\n
sepal length:  4.3  7.9   5.84  0.83   0.7826\n      sepal width:    2.0  4.4
3.05  0.43  -0.4194\n      petal length:   1.0  6.9   3.76  1.76   0.9490
(high!)\n      petal width:    0.1  2.5   1.20  0.76   0.9565 (high!)\n
===== \n\n      :Missing
Attribute Values: None\n      :Class Distribution: 33.3% for each of 3 classes.\n
:Creator: R.A. Fisher\n      :Donor: Michael Marshall
(MARSHALL%PLU@io.arc.nasa.gov)\n      :Date: July, 1988\n\nThe famous Iris
database, first used by Sir R.A. Fisher. The dataset is taken\nfrom Fisher\'s
paper. Note that it\'s the same as in R, but not as in the UCI\nMachine Learning
Repository, which has two wrong data points.\n\nThis is perhaps the best known
database to be found in the\npattern recognition literature. Fisher\'s paper is
a classic in the field and\nis referenced frequently to this day. (See Duda &
Hart, for example.) The\ndata set contains 3 classes of 50 instances each,
where each class refers to a\ntype of iris plant. One class is linearly
separable from the other 2; the\nlatter are NOT linearly separable from each
other.\n\n.. topic:: References\n\n    - Fisher, R.A. "The use of multiple
measurements in taxonomic problems"\n        Annual Eugenics, 7, Part II, 179-188
(1936); also in "Contributions to\n        Mathematical Statistics" (John Wiley,
NY, 1950).\n    - Duda, R.O., & Hart, P.E. (1973) Pattern Classification and
Scene Analysis.\n        (Q327.D83) John Wiley & Sons. ISBN 0-471-22361-1. See
page 218.\n    - Dasarathy, B.V. (1980) "Nosing Around the Neighborhood: A New
System\n        Structure and Classification Rule for Recognition in Partially
Exposed\n        Environments". IEEE Transactions on Pattern Analysis and
Machine\n        Intelligence, Vol. PAMI-2, No. 1, 67-71.\n    - Gates, G.W. (1972)
"The Reduced Nearest Neighbor Rule". IEEE Transactions\n        on Information
Theory, May 1972, 431-433.\n    - See also: 1988 MLC Proceedings, 54-64.
Cheeseman et al\'s AUTOCLASS II\n        conceptual clustering system finds 3
classes in the data.\n    - Many, many more ...',
'feature_names': ['sepal length (cm)',
'sepal width (cm)',
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'filename': '/opt/conda/lib/python3.7/site-
packages/sklearn/datasets/data/iris.csv'}

```

```

[4]: X = iris.data[50:, 2:]
     y = iris.target[50:] - 1

```

```

[5]: X

```

```

[5]: array([[4.7, 1.4],
           [4.5, 1.5],
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           [4.6, 1.5],
           [4.5, 1.3],

```

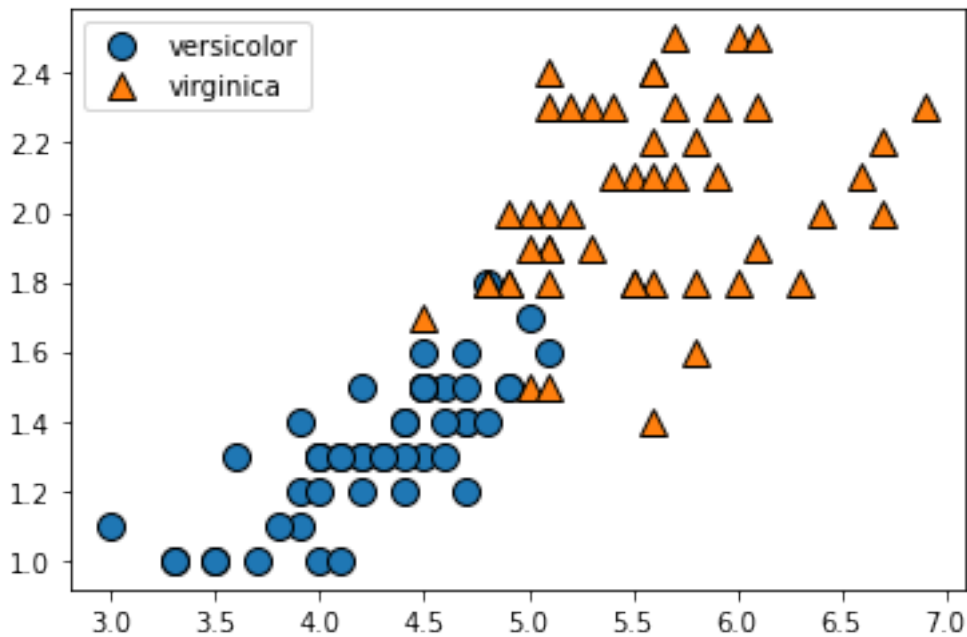
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```
[6]: y
```

```
[6]: array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
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         1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
         1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1])
```

```
[7]: mglearn.discrete_scatter(X[:, 0], X[:, 1], y)
plt.legend(['versicolor', 'virginica'], loc='best')
plt.show()
```



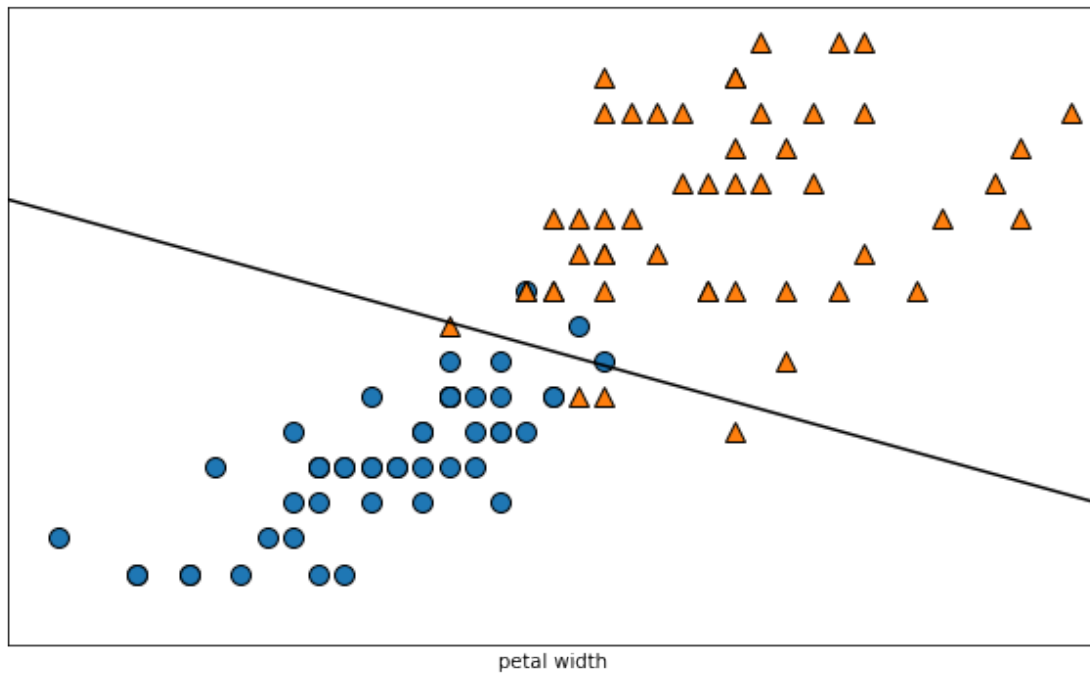
```
[8]: X_train, X_test, y_train, y_test = train_test_split(X, y, stratify=y,
    ↪ random_state=0)
```

```
[9]: svm = LinearSVC().fit(X_train, y_train)
```

```
[10]: def plot_separator(model):
    plt.figure(figsize=(10, 6))
    mglearn.plots.plot_2d_separator(model, X)
    mglearn.discrete_scatter(X[:, 0], X[:, 1], y)
    plt.xlabel('petal length')
    plt.xlabel('petal width')
    plt.xlim(2.8, 7.0)
    plt.ylim(0.8, 2.6)
    plt.show()
```

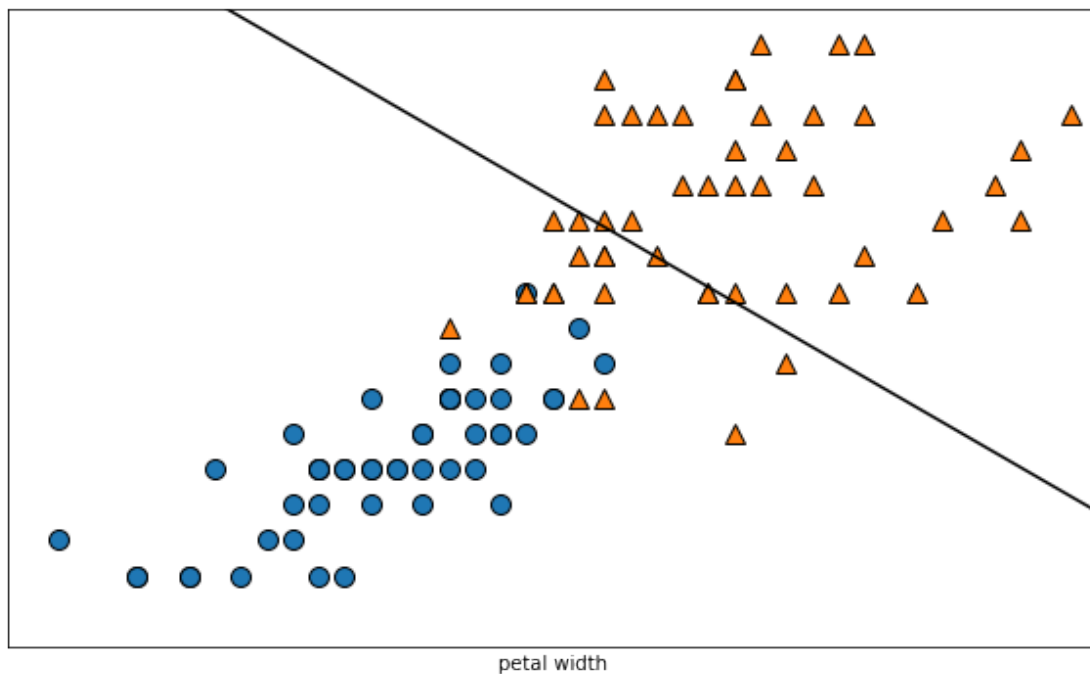


```
[11]: plot_separator(svm)
```



```
[12]: svm_100 = LinearSVC(C=100).fit(X_train, y_train)
      plot_separator(svm_100)
```

```
/opt/conda/lib/python3.7/site-packages/sklearn/svm/_base.py:947:
ConvergenceWarning: Liblinear failed to converge, increase the number of
iterations.
    "the number of iterations.", ConvergenceWarning)
```



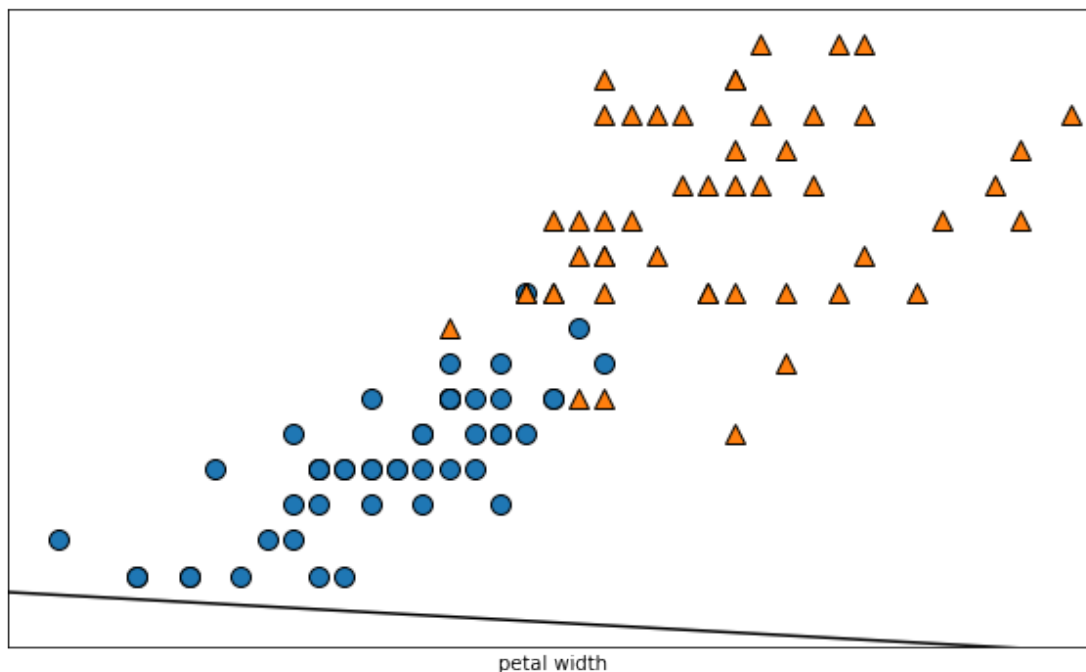
```
[13]: print('score on training set: {:.2f}'.format(svm.score(X_train, y_train)))
      print('score on test set: {:.2f}'.format(svm.score(X_test, y_test)))
```

```
score on training set: 0.91
score on test set: 1.00
```

```
[14]: print('score on training set: {:.2f}'.format(svm_100.score(X_train, y_train)))
      print('score on test set: {:.2f}'.format(svm_100.score(X_test, y_test)))
```

```
score on training set: 0.81
score on test set: 0.88
```

```
[15]: svm_001 = LinearSVC(C=0.01).fit(X_train, y_train)
      plot_separator(svm_001)
```



```
[16]: print('score on training set: {:.2f}'.format(svm_001.score(X_train, y_train)))
      print('score on test set: {:.2f}'.format(svm_001.score(X_test, y_test)))
```

```
score on training set: 0.51
score on test set: 0.48
```

```
[17]: import mglearn
      import numpy as np
      import matplotlib.pyplot as plt
      from sklearn.datasets import make_moons
```

```
[18]: moons = make_moons(n_samples=200, noise=0.1, random_state=0)
      moons
```

```
[18]: (array([[ 7.92357355e-01,  5.02648573e-01],
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               [-1.04412427e+00, -1.82607610e-01],
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 [ 9.24799914e-01, 4.94247065e-01],  
 [ 1.08911468e+00, -4.40836789e-01],  
 [-1.16502510e+00, 2.52779074e-01],  
 [-1.75082328e-01, 1.04012819e+00],  
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 [ 1.08086088e-01, 9.56975505e-01],  
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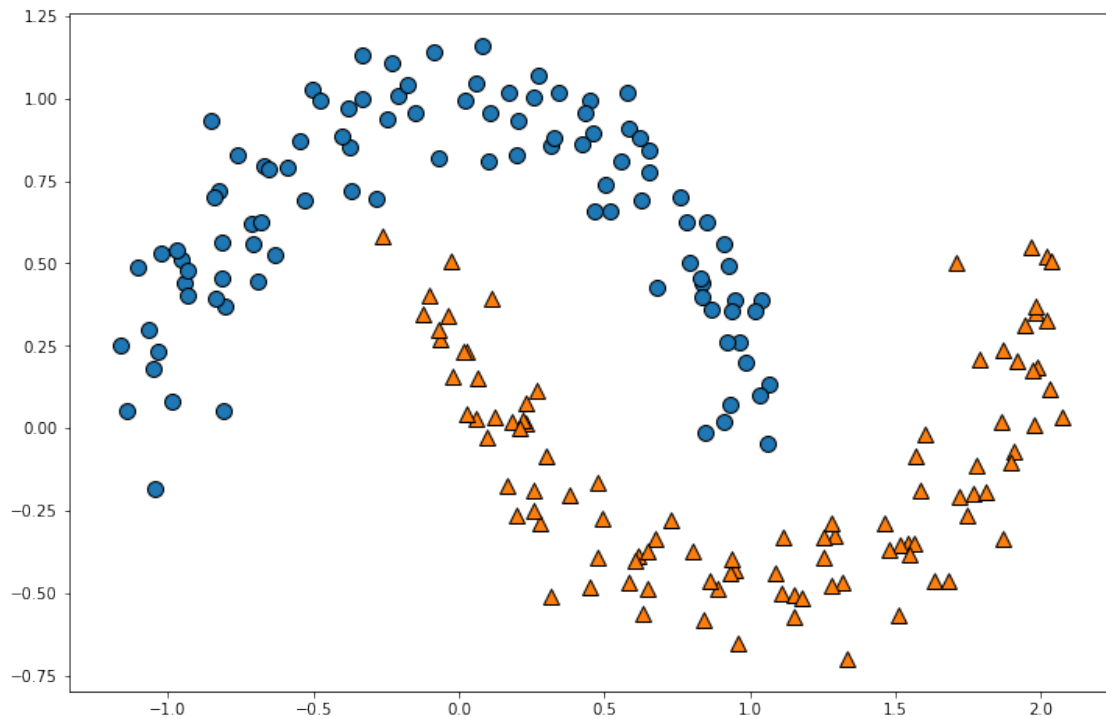
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       0, 1]))
```

```
[19]: X = moons[0]
      y = moons[1]
```

```
[20]: plt.figure(figsize=(12, 8))
      mglearn.discrete_scatter(X[:, 0], X[:, 1], y)
```

```
[20]: [<matplotlib.lines.Line2D at 0x7f441cb7e190>,
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```



```
[21]: from sklearn.model_selection import train_test_split
      from sklearn.preprocessing import StandardScaler
      from sklearn.svm import LinearSVC
```

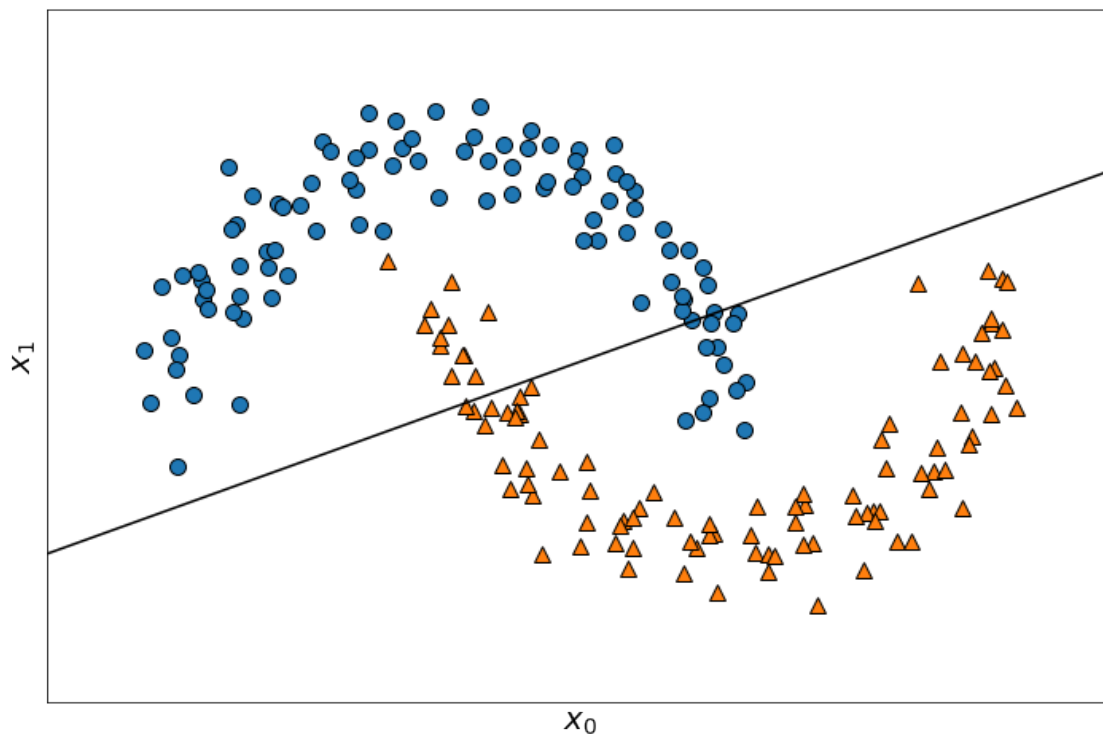


```
[22]: X_train, X_test, y_train, y_test = train_test_split(X, y, stratify=y,
↳random_state=0)
```

```
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.fit_transform(X_test)
```

```
[23]: lin_svm = LinearSVC().fit(X_train_scaled, y_train)
```

```
[24]: plt.figure(figsize=(12, 8))
mglearn.plots.plot_2d_separator(lin_svm, X)
mglearn.discrete_scatter(X[:, 0], X[:, 1], y)
plt.xlabel('$x_0$', fontsize=20)
plt.ylabel('$x_1$', fontsize=20)
plt.show()
```



```
[25]: from sklearn.preprocessing import PolynomialFeatures
```

```
[26]: poly = PolynomialFeatures(degree=3)
X_train_poly = poly.fit_transform(X_train)
X_test_poly = poly.fit_transform(X_test)

print(X_train_poly)
```

```
print(X_test_poly)
```

```
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```
[27]: poly.get_feature_names()
```

```
[28]: X_train_poly_scaled = scaler.fit_transform(X_train_poly)
      X_test_poly_scaled = scaler.fit_transform(X_test_poly)

      lin_svm = LinearSVC().fit(X_train_poly_scaled, y_train)
      lin_svm.predict(X_test_poly_scaled) == y_test
```

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```
True, True, True, True, True])
```

```
[29]: from sklearn.pipeline import Pipeline
```

```
poly_svm = Pipeline([
    ('poly', PolynomialFeatures(degree=3)),
    ('scaler', StandardScaler()),
    ('svm', LinearSVC())
])

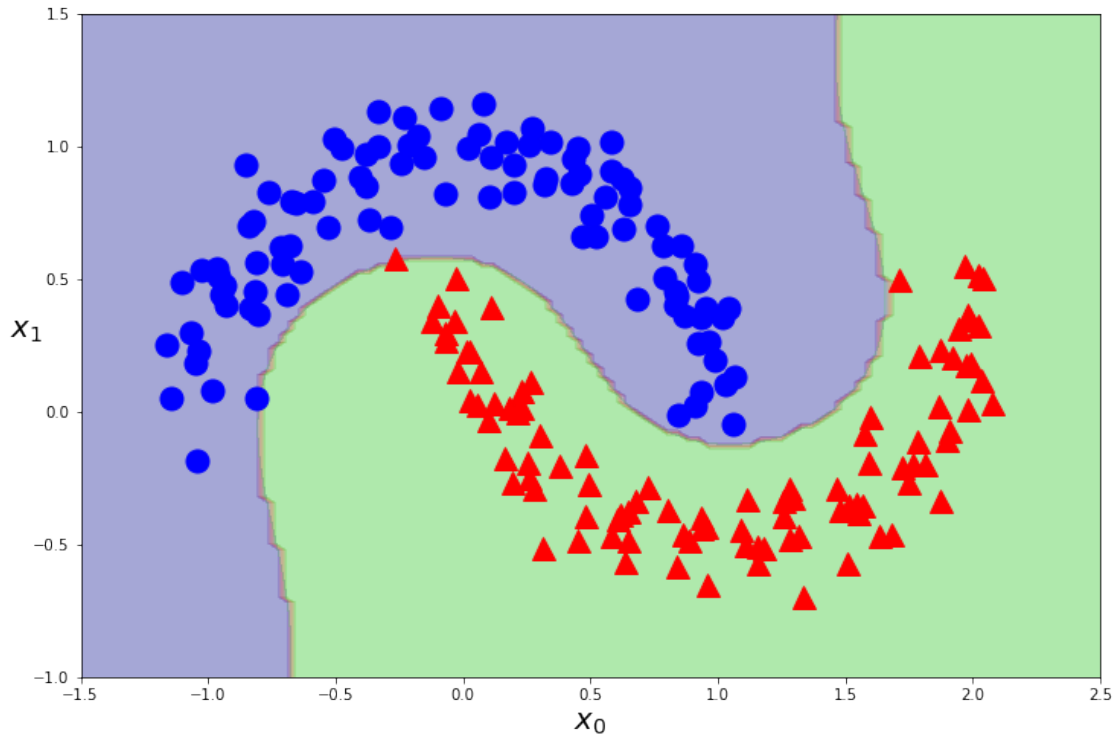
poly_svm.fit(X, y)
```

```
[29]: Pipeline(memory=None,
              steps=[('poly',
                      PolynomialFeatures(degree=3, include_bias=True,
                                           interaction_only=False, order='C')),
                     ('scaler',
                      StandardScaler(copy=True, with_mean=True, with_std=True)),
                     ('svm',
                      LinearSVC(C=1.0, class_weight=None, dual=True,
                                fit_intercept=True, intercept_scaling=1,
                                loss='squared_hinge', max_iter=1000,
                                multi_class='ovr', penalty='l2', random_state=None,
                                tol=0.0001, verbose=0))],
              verbose=False)
```

```
[30]: def plot_decision_function(model):
    _x0 = np.linspace(-1.5, 2.5, 100)
    _x1 = np.linspace(-1.0, 1.5, 100)
    x0, x1 = np.meshgrid(_x0, _x1)
    X = np.c_[x0.ravel(), x1.ravel()]
    y_pred = model.predict(X).reshape(x0.shape)
    y_decision = model.decision_function(X).reshape(x0.shape)
    plt.contourf(x0, x1, y_pred, cmap=plt.cm.brg, alpha=0.2)
    plt.contourf(x0, x1, y_decision, levels=[y_decision.min(), 0, y_decision.
    ↪max()], alpha=0.3)
```

```
[31]: def plot_dataset(X, y):
    plt.plot(X[:, 0][y==0], X[:, 1][y==0], 'bo', ms=15)
    plt.plot(X[:, 0][y==1], X[:, 1][y==1], 'r^', ms=15)
    plt.xlabel('$x_0$', fontsize=20)
    plt.ylabel('$x_1$', fontsize=20, rotation=0)
```

```
[32]: plt.figure(figsize=(12, 8))
    plot_decision_function(poly_svm)
    plot_dataset(X, y)
    plt.show()
```



```
[33]: from sklearn.svm import SVC
```

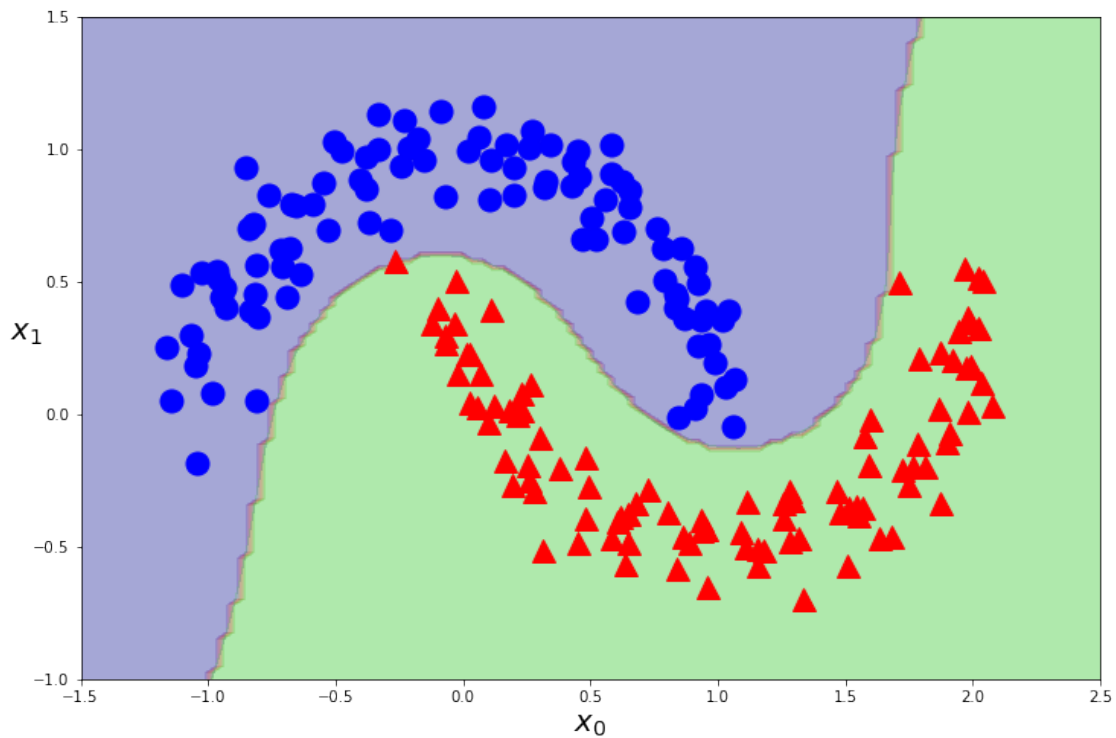
```
[34]: kernel_svm = Pipeline([
    ('scaler', StandardScaler()),
    ('svm', SVC(kernel='poly', degree=3, coef0=1))
])
```

```
[35]: kernel_svm.fit(X, y)
```

```
[35]: Pipeline(memory=None,
    steps=[('scaler',
        StandardScaler(copy=True, with_mean=True, with_std=True)),
    ('svm',
        SVC(C=1.0, break_ties=False, cache_size=200, class_weight=None,
        coef0=1, decision_function_shape='ovr', degree=3,
        gamma='scale', kernel='poly', max_iter=-1,
        probability=False, random_state=None, shrinking=True,
        tol=0.001, verbose=False))],
    verbose=False)
```

```
[36]: plt.figure(figsize=(12, 8))
    plot_decision_function(kernel_svm)
    plot_dataset(X, y)
```

```
plt.show()
```



```
[37]: plt.figure(figsize=(20, 15))

for i, degree in enumerate([2, 3, 5, 10]):
    poly_kernel_svm = Pipeline([
        ('scaler', StandardScaler()),
        ('svm', SVC(kernel='poly', degree=degree, coef0=1))
    ])
    poly_kernel_svm.fit(X, y)

    plt.subplot(221 + i)
    plot_decision_function(poly_kernel_svm)
    plot_dataset(X, y)
    plt.title('d = {}'.format(degree), fontsize=20)

plt.show()
```



