

Problem D. We need some math...

Time limit 3000 ms
Memory limit 256MB

Problem Description

How many tuples (a, b, c) exist such that $a \leq X, b \leq Y, c \leq Z$, and $\frac{ab}{c}$ is an irreducible fraction? Furthermore, what is the sum of all these irreducible fractions?

12/05 UPD: a, b, c have to be positive integers.

Here, an irreducible fraction $\frac{a}{b}$ is defined as a fraction where $\gcd(a, b) = 1$.

Input format

There only one line input, containing three integers $X, Y, Z (1 \leq X, Y, Z \leq 3 \times 10^5)$

Output format

Print two integers — the number of tuples and the sum of these irreducible fractions, taken modulo 998244353 (the answer can always be represented as an irreducible fraction $\frac{a}{b}$, where $b \bmod 998244353 \neq 0$; you have to print $a \cdot b^{-1} \bmod 998244353$).

Subtask score

| Subtask | Score | Additional Constraints |
|---------|-------|------------------------|
| 1 | 59 | $X, Y, Z \leq 100$. |
| 2 | 41 | No constraints |

Sample

Sample Input 1

11 22 33

Sample Output 1

3739 787081510

Sample Input 2

2 2 2

Sample Output 2

5 499122186

Sample Input 2

998 244 353

Sample Output 2

| |
|--------------------|
| 37040959 418691757 |
|--------------------|

Notes

For sample input 2, there are 5 tuples $(1, 1, 1), (1, 1, 2), (1, 2, 1), (2, 1, 1), (2, 2, 1)$. The sum of the fractions is $\frac{19}{2}$ so you should output "5 499122186" while $499122186 = 19 \times 2^{-1} \mod 998344353$.