$$\binom{N}{k} \ge \left(\frac{N}{k}\right)^k$$

We say in recitation 2 that if $2 \leq y \leq \frac{x}{2}$ then $\frac{x}{y} \leq \frac{x-1}{y-1} \iff -xy-x \leq xy-y \iff y \leq x$ So why isn't it enough that $y \leq x$?