
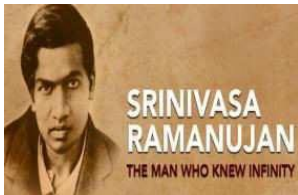


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|  | SRM Institute of Science and<br>Technology<br>Kattankulathur  |  |   |
|   | DEPARTMENT OF MATHEMATICS   |  |   |
|   | 18MAB101T Calculus and Linear Algebra   |  |   |
|   | UNIT - IV   |  |   |
|   | Tutorial Sheet -2   |  | Answers   |
| 1.  | State two properties of the evolute of the curve.   |  |   |
| 2.  | Find the envelope of the family of straight lines $y = mx + am^2$ , m being the parameter   |  | Ans: $x^2+ 4ay = 0$   |
| 3.  | Define envelope of a family of curves.  |  |   |
| 4.  | Find the envelope of the family of straight lines $x \cos \alpha + y \sin \alpha = a \sec \alpha$ , $\alpha$ being the parameters.  |  | <b>Ans: <math>y^2 - 4a(a - x) = 0</math></b>  |
| 5.  | Define involutes and evolutes.  |  |   |
| 6.  | Find the equation of the circle of curvature at (c, c) on $xy = c^2$ .  |  | <b>Ans: <math>(x - 2c)^2 + (y - 2c)^2 = (\sqrt{2}c)^2</math></b>  |
| 7.  | Find the equation of the evolute of the<br>a) parabola $y^2 = 4ax$ ; b) ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ;<br>c) hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ ; d) rectangular hyperbola $xy = c^2$<br>and e) curve $x^{2/3} + y^{2/3} = a^{2/3}$ . |  | Ans:<br>a) <b><math>27ay^2 = 4(x - 2a)^3</math></b><br>b) $(ax)^{\frac{2}{3}} + (by)^{\frac{2}{3}} = (a^2 - b^2)^{\frac{2}{3}}$<br>c) $(ax)^{\frac{2}{3}} - (by)^{\frac{2}{3}} = (a^2 + b^2)^{\frac{2}{3}}$<br>d) $(x + y)^{\frac{2}{3}} - (x - y)^{\frac{2}{3}} = (4c)^{\frac{2}{3}}$<br>e) $(x + y)^{\frac{2}{3}} + (x - y)^{\frac{2}{3}} = 2a^{\frac{2}{3}}$ |
| 8.  | Show that the evolute of the cycloid<br>$x = a(\theta - \sin \theta)$ , $y = a(1 - \cos \theta)$ is another equal cycloid.  |  |   |
| 9.  | Find the evolute of the tractrix<br>$x = a \left( \cos t + \log \tan \left( \frac{t}{2} \right) \right)$ , $y = a \sin t$ .   |  | Ans: $y = a \cosh \frac{x}{a}$  |
| 10.   | Show that the evolute of the curve<br>$x = a(\cos \theta + \theta \sin \theta)$ , $y = a(\sin \theta - \theta \cos \theta)$ is a circle.  |  |   |