Dag Na								
Reg. No.								

## B.Tech. / M.Tech (Integrated) DEGREE EXAMINATION, JANUARY 2023

First Semester

## 21MAB101T - CALCULUS AND LINEAR ALGEBRA

(For the candidates admitted from the academic year 2022-2023)

**Note:** 

- (i) **Part A** should be answered in OMR sheet within first 40 minutes and OMR sheet should be handed over to hall invigilator at the end of 40<sup>th</sup> minute.
- (ii) **Part B** and **Part C** should be answered in answer booklet.

Time: 3 Hours

Max. Marks: 75

$$PART - B (5 \times 8 = 40 \text{ Marks})$$

Answer ALL Questions

Marks BL CO PO

21. a. Find the Eigen values and Eigen vectors of the matrix  $\begin{pmatrix} 10 & -2 & -5 \\ -2 & 2 & 3 \\ -5 & 3 & 5 \end{pmatrix}$ .

(OR)

- b. Verify Cayley Hamilton theorem for the matrix  $\begin{pmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{pmatrix}$ .
- 22. a. Expand  $e^x \cos y$  at  $\left(1, \frac{\pi}{4}\right)$  as a Taylor series upto second degree terms.

b. If u = u(x, y) and  $x = e^r \cos \theta$  and  $y = e^r \sin \theta$  show that  $\left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial u}{\partial y} \right)^2 = e^{-2r} \left[ \left( \frac{\partial u}{\partial r} \right)^2 + \left( \frac{\partial u}{\partial \theta} \right)^2 \right].$ 

- 23. a. Solve  $(D^2 + 2D + 1)y = e^{3x} + \sin 2x$ .
  - b. Solve  $(D^2 + 1)y = \tan x$  by the method of variation of parameters.
- 24. a. Find the radius of curvature of the curve  $r = a(1 + \cos \theta)$  at the point  $\theta = \frac{\pi}{2}$ .

b. Find the evolute of the parabola  $y^2 = 4ax$ .

Page 1 of 2

25. a. Test the convergence of the series 
$$\sum_{n=1}^{\infty} \left( \sqrt{n^4 + 1} - \sqrt{n^4 - 1} \right)$$
.

b. Test the convergence of the series, 
$$\frac{2}{3.4} + \frac{2.4}{3.5.6} + \frac{2.4.6}{3.5.7.8} + \frac{2.4.6.8}{3.5.7.9.10} + \dots \infty$$
.

## $PART - C (1 \times 15 = 15 Marks)$ Answer **ANY ONE** Question

26. Reduce the quadratic form  $3x^2 - 2y^2 - z^2 - 4xy + 8xz + 12yz$  to canonical form by an orthogonal transformation. Discuss the nature of the quadratic form and also find rank, index, and signature.

Marks

27. Find the dimensions of the rectangular box open at the top, of maximum <sup>15</sup> <sup>4</sup> <sup>2</sup> capacity whose surface area is 432 sq.cm.

\* \* \* \* \*