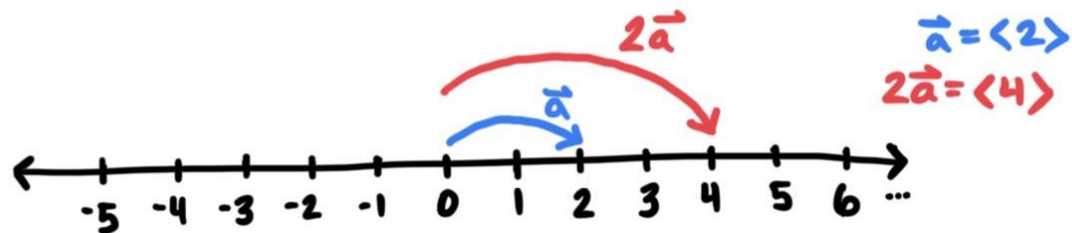
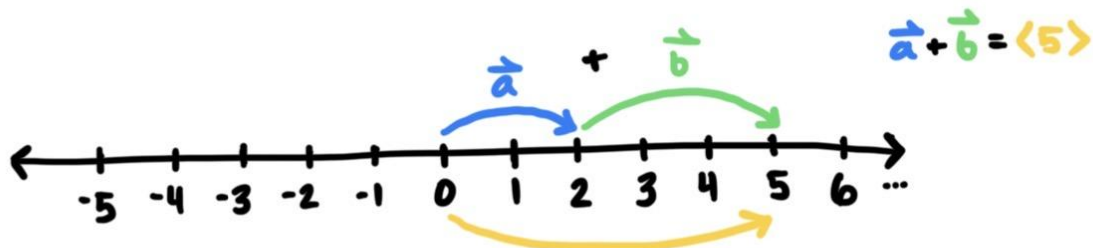
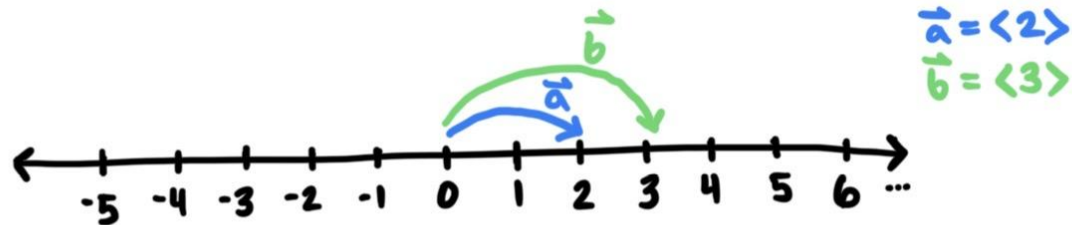
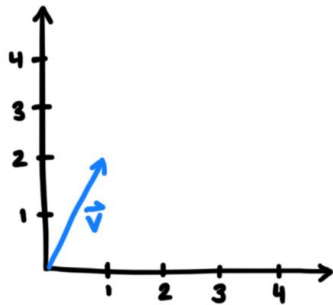


What's a vector?

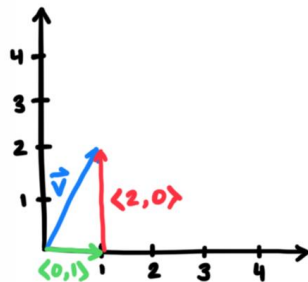


What's a vector?



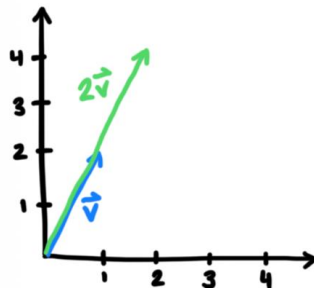
$$\vec{v} = \langle 1, 2 \rangle$$

1 and 2 are components



$$\vec{v} = \langle 1, 0 \rangle + \langle 0, 2 \rangle = \langle 1, 2 \rangle$$

add corresponding components



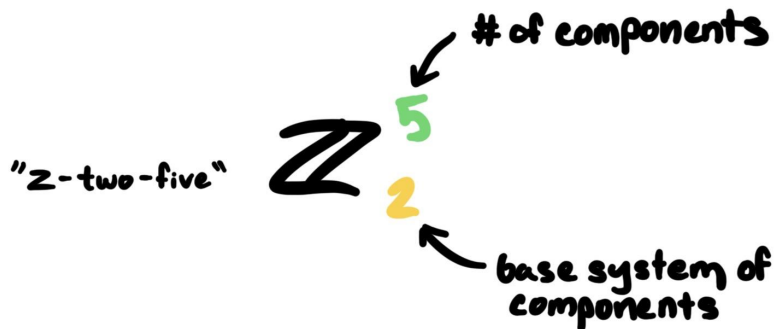
$$2\vec{v} = 2 \cdot \vec{v} = 2 \cdot \langle 1, 2 \rangle = \langle 2, 4 \rangle$$

distribute multiplication to components

What's a vector space?

A **vector space** describes a certain “type” of vector, based on 2 aspects of the vector:

- The number of **components** it has, called the **degree**
- The number base system the components are within, called the **order**



(note: in general, any space \mathbb{Z}_2^n is called a Hamming space, and we'll use them a bunch when we learn about Hamming codes later)

$\langle 1, 1, 1, 0, 0 \rangle \in \mathbb{Z}_2^5$

("is within")

What're some vectors within \mathbb{Z}_4^3 ?

And why do we care about vector spaces?

A binary message can be represented by a vector, for example,

$$1011010 \rightarrow \langle 1, 0, 1, 1, 0, 1, 0 \rangle \text{ which is within } \mathbb{Z}_2^7$$

So when we start learning about Hamming codes, we'll be talking about vector spaces and subspaces.