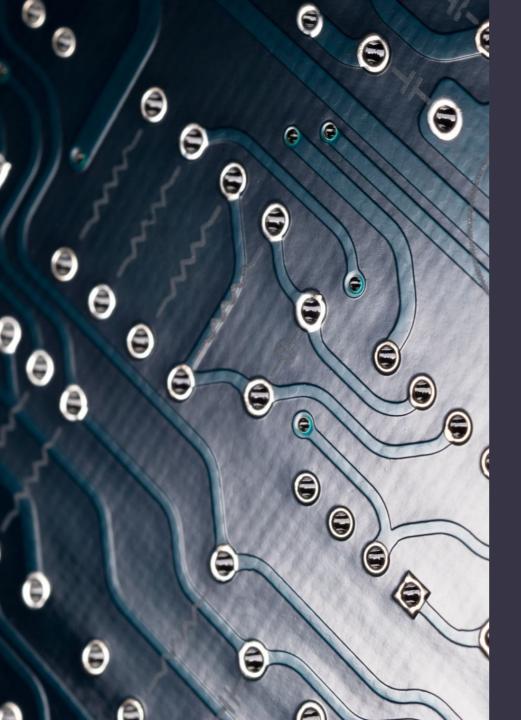




Introduction- The Challenge of High-Dimensional Data The Data Deluge

- Modern datasets often contain a vast number of features (dimensions).
- **•**Curse of Dimensionality:
- Increased computational cost and time.
- Difficulty in visualization.
- Degraded model performance (overfitting, sparsity).
- More data required to achieve statistical significance.



What is Dimensionality Reduction?

The Core Idea

- •Process of reducing the number of random variables under consideration.
- •Transforms data from a high-dimensional space to a low-dimensional space.
- •Aims to preserve meaningful properties of the original data as much as possible.

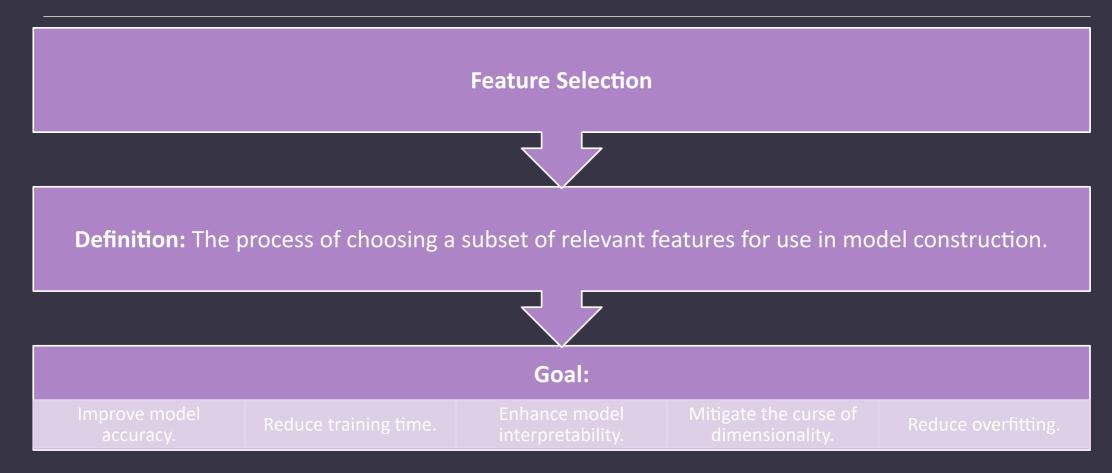


Two Main Categories

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- **1.Feature Selection:** Selecting a subset of the original features.
- **2.Feature Extraction:** Transforming features into a new, smaller set of features.

Feature Selection - Definition & Goal



Types of Feature Selection Methods

1. Filter Methods

Concept: Select features based on their intrinsic properties (e.g., correlation, statistical scores) without involving any learning algorithm.

Pros: Computationally efficient, independent of the learning algorithm.

Cons: May select redundant features, ignores interaction with the model.

Examples:

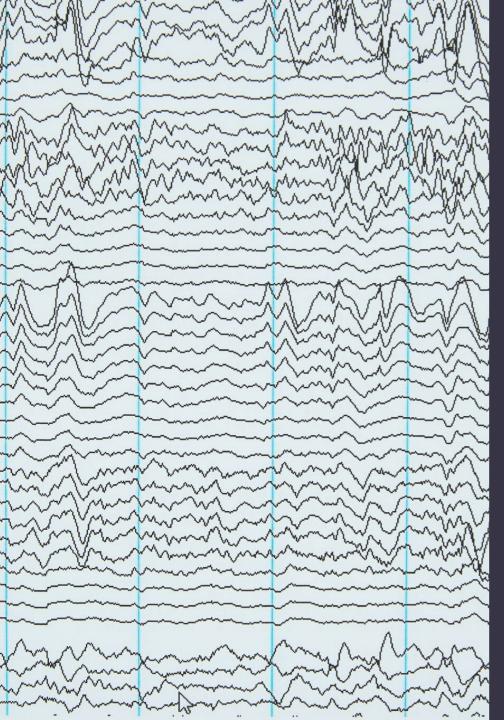
- Variance Threshold
- Chi-squared test (χ2)
- Information Gain
- Correlation Coefficient

Wrapper Methods

- ***Concept:** Use a specific machine learning algorithm to evaluate the performance of different subsets of features.
- •Pros: Account for model bias, often yield better predictive accuracy.
- *Cons: Computationally intensive, prone to overfitting to the specific model.
- **•**Examples:
- Forward Selection
- Backward Elimination
- Recursive Feature Elimination (RFE)

Embedded Methods

- •Concept: Feature selection is integrated into the model training process itself.
- Pros: Less computationally expensive than wrappers, considers feature interactions.
- **•Cons:** Method-dependent.
- •Examples:
 - Lasso Regression (L1 regularization)
 - Ridge Regression (L2 regularization)
 - Decision Trees (feature importance)



Principal Component Analysis (PCA)

•Definition: A statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components.

*Goal:

- •Reduce dimensionality while retaining as much variance as possible.
- Visualize high-dimensional data.
- Remove noise from data.
- Pre-processing for other machine learning algorithms.

How PCA Works (Simplified)

The Core Steps

- 1. Standardize the Data: Ensure all features contribute equally by scaling them.
- 2. Calculate the Covariance Matrix: Understand how features vary with respect to each other.
- **3.Compute Eigenvectors and Eigenvalues:**
 - 1. **Eigenvectors:** Represent the directions (principal components) of maximum variance.
 - **2. Eigenvalues:** Indicate the magnitude of variance along each eigenvector.
- **4.Sort Eigenvalues:** Order principal components by their explained variance (from highest to lowest).
- **5.Select Principal Components:** Choose the top 'k' eigenvectors that capture a significant amount of variance.
- **6.Transform the Data:** Project the original data onto the new subspace defined by the selected principal components.



PCA- Key Concepts

Principal Components

- New variables that are linear combinations of the original variables.
- Orthogonal (uncorrelated) to each other.
- •The first principal component accounts for the largest possible variance, and each succeeding component accounts for the highest remaining variance.

Explained Variance Ratio

- Indicates the proportion of variance in the original data that is captured by each principal component.
- Helps in determining the optimal number of components to retain.