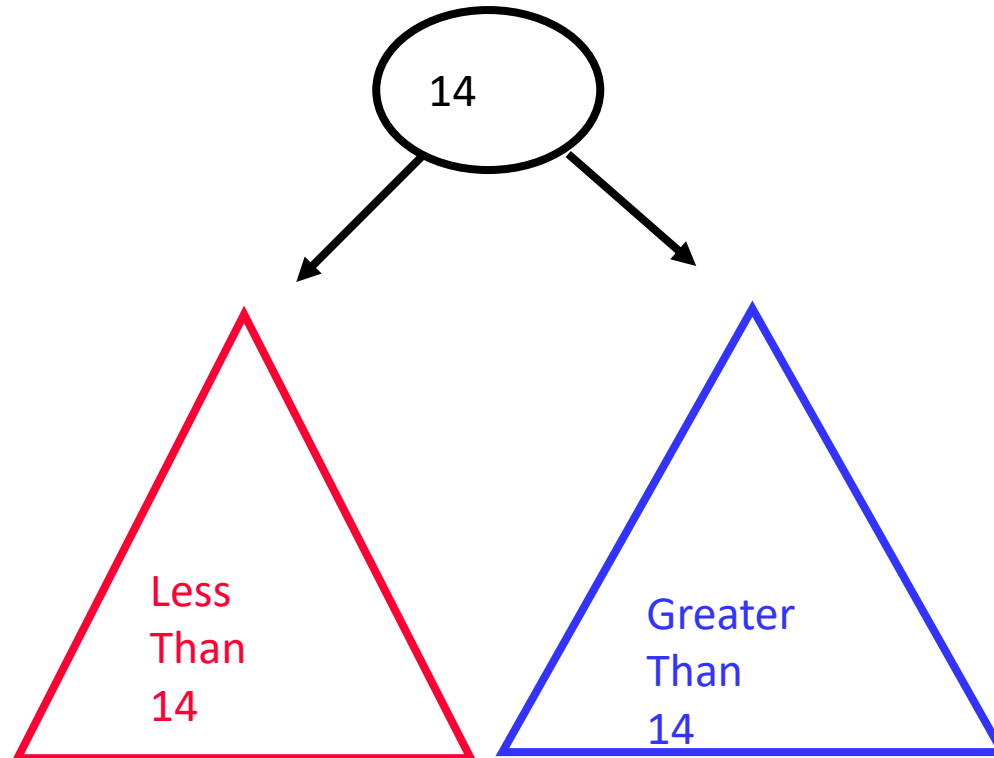


SEARCH A NODE

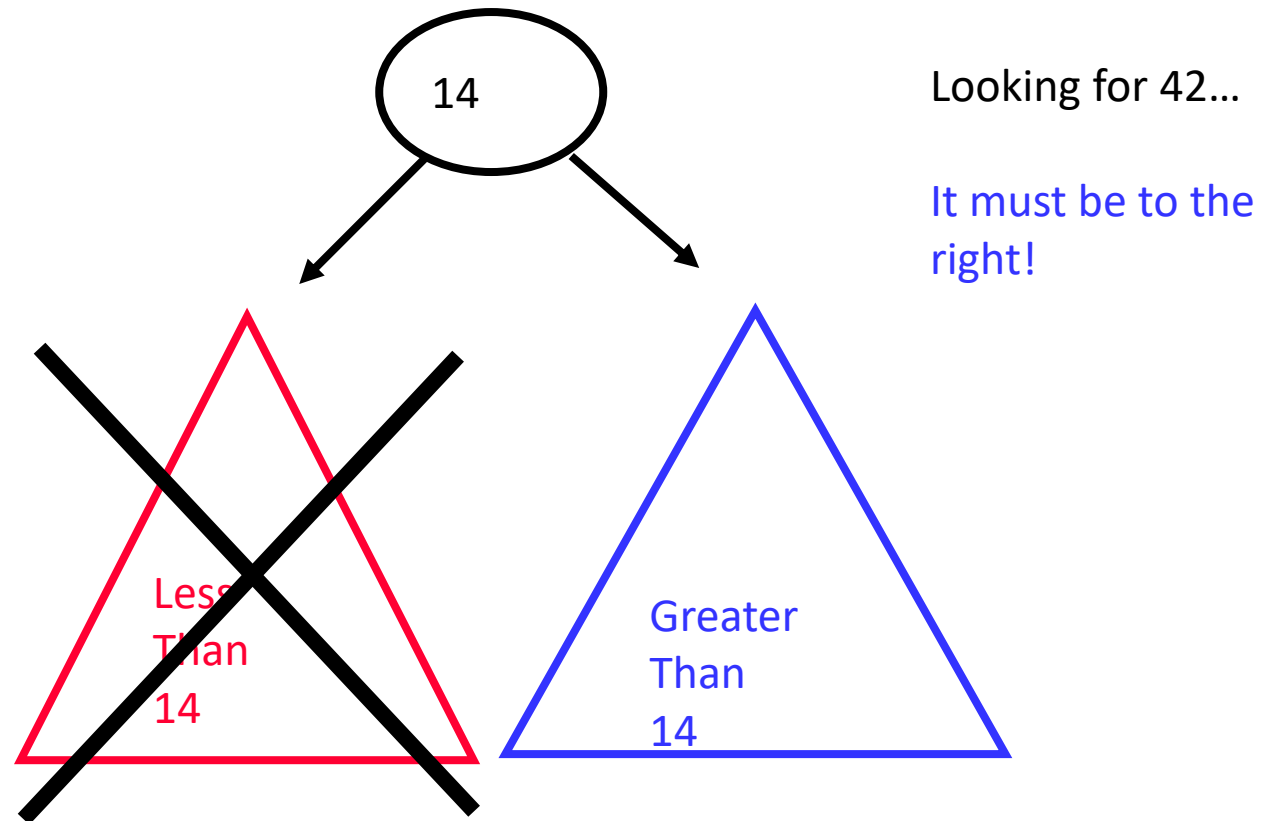
Search a Node

- **We've got a Binary Search Tree and we want to determine if an element is in the collection.**



Cutting the Work in Half

- In searching for a match, we can ignore half of the tree at each comparison.



The Binary Search Algorithm

```
if at NIL // not found
    DO NOT FOUND WORK
elseif ( match ) then // found
    DO FOUND WORK
elseif ( value to match < current value )
    recurse left // must be to left
else
    recurse right // must be to right
```

The Binary Search for a BST

```
procedure Search(cur iot in Ptr to a
Node,
                target isotype in Num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search
```

•

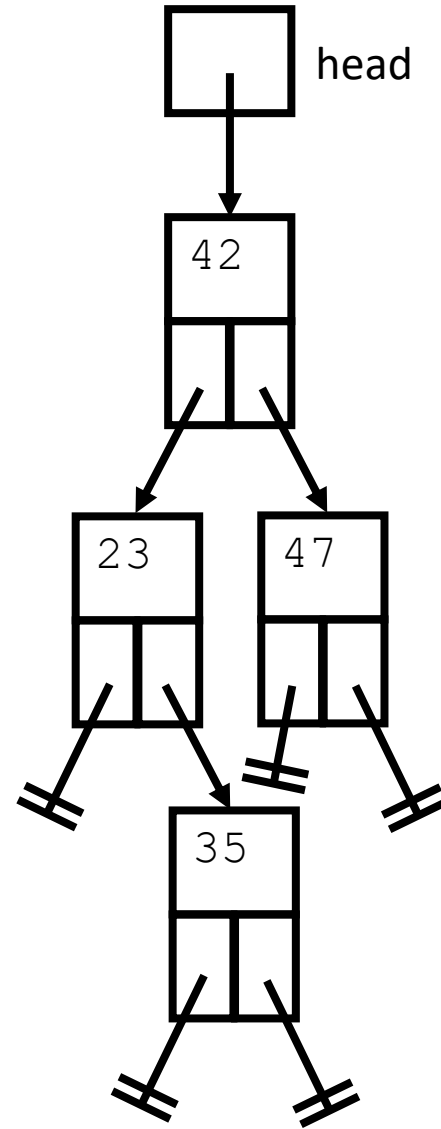
•

Search(head, 35)

Search(head, 87)

•

•



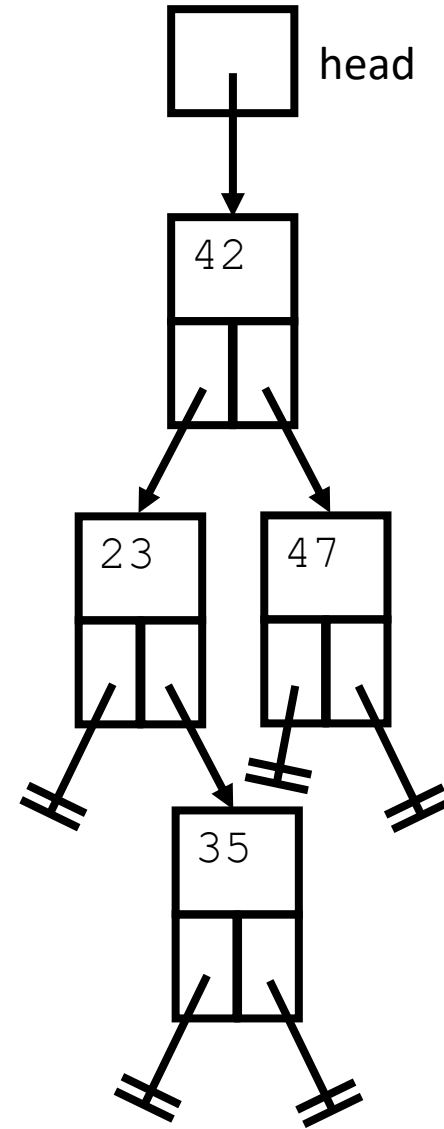
-
-

`Search(head, 35)`

`Search(head, 87)`

-

-

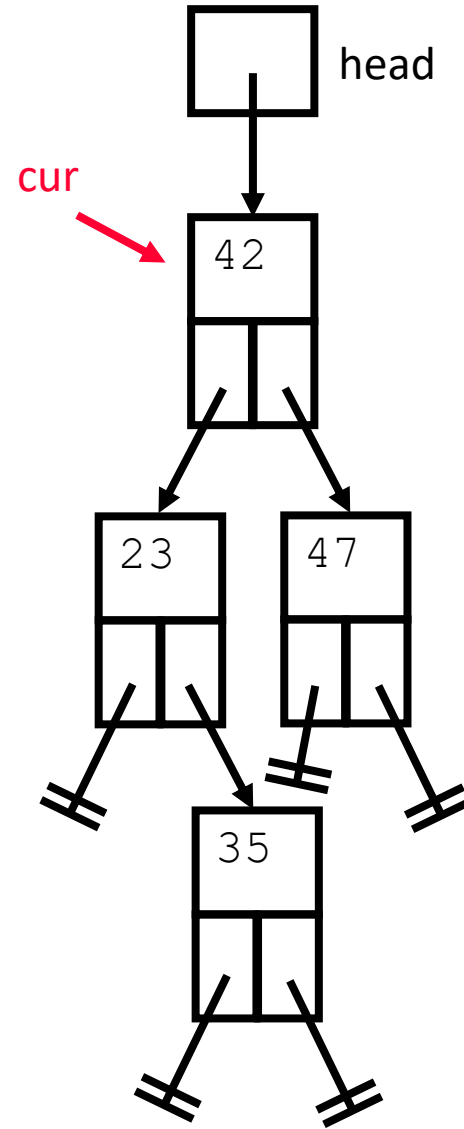


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search

```

target = 35

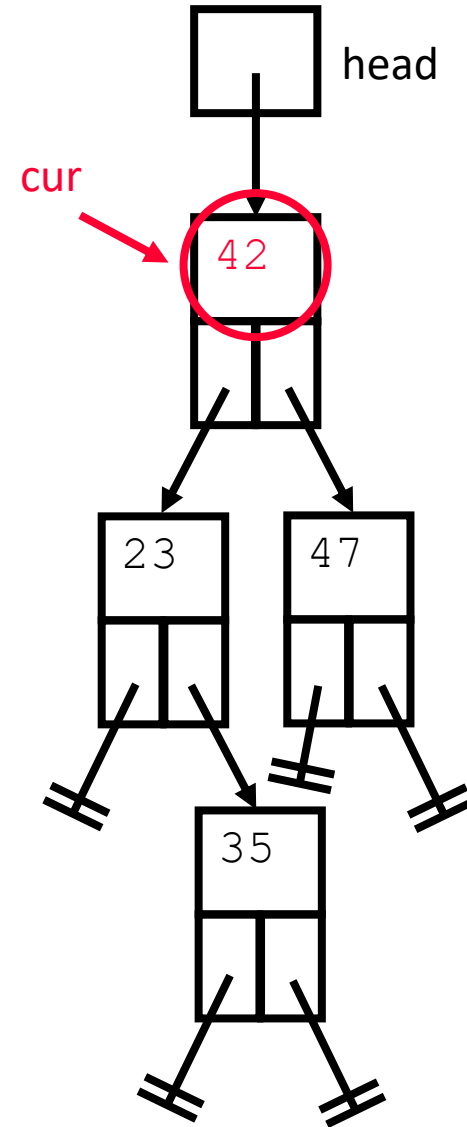



```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

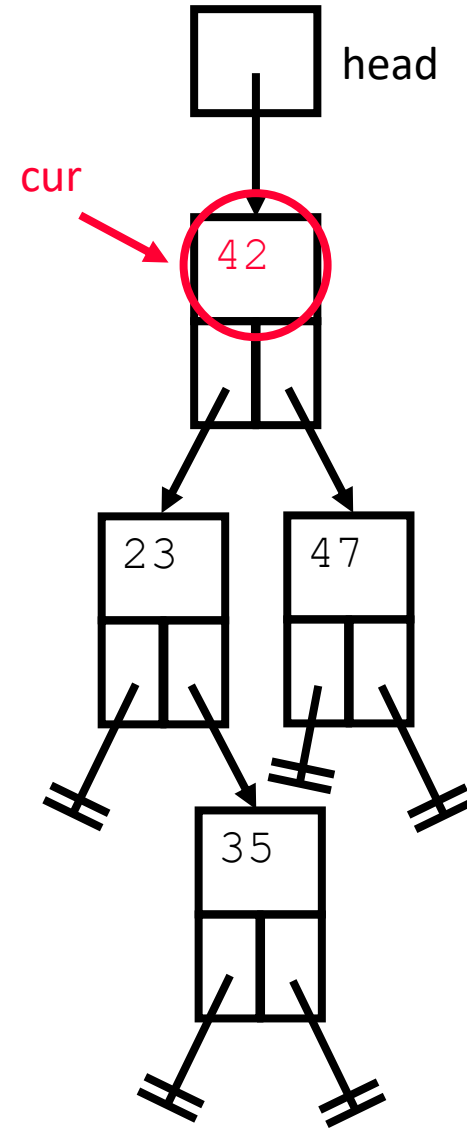
```

target = 35



```
Procedure Search(  
  cur iot in Ptr to a Node,  
  target iot in num)  
  if (cur = NIL) then  
    print("Not Found")  
  elseif (cur^.data = target)  
    print("Target Found")  
  elseif (cur^.data > target)  
    Search(cur^.left, target)  
  else  
    Search(cur^.right, target)  
  endif  
endprocedure // Search
```

target = 35

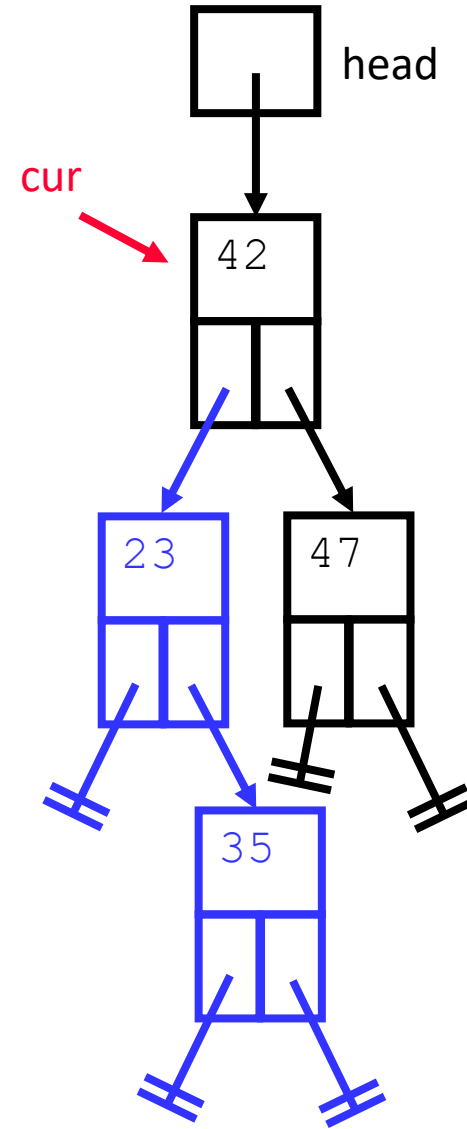


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 35

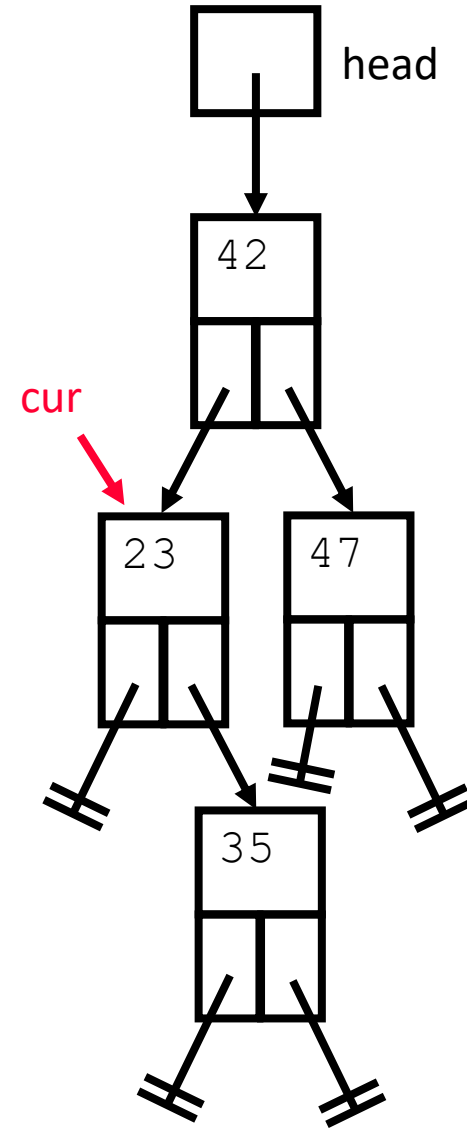


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search

```

target = 35

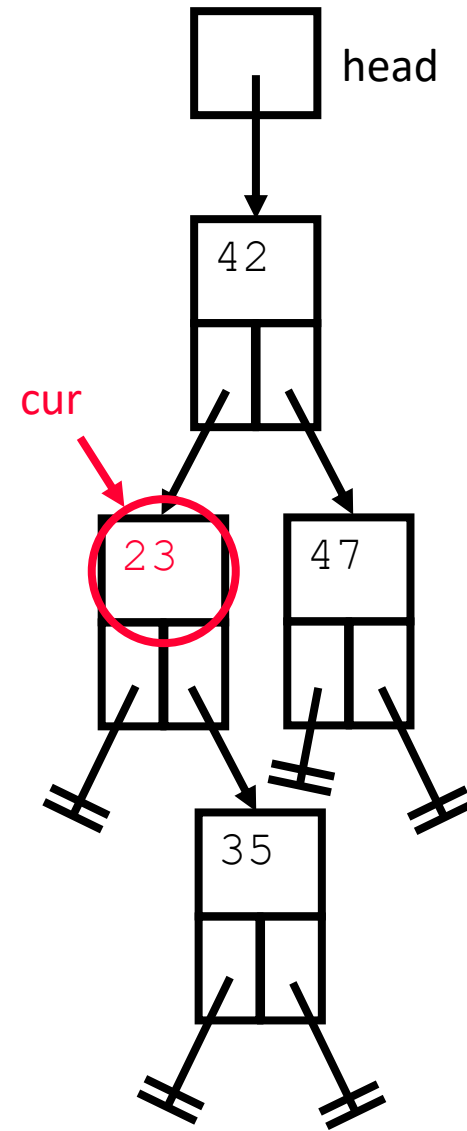


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if(cur = NIL) then
  print("Not Found")
elseif(cur^.data = target)
  print("Target Found")
elseif(cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 35

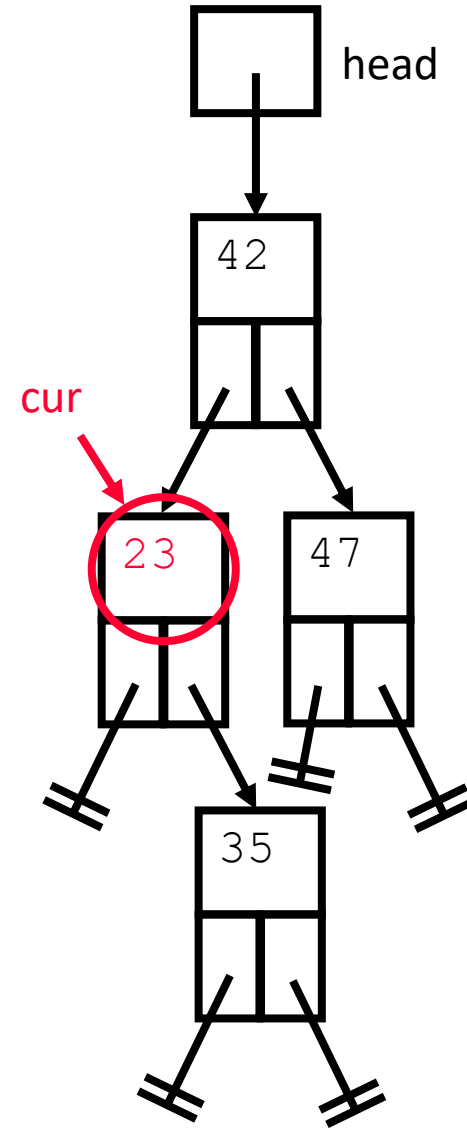


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 35

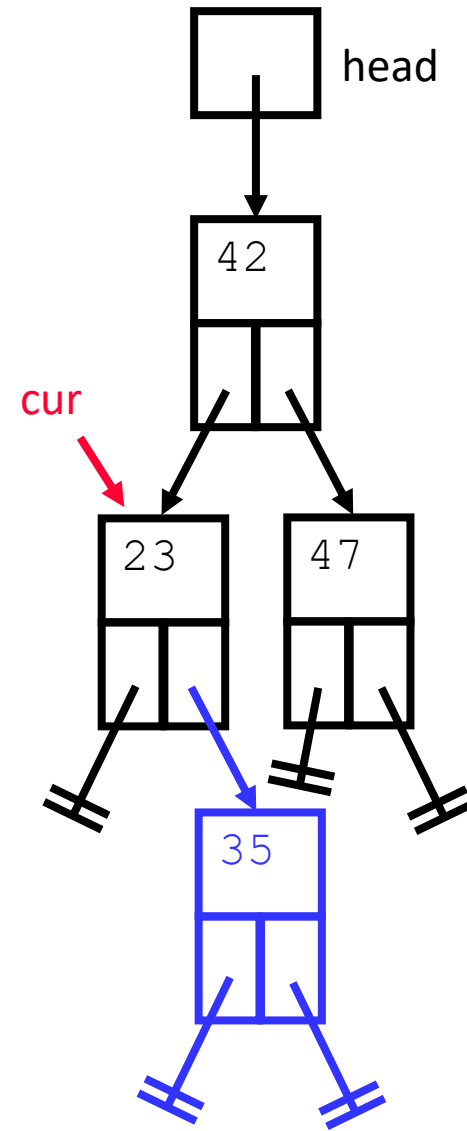


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 35

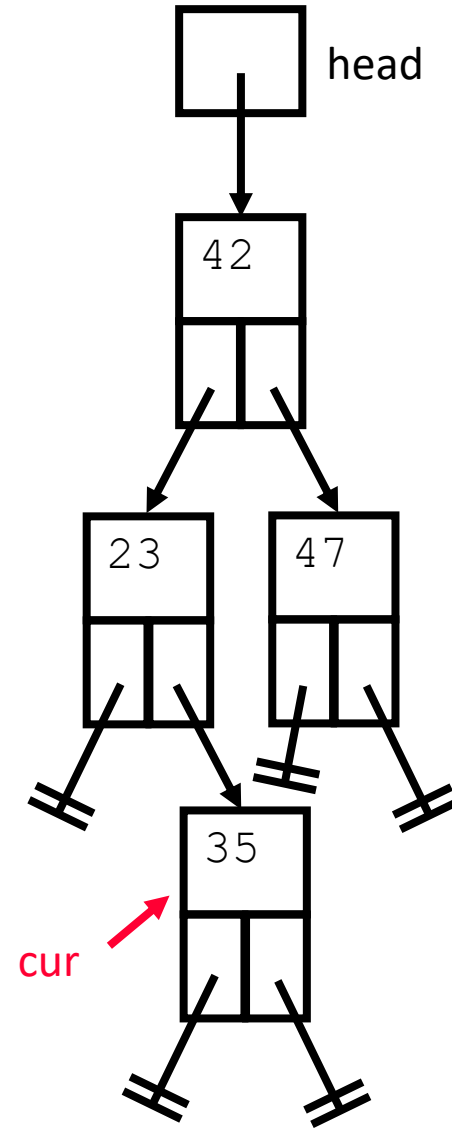


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search

```

target = 35

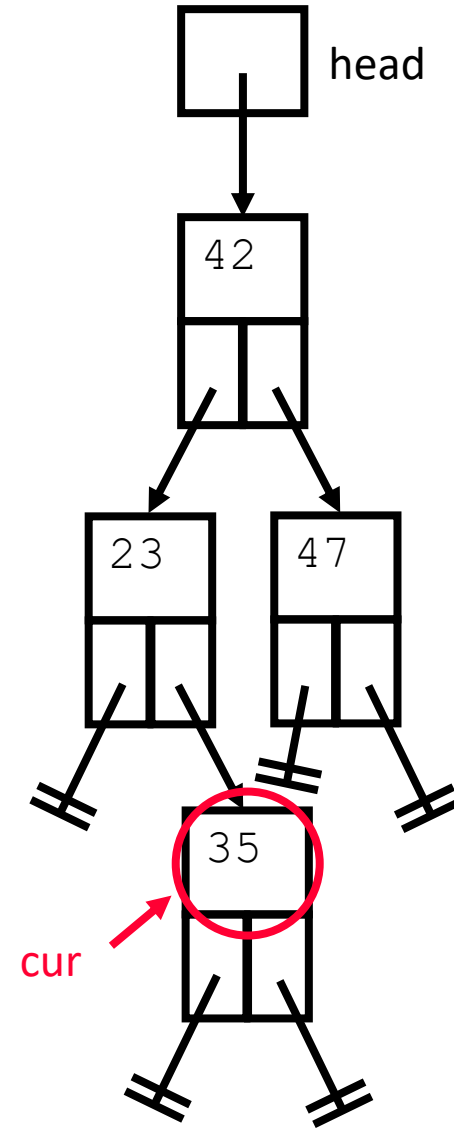



```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

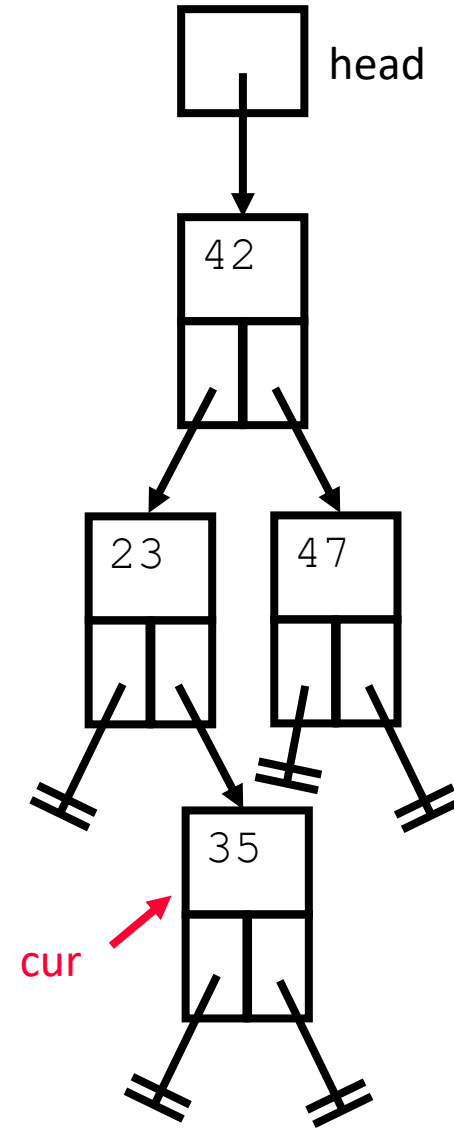
target = 35




```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if(cur = NIL) then
  print("Not Found")
elseif(cur^.data = target)
  print("Target Found")
elseif(cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

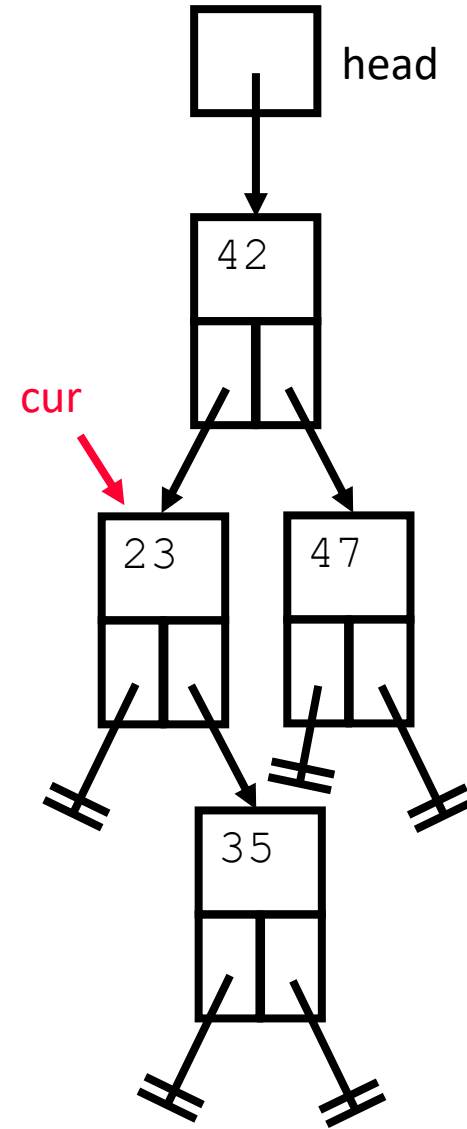
```



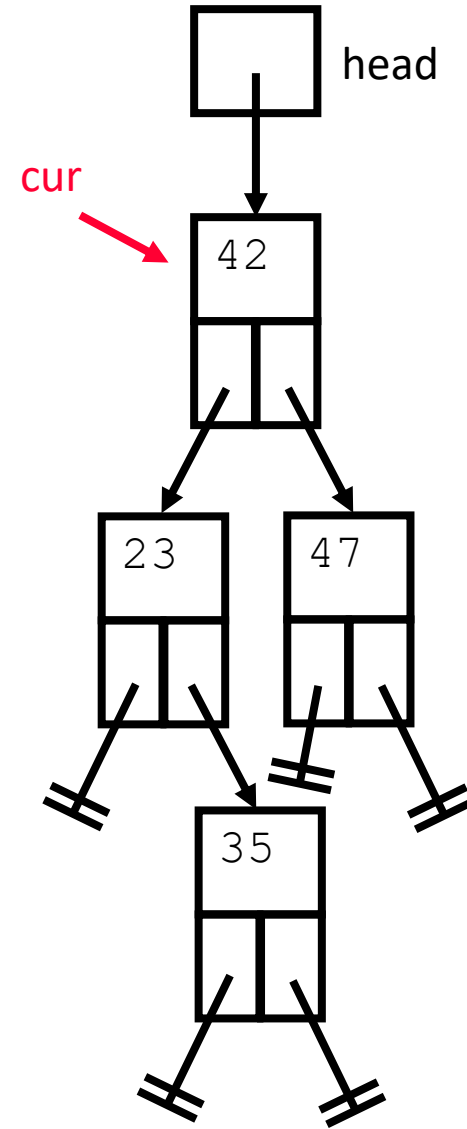
```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

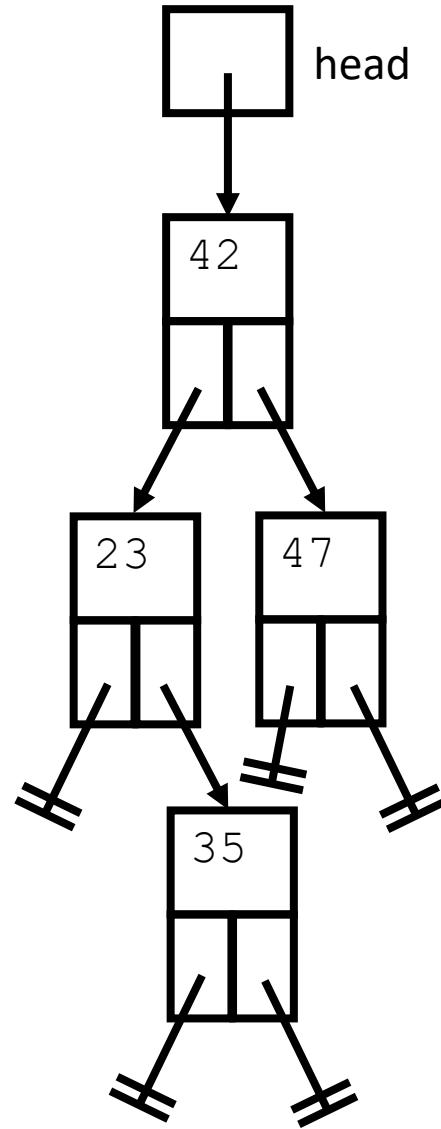
```



```
Procedure Search(  
  cur iot in Ptr to a Node,  
  target iot in num)  
  if (cur = NIL) then  
    print("Not Found")  
  elseif (cur^.data = target)  
    print("Target Found")  
  elseif (cur^.data > target)  
    Search(cur^.left, target)  
  else  
    Search(cur^.right, target)  
  endif  
endprocedure // Search
```

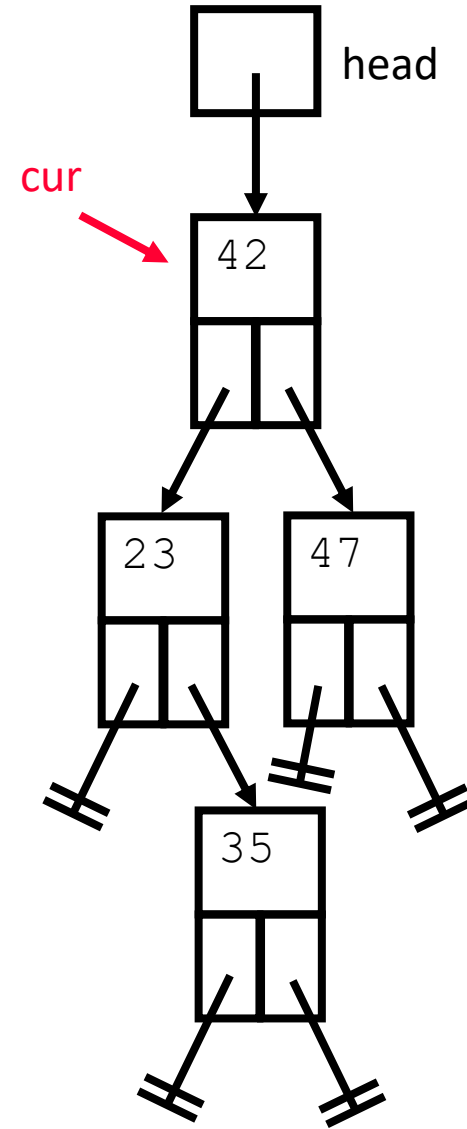


•
•
Search(head, 35)
Search(head, 87)
•
•



```
Procedure Search(  
  cur iot in Ptr to a Node,  
  target iot in num)  
  if (cur = NIL) then  
    print("Not Found")  
  elseif (cur^.data = target)  
    print("Target Found")  
  elseif (cur^.data > target)  
    Search(cur^.left, target)  
  else  
    Search(cur^.right, target)  
  endif  
endprocedure // Search
```

target = 87

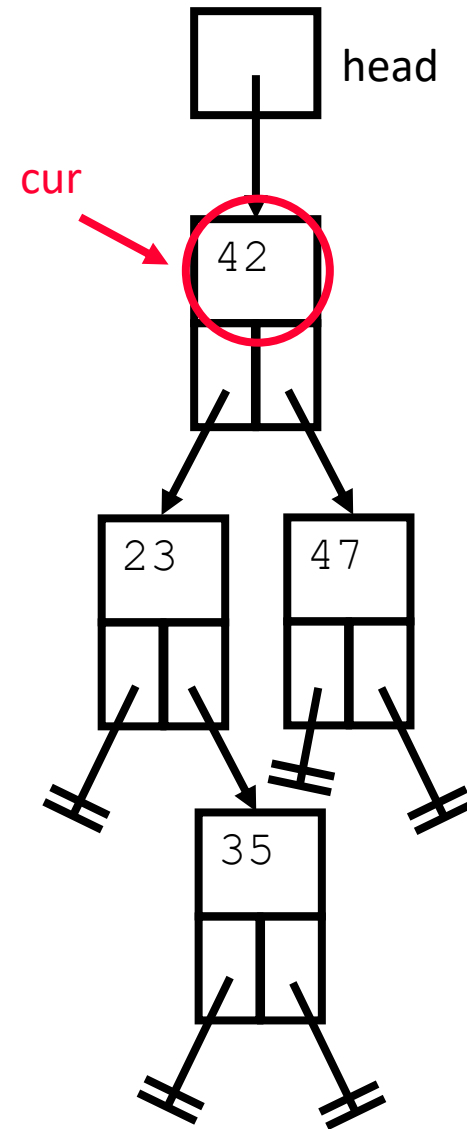


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

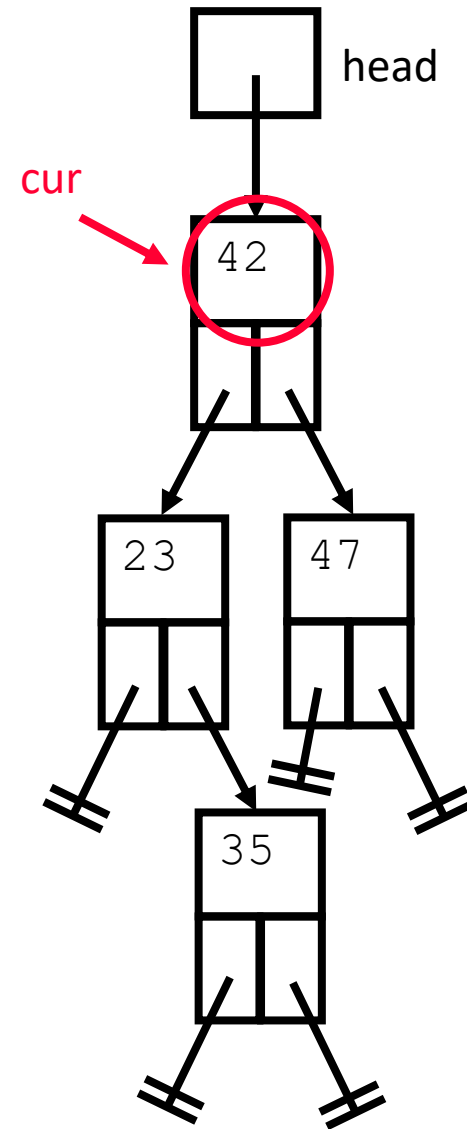
```

target = 87




```
Procedure Search(  
  cur iot in Ptr to a Node,  
  target iot in num)  
  if (cur = NIL) then  
    print("Not Found")  
  elseif (cur^.data = target)  
    print("Target Found")  
  elseif (cur^.data > target)  
    Search(cur^.left, target)  
  else  
    Search(cur^.right, target)  
  endif  
endprocedure // Search
```

target = 87

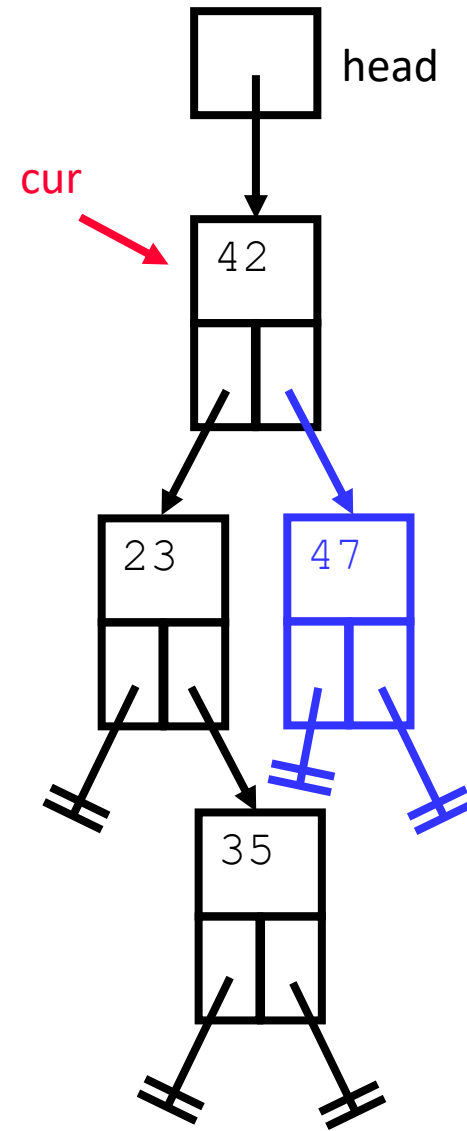


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 87

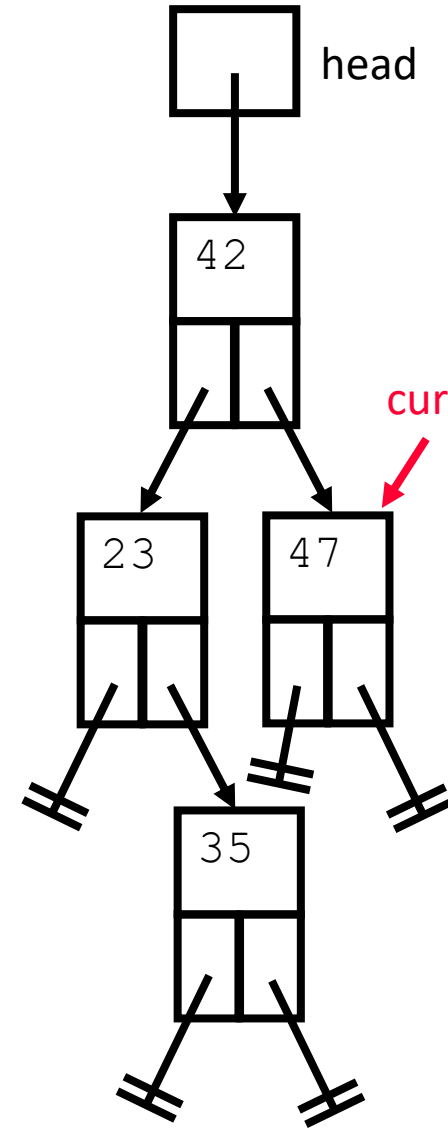


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search

```

target = 87

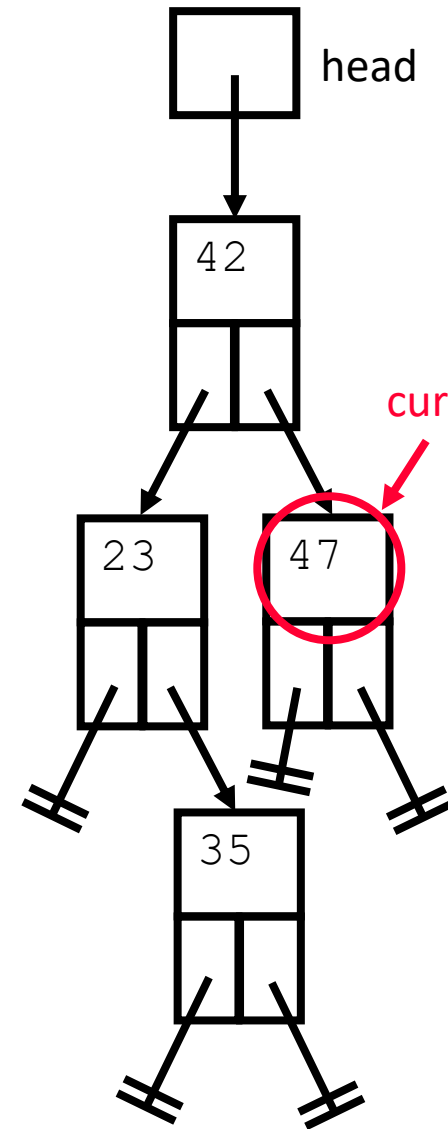


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if(cur = NIL) then
  print("Not Found")
elseif(cur^.data = target)
  print("Target Found")
elseif(cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 87

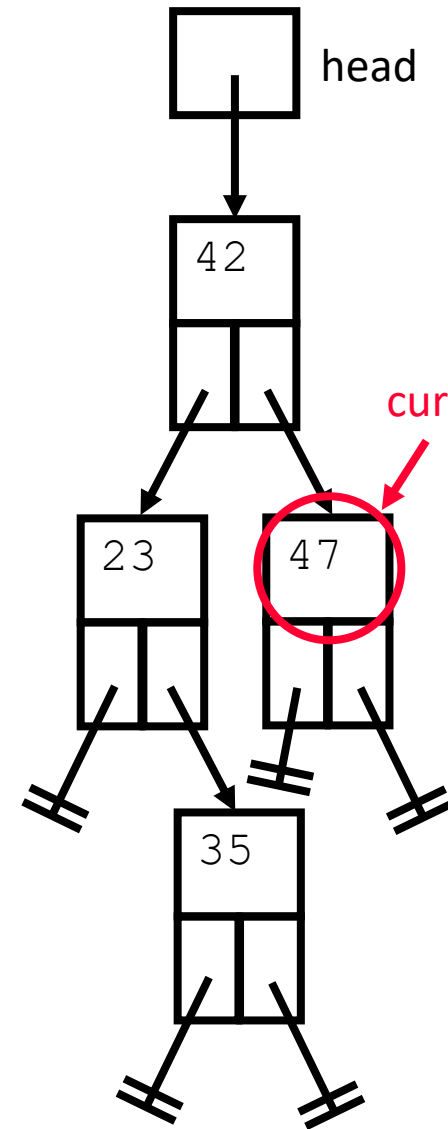


```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```

target = 87

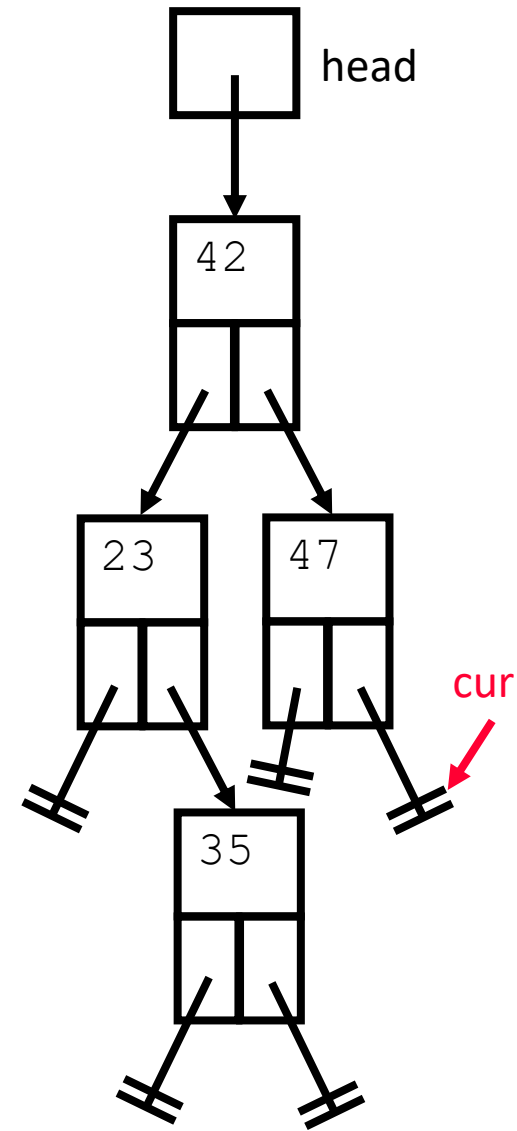



```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
  if(cur = NIL) then
    print("Not Found")
  elseif(cur^.data = target)
    print("Target Found")
  elseif(cur^.data > target)
    Search(cur^.left, target)
  else
    Search(cur^.right, target)
  endif
endprocedure // Search

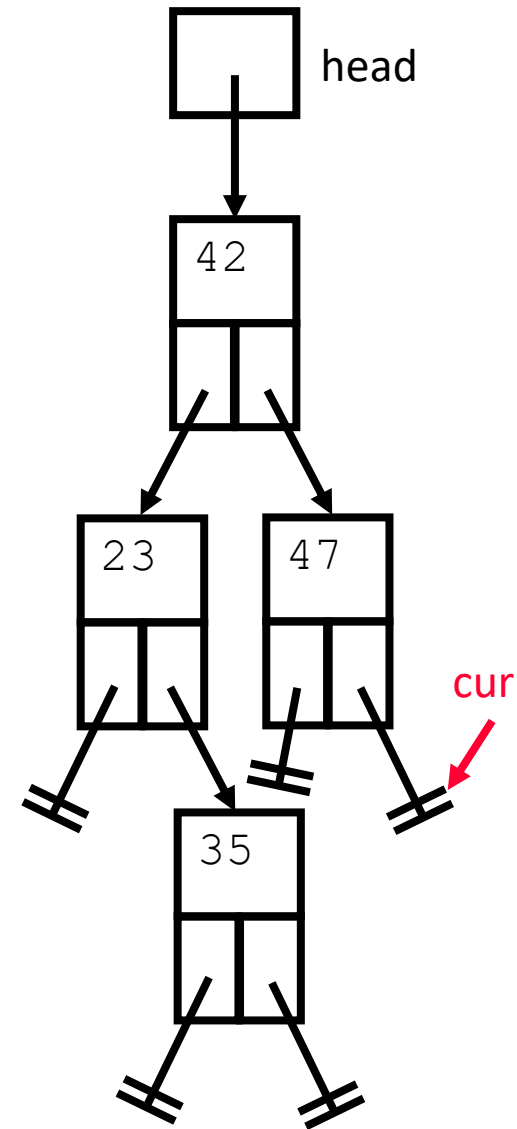
```

target = 87



```
Procedure Search(  
  cur iot in Ptr to a Node,  
  target iot in num)  
  if (cur = NIL) then  
    print("Not Found")  
  elseif (cur^.data = target)  
    print("Target Found")  
  elseif (cur^.data > target)  
    Search(cur^.left, target)  
  else  
    Search(cur^.right, target)  
  endif  
endprocedure // Search
```

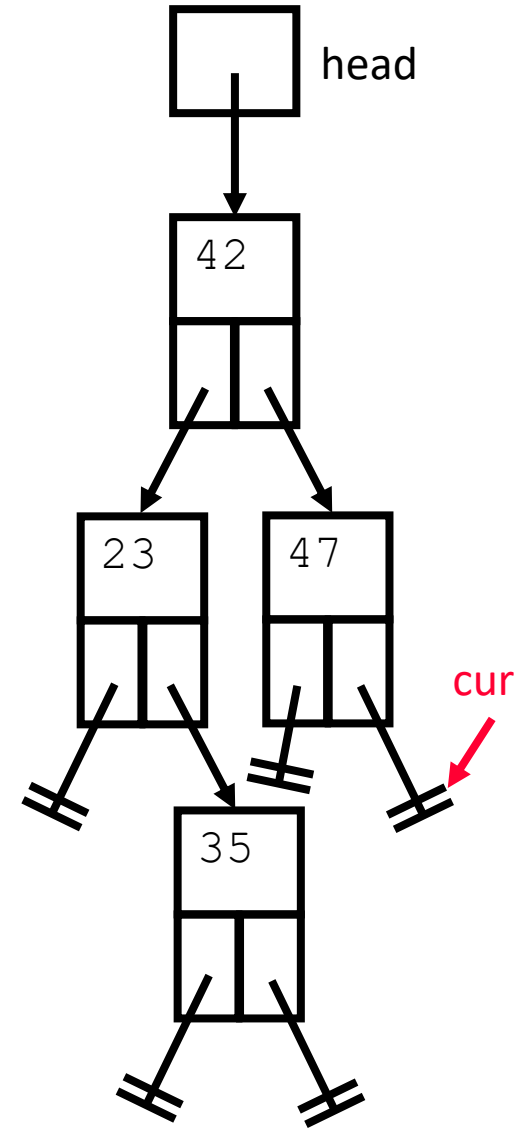
Not Found




```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if(cur = NIL) then
  print("Not Found")
elseif(cur^.data = target)
  print("Target Found")
elseif(cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

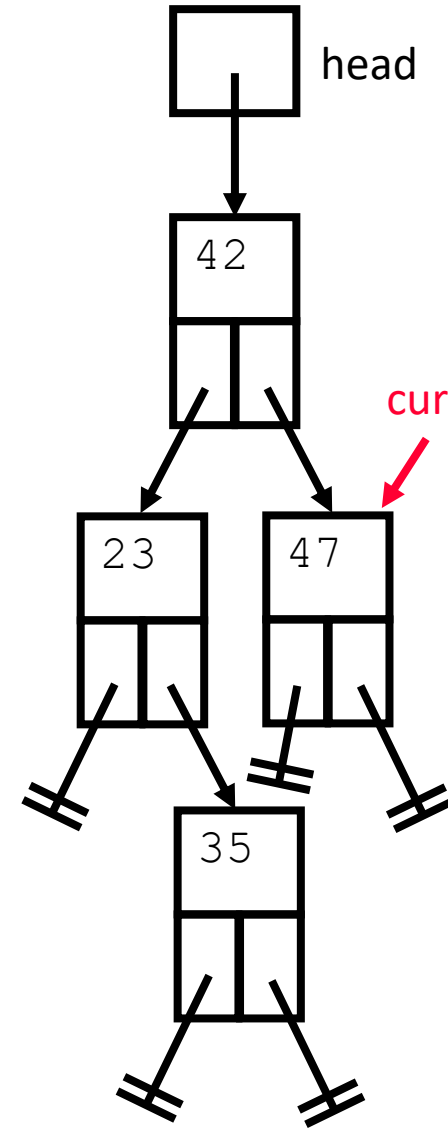
```



```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if(cur = NIL) then
  print("Not Found")
elseif(cur^.data = target)
  print("Target Found")
elseif(cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

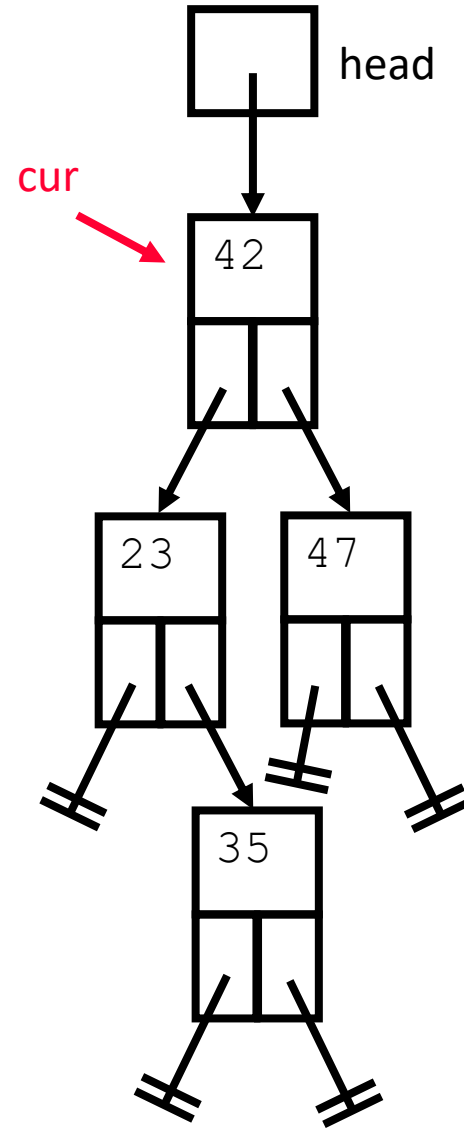
```



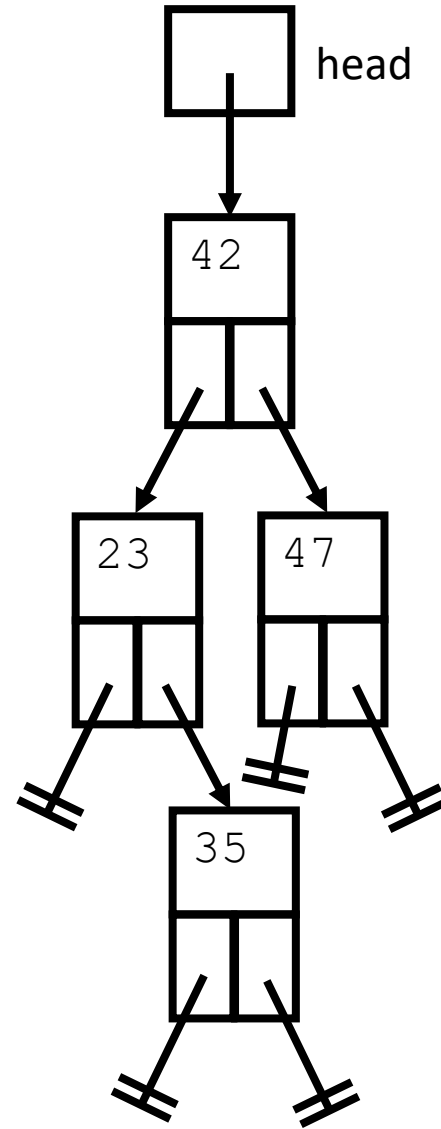
```

Procedure Search(
  cur iot in Ptr to a Node,
  target iot in num)
if (cur = NIL) then
  print("Not Found")
elseif (cur^.data = target)
  print("Target Found")
elseif (cur^.data > target)
  Search(cur^.left, target)
else
  Search(cur^.right, target)
endif
endprocedure // Search

```



```
•  
•  
Search(head, 35)  
Search(head, 87)  
•  
•
```



Summary

- We can **cut the work in half** after each comparison.
- **Recurse in one direction – left or right.**
- When we reach NIL, then we no the value wasn't in the binary search tree.

ADDING A NODE

Adding the Node

- **Current is an in/out pointer**
 - We need information IN to evaluate current
 - We need to send information OUT because we're changing the tree (adding a node)
- **Once we've found the correct location:**
 - Create a new node
 - Fill in the data field
(with the new value to add)
 - Make the left and right pointers point to nil (to cleanly terminate the tree)

Adding the Node

```
current <- new(Node)
current^.data <- value_to_add
current^.left <- nil
current^.right <- nil
```


The Entire Module

```
procedure Insert(cur iot in/out Ptr toa Node,  
                data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

Tracing Example

The following example shows a trace of the BST insert.

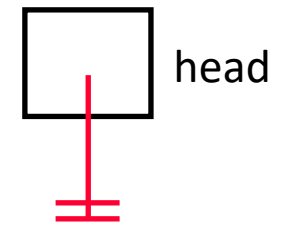
- **Begin with an empty BST (a pointer)**
- **Add elements 42, 23, 35, 47 in the correct positions.**

```
Head iot Ptr toa Node  
head <- NIL  
Insert(head, 42)
```

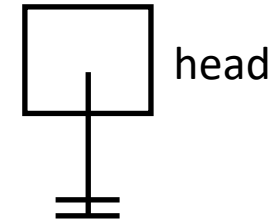
```
Head iot Ptr toa Node  
head <- NIL  
Insert(head, 42)
```



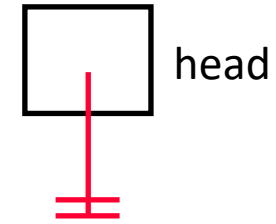
```
Head iot Ptr toa Node  
head <- NIL  
Insert(head, 42)
```



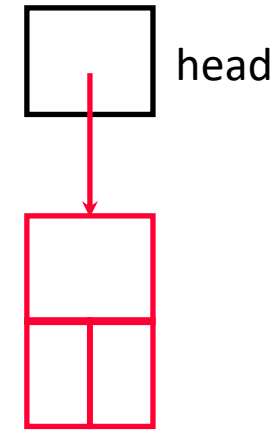
```
Head iot Ptr toa Node  
head <- NIL  
Insert(head, 42)
```



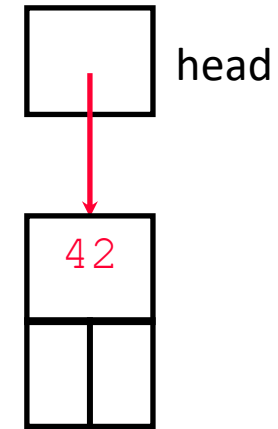
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```



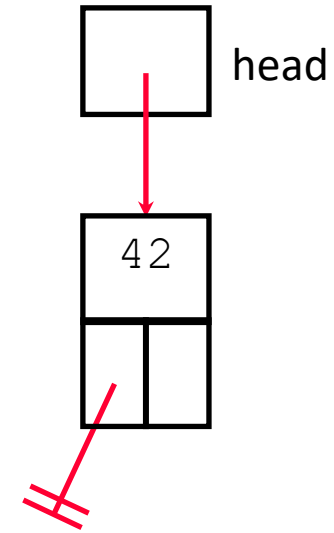
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```




```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```



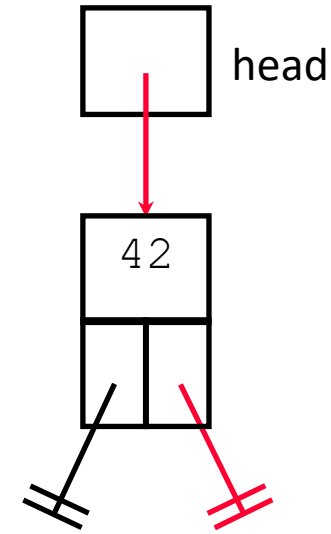
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```



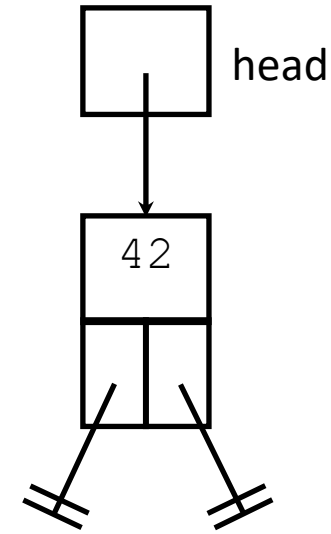
```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

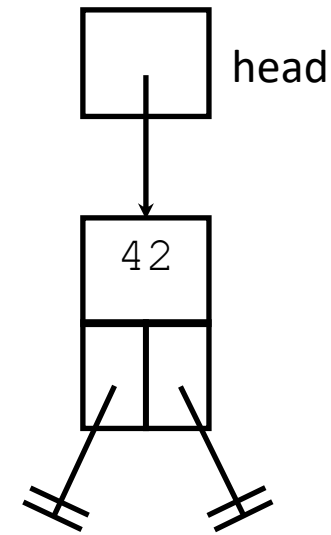
```



```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

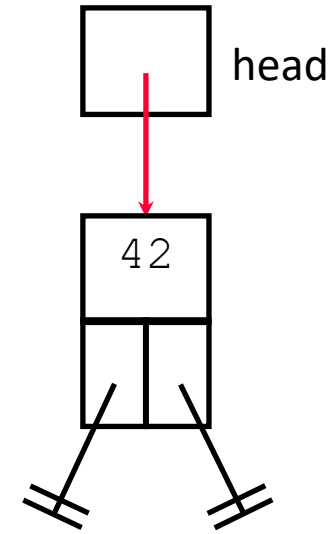


```
•  
•  
Insert(head, 23)  
Insert(head, 35)  
Insert(head, 47)  
•  
•
```



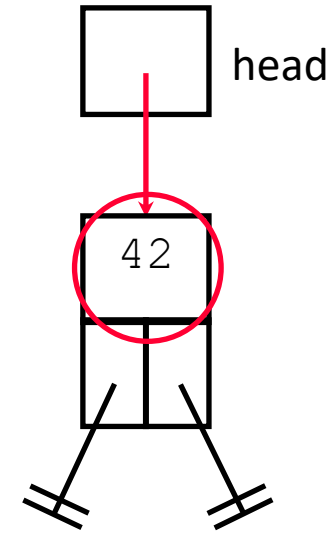
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23



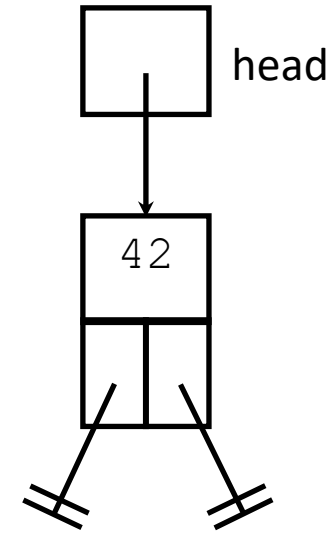
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23



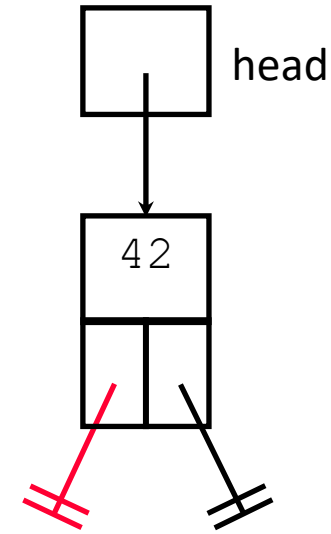
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23




```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23

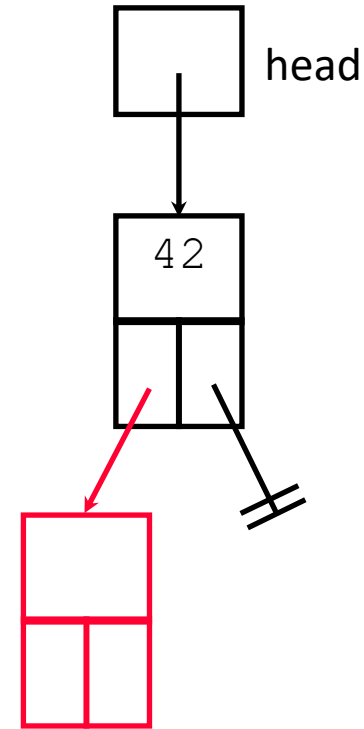


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

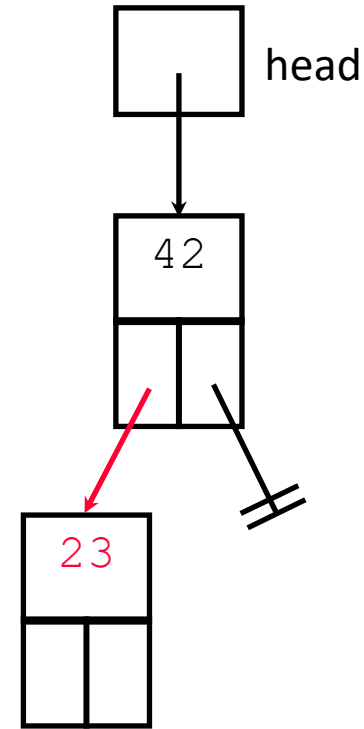
```

data_in = 23



```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23

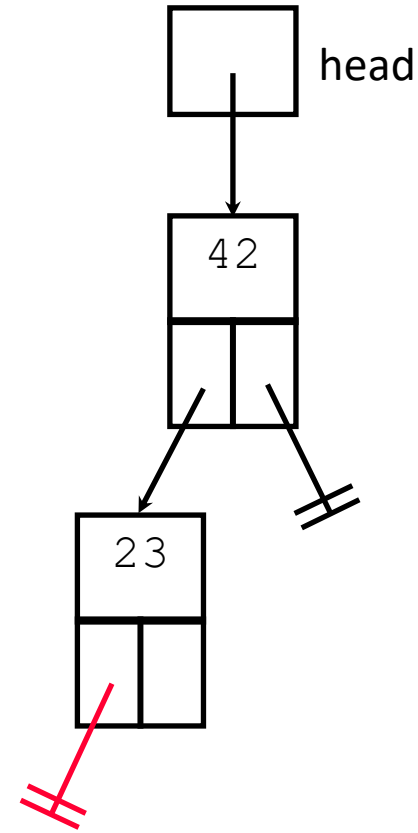


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 23

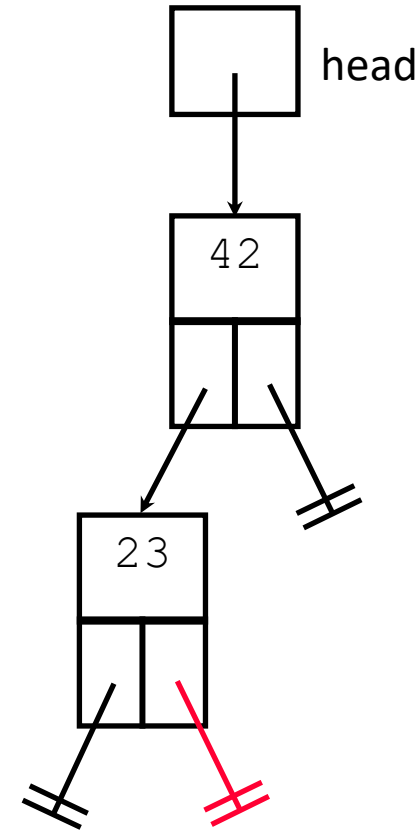


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

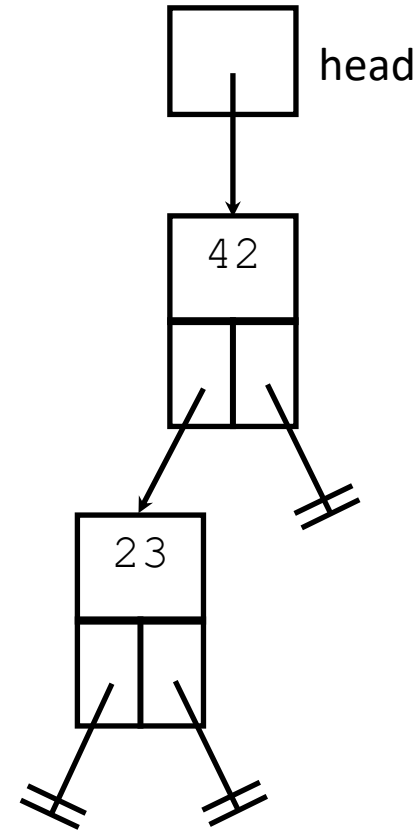
```

data_in = 23



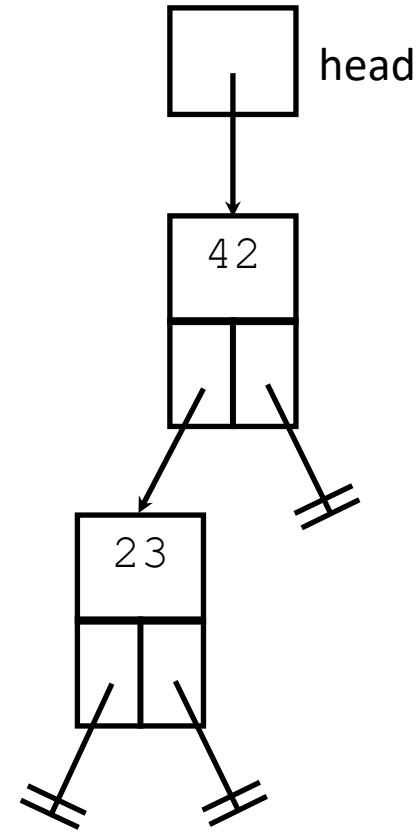
```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23

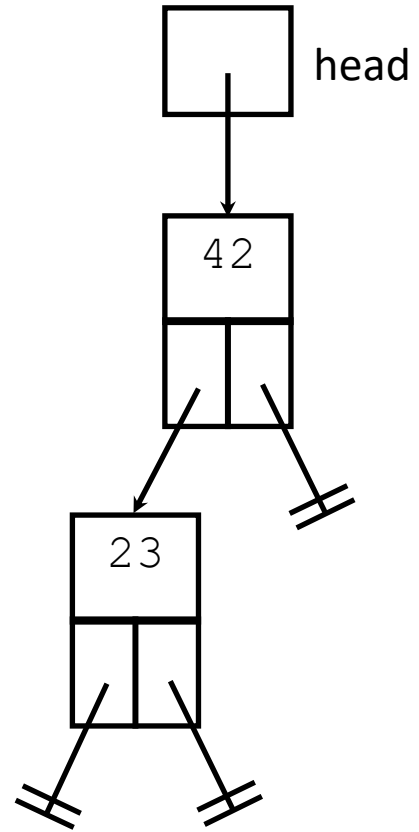


```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 23

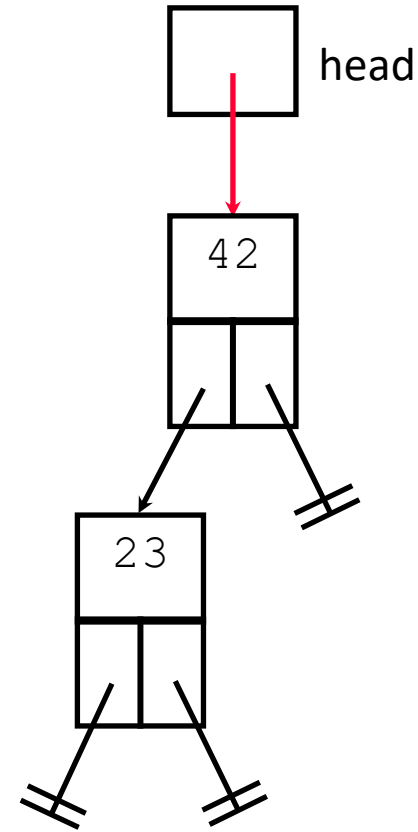


```
•  
•  
Insert(head, 23)  
Insert(head, 35)  
Insert(head, 47)  
•  
•
```




```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

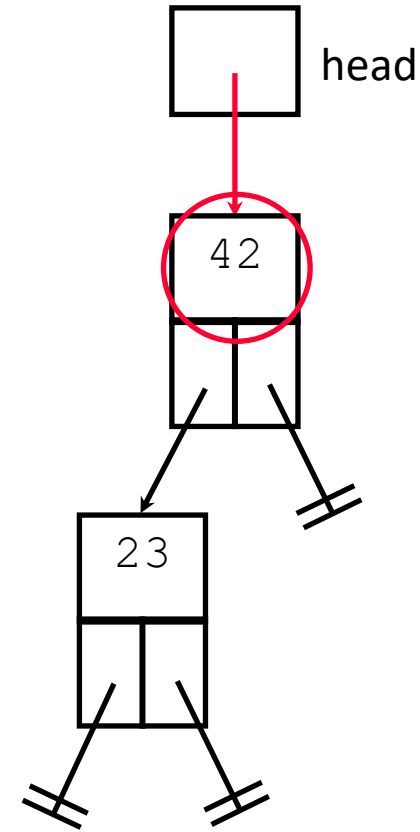
data_in = 35



```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```



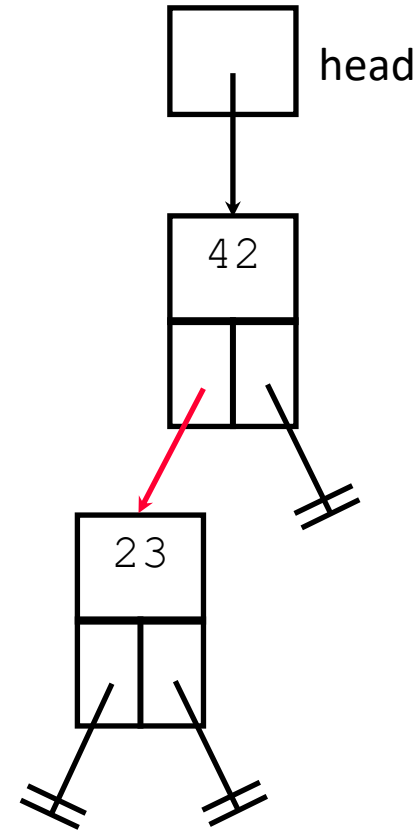
data_in = 35

```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 35

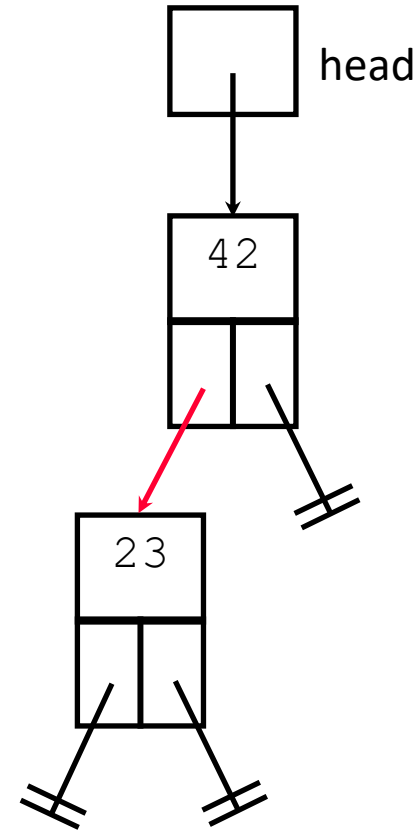


```

procedure Insert(
  cur iot in/out Ptr to a Node,
  data_in iot in num)
  if(cur = NIL) then
    cur <- new(Node)
    cur^.data <- data_in
    cur^.left <- NIL
    cur^.right <- NIL
  elseif(cur^.data > data_in)
    Insert(cur^.left, data_in)
  else
    Insert(cur^.right, data_in)
  endif
endprocedure // Insert

```

data_in = 35

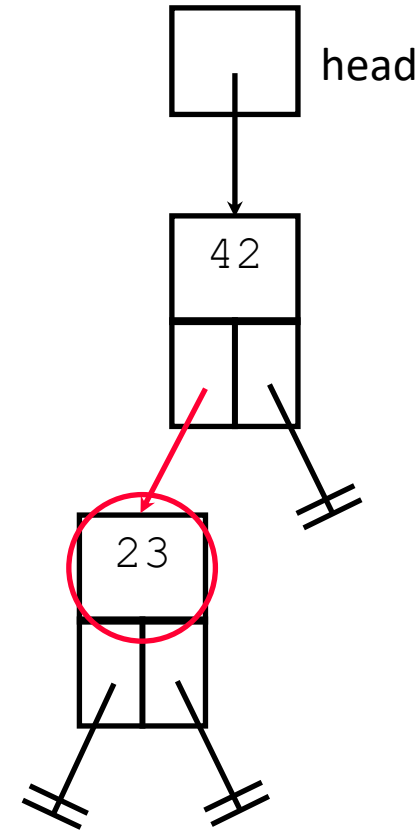


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 35

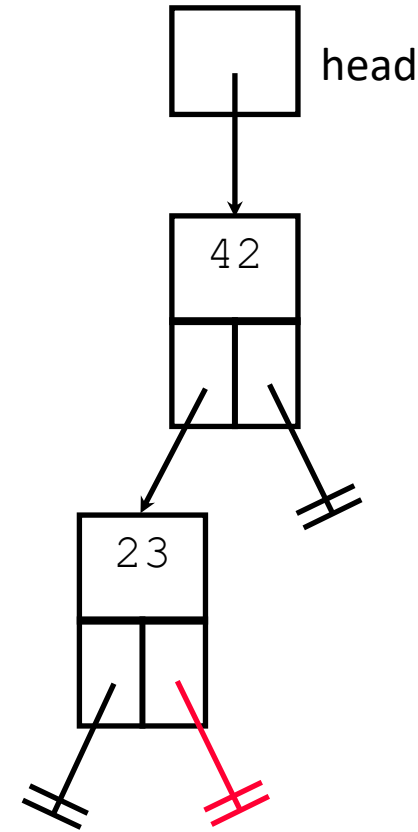


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

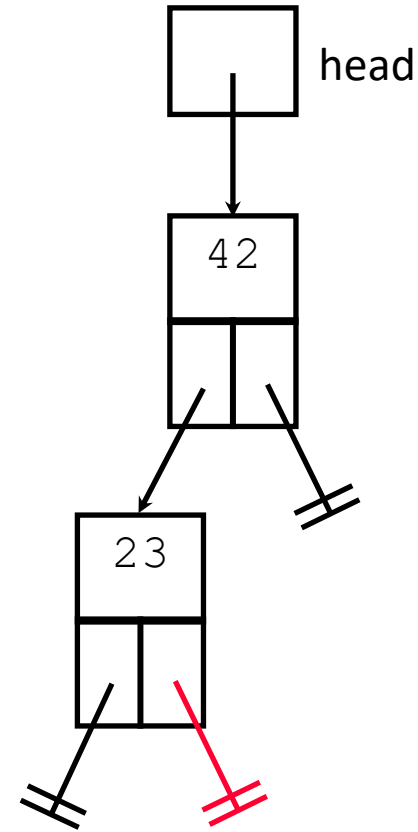
```

data_in = 35



```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 35

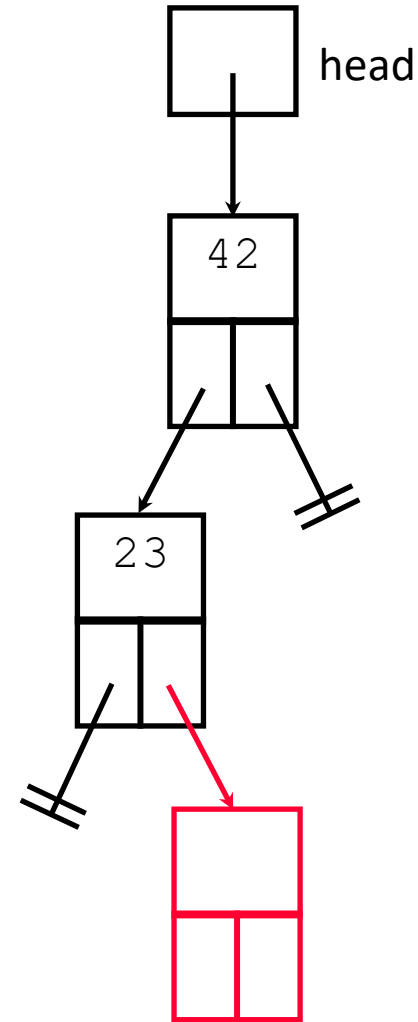


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

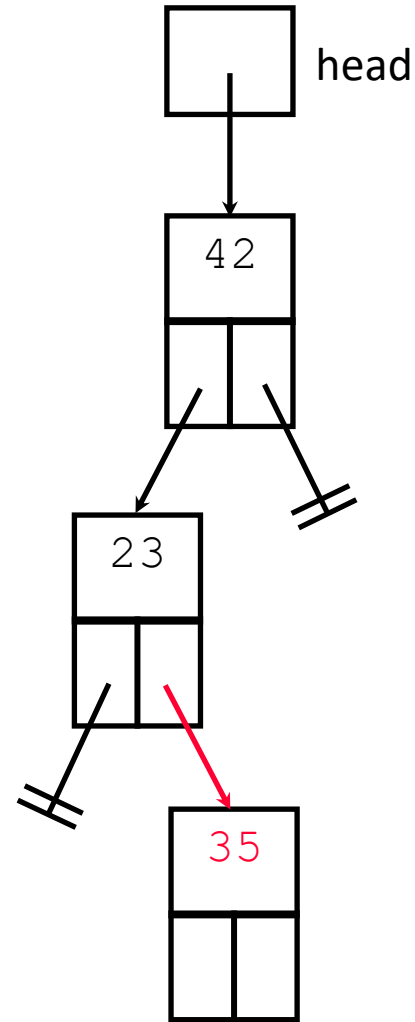
```

data_in = 35




```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if (cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif (cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 35

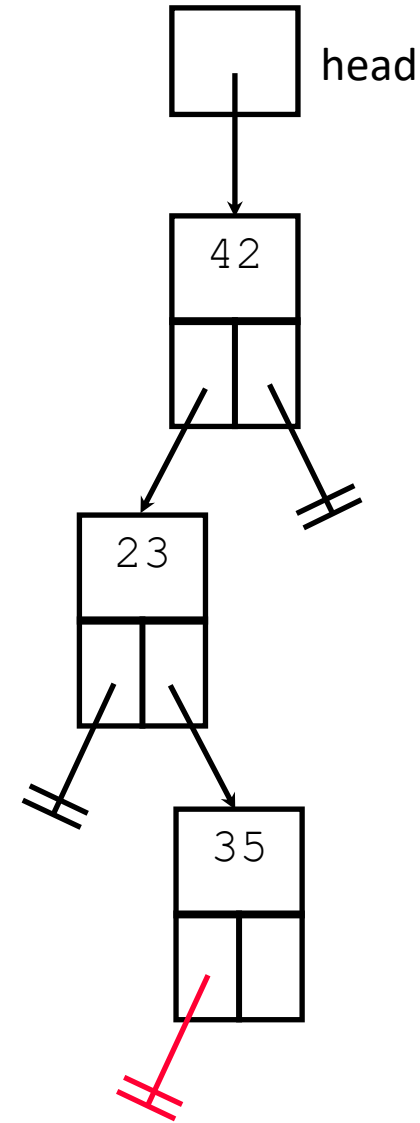


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 35

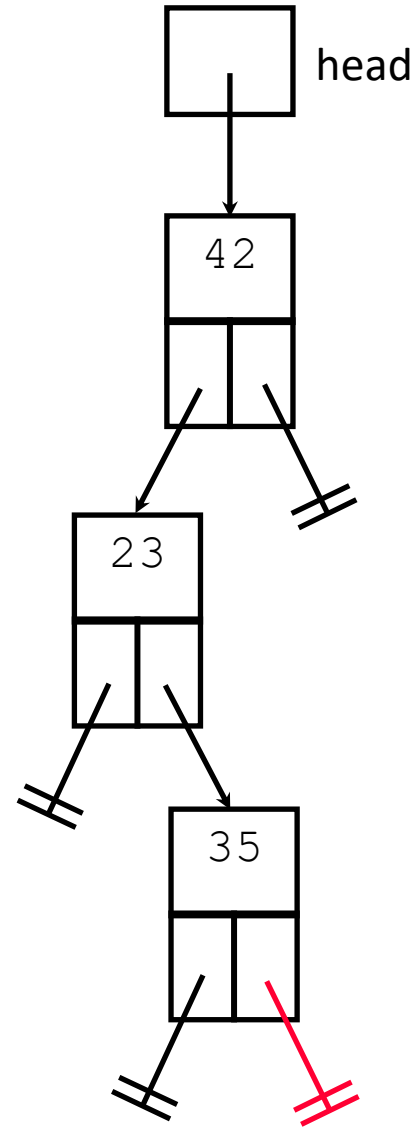


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

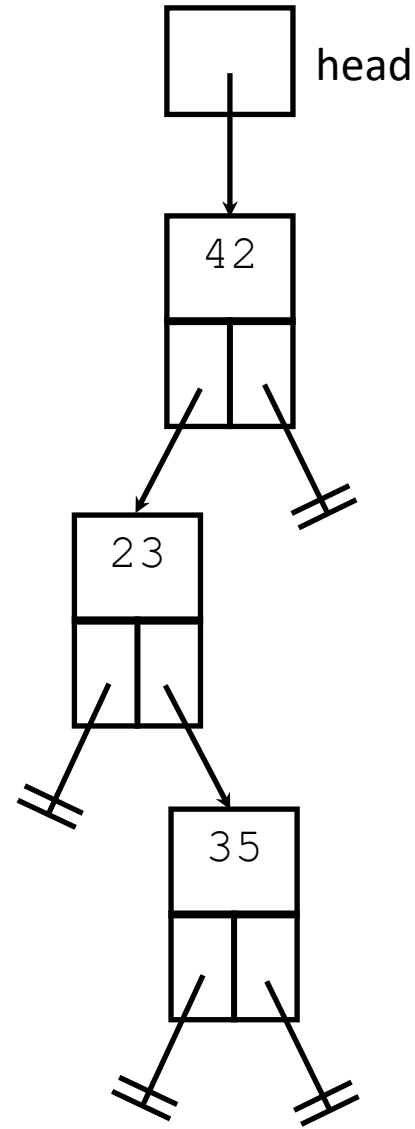
```

data_in = 35



```
procedure Insert(  
  cur iot in/out Ptr toa Node,  
  data_in iot in num)  
  if(cur = NIL) then  
    cur <- new(Node)  
    cur^.data <- data_in  
    cur^.left <- NIL  
    cur^.right <- NIL  
  elseif(cur^.data > data_in)  
    Insert(cur^.left, data_in)  
  else  
    Insert(cur^.right, data_in)  
  endif  
endprocedure // Insert
```

data_in = 35

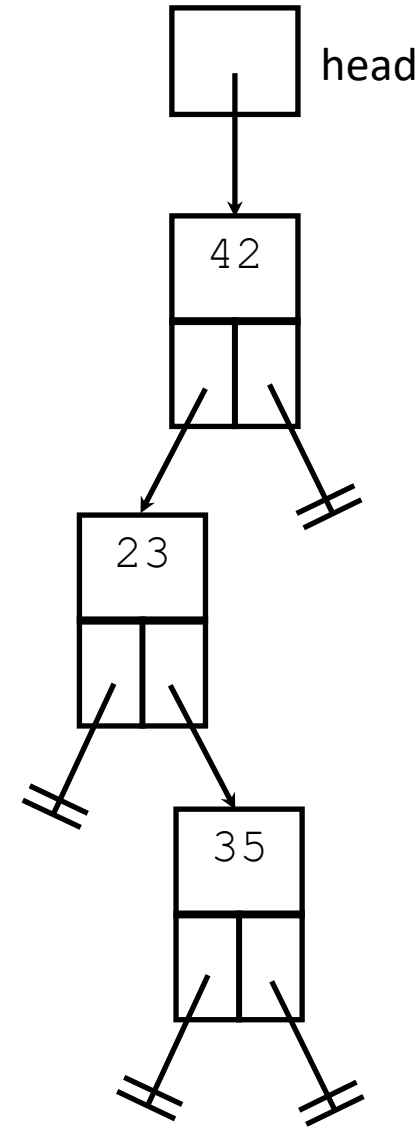


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 35

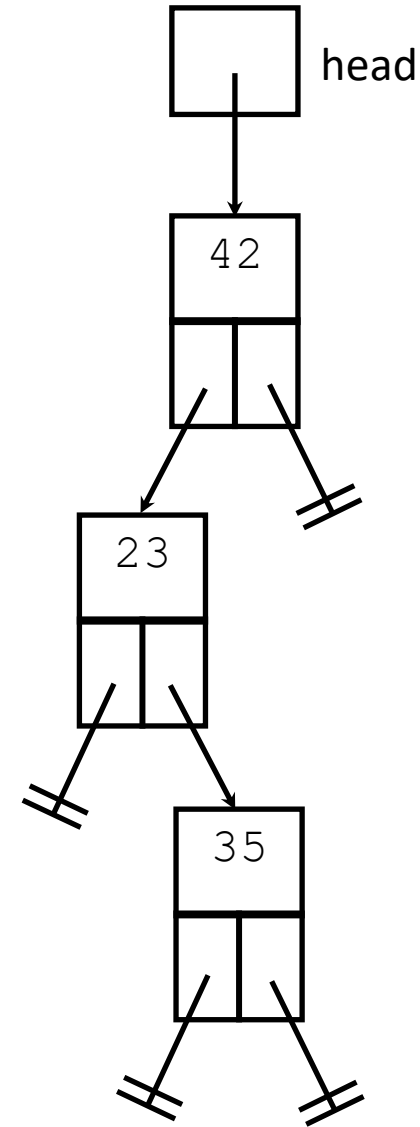


```

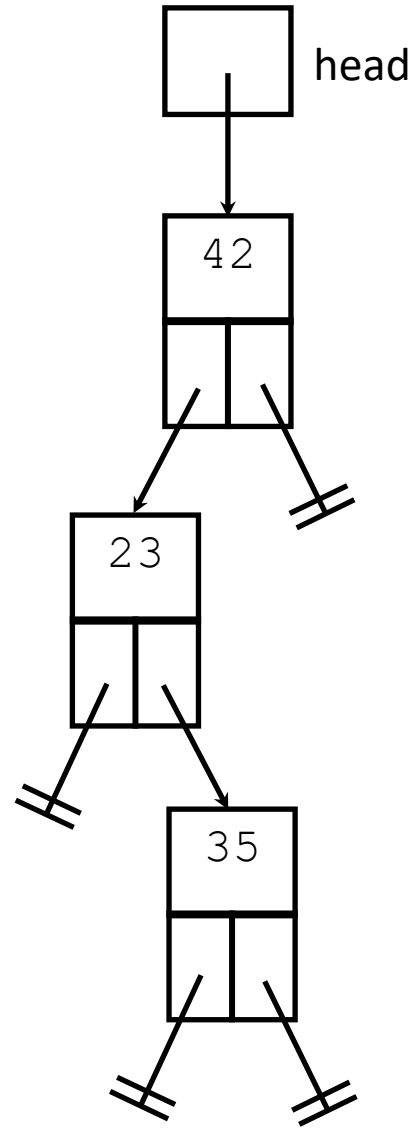
procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 35



```
•  
•  
Insert(head, 23)  
Insert(head, 35)  
Insert(head, 47)  
•  
•
```

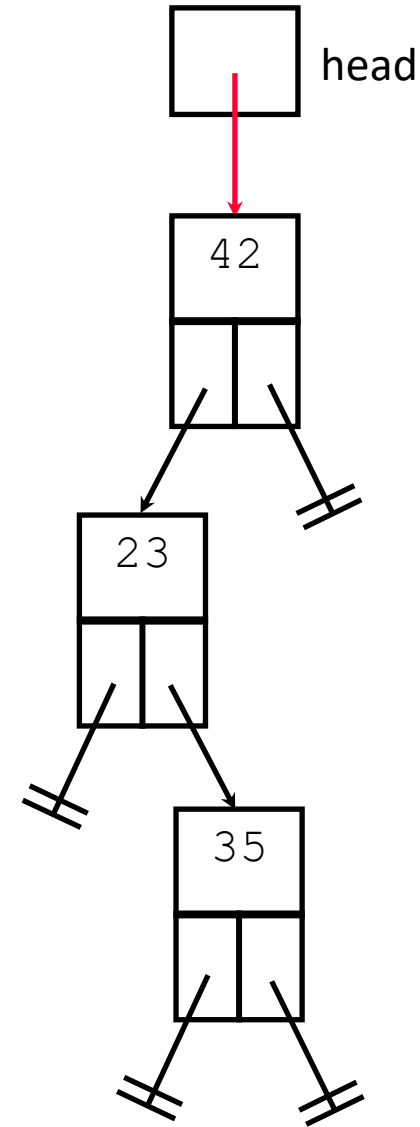


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
  if(cur = NIL) then
    cur <- new(Node)
    cur^.data <- data_in
    cur^.left <- NIL
    cur^.right <- NIL
  elseif(cur^.data > data_in)
    Insert(cur^.left, data_in)
  else
    Insert(cur^.right, data_in)
  endif
endprocedure // Insert

```

data_in = 47

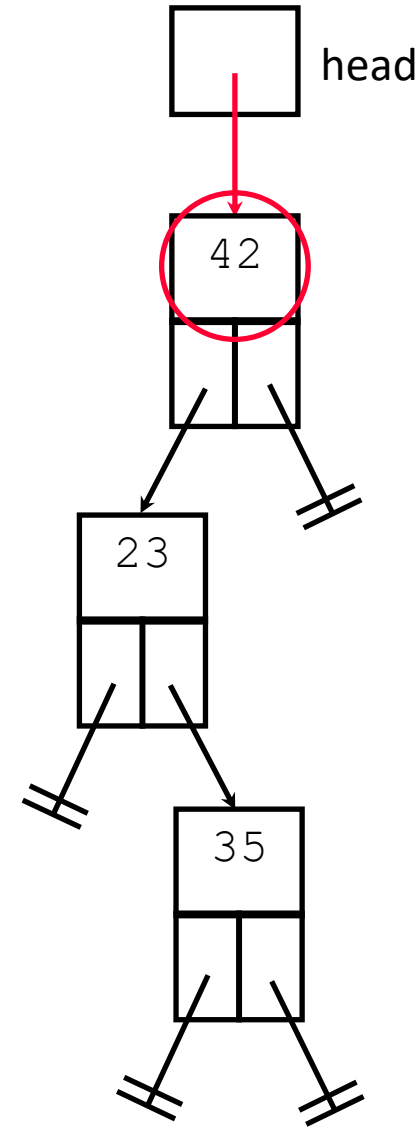



```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

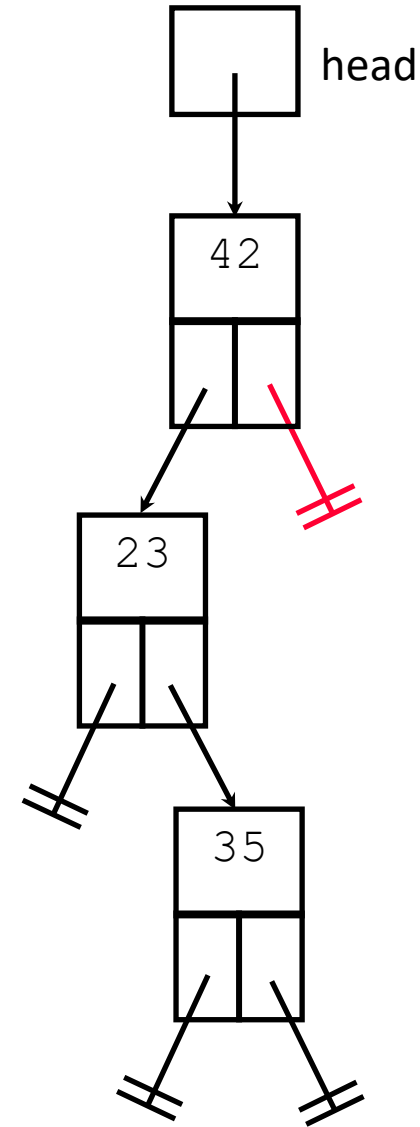


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

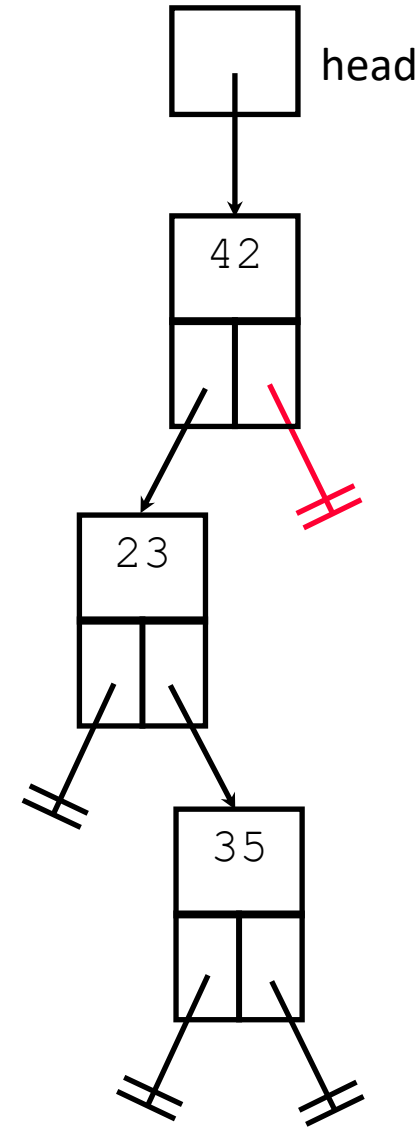


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
  if(cur = NIL) then
    cur <- new(Node)
    cur^.data <- data_in
    cur^.left <- NIL
    cur^.right <- NIL
  elseif(cur^.data > data_in)
    Insert(cur^.left, data_in)
  else
    Insert(cur^.right, data_in)
  endif
endprocedure // Insert

```

data_in = 47

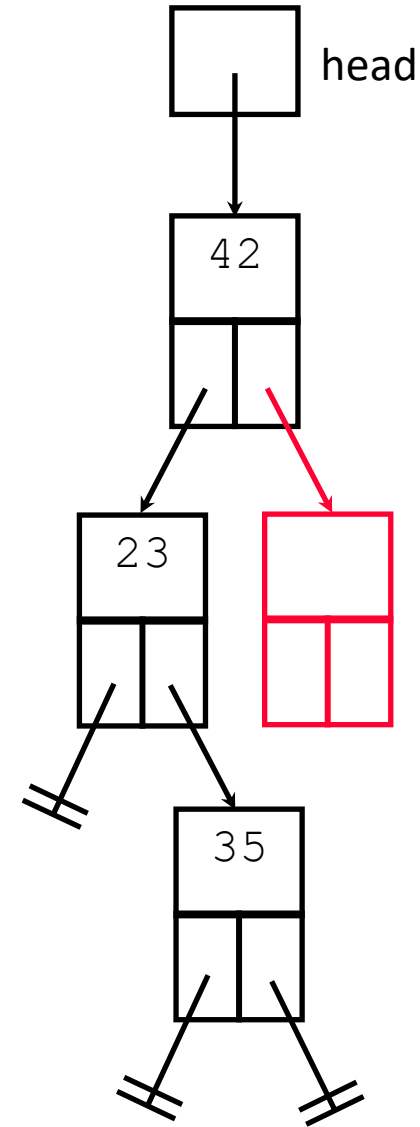


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

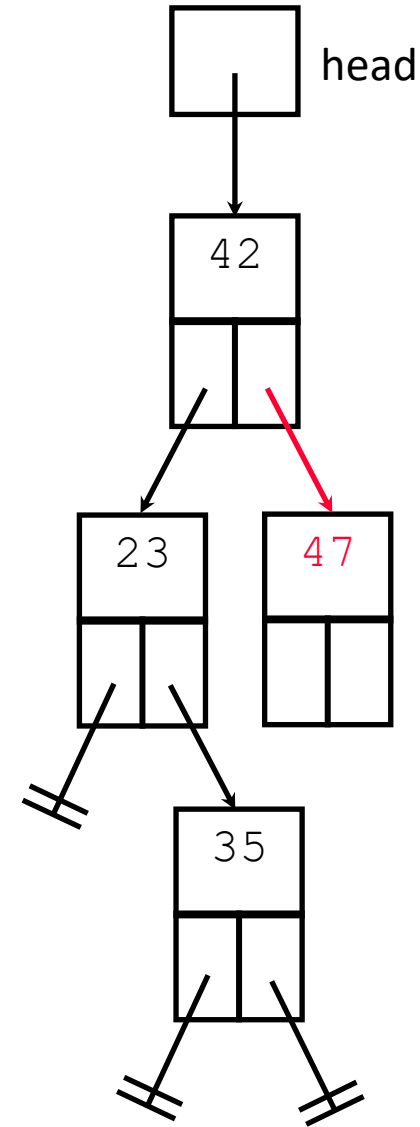


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

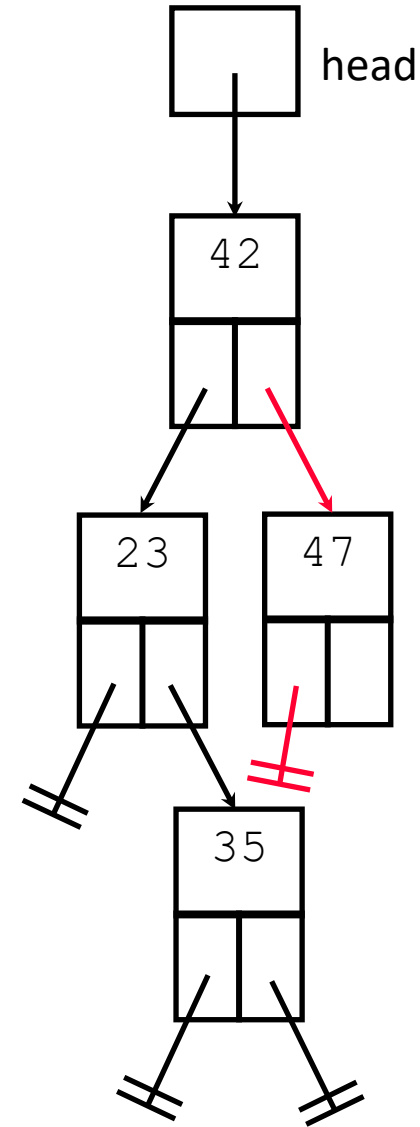


```

procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

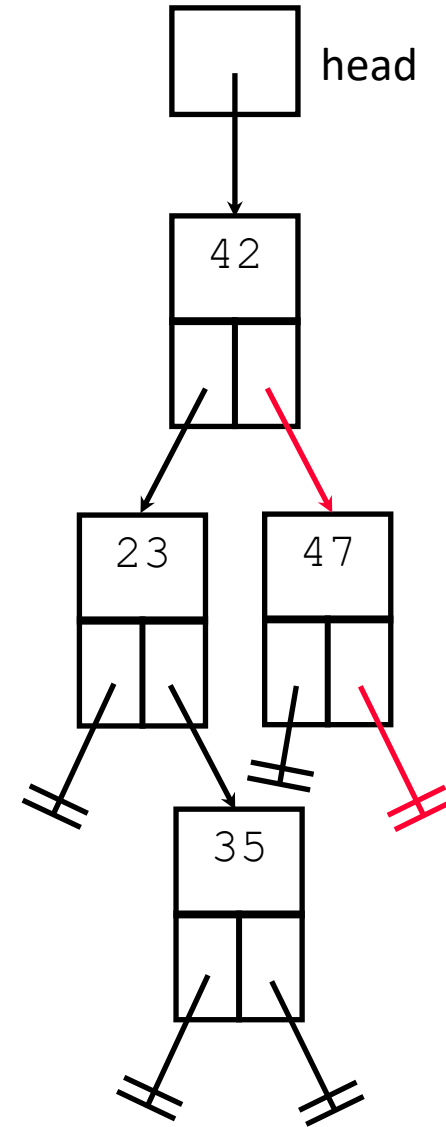


```

procedure Insert(
  cur iot in/out Ptr to a Node,
  data_in iot in num)
if (cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif (cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

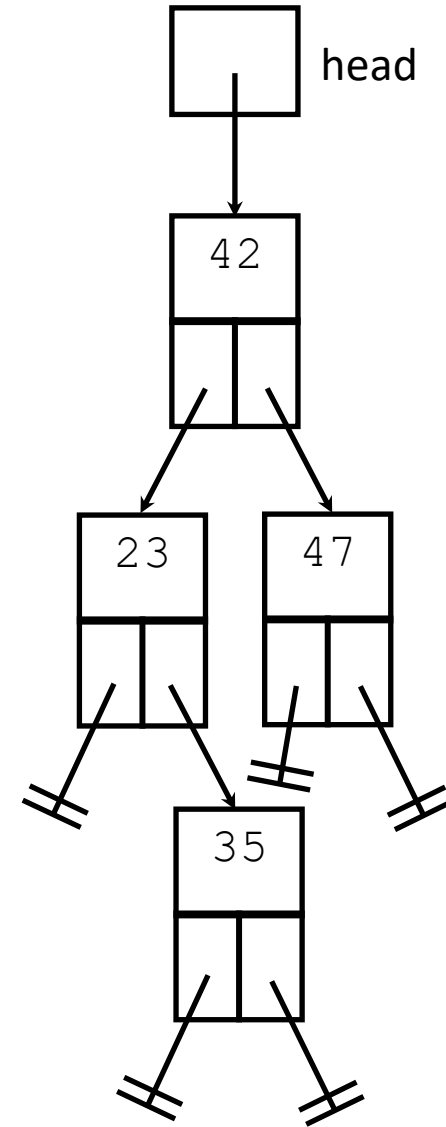


```

procedure Insert(
  cur iot in/out Ptr to a Node,
  data_in iot in num)
if (cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif (cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47

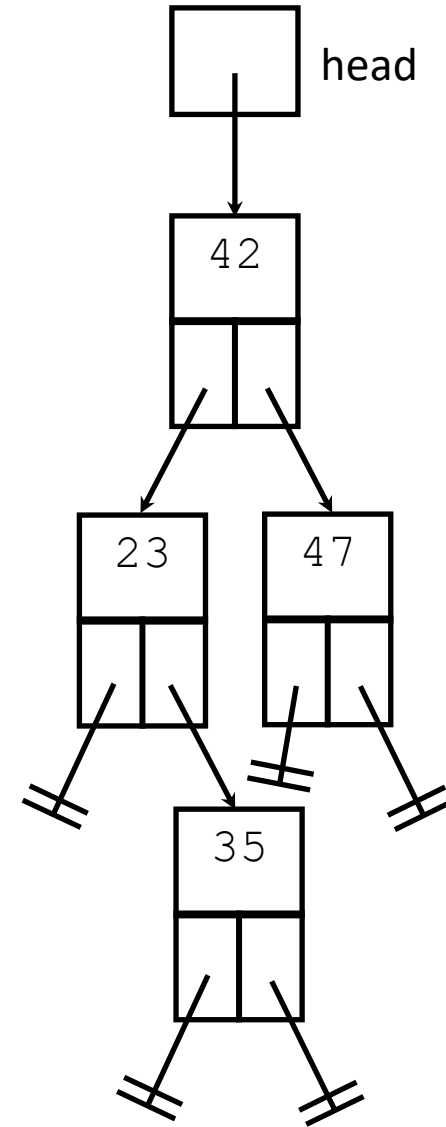



```

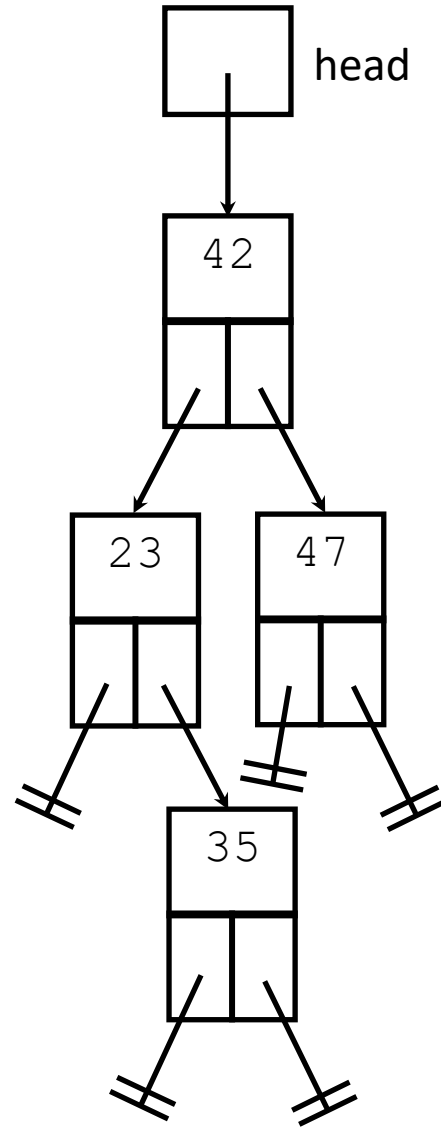
procedure Insert(
  cur iot in/out Ptr toa Node,
  data_in iot in num)
if(cur = NIL) then
  cur <- new(Node)
  cur^.data <- data_in
  cur^.left <- NIL
  cur^.right <- NIL
elseif(cur^.data > data_in)
  Insert(cur^.left, data_in)
else
  Insert(cur^.right, data_in)
endif
endprocedure // Insert

```

data_in = 47



•
•
Insert(head, 23)
Insert(head, 35)
Insert(head, 47)
•
•



Summary

- **Preserve “search” structure!**
- **Inserting involves 2 steps:**
 - **Find the correct location**
 - For a BST insert, always **insert at the “bottom” of the tree**
 - **Do commands to add node**
 - **Create node**
 - **Add data**
 - **Make left and right pointers point to nil**

DELETION OF A NODE

Deleting a Node in BST

- We have a Binary **Search** Tree and want to remove some element based upon a match.
- Must preserve “search” property
- Must not lose any elements (i.e. only remove the one element)

BST Deletion

- **Search** for desired item.
- If **not found**, then return NIL or print error.
- If **found**, perform steps necessary to accomplish removal from the tree.

Four Cases for Deletion

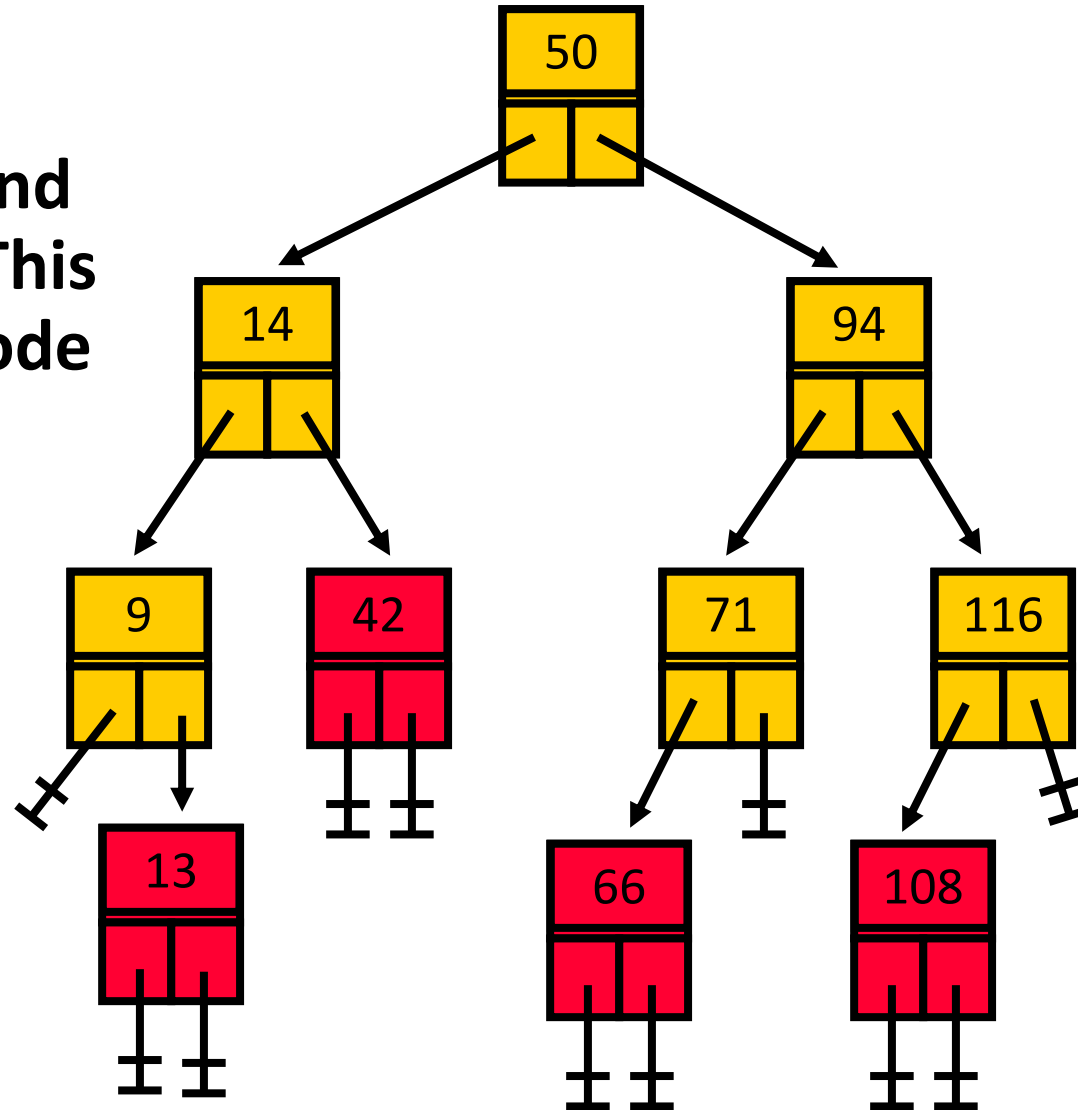
- Delete a **leaf** node
- Delete a node with **only one child (left)**
- Delete a node with **only one child (right)**
- Delete a node with **two children**

Cases 2 and 3 are comparable and only need slight changes in the conditional statement used

Delete a Leaf Node

Simply use an
“in/out” pointer and
assign it to “nil”. This
will remove the node
from the tree.

`cur <- nil`

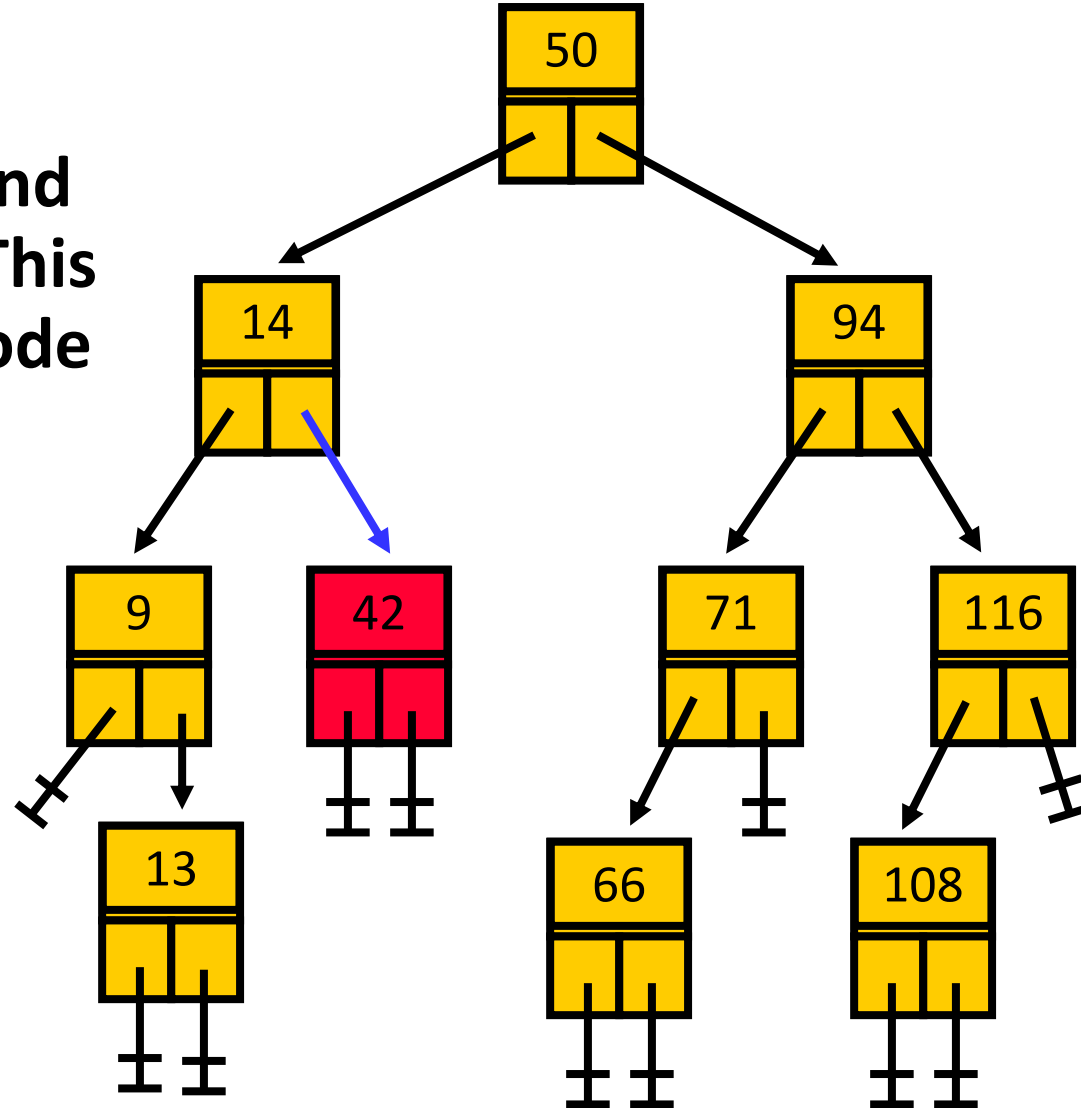


Delete a Leaf Node

Simply use an
“in/out” pointer and
assign it to “nil”. This
will remove the node
from the tree.

`cur <- nil`

Let's delete 42.

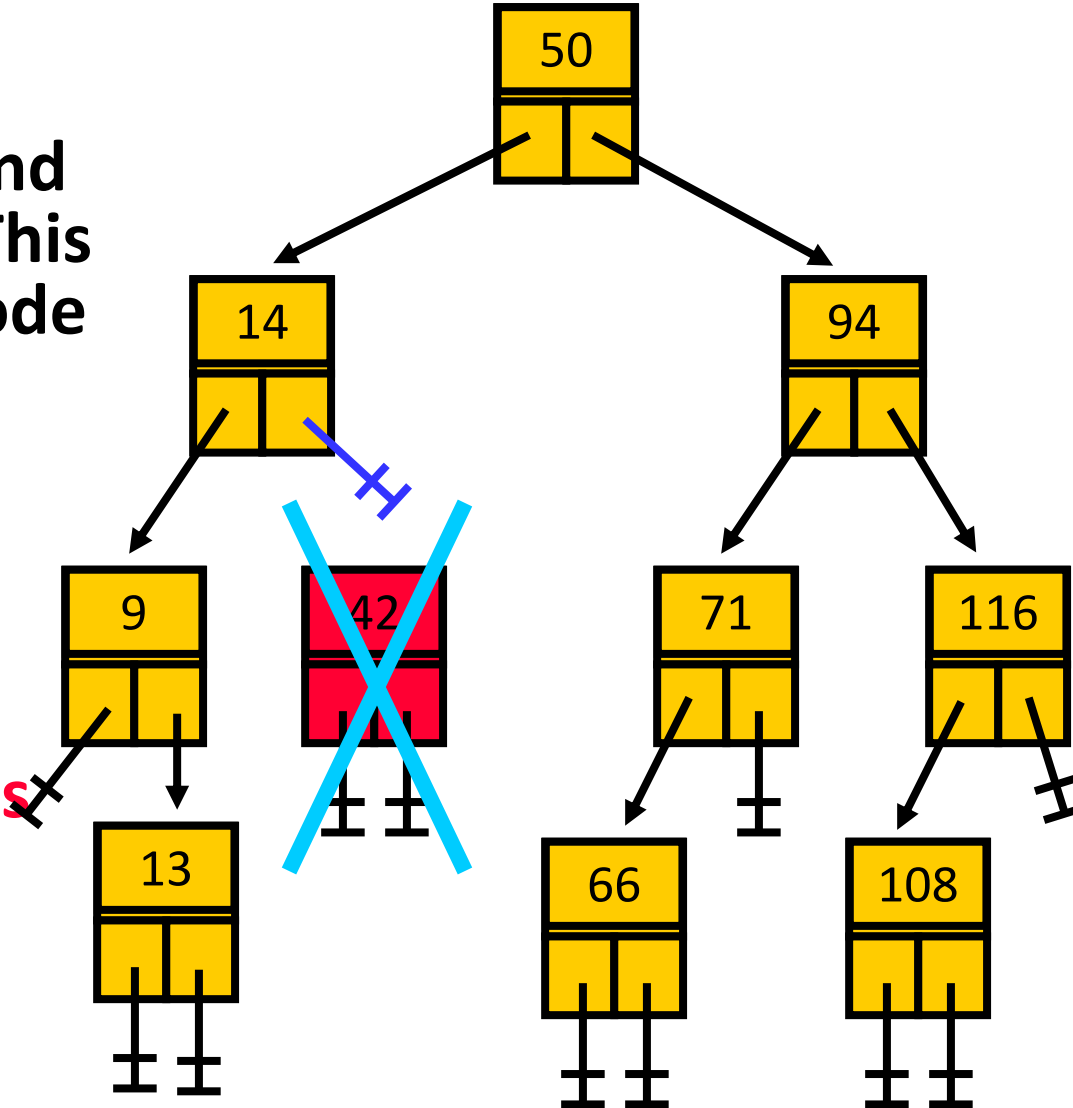


Delete a Leaf Node

Simply use an
“in/out” pointer and
assign it to “nil”. This
will remove the node
from the tree.

`cur <- nil`

Move the pointer;
now nothing points
to the node.

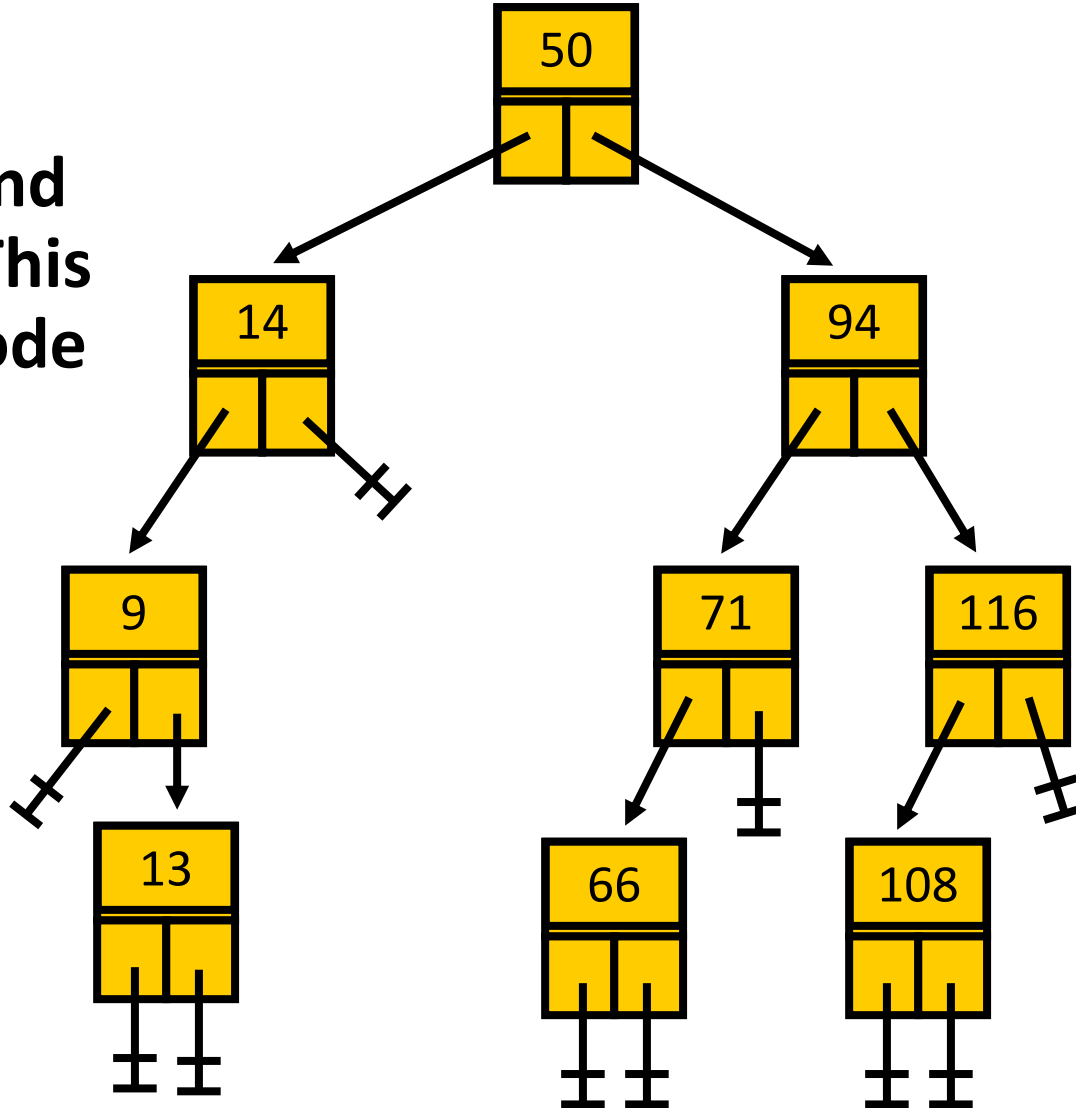


Delete a Leaf Node

Simply use an
“in/out” pointer and
assign it to “nil”. This
will remove the node
from the tree.

`cur <- nil`

The resulting tree.



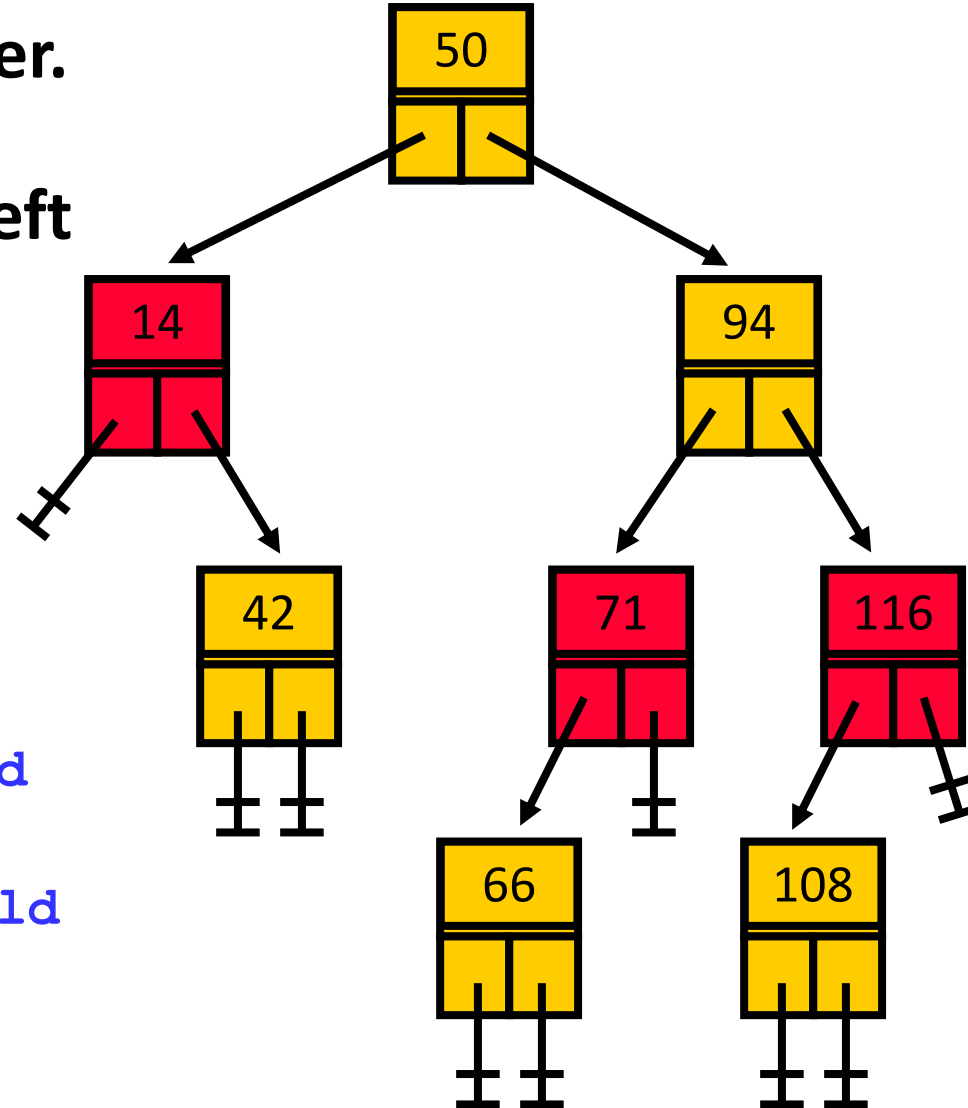
Delete a Node with One Child

Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.left_child  
or  
cur <- cur^.right_child
```



Delete a Node with One Child

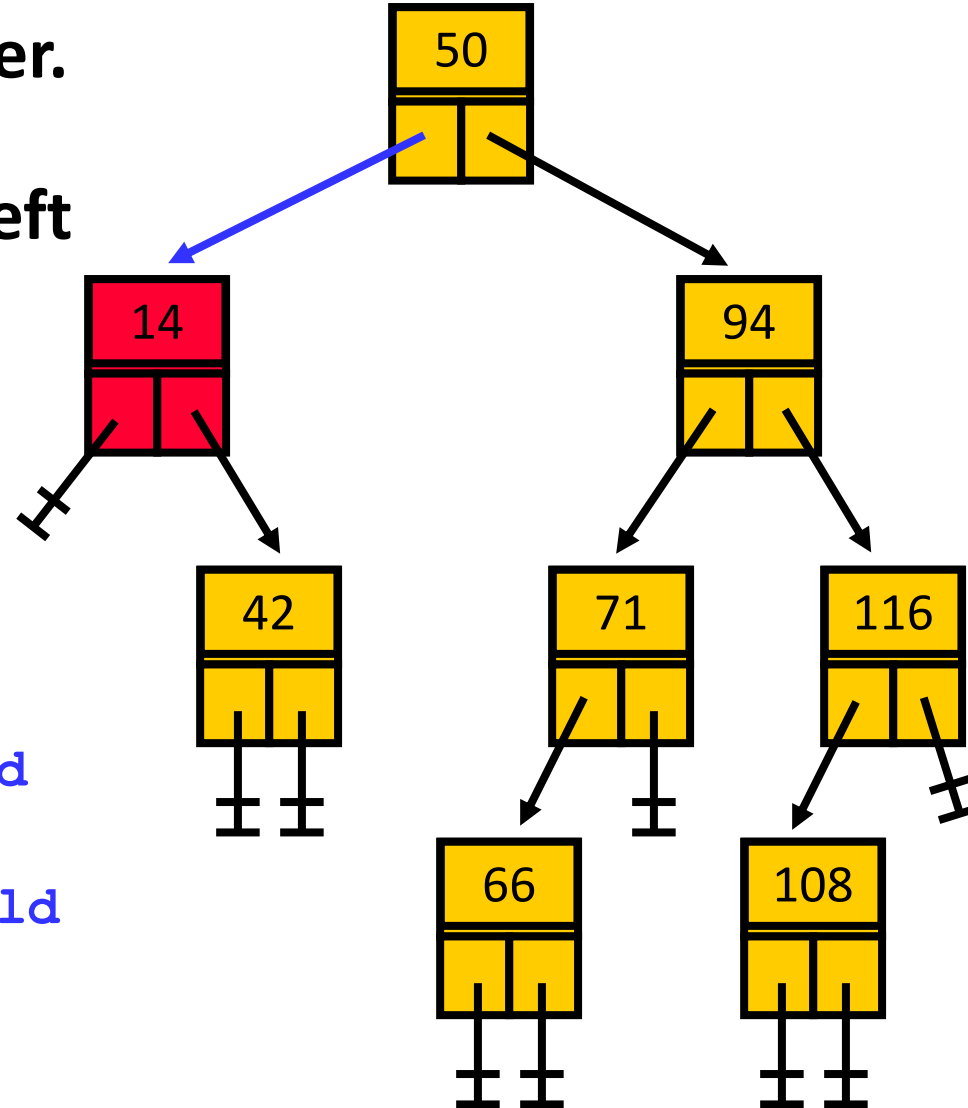
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.left_child  
or  
cur <- cur^.right_child
```

Let's delete 14.



Delete a Node with One Child

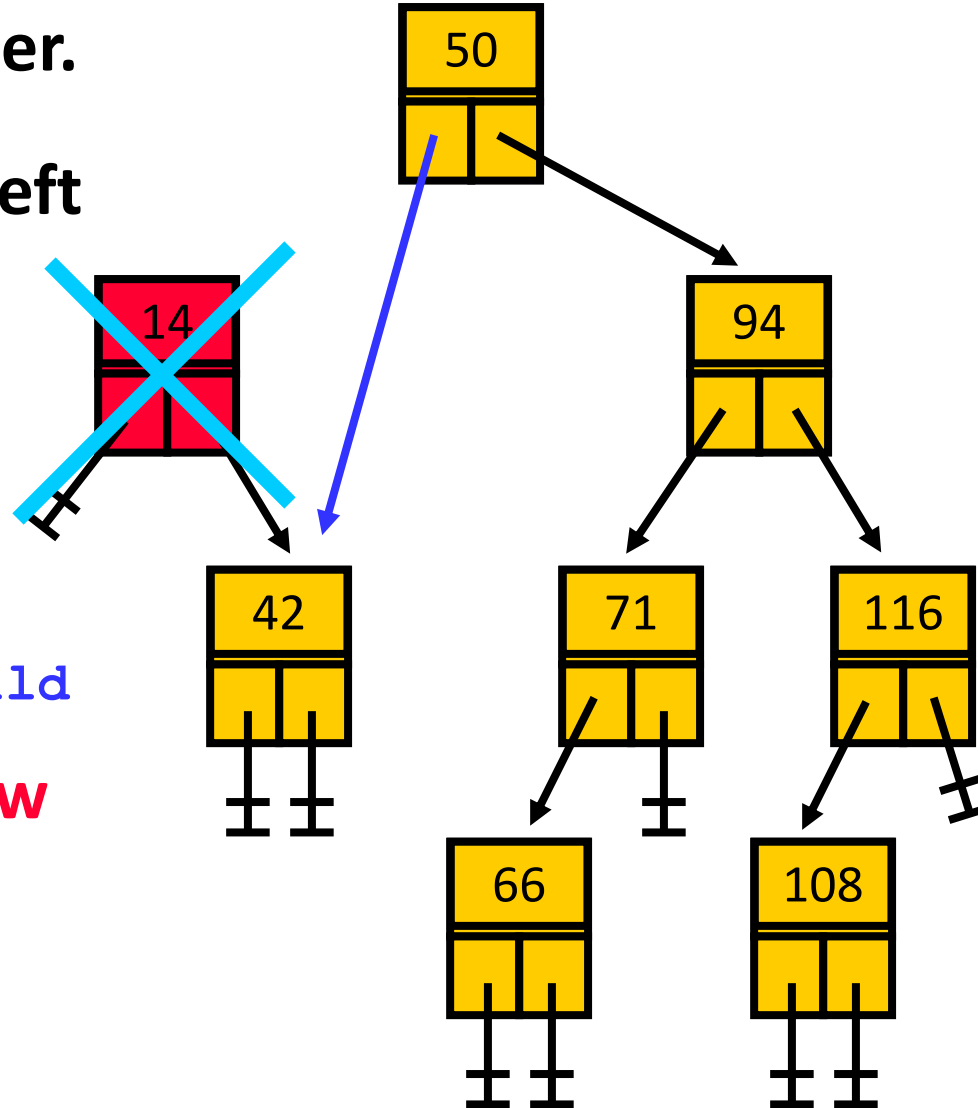
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.right_child
```

Move the pointer; now nothing points to the node.



Delete a Node with One Child

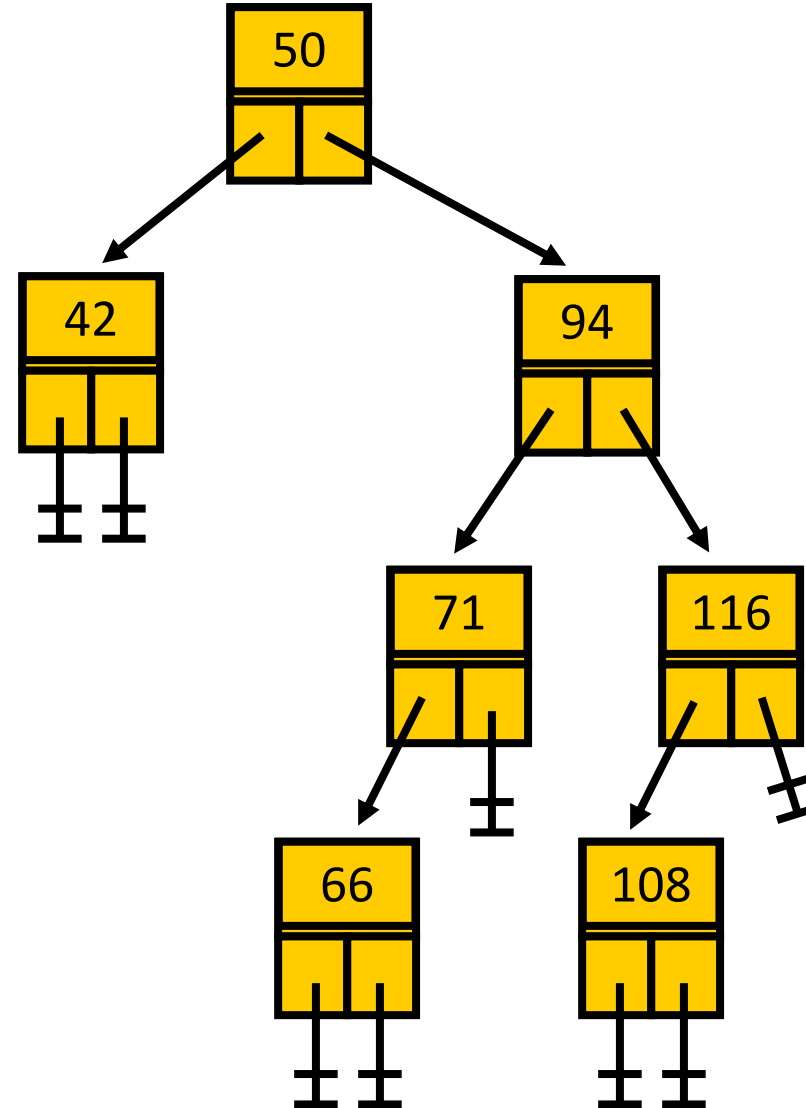
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.right_child
```

The resulting tree.



Delete a Node with One Child

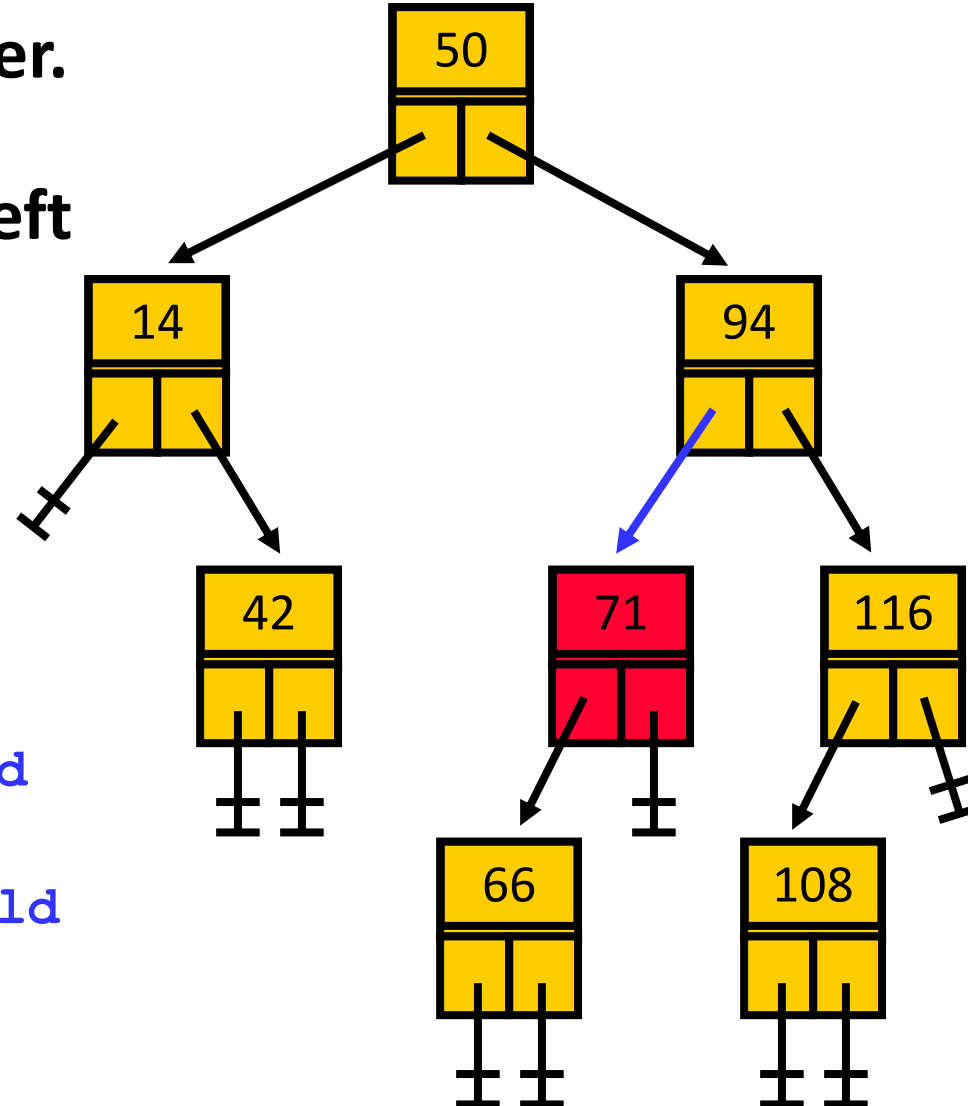
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.left_child  
or  
cur <- cur^.right_child
```

Let's delete 71.



Delete a Node with One Child

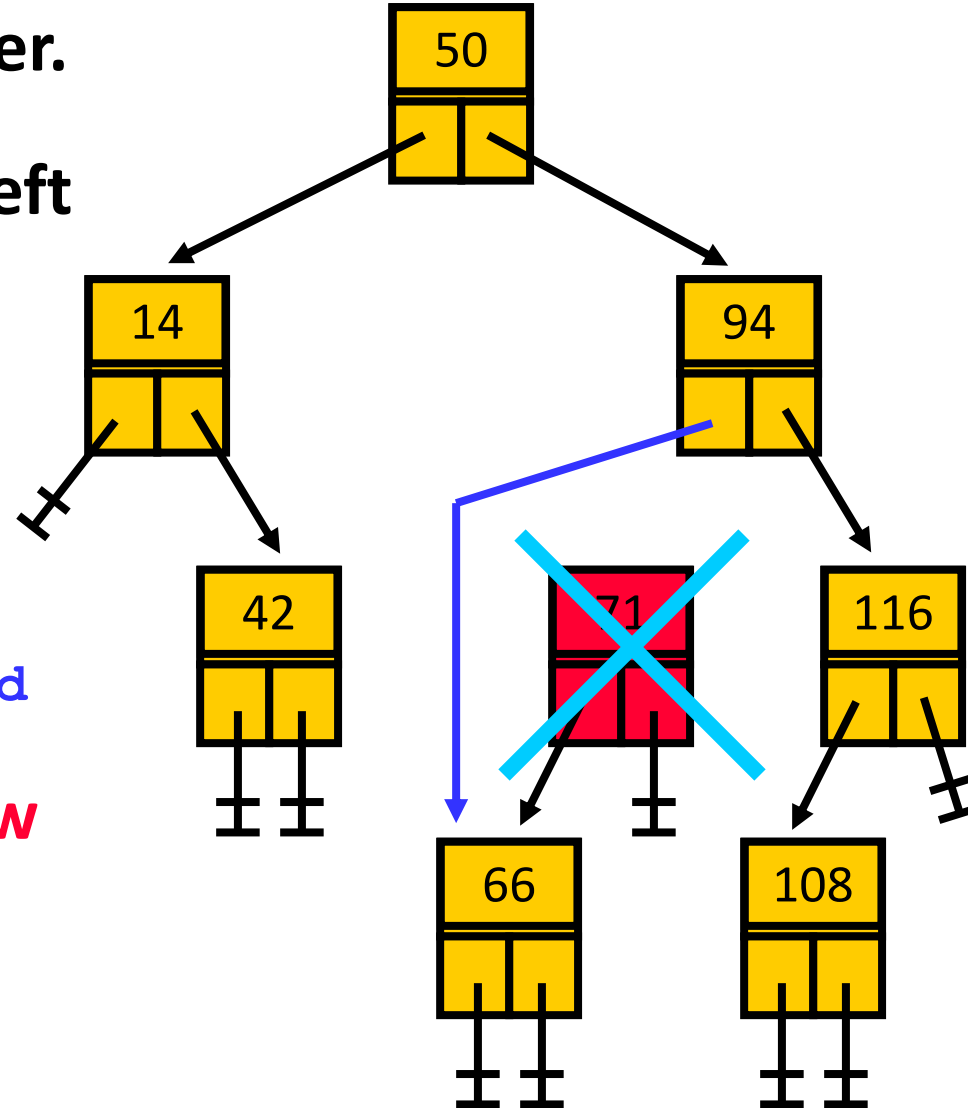
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.left_child
```

Move the pointer; now nothing points to the node.



Delete a Node with One Child

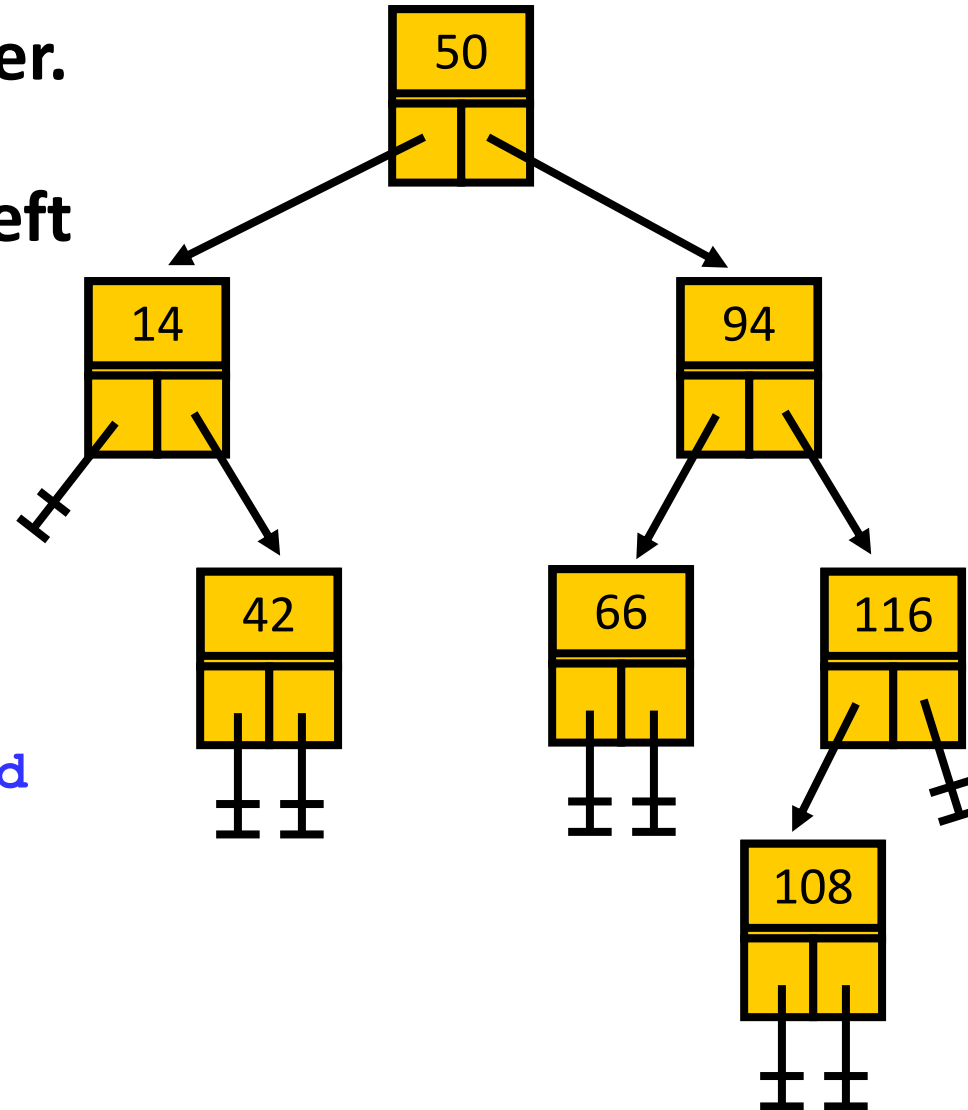
Use an “in/out” pointer.

Determine if it has a left or a right child.

Point the current pointer to the appropriate child:

```
cur <- cur^.left_child
```

The resulting tree.



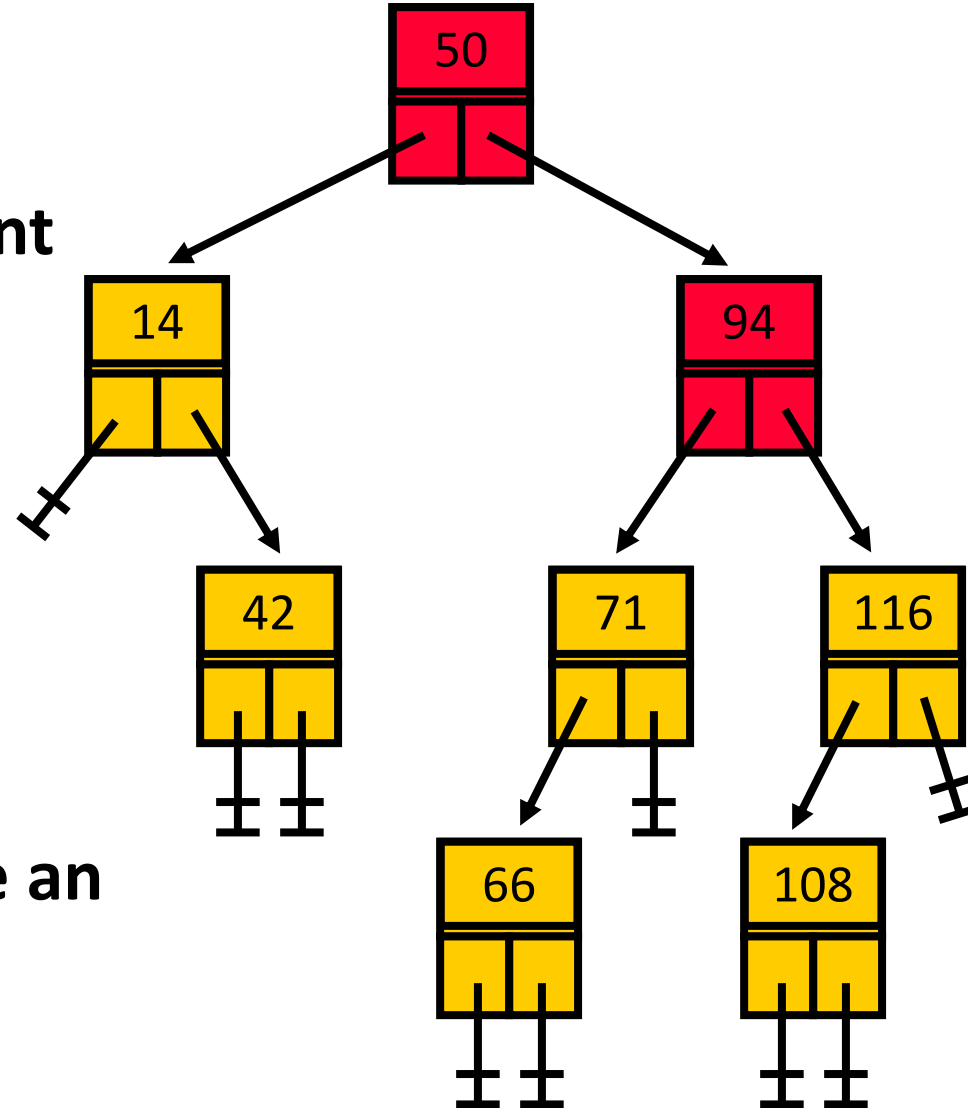
Delete a Node with Two Children

Copy a replacement value from a descendant node.

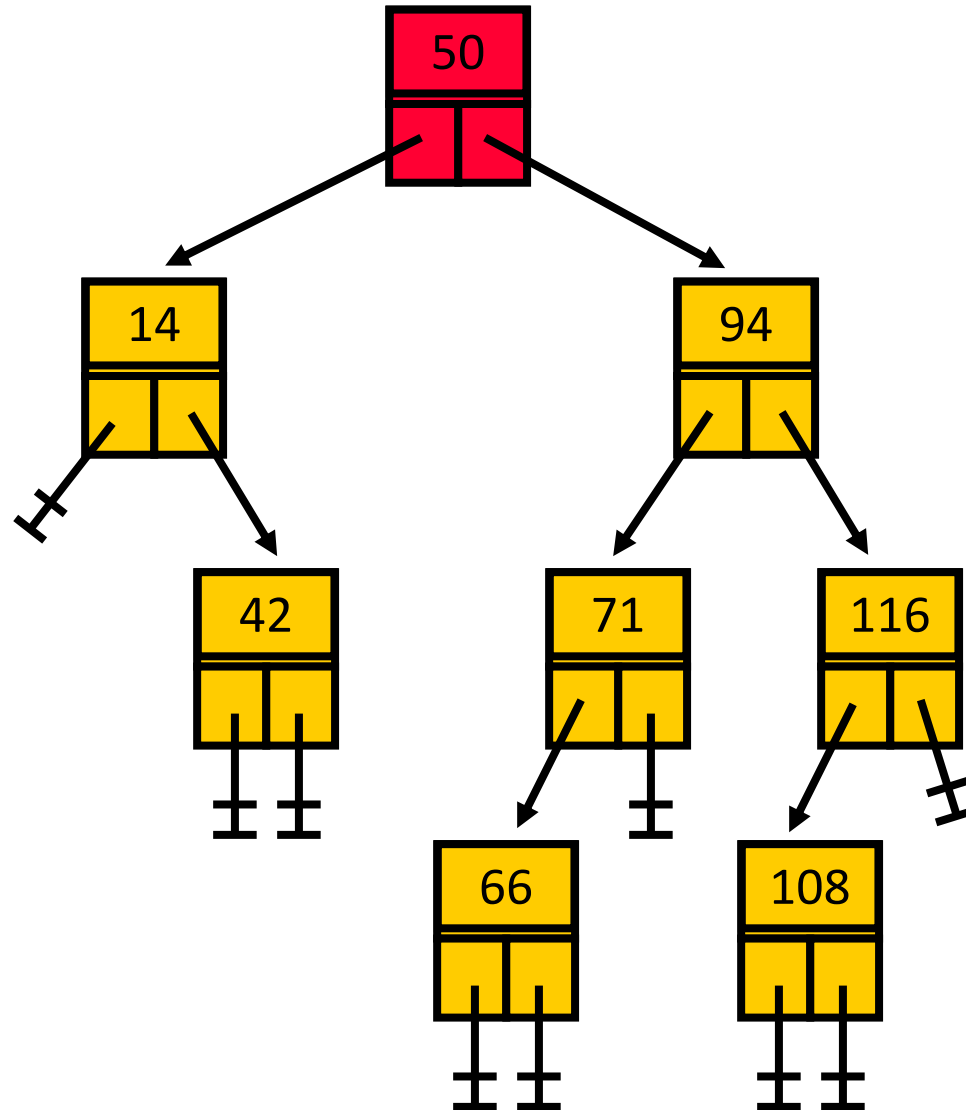
- Largest from left
- Smallest from right

Then **delete that descendant** node to remove the duplicate value.

- We know this will be an **easier case**.

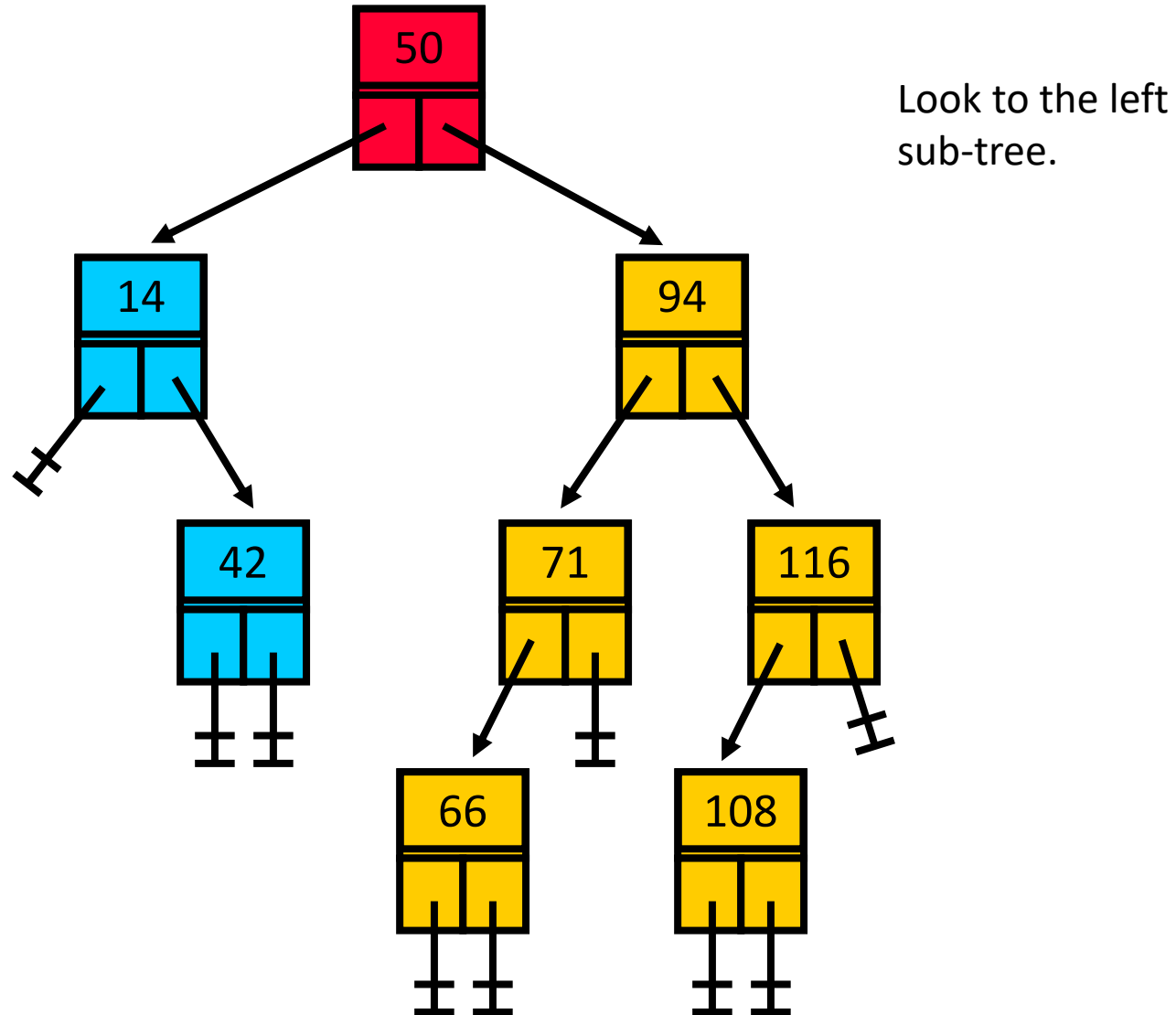


Delete a Node with Two Children

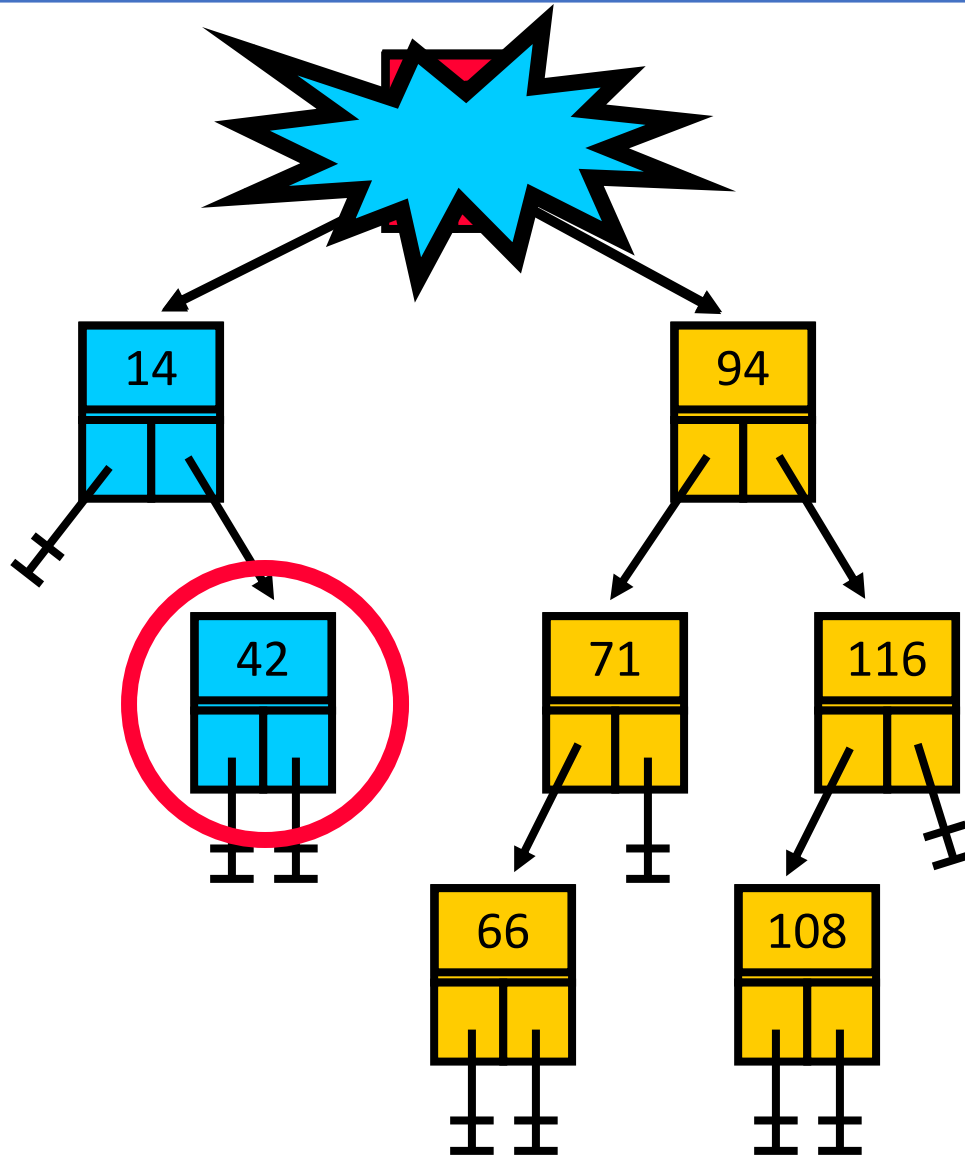


Let's delete 50.

Delete a Node with Two Children

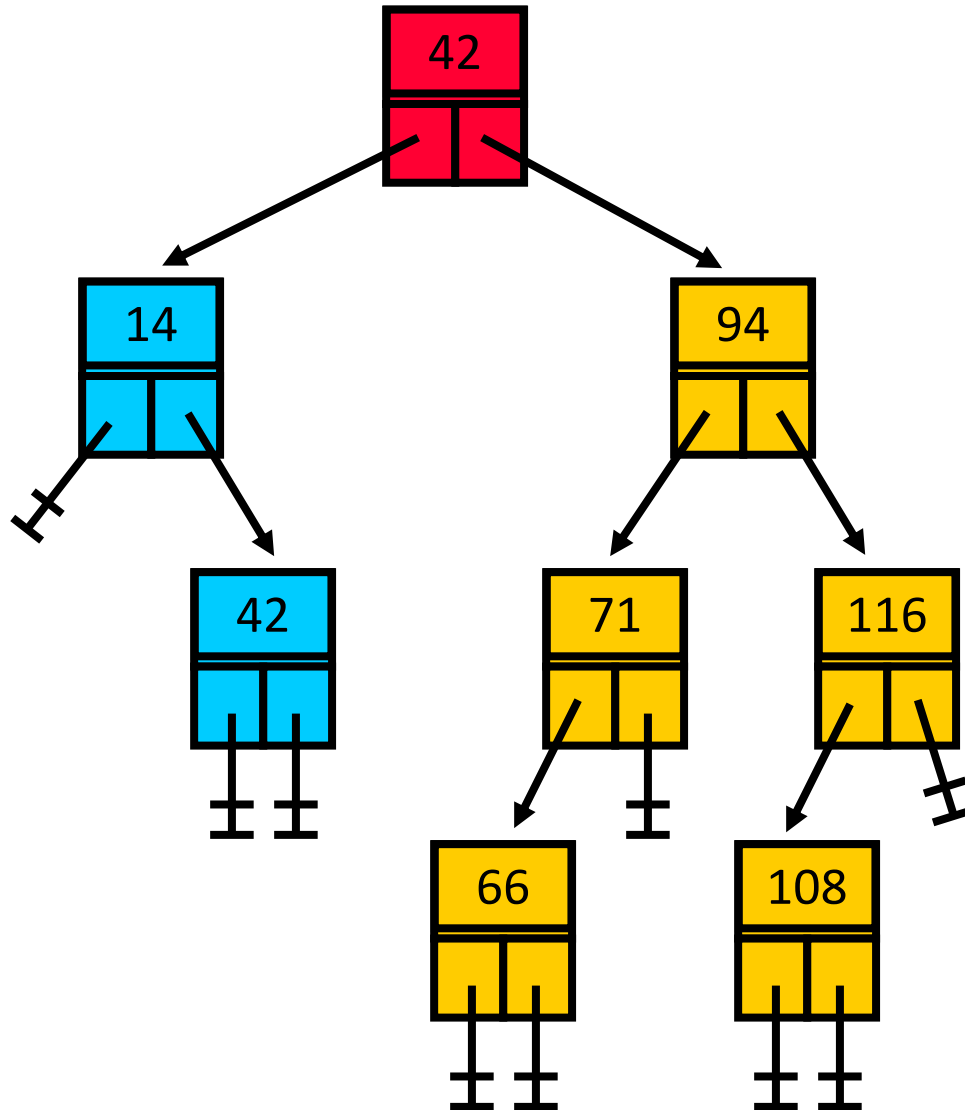


Delete a Node with Two Children



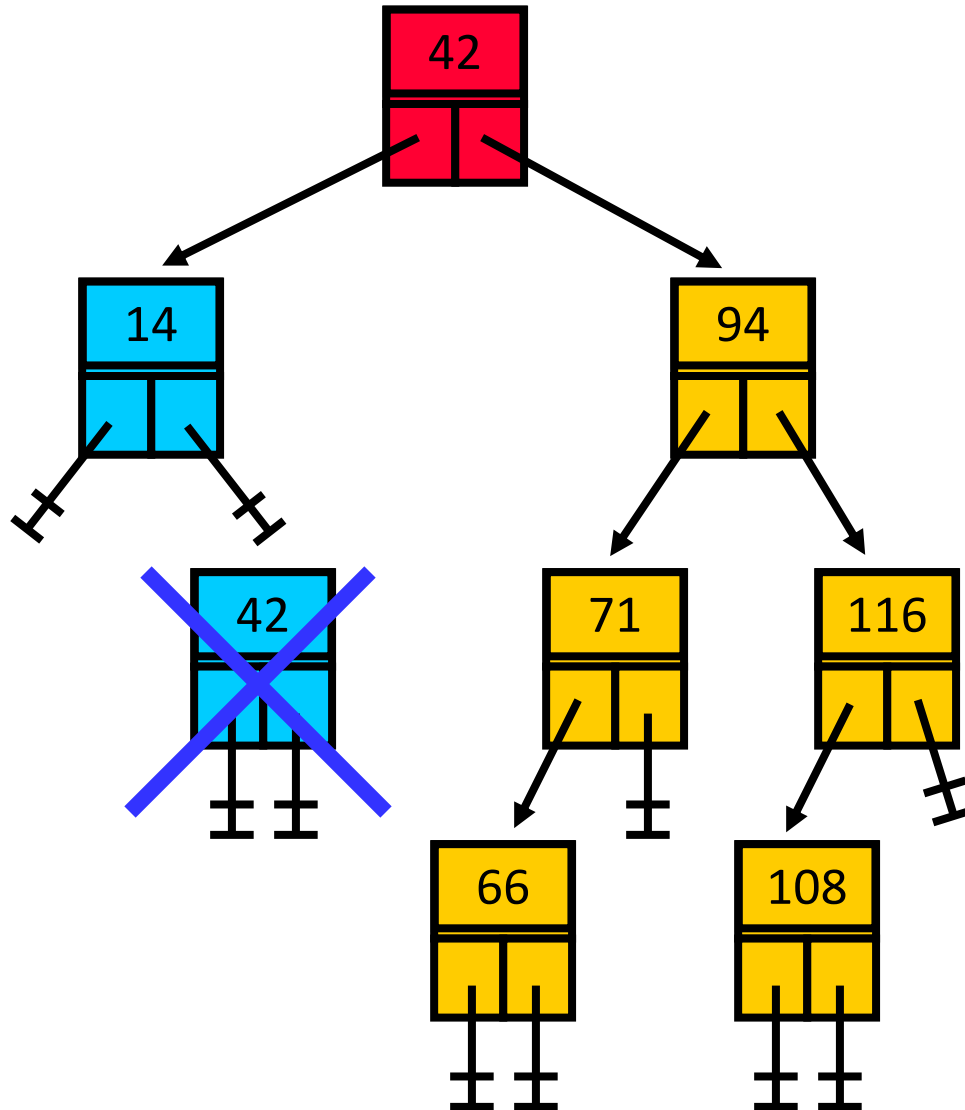
Find and copy the largest value (this will erase the old value but creates a duplicate).

Delete a Node with Two Children



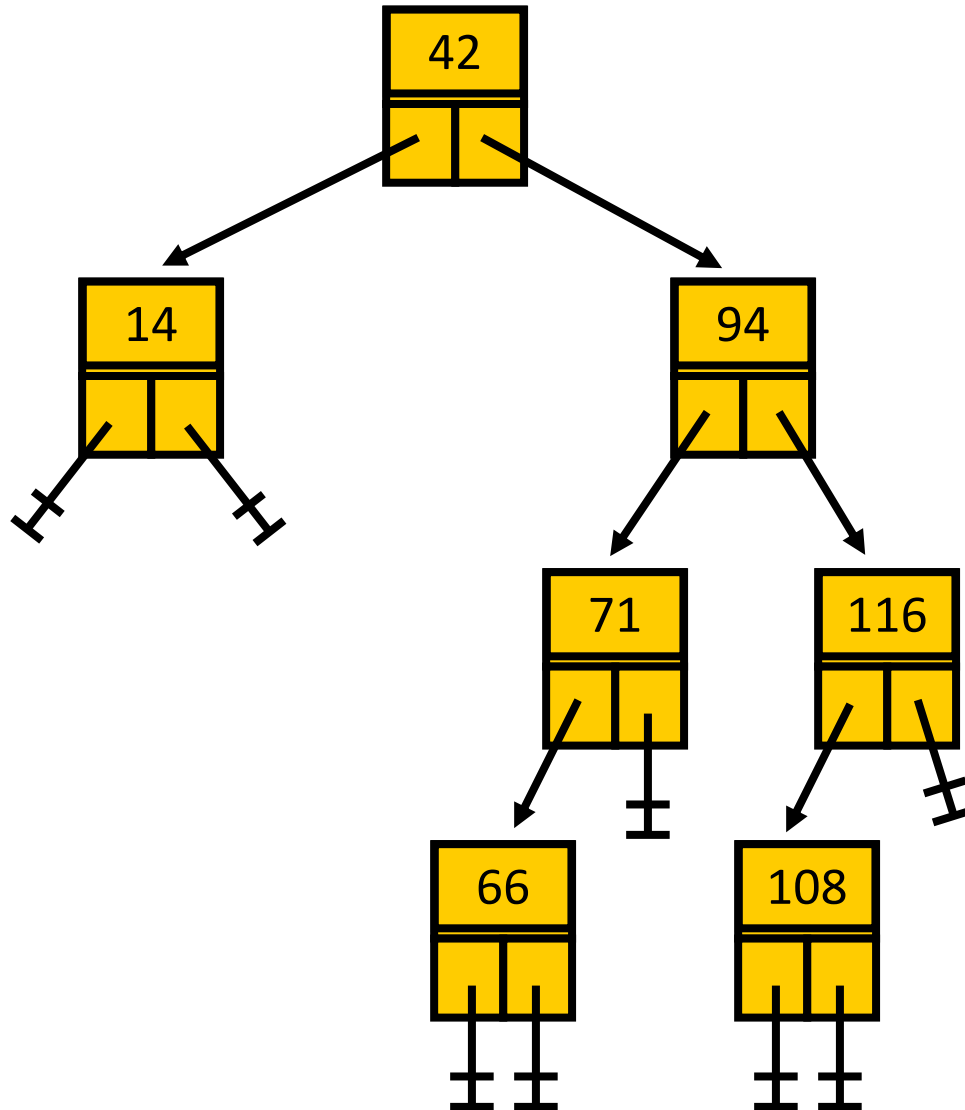
The resulting tree
so far.

Delete a Node with Two Children



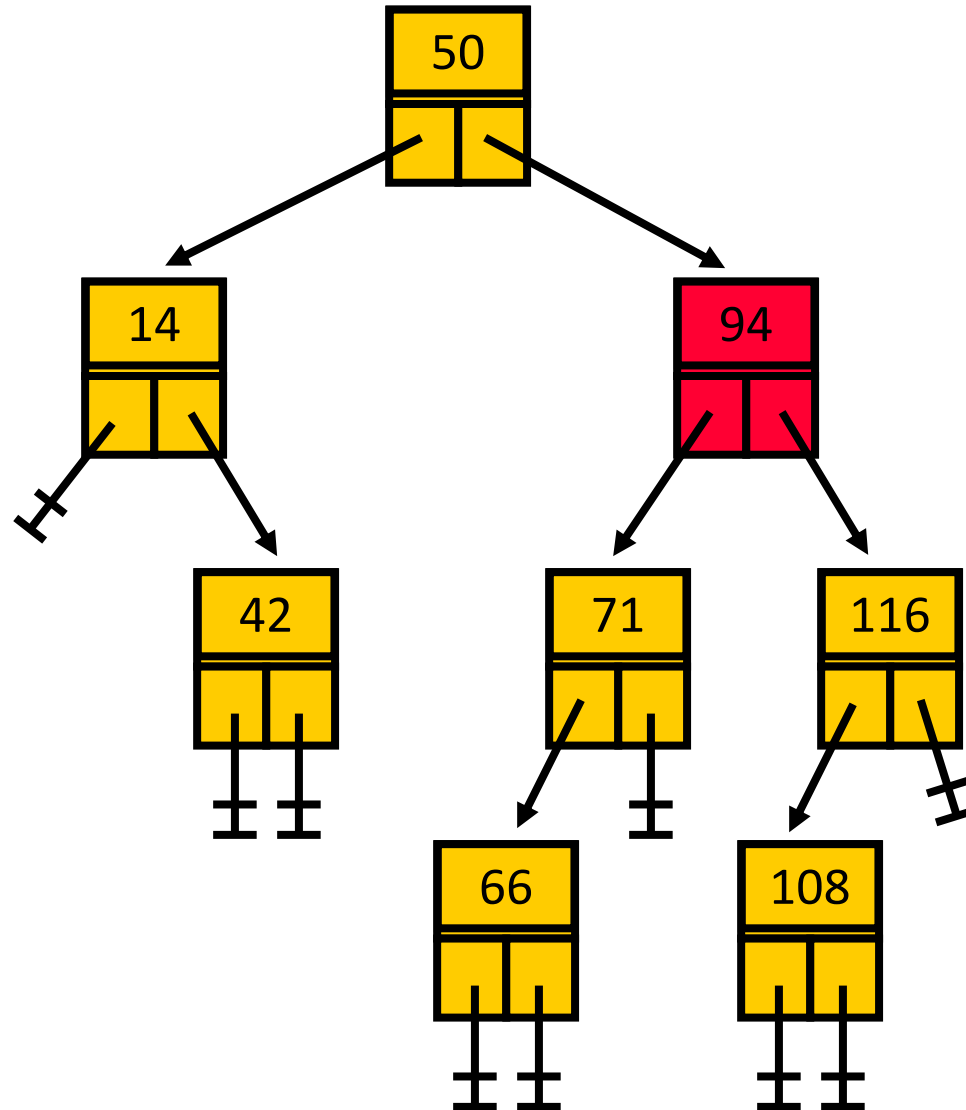
Now delete the duplicate from the left sub-tree.

Delete a Node with Two Children



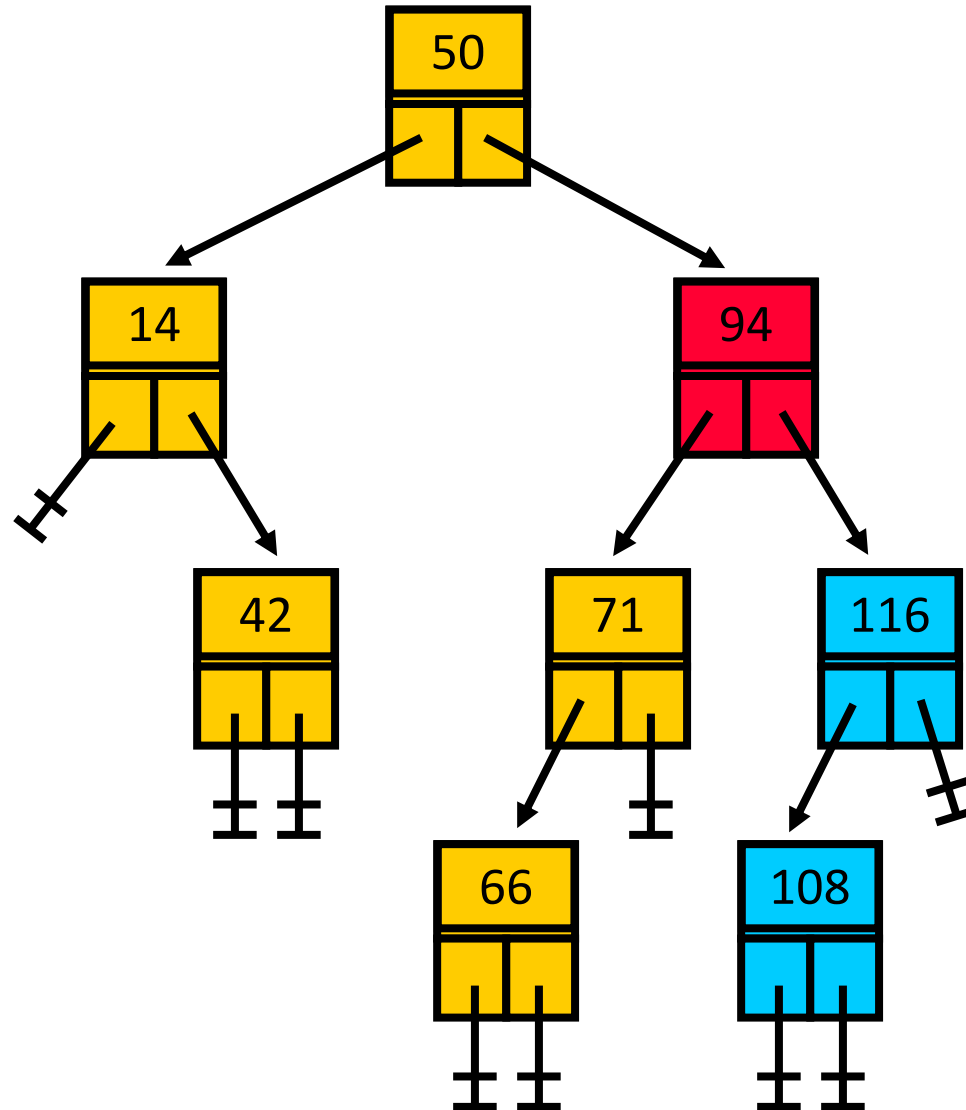
The final resulting tree – still has search structure.

Delete a Node with Two Children

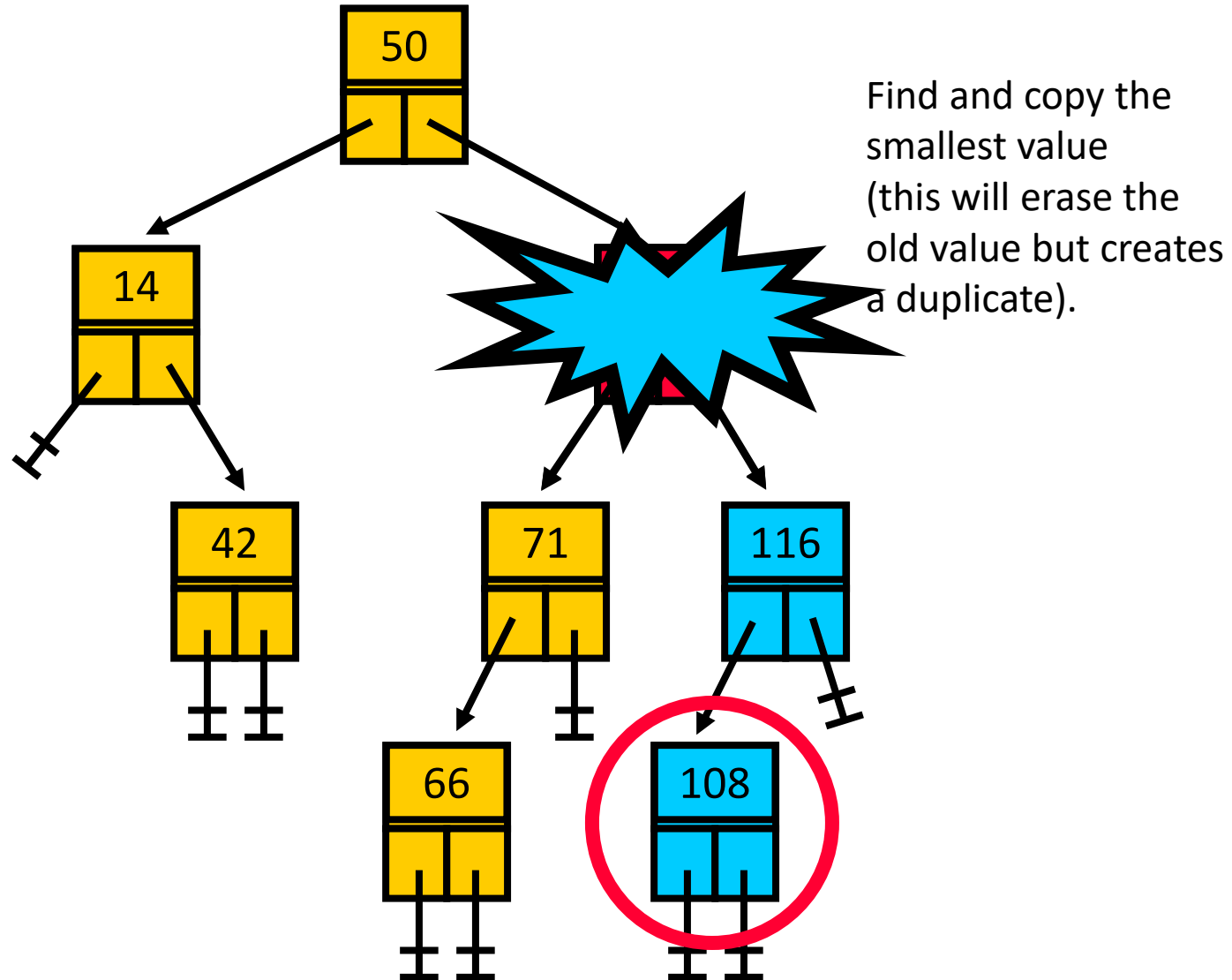


Let's delete 94.

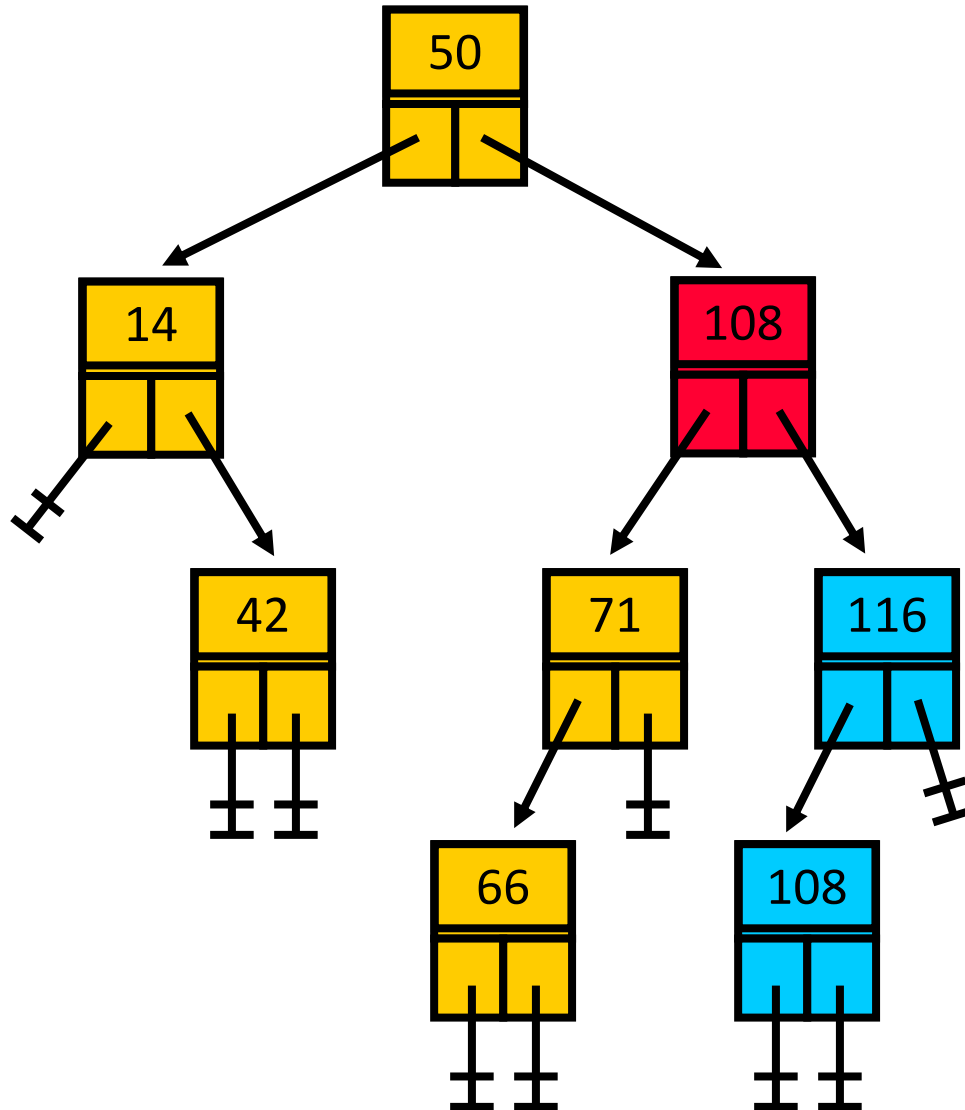
Delete a Node with Two Children



Delete a Node with Two Children

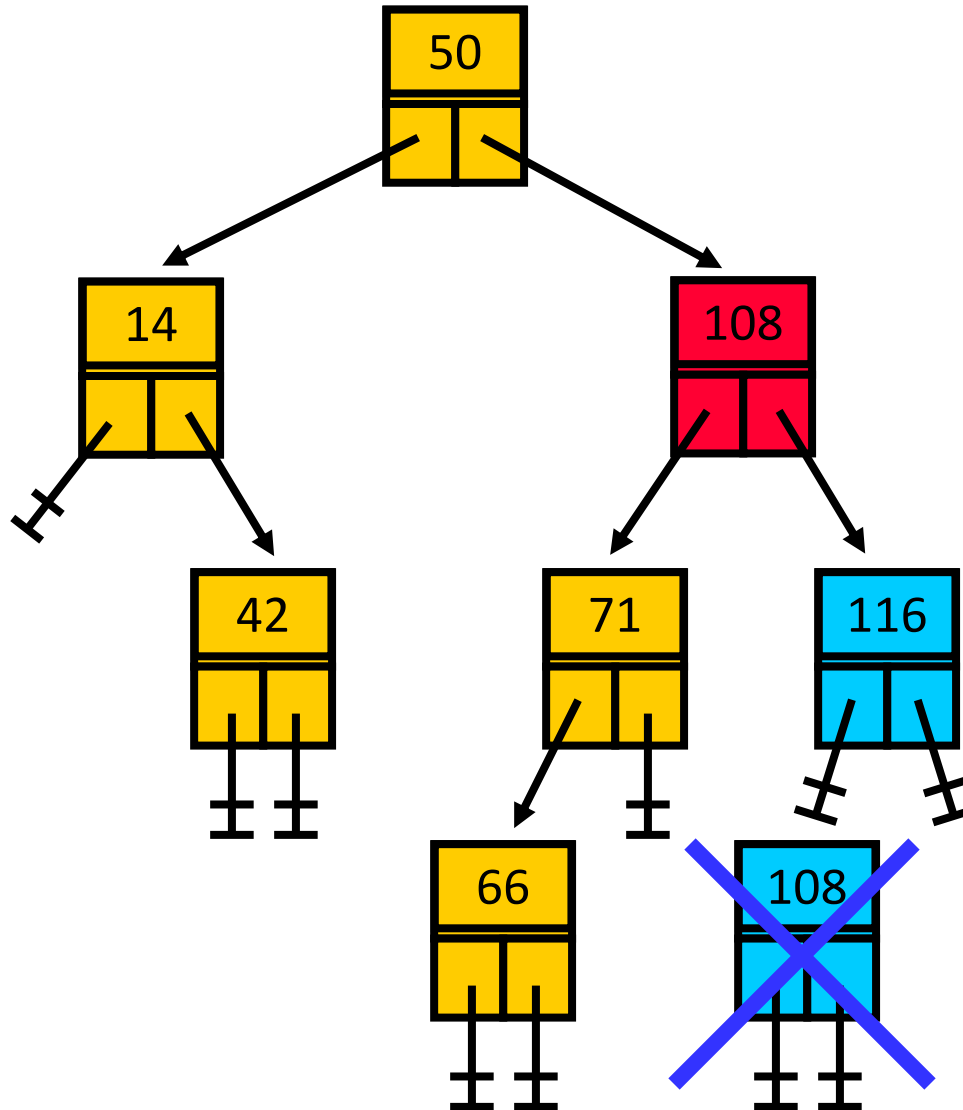


Delete a Node with Two Children



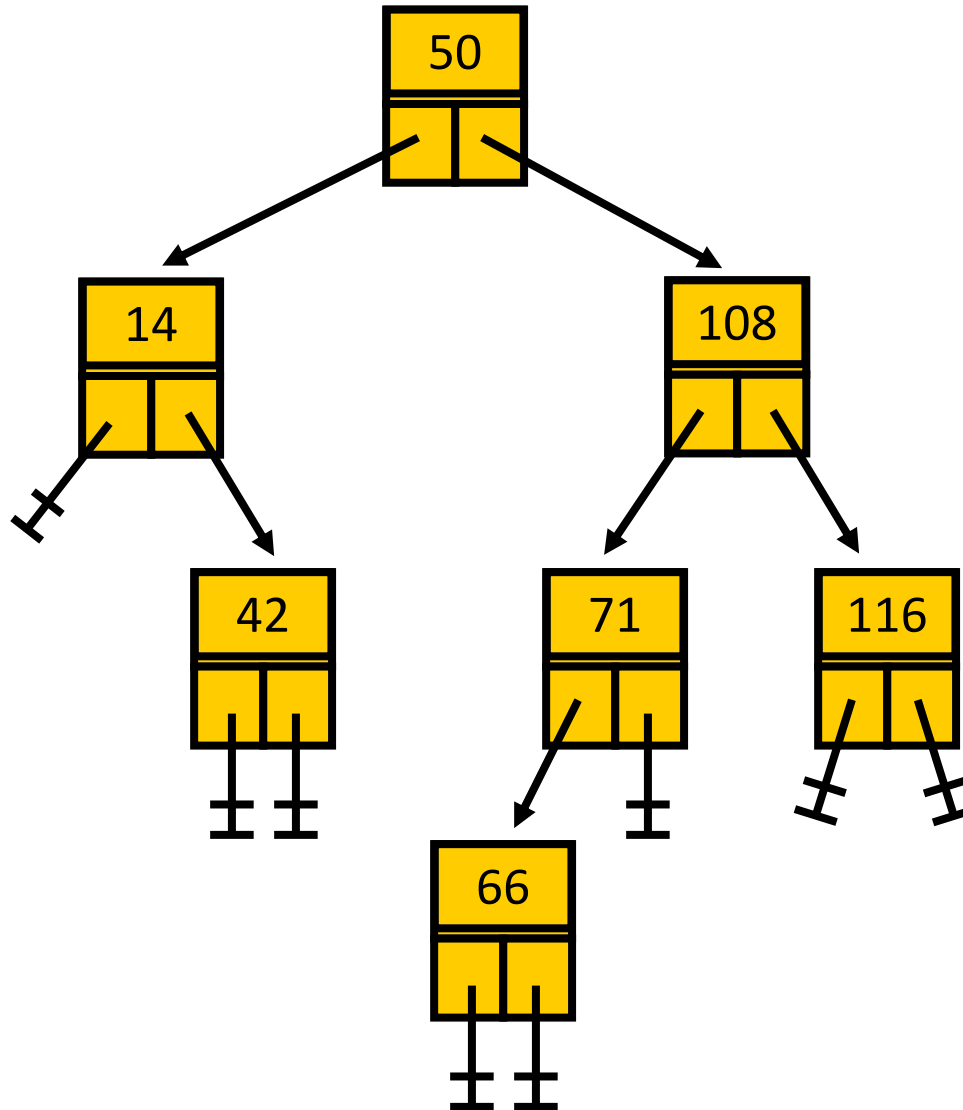
The resulting tree
so far.

Delete a Node with Two Children



Now delete the
duplicate from
the left sub-tree.

Delete a Node with Two Children



The final resulting tree – still has search structure.

Summary

- **Deleting a node from a binary search tree involves two steps:**
 - Search for the element
 - Then perform the deletion
- **We must preserve the search structure and only delete the element which matches.**
- **Four cases:**
 - Deleting a leaf node
 - Deleting a node with only the left child
 - Deleting a node with only the right child
 - Deleting a node with both children

**DEPTH FIRST
SEARCH
and
BREADTH FIRST
SEARCH**

Depth vs. Breadth First Traversals

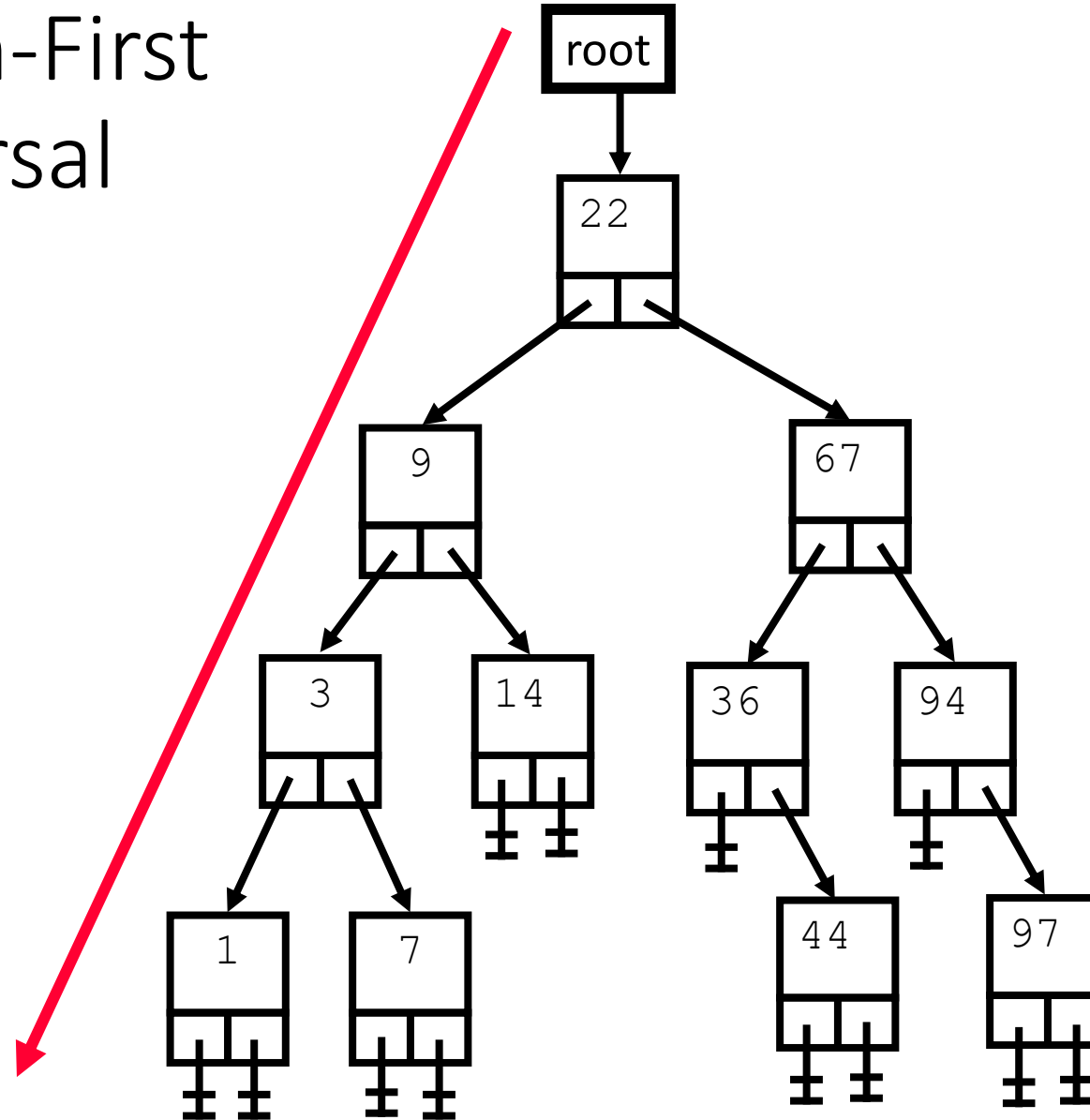
- **Depth First Traversals**

- Go down (deep)
- In-, Pre-, Post-order

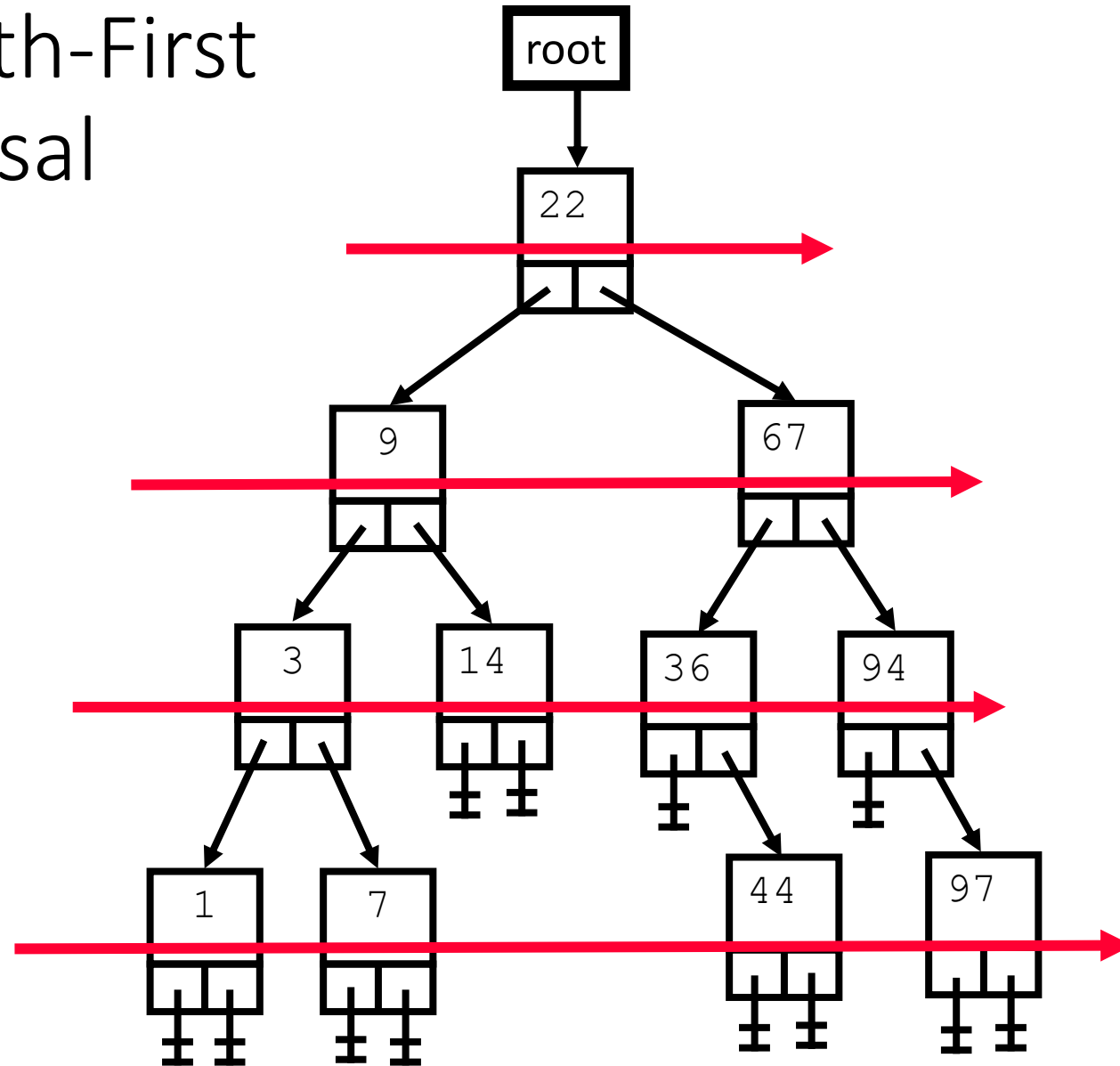
- **Breadth First Traversals**

- Go across (shallow)
- Require a queue to help

Depth-First Traversal



Breadth-First Traversal



Depth First Traversal (In-Order)

Procedure DFT

 (current isoftype in Ptr to a Node)

// In order DFT

 if (current <> NIL) then

 DFT (current^.left)

 print (current^.data)

 DFT (Current^.right)

 endif

endprocedure

Depth First Traversal (Pre-Order)

Procedure DFT

(current isoftype in Ptr to a Node)

// In order DFT

if(current <> NIL) then

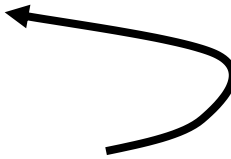
DFT(current^.left)

print(current^.data)

DFT(Current^.right)

endif

endprocedure



Move this here
to make a
Preorder DFT

Depth First Traversal (Post-Order)

Procedure DFT

(current isoftype in Ptr to a Node)

// In order DFT

if(current <> NIL) then

DFT(current^.left)

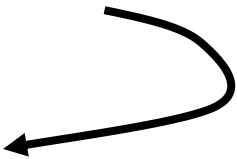
print(current^.data)

DFT(Current^.right)

endif

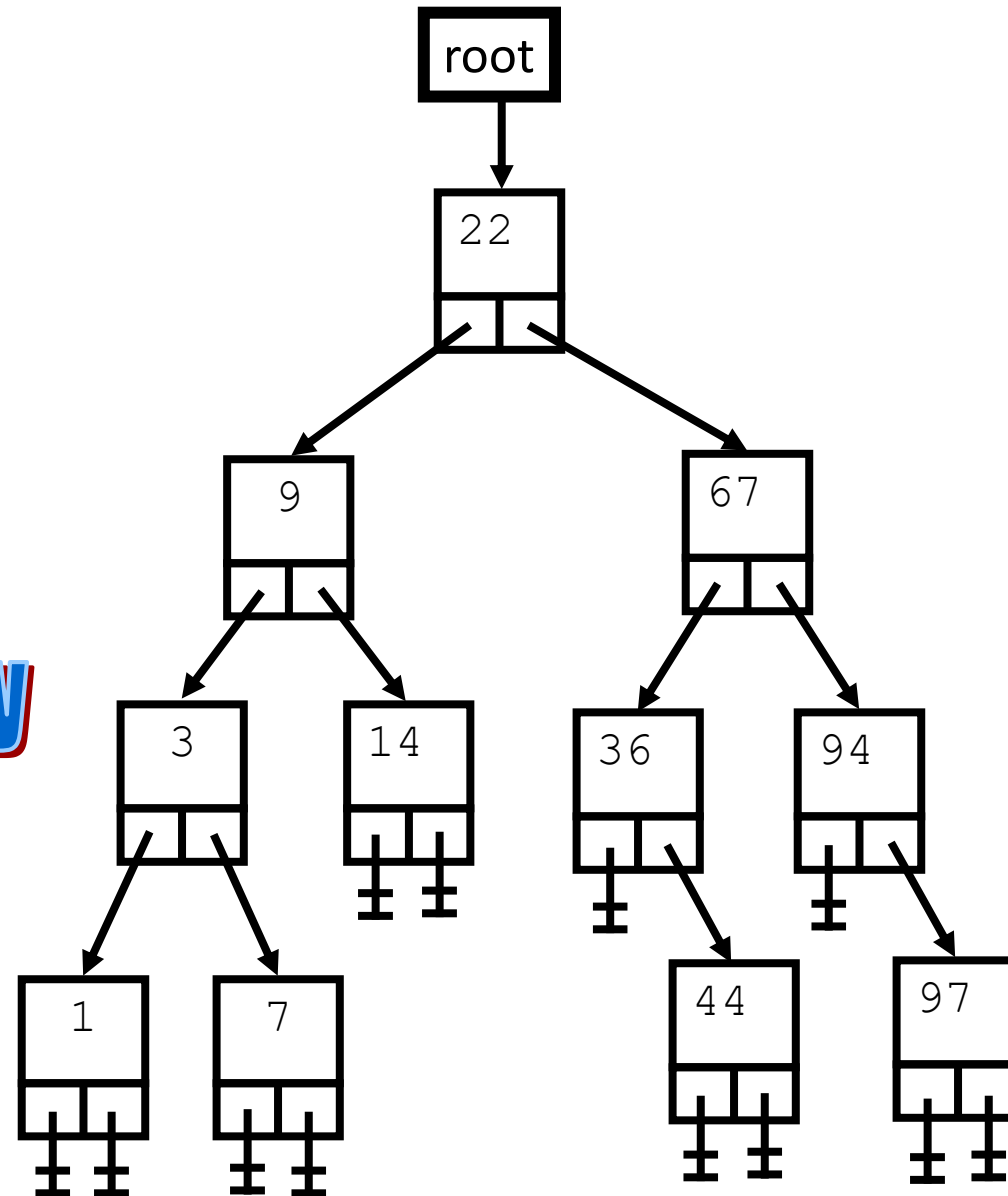
endprocedure

Move this here
to make a
Postorder DFT



```
Proc DFT(pointer)
  pointer NOT NIL?
    DFT(left child)
    print(data)
    DFT(right child)
```

**We have already
seen these!**



Breadth-First Traversal

Requires a **queue** to maintain which nodes to visit next.

Enqueue the root pointer

Loop until no elements in the queue

 Dequeue(current)

 Enqueue current's left and right children

 Do work at current

Breadth-First Traversal

```
Procedure BFT(root isoftype in Ptr toa Node)
  Q isoftype Queue
  Initialize(Q)
  temp isoftype Ptr toa Node
  OK isoftype Boolean
  enqueue(Q, root)
  // continued
```

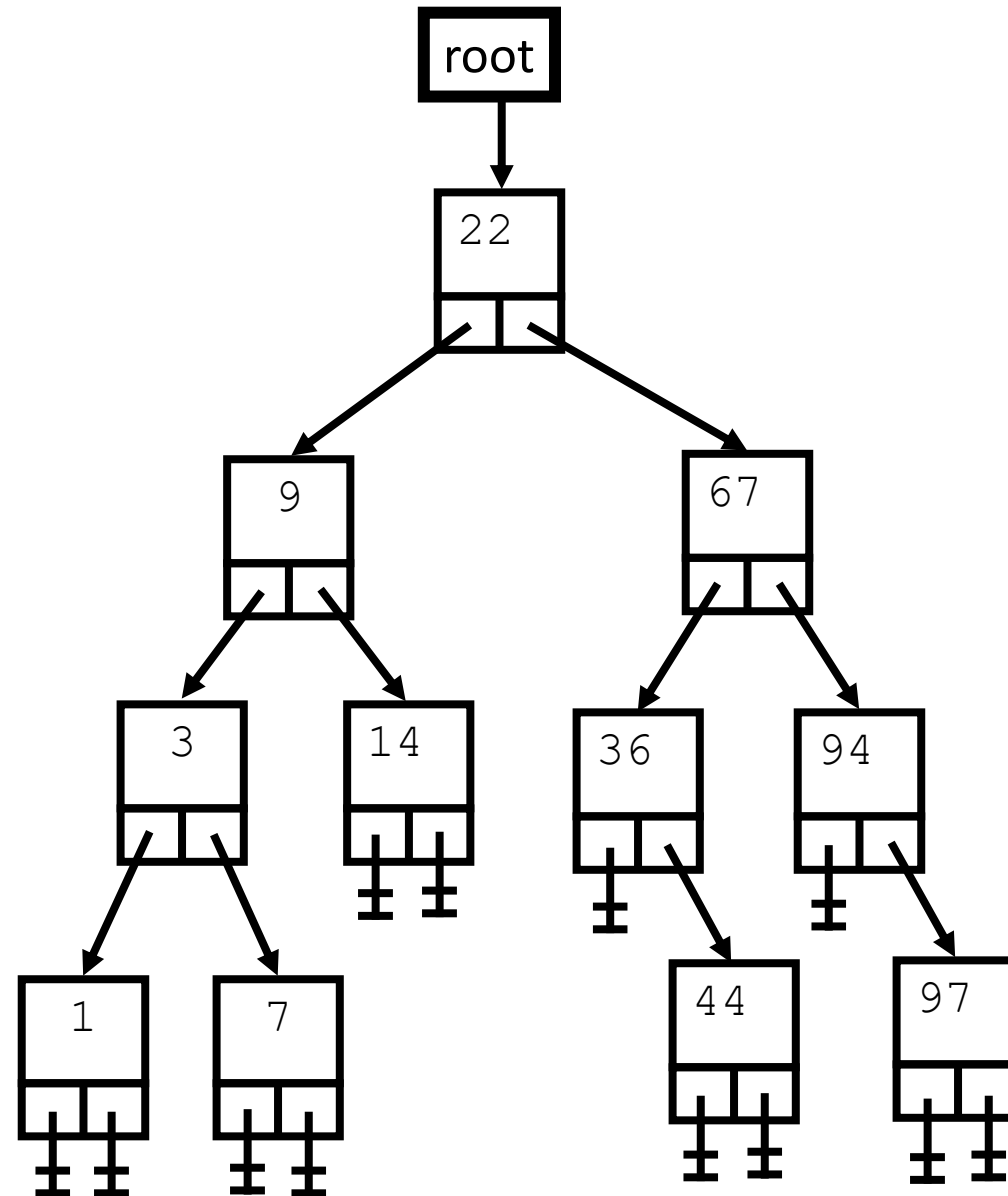
Breadth-First Traversal

```
loop
  dequeue(temp, OK, Q)
  exitif(NOT OK)
  if(temp^.left <> NIL) then
    enqueue(temp^.left, Q)
  endif
  if(temp^.right <> NIL) then
    enqueue(temp^.right, Q)
  endif
  print(temp^.data) // processing node
endloop
endprocedure
```

```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (data)
endloop
```

Q:

aNode:



Enqueue (root)

loop

 exitif Q empty

 dequeue (aNode)

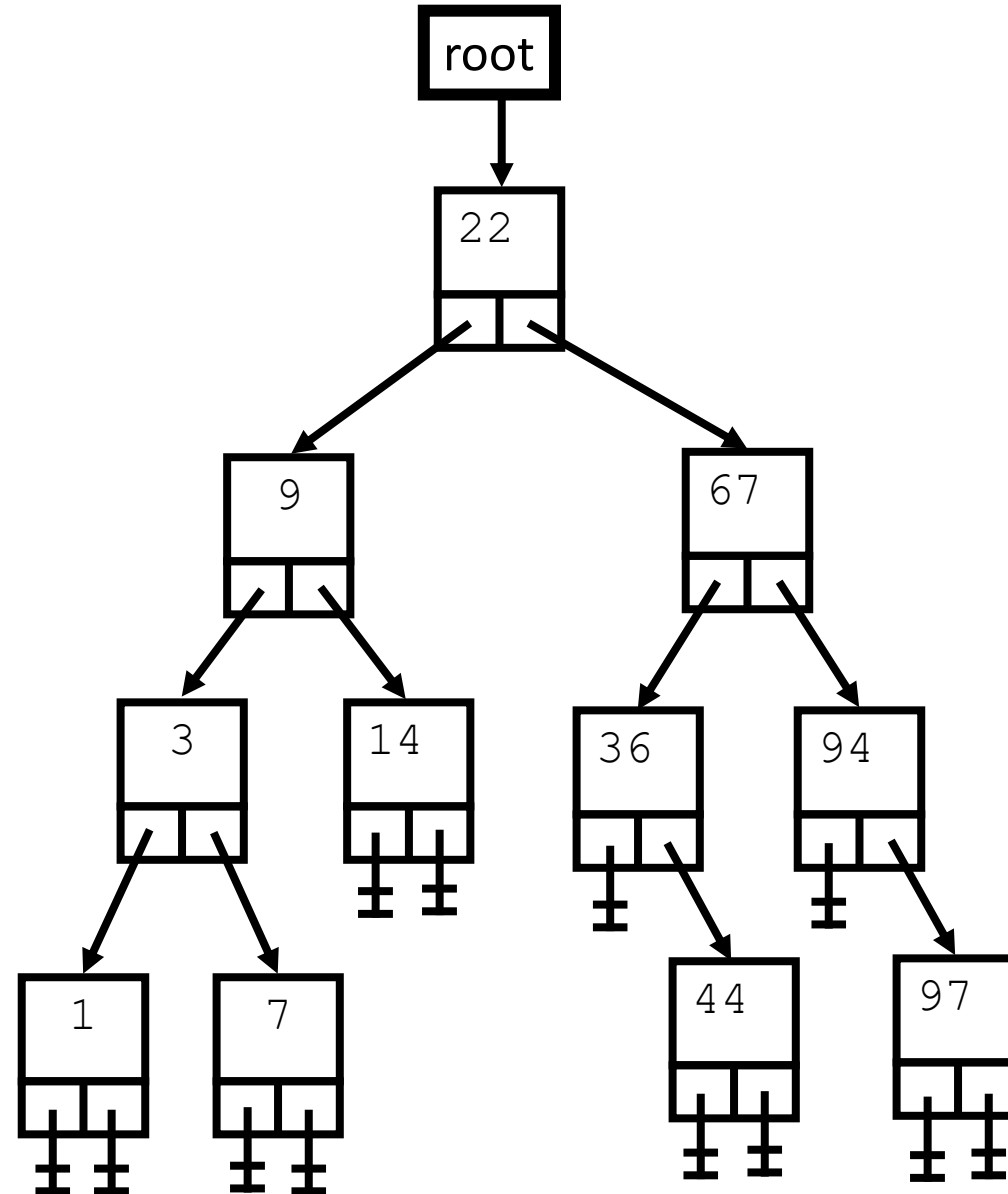
 enqueue (children)

 print (data)

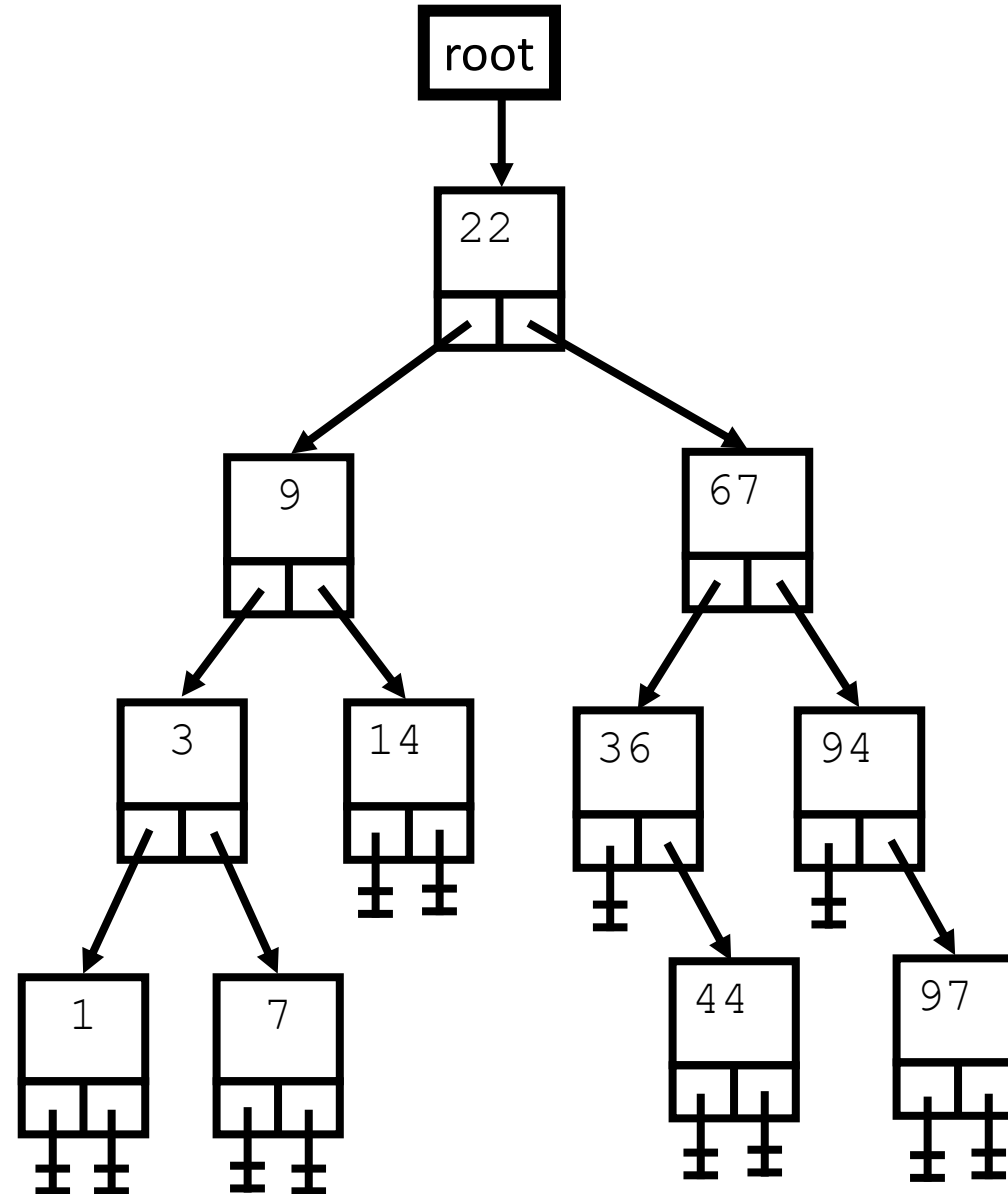
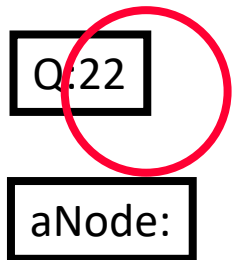
endloop

Q:22

aNode:



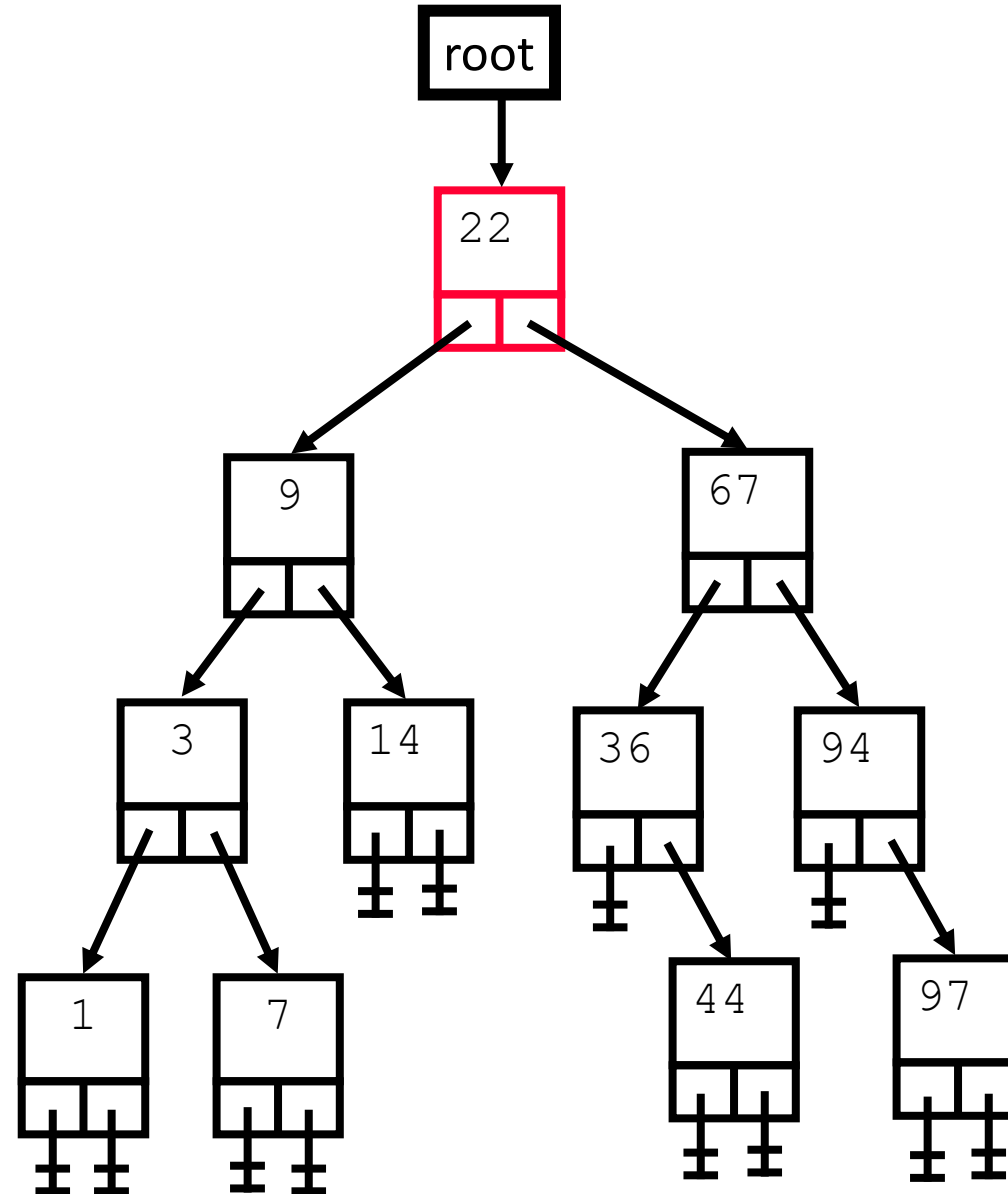
```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (data)
endloop
```



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:

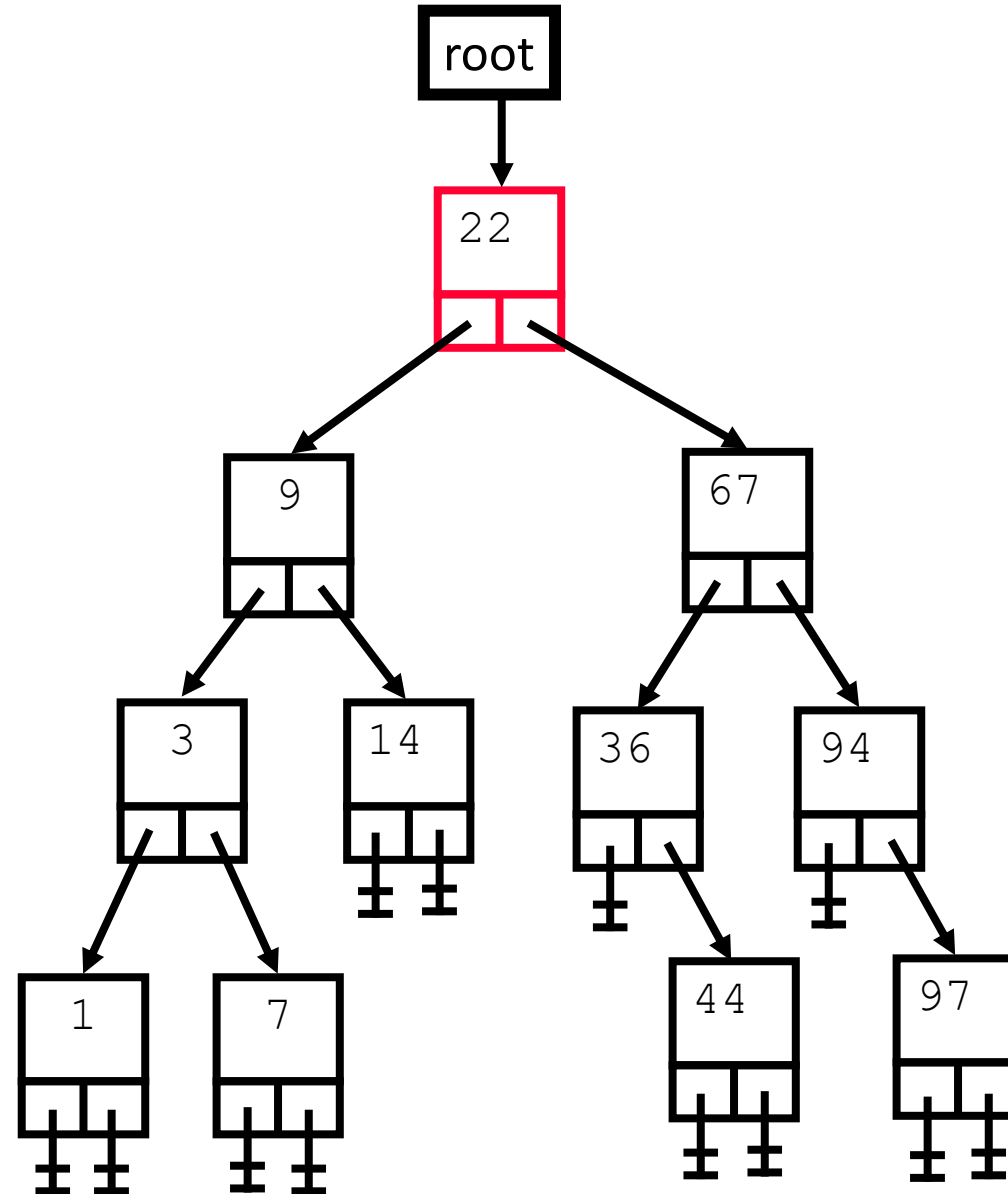
aNode:22



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:9 67

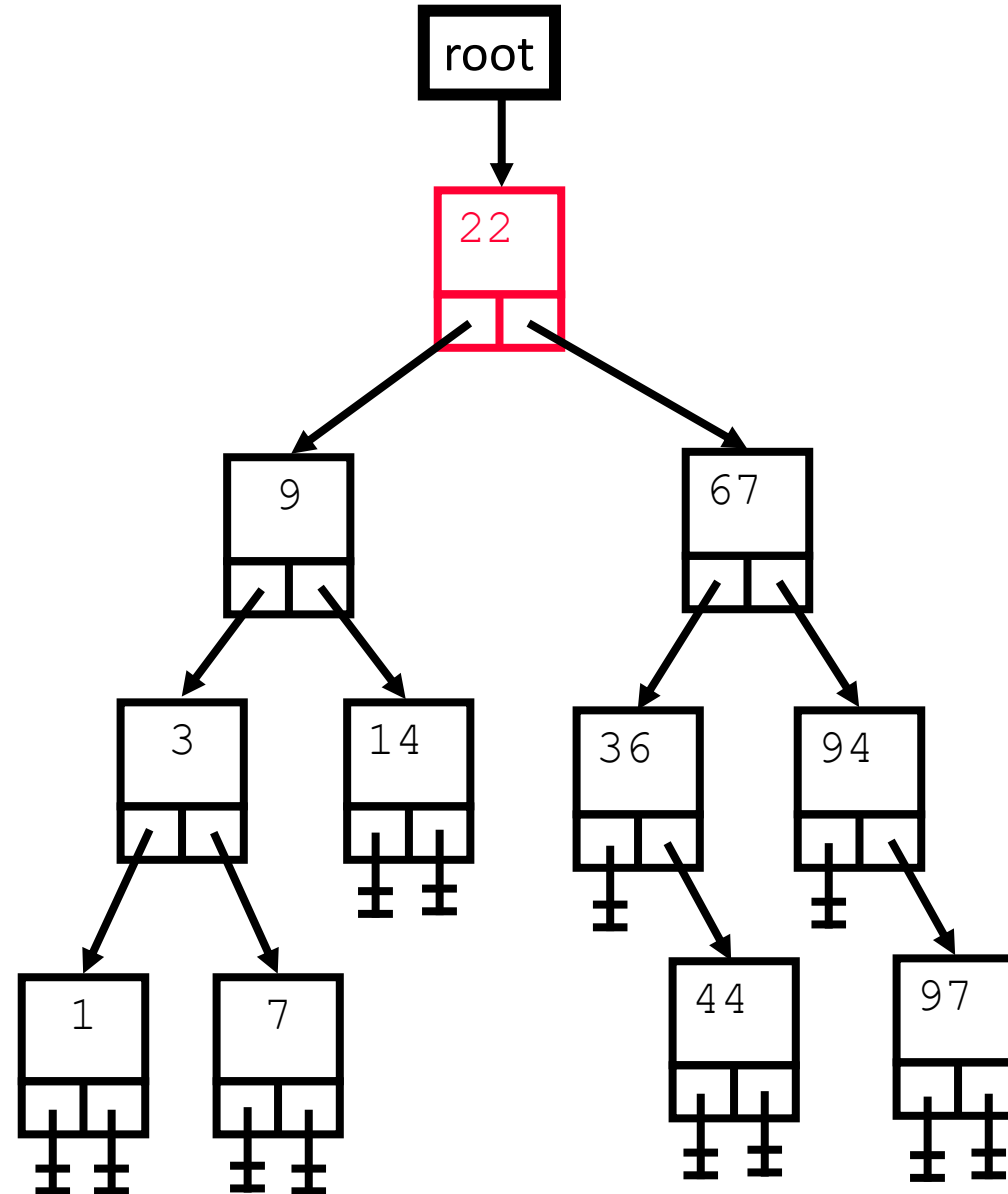
aNode:22




```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:9 67

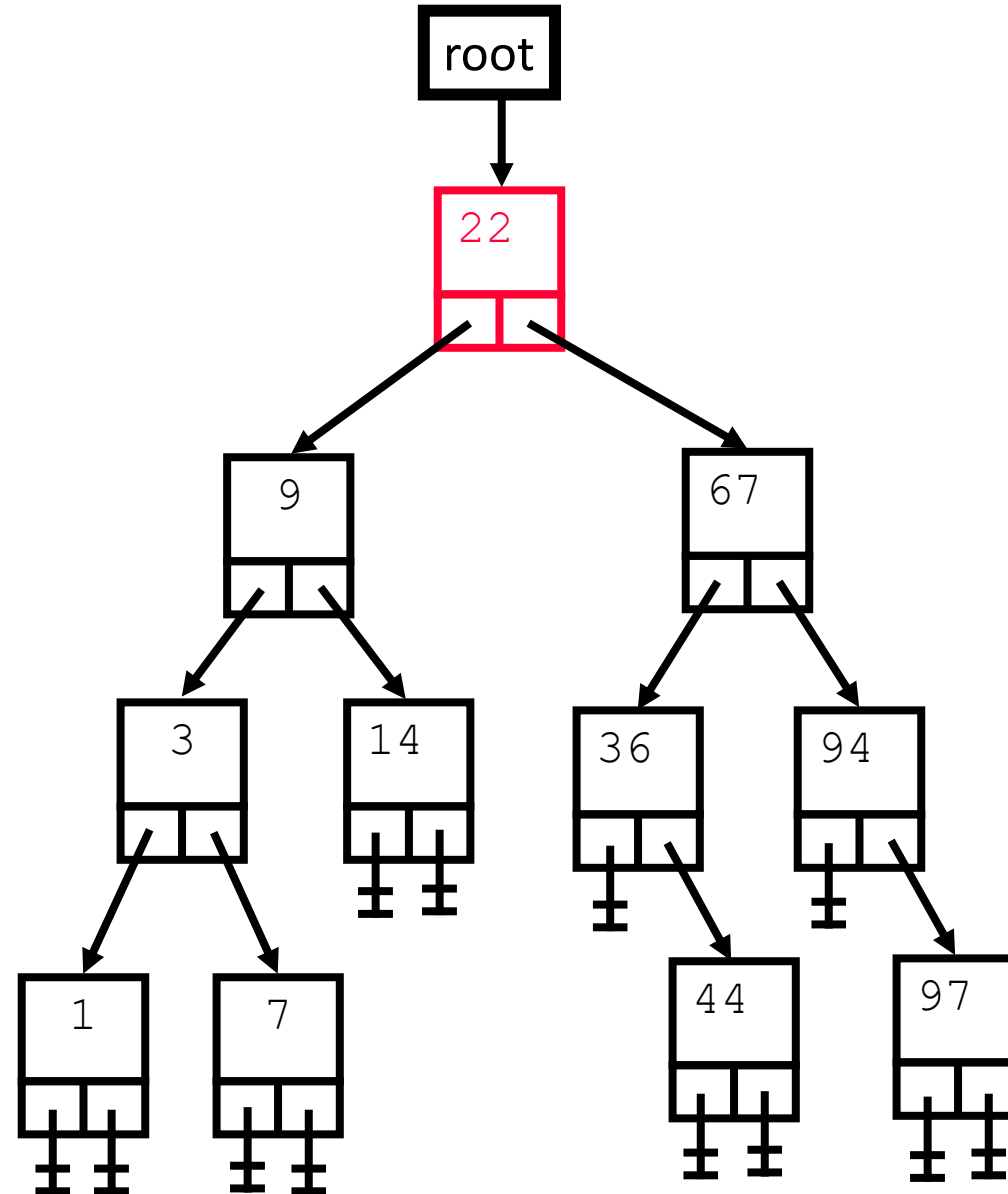
aNode:22



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:9 67

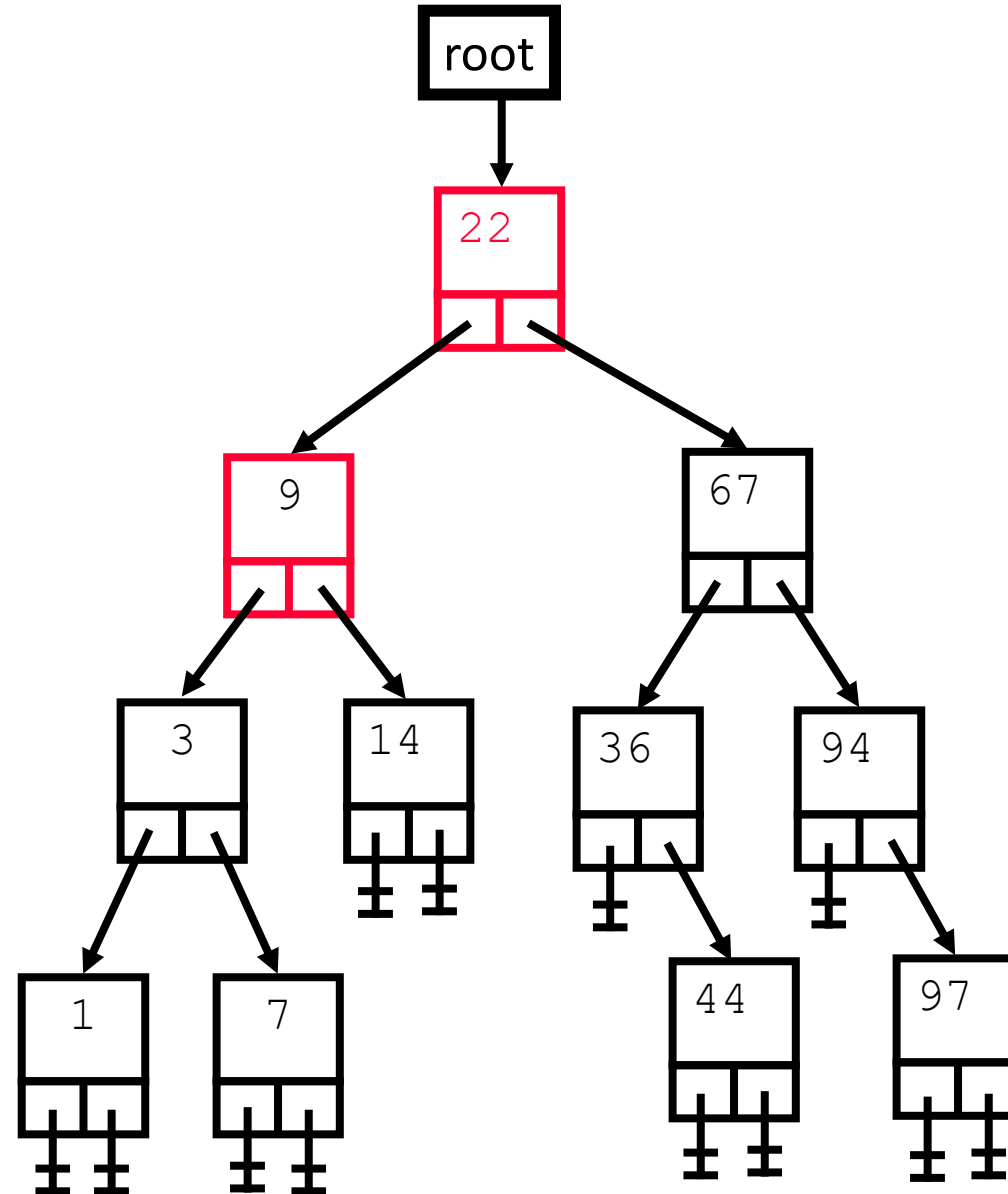
aNode:22



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:67

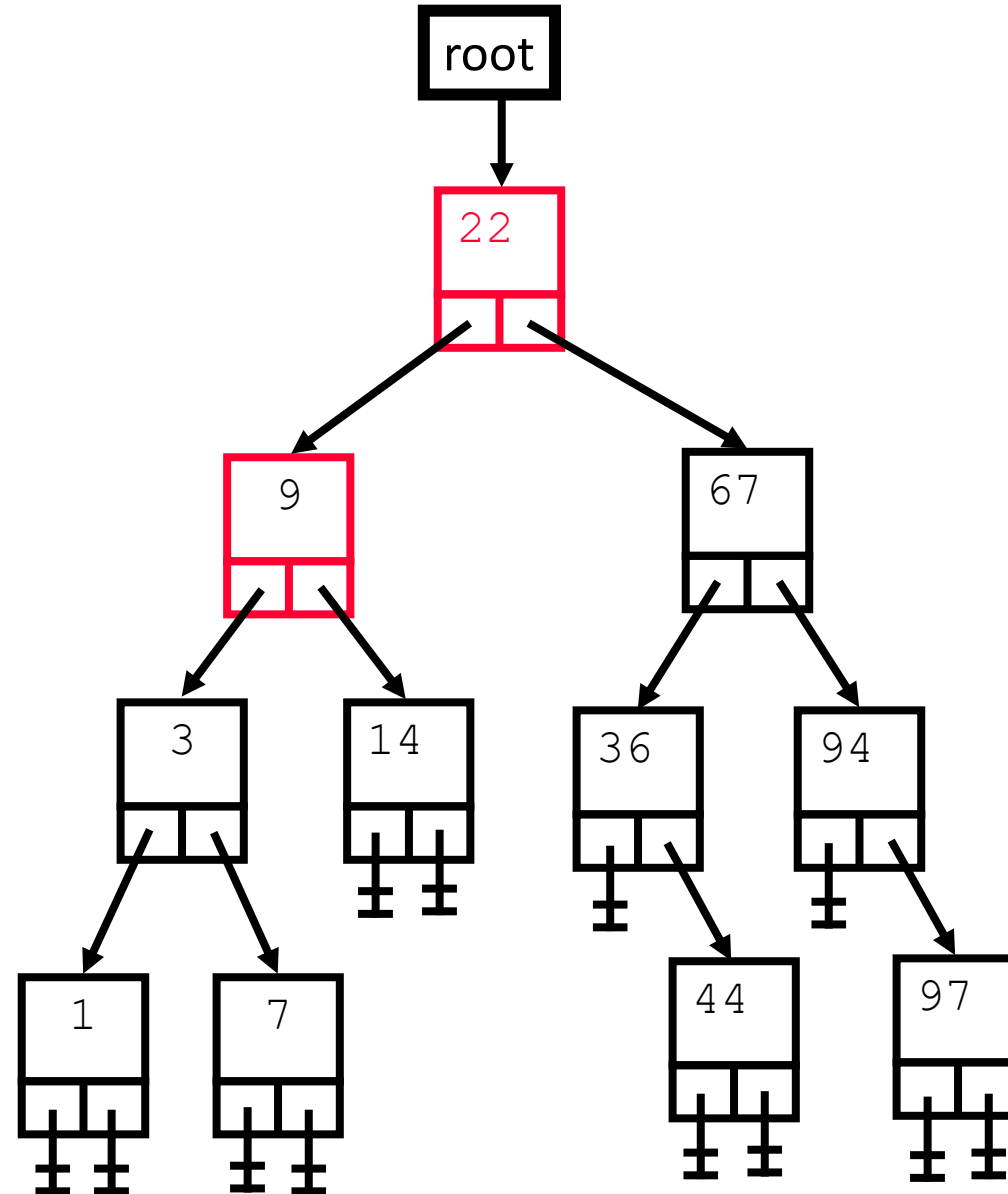
aNode:9



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:67 3 14

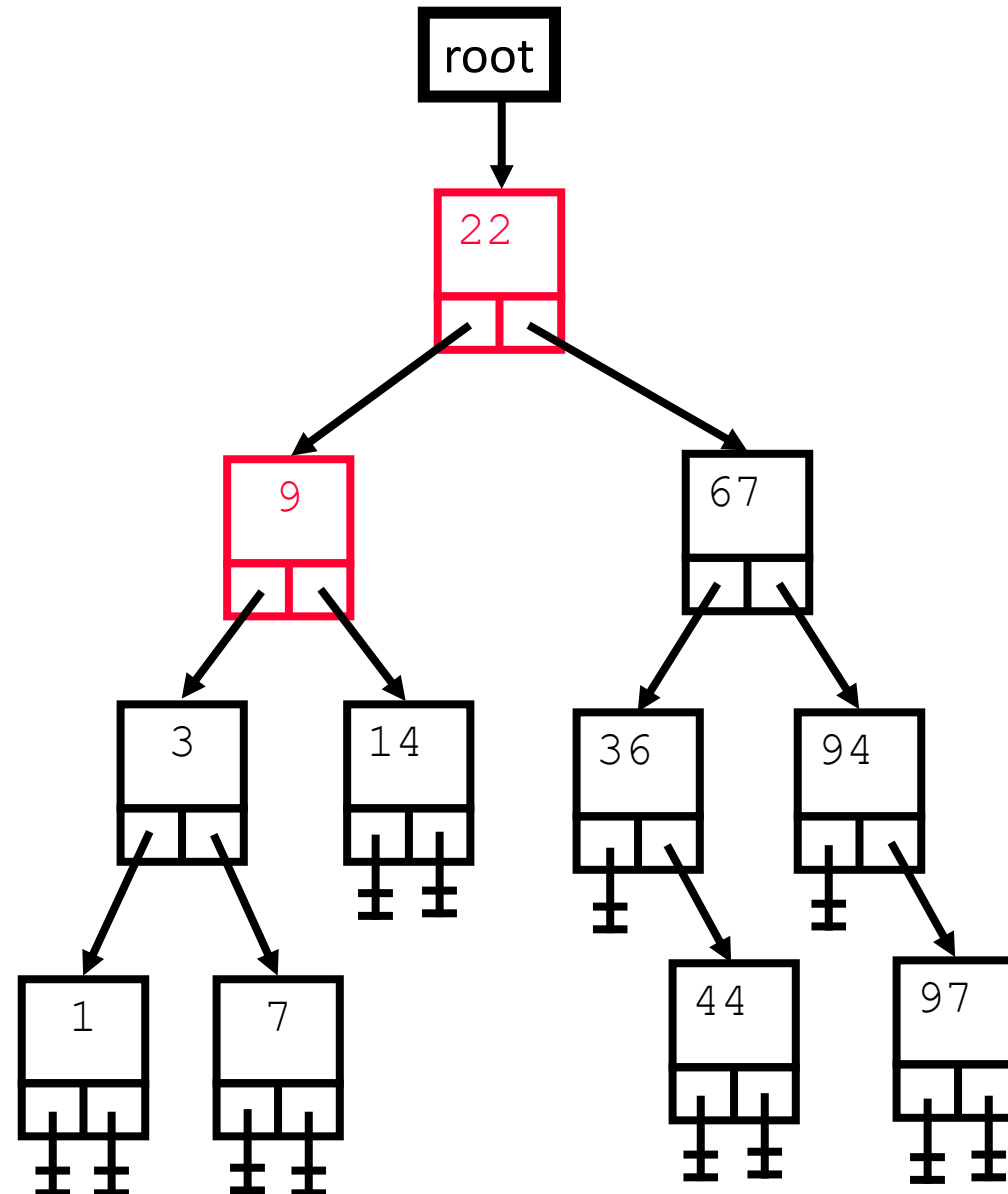
aNode:9



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:67 3 14

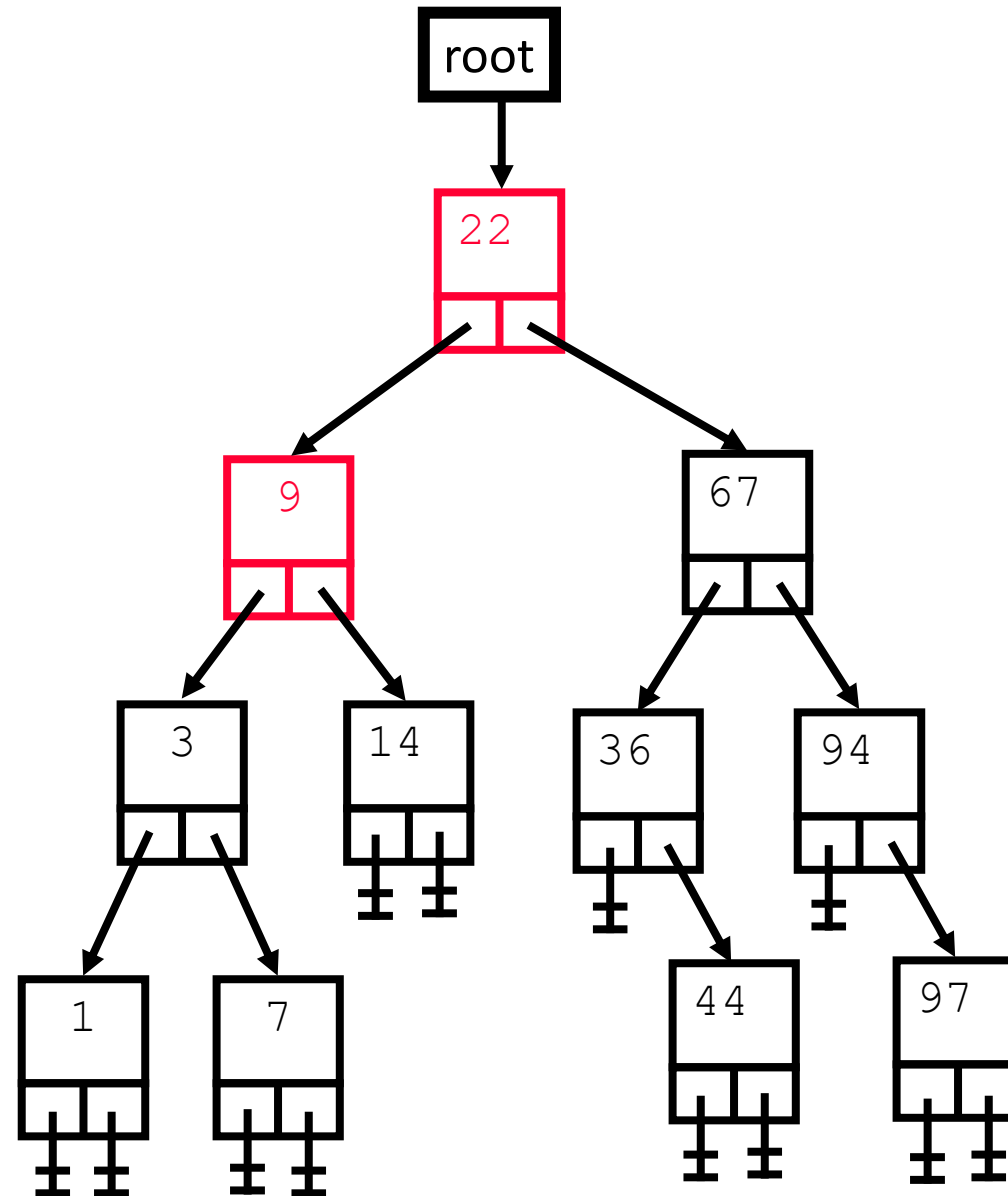
aNode:9



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:67 3 14

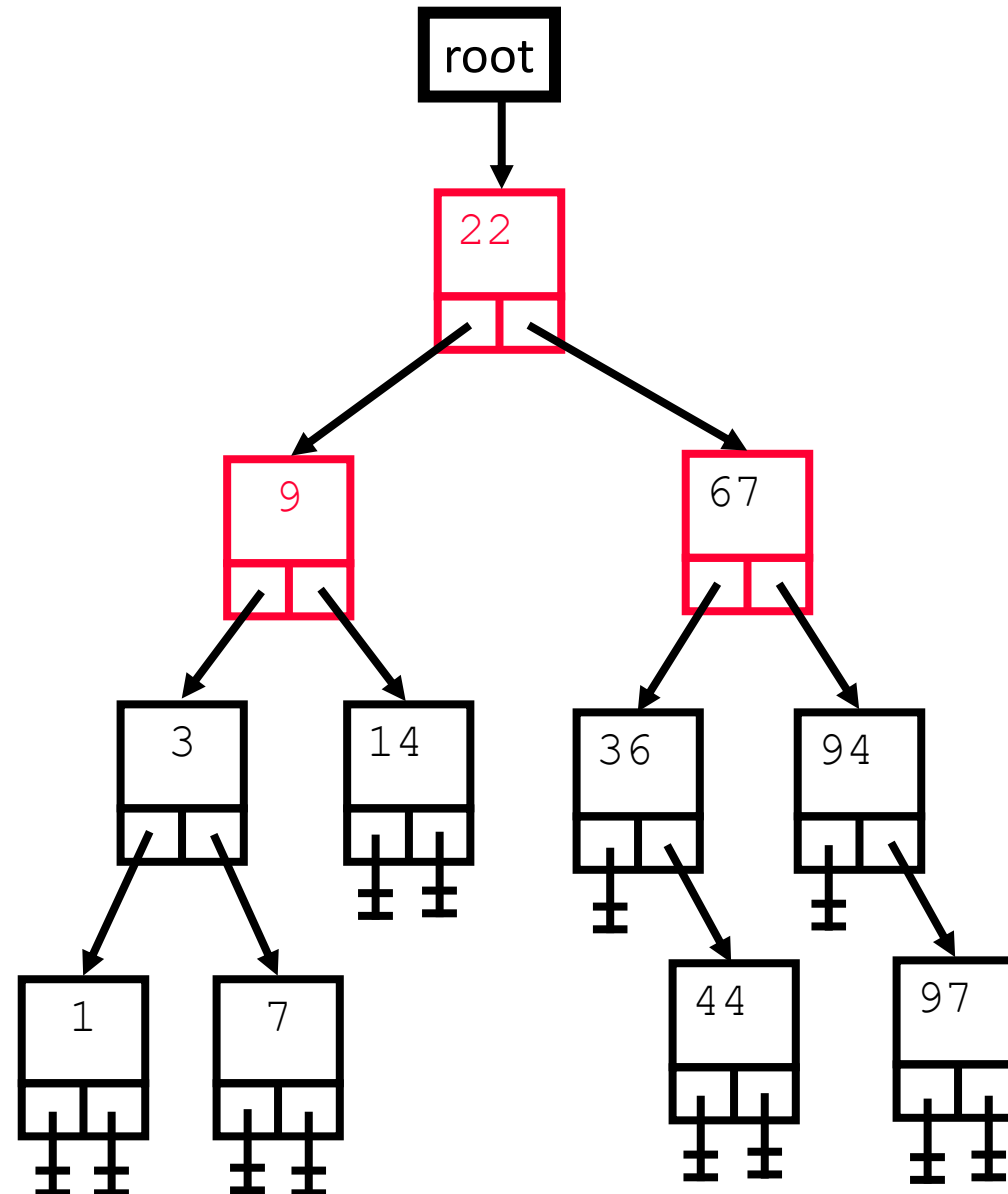
aNode:9



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:3 14

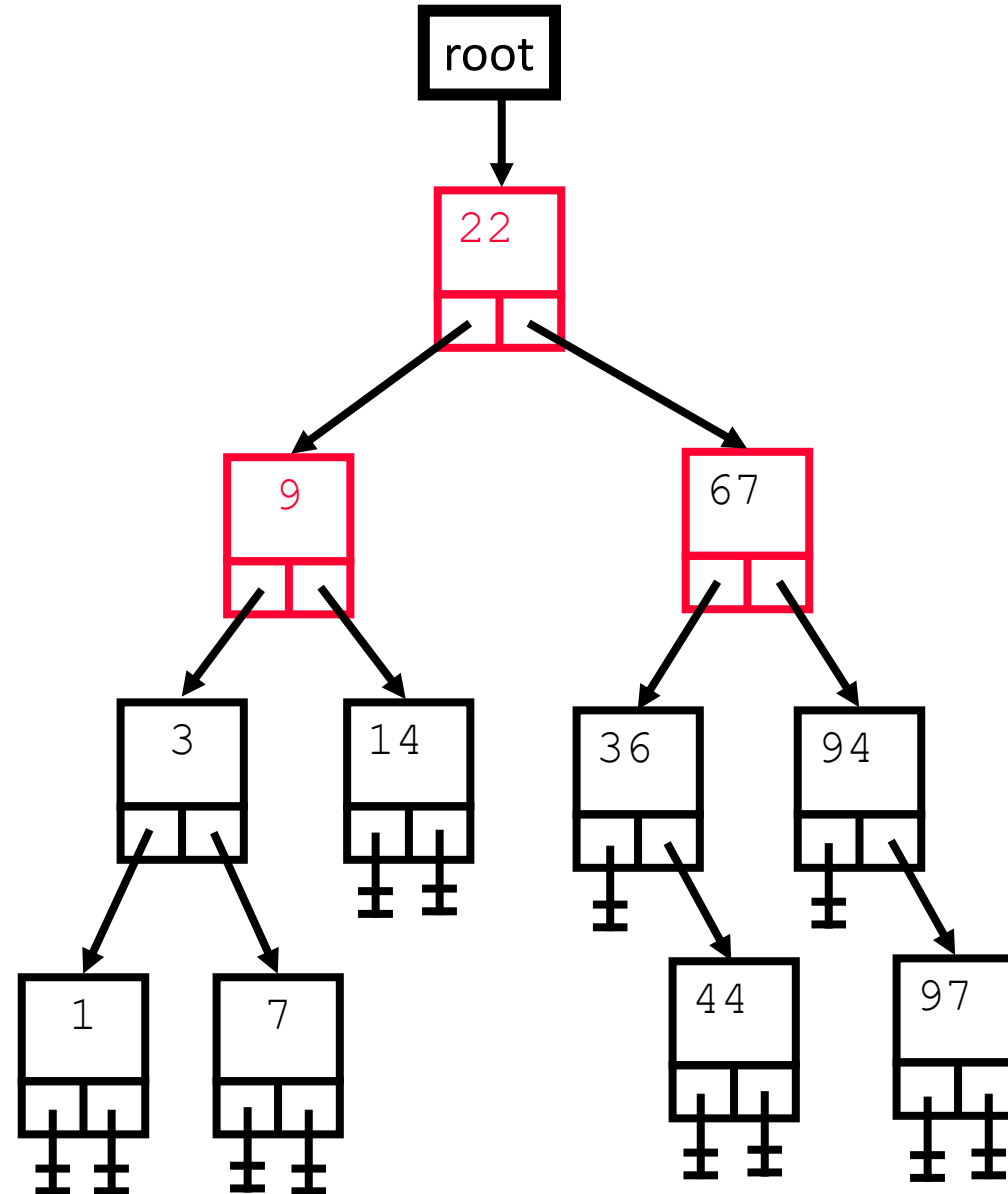
aNode:67



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:3 14 36 94

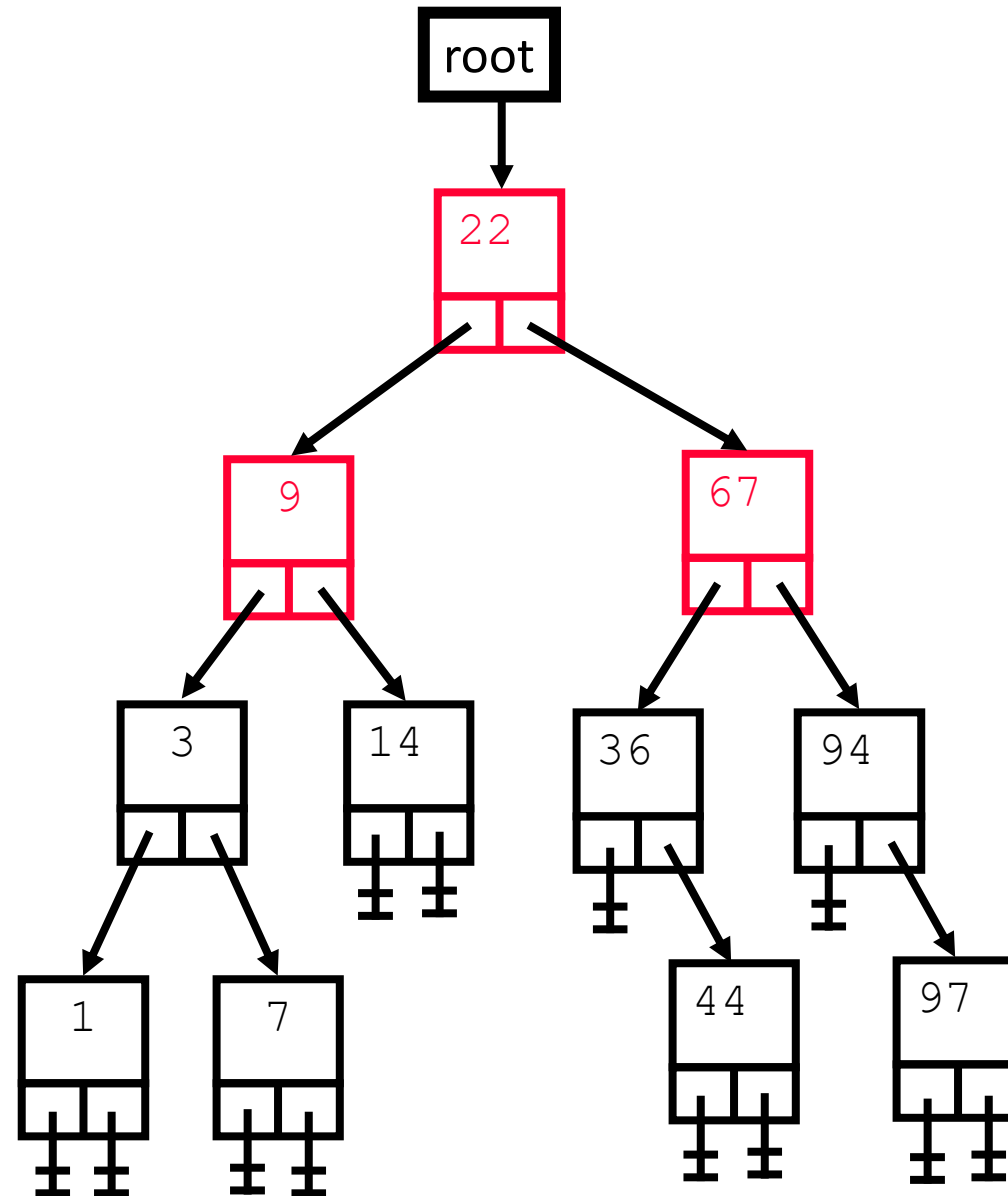
aNode:67




```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:3 14 36 94

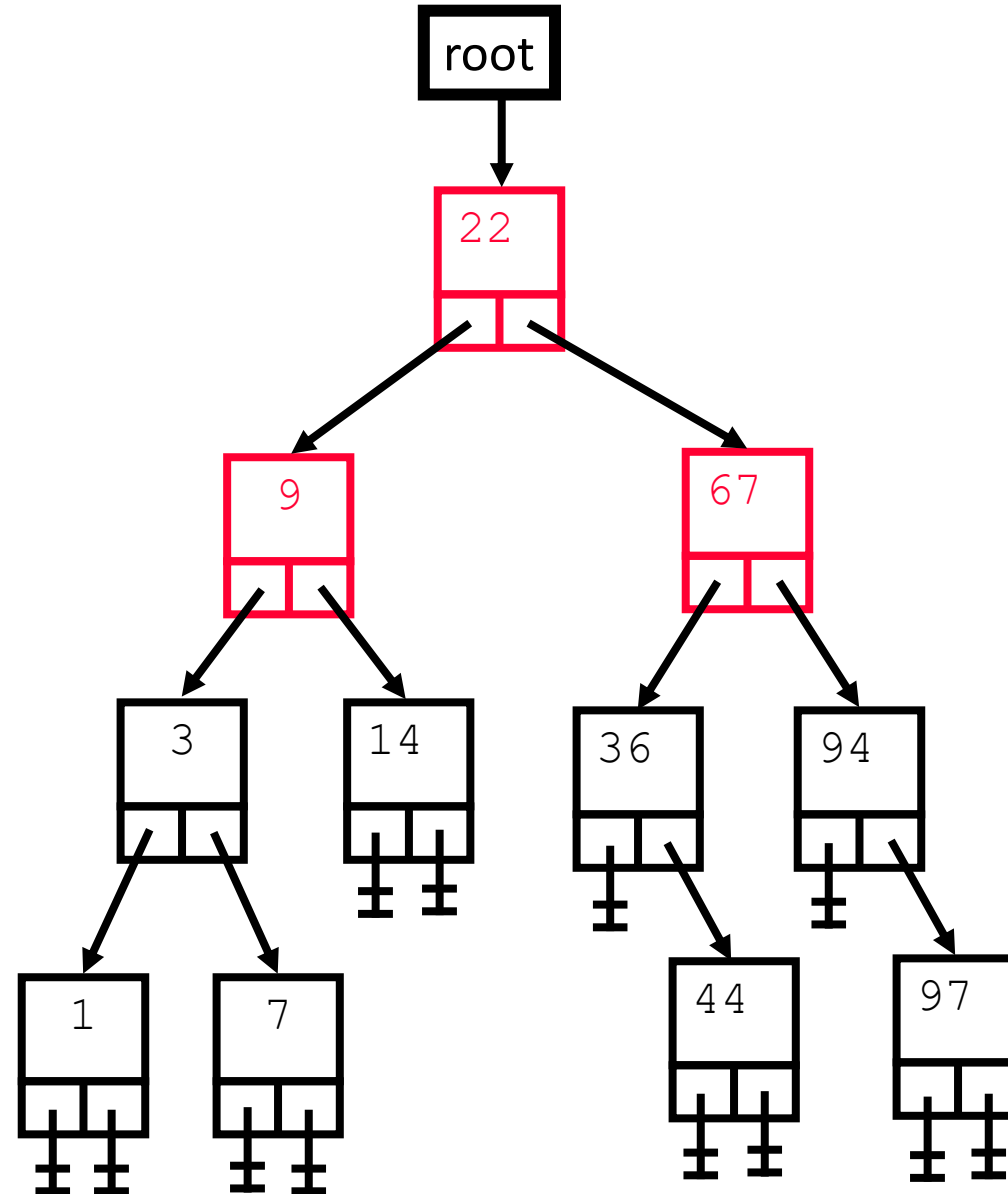
aNode:67



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:3 14 36 94

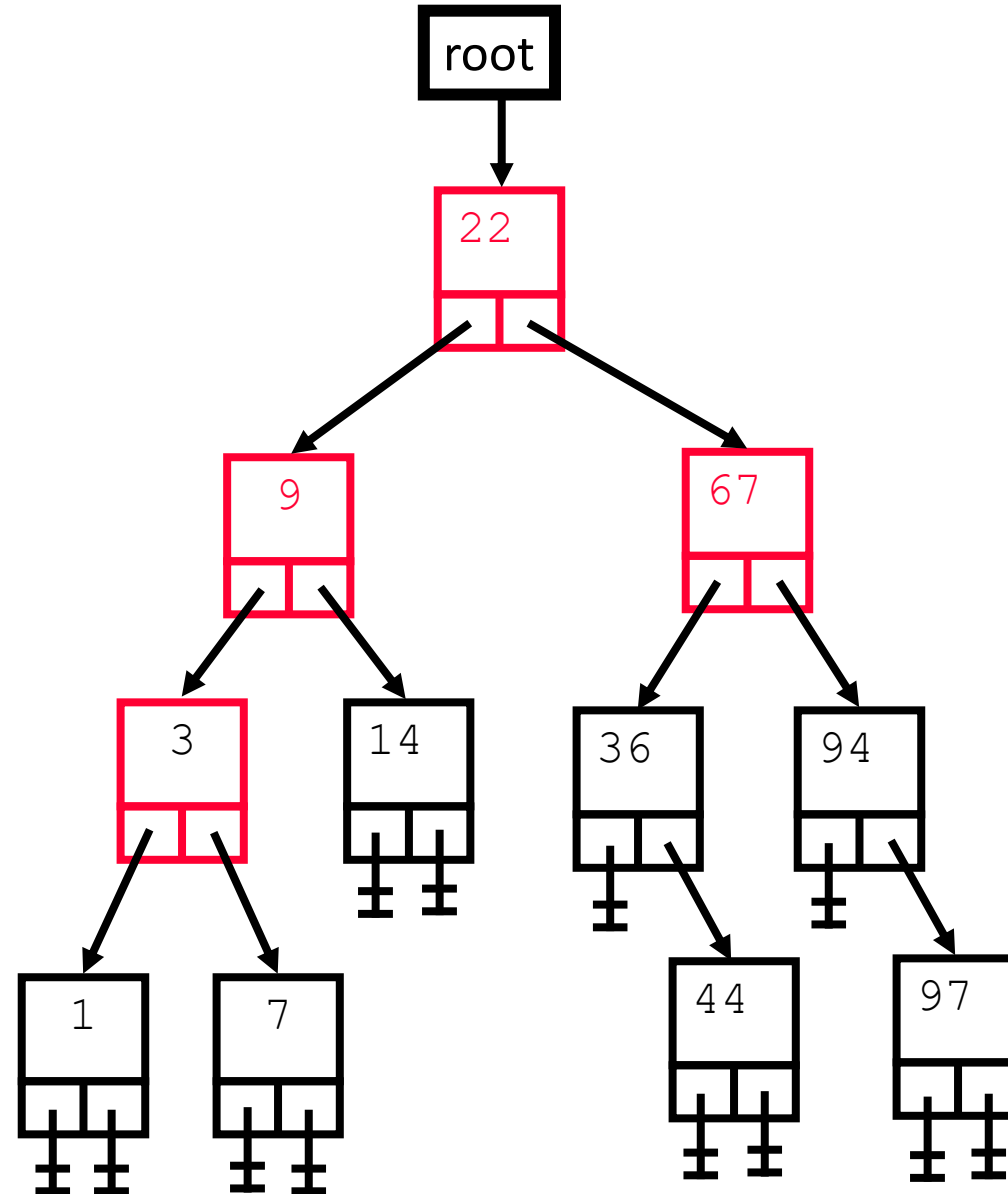
aNode:67



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:14 36 94

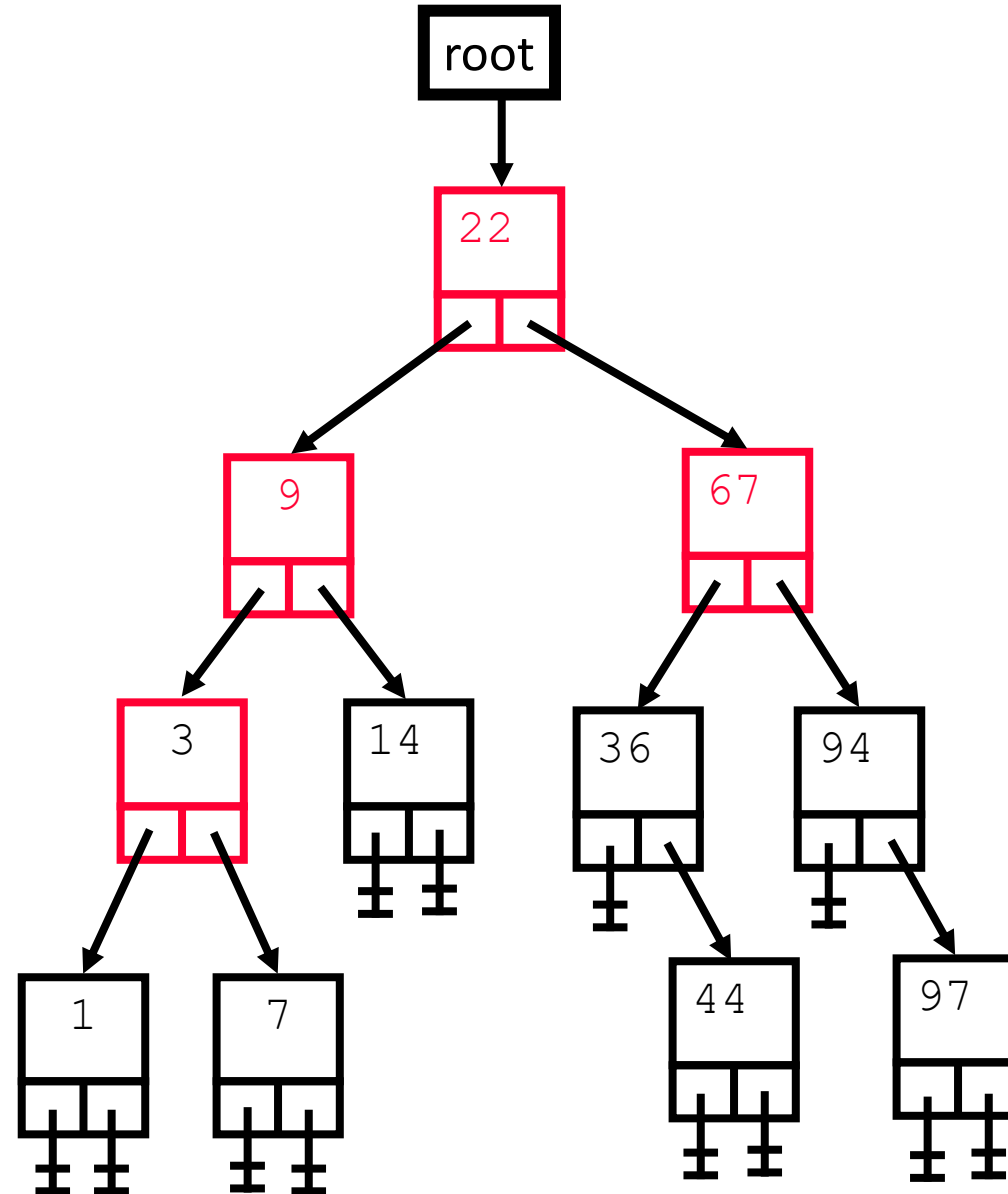
aNode:3



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:14 36 94 1 7

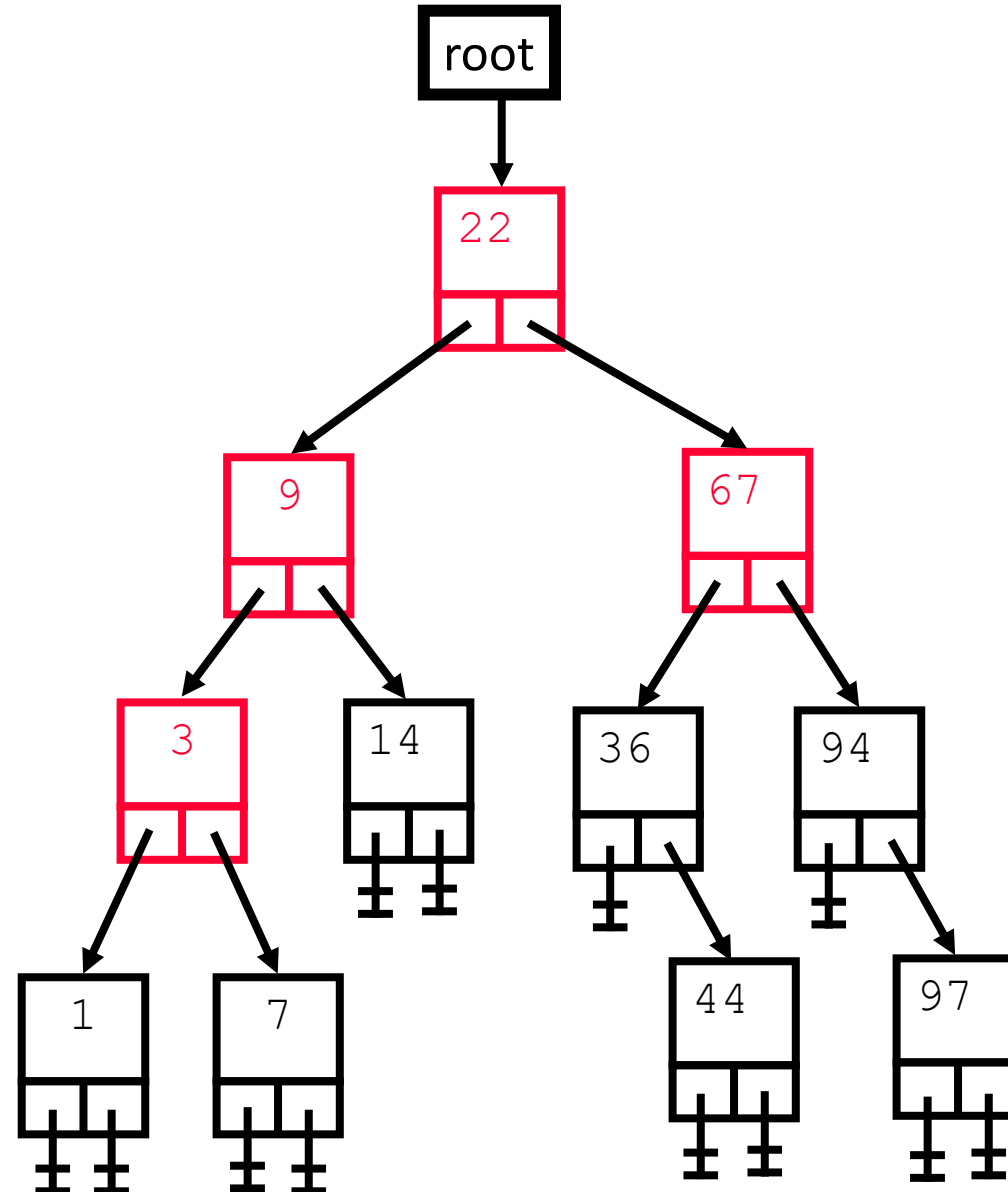
aNode:3



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:14 36 94 1 7

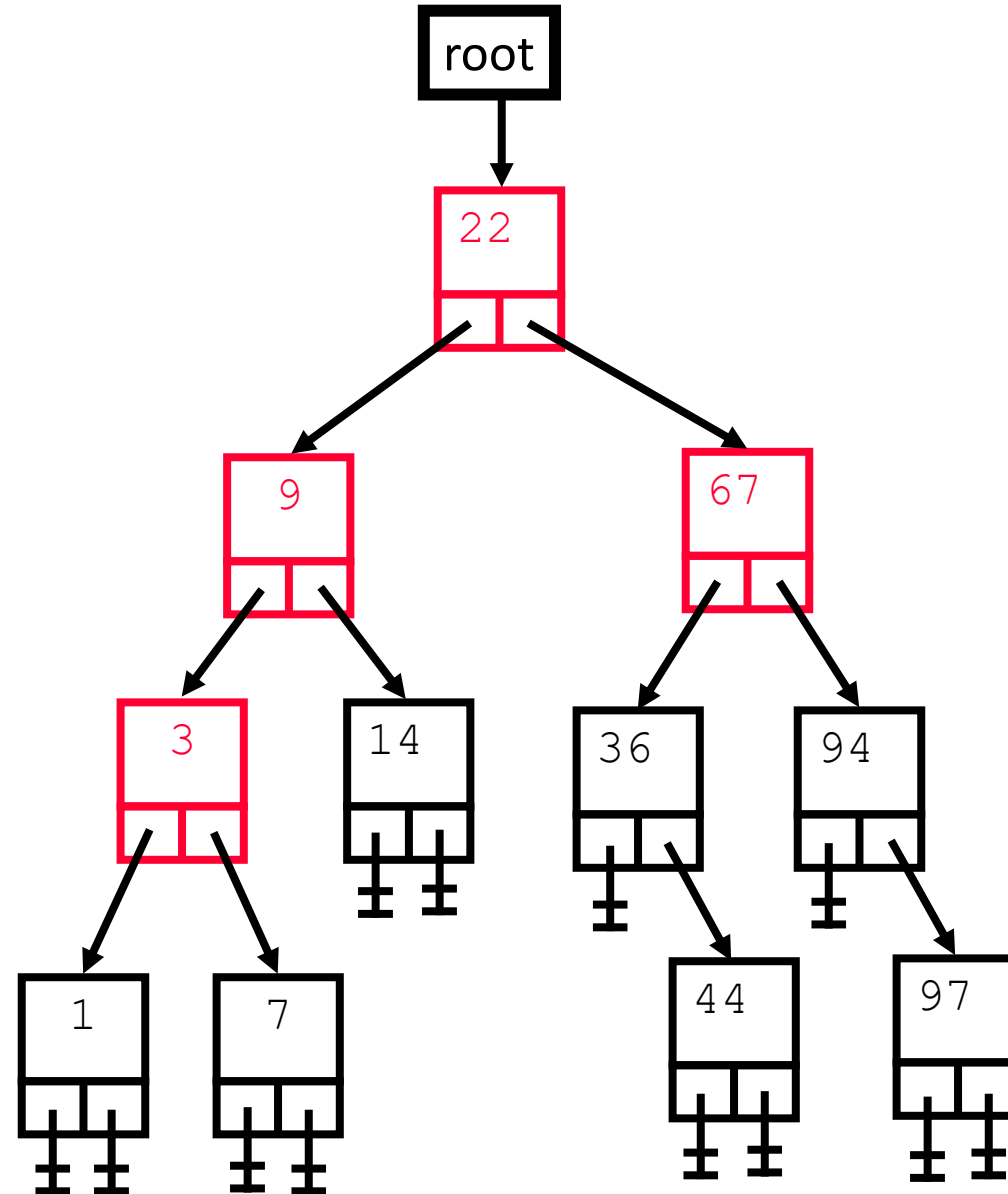
aNode:3



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:14 36 94 1 7

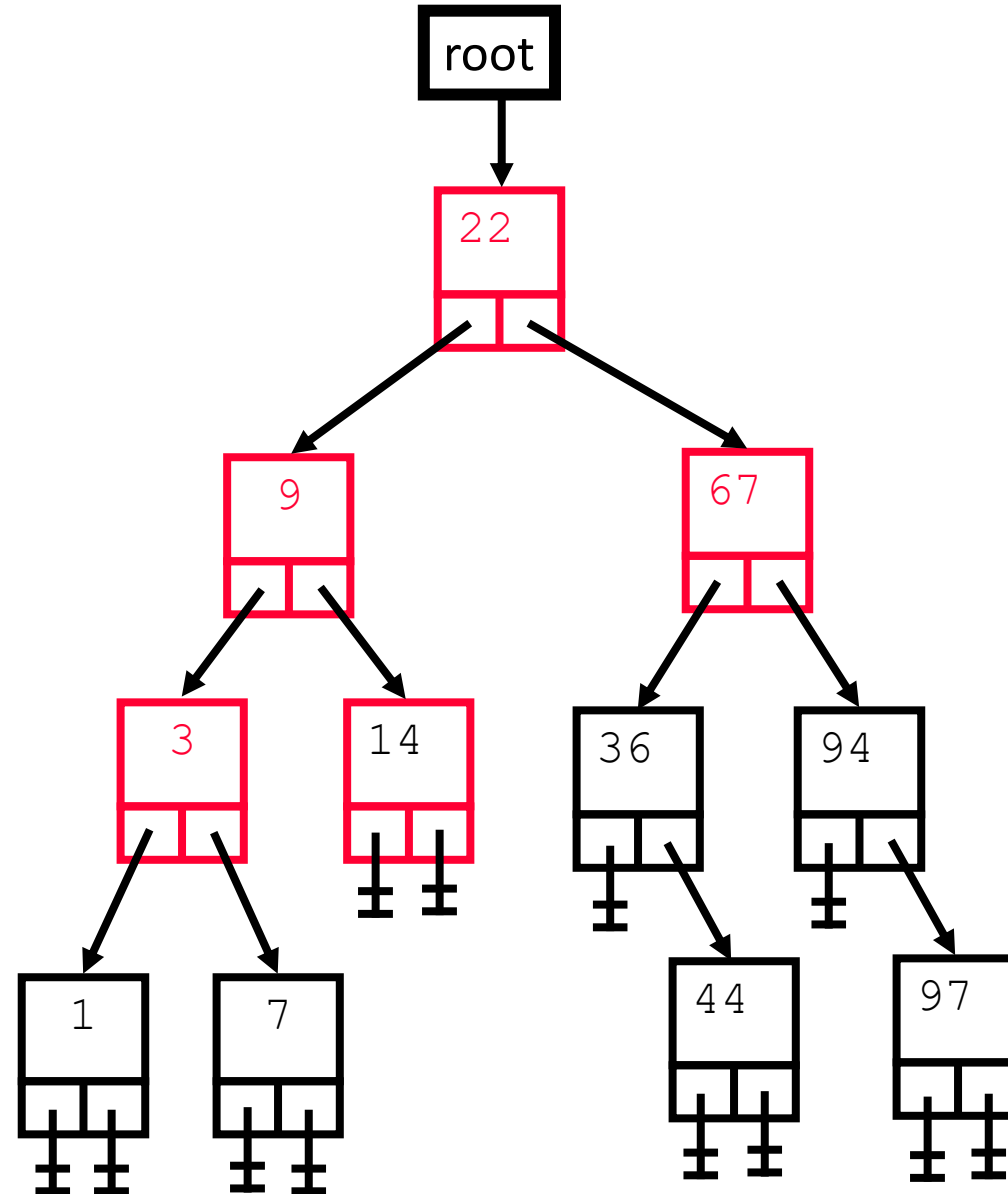
aNode:3



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:36 94 1 7

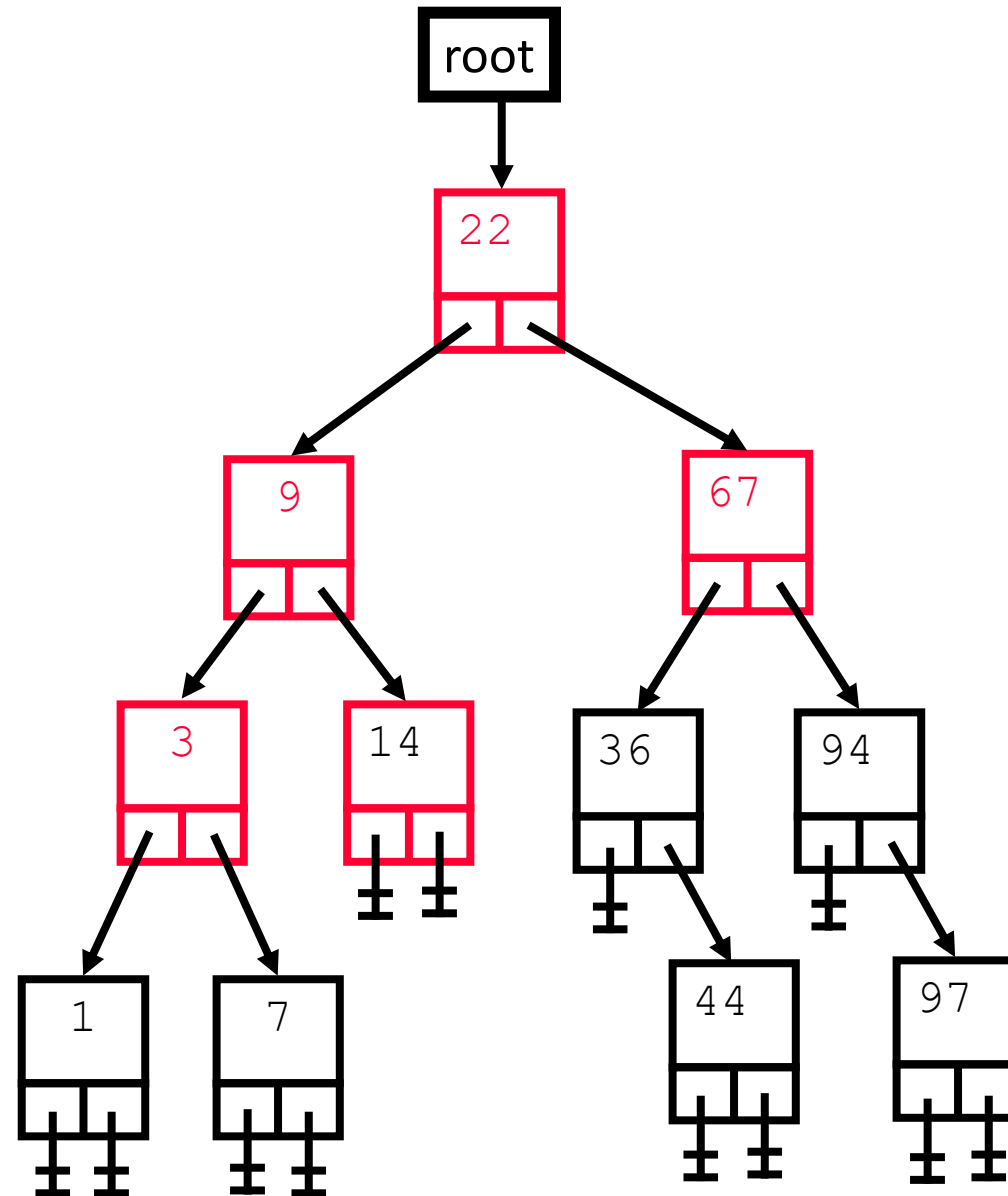
aNode:14



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:36 94 1 7

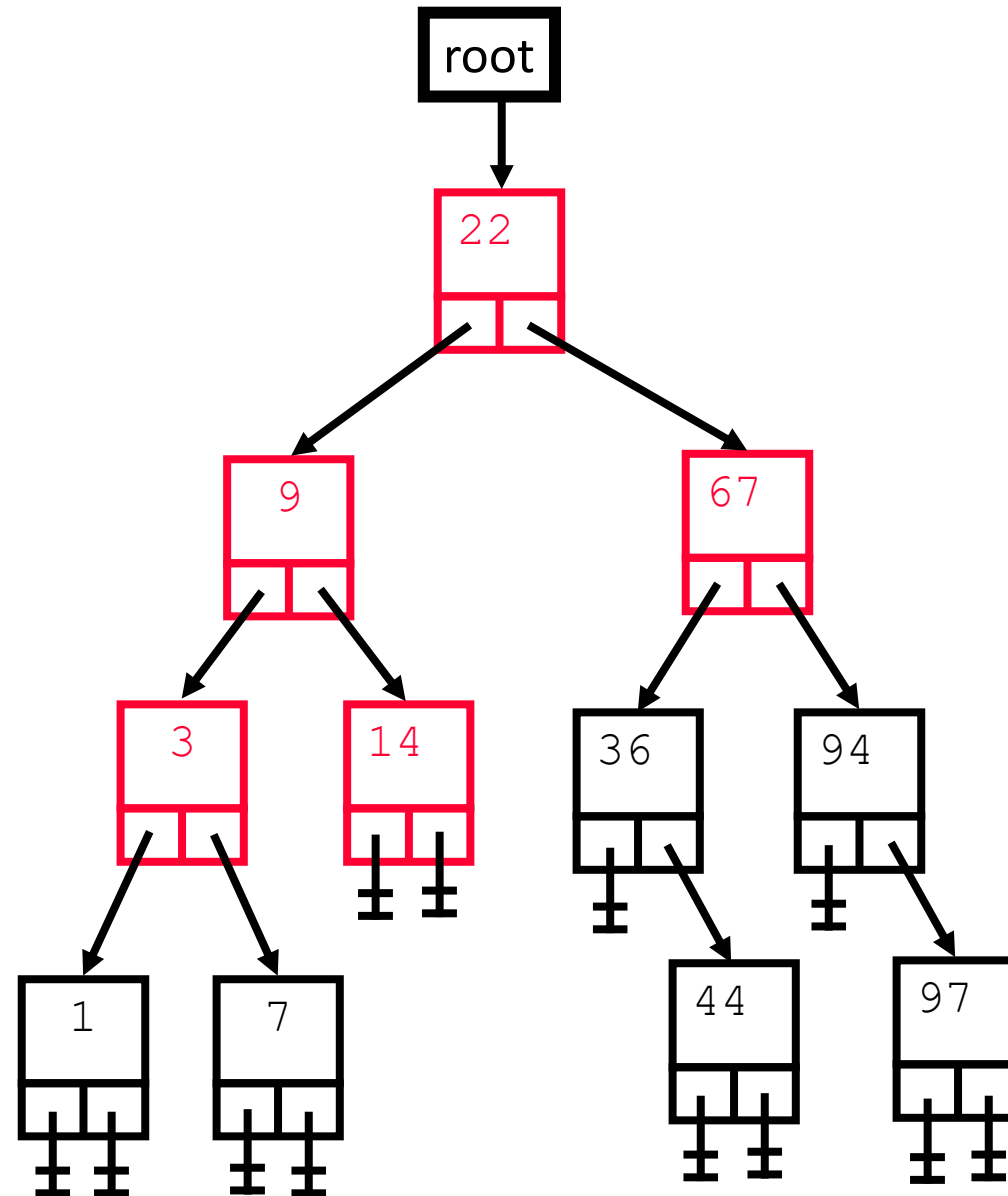
aNode:14




```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:36 94 1 7

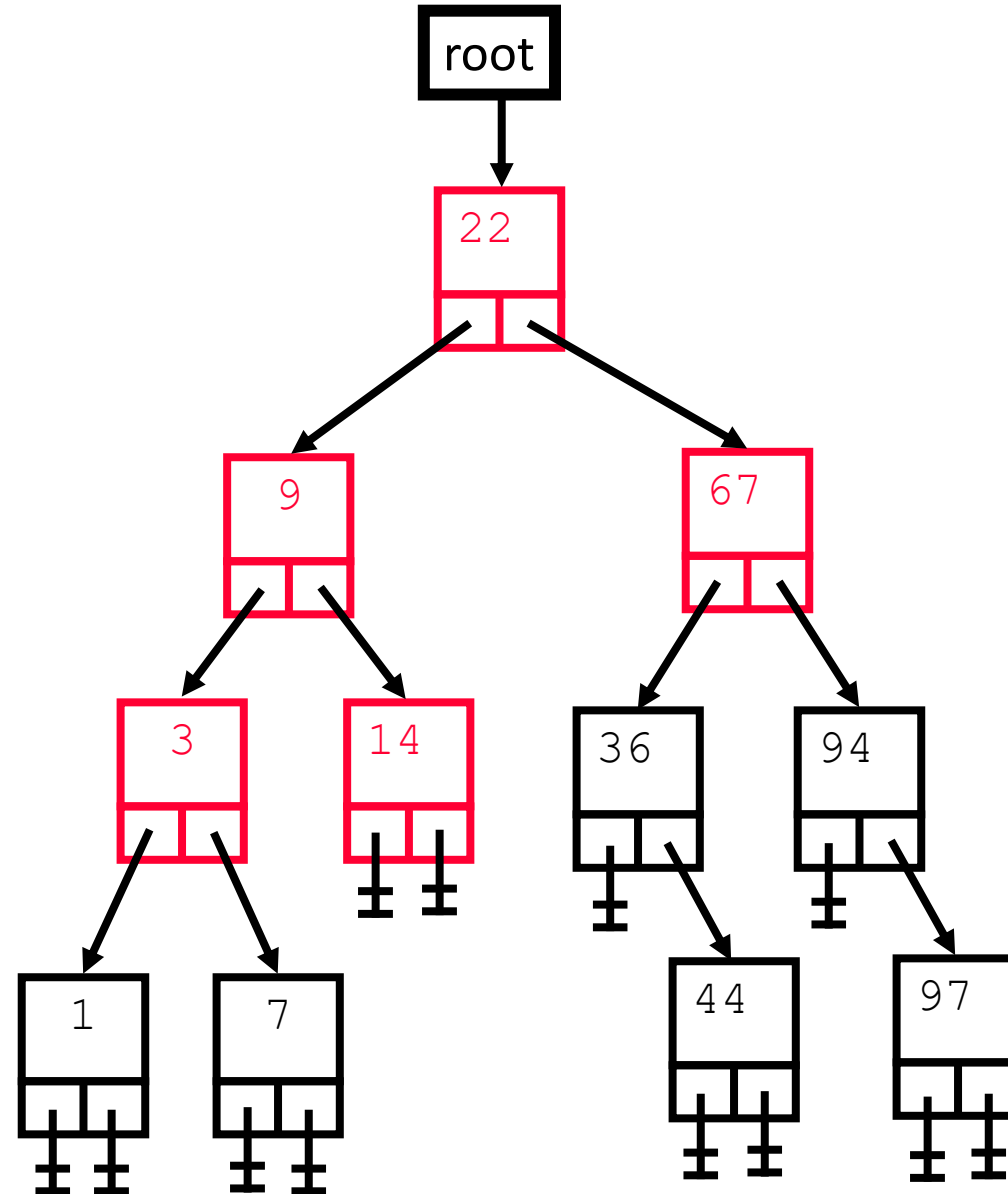
aNode:14



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:36 94 1 7

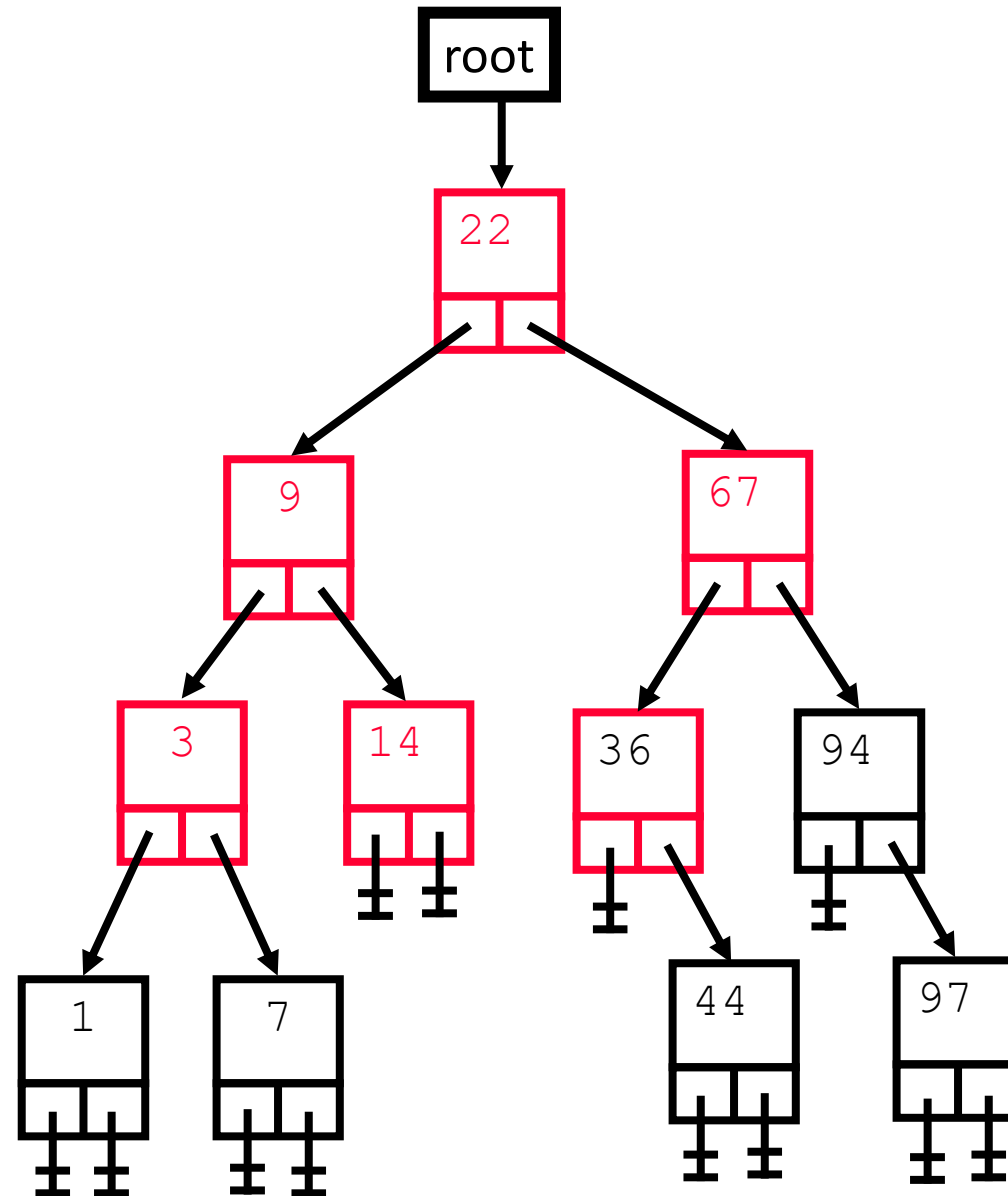
aNode:14



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:94 1 7

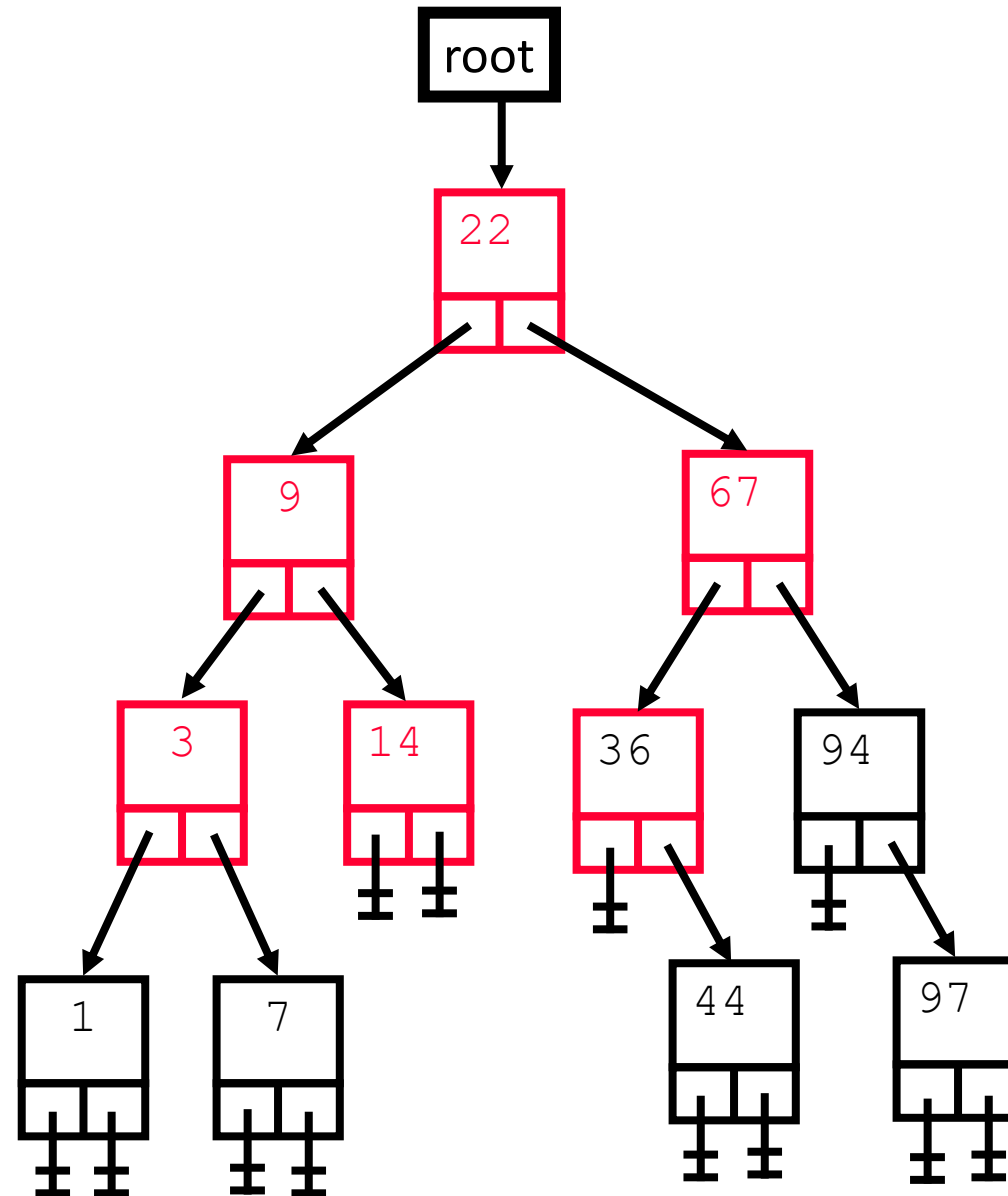
aNode:36



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:94 1 7 44

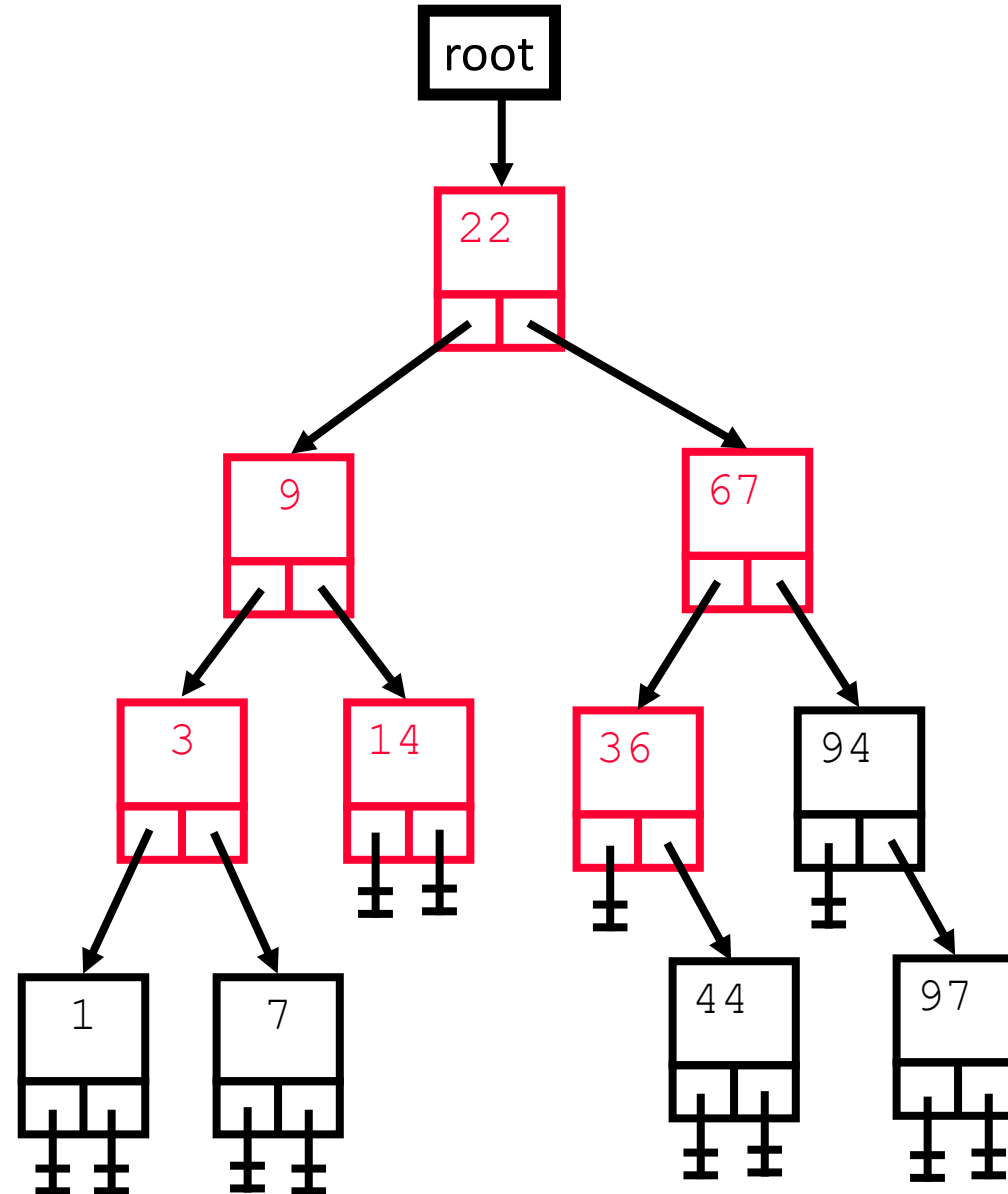
aNode:36



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:94 1 7 44

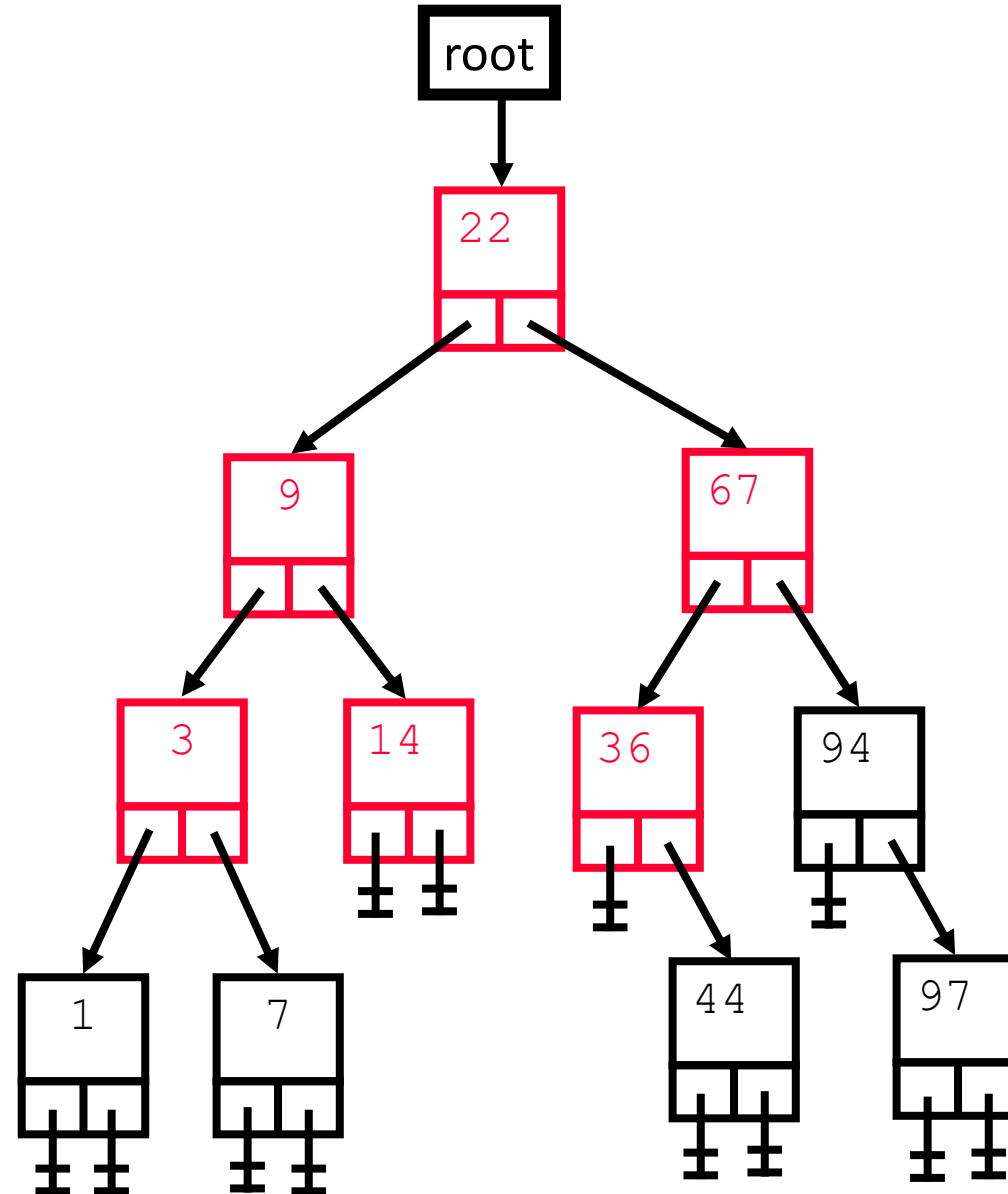
aNode:36



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:94 1 7 44

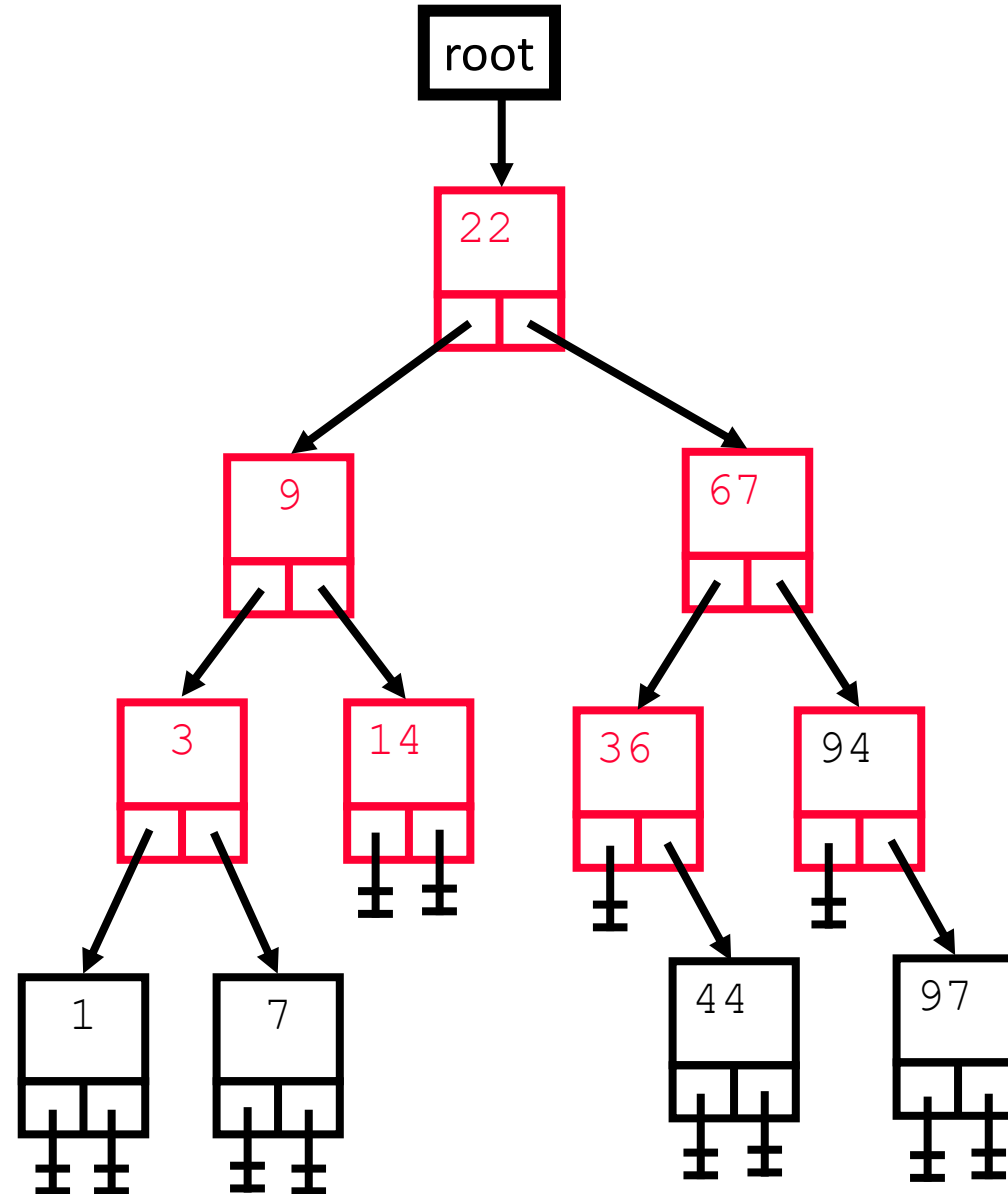
aNode:36



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:1 7 44

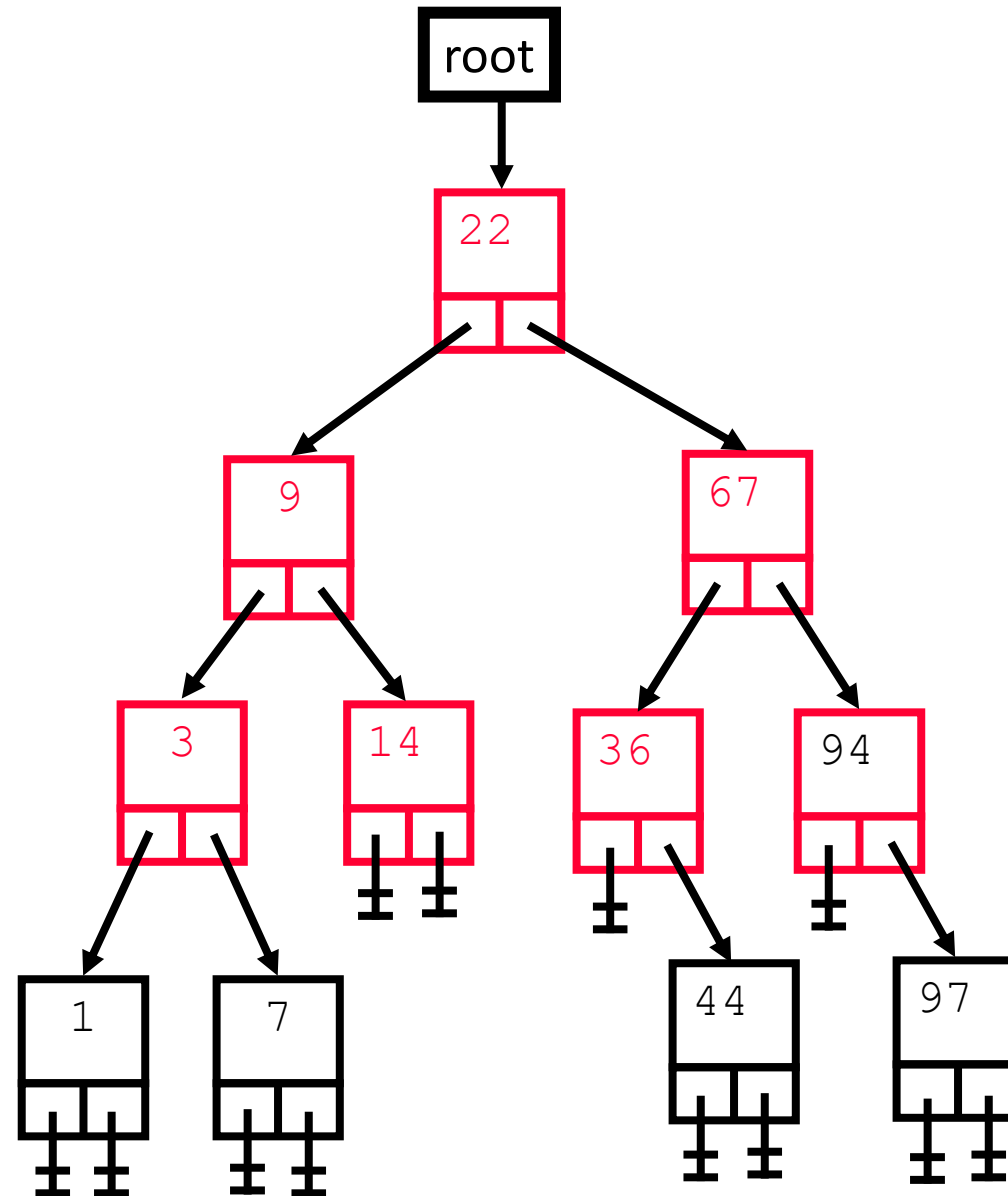
aNode:94



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:1 7 44 97

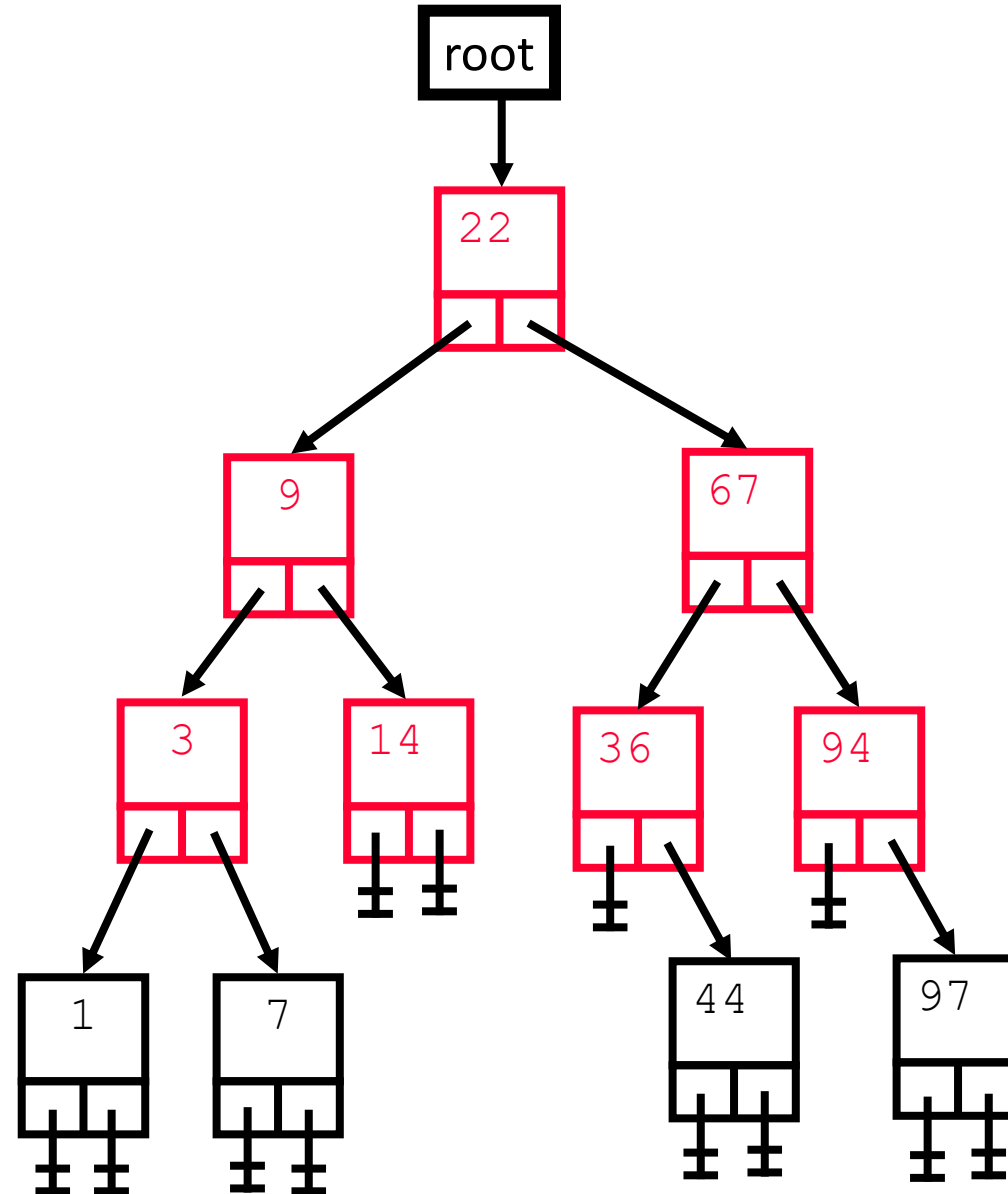
aNode:94




```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:1 7 44 97

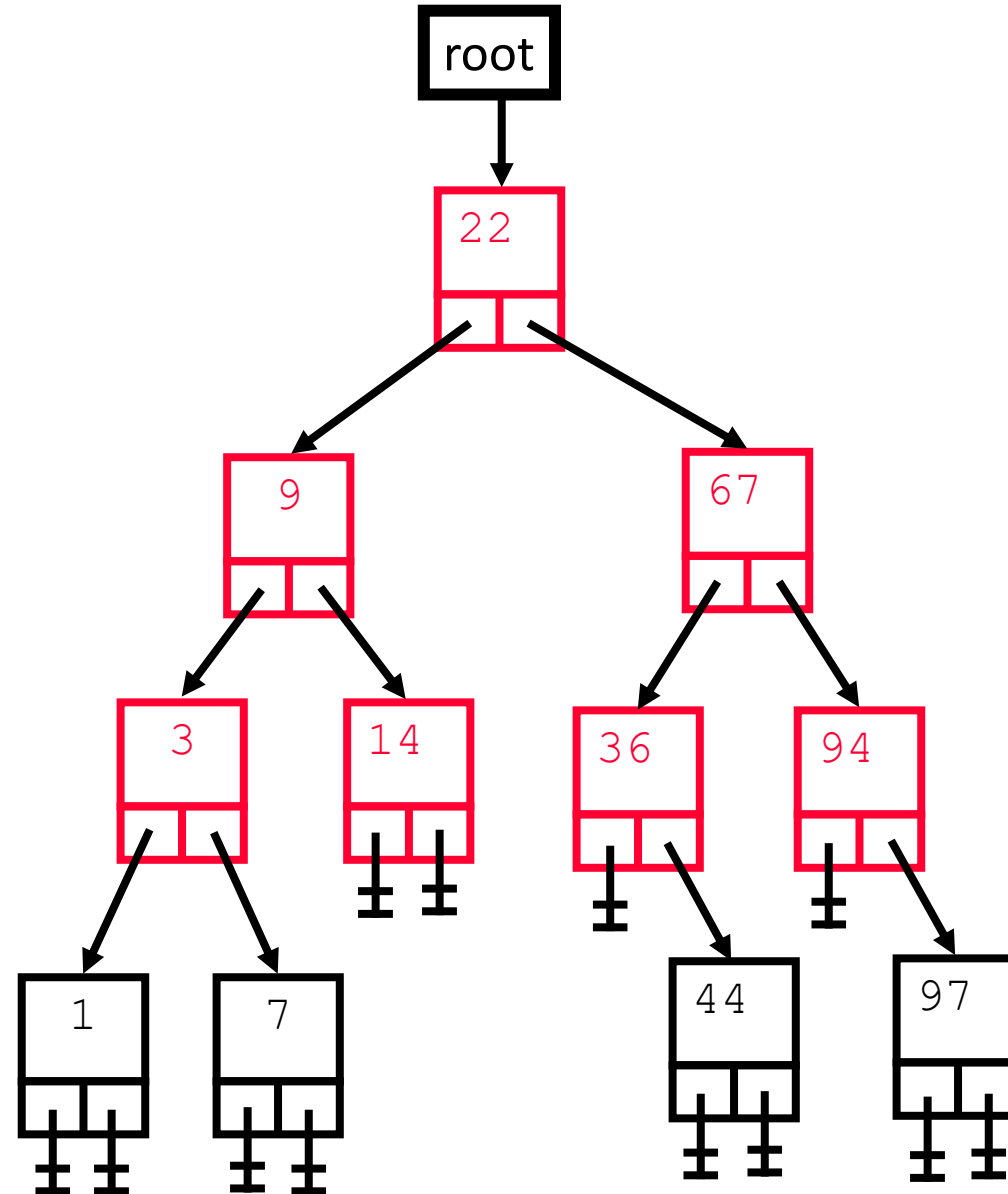
aNode:94



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:1 7 44 97

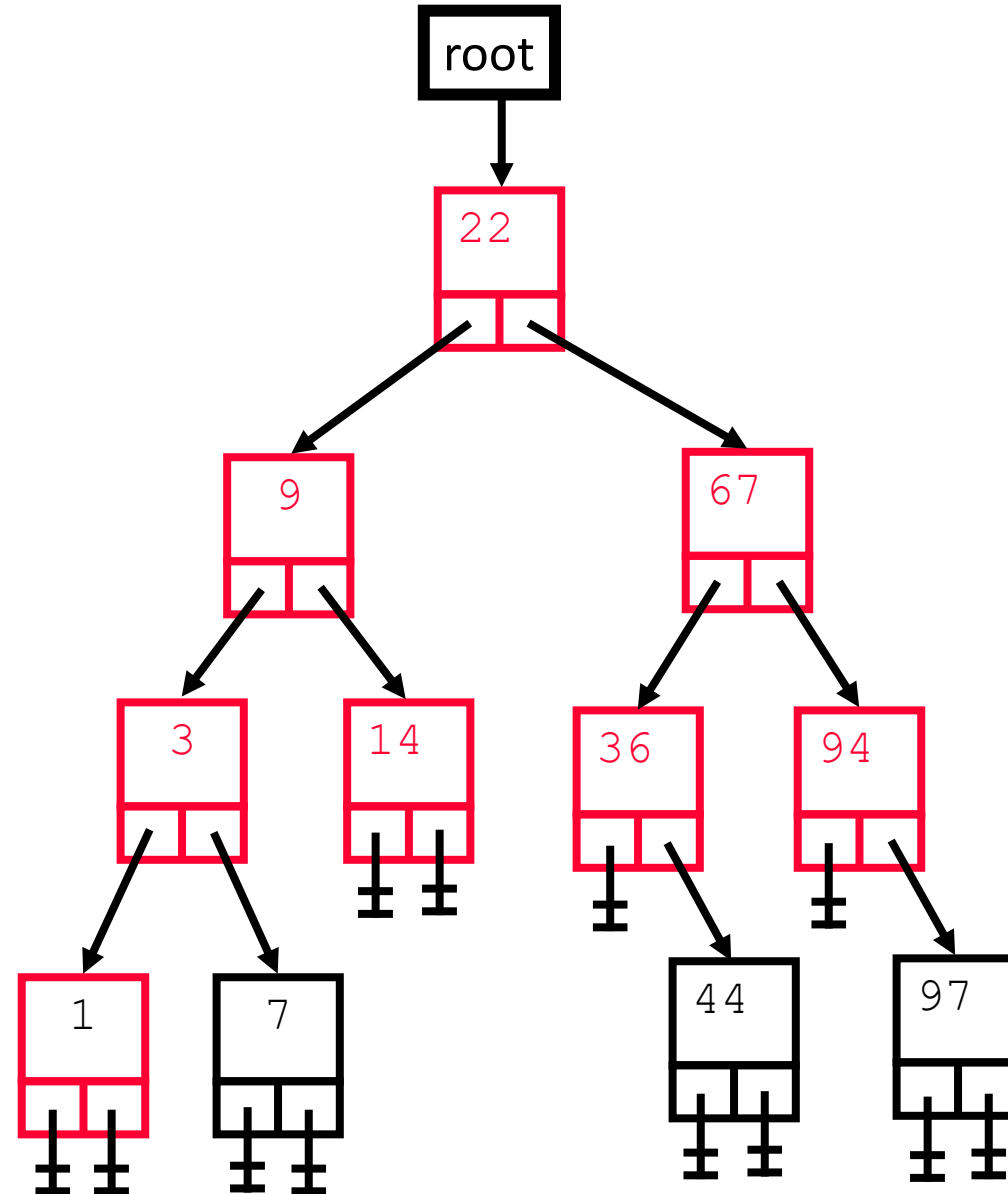
aNode:94



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:7 44 97

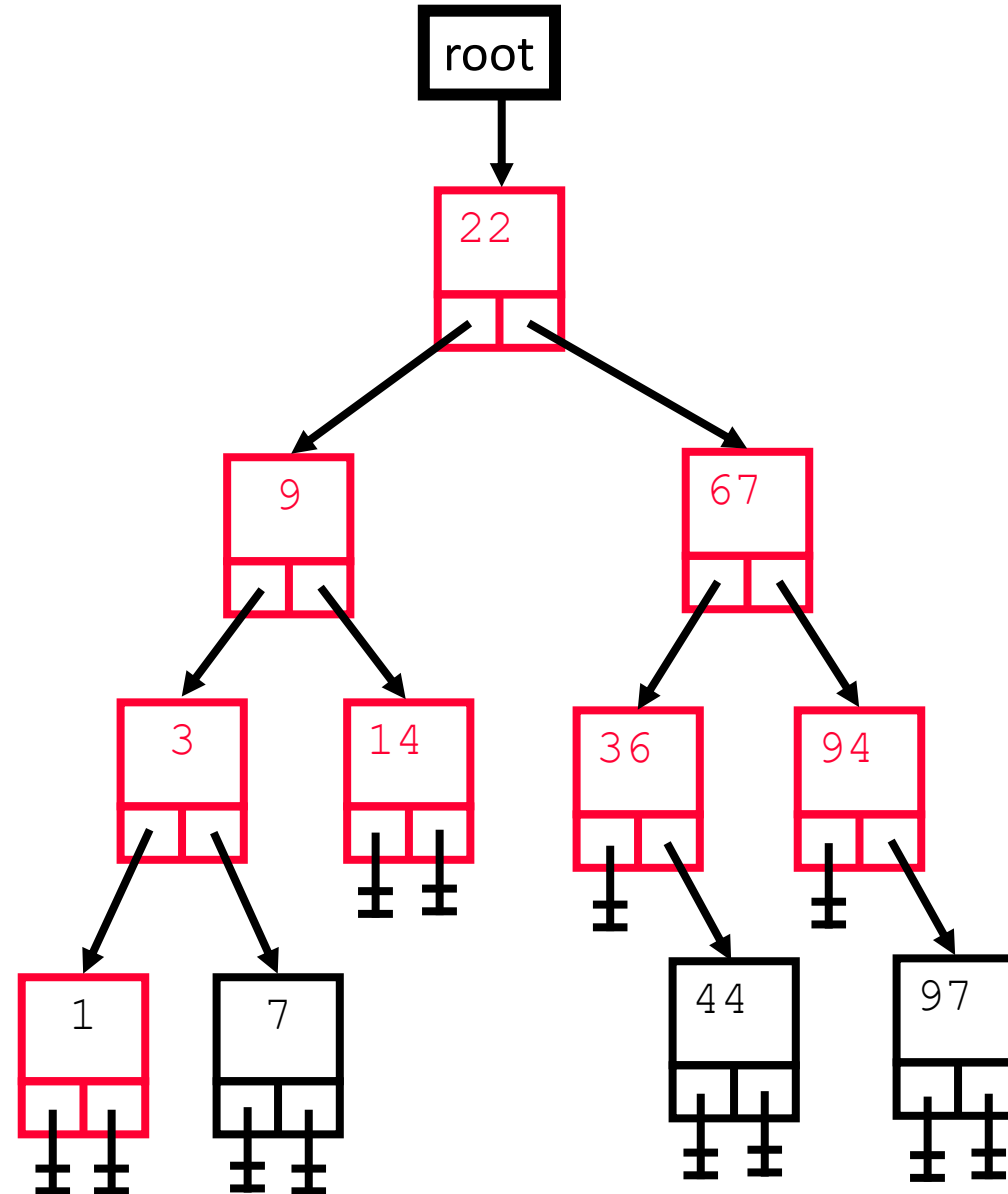
aNode:1



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:7 44 97

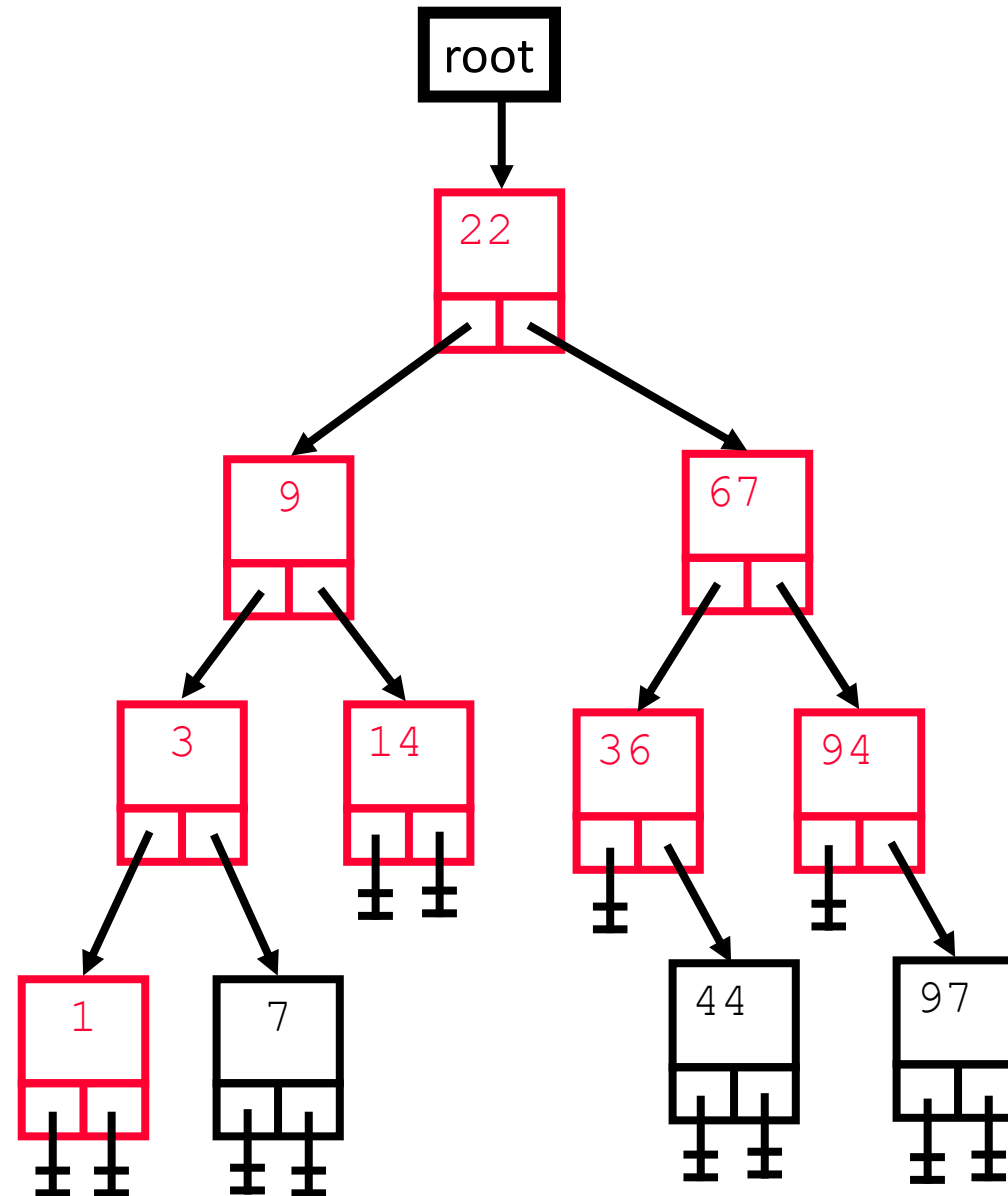
aNode:1



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:7 44 97

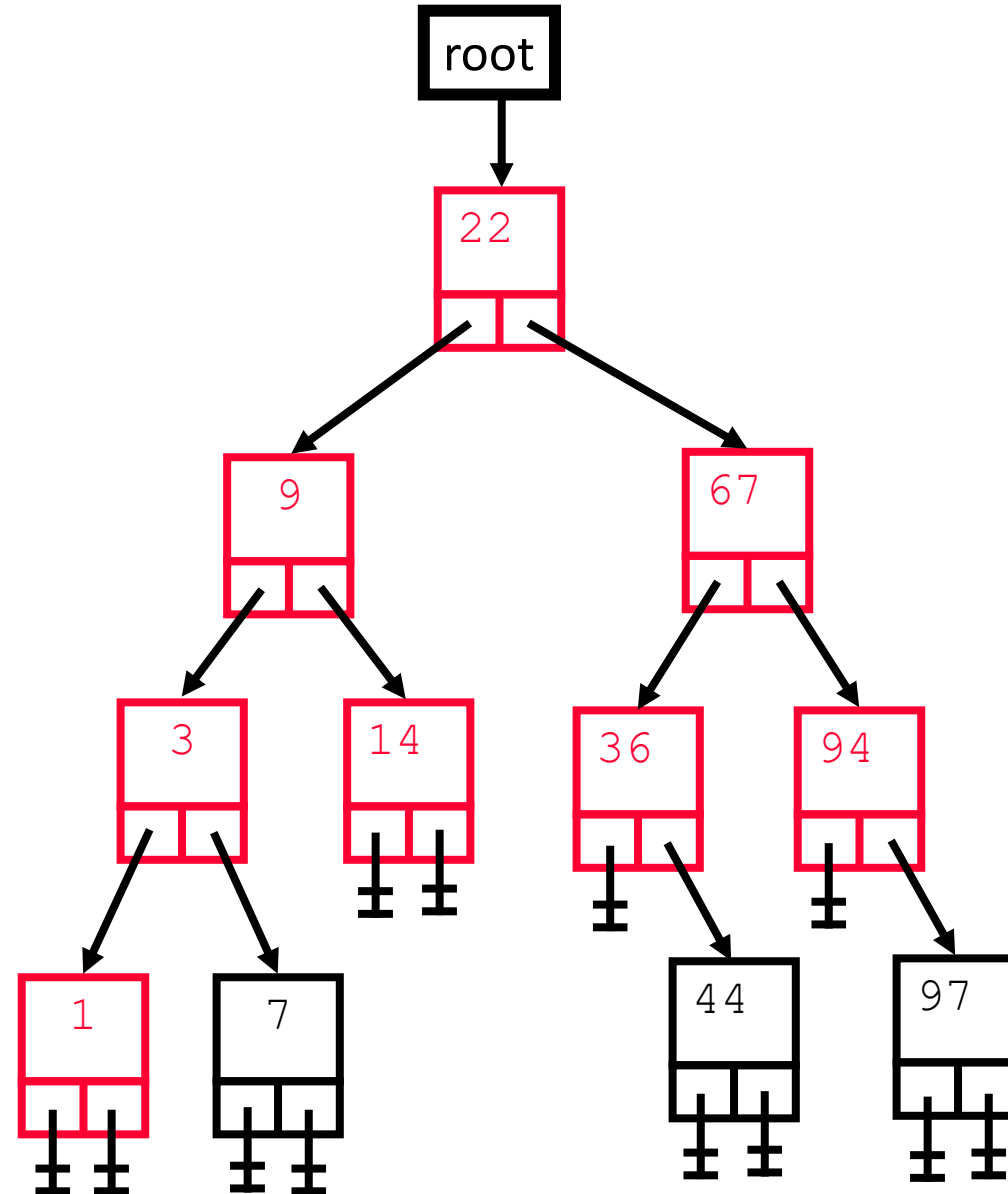
aNode:1



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:7 44 97

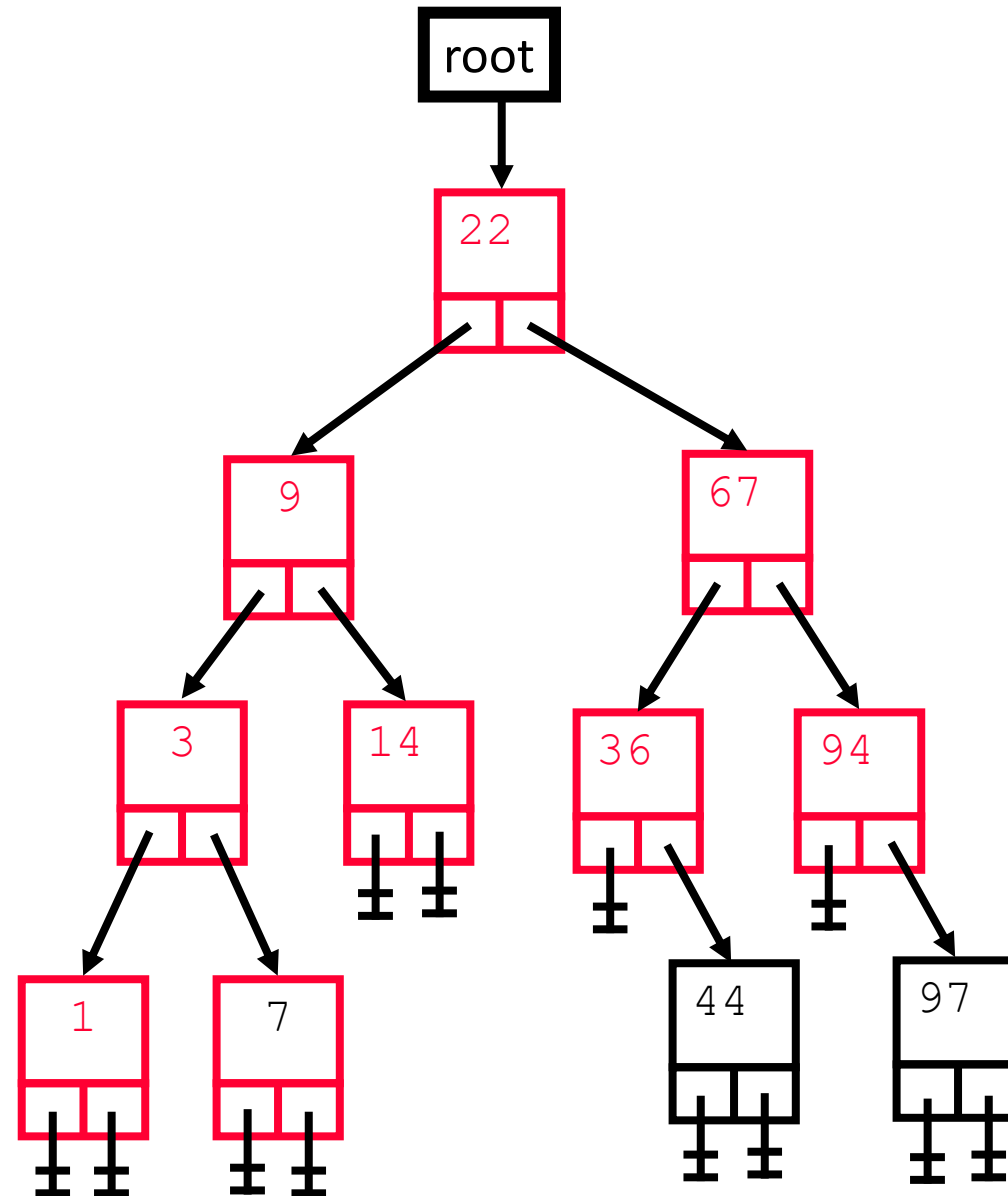
aNode:1



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:44 97

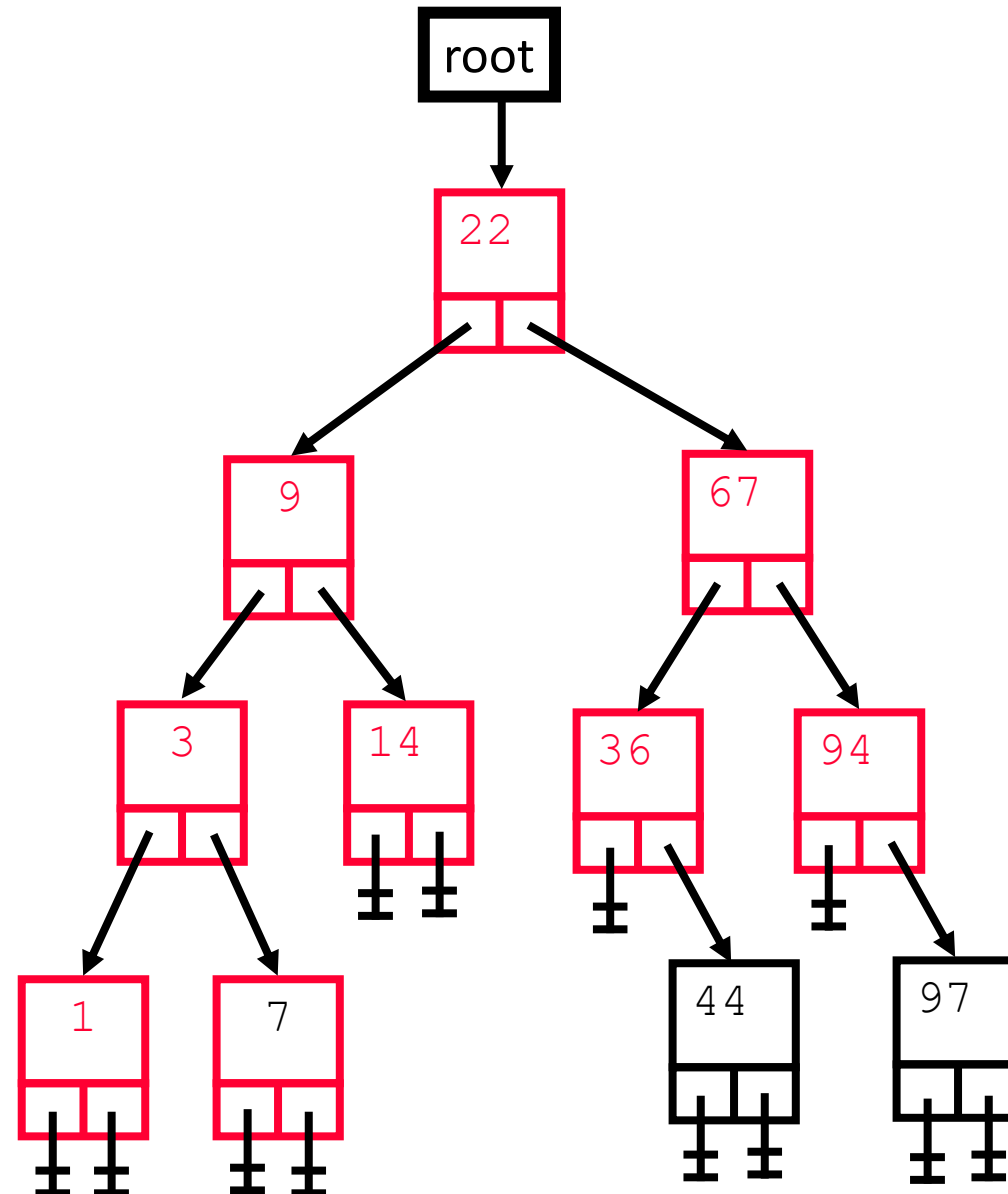
aNode:7



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:44 97

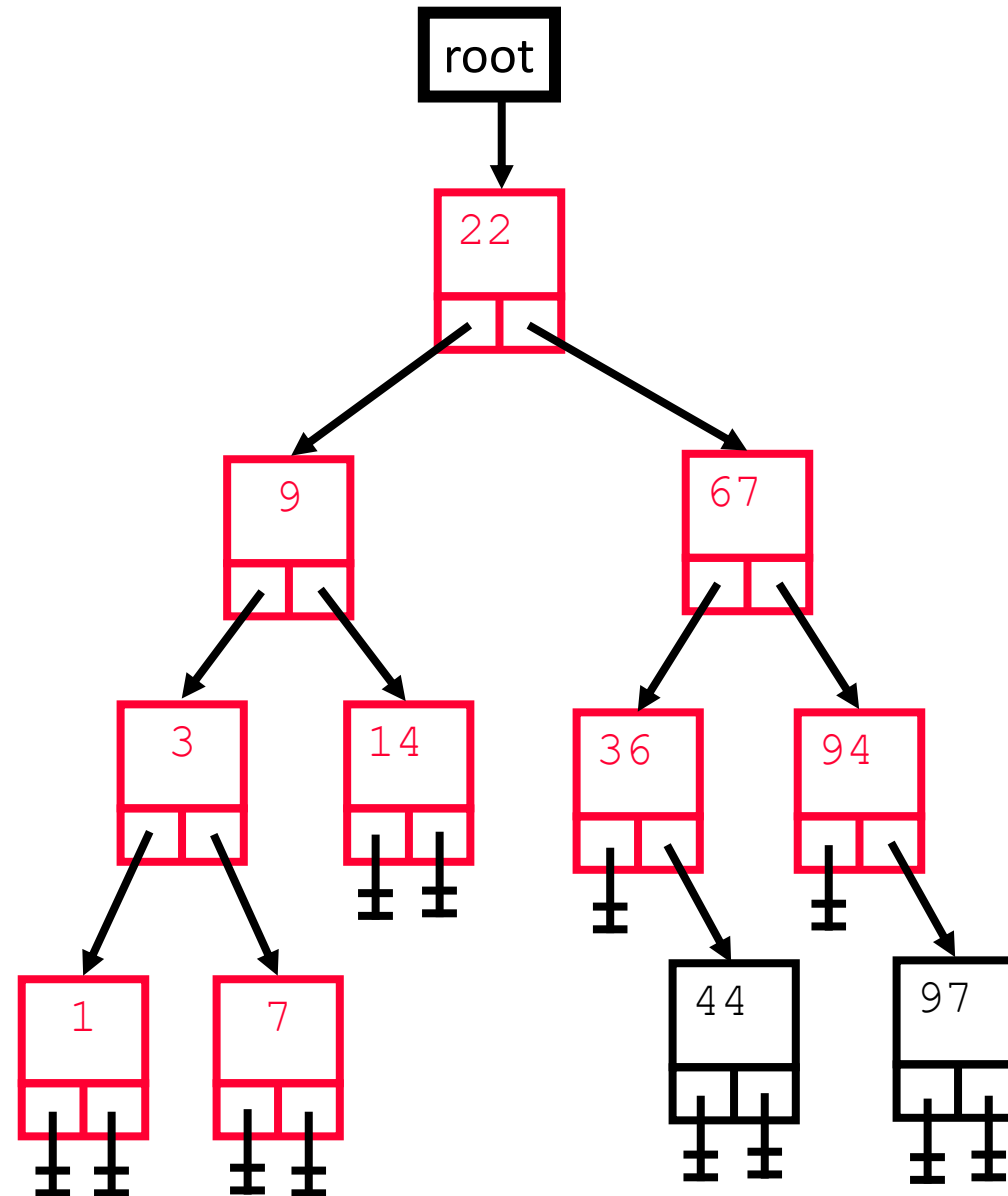
aNode:7




```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:44 97

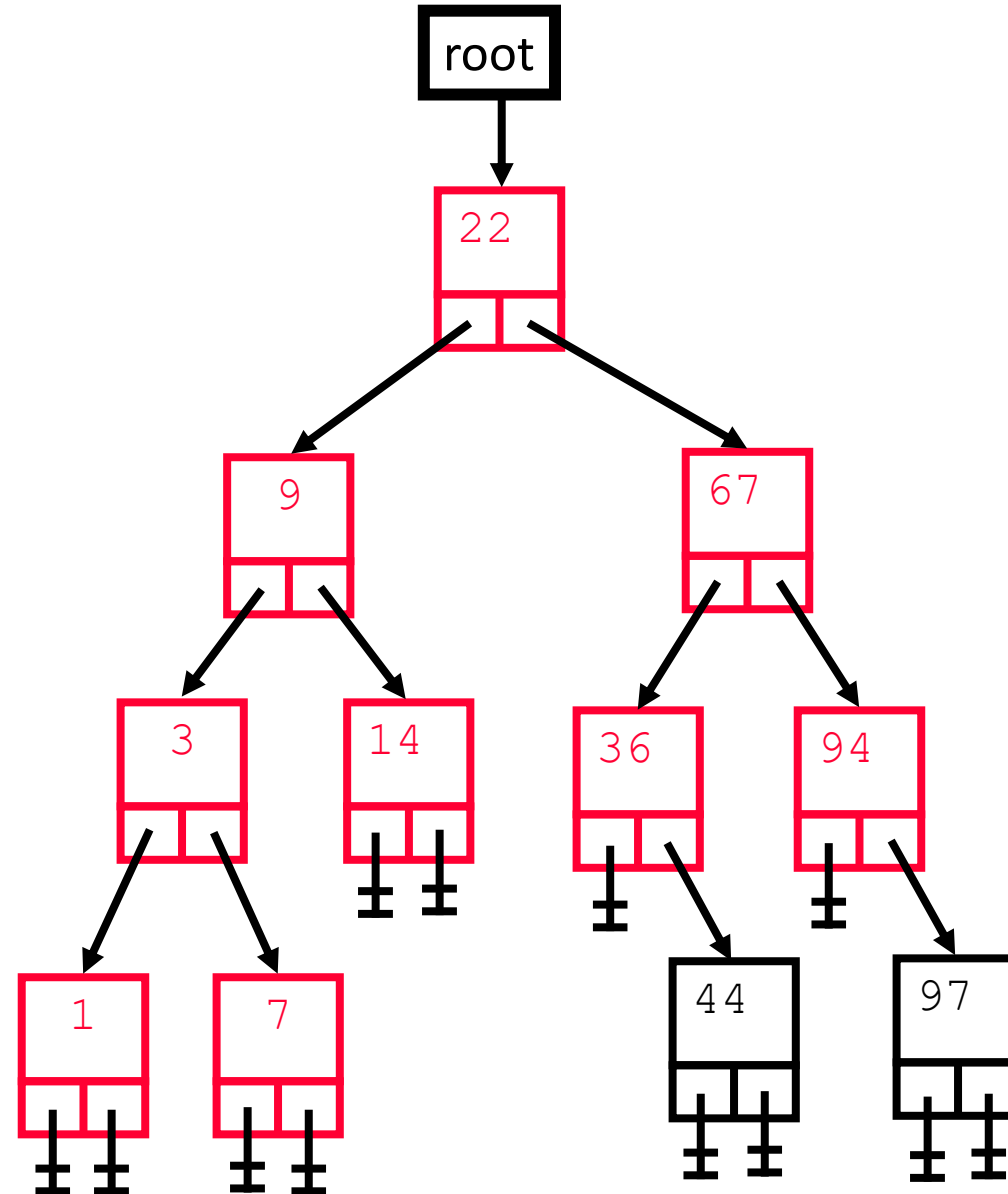
aNode:7



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:44 97

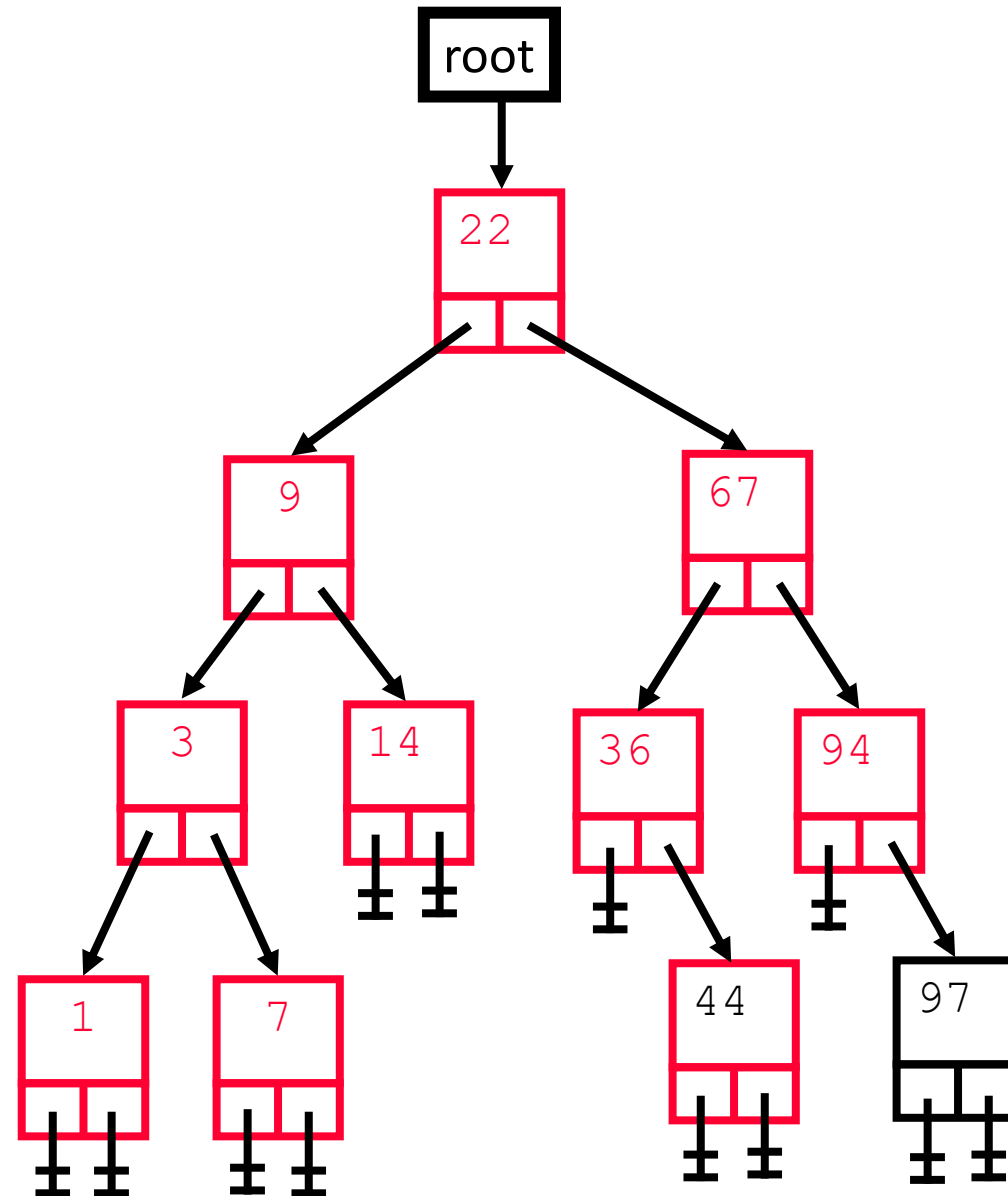
aNode:7



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:97

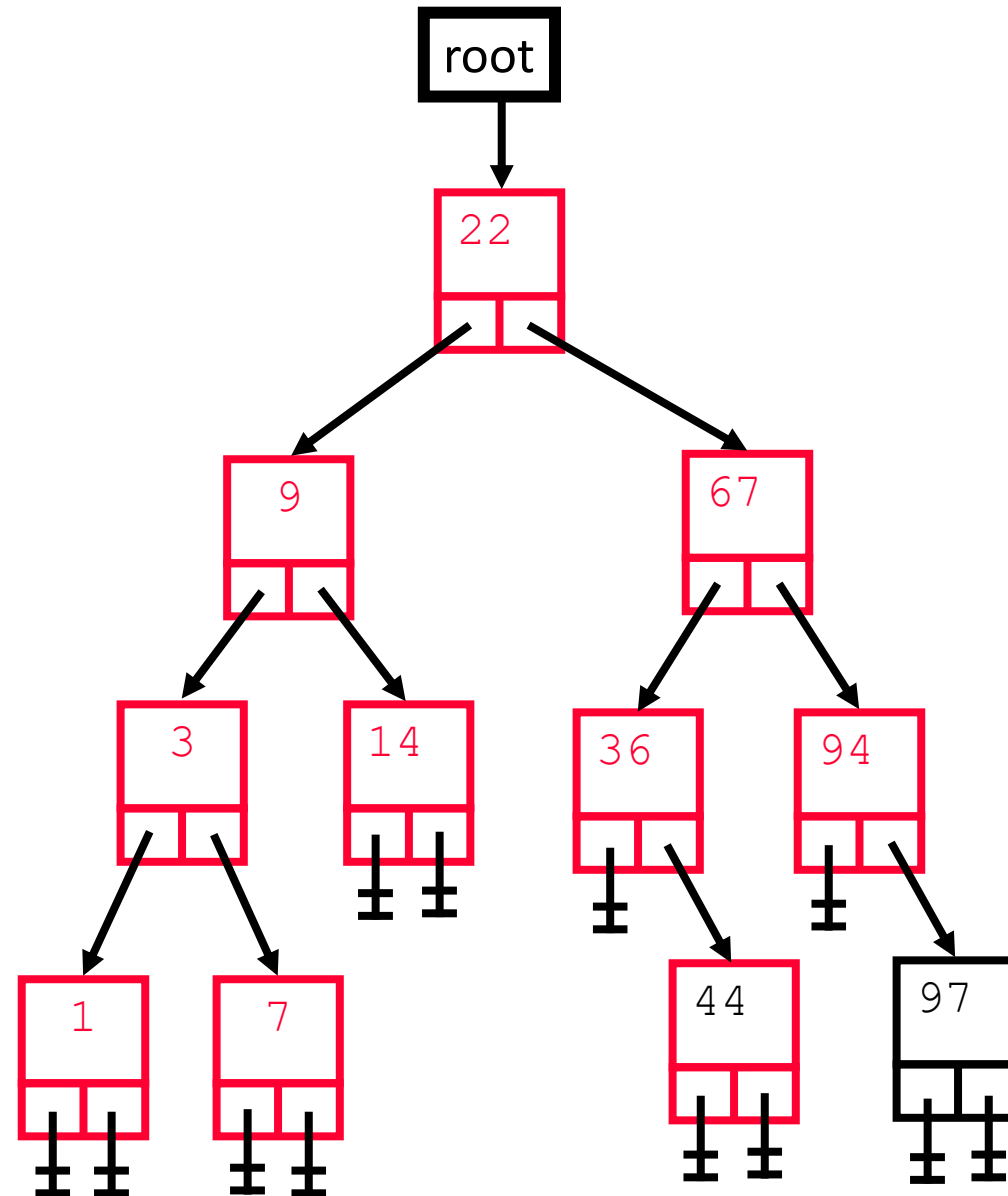
aNode:44



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:97

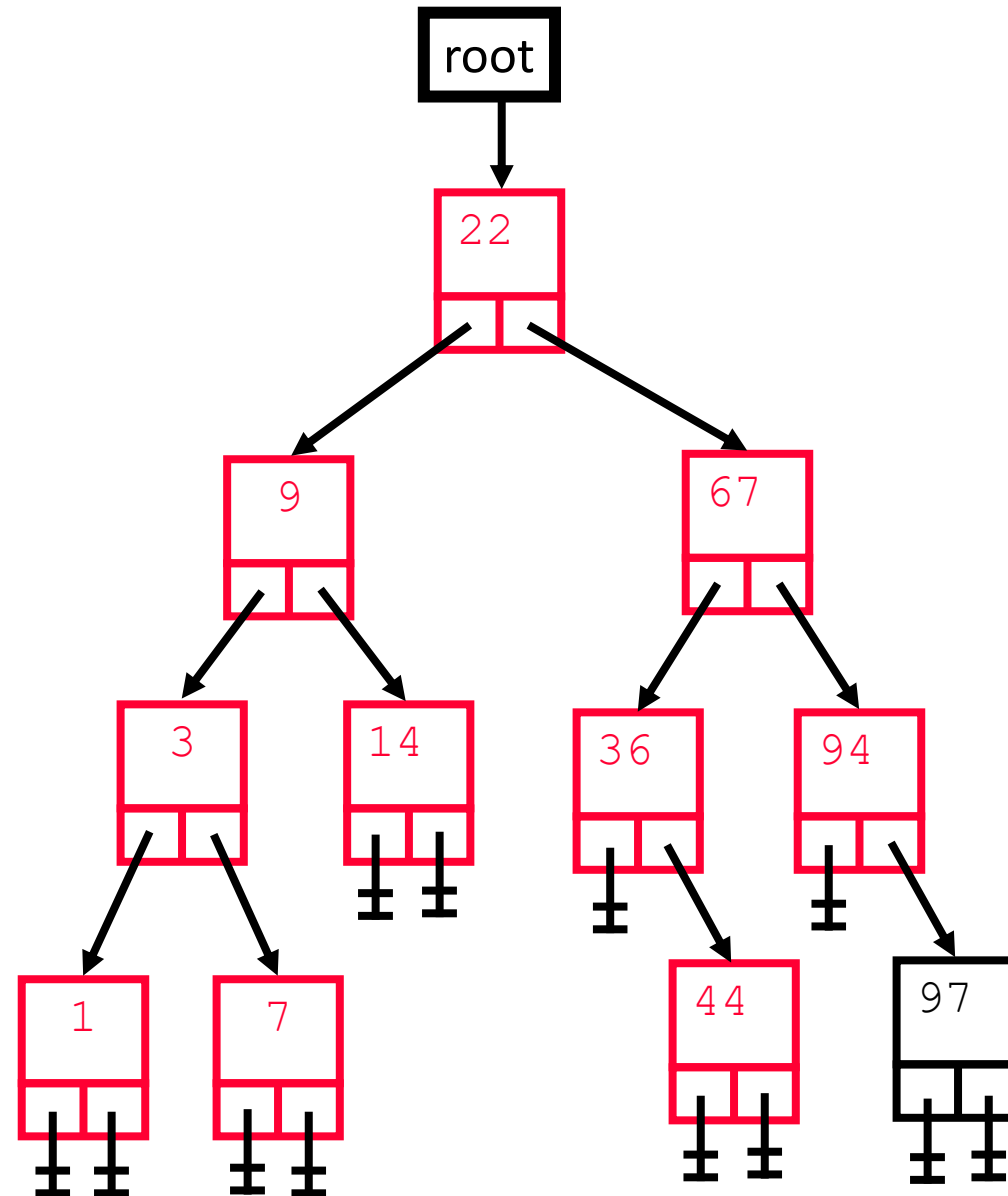
aNode:44



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:97

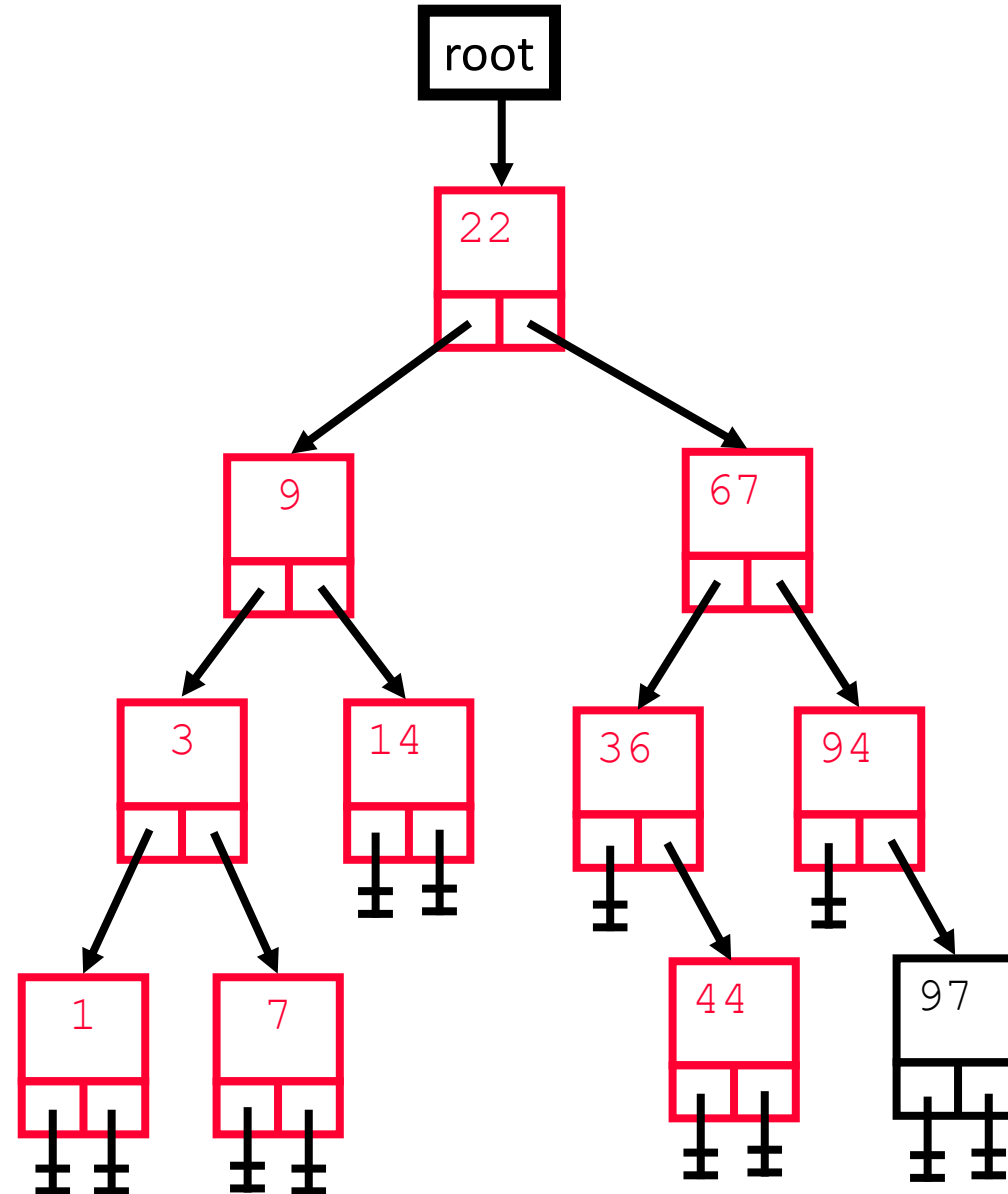
aNode:44



```
Enqueue (root)
loop
  exit if Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:97

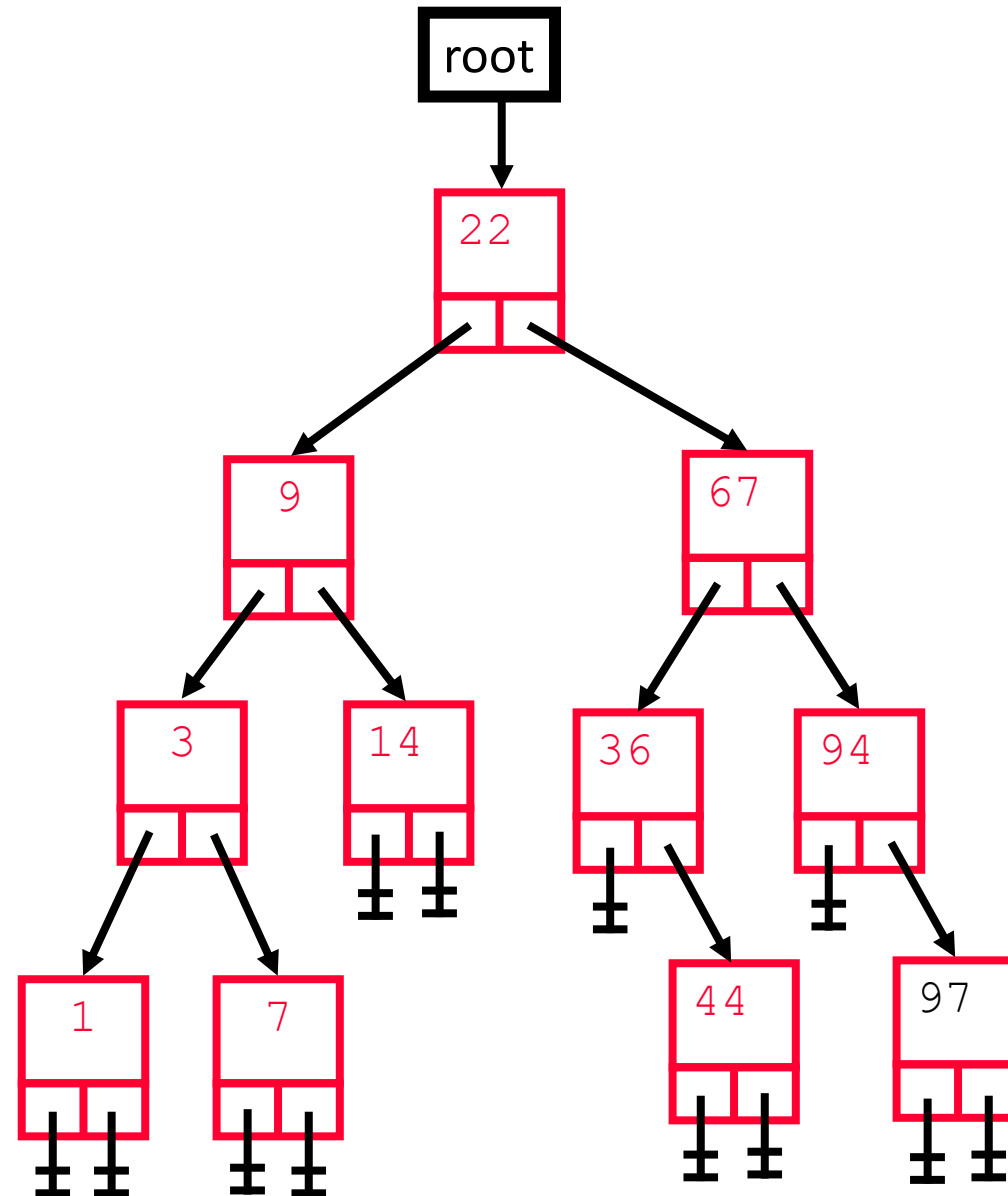
aNode:44



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:

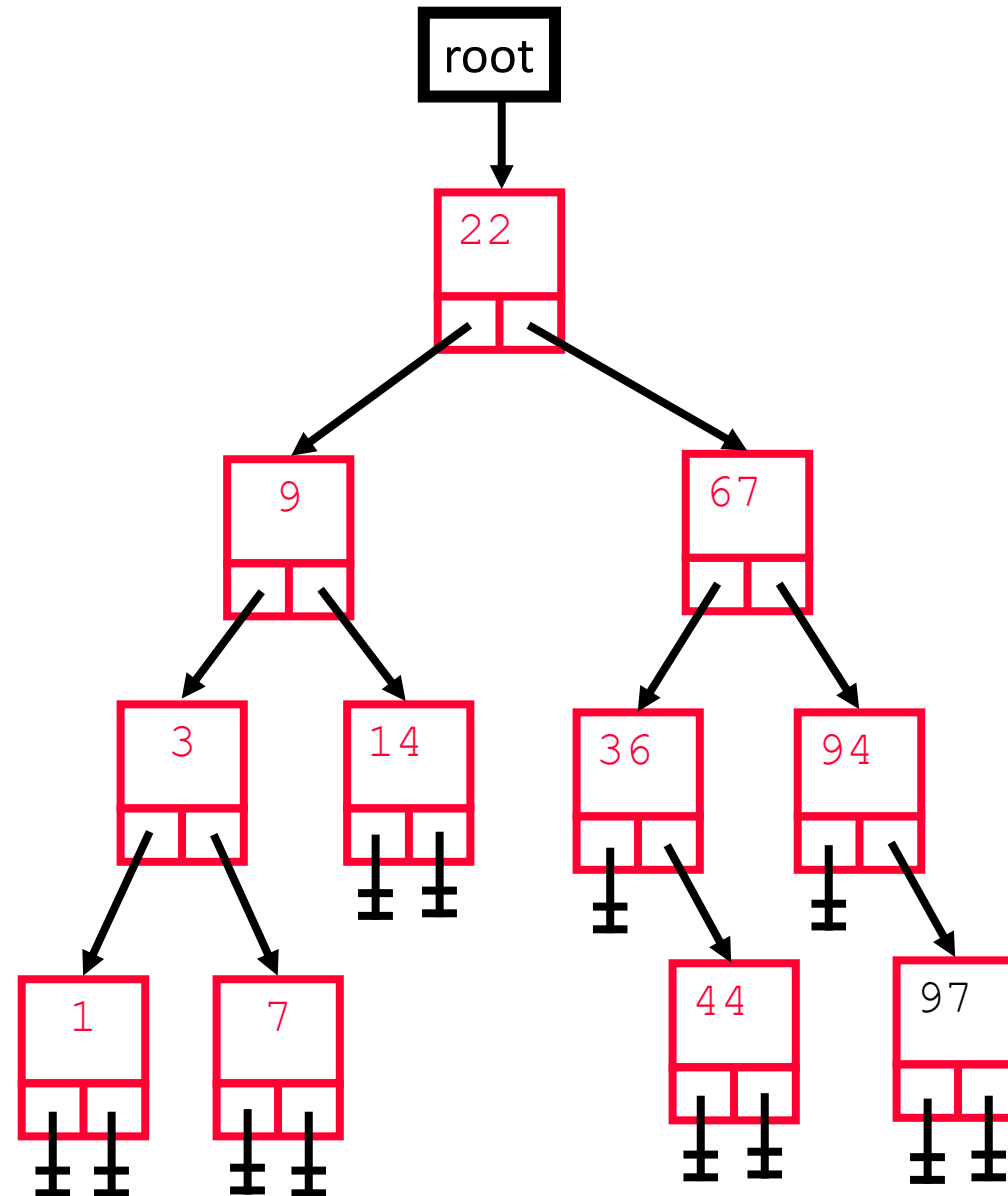
aNode:97



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:

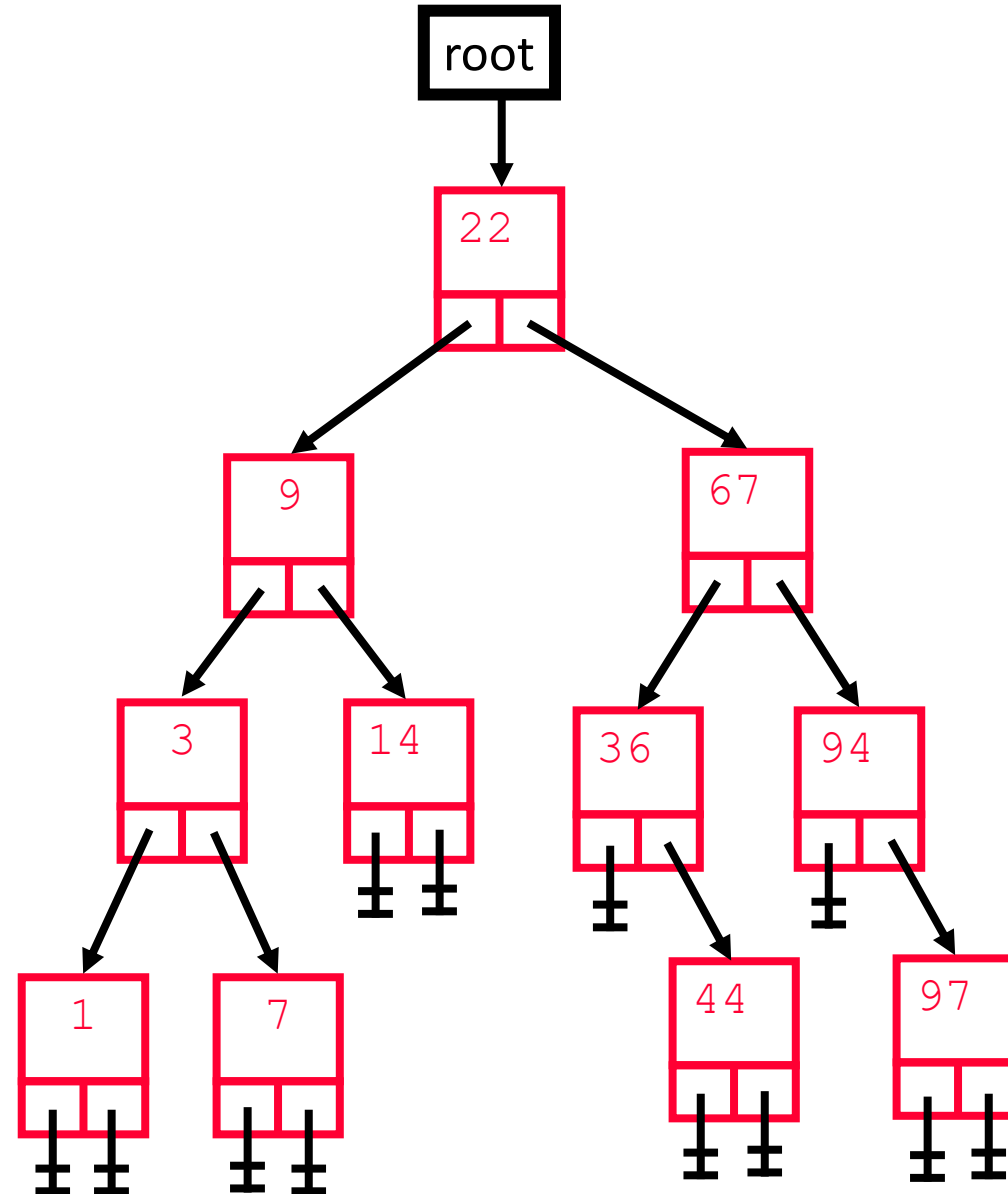
aNode:97



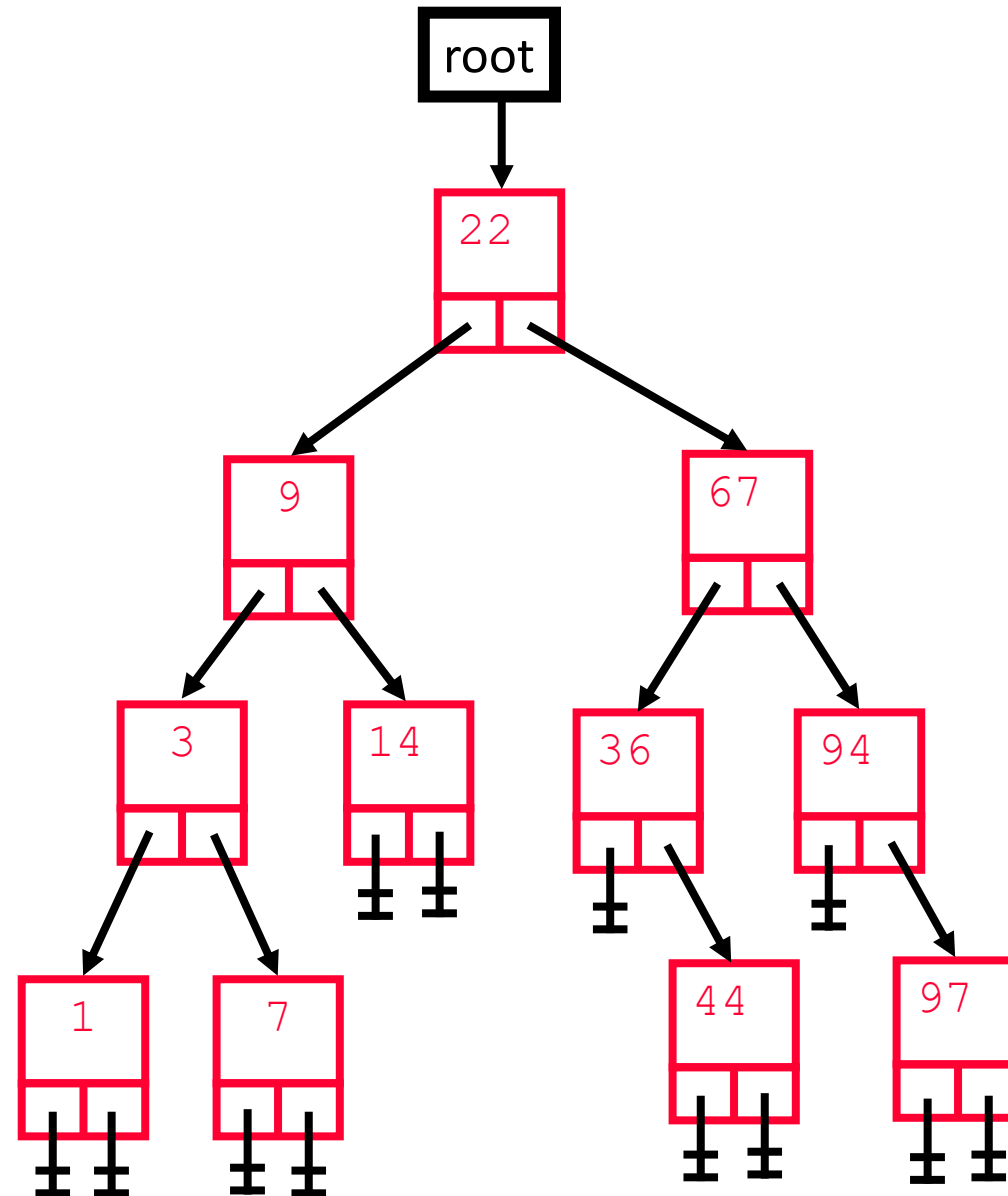
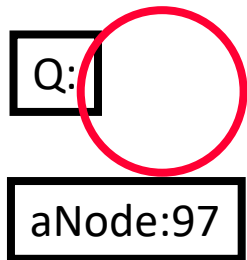

```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```

Q:

aNode:97



```
Enqueue (root)
loop
  exitif Q empty
  dequeue (aNode)
  enqueue (children)
  print (aNode.data)
endloop
```



Reference

- <https://www.cc.gatech.edu/~bleahy/>
- **Prof. Bill Leahy, Georgia Tech. College of Computing**

Thank You