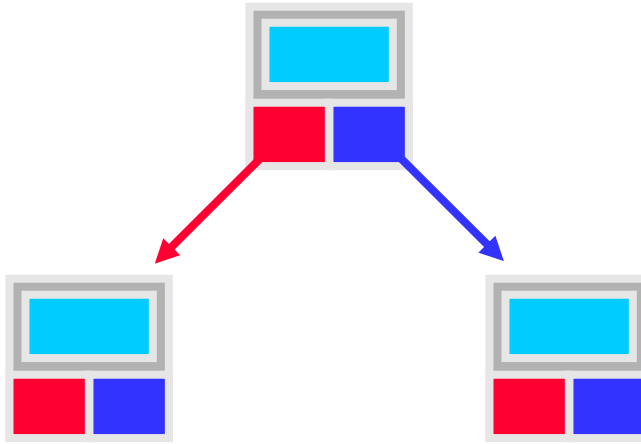


In-order Traversal

Outline of In-Order Traversal

- **Three principle steps:**
 - Traverse **Left**
 - Do work (**Current**)
 - Traverse **Right**
- **Work can be anything**
- **Separate work from traversal**

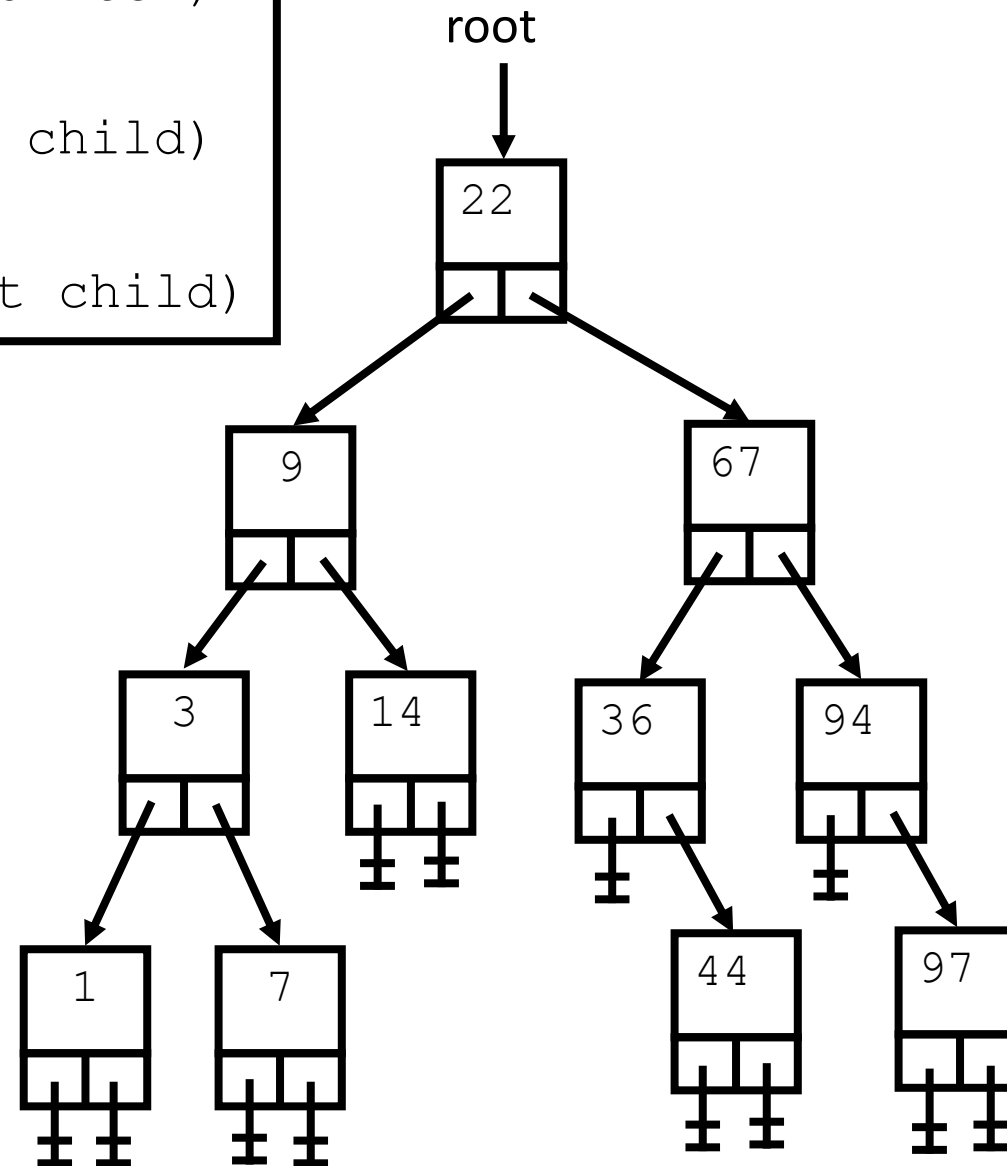


- Traverse the tree "In order":
 - Visit the tree's left sub-tree
 - Visit the current and do work
 - Visit right sub-tree

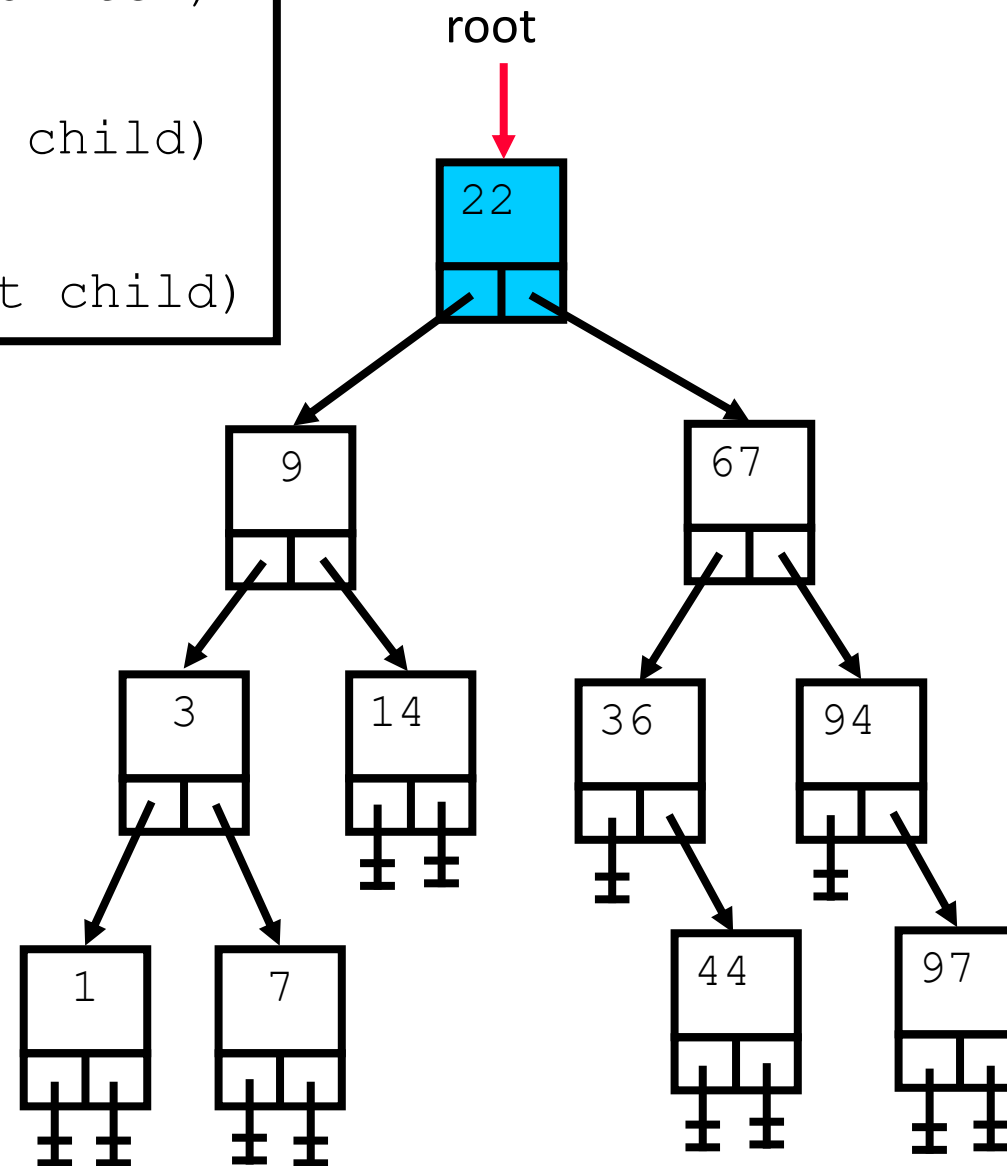
In-Order Traversal Procedure

```
procedure In_Order(cur iot in Ptr toa Tree_Node)
// Purpose: perform in-order traversal, call
//           Do_Something for each node
// Preconditions: cur points to a binary tree
// Postcondition: Do_Something on each tree
//              node in "in-order" order
  if( cur <> NIL ) then
    In_Order( cur^.left_child )
    Do_Something( cur^.data )
    In_Order( cur^.right_child )
  endif
endprocedure    // In_Order
```

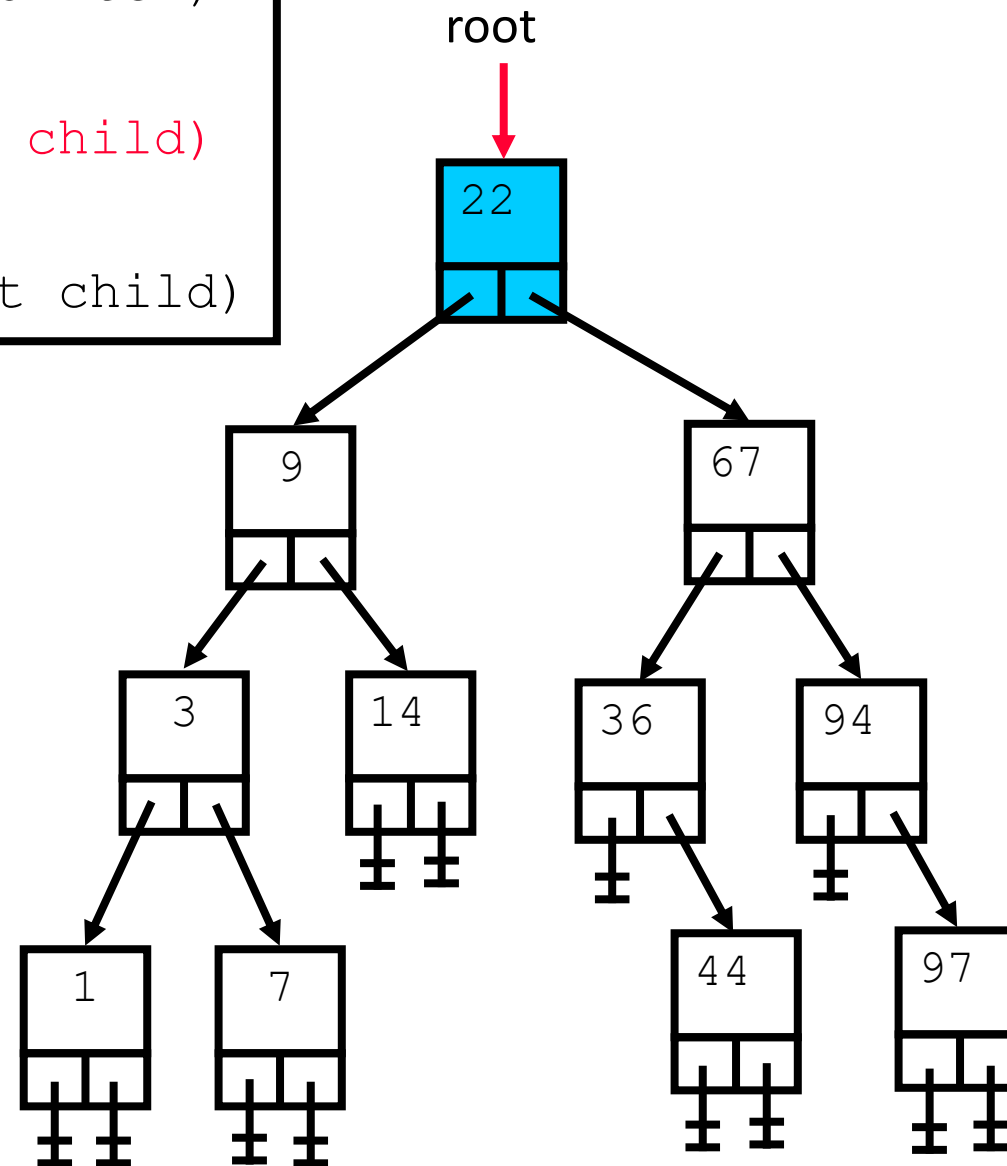
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



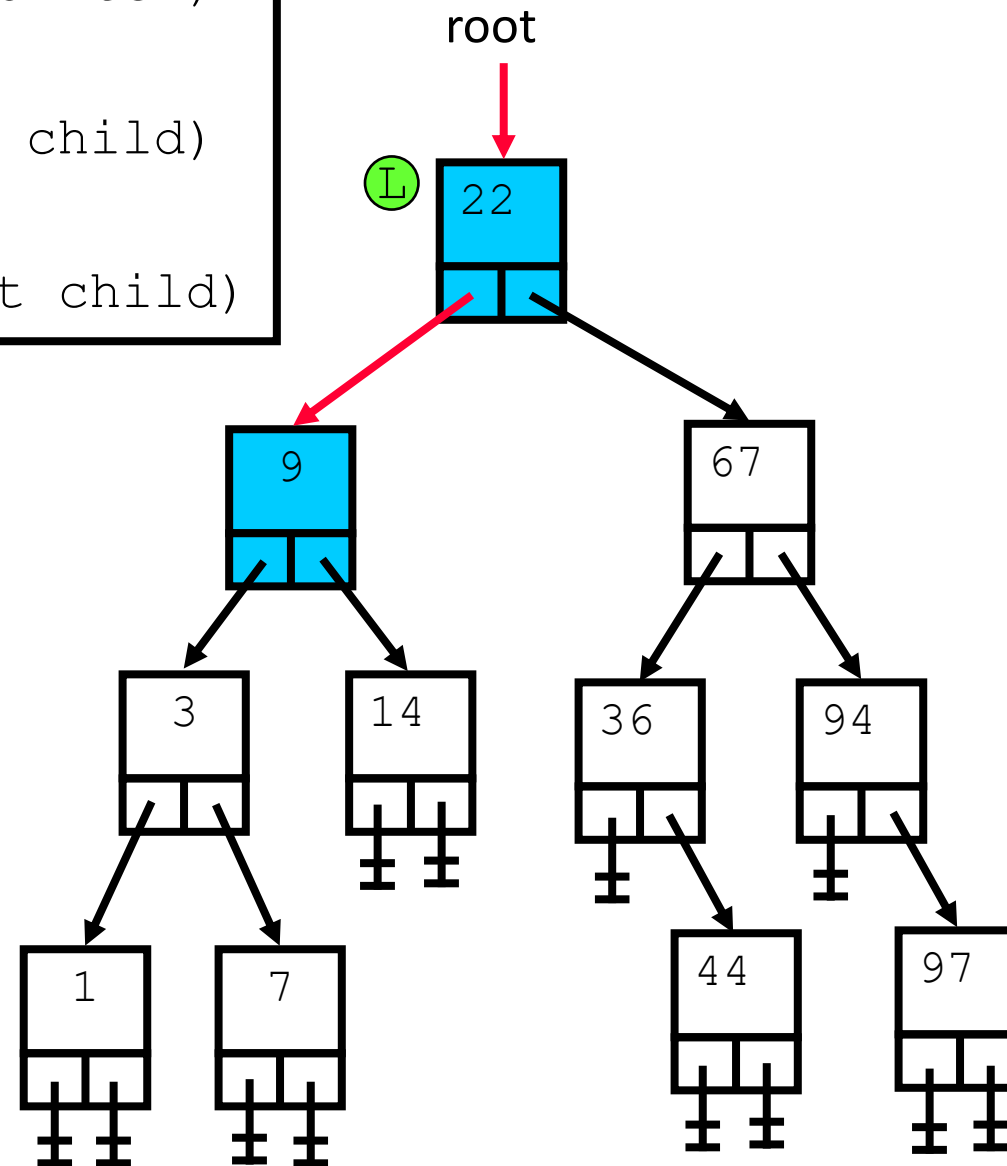
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



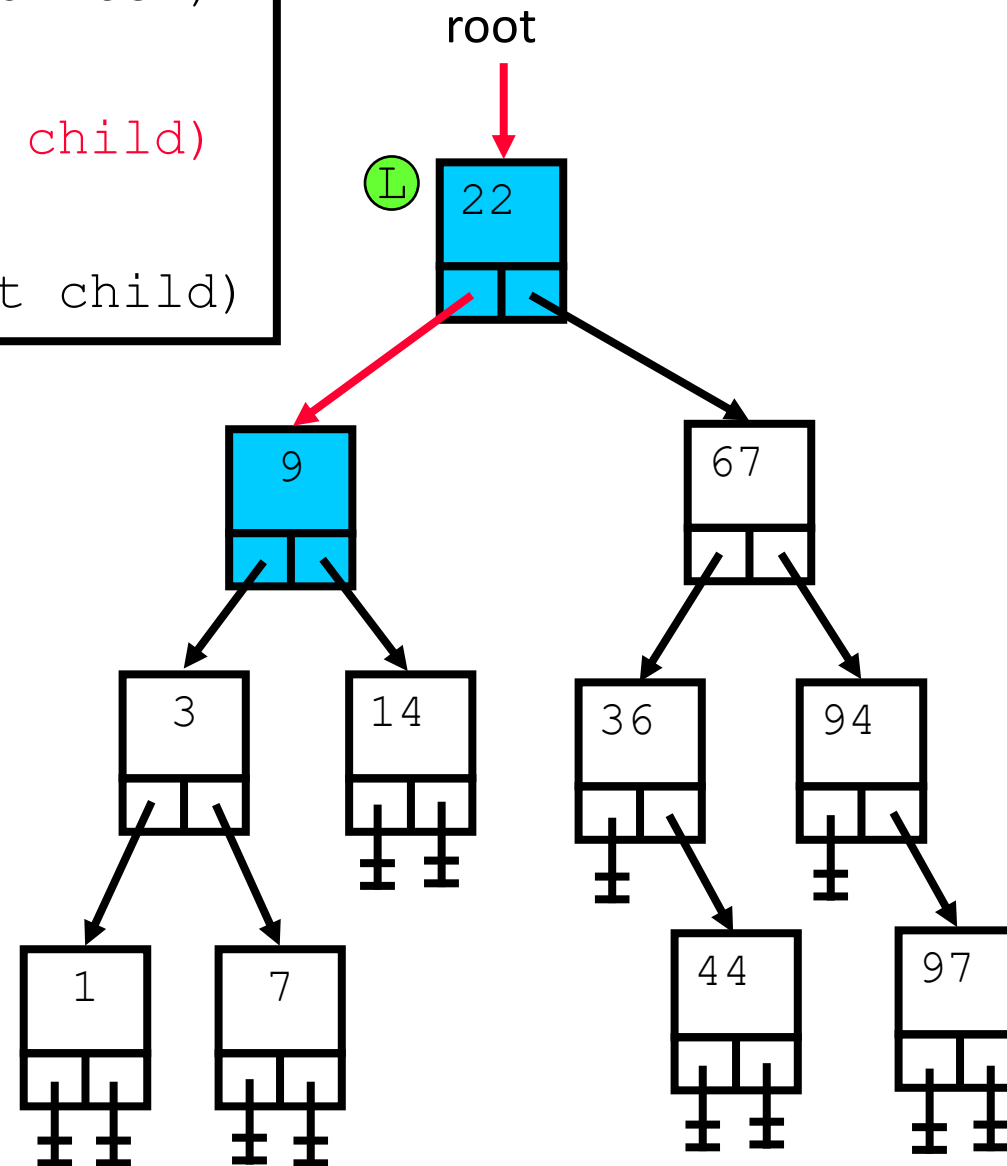
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  Ⓛ InOrderPrint(left child)
  Ⓟ print(data)
  Ⓡ InOrderPrint(right child)
```



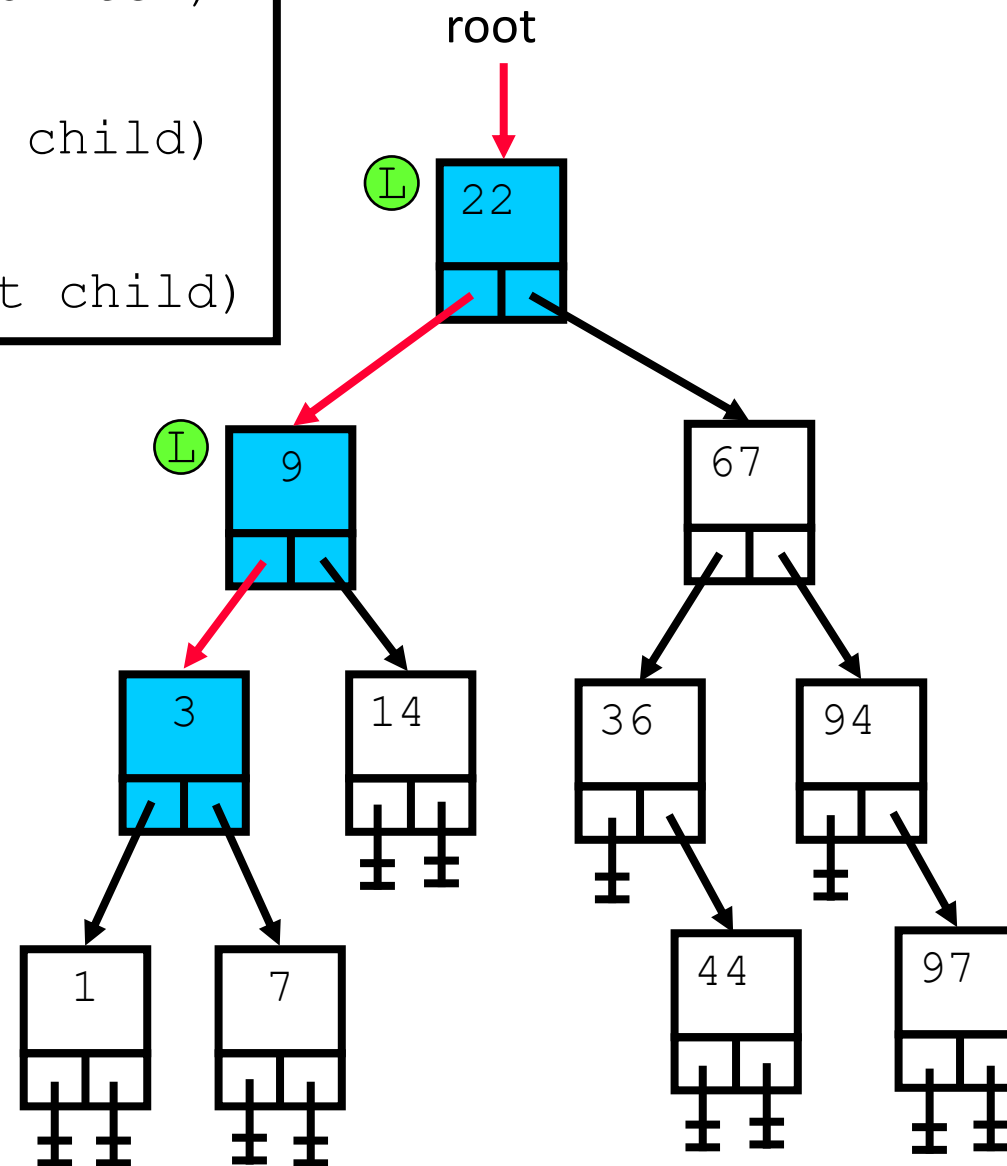
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



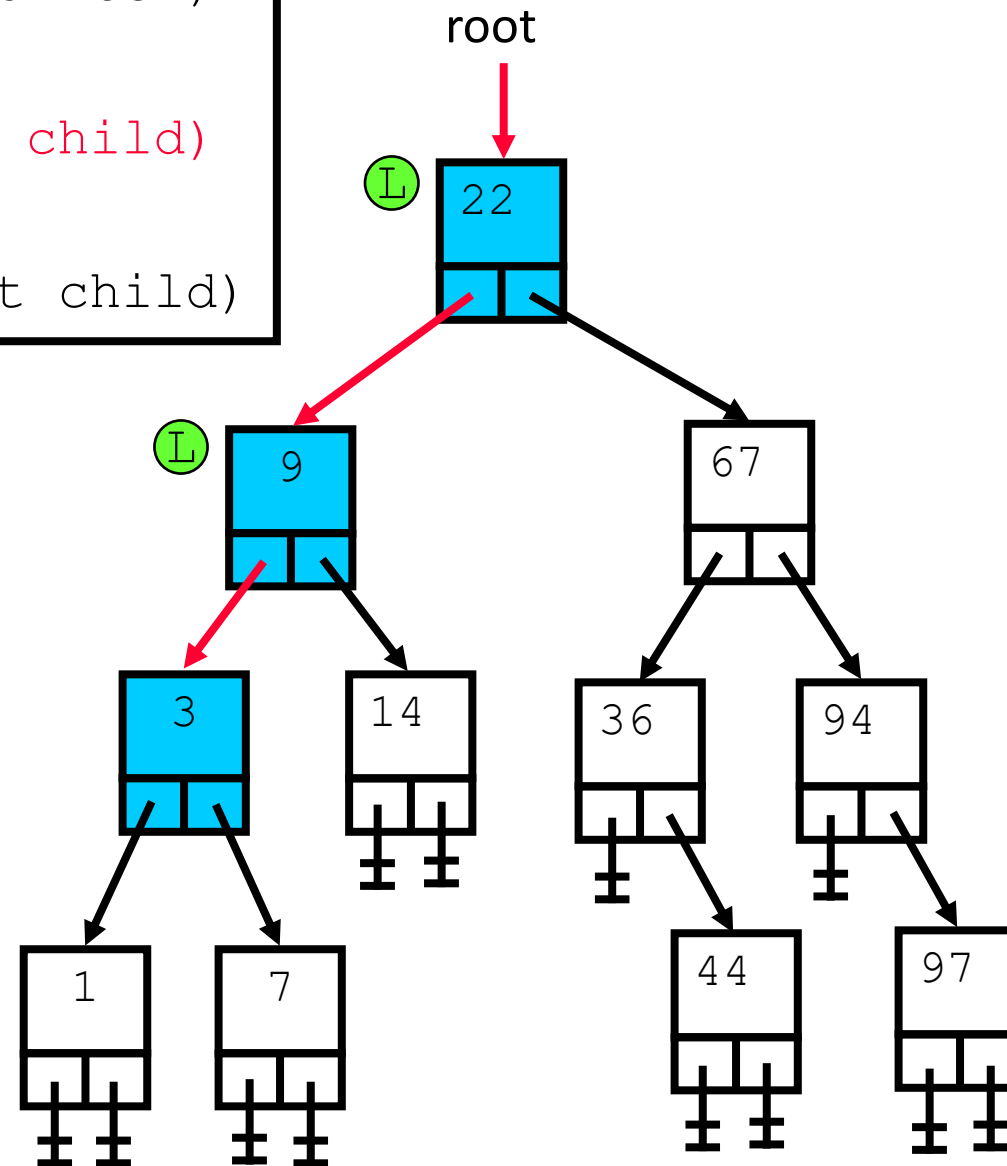

```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



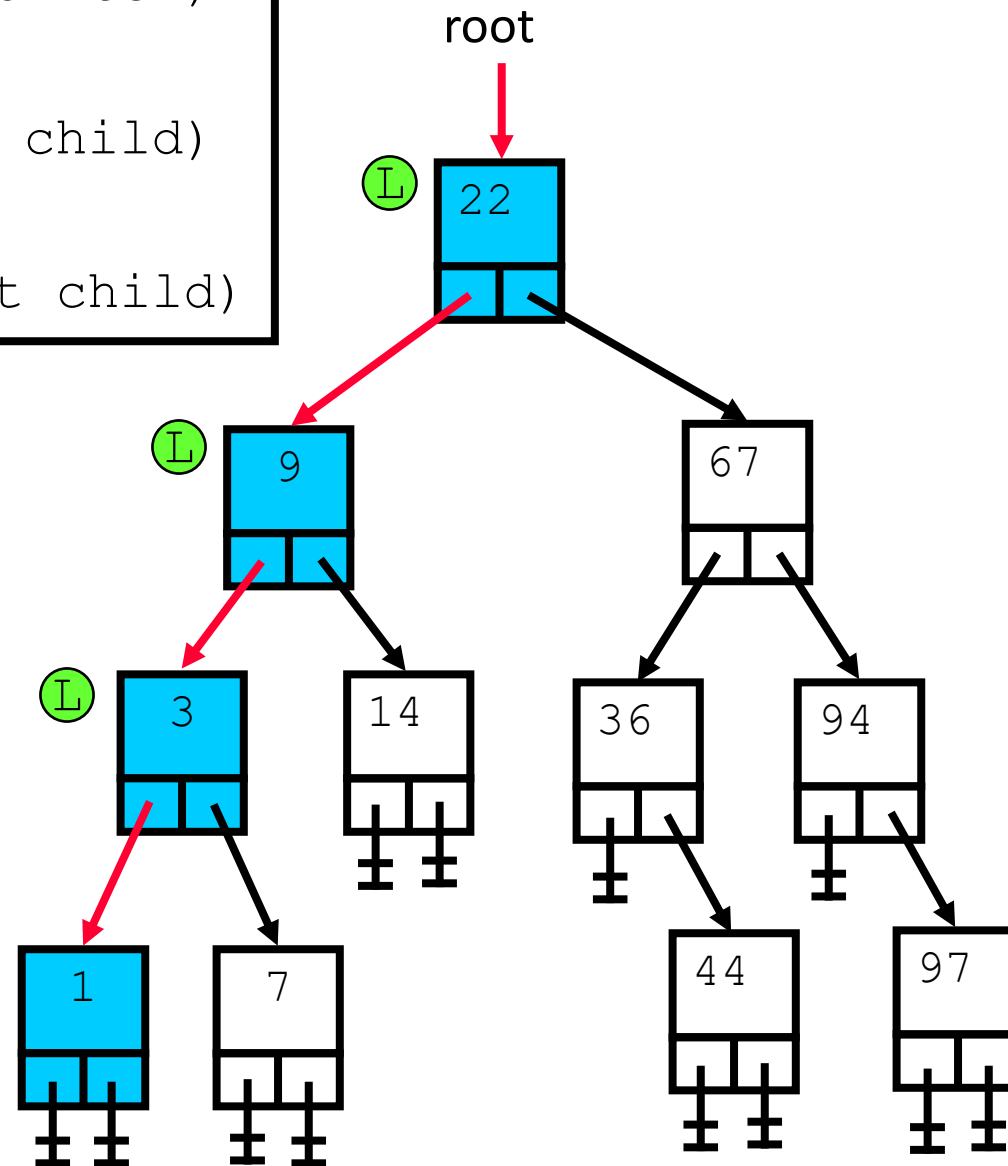
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



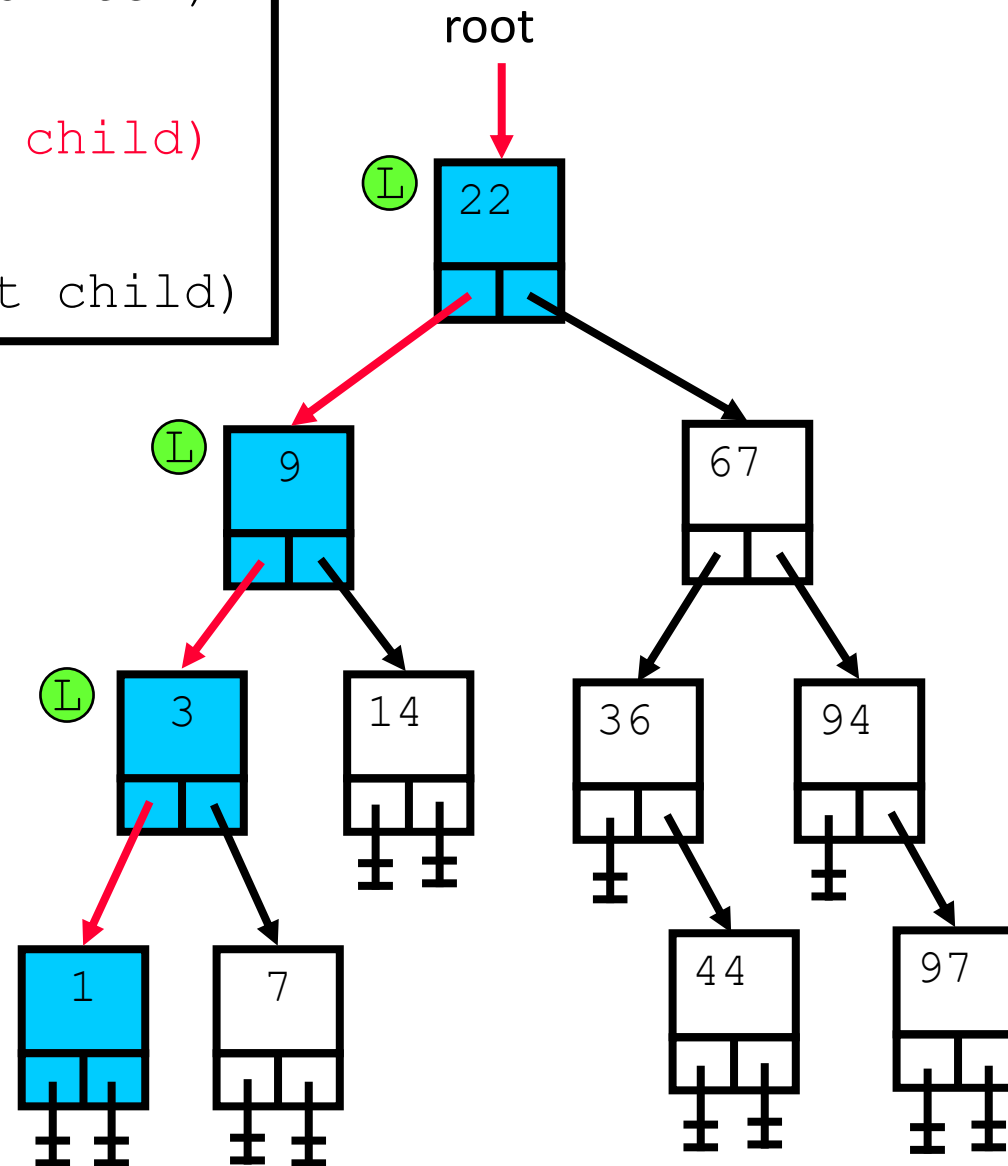
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



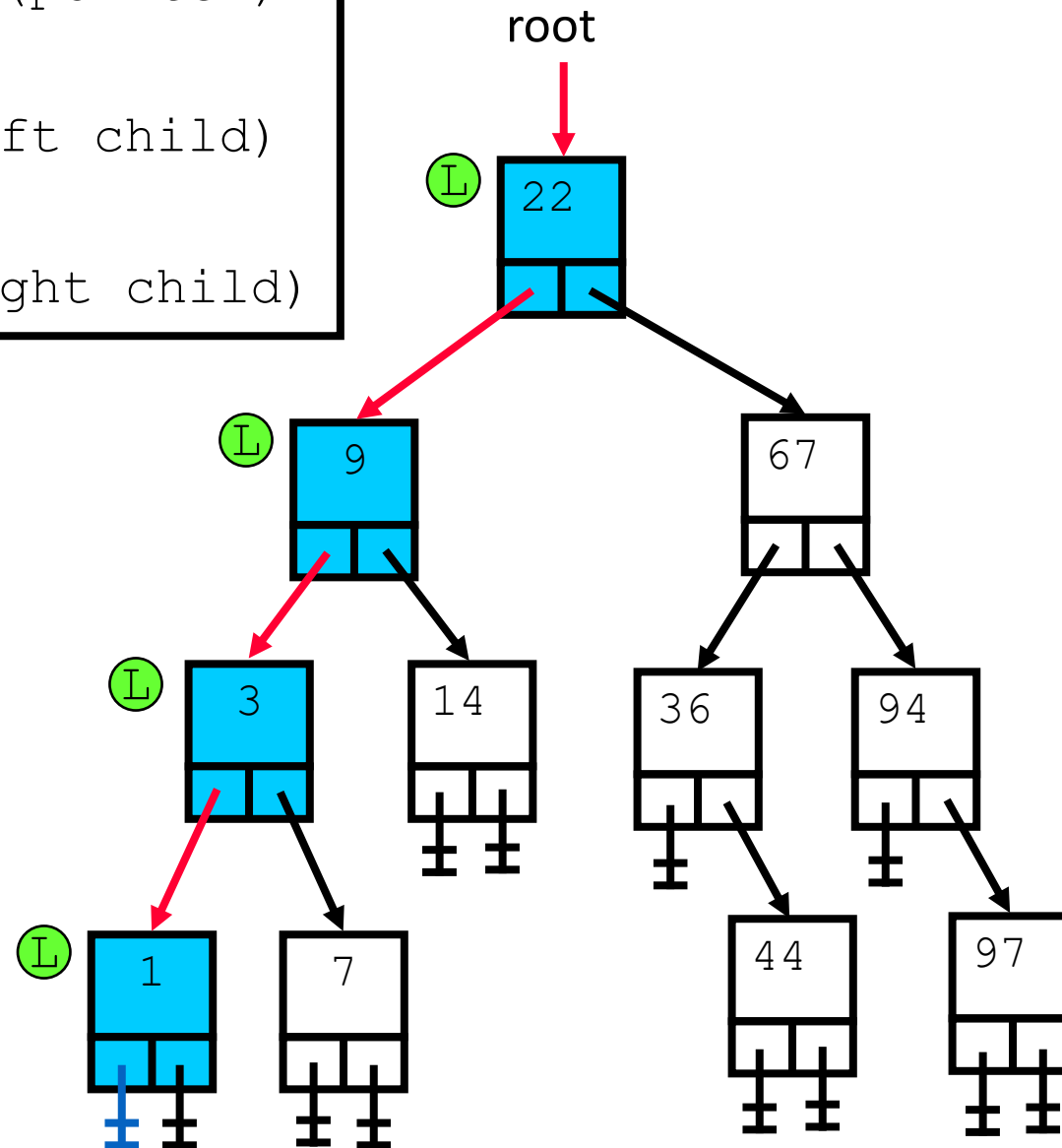
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



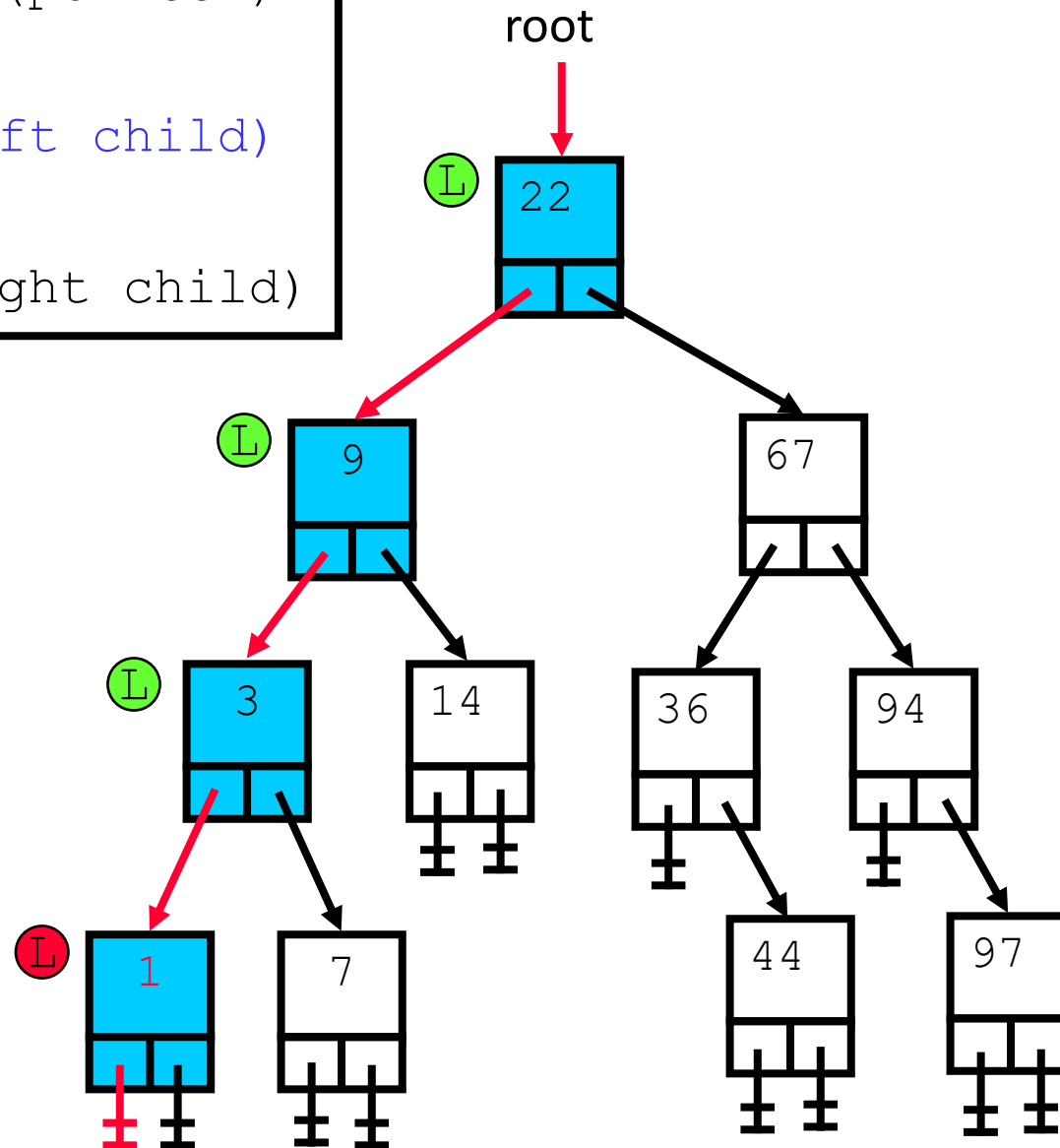
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

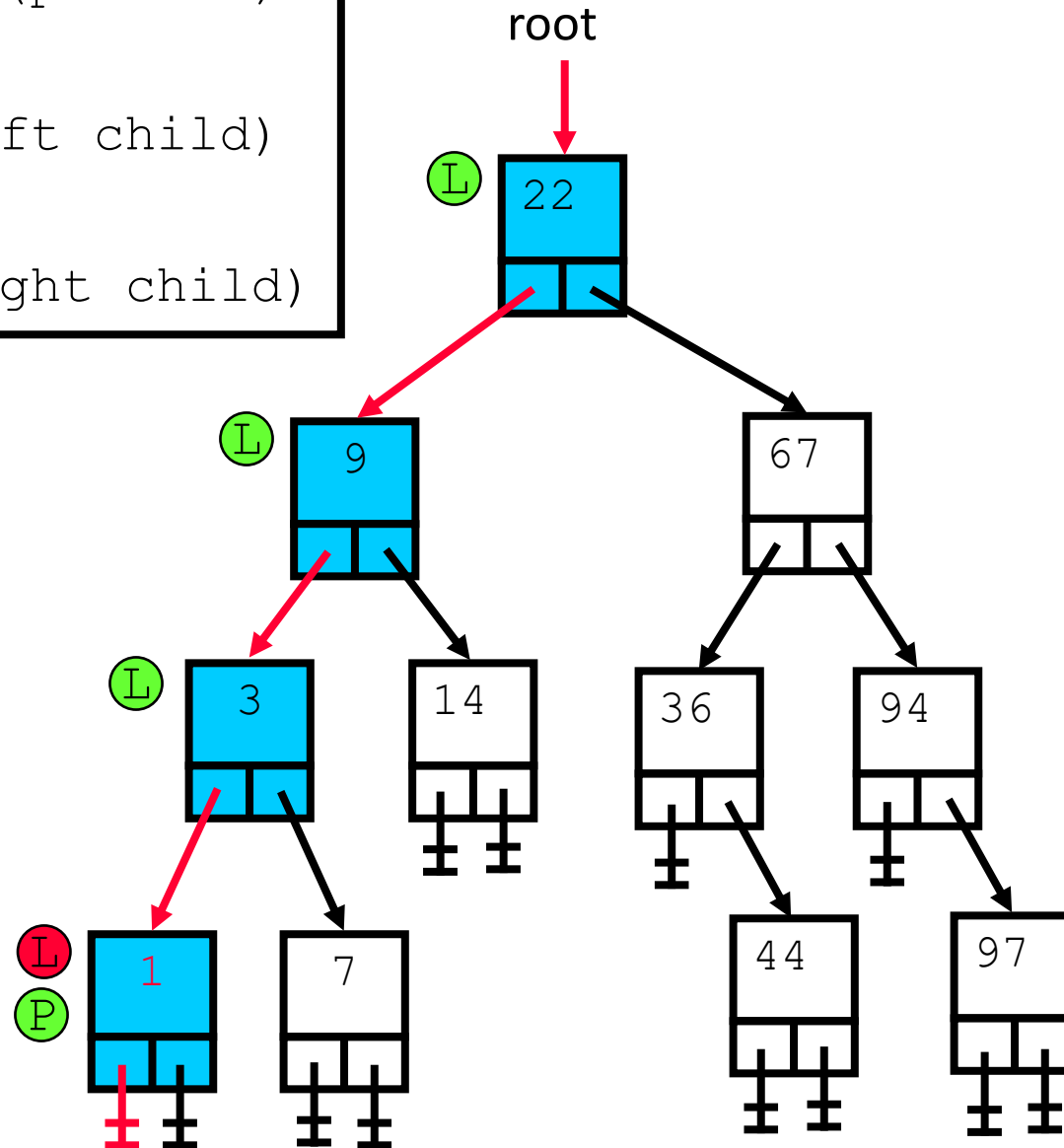


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

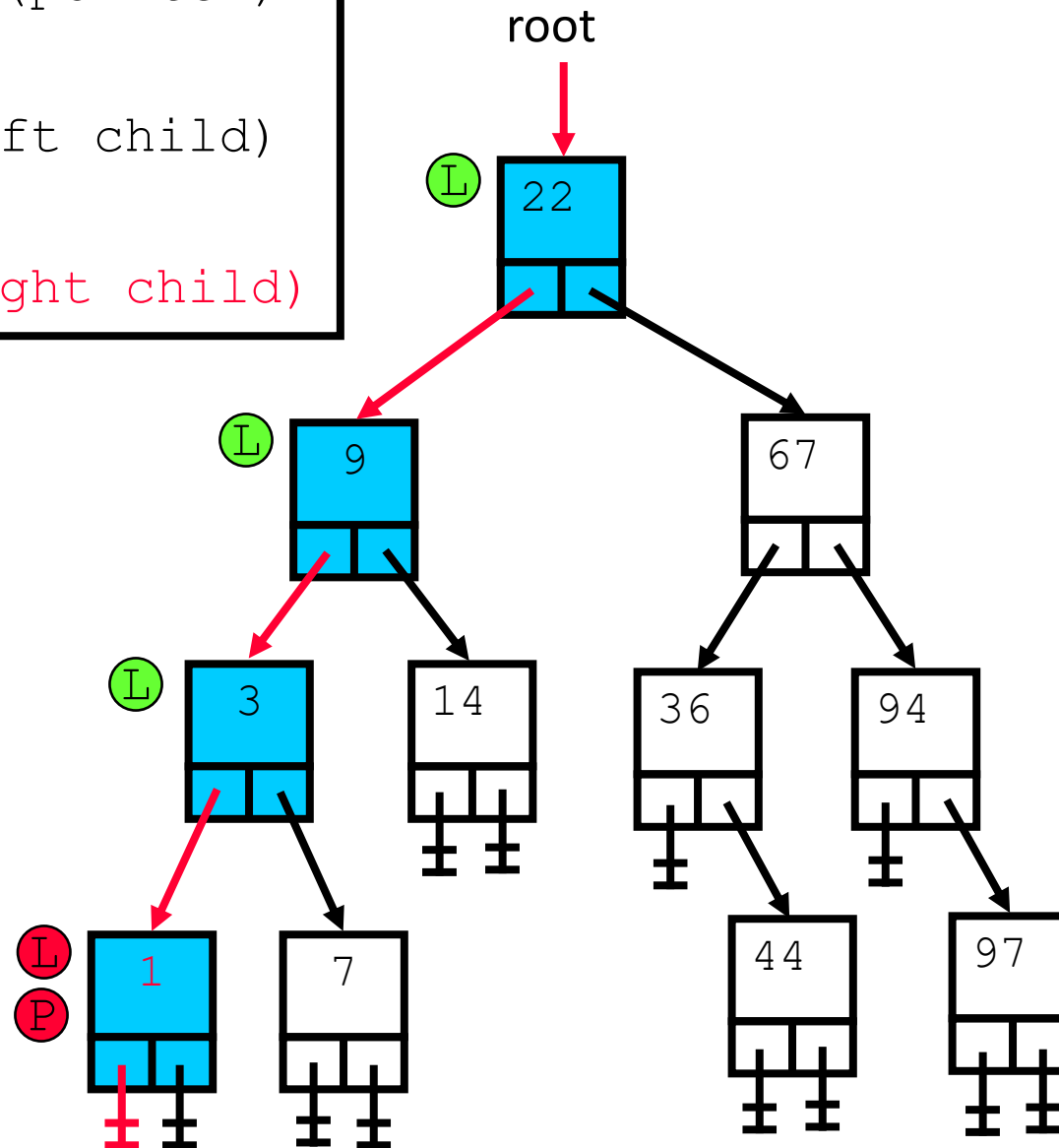
```

Output: 1




```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1

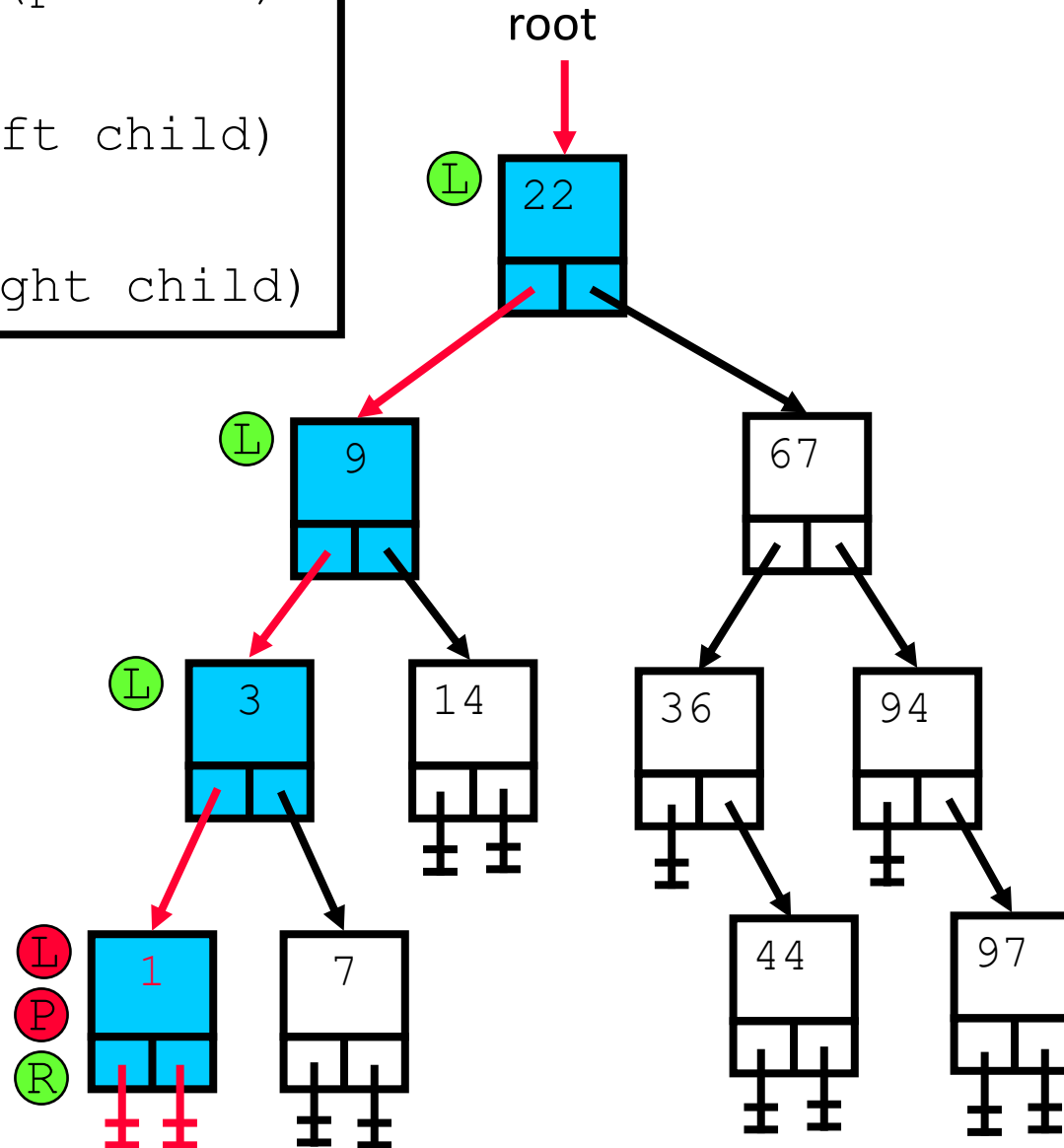


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

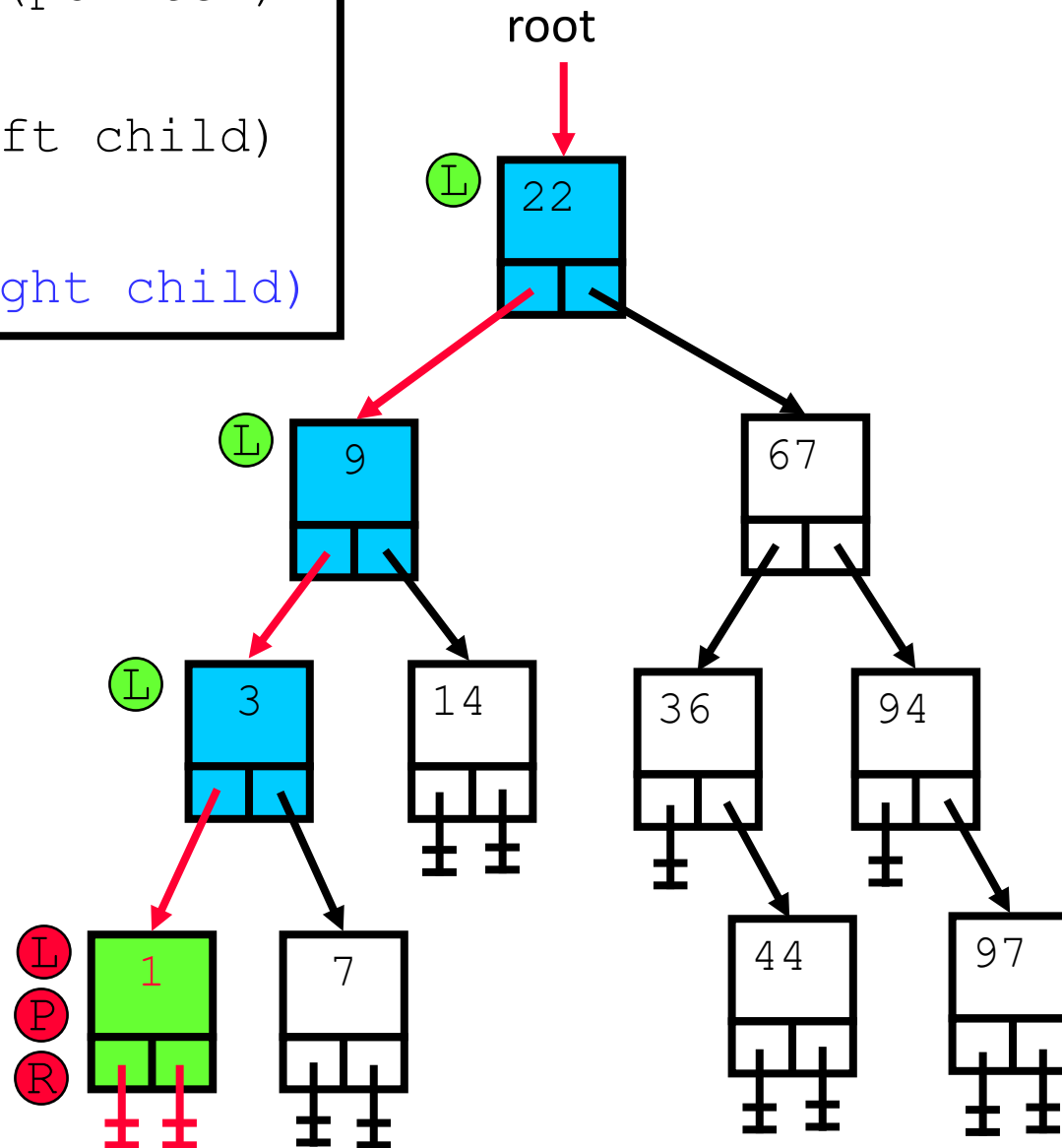
```

Output: 1



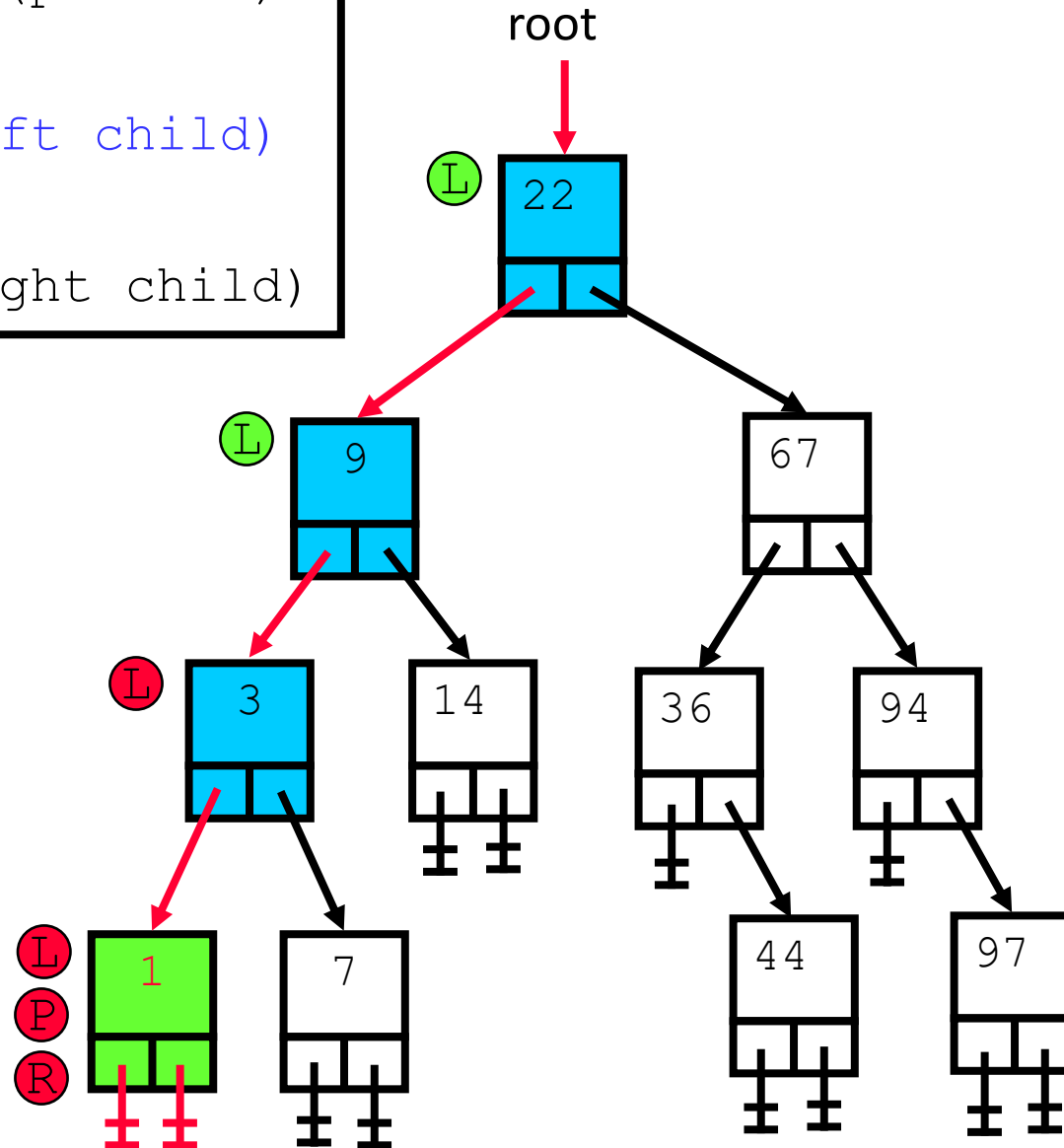
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1



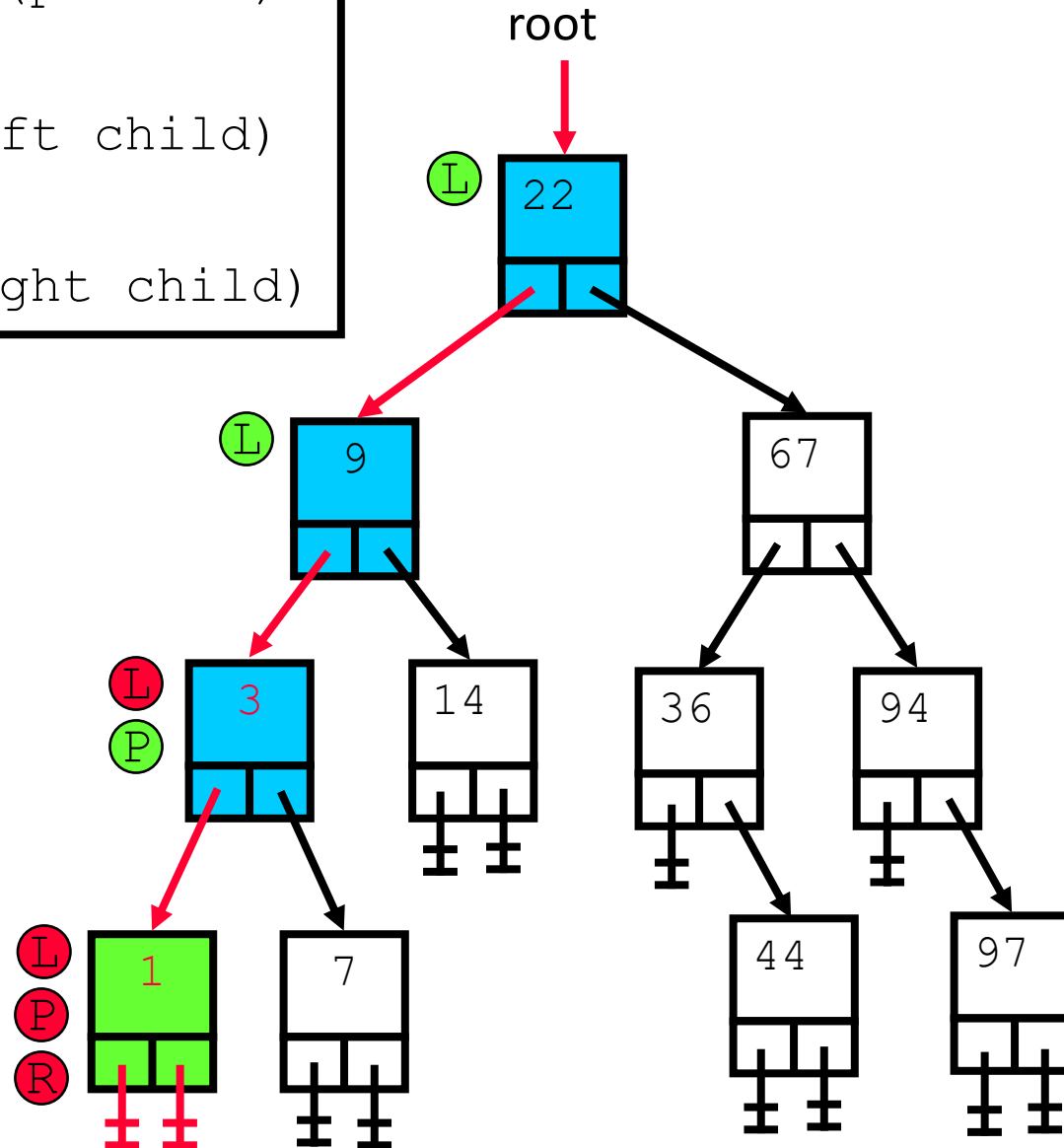
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3

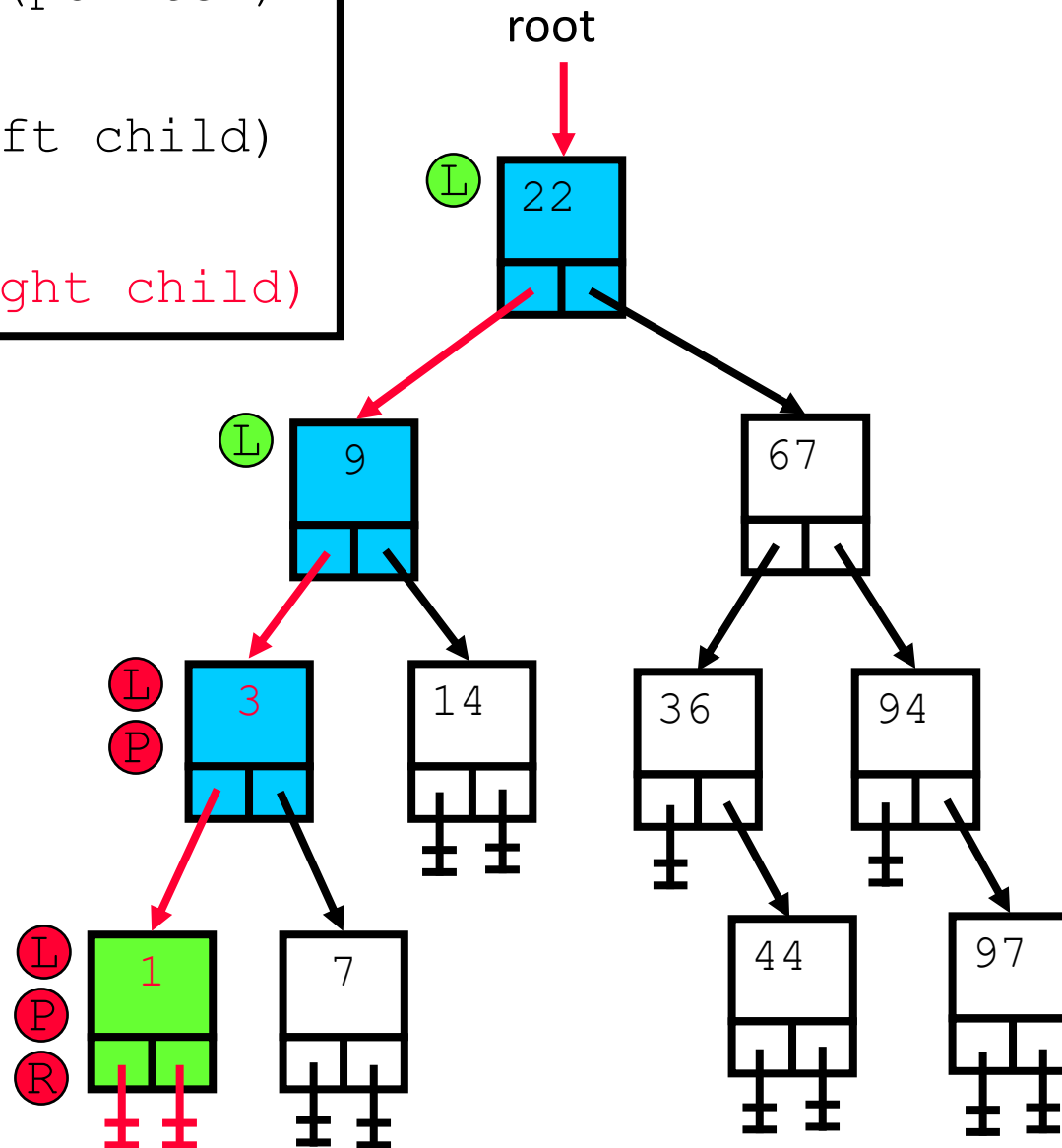


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

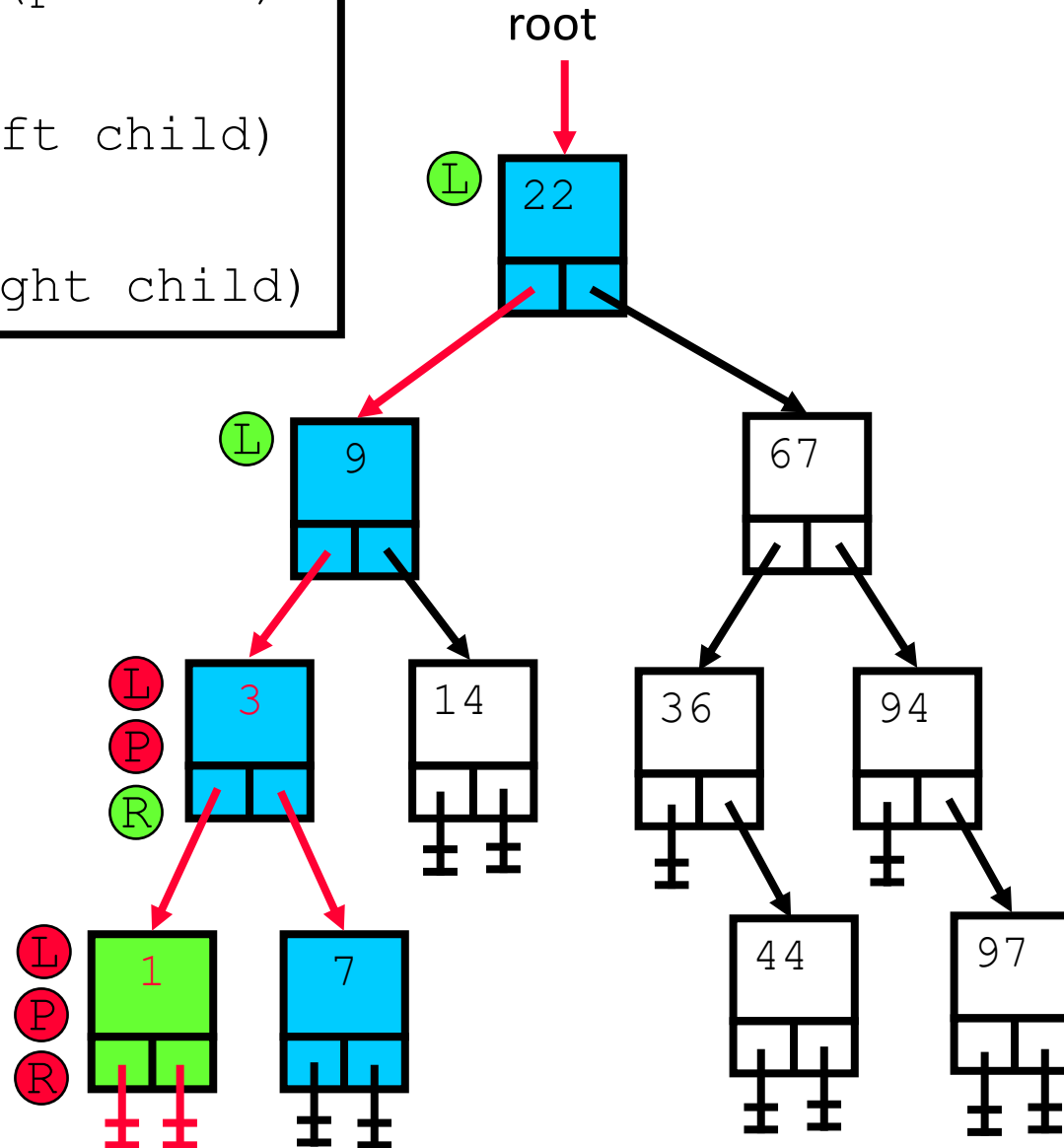
```

Output: 1 3



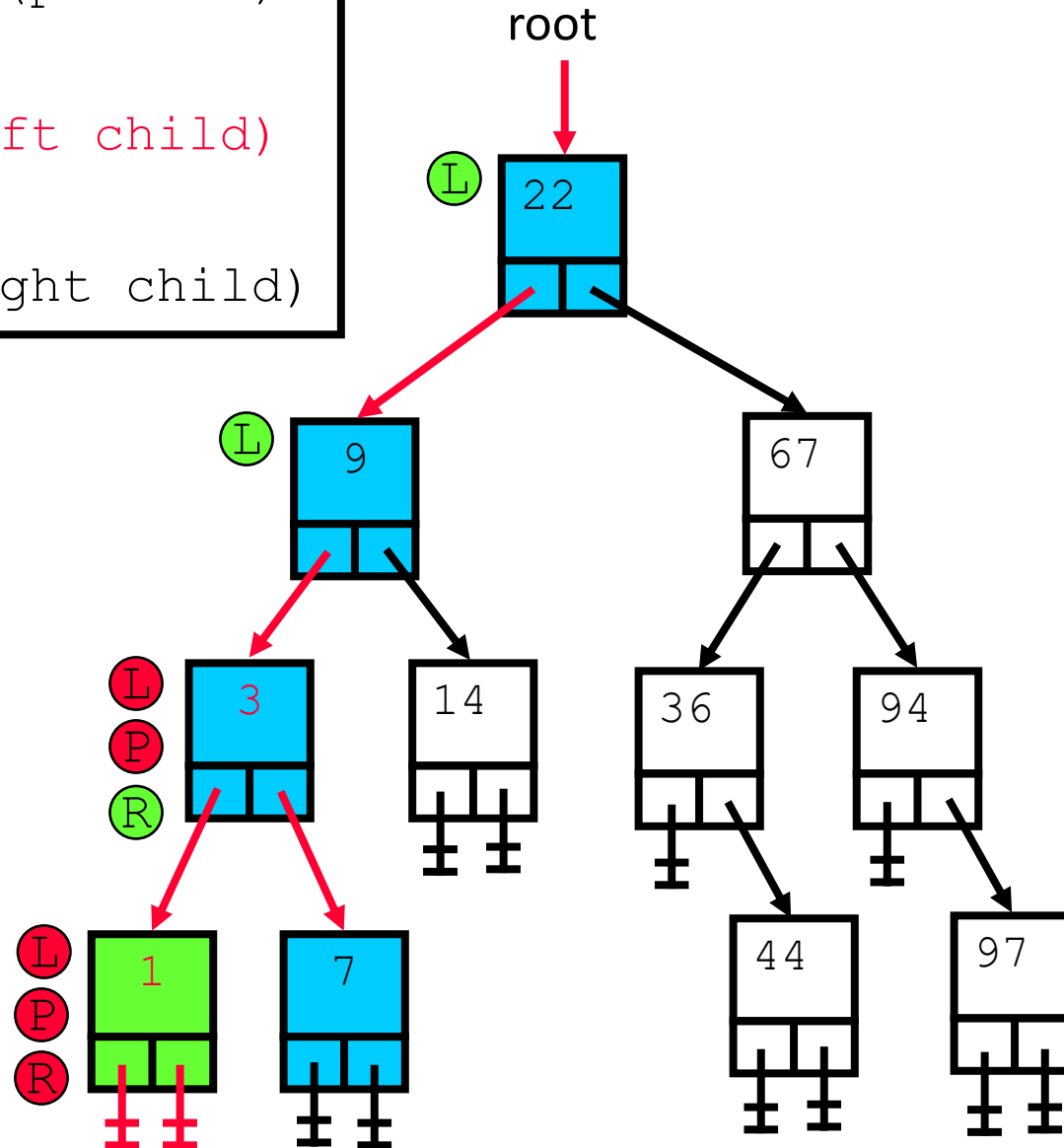
```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3

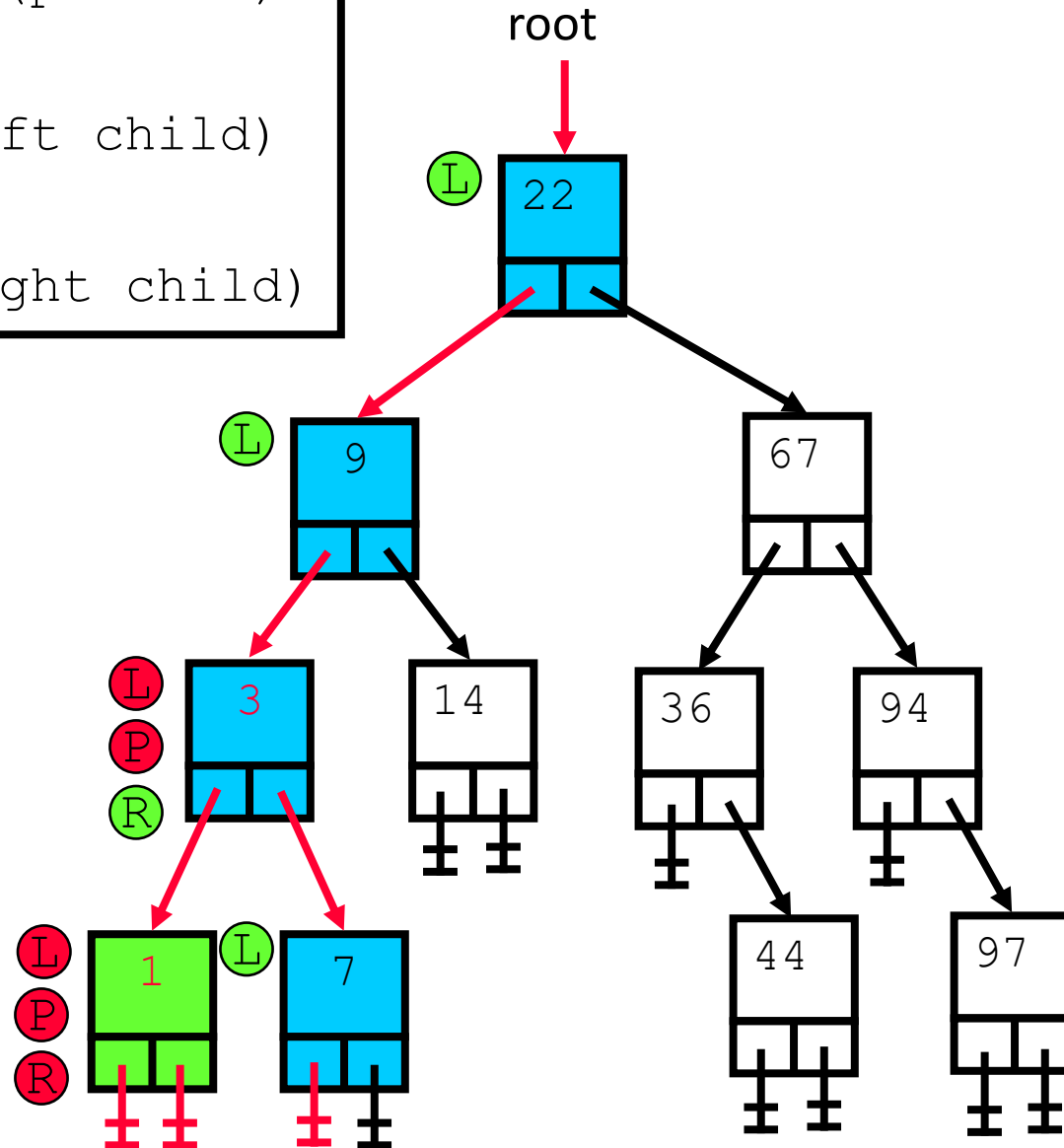



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3

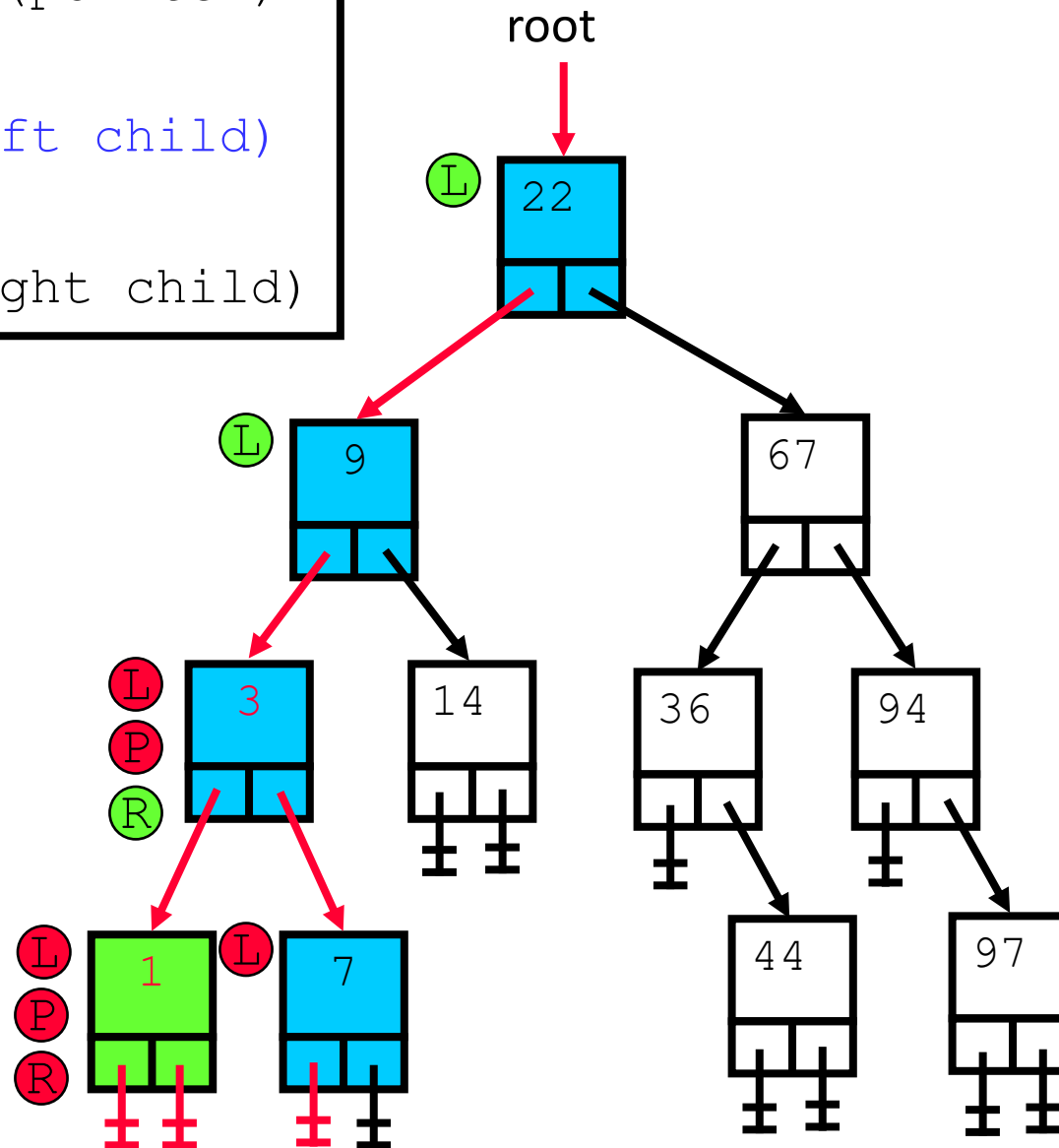


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3

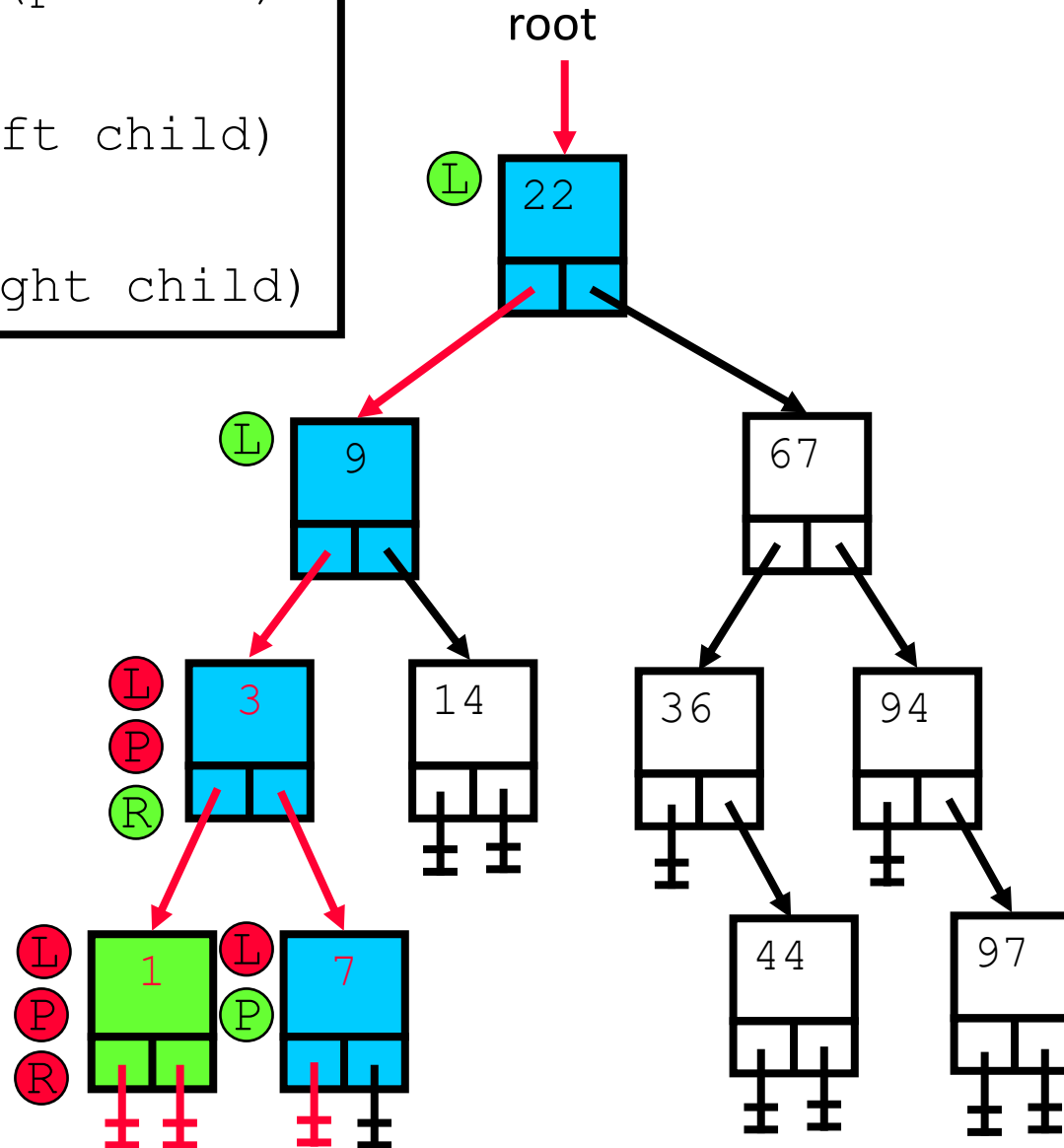


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

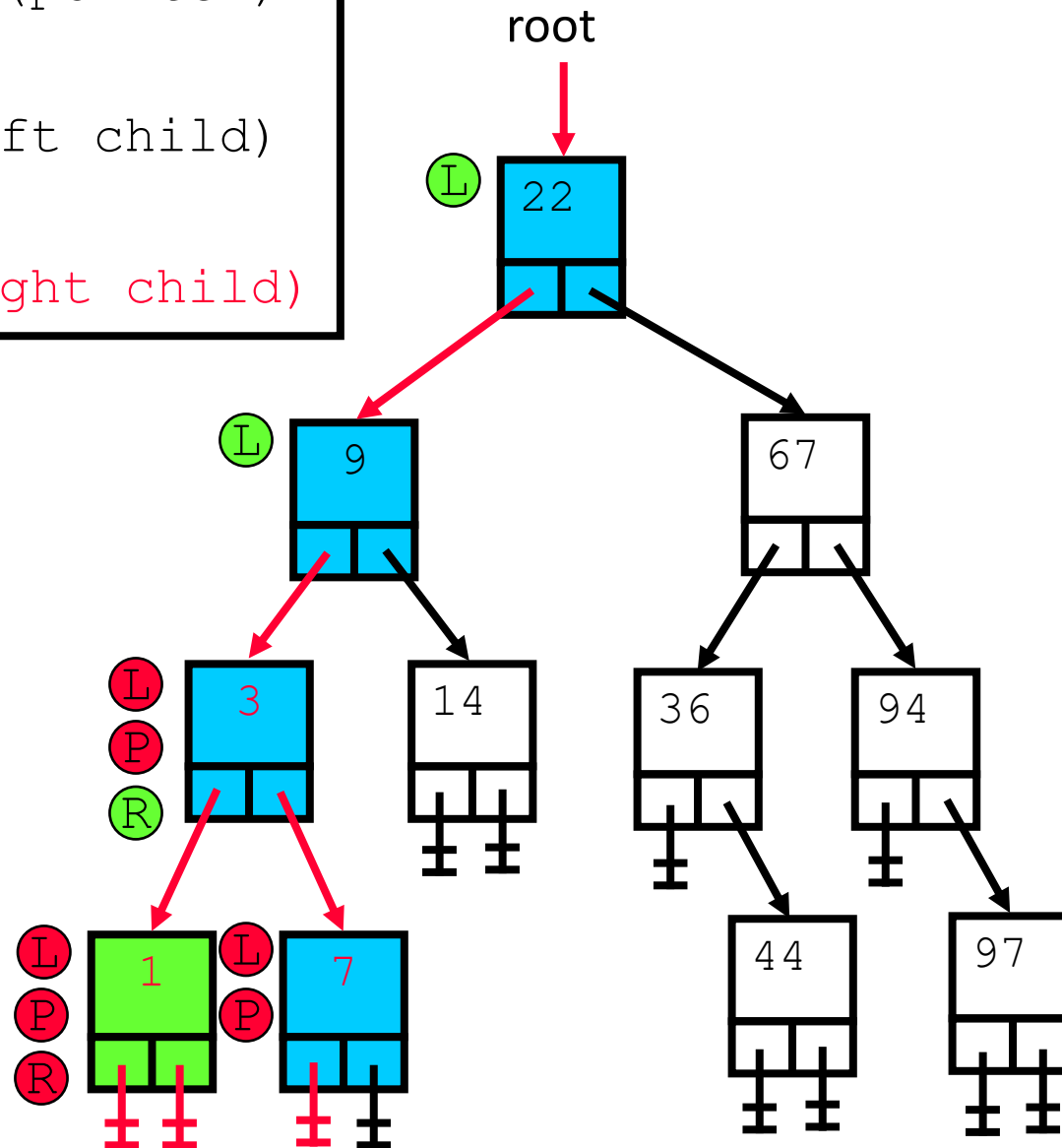
```

Output: 1 3 7



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3 7

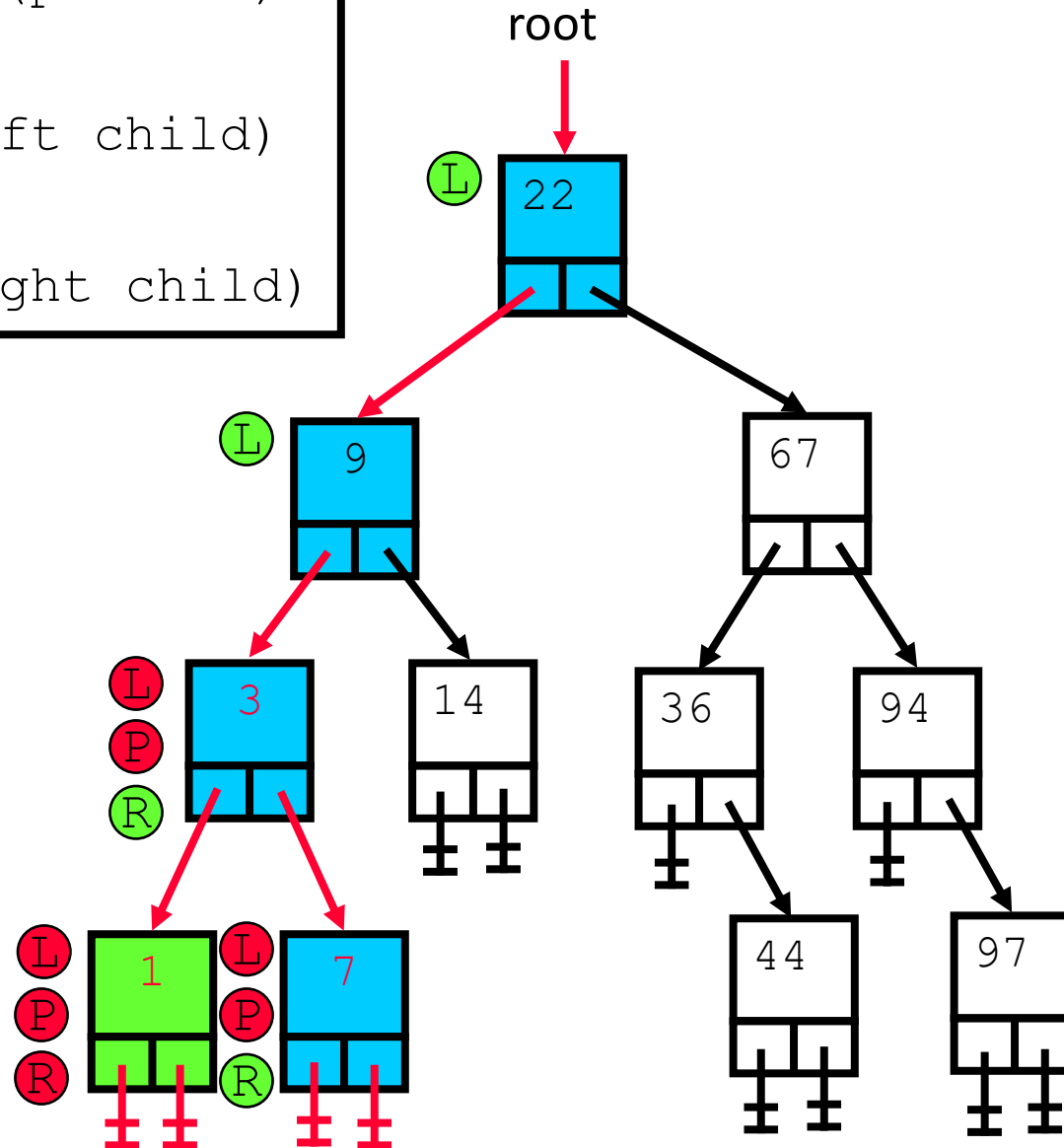


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

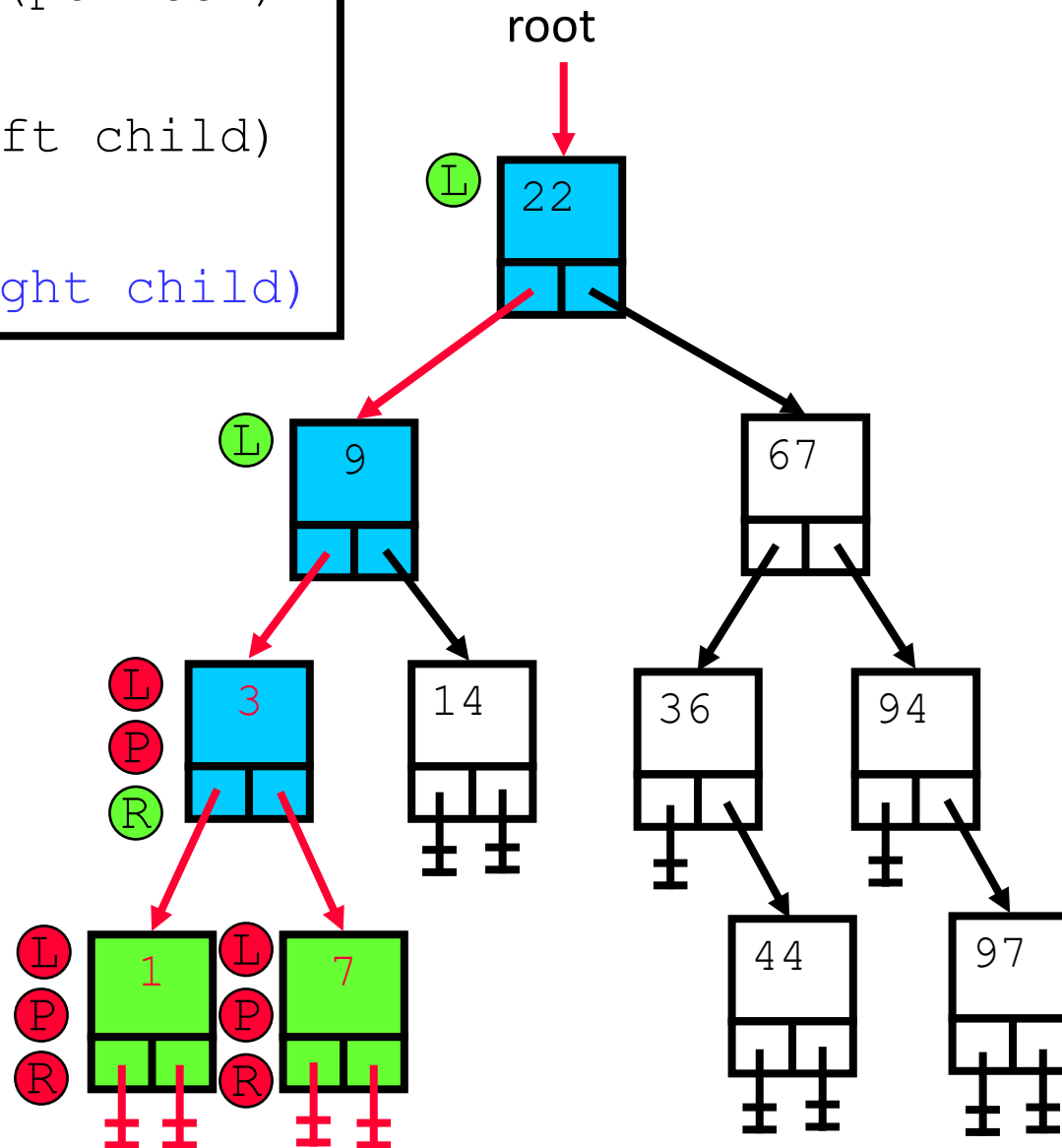
```

Output: 1 3 7



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3 7

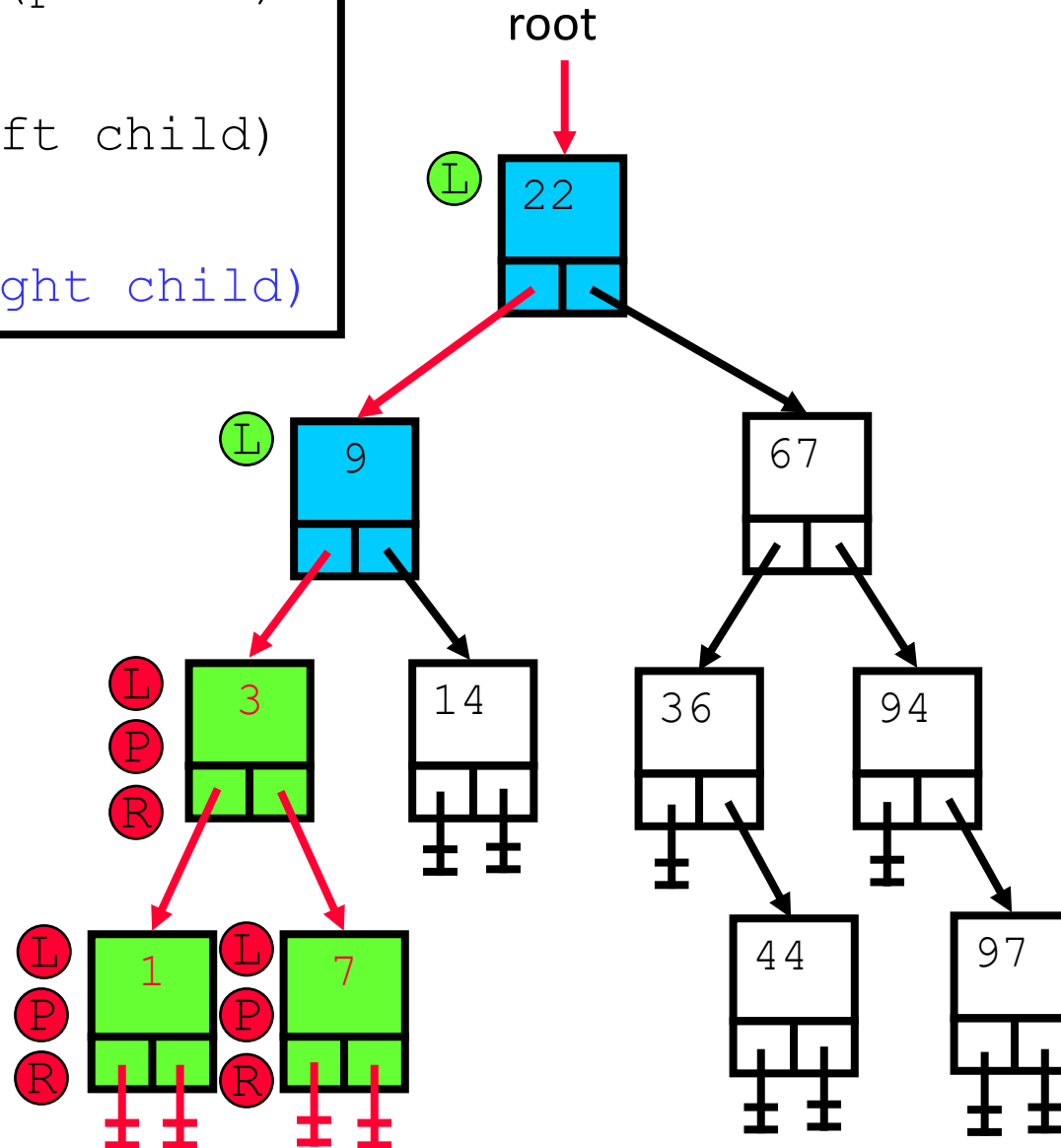


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7

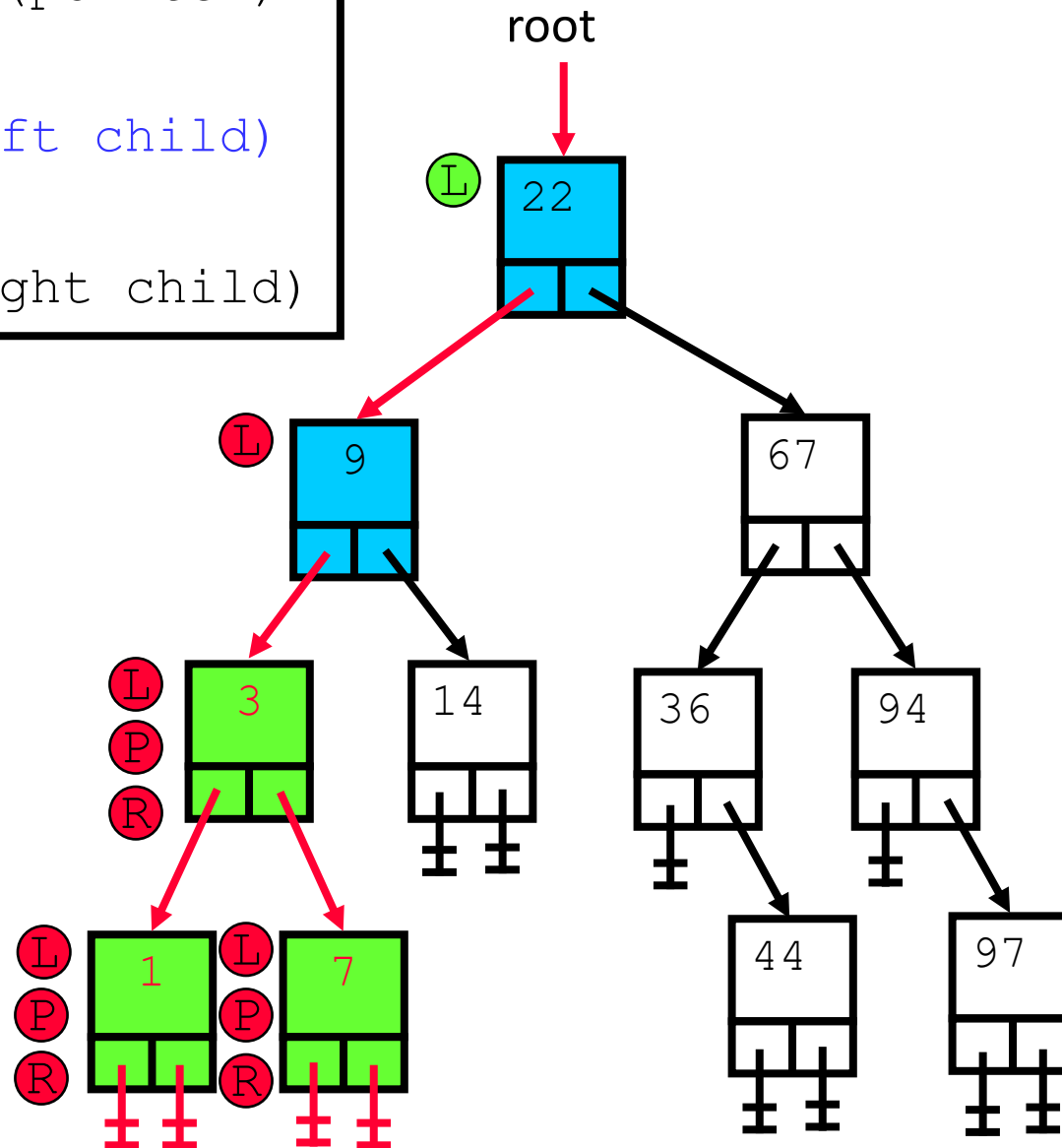


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

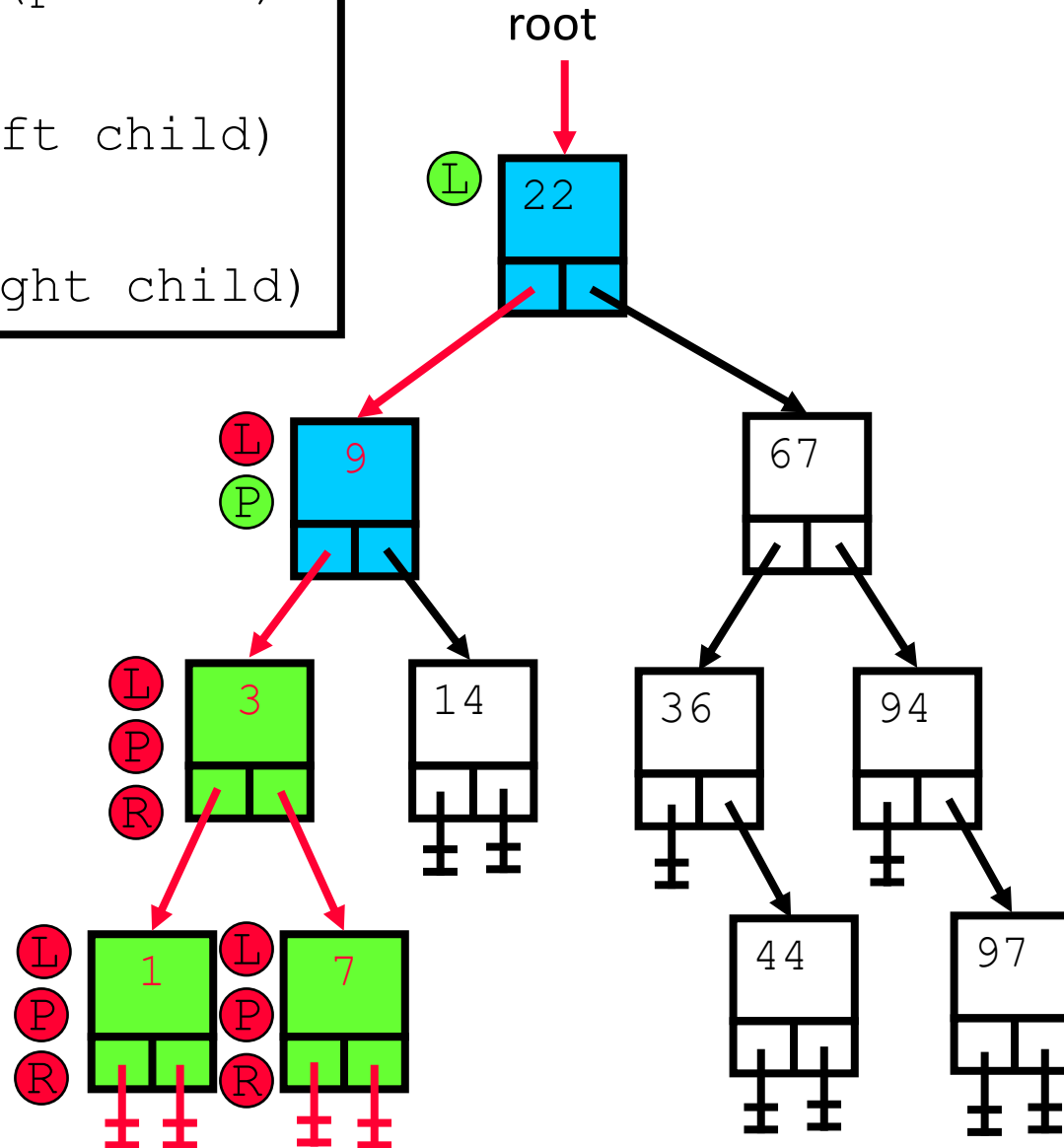
```

Output: 1 3 7



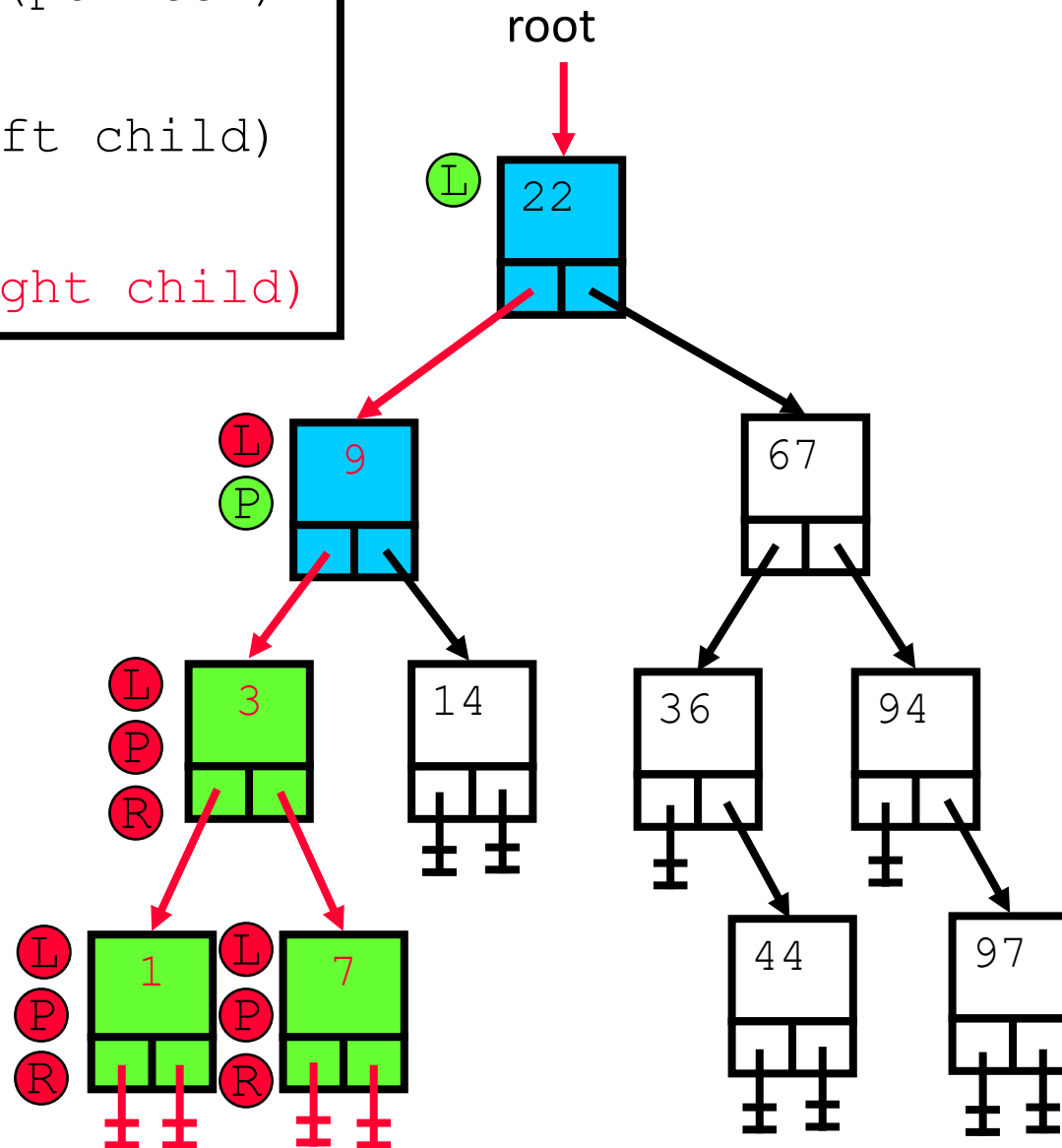

```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3 7 9



```
Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)
```

Output: 1 3 7 9

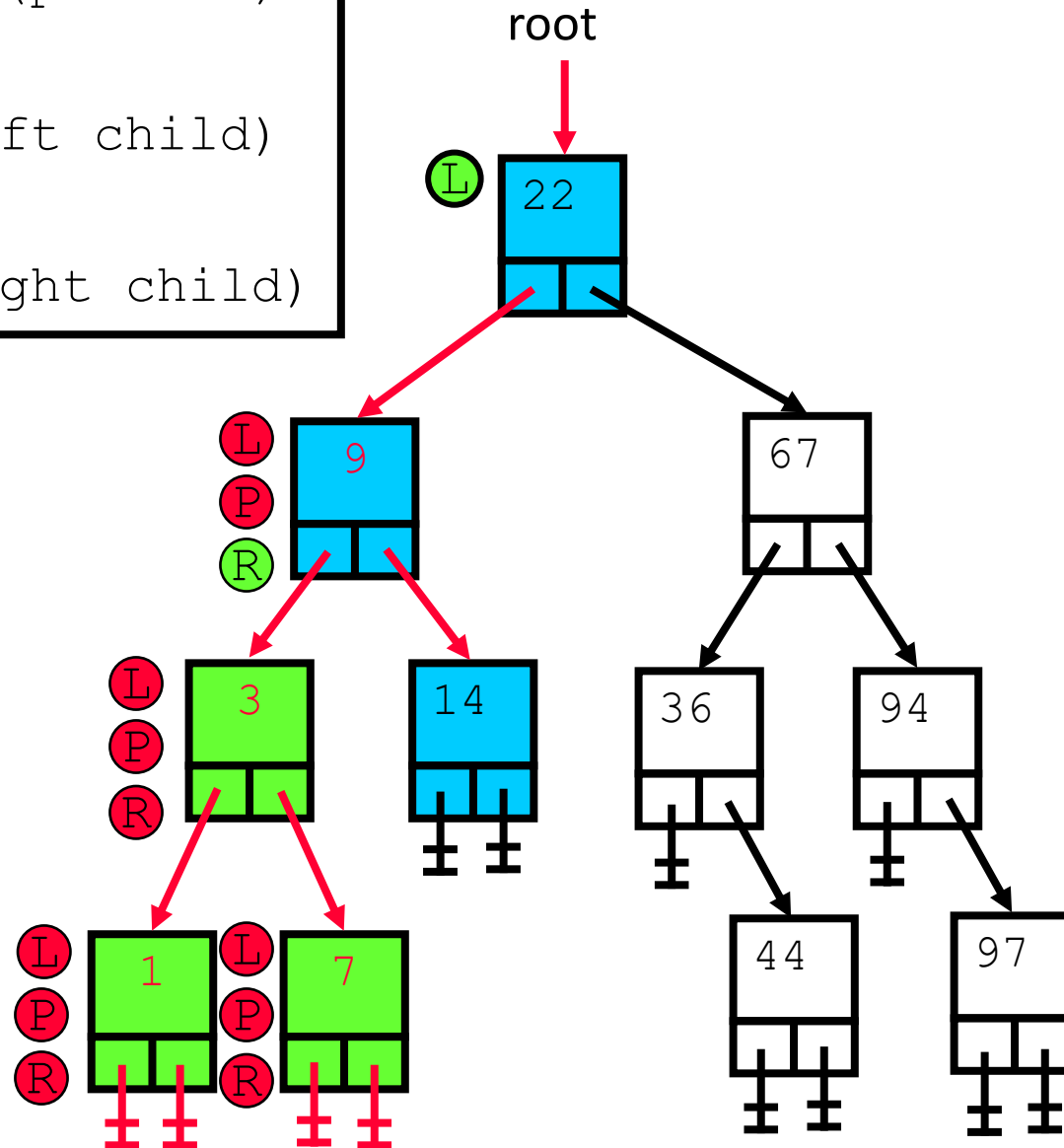


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9

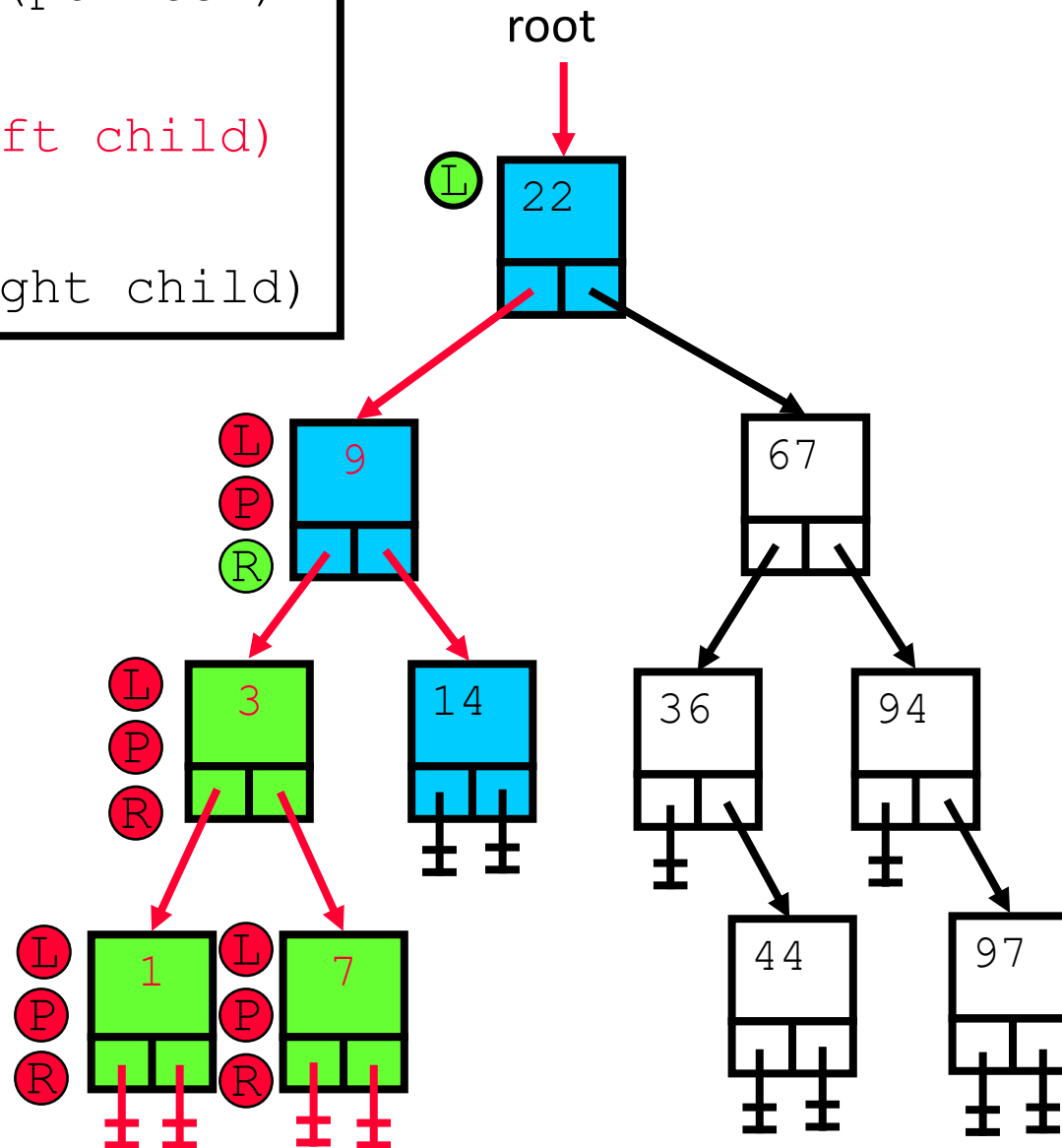


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9

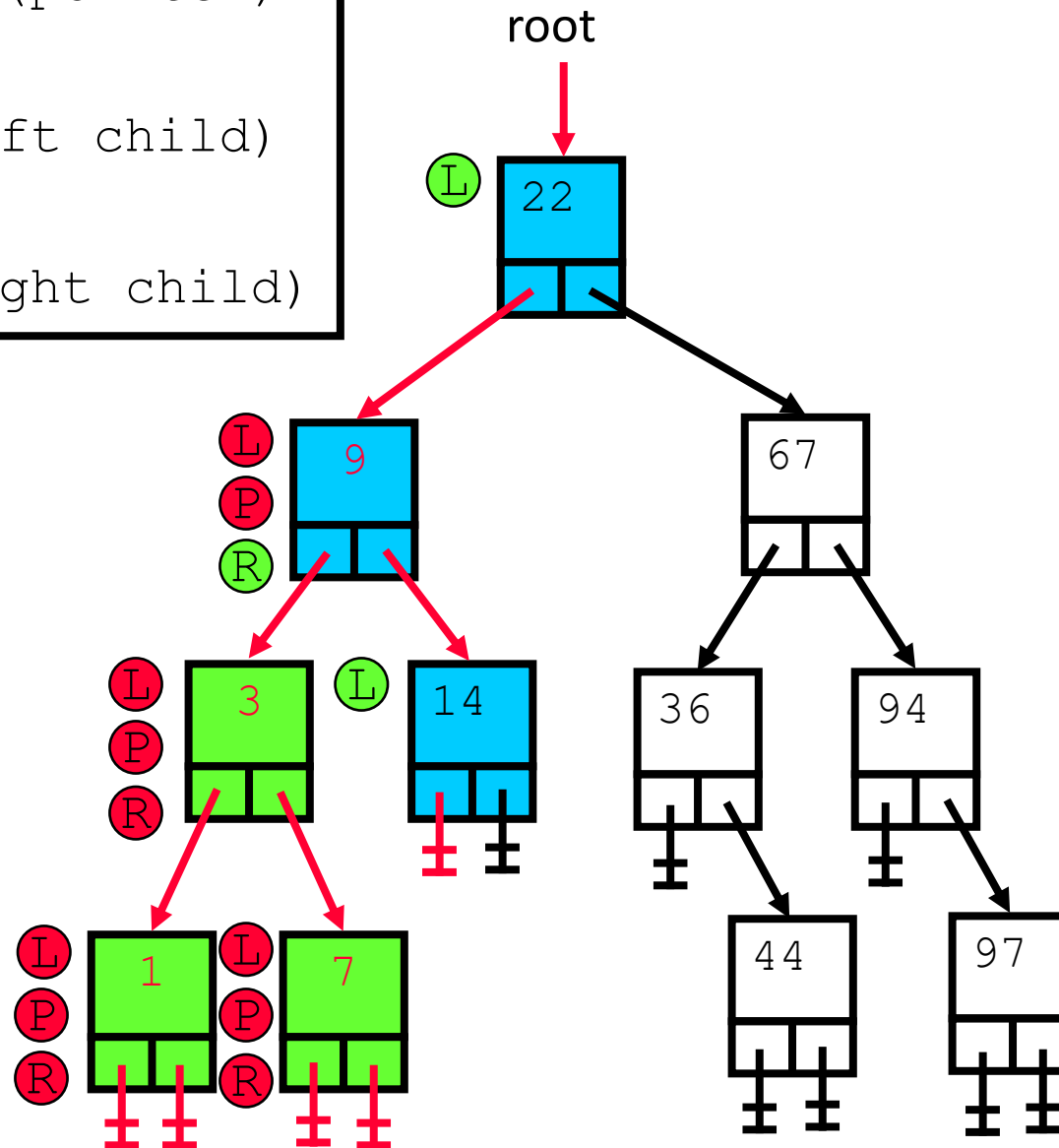


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9

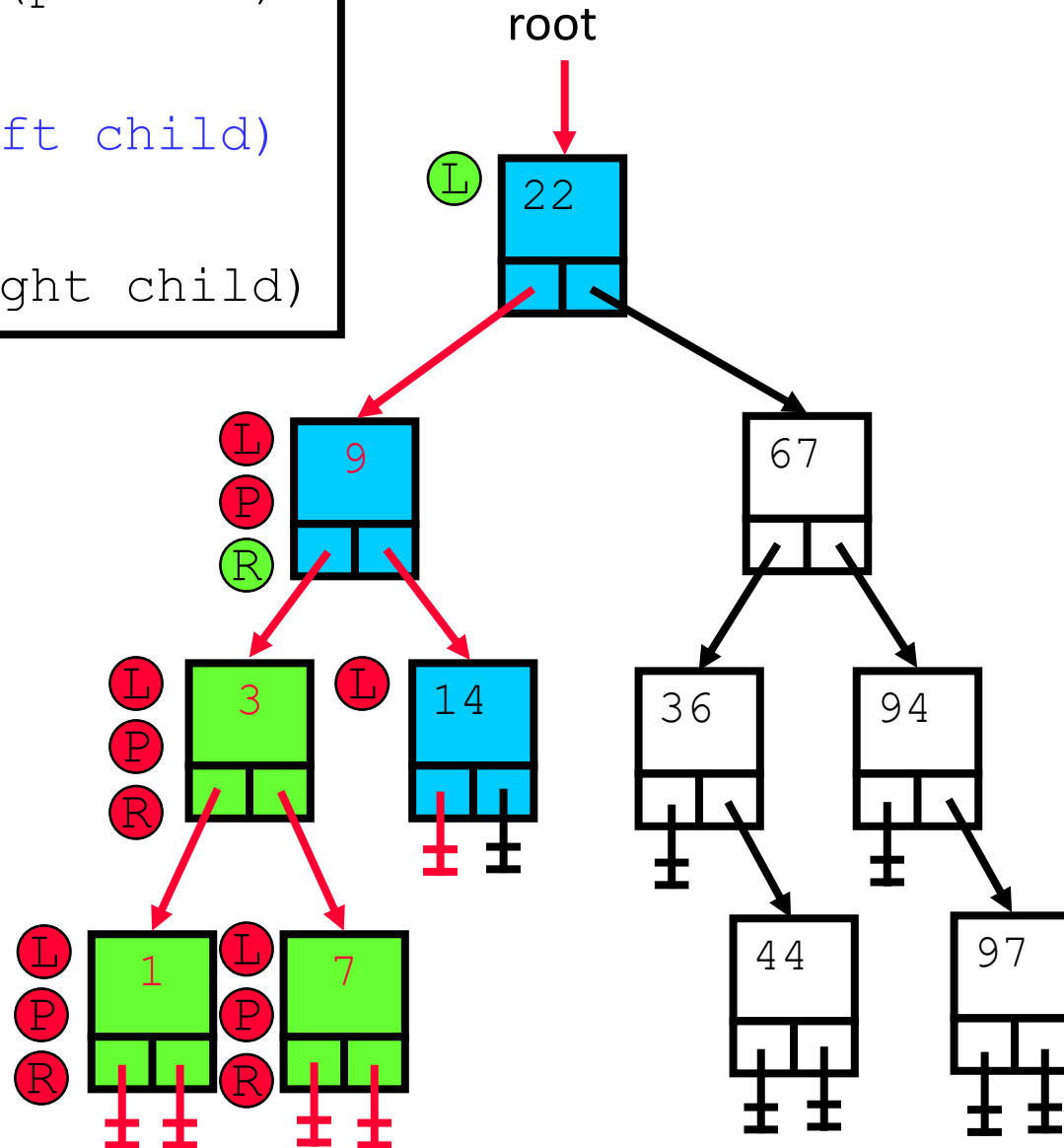


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9

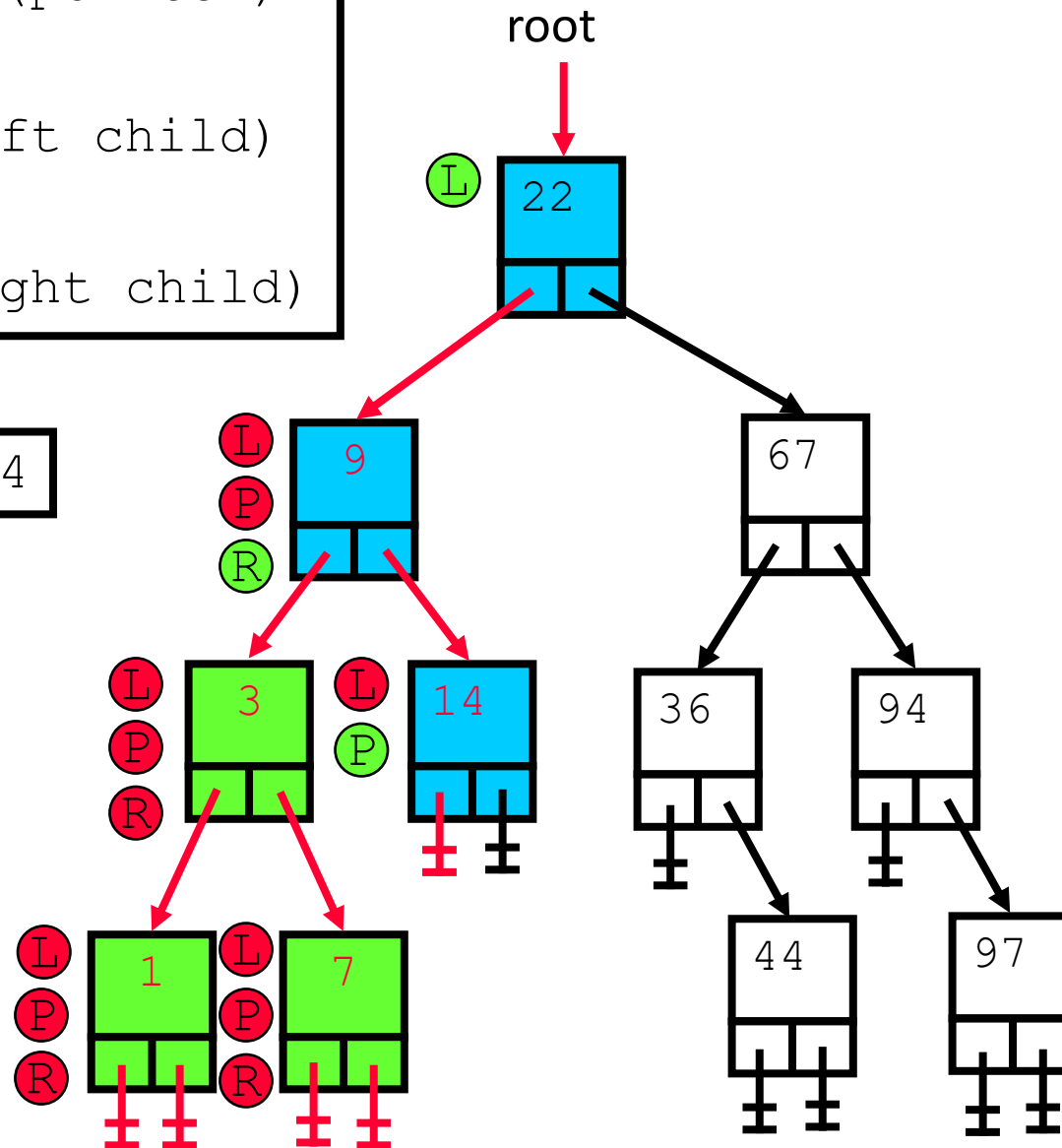


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

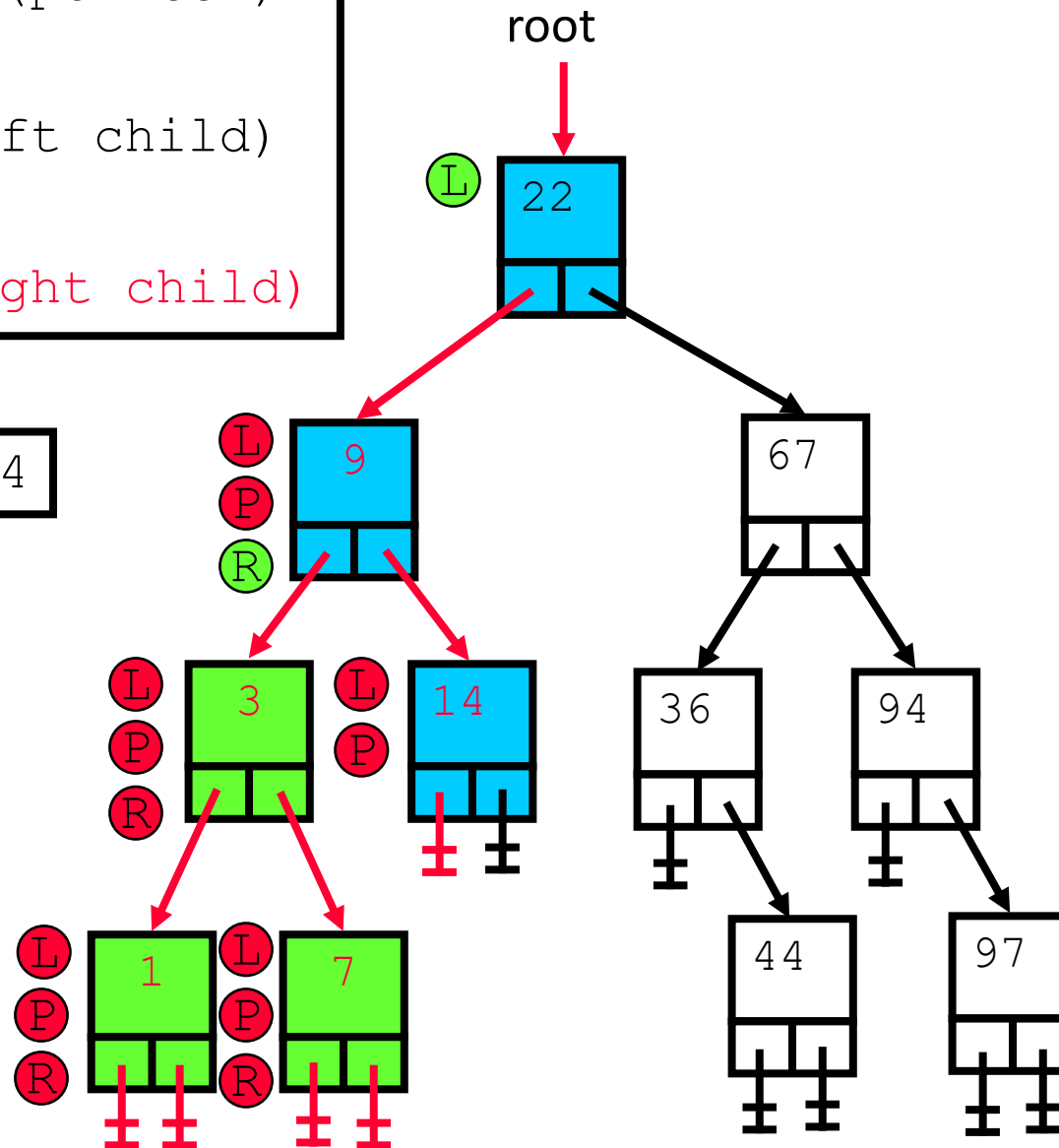


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

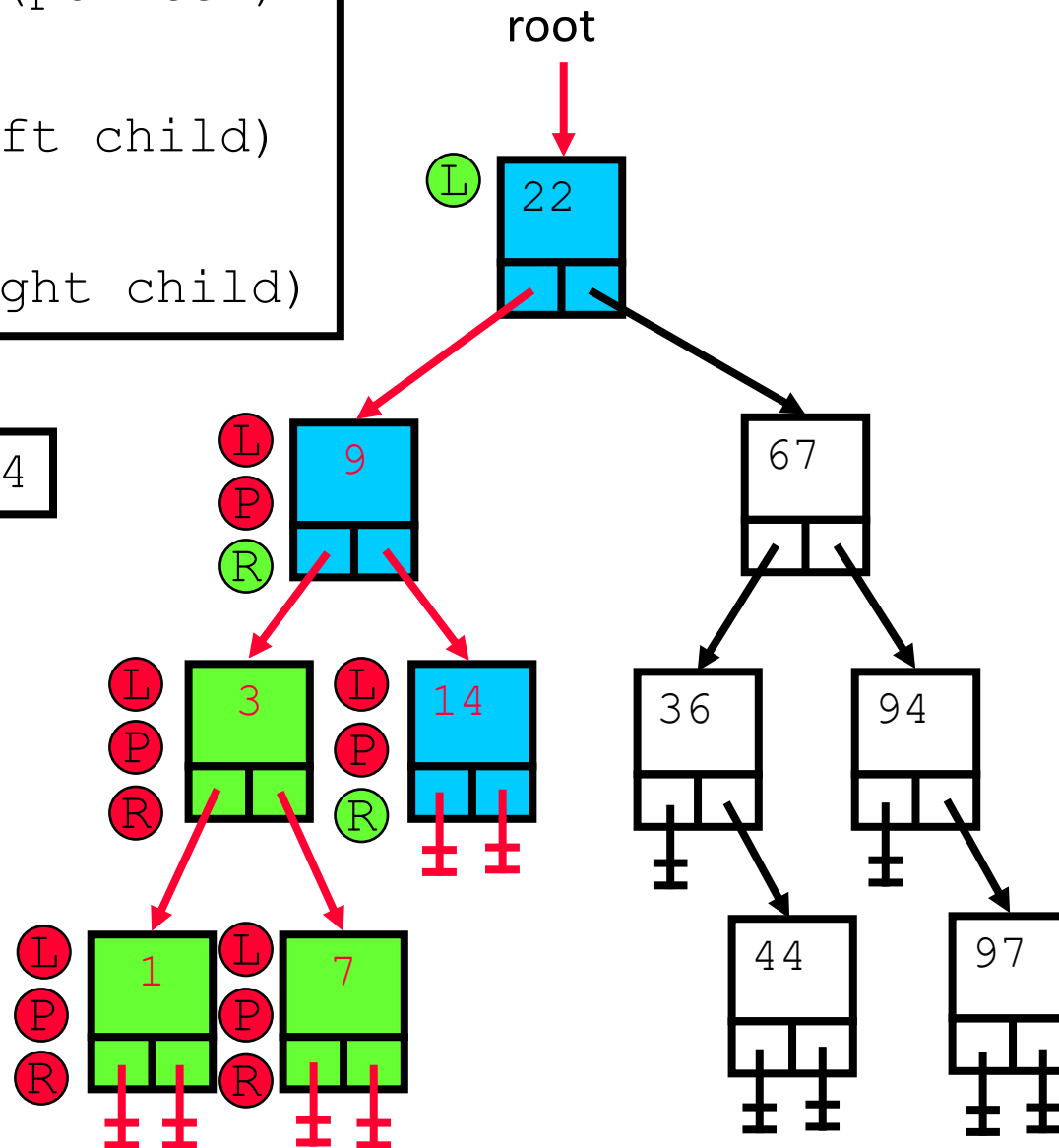



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

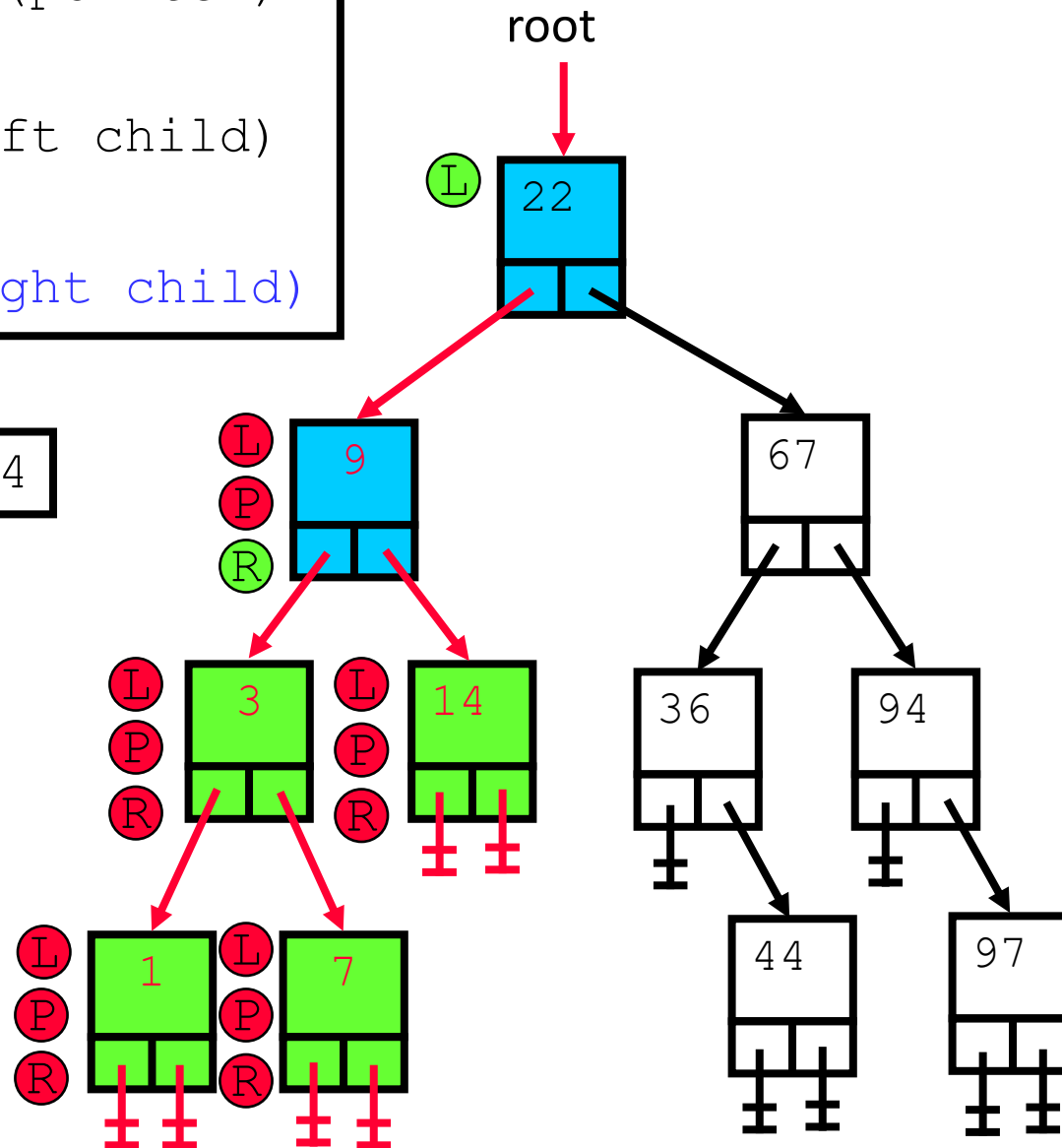


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

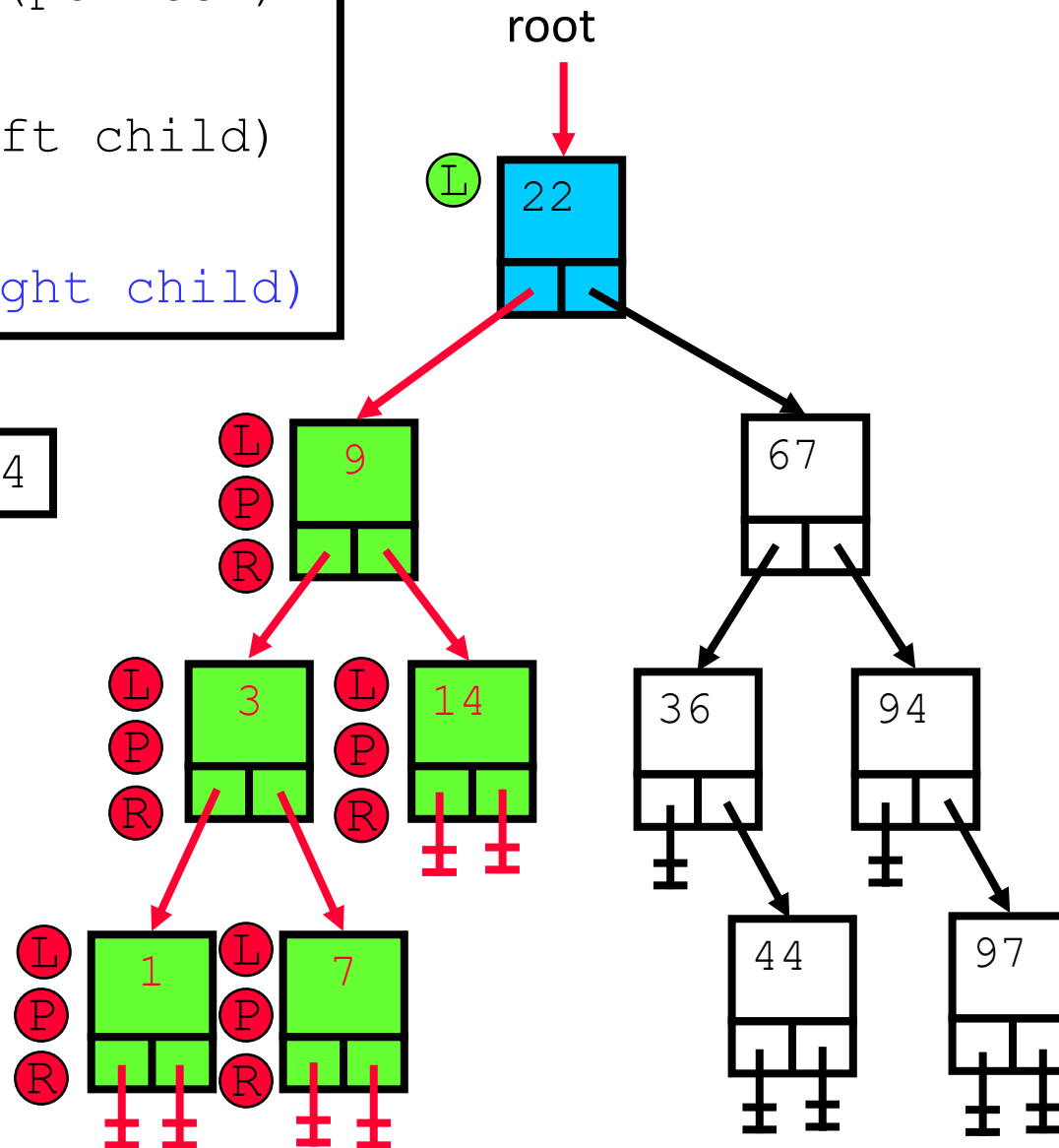


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

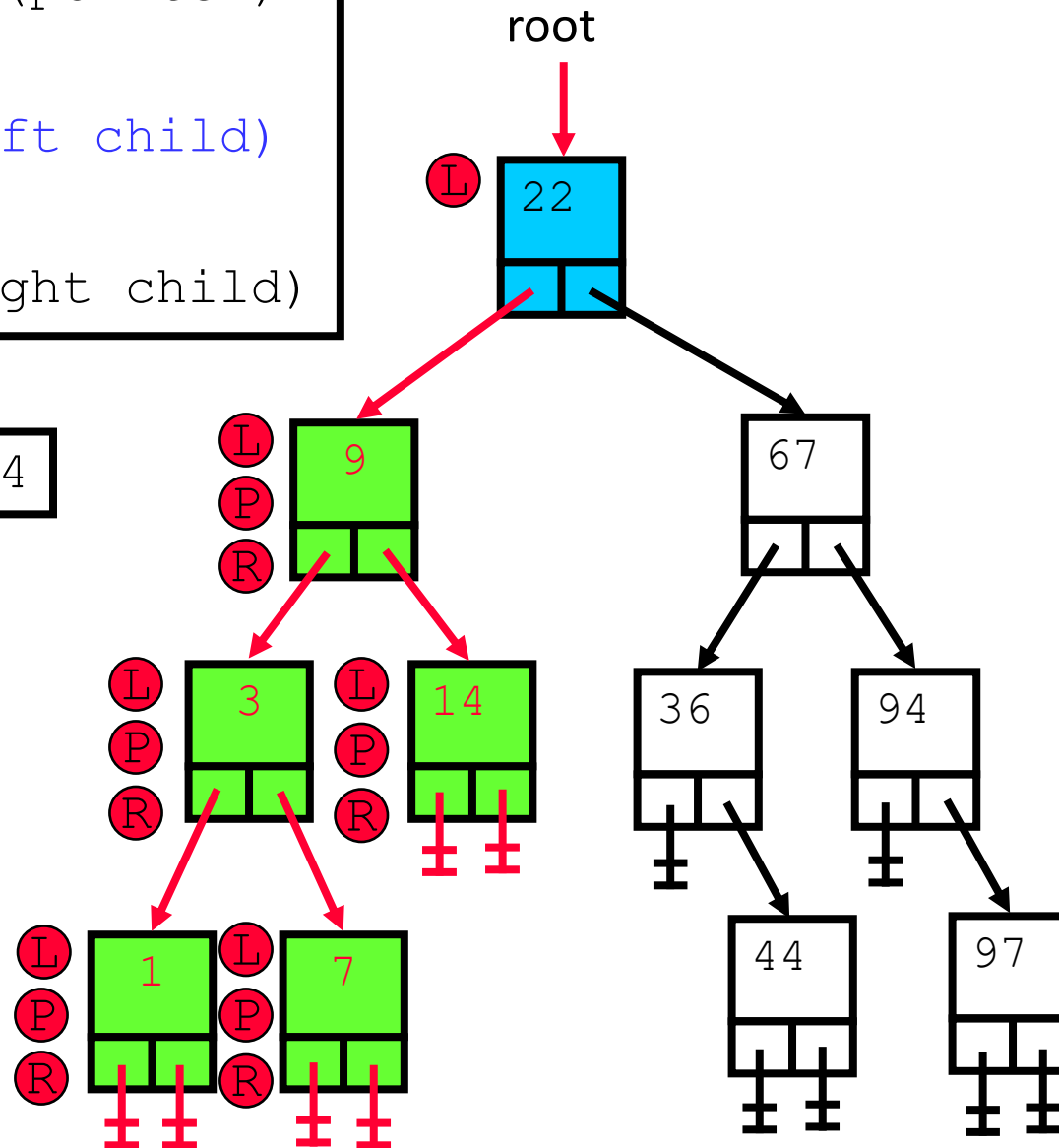


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14

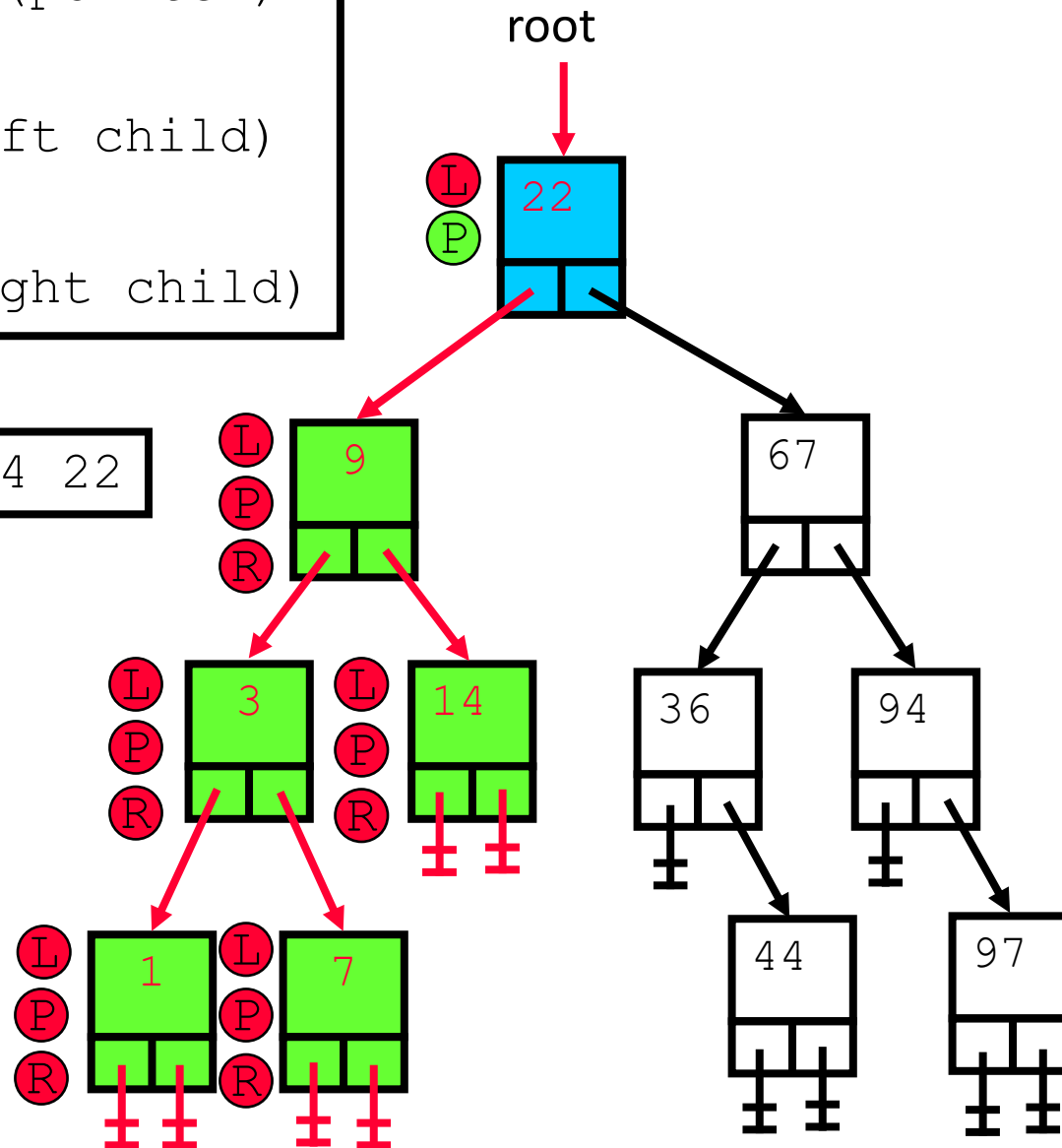


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

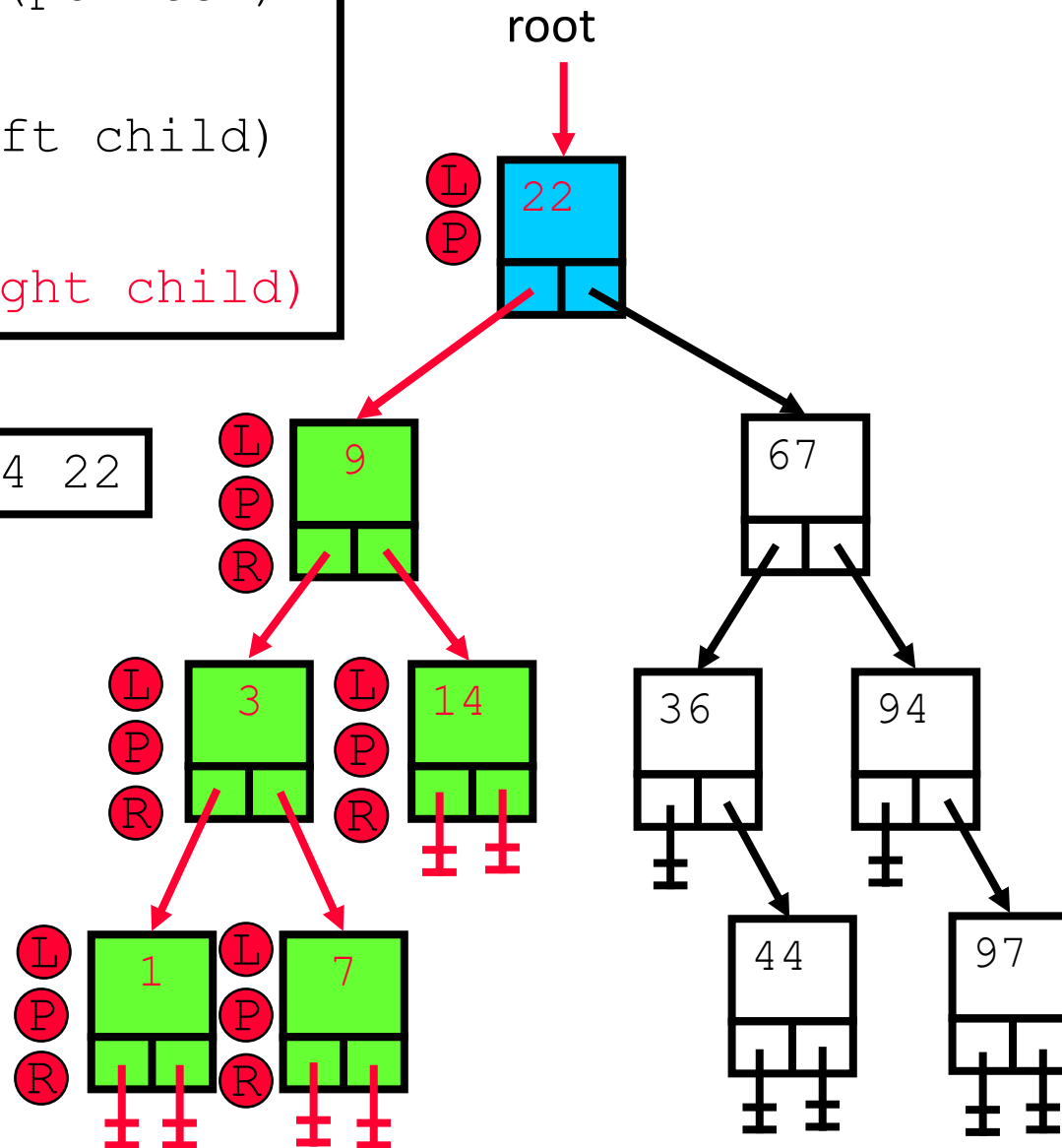


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

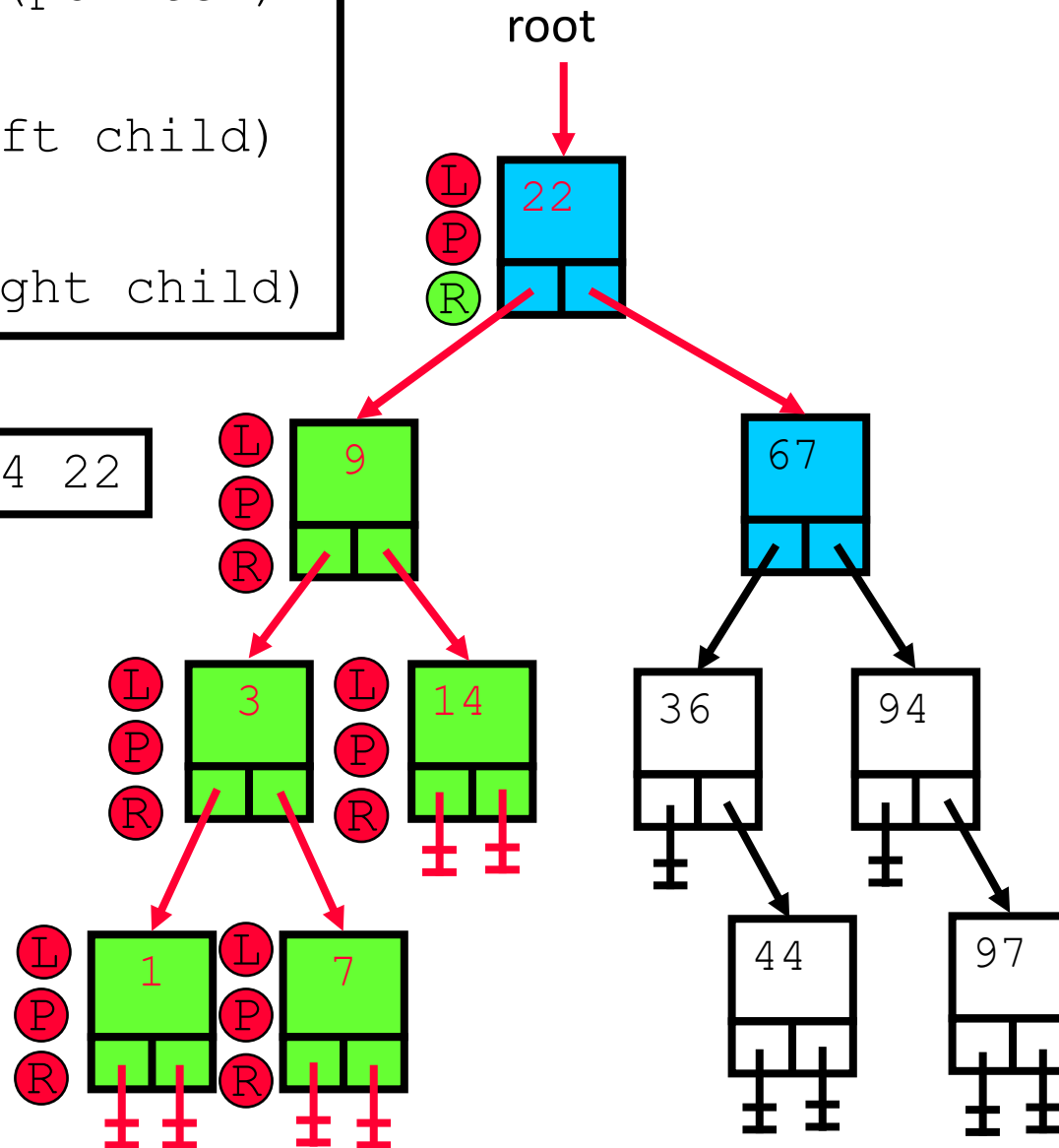


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

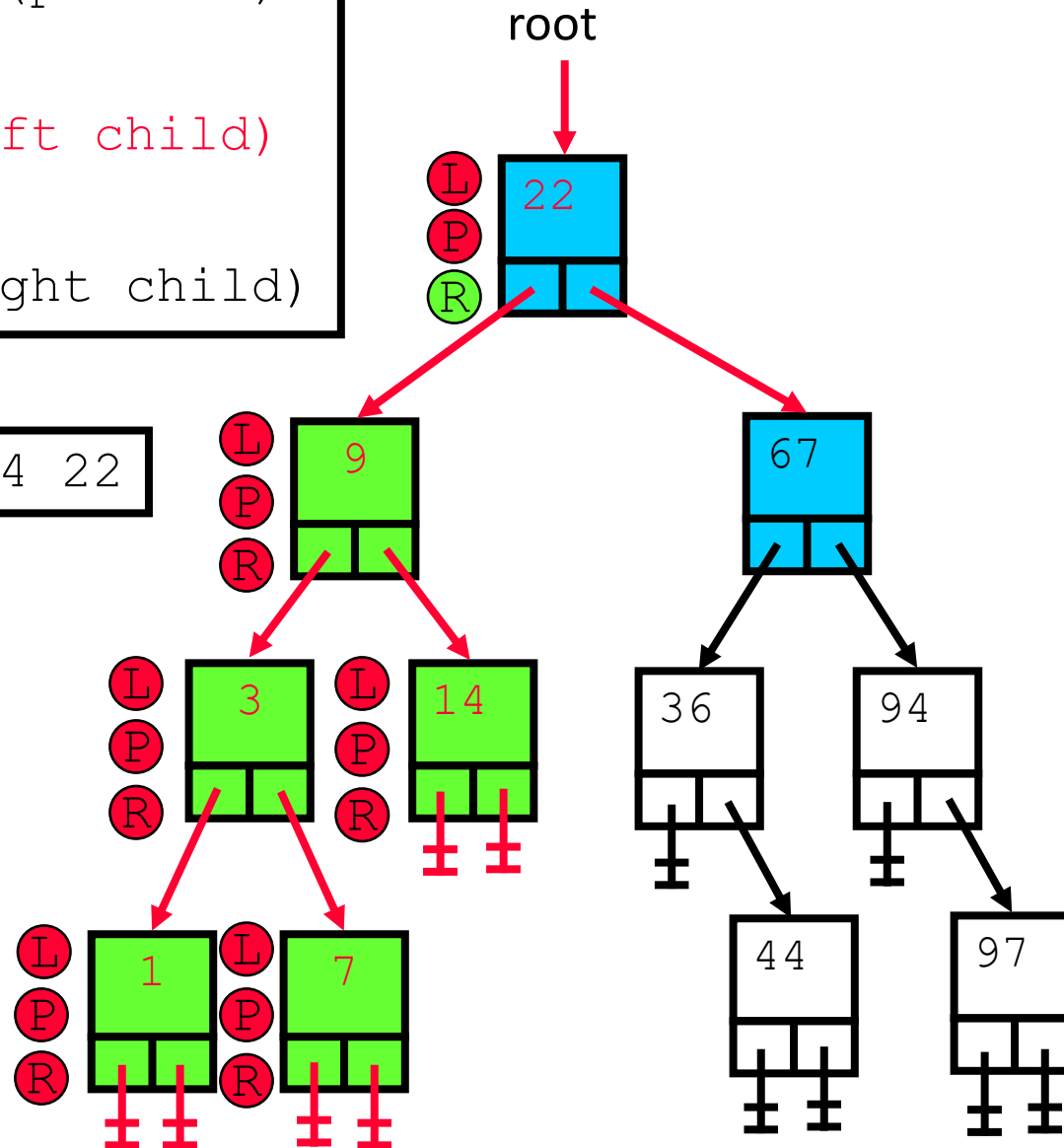


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

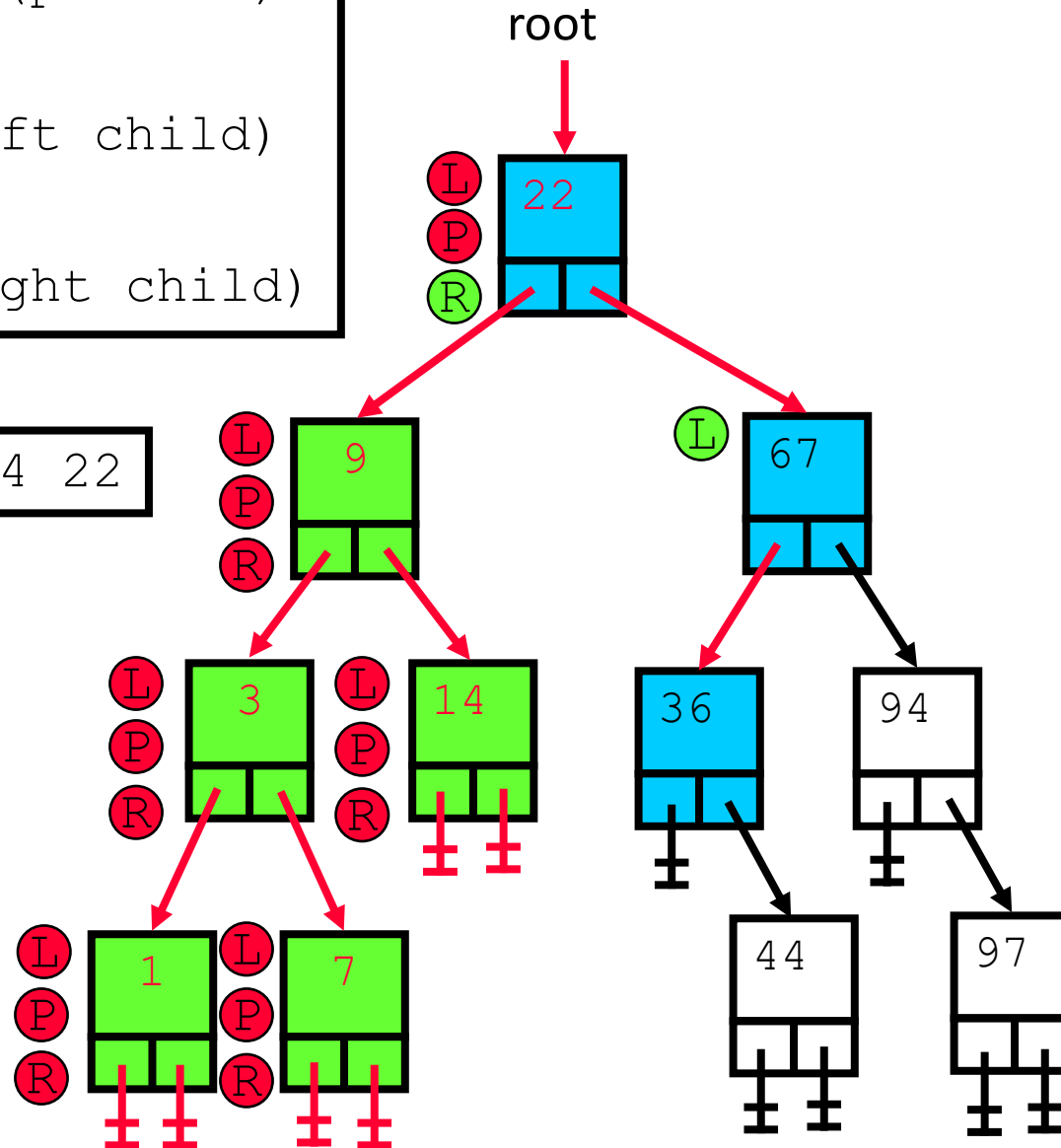



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

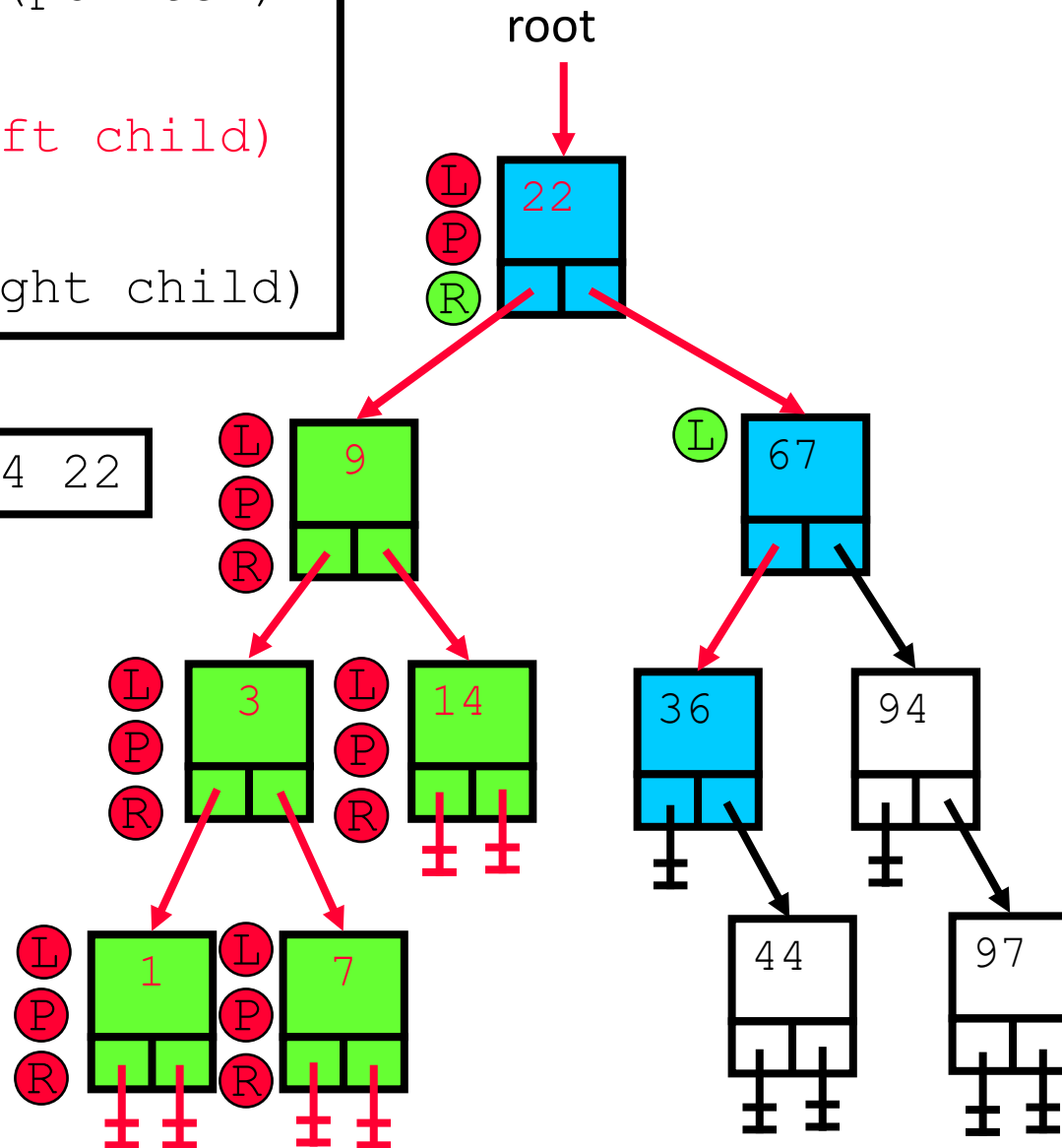


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

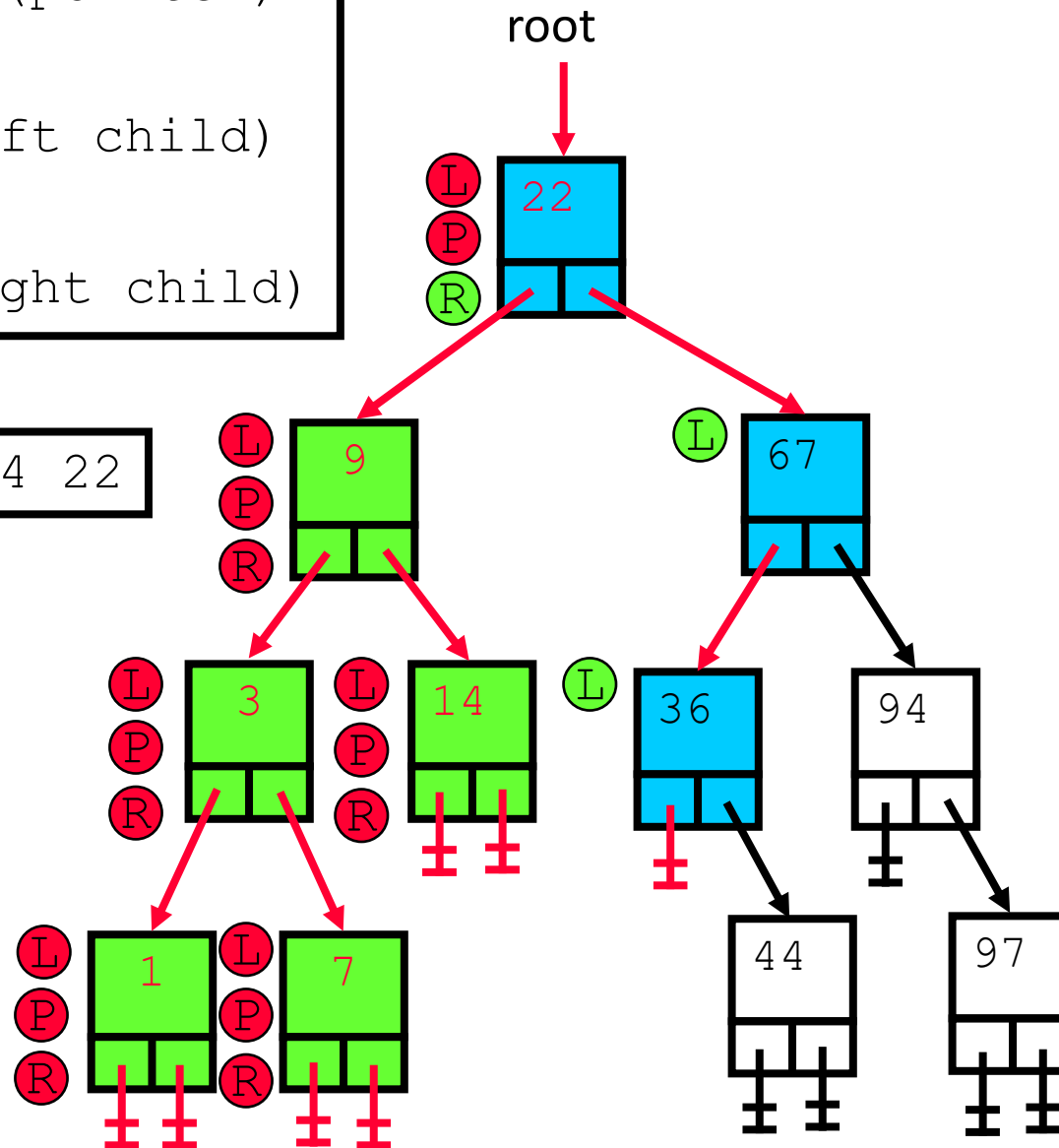


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

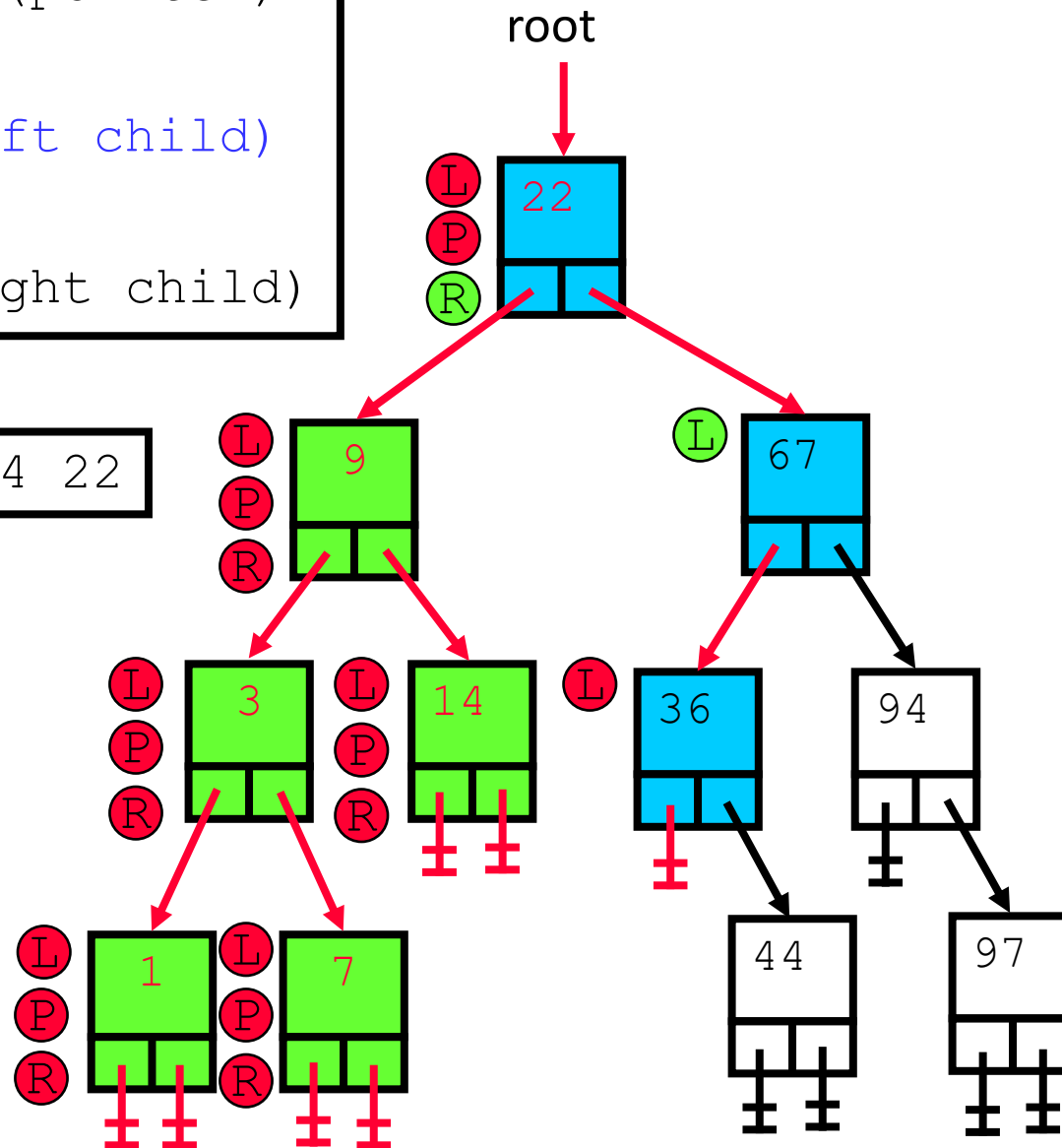


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22

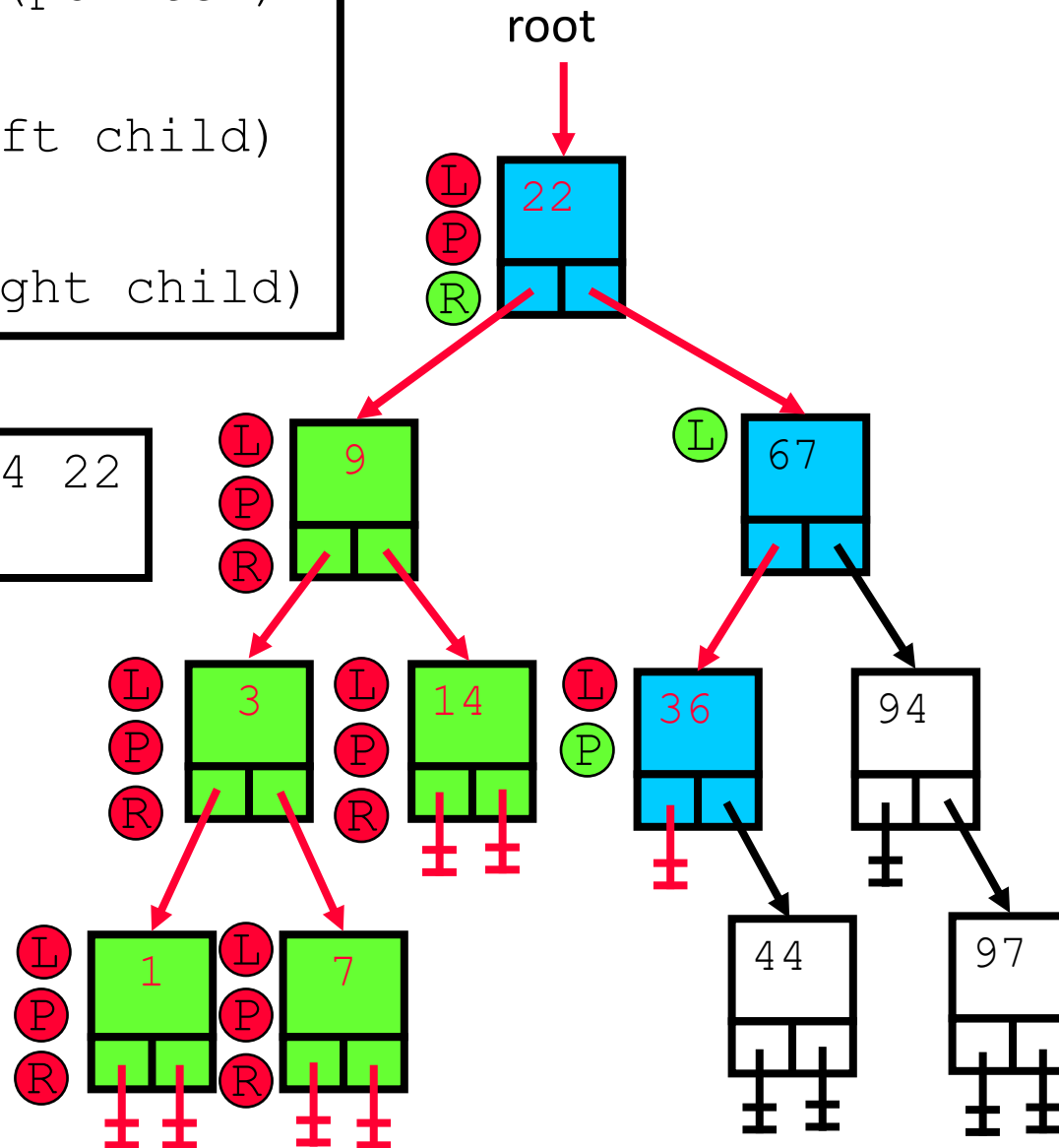


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36

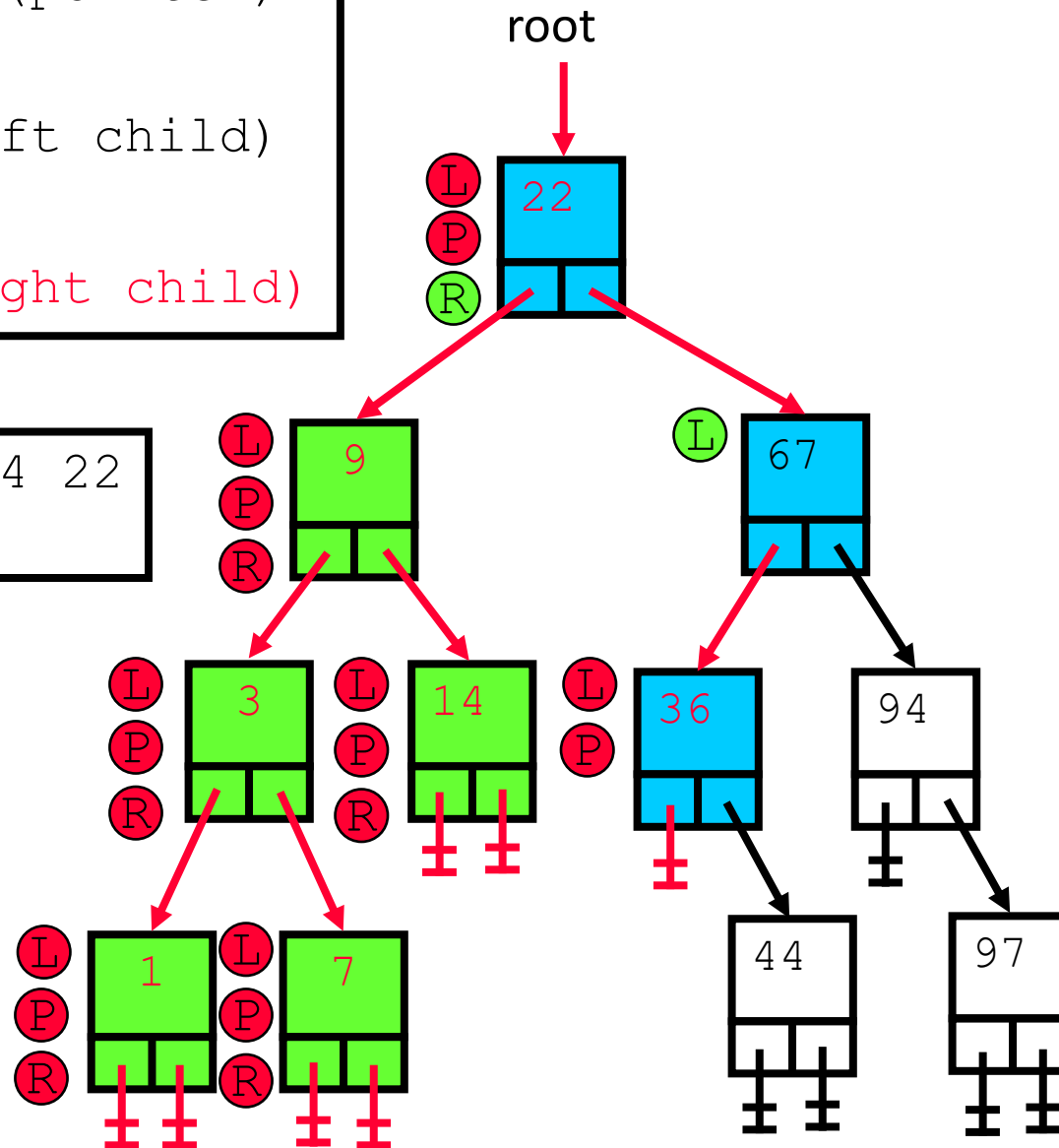


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36

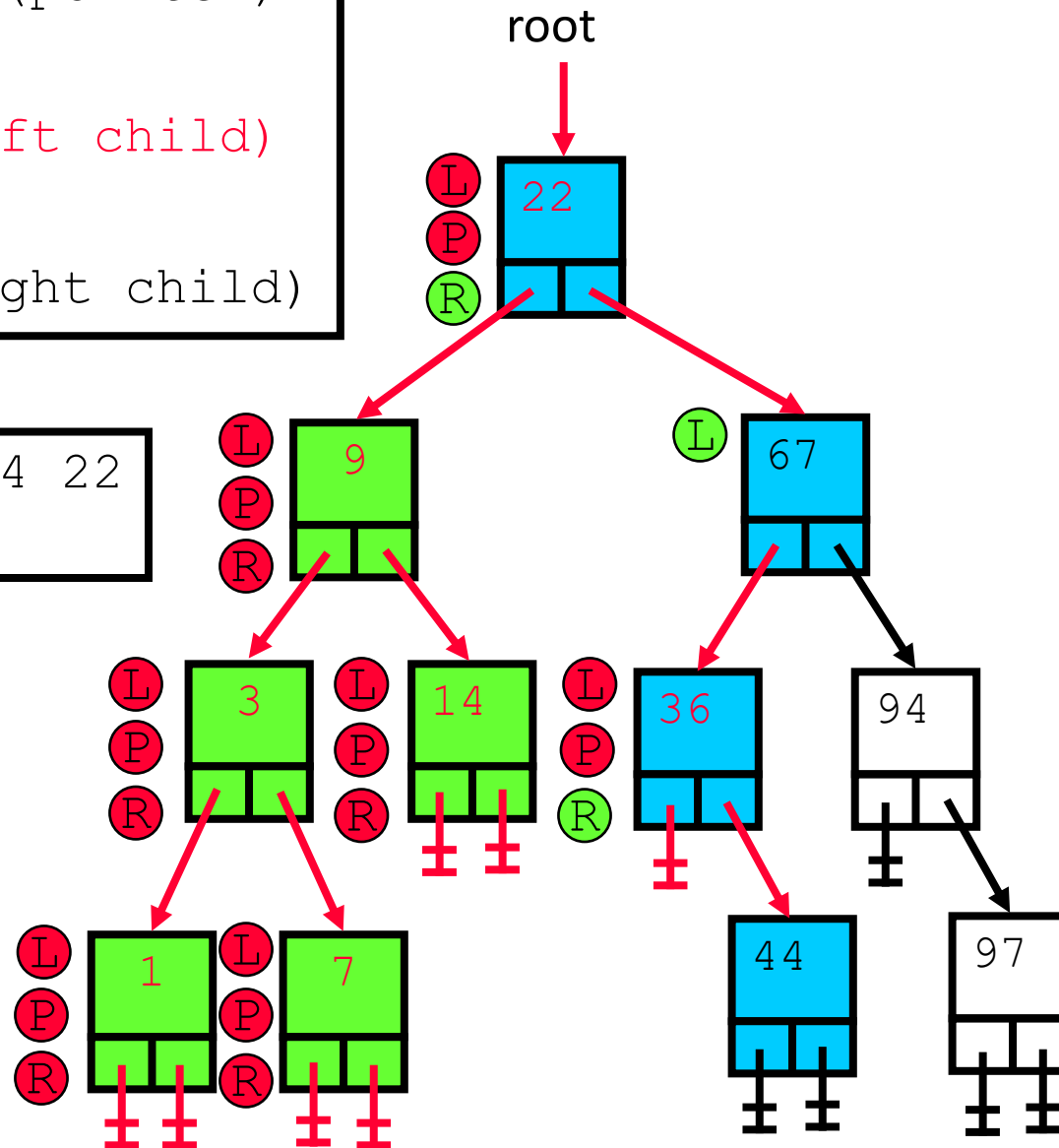



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36

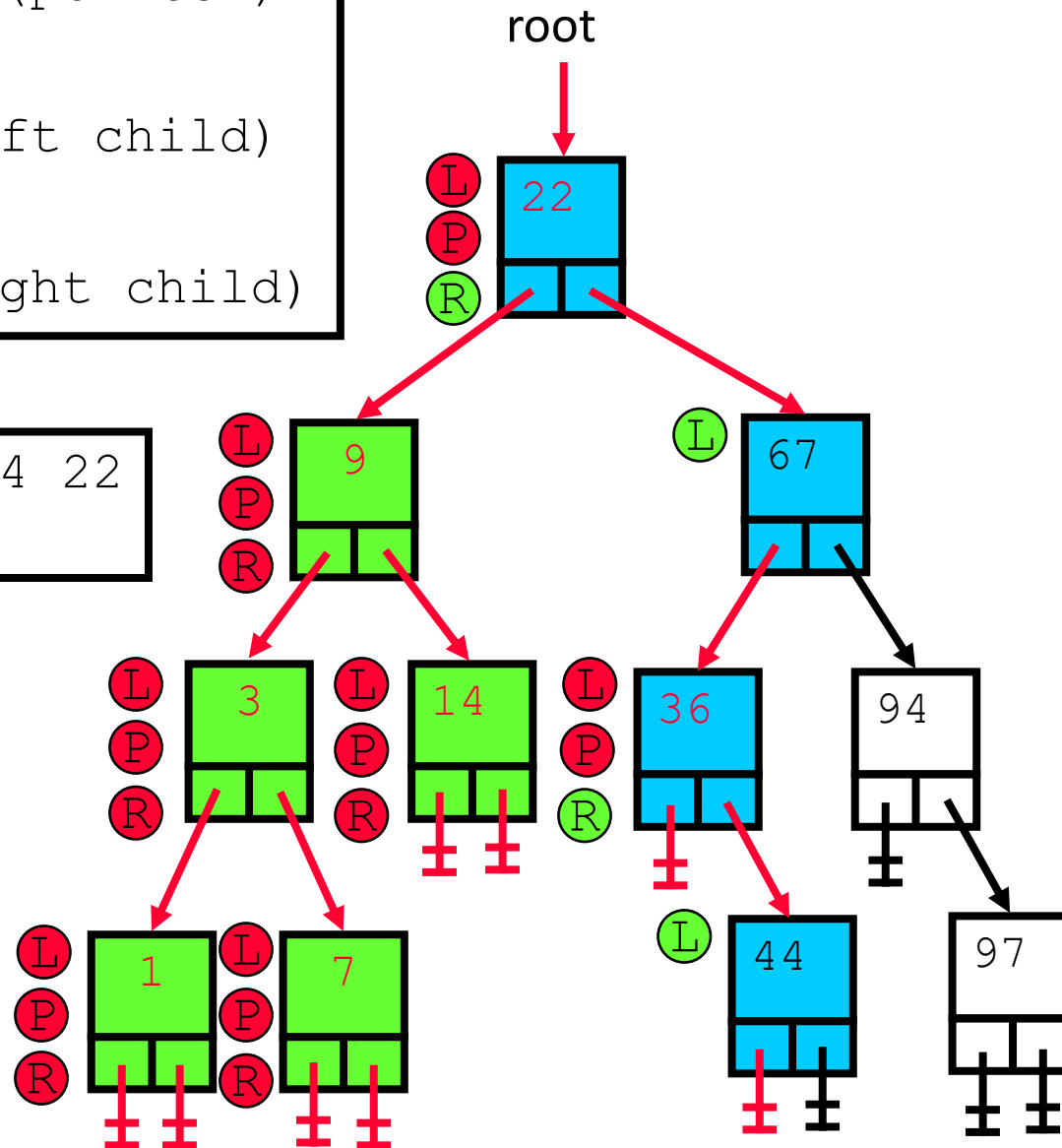



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36

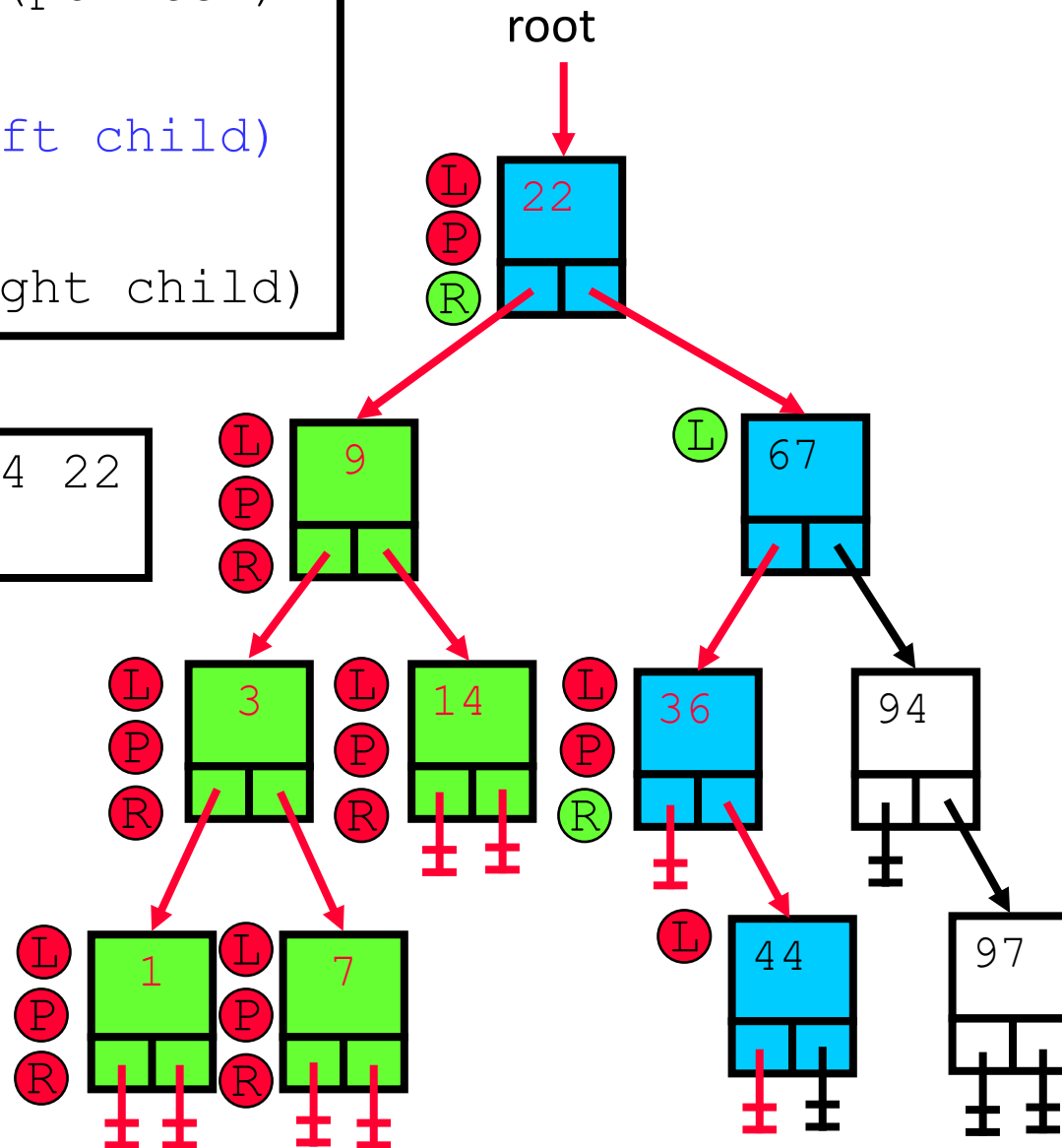


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36

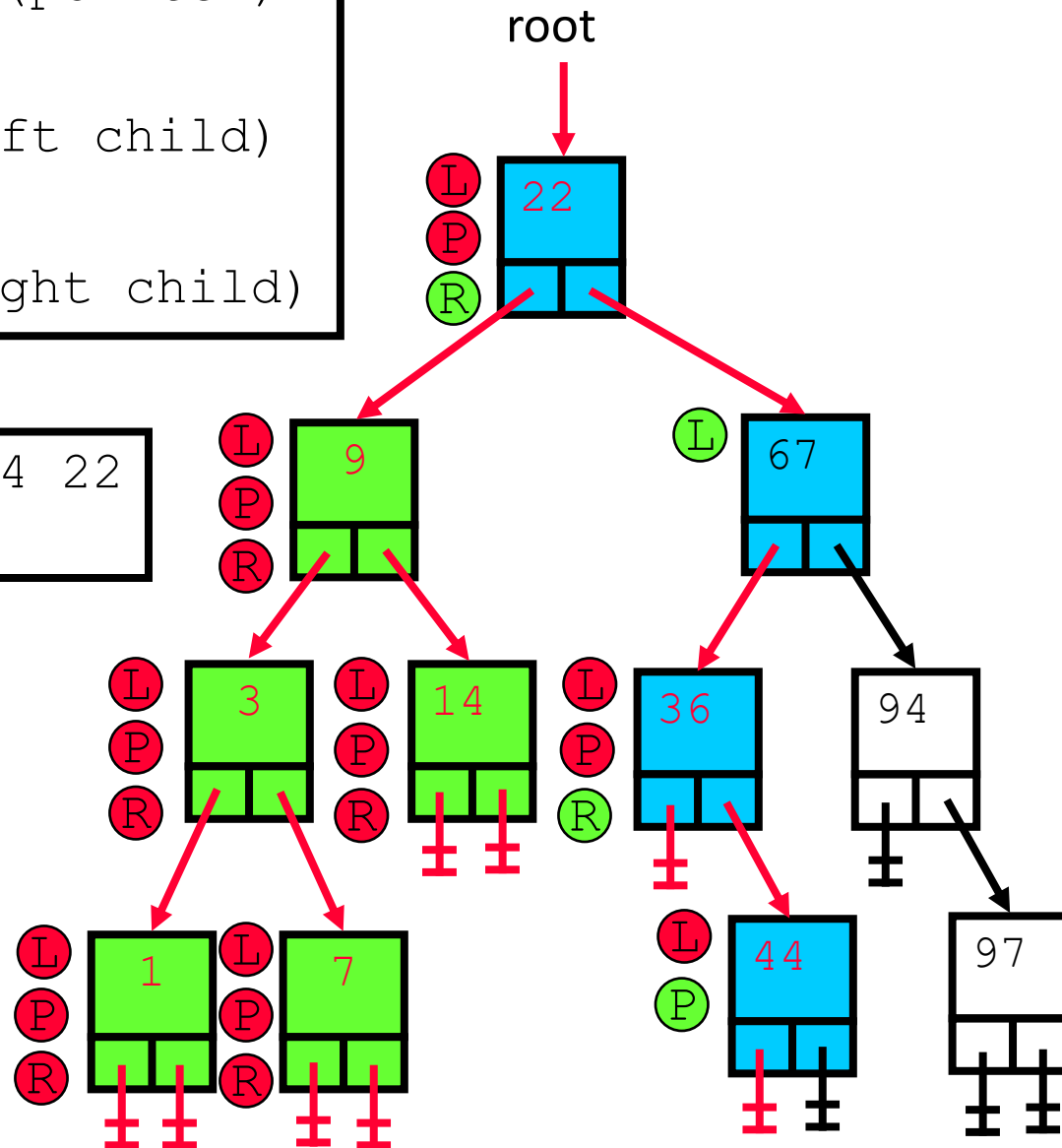


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

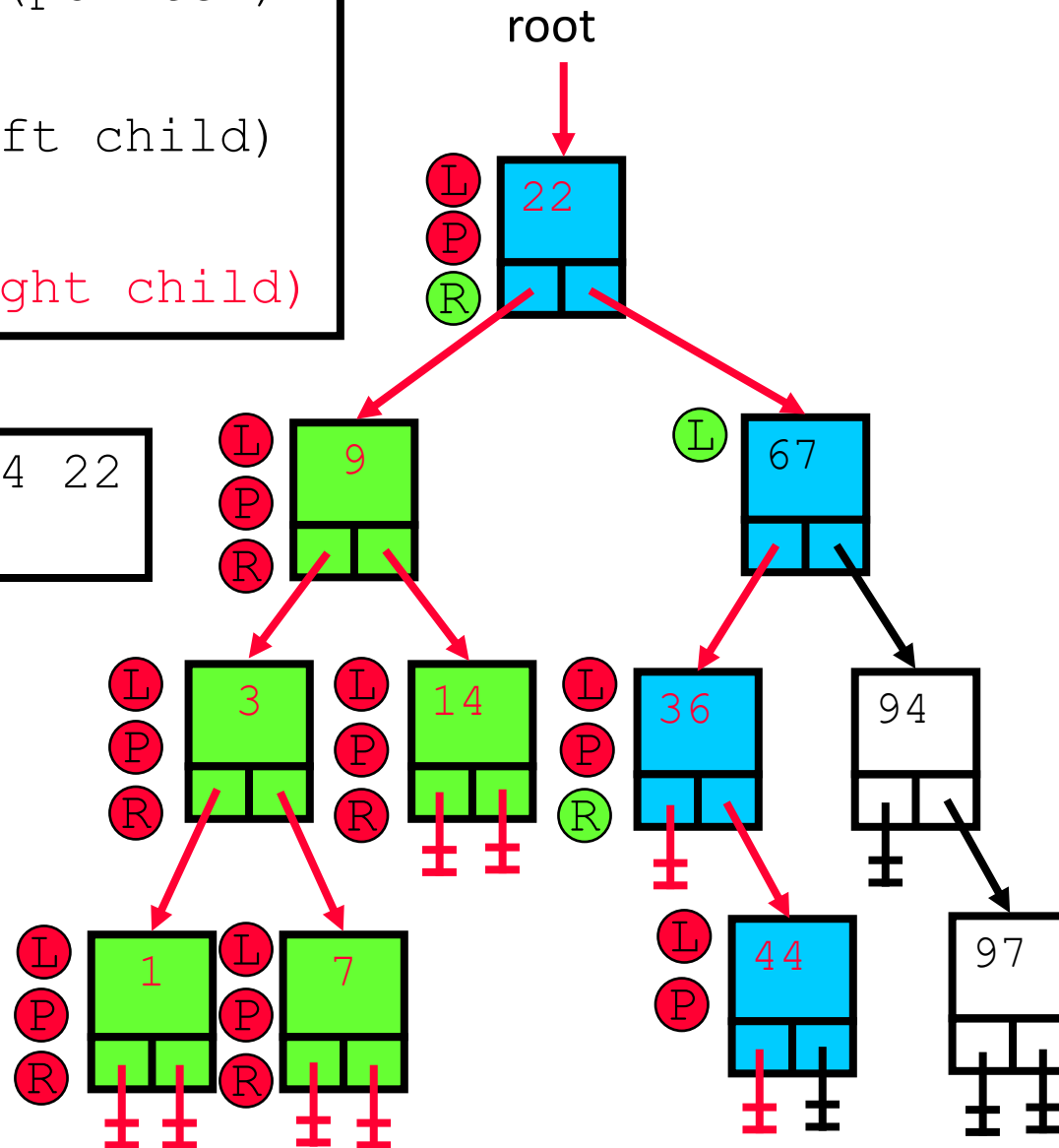


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

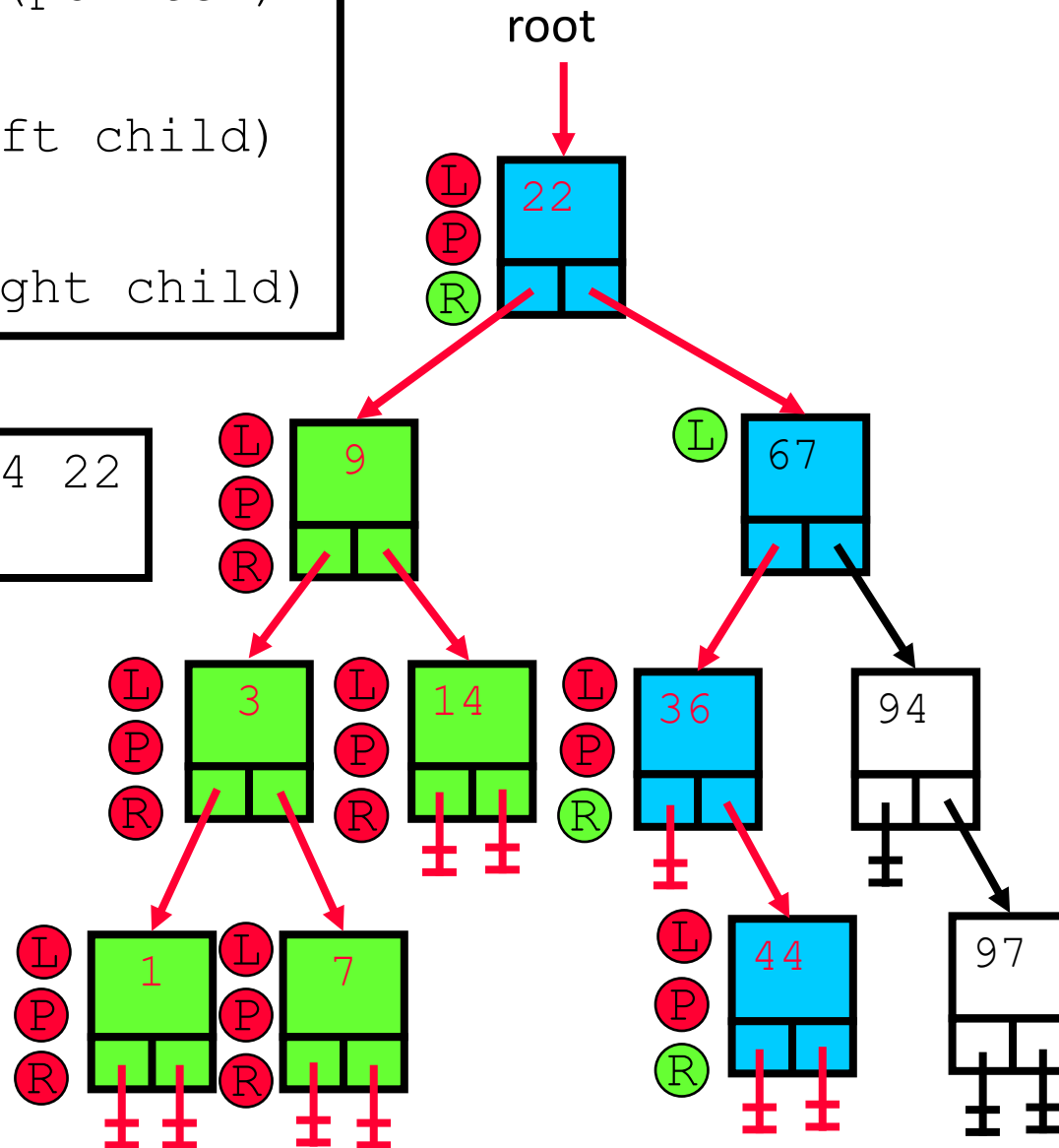


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

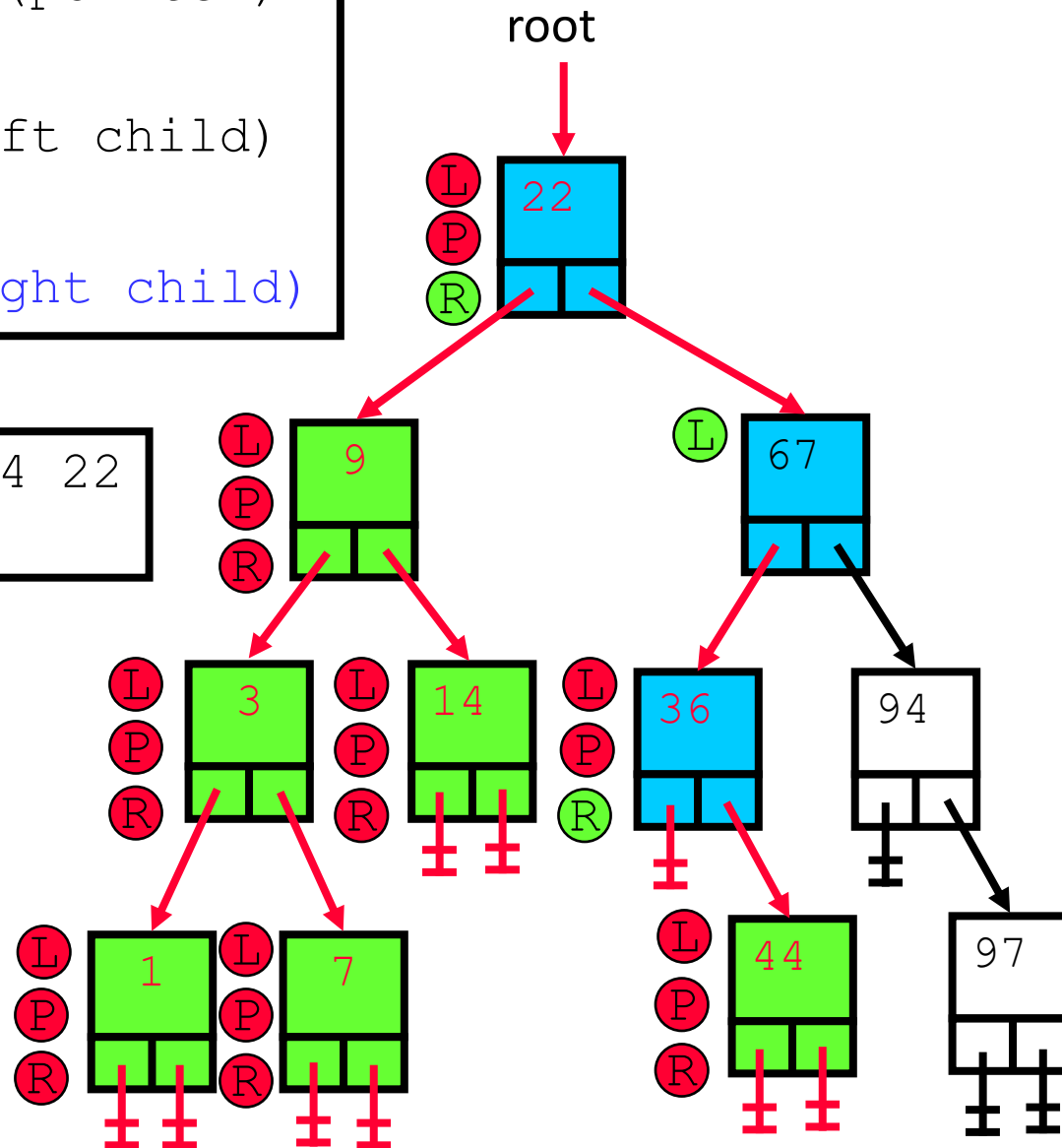


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

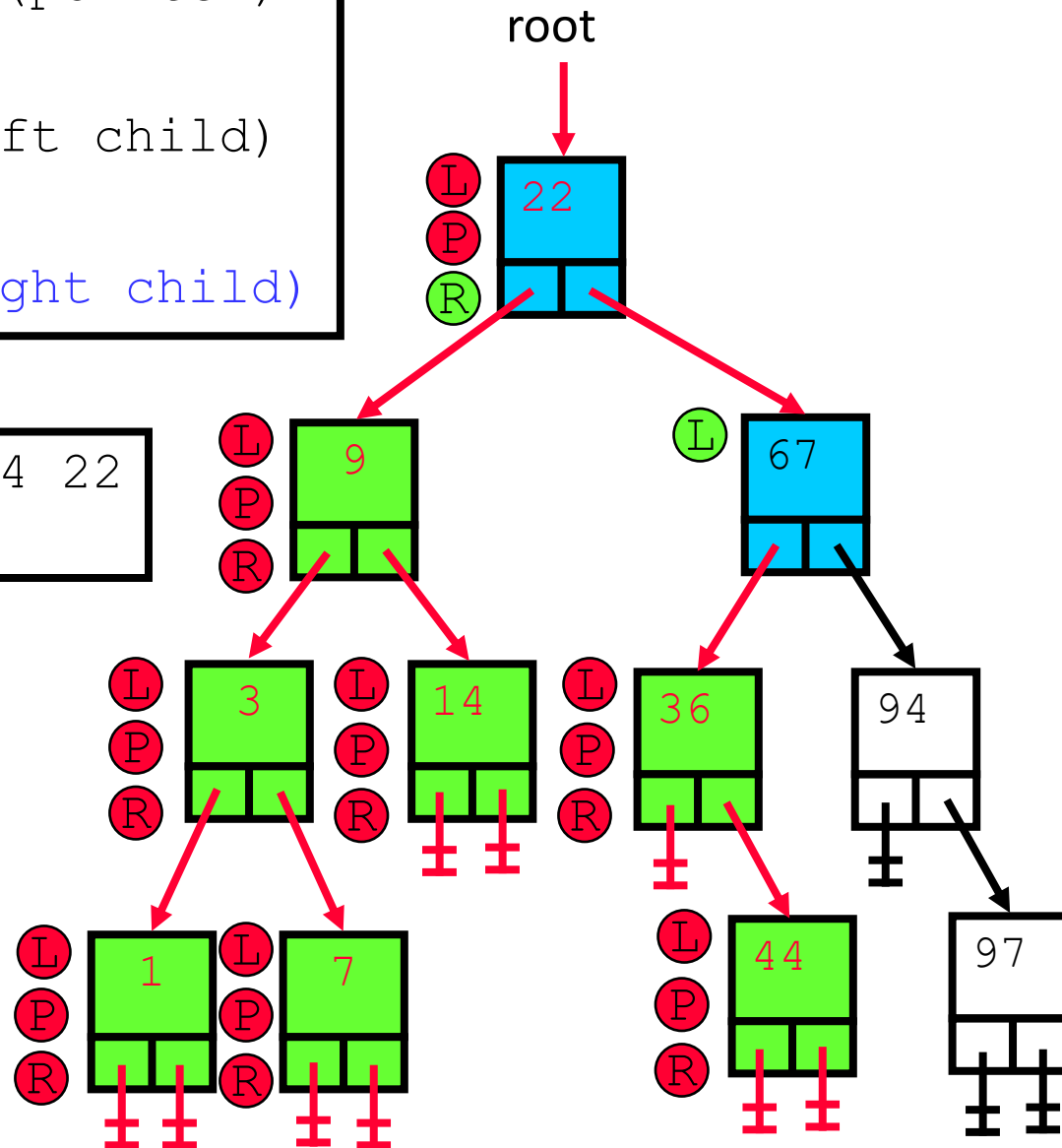


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

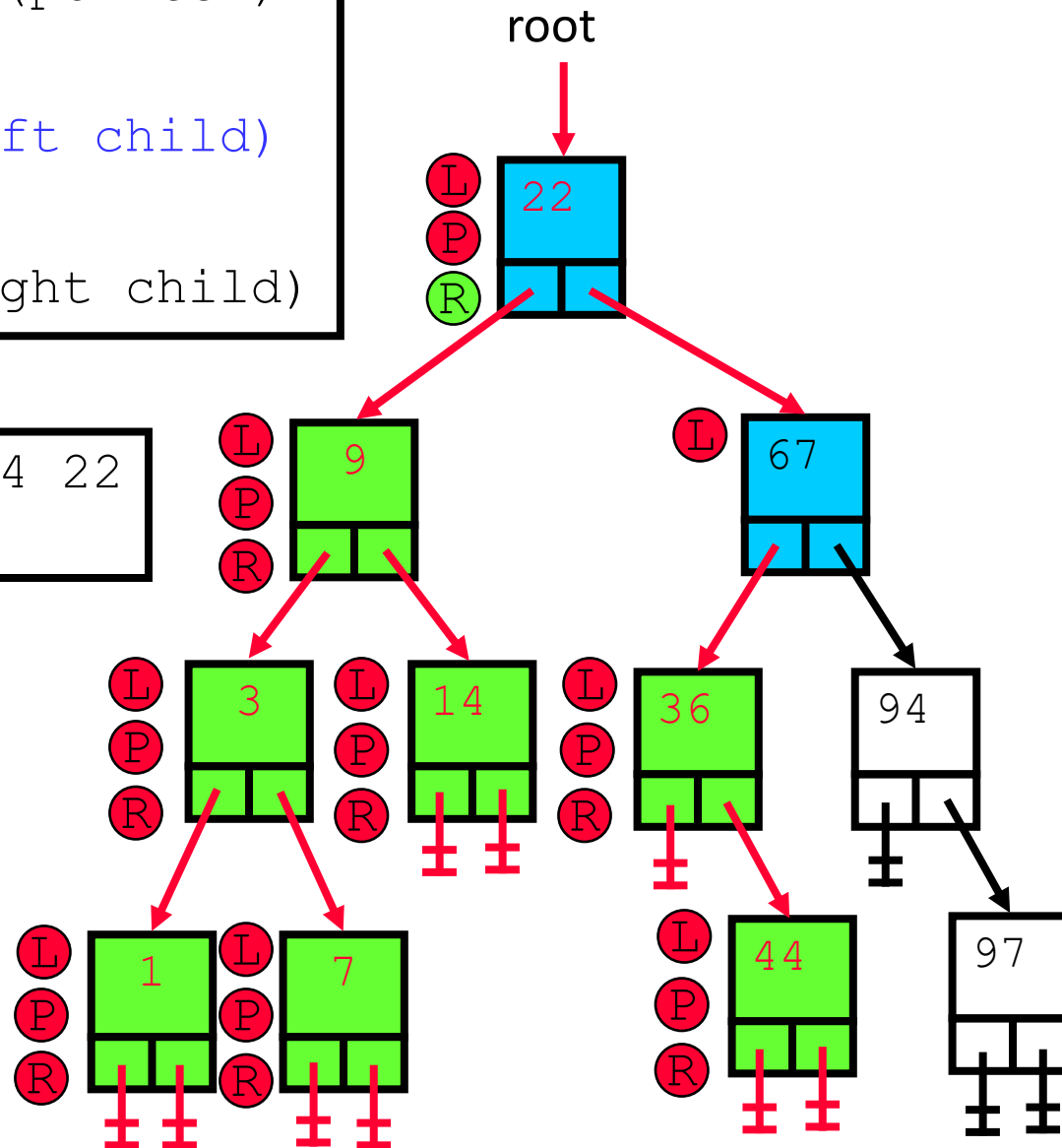


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44

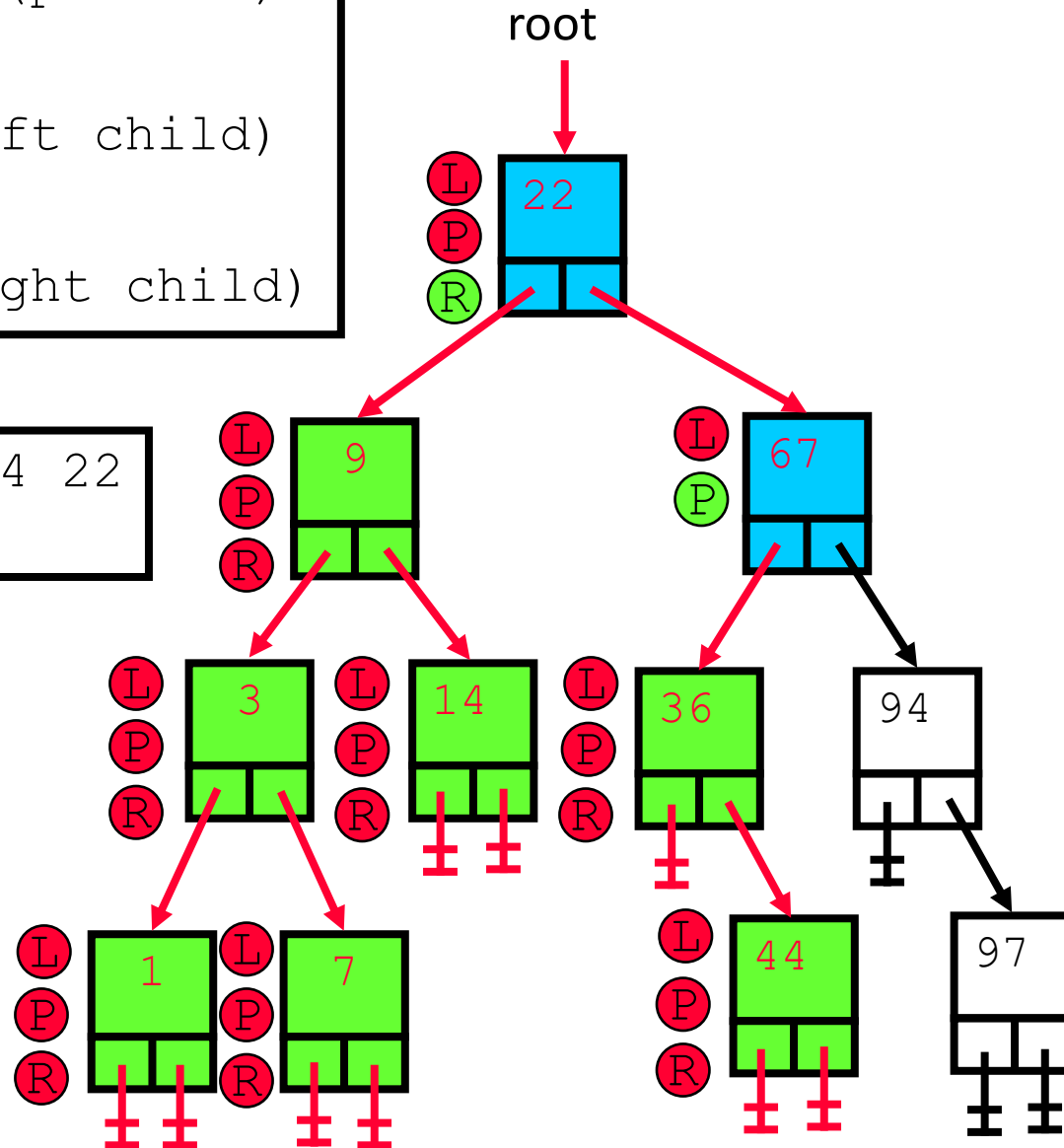



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

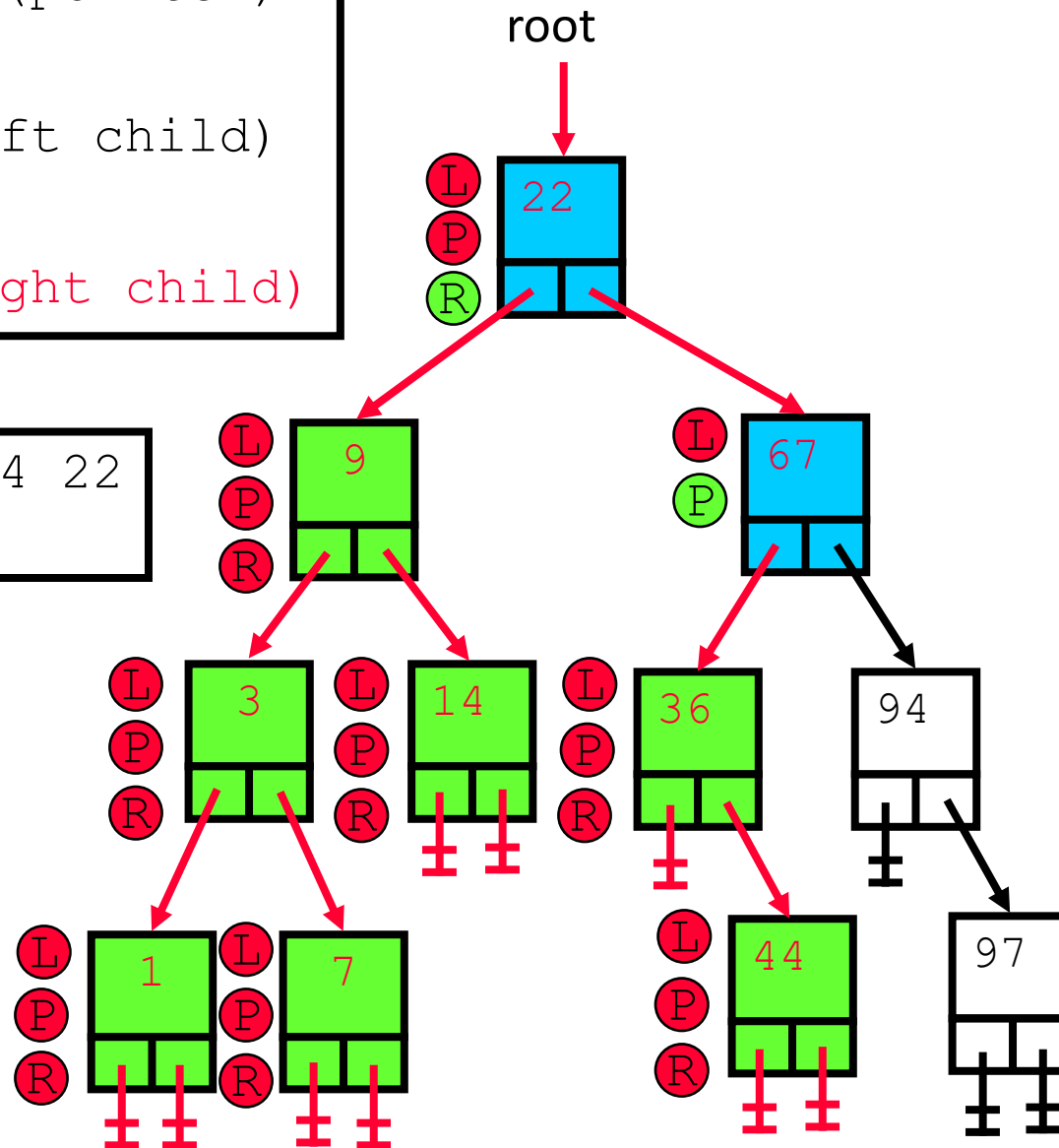


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

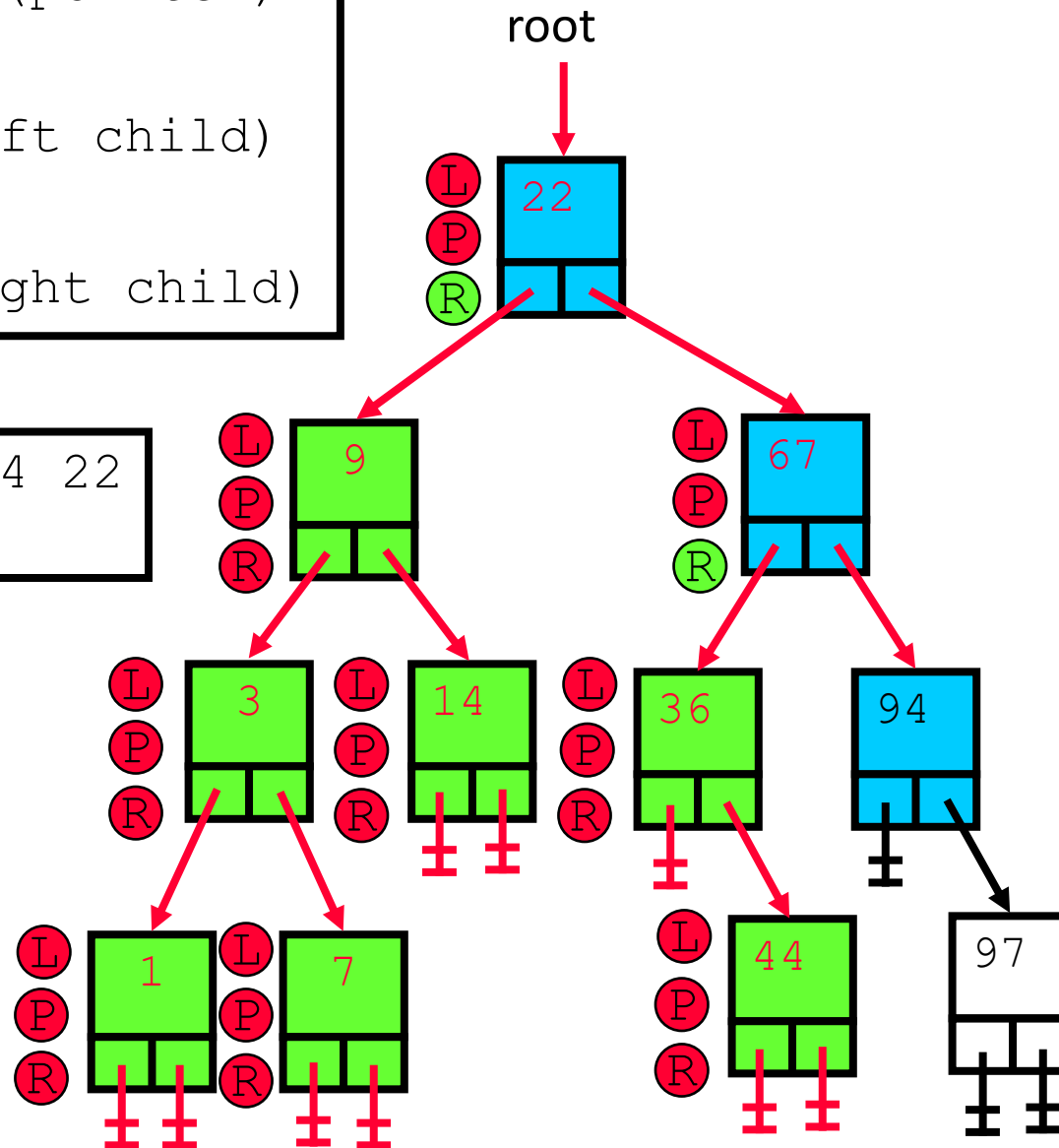


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

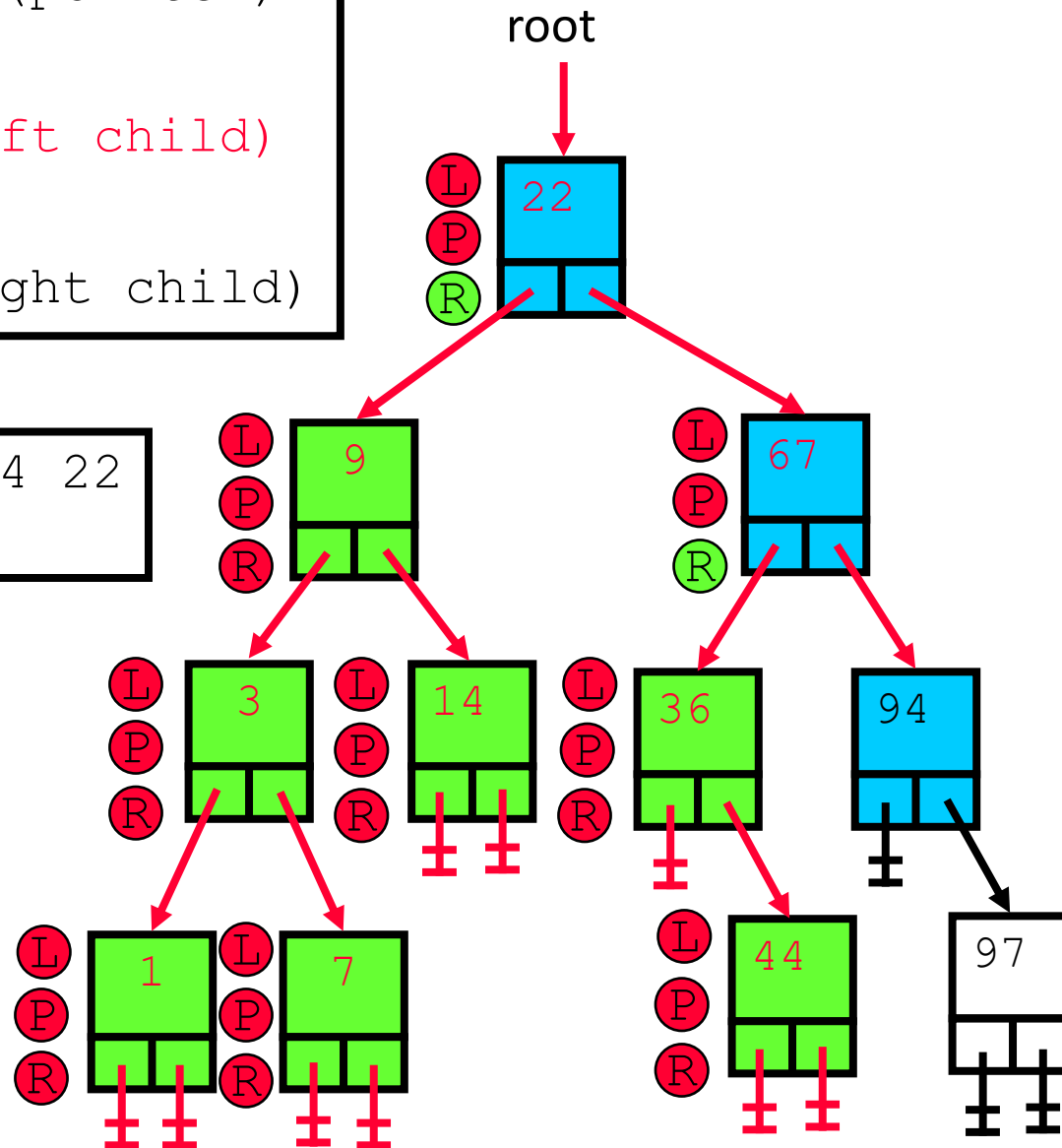


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

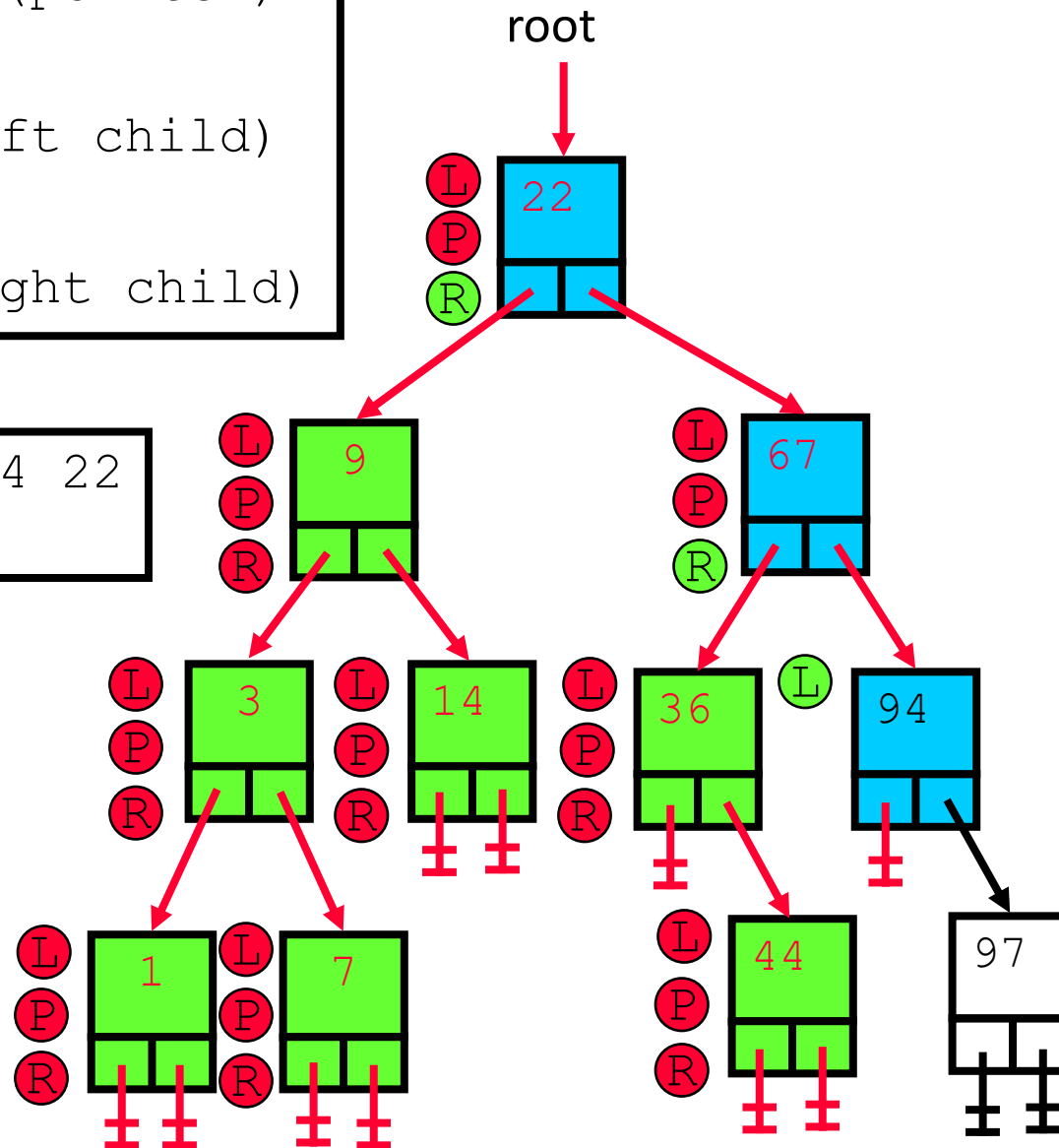


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

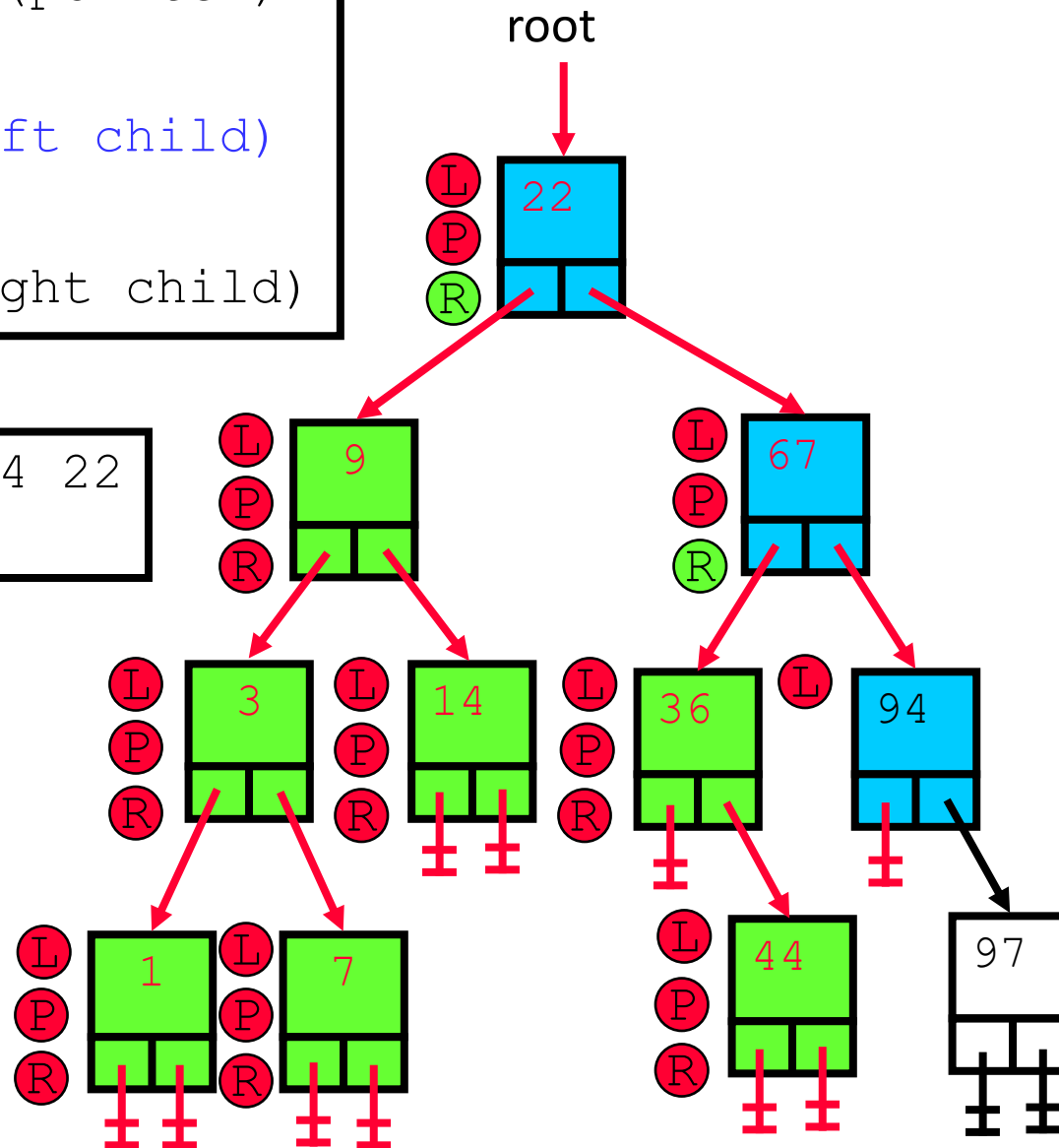


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  L InOrderPrint(left child)
  P print(data)
  R InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67

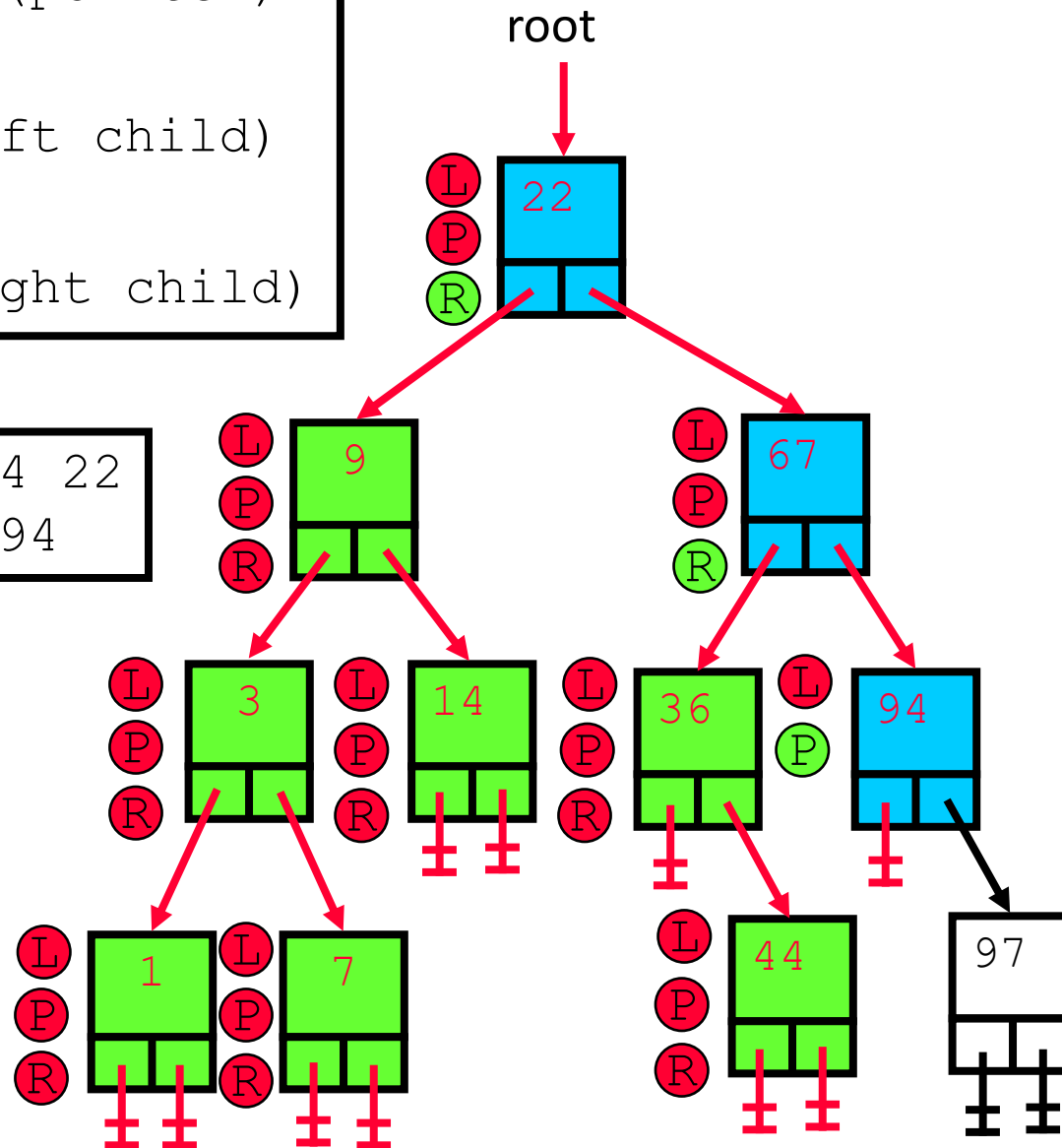


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

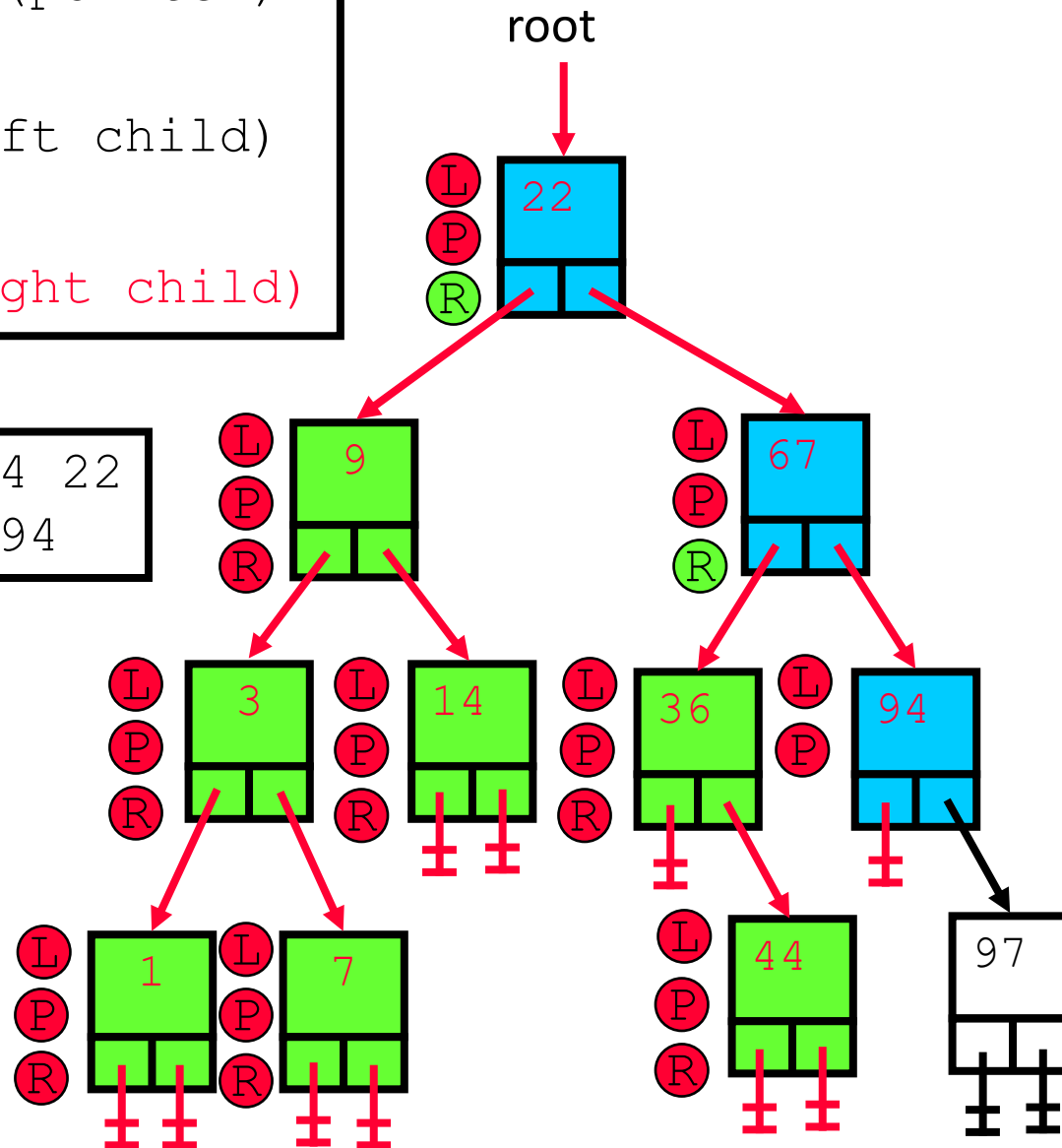


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

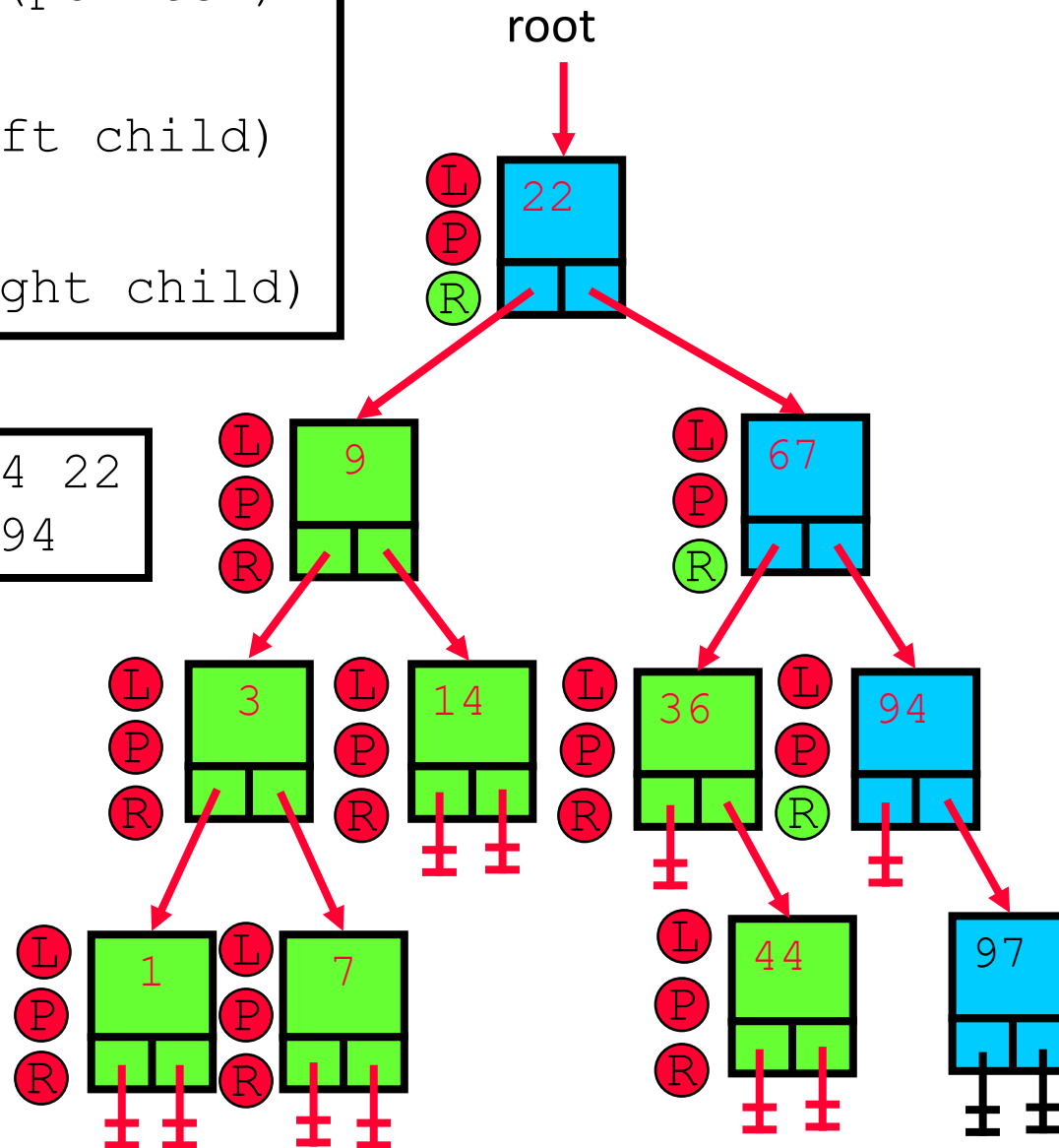



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

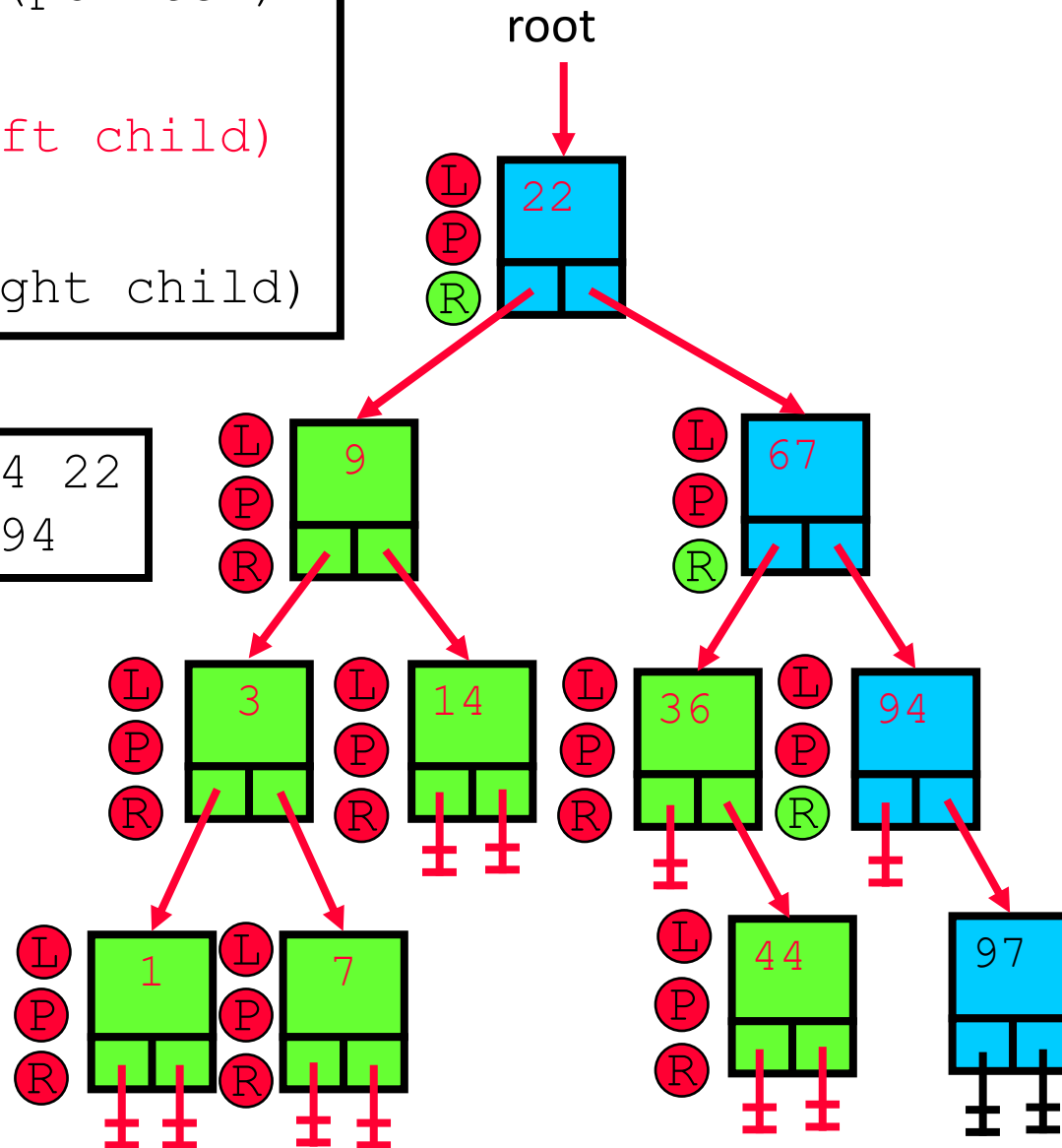


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

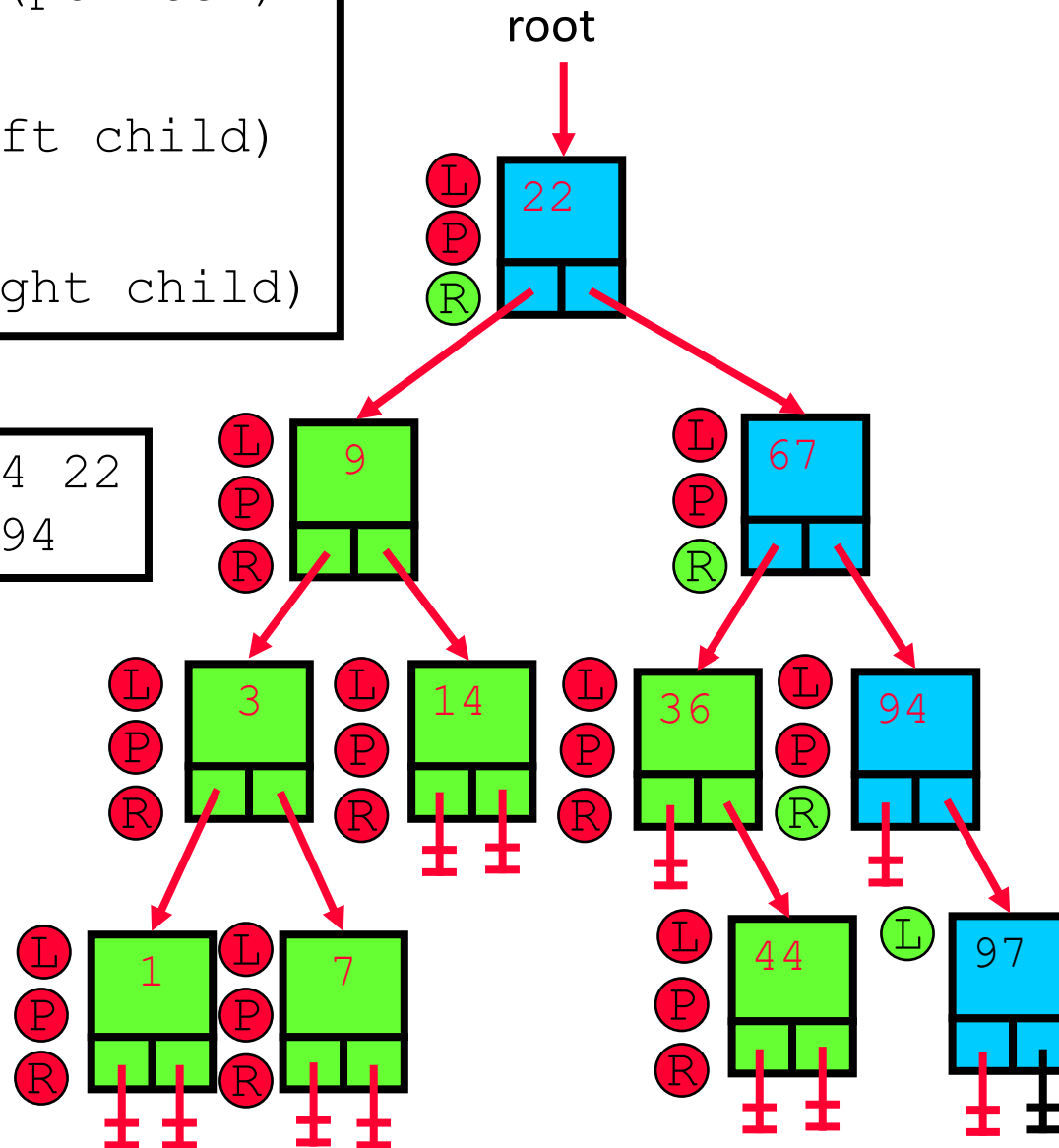


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

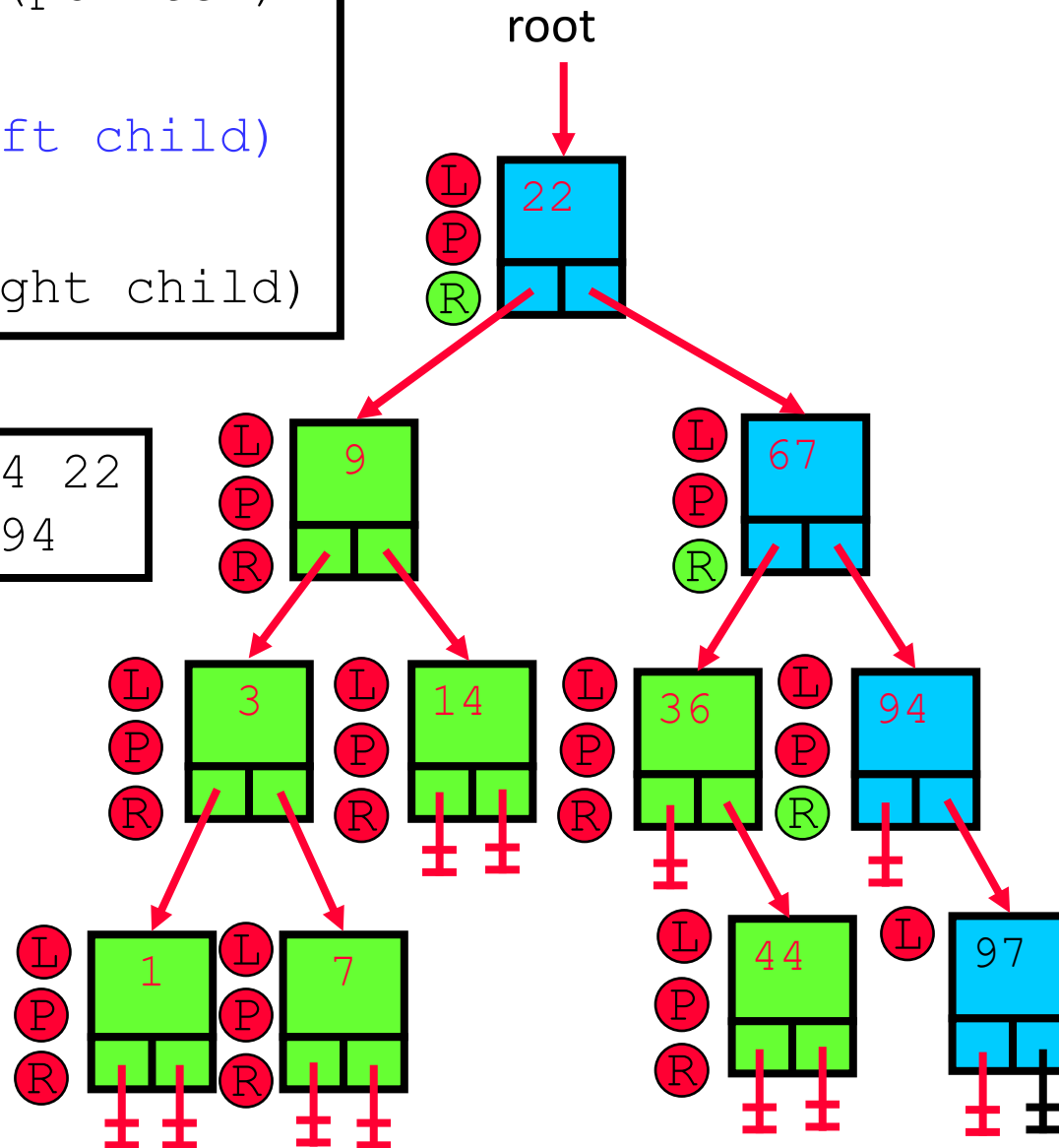


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94

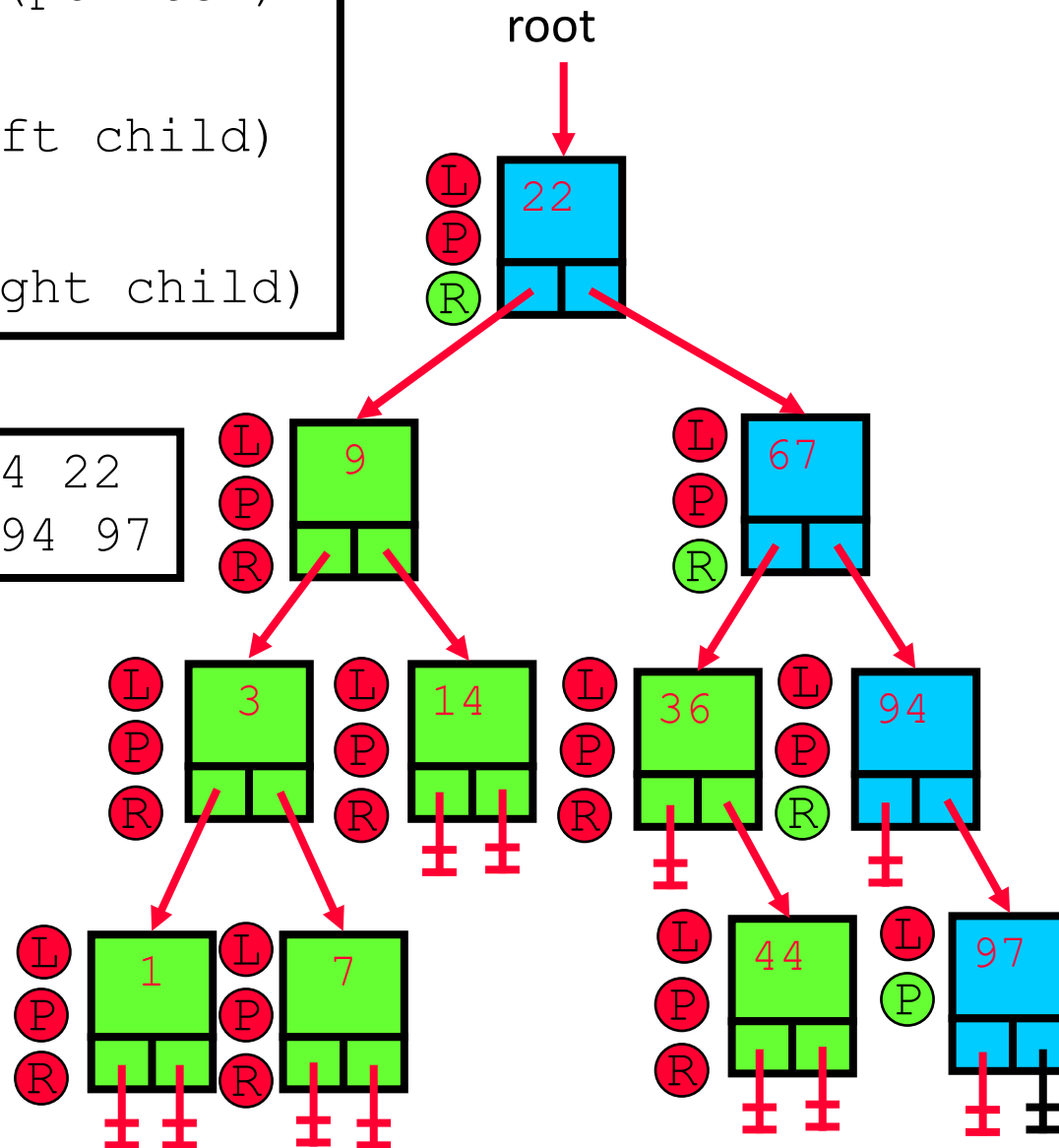


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

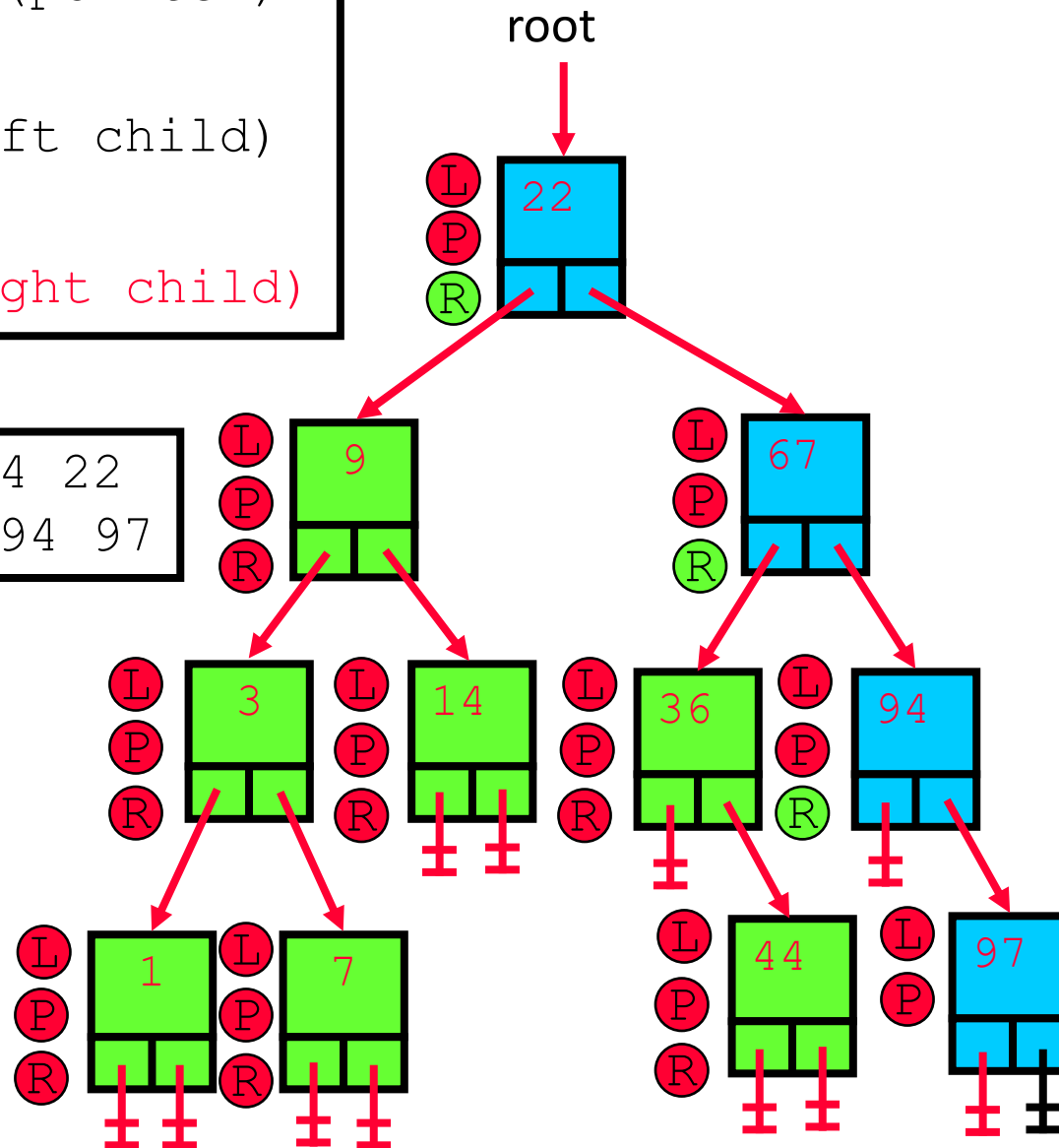


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

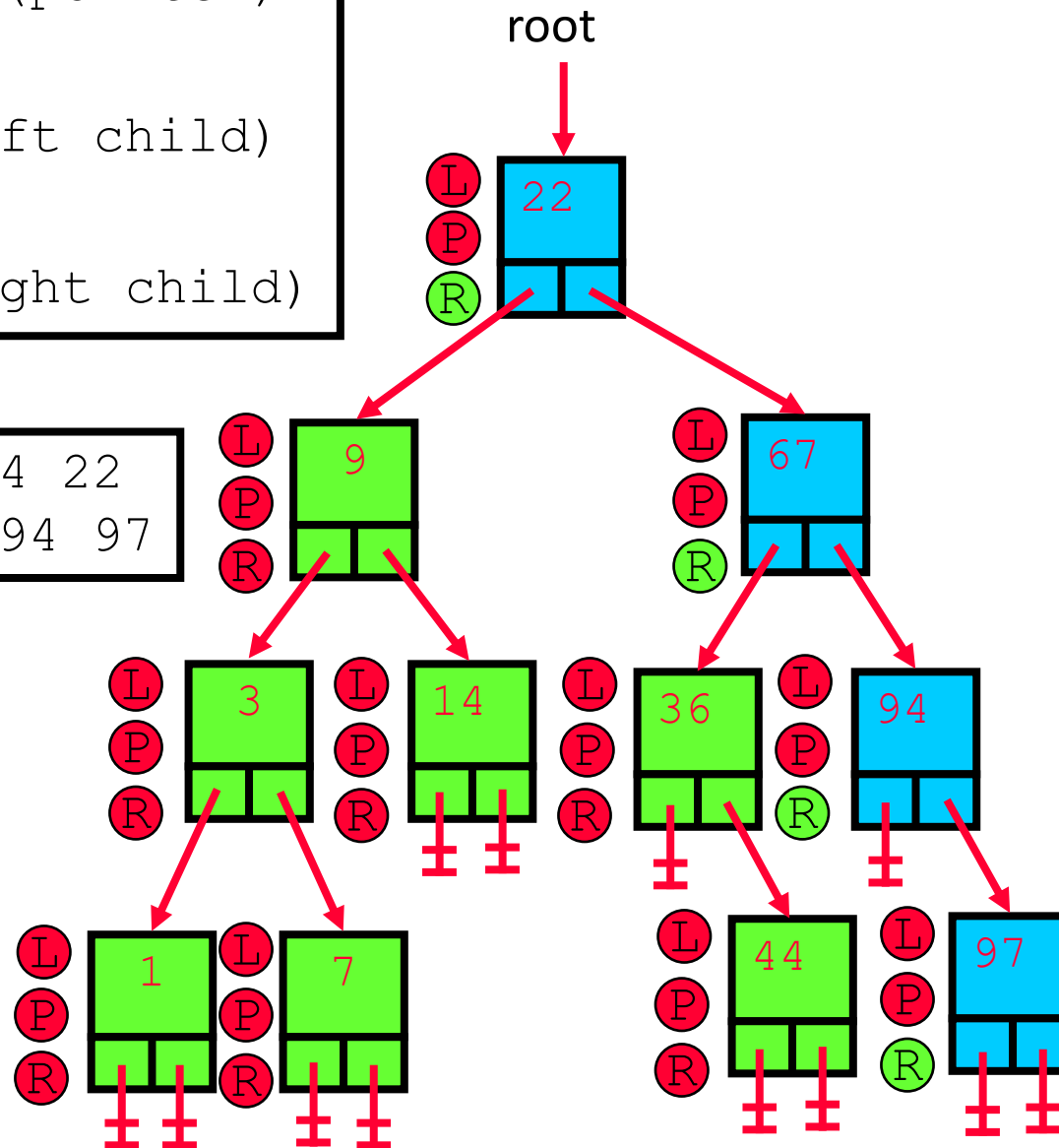


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

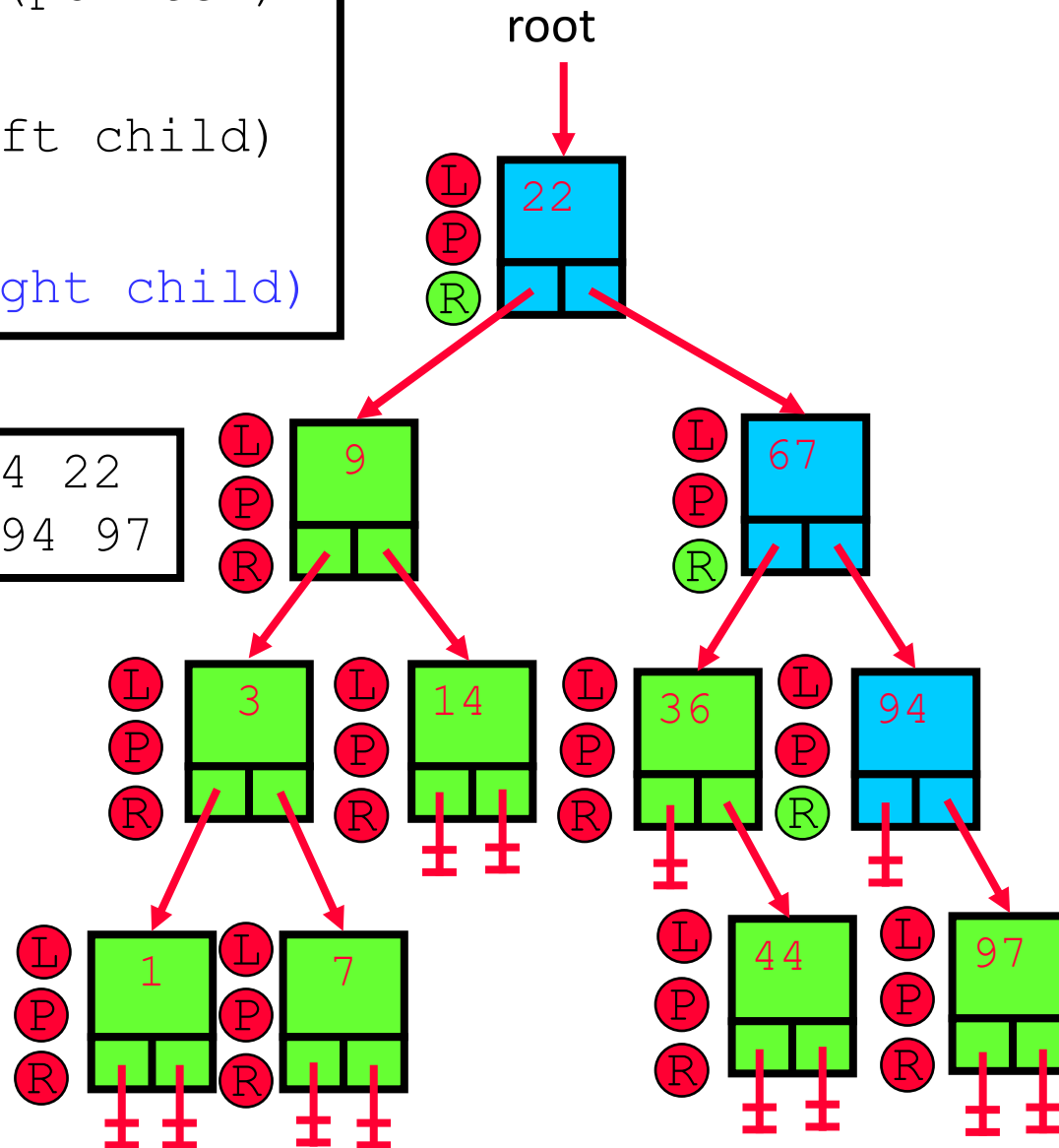


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

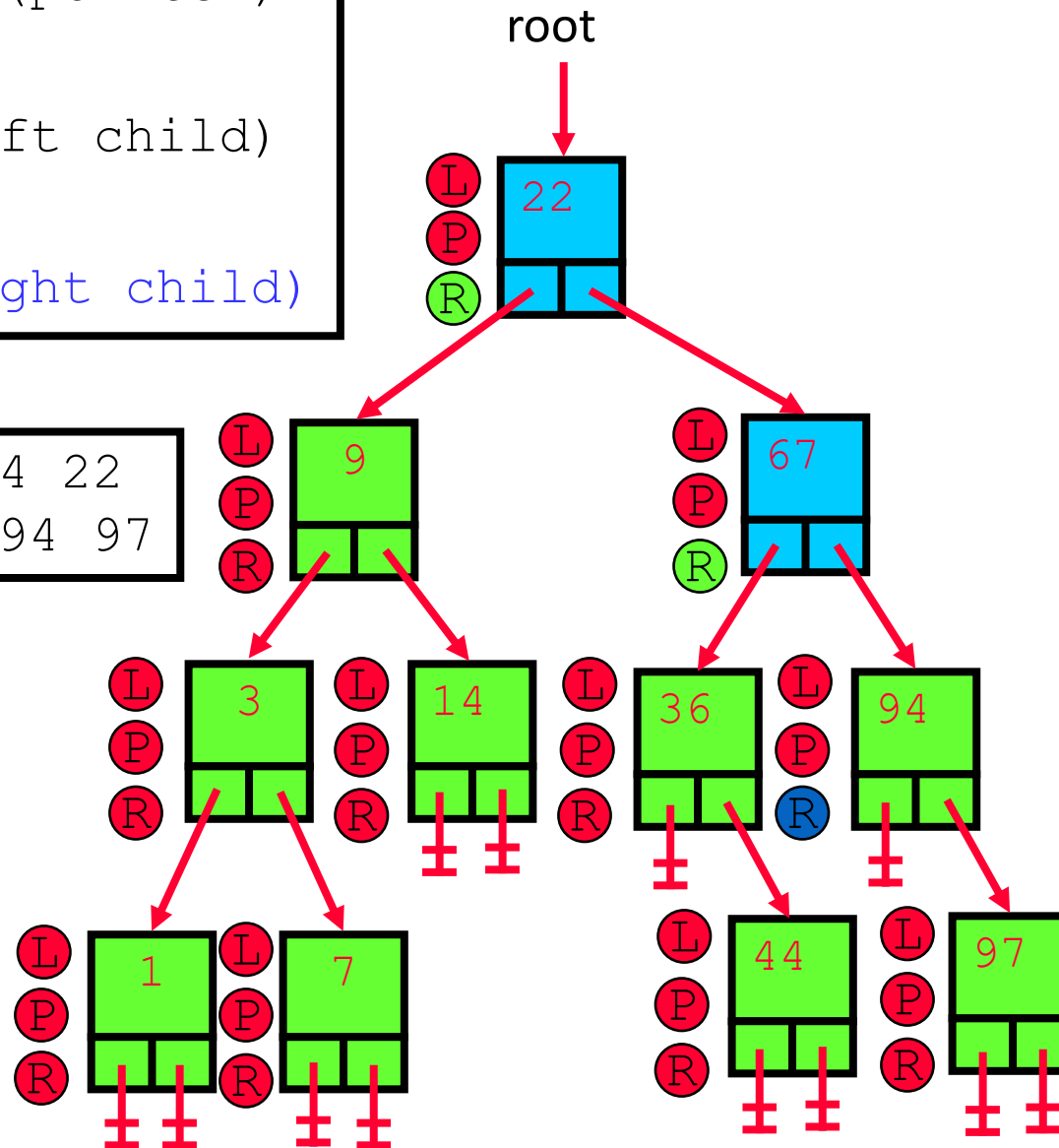



```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

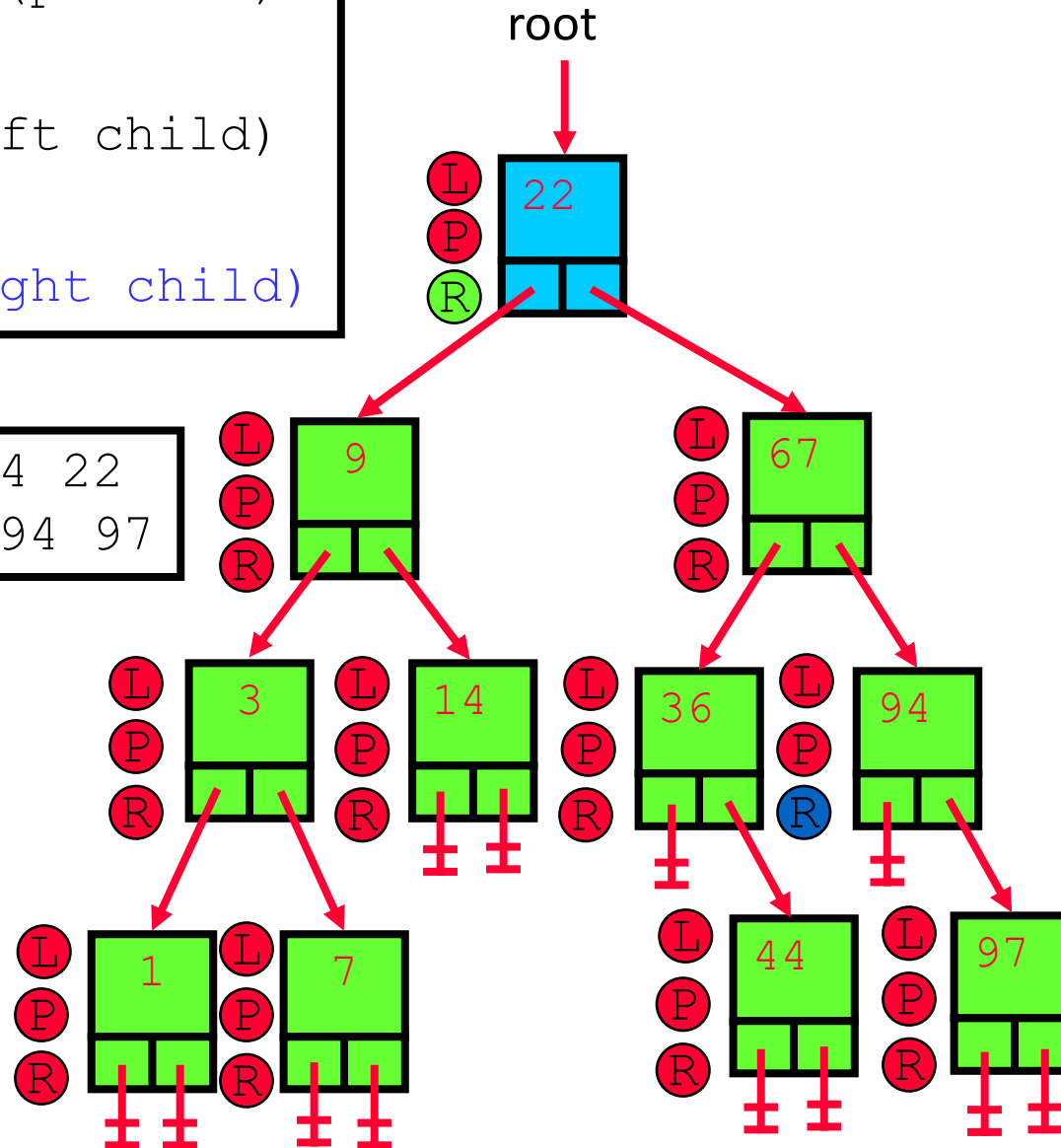


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97

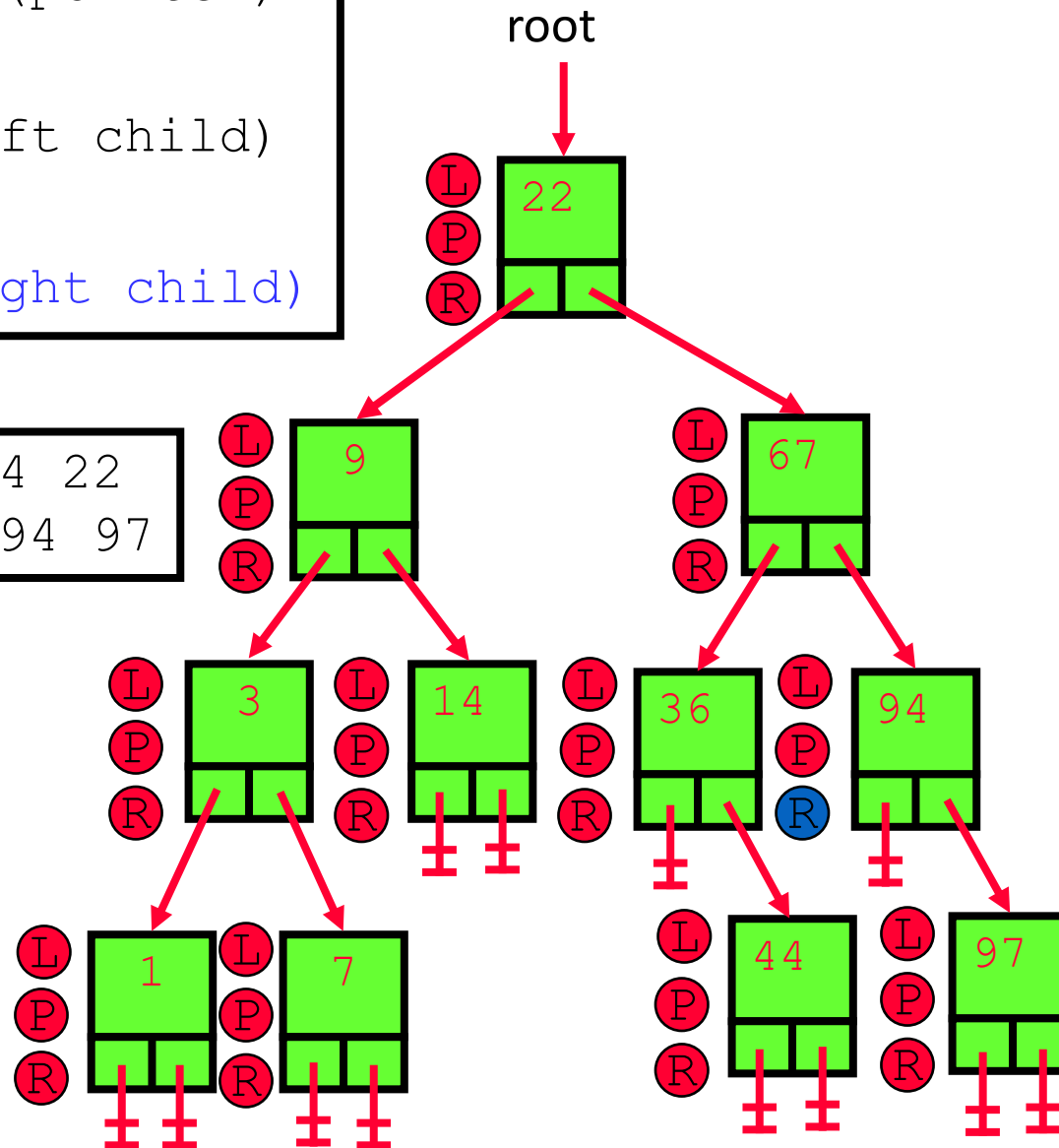


```

Proc InOrderPrint(pointer)
  pointer NOT NIL?
  (L) InOrderPrint(left child)
  (P) print(data)
  (R) InOrderPrint(right child)

```

Output: 1 3 7 9 14 22
36 44 67 94 97



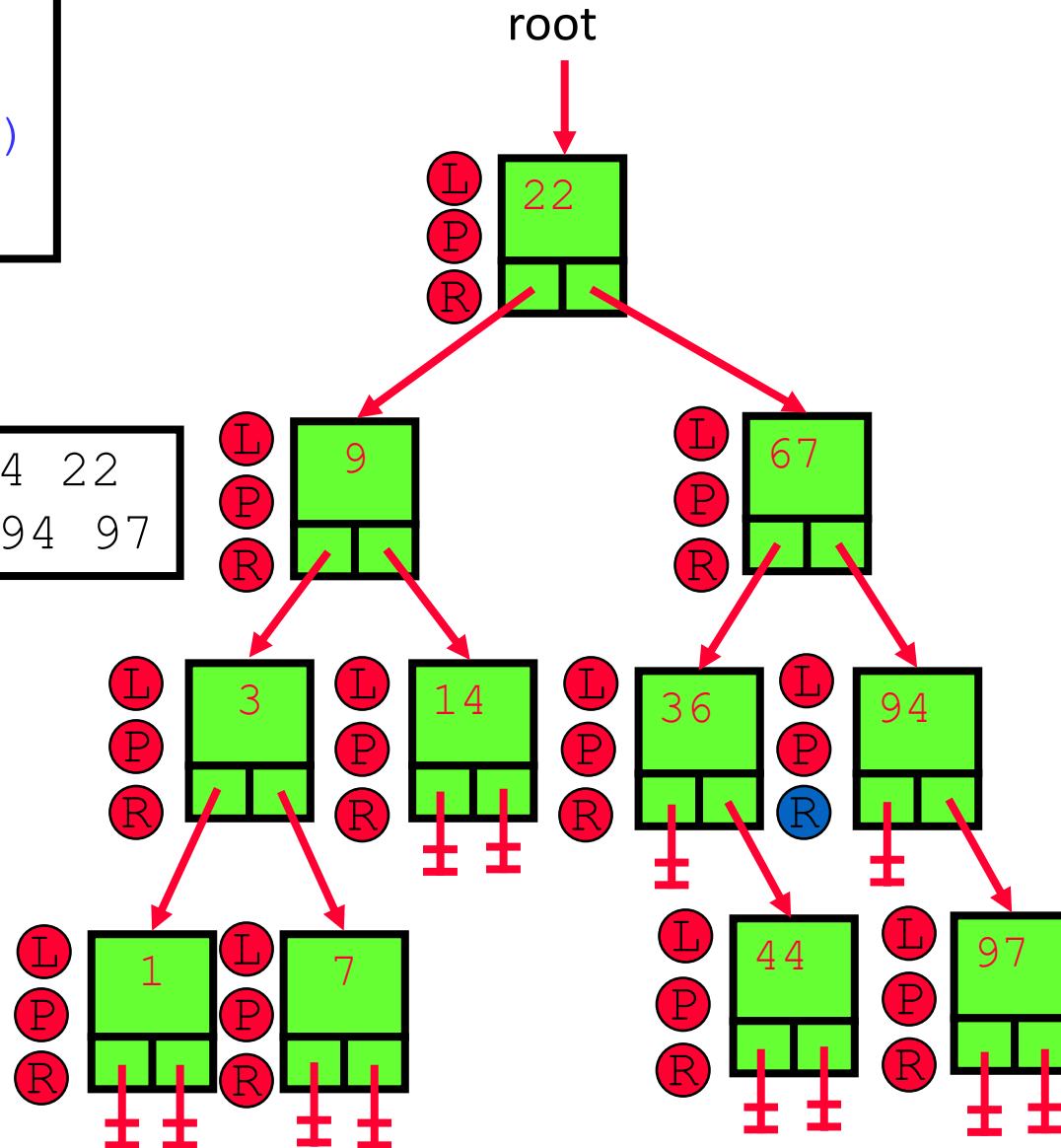
Algorithm Example

. . .

`InOrderPrint(root)`

. . .

Output: 1 3 7 9 14 22
36 44 67 94 97



Summary

- An In-Order traversal visits every node
 - Recurse **left first**
 - Do something with current
 - Recurse **right last**
- The “left, current, right” logic is **repeated recursively** at every node.
- For a BST, an in-order traversal accesses the elements in ascending order.