

Universitatea “Alexandru Ioan Cuza” din Iași
Facultatea de Informatică



LUCRARE DE DISERTAȚIE

A Model for Heart Sounds Segmentation and Classification using Neural Networks

propusă de

Student: Oriana-Maria Oniciuc

Coordonator științific: Conf. Dr. Liviu Ciortuz

Sesiunea: iulie
2018

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Avizat,
Îndrumător Lucrare de Disertație,
Conf. Dr. Ciortuz Liviu

Data 28.06.2018 Semnătura _____

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Abstract

This study aims to produce a method that classifies phonocardiograms corresponding to different heart symptoms that are extremely subtle and challenging to separate. The problem is of particular interest to machine learning researchers as it involves classification of audio sample data, where distinguishing between classes of interest is non-trivial. Data is gathered in real-world situations and frequently contains background noise of every conceivable type.

Some attempts to segment phonocardiograms (PCG) into heartbeats can be found in the literature. The characteristics of the PCG signal and other features such as heart sounds S1 and S2 location can be measured more accurately by digital signal processing techniques. We normalized the data using the L^2 norm and used a sliding window technique for which we used a peak detection algorithm. The models we used in classification are CNN and Adaboost.

For the classification task some of the representative work that was done, has been presented in Classifying Heart Sounds Workshop. The teams used the J48 and MLP algorithms (using Weka) to train and classify the computed features, or exploit domain knowledge and compares the features of heartbeat before and after dropping out extra peaks and the smallest interval, used partial least squares regression, neural networks and convolution neural networks. The classification task in this project aims to give an alternative architecture for the model using Convolution Neural Network.

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I. Introduction

According to the World Health Organization, ischaemic heart disease and stroke are the world's biggest killers, accounting for 15.2 million deaths in 2016. These diseases have remained the leading causes of death globally in the last 15 years. [1] Any work done in detecting signs of heart disease could therefore have a significant impact on world health.

Classifying Heart Sounds PASCAL provides us with a dataset that is gathered in real-world situations. Many recordings from the dataset contain background noise, being recorded both in a hospital environment by a doctor (using a digital stethoscope) and at home by the patient (using a mobile device). Success in classifying this form of data requires multiples preprocessing of the audio recordings. [2] This dissertation presents an overview of two approaches to analysis and classification of heart sound signals. The main purpose of this study is developing an automatic methodology for identifying systole and diastole in the phonocardiograms and to classify the heartbeats in three classes.

Big companies are interested in medical health activity which is one of the largest component of the economy. In 2017 Apple started to work with Stanford and American Well to determine if the heart rate sensor in the Apple Watch can be used to detect abnormal heart rhythms and common heart conditions. The study ended in 2018 and proved that the smart watch reaches a 97% accuracy rate, 98% sensitivity and 90% specificity. [3]

I.1. Heart sounds

The cardiac cycle is the performance of the human heart from the beginning of one heartbeat to the next one. In each cardiac cycle, the heart contracts (systole), pushing out the blood and pumping it through the body; this is followed by a relaxation phase (diastole), where the heart fills with blood, as illustrated in the next figure.

The atria contracts at the same time, forcing blood through valves into the ventricles. Closing of the atrioventricular valves produces a monosyllabic “lup” sound (S1). Following a brief delay, the ventricles contract at the same time forcing blood through the valves into the aorta and the artery transporting blood to the lungs. Closing of the semilunar valves produces a monosyllabic “dup” sound (S2).

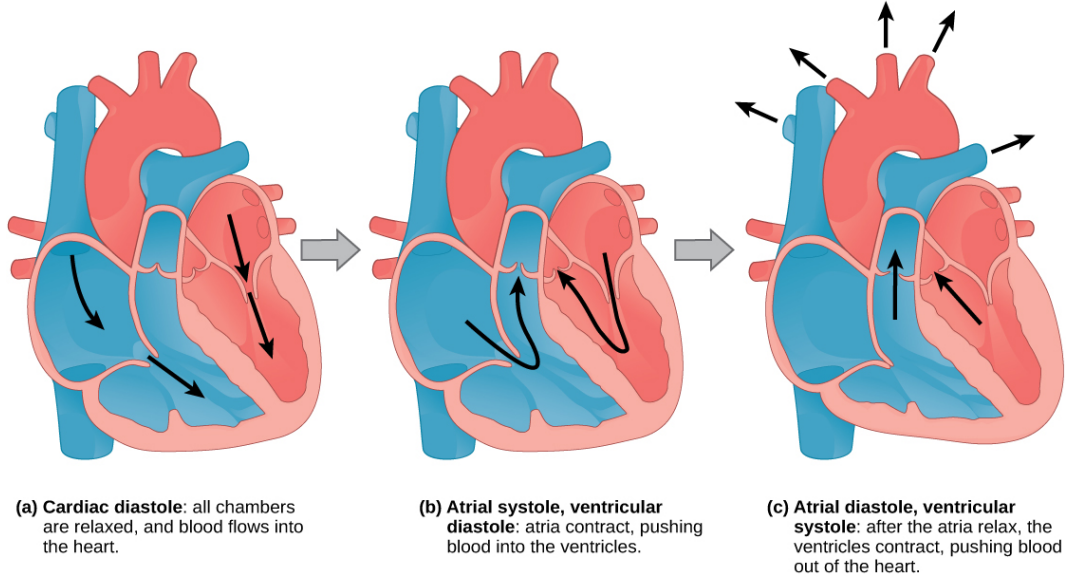


Figure 1: Heart contractions during a cardiac cycle

Mechanical vibrations reflect the turbulence that occurs when heart valves close. Traditionally, a stethoscope is used in cardiac auscultation to listen to these sounds that provide important acoustic information regarding the health condition of the heart. [4]

Phonocardiography, is a diagnostic technique that creates a graphic record, called phonocardiogram, of the sounds and murmurs produced by the contracting heart. The phonocardiogram is obtained either with a chest microphone or with a miniature sensor in a small tubular instrument that is introduced through the blood vessels into one of the heart chambers. The phonocardiogram usually supplements the information obtained by listening to body sounds with a stethoscope (auscultation) and is of special diagnostic value when performed simultaneously with measurement of the electrical properties of the heart (electrocardiography) and pulse rate.[6]

The time-frequency analysis of the PCG signals permits detecting and characterizing abnormal murmurs or extra sounds (systole or diastole) in the diagnosis of heart disease. In this study, we analyze normal, murmur and extra heart sounds recordings, separating them from artifacts. Most often, the symptoms of cardiovascular diseases become worse over time and detecting them with noninvasive techniques in early stages is crucial.

The correlation among the phonocardiogram and the biological phenomenon is presented in the following diagram:

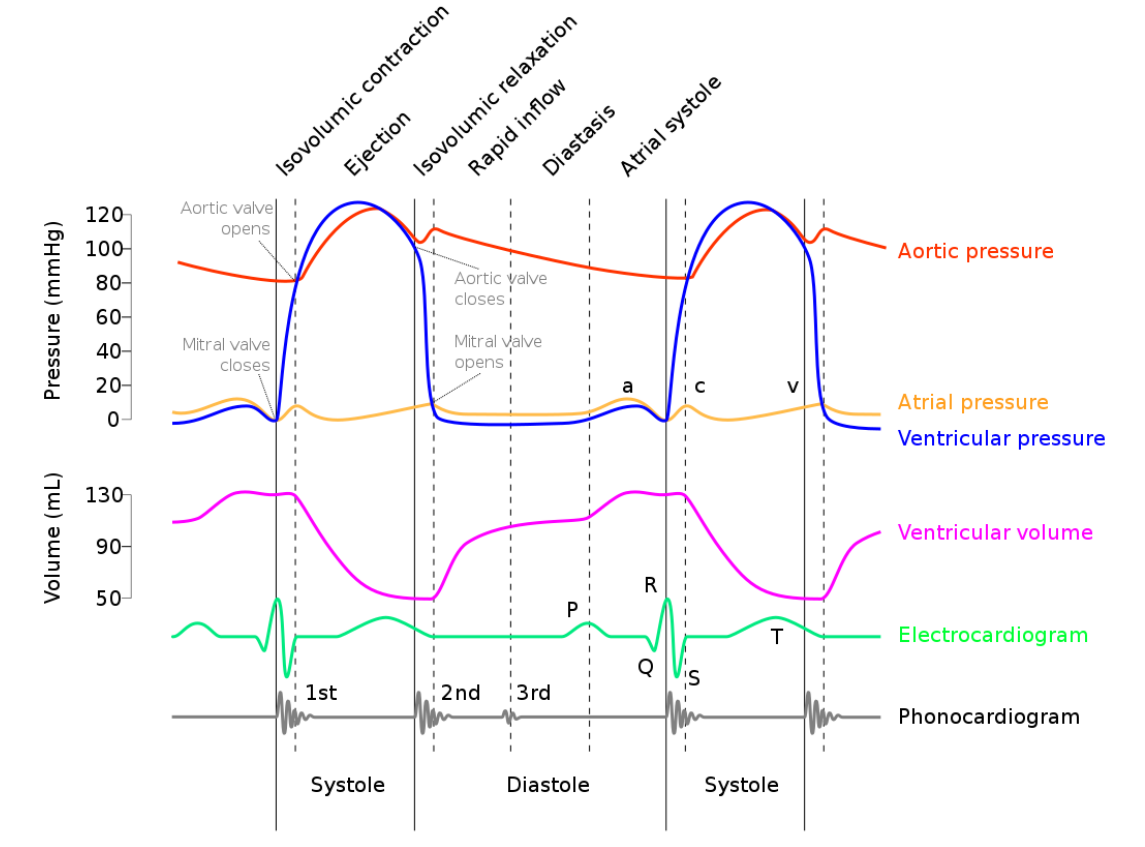


Figure 2: The Wiggers Diagram illustrating the cardiac cycle

Heart murmur

Heart murmurs are heart sounds produced when blood flows across one of the heart valves that are loud enough to be heard with a stethoscope. Heart murmurs are most frequently categorized, into systolic murmurs and diastolic murmurs, differing in the part of the heartbeat on which they can be heard. There are also, continuous murmurs cannot be directly placed into either category.

Systolic murmurs are due to blood flow through the semilunar valves. They occur at the start of blood ejection — which starts after S1 — and ends with the cessation of the blood flow — which is before S2. Diastolic murmurs start after S2 and end before S1. Many involve stenosis of the atrioventricular valves or regurgitation of the semilunar valves. [10]

Heart arrhythmia and extra beats

Heart arrhythmia (also known irregular heartbeat) is a group of conditions in which the heartbeat is irregular, too fast, or too slow. There are four main types of arrhythmia: extra beats, supraventricular tachycardias, ventricular arrhythmias, and bradyarrhythmias. Extra beats, part of our dataset, come in two different types, premature atrial contractions and pre-

mature ventricular contractions. Often they cause no symptoms but may present with fluttering in the chest or a skipped beat. [11]

I.2. Previous work

Many studies have been done on phonocardiogram signal so far. The research on this topic increased nowadays due to improvement in signal processing techniques and new methods in big data analysis. A summary of the most important results obtained with the Classifying Heart Sounds PASCAL Challenge dataset can be found here [24-25].

The Classifying Heart Sounds Workshop 2012 is the first international workshop to focus on the use of statistical machine learning techniques to segment and classify real-world heart audio. The challenge for this workshop was to create a first level of screening of cardiac pathology both in a Hospital environment by a doctor (using a digital stethoscope) and at home by the patient (using a mobile device).

The problem is of particular interest to machine learning researchers as it involves classification of audio sample data, where distinguishing between classes of interest is non-trivial. Success in classifying this form of data requires extremely robust classifiers.

		ISEP/IPP Portugal J48 / MLP	CS UCL	SLAC Stanford
Challenge 1 A	Total error	4 219 736.5	3 394 378.8	1 243 640.7
Challenge 1 B	Total error	72 242.8	75 569.8	76 444.4
Challenge 2 A	Precision of Normal	0.25 / 0.35	0.46	
	Precision of Murmur	0.47 / 0.67	0.31	
	Precision of ExtraS	0.27 / 0.18	0.11	
	Precision of Artifact	0.71 / 0.92	0.58	
	Artifact Sensitivity	0.63 / 0.69	0.44	
	Artifact Specificity	0.39 / 0.44	0.44	
	Youden Idx Artifact	0.01 / 0.13	-0.09	
	F-score	0.20 / 0.20	0.14	
	Total Precision	1.71 / 2.12	1.47	
Challenge 2 B	Precision of Normal	0.72 / 0.70	0.77	
	Precision of Murmur	0.32 / 0.30	0.37	
	Precision of ExtraS	0.33 / 0.67	0.17	
	Heart prb Sensitivity	0.22 / 0.19	0.51	
	Heart prb Specificity	0.82 / 0.84	0.59	
	Youden Idx Hrt prb	0.04 / 0.02	0.01	
	Discriminant Power	0.05 / 0.04	0.09	
	Total Precision	1.37 / 1.67	1.31	

Figure 3: A summary of the results of the three finalists from their approaches

The first team uses, after the segmentation, the J48 and MLP algorithms (using Weka) to train and classify the computed features. The UCL team exploits domain knowledge and compares the features of heartbeat before and after dropping out extra peaks and the smallest interval. By doing so they try to minimize the negative effect of noise. [24-25] In the literature there are other proposed ways to tackle this challenge: partial least squares regression, neural networks and convolution neural networks.

Other models for classifying the heart sounds can be found [27], where the best general accuracy obtained was 93,18% for all the classes. The model proposed is a neural network.

II. Methodology and research methods

II.1. CRISP-DM Methodology

Cross-industry standard process for data mining, commonly known by its acronym CRISP-DM, is a data mining process model that describes commonly used approaches used to tackle problems. The current process model for data mining provides an overview of the life cycle of a data mining project. It contains the phases of a project, their respective tasks, and the relationships between these tasks. At this level, it is not possible to identify all relationships. Relationships could exist between any data mining tasks depending on the goals, the background, the interest of the user and on the data. [12]

The life cycle of a data mining project consists of six phases, shown in the next figure. The sequence of the phases is not fixed. Moving back and forth between different phases can be required. The outcome of each phase determines which phase has to be performed next. The arrows indicate the most important and frequent dependencies between phases.

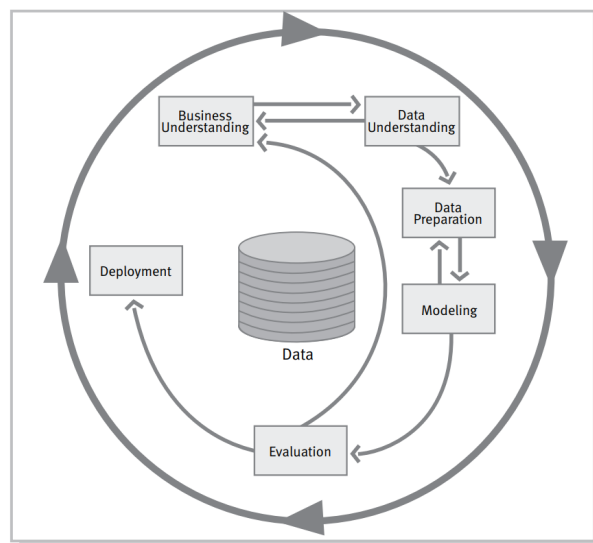


Figure 4: Phases of the CRISP-DM model

Business understanding

The initial phase main purpose is understanding the project objectives and requirements from a business perspective, analyzing the available resources, and then converting this knowledge into a data mining problem definition, and a plan designed to achieve all the objectives.

For our study the main objective is to predict with a high rate of trust if a person has arrhythmia or murmurs through a phonocardiogram. The resources available for us are a dataset of different types of recordings, a graphic card GeForce GTX 1050 (2GB) and a Intel(R) Core(TM) i7-7700HQ CPU @ 2.80GHz. Our initial goal would be to get a good accuracy at test.

Data understanding

The data understanding phase starts with an initial data collection and proceeds with activities that can give insides about the data, to identify data quality problems, or to detect interesting subsets to form hypotheses for hidden information.

Our dataset has been gathered from two sources. All the files are .wav files with lengths between 1 second and 30 seconds and two frequencies: 44100 Hz and 4000 Hz. We also have examples of recordings there are not heartbeats, but artifacts.

Data preparation

This phase covers all activities to construct the final dataset (data that will be used for creating the model) from the initial raw data. Tasks representative for the data preparation phase include table, record, and attribute selection as well as transformation and cleaning of data for modeling tools.

In this phase we normalized each recording using the Frobenius norm and after this, using a peak detection algorithm, we identified the sounds S1 and S2 in each recording. We searched for the peaks starting with second 0,5 and ended at $\text{len}(\text{rec}) - 0,5$ seconds. For each peak we sliced a 1 second piece of the record, obtaining multiple one second recordings. In order to get a better accuracy through multiplying the data we used a sliding window technique.

Modeling

In this phase, various modeling techniques are selected and applied, and their parameters are calibrated to optimal values. Usually, there are several techniques for the same data mining problem type. Some techniques have specific requirements on the form of data.

The models we created are one Convolutional Neural Networks that classifies each record in one of the four classes, and the second model uses a Multi-Task Learning technique in Convolutional Neural Networks.

Evaluation

At this stage in the project you have built a model (or models) that appears to have good quality, from a data analysis perspective. Before proceeding to final deployment of the model, it is important to evaluate the model, and review the steps executed to construct the model, to be certain it achieves the business objectives.

The metrics we used for evaluating the models is the accuracy of the test dataset. Other metrics that we used are the validation dataset accuracy, the value of the loss function, the sensitivity and the specificity.

Deployment

Creation of the model is not the end of the project. Even if the purpose of the model is to increase knowledge of the data, the knowledge gained will need to be organized and presented in a way that is useful to the users. Depending on the requirements, the deployment phase can be as simple as generating a report or as complex as implementing an application from scratch. In many cases it will be the customer who will carry out the deployment steps.

Business Understanding	Data Understanding	Data Preparation	Modeling	Evaluation	Deployment
Determine Business Objectives Background Business Objectives Business Success Criteria Assess Situation Inventory of Resources Requirements, Assumptions, and Constraints Risks and Contingencies Terminology Costs and Benefits Determine Data Mining Goals Data Mining Goals Data Mining Success Criteria Produce Project Plan Project Plan Initial Assessment of Tools and Techniques	Collect Initial Data Initial Data Collection Report Describe Data Data Description Report Explore Data Data Exploration Report Verify Data Quality Data Quality Report	Select Data Rationale for Inclusion/Exclusion Clean Data Data Cleaning Report Construct Data Derived Attributes Generated Records Integrate Data Merged Data Format Data Reformatted Data Dataset Dataset Description	Select Modeling Techniques Modeling Technique Modeling Assumptions Generate Test Design Test Design Build Model Parameter Settings Models Model Descriptions Assess Model Model Assessment Revised Parameter Settings	Evaluate Results Assessment of Data Mining Results w.r.t. Business Success Criteria Approved Models Review Process Review of Process Determine Next Steps List of Possible Actions Decision	Plan Deployment Deployment Plan Plan Monitoring and Maintenance Monitoring and Maintenance Plan Produce Final Report Final Report Final Presentation Review Project Experience Documentation

Figure 5: Generic tasks and outputs of the CRISP-DM model

In the next sections we will detail some of the most important and time consuming phases of the project, detailing the mathematical and biological background for each stage.

II.2. Data understanding and preparation

II.2.1. Data Description and Selection

The dataset is split into two sources, A and B. The recordings from the A dataset are gathered from the general public via the iStethoscope Pro iPhone app. The second dataset, B, is collected from a clinic trial in hospitals using the digital stethoscope DigiScope. Most information in heart sounds is contained in the low frequency components, with noise in the higher frequencies. [2]

The audio files have varying lengths, between 1 second and 30 seconds (some have been clipped to reduce excessive noise and provide the salient fragment of the sound). The two datasets differ in number, frequency and other proprieties of the .wav files.

A file with the `.wav` file extension is a Waveform Audio file. This is a standard audio format. It is an extension of the bitstream format Resource Interchange File Format (RIFF). WAV is similar to AIFF and 8SVX files.

Dataset A

The recordings from this dataset are gathered using the iStethoscope Pro iPhone app. All of them are represented with on a 705 bitrate, through a mono channel. The samples rate is 44100 Hz. The following types of heartbeats are recorded and labeled:

Atraining_normal 14Mb 31 files
Atraining_murmur 17.3Mb 34 files
Atraining_extrahs 6.9Mb 19 files
Atraining_artifact 22.5Mb 40 files

Dataset B

The recordings from this dataset are gathered using DigiScope. All of them are represented with on a 705 bitrate, through a mono channel. The samples rate is 4000 Hz. The following types of heartbeats are recorded and labeled:

Btraining_normal (containing sub directory Btraining_noisynormal) 13.8Mb 320 files
Btraining_murmur (containing sub directory Btraining_noisymurmur) 5.3Mb 95 files
Btraining_extrasystole 1.9Mb 46 files

II.2.2. Preprocess Data

Data preparation is the process of getting data ready for applying different models. During data preparation, we have to take the data that is stored in raw form and transform it so that it can be effectively used by machine learning algorithms.

II.2.2.a. Frames retrieval

In order to use the whole dataset (A and B) we need to transform the recordings at the same frame-rate. We choose 16000 Hz in order not to lose much information from the B dataset, and to enhance the A dataset with more values for the same unit of time.

We used `ffmpeg` command to transform all the data. With a bash script we iterated through the `.wav` files and changed all of them at 16000 Hz. [5]

```
ffmpeg -i {file} -ar 16000 {file} -y
```

After all the recording had the same meta-data (except the length), we iterated through the dataset and parse each file in Python, in order to process them. We use the `wave` library to open the recordings and read them frame by frame. We obtained arrays of length equal with the duration in time of the recording multiplied with the framerate (16000 Hz).

An audio frame, or sample, contains amplitude (loudness) information at that particular point in time. To produce sound, tens of thousands of frames are played in sequence to produce frequencies.

In our case there are 16000 frames/samples per second. Each of those frames contains 16-bits of resolution, allowing precise representations of the sound levels. When we use the `sound` module in Python to get a frame, it will be returned as a series of hexadecimal characters, two characters for 16-bit mono.

```
b'\x0e\x00\x11\x00\x0e\x00\x00\x00\x02\x00\x0b\x00\xfe\xff'
```

We unpack the bytestring by using the `struct` library in Python. `struct` requires a format string based on C format characters, so we use the signed format that corresponds to 2 bytes; according to the C format characters, we should use the format character `'h'`.

A slight trick in the `struct` library is that it wants its format string to exactly match the expected size, so we have to multiply the format character `'h'` by the number of frames in the bytestring.

```
samples = struct.unpack('h' * f.getnframes(), frames)
#frames holds the bytestring representing the audio frames
(14, 17, 14, 0, 2, 11, -2) - for the previous example
```

II.2.2.b. Plotting

For plotting the recordings to better visualize the samples from the dataset we need a different tool. To get the timing, we'll grab the sampling rate from the wave object. In order to get better conclusions we plotted the whole record.

We have here some examples of the records with normal, murmur and extrasystole sounds, but also some examples of artifacts.

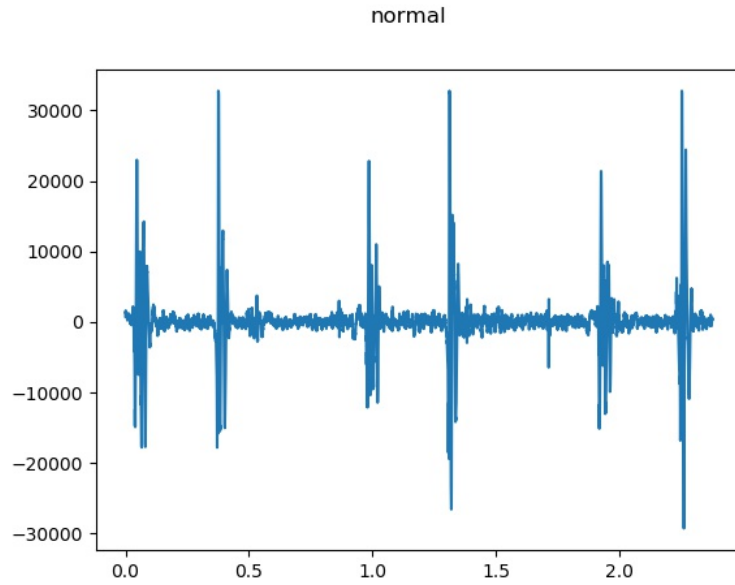


Figure 6: Example of normal heartbeat phonocardiogram

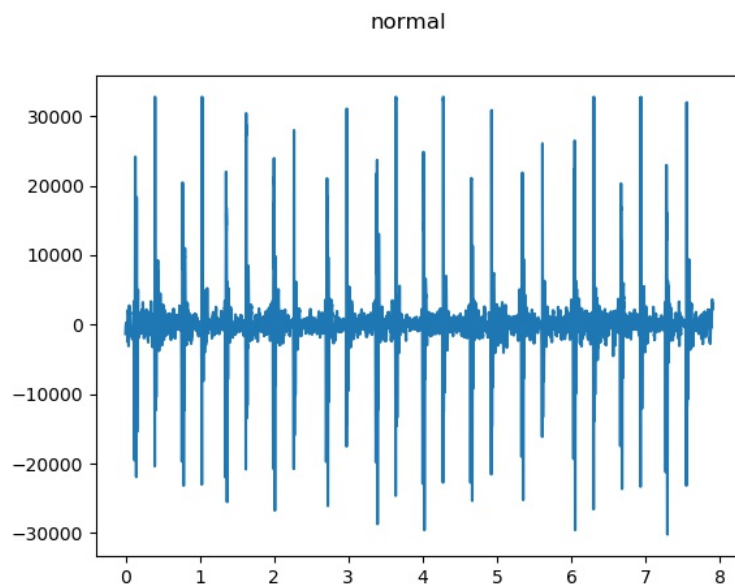


Figure 7: Example of normal heartbeat phonocardiogram

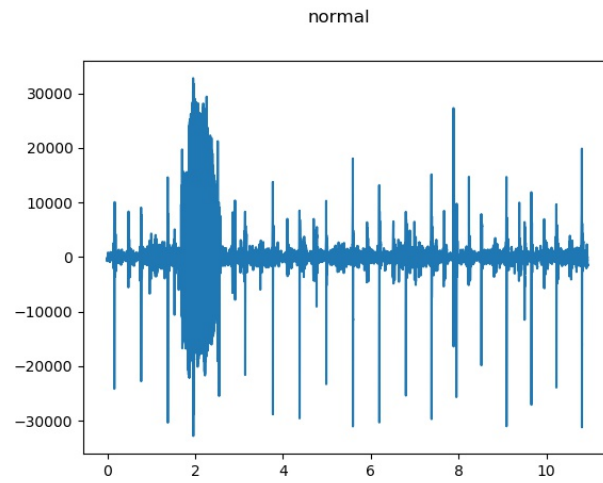


Figure 8: Example of noisy normal heartbeat phonocardiogram

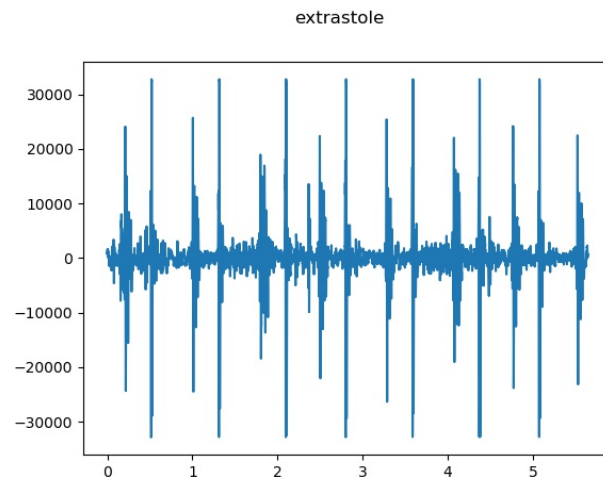


Figure 9: Example of extrasystole heartbeat phonocardiogram

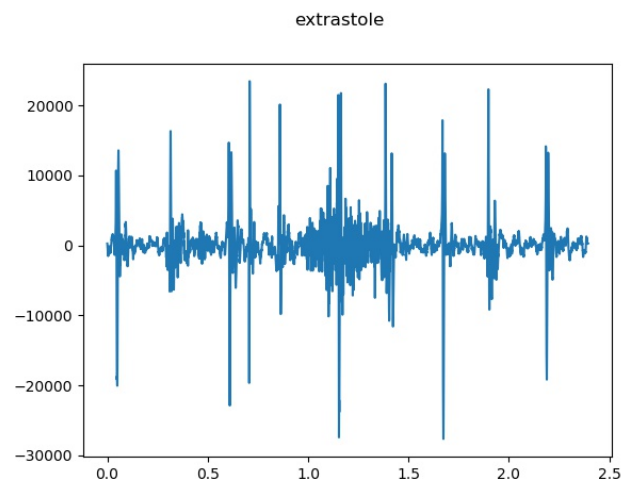


Figure 10: Example of extrasystole heartbeat phonocardiogram

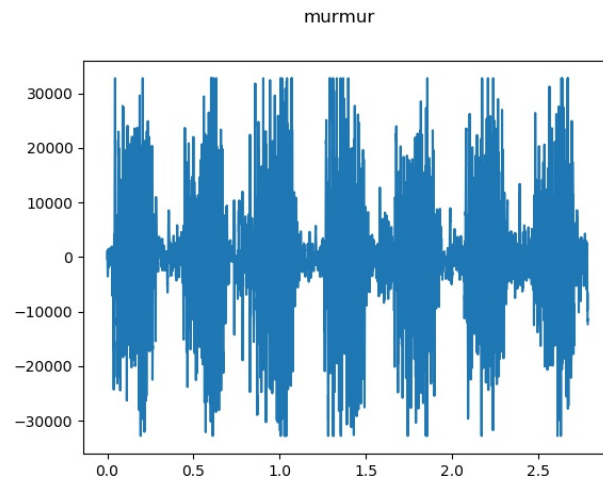


Figure 11: Example of murmur heartbeat phonocardiogram

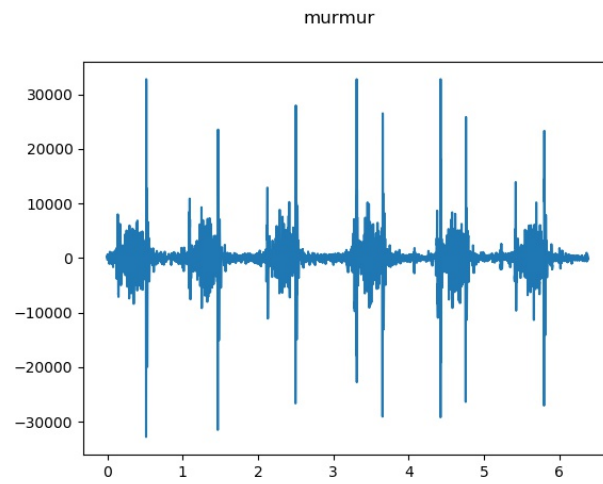


Figure 12: Example of murmur heartbeat phonocardiogram

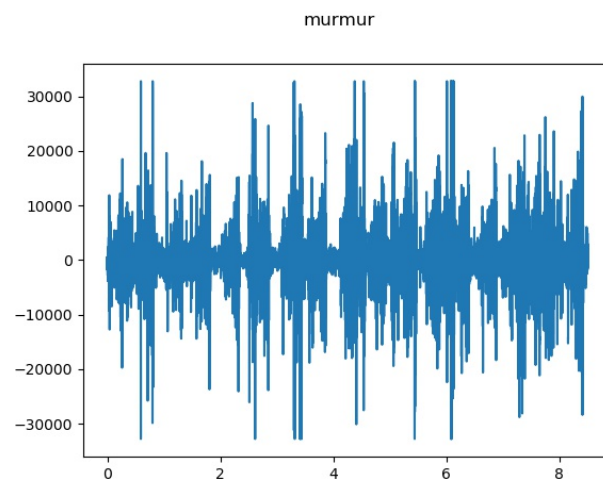


Figure 13: Example of noisy murmur heartbeat phonocardiogram

II.2.2.c. Peak Analysis

Another step of the data preprocessing phase is the peak detection. Identifying and analyzing peaks (also called spikes) in a given time-series is important in many applications, because peaks are useful topological features of a time-series. In phonocardiograms, a peak is one of the sounds that the heart produces. [17]

This problem was encountered in many signal processing applications. Up to now, many different methods have been developed and the window-threshold technique is the one we implemented.

```
def is_peak (x, left, right):
    return np.amax(left) < x and np.amax(right) < x

def get_peaks(samples):
    std = np.std(samples)
    for i in range(len(samples)):
        if samples[i] > std * 2.8:
            if is_peak(samples[i],
                        samples[i - Cframerate // 5 : i],
                        samples[i + 1 : i + Cframerate // 5]):
                sol.append(i)
    return sol
```

The algorithm presented has as input the array that represents a whole recording and the output is a list that has all the peaks positions in time.

We need the variation of the dataset in order to create a threshold for selecting the possible heartbeat. Because of the noise that each recording has, we need to approximate where do most of the heartbeats start. The value we picked is 2.8 multiplied with one standard deviation. In this interval we have about 99% of the data, and the other values will be tested if they are peaks. [21]

We will check for each feasible solution, if it satisfies our criteria. In order to call a frame, peak, it should be the greatest value in the window we created. The window size is 0.2 seconds, and we test if the current value is the peak of this interval. When we find a value suitable, we append it to the list of solutions.

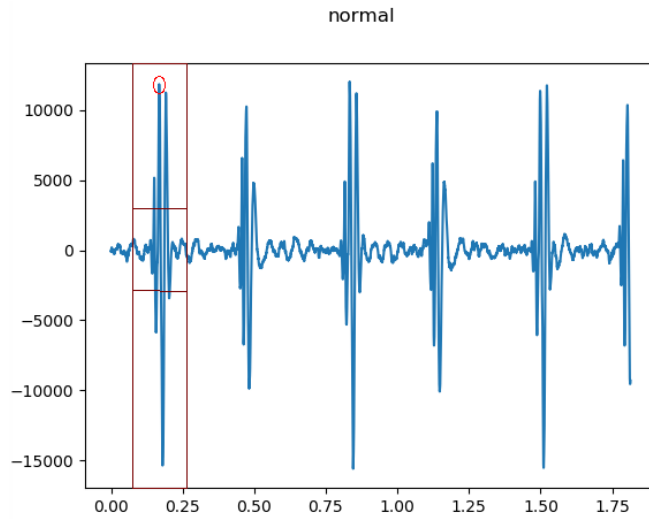


Figure 14: Identifying the first heartbeat sound in a record. In a window of size 0.2 seconds we found the value that is the peak and respects all the conditions

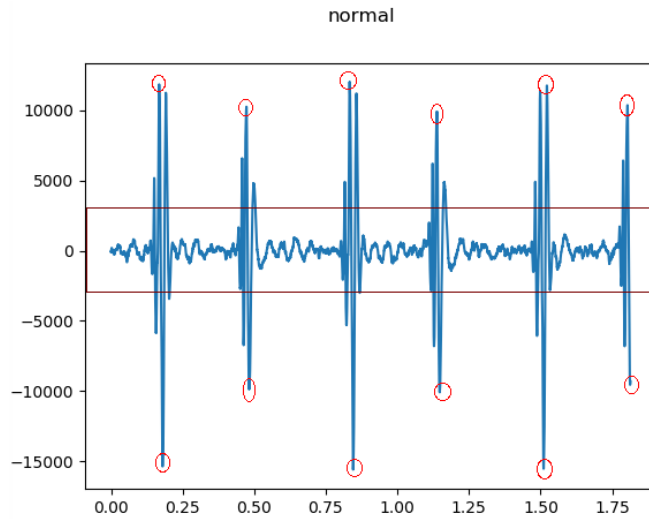


Figure 15: All detected heartbeat sounds in a record. All absolute values of the peaks are greater than $2.8 * std(rec)$

II.2.3. Data Transformations

The final step of the data preparation phase is to transform the processed data. The specific algorithm we will be working with and the knowledge of the problem domain influence this step. The following data transformations were applied on our dataset, while scaling, attribute decomposition and attribute aggregation are the most common techniques used. This step is also referred to as feature engineering.

II.2.3.a. L^2 norm

In this point we have 585 arrays of different lengths that contain negative and positive values that represent the amplitude of the recording in a unit of time. These values are between $[-40000, 40000]$, and so they are difficult to work with, because the result of different computations can exceed the limits.

A solution for this problem would be to normalize all the arrays. We choose to use the L^2 norm for this task. The value of the L^2 norm is between $[L^\infty = \max_{x_i \in rec}(x_i), L^1 = \sum_{x_i \in rec}(x_i)]$, so the values for each frame will be divided by a value greater than it. [15] This means that all the values will be much smaller than 1 (or -1). In order not to lose precision we multiplied the values with 100. To compute the L^2 norm we used the Numpy library.

```
fac_norm = np.linalg.norm(samples)
samples = (samples / fac_norm) * 100
```

Next we will present the mathematical background for computing the norms.

Given an n -dimensional vector $x \in \mathbb{R}^n$, the L^2 norm, also called Euclidean norm, is captured by the formula :

$$x = \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_n \end{bmatrix} \in \mathbb{R}^n,$$

$$\|x\|_2 = \sqrt{x_1^2 + x_2^2 + \dots + x_n^2}$$

The L^2 norm is a particular case for the p -norm, where $p = 2$. [16]

$$\|x\|_p = \sqrt[p]{|x_1|^p + |x_2|^p + \dots + |x_n|^p}$$

After we divided by the norm, we multiplied the values with 100, and we obtained the exact values heartbeats with values greater than 1, or lower than -1.

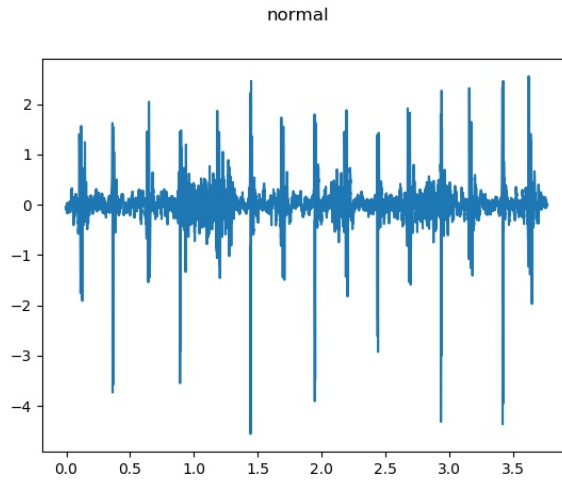


Figure 16: Heartbeat phonocardiogram normalized

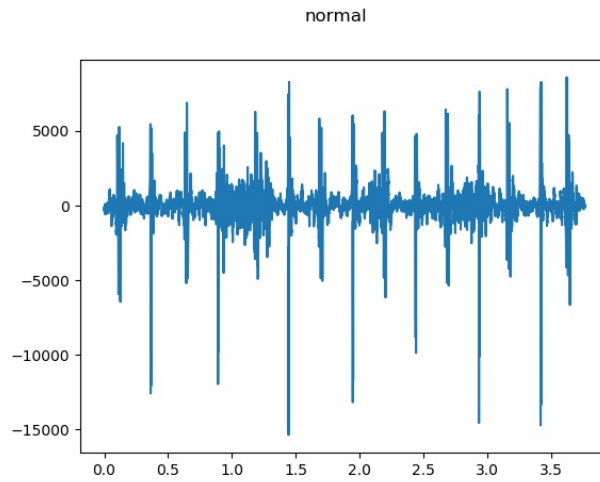


Figure 17: Heartbeat phonocardiogram before normalization

II.2.3.b. Sliding window for data selection

A sliding window is a sublist that runs over an underlying collection. After we have the list of the peaks from our recordings, we sliced one second of the audio file, centered in each peak. We choose this approach according to the results obtained by [14].

In order to increase the accuracy of our models, we tried to move this window with 0,0025 seconds and 0.005 seconds, left and right. This way, from only one array of values we got now five new entries in our dataset. This method for multiplying the data we use as input for the classifiers, helps better generalize the rules for obtaining good results. [19]

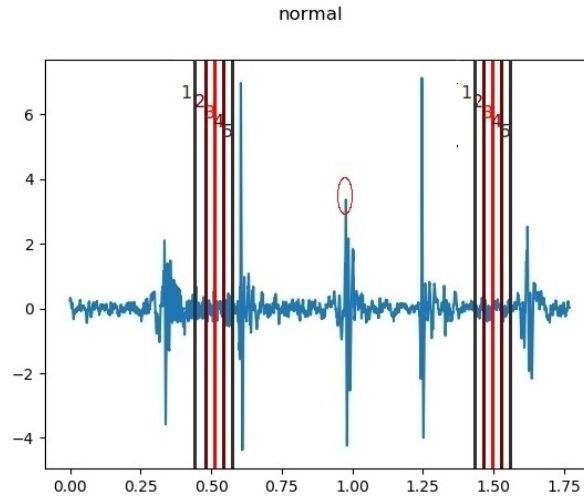


Figure 18: The 5 segments of audio recording that are centered in the peak pointed

II.2.3.c. Feature extraction

Given a set of samples on which a decision should be made, a feature is a value that would possibly be different among those samples and discriminate one sample from another. This decision may be, as in our case, to classify the sample to a finite set. Feature extraction is the process of collecting discriminatory information from a set of samples.

The CNN we built have as input the raw recordings, but in the multi task learning model, for classifying the extrastole, we compared the AdaBoost Classifier and a decision tree. In order to be able to use this classifiers, we needed real values that can After features are extracted, Classification is performed based on the selected features. The performance of classifier depends on both how good the signals are pre-processed and how good the features are extracted. [14]

In this thesis a total of 11 features from time domain, frequency domain and statistical features were extracted that could have potential to discriminate among the extrastole and other(normal and murmur) signals. The features in the whole signal have been extracted in order to deal with the situations of extrasystole sounds. [7]

```
def features(arr):
    peaks_list = get_peaks (arr)
    dists = distances (peaks_list)

    getInfo = lambda x, f1, f2: [f1(x), f2(x)]

    sol += getInfo(dists, np.mean, np.std)
    sol += getInfo(peaks_list, np.mean, np.std)
    sol += getInfo(dists, np.min, np.max)
```

```

sol += getInfo(peaks_list, np.min, np.max)
sol += getInfo(arr, np.mean, np.std)
sol.append(len(peaks_list))

return sol

```

The potential seen in these features and hence the reason for evaluating these features is explained further.

No.	Feature	Feature domain	Details
1	Peak Frequency	Frequency domain	It shows the frequency at which the peak amplitude occurs. Since the extra sounds appear between the intervals of regular sounds, it could have been a potential feature.
2	Peak Frequency Standard Deviation	Frequency domain	It quantifies the amount of dispersion of the peak occurrences. The existence of extra sounds should indicate a greater value.
3	Peak Amplitude	Time domain	The mean peak amplitude shows the peak value of the signal. The extra sounds and normal signals can vary in amplitude so this feature has potential.
4	Peak Amplitude Standard Deviation	Time domain	If the standard deviation of the peak amplitude is greater, it means that the sounds have different intensity, and this can be a sign of extra sounds.
5	Minimum Peak Distance	Frequency domain	It represents the smallest distance between 2 consecutive heartbeat sounds identified in the record. If this value is small it can be the distance between an extra sound and a regular beat.
6	Maximum Peak Distance	Frequency domain	It represents the longest time between 2 consecutive heartbeat sounds identified in the record. This value can show if there is an abnormal distance between consecutive sounds.

7	Minimum Peak Amplitude	Time domain	Normal heart sounds have about the same amplitude (assuming that that systole is not very shorter than diastole). An extra sound is a variation of these values, so a small value can be an extra sound.
8	Maximum Peak Amplitude	Time domain	Normal heart sounds have about the same amplitude (assuming that that systole is not very shorter than diastole). An extra sound is a variation of these values, so a big value can represent an extra sound.
9	Mean Amplitude	Time domain	The mean amplitude of the one second window can be correlate with the standard deviation of all the values.
10	Standard Devia- tion Amplitude	Time domain	If the dispersion of all the values in the one second window is big than it means that we have more values that have different values than the mean.
11	Number of Peaks	Statistical	The only discrete feature we used for classification, the number of peaks in one second represents the number of heart sounds we identified in this interval.

Table 1: List of Features Extracted for Classification

All the features are calculated from the PCG signals. Two algorithms for Attribute Evaluation are applied on the feature set to find the most significant features. The results are presented in the next chapter.

II.3. Classification Models

As the first step in modeling, we select the actual modeling technique that is to be used. Out picks are CNN and AdaBoost. The models we created and used for testing are presented in the following subsections.

II.3.1. Multi-Class CNN

Using the normalized and segmented sound recordings, a CNN is trained to extract features and construct a classification function. The CNN consists of 6 layers, namely convolution layers and fully connected layers. [18]

First, the convolution layer extracts high level (abstracted) features by sequentially transforming raw input data into high-level abstract features. The convolution layer contains a non-linear activation function, kernel regularizer and max pooling layers.

The non-linear activation function is Relu and is used to increase the representability of a network (increase the fitness of a model). We used the L2 regularization. The max pooling layer selects the maximum value among its neighbors to reduce noise and extract abstract features. After having gone through the convolution layer, the features are autonomously extracted from the segmented signals.

Fully connected layers output values for classification predictions by linearly combining the features extracted from convolutions layers and having the combined values go through non-linear activation functions. The last layer uses the softmax activation function. As one segmented signal goes through the convolution and fully-connected layers, the features are extracted and used to classify the signal, respectively.

After an architecture of CNN is designed, the parameters of CNN have been trained by back propagation algorithm with the categorical crossentropy loss function and mini-batch learning using training data. We use Keras to construct and train our model.

Layer (type)	Output Shape	Param #
conv1d_1 (Conv1D)	(None, 15991, 12)	132
max_pooling1d_1 (MaxPooling1D)	(None, 3198, 12)	0
flatten_1 (Flatten)	(None, 38376)	0
dense_1 (Dense)	(None, 500)	19188500

dense_2 (Dense)	(None, 100)	50100
dense_3 (Dense)	(None, 20)	2020
dense_4 (Dense)	(None, 3)	63
=====		
Total params: 19,240,815		
Trainable params: 19,240,815		

II.3.2. Multi-Task Learning

In Machine Learning, we typically care about optimizing for a particular metric. By sharing representations between related tasks, we can enable our model to generalize better on our original task. This approach is called Multi-Task Learning (MTL).

In the context of Deep Learning, multi-task learning is typically done with either hard or soft parameter sharing of hidden layers. Our approach uses soft parameter sharing. In soft parameter sharing on the other hand, each task has its own model with its own parameters. MTL is a natural fit in situations where we are interested in obtaining predictions for multiple tasks at once, so this method can be applied to our problem. We split the multi class-decision in three different tasks. [23]

II.3.2.a. Neural Network Normal heartbeat

For deciding weather a heartbeat is normal or not, we trained a CNN to extract features and construct a classification function. The CNN consists of 6 layers.

First, the convolution layer extracts high level (abstracted) features with 4 filters. The convolution layer uses Relu as activation function, kernel regularizer and max pooling layers. We used the L2 regularization. The max pooling layer selects the maximum value among its neighbors. The fully connected layers linearly combine the features extracted from convolutions layers. The last layer uses the softmax activation function. As one segmented signal goes through the convolution and fully-connected layers, the features are extracted and used to classify the record.

The parameters of CNN have been trained by back propagation algorithm with the Kullback Leibler divergence loss function and mini-batch learning using training data.

Consider two probability distribution P and Q over the same domain X . The Kullbach-Leibler divergence is computed in the following way.

$$D_{KL}(P, Q) = \sum_{x \in X} P(x) \log \frac{P(x)}{Q(x)}$$

Layer (type)	Output Shape	Param #
conv1d_1 (Conv1D)	(None, 15991, 4)	44
max_pooling1d_1 (MaxPooling1D)	(None, 3198, 4)	0
flatten_1 (Flatten)	(None, 12792)	0
dense_1 (Dense)	(None, 500)	6396500
dense_2 (Dense)	(None, 100)	50100
dense_3 (Dense)	(None, 20)	2020
dense_4 (Dense)	(None, 2)	42
Total params: 6,448,706		
Trainable params: 6,448,706		

II.3.2.b. Neural Network Murmur heartbeat

The CNN used for classifying murmur heartbeats is trained to extract features and construct a classification function. The CNN consists of 6 layers, namely convolution layers and fully connected layers.

The convolution layer extracts abstract features from raw input data. The convolution layer is formed from Relu activation function, L2 regularization and max pooling layers. The max pooling layer selects the maximum value among its neighbors to reduce noise and extract abstract features.

Fully connected layers output values for classification predictions by linearly combining the features extracted from convolutions layers. The last layer uses the softmax activation function. As one segmented signal goes through the convolution and fully-connected layers, the features are extracted and used to classify the signal, respectively.

After an architecture of CNN is designed, the parameters of CNN have been trained by back propagation algorithm with the Kullback Leibler divergence loss function and mini-batch learning using training data.

Layer (type)	Output Shape	Param #
conv1d_1 (Conv1D)	(None, 15991, 4)	44
max_pooling1d_1 (MaxPooling1D)	(None, 3198, 4)	0
flatten_1 (Flatten)	(None, 12792)	0
dense_1 (Dense)	(None, 500)	6396500
dense_2 (Dense)	(None, 100)	50100
dense_3 (Dense)	(None, 20)	2020
dense_4 (Dense)	(None, 2)	42
Total params: 6,448,706		
Trainable params: 6,448,706		

II.3.2.c. AdaBoost Classifier

AdaBoost is a boosting method. There are m trees defined, where each of them has a value used in the standard AdaBoost method. We are changing the weight of each event. Each classifier (tree) is required to be better than random guessing with respect to the weighted distribution upon which the classifier is trained. Thus, error is required to be less than 0.5, since, otherwise, the weights would be updated in the wrong direction.

After computing the error for each tree, the weight of the tree will be $\alpha_i = \ln(\frac{1-\text{err}_i}{\text{err}_i})$. The weight of each event will be $w_k = w_k \cdot e^{\alpha_i I(y_k \neq T_i(x_k))}$. After renormalizing the weights, the score for a given event is the weighted sum of the scores over the individual trees.

At each iteration, adaptive boosting changes the sample distribution by modifying the weights attached to each of the instances. It increases the weights of the wrongly predicted instances and decreases the ones of the correctly predicted instances. The weak learner thus focuses more on the difficult instances. After being trained, the weak learner is added to the strong one according to his performance (so-called alpha weight). The higher it performs, the more it contributes to the strong learner. Finally, AdaBoost gives different weights to data points that are hard to predict. [28]

II.4. Technologies

In this section we will present the technologies we used for the application. The main characteristics we looked for are: scalability and creating reusable components. The following technologies helped us reaching our goals.

II.4.1. WAV

A file with the `.wav` file extension is a Waveform Audio file. This is a standard audio format. WAV files are usually uncompressed but compression is supported. It is an extension of the bit-stream format Resource Interchange File Format (RIFF). WAV is similar to AIFF and 8SVX files, both of which are more commonly seen on Mac operating systems. [13]

All the recordings are stored as `.wav` files. For processing we used the `wave` library in `Python`. The `wave` module provides a convenient interface to the `.wav` sound format. It does not support compression/decompression, but it does support mono/stereo. The `wave` module defines reading functions and facilitates access to properties.

The Canonical WAVE file format

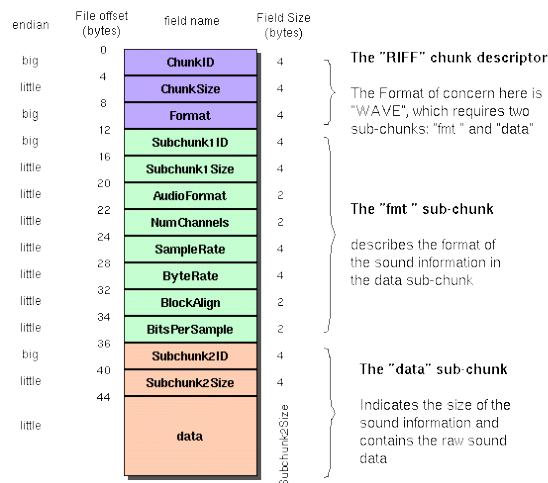


Figure 19: Wave file format

II.4.2. Python

`Python` is an interpreted high-level programming language for general-purpose programming. `Python` provides constructs that enable clear programming on both small and large scales. It features a dynamic type system and automatic memory management. It supports multiple programming paradigms, including object-oriented, imperative, functional and procedural, and has

a large and comprehensive standard library.

There are available interpreters for many operating systems. `CPython`, the reference implementation of `Python`, is open source software and has a community-based development model. Because of the many resources and documentation for working with data. We used the following libraries in creating models (CNN and AdaBoost).

II.4.2.a. Sklearn

`Scikit-learn` is a module Machine Learning in `Python`. It provides diverse and efficient tools for data mining and data analysis that are accessible and has reusable in various contexts. It is built on `NumPy`, `SciPy`, and `matplotlib`. Another bonus is that it is open source.

II.4.2.b. Keras

`Keras` is a high-level neural networks API, written in `Python` and capable of running on top of `TensorFlow`, `CNTK`, or `Theano`. It was developed with a focus on enabling fast experimentation. Being able to go from idea to result with the least possible delay is key to doing good research. The guiding principles are: user friendliness, modularity, easy extensibility and work with `Python`.

We use `TensorFlow` as back end for `Keras` models. `TensorFlow` is an interface for expressing machine learning algorithms, and an implementation for executing such algorithms. A computation expressed using `TensorFlow` can be executed with little or no change on a wide variety of heterogeneous systems and can be used computational devices such as GPU cards.

II.4.3. CUDA

`CUDA` (Compute Unified Device Architecture) is a parallel computing platform and programming model developed by `NVIDIA` for general computing on graphical processing units (GPUs). It allows to use a `CUDA`-enabled graphics processing unit (GPU) for general purpose processing.

A big improvement in the results we obtain is using powerful and efficient parallel computing provided by GPU computing. GPUs are used to train deep neural networks using larger training sets, in an order of magnitude less time. We used GPU parallel computing power to speed up the training of the CNN.

III. Results

The experimental results on the two datasets can be compared with the three best methods in the Classifying Heart Sounds PASCAL Challenge. The evaluation of our models is performed on samples from the same datasets using the same evaluation criteria.

In order to evaluate our method, we computed the total accuracy and we will present the confusion matrix for the categorical classifier. For the multi-task learning methods we will present the accuracy for discrimination extrastole, murmur and normal heartbeats, one from the others. We will show our accuracy and the results for the feature selection part.

The data set we have for training has 451 recordings. After the processing steps we obtained 17901 segments of records, in the normal, extrastole and murmur classes. Out of these we use 15991 for training and the others for validation. These recordings have the following partition [12549, 3648, 1527] in the normal, murmur and extrastole classes.

The evaluation dataset consists of 30 recordings, segmented in [102, 111, 104] segments of records in the normal, murmur and extrastole classes.

III.1. Feature selection

After the feature extraction phase we wanted to rank these features on their importance in classification. For this task we ran 3 classifiers (a Decision Tree, Random Forest and AdaBoost) and the results are presented in the following table.

No.	Feature	Decision tree importance	Random Forest importance	AdaBoost importance
1	Peak Frequency	0.06358505	0.10835463	0.1
2	Peak Frequency Standard Deviation	0.05584003	0.08143857	0.02
3	Peak Amplitude	0.07775618	0.08109412	0.04

4	Peak Amplitude Standard Deviation	0.05335595	0.07786953	0.12
5	Minimum Peak Dis- tance	0.22781165	0.12076171	0.28
6	Maximum Peak Distance	0.0940705	0.10498685	0.18
7	Minimum Peak Amplitude	0.03635814	0.07228694	0.02
8	Maximum Peak Amplitude	0.03169072	0.07434332	0.04
9	Mean Amplitude	0.15517295	0.11145975	0.02
10	Standard Deviation Amplitude	0.18334003	0.15667982	0.14
11	Number of Peaks	0.02251938	0.01072477	0.04

Table 2: Feature importance for 3 classifiers

According to these results, the features that have the greatest impact in classifying the extrastole from the other heartbeats are: Minimum Peak Distance, Standard Deviation Amplitude, Mean Amplitude and Maximum Peak Distance.

We will see the impact of these results in the accuracy of the AdaBoost model in the following section.

III.2. Classification results

The results we obtained on the test data set is presented according the models we created: the multi-class CNN, the two CNN for normal and murmur datasets, and the AdaBoost Classifier. We present in this section the accuracy and the confusion matrix, beside other metrics. To better evaluate our models, we will take the result presented in section I.2 and compare them with the ones we obtained.

The dataset is imbalanced so the model evaluation part was difficult. The test dataset has almost equals parts of the 3 recording types.

III.2.1. Multi-class CNN

The accuracy representing how often the classifier gave the right answer, overall. The training accuracy resulted in the first epoch was 0.7615, followed by 0.9802. In order to avoid overfitting we used another dataset for validation. The validation dataset is not used for training, just for parameter optimisation.

The value of the loss function and the accuracy on the test dataset are the following:

Test loss: 2.7176815245858754

Test accuracy: 65.74923552868927

For a better understanding we present here the confusion matrix for the 3 class CNN we built. The recordings from the Normal class were in 87,6% of cases classified correctly, the Murmur recordings we 80,7%. The Extrastole category has about 30% accuracy, most of the cases being confused with Normal heartbeats. A cause for this can be the fact that a extra systole can appear between sounds, but are not periodical.

```
[[92 20 71]
 [ 9 92 6]
 [ 4 2 31]]
```

III.2.2. Normal heartbeats identification

We created a CNN that selects the normal heartbeats from the others. The training accuracy resulted was 97,74%. The value of the loss function and the accuracy on the test dataset are the following:

Test loss: 2.9659911798774647

Test accuracy: 55.65749240942323

The resulted confusion matrix can show us that the accuracy for the normal heatbeats classified as normal increased compared to the multi-class CNN, but the other sounds have a small accuracy.

```
[[ 93 133]
 [ 12 89]]
```

In the Classifying Heart Sounds PASCAL Challenge the results on the two datasets are: 46% and 77%, while we obtained a 55% on the combined datasets.

III.2.3. Murmur heartbeats identification

For identifying murmur heartbeats from the other types, we trained a CNN. The training accuracy resulted was 98,96%. The value of the loss function and the accuracy on the test dataset are the following:

Test loss: 1.2620686471279972

Test accuracy: 79.81651379792332

The resulted confusion matrix can show us that the accuracy for the murmur heartbeats classified as normal decreased compared to the multi-class CNN, but the other sounds have a good result.

```
[[ 62 14]
 [ 52 199]]
```

In the Classifying Heart Sounds PASCAL Challenge the results on the two datasets are: 67% and 37%, while we obtained a 79% on the combined datasets.

III.2.4. Extrastole heartbeats identification

For the extrastole identification, we used an AdaBoost classifier that uses as training data the features explained in the previous chapter. The test accuracy we obtained is:

Test accuracy: 0.7003154574132492

The resulted confusion matrix can show us that the accuracy for the extrastole heartbeats classified correct, decreased compared to the multi-class CNN, but the other sounds have a good result.

```
[[ 19 10]
 [ 85 203]]
```

In the Classifying Heart Sounds PASCAL Challenge the results on the two datasets are: 27% and 67%, while we obtained a 70% on the combined datasets.

III.3. Contributions

Some attempts to segment phonocardiograms (PCG) into heartbeats can be found in the literature. The characteristics of the PCG signal and other features such as heart sounds S1 and S2 location can be measured more accurately by digital signal processing techniques. We normalized the data using the L^2 norm and used a sliding window technique for which we used a peak detection algorithm.

In this thesis we extracted 11 features from time domain, frequency domain and statistical features that have potential to discriminate among the extrastole and other(normal and murmur) signals. Then we create models that we used in classification (CNN) and for the multi-task learning (CNN and AdaBoost). We compared the results with the ones presented in the Classifying Heart Sounds PASCAL Challenge and we present all the results in the corresponding chapter.

IV. Conclusion

In this paper, we present a methodology for the Classifying Heart Sounds PASCAL Challenge. We propose an algorithm for S1 and S2 heart sound identification. We normalized the data using the L^2 norm and used a sliding window technique for which we used a peak detection algorithm. The models we used in classification are CNN and Adaboost. After the segmentation, we used two methods to train and classify the computed features into Normal, Murmur or Extrasystole (Extrasound).

We think this is a good basis for further analysis of the heart sound signals. In future, the proposed method can also be implemented in latest mobile phones and can be used for early detection of some common heart diseases. This method would be extremely useful for the developing countries and for rural health management.

The characteristics of the PCG signal and other features can be measured more accurately by digital signal processing techniques. We think we can improve our method by improving the correct identification of S1 and S2 in the segmentation and by finding new features that take advantage of this identification. As future improvement the FFT (Fast Fourier Transform) can provide a better understanding of the frequency contents of the heart sounds. An alternative way to analyse the non-stationary signals is the wavelet transform (WT). Despite its medical significance, developing signal processing techniques with great impact can be an application for machine learning.

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