Motif Counting Algorithm

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Abstract

This report aims to describe the algorithm used to count all the motifs of a graph in an Optimal manner. The algorithm is optimal in the sense that each motif is only counted once, resulting in an algorithm that is linear in the number of motifs in the graph. The algorithm takes advantage of the combinatorics of the 3- and 4-motifs to explicitly iterate over them. This report further describes the new c++ kernel that has been implemented to facilitate work on large graphs, which can run both on CPU and GPU devices.

This report presents a top-down approach to the algorithm and the theory behind it.

All the code described in this report can be found as an open source library at the $GitHub\ repository^1$.

¹https://github.com/oricc/graph measures

Contents

1	Alge	orithm Description	3
	1.1	The Short Version	3
	1.2	Overview	3
	1.3	Motif combinatorics	3
	1.4	Subtree Construction	5
	1.5	Motif Counting	6
		1.5.1 Motif Counter updating	6
		1.5.2 3-Motif building algorithms	7
		1.5.3 4-Motif Building algorithms	9
	1.6	9 9	12
	1.7	Motif Visualization	14
2	C+-	+ Kernel	15
	2.1	Overview	15
	2.2	Algorithm changes	15
		2.2.1 Graph Format	15
		2.2.2 Removal Index	16
			16
	2.3	<u> </u>	17
	2.4		17
	2.5	Future work	18
\mathbf{A}	Con	abinatorical functions	19
	A.1	Permutations	19
	A.2	Combinations	19
В	Mot	if variations	20
	B.1	3-Motif Variations	20
		B.1.1 Undirected	20
		B.1.2 Directed	20
	B.2	4-Motif Variations	21
		B.2.1 Undirected	21
		B.2.2 Directed	21
т 1		C Almonialismo	
L	IST (of Algorithms	
	1	Motif Counter Overview	4
	2	Create Node Subtree for 3-motifs	6
	3	Create Node Subtree for 4-motifs	6
	4	Updating Motif Counters	7
	5	Motif 3 builders	8
	6	•	10
	7	±	11
	8	Motif to number representation	14

1 Algorithm Description

1.1 The Short Version

This section aims to describe the essence of the algorithm without going into the details, for those who are only interested in a high level view.

There are three main principles in the algorithm:

- 1. **Divide and conquer**. As we discussed above, we sort the nodes by their degree, from the node with the highest degree to that with the lowest. This allows us to quickly separate the graph into smaller, unconnected sub-graphs.
- 2. **Known motif structure.** As we can see in figure 2, we can list all of the options for the different motif structures. The algorithm is build so that it enumerates all the motifs of a certain structure before moving on to the next one, allowing us to make assumptions about the next motifs we should count.
- 3. Conditions to stop double-counting. Following the previous principle, we can make assumptions about the order in which the motifs are counted, and so we can write specific conditions that stop the code from counting certain motifs twice.

All motif building algorithms are a combination of these principles, allowing us to efficiently count all motifs in a graph. The rest of this report describes the algorithms with all details.

1.2 Overview

There are two main ideas implemented in this algorithm.

The first is that of explicit counting - since we know all the possible ways a motif can look, we can iterate over them directly, thus enabling us to enumerate all of them in an efficient fashion, both in memory and in time.

The second is the well known concept of divide and conquer. We use this concept by removing from the graph each node we have gone over. This concept is strengthened by a simple preprocessing of the graph, sorting all the nodes by their degree from highest to lowest. Having the nodes sorted in this way allows us to deal with the "heavier" nodes (the ones with a higher degree) first, and in so doing break up the graph into smaller, independent sub-graphs.

These two ideas give us the general shape of the algorithm, which can be seen, from above, as an iteration over the sorted nodes.

The *CreateNodeSubtree* function is where most of the hard work occurs, as that is the function where the actual motif counting is performed.

1.3 Motif combinatorics

Counting all motifs containing a given node is done using a **breadth first** approach. For each motif, we can define a *depth*. The depth of a motif is

Algorithm 1 Motif Counter Overview

```
\mathbf{function}\ \mathrm{Motif}\,\mathrm{Counter}(g,level)
```

```
 > g \text{ is a graph (either directed or undirected)} 
 > level \text{ is either 3 or 4, the level of motif to count} 
 \textbf{global } motif Counter \leftarrow \text{ list of motif counters} 
 > A \text{ motif counter is a dictionary containing a counter for each motif } sortdNodes \leftarrow \text{g.vertices} 
 \text{sort } sortedNodes \text{ by node degree} 
 \textbf{for } node \text{ in } sortedNodes \text{ do} 
 \textbf{if } level == 3 \textbf{ then} 
 \text{CREATENODESUBTREE3}(g,node) 
 \textbf{else} 
 > \text{level is 4}
```

CREATENODESUBTREE4(g, node)

end if

g.remove(node)

▶ We remove the node after iterating over it so as to not repeat the motifs that were already seen.

end for end function

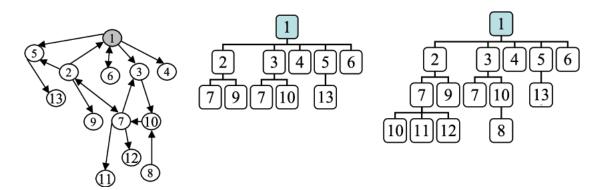


Figure 1: Node order

This figure describes the order of counting all motifs with node 1, which is also the node with the highest rank and so is the first node to be the root for motif counting.

From left to right: the graph itself, the order of counting 3-motifs and the order of counting 4-motifs.

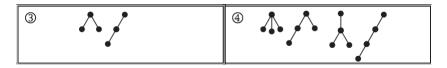


Figure 2: 3- and 4-motif variations From left to right: 3-motif of depths 1 and 2, 4-motifs of depth 1, 2 (option 1), 2 (option 2), and 3.

defined as the distance of the furthest vertex in the motif from the root node. This can also be though of as the furthest ring of neighbors that needs to be accessed to build the motif (for example, for a motif a depth 2 we must first select a vertex from the root's first neighbors, and then proceed to selecting a node from that vertex's neighbors, totaling two neighbor rings that we needed to see to build the motif). The second view is the one employed by us in implementing this algorithm. We separate the motifs by their depth and count all motifs of the same depth together.

It is obvious that the depth of a motif is bound by the number of nodes in the motif:

- A 3-motif can only be of depth 1 or 2
- A 4-motif can be of depth 1,2 (with two variations) or 3

In order to count all of the motifs of a certain depth, we must understand how each motif looks.

It can be seen that we can easily iterate over the necessary neighbors (whether they are first degree or second degree neighbors) to construct all the possible motifs containing the root vertex.

1.4 Subtree Construction

A *subtree* is considered to be the vicinity of the node where motifs containing is could appear. The *CreateNodeSubtree* is responsible for going over all the possible depths and counting all the motifs in each. For readability, we have separated the depths into separate functions.

It is important to note that when we say we iterate over all of a node's neighbors, we iterate over the neighbors in the *full graph*, i.e. we consider both the vertices connected to the node and the ones the node is connected to (which, in a directed graph, are not equivalent).

Algorithm 2 Create Node Subtree for 3-motifs

```
function CreateNodeSubtree3(g,root)

 > g \text{ is a graph (either directed or undirected)} 
 > root \text{ is the vertex that must be in all motifs} 
for n_1 in root's neighbors do

Mark that we saw n_1
end for

Count3MotifsDepth2(g,root)
Count3MotifsDepth1(g,root)
end function
```

Algorithm 3 Create Node Subtree for 4-motifs

```
function CreateNodeSubtree4(g,root)

\Rightarrow g is a graph (either directed or undirected)

\Rightarrow root is the vertex that must be in all motifs

for n_1 in root's first neighbors do

Mark n_1 as seen at level 1

end for

Count4MotifsDepth1(g,root)

Count4MotifsDepth2(g,root)

Count4MotifsDepth3(g,root)

end function
```

1.5 Motif Counting

1.5.1 Motif Counter updating

While each is slightly different, all motif counting function are essentially the same.

All of these functions, broadly speaking, have similar behavior:

- Iterate over all the motifs of the specified depth that you can build
 - For each of those motif update the relevant motif counters

The way of iterating over the motifs is the main difference between each of the functions.

Updating the motif counters is done by calculating the motif index (as discussed in the next section), and is relatively straightforward:

Algorithm 4 Updating Motif Counters

```
      function
      UPDATEMOTIFCOUNT(g,motif)

      > g is a graph (either directed or undirected)

      > motif is the motif that is being updated

      motifIndex \leftarrow GETMOTIFINDEX(g,motif)

      for n doode in motif

      motifCounters[node][motifIndex] + +

      end for

      end function
```

1.5.2 3-Motif building algorithms

As we discussed in the previous section, 3-motifs can only be of depth 1 or 2. For both depths, we know what their form looks like:

- A 3-motif of depth 1 must be the root node connected to two of it's first neighbors.
- A 3-motif of depth 2 can only be the root, a first neighbor and a second neighbor.

Algorithm 5 Motif 3 builders

```
function COUNT3MOTIFSDEPTH2(g,root)
                                  \triangleright g is a graph (either directed or undirected)
                                 \triangleright root is the vertex that must be in all motifs
   for n_1 in root's neighbors do
       for n_2 in n_1's neighbors do
           if n_2 is a neighbor of root's then
              if we saw n_1 before n_2 then
                                                      ▶ Count the pair only once
                   UPDATEMOTIFCOUNT(g,[root,n_1,n_2])
               end if
           else
               Mark that we saw n2
               UPDATEMOTIFCOUNT(g,[root,n_1,n_2])
           end if
       end for
   end for
end function
function COUNT3MOTIFSDEPTH1(g,root)
                                  \triangleright g is a graph (either directed or undirected)
                                 \triangleright root is the vertex that must be in all motifs
   neighborCombinations \leftarrow all 2-combinations of root's neighbors
   {f for} \ tuple \ {f in} \ neighborCombinations \ {f do}
       n_1 \leftarrow tuple.first
       n_2 \leftarrow tuple.second
       if we saw n_1 before n_2 and they aren't neighbors then
 \triangleright We only want to count (n_1, n_2) once, and if they are neighbors, we would
                                have discovered the motif as a motif of depth 2
           UPDATEMOTIF COUNT (g, [root, n_1, n_2])
       end if
   end for
end function
```

1.5.3 4-Motif Building algorithms

Like 3-motifs, we can separate the different 4-motifs into groups by their respective depths $\frac{1}{2}$

- **Depth 1** are 4- motifs constructed from the root and three of it's first neighbors
- ullet **Depth 2** can be one of two options:
 - The root, two of it's first neighbors and one of it's second neighbors (which is a neighbor of one of the first neighbors)
 - The root, one first neighbors, and two second neighbors who are connected to the first neighbor.
- **Depth 3** can only be a chain of the root, and a first, second and third neighbors.

```
Algorithm 6 Motif 4 depth 1 and 2 builders
```

```
function Count4MotifsDepth1(g,root)
                                   \triangleright g is a graph (either directed or undirected)
                                  \triangleright root is the vertex that must be in all motifs
    neighborCombinations \leftarrow all 3-combinations of root's neighbors
    for tuple in neighborCombinations do
       n_{11} \leftarrow tuple.first
       n_{12} \leftarrow tuple.second
       n_{13} \leftarrow tuple.third
       UPDATEMOTIFCOUNT(g,[root, n_{11}, n_{12}, n_{13}])
    end for
end function
function COUNT4MOTIFSDEPTH2(g,root)
                                   \triangleright q is a graph (either directed or undirected)
                                  \triangleright root is the vertex that must be in all motifs
    for n_1 in root's neighbors do
       for n_2 in n_1's neighbors do
           if n_2 was not seen at level 1 then
               \mathbf{Mark} \ n_2 as seen at level 2
         ▶ Motifs of the form root, two first neighbors and a second neighbor
           for n_{11} in root's neighbors do
               if n_2 was seen at level 2 and n_1 \neq n_{11} then
                   edgeExists \leftarrow (n_2, n_{11}) \in E or (n_{11}, n_2) \in E
                   if not edgeExists or (edgeExists and n_1 < n_{11}) then
                                       \triangleright If there is an edge between n_1 and n_{11},
                                       we would have already counted the motif
                                   as a motif of depth 2. If no such edge exists,
                                           we only want to count the motif once.
                       UPDATEMOTIFCOUNT(g,[root, n_1, n_{11}, n_2])
                   end if
               end if
           end for
       end for
    end for
        ▶ Motifs of the form root, a first neighbors and two second neighbors
    secondNeighborCombinations \leftarrow \text{all 2-combinations of } n_1's neighbors
    for combination in secondNeighborCombinations do
       n_{21} \leftarrow secondNeighborCombinations.first
       n_{22} \leftarrow secondNeighborCombinations.second
       if n_{21} and n_{22} were seen at level 2 then
      ▷ If both nodes were seen at level 2 then the motif wasn't counted as a
                                                                      depth 1 motif
           UPDATEMOTIF COUNT (g, [rot, n_1, n_{21}, n_{22}])
       end if
    end for
end function
```

Algorithm 7 Motif 4 depth 3 builder

```
function Count4MotifsDepth3(g,root)
                                                     \triangleright g and root are as before
   for n_1 in root's neighbors do
       for n_2 in n_1's neighbors do
          if n_2 was seen at level 1 then
          \triangleright If n_2 was seen at level 1 then we can't complete a depth-3 motif
              continue
          end if
          for n_3 in n_2's neighbors do
              if n_3 was not seen yet then
                  Mark n_3 as seen at level 3
                  if n_2 was seen at level 2 then
                     UPDATEMOTIFCOUNT(g,[root, n_1, n_2, n_3])
                  end if
              else
                  if n_3 was seen at level 1 then
                   ▷ This motif was already counted as a depth-1 or -2 motif
                     continue
                  end if
                  edgeExists \leftarrow (n_1, n_3) \in E or (n_1, n_3) \in E
                 if n_3 was seen at level 2 and not edgeExists then
                                        ▶ If an edge exists we already counted
                                            this motif as a depth-1 or -2 motif
                     UPDATEMOTIFCOUNT(g,[root, n_1, n_2, n_3])
                  end if
                 if n_3 was seen at level 3 and n_2 was seen at level 2 then
                     UPDATEMOTIFCOUNT (g, [root, n_1, n_2, n_3])
                  end if
              end if
          end for
       end for
   end for
end function
```

1.6 Motif representation

Another important idea contributing to the efficiency of this method is that we can generate a list of all possible motifs and their corresponding isomorphisims beforehand. We can then build a list of all motifs and the motif index they correspond to, and access that list at run-time. The full list can be found in appendix B

In order to build such a list we must be able to represent each motif in a fashion that is both unique and concise. The representation we use is that of a bit array of adjacency. Since each motif contains only 3 or 4 nodes, we can build a miniature adjacency matrix which represents the motif. If we then read the matrix as a single string of bits and convert it to an unsigned int - we have effectively represented the motif using a single, easy to interpret, number.

There are two important points to note about this representation method:

- The connections between a node and itself is not considered when transforming the adjacency matrix of the motif into a number. The reason for that is simply that we assume we are dealing with a graph **without self-loops**. As this is a common assumption, it is considered legitimate in this case.
- The way of building the adjacency matrix for directed and undirected graphs is slightly different. While for a motif in a directed graph a link of $a \to b$ does not necessarily imply a connection in the other direction $(b \to a)$, In an **undirected** graph we do know this, and therefor can limit ourselves to writing only *half* of the adjacency matrix.

Algorithmically, this distinction is implemented by using different combinatorical functions.

- For a directed graph we use the *permutations* function
- For an undirected graph we use the *combinations* function.

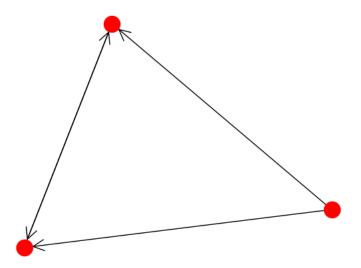
For a further explanation about these functions, refer to Appendix A.

The Transformation itself consists of 4 steps.

- 1. The motif must be transformed into it's adjacency matrix.
- 2. The matrix is flattened into a bitstring.
- 3. The bitstring is read as an unsigned int representation and transformed into such a number.
- 4. The number is then looked up in the variations table to find the corresponding motif index.

The motif indices and their variations can be found in Appendix B.

Motif with index 10



$$matrix = \left(\begin{array}{ccc} - & 1 & 1 \\ 0 & - & 1 \\ 0 & 1 & - \end{array} \right) \Rightarrow bitstring = 110101 \Rightarrow number = 53 \Rightarrow index = 10$$

Figure 3: Motif to number transformation example An example of the entire motif transformation, from the motif to it's corresponding index.

Algorithm 8 Motif to number representation

```
function GetMotifIndex(g, motif)
                                   \triangleright g is a graph (either directed or undirected)
                                  \triangleright motif is the motif that is being represented
    edges is an empty list of booleans
   if g is directed then
       options \leftarrow permutations(motif)
    else
       options \leftarrow combinations(motif)
   end if
   for tuple in options do
       n_1 \leftarrow tuple.first
       n_2 \leftarrow tuple.second
       neighbors \leftarrow whether n_1 and n_2 are neighbors in g
       append neighbors to edges
    end for
   motifNumber \leftarrow the unsigned int represented by edges
   motifIndex \leftarrow the index corresponding to the motif number
             ▶ The index is read from the index file we created ahead of time
    {f return} \ {f motifIndex}
end function
```

1.7 Motif Visualization

To assist with both understanding and debugging, a motif visualization script was written. The script can be found under the measure_tests directory with the name draw_motifs.py.

Running the script is simply a matter of changing the values given in the main section on the bottom of the script. The scripts outputs an image using networkx and matplotlib of the motif with the given index. You can also change the motif level and toggle whether the graph is directional. An example output is the motif given in figure 1.

2 C++ Kernel

2.1 Overview

As we have reached the optimal algorithmic performance of motif counting (we count each motif only once), in order to facilitate analyzing motifs in larger graphs, we must write faster **code**.

Previously, the code to count the motifs has been written in Python. Python, while easy to use and develop code in, is inherently slow, as the language itself is interpreted. Faster code performance is obtained through the use of code in C++, both running on the CPU and on the GPU. Running the algorithms using a C++ kernel requires two additional changes:

- 1. The graph must be saved in a LIL (List of Lists) format.
- 2. The algorithm must be modified so as to that the nodes are not actually removed from the graph, as that is inefficient using this format.

2.2 Algorithm changes

2.2.1 Graph Format

In the C++ kernel, the graph is saved using a graph format which is commonly used for sparse graph, but can be used to our advantage in this case.

As our format is aimed at increasing the efficiency of our code by leveraging the computer's internal cache mechanism, we call this structure a CacheGraph.

The CacheGraph is composed of two arrays:

- 1. An array which is composed of all the neighborhood lists placed back to back (Neighbors).
- 2. An array which holds the starting index of each node's neighbor list (Indices).

There follows an example of the conversion routine for a simple graph. The given graph is the one composed of these edges: (0->1, 0->2, 0->3, 2->0, 3->1, 3->2).

The behavior of the conversion now depends on whether the graph is directed or undirected.

- If the graph is directed, the result is as follows: Indices: [0, 3, 3, 4, 6], Neighbors: [1, 2, 3, 0, 1, 2]
- Else, the results for the undirected graph are: Indices: [0, 3, 5, 7, 10], Neighbors: [1, 2, 3, 0, 3, 0, 3, 0, 1, 2]

The CacheGraph object is designed around the principle of cache-awareness. The most important thing to remember when accessing the graph in the C++ code is that we are aiming to accelerate the computations by loading sections of the graph into the cache ahead of time for quick access. When using the CacheGraph, this comes into effect when we iterate over the offset vector first

and then access the blocks of neighbor nodes in the graph vector. By doing this, we are pulling the entire list of a certain node's neighbors into the cache, allowing us to iterate over them extremely quickly.

A concrete example of a good use and bad use case of the CacheGraph are the two popular search strategies BFS and DFS. When using BFS we are utilizing the full power of the cache-aware storage mechanism by pulling in the entire list of a node's neighbors to be processed at once, which is fast due to the fact that the neighbors are in the cache. In contrast, when using DFS, we are not going over all of a node's neighbors at once but jumping from one node to the other, which completely nullifies the speed advantage that the cache can give us, as the contents of the cache need to be constantly swapped out by the processor.

2.2.2 Removal Index

One disadvantage of the CacheGraph is that it can't be modified at runtime, as that is an extremely costly operation. Instead, we will hold an array where each node has a corresponding "removal index", which will be the first iteration where the node no longer exists in the graph. As the algorithm removes each node immediately after it iterates it's subtree, computing the removal indices of all nodes is simply a matter of "flipping" the list which contains the order in which the nodes will be traversed, i.e. the nodes as ordered by their degree. "Flipping" the list entails saving each node's position in the nodes list as the value corresponding to that node in the removal indices array.

For example, if the nodes were traversed in this order: [2,0,1], then the corresponding removal indices array will be [1,2,0] (i.e. node 0 is removed at iteration 1, node 1 at iteration 2, etc.)

We now need to further modify our code to check each node we use, to verify that it's removal index of the node is lower than the removal index of the root of the current subtree.

2.2.3 GPU Changes

To further accelerate the motif counting code, a version of it was written for the GPU using the CUDA library. Writing the code for the GPU means that we will run all of the motif subtree calculations for each node in parallel, which in turn means we must be able to run each of those calculations independently of the others. Luckily, using the removal indices we can already make the subtrees independent of one another, as the removal indices were pre-computed.

As the programming model we can use on the GPU itself is quiet limited (in essence, we are restricted to basic C code i.e. we must use the malloc and free function together with pointers), and as we want to limit the amount of memory used, we must make further modifications to the code.

1. **GPU functions** are written outside the main bodies of code (MotifCalculator,MotifUtils, CacheGraph), as they cannot be member functions. They are instead re-written as stand-alone functions within the file.

- 2. Global variables are used to communicate between the class methods, which provide the CPU-side pre- and post-processing of the results, and the GPU functions.
- 3. **Atomic add** is used to update the motif counters, so that the GPU threads won't interfere with one another.
- 4. **All data** which is used in the GPU must be copied into GPU memory. Additionally, the data is prefetched asynchronously to improve the code's performance.
- 5. Visited vertices (which saves which nodes were already visited) is no longer a map, as those can't be used in the GPU. Instead, it is an matrix of size n^2 in which each row corresponds to one node. The type of the matrix changes depending on the motif level. For level 3 a matrix of booleans is used, and for level 4 a matrix of short ints.
- 6. No vectors can be used in the GPU. In order to provide a unified interface, CPU code at the end of the calculation converts the feature from a matrix to the vector of vectors returned by the CPU motif calculator.

2.3 GPU requirements

In order to run the GPU code, some requirements must be met, in both software and hardware.

- The GPU must be an NVIDIA GPU of compute capability 3.5 or higher.
- Version 8.0 of the CUDA Toolkit must be installed and in the PATH of the system. Higher versions may work, but were not tested.
- The GPU drivers must be compatible with the CUDA Toolkit.

Specifically, the code was tested on a system with the following specs:

- Centos 7 Linux distribution
- A GeForce GTX 1080 Ti with compute capability 6.1
- CUDA Toolkit version 8.0
- GPU drivers version 396.26

2.4 Performance comparison

The C++ kernel gives us code that runs several times faster than the original python code, and the GPU version gives us an additional 10X factor on top of the regular C++ code. Below are graph comparing the run-time of the various kernels on Erdos-renyi graphs of varying size. Figures 1 & 2 show the comparisons between the various kernels.

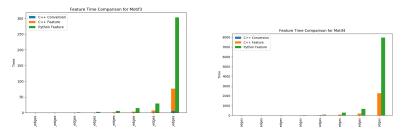


Figure 4: Run time comparison for python/C++ kernels

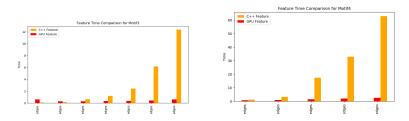


Figure 5: Run time comparison for C++/GPU kernels

2.5 Future work

We are yet to implement one variation of the motif code (which exists in python). This variation is that of counting motifs for edges, rather than nodes.

This change requires minimal work, as the bulk of the code is already written for the node-based motif algorithm. Basically, the algorithm must accept the motifs found by the subtree functions and update the counters for each edge in the motif.

Further work could also include an implementation of the algorithm with the nodes used in chunks. Some of the time limitations we are faced with today could be solved if the code could be run on several CPUs/GPUs together. In order to enable this, the algorithm must be able to divide the nodes into smaller groups, perform the algorithm on each group and combine the results. This step is not as trivial as it seems, as it requires coordination between the different groups so that motifs are not double counted.

A Combinatorical functions

A.1 Permutations

The *permutations* function is used to create all the possible tuples of a given size which are comprised of elements of the original set **with respect to order**. In our case we only use 2-permutations, which give us all the possible edges that can exist between a given set of nodes.

For example, assume our motif is comprised of nodes 1,2 and 3. The possible 2-permutations in this case would be:

$$perm(\{1,2,3\}) = \{(1,2), (1,3), (2,1), (2,3), (3,1), (3,2)\}$$

And since the order matters, we can see that, for example, both (1,2) and (2,1) appear in the resulting list.

A more intuitive way to view this function, and the one employed by us, is as looking at all of the elements of a matrix, without the main diagonal:

$$\begin{array}{cccc} 0 & X & X \\ X & 0 & X \\ X & X & 0 \end{array}$$

Where X is an element accessed by the permutations, 0 is one which was not.

A.2 Combinations

The *combinations* function is very similar to the *permutations* function in that it gives us a list of tuples derived from the original sets, but differs from it in that it **does not respect order**, and so only gives us a single instance of each tuple:

$$comb(\{1,2,3\}) = \{(1,2),(1,3),(2,3)\}$$

In the context of adjacency matrices, the function only iterated over the top half of the matrix:

$$\begin{array}{cccc} 0 & X & X \\ 0 & 0 & X \\ 0 & 0 & 0 \end{array}$$

B Motif variations

A core part of this algorithm is it's ability to use a precomputed table of the various motif variations and their corresponding motif index. As was discussed, each motif is represented using a single integer which is read from it's representing bit matrix. The following tables map each such integer to a "motif index", which is shared among all isomorphic motifs.

There are four tables in total, for 3- and 4-motifs in both directed and undirected cases. The code for generating these tables, along with pickle files containing the dictionaries which can be used in the python code can be found in the GitHub repository².

The actual implementation of the tables is reverse than the one displayed here. In the code, each motif number is mapped to it's index for quick access. The following tables are meant for quick reference and some examples, and so each index is mapped to all of the motif numbers corresponding to it.

B.1 3-Motif Variations

B.1.1 Undirected

0	3,5,6
1	7
None	0,1,2,4

B.1.2 Directed

0	3,12,48
1	6,9,17,24,34,36
2	7,13,19,44,50,56
3	10,20,33
4	11,14,28,35,49,52
5	15,51,60
6	21,22,26,37,41,42
7	23,45,58
8	25,38
9	27,29,39,46,54,57
10	30,43,53
11	31,47,55,59,61,62
12	63
None	0,1,2,4,5,8,16,18,32,40

 $^{^2} https://github.com/oricc/graph_measures/tree/master/features_algorithms/motif_variations$

B.2 4-Motif Variations

B.2.1 Undirected

0	7,25,42,52
1	13,14,19,22,26,28,35,37,41,44,49,50
2	15,23,27,29,39,43,46,53,54,57,58,60
3	30,45,51
4	31,47,55,59,61,62
5	63
None	0,1,2,3,4,5,6,8,9,10,11,12,16,17,18,20,21,24,32,33,34,36,38,40,48,56

B.2.2 Directed

0	7,56,448,3584
1	14,49,69,168,336,386,515,1048,1792,2240,2592,3076
2	15,57,71,184,450,464,519,1080,2496,3588,3616,3840
3	21,28,35,42,112,134,196,224
	259,280,321,392,560,896,1030,1344
	1538,1552,2053,2088,2561,2688,3080,3136
4	22,38,50,52,104,133,261,296
	328,352,385,388,536,704,1027,1216
	1600,1664,2051,2072,2568,2576,3073,3074
5	23,39,58,60,120,135,263,312
	449,452,456,480,568,960,1031,1472
	2055,2104,3585,3586,3592,3600,3648,3712
6	29,43,198,240,323,408,1542,1584,2565,2944,3112,3392
7	30,46,51,53,197,232,325,344
	368,387,390,424,1539,1560,1856,1920
	2563,2600,2608,2752,3077,3078,3096,3264
8	31,47,59,61,199,248,327,440
	451,454,472,496,1543,1592,2567,3008
	3128,3520,3589,3590,3624,3632,3904,3968
9	54,360,389,1728,2584,3075
10	55,62,376,391,453,488,1984,2616,3079,3587,3608,3776
11	63,455,504,3591,3640,4032
12	76,161,274,522,577,800,1041,1160,1284,2084,2128,2178

13	77,78,169,177,338,402,523,526
	579,581,1049,1073,1176,1192,1796,1824
	2242, 2256, 2384, 2434, 2596, 2848, 3108, 3332
14	79,185,466,527,583,1081,1208,2498,2512,3620,3844,3872
15	84,97,140,162,266,273,529,546
	642,672,769,784,1034,1044,1092,1104
	1282,1288,2060,2081,2113,2144,2180,2184
16	85,113,142,170,337,394,547,561
	771,898,1038,1052,1304,1360,1794,1808
	2117,2216,2244,2272,2593,2720,3084,3140
17	86,105,141,178,330,401,537,550
	706,773,1035,1076,1232,1320,1604,1696
	2115,2200,2400,2436,2572,2832,3105,3330
18	87,121,143,186,458,465,551,569
	775,962,1039,1084,1336,1488,2119,2232
	2500,2528,3596,3617,3652,3744,3842,3856
19	92,163,204,225,275,282,554,816
	833,928,1045,1286,1348,1416,1546,1553
	2085,2092,2160,2182,2625,2690,3152,3208
20	93,171,206,241,339,410,555,835
	$1053,\!1432,\!1550,\!1585,\!1798,\!1840,\!2246,\!2288$
	2597,2629,2946,2976,3116,3240,3396,3408
21	94,179,205,233,346,403,558,837
	1077,1448,1547,1561,1860,1952,2416,2438
	2604,2627,2754,2864,3109,3224,3280,3334
22	95,187,207,249,467,474,559,839
	1085,1464,1551,1593,2502,2544,2631,3010
	3256,3536,3621,3628,3846,3888,3908,4000
23	99,156,212,226,267,281,533,646
	688,912,1066,1094,1136,1346,1556,1570
	2061,2089,2369,2440,2692,2817,3168,3336

$\begin{array}{c} 608,641,648,776,1042,1089,1096,1154\\ 1156,1281,2058,2065,2068,2082,2120,2177 \\ \hline \\ 25 & 101,172,270,305,340,418,531,643\\ & 680,848,1050,1093,1112,1410,1793,1800\\ 2062,2097,2241,2248,2594,2656,3092,3204 \\ \hline \\ 26 & 102,180,269,297,354,404,534,645\\ & 664,720,1074,1091,1128,1218,1632,1668\\ & 2059,2073,2376,2433,2580,2824,3106,3329 \\ \hline \\ 27 & 103,188,271,313,468,482,535,647\\ & 699,976,1082,1095,1144,1474,2063,2105\\ & 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564\\ & 708,900,1059,1062,1248,1376,1602,1680\\ & 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ & 1067,1264,1574,1588,1606,1712,2371,2456\\ & 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ & 808,864,1043,1224,1285,1412,1601,1672\\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ & 1051,1240,1605,1704,1797,1832,2243,2264\\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ & 1075,1226,1603,1688,1888,1924,2392,2435\\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ & 1083,1272,1607,1720,2499,2520,2575,3024\\ & 3129,3522,3622,3636,3845,3880,3936,3972 \\ \hline \end{array}$	24	100,164,268,276,289,290,530,592
$\begin{array}{c} 1156,1281,2058,2065,2068,2082,2120,2177 \\ \hline \\ 25 & 101,172,270,305,340,418,531,643 \\ 680,848,1050,1093,1112,1410,1793,1800 \\ 2062,2097,2241,2248,2594,2656,3092,3204 \\ \hline \\ 26 & 102,180,269,297,354,404,534,645 \\ 664,720,1074,1091,1128,1218,1632,1668 \\ 2059,2073,2376,2433,2580,2824,3106,3329 \\ \hline \\ 27 & 103,188,271,313,468,482,535,647 \\ 696,976,1082,1095,1144,1474,2063,2105 \\ 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564 \\ 708,900,1059,1062,1248,1376,1602,1680 \\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ 1067,1264,1574,1588,1606,1712,2371,2456 \\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ 808,864,1043,1224,1285,1412,1601,1672 \\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ 1051,1240,1605,1704,1797,1832,2243,2264 \\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ 1075,1256,1603,1688,1888,1924,2392,2435 \\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 680,848,1050,1093,1112,1410,1793,1800 \\ 2062,2097,2241,2248,2594,2656,3092,3204 \\ \hline \\ 26 & 102,180,269,297,354,404,534,645 \\ 664,720,1074,1091,1128,1218,1632,1668 \\ 2059,2073,2376,2433,2580,2824,3106,3329 \\ \hline \\ 27 & 103,188,271,313,468,482,535,647 \\ 696,976,1082,1095,1144,1474,2063,2105 \\ 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564 \\ 708,900,1059,1062,1248,1376,1602,1680 \\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ 1067,1264,1574,1588,1606,1712,2371,2456 \\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ 808,864,1043,1224,1285,1412,1601,1672 \\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ 1051,1240,1605,1704,1797,1832,2243,2264 \\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ 1075,1256,1603,1688,1888,1924,2392,2435 \\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 680,848,1050,1093,1112,1410,1793,1800 \\ 2062,2097,2241,2248,2594,2656,3092,3204 \\ \hline \\ 26 & 102,180,269,297,354,404,534,645 \\ 664,720,1074,1091,1128,1218,1632,1668 \\ 2059,2073,2376,2433,2580,2824,3106,3329 \\ \hline \\ 27 & 103,188,271,313,468,482,535,647 \\ 696,976,1082,1095,1144,1474,2063,2105 \\ 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564 \\ 708,900,1059,1062,1248,1376,1602,1680 \\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ 1067,1264,1574,1588,1606,1712,2371,2456 \\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ 808,864,1043,1224,1285,1412,1601,1672 \\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ 1051,1240,1605,1704,1797,1832,2243,2264 \\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ 1075,1256,1603,1688,1888,1924,2392,2435 \\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$ \begin{array}{c} 2062,2097,2241,2248,2594,2656,3092,3204 \\ \hline \\ 26 & 102,180,269,297,354,404,534,645 \\ & 664,720,1074,1091,1128,1218,1632,1668 \\ & 2059,2073,2376,2433,2580,2824,3106,3329 \\ \hline \\ 27 & 103,188,271,313,468,482,535,647 \\ & 696,976,1082,1095,1144,1474,2063,2105 \\ & 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564 \\ & 708,900,1059,1062,1248,1376,1602,1680 \\ & 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ & 1067,1264,1574,1588,1606,1712,2371,2456 \\ & 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ & 808,864,1043,1224,1285,1412,1601,1672 \\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$	25	
$ \begin{array}{c} 26 & 102,180,269,297,354,404,534,645 \\ & 664,720,1074,1091,1128,1218,1632,1668 \\ & 2059,2073,2376,2433,2580,2824,3106,3329 \\ \\ \hline \\ 27 & 103,188,271,313,468,482,535,647 \\ & 696,976,1082,1095,1144,1474,2063,2105 \\ & 2497,2504,3604,3618,3680,3716,3841,3848 \\ \\ \hline \\ 28 & 106,114,149,150,329,393,540,564 \\ & 708,900,1059,1062,1248,1376,1602,1680 \\ & 2307,2309,2328,2344,2569,2704,3081,3138 \\ \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ & 1067,1264,1574,1588,1606,1712,2371,2456 \\ & 2573,2821,2948,2960,3113,3368,3394,3424 \\ \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ & 808,864,1043,1224,1285,1412,1601,1672 \\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 664,720,1074,1091,1128,1218,1632,1668\\ 2059,2073,2376,2433,2580,2824,3106,3329\\ \hline \\ 27 & 103,188,271,313,468,482,535,647\\ & 696,976,1082,1095,1144,1474,2063,2105\\ & 2497,2504,3604,3618,3680,3716,3841,3848\\ \hline \\ 28 & 106,114,149,150,329,393,540,564\\ & 708,900,1059,1062,1248,1376,1602,1680\\ & 2307,2309,2328,2344,2569,2704,3081,3138\\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ & 1067,1264,1574,1588,1606,1712,2371,2456\\ & 2573,2821,2948,2960,3113,3368,3394,3424\\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ & 808,864,1043,1224,1285,1412,1601,1672\\ & 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ & 1051,1240,1605,1704,1797,1832,2243,2264\\ & 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ & 1075,1256,1603,1688,1888,1924,2392,2435\\ & 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ & 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$		2062,2097,2241,2248,2594,2656,3092,3204
$\begin{array}{c} 664,720,1074,1091,1128,1218,1632,1668\\ 2059,2073,2376,2433,2580,2824,3106,3329\\ \hline\\ 27 & 103,188,271,313,468,482,535,647\\ & 696,976,1082,1095,1144,1474,2063,2105\\ & 2497,2504,3604,3618,3680,3716,3841,3848\\ \hline\\ 28 & 106,114,149,150,329,393,540,564\\ & 708,900,1059,1062,1248,1376,1602,1680\\ & 2307,2309,2328,2344,2569,2704,3081,3138\\ \hline\\ 29 & 107,157,214,242,331,409,541,710\\ & 1067,1264,1574,1588,1606,1712,2371,2456\\ & 2573,2821,2948,2960,3113,3368,3394,3424\\ \hline\\ 30 & 108,165,278,306,332,417,538,705\\ & 808,864,1043,1224,1285,1412,1601,1672\\ & 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline\\ 31 & 109,173,334,342,433,434,539,707\\ & 1051,1240,1605,1704,1797,1832,2243,2264\\ & 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline\\ 32 & 110,181,333,370,406,425,542,709\\ & 1075,1256,1603,1688,1888,1924,2392,2435\\ & 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline\\ 33 & 111,189,335,441,470,498,543,711\\ & 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$	26	102,180,269,297,354,404,534,645
$\begin{array}{c} 2059,2073,2376,2433,2580,2824,3106,3329\\ \hline \\ 27 & 103,188,271,313,468,482,535,647\\ & 696,976,1082,1095,1144,1474,2063,2105\\ & 2497,2504,3604,3618,3680,3716,3841,3848\\ \hline \\ 28 & 106,114,149,150,329,393,540,564\\ & 708,900,1059,1062,1248,1376,1602,1680\\ & 2307,2309,2328,2344,2569,2704,3081,3138\\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ & 1067,1264,1574,1588,1606,1712,2371,2456\\ & 2573,2821,2948,2960,3113,3368,3394,3424\\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ & 808,864,1043,1224,1285,1412,1601,1672\\ & 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ & 1051,1240,1605,1704,1797,1832,2243,2264\\ & 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ & 1075,1256,1603,1688,1888,1924,2392,2435\\ & 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ & 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$		664,720,1074,1091,1128,1218,1632,1668
$\begin{array}{c} 696,976,1082,1095,1144,1474,2063,2105\\ 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564\\ 708,900,1059,1062,1248,1376,1602,1680\\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ 1067,1264,1574,1588,1606,1712,2371,2456\\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 696,976,1082,1095,1144,1474,2063,2105\\ 2497,2504,3604,3618,3680,3716,3841,3848 \\ \hline \\ 28 & 106,114,149,150,329,393,540,564\\ 708,900,1059,1062,1248,1376,1602,1680\\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ 1067,1264,1574,1588,1606,1712,2371,2456\\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	27	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
$\begin{array}{c} 708,900,1059,1062,1248,1376,1602,1680\\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ 1067,1264,1574,1588,1606,1712,2371,2456\\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		2497,2504,3604,3618,3680,3716,3841,3848
$\begin{array}{c} 708,900,1059,1062,1248,1376,1602,1680\\ 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710\\ 1067,1264,1574,1588,1606,1712,2371,2456\\ 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$	28	106.114.149.150.329.393.540.564
$\begin{array}{c} 2307,2309,2328,2344,2569,2704,3081,3138 \\ \hline \\ 29 & 107,157,214,242,331,409,541,710 \\ & 1067,1264,1574,1588,1606,1712,2371,2456 \\ & 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ & 808,864,1043,1224,1285,1412,1601,1672 \\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 29 & 107,157,214,242,331,409,541,710 \\ & 1067,1264,1574,1588,1606,1712,2371,2456 \\ & 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline \\ 30 & 108,165,278,306,332,417,538,705 \\ & 808,864,1043,1224,1285,1412,1601,1672 \\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		
$\begin{array}{c} 1067,1264,1574,1588,1606,1712,2371,2456\\ 2573,2821,2948,2960,3113,3368,3394,3424\\ \hline \\ 30 & 108,165,278,306,332,417,538,705\\ 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ & 1051,1240,1605,1704,1797,1832,2243,2264\\ & 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ & 1075,1256,1603,1688,1888,1924,2392,2435\\ & 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ & 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$		
$\begin{array}{c} 2573,2821,2948,2960,3113,3368,3394,3424 \\ \hline 30 & 108,165,278,306,332,417,538,705 \\ & 808,864,1043,1224,1285,1412,1601,1672 \\ & 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$	29	107,157,214,242,331,409,541,710
$\begin{array}{c} 30 & 108,165,278,306,332,417,538,705 \\ 808,864,1043,1224,1285,1412,1601,1672 \\ 2086,2100,2136,2179,2570,2640,3089,3202 \\ \\ \hline 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \hline 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \hline 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$		1067, 1264, 1574, 1588, 1606, 1712, 2371, 2456
$\begin{array}{c} 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$		2573,2821,2948,2960,3113,3368,3394,3424
$\begin{array}{c} 808,864,1043,1224,1285,1412,1601,1672\\ 2086,2100,2136,2179,2570,2640,3089,3202\\ \hline \\ 31 & 109,173,334,342,433,434,539,707\\ 1051,1240,1605,1704,1797,1832,2243,2264\\ 2574,2598,2896,2912,3121,3124,3458,3460\\ \hline \\ 32 & 110,181,333,370,406,425,542,709\\ 1075,1256,1603,1688,1888,1924,2392,2435\\ 2571,2612,2768,2856,3097,3110,3266,3333\\ \hline \\ 33 & 111,189,335,441,470,498,543,711\\ 1083,1272,1607,1720,2499,2520,2575,3024\\ \hline \end{array}$	30	108 165 278 306 332 417 538 705
$\begin{array}{c} 2086,2100,2136,2179,2570,2640,3089,3202 \\ \hline \\ 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array}$	30	
$\begin{array}{c} 31 & 109,173,334,342,433,434,539,707 \\ & 1051,1240,1605,1704,1797,1832,2243,2264 \\ & 2574,2598,2896,2912,3121,3124,3458,3460 \\ \\ 32 & 110,181,333,370,406,425,542,709 \\ & 1075,1256,1603,1688,1888,1924,2392,2435 \\ & 2571,2612,2768,2856,3097,3110,3266,3333 \\ \\ 33 & 111,189,335,441,470,498,543,711 \\ & 1083,1272,1607,1720,2499,2520,2575,3024 \\ \end{array}$		
$ \begin{array}{c} 1051,1240,1605,1704,1797,1832,2243,2264 \\ 2574,2598,2896,2912,3121,3124,3458,3460 \\ \hline \\ 32 & 110,181,333,370,406,425,542,709 \\ 1075,1256,1603,1688,1888,1924,2392,2435 \\ 2571,2612,2768,2856,3097,3110,3266,3333 \\ \hline \\ 33 & 111,189,335,441,470,498,543,711 \\ 1083,1272,1607,1720,2499,2520,2575,3024 \\ \hline \end{array} $		2000,2100,2170,2173,2070,2040,3003,3202
2574,2598,2896,2912,3121,3124,3458,3460 32	31	109,173,334,342,433,434,539,707
32		1051,1240,1605,1704,1797,1832,2243,2264
33 111,189,335,441,470,498,543,711 1083,1272,1607,1720,2499,2520,2575,3024		2574,2598,2896,2912,3121,3124,3458,3460
33 111,189,335,441,470,498,543,711 1083,1272,1607,1720,2499,2520,2575,3024	32	110 181 333 370 406 425 542 709
33 111,189,335,441,470,498,543,711 1083,1272,1607,1720,2499,2520,2575,3024	~~	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		
1083, 1272, 1607, 1720, 2499, 2520, 2575, 3024		
	33	111,189,335,441,470,498,543,711
3129,3522,3622,3636,3845,3880,3936,3972		
		3129,3522,3622,3636,3845,3880,3936,3972
34 115,158,213,234,345,395,565,902	34	115 158 213 234 345 395 565 902
1070,1392,1564,1571,1858,1936,2373,2472	54	
2601,2736,2756,2819,3085,3142,3296,3352		
2001,2100,2100,2010,0000,0112,0200,0002		2001,2100,2010,0000,0112,0200,0002

35	116,166,277,298,353,396,562,736
30	
	792,897,1046,1220,1283,1352,1616,1666
	2076,2083,2152,2181,2577,2696,3082,3137
36	117,174,341,369,398,426,563,899
	1054,1368,1795,1816,1872,1922,2245,2280
	2595,2609,2728,2784,3086,3100,3141,3268
37	118,182,361,362,397,405,566,901
	1078,1384,1730,1732,1744,1760,2408,2437
	2585,2588,2712,2840,3083,3107,3139,3331
38	119,190,377,399,469,490,567,903
	1086,1400,1986,2000,2501,2536,2617,2744
	3087,3143,3612,3619,3780,3808,3843,3864
	, ., ,,,,,
39	122,151,457,572,964,1063,1504,2311,2360,3593,3650,3728
40	123,159,215,250,459,473,573,966
	1071,1520,1575,1596,2375,2488,2823,3012
	3384,3552,3597,3625,3654,3760,3906,3984
41	124,167,279,314,460,481,570,824
	961,992,1047,1287,1476,1480,2087,2108
	2168,2183,3594,3601,3649,3664,3714,3720
42	125,175,343,442,462,497,571,963
	1055,1496,1799,1848,2247,2296,2599,3040
	3132,3524,3598,3633,3653,3752,3920,3970
43	126,183,378,407,461,489,574,965
	1079,1512,1988,2016,2424,2439,2620,2872
	3111,3335,3595,3609,3651,3736,3778,3792
44	127,191,463,471,505,506,575,967
	1087,1528,2503,2552,3599,3623,3641,3644
	3655,3768,3847,3896,4034,4036,4048,4064
45	220,227,283,944,1350,1557,1578,2093,2694,2881,3184,3464
46	221,222,235,243,347,411,1565,1579
	1582,1589,1862,1968,2605,2758,2883,2885
	2950,2992,3117,3312,3398,3440,3480,3496
47	223,251,475,1583,1597,2887,3014,3512,3568,3629,3910,4016
48	228,284,291,624,904,1158,1345,1554,2069,2090,2689,3144

49	229,236,286,307,348,419,880,936
	1349,1414,1555,1562,1857,1928,2094,2101
	2602,2672,2691,2753,3093,3160,3206,3272
50	230,244,285,299,355,412,752,920
	1222,1347,1558,1586,1648,1670,2077,2091
	2581,2693,2945,2952,3114,3176,3393,3400
51	231,252,287,315,476,483,952,1008
"-	1351,1478,1559,1594,2095,2109,2695,3009
	3192,3528,3605,3626,3696,3718,3905,3976
52	237,350,435,1563,1861,1960,2606,2755,2928,3125,3288,3462
53	238,245,349,371,414,427,1566,1587
	1859,1904,1926,1944,2603,2613,2757,2800
	2947,2984,3101,3118,3270,3304,3397,3416
54	239,253,351,443,478,499,1567,1595
94	1863,1976,2607,2759,3011,3056,3133,3320
	3526,3544,3630,3637,3909,3952,3974,4008
	3020,3044,3000,3007,3000,3002,3074,4000
55	246,363,413,1590,1734,1776,2589,2949,2968,3115,3395,3432
56	247,254,379,415,477,491,1591,1598
	1990,2032,2621,2951,3000,3013,3119,3399
	3448,3560,3613,3627,3782,3824,3907,3992
57	255,479,507,1599,3015,3576,3631,3645,3911,4024,4038,4080
58	292,584,1153,2066
59	293,294,300,308,356,420,600,616
99	712,840,1155,1157,1217,1409,1608,1665
	2067,2070,2074,2098,2578,2632,3090,3201
	2001,2010,2014,2098,2318,2032,3090,3201
60	295,316,484,632,968,1159,1473,2071,2106,3602,3656,3713
61	301, 358, 436, 728, 1219, 1640, 1669, 2075, 2582, 2888, 3122, 3457
62	302,309,357,372,422,428,744,856
	1221,1411,1624,1667,1864,1921,2078,2099
	2579,2610,2664,2760,3094,3098,3205,3265
63	303,317,359,444,486,500,760,984
	1223,1475,1656,1671,2079,2107,2583,3016
	3130,3521,3606,3634,3688,3717,3912,3969
64	310,364,421,872,1413,1729,1736,2102,2586,2648,3091,3203
04	310,304,421,672,1413,1729,1730,2102,2380,2048,3091,3203

65	311,318,380,423,485,492,888,1000
	1415,1477,1985,1992,2103,2110,2618,2680
	3095, 3207, 3603, 3610, 3672, 3715, 3777, 3784
0.0	010 10 700 1010 1 1 70 0111 000 0010 0010 1010 1000 1010
66	319,487,508,1016,1479,2111,3607,3642,3704,3719,4033,4040
67	365,366,374,429,437,438,1731,1733
	1752,1768,1896,1925,2587,2590,2614,2776
	2904,2920,3099,3123,3126,3267,3459,3461
68	367,445,502,1735,1784,2591,3032,3131,3523,3638,3944,3973
69	373,430,1880,1923,2611,2792,3102,3269
70	375,381,431,446,494,501,1912,1927
	1987,2008,2615,2619,2808,3048,3103,3134
	3271,3525,3614,3635,3781,3816,3928,3971
71	382, 439, 493, 1989, 2024, 2622, 2936, 3127, 3463, 3611, 3779, 3800
72	383,447,495,503,509,510,1991,2040
	2623,3064,3135,3527,3615,3639,3643,3646
	3783,3832,3960,3975,4035,4037,4056,4072
70	M11 0047 4000 4000
73	511,3647,4039,4088
74	585,586,588,804,1161,1169,1185,1316,2130,2194,2322,2340
75	587,589,590,1177,1193,1201,1828,2258,2386,2450,2852,3364
76	591,1209,2514,3876
77	593,609,650,673,778,786,801,802
	1100,1105,1162,1164,1292,1297,1298,1300
	2124,2129,2132,2148,2186,2209,2210,2212
78	594,612,649,780,1097,1170,1188,1313,2122,2193,2324,2338
79	595,613,651,681,782,850,1101,1113
	1178,1196,1329,1426,1804,1825,2126,2225
	2250,2257,2388,2466,2660,2850,3236,3348
80	596,610,652,657,658,676,777,788
	1098,1106,1121,1124,1172,1186,1289,1314
	2121,2146,2185,2196,2314,2316,2321,2337
81	597,611,654,689,779,914,1102,1137
01	1180,1194,1305,1362,1812,1826,2125,2217
	2260,2274,2385,2442,2724,2849,3172,3340

82	598,614,653,665,722,781,1099,1129
	1202,1204,1234,1321,1636,1700,2123,2201
	2378,2402,2449,2452,2828,2836,3361,3362
0.0	FOO C1F CFF COM TOO ONO 1100 114F
83	599,615,655,697,783,978,1103,1145
	1210,1212,1337,1490,2127,2233,2506,2513
	2516,2530,3684,3748,3852,3860,3873,3874
84	601,617,714,805,806,842,1163,1165
	1233,1324,1332,1425,1612,1697,2131,2134
	2202,2226,2404,2468,2636,2834,3233,3346
85	602,620,713,812,844,868,1171,1189
00	1225,1317,1441,1444,1609,1673,2138,2195
	2326,2342,2354,2356,2634,2642,3217,3218
86	603,621,715,846,1179,1197,1241,1457
	1613,1705,1829,1836,2259,2266,2390,2482
	2638,2854,2898,2916,3249,3380,3474,3492
87	604,618,716,820,841,932,1173,1187
ਂ'	1249,1318,1380,1417,1610,1681,2162,2198
	2323,2330,2341,2348,2633,2706,3154,3209
88	605,619,718,843,1181,1195,1265,1433
	1614,1713,1830,1844,2262,2290,2387,2458
	2637,2853,2962,2980,3241,3372,3410,3428
89	606,622,717,845,1203,1205,1257,1449
	1611,1689,1892,1956,2394,2418,2451,2454
	2635,2770,2860,2868,3225,3282,3365,3366
90	607,623,719,847,1211,1213,1273,1465
	$1615,\!1721,\!2515,\!2518,\!2522,\!2546,\!2639,\!3026$
	3257,3538,3877,3878,3884,3892,3940,4004
91	625,803,906,1166,1308,1361,1810,2133,2218,2276,2721,3148
92	626,628,740,796,905,908,1174,1190
	1252,1315,1353,1377,1618,1682,2154,2197
	2325,2332,2339,2346,2697,2705,3145,3146

93	627,629,907,910,1182,1198,1369,1393
	1820,1827,1874,1938,2261,2282,2389,2474
	2729,2737,2788,2851,3149,3150,3300,3356
94	630,909,1206,1385,1746,1764,2410,2453,2713,2844,3147,3363
95	631,911,1214,1401,2002,2517,2538,2745,3151,3812,3868,3875
96	633,807,970,1167,1340,1489,2135,2234,2532,3660,3745,3858
97	634,636,828,969,972,996,1175,1191
	1319,1481,1505,1508,2170,2199,2327,2343
	2362,2364,3657,3658,3666,3721,3729,3730
	,,
98	635,637,971,974,1183,1199,1497,1521
	1831,1852,2263,2298,2391,2490,2855,3044
	3388,3556,3661,3662,3753,3761,3922,3986
	3333,3333,3332,3002,3103,3102,30022,3000
99	638,973,1207,1513,2020,2426,2455,2876,3367,3659,3737,3794
100	639,975,1215,1529,2519,2554,3663,3769,3879,3900,4050,4068
101	659,684,852,1114,1125,1442,1801,2249,2318,2353,2658,3220
102	661,662,668,692,724,916,1123,1126
102	1130,1138,1250,1378,1634,1684,2315,2317
	2329,2345,2377,2441,2708,2825,3170,3337
	2020,2040,2011,2441,2100,2020,0110,0001
103	663,700,980,1127,1146,1506,2319,2361,2505,3682,3732,3849
104	666,677,721,790,809,866,1107,1132
	1226,1293,1330,1428,1633,1676,2137,2150
	2187,2228,2380,2465,2644,2826,3234,3345
105	667,685,723,854,1115,1133,1242,1458
	1637,1708,1805,1833,2251,2265,2382,2481
	2662,2830,2900,2914,3252,3377,3476,3490
106	669,726,1131,1266,1638,1716,2379,2457,2829,2964,3369,3426
107	670,693,725,918,1134,1139,1258,1394
	1635,1692,1890,1940,2381,2393,2443,2473
	2740,2772,2827,2857,3174,3298,3341,3353
108	671,701,727,982,1135,1147,1274,1522
	1639,1724,2383,2489,2507,2521,2831,3028
	3385,3554,3686,3764,3853,3881,3938,3988
109	674,785,1108,1290,2145,2188

110	675,682,787,817,849,930,1109,1116
	1294,1306,1364,1418,1802,1809,2149,2161
	2190,2220,2252,2273,2657,2722,3156,3212
111	678,690,738,789,793,913,1110,1140
	1236,1291,1322,1354,1620,1698,2147,2153
	2189,2204,2401,2444,2700,2833,3169,3338
112	679,698,791,825,977,994,1111,1148
	1295,1338,1482,1492,2151,2169,2191,2236
	2508,2529,3668,3681,3724,3746,3850,3857
113	683,851,1117,1434,1806,1841,2254,2289,2661,2978,3244,3412
114	686,691,853,915,1118,1141,1370,1450
	1803,1817,1876,1954,2253,2281,2417,2446
	2659,2732,2786,2865,3173,3228,3284,3342
115	687,699,855,979,1119,1149,1466,1498
	1807,1849,2255,2297,2510,2545,2663,3042
	3260,3540,3685,3756,3854,3889,3924,4002
116	694,917,1142,1386,1748,1762,2409,2445,2716,2841,3171,3339
117	695,702,919,981,1143,1150,1402,1514
	2004,2018,2425,2447,2509,2537,2748,2873
	3175,3343,3683,3740,3796,3810,3851,3865
118	703,983,1151,1530,2511,2553,3687,3772,3855,3897,4052,4066
119	729,730,813,870,1227,1235,1325,1460
	1641,1644,1677,1701,2139,2203,2406,2484
	2646,2838,2890,2892,3250,3378,3473,3489
120	731,1243,1645,1709,1837,2267,2894,2902,2918,3505,3506,3508
121	732,948,1251,1382,1642,1685,2331,2349,2710,2889,3186,3465
122	733,734,1259,1267,1643,1646,1693,1717
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123	735,1275,1647,1725,2523,2895,3030,3513,3570,3885,3942,4020
124	737,794,810,818,865,929,1228,1299
	1301,1302,1356,1420,1617,1674,2140,2156
	2164,2211,2213,2214,2641,2698,3153,3210

125	739,795,945,946,1244,1307,1358,1366
	1621,1706,1813,1834,2157,2221,2268,2275
	2702,2726,2897,2913,3185,3188,3466,3468
126	741,798,882,937,1260,1331,1357,1430
	1619,1690,1889,1932,2158,2229,2396,2467
	2676,2699,2769,2858,3161,3238,3274,3349
	2010,2099,2109,2090,3101,3230,3214,3349
127	742,754,797,921,1238,1268,1323,1355
12.	1622,1652,1702,1714,2155,2205,2403,2460
	2701,2837,2956,2961,3177,3370,3402,3425
	2701,2837,2930,2901,3177,3370,3402,3423
128	743,799,953,1010,1276,1339,1359,1494
120	1623,1722,2159,2237,2524,2531,2703,3025
	3193,3530,3700,3750,3861,3882,3937,3980
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129	745,814,858,869,1229,1333,1427,1452
	1625,1675,1868,1953,2142,2227,2420,2470
	2643,2668,2762,2866,3226,3237,3281,3350
	2040,2000,2102,2000,9220,9201,9201,9300
130	746,821,857,934,1237,1326,1396,1419
	1628,1699,1866,1937,2163,2206,2405,2476
	2665,2738,2764,2835,3158,3213,3297,3354
	2000,2100,2101,2000,0210,0201,00001
131	747,859,1245,1435,1629,1707,1838,1845
	1870,1969,2270,2291,2669,2766,2899,2917
	2982,2994,3245,3313,3414,3444,3482,3500
	2002,200 1,02 10,00 10,0 11 1,0 11 1,0 102,00 00
132	748,860,884,940,1253,1381,1443,1446
	1626,1683,1865,1929,2334,2350,2355,2357
	2666,2674,2707,2761,3162,3221,3222,3273
133	749,862,1261,1459,1627,1691,1869,1893
	1961,1964,2398,2483,2670,2763,2771,2862
	2930,2932,3253,3289,3290,3381,3478,3494
134	750,861,1269,1451,1630,1715,1867,1908
	1945,1958,2419,2462,2667,2765,2802,2869
	2963,2988,3229,3286,3305,3374,3418,3429
135	751,863,1277,1467,1631,1723,1871,1977
	2526,2547,2671,2767,3027,3058,3261,3321
	3542,3546,3886,3893,3941,3956,4006,4012

136	753,811,867,922,1230,1309,1363,1436
	1649,1678,1814,1842,2141,2219,2278,2292
	2645,2725,2954,2977,3180,3242,3404,3409
137	755,923,1246,1371,1653,1710,1821,1835
197	1878,1970,2269,2283,2733,2790,2901,2915
	2958,2993,3181,3316,3406,3441,3484,3498
138	756,924,1254,1379,1650,1686,2333,2347,2709,2953,3178,3401
139	757,926,1262,1395,1651,1694,1891,1906
	1942,1948,2397,2475,2741,2773,2804,2859
	2955,2985,3182,3302,3306,3357,3405,3417
140	758,925,1270,1387,1654,1718,1750,1766
	1778,1780,2411,2461,2717,2845,2957,2965
	2969,2972,3179,3371,3403,3427,3433,3434
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141	759,927,1278,1403,1655,1726,2006,2034
1 11	2525,2539,2749,2959,3001,3029,3183,3407
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143	762,829,985,998,1239,1327,1483,1524
	1660,1703,2171,2207,2407,2492,2839,3020
	3386,3553,3670,3689,3725,3762,3914,3985
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	3569,3572,3693,3757,3918,3926,4017,4018
	0000,0012,0000,0101,0010,0020,4011,4010
145	764,956,988,1012,1255,1383,1507,1510
	1658,1687,2335,2351,2363,2365,2711,3017
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	3450,3561,3691,3741,3798,3826,3915,3993
148	767,991,1279,1531,1663,1727,2527,2555
	3023,3031,3577,3578,3695,3773,3887,3901
	3919,3943,4025,4028,4054,4070,4082,4084
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149	819,881,931,938,1310,1365,1372,1422
140	1811,1818,1873,1930,2165,2222,2277,2284
	2673,2723,2730,2785,3157,3164,3214,3276
	2013,2123,2130,2163,3131,3104,3214,3210
150	822,873,874,933,1334,1388,1421,1429
150	
	1738,1740,1745,1761,2166,2230,2412,2469
	2649,2652,2714,2842,3155,3211,3235,3347
151	823,889,935,1002,1342,1404,1423,1493
191	
	1994,2001,2167,2238,2533,2540,2681,2746
	3159,3215,3676,3747,3788,3809,3859,3866
152	826,993,1303,1484,2172,2215,3665,3722
153	827,954,995,1009,1311,1367,1486,1500
100	1815,1850,2173,2223,2279,2300,2727,3041
	3196,3532,3669,3697,3726,3754,3921,3978
	3190,3332,3009,3097,3120,3104,3921,3910
154	830,890,997,1001,1335,1431,1485,1516
101	1996,2017,2174,2231,2428,2471,2684,2874
	3239,3351,3667,3673,3723,3738,3786,3793
	0200,0001,0001,0120,0120,0100,0100
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	3751,3770,3863,3898,4042,4044,4049,4065
156	875,1437,1742,1777,1846,2294,2653,2970,2981,3243,3411,3436
157	876,1445,1737,2358,2650,3219
158	877,878,1453,1461,1739,1741,1753,1769
-	1900,1957,2422,2486,2651,2654,2778,2870
	2906,2924,3227,3251,3283,3382,3475,3493
159	879,1469,1743,1785,2550,2655,3034,3259,3539,3894,3948,4005
160	883,939,1373,1438,1822,1843,1875,1905
	1934,1946,2286,2293,2677,2731,2789,2801
	2979,2986,3165,3246,3278,3308,3413,3420

161	885,942,1397,1454,1881,1882,1884,1931
	1939,1955,2421,2478,2675,2739,2793,2794
	2796,2867,3166,3230,3277,3285,3301,3358
162	886,941,1389,1462,1747,1754,1765,1772
	1897,1933,2414,2485,2678,2715,2777,2846
	2908,2922,3163,3254,3275,3379,3477,3491
163	887,943,1405,1470,1913,1935,2003,2010
	2542,2549,2679,2747,2809,3050,3167,3262
	3279,3541,3813,3820,3870,3891,3932,4003
164	891,1003,1439,1501,1847,1854,1998,2033
	2295,2302,2685,2983,3002,3045,3247,3415
	3452,3564,3677,3755,3790,3825,3923,3994
165	892,1004,1447,1509,1993,2359,2366,2682,3223,3674,3731,3785
166	893,1006,1455,1525,1916,1959,1995,2009
	2423,2494,2683,2810,2871,3052,3231,3287
	3390,3557,3678,3763,3789,3817,3930,3987
167	894,1005,1463,1517,1997,2021,2025,2028
	2430,2487,2686,2878,2938,2940,3255,3383
	$\left[\begin{array}{c} 3479, 3495, 3675, 3739, 3787, 3795, 3801, 3802 \\ \end{array}\right]$
168	895,1007,1471,1533,1999,2041,2551,2558
	2687,3066,3263,3543,3679,3771,3791,3833
	3895,3902,3964,4007,4051,4058,4069,4076
169	947,1374,1819,1877,1962,2285,2734,2787,2929,3189,3292,3470
170	949,950,1390,1398,1749,1756,1763,1770
	1898,1941,2413,2477,2718,2742,2780,2843
	$\left[\begin{array}{c} 2905,2921,3187,3190,3299,3355,3467,3469 \\ \end{array}\right]$
171	951,1406,2005,2026,2541,2750,2937,3191,3471,3804,3811,3867
172	955,1011,1375,1502,1823,1851,1879,1978
	2287,2301,2735,2791,3043,3057,3197,3324
	3534,3548,3701,3758,3925,3953,3982,4010
173	957,1014,1391,1526,1751,1767,1786,1788
	2415,2493,2719,2847,3033,3036,3195,3387
	3531,3555,3702,3766,3945,3946,3981,3989
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174	958,1013,1399,1518,1914,1943,2012,2019
	2429,2479,2743,2812,2875,3049,3198,3303
	3359,3533,3699,3742,3797,3818,3929,3979
175	959,1015,1407,1534,2007,2042,2543,2557
	2751,3065,3199,3535,3703,3774,3815,3836
	3871,3899,3961,3983,4053,4060,4067,4074
176	1019,1503,1855,2303,3047,3580,3709,3759,3927,4026,4046,4081
177	1020,1511,2367,3706,3735,4041
178	1021,1022,1519,1527,2023,2044,2431,2495
	2879,3068,3391,3559,3707,3710,3743,3767
	3799,3834,3962,3991,4043,4045,4057,4073
179	1023, 1535, 2559, 3711, 3775, 3903, 4047, 4055, 4071, 4089, 4090, 4092
180	1755, 1773, 1901, 1965, 2779, 2910, 2926, 2934, 3291, 3507, 3509, 3510
181	1757,1771,1902,1973,2782,2907,2925,2998,3315,3446,3483,3501
182	1758,1774,1779,1781,1899,1910,1949,1974
	2781,2806,2909,2923,2971,2974,2989,2997
	3307,3318,3419,3437,3438,3443,3485,3499
183	1759,1775,1787,1789,1903,1981,2783,2911
	2927,3035,3038,3062,3323,3515,3517,3547
	3571,3574,3949,3950,3958,4013,4021,4022
184	1782,2973,3435
185	1783,1790,2038,2975,3005,3037,3439,3451,3563,3830,3947,3997
186	1791,3039,3579,3951,4029,4086
187	1883,1885,1886,1909,1947,1963,1966,1971
	2795,2797,2798,2803,2931,2933,2990,2995
	3293,3294,3309,3317,3422,3445,3486,3502
188	1887,1979,2799,3059,3325,3550,3957,4014
189	1907,1950,2805,2987,3310,3421
190	1911,1915,1951,1982,2014,2035,2807,2813
	2991,3003,3051,3061,3311,3326,3423,3453
	3549,3566,3822,3829,3933,3955,3998,4011
191	1917,1967,2011,2811,2935,3054,3295,3518,3573,3821,3934,4019
192	1918,1975,2013,2027,2030,2037,2814,2939
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	3503,3565,3805,3806,3819,3827,3931,3995

193	1919,1983,2015,2043,2815,3055,3063,3067
195	3327,3551,3581,3582,3823,3837,3935,3959
	3965,4015,4027,4030,4062,4078,4083,4085
	3905,4015,4027,4050,4002,4075,4065,4065
194	2029,2942,3511,3803
195	2031,2045,2943,3070,3519,3575,3807,3835,3966,4023,4059,4077
196	2039, 2046, 3007, 3069, 3455, 3567, 3831, 3838, 3963, 3999, 4061, 4075
197	2047,3071,3583,3839,3967,4031,4063,4079,4087,4091,4093,4094
198	4095
None	0,1,2,3,4,5,6,8
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	19,20,24,25,26,27,32,33
	34,36,37,40,41,44,45,48
	64,65,66,67,68,70,72,73
	74,75,80,81,82,83,88,89
	90,91,96,98,128,129,130,131
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	147,148,152,153,154,155,160,176
	192,193,194,195,200,201,202,203
	208,209,210,211,216,217,218,219
	256,257,258,260,262,264,265,272
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	1580,1581,2048,2049,2050,2052,2054,2056
	2057,2064,2080,2096,2112,2114,2116,2118
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