

Report of ECE4016 HW2 --- BOLA

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1. Introduction

I choose the task 1 for this assignment, and the ABR algorithm I implemented is BOLA ([BOLA: Near-Optimal Bitrate Adaptation for Online Videos. \(2016\)](#)).

ABR streaming requires that each video is partitioned into chunks, where each chunk corresponds to a few seconds of play. Each chunk is then encoded in a number of different bitrates to accommodate a range of device types and network connectivities. The decision of which chunks to download at what bitrates is made by a bitrate adaptation algorithm within the video player, while each chunk has a fixed playback time of p seconds, the size of the chunk (in bits) can be different depending on its bitrate. This can be seen in the manifest file for each chunks' size. Thus, the choice of bitrate for a chunk impacts its download time.

There are mainly two types of ABR algorithms, one uses both prediction of network throughput and buffer occupancy, the other primarily bases on buffer occupancy, and BOLA is the latter one.

2. BOLA algorithm analysis

BOLA, which is fully called Buffer Occupancy based Lyapunov Algorithm, is a classic algorithm for online video streaming. BOLA is a buffer-based bitrate adaptive algorithm which uses Lyapunov optimization techniques to minimize rebuffering and maximize video quality.

BOLA formulate bitrate adaptation as a utility maximization problem, they define the QoE as the average bitrate of the video experienced by the user \bar{v}_N and the duration of the rebuffer events \bar{s}_N . And BOLA designs a control algorithm that maximizes the joint utility $\bar{v}_N + \gamma \bar{s}_N$ subject to the constraints of the model, where γ is for balance between utility and smoothness. The formulas for the utility are as follows:

$$\bar{v}_N \triangleq \frac{\mathbb{E}\left\{\sum_{k=1}^{K_N} \sum_{m=1}^M a_m(t_k) v_m\right\}}{\mathbb{E}\{T_{\text{end}}\}}$$

$$\bar{s}_N \triangleq \frac{Np}{\mathbb{E}\{T_{\text{end}}\}} = \frac{\mathbb{E}\left\{\sum_{k=1}^{K_N} \sum_{m=1}^M a_m(t_k) p\right\}}{\mathbb{E}\{T_{\text{end}}\}}$$

BOLA use the buffer level for the buffer stability maximization problem, which denotes by $Q(t_k)$, and the maintain of $Q(t_k)$ can be seen in the following figure, in which the sum of $a_m(t_k)$ is the download decision (if download equals 1, otherwise 0). BOLA proves that we achieve buffer stability by minimizing

$Q(t_k) \left(\sum_{m=1}^M a_m - T_k/p \right)$ and the performance objective to maximize $\bar{v}_N + \gamma \bar{s}_N$ is

achieved by maximizing $\left(\sum_{m=1}^M a_m(t_k) (v_m + \gamma p) \right)$. In conclusion, the control decision is solving the following deterministic optimization problem:

$$Q(t_{k+1}) = \max[Q(t_k) - T_k/p, 0] + \sum_{m=1}^M a_m(t_k)$$

$$\begin{aligned} &\text{Maximize } \frac{\sum_{m=1}^M a_m(t_k)(Vv_m + V\gamma p - Q(t_k))}{\sum_{m=1}^M a_m(t_k)S_m} \\ &\text{subject to } \sum_{m=1}^M a_m(t_k) \leq 1, a_m(t_k) \in \{0, 1\} \end{aligned}$$

3. Implementation

To implement the ABR algorithm in the simulator, I first get to know the input parameters for the method.

```
=====
Measured Bandwidth: 10000.0
Previous_Throughput: 9999.610667704887
Buffer_Occupancy: {'size': 200000, 'current': 6421, 'time': 2}
Available_Bitrates,: {'500000': 5764, '1000000': 14391, '5000000': 57155}
Video_Time 138.742
Chunk: {'left': 2, 'time': 2, 'current': '28'}
Rebuffering_Time: 3.1369999999999996
Preferred_Bitrate None
=====
```

After knowing the input parameters, I begin to write the code. In the paper's example, γp and V is given as the following: "let $v_m = \ln(S_m/S_M)$. Pick $\gamma = 5.0/p$ and $V = 0.93$." And I follows this example to implement BOLA. BOLA provided psuedocode for easier implementing.

```

1: for  $n$  in  $[1, N]$  do
2:    $t \leftarrow \min[\text{playtime from begin, playtime to end}]$ 
3:    $t' \leftarrow \max[t/2, 3p]$ 
4:    $Q_{\max}^D \leftarrow \min[Q_{\max}, t'/p]$ 
5:    $V^D \leftarrow (Q_{\max}^D - 1)/(v_1 + \gamma p)$ 
6:    $m^*[n] \leftarrow \arg \max_m (V^D v_m + V^D \gamma p - Q)/S_m$ 
7:   if  $m^*[n] < m^*[n-1]$  then
8:      $r \leftarrow$  bandwidth measured when downloading chunk  $(n-1)$ 
9:      $m' \leftarrow \min m$  such that  $S_m/p \leq \max[r, S_M/p]$ 
10:    if  $m' \leq m^*[n]$  then
11:       $m' \leftarrow m^*[n]$ 
12:    else if  $m' > m^*[n-1]$  then
13:       $m' \leftarrow m^*[n-1]$ 
14:    else if some utility sacrificed for fewer oscillations then
15:      pause until  $(V^D v_{m'} + V^D \gamma p - Q)/S_{m'} \geq$   $(V^D v_{m'-1} + V^D \gamma p - Q)/S_{m'-1}$   $\triangleright$  BOLA-O
16:    else
17:       $m' \leftarrow m' - 1$   $\triangleright$  BOLA-U
18:    end if
19:     $m^*[n] \leftarrow m'$ 
20:  end if
21:  pause for  $\max[p \cdot (Q - Q_{\max}^D + 1), 0]$ 
22:  download chunk  $n$  at bitrate index  $m^*[n]$ , possibly abandoning
23: end for

```

Since the provided entry is for each chunk, I do not need to do the for loop manually, and I define a global variable `prev_m` to store the previous download decision since I don't maintain a `m` array like the pseudocode. For the buffer size, level and minimum utility, the getting process is quite similar as the pseudocode. But for the `argmax` to get the optimal bitrate index, is more complex but still follows the formula in BOLA algorithm analysis.

```

# argmax index m
# calculate the optimal bitrate index that maximizes the utility function
m = max(range(len(S_m)) , key = lambda index : (V_D * math.log(int(S_m[index][0])
/ int(S_m[-1][0]), math.e) + V_D * 5 - Buffer_Occupancy['time'] / Chunk['time']) /
S_m[index][1])

```

For the next `if else` conditional judgement part, since there's no function for the simulator to pause or create oscillation, I just eliminate these parts. There are more detailed comments in the code file, please check for further information.

4. Evaluation

It's hard to conduct experiment on a simulator, but likely, the grader actually helps to evaluate the performance of the ABR algorithm. Here's my result for the grader, where the `badtest`, `testALThard`, `TestALTsoft`. etc has a significant improvement comparing with the ground truth buffer-based method:

```
grade.txt
1  badtest:
2  Your trace file is poorly formed!
3  Results:
4  Average bitrate:2250000.0
5  buffer time:8.507000000000001
6  switches:22
7
8  Score:232278.72308615994
9
10
11  testALThard:
12  Results:
13  Average bitrate:2250000.0
14  buffer time:8.507000000000001
15  switches:22
16
17  Score:232278.72308615994
18
19
20  testALTsoft:
21  Results:
22  Average bitrate:3950000.0
23  buffer time:4.702000000000002
24  switches:8
25
26  Score:1592781.1468109528
27
28
29  testHD:
30  Results:
31  Average bitrate:4700000.0
32  buffer time:0.101
33  switches:1
34
35  Score:4301656.912826439
```

5. Conclusion

This is a helpful task for learning ABR algorithm and improves my ability to implement code from papers. And thanks for your patience for finishing reading this report.