

```
(* Lax-Friedrichs Finite Difference Method in 2D *)
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```
(* Givens Conditions *)
```

```
 $\Delta x = 5;$   
 $\Delta y = 5;$   
 $\alpha = 300;$   
regionx = 300;  
regiony = 300;  
 $\Delta t = 0.0015;$   
 $c1 = \alpha * \Delta t / \Delta x;$   
 $c2 = \alpha * \Delta t / \Delta y;$   
cx = {};  
cy = {};  
u0 = {};
```

```
(* creating initial vector by organizing x,  
y coordinates to give z coordinate by evaluating *)
```

```
For[x = 0, x ≤ regionx, x = x + Δx,  
  For[y = 0, y ≤ regiony, y = y + Δy,  
  
    AppendTo[cx, x];  
    AppendTo[cy, y];  
  
    If[50 ≤ x && x ≤ 110 && 50 ≤ y ≤ 110,  
      AppendTo[u0,  
        (100 * Sin[Pi * (x - 50) / 60]) * (100 * Sin[Pi * (y - 50) / 60]), AppendTo[u0, 0];  
      ];  
    ];  
  ];
```

```
(* creating scheme matrix and diagonalizing things *)
```

```
A = ConstantArray[0, {Length[cx], Length[cy]}];
```

```
For[i = 2, i ≤ Length[cx], i++,  
  A[[i - 1, i]] = (1 / 4) - c1;  
  A[[i, i - 1]] = (1 / 4) + c2;  
];  
  
For[j = 1, j ≤ Length[cx] - (regionx / Δx), j++,  
  A[[j, j + (regionx / Δx)]] = (1 / 4) - c1;  
];  
  
For[k = 1, k ≤ Length[cy] - (regiony / Δy), k++,  
  A[[k + (regionx / Δy), k]] = (1 / 4) - c2;  
];
```

```
(* creating vector of z values at any arbitrary time *)
```

```
timestart = 1;
timefinish = 50;
```

```
For[n = timestart, n ≤ timefinish, n++,
```

```
  un = A.un-1;
  un = ReplacePart[un, 1 → 0];
  un = ReplacePart[un, Length[un] → 0];
  vn = Transpose[{cx, cy, un}]
```

```
];
```

```
(* random time generator to plot the graph at a random time *)
```

```
time = RandomInteger[{timestart, timefinish}];
graph = ListPlot3D[vtime, PlotRange → All,
  AxesLabel → {"x-coordinate", "y-coordinate", "z-coordinate"}];
Print["3D Plot of scheme at the randomly generated time: ", time];
Print[graph];
```

3D Plot of scheme at the randomly generated time: 36

