

```
(*Gauss-Seidel Method*)
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```
(*We can extend this to whatever size matrix we  
want. Will use a small 10x10 matrix as proof of concept*)  
size = 10;
```

```
(*create matrix A*)  
A = ConstantArray[0, {size, size}];
```

```
min = 1;  
max = 9;
```

```
(*creating a strictly positive matrix*)  
For[i = 1, i ≤ size, i++,  
  For[j = 1, j ≤ size, j++,  
    If[i ≤ j, A[[i, j]] = RandomInteger[{min, max}]]];  
  ];  
];
```

```
For[i = 1, i ≤ size, i++,  
  For[j = 1, j ≤ size, j++,  
    If[i ≥ j, A[[i, j]] = A[[j, i]]];  
  ];  
];
```

```
(*adding up the columns of each row to force diagonal dominance*)  
sums = Total[A];
```

```
(*enforcing diagonal dominance on matrix A*)  
For[i = 1, i ≤ size, i++,  
  A[[i, i]] = RandomInteger[{sums[[i]], sums[[i]] + 1}];  
];
```

```
b = ConstantArray[0, {Length[A], 1}];
```

```
(*making the vector b to be <1,2,3,4,5,6,7,8,9,10>*)  
For[i = 1, i ≤ size, i++,  
  b[[i]] = i;  
];
```

```
(*creating L and U to be zero matrices*)  
U = ConstantArray[0, {size, size}];  
L = ConstantArray[0, {size, size}];
```

```
(* making L matrix the lower half of A,  
including the diagonal and U matrix the upper half of A*)  
For[i = 1, i ≤ size, i++,  
  For[j = 1, j ≤ size, j++,  
    If[i ≥ j,  
      L[[i, j]] = A[[i, j]],
```

```

        U[[i, j]] = A[[i, j]];
    ]
]
];

(*choose x1 = vector of all 1's because, why not... *)
x1 = ConstantArray[1, {size, 1}];

(*looking at the structure of the matrices and vectors*)
MatrixForm[A]
MatrixForm[U]
MatrixForm[L]
MatrixForm[b]

(*iterative step of GS method*)
For[i = 1, i ≤ 500, i++,
    xi+1 = Inverse[L].(b - U.xi);
    last = xi+1
];

xreal = LinearSolve[A, b]; (*since we chose a small system, this is the actual *)
xbar = last; (*the 500's iteration of the iterated x*)
b1 = A.xbar; (*creating vector b1, which should approximate vector b*)
precision = 30; (*going to numerically round to the nearest 30th decimal*)
Print[MatrixForm[N[b1, precision]]]; (*if b1 ~ b, then we're correct*)

```