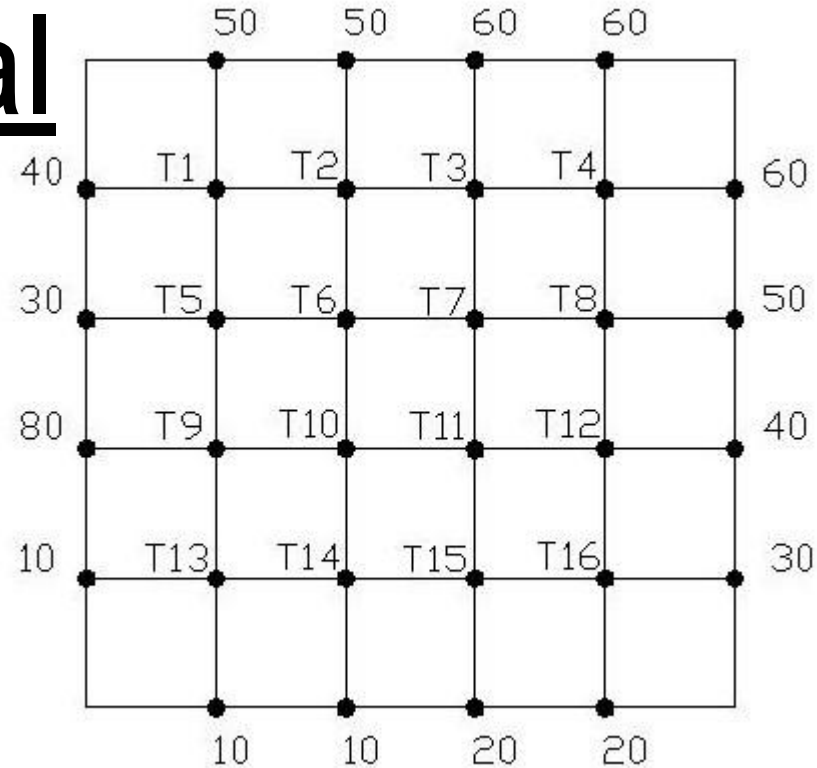


Temperatura sobre placa de metal



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Planteo del Sistema

$$T_1 = \frac{50+40+T_2+T_5}{4} \Rightarrow 4T_1 - T_2 - T_5 = 90$$

$$T_2 = \frac{T_1+50+T_3+T_6}{4} \Rightarrow 4T_2 - T_1 - T_3 - T_6 = 50$$

$$T_3 = \frac{60+T_4+T_7+T_2}{4} \Rightarrow 4T_3 - T_4 - T_7 - T_2 = 60$$

$$T_4 = \frac{T_3+60+60+T_8}{4} \Rightarrow 4T_4 - T_3 - T_8 = 120$$

$$T_5 = \frac{30+T_1+T_6+T_9}{4} \Rightarrow 4T_5 - T_1 - T_9 = 30$$

$$T_6 = \frac{T_5+T_2+T_7+T_{10}}{4} \Rightarrow 4T_6 - T_5 - T_2 - T_7 - T_{10} = 0$$

$$T_7 = \frac{T_6+T_3+T_8+T_{11}}{4} \Rightarrow 4T_7 - T_6 - T_3 - T_8 - T_{11} = 0$$

$$T_8 = \frac{T_7+T_4+50+T_{12}}{4} \Rightarrow 4T_8 - T_7 - T_4 - T_{12} = 50$$

$$T_9 = \frac{20+T_3+T_{10}+T_{13}}{4} \Rightarrow 4T_9 - T_3 - T_{10} - T_{13} = 20$$

$$T_{10} = \frac{T_9+T_6+T_{11}+T_{14}}{4} \Rightarrow 4T_{10} - T_9 - T_6 - T_{11} - T_{14} = 0$$

$$T_{11} = \frac{T_{10}+T_7+T_{12}+T_{15}}{4} \Rightarrow 4T_{11} - T_{10} - T_7 - T_{15} = 0$$

$$T_{12} = \frac{T_{11}+T_8+40+T_{16}}{4} \Rightarrow 4T_{12} - T_{11} - T_8 - T_{16} = 40$$

$$T_{13} = \frac{10+T_9+T_{14}+10}{4} \Rightarrow 4T_{13} - T_9 - T_{14} = 20$$

$$T_{14} = \frac{T_{13}+T_{10}+T_{15}+10}{4} \Rightarrow 4T_{14} - T_{13} - T_{10} - T_{15} = 10$$

$$T_{15} = \frac{T_{14}+T_{11}+T_{16}+20}{4} \Rightarrow 4T_{15} - T_{14} - T_{16} = 20$$

$$T_{16} = \frac{T_{15}+T_{12}+30+20}{4} \Rightarrow 4T_{16} - T_{15} - T_{12} = 50$$

Codigo en Scilab

```
1 m=[4 -1 0 0 -1 0 0 0 0 0 0 0 0 0 0;
2 -1 4 -1 0 0 -1 0 0 0 0 0 0 0 0 0;
3 0 -1 4 -1 0 0 -1 0 0 0 0 0 0 0 0;
4 0 0 -1 4 0 0 0 -1 0 0 0 0 0 0 0;
5 -1 0 0 0 4 -1 0 0 -1 0 0 0 0 0 0;
6 0 -1 0 0 -1 4 -1 0 0 -1 0 0 0 0 0;
7 0 0 -1 0 0 -1 4 -1 0 0 -1 0 0 0 0;
8 0 0 0 -1 0 0 -1 4 0 0 0 -1 0 0 0;
9 0 0 0 0 -1 0 0 0 4 -1 0 0 -1 0 0;
10 0 0 0 0 0 -1 0 0 -1 4 -1 0 0 -1 0;
11 0 0 0 0 0 0 -1 0 0 -1 4 -1 0 0 -1;
12 0 0 0 0 0 0 0 -1 0 0 -1 4 0 0 -1;
13 0 0 0 0 0 0 0 0 -1 0 0 0 4 -1 0;
14 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4 -1;
15 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4 -1;
16 0 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4];
```

```
17
18 aum=[4 -1 0 0 -1 0 0 0 0 0 0 0 0 0 0 90;
19 -1 4 -1 0 0 -1 0 0 0 0 0 0 0 0 0 50;
20 0 -1 4 -1 0 0 -1 0 0 0 0 0 0 0 0 60;
21 0 0 -1 4 0 0 0 -1 0 0 0 0 0 0 0 120;
22 -1 0 0 0 4 -1 0 0 -1 0 0 0 0 0 0 30;
23 0 -1 0 0 -1 4 -1 0 0 -1 0 0 0 0 0 0;
24 0 0 -1 0 0 -1 4 -1 0 0 -1 0 0 0 0 0;
25 0 0 0 -1 0 0 -1 4 0 0 0 -1 0 0 0 50;
26 0 0 0 0 -1 0 0 0 4 -1 0 0 -1 0 0 20;
27 0 0 0 0 0 -1 0 0 -1 4 -1 0 0 -1 0 0;
28 0 0 0 0 0 0 -1 0 0 -1 4 -1 0 0 -1 0;
29 0 0 0 0 0 0 0 -1 0 0 -1 4 0 0 0 -1 40;
30 0 0 0 0 0 0 0 0 -1 0 0 0 4 -1 0 0 20;
31 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4 -1 0 10;
32 0 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4 -1 20;
33 0 0 0 0 0 0 0 0 0 0 0 -1 0 0 -1 4 50];
```

```
34
35 r=[90;50;60;120;30;0;0;50;20;0;0;40;20;10;20;50];
```

```
36
37 rref(aum) //Eliminacion gauss-jordan de la matriz aumentada
38 minv=inv(m) //Invertida de la matriz m
39 i=minv*r //Producto de la matriz invertida y el resultado
40
41 [L,U]=lu(aum) //U matriz por eliminacion de gauss, sin pivote 1
42
43 //Operaciones con filas para que los pivotes nos den 1
```

```
44
45 U(1,:)=U(1,:)/4
46 U(2,:)=U(2,:)/3.75
47 U(3,:)=U(3,:)/3.7333333
48 U(4,:)=U(4,:)/3.7321429
49 U(5,:)=U(5,:)/3.7320574
50 U(6,:)=U(6,:)/3.4051282
51 U(7,:)=U(7,:)/3.3689759
52 U(8,:)=U(8,:)/3.3867903
53 U(9,:)=U(9,:)/3.7047352
54 U(10,:)=U(10,:)/3.3495707
55 U(11,:)=U(11,:)/3.3022233
56 U(12,:)=U(12,:)/3.3338173
57 U(13,:)=U(13,:)/3.7000435
58 U(14,:)=U(14,:)/3.3362099
59 U(15,:)=U(15,:)/3.2846019
60 U(16,:)=U(16,:)/3.3215903
```

```
61
```

```
62
63 tic();i=minv*r;toc() //Tiempo que tarda en dar el resultado habiendo invertido antes la matriz
64 tic();i=inv(m)*r;toc() //Tiempo que tarda en dar el resultado sin haber invertido antes la matriz
65 tic();i=rref(aum);toc() //Tiempo que tarda en hacer gauss-jordan
66
67 tic();[L,U]=lu(aum) //Tiempo que tarda en hacer eliminacion por Gauss
```

```
68
```

```
69 U(1,:)=U(1,:)/4
70 U(2,:)=U(2,:)/3.75
71 U(3,:)=U(3,:)/3.7333333
72 U(4,:)=U(4,:)/3.7321429
73 U(5,:)=U(5,:)/3.7320574
74 U(6,:)=U(6,:)/3.4051282
75 U(7,:)=U(7,:)/3.3689759
76 U(8,:)=U(8,:)/3.3867903
77 U(9,:)=U(9,:)/3.7047352
78 U(10,:)=U(10,:)/3.3495707
79 U(11,:)=U(11,:)/3.3022233
80 U(12,:)=U(12,:)/3.3338173
81 U(13,:)=U(13,:)/3.7000435
82 U(14,:)=U(14,:)/3.3362099
83 U(15,:)=U(15,:)/3.2846019,toc()
84
```

Resolución por método de Gauss-Jordan

```
--> rref(aum)
```

```
ans =
```

1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	42.045455
0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	44.772727
0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	50.
0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	53.863636
0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	33.409091
0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	37.045455
0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	41.363636
0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	0.	45.454545
0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	0.	24.545455
0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	0.	28.636364
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	0.	32.954545
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	0.	36.590909
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	0.	16.136364
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	0.	20.
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	0.	25.227273
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	27.954545

```
--> tic();i=rref(aum);toc()
```

```
ans =
```

```
0.0019773
```

=1977,3 μ s

Resolución por método de matriz invertida

```
--> minv=inv(m)
minv =
```

column 1 to 14

```
0.3010606 0.1021212 0.0380303 0.0133333 0.1021212 0.0693939 0.0366667 0.015303 0.0380303 0.0366667 0.0239394 0.0112121 0.0133333 0.015303
0.1021212 0.3390909 0.1154545 0.0380303 0.0693939 0.1387879 0.084697 0.0366667 0.0366667 0.0619697 0.0478788 0.0239394 0.015303 0.0245455
0.0380303 0.1154545 0.3390909 0.1021212 0.0366667 0.084697 0.1387879 0.0693939 0.0239394 0.0478788 0.0619697 0.0366667 0.0112121 0.0209091
0.0133333 0.0380303 0.1021212 0.3010606 0.015303 0.0366667 0.0693939 0.1021212 0.0112121 0.0239394 0.0366667 0.0380303 0.0056061 0.0112121
0.1021212 0.0693939 0.0366667 0.015303 0.3390909 0.1387879 0.0619697 0.0245455 0.1154545 0.084697 0.0478788 0.0209091 0.0380303 0.0366667
0.0693939 0.1387879 0.084697 0.0366667 0.1387879 0.4010606 0.1633333 0.0619697 0.084697 0.1633333 0.1056061 0.0478788 0.0366667 0.0619697
0.0366667 0.084697 0.1387879 0.0693939 0.0619697 0.1633333 0.4010606 0.1387879 0.0478788 0.1056061 0.1633333 0.084697 0.0239394 0.0478788
0.015303 0.0366667 0.0693939 0.1021212 0.0245455 0.0619697 0.1387879 0.3390909 0.0209091 0.0478788 0.084697 0.1154545 0.0112121 0.0239394
0.0380303 0.0366667 0.0239394 0.0112121 0.1154545 0.084697 0.0478788 0.0209091 0.3390909 0.1387879 0.0619697 0.0245455 0.1021212 0.0693939
0.0366667 0.0619697 0.0478788 0.0239394 0.084697 0.1633333 0.1056061 0.0478788 0.1387879 0.4010606 0.1633333 0.0619697 0.0693939 0.1387879
0.0239394 0.0478788 0.0619697 0.0366667 0.0478788 0.1056061 0.1633333 0.084697 0.0619697 0.1633333 0.4010606 0.1387879 0.0366667 0.084697
0.0112121 0.0239394 0.0366667 0.0380303 0.0209091 0.0478788 0.084697 0.1154545 0.0245455 0.0619697 0.1387879 0.3390909 0.015303 0.0366667
0.0133333 0.015303 0.0112121 0.0056061 0.0380303 0.0366667 0.0239394 0.0112121 0.1021212 0.0693939 0.0366667 0.015303 0.3010606 0.1021212
0.015303 0.0245455 0.0209091 0.0112121 0.0366667 0.0619697 0.0478788 0.0239394 0.0693939 0.1387879 0.084697 0.0366667 0.1021212 0.3390909
0.0112121 0.0209091 0.0245455 0.015303 0.0239394 0.0478788 0.0619697 0.0366667 0.084697 0.1387879 0.0693939 0.0380303 0.1154545
0.0056061 0.0112121 0.015303 0.0133333 0.0112121 0.0239394 0.0366667 0.0380303 0.015303 0.0366667 0.0693939 0.1021212 0.0133333 0.0380303
```

column 15 to 16

```
0.0112121 0.0056061
0.0209091 0.0112121
0.0245455 0.015303
0.015303 0.0133333
0.0239394 0.0112121
0.0478788 0.0239394
0.0619697 0.0366667
0.0366667 0.0380303
0.0366667 0.015303
0.084697 0.0366667
0.1387879 0.0693939
0.0693939 0.1021212
0.0380303 0.0133333
0.1154545 0.0380303
0.3390909 0.1021212
0.1021212 0.3010606
```

```
--> inv(m)*r
ans =
```

```
42.045455
44.772727
50.
53.863636
33.409091
37.045455
41.363636
45.454545
24.545455
28.636364
32.954545
36.590909
16.136364
20.
25.227273
27.954545
```

```
--> tic();i=minv*r;toc()
ans =
```

0.0000365 = 36,5 μ s

```
--> tic();i=inv(m)*r;toc()
ans =
```

0.0001029 = 102,9 μ s

$$m \times x = r$$

$$m^{-1} \times m \times x = m^{-1} \times r \Rightarrow I \times x = m^{-1} \times r \Rightarrow x = m^{-1} \times r$$

Metodo de eliminacion por Gauss

```
--> tic();[L,U]= lu(aum)
U =
```

column 1 to 15

4.	-1.	0.	0.	-1.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	3.75	-1.	0.	-0.25	-1.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.	3.7333333	-1.	-0.0666667	-0.2666667	-1.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.	0.	3.7321429	-0.0178571	-0.0714286	-0.2678571	-1.	0.	0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	3.7320574	-1.0717703	-0.0191388	-0.0047847	-1.	0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	3.4051282	-1.0820513	-0.0205128	-0.2871795	-1.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.	3.3689759	-1.0783133	-0.0963855	-0.3177711	-1.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.	0.	3.3867903	-0.0338623	-0.1077336	-0.3200715	-1.	0.	0.	0.
0.	0.	0.	0.	0.	0.	0.	0.	3.7047352	-1.0945059	-0.0318099	-0.0099984	-1.	0.	0.
0.	0.	0.	0.	0.	0.	0.	0.	0.	3.3495707	-1.113902	-0.0347638	-0.2954343	-1.	0.
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	3.3022233	-1.1061524	-0.1068332	-0.3325507	-1.
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	3.3338173	-0.0415511	-0.1217737	-0.334972
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	3.7000435	-1.100477	-0.0365268
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	3.3362099	-1.1238045
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	3.2846019
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

column 16 to 17

0.	90.
0.	72.5
0.	79.333333
0.	141.25
0.	59.425837
0.	44.769231
0.	45.918675
0.	102.89003
0.	42.041247
0.	33.172118
0.	34.74596
-1.	82.47647
-0.0124635	36.425824
-0.0402338	37.248959
-1.1141528	51.715912
3.3215903	92.853548


```
--> U(15,:) = U(15,:)/3.2846019, toc()
```

```
U =
```

```
column 1 to 15
```

1.	-0.25	0.	0.	-0.25	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	1.	-0.2666667	0.	-0.0666667	-0.2666667	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.	1.	-0.2678571	-0.0178571	-0.0714286	-0.2678571	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.	0.	1.	-0.0047847	-0.0191388	-0.0717703	-0.2679426	0.	0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	1.	-0.2871795	-0.0051282	-0.0012821	-0.2679487	0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	1.	-0.3177711	-0.0060241	-0.0843373	-0.2936747	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.	1.	-0.3200715	-0.0286097	-0.0943228	-0.2968261	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.	0.	1.	-0.0099984	-0.0318099	-0.0945059	-0.2952648	0.	0.	0.
0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.2954343	-0.0085863	-0.0026988	-0.2699248	0.	0.
0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.3325507	-0.0103786	-0.0882006	-0.2985457	0.
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.334972	-0.0323519	-0.1007051	-0.3028263
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.0124635	-0.0365268	-0.100477
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.2974227	-0.009872
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.	-0.3368506
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	1.
0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

```
column 16 to 17
```

0.	22.5
0.	19.333333
0.	21.25
0.	37.84689
0.	15.923077
0.	13.14759
0.	13.629861
0.	30.379806
0.	11.347976
0.	9.9033938
0.	10.52199
-0.2999564	24.739349
-0.0033685	9.8447014
-0.0120597	11.165053
-0.3392048	15.744956
3.3215903	92.853548

```
ans =
```

```
0.2071878 =207,1878 ms
```


Conclusiones

Gauss-Jordan: $1977,3\mu s$

Método de la matriz invertida: $102,9\mu s$

Eliminacion por Gauss: $207,1878 ms$