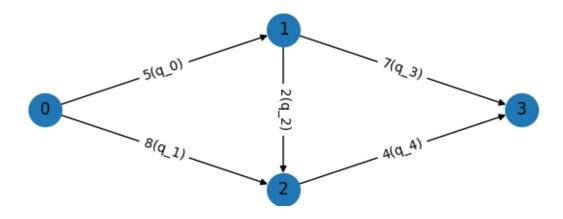
# Fórmulas



# 1 Formulación del problema

• Objetivo:

$$min(5X_{01} + 8X_{02} + 2X_{12} + 7X_{13} + 4X_{23})$$

• Restricciones:

$$X_{01} + X_{02} = 1 (1)$$

$$X_{01} = X_{12} + X_{13} (2)$$

$$X_{02} + X_{12} = X_{23} (3)$$

$$X_{13} + X_{23} = 1$$

## 2 Función de coste (QUBO)

$$C(X) = 5X_{01} + 8X_{02} + 2X_{12} + 7X_{13} + 4X_{23} + P(X_{01} + X_{02} - 1)^{2}$$

$$P(X_{01} - X_{12} - X_{13})^{2}$$

$$P(X_{02} + X_{12} - X_{23})^{2}$$

$$P = 1 + \sum_{(i,j) \in E} w_{ij} = 27$$

#### 3 Correspondencia

$$X_{01} \rightarrow z_o$$

$$X_{02} \rightarrow z_1$$

$$X_{12} \rightarrow z_2$$

$$X_{13} \rightarrow z_3$$

$$X_{23} \rightarrow z_4$$

$$z_a = \begin{cases} 1 & \text{si } X_{ij} = 0 \\ -1 & \text{si } X_{ij} = 1 \end{cases}$$
$$X_{ij} \to \frac{1 - z_a}{2}$$

### 4 Función de coste (Ising)

$$\begin{split} C(X) \to g(z) = & 5\frac{1-z_0}{2} + 8\frac{1-z_1}{2} + 2\frac{1-z_2}{2} + 7\frac{1-z_3}{2} + 4\frac{1-z_4}{2} + \\ & P(\frac{1-z_0}{2} + \frac{1-z_1}{2} - 1)^2 \\ & P(\frac{1-z_0}{2} - \frac{1-z_2}{2} - \frac{1-z_3}{2})^2 \\ & P(\frac{1-z_1}{2} + \frac{1-z_2}{2} - \frac{1-z_4}{2})^2 \end{split}$$

$$g(z) = 11z_0 - 17.5z_1 - 28z_2 - 17z_3 + 11.5z_4 + 13.5(-z_0z_2 + z_1z_2 + z_2z_3 - z_2z_4 + z_0z_1 - z_0z_3 - z_1z_4) + (13.5z_0^2 + 13.5z_1^2 + 13.5z_2^2 + 6.75z_3^2 + 6.75z_4^2) + 26.5$$

#### 5 Hamiltonian problem y mixer

Donde Z es una puerta Pauli-Z y X una puerta Pauli-X

$$H_p = 11Z_0 - 17.5Z_1 - 28Z_2 - 17Z_3 + 11.5Z_4 + 13.5(-Z_0Z_2 + Z_1Z_2 + Z_2Z_3 - Z_2Z_4 + Z_0Z_1 - Z_0Z_3 - Z_1Z_4) + (13.5Z_0^2 + 13.5Z_1^2 + 13.5Z_2^2 + 6.75Z_3^2 + 6.75Z_4^2) + 26.5$$

$$\begin{split} U(H_p,\gamma_i) &= e^{-i\gamma_i H_p} = &Rz_0(11*2\gamma_i)*Rz_1(-17.5*2\gamma_i)*Rz_2(-28*2\gamma_i)*Rz_3(-17*2\gamma_i)*Rz_4(11.5*2\gamma_i)*\\ &Rz_0z_2(-13.5*2\gamma_i)*Rz_1z_2(+13.5*2\gamma_i)*Rz_2z_3(+13.5*2\gamma_i)*Rz_2z_4(-13.5*2\gamma_i)*\\ &Rz_0z_1(+13.5*2\gamma_i)*Rz_0z_3(-13.5*2\gamma_i)*Rz_1z_4(-13.5*2\gamma_i) \end{split}$$

Pero en el paper:

$$U(H_p, \gamma_i) = e^{-i\gamma_i H_p} = Rz_0(11) * Rz_1(-17.5) * Rz_2(-28) * Rz_3(-17) * Rz_4(11.5) *$$

$$Rz_0z_2(-13.5\gamma_i) * Rz_1z_2(+13.5\gamma_i) * Rz_2z_3(+13.5\gamma_i) * Rz_2z_4(-13.5\gamma_i) *$$

$$Rz_0z_1(+13.5\gamma_i) * Rz_0z_3(-13.5\gamma_i) * Rz_1z_4(-13.5\gamma_i)$$

$$H_m = \sum_{i=0}^{n-1} X_i$$

$$U(H_m, \beta_i) = e^{i\beta_i H_m} = \prod_{i=0}^{n-1} Rx_i(2\beta_i)$$

#### 5.1 Definiciones

$$Rx_{i}(\lambda) = exp(-i\frac{\lambda}{2}X_{i})$$

$$Rz_{i}(\lambda) = exp(-i\frac{\lambda}{2}Z_{i})$$

$$Rz_{i}z_{j}(\lambda) = exp(-i\frac{\lambda}{2}Z_{i} \otimes Z_{j})$$

# 6 Hamiltonian

• Parámetros:

$$\vec{\beta} = [\beta_0, ..., \beta_{p-1}]$$
  
 $\vec{\gamma} = [\gamma_0, ..., \gamma_{p-1}]$ 

• Hamiltonian

$$H(\vec{\beta}, \vec{\gamma}) = U(H_p, \gamma_0)U(H_m, \beta_0)...U(H_p, \gamma_{p-1})U(H_m, \beta_{p-1})$$