

## עבודה 4

### חלק 1

1.  $((\text{lambda } (x1 \ y1) (\text{if } (> \ x1 \ y1) \ \#t \ \#f)) \ 8 \ 3))$

נעבוד לפי ארבעת השלבים שהוגדרו בכיתה:

**Stage I:** Rename bound variables:

$((\text{lambda } (x \ y) (\text{if } (> \ x \ y) \ \#t \ \#f)) \ 8 \ 3)$

**Stage II:** Assign type variables for every sub expression:

Expression	Variable
$((\text{lambda } (x \ y) (\text{if } (> \ x \ y) \ \#t \ \#f)) \ 8 \ 3)$	$T_0$
$(\text{lambda } (x \ y) (\text{if } (> \ x \ y) \ \#t \ \#f))$	$T_1$
$(\text{if } (> \ x \ y) \ \#t \ \#f)$	$T_{if}$
$(> \ x \ y)$	$T_{cond}$
$>$	$T_>$
$\#t$	$T_{\#t}$
$\#f$	$T_{\#f}$
$x$	$T_x$
$y$	$T_y$
$8$	$T_{num8}$
$3$	$T_{num3}$

**Stage III:** Construct type equations:

The equations for the sub-expressions are:

Expression	Equation
$((\text{lambda } (x\ y) (\text{if } (> x\ y) \#t \#f))\ 8\ 3)$	$T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$
$(\text{lambda } (x\ y) (\text{if } (> x\ y) \#t \#f))$	$T_1 = [T_x * T_y \rightarrow T_{if}]$
$(\text{if } (> x\ y) \#t \#f)$	$T_{if} = T_{\#t} = T_{\#f}$
$(> x\ y)$	$T_{cond} = [T_x * T_y \rightarrow bool]$

The equations for the primitives are:

Expression	Equation
$>$	$T_{>} = [number * number \rightarrow bool]$
$\#t$	$T_{\#t} = bool$
$\#f$	$T_{\#f} = bool$
$8$	$T_{num8} = number$
$3$	$T_{num3} = number$

**Stage IV:** Solve the equations:

1:

Equation	Substitution
$T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$	1) $T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$
$T_1 = [T_x * T_y \rightarrow T_{if}]$	
$T_{if} = T_{\#t} = T_{\#f}$	
$T_{cond} = [T_x * T_y \rightarrow bool]$	
$T_{>} = [number * number \rightarrow bool]$	
$T_{\#t} = bool$	
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	

2:

Equation	Substitution
$T_1 = [T_x * T_y \rightarrow T_{if}]$	1) $T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$
$T_{if} = T_{\#t} = T_{\#f}$	
$T_{cond} = [T_x * T_y \rightarrow bool]$	
$T_{>} = [number * number \rightarrow bool]$	
$T_{\#t} = bool$	
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	
$T_x := T_{num8}$	
$T_y := T_{num3}$	

$T_{if} := T_0$	
-----------------	--

3:

Equation	Substitution
$T_{if} = T_{\#t} = T_{\#f}$	1) $T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$ 2) $T_{if} = T_{\#t} = T_{\#f}$
$T_{cond} = [T_x * T_y \rightarrow bool]$	
$T_{>} = [number * number \rightarrow bool]$	
$T_{\#t} = bool$	
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	
$T_x := T_{num8}$	
$T_y := T_{num3}$	
$T_{if} := T_0$	

4:

Equation	Substitution
$T_{cond} = [T_x * T_y \rightarrow bool]$	1) $T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$ 2) $T_{if} = T_{\#t} = T_{\#f}$ 3) $T_{cond} = [T_x * T_y \rightarrow bool]$
$T_{>} = [number * number \rightarrow bool]$	
$T_{\#t} = bool$	
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	
$T_x := T_{num8}$	
$T_y := T_{num3}$	
$T_{if} := T_0$	

5:

Equation	Substitution
$T_{>} = [number * number \rightarrow bool]$	1) $T_1 = [T_{num8} * T_{num3} \rightarrow T_0]$ 2) $T_{if} = T_{\#t} = T_{\#f}$ 3) $T_{cond} = [T_x * T_y \rightarrow bool]$ 4) $T_{>} = [number * number \rightarrow bool]$
$T_{\#t} = bool$	
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	
$T_x := T_{num8}$	
$T_y := T_{num3}$	
$T_{if} := T_0$	

6: (Fast forward...)

Equation	Substitution
$T_{\#t} = bool$	1) $T_1 = number * number \rightarrow T_0]$ 2) $T_{if} = bool$ 3) $T_{cond} = [T_x * T_y \rightarrow bool]$ 4) $T_{>} = [number * number \rightarrow bool]$ 5) $T_{\#t} = bool$ 6) $T_{\#f} = bool$ 7) $T_{num8} = number$ 8) $T_{num3} = number$
$T_{\#f} = bool$	
$T_{num8} = number$	
$T_{num3} = number$	
$T_x := T_{num8}$	
$T_y := T_{num3}$	
$T_{if} := T_0$	

7:

Equation	Substitution
$T_x := T_{num8}$	1) $T_1 = number * number \rightarrow T_0]$ 2) $T_{if} = bool$ 3) $T_{cond} = [number * number \rightarrow bool]$ 4) $T_{>} = [number * number \rightarrow bool]$ 5) $T_{\#t} = bool$ 6) $T_{\#f} = bool$ 7) $T_{num8} = number$ 8) $T_{num3} = number$ 9) $T_x := number$ 10) $T_y := number$
$T_y := T_{num3}$	
$T_{if} := T_0$	

8:

Equation	Substitution
$T_{if} := T_0$	1) $T_1 = number * number \rightarrow bool]$ 2) $T_{if} = bool$ 3) $T_{cond} = [number * number \rightarrow bool]$ 4) $T_{>} = [number * number \rightarrow bool]$ 5) $T_{\#t} = bool$ 6) $T_{\#f} = bool$ 7) $T_{num8} = number$ 8) $T_{num3} = number$ 9) $T_x := number$ 10) $T_y := number$ 11) $T_0 := bool$

2.

- a.  $\{f: [T1 \rightarrow T2], x: T1\} \vdash (f\ x): T2$   
**true** because the type of a function is its return type.
- b.  $\{f: [T1 \rightarrow T2], g: [T2 \rightarrow T3]\}, x: T2 \vdash (f\ g\ x): T3$   
**false** because the types are incompatible. The type of g is  $[T2 \rightarrow T3]$  but the function f gets the type T1.
- c.  $\{f: [T2 \rightarrow T1], g: [T1 \rightarrow T2], x: T1\} \vdash (f\ (g\ x)): T1$   
**true**. g(x) returns T2 and f goes from T2 to T1, so the type of the expression is T1.
- d.  $\{f: [T2 \rightarrow \text{Number}], x: \text{Number}\} \vdash (f\ x\ x): \text{Number}$   
**false** because the types are incompatible. f goes from T2 to number but x is of type number, so f cannot accept x.

3.

- a.  $\text{cons}: (x: T1, y: T2) \rightarrow \text{Pair}(T1, T2)$
- b.  $\text{car}: (\text{Pair}(T1, T2)) \rightarrow T1$
- c.  $\text{cdr}: (\text{Pair}(T1, T2)) \rightarrow T2$

4.

$f(x: T1) \rightarrow \text{Tuple}(T1, T1, T1)$

5.

- a.  $T1, T2 \Rightarrow \{T1 = T2\}$
- b.  $\text{Number}, \text{Number} \Rightarrow \{\}$  - (since number always equals number)
- c.  $[T1 * [T1 \rightarrow T2] \rightarrow \text{Number}], [[T3 \rightarrow \text{Number}][T4 \rightarrow \text{Number}] \rightarrow \text{Number}] \Rightarrow \{T1 = T4 = [T3 \rightarrow \text{Number}], T2 = \text{Number}\}$
- d.  $[T1 \rightarrow T1], [T1 \rightarrow [\text{Number} \rightarrow \text{Number}]] \Rightarrow \{T1 = [\text{Number} \rightarrow \text{Number}]\}$

## חלק 2.3

```
(define f
  (lambda (x)
    (values x (+ x 1))))
[(Number) => Tuple(Number, Number)]

(define g
  (lambda (x)
    (values "x" x)))
[(T) => Tuple(string,T)]
```

## חלק 4

As we learned in class:

- The type of functions returning Promises is more informative and similar to the simple types of synchronous versions
- We can chain sequences of asynchronous calls in a chain of `.then()` calls.
- We can aggregate error handling in a single handler for a chain of calls, in a way similar to exception handling.



```
export function* braid(generator1: Generator, generator2: Generator){
  const gen10p = generator1;
  const gen20p = generator2;
  for(let n=0;; n++){
    let x = gen10p.next()
    let y = gen20p.next()
    if(! (x.value === undefined) )
      yield x.value
    if(! (y.value === undefined) )
      yield y.value
    if ((x.value === undefined)&&(y.value === undefined))
      return x.value
  }
}
```

```
export function* biased(generator1: Generator, generator2: Generator){
  const gen10p = generator1;
  const gen20p = generator2;
  for(let n=0;; n++){
    let x = gen10p.next()
    let y = gen20p.next()
    if(! (x.value === undefined) )
      yield x.value;
    x = gen10p.next()
    if(! (x.value === undefined) )
      yield x.value;
    if(! (y.value === undefined) )
      yield y.value;
    if ((x.value === undefined) && (y.value === undefined))
      return x.value
  }
}
```

```
export function f(x: number): Promise<number>{  
  return new Promise<number>( (resolve : any, reject: any) => {  
    if( x != 0)  
      resolve(1/x);  
    else  
      reject("x = 0\n");  
  })  
}  
  
export function g (x: number): number{  
  return (x * x);  
}  
  
export function h (x: number): Promise<number> {  
  return f(g(x))  
}
```

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```
export const slower = (p1: Promise<any>, p2: Promise<any>): Promise<[number, string]> => {
  const pArr = [p1, p2];
  return new Promise<[number, string]>((resolve, reject) => {
    Promise.race([p1, p2]).then((value) => {
      Promise.all([p1, p2]).then((valsArr) => {
        pArr[getTheOtherOne(value, valsArr)].then((val) => {
          resolve ([getTheOtherOne(value, valsArr), val])).catch((v) => {reject(new
Error("error"))}))
        }).catch((v) => {reject(new Error("error"))}))
      }).catch((v) => {reject(new Error("error"))}))
    })
  })
}

const getTheOtherOne = (x: any, arr: any[2]) => {
  if(arr.indexOf(x) === 0){
    return 1;
  }
  else
    return 0;
}
```