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Tables and Figures

- Frequency Table

| Previous Ownership | Frequency | Relative Frequency |
|--------------------|-----------|--------------------------|
| None | 85 | $\frac{85}{500} = 0.17$ |
| Windows | 60 | $\frac{60}{500} = 0.12$ |
| Macintosh | 355 | $\frac{355}{500} = 0.71$ |
| Total | 500 | $\frac{500}{500} = 1$ |

- Stem and Leaf

| |
|---|
| 3 2337 2 001112223889 1 2244456888899 0 69 |
|---|

| |
|---|
| 3 7 3 233 2 889 2 001112223 1 56888899 1 22444 0 69 |
|---|

| | | |
|-----------|---|-----------|
| 11 | 4 | |
| | 3 | 7 |
| 332 | 3 | 233 |
| 8865 | 2 | 889 |
| 44331110 | 2 | 001112223 |
| 987776665 | 1 | 56888899 |
| 321 | 1 | 22444 |
| 7 | 0 | 69 |

Formulas

1. Box and Plot

| Name | Formula |
|-----------------------------|---|
| 25th Quartile / Lower Hinge | $\frac{(n+1)}{4}$ th term |
| 50th Quartile / Median | <p>When n is odd: $\frac{(n+1)}{2}$th term</p> <p>When n is even: $\frac{(\frac{n}{2})th\ term + ((\frac{n}{2})+1)th\ term}{2}$</p> |
| 75th Quartile / Upper Hinge | $\frac{3(n+1)}{4}$ th term |
| IQR / H-spread | Upper Hinge - Lower Hinge |
| Step | $1.5 \times HSpread$ |
| Upper Inner Fence | Upper Hinge + 1 Step |
| Lower Inner Fence | Lower Hinge - 1 Step |
| Upper Outer Fence | Upper Hinge + 2 Step |
| Lower Outer Fence | Lower Hinge - 2 Step |
| Upper Adjacent | Largest value below Upper Inner Fence |
| Lower Adjacent | Smallest value below Lower Inner Fence |
| Outlier | Values beyond Upper and Inner Fence |
| Extreme outlier | Values beyond Upper and Outer Fence |
| Outside Value | A value beyond an Inner fence but not beyond an Outer Fence |
| Far Out Value | A value beyond an Outer Fence |

2. Trimean

$$- \text{Trimean} = \frac{Q_1 + 2Q_2 + Q_3}{4}$$

3. Geometric Mean

- $\bar{x}_{geom} = \sqrt[n]{x_1 \times x_2 \times \dots \times x_n}$
- Usually questions will be per year/certain time frame with percentages of growth.
The growth will be in positive/negative percentages.
- Remember to change these into decimals then add 1.
- Ex: 10% = 0.1 = 1+0.1 = 1.1 (this is the growth)
- THEN you can put it in the formula
- Even after you get the result, subtract it by 1 again and convert to percentage.
- Ex: Geom = 1,045 = 1,045 - 1 = 0,045 = 4,5% (this is the average population grown based on the time frame given)

4. Trimmed Mean

- o Remove the values in the bottom X% and top X% of the dataset. Then, calculate the mean of the remaining values.
- o For these trimmed means, don't be confused if the trim given is the overall trim or the trim for each side.
- o Make it make sense, if the number of elements matches the amount to trim, then follow suit.
- o Example: 10 total elements, but it says trim by 10%. 5% off the front and back doesn't make sense, since 5% of 10 it's barely one element, so just do 10% off front and back.

5. Pearson's correlation

- o $r = \frac{\sum xy}{\sqrt{\sum x^2 \sum y^2}}$, where x is $X - \bar{X}$ and y is $Y - \bar{Y}$

6. Probability of a Single Event

- o $probability = \frac{possible\ outcomes}{total\ outcomes}$

7. Probability of 2 or more independent events

- o $P(A\ and\ B) = P(A) \times P(B)$

8. Probability of 2 or more dependent events

- o $P(A\ or\ B) = P(A) + P(B) - P(A\ and\ B)$

- It covers 3 possibilities:
 - 1) A occurs and B doesn't occur
 - 2) B occurs and A doesn't occur
 - 3) Both A and B occur

9. Permutations

- Used when the order matters
- ${}_nP_r = \frac{n!}{(n-r)!}$

10. Combinations

- Used when the order doesn't matter
- ${}_nC_r = \frac{n!}{r!(n-r)!}$

11. Binomial Distribution

- $P(x) = \frac{N!}{x!(N-x)!} \pi^x (1 - \pi)^{N-x}$
- N = number of trials
- x = number of successes
- π = probability of success
- $mean = N \times \pi$
- $\sigma^2 = N\pi(1 - \pi) \rightarrow$ variance

12. Poisson Distribution

- A discrete (countable) probability distribution, used to predict the number of times an event occurs.
- $p = \frac{e^{-\mu} \mu^x}{x!}$
- e = base of natural logarithms (2.7183)
- μ = mean number of successes
- x = number of successes in question
- example:

The mean number of calls to a fire station on a weekday is 8.

The probability that on a given weekday there would be 11 calls:

$$\circ p = \frac{e^{-8} 8^{11}}{11!} = 0.072$$

13. Multinomial Distribution

- Obtains a specific set of outcomes when there are k possible outcomes for every event.
- $$p = \frac{n!}{(n_1!)(n_2!)\dots(n_k!)} p_1^{n_1} p_2^{n_2} \dots p_k^{n_k}$$
- p = probability
- n = total number of events
- n_1 = number of times Outcome 1 occurs
- n_k = number of times Outcome k occurs
- p_1 = probability of Outcome 1
- p_k = probability of Outcome k

14. Hypergeometric Distribution

- Used to calculate probabilities when sampling without replacement
- $$p = \frac{{}_k C_x {}_{(N-k)} C_{(n-x)}}{{}_N C_n}$$
- k = total number of the group for success in the population (if your success is a red ball, how many red balls are there in total?)
- x = number of successes in the sample (what probability is it asking for?)
- N = total number of population (all the objects together without category)
- n = number of selections or samples (how many are we picking from the total?)
- ${}_k C_x$ = number of combinations of k things taken x at a time
- $mean = \frac{nk}{N}$
- $sd = \sqrt{\frac{(n)(k)(N-k)(N-n)}{N^2(N-1)}}$

15. Variance and Standard Deviation

- $Variance = \sigma^2 = \frac{\Sigma(x-\bar{x})^2}{N}$
- $SD = \sigma = \sqrt{npq} \rightarrow$ In normal distribution
- $SD = \sigma = \sqrt{\frac{\Sigma(x-\bar{x})^2}{N}} \rightarrow$ population
- $SD = \sigma = \sqrt{\frac{\Sigma(x-\bar{x})^2}{N-1}} \rightarrow$ sample (for t-test)

16. t-test for one sample

- $t = \frac{\bar{x} - \mu}{\frac{SD}{\sqrt{n}}}$
- \bar{x} = calculated mean
- μ = mean given in the question
- n = number of samples
- $df = n - 1$
- Reject the H_0 if the calculated t-value is beyond the t-critical value

17. t-test for two independent samples

- To test if the mean of two independent groups are different.
- $H_0 = \mu_1 = \mu_2$

Nondirectional:

$$\begin{aligned} H_0 : \mu_1 - \mu_2 &= 0 \\ H_1 : \mu_1 - \mu_2 &\neq 0 \end{aligned}$$

Directional, lower tail critical:

$$\begin{aligned} H_0 : \mu_1 - \mu_2 &\geq 0 \\ H_1 : \mu_1 - \mu_2 &< 0 \end{aligned}$$

Directional, upper tail critical:

$$\begin{aligned} H_0 : \mu_1 - \mu_2 &\leq 0 \\ H_1 : \mu_1 - \mu_2 &> 0 \end{aligned}$$

- “increases” or “improves” \rightarrow right tailed. Reject H_0 if t-value $>$ t-critical value
- “decreases” or “reduces” \rightarrow left tailed. Reject H_0 if t-value $<$ t-critical value

- $t = \frac{\bar{x}_A - \bar{x}_B}{\sqrt{\frac{SD_A^2}{n_A} + \frac{SD_B^2}{n_B}}}$

18. t-test for two related samples

Nondirectional:

$$H_0: \mu_D = 0$$

$$H_1: \mu_D \neq 0$$

Directional, lower tail critical:

$$H_0: \mu_D \geq 0$$

$$H_1: \mu_D < 0$$

Directional, upper tail critical:

$$H_0: \mu_D \leq 0$$

$$H_1: \mu_D > 0$$

$$\circ \quad t = \frac{\bar{x} - \mu}{\frac{SD}{\sqrt{n}}}$$

Step-by-Step Tutorials

Reminder: Critical Values and p-values are different variables.

1. Critical Values are obtained from the distribution tables for certain tests:
 - t-table ([one-tailed](#) / [two tailed](#))
 - One-tailed t-table critical values only cover left side, so if hypothesis asks for something increasing/involves using \geq , then it's $1 - P(X)$
 - Two-tailed critical value is \pm , reject null hypothesis if t-value is within the crit value
 - z-table ([negative](#) / [positive](#))
 - Left side describes the first two parts of the decimal of your calculated Z value.
 - Top side describes the hundredths place of your Z value.
 - f-table ($\alpha =$ [0.10](#) / [0.05](#) / [0.01](#))
 - Chi squared (pake calculator :D)
2. P-values are more of the probability, which you need to use a calculator to get. Usually, the p-value you can get from the calculated statistic and degree of freedom. After getting the p-value, compare it with the significance level which is the α . Reject H_0 if the p-value is less than the α .

- One Way ANOVA - Independent Measures

N = Total no. of ppl/objects in the experiment

n = No. of ppl/objects per group

a = No. of experimental groups/conditions

μ = Sample mean

SS = Sum of Squares

1. State Null and Alternate Hypothesis
 - $H_0 = \mu_1 = \mu_2 = \dots = \mu_n$.
 - H_1 = Not all μ 's are the same.
2. Find degrees of freedom
 - $df_{\text{between}} = a - 1$ (df numerator)

- $df_{\text{within}} = N - a$ (df denominator)
 - $df_{\text{total}} = N - 1$
3. Find critical value with the 2 df's calculated.

○ [Calculator](#) / [Table](#)

4. Calculate F-Statistic Value:

SS Between:

- $SS_{\text{between}} = \frac{\Sigma(\Sigma a_i)^2}{n} - \frac{T^2}{N}$ where:
 - i. $\Sigma(\Sigma a_i)^2$ is the sum of squared sums of all groups. $[(\Sigma A)^2 + (\Sigma B)^2 + \dots + (\Sigma Z)^2]$
 - Find total for Group A and square it, find total for Group B and square it, and so on for all groups.
 - ii. T^2 is the sum of all elements and then squared $[(\Sigma A) + (\Sigma B) + \dots + (\Sigma Z)]^2$
 - Add all elements together, then square it.

OR USE THIS:

Stupid Language Formula:

- $SS_{\text{between}} = n [(\text{mean of every group} - \text{grand mean})^2 + \dots + (\text{mean of every group} - \text{grand mean})^2]$

SS Within:

- $SS_{\text{within}} = \Sigma Y^2 - \frac{\Sigma(\Sigma a_i)^2}{n}$ where:
 - i. ΣY^2 is the sum of each value squared $[a^2 + b^2 + c^2 + \dots + z^2]$

OR USE THIS:

Stupid Language Formula:

- Calculate for every group:
 - $SS_{\text{within}} (\text{group A}) = (\text{every value in group A} - \text{mean of group A})^2 + \dots + (\text{every value in group A} - \text{mean of group A})^2$
 - $SS_{\text{within}} (\text{group B}) = (\text{every value in group B} - \text{mean of group B})^2 + \dots + (\text{every value in group B} - \text{mean of group B})^2$
- Continue for all groups
 - $SS_{\text{within}} = \text{Sum of all } SS_{\text{within}} \text{ groups}$

SS Total:

- $SS_{\text{total}} = SS_{\text{between}} + SS_{\text{within}}$

5. Find Mean Squares:

- $MS_{\text{between}} = \frac{SS_{\text{between}}}{df_{\text{between}}}$

- $MS_{\text{within}} = \frac{SS_{\text{within}}}{df_{\text{within}}}$

6. Calculate F Statistic:

- $F = \frac{MS_{\text{between}}}{MS_{\text{within}}}$

7. Compare F with the Critical Value:

- If calculated F-statistic > critical value, reject the null hypothesis.
- If calculated p-value < significance level, reject null hypothesis
 - There is **no accepting** of the null hypothesis, only rejecting and failure to reject it.

- Two Way ANOVA

N = Total no. of ppl/objects in the experiment

n = No. of ppl/objects per group

a = No. of experimental groups/conditions

μ = Sample mean

SS = Sum of Squares

p = number of categories in Group 1

q = number of categories in Group 2

σ = Mean Square

1. State Null and Alternate Hypothesis:

- H_0 = Means across Group 1 is the same
- H_0 = Means across Group 2 is the same
- H_0 = There is no interaction between Group 1 and Group 2

2. Calculate:

- Grand Mean = $\frac{\text{sum of all values}}{N}$
- Group 1 Mean = $\frac{\text{sum of values in group 1}}{n}$
- Group 2 Mean = $\frac{\text{sum of values in group 2}}{n}$
- Mean for every Group 1 x Group 2 combination
 - If Group 1 has m categories, and Group 2 has n categories, you need to find $m \times n$ different means.
 - Example, Group 1: Python, Java, C++ | Group 2: Self-learn, Instructed
 - Find mean of Python and Self-learn, Python and Instructed, Java and Self-learn, etc. (in this case you'll have 6 different means)

3. Total:

- $SS_{\text{total}} = (x_1 - \text{grand mean})^2 + \dots + (x_n - \text{grand mean})^2$
 - x here refers to each and every individual recorded value in the dataset.
- $df_{\text{total}} = n \times p \times q - 1$
- Mean Square $_{\text{total}} = \frac{SS_{\text{total}}}{df_{\text{total}}}$

4. Between:

- $SS_{\text{between}} = n \times ((\text{mean of every category} - \text{grand mean})^2 + \dots + (\text{mean of every category} - \text{grand mean})^2)$
 - Get the sum first THEN multiply with the n.
 - Mean of every category is the one from the previous example where its the mean of the combination of Group 1 and Group 2
 - Example, Mean of Python and Self-learn is 6.4:
 - In formula, that would be $(6.4 - \text{Grand Mean})^2 + \dots$
- $df_{\text{between}} = p \times q - 1$
- $\text{Mean Square}_{\text{between}} = \frac{SS_{\text{between}}}{df_{\text{between}}}$

5. Group 1:

- $SS_{\text{group 1}} = n \times q \times (\text{mean of every category for group 1} - \text{grand mean})^2 + \dots + (\text{mean of every category for group 1} - \text{grand mean})^2$
 - Example, if the categories in group 1 are Python, Java and C++, only use the means of those values.
- $df_{\text{group 1}} = p - 1$
- $\text{Mean Square}_{\text{group 1}} = \frac{SS_{\text{group 1}}}{df_{\text{group 1}}}$

6. Group 2:

- $SS_{\text{group 2}} = n \times p \times [(\text{mean of every category for group 2} - \text{grand mean})^2 + \dots + (\text{mean of every category for group 2} - \text{grand mean})^2]$
- Example, if the categories in Group 2 are Self-learn and Instructed, only use the means of those values.
- $df_{\text{group 2}} = q - 1$
- $\text{Mean Square}_{\text{group 2}} = \frac{SS_{\text{group 2}}}{df_{\text{group 2}}}$

7. Interaction:

- $SS_{\text{interaction}} = SS_{\text{between}} - SS_{\text{group 1}} - SS_{\text{group 2}}$
- $Df_{\text{interaction}} = (p - 1)(q - 1)$
- $\text{Mean Square}_{\text{interaction}} = \frac{SS_{\text{interaction}}}{df_{\text{interaction}}}$

8. Error:

- $SS_{\text{error}} = (\text{every sample} - \text{the mean of its respective category})^2 + \dots + (\text{every sample} - \text{the mean of its respective category})^2$
- $Df_{\text{error}} = (n - 1) \times p \times q$
- $\text{Mean Squares}_{\text{error}} = \frac{SS_{\text{error}}}{df_{\text{error}}}$

9. F-Values:

- F Value Group 1: $\frac{\text{Mean Square}_{\text{Group 1}}}{\text{Mean Square}_{\text{Error}}}$
- F Value Group 2: $\frac{\text{Mean Square}_{\text{Group 2}}}{\text{Mean Square}_{\text{Error}}}$
- F Value Interaction: $\frac{\text{Mean Square}_{\text{Interaction}}}{\text{Mean Square}_{\text{Error}}}$

10. Null Hypothesis:

- Pick either method depending on what ur told to do in the question
- P-Value Method
 - Input into P Value Calculator, find P value.
 - Input F-Value Group 1, $df_{\text{group 1}}$ (df numerator), and Df_{error} (df denominator)
 - Continue for F values of Group 2 and Interaction (df denominator is df_{error} for all)
 - If value is less than the alpha given in question (in this case 0.05), reject null hypothesis.
 - If any of the f values are greater than the null hypothesis, then fail to reject hypothesis.
- F-Critical Method
 - Find F-Critical Value with calculator/table.
 - Input alpha (α), $Df_{\text{group 1}}$ (df numerator), and Df_{error} (df denominator)
 - Find F-Critical Value for Group 2 and Interaction as well.
 - If F value greater than F-Critical, reject null hypothesis. If smaller than, fail to reject null hypothesis.
- **Chi Square**

<https://www.socscistatistics.com/tests/chisquare2/default2.aspx>

- 1) H_0 = The 2 groups are independent
 H_1 = The 2 groups are not independent.

- 2) Calculate expected Frequency Table:

$$E_{ij} = \frac{\text{Row Total} \times \text{Column Total}}{\text{Grand Total}}$$

- 3) Calculate the Chi-Square

For every cell:

$$X = \frac{(\text{Original value} - \text{expected frequency})^2}{\text{expected frequency}}$$

$$X^2 = \text{Sum of all } X \text{ from all cells}$$

- 4) Calculate Degree of Freedom

$$df = (\text{no of rows} - 1) \times (\text{no of columns} - 1)$$

- 5) Get the critical value from the table or get p value with calculator.

- 6) Reject H_0 if $X^2 > \text{critical value}$.

Reject H_0 if p value < significance level.

Links

1. Casio Scientific Calculator:
 - <https://mathda.com/calculator/>
2. 5 Number Summary + IQR + Inner Outer Fence + Outliers + Geometric Mean + Sum of Squares + Standard Deviation (Sample/Population) + Variance Calculator:
 - <https://www.hackmath.net/en/calculator/five-number-summary>
3. Trimmed Mean Calculator:
 - [Trimmed Mean Calculator](#)
4. Permutation Combination Calculator:
 - <https://www.calculator.net/permutation-and-combination-calculator.html>
5. Binomial Distribution (Singular and Cumulative):
 - <https://stattrek.com/online-calculator/binomial>
6. Pearson's Correlation Coefficient:
 - <https://www.socscistatistics.com/tests/pearson/default2.aspx>
7. One Way ANOVA - Independent Measures
 - <https://www.socscistatistics.com/tests/anova/default2.aspx>
8. Two Way ANOVA
 - [Two-Way-ANOVA Calculator - With AI Interpretation - DATAtab](#)
9. Single Sample T-Test:
 - <https://www.socscistatistics.com/tests/tsinglesample/default.aspx>
10. Chi-Square Test:
 - <https://www.socscistatistics.com/tests/chisquare2/default2.aspx>
11. Critical Value for Multiple Tests:
 - <https://www.socscistatistics.com/tests/criticalvalues/default.aspx>
12. P Value Calculator and F Critical Table for ANOVA Test:
 - <https://datatab.net/tutorial/f-distribution>
13. Pearson Edexcel Formula Book, Statistics S1, S2 and S3 with complete Z table, Normal Distribution Table (z table), and Statistical Formula(Page 14 - 23)
 - <https://qualifications.pearson.com/content/dam/pdf/International%20Advanced%20Level/Mathematics/2018/Specification-and-Sample-Assessment/IAL-Mathematics-Formula-Book.pdf>

Exercises

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[Exercise 1 - Answers](#)

[Exercise 2 - Answers](#)

[Exercise 3 - Answers](#)

[Exercise 4 - Answers](#)

[Exercise 5 - Answers](#)

[Exercise 6 - Answers](#)

[Exercise 7 - Answers](#)