EDDA Assignment2 - Group 22

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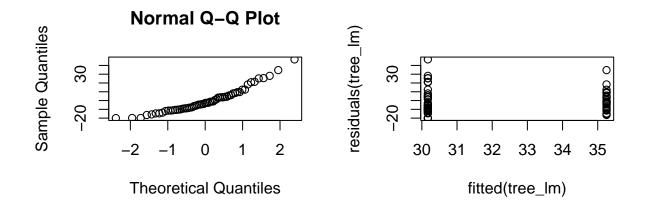
Exercise 1 a)

```
tree = read.table(file = "treeVolume.txt", header = TRUE)
tree$type = as.factor(tree$type)
```

ANOVA: The null hypothesis is that the mean volume of type beech is equal to the mean volume of type oak.

The p-value (0.1736) is not significant. So H_0 cannot be rejected and we cannot say that tree type has any significant influence on volume.

Diagnostics for ANOVA



The residuals QQ-norm plot looks normal and the plot of the fitted model and residuals show no pattern. Hence, the assumptions of ANOVA hold.

summary(tree_lm)\$coefficients

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 30.170968 2.539425 11.88102 4.681462e-17
## typeoak 5.079032 3.686229 1.37784 1.736384e-01
```

We can estimate the volumes of the two tree types. For type: beech, $Volume = \mu + \alpha_1 = 30.171$ and for type: oak, $Volume = \mu + \alpha_2 = 30.171 + 5.079 = 35.25$.

t-test Yes, the t-test is related to the above test; because we only have one factor with two levels, we can do a two-sample t-test to see if there is a difference in mean tree volume among these tree types and end up with the same conclusion.

```
library(tidyr)
tree_table_2 <- tree[, c("type", "volume")]
t.test(tree_table_2[tree_table_2$type == "beech", ]$volume, tree_table_2[tree_table_2$type == "oak", ]$volume, paired = FALSE)</pre>
```

T-test also not rejected, the mean volume of the two types of trees is not significantly different. b)

```
tree_model1 <- lm(volume ~ diameter * type, data = tree)
summary(tree_model1)$coefficients</pre>
```

```
## (Intercept) -36.9434591 3.1890267 -11.5845561 2.217267e-16
## diameter 5.0658564 0.2344302 21.6092285 1.506778e-28
## typeoak 2.8090341 6.1252469 0.4585993 6.483290e-01
## diameter:typeoak -0.3250953 0.4241775 -0.7664134 4.467075e-01
```

We see that diameter has a significant influence on volume. But the interaction between type and diameter is not significant (p-value > 0.05). This means that there is no significant dependence between the two. So, there is no significant difference in the influence of diameter on volume for the two different tree types. They are similar.

```
tree_model2 <- lm(volume ~ height * type, data = tree)
summary(tree_model2)$coefficients</pre>
```

```
## (Intercept) -87.123614 27.0249998 -3.223816 2.129291e-03
## height 1.543350 0.3543888 4.354962 5.848926e-05
## typeoak 98.699466 42.4745519 2.323732 2.386271e-02
## height:typeoak -1.230525 0.5586737 -2.202582 3.183357e-02
```

The above results suggests significant influence of height on volume as well as the interaction on the volume. This means the effect of height on the volume depends on the type of tree.

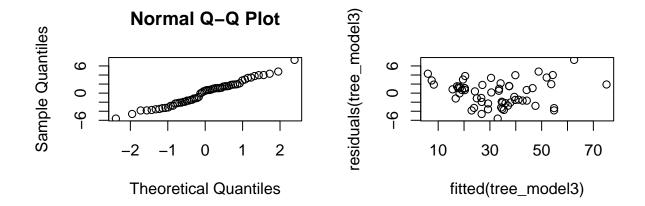
```
tree_model3 <- lm(volume ~ height * diameter, data = tree)
summary(tree_model3)</pre>
```

```
##
## Call:
  lm(formula = volume ~ height * diameter, data = tree)
## Residuals:
##
       Min
                10
                    Median
                                3Q
                                        Max
## -5.6159 -2.1025
                    0.5296
                                    7.3380
                            1.6942
##
##
  Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              19.76957
                                          1.338
                                                0.18642
                   26.45042
## height
                   -0.79381
                               0.26630
                                         -2.981
                                                 0.00427 **
## diameter
                   -1.86698
                                1.38049
                                         -1.352
                                                 0.18178
## height:diameter
                   0.08713
                                          4.731
                                                 1.6e-05 ***
                               0.01842
## ---
                   0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 2.788 on 55 degrees of freedom
## Multiple R-squared: 0.9637, Adjusted R-squared: 0.9617
## F-statistic: 486.5 on 3 and 55 DF, p-value: < 2.2e-16
```

The above model also suggests a very significant interaction between height and diameter. **c)** We also try including the type to the $tree_model3$ above. But we can see that now, the it is not significant enough and the R^2 value doesn't change and adjusted- R^2 slightly decreases. So we prefer $tree_model3$ without the type factor.

```
tree_model4 <- lm(volume ~ height * diameter + type, data = tree)
summary(tree_model4)$adj.r.squared</pre>
```

[1] 0.9612065



Predicting Volume

```
avg_diameter = mean(tree$diameter)
avg_height = mean(tree$height)
volume_oak = predict(tree_model3, (data.frame(diameter = avg_diameter,
    height = avg_height, type = "oak")), type = "response")[[1]]
volume_beech = predict(tree_model3, (data.frame(diameter = avg_diameter,
    height = avg_height, type = "beech")), type = "response")[[1]]
volume_oak
```

[1] 32.1868

```
volume_beech
```

```
## [1] 32.1868
```

d) We know that volume of a tree trunk can be approximately written as: $\pi * (diameter/2)^2 * height$. So, we propose a transformation $diameter \rightarrow diameter^2$.

```
tree$diametersq = tree$diameter * tree$diameter
final_model = lm(volume ~ diametersq * height, data = tree)
summary(final_model)
```

```
##
## Call:
## lm(formula = volume ~ diametersq * height, data = tree)
## Residuals:
               1Q Median
                               3Q
                                      Max
## -5.4173 -1.1104 -0.2242 1.4632 5.3837
##
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    -3.894320 8.794942 -0.443
                                                    0.66
## diametersq
                    -0.002424
                               0.038491 -0.063
                                                    0.95
## height
                     0.050646
                                0.118361
                                         0.428
                                                    0.67
## diametersq:height 0.002155
                                0.000511
                                         4.217 9.3e-05 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 2.303 on 55 degrees of freedom
## Multiple R-squared: 0.9752, Adjusted R-squared: 0.9739
## F-statistic: 721.7 on 3 and 55 DF, p-value: < 2.2e-16
```

Clearly, this is a better model with a higher R^2 and adjusted- R^2 value. The interaction between diameter-square is significant too.

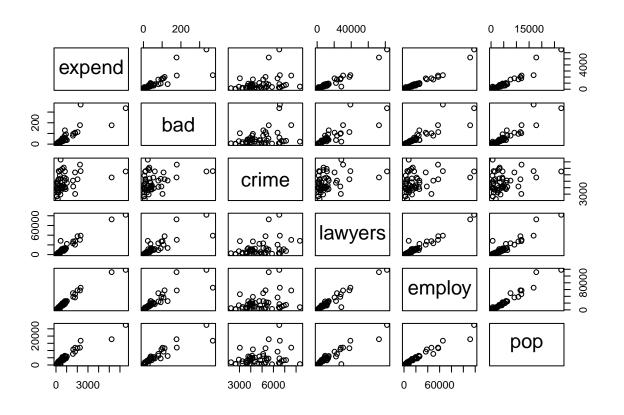
Exercise 2 a)

```
expense = read.table("expensescrime.txt", header = TRUE)
```

summary(expense)

```
##
      state
                                                          crime
                         expend
                                          bad
                     Min. : 74.0
                                      Min. : 2.40
##
   Length:51
                                                      Min.
                                                             :2253
                      1st Qu.: 214.5
##
   Class : character
                                      1st Qu.: 10.30
                                                      1st Qu.:3898
   Mode :character
                     Median : 463.0
                                      Median : 31.30
                                                      Median:4549
                      Mean : 847.8
                                      Mean : 54.12
##
                                                      Mean
                                                             :4802
##
                      3rd Qu.: 850.5
                                      3rd Qu.: 58.00
                                                      3rd Qu.:5576
##
                      Max. :6539.0
                                      Max.
                                           :370.10
                                                      Max.
                                                             :8339
##
      lawyers
                       employ
                                        pop
   Min. : 1116
                   Min. : 1969
                                   Min. : 490
##
   1st Qu.: 2811
                   1st Qu.: 5304
                                   1st Qu.: 1135
##
   Median: 7535
                   Median : 13167
                                   Median: 3296
##
##
   Mean
         :12892
                   Mean : 20602
                                   Mean
                                        : 4773
                                   3rd Qu.: 5693
##
   3rd Qu.:13128
                   3rd Qu.: 23692
   Max.
        :82001
                   Max.
                        :118149
                                   Max.
                                        :27663
```

pairs(expense[, -1])



round(cor(expense[, -1]), 2)

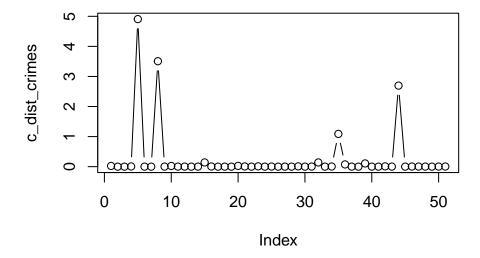
```
## expend bad crime lawyers employ pop
## expend 1.00 0.83 0.33 0.97 0.98 0.95
## bad 0.83 1.00 0.37 0.83 0.87 0.92
```

```
## crime
             0.33 0.37 1.00
                                 0.38
                                         0.31 0.28
## lawyers
             0.97 0.83
                         0.38
                                 1.00
                                         0.97 0.93
             0.98 0.87
                                         1.00 0.97
## employ
                         0.31
                                 0.97
             0.95 0.92
                                 0.93
                                         0.97 1.00
## pop
                         0.28
```

The following pairs seems to have high collinearity: expend-lawyers (0.97), expend-employ (0.98), expend-pop (0.95), bad-pop (0.92), pop-lawyers (0.93), employ-lawyers (0.97), employ-pop (0.97).

Investigating Influence points:From the pairwise scatterplots, we can clearly see linear relations between many variables. To check influence points we can do cooks distance

```
c_dist_crimes = cooks.distance(lm(expend ~ bad + crime + lawyers +
    employ + pop, data = expense))
plot(c_dist_crimes, type = "b")
```



```
influence = c_dist_crimes > 1
influence[influence == TRUE]
```

```
## 5 8 35 44
## TRUE TRUE TRUE TRUE
```

Points 5, 8, 35, and 44 in the figure above have Cook's distances greater than one, so they were classified as influence points.

b.) STEP UP: Step1:

```
library(broom)
mod1 = lm(expend ~ bad, data = expense)
summary(mod1)$r.squared
```

[1] 0.6963839

```
mod2 = lm(expend ~ crime, data = expense)
summary(mod2)$r.squared
## [1] 0.1118564
mod3 = lm(expend ~ lawyers, data = expense)
summary(mod3)$r.squared
## [1] 0.9372789
mod4 = lm(expend ~ employ, data = expense)
summary(mod4)$r.squared # has greatest r^2 value
## [1] 0.9539745
mod5 = lm(expend ~ pop, data = expense)
summary(mod5)$r.squared
## [1] 0.9073261
summary(mod4) #p-value significant
##
## Call:
## lm(formula = expend ~ employ, data = expense)
##
## Residuals:
##
      Min
                                3Q
                1Q Median
                                       Max
## -636.04 -84.35 47.60 107.99 1124.70
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.167e+02 4.706e+01 -2.48 0.0166 *
            4.681e-02 1.469e-03 31.87 <2e-16 ***
## employ
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 257.4 on 49 degrees of freedom
## Multiple R-squared: 0.954, Adjusted R-squared: 0.953
## F-statistic: 1016 on 1 and 49 DF, p-value: < 2.2e-16
The model with employ variable yields the highest R^2 = 0.954 value. As it is also significant (p-value
<2e-16), we add employ to our model.
Step2:
mod6 = lm(expend ~ employ + bad, data = expense)
summary(mod6)$r.squared
```

```
mod7 = lm(expend ~ employ + crime, data = expense)
summary(mod7)$r.squared
## [1] 0.9550501
mod8 = lm(expend ~ employ + lawyers, data = expense)
summary(mod8)$r.squared
## [1] 0.9631745
summary(mod8)
## Call:
## lm(formula = expend ~ employ + lawyers, data = expense)
## Residuals:
##
      Min
                1Q Median
                                3Q
## -599.47 -94.43 36.01 91.98 936.55
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.107e+02 4.257e+01 -2.600 0.01236 *
## employ
              2.971e-02 5.114e-03 5.810 4.89e-07 ***
               2.686e-02 7.757e-03 3.463 0.00113 **
## lawyers
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 232.6 on 48 degrees of freedom
## Multiple R-squared: 0.9632, Adjusted R-squared: 0.9616
## F-statistic: 627.7 on 2 and 48 DF, p-value: < 2.2e-16
mod9 = lm(expend ~ employ + pop, data = expense)
summary(mod9)$r.squared
## [1] 0.95431
Adding variable lawyers results in maximum increase in \mathbb{R}^2 and it is also significant from the results above.
Step3:
mod10 = lm(expend ~ employ + lawyers + bad, data = expense)
summary(mod10)r.squared # r^2
## [1] 0.9638741
summary(mod10)$coefficients[4, 4] #p-value
```

[1] 0.344957

```
mod11 = lm(expend ~ employ + lawyers + crime, data = expense)
summary(mod11)$r.squared
```

[1] 0.9631881

```
summary(mod11)$coefficients[4, 4]
```

[1] 0.8957792

```
mod12 = lm(expend ~ employ + lawyers + pop, data = expense)
summary(mod12)$r.squared
```

[1] 0.9637326

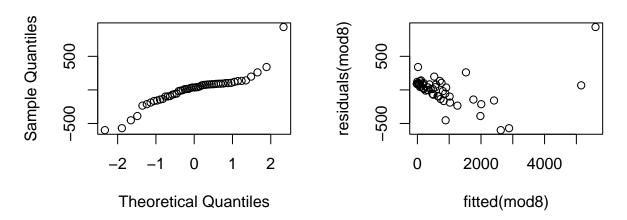
```
summary(mod12)$coefficients[4, 4]
```

[1] 0.399392

Adding any of the more variables does not cause a considerable increase in R^2 and all of them are insignificant (p-values>0.05). Hence, our best model is mod8: expend = (-1.107e+02)+(2.971e-02)*employ+(2.686e-02)*lawyers+error.

Diagnostics

Normal Q-Q Plot



Data does not look to be normal and the fitted-residuals plot seems to show some negative collinearity.

```
# Checking for collinearity
library(car)
```

Loading required package: carData

```
vif(mod8)
```

```
## employ lawyers
## 14.83915 14.83915
```

The Vif values very high. Hence, there might be slight collinearity between the variables (which we had also observed from our graphical analysis).

c) Prediction interval for a (hypothetical) state with bad=50, crime=5000, lawyers=5000, employ=5000 and pop=5000.

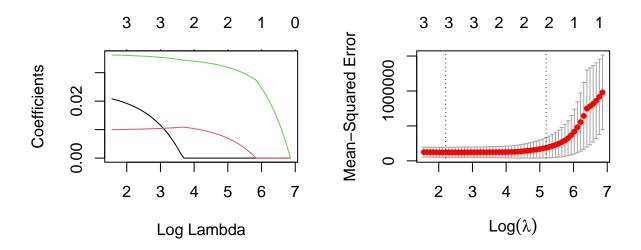
```
## fit lwr upr
## 1 172.2098 -302.9307 647.3504
```

x.train = x[train,]

We can improve this interval by taking the confidence-interval as it is narrower than the prediction interval since the error is not taken into account in CI.

```
newxdata = data.frame(bad = 50, crime = 5000, employ = 5000,
    lawyers = 5000, pop = 5000)
predict(mod8, newxdata, interval = "confidence", level = 0.95)
          fit
                   lwr
                            upr
## 1 172.2098 88.32196 256.0977
d) LASSO
expense = read.table("expensescrime.txt", header = TRUE)
library(glmnet)
## Loading required package: Matrix
##
## Attaching package: 'Matrix'
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
## Loaded glmnet 4.1-6
expense = expense[, -1]
x = as.matrix(expense[, -1]) # remove the response variable
y = as.double(as.matrix(expense[, 1])) # only the response variable expend
train = sample(1:nrow(x), 0.67 * nrow(x)) # train by using 2/3 of the data.
```

```
y.train = y[train] # data to train
x.test = x[-train, ]
y.test = y[-train] # data to test
lasso.mod = glmnet(x.train, y.train, alpha = 1) # lasso model
lasso.cv = cv.glmnet(x.train, y.train, alpha = 1, type.measure = "mse")
par(mfrow = c(1, 2))
plot(lasso.mod, label = T, xvar = "lambda") #have a look at the lasso path
plot(lasso.cv) # the best lambda by cross-validation
```



```
lambda.1se = lasso.cv$lambda.1se
coef(lasso.mod, s = lasso.cv$lambda.1se) #beta's for the best lambda

## 6 x 1 sparse Matrix of class "dgCMatrix"

## s1

## (Intercept) 1.098690e+02

## bad .

## crime .

## lawyers 5.876409e-03

## employ 3.118708e-02

## pop .
```

The LASSO regression method chooses lawyers and employ as the relevant variables. The coefficients can be observed in the output above.

```
# Prediction by using the linear model first fit linear
# model on the train data

y.predict.lm = predict(mod8, newdata = expense[-train, ]) # predict for the test rows
mse.lm = mean((y.test - y.predict.lm)^2)
mse.lm # prediction quality by the linear model
```

[1] 78414.05

```
lasso.pred = predict(lasso.mod, s = lambda.1se, newx = as.matrix(x.test))
mse2.lasso = mean((y.test - lasso.pred)^2)
mse2.lasso
```

[1] 311977

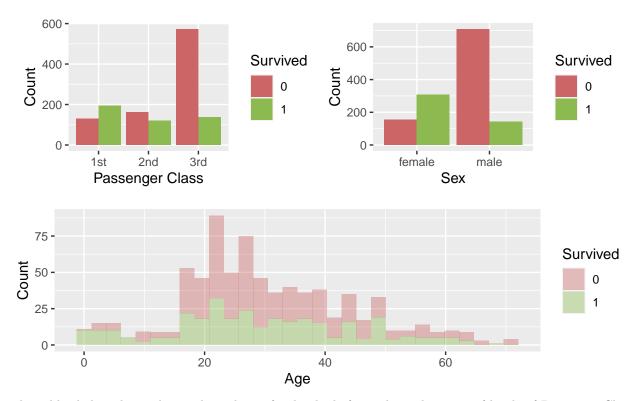
When we compare the mean-squared-errors of the Lasso model above with our linear model from b.(mod8), lasso yields a better mse.

Exercise 3

```
titanic = read.table(file = "titanic.txt", header = TRUE)
titanic_new <- na.omit(titanic)</pre>
```

The Age variable in the data has some 557 missing values. NA values have been omitted from the data.

a.)Graphics and tables



The tables below shows the total numbers of individuals for each combination of levels of Passenger Class and Sex, combination of Survival and Sex and number of survivals in terms of Passenger Class and Sex respectively.

```
tot = xtabs(~PClass + Sex, data = titanic)
knitr::kable(tot)
```

	female	male
1st	143	179
2nd	107	173

	female	male
3rd	212	499

```
tot.se = xtabs(~Survived + Sex, data = titanic)
knitr::kable(tot.se)
```

	female	male
0	154	709
1	308	142

```
tot.s = xtabs(Survived ~ PClass + Sex, data = titanic)
knitr::kable(tot.s)
```

	female	male
1st	134	59
2nd	94	25
3rd	80	58

Logistic Regression Model

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.75966210 0.397567324 9.456668 3.179129e-21
## PClass2nd -1.29196240 0.260075781 -4.967638 6.777324e-07
## PClass3rd -2.52141915 0.276656805 -9.113888 7.948131e-20
## Age -0.03917681 0.007616218 -5.143868 2.691392e-07
## Sexmale -2.63135683 0.201505379 -13.058494 5.684093e-39
```

```
drop1(model_titanic, test = "Chisq")
```

```
## Single term deletions
##
## Model:
## Survived ~ PClass + Age + Sex
         Df Deviance
                       AIC
                              LRT Pr(>Chi)
## <none>
              695.14 705.14
## PClass 2 795.59 801.59 100.445 < 2.2e-16 ***
## Age
         1 723.59 731.59 28.454 9.595e-08 ***
          1 909.92 917.92 214.776 < 2.2e-16 ***
## Sex
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Here we can see that all predictors are significant. The odds is the probability of success divided by the probability of failure. From the summary table we can see that the odds of survival for an individual is exp(3.7597 + PClass2nd* -1.2920 + PClass3rd* -2.5214 + Sexmale* -2.6314 + Age* -0.0392).

For example, odds of survival for a 26 year old middle class male and female passengers

[1] 0.3063889

```
female_middle_class
```

```
## [1] 4.256725
```

From the example above, 2nd PClass female has higher odds of survival compared to 2nd PClass male.

b)

```
model_1 <- glm(Survived ~ Age * Sex, data = titanic_new, family = binomial)
summary(model_1)$coefficients</pre>
```

```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.30110864 0.29897816 1.007126 3.138743e-01
## Age 0.02935105 0.01007529 2.913174 3.577757e-03
## Sexmale -0.59985816 0.40804956 -1.470062 1.415450e-01
## Age:Sexmale -0.06571791 0.01368620 -4.801765 1.572730e-06
```

```
model_2 <- glm(Survived ~ Age * PClass, data = titanic_new, family = binomial)
summary(model_2)$coefficients</pre>
```

```
## (Intercept) 1.922979534 0.436245818 4.4080183 1.043207e-05
## Age -0.035837742 0.009955455 -3.5998095 3.184504e-04
## PClass2nd -0.744276585 0.571547192 -1.3022137 1.928433e-01
## PClass3rd -2.290071973 0.540572606 -4.2363818 2.271504e-05
## Age:PClass2nd -0.013209098 0.015868842 -0.8323921 4.051877e-01
## Age:PClass3rd 0.004642132 0.015941232 0.2912028 7.708962e-01
```

To investigate the interaction of predictor Age with PClass, and the interaction of Age with Sex, two logistic regression models were created above. From these models we can see that there is significant interaction between Age and Sex, and there is no significant interaction between Age and PClass. Now we create a model with the Age and Sex interaction

```
## (Intercept) 2.75656302 0.43764171 6.2986753 3.002001e-10
## PClass2nd -1.54336652 0.28735776 -5.3708886 7.834962e-08
## PClass3rd -2.65398052 0.29142296 -9.1069712 8.471384e-20
## Age 0.00244348 0.01140798 0.2141903 8.303986e-01
## Sexmale -0.50818658 0.44251492 -1.1484055 2.508012e-01
## Age:Sexmale -0.07559126 0.01500877 -5.0364712 4.741923e-07
```

Age:Sexfemale 0.01080822 0.008942977 1.208570 2.268280e-01

Age:Sexmale

Now Age and sex are not significant anymore, therefore the final model would only consist of their interaction as an estimator. Then we end-up with the variables PClass and interaction of Age and Sex. Therfore, the chosen final model is shown below: $final_model$.

Then the estimate for the probability of survival for each combination of levels of the factors PClass and Sex for a person of age 55:

-0.08022407 0.009173972 -8.744747 2.235162e-18

PClass	Sex	Age	Survival
1st	female	55	0.957
2nd	female	55	0.820
3rd	female	55	0.606
1st	male	55	0.129
2nd	male	55	0.030
3rd	male	55	0.010

c) To predict the survival status we create a logistic regression model on our given data-set then use this model to make predictions for unseen data-points. For a new data vector X, we can predict its success probability $\hat{P} = \frac{1}{1+e^{-x^T\theta}}$. Now, we use \hat{P} to predict the new survival status by comparing with some threshold $p_0 \in [0, 1]$. We can use accuracy accuracy as a quality measure for our prediction. d) The Fischer test is appropriate for investigating the effect of sex on survival since the data is in a 2x2 contingency table.

```
# contingency table and Fisher's exact test for Sex and
# Survived
tab1 <- table(titanic$Survived, titanic$Sex)
tab1_margins <- addmargins(tab1)
knitr::kable(tab1_margins)</pre>
```

	female	male	Sum
0	154	709	863
1	308	142	450
Sum	462	851	1313

```
fisher_res <- fisher.test(tab1)
fisher_res</pre>
```

```
##
## Fisher's Exact Test for Count Data
##
## data: tab1
## p-value < 2.2e-16
## alternative hypothesis: true odds ratio is not equal to 1
## 95 percent confidence interval:
## 0.07620521 0.13155709
## sample estimates:
## odds ratio
## 0.1003494</pre>
```

A Chi-square test is suitable for examining the influence of class on survival since the data is in a 2x3 contingency table and over 80% of the values have a value of more than 5.

```
# contingency table and chi-square test for PClass and
# Survived
tab2 <- table(titanic$Survived, titanic$PClass)
tab2_margins <- addmargins(tab2)
knitr::kable(tab2_margins)</pre>
```

```
\operatorname{Sum}
        1st
               2nd
                      3rd
        129
                      573
               161
                               863
1
        193
               119
                      138
                               450
Sum
        322
               280
                      711
                             1313
```

```
chi_res <- chisq.test(tab2)
chi_res</pre>
```

```
##
## Pearson's Chi-squared test
##
## data: tab2
## X-squared = 172.3, df = 2, p-value < 2.2e-16</pre>
```

From the results of the chi-square and fisher tests it can be seen that both Sex and PClass have a significant effect on survival. e) The second approach, which involves using a contingency table with the Fisher and chi-squared test, is not necessarily wrong. However, the most appropriate method for answering this question is the contingency table with the Fisher and chi-squared test. This approach is suitable because it can help to determine whether the Survived variable is independent of the gender and class variables.

The choice between using the contingency table with the chi-squared test or logistic regression depends on the problem. Logistic regression is advantageous when we want to compute a probability, in this case, the probability that a person with a certain age, class, and gender will survive. On the other hand, the chi-squared test can be used to determine whether the reason a person survived is independent of their gender or class.

Exercise 4

```
coup_data = read.table(file = "coups.txt", header = TRUE)
```

a) Poisson regression

```
coup_data$pollib = as.factor(coup_data$pollib)
coupglm = glm(miltcoup ~ oligarchy + pollib + parties + pctvote +
    popn + size + numelec + numregim, family = poisson, data = coup_data)
summary(coupglm)
```

```
##
## Call:
  glm(formula = miltcoup ~ oligarchy + pollib + parties + pctvote +
##
       popn + size + numelec + numregim, family = poisson, data = coup_data)
##
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   30
                                           Max
  -1.5075
##
           -0.9533 -0.3100
                               0.4859
                                        1.6459
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -0.2334274 0.9976112 -0.234 0.81500
## oligarchy
                0.0725658
                           0.0353457
                                       2.053
                                              0.04007 *
## pollib1
               -1.1032439
                           0.6558114
                                     -1.682
                                              0.09252 .
## pollib2
               -1.6903057
                           0.6766503
                                      -2.498
                                              0.01249 *
                           0.0111663
## parties
                0.0312212
                                       2.796
                                              0.00517 **
## pctvote
                0.0154413
                           0.0101027
                                       1.528
                                              0.12641
## popn
                0.0109586
                           0.0071490
                                       1.533
                                              0.12531
## size
               -0.0002651
                           0.0002690
                                      -0.985
                                              0.32444
## numelec
               -0.0296185
                           0.0696248
                                      -0.425
                                              0.67054
                                       0.902
                0.2109432
                           0.2339330
                                              0.36720
## numregim
##
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##
       Null deviance: 65.945 on 35 degrees of freedom
## Residual deviance: 28.249 on 26 degrees of freedom
## AIC: 113.06
##
## Number of Fisher Scoring iterations: 5
```

Only oligarchy, pollib, and parties variables show a significant effect with a p-value < 0.05, for the pollib factor variable we also see that only pollib2 level (full civil rights) has a significant influence. Additionally, numelec and the number of regime (numregim) seem to have the least influence on the number of coups. b) **Step down Step 1:** Explanatory variable numelec has the highest p-value in the above model. So our first step in the step-down process is removing numelec.

```
coup_1 = glm(miltcoup ~ oligarchy + pollib + parties + pctvote +
    popn + size + numregim, family = poisson, data = coup_data)
summary(coup_1)$coefficients
```

```
##
                    Estimate
                               Std. Error
                                             z value
                                                        Pr(>|z|)
## (Intercept) -0.4577458289 0.8602344719 -0.5321175 0.594644608
## oligarchy
                0.0812015376 0.0288154207
                                           2.8179890 0.004832547
## pollib1
               -0.9642975542 0.5620939337 -1.7155452 0.086245314
## pollib2
              -1.5149509438 0.5269441006 -2.8749747 0.004040599
## parties
               0.0293409468 0.0103100564
                                           2.8458571 0.004429207
                0.0139115305 0.0094653971
## pctvote
                                           1.4697250 0.141636255
                0.0099592030 0.0067248724
                                           1.4809505 0.138619769
## popn
## size
               -0.0002687704 0.0002686512 -1.0004436 0.317095873
               0.1804415213 0.2241166271 0.8051233 0.420748524
## numregim
```

Step2: The next highest insignificant p-value is numeregim. So removing that-

```
coup_2 = glm(miltcoup ~ oligarchy + pollib + parties + pctvote +
    popn + size, family = poisson, data = coup_data)
summary(coup_2)$coefficients
```

```
##
                                                         Pr(>|z|)
                    Estimate
                               Std. Error
                                              z value
## (Intercept) 0.0419756813 0.5774100214 0.07269649 0.942047643
## oligarchy
               0.0894950616 0.0270440021 3.30923882 0.000935500
## pollib1
               -0.9673252804 0.5605601269 -1.72564054 0.084412101
## pollib2
              -1.5321125526 0.5232779163 -2.92791365 0.003412448
## parties
               0.0288170423 0.0102172799 2.82042211 0.004796051
               0.0149215757 0.0093762023 1.59143065 0.111512690
## pctvote
## popn
               0.0071646561 0.0056842444 1.26044124 0.207510232
               -0.0002579079 0.0002662008 -0.96884720 0.332621435
## size
```

Step3: Remove size next.

```
coup_3 = glm(miltcoup ~ oligarchy + pollib + parties + pctvote +
    popn, family = poisson, data = coup_data)
summary(coup_3)$coefficients
```

```
Pr(>|z|)
                   Estimate Std. Error
                                           z value
## (Intercept) -0.231434917 0.528887463 -0.4375882 0.661684821
## oligarchy
               0.083467586 0.025829007 3.2315445 0.001231231
## pollib1
               -0.683589192  0.495822322  -1.3786979  0.167987918
## pollib2
               -1.320568052 0.490268490 -2.6935609 0.007069322
## parties
                0.029769711 0.010309890 2.8874907 0.003883281
## pctvote
                0.013924684 0.009370609 1.4859956 0.137280288
## popn
                0.005659313 \ 0.005483446 \ 1.0320723 \ 0.302038232
```

Step4: Remove *popn*

```
coup_4 = glm(miltcoup ~ oligarchy + pollib + parties + pctvote,
    family = poisson, data = coup_data)
summary(coup_4)$coefficients
```

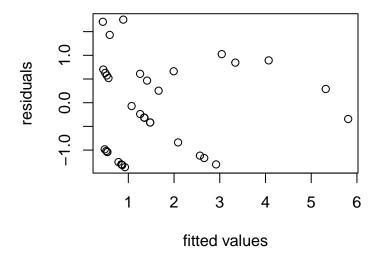
```
## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.11649888 0.513750518 -0.2267616 8.206091e-01
## oligarchy 0.09471197 0.023183825 4.0852606 4.402738e-05
## pollib1 -0.62075614 0.487525525 -1.2732793 2.029190e-01
## pollib2 -1.31037384 0.489017399 -2.6796058 7.370891e-03
## parties 0.02574472 0.009552367 2.6951146 7.036443e-03
## pctvote 0.01205704 0.009071988 1.3290409 1.838345e-01
```

Step5:remove pctvote

```
coup_5 = glm(miltcoup ~ oligarchy + pollib + parties, family = poisson,
    data = coup_data)
summary(coup_5)
```

```
##
## Call:
  glm(formula = miltcoup ~ oligarchy + pollib + parties, family = poisson,
##
       data = coup_data)
##
## Deviance Residuals:
      Min
                 1Q
                     Median
                                   3Q
                                           Max
## -1.3609
          -1.0407 -0.3153
                               0.6145
                                        1.7536
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.207981
                           0.445679
                                    0.467
                                              0.6407
## oligarchy
               0.091466
                           0.022563
                                     4.054 5.04e-05 ***
## pollib1
               -0.495414
                           0.475645
                                    -1.042
                                              0.2976
               -1.112086
                           0.459492
                                    -2.420
                                              0.0155 *
## pollib2
## parties
               0.022358
                           0.009098
                                     2.458
                                              0.0140 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
  (Dispersion parameter for poisson family taken to be 1)
##
      Null deviance: 65.945 on 35 degrees of freedom
## Residual deviance: 32.822 on 31 degrees of freedom
## AIC: 107.63
##
## Number of Fisher Scoring iterations: 5
```

The final Poisson model contains the same three variables that were previously identified as significant in question 4a(oligarchy, pollib, and parties). Furthermore, only one of the *pollib* factor levels (pollib2) remains significant. All the remaining variables are significant. So $coup_5$ is our final model. **Resulting model**: miltcoup = 0.207981 + 0.091466 * oligarchy - 0.495414 * pollib1 - 1.112086 * pollib2 + 0.022358 * parties.



Diagnostics:

c) We calculate the overall average values for parties and oligarchy and predict the number of coups for all the three levels of political liberalization for those values.

```
predict/codp_o, new_datao, type response /[[1]]
```

[1] 2.908352

```
predict(coup_5, new_data1, type = "response")[[1]]
```

[1] 1.772113

```
predict(coup_5, new_data2, type = "response")[[1]]
```

[1] 0.9564757

So, pollib = 0, i.e. no civil rights for political expression has the highest probability of a military coup, with limited civil rights(pollib = 1) having the next highest chance and the full civil rights(pollib = 1) with least probability of military coups.