Finalized Notebook

April 14, 2021

1 Credit Default Prediction: Code Notebook with Annotations

Code is in Python using Jupyter Notebook Exported using LaTex

(n) indicates code reference was used, go to code references at the bottom to find references with links

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2 Exploratory Data Analysis

Importing packages used in our analysis:

Numpy for scientific computing

Pandas for dealing with data tables

Matplotlib and seaborn for visualization

Statsmodels for calculating multicollinearity

Sklearn for building models and model interpretation, hyperparameter tuning

Autoimpute for imputation

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sn
from statsmodels.stats.outliers_influence import variance_inflation_factor
from sklearn.model_selection import RepeatedStratifiedKFold, GridSearchCV,

learning_curve, ShuffleSplit
from sklearn.linear_model import LogisticRegression
from sklearn.metrics import classification_report, confusion_matrix
from sklearn.ensemble import RandomForestClassifier
from sklearn.metrics import roc_curve, roc_auc_score
from autoimpute.imputations import SingleImputer
```

Importing all of our data sets:

```
[235]: df_test = pd.read_csv('Simulated_Data_Test.csv')
    df_train = pd.read_csv('Simulated_Data_Train.csv')
    df_validation = pd.read_csv('Simulated_Data_Validation.csv')
```

The first thing is to just get a basic summary of the train data we were given by looking at the raw data.

As we can see below, all variables except for state are of type float, and upon first glance it seems that the train data has imported correctly.

```
[240]: print(df_train.sample) print(df_train.dtypes)
```

```
2
               75212.76
                                                261.0
                                                                             260.0
                               12052.24
                                                                   149.0
3
               70727.84
                                8416.80
                                                227.0
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               78787.72
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                               10053.16
                                                348.0
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       non_mtg_acc_past_due_12_months_num
                                              non_mtg_acc_past_due_6_months_num
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                                                         auto open 36 month num
       inq_12_month_num
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```

```
uti_card_50plus_pct
       uti_card
                 uti_50plus_pct
                                  uti_max_credit_line
0
       0.365902
                        0.475594
                                              0.410504
                                                                          NaN
1
       0.542786
                        0.543158
                                                                    0.587351
                                              0.535147
2
       0.323678
                        0.321776
                                              0.348713
                                                                    0.413293
3
                        0.422809
                                                                    0.466810
       0.448721
                                              0.491365
4
       0.644030
                        0.619987
                                              0.546655
                                                                    0.588442
19995
       0.437699
                        0.557576
                                              0.472592
                                                                    0.481113
19996
       0.637746
                        0.484714
                                              0.734825
                                                                          NaN
                                                                    0.463120
19997
       0.486259
                        0.563475
                                              0.406215
19998
       0.299035
                        0.283815
                                              0.255758
                                                                    0.281647
19999
       0.574453
                        0.540931
                                              0.540706
                                                                    0.512513
       ind_acc_XYZ
                     rep_income
                                 States Default_ind
0
               0.0
                        69000.0
                                      ΑL
1
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19999
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[20000 rows x 21 columns]>
tot_credit_debt
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avg_card_debt
                                        float64
credit_age
                                        float64
credit_good_age
                                        float64
card_age
                                        float64
non_mtg_acc_past_due_12_months_num
                                        float64
non_mtg_acc_past_due_6_months_num
                                        float64
mortgages_past_due_6_months_num
                                        float64
credit_past_due_amount
                                        float64
inq_12_month_num
                                        float64
card_inq_24_month_num
                                        float64
card_open_36_month_num
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auto_open_ 36_month_num
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uti_card
                                        float64
uti_50plus_pct
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uti_max_credit_line
                                        float64
uti_card_50plus_pct
                                        float64
ind_acc_XYZ
                                        float64
rep_income
                                        float64
States
                                         object
```

Default_ind float64

dtype: object

2997

Before we get ahead of ourselves, we want to check that there is nothing wrong with the test and validation datasets when compared to the train dataset.

Everything seems to be in order: correct data types, same number of variables, nothing seems out of the ordinary.

```
[236]: print(df_validation.sample) print(df_validation.dtypes)
```

	<pre>method NDFrame.samp good_age card_age</pre>		tot_credit_debt	avg_card_debt	credit_age		
oreart. O	_good_age	9019.99	484.0	242.0	395.0		
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2995	90748.88	11481.81	274.0	161.0	268.0		
2996	101930.98	15242.30	243.0	161.0	213.0		
2997	74738.73	12175.49	351.0	179.0	271.0		
2998	120357.58	14477.70	308.0	178.0	298.0		
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[3000 rows x 21 columns]>
tot_credit_debt
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avg_card_debt
                                         float64
credit_age
                                         float64
credit_good_age
                                         float64
card_age
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```

```
non_mtg_acc_past_due_12_months_num
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      non_mtg_acc_past_due_6_months_num
                                              float64
      mortgages_past_due_6_months_num
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      credit_past_due_amount
                                              float64
      ing 12 month num
                                              float64
      card_inq_24_month_num
                                              float64
      card_open_36_month_num
                                              float64
      auto_open_ 36_month_num
                                              float64
      uti card
                                              float64
      uti_50plus_pct
                                              float64
      uti_max_credit_line
                                              float64
                                              float64
      uti_card_50plus_pct
      ind_acc_XYZ
                                              float64
                                              float64
      rep_income
      States
                                               object
      Default_ind
                                              float64
      dtype: object
[238]: print(df_test.sample)
       print(df_test.dtypes)
      <bound method NDFrame.sample of</pre>
                                              tot_credit_debt avg_card_debt
                                                                                credit_age
      credit_good_age card_age \
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                   121428.34
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                                    11646.36
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      4996
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                                                                                285.0
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      4997
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                                    11512.18
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                                                    192.0
      4999
                                                                      99.0
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mortgages_past_due_6_months_num
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4998
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                                                  0.0
                                                                             0.0
4999
                    4.0
                                                  1.0
                                                                             0.0
                 uti_50plus_pct
                                  uti_max_credit_line
                                                         uti_card_50plus_pct
      uti_card
0
      0.588301
                        0.711887
                                               0.538456
                                                                      0.633699
      0.707799
                        0.739732
1
                                               0.562194
                                                                     0.746901
2
      0.479711
                        0.434104
                                               0.374705
                                                                     0.458438
3
      0.443710
                        0.474768
                                               0.372028
                                                                      0.582352
4
      0.571004
                        0.472634
                                               0.605137
                                                                      0.577697
     0.444254
                        0.629877
                                               0.496559
                                                                     0.398411
4995
4996
      0.330706
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                                                                     0.286623
4997
      0.469755
                        0.478526
                                               0.460937
                                                                      0.443688
4998
      0.089534
                        0.259846
                                               0.127144
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4999
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                                 States Default_ind
      ind_acc_XYZ
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1
               1.0
                        47000.0
                                      AL
2
               0.0
                        71000.0
                                      MS
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3
               1.0
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```

4997	1.0	94000.0	LA		0.0			
4998	0.0	70000.0	MS		0.0			
4999	0.0	111000.0	MS		0.0			
[5000 rows x	21 colu	mns]>						
tot_credit_de			float64					
avg_card_debt				float64				
credit_age				float64				
credit_good_a	ge			float64				
card_age				float64				
non_mtg_acc_p	ast_due	_12_months_num	l	float64				
non_mtg_acc_p	ast_due	_6_months_num		float64				
mortgages_pas	t_due_6	_months_num		float64				
credit_past_d	ue_amou	nt		float64				
inq_12_month_	num			float64				
card_inq_24_m	onth_nu	m		float64				
card_open_36_	month_n	um		float64				
auto_open_ 36	_month_	num		float64				
uti_card				float64				
uti_50plus_pc	t			float64				
uti_max_credi	t_line			float64				
uti_card_50plus_pct float64								
ind_acc_XYZ floa								
rep_income float64								
States object								
Default_ind float64								
dtype: object								

Now we will garner summary stats about the all the variables. Important notes: - reported income mean is much higher than national mean. - 7.93% of population in train data set has defaulted - 25.855% of population already had an account with XYZ - All utilization variables have a mean around 50% - Standard deviation is relatively large for average card debt (0.66 as a proportion of the mean).

[49]: df_train.describe()

```
avg_card_debt
[49]:
             tot_credit_debt
                                                  credit_age
                                                              credit_good_age
                 20000.000000
                                 20000.000000
                                               20000.000000
                                                                  20000.000000
      count
                 94563.702530
                                 14088.235475
                                                  296.697000
      mean
                                                                    149.771750
                 23546.443862
                                  9314.495936
                                                   61.711702
                                                                     34.016476
      std
                  2367.430000
                                  2363.120000
                                                  54.000000
                                                                     21.000000
      min
      25%
                 78743.750000
                                 11321.502500
                                                  255.000000
                                                                    127.000000
      50%
                 94670.630000
                                 13243.750000
                                                  297.000000
                                                                    150.000000
               110329.335000
                                 15196.060000
      75%
                                                  339.000000
                                                                    172.000000
      max
               188890.960000
                                 99999.000000
                                                  545.000000
                                                                    296.000000
```

card_age non_mtg_acc_past_due_12_months_num \
count 20000.000000 20000.00000

```
268.015200
                                                   0.11135
mean
                                                   0.43389
          59.364769
std
min
          41.000000
                                                   0.00000
25%
         227.000000
                                                   0.00000
50%
         268,000000
                                                   0.00000
75%
         308.000000
                                                   0.00000
         520.000000
                                                   4.00000
max
       non_mtg_acc_past_due_6_months_num
                                            mortgages_past_due_6_months_num
                              20000.000000
                                                                 20000.000000
count
                                  0.027400
                                                                     0.030200
mean
std
                                  0.171903
                                                                     0.171142
min
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                                                                     0.00000
25%
                                  0.000000
                                                                     0.000000
50%
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                                                                     0.00000
75%
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                                  2.000000
                                                                     1.000000
max
       credit_past_due_amount
                                 inq_12_month_num
                                                    card_inq_24_month_num
                  20000.000000
                                     20000.000000
                                                              20000.000000
count
                    329.287867
                                         1.762700
                                                                  3,409600
mean
                   2073.899357
                                         1.740816
                                                                  2.926697
std
min
                      0.00000
                                         0.00000
                                                                  0.00000
25%
                                                                  1.000000
                      0.000000
                                         0.000000
50%
                      0.000000
                                         1.000000
                                                                  3.000000
75%
                      0.000000
                                         3.000000
                                                                  5.000000
                  32662.980000
max
                                        10.000000
                                                                 18.000000
       card_open_36_month_num
                                 auto_open_ 36_month_num
                                                                uti_card
                  20000.000000
                                             20000.000000
                                                            20000.000000
count
                      0.163050
                                                 0.141000
                                                                0.503157
mean
                      0.386099
                                                 0.349607
                                                                0.109354
std
min
                      0.000000
                                                 0.000000
                                                                0.065120
25%
                      0.000000
                                                 0.00000
                                                                0.429611
50%
                      0.000000
                                                 0.000000
                                                                0.502800
75%
                      0.00000
                                                 0.000000
                                                                0.577412
                      2.000000
                                                 2.000000
                                                                0.969289
max
       uti 50plus pct
                        uti max credit line
                                               uti card 50plus pct
                                                                      ind acc XYZ
         20000.000000
                                20000.000000
                                                      17945.000000
                                                                     20000.000000
count
              0.511007
                                    0.507629
mean
                                                          0.489594
                                                                         0.258550
std
              0.113456
                                    0.108624
                                                          0.119701
                                                                         0.437849
min
              0.033749
                                    0.005174
                                                          0.00000
                                                                         0.00000
25%
              0.435171
                                    0.433550
                                                          0.409794
                                                                         0.000000
50%
              0.509922
                                    0.507193
                                                                         0.00000
                                                          0.490074
75%
              0.588418
                                    0.581376
                                                          0.569036
                                                                          1.000000
              0.988964
max
                                    1.000000
                                                          0.970776
                                                                          1.000000
```

	rep_income	Default_ind
count	18430.000000	20000.000000
mean	75499.511666	0.079300
std	16361.955146	0.270213
min	12000.000000	0.000000
25%	64000.000000	0.000000
50%	75000.000000	0.000000
75%	86000.000000	0.000000
max	150000.000000	1.000000

We want to check which values are missing.

At this point, we are considering dropping the reported income variable due to its self reported nature.

We will need to find a way to deal with uti_card_50plus_pct as that may be an important variable.

```
[23]: print(df_train.isnull().sum()) print(df_train[['uti_card_50plus_pct','rep_income']].isnull().sum())
```

```
tot_credit_debt
                                           0
                                           0
avg_card_debt
credit_age
                                           0
credit_good_age
                                           0
card_age
                                           0
non_mtg_acc_past_due_12_months_num
                                           0
non_mtg_acc_past_due_6_months_num
                                           0
mortgages_past_due_6_months_num
                                           0
credit_past_due_amount
                                           0
inq_12_month_num
                                           0
card_inq_24_month_num
                                           0
card_open_36_month_num
                                           0
auto_open_ 36_month_num
                                           0
uti_card
                                           0
                                           0
uti_50plus_pct
uti_max_credit_line
                                           0
uti_card_50plus_pct
                                        2055
ind_acc_XYZ
                                           0
rep_income
                                        1570
ΑL
                                           0
FL
                                           0
                                           0
GA
                                           0
LA
MS
                                           0
                                           0
NC
SC
                                           0
```

Default_ind 0

dtype: int64

uti_card_50plus_pct 2055 rep_income 1570

dtype: int64

It is important to compare the statistics of the defaulting population to the non defaulting population.

We note the following: - The mean average card debt, credit past due amount, and utilization variables are much higher in the defaulting population than the non-defaulting population - For average card debt and credit past due amount, the defaulting population had a much greater std, suggesting high variance in the defaulting population - Reported income stats for both populations is very similar

```
[8]: defaulting_population = df_train[df_train["Default_ind"] == 1]
non_defaulting_population = df_train[df_train["Default_ind"] == 0]
```

```
[9]: defaulting_population.describe()
```

[9]:		tot_credit_debt	avg_card_debt	credit_age	credit_good_age	\
	count	1586.000000	1586.000000	1586.000000	1586.000000	
	mean	91915.567554	17880.428821	275.160151	140.535309	
	std	29920.362673	21195.058690	61.986033	33.557997	
	min	6898.500000	2363.120000	54.000000	21.000000	
	25%	70589.517500	9864.232500	233.000000	118.000000	
	50%	91235.590000	13125.530000	274.000000	140.000000	
	75%	112973.610000	16356.372500	316.000000	163.000000	
	max	188890.960000	99999.000000	521.000000	274.000000	

	card_age	non_mtg_acc_past_due_12_months_num	'
count	1586.000000	1586.000000	
mean	247.708701	0.706810	
std	58.602115	1.035236	
min	41.000000	0.000000	
25%	206.000000	0.000000	
50%	247.000000	0.000000	
75%	288.000000	2.000000	
max	463.000000	4.000000	

	non_mtg_acc_past_due_6_months_num	mortgages_past_due_6_months_num	\
count	1586.000000	1586.000000	
mean	0.249685	0.268600	
std	0.473343	0.443371	
min	0.000000	0.000000	
25%	0.000000	0.000000	
50%	0.000000	0.000000	
75%	0.000000	1.000000	

max 2.000000 1.000000

```
credit_past_due_amount
                                 inq_12_month_num
                                                    card_inq_24_month_num
                   1586.000000
                                      1586.000000
                                                               1586.000000
count
                   3060.922629
                                          2.288777
                                                                  4.163934
mean
std
                   5777.479779
                                          1.867494
                                                                  3.137177
                                          0.000000
                                                                  0.00000
min
                      0.000000
25%
                      0.000000
                                          1.000000
                                                                  2.000000
50%
                      0.000000
                                          2.000000
                                                                  4.000000
75%
                                                                  6.000000
                   4905.157500
                                          4.000000
max
                  32662.980000
                                          9.000000
                                                                 15.000000
       card_open_36_month_num
                                 auto_open_ 36_month_num
                                                               uti card
                   1586.000000
                                              1586.000000
                                                            1586.000000
count
                      0.192938
                                                 0.149433
                                                               0.560360
mean
std
                      0.419524
                                                 0.356627
                                                               0.110701
                      0.00000
                                                 0.000000
                                                               0.208749
min
25%
                      0.000000
                                                 0.000000
                                                               0.487653
50%
                      0.000000
                                                 0.00000
                                                               0.564220
75%
                      0.000000
                                                 0.000000
                                                               0.636084
                      2.000000
                                                 1.000000
                                                               0.969289
max
       uti_50plus_pct
                        uti_max_credit_line
                                               uti_card_50plus_pct
                                                                      ind_acc_XYZ
           1586.000000
                                 1586.000000
                                                        1412.000000
                                                                      1586.000000
count
              0.557966
                                    0.551171
                                                                         0.206810
mean
                                                           0.544364
std
              0.114920
                                    0.109630
                                                           0.123059
                                                                         0.405145
              0.163960
min
                                    0.186306
                                                           0.118153
                                                                         0.000000
25%
              0.476796
                                    0.476078
                                                           0.462664
                                                                         0.000000
50%
              0.558708
                                    0.550171
                                                           0.547647
                                                                         0.000000
75%
              0.638486
                                    0.623271
                                                           0.629132
                                                                         0.000000
              0.894996
                                    1.000000
                                                           0.970776
                                                                         1.000000
max
                       Default ind
          rep_income
                             1586.0
count
         1457.000000
        74522.992450
                                1.0
mean
std
        16775.126303
                                0.0
        26000.000000
                                1.0
min
25%
        63000.000000
                                1.0
50%
        74000.000000
                                1.0
75%
        85000.000000
                                1.0
max
       123000.000000
                                1.0
```

[242]: non_defaulting_population.describe()

[242]: tot_credit_debt avg_card_debt credit_age credit_good_age \(\) count 18414.000000 18414.000000 18414.000000 18414.000000 mean 94791.786710 13761.613413 298.551971 150.567286

```
std
          22901.385098
                           7363.255055
                                            61.336991
                                                               33.939197
min
           2367.430000
                           4595.020000
                                            78.000000
                                                               27.000000
25%
          79292.612500
                          11401.827500
                                            257.000000
                                                              128.000000
50%
           94912.085000
                          13251.240000
                                            299.000000
                                                              151.000000
75%
         110188.782500
                          15138.300000
                                            340.000000
                                                              173.000000
         182858.990000
                          99999.000000
                                            545.000000
                                                              296.000000
max
                      non_mtg_acc_past_due_12_months_num
           card_age
       18414.000000
                                              18414.000000
count
         269.764201
                                                  0.060063
mean
std
          59.106129
                                                  0.281161
min
          56.000000
                                                  0.00000
25%
         229.000000
                                                  0.00000
50%
         270.000000
                                                  0.00000
75%
         310.000000
                                                  0.00000
max
         520.000000
                                                  3.000000
       non_mtg_acc_past_due_6_months_num
                                            mortgages_past_due_6_months_num
                              18414.000000
                                                                 18414.000000
count
                                  0.008255
                                                                     0.009667
mean
                                  0.090481
                                                                     0.097845
std
min
                                  0.000000
                                                                     0.000000
25%
                                  0.000000
                                                                     0.00000
50%
                                  0.000000
                                                                     0.000000
75%
                                  0.00000
                                                                     0.00000
                                  1.000000
                                                                     1.000000
max
                                                    card_inq_24_month_num
       credit_past_due_amount
                                 inq_12_month_num
count
                  18414.000000
                                     18414.000000
                                                              18414.000000
                                         1.717389
                                                                  3.344629
                     94.011842
mean
                                         1.722024
                                                                  2.898779
std
                   1048.877699
min
                      0.000000
                                         0.000000
                                                                  0.00000
25%
                      0.000000
                                         0.000000
                                                                  1.000000
50%
                      0.000000
                                         1.000000
                                                                  3.000000
75%
                      0.000000
                                         3.000000
                                                                  5.000000
                  24211.550000
                                        10.000000
                                                                 18.000000
max
       card_open_36_month_num
                                 auto_open_ 36_month_num
                                                                uti_card
                  18414.000000
                                             18414.000000
                                                            18414.000000
count
mean
                      0.160476
                                                 0.140274
                                                                0.498230
std
                      0.382987
                                                 0.348996
                                                                0.107830
min
                      0.000000
                                                 0.000000
                                                                0.065120
25%
                      0.00000
                                                 0.00000
                                                                0.425885
50%
                      0.000000
                                                 0.000000
                                                                0.498045
75%
                      0.00000
                                                 0.000000
                                                                0.571530
                      2.000000
                                                 2.000000
                                                                0.922326
max
```

	uti_50plus_pct	uti_max_cre	edit_line	uti_card_50plus_pct	ind_acc_XYZ	\
count	18414.000000	1841	4.000000	16533.000000	18414.000000	
mean	0.506963		0.503879	0.484916	0.263006	
std	0.112418		0.107720	0.118243	0.440278	
min	0.033749		0.005174	0.000000	0.000000	
25%	0.431793		0.430766	0.405870	0.000000	
50%	0.506286		0.503482	0.485286	0.000000	
75%	0.583785		0.577646	0.563275	1.000000	
max	0.988964		0.971640	0.949959	1.000000	
	rep_income	${\tt Default_ind}$				
count	16973.000000	18414.0				
mean	75583.338243	0.0				
std	16323.783467	0.0				
min	12000.000000	0.0				
25%	65000.000000	0.0				
50%	76000.000000	0.0				
75%	87000.000000	0.0				
max	150000.000000	0.0				

Do we have enough observations for the amount of explanatory variables? One way to check this for regression analysis is the rule of ten test. If 10k/p > n, there are too many explanatory variables and not enough observations. - k = explantory variables = 20 - p = probability that account defaulted = 0.0793 (found in summary stats) - n = number of observations = 20,000

Data has passed rule of ten test since 20,000 is much larger than 2522.

For random forest, the number of observations is less of a concern for us as random forests are good with both large and small data sets.

```
[201]: print((10 * 20) / 0.0793)
```

2522.068095838588

We can check for multicollinearity by finding each variable's variance inflation factor. This is extremely important to consider for the logistic regression model, as one of the main assumptions is that there is little to no collinearity explantory variables.

As can be seen, there are many VIF values which are greater than 10, an unacceptable result. Additionally, there some VIF values that are less than 10 but greater than 5, a cause for concern (1).

```
[17]: def calc_vif(X):
    vif = pd.DataFrame()
    vif["variables"] = X.columns
    vif["VIF"] = [variance_inflation_factor(X.values, i) for i in range(X.
    →shape[1])]
```

```
return(vif)

columns = []
for num in range(0,18):
    if num == 16:
        pass
    else:
        columns.append(num)

calc_vif(df_train.iloc[:,columns])
```

```
[17]:
                                     variables
                                                        VIF
      0
                              tot_credit_debt
                                                  16.224066
      1
                                 avg_card_debt
                                                   3.835799
      2
                                    credit_age
                                                232.525965
      3
                              credit_good_age
                                                 52.883615
      4
                                      card_age
                                                174.509147
      5
          non_mtg_acc_past_due_12_months_num
                                                   4.612476
      6
           non_mtg_acc_past_due_6_months_num
                                                   3.462795
      7
             mortgages_past_due_6_months_num
                                                   6.670029
      8
                       credit_past_due_amount
                                                   6.570714
      9
                             ing 12 month num
                                                   7.769188
      10
                        card_inq_24_month_num
                                                   9.002325
      11
                       card_open_36_month_num
                                                   1.188654
      12
                      auto_open_ 36_month_num
                                                   1.172338
      13
                                      uti_card
                                                  78.503559
      14
                               uti_50plus_pct
                                                  46.474318
                          uti_max_credit_line
      15
                                                  49.135164
      16
                                   ind_acc_XYZ
                                                   1.348725
```

Let's check for collinearity between specific variables, including the response variable. This will help shed light on which explanatory variables are collinear, which will be extremely important for logistic regression. We will also discover which explanatory variables we may consider to have too low of a correlation to the default indicator, which we want to minimize for our random tree model.

To create a correlation matrix of all variables, we will firstly create dummy variables for the states.

```
[204]: dummies = pd.get_dummies(df_train['States'])
    default_ind = df_train['Default_ind']
    df_train = df_train.drop(columns=['States', 'Default_ind'])
    df_train = df_train.join(dummies)
    df_train = df_train.join(default_ind)
```

Now the data is ready for a correlation matrix.

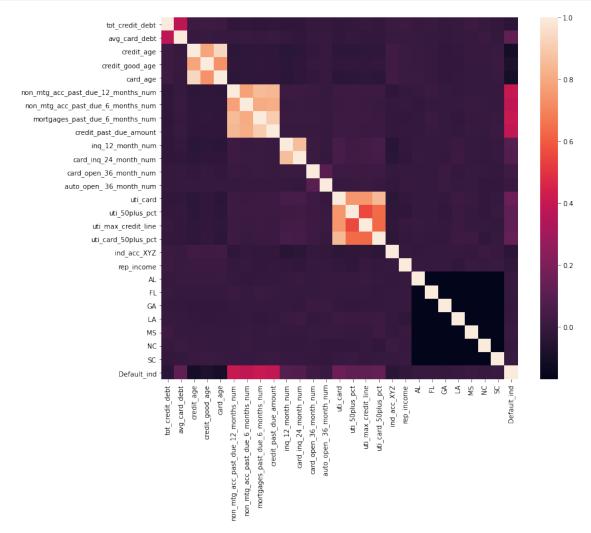
Logistic regression notes:

It seems that reported income does not have a high correlation with the response variable. This confirms to us that it is no longer worth keeping. The first five columns present unacceptable levels of colinearity. With no easy way to combine them, the four with least amount of correlation to the response variable will be dropped. Since the 12 month and 24 month card inquiry variables are highly colinear and since the 24 month card inquiry variable is cumulative, we will drop the 12 month card inquiry variable.

Random forest notes:

For now, we will consider credit age, credit good age, and card age to have too low of a correlation to the default indicator and disregard them for our random tree model.

```
[22]: columns = []
  fig, ax = plt.subplots(figsize=(12,10))
  for num in range(0,27):
        columns.append(num)
  corrMatrix = df_train.iloc[:,columns].corr()
  sn.heatmap(corrMatrix, annot=False, ax=ax)
  plt.show()
```

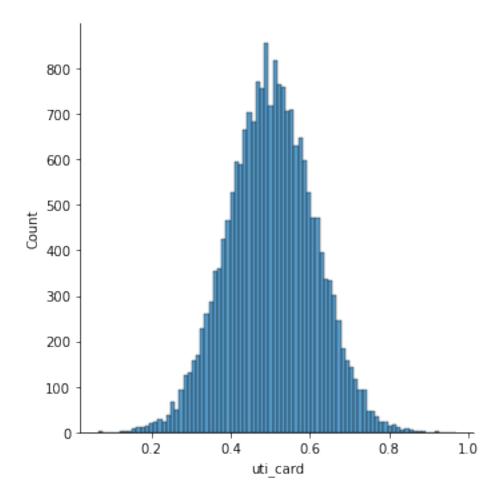


For logistic regression, we will need to deal with missing values, as the model will not do this for us. Since the only variable with missing values we decided to keep is uti_card_50plus_pct, we will need to find a way to deal with missing values for this column. Our first idea is, since utilization variables have high collinearity and are on the same scale, to combine all utilization variables into a mean utilization variable which will consider uti_card_50plus_pct only if available for the observation. To make sure this is feasable, we must first check the normality of the utilization variables.

As can be seen below, the distribution of all utilization variables is approximately normal, meaning that mean utilization could be a useful variable.

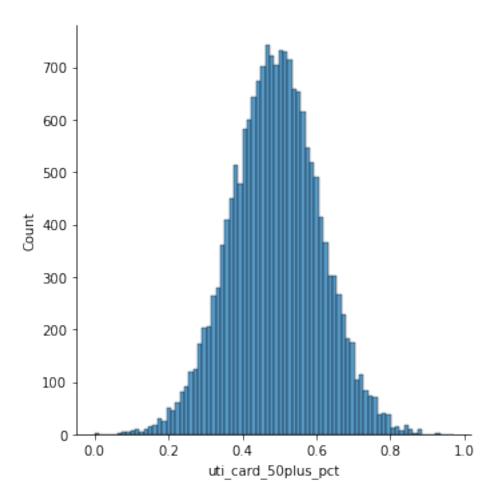
[13]: sn.displot(df_train,x="uti_card")

[13]: <seaborn.axisgrid.FacetGrid at 0x2126627ed30>



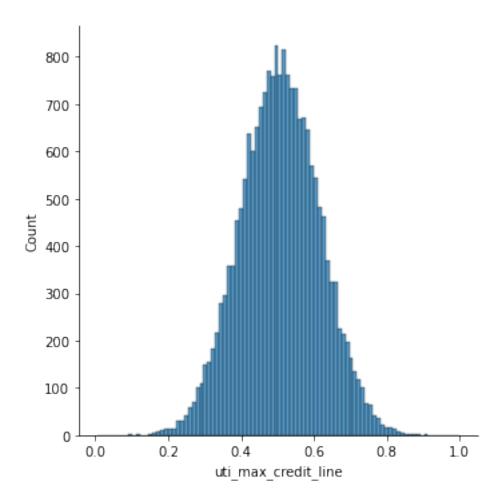
[18]: sn.displot(df_train,x="uti_card_50plus_pct")

[18]: <seaborn.axisgrid.FacetGrid at 0x212669e4a00>



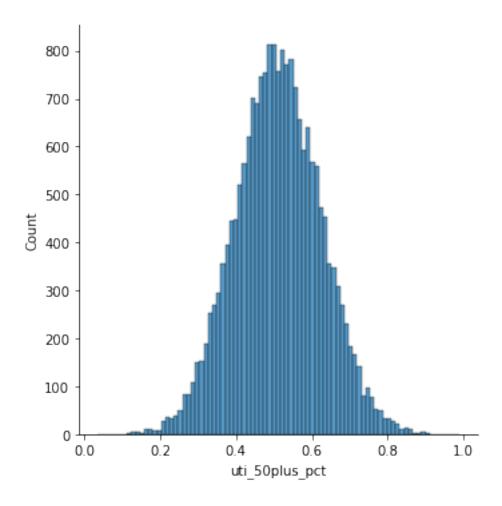
[15]: sn.displot(df_train,x="uti_max_credit_line")

[15]: <seaborn.axisgrid.FacetGrid at 0x212669ee790>



```
[19]: sn.displot(df_train,x="uti_50plus_pct")
```

[19]: <seaborn.axisgrid.FacetGrid at 0x212672312e0>



3 Data Preprocessing - Logistic Regression

have determined EDAwhich variables We already based on explanatory to be dropped:tot_credit_debt, credit_age, credit_good_age, card_age, need rep income,ing 12 month num.

Next comes the process of combining all utilization variables into one variable, and replacing all the instances with the new overlapping variable. By taking the average utilization, we are able to preserve the available data in uti-card 50plus pct.

```
[206]: util_vars = ["uti_card", "uti_50plus_pct", "uti_max_credit_line", □

⇔"uti_card_50plus_pct"]

util_credit = df_train[util_vars]

util_credit["mean"] = util_credit.mean(axis=1)
```

<ipython-input-206-543dfd05b1c6>:3: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy util_credit["mean"] = util_credit.mean(axis=1)

Past due variables have unacceptable levels of colinearity. It makes sense to combine the non mortgage and mortgages past due 6 month variables as they span the same time period and are highly colinear. For now, the other past due variables are not dropped due to their high correlation with the response variable.

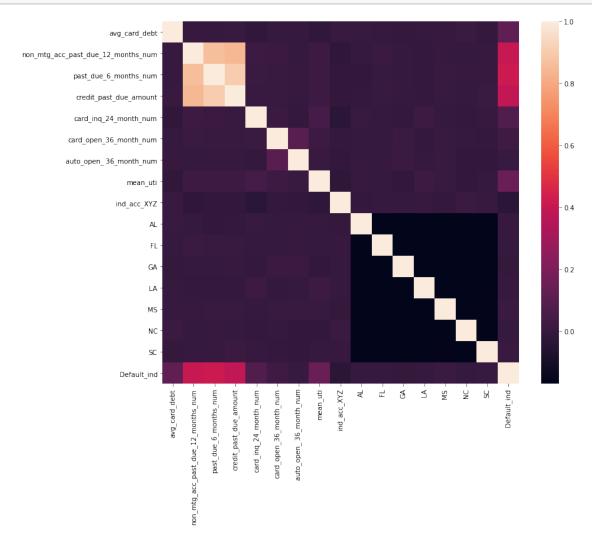
<ipython-input-207-db6338c54e88>:3: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy past_due_credit["past_due_6_months_num"] = past_due_credit["non_mtg_acc_past_due_6_months_num"] + past_due_credit["mortgages_past_due_6_months_num"]

We will check collinearity and multicollinearity again to see if we have reduced it to an acceptable level.

While colinearity between the past due variables' colinearity is worrying, they are simply too valuable to drop for now due to their high linearity with the response variable. The VIF values give an encouraging picture, however, as values, while slightly high, are in an acceptable range (1).

```
[31]: columns = []
fig, ax = plt.subplots(figsize=(12,10))
for num in range(0,17):
        columns.append(num)
corrMatrix = df_train.iloc[:,columns].corr()
sn.heatmap(corrMatrix, annot=False, ax=ax)
plt.show()
```



```
[33]:
                                    variables
                                                     VIF
      0
                                avg_card_debt
                                               1.000904
      1
          non_mtg_acc_past_due_12_months_num
                                               4.245805
      2
                       past_due_6_months_num
                                               6.522983
      3
                      credit past due amount
                                               5.945257
      4
                       card_inq_24_month_num
                                               1.004331
                      card_open_36_month_num
      5
                                               1.010175
      6
                      auto_open_ 36_month_num
                                               1.009894
      7
                                     mean_uti
                                               1.004178
      8
                                  ind_acc_XYZ
                                               1.002969
      9
                                           AL
                                               5.388244
      10
                                           FL
                                               5.303679
      11
                                           GA 5.263706
      12
                                           LA 5.365403
      13
                                           MS
                                               5.287676
      14
                                           NC
                                               5.340952
      15
                                           SC 5.242121
```

Last thing left to do is normalize data:

```
[208]: df_train_norm=((df_train-df_train.min())/(df_train.max()-df_train.min()))*20
```

Check preprocessed data:

Everything seems to be in order. Time to move on to model building.

```
[36]: print(df_train_norm.sample) print(df_train_norm.shape) print(df_train_norm.dtypes)
```

```
<bound method NDFrame.sample of</pre>
                                         avg_card_debt
non_mtg_acc_past_due_12_months_num
0
            2.767399
                                                         0.0
1
            2.010511
                                                         0.0
2
                                                         0.0
             1.984746
3
             1.240052
                                                        10.0
4
             1.689717
                                                         0.0
19995
            2.364352
                                                         0.0
            1.630937
19996
                                                         0.0
19997
            3.170078
                                                         5.0
                                                         0.0
19998
             1.860892
19999
            1.575249
                                                         0.0
                                                         card_inq_24_month_num
       past_due_6_months_num
                                credit_past_due_amount
0
                     0.000000
                                               0.00000
                                                                        4.44444
1
                     0.00000
                                               0.00000
                                                                        4.44444
2
                     0.00000
                                               0.00000
                                                                        3.333333
3
                    13.333333
                                               6.744002
                                                                        1.111111
```

```
4
                     0.000000
                                               0.000000
                                                                        2,222222
                     0.000000
                                               0.000000
                                                                        4.44444
19995
19996
                     0.00000
                                               0.00000
                                                                        1.111111
                                                                        3.333333
19997
                     0.000000
                                               0.000000
19998
                     0.000000
                                               0.00000
                                                                        2.22222
19999
                     0.000000
                                               0.000000
                                                                        4.44444
       card_open_36_month_num
                                 auto_open_ 36_month_num
                                                             mean_uti
0
                                                             7.470849
                            0.0
                                                       0.0
1
                           10.0
                                                       0.0
                                                            10.830203
2
                            0.0
                                                      10.0
                                                             5.839036
3
                                                       0.0
                           10.0
                                                             8.470172
4
                            0.0
                                                       0.0
                                                            12.018333
19995
                            0.0
                                                       0.0
                                                             9.213416
19996
                            0.0
                                                       0.0
                                                            12.499806
                            0.0
                                                      10.0
19997
                                                             9.027027
19998
                            0.0
                                                       0.0
                                                             4.049374
19999
                            0.0
                                                       0.0
                                                            10.581955
       ind acc XYZ
                              FL
                                    GA
                                           LA
                                                       NC
                                                                 Default ind
                       ΑL
                                                MS
                                                                          0.0
0
                0.0
                     20.0
                             0.0
                                   0.0
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                                                      0.0
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1
                0.0
                      0.0 20.0
                                   0.0
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2
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3
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                                          0.0
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                                                                         20.0
                                                      0.0
4
               20.0
                                         20.0
                      0.0
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                                               0.0
                                                      0.0
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                                                     0.0
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19995
                      0.0
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                                  20.0
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19996
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                                               0.0
                                                     20.0
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                                                           20.0
19997
                0.0
                      0.0
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19998
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                                                      0.0
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                0.0
                     20.0
                                          0.0 0.0
19999
                             0.0
                                   0.0
                                                      0.0
                                                            0.0
                                                                          0.0
[20000 rows x 17 columns]>
(20000, 17)
avg card debt
                                         float64
non_mtg_acc_past_due_12_months_num
                                         float64
past_due_6_months_num
                                         float64
credit_past_due_amount
                                         float64
card_inq_24_month_num
                                         float64
card_open_36_month_num
                                         float64
auto_open_ 36_month_num
                                         float64
mean uti
                                         float64
ind_acc_XYZ
                                         float64
ΑL
                                         float64
FL
                                         float64
GA
                                         float64
```

```
LA float64
MS float64
NC float64
SC float64
Default_ind float64
dtype: object
```

4 Model Building and Testing - Logistic Regression

We will begin by performing hyper parameter optimization on the validation data set for logistic regression. In order to do this, we must manipulate the validation data set in the same way we have manipulated the training data set.

```
[209]: dummies = pd.get dummies(df validation['States'])
      default_ind = df_validation['Default_ind']
      df_validation = df_validation.

¬drop(columns=["Default_ind", "States", "tot_credit_debt", "credit_age",
□

¬"credit_good_age", "card_age", "rep_income", "inq_12_month_num"])

      df validation = df validation.join(dummies)
      df_validation = df_validation.join(default_ind)
      util_vars = ["uti_card", "uti_50plus_pct", "uti_max_credit_line", __

¬"uti_card_50plus_pct"]

      util_credit = df_validation[util_vars]
      util_credit["mean"] = util_credit.mean(axis=1)
      df_validation = df_validation.drop(columns=["uti_50plus_pct",_
       →"uti_max_credit_line", "uti_card_50plus_pct"])
      df_validation["uti_card"] = util_credit["mean"]
      df_validation = df_validation.rename(columns={"uti_card":"mean_uti"})
      past_due_vars = ["non_mtg_acc_past_due_6_months_num",_
       →"mortgages_past_due_6_months_num"]
      past_due_credit = df_validation[past_due_vars]
      past due credit["past due 6 months num"] = []
       →past_due_credit["non_mtg_acc_past_due_6_months_num"] +_
       →past_due_credit["mortgages_past_due_6_months_num"]
      df_validation = df_validation.drop(columns=["mortgages_past_due_6 months_num"])
      df_validation["non_mtg_acc_past_due_6_months_num"] = __
       →past_due_credit["past_due_6_months_num"]
      df validation = df validation.
       -rename(columns={"non_mtg_acc_past_due_6_months_num":"past_due_6_months_num"})
      df_validation_norm=((df_validation-df_validation.min())/(df_validation.
        →max()-df_validation.min()))*20
```

<ipython-input-209-959fbd1f3629>:8: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-

```
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
       util_credit["mean"] = util_credit.mean(axis=1)
     <ipython-input-209-959fbd1f3629>:14: SettingWithCopyWarning:
     A value is trying to be set on a copy of a slice from a DataFrame.
     Try using .loc[row_indexer,col_indexer] = value instead
     See the caveats in the documentation: https://pandas.pydata.org/pandas-
     docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
       past_due_credit["past_due_6_months_num"] =
     past_due_credit["non_mtg_acc_past_due_6_months_num"] +
     past_due_credit["mortgages_past_due_6_months_num"]
     Everything looks in order:
[39]: print(df_validation_norm.sample)
      print(df_validation_norm.shape)
      print(df_validation_norm.dtypes)
     <bound method NDFrame.sample of</pre>
                                             avg_card_debt
     non_mtg_acc_past_due_12_months_num
                                                            0.0
     0
                 1.258527
     1
                 2.838983
                                                            0.0
     2
                                                            0.0
                 1.565286
     3
                                                            0.0
                 2.258434
     4
                                                            0.0
                 2.612365
     2995
                 1.765656
                                                            0.0
     2996
                 2,540309
                                                            0.0
     2997
                 1.908553
                                                            0.0
                                                            0.0
     2998
                 2.382803
     2999
                 1.846333
                                                            0.0
            past_due_6_months_num
                                   credit_past_due_amount
                                                             card_inq_24_month_num \
     0
                               0.0
                                                        0.0
                                                                           0.000000
                              0.0
                                                        0.0
                                                                          10.769231
     1
     2
                               0.0
                                                        0.0
                                                                           4.615385
     3
                               0.0
                                                        0.0
                                                                           1.538462
     4
                               0.0
                                                                          13.846154
                                                        0.0
                              0.0
                                                        0.0
                                                                           0.000000
     2995
     2996
                               0.0
                                                        0.0
                                                                           0.000000
     2997
                               0.0
                                                        0.0
                                                                           6.153846
     2998
                               0.0
                                                        0.0
                                                                           3.076923
     2999
                              0.0
                                                        0.0
                                                                          10.769231
            card_open_36_month_num
                                     auto_open_ 36_month_num
                                                                           ind_acc_XYZ
                                                                {\tt mean\_uti}
     0
                               0.0
                                                          0.0 14.171756
                                                                                   0.0
     1
                               0.0
                                                         10.0
                                                                9.861754
                                                                                   0.0
     2
                               0.0
                                                          0.0 10.139092
                                                                                   0.0
```

3 4				0.0				0.0	13.427118 14.453941	0.0 20.0
 2995								10.0	 15.295818	
2996				0.0				10.0	13.714113	0.0
2997				0.0				0.0	15.768993	0.0
2998				0.0				10.0	12.947497	20.0
2999				10.0				10.0	17.795304	0.0
	AL	FL	GA	LA	MS	NC	SC	Default_	ind	
0	0.0	20.0	0.0	0.0	0.0	0.0	0.0	2	0.0	
1	0.0	0.0	0.0	0.0	20.0	0.0	0.0		0.0	
2	0.0	0.0	0.0	0.0	20.0	0.0	0.0		0.0	
3	0.0	0.0	0.0	0.0	20.0	0.0	0.0		0.0	
4	0.0	0.0	0.0	0.0	0.0	20.0	0.0		0.0	
 0005							0 0		0.0	
2995	0.0	20.0	0.0	0.0	0.0	0.0	0.0		0.0	
2996	20.0	0.0	0.0	0.0	0.0	0.0	0.0		0.0	
2997	0.0	0.0	0.0	20.0	0.0	0.0	0.0		0.0	
2998	0.0	0.0	0.0	0.0	0.0	20.0	0.0		0.0	
2999	0.0	0.0	0.0	0.0	20.0	0.0	0.0		0.0	
[3000) rows	х 17 с	olumn	.s]>						
), 17)									
avg_c	ard_de	bt				fl	oat64			
non_m	tg_acc	_past_	due_1	2_mont	hs_num	fl	oat64			
past_	due_6_	months	_num			fl	oat64			
credi	t_past	_due_a	mount			fl	oat64			
card_	inq_24	_month	_num			fl	oat64			
card_	open_3	6_mont	h_num	L		fl	oat64			
auto_	open_	36_mon	th_nu	m		fl	oat64			
mean_	uti					fl	oat64			
ind_acc_XYZ					fl	oat64				
AL	AL					fl	oat64			
FL							oat64			
GA	GA						oat64			
LA							oat64			
MS							oat64			
NC							oat64			
	SC						oat64			
Default_ind						fl	oat64			
dtype	dtype: object									

We will now perform hyperparamter tuning using our validation data set (2a).

The parameters we have chosen are: - solvers: newtown conjugate gradient, limited memory bfgs, and liblinear - penalty: 12 only (since it works for all three solvers) - C values: 100, 10, 1.0, 0.1, 0.01

```
[210]: model = LogisticRegression()
       solvers = ['newton-cg', 'lbfgs', 'liblinear']
       penalty = ['12']
       c_values = [100, 10, 1.0, 0.1, 0.01]
       grid = dict(solver=solvers,penalty=penalty,C=c_values)
       cv = RepeatedStratifiedKFold(n_splits=10, n_repeats=3, random_state=1)
       grid_search = GridSearchCV(estimator=model, param_grid=grid, n_jobs=-1, cv=cv,_u

⇒scoring='accuracy',error_score=0)
       grid_result = grid_search.fit(df_validation_norm.iloc[:,range(0,16)],__

→df_validation_norm.iloc[:,16])
       print("Best: %f using %s" % (grid_result.best_score_, grid_result.best_params_))
       means = grid_result.cv_results_['mean_test_score']
       stds = grid result.cv results ['std test score']
       params = grid_result.cv_results_['params']
       for mean, stdev, param in zip(means, stds, params):
           print("%f (%f) with: %r" % (mean, stdev, param))
```

```
Best: 0.937778 using {'C': 0.1, 'penalty': '12', 'solver': 'liblinear'}
0.937667 (0.009195) with: {'C': 100, 'penalty': 'l2', 'solver': 'newton-cg'}
0.937667 (0.009195) with: {'C': 100, 'penalty': '12', 'solver': 'lbfgs'}
0.937667 (0.009195) with: {'C': 100, 'penalty': 'l2', 'solver': 'liblinear'}
0.937667 (0.009195) with: {'C': 10, 'penalty': '12', 'solver': 'newton-cg'}
0.937667 (0.009195) with: {'C': 10, 'penalty': '12', 'solver': 'lbfgs'}
0.937667 (0.009195) with: {'C': 10, 'penalty': '12', 'solver': 'liblinear'}
0.937667 (0.009195) with: {'C': 1.0, 'penalty': 'l2', 'solver': 'newton-cg'}
0.937667 (0.009195) with: {'C': 1.0, 'penalty': '12', 'solver': 'lbfgs'}
0.937667 (0.009195) with: {'C': 1.0, 'penalty': 'l2', 'solver': 'liblinear'}
0.937667 (0.009195) with: {'C': 0.1, 'penalty': 'l2', 'solver': 'newton-cg'}
0.937667 (0.009195) with: {'C': 0.1, 'penalty': '12', 'solver': 'lbfgs'}
0.937778 (0.009081) with: {'C': 0.1, 'penalty': 'l2', 'solver': 'liblinear'}
0.937778 (0.008664) with: {'C': 0.01, 'penalty': '12', 'solver': 'newton-cg'}
0.937778 (0.008664) with: {'C': 0.01, 'penalty': 'l2', 'solver': 'lbfgs'}
0.936667 (0.008300) with: {'C': 0.01, 'penalty': '12', 'solver': 'liblinear'}
```

Based on this, the most accurate model has the following hyperparameters: - solver: liblinear - penalty: 12 - C value: 0.1

Train model based on chosen hyperparameters using the train data set:

```
[211]: lrModel = LogisticRegression(C = 0.1, penalty = "12", solver="liblinear") lrModel = lrModel.fit(df_train_norm.iloc[:,range(0,16)], df_train_norm.iloc[: \( \to \),16])
```

Transforming test data to match training data:

```
df_test = df_test.join(dummies)
      df_test = df_test.join(default_ind)
      util_vars = ["uti_card", "uti_50plus_pct", "uti_max_credit_line", __

¬"uti_card_50plus_pct"]

      util credit = df test[util vars]
      util credit["mean"] = util credit.mean(axis=1)
      df_test = df_test.drop(columns=["uti_50plus_pct", "uti_max_credit_line",__

¬"uti_card_50plus_pct"])
      df_test["uti_card"] = util_credit["mean"]
      df_test = df_test.rename(columns={"uti_card":"mean_uti"})
      past_due_vars = ["non_mtg_acc_past_due_6_months_num",__

¬"mortgages past due 6 months num"]

      past_due_credit = df_test[past_due_vars]
      past_due_credit["past_due_6_months_num"] =__
       →past_due_credit["non_mtg_acc_past_due_6_months_num"] +__
      →past_due_credit["mortgages_past_due_6_months_num"]
      df_test = df_test.drop(columns=["mortgages_past_due_6_months_num"])
      df_test["non_mtg_acc_past_due_6_months_num"] =__
      →past_due_credit["past_due_6_months_num"]
      df_test = df_test.rename(columns={"non mtg_acc_past_due 6 months num":

¬"past_due_6_months_num"})
      df_test_norm=((df_test-df_test.min())/(df_test.max()-df_test.min()))*20
     <ipython-input-212-fd2b47dd7047>:8: SettingWithCopyWarning:
     A value is trying to be set on a copy of a slice from a DataFrame.
     Try using .loc[row_indexer,col_indexer] = value instead
     See the caveats in the documentation: https://pandas.pydata.org/pandas-
     docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
       util_credit["mean"] = util_credit.mean(axis=1)
     <ipython-input-212-fd2b47dd7047>:14: SettingWithCopyWarning:
     A value is trying to be set on a copy of a slice from a DataFrame.
     Try using .loc[row_indexer,col_indexer] = value instead
     See the caveats in the documentation: https://pandas.pydata.org/pandas-
     docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
       past_due_credit["past_due_6_months_num"] =
     past_due_credit["non_mtg_acc_past_due_6_months_num"] +
     past_due_credit["mortgages_past_due_6_months_num"]
     Check data:
[43]: print(df_test_norm.sample)
      print(df_test_norm.shape)
      print(df_test_norm.dtypes)
     <bound method NDFrame.sample of</pre>
                                            avg_card_debt
     non_mtg_acc_past_due_12_months_num \
```

```
0.0
0
            0.723813
            2.571408
                                                         0.0
1
2
                                                         0.0
            2.007778
3
            2.326841
                                                         0.0
4
                                                         0.0
            2.071129
4995
            1.534659
                                                         0.0
                                                         0.0
4996
            2.550137
4997
            1.506616
                                                         0.0
4998
                                                         0.0
            1.193691
4999
            2.871439
                                                         0.0
      past_due_6_months_num
                                credit_past_due_amount
                                                           card_inq_24_month_num
0
                          0.0
                                                     0.0
                                                                         5.333333
1
                          0.0
                                                     0.0
                                                                         5.333333
                          0.0
2
                                                     0.0
                                                                         1.333333
3
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4
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4995
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4996
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4997
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                                                                         6.66667
4998
                          0.0
                                                     0.0
                                                                         2.666667
                                                     0.0
4999
                          0.0
                                                                        10.666667
      card_open_36_month_num
                                 auto_open_ 36_month_num
                                                                         ind_acc_XYZ
                                                              mean_uti
0
                                                                                  0.0
                           0.0
                                                      10.0
                                                             13.749481
1
                           0.0
                                                       0.0
                                                                                 20.0
                                                             15.757954
2
                           0.0
                                                       0.0
                                                              8.624625
                                                                                  0.0
3
                           0.0
                                                       0.0
                                                              9.514111
                                                                                 20.0
4
                           0.0
                                                       0.0
                                                             12.012403
                                                                                  0.0
4995
                           0.0
                                                       0.0
                                                             10.194068
                                                                                  0.0
4996
                           0.0
                                                       0.0
                                                                                 20.0
                                                              6.574378
4997
                           10.0
                                                      10.0
                                                                                 20.0
                                                              9.373143
4998
                           0.0
                                                       0.0
                                                              0.907474
                                                                                  0.0
4999
                           10.0
                                                             12.528196
                                                                                  0.0
                                                       0.0
        AL
               FL
                      GA
                            LA
                                   MS
                                         NC
                                               SC
                                                    Default_ind
0
             20.0
                     0.0
                           0.0
                                  0.0
                                        0.0
                                              0.0
       0.0
                                                             0.0
                                                             0.0
1
      20.0
              0.0
                     0.0
                           0.0
                                  0.0
                                        0.0
                                              0.0
2
                                                             0.0
       0.0
              0.0
                     0.0
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                                 20.0
                                        0.0
                                              0.0
3
      20.0
              0.0
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                                              0.0
                                                             0.0
4
        0.0
              0.0
                    20.0
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                                  0.0
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                                                             0.0
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4995
       0.0
              0.0
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4996
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              0.0
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                                             20.0
                                                             0.0
4997
        0.0
              0.0
                     0.0
                          20.0
                                  0.0
                                       0.0
                                              0.0
                                                             0.0
```

```
[5000 rows x 17 columns]>
      (5000, 17)
      avg card debt
                                              float64
      non_mtg_acc_past_due_12_months_num
                                              float64
      past_due_6_months_num
                                               float64
      credit_past_due_amount
                                              float64
      card_inq_24_month_num
                                              float64
      card_open_36_month_num
                                              float64
      auto_open_ 36_month_num
                                              float64
                                              float64
      mean_uti
      ind_acc_XYZ
                                              float64
      ΑL
                                              float64
      FL
                                              float64
      GA
                                              float64
      LA
                                              float64
      MS
                                              float64
      NC
                                              float64
      SC
                                              float64
      Default ind
                                              float64
      dtype: object
      Scoring test data:
[139]: lrModel.score(df_test_norm.iloc[:,range(0,16)], df_test_norm.iloc[:,16])
[139]: 0.9358
      Testing with a confusion matrix:
[140]: confusion_matrix(df_test_norm.iloc[:,16],lrModel.predict(df_test_norm.iloc[:
        \rightarrow, range(0,16)]))
[140]: array([[4552,
                        47],
              [ 274, 127]], dtype=int64)
      Interpreting logistic regression model using ROC curve (2b):
[131]: | lr_probs = lr.predict_proba(df_test_norm.iloc[:,range(0,16)])
       lr_probs = lr_probs[:, 1]
       lr_fpr, lr_tpr, _ = roc_curve(df_test_norm.iloc[:,16], lr_probs, pos_label = 20.
        →0)
       plt.plot(lr_fpr, lr_tpr, marker='.', label='Logistic Regression Classifier')
       plt.xlabel('False Positive Rate')
       plt.ylabel('True Positive Rate')
       plt.legend()
       plt.show()
```

4998

4999

0.0

0.0

0.0

0.0

0.0

0.0

0.0 20.0 0.0

20.0 0.0

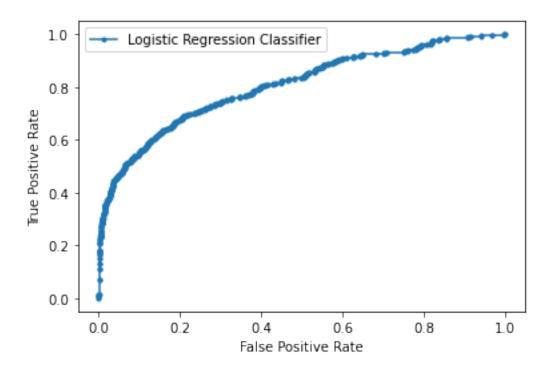
0.0

0.0

0.0

0.0

0.0



Find feature importance (2c):

A positive score indicates the greater the value of the feature, the more likely the person is to default, while a negative score indicates the greater the value of the feature, the less likely the person is to default.

A high absolute score indicates strong importance in model, while a low absolute score indicates weak importance in model.

Important Notes: - Having had an account in XYZ does not seem to impact the model by much - Average card debt, past due variables for 12 and 6 months, and utilization variables seem to have the greatest impact - Although the state variables seem to cause a great impact, in reality each observation must be one of them, and thus, the difference between them is the only thing that matters for interpretation. In this case, since the importance of all state variables is very close overall, it seems that states do not have a great deal of impact on model prediction

```
[179]: variables = []
for var in df_train_norm.columns:
    variables.append(var)
importance = lrModel.coef_[0]
index = 0
for i,v in enumerate(importance):
    print('Feature: {variable}\n Score: {v}\n\n'.format(variable =_\u00fc)
    variables[index],v = v))
    index += 1
```

plt.bar([x for x in range(len(importance))], importance)
plt.show()

Feature: avg_card_debt Score: 0.1499596391270964

Feature: non_mtg_acc_past_due_12_months_num

Score: 0.23556759045910966

Feature: past_due_6_months_num Score: 0.1542133033538216

Feature: credit_past_due_amount Score: -0.04906488819908006

Feature: card_inq_24_month_num Score: 0.08606432328090474

Feature: card_open_36_month_num Score: 0.016807004273557042

Feature: mean_uti

Score: 0.27185106310181156

Feature: ind_acc_XYZ

Score: -0.013710761590003758

Feature: AL

Score: -0.3130380831427379

Feature: FL

Score: -0.317889156327858

Feature: GA

Score: -0.318481497908399

Feature: LA

Score: -0.31415871337745066

Feature: MS

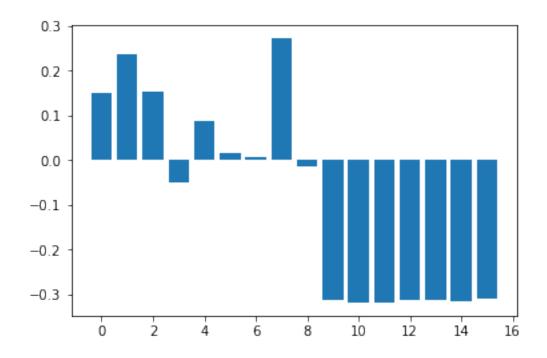
Score: -0.3113582401283215

Feature: NC

Score: -0.31565900138163133

Feature: SC

Score: -0.3103977152431603



5 Data Preprocessing - Random Forests

We will reimport the data since we will be using a different approach to data preprocessing in preperation of random forest model.

```
[144]: df_test = pd.read_csv('Simulated_Data_Test.csv')
    df_train = pd.read_csv('Simulated_Data_Train.csv')
    df_validation = pd.read_csv('Simulated_Data_Validation.csv')
```

Based on EDA, we have determined which explanatory variables need to be dropped: rep_income, credit_age, credit_good_age, and card_age.

```
[145]: df_train = df_train.drop(columns=["credit_age", "credit_good_age", 

→"card_age", "rep_income"])
```

Next, let's create dummy variables for states

```
[146]: dummies = pd.get_dummies(df_train['States'])
    default_ind = df_train['Default_ind']
    df_train = df_train.drop(columns=['States', 'Default_ind'])
    df_train = df_train.join(dummies)
    df_train = df_train.join(default_ind)
```

We need to get rid of NA values next. let's check how many there are:

```
[147]: print(df_train.isnull().sum())
```

```
0
tot credit debt
                                           0
avg_card_debt
                                           0
non_mtg_acc_past_due_12_months_num
non_mtg_acc_past_due_6_months_num
                                           0
                                           0
mortgages_past_due_6_months_num
credit_past_due_amount
                                           0
                                           0
inq_12_month_num
                                           0
card_inq_24_month_num
card_open_36_month_num
                                           0
auto_open_ 36_month_num
                                           0
uti_card
                                           0
uti_50plus_pct
                                           0
uti_max_credit_line
                                           0
uti_card_50plus_pct
                                        2055
                                           0
ind_acc_XYZ
                                           0
AL
FL
                                           0
GA
                                           0
                                           0
LA
                                           0
MS
NC
                                           0
SC
                                           0
                                           0
Default_ind
dtype: int64
```

We want to preserve the utilization features as we are not concenred with collinearity for this model. Thus, we have two options: - Remove observations or column with missing values. - Impute missing values for uti_card_50plus_pct

Removing observations will rid us of 10% of our data, which is not ideal. Removing uti_card_50plus_pct is detrimental since we will be getting rid of a feature which is highly correlated with the response variable. Thus we decide to impute the missing values of uti_card_50plus_pct.

We know uti_card_50plus_pct is highly collinear with the other utilization features. Therefore, we will be using simple mean imputation with the utilization variables.

```
[148]: imputer = SingleImputer(
    strategy='mean',
    predictors=['uti_max_credit_line','uti_50plus_pct','uti_card'],
    seed = 100)
    imputed_df_train = imputer.fit_transform(df_train)
```

Check if imputation was successful:

```
[149]: print(imputed_df_train.isnull().sum())
```

```
0
tot_credit_debt
avg_card_debt
                                        0
non_mtg_acc_past_due_12_months_num
                                        0
non_mtg_acc_past_due_6_months_num
                                        0
mortgages_past_due_6_months_num
                                        0
credit_past_due_amount
                                        0
inq_12_month_num
                                        0
card_inq_24_month_num
                                        0
card_open_36_month_num
                                         0
auto_open_ 36_month_num
                                         0
uti_card
                                         0
uti_50plus_pct
                                         0
uti_max_credit_line
                                         0
uti_card_50plus_pct
                                        0
                                         0
ind_acc_XYZ
                                         0
ΑL
                                        0
FI.
GA
                                         0
T.A
                                        0
MS
                                        0
NC
                                        0
SC
                                        0
                                        0
Default_ind
dtype: int64
```

Everything looks ready for the model.

Check data:

```
[150]: print(imputed_df_train.sample) print(imputed_df_train.shape)
```

print(imputed_df_train.dtypes) <bound method NDFrame.sample of</pre> non_mtg_acc_past_due_12_months_num \

```
tot_credit_debt avg_card_debt
```

	- -		
0	80826.71	15872.99	0.0
1	96052.60	12178.02	0.0
2	75212.76	12052.24	0.0
3	70727.84	8416.80	2.0
4	41604.47	10611.97	0.0
•••	•••		
19995	104765.01	13905.40	0.0
19996	83990.07	10325.02	0.0
19997	107606.69	17838.79	1.0
19998	78787.72	11447.61	0.0
	10101.12	11111.01	
19999	78296.90	10053.16	0.0

	non_mtg_acc_past_due_6_months_num	mortgages_past_due_6_months_num	\
0	0.0	0.0	
1	0.0	0.0	
2	0.0	0.0	
3	1.0	1.0	
4	0.0	0.0	
•••	•••	•••	
19995	0.0	0.0	
19996	0.0	0.0	
19997	0.0	0.0	
19998	0.0	0.0	
19999	0.0	0.0	

	credit_past_due_amount	inq_12_month_num	card_inq_24_month_num	\
0	0.00	3.0	4.0	
1	0.00	2.0	4.0	
2	0.00	1.0	3.0	
3	11013.96	0.0	1.0	
4	0.00	0.0	2.0	
•••		•••		
19995	0.00	4.0	4.0	
19996	0.00	0.0	1.0	
19997	0.00	3.0	3.0	
19998	0.00	1.0	2.0	
19999	0.00	2.0	4.0	

	card_open_36_month_num	auto_open_ 36_month_num		\
0	0.0	0.0	•••	
1	1.0	0.0	•••	
2	0.0	1.0	•••	
3	1.0	0.0		
4	0.0	0.0	•••	

```
19995
                            0.0
                                                       0.0
                            0.0
19996
                                                       0.0
19997
                            0.0
                                                       1.0
                            0.0
                                                       0.0
19998
19999
                            0.0
                                                       0.0
       uti_card_50plus_pct
                              ind_acc_XYZ
                                            ΑL
                                                 FL
                                                     GA
                                                         LA
                                                              MS
                                                                  NC
                                                                       SC
0
                   0.489594
                                       0.0
                                              1
                                                  0
                                                      0
                                                           0
                                                               0
                                                                    0
                                                                        0
1
                   0.587351
                                       0.0
                                                           0
                                              0
                                                  1
                                                      0
                                                               0
                                                                    0
                                                                        0
2
                   0.413293
                                       0.0
                                                  0
                                                      0
                                                           0
                                                               0
                                                                    0
                                                                        0
                                              1
3
                   0.466810
                                       0.0
                                              0
                                                      0
                                                           0
                                                               0
                                                                    0
                                                                        1
4
                                                      0
                                                           1
                                                               0
                                                                    0
                                                                        0
                   0.588442
                                       1.0
                                              0
                                                                        0
19995
                   0.481113
                                       1.0
                                              0
                                                  0
                                                      1
                                                           0
                                                                    0
19996
                   0.489594
                                       0.0
                                              0
                                                      0
                                                           0
                                                               0
                                                                    1
                                                                        0
                                                  0
19997
                   0.463120
                                       0.0
                                              0
                                                  0
                                                      0
                                                           0
                                                               0
                                                                    0
                                                                        1
                                                      0
                                                           0
                                                                    0
                                                                        0
19998
                   0.281647
                                       0.0
                                              1
                                                  0
                                                               0
19999
                   0.512513
                                       0.0
                                              1
                                                  0
                                                      0
                                                           0
                                                               0
                                                                    0
                                                                        0
       Default_ind
0
                0.0
                0.0
1
2
                0.0
3
                1.0
4
                0.0
                0.0
19995
                0.0
19996
19997
                0.0
19998
                0.0
19999
                0.0
[20000 rows x 23 columns]>
(20000, 23)
tot_credit_debt
                                         float64
avg_card_debt
                                         float64
non_mtg_acc_past_due_12_months_num
                                         float64
non_mtg_acc_past_due_6_months_num
                                         float64
mortgages_past_due_6_months_num
                                         float64
credit_past_due_amount
                                         float64
inq_12_month_num
                                         float64
card_inq_24_month_num
                                         float64
card_open_36_month_num
                                         float64
auto_open_ 36_month_num
                                         float64
uti_card
                                         float64
uti_50plus_pct
                                         float64
uti_max_credit_line
                                         float64
```

```
uti_card_50plus_pct
                                         float64
ind_acc_XYZ
                                         float64
ΑL
                                           uint8
FL
                                           uint8
GA
                                           uint8
LA
                                           uint8
MS
                                           uint8
NC
                                           uint8
SC
                                           uint8
Default_ind
                                         float64
dtype: object
```

6 Model Building and Testing - Random Forests

We will firstly preprocess the validation data set in same way as train set to prepare for hyperparameter tuning.

Check validation data:

Everything looks in order.

```
[152]: print(imputed_df_validation.sample)
print(imputed_df_validation.shape)
print(imputed_df_validation.dtypes)
```

```
<bound method NDFrame.sample of</pre>
                                         tot_credit_debt avg_card_debt
non_mtg_acc_past_due_12_months_num \
                                                                          0.0
              63651.27
                               9019.99
             105559.29
                              16692.19
                                                                          0.0
1
2
              96062.99
                              10509.13
                                                                          0.0
3
              84417.40
                              13873.96
                                                                          0.0
                                                                          0.0
4
             100623.91
                              15592.09
2995
                              11481.81
                                                                          0.0
              90748.88
                                                                          0.0
2996
             101930.98
                              15242.30
                                                                          0.0
2997
             74738.73
                              12175.49
             120357.58
                              14477.70
                                                                          0.0
2998
2999
             74240.17
                              11873.45
                                                                          0.0
```

```
non_mtg_acc_past_due_6_months_num mortgages_past_due_6_months_num
0
                                        0.0
                                                                             0.0
1
                                        0.0
                                                                             0.0
2
                                        0.0
                                                                             0.0
3
                                        0.0
                                                                             0.0
4
                                        0.0
                                                                             0.0
                                                                             0.0
2995
                                        0.0
2996
                                        0.0
                                                                             0.0
2997
                                        0.0
                                                                             0.0
                                        0.0
                                                                             0.0
2998
2999
                                        0.0
                                                                             0.0
                                 inq_12_month_num
                                                     card_inq_24_month_num \
      credit_past_due_amount
0
                           0.0
                                                0.0
                                                                         0.0
                           0.0
                                                4.0
                                                                         7.0
1
2
                           0.0
                                                2.0
                                                                         3.0
3
                           0.0
                                                1.0
                                                                         1.0
4
                           0.0
                                                6.0
                                                                         9.0
2995
                                                0.0
                                                                         0.0
                           0.0
2996
                           0.0
                                                2.0
                                                                         0.0
                           0.0
                                                2.0
                                                                         4.0
2997
2998
                           0.0
                                                2.0
                                                                         2.0
2999
                           0.0
                                                4.0
                                                                         7.0
      card_open_36_month_num
                                 auto_open_ 36_month_num
0
                           0.0
                                                       0.0
1
                           0.0
                                                        1.0
                                                       0.0
2
                           0.0
3
                           0.0
                                                       0.0
4
                           0.0
                                                       0.0
2995
                           0.0
                                                        1.0
2996
                           0.0
                                                        1.0
2997
                           0.0
                                                       0.0
                           0.0
2998
                                                        1.0
2999
                           1.0
                                                        1.0
      uti_card_50plus_pct
                             ind_acc_XYZ
                                                 FL
                                                     GA
                                                              MS
                                                                   NC
                                                                       SC
                                                                           \
                                            AL
                                                         LA
0
                   0.530109
                                       0.0
                                             0
                                                               0
                                                                    0
                                                                        0
                                                  1
                                                      0
                                                           0
1
                   0.388792
                                       0.0
                                             0
                                                  0
                                                       0
                                                           0
                                                               1
                                                                    0
                                                                        0
2
                   0.450523
                                       0.0
                                             0
                                                  0
                                                      0
                                                           0
                                                               1
                                                                    0
                                                                        0
3
                                       0.0
                                             0
                                                  0
                                                           0
                                                                    0
                                                                        0
                   0.562153
4
                   0.576409
                                       1.0
                                             0
                                                  0
                                                                    1
2995
                   0.559056
                                       0.0
                                             0
                                                  1
                                                       0
                                                           0
                                                               0
                                                                    0
                                                                        0
2996
                   0.564803
                                       0.0
                                             1
                                                  0
                                                       0
                                                           0
                                                               0
                                                                    0
                                                                        0
```

```
2997
                  0.651801
                                     0.0
                                           0
                                               0
                                                    0
                                                        1
                                                            0
                                                                 0
                                                                     0
2998
                  0.557991
                                     1.0
                                           0
                                                0
                                                    0
                                                        0
                                                            0
                                                                 1
                                                                     0
2999
                  0.736850
                                     0.0
                                           0
                                                                     0
      Default ind
0
               1.0
1
              0.0
2
               0.0
3
               0.0
4
              0.0
              0.0
2995
2996
               0.0
2997
              0.0
              0.0
2998
2999
              0.0
[3000 rows x 23 columns]>
(3000, 23)
tot_credit_debt
                                        float64
avg_card_debt
                                        float64
non_mtg_acc_past_due_12_months_num
                                        float64
non_mtg_acc_past_due_6_months_num
                                        float64
mortgages_past_due_6_months_num
                                        float64
credit_past_due_amount
                                        float64
inq_12_month_num
                                        float64
card_inq_24_month_num
                                        float64
card_open_36_month_num
                                        float64
auto_open_ 36_month_num
                                        float64
uti_card
                                        float64
uti_50plus_pct
                                        float64
uti_max_credit_line
                                        float64
uti_card_50plus_pct
                                        float64
ind_acc_XYZ
                                        float64
                                          uint8
AL
FL
                                          uint8
GA
                                          uint8
LA
                                          uint8
MS
                                          uint8
NC
                                          uint8
SC
                                          uint8
                                        float64
Default_ind
dtype: object
```

We will now perform hyperparamter tuning using our validation data set (2a).

The parameters we have chosen are: - Number of estimators: 10, 100, 1000 - Max features: square root, log base 2

```
Best: 0.941111 using {'max_features': 'log2', 'n_estimators': 100} 0.936222 (0.009574) with: {'max_features': 'sqrt', 'n_estimators': 10} 0.940667 (0.010306) with: {'max_features': 'sqrt', 'n_estimators': 100} 0.940556 (0.009929) with: {'max_features': 'sqrt', 'n_estimators': 1000} 0.937778 (0.009480) with: {'max_features': 'log2', 'n_estimators': 10} 0.941111 (0.010830) with: {'max_features': 'log2', 'n_estimators': 100} 0.940444 (0.010532) with: {'max_features': 'log2', 'n_estimators': 1000}
```

Based on this, the most accurate model has the following hyperparameters: - Number of estimators: 100 - Max features: log base 2

Train model based on chosen hyperparameters using the train data set:

```
[153]: rfModel = RandomForestClassifier(max_features="log2",n_estimators=100)
rfModel = rfModel.fit(imputed_df_train.iloc[:,range(0,22)], imputed_df_train.

iloc[:,22])
```

Transforming test data to match training data:

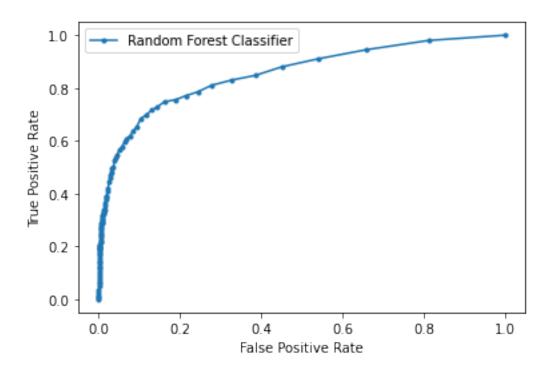
Check data:

```
[155]: print(imputed_df_test.sample)
    print(imputed_df_test.shape)
    print(imputed_df_test.dtypes)
```

```
<bound method NDFrame.sample of</pre>
                                         tot_credit_debt avg_card_debt
non_mtg_acc_past_due_12_months_num \
             40477.81
                               7766.64
                                                                           0.0
1
             106760.98
                              16606.98
                                                                           0.0
2
                                                                           0.0
             121428.34
                              13910.13
3
              96515.05
                              15436.78
                                                                           0.0
4
             123760.22
                              14213.25
                                                                           0.0
                               ...
                 •••
4995
              90788.44
                              11646.36
                                                                           0.0
              91052.81
4996
                              16505.20
                                                                           0.0
4997
              71061.71
                              11512.18
                                                                           0.0
4998
              82162.45
                              10014.90
                                                                           0.0
4999
                              18042.56
                                                                           0.0
             116943.32
      non_mtg_acc_past_due_6_months_num
                                           mortgages_past_due_6_months_num
0
                                       0.0
1
                                       0.0
                                                                           0.0
2
                                       0.0
                                                                           0.0
3
                                       0.0
                                                                           0.0
                                                                           0.0
4
                                       0.0
4995
                                       0.0
                                                                           0.0
4996
                                       0.0
                                                                           0.0
4997
                                       0.0
                                                                           0.0
4998
                                       0.0
                                                                           0.0
4999
                                       0.0
                                                                           0.0
      credit_past_due_amount
                                                   card_inq_24_month_num \
                                inq_12_month_num
0
                                              2.0
                                                                       4.0
                           0.0
1
                           0.0
                                              2.0
                                                                       4.0
2
                           0.0
                                              0.0
                                                                       1.0
3
                           0.0
                                              0.0
                                                                       0.0
4
                           0.0
                                                                       0.0
                                              0.0
4995
                           0.0
                                              0.0
                                                                       4.0
                                                                       5.0
4996
                           0.0
                                              3.0
                                                                       5.0
4997
                           0.0
                                              3.0
4998
                           0.0
                                              1.0
                                                                       2.0
4999
                           0.0
                                              4.0
                                                                       8.0
      card_open_36_month_num
                                auto_open_ 36_month_num
0
                                                      1.0
                           0.0
                                                      0.0
1
                           0.0
2
                                                      0.0
                           0.0
3
                           0.0
                                                      0.0
4
                           0.0
                                                      0.0
4995
                           0.0
                                                      0.0 ...
```

```
0.0
                                                       0.0
4996
4997
                           1.0
                                                       1.0
4998
                           0.0
                                                       0.0
4999
                           1.0
                                                       0.0 ...
      uti_card_50plus_pct
                             ind_acc_XYZ
                                           AL
                                                    GA
                                                         LA
                                                             MS
                                                                  NC
                                                                      SC
                                                FL
0
                  0.633699
                                      0.0
                                             0
                                                 1
                                                      0
                                                          0
                                                              0
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                                                                       0
                                      1.0
1
                  0.746901
                                             1
                                                 0
                                                      0
                                                          0
                                                              0
                                                                   0
                                                                       0
2
                  0.458438
                                      0.0
                                             0
                                                 0
                                                      0
                                                          0
                                                              1
                                                                   0
                                                                       0
3
                                      1.0
                                                          0
                                                              0
                  0.582352
                                             1
                                                 0
                                                      0
                                                                   0
                                                                       0
4
                  0.577697
                                      0.0
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                                                      1
                                                          0
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                                                                       0
                                      0.0
                                                                       0
4995
                  0.398411
                                             0
                                                 0
                                                              0
                                                                   0
                                                          1
4996
                  0.286623
                                      1.0
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                                                                   0
                                                                       1
                                      1.0
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                                                              0
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4997
                  0.443688
                                                      0
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4998
                  0.178131
                                      0.0
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                                                                   0
4999
                  0.503552
                                      0.0
                                             0
                                                 0
                                                      0
                                                          0
                                                                   0
                                                                       0
      Default_ind
               0.0
0
1
               0.0
2
               0.0
3
               0.0
4
               0.0
               0.0
4995
4996
               0.0
               0.0
4997
               0.0
4998
4999
               0.0
[5000 rows x 23 columns]>
(5000, 23)
tot_credit_debt
                                         float64
avg card debt
                                         float64
non_mtg_acc_past_due_12_months_num
                                         float64
non_mtg_acc_past_due_6_months_num
                                         float64
mortgages_past_due_6_months_num
                                          float64
credit_past_due_amount
                                         float64
inq_12_month_num
                                         float64
card_inq_24_month_num
                                         float64
card_open_36_month_num
                                         float64
auto_open_ 36_month_num
                                         float64
uti_card
                                         float64
uti_50plus_pct
                                         float64
uti_max_credit_line
                                         float64
uti_card_50plus_pct
                                         float64
{\tt ind\_acc\_XYZ}
                                         float64
```

```
ΑL
                                                uint8
      FL
                                                uint8
      GA
                                                uint8
      LA
                                                uint8
      MS
                                                uint8
      NC
                                                uint8
      SC
                                                uint8
      Default_ind
                                              float64
      dtype: object
      Scoring test data:
[156]: rfModel.score(imputed_df_test.iloc[:,range(0,22)], imputed_df_test.iloc[:,22])
[156]: 0.9366
      Testing with a confusion matrix:
[157]: confusion_matrix(imputed_df_test.iloc[:,22],rfModel.predict(imputed_df_test.
        \rightarrowiloc[:,range(0,22)]))
[157]: array([[4568,
                        31],
              [ 286, 115]], dtype=int64)
      ROC curve for random forest classifier (2b):
[158]: rf_probs = rfModel.predict_proba(imputed_df_test.iloc[:,range(0,22)])
       rf_probs = rf_probs[:, 1]
       rf_fpr, rf_tpr, _ = roc_curve(imputed_df_test.iloc[:,22], rf_probs)
       plt.plot(rf_fpr, rf_tpr, marker='.', label='Random Forest Classifier')
       plt.xlabel('False Positive Rate')
       plt.ylabel('True Positive Rate')
       plt.legend()
       plt.show()
```



Find feature importance (2c):

The higher the score, the more important the feature.

Important Notes: - Despite not presenting much correlation with response variable, total credit debt and average card debt play the most important roles in determining defaults - Utilization variables are all very important - State, XYZ previous account indicator, and credit products opened in 36 months variables play a marginal role

```
[182]: variables = []
for var in imputed_df_train.columns:
    variables.append(var)
importance = rfModel.feature_importances_
index = 0
for i,v in enumerate(importance):
    print('Feature: {variable}\n Score: {v}\n\n'.format(variable =_\u00fc)
    variables[index],v = v))
    index += 1
plt.bar([x for x in range(len(importance))], importance)
plt.show()
```

Feature: tot_credit_debt Score: 0.10116110103522905 Feature: avg_card_debt Score: 0.15612549704029433

Feature: non_mtg_acc_past_due_12_months_num

Score: 0.051588433741830204

Feature: non_mtg_acc_past_due_6_months_num

Score: 0.026114066030776564

Feature: mortgages_past_due_6_months_num

Score: 0.04471094287968974

Feature: credit_past_due_amount Score: 0.07272974478355873

Feature: inq_12_month_num Score: 0.040155479644069965

Feature: card_inq_24_month_num Score: 0.0476335411984235

Feature: card_open_36_month_num Score: 0.012521132722843388

Feature: auto_open_ 36_month_num Score: 0.009328620784239058

Feature: uti_card

Score: 0.10270683546384929

Feature: uti_50plus_pct Score: 0.08696333953190324

Feature: uti_max_credit_line Score: 0.09047046122791504

Feature: uti_card_50plus_pct Score: 0.08913573380667056

 $Feature: \ ind_acc_XYZ$

Score: 0.011392454240505133

Feature: AL

Score: 0.008526349581013072

Feature: FL

Score: 0.00890519489911215

Feature: GA

Score: 0.007348783410222652

Feature: LA

Score: 0.008199211337674586

Feature: MS

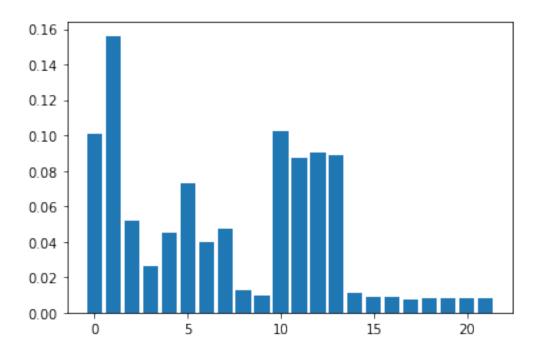
Score: 0.008037655223021628

Feature: NC

Score: 0.008202140317150004

Feature: SC

Score: 0.008043281100008147

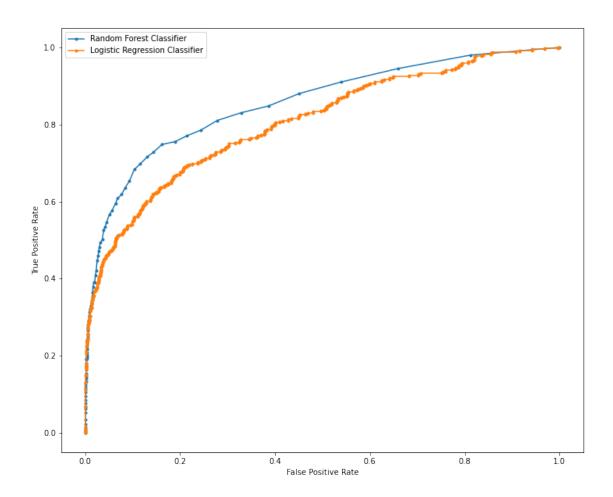


7 Comparing Models

Comparing ROC curves and AUC (2b):

Random forest performs better, as expected, because the true positive rate was better. This is confirmed by the AUC calculation as well.

```
fig, ax = plt.subplots(figsize=(12,10))
plt.plot(rf_fpr, rf_tpr, marker='.', label='Random Forest Classifier')
plt.plot(lr_fpr, lr_tpr, marker='.', label='Logistic Regression Classifier')
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.legend()
plt.show()
```

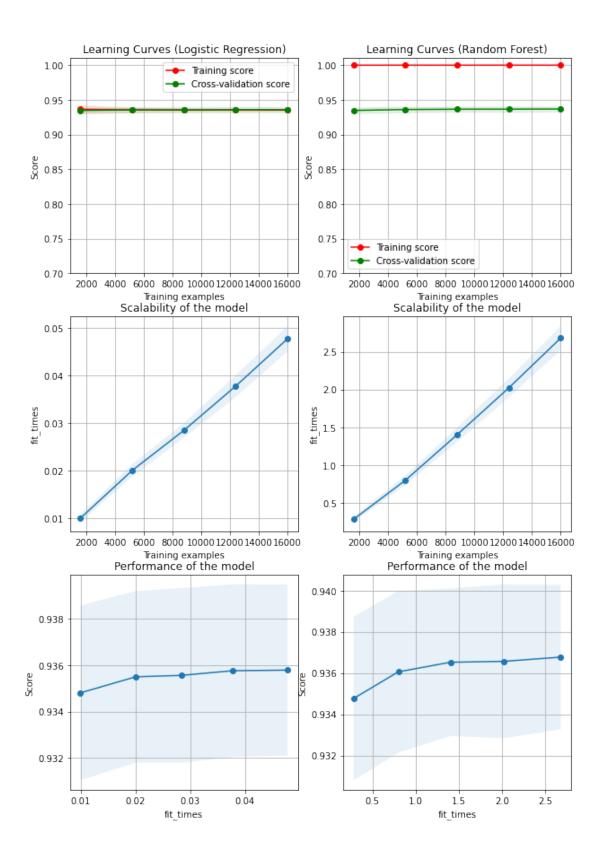


```
[136]: lr_auc = roc_auc_score(df_test_norm.iloc[:,16], lr_probs)
    rf_auc = roc_auc_score(imputed_df_test.iloc[:,22], rf_probs)
    print('Logistic Regression: ROC AUC=%.3f' % (lr_auc))
    print('Random Forest: ROC AUC=%.3f' % (rf_auc))
```

Logistic Regression: ROC AUC=0.806 Random Forest: ROC AUC=0.852

Comparing Learning curves (3): - While the training score for the random forest model is very high (a natural consequence of an algorithm that is extremely robust), the cross validation scores are very comperable throughout - Unsurpisingly, logistic regression is found to be much more scalable - Model performence is slightly higher for random forest model

```
if ylim is not None:
    axes[0].set_ylim(*ylim)
axes[0].set_xlabel("Training examples")
axes[0].set_ylabel("Score")
train_sizes, train_scores, test_scores, fit_times, _ = \
    learning_curve(estimator, X, y, cv=cv, n_jobs=n_jobs,
                   train_sizes=train_sizes,
                   return times=True)
train_scores_mean = np.mean(train_scores, axis=1)
train scores std = np.std(train scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)
fit_times_mean = np.mean(fit_times, axis=1)
fit_times_std = np.std(fit_times, axis=1)
axes[0].grid()
axes[0].fill_between(train_sizes, train_scores_mean - train_scores_std,
                     train_scores_mean + train_scores_std, alpha=0.1,
                     color="r")
axes[0].fill_between(train_sizes, test_scores_mean - test_scores_std,
                     test_scores_mean + test_scores_std, alpha=0.1,
                     color="g")
axes[0].plot(train_sizes, train_scores_mean, 'o-', color="r",
             label="Training score")
axes[0].plot(train_sizes, test_scores_mean, 'o-', color="g",
             label="Cross-validation score")
axes[0].legend(loc="best")
axes[1].grid()
axes[1].plot(train_sizes, fit_times_mean, 'o-')
axes[1].fill_between(train_sizes, fit_times_mean - fit_times_std,
                     fit_times_mean + fit_times_std, alpha=0.1)
axes[1].set_xlabel("Training examples")
axes[1].set_ylabel("fit_times")
axes[1].set_title("Scalability of the model")
axes[2].grid()
axes[2].plot(fit times mean, test scores mean, 'o-')
axes[2].fill_between(fit_times_mean, test_scores_mean - test_scores_std,
                     test_scores_mean + test_scores_std, alpha=0.1)
axes[2].set_xlabel("fit_times")
axes[2].set ylabel("Score")
axes[2].set_title("Performance of the model")
return plt
```



8 Code References

Thank you to the following:

(1) Aniruddha Bhandari:

What is Multicollinearity? Here's Everything You Need to Know

- (2) Jason Brownlee, PhD of Machine Learning Mastery:
- a. Tune Hyperparameters for Classification Machine Learning Algorithms
- b. How to Use ROC Curves and Precision-Recall Curves for Classification in Python
- c. How to Calculate Feature Importance With Python
- (3) SKLearn:

Plotting Learning Curves