## **Analytic Rotation Curves Without Dark Matter Fluid**

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## **ABSTRACT**

This paper investigates the astrophysical implications of incorporating Gravitational Friction (GF) into the dynamics of gravitational systems, particularly focusing on galaxy rotation curves without invoking dark matter. We analyze rotation curves from 175 late-type galaxies using data from the Spitzer Photometry & Accurate Rotation Curves (SPARC) database to determine the free parameter of the proposed model. Our results are compared with leading dark matter density profiles, including the Pseudoisothermal (pISO), Navarro-Frenk-White (NFW), and Burkert models, to evaluate the viability of GF as a competitive alternative to traditional dark matter explanations.

**Key words:** Gravitational friction – Stellar dynamics – Galaxy dynamics

## 1 PISO, NFW AND BURKERT ROTATION VELOCITIES

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| Index | Name               | GF    | NFW   | pISO         | Einasto      | Burkert | Inde | ex | Name               | GF    | NFW   | pISO  | Einasto | Burkert      |
|-------|--------------------|-------|-------|--------------|--------------|---------|------|----|--------------------|-------|-------|-------|---------|--------------|
| 1     | CamB               | 3.746 | 8.61  | 2.99         | 4.01         | 3.01    | 5    | 51 | NGC3877            | 1.888 | 5.95  | 3.47  | 2.75    | 2.44         |
| 2     | D631-7             | 2.362 | 6.05  | 0.85         | 0.72         | 0.95    | 5    | 52 | NGC3893            | 0.709 | 0.99  | 0.69  | 0.54    | 0.31         |
| 3     | DDO064             | 0.066 | 0.69  | 0.48         | 0.46         | 0.45    | 5    | 53 | NGC3917            | 0.996 | 3.33  | 1.64  | 1.38    | 1.31         |
| 4     | DDO154             | 1.745 | 13.70 | 3.23         | 0.83         | 1.63    | 5    | 54 | NGC3949            | 0.284 | 0.80  | 0.84  | 1.62    | 0.84         |
| 5     | DDO161             | 0.400 | 1.01  | 0.36         | 0.24         | 0.29    | 5    | 55 | NGC3953            | 0.430 | 0.52  | 0.56  | 0.64    | 0.28         |
| 6     | DDO168             | 4.072 | 14.40 | 6.03         | 4.76         | 6.06    | 5    | 6  | NGC3972            | 0.777 | 1.81  | 0.80  | 1.24    | 1.13         |
| 7     | DDO170             | 2.936 | 4.32  | 2.45         | 4.77         | 2.70    | 5    | 57 | NGC3992            | 1.085 | 0.72  | 0.71  | 0.92    | 1.00         |
| 8     | ESO079-G014        | 1.207 | 4.68  | 1.61         | 0.97         | 1.15    | 5    | 8  | NGC4010            | 0.702 | 3.09  | 2.16  | 1.56    | 1.98         |
| 9     | ESO116-G012        | 0.559 | 3.02  | 1.27         | 0.95         | 0.98    | 5    | 9  | NGC4013            | 0.781 | 0.81  | 0.84  | 0.85    | 0.84         |
| 10    | ESO444-G084        | 0.542 | 1.49  | 2.74         | 0.48         | 3.98    | 6    | 60 | NGC4051            | 0.806 | 1.72  | 1.73  | 1.67    | 1.26         |
| 11    | ESO563-G021        | 7.377 | 19.15 | 12.37        | 8.98         | 8.41    | 6    | 51 | NGC4085            | 0.868 | 9.76  | 5.28  | 7.84    | 5.20         |
| 12    | F563-1             | 0.563 | 1.34  | 0.70         | 0.93         | 0.70    | 6    | 52 | NGC4088            | 0.469 | 0.59  | 0.64  | 0.74    | 0.63         |
| 13    | F563-V2            | 0.055 | 1.91  | 0.47         | 0.14         | 0.28    |      | 63 | NGC4100            | 1.269 | 0.99  | 1.21  | 0.44    | 0.59         |
| 14    | F565-V2            | 0.032 | 0.94  | 0.16         | 0.32         | 0.14    |      | 64 | NGC4157            | 0.257 | 0.49  | 0.45  | 0.47    | 0.45         |
| 15    | F568-1             | 0.231 | 1.19  | 0.18         | 0.18         | 0.13    |      | 55 | NGC4183            | 1.071 | 0.20  | 0.14  | 0.20    | 0.44         |
| 16    | F568-3             | 1.024 | 3.89  | 1.18         | 1.23         | 1.17    |      | 66 | NGC4214            | 0.710 | 0.64  | 0.77  | 0.19    | 1.07         |
| 17    | F568-V1            | 0.092 | 0.28  | 0.19         | 0.12         | 0.07    |      | 57 | NGC4217            | 1.208 | 3.74  | 2.23  | 1.39    | 1.49         |
| 18    | F571-8             | 3.973 | 2.12  | 0.75         | 0.55         | 0.53    |      | 68 | NGC4559            | 0.254 | 0.24  | 0.35  | 0.11    | 0.26         |
| 19    | F571-V1            | 0.039 | 0.76  | 0.18         | 0.21         | 0.08    |      | 59 | NGC5005            | 0.122 | 0.09  | 0.10  | 0.12    | 0.10         |
| 20    | F574-1             | 0.215 | 2.19  | 0.35         | 0.23         | 0.12    |      | 0  | NGC5033            | 1.111 | 3.53  | 7.15  | 2.21    | 2.54         |
| 21    | F579-V1            | 0.443 | 0.25  | 0.06         | 0.22         | 0.18    | 7    |    | NGC5055            | 1.626 | 2.58  | 6.19  | 2.70    | 2.10         |
| 22    | F583-1             | 0.455 | 1.79  | 0.36         | 0.18         | 0.21    |      | 2  | NGC5585            | 4.320 | 6.65  | 5.18  | 4.24    | 4.98         |
| 23    | F583-4             | 0.254 | 0.21  | 0.42         | 0.23         | 0.64    |      | 13 | NGC5907            | 4.980 | 5.24  | 3.30  | 3.57    | 6.05         |
| 24    | IC2574             | 1.661 | 36.55 | 2.51         | 2.05         | 2.41    |      | 74 | NGC5985            | 4.652 | 1.91  | 2.54  | 2.14    | 2.95         |
| 25    | IC4202             | 8.698 | 20.17 | 8.67         | 5.43         | 2.95    | 7    |    | NGC6195            | 1.241 | 2.08  | 1.81  | 1.84    | 1.79         |
| 26    | KK98-251           | 0.119 | 1.57  | 0.35         | 0.34         | 0.37    |      | 76 | NGC6503            | 2.204 | 1.55  | 1.29  | 1.41    | 2.53         |
| 27    | NGC0024            | 1.727 | 0.93  | 0.33         | 0.34         | 0.86    |      | 7  | NGC6503            | 5.128 | 2.78  | 1.47  | 1.63    | 1.44         |
| 28    | NGC0024<br>NGC0055 | 0.093 | 2.85  | 0.57         | 0.17         | 0.41    |      | 78 | NGC6946            | 1.288 | 1.69  | 1.55  | 1.57    | 1.53         |
| 29    | NGC0100            | 0.093 | 0.89  | 0.33         | 0.17         | 0.41    |      | 19 | NGC0940<br>NGC7331 | 0.704 | 0.81  | 0.95  | 0.74    | 1.29         |
| 30    | NGC0247            | 2.854 | 2.03  | 2.38         |              | 2.06    |      | 30 | NGC7331<br>NGC7793 | 0.704 | 0.90  | 0.93  | 0.74    |              |
|       | NGC0247<br>NGC0289 | 1.222 | 1.95  | 2.38<br>1.97 | 1.77<br>2.03 |         | 8    |    | NGC7793<br>NGC7814 | 0.394 | 0.56  | 0.79  | 0.59    | 0.76<br>0.87 |
| 31    | NGC0289<br>NGC0300 | 0.423 |       | 0.47         |              | 2.06    |      |    |                    |       | 5.96  |       |         |              |
| 32    |                    |       | 0.74  |              | 0.50         | 0.62    |      | 32 | UGC00191           | 4.650 |       | 1.97  | 5.15    | 6.73         |
| 33    | NGC0801            | 3.574 | 6.77  | 7.07         | 7.70         | 7.10    |      | 33 | UGC00731           | 0.393 | 0.45  | 0.22  | 0.13    | 0.56         |
| 34    | NGC0891            | 1.203 | 3.46  | 4.24         | 1.35         | 2.01    |      | 34 | UGC01230           | 0.356 | 1.61  | 1.18  | 0.74    | 0.37         |
| 35    | NGC1003            | 3.009 | 2.48  | 2.67         | 2.47         | 3.01    |      | 35 | UGC01281           | 0.216 | 1.08  | 0.14  | 0.03    | 0.14         |
| 36    | NGC1090            | 1.905 | 2.73  | 1.54         | 1.79         | 1.41    |      | 36 | UGC02259           | 2.989 | 1.39  | 0.96  | 1.97    | 4.53         |
| 37    | NGC1705            | 0.255 | 0.15  | 0.08         | 0.07         | 0.84    | 8    |    | UGC02455           | 1.960 | 3.50  | 1.07  | 1.58    | 1.06         |
| 38    | NGC2366            | 0.181 | 3.49  | 1.09         | 0.24         | 0.86    |      | 88 | UGC02487           | 3.241 | 5.24  | 4.86  | 5.76    | 4.84         |
| 39    | NGC2683            | 0.497 | 1.50  | 1.89         | 1.71         | 1.25    |      | 39 | UGC02885           | 0.588 | 0.99  | 0.84  | 1.04    | 1.10         |
| 40    | NGC2841            | 2.014 | 1.48  | 1.58         | 1.36         | 1.81    |      | 00 | UGC02916           | 9.689 | 11.37 | 11.58 | 9.18    | 10.55        |
| 41    | NGC2903            | 5.694 | 6.34  | 6.67         | 6.19         | 7.20    | 9    |    | UGC02953           | 5.836 | 5.64  | 4.97  | 5.70    | 6.07         |
| 42    | NGC2915            | 0.536 | 0.97  | 0.71         | 0.71         | 0.56    |      | 2  | UGC03205           | 3.501 | 3.08  | 3.82  | 2.94    | 3.84         |
| 43    | NGC2955            | 4.565 | 4.03  | 4.21         | 2.89         | 3.71    |      | 93 | UGC03546           | 0.606 | 0.96  | 0.99  | 0.75    | 0.72         |
| 44    | NGC2976            | 0.242 | 0.85  | 0.33         | 0.34         | 0.34    |      | 94 | UGC03580           | 2.658 | 2.34  | 2.40  | 2.35    | 2.69         |
| 45    | NGC2998            | 2.022 | 3.05  | 1.47         | 1.09         | 3.52    |      | 95 | UGC04278           | 1.099 | 1.37  | 0.58  | 0.57    | 0.58         |
| 46    | NGC3109            | 0.295 | 9.92  | 0.23         | 0.22         | 0.20    |      | 96 | UGC04305           | 1.366 | 1.81  | 1.45  | 0.71    | 1.08         |
| 47    | NGC3198            | 1.416 | 1.46  | 1.31         | 1.08         | 1.47    |      | 97 | UGC04325           | 0.530 | 5.31  | 2.89  | 1.44    | 0.80         |
| 48    | NGC3521            | 0.399 | 0.25  | 0.20         | 0.12         | 0.20    | 9    | 8  | UGC04483           | 0.130 | 1.19  | 0.54  | 0.92    | 0.50         |
| 49    | NGC3741            | 0.177 | 0.41  | 0.90         | 0.44         | 0.93    | 9    | 9  | UGC04499           | 0.335 | 1.78  | 0.46  | 0.61    | 0.39         |
| 50    | NGC3769            | 0.344 | 0.93  | 0.88         | 1.00         | 0.77    | 10   | 00 | UGC05005           | 9.250 | 0.33  | 0.05  | 0.01    | 0.02         |

**Table 1.** with Burkert and surface tension rotation velocities. From left to right, the columns read: name of the galaxy; central density in units of  $M_{\odot}/\mathrm{pc}^3$ ; central radius in kpc and the  $\chi^2_{\mathrm{red}}$  value for the Burkert and our model cases.

**Table 2.** Table with the index starting from 51 and ending at 100.

| Index | Name     | GF    | NFW    | pISO   | Einasto | Burkert |
|-------|----------|-------|--------|--------|---------|---------|
| 101   | UGC05253 | 1.172 | 2.42   | 3.79   | 0.77    | 0.95    |
| 102   | UGC05716 | 1.059 | 2.49   | 3.07   | 2.54    | 2.35    |
| 103   | UGC05721 | 0.222 | 1.09   | 0.94   | 0.53    | 0.44    |
| 104   | UGC05750 | 0.071 | 1.44   | 0.26   | 0.08    | 0.18    |
| 105   | UGC05764 | 1.503 | 10.58  | 7.05   | 4.04    | 4.05    |
| 106   | UGC05829 | 0.100 | 0.13   | 0.19   | 0.12    | 0.26    |
| 107   | UGC05918 | 0.071 | 0.29   | 0.03   | 0.12    | 0.09    |
| 108   | UGC05986 | 0.238 | 5.89   | 1.72   | 0.09    | 1.13    |
| 109   | UGC06399 | 0.035 | 1.14   | 0.15   | 0.12    | 0.08    |
| 110   | UGC06446 | 0.266 | 0.27   | 0.22   | 0.25    | 0.51    |
| 111   | UGC06614 | 0.202 | 0.27   | 0.18   | 0.11    | 0.10    |
| 112   | UGC06628 | 0.040 | 0.25   | 0.31   | 0.17    | 0.16    |
| 113   | UGC06667 | 0.263 | 2.28   | 0.39   | 0.15    | 0.17    |
| 114   | UGC06786 | 1.579 | 0.69   | 0.69   | 0.54    | 2.26    |
| 115   | UGC06818 | 0.582 | 5.89   | 2.10   | 3.13    | 2.18    |
| 116   | UGC06917 | 0.153 | 1.17   | 0.39   | 0.45    | 0.29    |
| 117   | UGC06930 | 0.293 | 0.44   | 0.22   | 0.34    | 0.28    |
| 118   | UGC06973 | 0.172 | 1.68   | 1.45   | 3.00    | 1.61    |
| 119   | UGC06983 | 0.305 | 0.74   | 0.58   | 0.60    | 0.53    |
| 120   | UGC07089 | 0.088 | 0.36   | 0.23   | 0.15    | 0.22    |
| 121   | UGC07125 | 0.572 | 0.82   | 0.40   | 0.30    | 0.27    |
| 122   | UGC07151 | 0.522 | 3.64   | 1.58   | 2.01    | 1.36    |
| 123   | UGC07261 | 0.556 | 0.12   | 0.16   | 0.14    | 0.86    |
| 124   | UGC07323 | 0.132 | 1.04   | 0.43   | 0.44    | 0.40    |
| 125   | UGC07399 | 0.460 | 1.61   | 0.36   | 0.99    | 1.28    |
| 126   | UGC07524 | 0.181 | 0.89   | 0.34   | 0.21    | 0.25    |
| 127   | UGC07559 | 0.070 | 1.07   | 0.26   | 0.36    | 0.27    |
| 128   | UGC07577 | 0.178 | 0.36   | 0.22   | 0.29    | 0.22    |
| 129   | UGC07603 | 0.132 | 2.14   | 0.47   | 0.36    | 0.28    |
| 130   | UGC07608 | 0.073 | 0.89   | 0.14   | 0.30    | 0.16    |
| 131   | UGC07690 | 0.051 | 0.84   | 0.87   | 0.75    | 0.29    |
| 132   | UGC07866 | 0.042 | 0.11   | 0.12   | 0.19    | 0.18    |
| 133   | UGC08286 | 2.490 | 2.87   | 1.00   | 1.88    | 1.48    |
| 134   | UGC08490 | 0.405 | 0.13   | 0.21   | 0.12    | 0.42    |
| 135   | UGC08550 | 0.601 | 1.08   | 0.55   | 0.91    | 1.30    |
| 136   | UGC08699 | 0.720 | 0.73   | 0.87   | 0.70    | 0.97    |
| 137   | UGC08837 | 0.432 | 8.32   | 0.68   | 1.02    | 0.67    |
| 138   | UGC09037 | 0.781 | 2.03   | 1.09   | 1.13    | 1.02    |
| 139   | UGC09133 | 6.268 | 7.15   | 6.78   | 6.36    | 7.89    |
| 140   | UGC10310 | 0.053 | 1.39   | 0.64   | 0.40    | 0.23    |
| 141   | UGC11455 | 3.076 | 5.40   | 2.40   | 2.10    | 1.64    |
| 142   | UGC11557 | 0.433 | 1.59   | 0.67   | 0.51    | 0.66    |
| 143   | UGC11820 | 5.470 | 1.82   | 3.46   | 1.51    | 2.42    |
| 144   | UGC11914 | 0.686 | 0.86   | 0.65   | 0.53    | 0.59    |
| 145   | UGC12506 | 1.492 | 0.18   | 0.29   | 0.17    | 0.77    |
| 146   | UGC12632 | 0.050 | 0.43   | 0.17   | 0.11    | 0.09    |
| 147   | UGC12732 | 0.245 | 0.24   | 0.24   | 0.21    | 0.44    |
| 148   | UGCA281  | 0.140 | 1.29   | 0.38   | 0.59    | 0.29    |
| 149   | UGCA442  | 0.392 | 3.85   | 1.60   | 1.43    | 1.24    |
| 150   | UGCA444  | 0.399 | 0.07   | 0.22   | 0.07    | 0.24    |
|       | TOTAL    | 205.3 | 426.56 | 243.33 | 208.68  | 225.93  |
|       | INF      | 7     | 10     | 10     | 19      | 10      |

Table 3. Your table caption here