

Lab1

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1 Statement of Contribution

In Assignment 1, Xiaochen Liu was mainly responsible for code writing while Liuxi Mei was responsible for the analyses. Assignment 2 was mainly contributed by Han Xia. In assignment 3, Liuxi Mei was responsible for code writing while Han Xia was responsible for the analysis. Assignment 4 was mainly contributed by Xiaochen Liu and Liuxi Mei. Results from all assignments have been discussed afterwards between Liuxi Mei, Xiaochen Liu and Han Xia and the group report was created based on this discussion.

2 Introduction

This is the first lab in the Machine Learning In this lab, contains the following tasks:1. Handwritten digit recognition with K-nearest neighbors.2.Linear regression and ridge regression.3. Logistic regression and basis function expansion.4. Theory

3 Assignment 1: Handwritten digit recognition with K-nearest neighbors

3.1 Load and check data

```
# Load packages  
library('ggplot2') # visualization  
library('ggthemes') # visualization
```

```
## Warning: package 'ggthemes' was built under R version 4.4.2
```

```
library('scales') # visualization  
library('dplyr') # data manipulation  
library('randomForest') # classification algorithm
```

```
## Warning: package 'randomForest' was built under R version 4.4.2
```

```
library('caret')
```

```
## Warning: package 'caret' was built under R version 4.4.2
```

Now that our packages are loaded and we divide it into training, validation and test sets (50%/25%/25%)

```
# do not use StringAsFactor = FALSE
digitals <- read.csv('../data/optdigits.csv',header = FALSE)
# change all the columns to factor
#digitals <- digitals %>% mutate_all(as.factor)
digitals$V65 <- as.factor(digitals$V65)
train_index <- createDataPartition(digitals$V65, p = 0.5, list = F)
train_digitals <- digitals[train_index,]
remainingData <- digitals[-train_index, ]
validationIndex <- createDataPartition(remainingData$V65, p = 0.5, list = FALSE)
valid_digitals <- remainingData[validationIndex, ]
test_digitals <- remainingData[-validationIndex, ]
cat("train length:", nrow(train_digitals),'\n')
```

```
## train length: 1914
```

```
cat("test length:", nrow(valid_digitals),'\n')
```

```
## test length: 956
```

```
cat("valid length:", nrow(test_digitals),'\n')
```

```
## valid length: 953
```

3.2 KNN to fit classification model using train data

```
library(kknn)
formula <- V65~.
# if kernel = 'rectangular' , so every point in the neighborhood is weighted equally
# both of the parameters of train and test use train_digital data
# if your predict columns is continuous, kknn will recognized as a regression task
# under this situation, you can not get a probability of the prediction
knn_train_model <- kknn(formula, train_digitals, train_digitals, kernel = 'rectangular',distance = 1,)
train_predictions <- fitted(knn_train_model)
print(length(train_predictions))
```

```
## [1] 1914
```

```
summary(knn_train_model)
```

```
##
## Call:
## kknnc(formula = formula, train = train_digitals, test = train_digitals, distance = 1, kernel = "r
##
## Response: "nominal"
##      fit      prob.0      prob.1      prob.2      prob.3      prob.4      prob.5      prob.6
## 1      5 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000
## 2      0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 3      8 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 4      1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 5      9 0.0000000 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000
## 6      3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 7      4 0.0000000 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
## 8      7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 9      4 0.0000000 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
## 10     7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 11     5 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000
## 12     9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 13     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 14     6 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000
## 15     8 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 16     7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 17     6 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000
## 18     3 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.2857143 0.0000000
## 19     9 0.0000000 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000
## 20     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 21     9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 22     9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 23     8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 24     2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 25     7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 26     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 27     4 0.0000000 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
## 28     0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 29     4 0.0000000 0.1428571 0.0000000 0.0000000 0.5714286 0.0000000 0.0000000
## 30     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 31     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 32     0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 33     2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 34     5 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000
## 35     4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 36     8 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 37     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 38     7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 39     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 40     0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 41     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 42     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 43     1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 44     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 45     3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 46     8 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 47     9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 48     4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
```

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##	427	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	428	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	429	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	430	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	431	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	432	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	433	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571
##	434	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	435	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	436	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	437	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	438	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000
##	439	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	440	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	441	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	442	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	443	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	444	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.1428571	0.0000000
##	445	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	446	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	447	4	0.0000000	0.0000000	0.0000000	0.0000000	0.7142857	0.0000000	0.0000000
##	448	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	449	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	450	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	451	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	452	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	453	3	0.0000000	0.1428571	0.0000000	0.7142857	0.0000000	0.0000000	0.0000000
##	454	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	455	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	456	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000
##	457	8	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000
##	458	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	459	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	460	8	0.0000000	0.0000000	0.0000000	0.			

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## 589	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.7142857	0.0000000
## 590	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
## 591	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 592	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 593	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 594	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 595	9	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000	0.0000000	0.0000000
## 596	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 597	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 598	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 599	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 600	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 601	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 602	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000
## 603	5	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.8571429	0.0000000
## 604	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000
## 605	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 606	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 607	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 608	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 609	5	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.4285714	0.0000000
## 610	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 611	2	0.0000000	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000	0.0000000
## 612	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 613	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 614	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 615	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 616	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 617	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 618	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 619	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 620	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 621	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 622	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 623	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000		

##	643	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	644	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	645	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	646	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	647	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	648	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	649	2	0.0000000	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000
##	650	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	651	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	652	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	653	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	654	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	655	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	656	3	0.0000000	0.0000000	0.0000000	0.5714286	0.0000000	0.1428571
##	657	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	658	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	659	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	660	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	661	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	662	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	663	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	664	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	665	8	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000
##	666	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000
##	667	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	668	3	0.0000000	0.0000000	0.0000000	0.7142857	0.0000000	0.1428571
##	669	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	670	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	671	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	672	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	673	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	674	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	675	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	676	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	677	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	678	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	679	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	680	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.00

## 697	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 698	9	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000
## 699	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 700	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 701	6	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429
## 702	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 703	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 704	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 705	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 706	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 707	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 708	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 709	8	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000
## 710	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571
## 711	4	0.0000000	0.0000000	0.0000000	0.0000000	0.5714286	0.0000000
## 712	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 713	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000
## 714	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 715	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 716	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 717	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 718	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 719	8	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000
## 720	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 721	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 722	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 723	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 724	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 725	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 726	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 727	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 728	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 729	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 730	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 731	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 732	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 733	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 734	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 735	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 736	3	0.0000000	0.00				

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## 805	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 806	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 807	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 808	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 809	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 810	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 811	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 812	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 813	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 814	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 815	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 816	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 817	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 818	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 819	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 820	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
## 821	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 822	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.1428571
## 823	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 824	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 825	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 826	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 827	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 828	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 829	8	0.0000000	0.2857143	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 830	8	0.0000000	0.0000000	0.0000000	0.2857143	0.0000000	0.1428571	0.0000000
## 831	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 832	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 833	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 834	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 835	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 836	4	0.1428571	0.1428571	0.0000000	0.0000000	0.7142857	0.0000000	0.0000000
## 837	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 838	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 839	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000		

[illegible]

[illegible]

[illegible]

##	1021	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1022	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1023	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1024	8	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000
##	1025	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1026	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1027	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1028	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1029	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1030	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1031	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1032	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1033	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1034	9	0.0000000	0.1428571	0.0000000	0.0000000	0.1428571	0.0000000
##	1035	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1036	2	0.0000000	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000
##	1037	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1038	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1039	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1040	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1041	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.7142857
##	1042	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1043	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1044	3	0.0000000	0.0000000	0.1428571	0.7142857	0.0000000	0.0000000
##	1045	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1046	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1047	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1048	9	0.0000000	0.1428571	0.0000000	0.1428571	0.1428571	0.0000000
##	1049	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1050	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1051	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1052	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1053	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1054	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429
##	1055	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1056	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1057	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1058	0	1.0000000	0.0000000	0.000000			

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##	1129	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1130	9	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000
##	1131	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1132	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1133	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1134	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1135	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1136	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1137	2	0.0000000	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000
##	1138	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1139	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1140	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1141	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1142	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1143	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1144	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1145	2	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
##	1146	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1147	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	1148	1	0.1428571	0.4285714	0.0000000	0.0000000	0.0000000	0.0000000
##	1149	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1150	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1151	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1152	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1153	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1154	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1155	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1156	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1157	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1158	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1159	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1160	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1161	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1162	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1163	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1164	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1165	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1166	0	1.0000000	0.0000000	0.000000			

## 1183	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1184	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 1185	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 1186	9	0.0000000	0.0000000	0.0000000	0.2857143	0.0000000	0.0000000	0.0000000
## 1187	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 1188	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1189	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1190	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 1191	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
## 1192	8	0.0000000	0.0000000	0.2857143	0.0000000	0.0000000	0.0000000	0.0000000
## 1193	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1194	8	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000	0.0000000	0.0000000
## 1195	6	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571	0.2857143	0.5714286
## 1196	3	0.0000000	0.0000000	0.1428571	0.7142857	0.0000000	0.0000000	0.0000000
## 1197	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 1198	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1199	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.5714286	0.4285714
## 1200	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1201	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
## 1202	9	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1203	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
## 1204	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1205	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1206	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1207	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1208	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1209	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 1210	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1211	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1212	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 1213	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
## 1214	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
## 1215	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
## 1216	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
## 1217	3	0.0000000	0.0000000					

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##	1291	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1292	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1293	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1294	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1295	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1296	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1297	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1298	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1299	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1300	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1301	2	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
##	1302	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1303	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1304	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1305	9	0.0000000	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000
##	1306	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1307	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1308	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000
##	1309	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1310	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1311	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000
##	1312	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1313	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1314	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1315	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1316	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1317	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1318	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000
##	1319	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1320	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1321	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.2857143
##	1322	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1323	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1324	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.4285714
##	1325	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1326	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1327	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1328	4	0.0000000	0.0000000	0.000000			

[illegible]

[illegible]

##	1453	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1454	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1455	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1456	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1457	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1458	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1459	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1460	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1461	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1462	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1463	1	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000	0.0000000
##	1464	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1465	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	1466	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1467	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429
##	1468	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1469	0	0.5714286	0.0000000	0.0000000	0.0000000	0.0000000	0.4285714
##	1470	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1471	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1472	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1473	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1474	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1475	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1476	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1477	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429
##	1478	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1479	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1480	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1481	5	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1482	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1483	5	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1484	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1485	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1486	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1487	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1488	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1489	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1490	7	0.0000000	0.0000000	0.000000			

##	1507	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1508	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1509	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1510	3	0.0000000	0.0000000	0.0000000	0.7142857	0.0000000	0.0000000
##	1511	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1512	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1513	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1514	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1515	1	0.0000000	0.5714286	0.0000000	0.0000000	0.0000000	0.0000000
##	1516	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1517	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1518	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1519	8	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000
##	1520	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.7142857
##	1521	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1522	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1523	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1524	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1525	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1526	9	0.0000000	0.4285714	0.0000000	0.0000000	0.0000000	0.0000000
##	1527	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1528	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1529	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1530	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1531	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1532	1	0.0000000	0.7142857	0.0000000	0.1428571	0.0000000	0.0000000
##	1533	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1534	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1535	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1536	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1537	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1538	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1539	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1540	1	0.0000000	0.8571429	0.0000000	0.1428571	0.0000000	0.0000000
##	1541	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1542	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1543	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1544	2	0.0000000	0.0000000	1.000000			

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##	1615	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1616	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000
##	1617	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1618	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1619	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1620	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1621	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1622	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1623	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1624	2	0.0000000	0.0000000	0.8571429	0.1428571	0.0000000	0.0000000	0.0000000
##	1625	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1626	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1627	1	0.0000000	0.5714286	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1628	5	0.0000000	0.0000000	0.0000000	0.2857143	0.0000000	0.5714286	0.0000000
##	1629	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1630	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1631	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1632	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	1633	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1634	1	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1635	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1636	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1637	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1638	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1639	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1640	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1641	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1642	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1643	3	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000
##	1644	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1645	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1646	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1647	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1648	3	0.0000000</						

##	1669	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1670	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1671	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1672	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1673	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1674	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1675	8	0.0000000	0.1428571	0.0000000	0.1428571	0.0000000	0.0000000
##	1676	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1677	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1678	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1679	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1680	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1681	8	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000
##	1682	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1683	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1684	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1685	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1686	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1687	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1688	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1689	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1690	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1691	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1692	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1693	7	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000	0.0000000
##	1694	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1695	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1696	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1697	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1698	8	0.0000000	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000
##	1699	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1700	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1701	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1702	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1703	4	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1704	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1705	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000
##	1706	6	0.0000000	0.0000000	0.000000			

[illegible]

[illegible]

##	1831	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1832	5	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.8571429	0.0000000
##	1833	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1834	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1835	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1836	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1837	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1838	9	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1839	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1840	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1841	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	1842	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1843	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1844	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1845	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1846	8	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1847	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1848	2	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000	0.0000000
##	1849	1	0.0000000	0.8571429	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1850	3	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000
##	1851	0	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1852	6	0.0000000	0.1428571	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429
##	1853	8	0.0000000	0.0000000	0.0000000	0.1428571	0.0000000	0.2857143	0.2857143
##	1854	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1855	1	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1856	9	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000	0.0000000	0.0000000
##	1857	8	0.0000000	0.2857143	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1858	6	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000
##	1859	7	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1860	4	0.0000000	0.0000000	0.0000000	0.0000000	0.8571429	0.0000000	0.0000000
##	1861	7	0.0000000	0.0000000	0.0000000	0.4285714	0.0000000	0.1428571	0.0000000
##	1862	2	0.0000000	0.0000000	1.0000000	0.0000000	0.0000000	0.0000000	0.0000000
##	1863	5	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	1.0000000	0.0000000
##	1864	0	1.0000000</						

```

## 1885 1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1886 1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1887 1 0.0000000 0.4285714 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1888 7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1889 9 0.0000000 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000
## 1890 7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1891 2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1892 1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1893 6 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000
## 1894 5 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000
## 1895 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1896 0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1897 7 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1898 2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1899 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1900 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1901 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1902 9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1903 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1904 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1905 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1906 0 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1907 1 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1908 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1909 4 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000
## 1910 1 0.0000000 0.5714286 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1911 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1912 9 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000
## 1913 6 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000
## 1914 6 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0000000
##      prob.7   prob.8   prob.9
## 1      0.0000000 0.0000000 0.0000000
## 2      0.0000000 0.0000000 0.0000000
## 3      0.0000000 1.0000000 0.0000000
## 4      0.0000000 0.0000000 0.0000000
## 5      0.0000000 0.0000000 0.7142857
## 6      0.0000000 0.0000000 0.0000000
## 7      0.0000000 0.0000000 0.2857143
## 8      1.0000000 0.0000000 0.0000000
## 9      0.0000000 0.0000000 0.2857143
## 10     1.0000000 0.0000000 0.0000000
## 11     0.0000000 0.0000000 0.0000000
## 12     0.0000000 0.0000000 1.0000000
## 13     0.0000000 0.0000000 0.0000000
## 14     0.0000000 0.0000000 0.0000000
## 15     0.0000000 0.8571429 0.1428571
## 16     1.0000000 0.0000000 0.0000000
## 17     0.0000000 0.0000000 0.0000000
## 18     0.0000000 0.0000000 0.2857143
## 19     0.0000000 0.0000000 0.7142857
## 20     0.0000000 0.0000000 0.0000000
## 21     0.0000000 0.0000000 1.0000000
## 22     0.0000000 0.0000000 1.0000000
## 23     0.0000000 0.7142857 0.1428571

```

## 24	0.0000000	0.0000000	0.0000000
## 25	0.8571429	0.0000000	0.1428571
## 26	0.0000000	0.0000000	0.0000000
## 27	0.0000000	0.0000000	0.2857143
## 28	0.0000000	0.0000000	0.0000000
## 29	0.0000000	0.0000000	0.2857143
## 30	0.0000000	0.0000000	0.0000000
## 31	0.0000000	0.0000000	0.0000000
## 32	0.0000000	0.0000000	0.0000000
## 33	0.0000000	0.0000000	0.0000000
## 34	0.0000000	0.0000000	0.2857143
## 35	0.0000000	0.0000000	0.0000000
## 36	0.0000000	1.0000000	0.0000000
## 37	0.0000000	0.0000000	0.0000000
## 38	1.0000000	0.0000000	0.0000000
## 39	0.0000000	0.0000000	0.0000000
## 40	0.0000000	0.0000000	0.0000000
## 41	0.0000000	0.0000000	0.0000000
## 42	0.0000000	0.0000000	0.0000000
## 43	0.0000000	0.0000000	0.0000000
## 44	0.0000000	0.0000000	0.0000000
## 45	0.0000000	0.0000000	0.0000000
## 46	0.0000000	1.0000000	0.0000000
## 47	0.0000000	0.1428571	0.8571429
## 48	0.0000000	0.0000000	0.0000000
## 49	0.0000000	0.0000000	0.0000000
## 50	0.0000000	0.0000000	0.0000000
## 51	0.0000000	0.0000000	0.0000000
## 52	1.0000000	0.0000000	0.0000000
## 53	0.0000000	0.0000000	0.0000000
## 54	0.0000000	0.0000000	0.0000000
## 55	0.0000000	0.0000000	0.0000000
## 56	0.0000000	0.0000000	1.0000000
## 57	0.0000000	0.0000000	0.0000000
## 58	0.0000000	0.0000000	0.0000000
## 59	0.0000000	0.0000000	0.0000000
## 60	0.0000000	0.0000000	0.0000000
## 61	1.0000000	0.0000000	0.0000000
## 62	1.0000000	0.0000000	0.0000000
## 63	0.0000000	0.0000000	0.0000000
## 64	0.0000000	0.0000000	0.0000000
## 65	0.0000000	1.0000000	0.0000000
## 66	0.0000000	0.0000000	0.0000000
## 67	0.0000000	0.0000000	0.0000000
## 68	0.0000000	0.0000000	0.0000000
## 69	0.0000000	0.0000000	0.0000000
## 70	0.0000000	0.0000000	0.0000000
## 71	0.0000000	1.0000000	0.0000000
## 72	0.0000000	0.1428571	0.8571429
## 73	0.0000000	0.0000000	0.0000000
## 74	0.0000000	0.0000000	0.0000000
## 75	0.0000000	0.0000000	0.0000000
## 76	0.0000000	0.0000000	0.0000000
## 77	0.0000000	0.0000000	0.0000000

## 78	0.0000000	0.0000000	0.0000000
## 79	1.0000000	0.0000000	0.0000000
## 80	0.0000000	0.0000000	0.0000000
## 81	0.0000000	0.0000000	0.0000000
## 82	0.0000000	0.0000000	0.0000000
## 83	0.0000000	0.0000000	0.0000000
## 84	0.0000000	0.0000000	0.0000000
## 85	0.0000000	1.0000000	0.0000000
## 86	0.0000000	0.0000000	1.0000000
## 87	0.0000000	0.0000000	0.0000000
## 88	0.0000000	0.7142857	0.0000000
## 89	0.0000000	0.0000000	0.0000000
## 90	0.0000000	0.0000000	0.0000000
## 91	0.0000000	0.0000000	0.0000000
## 92	0.0000000	1.0000000	0.0000000
## 93	0.0000000	0.0000000	0.0000000
## 94	0.0000000	0.0000000	0.0000000
## 95	0.0000000	0.0000000	0.0000000
## 96	0.0000000	0.0000000	0.7142857
## 97	0.0000000	0.0000000	0.0000000
## 98	0.0000000	0.0000000	0.0000000
## 99	0.0000000	0.0000000	1.0000000
## 100	0.0000000	0.0000000	0.0000000
## 101	0.0000000	0.0000000	0.0000000
## 102	0.0000000	0.0000000	0.1428571
## 103	0.0000000	0.0000000	0.0000000
## 104	1.0000000	0.0000000	0.0000000
## 105	0.0000000	0.0000000	0.0000000
## 106	0.0000000	0.0000000	0.0000000
## 107	0.0000000	0.0000000	0.0000000
## 108	0.0000000	0.0000000	0.0000000
## 109	0.0000000	0.0000000	0.0000000
## 110	0.0000000	0.0000000	0.0000000
## 111	1.0000000	0.0000000	0.0000000
## 112	0.0000000	0.0000000	0.5714286
## 113	0.0000000	0.0000000	0.0000000
## 114	0.0000000	0.0000000	0.0000000
## 115	0.0000000	0.0000000	0.0000000
## 116	0.0000000	0.0000000	0.0000000
## 117	0.0000000	0.0000000	0.0000000
## 118	0.0000000	0.0000000	0.0000000
## 119	0.0000000	0.0000000	0.2857143
## 120	0.0000000	0.0000000	0.0000000
## 121	0.0000000	0.0000000	0.0000000
## 122	1.0000000	0.0000000	0.0000000
## 123	0.0000000	0.0000000	0.0000000
## 124	0.0000000	0.0000000	0.0000000
## 125	0.0000000	1.0000000	0.0000000
## 126	0.0000000	0.0000000	0.0000000
## 127	0.0000000	1.0000000	0.0000000
## 128	0.0000000	1.0000000	0.0000000
## 129	1.0000000	0.0000000	0.0000000
## 130	0.0000000	0.0000000	0.0000000
## 131	0.0000000	0.0000000	0.7142857


```

## 132 0.0000000 0.0000000 0.0000000
## 133 0.0000000 0.0000000 0.0000000
## 134 0.0000000 1.0000000 0.0000000
## 135 0.0000000 0.0000000 0.0000000
## 136 0.0000000 0.0000000 0.0000000
## 137 0.4285714 0.0000000 0.1428571
## 138 0.0000000 0.0000000 0.0000000
## 139 0.0000000 0.0000000 0.0000000
## 140 0.0000000 0.0000000 0.0000000
## 141 0.0000000 0.0000000 0.0000000
## 142 0.0000000 0.0000000 0.8571429
## 143 1.0000000 0.0000000 0.0000000
## 144 0.0000000 0.8571429 0.0000000
## 145 0.0000000 0.0000000 0.8571429
## 146 0.0000000 0.0000000 0.0000000
## 147 0.0000000 1.0000000 0.0000000
## 148 0.0000000 0.7142857 0.0000000
## 149 0.0000000 1.0000000 0.0000000
## 150 0.0000000 0.0000000 0.0000000
## 151 0.0000000 0.0000000 0.0000000
## 152 0.0000000 0.0000000 0.0000000
## 153 0.0000000 0.0000000 0.0000000
## 154 0.0000000 0.0000000 0.0000000
## 155 0.0000000 0.0000000 0.0000000
## 156 1.0000000 0.0000000 0.0000000
## 157 0.0000000 0.0000000 0.0000000
## 158 0.0000000 0.0000000 0.0000000
## 159 0.0000000 0.0000000 0.0000000
## 160 0.0000000 0.0000000 1.0000000
## 161 0.0000000 0.0000000 0.0000000
## 162 0.0000000 0.0000000 0.0000000
## 163 1.0000000 0.0000000 0.0000000
## 164 0.0000000 0.0000000 0.0000000
## 165 0.0000000 0.0000000 0.0000000
## 166 0.0000000 0.0000000 0.0000000
## 167 0.0000000 0.0000000 0.0000000
## 168 0.0000000 0.0000000 0.0000000
## 169 0.0000000 0.8571429 0.0000000
## 170 0.0000000 0.0000000 0.0000000
## 171 0.0000000 0.0000000 0.0000000
## 172 0.0000000 0.0000000 0.0000000
## 173 0.0000000 0.0000000 0.7142857
## 174 0.0000000 0.0000000 0.0000000
## 175 0.0000000 0.0000000 0.0000000
## 176 0.0000000 0.0000000 0.0000000
## 177 0.0000000 1.0000000 0.0000000
## 178 0.0000000 0.0000000 0.8571429
## 179 0.0000000 0.0000000 0.0000000
## 180 0.0000000 0.0000000 0.0000000
## 181 0.0000000 0.0000000 0.0000000
## 182 0.0000000 0.0000000 0.0000000
## 183 0.0000000 0.0000000 0.0000000
## 184 1.0000000 0.0000000 0.0000000
## 185 0.8571429 0.0000000 0.1428571

```

## 186	0.0000000	0.0000000	0.0000000
## 187	0.0000000	0.0000000	0.0000000
## 188	0.0000000	0.0000000	0.0000000
## 189	1.0000000	0.0000000	0.0000000
## 190	0.0000000	0.0000000	0.2857143
## 191	0.0000000	0.0000000	0.7142857
## 192	0.0000000	0.0000000	0.0000000
## 193	0.0000000	0.0000000	1.0000000
## 194	0.0000000	0.0000000	1.0000000
## 195	0.0000000	0.0000000	0.0000000
## 196	0.0000000	1.0000000	0.0000000
## 197	0.0000000	0.0000000	0.0000000
## 198	0.0000000	0.0000000	0.0000000
## 199	0.0000000	0.0000000	0.0000000
## 200	0.0000000	0.0000000	0.0000000
## 201	0.0000000	0.0000000	0.0000000
## 202	0.0000000	0.0000000	1.0000000
## 203	0.0000000	0.0000000	0.0000000
## 204	0.0000000	0.0000000	0.0000000
## 205	0.0000000	0.0000000	0.0000000
## 206	0.0000000	0.0000000	0.0000000
## 207	0.0000000	0.0000000	0.0000000
## 208	0.0000000	0.0000000	0.0000000
## 209	0.0000000	0.0000000	0.0000000
## 210	0.0000000	0.0000000	0.0000000
## 211	0.0000000	0.0000000	0.0000000
## 212	1.0000000	0.0000000	0.0000000
## 213	0.0000000	0.0000000	0.0000000
## 214	0.0000000	1.0000000	0.0000000
## 215	0.0000000	0.8571429	0.0000000
## 216	0.0000000	1.0000000	0.0000000
## 217	0.0000000	1.0000000	0.0000000
## 218	0.0000000	0.0000000	0.0000000
## 219	0.0000000	0.0000000	0.0000000
## 220	0.0000000	0.0000000	0.0000000
## 221	0.0000000	0.0000000	0.0000000
## 222	0.0000000	0.0000000	0.0000000
## 223	0.0000000	0.0000000	0.0000000
## 224	0.0000000	0.0000000	0.0000000
## 225	0.0000000	0.0000000	0.0000000
## 226	0.0000000	0.0000000	0.0000000
## 227	0.0000000	0.0000000	0.8571429
## 228	0.0000000	0.0000000	0.0000000
## 229	0.0000000	0.0000000	0.0000000
## 230	0.0000000	0.0000000	1.0000000
## 231	0.0000000	0.0000000	1.0000000
## 232	0.0000000	0.0000000	1.0000000
## 233	1.0000000	0.0000000	0.0000000
## 234	1.0000000	0.0000000	0.0000000
## 235	0.0000000	0.0000000	0.0000000
## 236	0.0000000	0.0000000	0.0000000
## 237	0.0000000	0.0000000	0.0000000
## 238	0.0000000	0.0000000	0.0000000
## 239	0.0000000	0.0000000	0.0000000

## 240	0.0000000	0.0000000	0.0000000
## 241	0.0000000	0.0000000	1.0000000
## 242	0.0000000	0.0000000	0.0000000
## 243	0.0000000	0.0000000	0.0000000
## 244	0.0000000	0.0000000	0.0000000
## 245	0.0000000	0.0000000	0.0000000
## 246	0.0000000	0.0000000	0.0000000
## 247	0.0000000	0.0000000	0.0000000
## 248	0.0000000	0.0000000	0.0000000
## 249	0.0000000	0.0000000	0.0000000
## 250	0.0000000	0.0000000	0.0000000
## 251	1.0000000	0.0000000	0.0000000
## 252	0.0000000	0.0000000	0.0000000
## 253	0.0000000	1.0000000	0.0000000
## 254	0.0000000	0.0000000	0.0000000
## 255	0.0000000	0.0000000	0.0000000
## 256	0.0000000	0.0000000	0.0000000
## 257	0.0000000	0.0000000	0.0000000
## 258	0.0000000	1.0000000	0.0000000
## 259	0.0000000	0.0000000	1.0000000
## 260	1.0000000	0.0000000	0.0000000
## 261	1.0000000	0.0000000	0.0000000
## 262	0.0000000	0.0000000	0.0000000
## 263	0.0000000	0.0000000	0.0000000
## 264	0.0000000	0.0000000	0.0000000
## 265	0.0000000	0.0000000	0.0000000
## 266	0.0000000	0.0000000	0.0000000
## 267	0.0000000	0.0000000	0.0000000
## 268	0.0000000	0.0000000	0.0000000
## 269	0.0000000	0.0000000	0.0000000
## 270	0.0000000	0.0000000	0.0000000
## 271	0.0000000	0.0000000	0.0000000
## 272	0.0000000	0.0000000	0.0000000
## 273	0.0000000	0.0000000	0.0000000
## 274	0.0000000	0.0000000	1.0000000
## 275	0.0000000	0.0000000	0.4285714
## 276	0.0000000	0.0000000	0.0000000
## 277	0.0000000	0.7142857	0.1428571
## 278	0.0000000	0.0000000	0.0000000
## 279	1.0000000	0.0000000	0.0000000
## 280	0.0000000	0.0000000	0.0000000
## 281	0.0000000	1.0000000	0.0000000
## 282	0.0000000	0.0000000	0.0000000
## 283	1.0000000	0.0000000	0.0000000
## 284	0.0000000	0.0000000	0.0000000
## 285	0.0000000	0.0000000	0.0000000
## 286	0.0000000	0.0000000	0.0000000
## 287	0.0000000	0.0000000	0.0000000
## 288	0.0000000	0.0000000	0.0000000
## 289	0.0000000	0.0000000	0.0000000
## 290	0.0000000	0.0000000	0.0000000
## 291	0.0000000	0.0000000	0.0000000
## 292	0.0000000	0.0000000	0.0000000
## 293	0.0000000	0.0000000	0.8571429

## 294	0.0000000	0.0000000	0.0000000
## 295	0.0000000	0.0000000	0.0000000
## 296	0.0000000	0.0000000	0.0000000
## 297	0.0000000	0.0000000	0.0000000
## 298	0.0000000	0.4285714	0.4285714
## 299	0.0000000	0.0000000	0.0000000
## 300	0.0000000	0.0000000	0.0000000
## 301	0.0000000	0.0000000	0.0000000
## 302	0.0000000	0.0000000	0.0000000
## 303	0.0000000	0.0000000	0.0000000
## 304	0.0000000	0.0000000	0.0000000
## 305	0.0000000	0.0000000	0.0000000
## 306	0.0000000	1.0000000	0.0000000
## 307	0.0000000	0.0000000	0.0000000
## 308	0.0000000	0.0000000	0.0000000
## 309	1.0000000	0.0000000	0.0000000
## 310	0.0000000	0.0000000	0.0000000
## 311	0.0000000	0.0000000	0.0000000
## 312	0.0000000	0.0000000	1.0000000
## 313	0.0000000	0.0000000	0.0000000
## 314	0.0000000	0.0000000	0.0000000
## 315	1.0000000	0.0000000	0.0000000
## 316	0.0000000	0.0000000	0.0000000
## 317	0.0000000	0.0000000	1.0000000
## 318	0.0000000	0.8571429	0.0000000
## 319	0.0000000	0.0000000	0.0000000
## 320	0.0000000	0.0000000	0.0000000
## 321	0.0000000	0.0000000	0.0000000
## 322	0.0000000	0.0000000	0.0000000
## 323	0.0000000	0.0000000	0.0000000
## 324	0.0000000	1.0000000	0.0000000
## 325	0.0000000	0.0000000	0.0000000
## 326	0.0000000	0.0000000	0.0000000
## 327	0.0000000	0.0000000	0.0000000
## 328	0.0000000	0.0000000	0.0000000
## 329	0.0000000	0.0000000	0.0000000
## 330	0.0000000	0.0000000	0.0000000
## 331	0.0000000	0.0000000	0.8571429
## 332	0.0000000	0.7142857	0.1428571
## 333	0.0000000	0.0000000	1.0000000
## 334	0.0000000	0.0000000	0.0000000
## 335	1.0000000	0.0000000	0.0000000
## 336	0.0000000	0.0000000	0.0000000
## 337	0.0000000	0.0000000	0.0000000
## 338	0.0000000	0.0000000	0.0000000
## 339	0.0000000	0.0000000	0.0000000
## 340	0.0000000	0.0000000	0.0000000
## 341	0.0000000	0.0000000	0.0000000
## 342	1.0000000	0.0000000	0.0000000
## 343	0.0000000	0.0000000	0.0000000
## 344	0.0000000	0.0000000	0.0000000
## 345	0.0000000	0.0000000	0.0000000
## 346	0.0000000	0.0000000	0.0000000
## 347	0.0000000	0.0000000	0.0000000

## 348	0.0000000	1.0000000	0.0000000
## 349	0.0000000	0.0000000	1.0000000
## 350	0.0000000	0.0000000	0.0000000
## 351	0.0000000	0.0000000	0.0000000
## 352	1.0000000	0.0000000	0.0000000
## 353	0.0000000	0.0000000	0.0000000
## 354	0.0000000	0.0000000	0.0000000
## 355	0.0000000	0.0000000	0.0000000
## 356	0.0000000	0.0000000	0.0000000
## 357	0.0000000	0.0000000	0.0000000
## 358	0.0000000	0.0000000	0.0000000
## 359	1.0000000	0.0000000	0.0000000
## 360	0.0000000	0.0000000	0.0000000
## 361	0.0000000	0.0000000	0.0000000
## 362	0.0000000	0.0000000	0.0000000
## 363	0.0000000	0.0000000	0.0000000
## 364	0.0000000	0.0000000	0.0000000
## 365	0.0000000	0.0000000	0.0000000
## 366	0.0000000	0.0000000	0.0000000
## 367	0.0000000	0.0000000	0.0000000
## 368	0.0000000	0.0000000	0.0000000
## 369	0.0000000	0.0000000	1.0000000
## 370	0.0000000	0.0000000	0.0000000
## 371	0.0000000	0.0000000	0.0000000
## 372	0.0000000	0.0000000	0.0000000
## 373	1.0000000	0.0000000	0.0000000
## 374	0.0000000	1.0000000	0.0000000
## 375	0.0000000	0.0000000	0.0000000
## 376	0.0000000	0.0000000	0.0000000
## 377	0.0000000	0.0000000	0.0000000
## 378	0.0000000	0.0000000	0.1428571
## 379	0.0000000	0.0000000	0.0000000
## 380	0.0000000	0.0000000	0.0000000
## 381	0.0000000	0.0000000	0.0000000
## 382	0.0000000	0.0000000	0.0000000
## 383	0.0000000	0.0000000	0.0000000
## 384	0.0000000	0.0000000	0.0000000
## 385	0.0000000	0.0000000	0.0000000
## 386	0.0000000	0.0000000	0.0000000
## 387	0.0000000	1.0000000	0.0000000
## 388	1.0000000	0.0000000	0.0000000
## 389	0.0000000	1.0000000	0.0000000
## 390	0.0000000	0.0000000	0.0000000
## 391	0.0000000	0.0000000	0.0000000
## 392	0.0000000	0.0000000	0.0000000
## 393	0.0000000	1.0000000	0.0000000
## 394	0.0000000	0.0000000	0.0000000
## 395	0.0000000	0.0000000	0.0000000
## 396	0.0000000	1.0000000	0.0000000
## 397	0.0000000	0.0000000	0.0000000
## 398	0.0000000	0.0000000	0.0000000
## 399	0.0000000	0.0000000	0.0000000
## 400	0.0000000	1.0000000	0.0000000
## 401	0.0000000	0.0000000	0.7142857

## 402	0.0000000	0.0000000	0.0000000
## 403	0.0000000	1.0000000	0.0000000
## 404	0.0000000	0.0000000	0.0000000
## 405	1.0000000	0.0000000	0.0000000
## 406	0.0000000	0.0000000	0.0000000
## 407	0.0000000	0.0000000	0.1428571
## 408	0.0000000	0.0000000	0.0000000
## 409	0.0000000	1.0000000	0.0000000
## 410	0.0000000	0.0000000	1.0000000
## 411	0.0000000	0.0000000	0.0000000
## 412	0.0000000	0.0000000	0.0000000
## 413	0.0000000	0.2857143	0.0000000
## 414	0.0000000	0.0000000	0.8571429
## 415	0.0000000	0.0000000	0.0000000
## 416	0.0000000	0.0000000	1.0000000
## 417	0.0000000	0.0000000	0.0000000
## 418	0.0000000	0.0000000	0.0000000
## 419	0.0000000	0.0000000	0.0000000
## 420	0.0000000	0.0000000	0.0000000
## 421	0.0000000	0.1428571	0.0000000
## 422	1.0000000	0.0000000	0.0000000
## 423	0.0000000	0.0000000	0.0000000
## 424	0.0000000	0.0000000	0.8571429
## 425	0.0000000	0.0000000	0.0000000
## 426	0.0000000	0.0000000	0.0000000
## 427	0.0000000	0.0000000	0.0000000
## 428	0.0000000	0.0000000	0.0000000
## 429	0.7142857	0.0000000	0.2857143
## 430	0.0000000	0.0000000	0.0000000
## 431	0.0000000	0.0000000	0.0000000
## 432	0.0000000	0.0000000	0.0000000
## 433	0.0000000	0.7142857	0.0000000
## 434	1.0000000	0.0000000	0.0000000
## 435	0.0000000	0.0000000	0.0000000
## 436	0.0000000	0.0000000	1.0000000
## 437	0.0000000	0.0000000	0.0000000
## 438	0.0000000	0.0000000	0.8571429
## 439	1.0000000	0.0000000	0.0000000
## 440	0.0000000	0.0000000	1.0000000
## 441	0.0000000	0.0000000	0.0000000
## 442	0.0000000	0.0000000	0.0000000
## 443	0.0000000	0.0000000	0.0000000
## 444	0.0000000	0.0000000	0.7142857
## 445	0.0000000	0.0000000	0.0000000
## 446	0.0000000	0.0000000	0.0000000
## 447	0.0000000	0.0000000	0.2857143
## 448	0.0000000	1.0000000	0.0000000
## 449	0.0000000	0.0000000	0.0000000
## 450	0.0000000	0.0000000	0.0000000
## 451	0.0000000	0.0000000	0.0000000
## 452	0.0000000	0.0000000	0.0000000
## 453	0.0000000	0.1428571	0.0000000
## 454	0.0000000	0.0000000	0.0000000
## 455	1.0000000	0.0000000	0.0000000

## 456	0.0000000	0.0000000	0.1428571
## 457	0.0000000	0.8571429	0.0000000
## 458	0.0000000	0.0000000	0.0000000
## 459	0.0000000	0.0000000	0.0000000
## 460	0.0000000	1.0000000	0.0000000
## 461	0.0000000	0.0000000	1.0000000
## 462	0.0000000	0.0000000	0.0000000
## 463	0.0000000	0.0000000	0.0000000
## 464	0.0000000	0.0000000	0.0000000
## 465	0.0000000	0.0000000	0.7142857
## 466	0.0000000	0.0000000	0.0000000
## 467	0.0000000	0.0000000	0.0000000
## 468	0.0000000	0.0000000	0.8571429
## 469	0.0000000	0.0000000	0.1428571
## 470	0.0000000	0.0000000	0.0000000
## 471	0.0000000	0.0000000	0.0000000
## 472	1.0000000	0.0000000	0.0000000
## 473	0.0000000	0.0000000	0.0000000
## 474	0.0000000	0.0000000	0.0000000
## 475	0.0000000	1.0000000	0.0000000
## 476	0.0000000	0.0000000	0.0000000
## 477	0.0000000	0.0000000	0.0000000
## 478	0.0000000	0.0000000	0.0000000
## 479	0.0000000	0.0000000	0.0000000
## 480	0.0000000	0.0000000	0.0000000
## 481	0.0000000	0.0000000	0.0000000
## 482	1.0000000	0.0000000	0.0000000
## 483	0.0000000	0.0000000	0.0000000
## 484	0.0000000	0.0000000	0.8571429
## 485	0.0000000	0.0000000	0.0000000
## 486	0.0000000	0.0000000	0.0000000
## 487	0.0000000	0.0000000	0.0000000
## 488	0.0000000	0.1428571	0.0000000
## 489	1.0000000	0.0000000	0.0000000
## 490	0.0000000	1.0000000	0.0000000
## 491	0.0000000	0.0000000	0.4285714
## 492	0.0000000	0.0000000	0.0000000
## 493	0.0000000	0.0000000	0.0000000
## 494	0.0000000	0.0000000	0.0000000
## 495	0.0000000	0.0000000	0.8571429
## 496	0.0000000	0.0000000	1.0000000
## 497	1.0000000	0.0000000	0.0000000
## 498	0.0000000	0.0000000	0.0000000
## 499	0.0000000	0.0000000	0.8571429
## 500	0.0000000	1.0000000	0.0000000
## 501	0.0000000	0.0000000	0.0000000
## 502	0.0000000	0.0000000	0.0000000
## 503	0.0000000	0.0000000	0.0000000
## 504	0.0000000	0.0000000	0.0000000
## 505	0.0000000	0.0000000	1.0000000
## 506	0.0000000	0.0000000	0.0000000
## 507	0.0000000	1.0000000	0.0000000
## 508	0.0000000	0.0000000	0.0000000
## 509	0.0000000	0.0000000	0.8571429

```

## 510 0.0000000 0.0000000 0.0000000
## 511 0.0000000 1.0000000 0.0000000
## 512 0.0000000 0.0000000 0.0000000
## 513 0.0000000 0.0000000 0.0000000
## 514 0.0000000 0.0000000 0.0000000
## 515 0.0000000 1.0000000 0.0000000
## 516 0.0000000 0.0000000 0.0000000
## 517 0.0000000 0.0000000 0.0000000
## 518 0.0000000 0.0000000 0.0000000
## 519 0.0000000 0.0000000 0.0000000
## 520 0.0000000 0.0000000 0.0000000
## 521 0.0000000 0.0000000 0.0000000
## 522 0.0000000 0.0000000 0.7142857
## 523 1.0000000 0.0000000 0.0000000
## 524 0.0000000 0.0000000 1.0000000
## 525 0.0000000 0.0000000 0.0000000
## 526 0.0000000 0.0000000 0.0000000
## 527 0.0000000 0.0000000 0.0000000
## 528 0.0000000 0.0000000 0.0000000
## 529 0.0000000 0.0000000 1.0000000
## 530 0.0000000 0.0000000 0.0000000
## 531 0.0000000 0.0000000 0.0000000
## 532 0.0000000 0.0000000 0.0000000
## 533 0.0000000 0.0000000 0.0000000
## 534 0.0000000 0.0000000 0.0000000
## 535 0.0000000 0.0000000 0.0000000
## 536 0.0000000 0.0000000 0.0000000
## 537 0.0000000 0.0000000 0.0000000
## 538 0.0000000 0.0000000 0.0000000
## 539 0.0000000 0.0000000 0.0000000
## 540 0.0000000 0.0000000 1.0000000
## 541 1.0000000 0.0000000 0.0000000
## 542 0.0000000 0.0000000 0.0000000
## 543 0.0000000 0.0000000 0.0000000
## 544 0.4285714 0.2857143 0.0000000
## 545 1.0000000 0.0000000 0.0000000
## 546 0.0000000 0.0000000 0.0000000
## 547 0.4285714 0.2857143 0.0000000
## 548 0.0000000 1.0000000 0.0000000
## 549 0.0000000 0.0000000 0.0000000
## 550 1.0000000 0.0000000 0.0000000
## 551 0.0000000 0.0000000 0.0000000
## 552 0.0000000 0.0000000 1.0000000
## 553 0.0000000 0.0000000 0.5714286
## 554 0.0000000 0.0000000 1.0000000
## 555 0.0000000 0.0000000 0.0000000
## 556 0.0000000 0.0000000 0.0000000
## 557 0.0000000 0.0000000 1.0000000
## 558 0.0000000 0.0000000 0.0000000
## 559 0.0000000 1.0000000 0.0000000
## 560 0.0000000 0.0000000 0.0000000
## 561 0.0000000 0.0000000 0.0000000
## 562 0.0000000 0.0000000 0.0000000
## 563 0.0000000 1.0000000 0.0000000

```


## 564	0.0000000	0.0000000	0.0000000
## 565	0.0000000	0.0000000	0.0000000
## 566	0.0000000	0.0000000	0.0000000
## 567	0.0000000	1.0000000	0.0000000
## 568	0.7142857	0.0000000	0.2857143
## 569	0.0000000	0.0000000	0.0000000
## 570	0.0000000	0.0000000	0.0000000
## 571	0.0000000	0.0000000	0.0000000
## 572	0.0000000	0.0000000	1.0000000
## 573	0.0000000	0.0000000	0.0000000
## 574	0.0000000	0.0000000	0.0000000
## 575	1.0000000	0.0000000	0.0000000
## 576	0.0000000	0.0000000	0.0000000
## 577	0.0000000	0.7142857	0.0000000
## 578	0.0000000	0.0000000	0.0000000
## 579	0.0000000	0.0000000	0.4285714
## 580	0.0000000	0.0000000	0.0000000
## 581	0.0000000	0.0000000	0.0000000
## 582	0.0000000	0.0000000	0.0000000
## 583	0.0000000	0.0000000	0.0000000
## 584	0.0000000	0.0000000	0.0000000
## 585	1.0000000	0.0000000	0.0000000
## 586	0.0000000	0.0000000	0.0000000
## 587	0.0000000	0.0000000	0.0000000
## 588	0.0000000	0.0000000	0.0000000
## 589	0.0000000	0.0000000	0.2857143
## 590	0.0000000	0.1428571	0.0000000
## 591	0.0000000	0.0000000	0.0000000
## 592	0.0000000	0.0000000	0.0000000
## 593	0.0000000	0.0000000	0.0000000
## 594	0.0000000	0.0000000	0.0000000
## 595	0.0000000	0.0000000	0.5714286
## 596	0.0000000	0.0000000	0.0000000
## 597	1.0000000	0.0000000	0.0000000
## 598	0.0000000	0.0000000	0.0000000
## 599	0.0000000	1.0000000	0.0000000
## 600	0.0000000	0.0000000	0.0000000
## 601	0.0000000	0.0000000	0.0000000
## 602	0.0000000	0.0000000	0.8571429
## 603	0.0000000	0.0000000	0.0000000
## 604	0.0000000	0.0000000	0.8571429
## 605	0.0000000	0.0000000	1.0000000
## 606	1.0000000	0.0000000	0.0000000
## 607	0.0000000	0.0000000	0.0000000
## 608	0.0000000	0.0000000	0.0000000
## 609	0.0000000	0.0000000	0.4285714
## 610	0.0000000	0.0000000	0.0000000
## 611	0.0000000	0.0000000	0.0000000
## 612	0.0000000	0.0000000	0.0000000
## 613	0.0000000	0.0000000	0.0000000
## 614	1.0000000	0.0000000	0.0000000
## 615	0.0000000	0.0000000	0.0000000
## 616	0.0000000	0.0000000	0.0000000
## 617	0.0000000	0.0000000	0.0000000

```

## 618 0.0000000 0.0000000 0.0000000
## 619 0.0000000 0.0000000 0.0000000
## 620 1.0000000 0.0000000 0.0000000
## 621 0.0000000 0.0000000 0.0000000
## 622 0.0000000 0.0000000 0.0000000
## 623 0.0000000 0.0000000 0.0000000
## 624 1.0000000 0.0000000 0.0000000
## 625 0.0000000 0.0000000 0.0000000
## 626 0.0000000 0.1428571 0.8571429
## 627 0.0000000 0.0000000 0.0000000
## 628 0.0000000 0.0000000 0.0000000
## 629 0.0000000 0.0000000 0.0000000
## 630 0.0000000 0.0000000 0.0000000
## 631 0.0000000 0.0000000 0.1428571
## 632 0.0000000 0.8571429 0.0000000
## 633 0.0000000 0.0000000 0.0000000
## 634 0.0000000 0.0000000 0.0000000
## 635 0.0000000 0.0000000 0.0000000
## 636 0.0000000 0.0000000 0.0000000
## 637 1.0000000 0.0000000 0.0000000
## 638 0.0000000 0.0000000 0.0000000
## 639 1.0000000 0.0000000 0.0000000
## 640 0.0000000 0.1428571 0.0000000
## 641 0.0000000 0.0000000 0.0000000
## 642 0.1428571 0.0000000 0.8571429
## 643 0.0000000 0.0000000 0.0000000
## 644 0.0000000 0.0000000 0.0000000
## 645 0.0000000 0.1428571 0.0000000
## 646 0.0000000 0.0000000 0.0000000
## 647 1.0000000 0.0000000 0.0000000
## 648 0.0000000 0.0000000 0.0000000
## 649 0.0000000 0.0000000 0.0000000
## 650 0.0000000 0.0000000 1.0000000
## 651 0.0000000 0.0000000 0.0000000
## 652 0.0000000 0.0000000 0.0000000
## 653 0.0000000 0.0000000 0.0000000
## 654 0.0000000 0.0000000 0.0000000
## 655 0.0000000 0.0000000 0.1428571
## 656 0.0000000 0.2857143 0.0000000
## 657 0.0000000 0.0000000 0.0000000
## 658 1.0000000 0.0000000 0.0000000
## 659 0.0000000 0.0000000 0.0000000
## 660 0.0000000 0.0000000 0.0000000
## 661 0.0000000 0.0000000 0.0000000
## 662 0.0000000 1.0000000 0.0000000
## 663 0.0000000 0.0000000 0.0000000
## 664 0.0000000 0.0000000 0.0000000
## 665 0.0000000 0.8571429 0.0000000
## 666 0.1428571 0.0000000 0.0000000
## 667 0.0000000 0.0000000 0.0000000
## 668 0.0000000 0.0000000 0.1428571
## 669 0.0000000 0.0000000 1.0000000
## 670 0.0000000 0.0000000 0.0000000
## 671 0.0000000 0.0000000 0.0000000

```

## 672	0.0000000	0.0000000	0.0000000
## 673	1.0000000	0.0000000	0.0000000
## 674	0.0000000	0.0000000	0.0000000
## 675	1.0000000	0.0000000	0.0000000
## 676	0.0000000	0.0000000	0.0000000
## 677	0.0000000	0.0000000	0.0000000
## 678	1.0000000	0.0000000	0.0000000
## 679	0.0000000	0.0000000	0.0000000
## 680	0.0000000	0.0000000	0.0000000
## 681	1.0000000	0.0000000	0.0000000
## 682	0.0000000	0.0000000	0.0000000
## 683	0.0000000	0.0000000	0.0000000
## 684	0.1428571	0.0000000	0.0000000
## 685	0.0000000	0.0000000	1.0000000
## 686	0.0000000	0.0000000	0.0000000
## 687	0.0000000	0.0000000	0.4285714
## 688	1.0000000	0.0000000	0.0000000
## 689	1.0000000	0.0000000	0.0000000
## 690	0.0000000	0.1428571	0.8571429
## 691	0.0000000	0.0000000	0.0000000
## 692	0.0000000	0.0000000	0.0000000
## 693	1.0000000	0.0000000	0.0000000
## 694	0.0000000	0.0000000	0.0000000
## 695	0.0000000	0.0000000	0.2857143
## 696	0.0000000	0.0000000	0.0000000
## 697	0.0000000	0.0000000	0.0000000
## 698	0.0000000	0.0000000	0.8571429
## 699	0.0000000	0.0000000	0.0000000
## 700	0.0000000	0.0000000	0.0000000
## 701	0.0000000	0.0000000	0.0000000
## 702	0.0000000	0.0000000	0.0000000
## 703	0.0000000	0.0000000	0.0000000
## 704	0.4285714	0.0000000	0.5714286
## 705	0.4285714	0.0000000	0.5714286
## 706	0.0000000	1.0000000	0.0000000
## 707	0.0000000	0.0000000	0.0000000
## 708	0.0000000	0.0000000	0.0000000
## 709	0.0000000	0.8571429	0.0000000
## 710	0.0000000	0.8571429	0.0000000
## 711	0.1428571	0.0000000	0.2857143
## 712	0.0000000	0.0000000	0.0000000
## 713	0.0000000	0.0000000	0.1428571
## 714	1.0000000	0.0000000	0.0000000
## 715	0.0000000	0.0000000	0.0000000
## 716	1.0000000	0.0000000	0.0000000
## 717	0.0000000	0.0000000	0.0000000
## 718	0.0000000	0.0000000	0.0000000
## 719	0.0000000	0.8571429	0.0000000
## 720	0.0000000	0.0000000	1.0000000
## 721	0.0000000	0.0000000	0.0000000
## 722	0.0000000	0.0000000	0.0000000
## 723	1.0000000	0.0000000	0.0000000
## 724	0.0000000	0.0000000	0.0000000
## 725	0.0000000	0.0000000	0.0000000

## 726	0.0000000	0.0000000	0.0000000
## 727	0.0000000	0.0000000	0.0000000
## 728	0.0000000	0.0000000	0.0000000
## 729	0.0000000	0.0000000	0.0000000
## 730	0.1428571	0.0000000	0.8571429
## 731	0.0000000	0.0000000	0.0000000
## 732	0.0000000	0.0000000	0.0000000
## 733	0.0000000	0.0000000	0.0000000
## 734	0.0000000	0.0000000	0.0000000
## 735	0.0000000	0.0000000	0.0000000
## 736	0.0000000	0.0000000	0.0000000
## 737	0.0000000	0.0000000	0.0000000
## 738	1.0000000	0.0000000	0.0000000
## 739	1.0000000	0.0000000	0.0000000
## 740	0.0000000	0.0000000	0.0000000
## 741	0.0000000	0.0000000	0.0000000
## 742	0.0000000	0.0000000	0.0000000
## 743	0.0000000	1.0000000	0.0000000
## 744	0.0000000	0.0000000	0.4285714
## 745	0.0000000	0.0000000	0.0000000
## 746	0.0000000	0.0000000	0.0000000
## 747	0.0000000	1.0000000	0.0000000
## 748	1.0000000	0.0000000	0.0000000
## 749	0.0000000	0.0000000	0.0000000
## 750	0.0000000	1.0000000	0.0000000
## 751	0.0000000	0.0000000	0.0000000
## 752	0.0000000	0.0000000	0.0000000
## 753	0.0000000	0.0000000	0.0000000
## 754	0.0000000	0.0000000	0.0000000
## 755	0.0000000	0.0000000	0.0000000
## 756	0.0000000	1.0000000	0.0000000
## 757	1.0000000	0.0000000	0.0000000
## 758	0.0000000	0.0000000	0.0000000
## 759	0.0000000	1.0000000	0.0000000
## 760	0.0000000	0.0000000	1.0000000
## 761	0.0000000	0.0000000	0.0000000
## 762	0.0000000	0.0000000	0.0000000
## 763	0.0000000	0.0000000	0.0000000
## 764	0.0000000	0.0000000	0.0000000
## 765	0.0000000	0.0000000	0.0000000
## 766	0.0000000	0.0000000	0.0000000
## 767	0.0000000	0.0000000	0.0000000
## 768	0.0000000	0.0000000	0.0000000
## 769	0.0000000	0.0000000	0.0000000
## 770	1.0000000	0.0000000	0.0000000
## 771	0.0000000	0.0000000	0.0000000
## 772	1.0000000	0.0000000	0.0000000
## 773	1.0000000	0.0000000	0.0000000
## 774	0.0000000	0.0000000	1.0000000
## 775	0.0000000	0.0000000	0.8571429
## 776	0.0000000	0.0000000	0.0000000
## 777	0.0000000	1.0000000	0.0000000
## 778	0.0000000	0.0000000	0.0000000
## 779	0.0000000	1.0000000	0.0000000

## 780	0.0000000	0.0000000	0.0000000
## 781	0.0000000	0.0000000	0.0000000
## 782	1.0000000	0.0000000	0.0000000
## 783	0.0000000	0.0000000	0.0000000
## 784	0.0000000	0.0000000	1.0000000
## 785	0.0000000	0.0000000	0.0000000
## 786	0.0000000	0.0000000	0.0000000
## 787	0.0000000	0.0000000	0.0000000
## 788	0.0000000	0.0000000	0.0000000
## 789	0.0000000	0.0000000	1.0000000
## 790	0.0000000	0.0000000	0.0000000
## 791	1.0000000	0.0000000	0.0000000
## 792	0.0000000	0.0000000	0.0000000
## 793	0.0000000	0.8571429	0.1428571
## 794	0.0000000	0.7142857	0.2857143
## 795	0.0000000	0.0000000	0.0000000
## 796	0.0000000	0.0000000	0.0000000
## 797	0.0000000	0.0000000	1.0000000
## 798	0.0000000	0.0000000	0.0000000
## 799	0.0000000	0.0000000	0.0000000
## 800	0.0000000	0.0000000	0.0000000
## 801	0.0000000	0.0000000	0.0000000
## 802	0.0000000	0.0000000	0.0000000
## 803	0.0000000	0.0000000	1.0000000
## 804	0.0000000	0.0000000	0.0000000
## 805	0.0000000	0.0000000	0.0000000
## 806	1.0000000	0.0000000	0.0000000
## 807	0.0000000	0.0000000	0.0000000
## 808	0.0000000	0.0000000	0.0000000
## 809	0.0000000	0.0000000	0.0000000
## 810	0.0000000	0.0000000	0.0000000
## 811	0.0000000	0.0000000	0.0000000
## 812	0.0000000	0.0000000	0.0000000
## 813	0.0000000	0.0000000	1.0000000
## 814	0.0000000	0.0000000	0.0000000
## 815	0.0000000	0.0000000	0.0000000
## 816	0.0000000	0.0000000	0.0000000
## 817	0.0000000	0.0000000	0.0000000
## 818	0.0000000	0.0000000	0.0000000
## 819	0.0000000	0.0000000	0.0000000
## 820	0.0000000	0.0000000	0.1428571
## 821	0.0000000	0.0000000	1.0000000
## 822	0.0000000	0.0000000	0.0000000
## 823	0.0000000	1.0000000	0.0000000
## 824	0.0000000	0.0000000	0.0000000
## 825	0.0000000	0.0000000	1.0000000
## 826	0.0000000	0.0000000	1.0000000
## 827	0.0000000	0.0000000	0.0000000
## 828	0.0000000	0.0000000	0.0000000
## 829	0.0000000	0.7142857	0.0000000
## 830	0.0000000	0.5714286	0.0000000
## 831	0.0000000	0.0000000	0.0000000
## 832	0.0000000	0.0000000	0.0000000
## 833	0.0000000	0.0000000	0.0000000

## 834	1.0000000	0.0000000	0.0000000
## 835	0.0000000	0.0000000	1.0000000
## 836	0.0000000	0.0000000	0.0000000
## 837	0.0000000	0.0000000	1.0000000
## 838	0.0000000	0.0000000	0.0000000
## 839	0.0000000	0.0000000	0.8571429
## 840	0.0000000	0.0000000	0.0000000
## 841	0.0000000	0.0000000	0.0000000
## 842	0.0000000	0.0000000	0.0000000
## 843	0.0000000	0.0000000	0.0000000
## 844	1.0000000	0.0000000	0.0000000
## 845	0.0000000	0.8571429	0.0000000
## 846	0.0000000	0.0000000	0.0000000
## 847	0.0000000	0.0000000	0.0000000
## 848	0.0000000	0.0000000	0.0000000
## 849	0.0000000	0.0000000	0.0000000
## 850	0.0000000	0.0000000	0.0000000
## 851	0.0000000	0.0000000	0.0000000
## 852	0.0000000	0.0000000	0.0000000
## 853	0.0000000	0.5714286	0.0000000
## 854	0.0000000	0.0000000	0.7142857
## 855	0.7142857	0.0000000	0.1428571
## 856	1.0000000	0.0000000	0.0000000
## 857	0.0000000	0.0000000	0.0000000
## 858	0.0000000	0.0000000	0.0000000
## 859	0.0000000	0.0000000	0.0000000
## 860	0.0000000	0.0000000	0.0000000
## 861	0.0000000	0.0000000	0.0000000
## 862	1.0000000	0.0000000	0.0000000
## 863	0.0000000	0.0000000	0.0000000
## 864	0.0000000	0.0000000	1.0000000
## 865	0.0000000	0.0000000	0.0000000
## 866	0.0000000	1.0000000	0.0000000
## 867	0.0000000	0.0000000	0.0000000
## 868	0.0000000	0.0000000	0.0000000
## 869	0.0000000	0.0000000	0.0000000
## 870	0.0000000	0.0000000	0.0000000
## 871	0.0000000	0.0000000	1.0000000
## 872	0.0000000	0.0000000	0.0000000
## 873	0.0000000	0.0000000	0.0000000
## 874	0.0000000	0.0000000	0.0000000
## 875	0.0000000	0.0000000	0.0000000
## 876	0.0000000	0.0000000	0.0000000
## 877	0.0000000	1.0000000	0.0000000
## 878	0.0000000	0.0000000	0.0000000
## 879	0.0000000	0.0000000	0.0000000
## 880	0.0000000	0.0000000	0.0000000
## 881	0.0000000	0.0000000	0.0000000
## 882	0.0000000	0.0000000	0.0000000
## 883	0.0000000	0.0000000	0.0000000
## 884	0.0000000	0.0000000	0.4285714
## 885	0.0000000	0.0000000	0.7142857
## 886	0.0000000	0.0000000	0.0000000
## 887	0.0000000	0.0000000	0.0000000

## 888	0.0000000	0.0000000	0.0000000
## 889	0.0000000	0.0000000	0.0000000
## 890	0.0000000	0.0000000	0.0000000
## 891	0.0000000	1.0000000	0.0000000
## 892	0.0000000	0.0000000	0.0000000
## 893	0.0000000	0.0000000	0.0000000
## 894	0.0000000	0.0000000	0.0000000
## 895	0.0000000	0.0000000	0.0000000
## 896	0.0000000	0.5714286	0.4285714
## 897	1.0000000	0.0000000	0.0000000
## 898	0.0000000	0.0000000	0.2857143
## 899	1.0000000	0.0000000	0.0000000
## 900	0.0000000	0.0000000	0.0000000
## 901	0.1428571	0.0000000	0.1428571
## 902	0.0000000	0.2857143	0.0000000
## 903	0.0000000	1.0000000	0.0000000
## 904	0.0000000	0.0000000	0.0000000
## 905	0.0000000	0.0000000	0.0000000
## 906	1.0000000	0.0000000	0.0000000
## 907	0.0000000	0.0000000	0.0000000
## 908	0.0000000	0.4285714	0.0000000
## 909	0.0000000	0.0000000	0.0000000
## 910	0.0000000	0.0000000	0.0000000
## 911	0.0000000	0.0000000	0.0000000
## 912	0.0000000	0.0000000	0.0000000
## 913	0.0000000	0.0000000	0.0000000
## 914	1.0000000	0.0000000	0.0000000
## 915	0.0000000	0.0000000	0.0000000
## 916	0.0000000	0.0000000	0.0000000
## 917	0.0000000	0.0000000	0.0000000
## 918	0.0000000	0.0000000	0.0000000
## 919	0.0000000	0.0000000	0.0000000
## 920	0.0000000	0.0000000	0.0000000
## 921	0.0000000	0.0000000	0.0000000
## 922	0.2857143	0.0000000	0.7142857
## 923	0.0000000	0.0000000	0.0000000
## 924	0.0000000	0.0000000	0.0000000
## 925	0.0000000	0.0000000	0.0000000
## 926	1.0000000	0.0000000	0.0000000
## 927	0.0000000	0.0000000	0.2857143
## 928	0.0000000	0.0000000	0.0000000
## 929	0.0000000	0.0000000	0.0000000
## 930	0.0000000	0.0000000	0.0000000
## 931	1.0000000	0.0000000	0.0000000
## 932	0.0000000	0.0000000	0.0000000
## 933	0.0000000	0.0000000	0.0000000
## 934	0.0000000	0.0000000	0.0000000
## 935	0.0000000	0.0000000	0.0000000
## 936	0.0000000	0.0000000	0.0000000
## 937	0.0000000	0.0000000	0.0000000
## 938	0.0000000	0.0000000	0.0000000
## 939	1.0000000	0.0000000	0.0000000
## 940	0.0000000	0.0000000	0.0000000
## 941	1.0000000	0.0000000	0.0000000

## 942	0.0000000	0.0000000	0.0000000
## 943	0.0000000	0.0000000	0.0000000
## 944	0.0000000	0.0000000	0.0000000
## 945	1.0000000	0.0000000	0.0000000
## 946	1.0000000	0.0000000	0.0000000
## 947	0.0000000	0.0000000	0.0000000
## 948	0.0000000	0.0000000	0.0000000
## 949	0.0000000	0.0000000	0.0000000
## 950	1.0000000	0.0000000	0.0000000
## 951	0.0000000	0.0000000	0.1428571
## 952	0.0000000	0.0000000	0.0000000
## 953	0.0000000	1.0000000	0.0000000
## 954	0.0000000	0.0000000	0.0000000
## 955	0.0000000	1.0000000	0.0000000
## 956	0.0000000	1.0000000	0.0000000
## 957	0.0000000	0.0000000	0.0000000
## 958	0.0000000	0.0000000	0.1428571
## 959	0.0000000	0.0000000	0.0000000
## 960	0.0000000	0.0000000	0.0000000
## 961	0.0000000	0.0000000	0.0000000
## 962	0.0000000	0.0000000	1.0000000
## 963	0.0000000	0.0000000	0.0000000
## 964	0.0000000	0.0000000	0.0000000
## 965	0.0000000	0.0000000	0.0000000
## 966	1.0000000	0.0000000	0.0000000
## 967	0.0000000	1.0000000	0.0000000
## 968	0.0000000	0.0000000	0.0000000
## 969	0.0000000	0.0000000	0.0000000
## 970	0.0000000	0.0000000	0.0000000
## 971	0.0000000	0.0000000	0.0000000
## 972	0.0000000	0.0000000	0.1428571
## 973	0.0000000	0.0000000	0.0000000
## 974	0.0000000	0.0000000	0.0000000
## 975	0.0000000	1.0000000	0.0000000
## 976	1.0000000	0.0000000	0.0000000
## 977	0.0000000	0.0000000	0.0000000
## 978	0.0000000	0.0000000	0.0000000
## 979	0.0000000	0.0000000	0.0000000
## 980	0.8571429	0.0000000	0.1428571
## 981	1.0000000	0.0000000	0.0000000
## 982	0.0000000	0.0000000	0.2857143
## 983	0.1428571	0.0000000	0.7142857
## 984	0.0000000	0.0000000	0.4285714
## 985	0.8571429	0.0000000	0.1428571
## 986	0.0000000	0.0000000	0.0000000
## 987	0.0000000	0.0000000	0.0000000
## 988	0.0000000	0.0000000	0.0000000
## 989	0.0000000	1.0000000	0.0000000
## 990	0.0000000	0.0000000	0.0000000
## 991	0.0000000	0.0000000	0.0000000
## 992	0.0000000	0.0000000	0.0000000
## 993	0.0000000	0.0000000	1.0000000
## 994	0.0000000	0.0000000	0.0000000
## 995	0.0000000	0.0000000	0.0000000


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## 996 0.4285714 0.0000000 0.5714286
## 997 0.0000000 1.0000000 0.0000000
## 998 0.2857143 0.0000000 0.7142857
## 999 0.0000000 0.0000000 0.0000000
## 1000 1.0000000 0.0000000 0.0000000
## 1001 0.0000000 0.0000000 1.0000000
## 1002 1.0000000 0.0000000 0.0000000
## 1003 0.0000000 0.0000000 0.0000000
## 1004 1.0000000 0.0000000 0.0000000
## 1005 0.0000000 0.0000000 0.0000000
## 1006 0.0000000 0.0000000 0.0000000
## 1007 0.0000000 0.0000000 0.0000000
## 1008 0.0000000 0.0000000 0.0000000
## 1009 0.0000000 0.0000000 1.0000000
## 1010 0.0000000 0.0000000 0.0000000
## 1011 0.0000000 0.0000000 0.0000000
## 1012 0.0000000 0.0000000 0.0000000
## 1013 0.0000000 0.0000000 0.0000000
## 1014 0.0000000 0.0000000 0.0000000
## 1015 0.0000000 0.0000000 0.0000000
## 1016 0.0000000 1.0000000 0.0000000
## 1017 0.0000000 0.0000000 0.0000000
## 1018 0.0000000 0.0000000 1.0000000
## 1019 0.0000000 0.0000000 0.0000000
## 1020 1.0000000 0.0000000 0.0000000
## 1021 0.0000000 0.0000000 0.0000000
## 1022 0.0000000 0.0000000 0.0000000
## 1023 0.0000000 0.0000000 0.0000000
## 1024 0.0000000 0.5714286 0.2857143
## 1025 0.0000000 0.0000000 0.0000000
## 1026 0.0000000 0.0000000 0.0000000
## 1027 0.0000000 0.8571429 0.1428571
## 1028 0.0000000 0.0000000 0.0000000
## 1029 0.0000000 1.0000000 0.0000000
## 1030 0.0000000 0.0000000 0.0000000
## 1031 0.0000000 0.0000000 0.0000000
## 1032 0.0000000 0.0000000 0.0000000
## 1033 0.0000000 0.0000000 0.0000000
## 1034 0.0000000 0.0000000 0.7142857
## 1035 0.0000000 0.0000000 0.0000000
## 1036 0.0000000 0.0000000 0.0000000
## 1037 0.0000000 0.0000000 0.0000000
## 1038 0.0000000 0.0000000 0.0000000
## 1039 0.0000000 0.0000000 1.0000000
## 1040 0.0000000 0.0000000 0.0000000
## 1041 0.0000000 0.2857143 0.0000000
## 1042 1.0000000 0.0000000 0.0000000
## 1043 0.0000000 0.0000000 0.0000000
## 1044 0.0000000 0.0000000 0.1428571
## 1045 0.0000000 0.0000000 0.0000000
## 1046 0.0000000 0.0000000 0.0000000
## 1047 1.0000000 0.0000000 0.0000000
## 1048 0.0000000 0.0000000 0.5714286
## 1049 0.0000000 1.0000000 0.0000000

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## 1050 0.0000000 0.0000000 0.0000000
## 1051 0.0000000 0.0000000 0.0000000
## 1052 0.0000000 0.0000000 0.0000000
## 1053 0.0000000 0.0000000 0.0000000
## 1054 0.0000000 0.1428571 0.0000000
## 1055 1.0000000 0.0000000 0.0000000
## 1056 0.0000000 1.0000000 0.0000000
## 1057 0.0000000 0.0000000 0.0000000
## 1058 0.0000000 0.0000000 0.0000000
## 1059 0.0000000 0.0000000 0.0000000
## 1060 0.0000000 0.0000000 0.5714286
## 1061 0.0000000 0.0000000 0.8571429
## 1062 0.0000000 0.0000000 0.8571429
## 1063 0.0000000 0.0000000 0.0000000
## 1064 0.0000000 0.2857143 0.0000000
## 1065 0.0000000 0.0000000 0.0000000
## 1066 0.0000000 0.0000000 0.5714286
## 1067 0.0000000 1.0000000 0.0000000
## 1068 0.0000000 0.0000000 0.0000000
## 1069 0.0000000 0.0000000 0.0000000
## 1070 0.0000000 0.0000000 0.0000000
## 1071 0.0000000 0.0000000 0.0000000
## 1072 0.0000000 0.0000000 0.0000000
## 1073 0.0000000 0.0000000 0.0000000
## 1074 0.0000000 0.0000000 0.0000000
## 1075 0.0000000 0.0000000 0.0000000
## 1076 0.0000000 0.0000000 0.0000000
## 1077 0.0000000 0.0000000 0.0000000
## 1078 1.0000000 0.0000000 0.0000000
## 1079 0.0000000 0.0000000 0.0000000
## 1080 0.0000000 0.0000000 0.0000000
## 1081 0.0000000 0.0000000 0.0000000
## 1082 0.0000000 0.0000000 0.0000000
## 1083 0.0000000 0.0000000 0.0000000
## 1084 0.0000000 0.0000000 0.0000000
## 1085 0.0000000 0.0000000 0.0000000
## 1086 0.0000000 0.0000000 0.0000000
## 1087 0.0000000 0.0000000 0.0000000
## 1088 0.0000000 0.0000000 0.0000000
## 1089 0.0000000 0.0000000 0.0000000
## 1090 0.0000000 0.0000000 0.0000000
## 1091 0.0000000 0.0000000 0.0000000
## 1092 0.0000000 0.0000000 0.0000000
## 1093 0.0000000 0.0000000 0.0000000
## 1094 1.0000000 0.0000000 0.0000000
## 1095 0.0000000 0.0000000 0.0000000
## 1096 0.0000000 0.0000000 0.0000000
## 1097 0.0000000 1.0000000 0.0000000
## 1098 0.0000000 0.0000000 0.0000000
## 1099 0.0000000 0.8571429 0.1428571
## 1100 0.0000000 0.0000000 0.0000000
## 1101 0.0000000 0.0000000 0.0000000
## 1102 1.0000000 0.0000000 0.0000000
## 1103 0.0000000 0.0000000 0.0000000

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## 1104 0.0000000 0.0000000 0.0000000
## 1105 1.0000000 0.0000000 0.0000000
## 1106 0.0000000 0.0000000 0.0000000
## 1107 0.0000000 0.0000000 0.0000000
## 1108 0.0000000 0.0000000 0.0000000
## 1109 0.0000000 0.0000000 0.0000000
## 1110 0.0000000 0.0000000 0.0000000
## 1111 1.0000000 0.0000000 0.0000000
## 1112 0.0000000 0.0000000 0.0000000
## 1113 0.0000000 0.0000000 0.0000000
## 1114 0.0000000 0.0000000 0.0000000
## 1115 0.0000000 1.0000000 0.0000000
## 1116 0.0000000 1.0000000 0.0000000
## 1117 0.0000000 1.0000000 0.0000000
## 1118 0.0000000 0.0000000 1.0000000
## 1119 0.0000000 0.0000000 0.0000000
## 1120 0.0000000 0.0000000 0.0000000
## 1121 0.0000000 0.0000000 0.0000000
## 1122 0.0000000 0.0000000 1.0000000
## 1123 0.0000000 0.0000000 0.0000000
## 1124 0.0000000 0.0000000 0.0000000
## 1125 0.0000000 1.0000000 0.0000000
## 1126 0.0000000 0.0000000 0.4285714
## 1127 1.0000000 0.0000000 0.0000000
## 1128 0.0000000 0.0000000 0.0000000
## 1129 0.0000000 0.0000000 0.0000000
## 1130 0.0000000 0.0000000 0.8571429
## 1131 0.0000000 0.0000000 0.0000000
## 1132 0.0000000 0.0000000 0.0000000
## 1133 0.0000000 0.0000000 0.0000000
## 1134 0.0000000 1.0000000 0.0000000
## 1135 0.0000000 0.0000000 0.0000000
## 1136 0.0000000 0.0000000 1.0000000
## 1137 0.0000000 0.0000000 0.0000000
## 1138 0.0000000 0.0000000 0.0000000
## 1139 0.0000000 0.0000000 0.0000000
## 1140 1.0000000 0.0000000 0.0000000
## 1141 0.0000000 0.0000000 0.0000000
## 1142 0.0000000 0.0000000 0.0000000
## 1143 0.0000000 0.0000000 0.0000000
## 1144 0.0000000 0.0000000 0.0000000
## 1145 0.0000000 0.1428571 0.0000000
## 1146 0.0000000 0.0000000 0.0000000
## 1147 0.0000000 0.0000000 0.1428571
## 1148 0.0000000 0.4285714 0.0000000
## 1149 0.0000000 0.0000000 0.0000000
## 1150 0.0000000 0.0000000 0.0000000
## 1151 0.0000000 0.0000000 0.0000000
## 1152 0.0000000 1.0000000 0.0000000
## 1153 0.0000000 0.0000000 0.0000000
## 1154 0.0000000 0.0000000 0.0000000
## 1155 0.0000000 1.0000000 0.0000000
## 1156 0.0000000 0.0000000 0.0000000
## 1157 0.0000000 0.0000000 1.0000000

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## 1158 0.0000000 0.0000000 1.0000000
## 1159 0.0000000 0.0000000 0.0000000
## 1160 0.0000000 0.0000000 1.0000000
## 1161 0.0000000 0.0000000 0.0000000
## 1162 0.0000000 0.0000000 0.0000000
## 1163 0.0000000 0.0000000 1.0000000
## 1164 1.0000000 0.0000000 0.0000000
## 1165 0.0000000 0.0000000 1.0000000
## 1166 0.0000000 0.0000000 0.0000000
## 1167 1.0000000 0.0000000 0.0000000
## 1168 0.0000000 0.0000000 0.0000000
## 1169 0.0000000 0.0000000 0.0000000
## 1170 0.0000000 0.0000000 0.0000000
## 1171 0.0000000 0.0000000 1.0000000
## 1172 0.0000000 0.0000000 0.0000000
## 1173 0.0000000 0.0000000 0.4285714
## 1174 1.0000000 0.0000000 0.0000000
## 1175 0.0000000 0.0000000 1.0000000
## 1176 0.0000000 1.0000000 0.0000000
## 1177 0.0000000 0.0000000 0.0000000
## 1178 0.0000000 0.0000000 0.0000000
## 1179 0.0000000 0.0000000 0.0000000
## 1180 0.0000000 0.0000000 0.0000000
## 1181 0.0000000 0.0000000 0.0000000
## 1182 0.0000000 0.0000000 0.0000000
## 1183 0.0000000 0.0000000 1.0000000
## 1184 0.0000000 0.0000000 0.0000000
## 1185 0.0000000 0.0000000 0.0000000
## 1186 0.0000000 0.0000000 0.7142857
## 1187 0.0000000 0.0000000 0.0000000
## 1188 0.0000000 0.0000000 0.0000000
## 1189 0.0000000 0.0000000 0.0000000
## 1190 0.0000000 0.0000000 0.0000000
## 1191 0.0000000 0.0000000 0.1428571
## 1192 0.0000000 0.7142857 0.0000000
## 1193 0.0000000 0.0000000 0.0000000
## 1194 0.0000000 0.5714286 0.0000000
## 1195 0.0000000 0.0000000 0.0000000
## 1196 0.0000000 0.1428571 0.0000000
## 1197 0.0000000 0.0000000 0.0000000
## 1198 1.0000000 0.0000000 0.0000000
## 1199 0.0000000 0.0000000 0.0000000
## 1200 0.0000000 0.0000000 0.0000000
## 1201 0.0000000 0.0000000 0.0000000
## 1202 0.0000000 0.0000000 0.8571429
## 1203 0.0000000 0.0000000 0.0000000
## 1204 1.0000000 0.0000000 0.0000000
## 1205 0.0000000 0.0000000 0.0000000
## 1206 0.0000000 0.0000000 1.0000000
## 1207 0.0000000 1.0000000 0.0000000
## 1208 0.0000000 0.0000000 0.0000000
## 1209 0.0000000 0.0000000 0.0000000
## 1210 0.0000000 0.0000000 0.0000000
## 1211 0.0000000 1.0000000 0.0000000

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## 1212 0.0000000 0.0000000 0.0000000
## 1213 0.0000000 0.0000000 0.0000000
## 1214 0.0000000 0.1428571 0.0000000
## 1215 0.0000000 0.0000000 0.0000000
## 1216 0.0000000 0.0000000 0.0000000
## 1217 0.0000000 0.0000000 0.0000000
## 1218 0.0000000 1.0000000 0.0000000
## 1219 0.0000000 0.0000000 0.7142857
## 1220 0.0000000 0.8571429 0.0000000
## 1221 0.8571429 0.0000000 0.1428571
## 1222 0.0000000 0.0000000 0.0000000
## 1223 0.0000000 0.0000000 0.0000000
## 1224 0.0000000 0.0000000 0.0000000
## 1225 0.0000000 0.0000000 0.0000000
## 1226 0.0000000 0.0000000 0.0000000
## 1227 0.0000000 0.0000000 0.0000000
## 1228 1.0000000 0.0000000 0.0000000
## 1229 0.0000000 0.0000000 0.0000000
## 1230 0.0000000 0.0000000 0.0000000
## 1231 0.0000000 0.0000000 0.0000000
## 1232 1.0000000 0.0000000 0.0000000
## 1233 0.0000000 1.0000000 0.0000000
## 1234 0.0000000 1.0000000 0.0000000
## 1235 0.0000000 0.0000000 0.0000000
## 1236 0.0000000 0.0000000 0.0000000
## 1237 0.0000000 0.0000000 0.0000000
## 1238 1.0000000 0.0000000 0.0000000
## 1239 0.0000000 0.0000000 0.0000000
## 1240 0.0000000 0.0000000 0.0000000
## 1241 0.0000000 0.0000000 0.0000000
## 1242 0.0000000 0.0000000 0.0000000
## 1243 0.0000000 0.0000000 0.0000000
## 1244 0.0000000 0.0000000 0.0000000
## 1245 0.0000000 0.0000000 0.1428571
## 1246 0.0000000 0.0000000 1.0000000
## 1247 0.0000000 0.0000000 0.0000000
## 1248 0.0000000 0.0000000 0.0000000
## 1249 0.0000000 0.0000000 0.0000000
## 1250 0.0000000 0.0000000 1.0000000
## 1251 0.0000000 0.0000000 0.0000000
## 1252 0.0000000 0.0000000 0.0000000
## 1253 1.0000000 0.0000000 0.0000000
## 1254 0.0000000 0.0000000 0.0000000
## 1255 0.0000000 0.0000000 0.0000000
## 1256 0.0000000 0.8571429 0.0000000
## 1257 0.0000000 0.0000000 1.0000000
## 1258 0.0000000 0.0000000 0.0000000
## 1259 0.0000000 0.0000000 0.0000000
## 1260 0.0000000 0.0000000 0.0000000
## 1261 1.0000000 0.0000000 0.0000000
## 1262 0.0000000 0.8571429 0.0000000
## 1263 1.0000000 0.0000000 0.0000000
## 1264 0.0000000 1.0000000 0.0000000
## 1265 0.0000000 0.0000000 0.0000000

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## 1266 0.0000000 0.0000000 0.0000000
## 1267 0.0000000 0.0000000 0.0000000
## 1268 0.0000000 0.0000000 0.0000000
## 1269 0.0000000 0.0000000 0.0000000
## 1270 0.0000000 0.0000000 0.0000000
## 1271 0.0000000 0.0000000 1.0000000
## 1272 0.0000000 0.0000000 0.0000000
## 1273 0.0000000 0.0000000 0.0000000
## 1274 0.0000000 0.0000000 0.0000000
## 1275 0.0000000 0.0000000 0.0000000
## 1276 0.0000000 0.0000000 0.0000000
## 1277 0.0000000 0.0000000 0.0000000
## 1278 0.0000000 0.0000000 0.0000000
## 1279 0.0000000 0.0000000 0.0000000
## 1280 0.0000000 0.0000000 1.0000000
## 1281 1.0000000 0.0000000 0.0000000
## 1282 0.0000000 0.0000000 0.0000000
## 1283 1.0000000 0.0000000 0.0000000
## 1284 0.0000000 0.0000000 0.0000000
## 1285 0.0000000 0.0000000 0.0000000
## 1286 0.0000000 0.0000000 0.0000000
## 1287 0.0000000 0.0000000 0.0000000
## 1288 1.0000000 0.0000000 0.0000000
## 1289 0.5714286 0.0000000 0.4285714
## 1290 0.0000000 0.0000000 0.0000000
## 1291 0.0000000 0.0000000 0.0000000
## 1292 0.0000000 0.0000000 0.0000000
## 1293 0.0000000 0.0000000 0.0000000
## 1294 0.0000000 0.0000000 1.0000000
## 1295 0.0000000 0.0000000 0.0000000
## 1296 0.0000000 0.0000000 0.0000000
## 1297 0.0000000 0.0000000 0.0000000
## 1298 0.0000000 0.0000000 0.0000000
## 1299 0.0000000 0.0000000 0.0000000
## 1300 0.0000000 0.0000000 0.0000000
## 1301 0.0000000 0.1428571 0.0000000
## 1302 0.0000000 0.0000000 0.0000000
## 1303 0.0000000 0.0000000 0.0000000
## 1304 0.0000000 1.0000000 0.0000000
## 1305 0.0000000 0.0000000 0.5714286
## 1306 0.0000000 0.0000000 0.0000000
## 1307 0.0000000 0.0000000 0.0000000
## 1308 0.0000000 0.1428571 0.0000000
## 1309 0.0000000 0.0000000 0.0000000
## 1310 0.0000000 0.0000000 0.0000000
## 1311 0.0000000 0.8571429 0.0000000
## 1312 0.0000000 0.0000000 0.0000000
## 1313 0.0000000 0.0000000 0.0000000
## 1314 0.0000000 0.0000000 0.0000000
## 1315 0.0000000 0.0000000 0.0000000
## 1316 0.0000000 0.0000000 0.0000000
## 1317 0.0000000 0.0000000 0.0000000
## 1318 0.0000000 0.1428571 0.0000000
## 1319 0.0000000 0.0000000 0.0000000

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## 1320 0.0000000 0.0000000 0.0000000
## 1321 0.0000000 0.5714286 0.0000000
## 1322 0.0000000 0.0000000 0.0000000
## 1323 0.0000000 1.0000000 0.0000000
## 1324 0.0000000 0.0000000 0.5714286
## 1325 0.0000000 0.0000000 0.0000000
## 1326 0.0000000 0.0000000 1.0000000
## 1327 1.0000000 0.0000000 0.0000000
## 1328 0.2857143 0.0000000 0.0000000
## 1329 0.0000000 0.0000000 0.0000000
## 1330 0.0000000 0.0000000 0.0000000
## 1331 0.0000000 0.0000000 0.0000000
## 1332 0.0000000 0.0000000 0.0000000
## 1333 0.0000000 0.0000000 0.0000000
## 1334 0.0000000 0.0000000 0.0000000
## 1335 0.0000000 0.0000000 0.0000000
## 1336 0.0000000 0.0000000 0.0000000
## 1337 1.0000000 0.0000000 0.0000000
## 1338 0.0000000 0.0000000 0.0000000
## 1339 1.0000000 0.0000000 0.0000000
## 1340 0.0000000 0.0000000 0.1428571
## 1341 0.0000000 0.0000000 0.0000000
## 1342 0.0000000 0.0000000 0.0000000
## 1343 0.0000000 0.8571429 0.0000000
## 1344 0.0000000 0.0000000 0.8571429
## 1345 0.0000000 0.0000000 1.0000000
## 1346 0.0000000 1.0000000 0.0000000
## 1347 0.0000000 0.0000000 0.8571429
## 1348 0.0000000 0.0000000 0.8571429
## 1349 0.0000000 1.0000000 0.0000000
## 1350 0.0000000 0.0000000 0.0000000
## 1351 0.0000000 0.0000000 0.0000000
## 1352 0.0000000 0.0000000 0.0000000
## 1353 0.0000000 0.0000000 0.0000000
## 1354 0.0000000 0.0000000 0.0000000
## 1355 0.0000000 0.0000000 0.0000000
## 1356 0.0000000 0.0000000 0.0000000
## 1357 0.0000000 0.0000000 0.0000000
## 1358 0.0000000 0.0000000 0.0000000
## 1359 0.0000000 0.0000000 0.0000000
## 1360 0.0000000 0.0000000 0.0000000
## 1361 0.0000000 0.0000000 0.0000000
## 1362 0.0000000 0.0000000 0.0000000
## 1363 1.0000000 0.0000000 0.0000000
## 1364 0.0000000 0.0000000 0.0000000
## 1365 0.0000000 0.0000000 0.0000000
## 1366 0.0000000 0.0000000 0.0000000
## 1367 0.0000000 0.0000000 0.0000000
## 1368 0.0000000 0.0000000 0.0000000
## 1369 0.0000000 0.0000000 0.0000000
## 1370 1.0000000 0.0000000 0.0000000
## 1371 0.0000000 0.0000000 0.0000000
## 1372 0.0000000 0.0000000 0.0000000
## 1373 0.0000000 0.0000000 0.0000000
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## 1374 0.8571429 0.0000000 0.0000000
## 1375 0.0000000 0.0000000 0.0000000
## 1376 0.0000000 0.0000000 0.0000000
## 1377 0.0000000 0.0000000 0.0000000
## 1378 0.0000000 0.0000000 0.0000000
## 1379 0.0000000 0.0000000 0.0000000
## 1380 0.0000000 0.0000000 1.0000000
## 1381 0.0000000 0.0000000 0.0000000
## 1382 0.0000000 0.0000000 0.0000000
## 1383 0.0000000 0.0000000 0.0000000
## 1384 1.0000000 0.0000000 0.0000000
## 1385 0.0000000 0.7142857 0.1428571
## 1386 0.0000000 1.0000000 0.0000000
## 1387 0.0000000 0.0000000 0.0000000
## 1388 0.0000000 0.0000000 0.0000000
## 1389 0.0000000 0.0000000 0.0000000
## 1390 0.0000000 0.0000000 1.0000000
## 1391 0.0000000 0.0000000 0.0000000
## 1392 0.0000000 0.0000000 0.0000000
## 1393 0.0000000 0.0000000 0.0000000
## 1394 0.0000000 1.0000000 0.0000000
## 1395 0.0000000 0.0000000 0.0000000
## 1396 1.0000000 0.0000000 0.0000000
## 1397 1.0000000 0.0000000 0.0000000
## 1398 0.0000000 1.0000000 0.0000000
## 1399 0.0000000 0.0000000 0.0000000
## 1400 0.1428571 0.1428571 0.1428571
## 1401 1.0000000 0.0000000 0.0000000
## 1402 1.0000000 0.0000000 0.0000000
## 1403 0.0000000 0.0000000 0.0000000
## 1404 0.0000000 0.0000000 0.0000000
## 1405 0.0000000 0.0000000 0.0000000
## 1406 0.0000000 0.0000000 0.0000000
## 1407 0.0000000 0.0000000 0.0000000
## 1408 0.0000000 1.0000000 0.0000000
## 1409 0.0000000 0.0000000 0.0000000
## 1410 0.0000000 0.8571429 0.0000000
## 1411 0.0000000 0.0000000 0.0000000
## 1412 0.0000000 0.0000000 0.0000000
## 1413 1.0000000 0.0000000 0.0000000
## 1414 0.0000000 0.0000000 0.0000000
## 1415 0.0000000 0.0000000 0.0000000
## 1416 0.0000000 0.0000000 0.0000000
## 1417 0.0000000 0.0000000 0.0000000
## 1418 0.0000000 0.0000000 0.0000000
## 1419 0.0000000 0.0000000 0.0000000
## 1420 0.0000000 0.0000000 0.0000000
## 1421 0.0000000 0.0000000 0.0000000
## 1422 0.0000000 0.0000000 0.0000000
## 1423 0.0000000 0.0000000 0.1428571
## 1424 0.0000000 0.0000000 0.0000000
## 1425 1.0000000 0.0000000 0.0000000
## 1426 0.0000000 0.0000000 0.0000000
## 1427 0.0000000 0.0000000 0.0000000

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## 1428 0.0000000 0.0000000 0.0000000
## 1429 0.0000000 0.0000000 0.0000000
## 1430 0.0000000 0.0000000 1.0000000
## 1431 0.0000000 0.0000000 0.0000000
## 1432 0.0000000 0.0000000 0.0000000
## 1433 0.0000000 0.0000000 0.0000000
## 1434 0.0000000 0.0000000 0.0000000
## 1435 0.0000000 0.0000000 0.0000000
## 1436 0.0000000 0.0000000 0.0000000
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## 1438 0.0000000 0.0000000 0.0000000
## 1439 0.0000000 0.0000000 0.0000000
## 1440 0.0000000 0.0000000 0.0000000
## 1441 1.0000000 0.0000000 0.0000000
## 1442 0.0000000 0.0000000 0.8571429
## 1443 0.0000000 0.0000000 1.0000000
## 1444 0.0000000 0.5714286 0.2857143
## 1445 0.0000000 0.0000000 0.0000000
## 1446 0.0000000 0.0000000 0.1428571
## 1447 0.0000000 0.0000000 0.0000000
## 1448 0.0000000 0.0000000 0.0000000
## 1449 0.0000000 0.0000000 0.0000000
## 1450 0.0000000 0.0000000 0.0000000
## 1451 0.0000000 0.0000000 0.0000000
## 1452 0.0000000 0.0000000 0.0000000
## 1453 1.0000000 0.0000000 0.0000000
## 1454 0.0000000 0.5714286 0.4285714
## 1455 0.0000000 0.0000000 0.0000000
## 1456 0.0000000 0.0000000 0.1428571
## 1457 0.0000000 0.0000000 1.0000000
## 1458 0.0000000 0.0000000 0.0000000
## 1459 0.0000000 0.0000000 0.0000000
## 1460 0.0000000 0.0000000 0.0000000
## 1461 0.0000000 0.0000000 0.0000000
## 1462 0.0000000 0.0000000 0.0000000
## 1463 0.0000000 0.0000000 0.0000000
## 1464 0.0000000 0.0000000 0.0000000
## 1465 0.0000000 0.0000000 0.1428571
## 1466 0.0000000 0.0000000 0.0000000
## 1467 0.0000000 0.0000000 0.1428571
## 1468 0.0000000 1.0000000 0.0000000
## 1469 0.0000000 0.0000000 0.0000000
## 1470 0.0000000 0.0000000 0.0000000
## 1471 0.0000000 0.0000000 0.0000000
## 1472 0.0000000 0.0000000 0.0000000
## 1473 0.0000000 0.0000000 0.0000000
## 1474 0.0000000 0.0000000 0.0000000
## 1475 0.0000000 0.0000000 0.0000000
## 1476 0.0000000 0.0000000 0.0000000
## 1477 0.0000000 0.0000000 0.1428571
## 1478 1.0000000 0.0000000 0.0000000
## 1479 0.0000000 0.0000000 1.0000000
## 1480 0.0000000 0.0000000 0.0000000
## 1481 0.0000000 0.0000000 0.0000000

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## 1482 0.0000000 0.0000000 0.0000000
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## 1484 1.0000000 0.0000000 0.0000000
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## 1487 0.0000000 0.0000000 0.0000000
## 1488 0.0000000 0.0000000 0.0000000
## 1489 0.0000000 0.0000000 0.0000000
## 1490 1.0000000 0.0000000 0.0000000
## 1491 0.0000000 1.0000000 0.0000000
## 1492 0.0000000 1.0000000 0.0000000
## 1493 0.0000000 0.0000000 0.0000000
## 1494 1.0000000 0.0000000 0.0000000
## 1495 0.0000000 0.0000000 0.0000000
## 1496 0.1428571 0.1428571 0.0000000
## 1497 0.0000000 0.0000000 0.8571429
## 1498 0.0000000 0.0000000 0.0000000
## 1499 0.0000000 0.0000000 0.0000000
## 1500 0.0000000 0.0000000 0.0000000
## 1501 0.0000000 0.1428571 0.0000000
## 1502 0.0000000 0.0000000 0.0000000
## 1503 0.0000000 0.0000000 0.4285714
## 1504 0.0000000 0.0000000 0.0000000
## 1505 0.0000000 0.7142857 0.0000000
## 1506 0.0000000 0.0000000 0.0000000
## 1507 0.0000000 0.8571429 0.1428571
## 1508 0.0000000 0.0000000 0.0000000
## 1509 0.0000000 0.0000000 0.0000000
## 1510 0.0000000 0.0000000 0.2857143
## 1511 1.0000000 0.0000000 0.0000000
## 1512 0.0000000 0.0000000 0.0000000
## 1513 0.0000000 0.0000000 0.0000000
## 1514 0.0000000 0.0000000 1.0000000
## 1515 0.2857143 0.0000000 0.1428571
## 1516 0.0000000 0.0000000 0.0000000
## 1517 0.0000000 0.8571429 0.1428571
## 1518 0.0000000 0.0000000 0.0000000
## 1519 0.0000000 0.8571429 0.0000000
## 1520 0.0000000 0.1428571 0.0000000
## 1521 0.0000000 0.0000000 0.0000000
## 1522 0.0000000 1.0000000 0.0000000
## 1523 0.0000000 1.0000000 0.0000000
## 1524 1.0000000 0.0000000 0.0000000
## 1525 1.0000000 0.0000000 0.0000000
## 1526 0.0000000 0.0000000 0.5714286
## 1527 0.0000000 0.0000000 0.0000000
## 1528 0.0000000 0.0000000 0.0000000
## 1529 0.0000000 0.0000000 0.0000000
## 1530 0.0000000 0.0000000 0.0000000
## 1531 1.0000000 0.0000000 0.0000000
## 1532 0.0000000 0.0000000 0.1428571
## 1533 0.0000000 0.0000000 0.0000000
## 1534 0.0000000 0.0000000 0.0000000
## 1535 0.0000000 0.0000000 0.0000000

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## 1536 0.0000000 0.0000000 0.0000000
## 1537 0.0000000 0.0000000 0.0000000
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## 1541 0.0000000 0.0000000 0.0000000
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## 1543 1.0000000 0.0000000 0.0000000
## 1544 0.0000000 0.0000000 0.0000000
## 1545 0.0000000 0.0000000 0.0000000
## 1546 0.0000000 0.0000000 0.0000000
## 1547 0.0000000 0.0000000 0.0000000
## 1548 0.0000000 1.0000000 0.0000000
## 1549 0.0000000 0.0000000 0.0000000
## 1550 0.0000000 0.0000000 0.0000000
## 1551 0.0000000 0.0000000 1.0000000
## 1552 1.0000000 0.0000000 0.0000000
## 1553 0.0000000 0.0000000 0.0000000
## 1554 0.0000000 0.7142857 0.0000000
## 1555 0.0000000 0.0000000 0.0000000
## 1556 0.0000000 0.0000000 0.0000000
## 1557 0.0000000 0.0000000 0.7142857
## 1558 0.0000000 0.0000000 0.0000000
## 1559 0.0000000 0.0000000 0.0000000
## 1560 0.0000000 0.0000000 0.0000000
## 1561 0.0000000 0.0000000 0.0000000
## 1562 0.0000000 0.0000000 0.0000000
## 1563 0.0000000 0.0000000 1.0000000
## 1564 0.0000000 0.0000000 0.7142857
## 1565 0.0000000 0.0000000 0.0000000
## 1566 0.0000000 0.0000000 1.0000000
## 1567 0.0000000 0.0000000 0.0000000
## 1568 0.0000000 0.0000000 0.0000000
## 1569 0.0000000 0.0000000 0.0000000
## 1570 0.0000000 0.0000000 0.0000000
## 1571 0.0000000 0.0000000 0.0000000
## 1572 0.0000000 0.0000000 0.0000000
## 1573 0.0000000 0.0000000 0.0000000
## 1574 0.0000000 0.0000000 0.0000000
## 1575 0.0000000 0.0000000 0.0000000
## 1576 0.0000000 0.0000000 0.0000000
## 1577 0.0000000 0.0000000 0.0000000
## 1578 1.0000000 0.0000000 0.0000000
## 1579 0.0000000 0.0000000 0.0000000
## 1580 0.0000000 0.1428571 0.8571429
## 1581 0.0000000 1.0000000 0.0000000
## 1582 0.0000000 0.8571429 0.0000000
## 1583 0.0000000 0.0000000 0.0000000
## 1584 0.0000000 0.0000000 0.0000000
## 1585 0.0000000 0.0000000 0.0000000
## 1586 0.0000000 0.0000000 1.0000000
## 1587 0.0000000 0.0000000 0.0000000
## 1588 0.0000000 0.0000000 1.0000000
## 1589 0.0000000 0.0000000 0.0000000

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## 1590 0.0000000 0.0000000 0.0000000
## 1591 0.0000000 0.0000000 0.0000000
## 1592 0.0000000 0.0000000 0.0000000
## 1593 0.0000000 0.0000000 0.0000000
## 1594 0.0000000 0.0000000 1.0000000
## 1595 0.0000000 0.0000000 0.0000000
## 1596 0.0000000 0.0000000 0.0000000
## 1597 0.0000000 0.0000000 0.0000000
## 1598 0.0000000 0.0000000 0.0000000
## 1599 1.0000000 0.0000000 0.0000000
## 1600 0.0000000 0.0000000 0.0000000
## 1601 1.0000000 0.0000000 0.0000000
## 1602 0.0000000 0.0000000 0.0000000
## 1603 0.0000000 1.0000000 0.0000000
## 1604 0.0000000 0.0000000 0.5714286
## 1605 0.0000000 0.0000000 0.0000000
## 1606 0.0000000 0.0000000 0.0000000
## 1607 0.0000000 0.0000000 0.2857143
## 1608 0.0000000 1.0000000 0.0000000
## 1609 0.0000000 0.0000000 0.2857143
## 1610 1.0000000 0.0000000 0.0000000
## 1611 0.0000000 0.0000000 0.8571429
## 1612 0.0000000 0.0000000 0.4285714
## 1613 1.0000000 0.0000000 0.0000000
## 1614 0.0000000 1.0000000 0.0000000
## 1615 0.0000000 0.0000000 0.0000000
## 1616 0.0000000 0.0000000 0.8571429
## 1617 0.0000000 1.0000000 0.0000000
## 1618 0.0000000 0.0000000 0.0000000
## 1619 0.0000000 0.0000000 0.0000000
## 1620 0.0000000 0.0000000 0.0000000
## 1621 0.0000000 0.0000000 0.0000000
## 1622 0.0000000 0.0000000 0.0000000
## 1623 0.0000000 0.0000000 0.0000000
## 1624 0.0000000 0.0000000 0.0000000
## 1625 1.0000000 0.0000000 0.0000000
## 1626 0.0000000 0.0000000 0.0000000
## 1627 0.0000000 0.4285714 0.0000000
## 1628 0.0000000 0.0000000 0.1428571
## 1629 0.0000000 0.0000000 0.0000000
## 1630 0.0000000 0.0000000 0.0000000
## 1631 0.0000000 0.8571429 0.0000000
## 1632 0.0000000 0.0000000 0.1428571
## 1633 0.0000000 1.0000000 0.0000000
## 1634 0.0000000 0.1428571 0.0000000
## 1635 0.0000000 1.0000000 0.0000000
## 1636 0.0000000 0.0000000 1.0000000
## 1637 0.0000000 0.0000000 0.0000000
## 1638 0.0000000 0.0000000 0.0000000
## 1639 0.0000000 0.0000000 0.0000000
## 1640 1.0000000 0.0000000 0.0000000
## 1641 0.0000000 0.8571429 0.0000000
## 1642 0.0000000 0.0000000 0.0000000
## 1643 0.0000000 0.0000000 0.1428571

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```
## 1644 0.0000000 0.0000000 1.0000000
## 1645 0.0000000 0.0000000 0.0000000
## 1646 0.0000000 0.0000000 0.0000000
## 1647 0.0000000 0.0000000 0.0000000
## 1648 0.0000000 0.0000000 0.0000000
## 1649 0.0000000 0.0000000 0.0000000
## 1650 0.0000000 0.0000000 0.0000000
## 1651 0.0000000 0.0000000 0.1428571
## 1652 0.0000000 0.0000000 0.0000000
## 1653 0.0000000 1.0000000 0.0000000
## 1654 1.0000000 0.0000000 0.0000000
## 1655 0.0000000 0.0000000 0.0000000
## 1656 0.0000000 0.0000000 0.0000000
## 1657 0.0000000 0.0000000 0.0000000
## 1658 0.7142857 0.0000000 0.2857143
## 1659 0.0000000 0.7142857 0.0000000
## 1660 0.0000000 0.0000000 0.0000000
## 1661 0.0000000 0.0000000 0.0000000
## 1662 0.0000000 0.0000000 0.0000000
## 1663 0.0000000 0.0000000 0.0000000
## 1664 0.0000000 0.8571429 0.0000000
## 1665 0.0000000 0.0000000 0.0000000
## 1666 0.0000000 0.0000000 1.0000000
## 1667 0.7142857 0.0000000 0.0000000
## 1668 0.0000000 0.0000000 0.0000000
## 1669 0.0000000 0.0000000 0.0000000
## 1670 0.0000000 0.0000000 0.0000000
## 1671 0.0000000 0.0000000 0.0000000
## 1672 0.0000000 0.0000000 0.0000000
## 1673 0.0000000 0.0000000 0.0000000
## 1674 0.0000000 0.0000000 0.0000000
## 1675 0.0000000 0.7142857 0.0000000
## 1676 0.0000000 0.0000000 0.0000000
## 1677 0.0000000 0.0000000 0.0000000
## 1678 1.0000000 0.0000000 0.0000000
## 1679 0.0000000 1.0000000 0.0000000
## 1680 0.0000000 0.0000000 0.0000000
## 1681 0.0000000 0.8571429 0.0000000
## 1682 0.0000000 0.0000000 1.0000000
## 1683 0.0000000 0.0000000 0.0000000
## 1684 1.0000000 0.0000000 0.0000000
## 1685 0.0000000 0.0000000 0.0000000
## 1686 0.0000000 0.0000000 0.0000000
## 1687 0.0000000 0.0000000 0.0000000
## 1688 0.0000000 0.0000000 0.0000000
## 1689 0.0000000 0.0000000 0.0000000
## 1690 1.0000000 0.0000000 0.0000000
## 1691 0.0000000 0.0000000 0.0000000
## 1692 0.0000000 0.0000000 0.0000000
## 1693 0.5714286 0.0000000 0.0000000
## 1694 0.0000000 0.0000000 0.0000000
## 1695 0.0000000 0.0000000 0.0000000
## 1696 0.0000000 0.0000000 0.0000000
## 1697 0.0000000 0.0000000 0.0000000
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## 1698 0.0000000 0.7142857 0.1428571
## 1699 1.0000000 0.0000000 0.0000000
## 1700 0.0000000 0.0000000 0.0000000
## 1701 0.0000000 0.0000000 0.0000000
## 1702 0.0000000 0.0000000 0.0000000
## 1703 0.0000000 0.0000000 0.0000000
## 1704 1.0000000 0.0000000 0.0000000
## 1705 0.0000000 0.0000000 0.0000000
## 1706 0.0000000 0.0000000 0.0000000
## 1707 0.0000000 0.0000000 0.0000000
## 1708 0.0000000 0.0000000 0.0000000
## 1709 1.0000000 0.0000000 0.0000000
## 1710 0.0000000 0.0000000 0.0000000
## 1711 0.0000000 1.0000000 0.0000000
## 1712 0.0000000 0.0000000 1.0000000
## 1713 0.0000000 0.0000000 1.0000000
## 1714 1.0000000 0.0000000 0.0000000
## 1715 0.0000000 0.0000000 0.0000000
## 1716 0.0000000 0.1428571 0.0000000
## 1717 0.0000000 1.0000000 0.0000000
## 1718 0.0000000 0.0000000 0.0000000
## 1719 0.0000000 0.0000000 0.0000000
## 1720 0.0000000 0.0000000 0.0000000
## 1721 0.0000000 0.0000000 0.0000000
## 1722 0.0000000 1.0000000 0.0000000
## 1723 0.0000000 0.0000000 0.0000000
## 1724 0.0000000 0.0000000 1.0000000
## 1725 0.0000000 0.0000000 0.0000000
## 1726 0.0000000 0.0000000 0.0000000
## 1727 0.0000000 0.0000000 0.8571429
## 1728 0.0000000 0.0000000 0.0000000
## 1729 0.0000000 0.0000000 0.0000000
## 1730 0.7142857 0.0000000 0.1428571
## 1731 0.0000000 0.0000000 0.0000000
## 1732 0.0000000 0.0000000 0.0000000
## 1733 0.0000000 0.0000000 0.1428571
## 1734 0.0000000 0.0000000 0.0000000
## 1735 1.0000000 0.0000000 0.0000000
## 1736 0.0000000 0.0000000 0.0000000
## 1737 0.0000000 0.0000000 0.0000000
## 1738 0.0000000 0.0000000 0.0000000
## 1739 0.0000000 0.0000000 0.8571429
## 1740 0.0000000 0.0000000 0.0000000
## 1741 1.0000000 0.0000000 0.0000000
## 1742 0.0000000 0.0000000 0.0000000
## 1743 0.0000000 0.0000000 0.0000000
## 1744 0.0000000 1.0000000 0.0000000
## 1745 0.0000000 1.0000000 0.0000000
## 1746 0.0000000 0.0000000 0.0000000
## 1747 0.0000000 0.0000000 0.0000000
## 1748 1.0000000 0.0000000 0.0000000
## 1749 0.0000000 0.0000000 0.0000000
## 1750 0.0000000 0.0000000 0.0000000
## 1751 0.0000000 0.0000000 0.0000000

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1752 0.0000000 0.0000000 1.0000000
1753 0.0000000 0.0000000 0.0000000
1754 0.0000000 0.0000000 0.0000000
1755 0.0000000 0.0000000 0.0000000
1756 0.0000000 0.0000000 1.0000000
1757 0.0000000 0.0000000 0.0000000
1758 0.0000000 0.0000000 0.0000000
1759 0.0000000 0.0000000 0.0000000
1760 0.0000000 0.0000000 1.0000000
1761 0.0000000 0.0000000 0.0000000
1762 0.0000000 0.0000000 0.0000000
1763 0.0000000 0.0000000 0.0000000
1764 0.0000000 0.0000000 0.0000000
1765 0.0000000 0.0000000 1.0000000
1766 0.0000000 1.0000000 0.0000000
1767 0.0000000 0.0000000 0.0000000
1768 0.0000000 0.7142857 0.0000000
1769 0.0000000 0.0000000 0.0000000
1770 0.0000000 0.0000000 1.0000000
1771 0.0000000 0.0000000 0.0000000
1772 0.7142857 0.0000000 0.0000000
1773 1.0000000 0.0000000 0.0000000
1774 0.0000000 0.0000000 0.0000000
1775 0.0000000 0.0000000 0.0000000
1776 0.0000000 0.0000000 0.0000000
1777 0.0000000 0.0000000 0.0000000
1778 0.0000000 0.7142857 0.0000000
1779 0.0000000 0.1428571 0.0000000
1780 0.0000000 0.0000000 0.0000000
1781 0.0000000 0.0000000 0.0000000
1782 0.0000000 0.0000000 0.0000000
1783 1.0000000 0.0000000 0.0000000
1784 0.0000000 0.0000000 0.0000000
1785 0.0000000 0.5714286 0.0000000
1786 0.0000000 0.0000000 0.0000000
1787 0.0000000 0.0000000 0.0000000
1788 0.0000000 0.0000000 0.0000000
1789 1.0000000 0.0000000 0.0000000
1790 1.0000000 0.0000000 0.0000000
1791 0.0000000 0.8571429 0.0000000
1792 0.0000000 0.0000000 0.0000000
1793 0.0000000 0.0000000 0.0000000
1794 0.0000000 0.0000000 0.0000000
1795 0.0000000 0.0000000 0.7142857
1796 0.0000000 1.0000000 0.0000000
1797 0.0000000 0.0000000 0.1428571
1798 0.0000000 0.0000000 0.0000000
1799 0.0000000 0.0000000 0.0000000
1800 0.0000000 0.0000000 0.0000000
1801 0.0000000 0.7142857 0.0000000
1802 0.0000000 0.0000000 0.0000000
1803 0.0000000 0.0000000 0.0000000
1804 0.0000000 0.0000000 0.0000000
1805 0.0000000 0.0000000 0.0000000

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## 1806 1.0000000 0.0000000 0.0000000
## 1807 0.0000000 0.0000000 0.0000000
## 1808 0.0000000 0.0000000 0.0000000
## 1809 0.0000000 0.0000000 0.0000000
## 1810 0.0000000 0.0000000 0.0000000
## 1811 0.0000000 0.0000000 0.1428571
## 1812 0.0000000 0.0000000 0.0000000
## 1813 0.0000000 0.0000000 0.0000000
## 1814 0.0000000 0.0000000 0.0000000
## 1815 0.0000000 0.0000000 0.0000000
## 1816 0.0000000 0.0000000 0.0000000
## 1817 0.0000000 0.0000000 0.0000000
## 1818 0.0000000 0.0000000 0.0000000
## 1819 0.0000000 0.8571429 0.0000000
## 1820 0.0000000 0.0000000 0.0000000
## 1821 0.0000000 0.0000000 0.0000000
## 1822 0.0000000 0.0000000 0.0000000
## 1823 0.0000000 0.0000000 0.0000000
## 1824 0.0000000 0.0000000 0.0000000
## 1825 0.0000000 0.0000000 0.0000000
## 1826 0.0000000 0.0000000 0.0000000
## 1827 0.0000000 0.0000000 0.0000000
## 1828 0.0000000 0.7142857 0.2857143
## 1829 0.0000000 0.0000000 1.0000000
## 1830 0.0000000 0.0000000 0.0000000
## 1831 0.0000000 0.0000000 0.0000000
## 1832 0.0000000 0.0000000 0.0000000
## 1833 0.0000000 0.0000000 0.0000000
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## 1835 0.0000000 0.0000000 0.0000000
## 1836 0.0000000 0.0000000 0.0000000
## 1837 0.0000000 0.0000000 1.0000000
## 1838 0.0000000 0.0000000 1.0000000
## 1839 0.0000000 0.0000000 0.0000000
## 1840 0.0000000 1.0000000 0.0000000
## 1841 0.0000000 0.0000000 0.1428571
## 1842 0.0000000 0.0000000 0.0000000
## 1843 0.0000000 1.0000000 0.0000000
## 1844 0.0000000 0.0000000 0.0000000
## 1845 0.0000000 1.0000000 0.0000000
## 1846 0.0000000 1.0000000 0.0000000
## 1847 0.0000000 0.0000000 0.0000000
## 1848 0.0000000 0.1428571 0.0000000
## 1849 0.0000000 0.1428571 0.0000000
## 1850 0.0000000 0.0000000 0.0000000
## 1851 0.0000000 0.0000000 0.0000000
## 1852 0.0000000 0.0000000 0.0000000
## 1853 0.0000000 0.2857143 0.0000000
## 1854 1.0000000 0.0000000 0.0000000
## 1855 0.0000000 0.0000000 0.0000000
## 1856 0.0000000 0.0000000 0.5714286
## 1857 0.0000000 0.7142857 0.0000000
## 1858 0.0000000 0.0000000 0.0000000
## 1859 1.0000000 0.0000000 0.0000000

```



```

## 1860 0.0000000 0.0000000 0.1428571
## 1861 0.4285714 0.0000000 0.0000000
## 1862 0.0000000 0.0000000 0.0000000
## 1863 0.0000000 0.0000000 0.0000000
## 1864 0.0000000 0.0000000 0.0000000
## 1865 1.0000000 0.0000000 0.0000000
## 1866 0.0000000 0.1428571 0.4285714
## 1867 1.0000000 0.0000000 0.0000000
## 1868 0.0000000 0.0000000 0.0000000
## 1869 0.0000000 0.0000000 0.2857143
## 1870 0.0000000 0.0000000 1.0000000
## 1871 0.0000000 0.0000000 0.0000000
## 1872 0.0000000 1.0000000 0.0000000
## 1873 0.0000000 0.0000000 0.0000000
## 1874 0.0000000 0.0000000 0.0000000
## 1875 0.0000000 0.0000000 0.0000000
## 1876 0.0000000 0.0000000 0.2857143
## 1877 0.0000000 0.0000000 0.0000000
## 1878 0.0000000 0.0000000 0.0000000
## 1879 0.0000000 0.0000000 0.0000000
## 1880 0.0000000 0.0000000 0.0000000
## 1881 0.0000000 0.0000000 0.0000000
## 1882 0.0000000 0.0000000 0.0000000
## 1883 0.0000000 0.0000000 0.0000000
## 1884 0.0000000 0.0000000 0.0000000
## 1885 0.0000000 0.0000000 0.0000000
## 1886 0.0000000 0.0000000 0.0000000
## 1887 0.0000000 0.1428571 0.2857143
## 1888 1.0000000 0.0000000 0.0000000
## 1889 0.0000000 0.0000000 0.8571429
## 1890 1.0000000 0.0000000 0.0000000
## 1891 0.0000000 0.0000000 0.0000000
## 1892 0.0000000 0.0000000 0.0000000
## 1893 0.0000000 0.0000000 0.0000000
## 1894 0.0000000 0.0000000 0.0000000
## 1895 0.0000000 0.0000000 0.0000000
## 1896 0.0000000 0.0000000 0.0000000
## 1897 1.0000000 0.0000000 0.0000000
## 1898 0.0000000 0.0000000 0.0000000
## 1899 0.0000000 0.0000000 0.0000000
## 1900 0.0000000 0.0000000 0.0000000
## 1901 0.0000000 0.0000000 0.0000000
## 1902 0.0000000 0.0000000 1.0000000
## 1903 0.0000000 0.0000000 0.0000000
## 1904 0.0000000 0.0000000 0.0000000
## 1905 0.0000000 0.0000000 0.0000000
## 1906 0.0000000 0.0000000 0.0000000
## 1907 0.0000000 0.0000000 0.0000000
## 1908 0.0000000 0.0000000 0.0000000
## 1909 0.0000000 0.0000000 0.0000000
## 1910 0.0000000 0.4285714 0.0000000
## 1911 0.0000000 0.0000000 0.0000000
## 1912 0.0000000 0.0000000 1.0000000
## 1913 0.0000000 0.0000000 0.0000000

```

```
## 1914 0.0000000 0.0000000 0.0000000
```

3.3 Predict on the test data

```
knn_test_model <- kknk(formula, train = train_digitals, test = test_digitals, k = 30, kernel = 'rectangl  
print(length(knn_test_model$fitted.values))
```

```
## [1] 953
```

3.4 Confusion matrices and Misclassification errors for train data and test data

```
train_confusion <- table(train_digitals$V65, train_predictions)  
test_confusion <- table(test_digitals$V65, knn_test_model$fitted.values)  
test_error_rate <- 1 - sum(diag(test_confusion)) / sum(test_confusion)  
train_error_rate <- 1 - sum(diag(train_confusion)) / sum(train_confusion)  
# only observe the top 10 rows  
cat("Misclassification errors on train data:", train_error_rate, '\n')
```

```
## Misclassification errors on train data: 0.01880878
```

```
cat("train_confusion:")
```

```
## train_confusion:
```

```
table(train_digitals$V65[1:10], train_predictions[1:10])
```

```
##  
##      0 1 2 3 4 5 6 7 8 9  
## 0 1 0 0 0 0 0 0 0 0  
## 1 0 1 0 0 0 0 0 0 0  
## 2 0 0 0 0 0 0 0 0 0  
## 3 0 0 0 1 0 0 0 0 0  
## 4 0 0 0 0 2 0 0 0 0  
## 5 0 0 0 0 0 1 0 0 0  
## 6 0 0 0 0 0 0 0 0 0  
## 7 0 0 0 0 0 0 0 2 0  
## 8 0 0 0 0 0 0 0 0 1  
## 9 0 0 0 0 0 0 0 0 1
```

```
cat("Misclassification errors on test data:", test_error_rate, '\n')
```

```
## Misclassification errors on test data: 0.05981112
```

```
cat("test confusion:")
```

```
## test confusion:
```

```
table(test_digitals$V65[1:10], knn_test_model$fitted.values[1:10])
```

```
##
##      0 1 2 3 4 5 6 7 8 9
## 0 4 0 0 0 0 0 0 0 0
## 1 0 0 0 0 0 0 0 0 0
## 2 0 0 1 0 0 0 0 0 0
## 3 0 0 0 0 0 0 0 0 0
## 4 0 0 0 0 0 0 0 0 0
## 5 0 0 0 0 0 1 0 0 0
## 6 0 0 0 0 0 0 1 0 0
## 7 0 0 0 0 0 0 0 1 0
## 8 0 0 0 0 0 0 0 0 1
## 9 0 0 0 0 0 0 0 1 0
```

3.5 Filter 2 cases of digit “8” in the training data which were easiest to classify and 3 cases that were hardest to classify

```
# filter the digital '8'
library(dplyr)

train_predict <- data.frame(train_digitals$V65, train_predictions,knn_train_model$prob)
train_predict$max_prob <- apply(train_predict[,3:12], 1, max)

train_predict_8 <- train_predict[train_predict$train_digitals.V65 == 8,]
# do not change the index while sorting
train_predict_8 <- train_predict_8[order(train_predict_8$X8), , drop = FALSE]

# get the 3 cases that were hardest to classify
hardest_cases_for_8 <- train_predict_8 %>% head(3)
easy_cases_for_8 <- train_predict_8 %>% tail(2)
```

3.6 Analysis the difference of the hardest case and easiest cases

we can see on the heatmap that the hardest cases are more complex than the easiest cases. Dark-colored squares concentrated in the middle of the matrix while the easiest cases are more concentrated on the edges which looking more like the number 8.

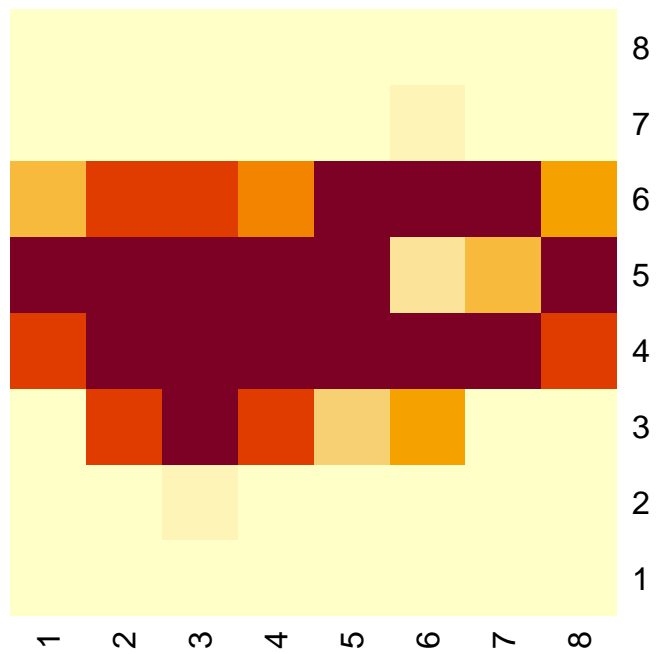
```
hardest_cases_index <- rownames(hardest_cases_for_8)
est_cases_index <- rownames(easy_cases_for_8)
# reindex the row index
row.names(train_digitals) <- NULL
full_hardest_cases <- train_digitals[hardest_cases_index,1:64]
full_est_cases <- train_digitals[est_cases_index,1:64]

hardest_matrixs <- lapply(1:nrow(full_hardest_cases), function(i) matrix(as.numeric(full_hardest_cases[i,]), 10, 10, drop = FALSE))
est_matrixs <- lapply(1:nrow(full_est_cases), function(i) matrix(as.numeric(full_est_cases[i,]), 10, 10, drop = FALSE))

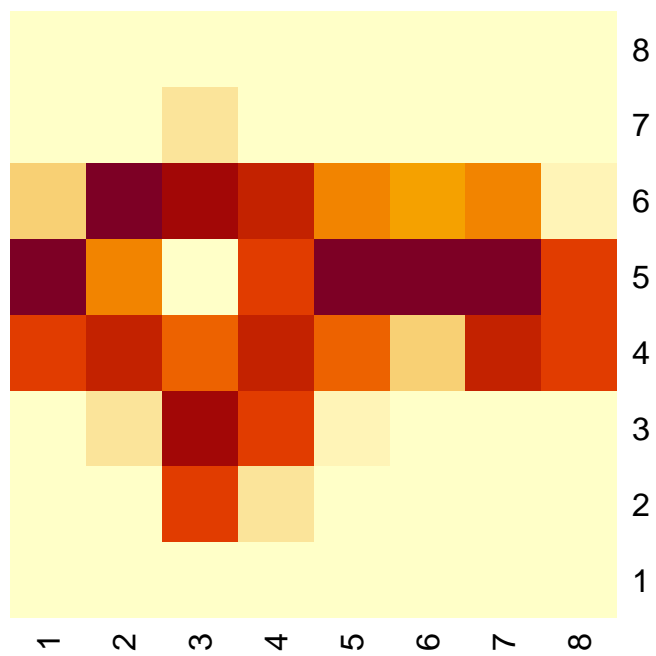
for (i in 1:length(hardest_matrixs)) {
  mat <- hardest_matrixs[[i]]
```

```
heatmap(mat, Colv = NA, Rowv = NA, scale = "none", main = paste("Hard Case", i))
}
```

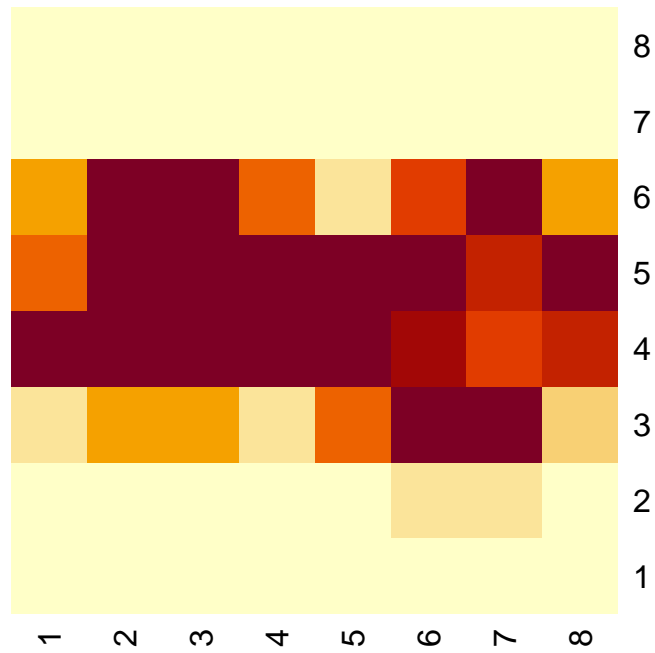
Hard Case 1



Hard Case 2

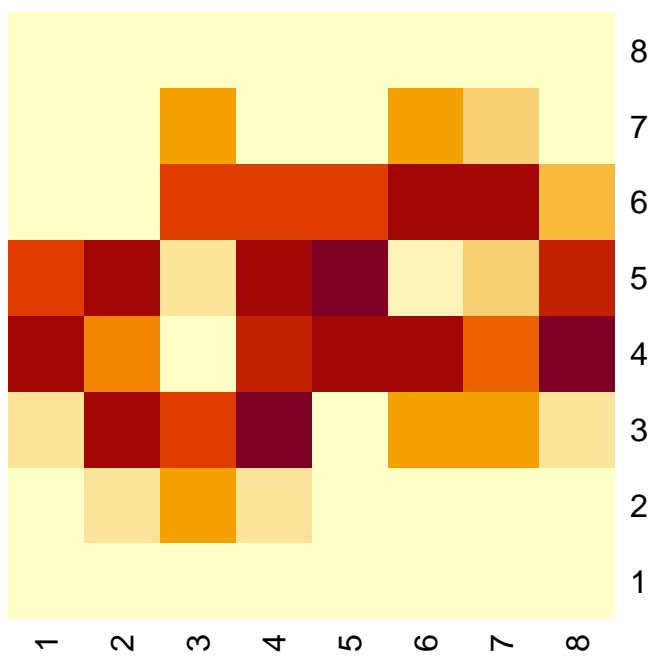


Hard Case 3

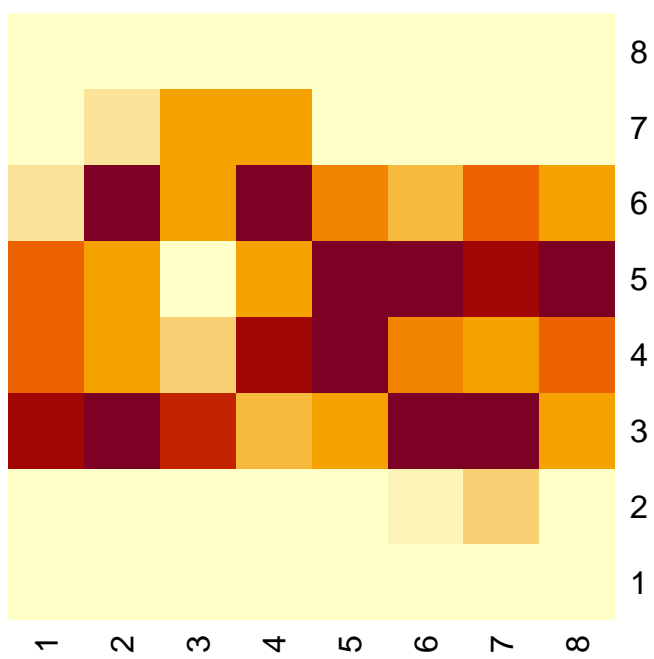


```
for (i in 1:length(est_matrixs)) {  
  mat <- est_matrixs[[i]]  
  heatmap(mat, Colv = NA, Rowv = NA, scale = "none", main = paste("Hard Case", i))  
}
```

Hard Case 1



Hard Case 2



3.7 Training via different k in on the training and validation data

according the plot , $k = 3$ is best value on training data and validation data, though the performance of $k = 1$ is better than $k = 3$ on training data, it is not the best value on validation data due to the weak generalization ability, but when we apply it on test data, its performance is not as good as predicted

```
library(ggplot2)
train_error_rates <- list()
valid_error_rates <- list()
test_error_rates <- list()

for (ki in 1:30) {
  # cat(paste("current k:",ki,"\n",sep=""))
  train_ki_model <- kknns(formula, train = train_digitals, test = train_digitals, k = ki, kernel = 'rectangular')
  valid_ki_model <- kknns(formula, train = train_digitals, test = valid_digitals, k = ki, kernel = 'rectangular')
  test_ki_model <- kknns(formula, train = train_digitals, test = test_digitals, k = ki, kernel = 'rectangular')

  train_confusion <- table(train_digitals$V65, train_ki_model$fitted.values)
  valid_confusion <- table(valid_digitals$V65, valid_ki_model$fitted.values)
  test_confusion <- table(test_digitals$V65, test_ki_model$fitted.values)

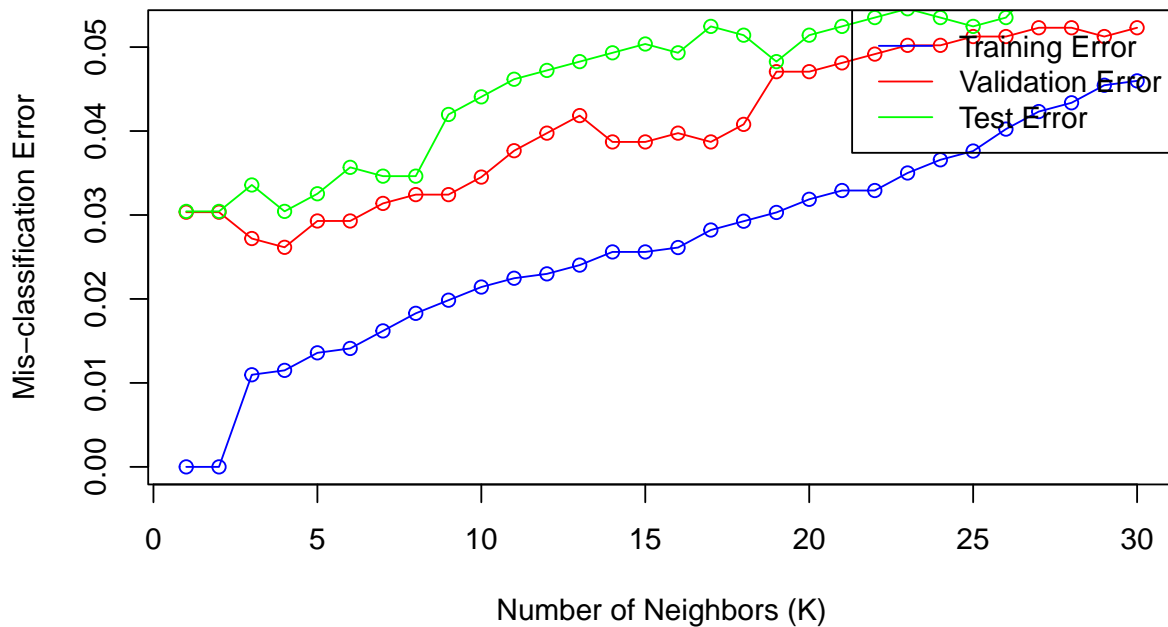
  train_error_rate <- sum(diag(train_confusion)) / sum(train_confusion)
  valid_error_rate <- sum(diag(valid_confusion)) / sum(valid_confusion)

  test_error_rate <- sum(diag(test_confusion)) / sum(test_confusion)

  # print(train_error_rate)
  # print(valid_error_rate)
  train_error_rates[[ki]] <- 1 - train_error_rate
  valid_error_rates[[ki]] <- 1 - valid_error_rate
  test_error_rates[[ki]] <- 1 - test_error_rate
}

plot(1:30, train_error_rates, type = "o", col = "blue", ylim = range(c(train_error_rates, valid_error_rates)),
     xlab = "Number of Neighbors (K)", ylab = "Mis-classification Error", main = "Training and Validation Error")
lines(1:30, valid_error_rates, type = "o", col = "red")
lines(1:30, test_error_rates, type = "o", col = "green")
legend("topright", legend = c("Training Error", "Validation Error", "Test Error"), col = c("blue", "red", "green"))
```

Training and Validation Errors



#

3.8 Change mis-classification error to cross-entropy

```
valid_cross_entropy_errors <- list()
train_cross_entropy_errors <- list()
test_cross_entropy_errors <- list()

for (ki in 1:30) {

  print(ki)
  valid_ki_model <- kknn(formula, train = train_digitals, test = valid_digitals, k = ki, kernel = 'rect')
  train_ki_model <- kknn(formula, train = train_digitals, test = train_digitals, k = ki, kernel = 'rect')
  test_ki_model <- kknn(formula, train = train_digitals, test = test_digitals, k = ki, kernel = 'rect')
  valid_probs <- valid_ki_model$prob
  train_probs <- train_ki_model$prob
  test_probs <- test_ki_model$prob

  valid_log_probs <- log(valid_probs + 1e-15) # Add small constant to avoid log(0)
  train_log_probs <- log(train_probs + 1e-15) # Add small constant to avoid log(0)
  test_log_probs <- log(test_probs + 1e-15) # Add small constant to avoid log(0)

  # -1 means do not contain intercept
  # One-hot encoding
  #This type of matrix is typically used in machine learning and statistical modeling for feature
  valid_correct_class <- model.matrix(~V65 - 1, data = valid_digitals) # One-hot encoding
```



```

train_correct_class <- model.matrix(~V65 - 1, data = train_digitals) # One-hot encoding
test_correct_class <- model.matrix(~V65 - 1, data = test_digitals) # One-hot encoding

valid_cross_entropy_errors[[ki]] <- -sum(valid_correct_class * valid_log_probs) / nrow(valid_digitals)
train_cross_entropy_errors[[ki]] <- -sum(train_correct_class * train_log_probs) / nrow(train_digitals)
test_cross_entropy_errors[[ki]] <- -sum(test_correct_class * test_log_probs) / nrow(test_digitals)
print(-sum(valid_correct_class * valid_log_probs) )
print(-sum(train_correct_class * train_log_probs))
print(-sum(test_correct_class * test_log_probs) )
}

```

```

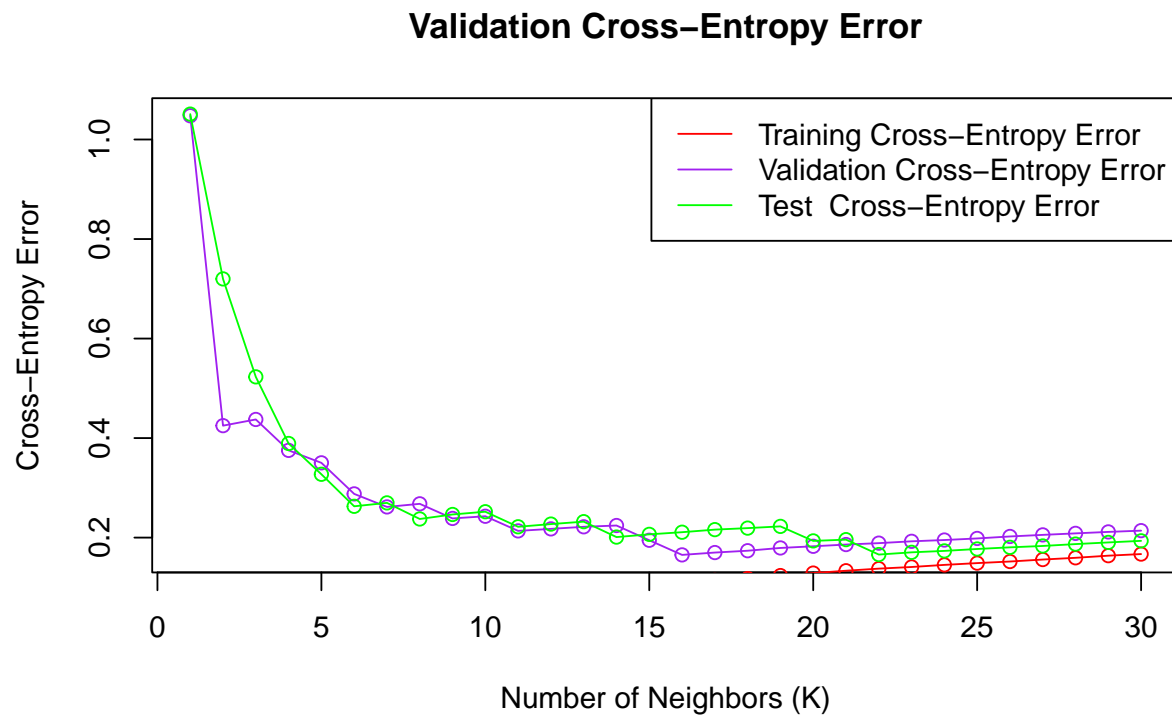
## [1] 1
## [1] 1001.625
## [1] -2.124967e-12
## [1] 1001.625
## [1] 2
## [1] 406.2661
## [1] 33.27106
## [1] 686.0421
## [1] 3
## [1] 418.1831
## [1] 59.73262
## [1] 498.4302
## [1] 4
## [1] 358.7783
## [1] 81.55162
## [1] 370.8495
## [1] 5
## [1] 334.8254
## [1] 95.51325
## [1] 311.8754
## [1] 6
## [1] 275.1721
## [1] 108.8384
## [1] 250.5404
## [1] 7
## [1] 250.1449
## [1] 115.3737
## [1] 257.104
## [1] 8
## [1] 256.0954
## [1] 127.5385
## [1] 226.2834
## [1] 9
## [1] 228.0128
## [1] 141.6817
## [1] 234.8888
## [1] 10
## [1] 232.234
## [1] 153.3003
## [1] 240.1743
## [1] 11
## [1] 204.1025

```

```
## [1] 163.4175
## [1] 211.306
## [1] 12
## [1] 207.9268
## [1] 172.1716
## [1] 216.4736
## [1] 13
## [1] 211.9284
## [1] 182.2941
## [1] 221.1315
## [1] 14
## [1] 214.4384
## [1] 193.1087
## [1] 191.5883
## [1] 15
## [1] 186.1193
## [1] 202.8563
## [1] 196.8141
## [1] 16
## [1] 158.0149
## [1] 210.2052
## [1] 200.9411
## [1] 17
## [1] 162.4651
## [1] 218.0311
## [1] 205.8701
## [1] 18
## [1] 165.9922
## [1] 225.1445
## [1] 208.752
## [1] 19
## [1] 171.3223
## [1] 236.7614
## [1] 212.0992
## [1] 20
## [1] 174.5003
## [1] 246.2878
## [1] 184.2784
## [1] 21
## [1] 177.8514
## [1] 255.3455
## [1] 186.6976
## [1] 22
## [1] 180.5634
## [1] 263.4285
## [1] 158.1037
## [1] 23
## [1] 184.0757
## [1] 269.7196
## [1] 162.3659
## [1] 24
## [1] 186.5343
## [1] 277.8804
## [1] 165.1231
```

```
## [1] 25
## [1] 189.6032
## [1] 284.666
## [1] 168.8127
## [1] 26
## [1] 193.3819
## [1] 290.7665
## [1] 171.958
## [1] 27
## [1] 196.4273
## [1] 298.4068
## [1] 174.5759
## [1] 28
## [1] 199.3273
## [1] 305.0539
## [1] 178.1607
## [1] 29
## [1] 202.1524
## [1] 313.2467
## [1] 181.3485
## [1] 30
## [1] 204.5686
## [1] 319.4817
## [1] 184.3878
```

```
# plot(1:30, train_error_rates, type = "o", col = "blue", ylim = range(c(train_error_rates, valid_error.
#   xlab = "Number of Neighbors (K)", ylab = "Mis-classification Error", main = "Training and Validati
# lines(1:30, valid_error_rates, type = "o", col = "red")
# lines(1:30, test_error_rates, type = "o", col = "green")
# legend("topright", legend = c("Training Error", "Validation Error", "Test Error"), col = c("blue", "re
plot(1:30, valid_cross_entropy_errors, type = "o", col = "purple",
  xlab = "Number of Neighbors (K)", ylab = "Cross-Entropy Error", main = "Validation Cross-Entropy Err
lines(1:30, train_cross_entropy_errors, type = "o", col = "red")
lines(1:30, test_cross_entropy_errors, type = "o", col = "green")
legend("topright", legend = c("Training Cross-Entropy Error", "Validation Cross-Entropy Error", "Test C
```



4 Assignment 2: Linear regression and ridge regression

4.1 set up

We need to download some useful packages before the start.

```
install.packages("caret")
```

```
## Warning: package 'caret' is in use and will not be installed
```

```
library(caret)
```

4.2 Prepare the dataset

Firstly, we read the file and divided the data into training and test data (60/40).

```
data <- read.csv("../data/parkinsons.csv") #
set.seed(42)
ini_sample<- sample(1:nrow(data),0.6*nrow(data))
train_data<- data[ini_sample,]
test_data<- data[-ini_sample,]
```

And then we scaled the dataset appropriately.

```
sacale_data<- train_data[,names(train_data)!="motor_UPDRS"]
scale_para<- preProcess(sacale_data)
train_data_scaled<- predict(scale_para,train_data)
test_data_scaled<- predict(scale_para,test_data)
train_data_scaled$motor_UPDRS <- train_data$motor_UPDRS
test_data_scaled$motor_UPDRS <- test_data$motor_UPDRS
```

4.3 Build models

Next, we computed a linear regression model , estimate training and test MSE

```
model<- lm(motor_UPDRS ~ .,train_data_scaled)
train_prediction<- predict(model,train_data_scaled)
train_mse<- mean((train_prediction - train_data_scaled$motor_UPDRS)^2)
test_prediction<- predict(model,test_data_scaled)
test_mse<- mean((test_prediction - test_data_scaled$motor_UPDRS)^2)
summary(model)
```

```
##
## Call:
## lm(formula = motor_UPDRS ~ ., data = train_data_scaled)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-8.4962	-1.3230	0.1978	1.6722	6.7627

```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	21.27888	0.04240	501.883	< 2e-16 ***
subject.	-0.12900	0.04908	-2.628	0.008618 **
age	-0.23517	0.04615	-5.095	3.66e-07 ***
sex	0.45948	0.05173	8.883	< 2e-16 ***
test_time	-0.05169	0.04293	-1.204	0.228664
total_UPDRS	7.81829	0.04892	159.827	< 2e-16 ***
Jitter...	1.48149	0.41073	3.607	0.000314 ***
Jitter.Abs.	-0.55937	0.11441	-4.889	1.06e-06 ***
Jitter.RAP	-49.61179	52.25757	-0.949	0.342498
Jitter.PPQ5	-0.31807	0.23637	-1.346	0.178500
Jitter.DDP	48.67488	52.25602	0.931	0.351675
Shimmer	1.00327	0.54793	1.831	0.067183 .
Shimmer.dB.	-0.06932	0.39046	-0.178	0.859095
Shimmer.APQ3	71.26529	209.14155	0.341	0.733311
Shimmer.APQ5	-1.36309	0.30045	-4.537	5.90e-06 ***
Shimmer.APQ11	0.57158	0.15977	3.577	0.000352 ***
Shimmer.DDA	-71.24366	209.14168	-0.341	0.733389
NHR	0.09299	0.12189	0.763	0.445542
HNR	0.16756	0.09855	1.700	0.089157 .
RPDE	-0.23042	0.06213	-3.709	0.000212 ***
DFA	-0.03420	0.05639	-0.606	0.544251
PPE	0.46026	0.09176	5.016	5.54e-07 ***

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 2.517 on 3503 degrees of freedom
## Multiple R-squared:  0.905, Adjusted R-squared:  0.9045
## F-statistic: 1590 on 21 and 3503 DF, p-value: < 2.2e-16
```

Implement 4 following functions:

loglikelihood function that for a given parameter vector theta and dispersion sigma.

```
logLikelihood <- function(theta, sigma, x, y) {
  n <- length(y)
  predictions <- x %*% theta
  residuals <- y - predictions
  log_likelihood <- -0.5 * n * log(2 * pi * sigma^2) - (t(residuals) %*% residuals) / (2 * sigma^2)
  return(as.numeric(log_likelihood))
}
```

Ridge function that for given vector theta, scalar sigma and scalar lambda and adds up a Ridge penalty to the minus loglikelihood.

```
ridge <- function(theta, sigma, lambda, x, y) {
  log_likelihood <- logLikelihood(theta, sigma, x, y)
  ridge_penalty <- lambda * sum(theta^2)
  return(-log_likelihood + ridge_penalty)
}
```

Use function optim() with method="BFGS" to find the optimal theta and sigma for the given lambda.

```
ridgeopt <- function(lambda, x, y) {
  n <- ncol(x)
  init_params <- c(rep(0, n), 1)
  ridge_obj <- function(params) {
    theta <- params[1:n]
    sigma <- params[n + 1]
    return(ridge(theta, sigma, lambda, x, y))
  }
  opt <- optim(init_params, ridge_obj, method = "BFGS")
  theta_opt <- opt$par[1:n]
  sigma_opt <- opt$par[n + 1]
  return(list(theta = theta_opt, sigma = sigma_opt))
}
```

computes the degrees of freedom of the Ridge model based on the training data.

```
freedom_degree <- function(lambda, x) {
  xT <- t(x) %*% x
  heat <- solve(xT + lambda * diag(ncol(x))) %*% t(x)
  df <- sum(diag(heat)) #trace
  return(df)
}
```

4.4 predict the values

Finally, we can compute optimal theta parameters for different lambda values by using function RidgeOpt.

```
train_data2 <- as.matrix(train_data[,names(train_data)!="motor_UPDRS"])
test_data2<- as.matrix(test_data[,names(test_data)!="motor_UPDRS"])
train_value <- train_data$motor_UPDRS
test_value <- test_data$motor_UPDRS

lambda_values <- c(1, 100, 1000)

train_mse2<- c()
test_mse2<- c()
df<- c()
theta_value<- list()
for (i in seq_along(lambda_values)){
  lambda<- lambda_values[i]
  ridgemodel<- ridgeopt(lambda,train_data2,train_value)
  thetavalue<- ridgemodel$theta

  theta_value[[i]]<- thetavalue

  train_predictions<- train_data2 %*% thetavalue
  train_mse2[i]<- mean((train_value - train_predictions)^2)

  test_predictions<- test_data2 %*% thetavalue
  test_mse2[i]<- mean((test_value - test_predictions)^2)

  df[i] <- freedom_degree(lambda,train_data2)

  result <- list(
    train_mse2 = train_mse2,
    test_mse2 = test_mse2,
    df = df,
    theta_value = theta_value
  )
}
print(result)

## $train_mse2
## [1] 6.465518 6.653863 6.846509
##
## $test_mse2
## [1] 6.387589 6.609421 6.787192
##
## $df
## [1] 0.009998311 0.001516241 0.000442187
##
## $theta_value
## $theta_value[[1]]
## [1] -0.0052580550 -0.0202829652 1.0515160348 -0.0008380227 0.7336342412
## [6] 0.0077671729 -0.0008418776 -0.0209940314 -0.0001519663 -0.0628711878
## [11] 0.0367333247 0.8557988044 -0.1154339829 -0.0815733362 0.3909625855
## [16] -0.3463559230 -0.2125478171 0.0539468078 -1.0994645885 -0.1441446539
```

```
## [21] 2.0815333869
##
## $theta_value[[2]]
## [1] 6.193772e-03 -8.526021e-03 3.650537e-01 -3.961347e-04 7.249791e-01
## [6] 2.022569e-03 7.405812e-05 1.225060e-03 1.374508e-03 2.701054e-03
## [11] 9.127526e-03 8.931548e-02 3.340734e-03 4.754327e-03 9.767899e-03
## [16] 9.350434e-03 1.924272e-02 2.616445e-02 -1.872273e-02 6.979124e-03
## [21] 4.345821e-02
##
## $theta_value[[3]]
## [1] 1.590115e-02 4.205629e-03 4.653460e-02 1.342374e-04 6.968982e-01
## [6] 2.437015e-04 1.712245e-05 1.013762e-04 1.472975e-04 3.740594e-04
## [11] 9.610700e-04 9.501445e-03 3.243690e-04 4.837515e-04 1.003988e-03
## [16] 1.009101e-03 2.221216e-03 1.972672e-02 -1.510650e-03 1.318646e-04
## [21] 4.337676e-03
```

In general, a lower test MSE indicates that the model generalizes better. Higher degrees of freedom mean that models are more flexible and tend to fit details in the data, but can lead to overfitting; Lower degrees of freedom mean that the model is smoother, limiting the fit to the training data.

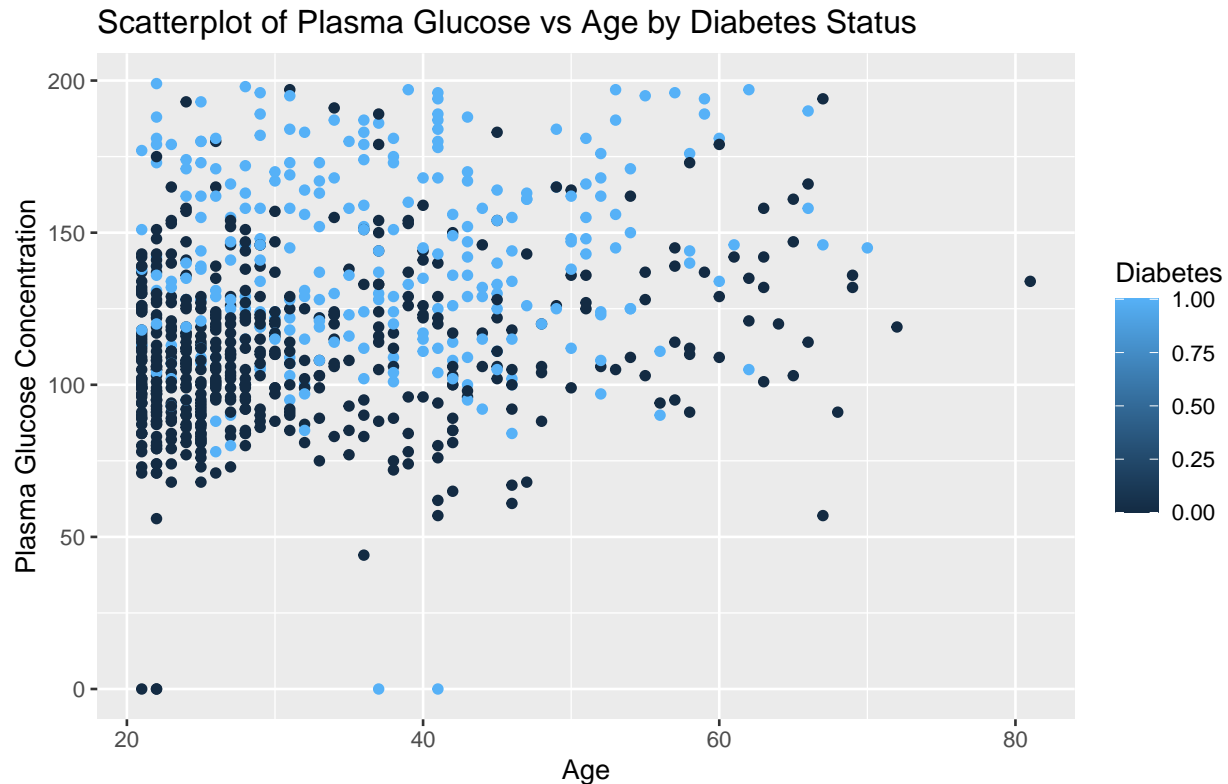
In this example, under penalty parameter equals to 1, the model's train_mse2 and test_mse2 are the lowest, and the degree of freedom is small but not too low. So it is the most appropriate parameter choice.

5 Assignment 3. Logistic regression and basis function expansion

5.1 Read Data and show scatter plot

read data and give a scatter plot showing a Plasma glucose concentration on Age where observations are colored by Diabetes levels

```
diabetes <- read.csv('../data/pima-indians-diabetes.csv', header = FALSE)
colnames(diabetes) <- c('Pregnancies', 'Plasma_glucose', 'blood_pressure', 'TricepsSkinFoldThickness', 'Serum_insulin', 'Diabetes_status')
#
ggplot(diabetes, aes( x = diabetes$Age, y = diabetes$Plasma_glucose, color = diabetes$Diabetes)) + geom_point()
labs(x = "Age", y = "Plasma Glucose Concentration", color = "Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by Diabetes Status")
```

5.2 Train a logistic regression model when the threshold $r = 0.5$

```
formula <- Diabetes ~ Age + Plasma_glucose
diabetes$Diabetes <- as.factor(diabetes$Diabetes)
gml_model <- caret::train(formula, data = diabetes, method = "glm", family = "binomial")
#type = "prob" predict probability
#type = "raw" predict the raw value/ class
#diabetes_pred <- predict(gml_model, type = "prob")

classify_pred_res <- function(r,gml_model) {

  diabetes_pred <- predict(gml_model, type = "prob")
  diabetes_pred$predict <- lapply(1:nrow(diabetes_pred), function(x) ifelse(diabetes_pred[x,2] > r, 1, 0))
  diabetes_pred$predict <- unlist(diabetes_pred$predict)
  diabetes_pred$raw <- diabetes$Diabetes
  diabetes_pred[, 3:4] <- lapply(diabetes_pred[, 3:4], as.factor)

  trainingData <- gml_model$trainingData %>% select(-.outcome)
  diabetes_pred <- cbind(diabetes_pred, trainingData)

  diabetes_pred$Age <- gml_model$trainingData$Age
  diabetes_pred$Plasma_glucose <- gml_model$trainingData$Plasma_glucose
  return(diabetes_pred)
}

diabetes_pred <- classify_pred_res(0.5,gml_model)
```

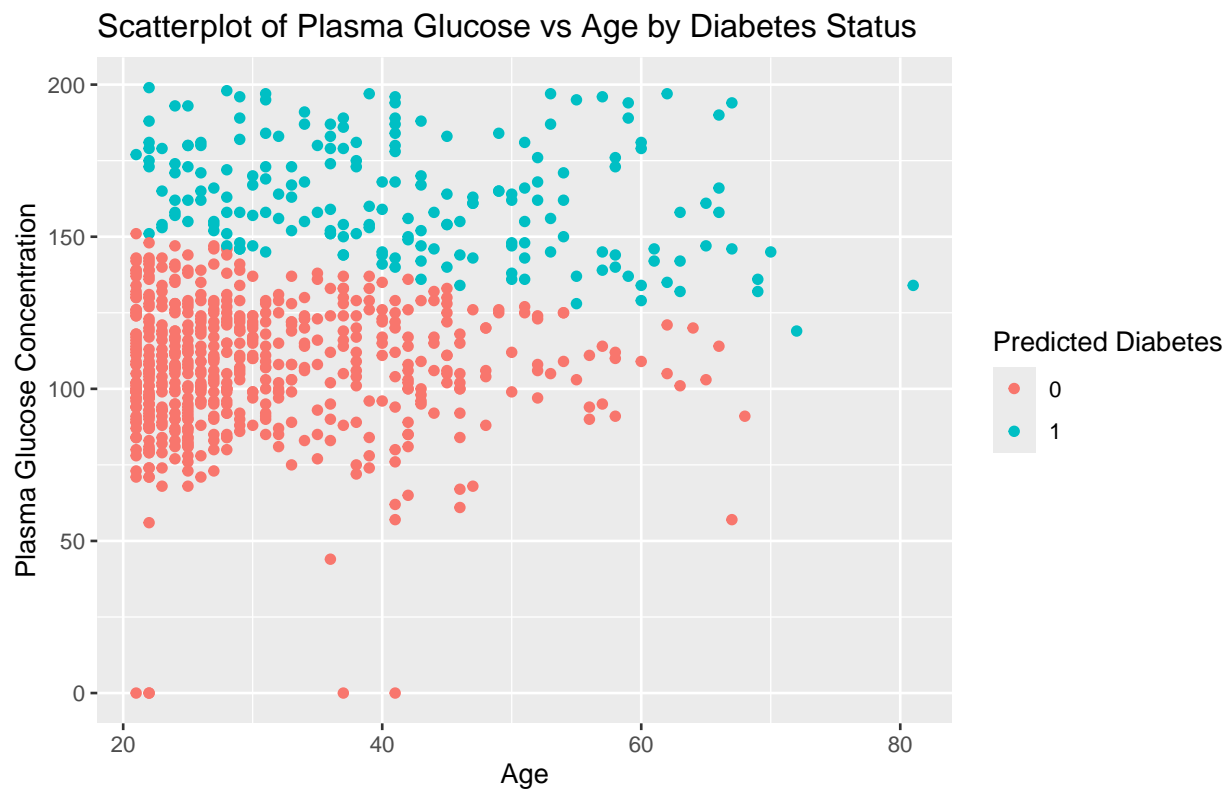
```
diabetes_confusion <- table(diabetes_pred$raw, diabetes_pred$predict)
error_rate <- 1 - (sum(diag(diabetes_confusion)) / sum(diabetes_confusion))
cat(" training misclassification error:",error_rate)
```

```
## training misclassification error: 0.2630208
```

5.3 Draw a scatter plot showing the predicted diabetes status

we can see that the logistic regression visually separates the two classes of diabetes status well, but the misclassification error is high due to the overlap of the two classes, maybe change can improve the performance. we will try later

```
ggplot(diabetes,aes( x = diabetes_pred$Age, y = diabetes_pred$Plasma_glucose, color = diabetes_pred$pre
labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by Diabetes Status")
```



5.4 Draw a decision boundary between the two predicted classes

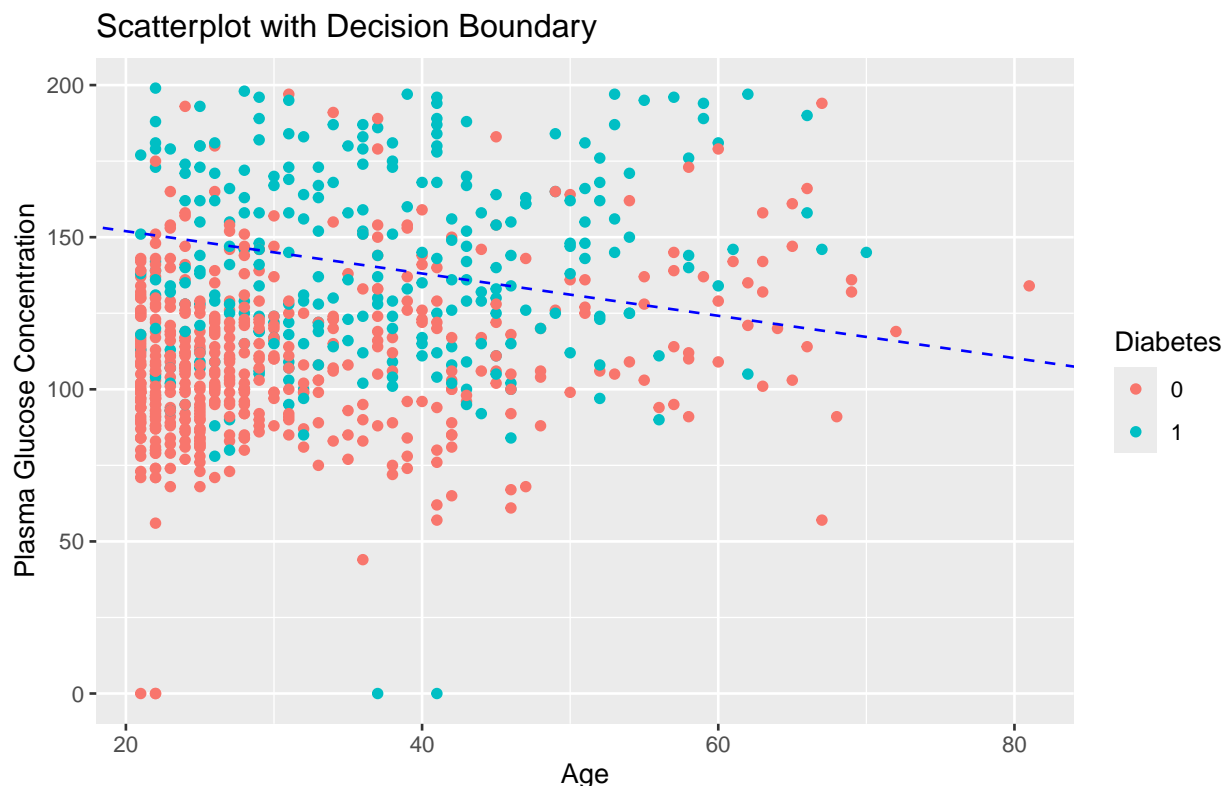
we can see that the boundary line try to split the dots into two classes and put the most the red dots below the line and the most blue dots above the line, but when the age exceed the 50, the performance of the model is not good. it seems that the number of red dot below the boundary line is same as the number above the line, it results the high misclassification error

```

get_boundary_line <- function(gml_model,r, y_name) {
  coefficients <- gml_model$finalModel$coefficients
  boundary_parameter <- list()
  coef_names <- names(coefficients)
  y_value <- coefficients[[y_name]]
  boundary_parameter$Intercept <- -(coefficients[['(Intercept)']] / y_value) - (log((1/r) - 1)/y_value)
  # boundary_parameter$intercept <- intercept
  for (name in coef_names){
    if (name != '(Intercept)'){
      boundary_parameter[name] <- -coefficients[[name]] / y_value
    }
  }
  return(boundary_parameter)
}

boundary_parameter <- get_boundary_line(gml_model,0.5,'Plasma_glucose')
ggplot(diabetes,aes( x = diabetes$Age, y = diabetes$Plasma_glucose, color = diabetes$Diabetes)) +
  geom_point()+
  geom_abline(slope = boundary_parameter$Age, intercept = boundary_parameter$Intercept, color = "blue",
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Diabetes") +
  ggtitle("Scatterplot with Decision Boundary")

```



5.5 Change the thresholds r to 0.2 , 0.8 to see the what happened

we can see that when $r = 0.2$, for the red dots , its TP is relatively high , but the Recall is low ,for the blue dots,its TP is lower than red dots, but the Recall is higher than red dots, it means that the model is

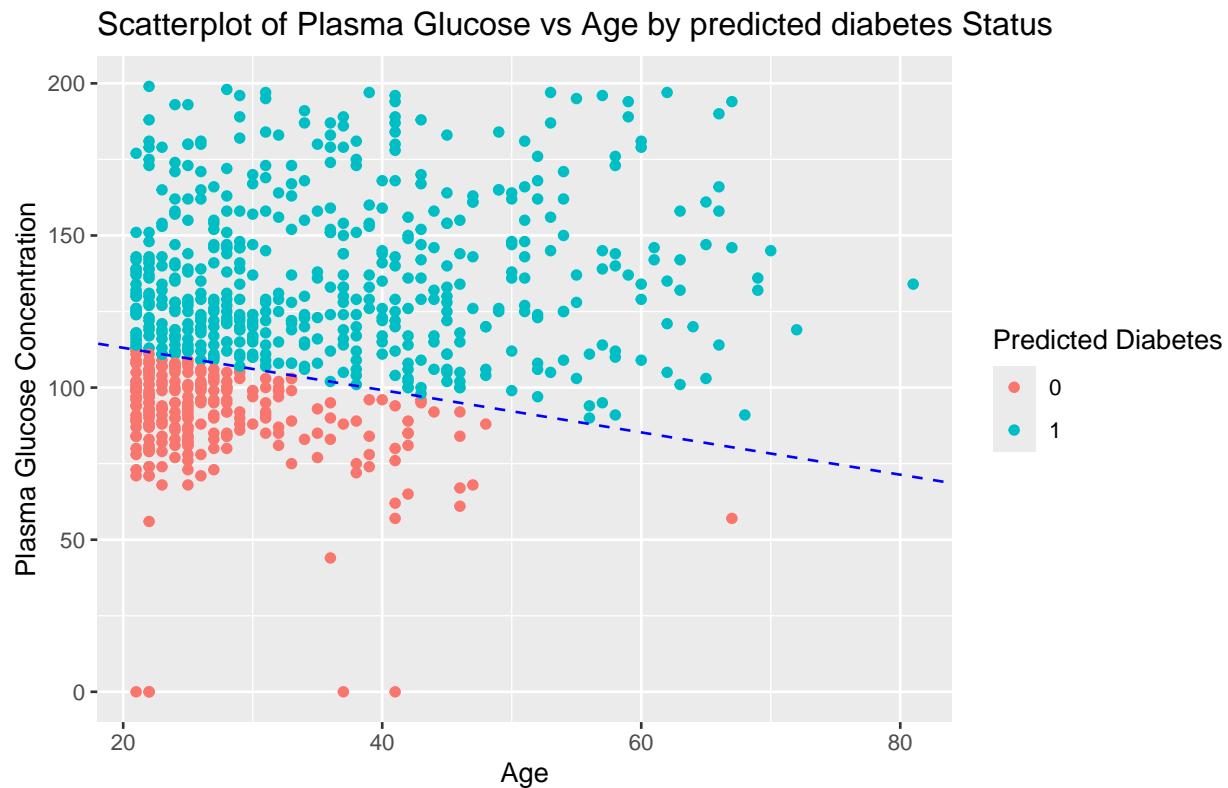
more likely to predict the blue dots as the positive class, but the blue dots are more likely to be the negative class, it results in the high misclassification error, when $r = 0.8$, the model is more likely to predict the red dots as the positive class, but the red dots are more likely to be the negative class, it results in the high misclassification error

```
pred_res_0.2 <- classify_pred_res(0.2,gml_model)
pred_res_0.8 <- classify_pred_res(0.8,gml_model)
```

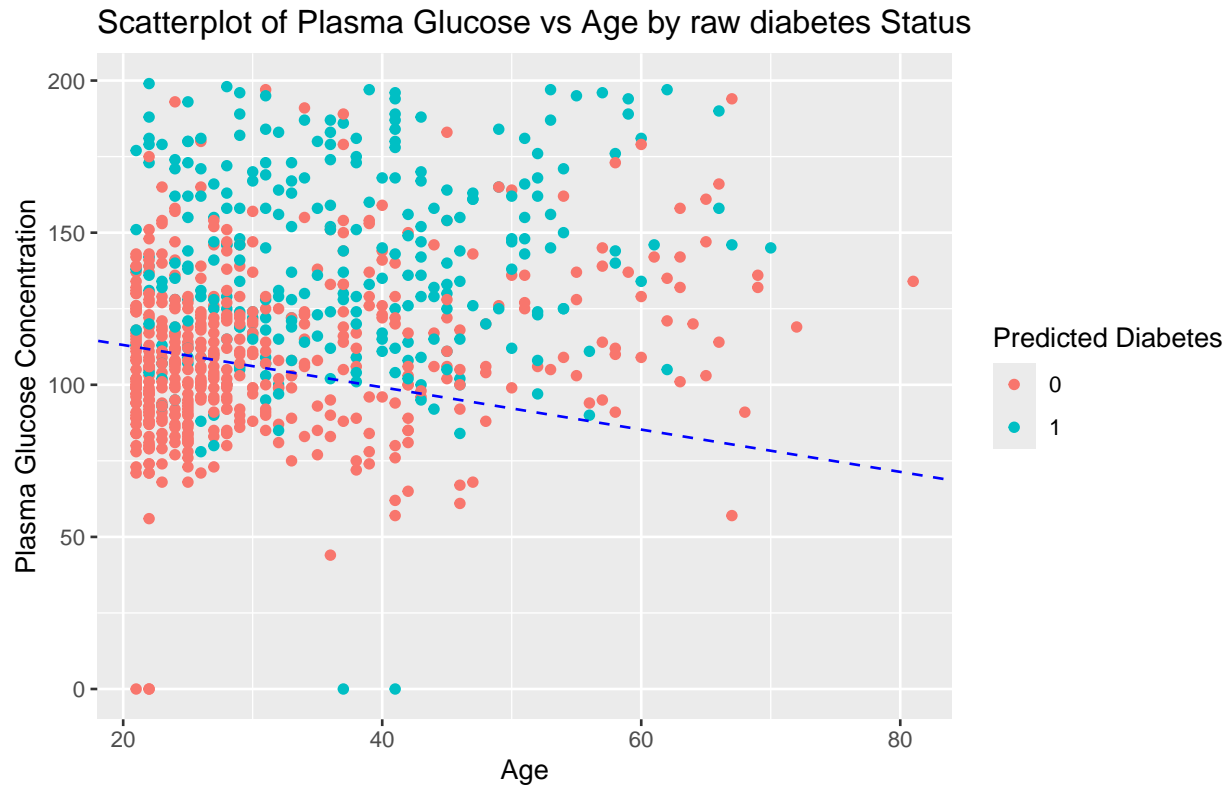
5.5.1 plot the scatter when $r = 0.2$

```
boundary_parameter_0.2 <- get_boundary_line(gml_model,0.2,'Plasma_glucose')

ggplot(diabetes,aes( x = pred_res_0.2$Age, y = pred_res_0.2$Plasma_glucose, color = pred_res_0.2$predicted_diabetes)) +
  geom_abline(slope = boundary_parameter_0.2$Age, intercept = boundary_parameter_0.2$Intercept, color = "blue") +
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
  ggtitle("Scatterplot of Plasma Glucose vs Age by predicted diabetes Status")
```



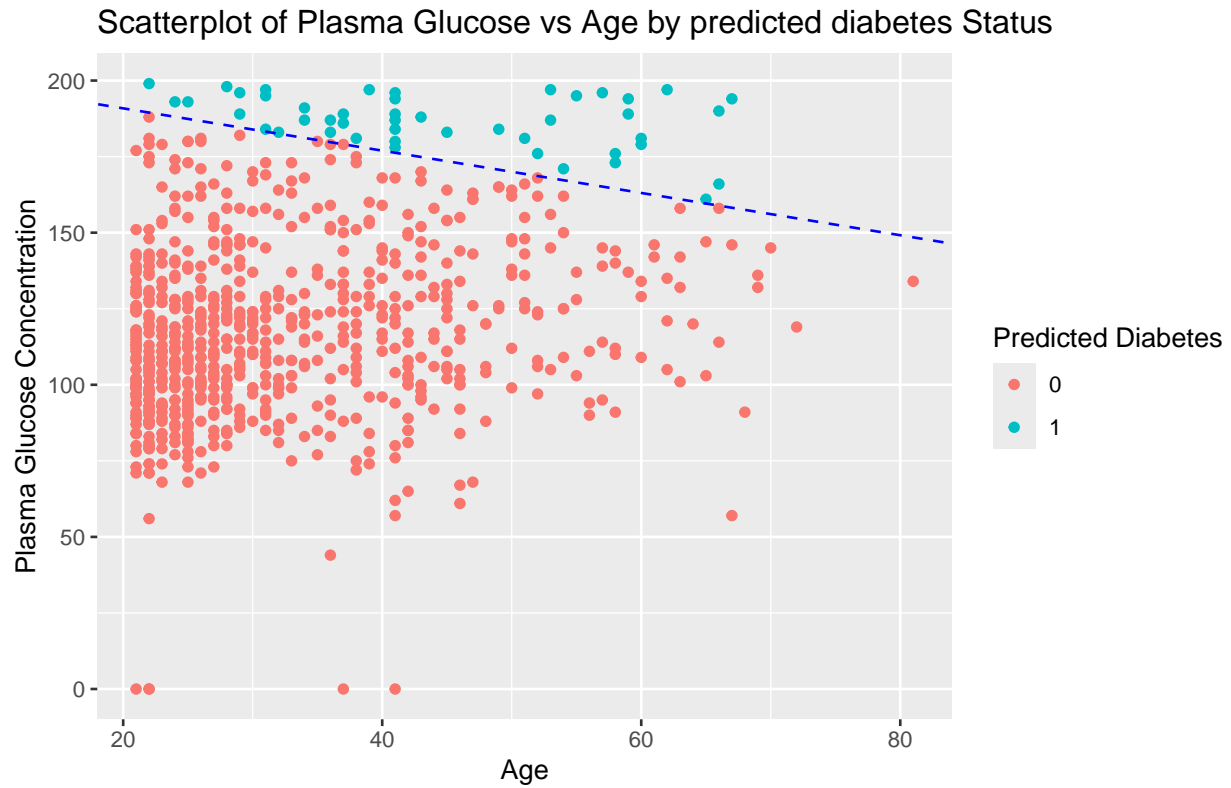
```
ggplot(diabetes,aes( x = pred_res_0.2$Age, y = pred_res_0.2$Plasma_glucose, color = pred_res_0.2$raw)) +
  geom_abline(slope = boundary_parameter_0.2$Age, intercept = boundary_parameter_0.2$Intercept, color = "blue") +
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
  ggtitle("Scatterplot of Plasma Glucose vs Age by raw diabetes Status")
```



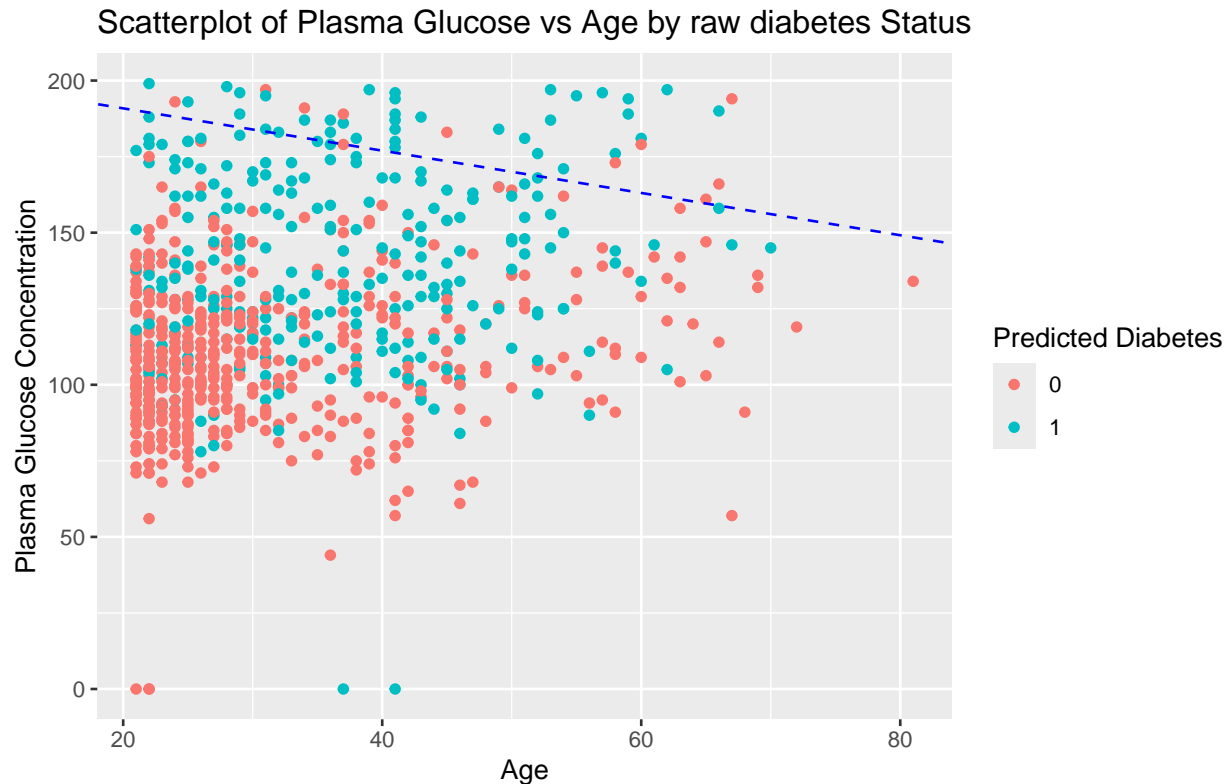
5.5.2 plot the scatter when $r = 0.8$

```
boundary_parameter_0.8 <- get_boundary_line(gml_model,0.8,'Plasma_glucose')

ggplot(diabetes,aes( x = pred_res_0.8$Age, y = pred_res_0.8$Plasma_glucose, color = pred_res_0.8$predicted_diabetes)) +
  geom_abline(slope = boundary_parameter_0.8$Age, intercept = boundary_parameter_0.8$Intercept, color = "blue") +
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
  ggtitle("Scatterplot of Plasma Glucose vs Age by predicted diabetes Status")
```



```
ggplot(diabetes,aes( x = pred_res_0.8$Age, y = pred_res_0.8$Plasma_glucose, color = pred_res_0.8$raw)) +
  geom_abline(slope = boundary_parameter_0.8$Age, intercept = boundary_parameter_0.8$Intercept, color = "blue") +
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
  ggtitle("Scatterplot of Plasma Glucose vs Age by raw diabetes Status")
```



5.5.3 Perform a basis function expansion trick

we can see that after add the basis function expansion, the misclassification error is lower than the previous model, it means that the basis function expansion can improve the performance of the model, look at the coefficients furtherly, the new added variables slightly affect the prediction, it means that the new added variables affect the prediction positively and the decision boundary become from a line to a multidimensional graphics

```
diabetes$z1 <- diabetes$Plasma_glucose^4
diabetes$z2 <- diabetes$Plasma_glucose^3 * diabetes$Age
diabetes$z3 <- diabetes$Plasma_glucose^2 * diabetes$Age^2
diabetes$z4 <- diabetes$Plasma_glucose * diabetes$Age^3
diabetes$z5 <- diabetes$Age^4
formula <- Diabetes ~ Age + Plasma_glucose + z1 + z2 + z3 + z4 + z5
new_gml_model <- caret::train(formula, data = diabetes, method = "glm", family = "binomial")
new_pred_res <- classify_pred_res(0.5,new_gml_model)
new_diabetes_confusion <- table(new_pred_res$raw, new_pred_res$predict)
error_rate <- 1 - (sum(diag(new_diabetes_confusion)) / sum(new_diabetes_confusion))
cat(" training misclassification error:",error_rate)
```

```
## training misclassification error: 0.2447917
```

```
new_boundary_parameter <- get_boundary_line(new_gml_model,0.5,'Plasma_glucose')
cat(new_gml_model$finalModel$coefficients)
```

```
## -9.309821 0.1456805 0.03793014 1.278015e-08 -1.7796e-07 8.51515e-07 -1.698011e-06 8.126623e-07
```

6 Assignment 4: Handwritten digit recognition with K-nearest neighbors

- Why can it be important to consider various probability thresholds in the classification problems, according to the book?

Probability thresholds serve as the reference point for evaluating performance of the model. Usually, a baseline is defined to indicate the model's worst performance level. And the achievable performance is defined by the maximum performance level. (Page 290 Baseline and Achievable Performance Level)

- What ways of collecting correct values of the target variable for the supervised learning problems are mentioned in the book?

In supervised learning problems, the target variables can be manually labelled by a domain expert. Target variables can also be labelled from predictive models based. Or the output is labelled naturally during the collection of training data. (Page 6, paragraph 2)

- How can one express the cost function of the linear regression in the matrix form, according to the book? The cost function for the linear regression model can be written with matrix notations as (Page 41):

$$J(\boldsymbol{\theta}) = \frac{1}{n} \sum_{i=1}^n (\hat{y}(x_i; \boldsymbol{\theta}) - y_i)^2 = \frac{1}{n} \|\hat{\mathbf{y}} - \mathbf{y}\|_2^2 = \frac{1}{n} \|\mathbf{X}\boldsymbol{\theta} - \mathbf{y}\|_2^2 = \frac{1}{n} \|\boldsymbol{\epsilon}\|_2^2$$