## Lab1

liume102@student.liu.se hanxi898@student.liu.se xiali125@student.liu.se

12 Nov 2024

### 1 Statement of Contribution

In Assignment 1, Xiaochen Liu was mainly responsible for code writing while Liuxi Mei was responsible for the analysis. Assignment 2 was mainly contributed by Han Xia. In assignment 3, Liuxi Mei was responsible for code writing while Han Xia was responsible for the analysis. Assignment 4 was mainly contributed by Xiaochen Liu and Liuxi Mei. Results from all assignments have been discussed afterwards between Liuxi Mei, Xiaochen Liu and Han Xia and the group report was created based on this discussion.

### 2 Introduction

This is the first lab in the Machine Learning In this lab, contains the following tasks:1. Handwritten digit recognition with K-nearest neighbors.2.Linear regression and ridge regression.3. Logistic regression and basis function expansion.4. Theory

# 3 Assignment 1: Handwritten digit recognition with K-nearest neighbors

#### 3.1 Load and check data

```
# Load packages
library('ggplot2') # visualization
library('ggthemes') # visualization

## Warning: package 'ggthemes' was built under R version 4.4.2

library('scales') # visualization
library('dplyr') # data manipulation
library('randomForest') # classification algorithm
```

## Warning: package 'randomForest' was built under R version 4.4.2

```
library('caret')
## Warning: package 'caret' was built under R version 4.4.2
Now that our packages are loaded and we divide it into training, validation and test sets (50\%/25\%/25\%)
# do not use StringAsFact = FALSE
digitals <- read.csv('../data/optdigits.csv',header = FALSE)</pre>
# change all the columns to factor
#digitals <- digitals %>% mutate_all(as.factor)
digitals$V65 <- as.factor(digitals$V65)</pre>
train_index <- createDataPartition(digitals$V65, p = 0.5, list = F)
train_digitals <- digitals[train_index,]</pre>
remainingData <- digitals[-train_index, ]</pre>
validationIndex <- createDataPartition(remainingData$V65, p = 0.5, list = FALSE)</pre>
valid_digitals <- remainingData[validationIndex, ]</pre>
test_digitals <- remainingData[-validationIndex, ]</pre>
cat("train length:", nrow(train digitals),'\n')
## train length: 1914
cat("test length:", nrow(valid_digitals),'\n')
## test length: 956
cat("valid length:", nrow(test_digitals),'\n')
## valid length: 953
```

## 3.2 KNN to fit classification model using train data

```
library(kknn)
formula <- V65~.
# if kenerl = 'rectangular' , so every point in the neighborhood is weighted equally
# both of the parameters of train and test use train_digital data
# if your predict columns is continuous, kknn will recognized as a regression task
# under this situation, you can not get a probability of the prediction
knn_train_model <- kknn(formula, train_digitals, train_digitals, kernel = 'rectangular',distance = 1,)
train_predictions <- fitted(knn_train_model)
print(length(train_predictions))

## [1] 1914

summary(knn_train_model)</pre>
```

```
##
## Call:
kknn(formula = formula, train = train digitals, test = train digitals,
                       distance = 1, kernel = "r
##
##
Response: "nominal"
##
  fit
       prob.1
          prob.2
             prob.3
                    prob.5
    prob.0
                 prob.4
                       prob.6
   ##
2
   ##
   ##
   ##
6
##
7
   ## 8
   ## 9
10
   ##
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
11
12
   ##
   ##
13
##
14
   ##
15
   9 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.1428571 0.0000000
##
16
   ## 17
   ##
18
   ##
19
20
   4 0.0000000 0.1428571 0.0000000 0.0000000 0.5714286 0.0000000 0.0000000
##
21
##
22
   23
   ##
##
24
   ##
25
   ##
26
   ##
27
   ##
28
29
   ##
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
30
##
31
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
32
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
33
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
34
   35
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
36
##
37
   8 0.0000000 0.2857143 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
   ##
38
##
39
   ##
40
##
41
   ##
42
##
43
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
44
   ##
45
##
46
   ## 47
   ## 48
```

```
## 49
  ##
50
##
51
  6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
  ##
52
##
53
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
54
##
  55
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 56
##
57
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
58
##
59
  ##
60
##
61
  ##
62
63
  ##
64
  ##
  65
##
  ##
66
  ##
67
##
68
  1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
##
69
  ##
70
  71
##
  ##
72
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
73
74
  ##
75
  ##
76
  ##
77
##
78
  ##
79
  ##
80
  81
  ##
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
82
  83
  ##
84
85
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ##
86
  ##
87
  88
##
  89
  ##
90
  ##
91
  ##
92
## 93
  9 0.0000000 0.1428571 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000
##
94
##
95
  ##
96
##
97
  1 0.0000000 0.4285714 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000
98
  ##
  ##
99
## 100
  1\ 0.0000000\ 0.5714286\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
## 101
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 102
```

```
## 103
  ## 104
## 105
  106
  ##
##
107
  ## 108
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 109
  ## 110
## 111
  ## 112
## 113
  ## 114
## 115
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 116
  ## 117
## 118
  ## 119
## 120
  ## 121
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
122
  ## 123
  ## 124
## 125
  ## 126
  ## 127
## 128
  129
  8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
##
130
  ## 131
## 132
  ## 133
  ## 134
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
135
136
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
137
  ## 138
## 139
  ## 140
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 141
  ## 142
  ## 143
  ##
144
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
145
  ##
146
## 147
  ## 148
## 149
  8 0.0000000 0.0000000 0.2857143 0.1428571 0.0000000 0.0000000 0.0000000
  ## 150
## 151
  152
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
153
## 154
  1 0.0000000 0.7142857 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 155
  3 0.0000000 0.0000000 0.0000000 0.5714286 0.0000000 0.1428571 0.0000000
## 156
```

```
## 157
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000
##
158
159
  160
  ##
##
161
  1\ 0.0000000\ 0.7142857\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.4285714 \ 0.0000000 \ 0.5714286 
## 162
  ## 163
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 164
## 165
  ## 166
167
  ##
168
##
169
  ## 170
  ## 171
  ## 172
  4 0.1428571 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000
  1\ 0.0000000\ 0.7142857\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
## 173
174
  ## 175
176
  ## 177
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 178
  ## 179
  ## 180
  ## 181
182
  183
  ##
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
184
  ##
185
## 186
  ## 187
  ##
188
  ##
189
  190
  ##
191
  ## 192
## 193
  ## 194
  ## 195
  ## 196
  197
198
  199
  200
##
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 201
## 202
  ## 203
  ## 204
205
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
206
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
207
## 208
  ## 209
  ## 210
```

```
## 211
  ## 212
## 213
  ## 214
## 215
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 216
  ## 217
  ## 218
## 219
  ## 220
221
  222
  1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
##
##
223
  ##
224
## 225
  226
  ##
227
228
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
229
  ##
230
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
231
  232
  ## 233
  2\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
  5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000
## 234
  ## 235
236
  237
  ##
##
238
  ##
239
## 240
  ## 241
  ##
242
  243
  ##
244
245
  ##
246
## 247
  ## 248
  ## 249
## 250
  9\ 0.0000000\ 0.0000000\ 0.0000000\ 0.1428571\ 0.0000000\ 0.0000000\ 0.0000000
  8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
251
252
  5 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.5714286 0.0000000
##
  ##
253
  ##
254
  255
  ## 256
## 257
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
258
##
259
  260
  ##
  ##
261
## 262
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 263
  ## 264
```

```
## 265
   266
267
   268
   ##
269
   5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.4285714 0.0000000
## 270
   ## 271
   ## 272
## 273
   ## 274
275
   276
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
##
277
   ## 278
## 279
   280
   ##
   ##
281
282
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
283
   4 0.0000000 0.1428571 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000
##
284
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
285
   286
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 287
   288
   ## 289
290
   291
   ##
   9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
##
292
   ##
293
## 294
   ## 295
   ##
296
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
297
   9 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.4285714 0.0000000
   2\ 0.0000000\ 0.4285714\ 0.5714286\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
##
298
299
   4 0.0000000 0.1428571 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000
   ##
300
## 301
   ## 302
   303
   ## 304
   305
306
   ##
   ##
 307
   4 0.0000000 0.2857143 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
##
308
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 309
   ## 310
## 311
   ## 312
##
313
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
314
   ##
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
315
## 316
   ## 317
   ## 318
```

```
## 319
  ## 320
321
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  322
##
##
323
  324
##
  325
  ## 326
327
  328
329
  330
  ##
##
331
  ##
332
333
  ##
334
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
  4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
##
335
336
  337
  ##
338
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
339
  340
  ## 341
  342
  ## 343
344
  345
  ##
  ##
346
  1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
##
347
348
  ##
349
  ##
350
  ##
351
  352
  ##
353
  354
  ##
355
  1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
356
  ##
357
  358
  ##
  359
360
  ##
  ##
361
  ##
362
363
  ##
364
##
365
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000
##
366
##
367
  368
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
369
## 370
  ## 371
  ## 372
```

```
## 373
  374
375
  376
  ##
377
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
  378
##
  379
  ## 380
381
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
382
383
  ##
384
##
385
  2 0.0000000 0.0000000 0.8571429 0.1428571 0.0000000 0.0000000 0.0000000
##
386
387
  ##
388
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
##
389
390
  391
  ##
392
  ##
393
  394
  ## 395
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
396
  ## 397
398
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
399
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
  ##
400
  ##
401
## 402
  ## 403
  ## 404
  405
  ##
406
407
  ##
408
## 409
  ## 410
  ## 411
  ## 412
  ## 413
  ## 414
  ## 415
  ## 416
  ## 417
  9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 418
## 419
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 420
## 421
  ## 422
  ## 423
## 424
  ## 425
  ## 426
```

```
## 427
   8 0.0000000 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000 0.0000000
   ## 428
429
   6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
430
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
##
431
   1\ 0.0000000\ 0.5714286\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
432
##
   ## 433
   3 0.0000000 0.4285714 0.0000000 0.5714286 0.0000000 0.0000000 0.0000000
## 434
## 435
   ## 436
## 437
   438
   1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
##
##
 439
   ##
 440
   1\ 0.0000000\ 0.8571429\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
## 441
## 442
   ## 443
444
   ## 445
446
   ##
447
   448
   8 0.1428571 0.1428571 0.0000000 0.0000000 0.0000000 0.1428571 0.1428571
## 449
   ## 450
   ## 451
452
   453
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
##
 454
   ##
 455
## 456
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 457
   ##
458
   ##
 459
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
460
   461
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000
##
462
463
   ## 464
   ## 465
   ## 466
   467
   ##
 468
   ##
 469
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
470
## 471
   ## 472
   ## 473
   3 0.0000000 0.1428571 0.1428571 0.7142857 0.0000000 0.0000000 0.0000000
   ## 474
## 475
   ## 476
   ## 477
## 478
   ## 479
   ## 480
```

```
## 481
  ##
482
483
  484
##
##
485
  486
##
  487
  ## 488
## 489
  ## 490
## 491
  492
  ##
##
493
  ##
494
## 495
  5 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.7142857 0.0000000
## 496
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 497
498
  ## 499
## 500
  ##
501
  ## 502
  ## 503
  ## 504
  ## 505
506
  507
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
  ##
508
  ## 509
## 510
  ## 511
  ## 512
  ## 513
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 514
## 515
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 516
## 517
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 518
  ## 519
  ## 520
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 521
## 522
  ## 523
  ## 524
  ## 525
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 526
## 527
  ## 528
## 529
  530
  ## 531
## 532
  ## 533
  ## 534
```

```
## 535
  ## 536
537
  538
##
##
539
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 540
  ## 541
  ## 542
## 543
  ## 544
## 545
  ##
546
##
547
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 548
## 549
  ## 550
  1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 551
552
  ##
553
554
  ##
555
  556
  ## 557
  ## 558
  ## 559
## 560
  ##
561
  ##
562
  ## 563
## 564
  ## 565
  ## 566
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
567
  ##
568
569
  ## 570
## 571
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 572
  ## 573
  ## 574
  ## 575
## 576
  ##
577
  ##
578
  ## 579
  ## 580
## 581
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
  ## 582
583
  584
  ##
585
## 586
  ## 587
  ## 588
```

```
## 589
   ## 590
591
   8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
   ## 592
##
 593
   594
##
   595
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 596
## 597
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ##
598
 599
   600
   ##
##
 601
   ##
 602
## 603
   604
   1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
   ## 605
 606
   5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.4285714 0.0000000
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
607
 608
   ##
 609
   ## 610
   ## 611
   612
   ## 613
## 614
   ## 615
   ##
 616
   1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
## 617
## 618
   ## 619
   3 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.2857143 0.0000000
## 620
   ##
621
   9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
622
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
##
 623
   ##
624
## 625
   6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
## 626
   ## 627
   ## 628
   629
630
   ##
   ##
 631
   ##
632
   ## 633
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 634
## 635
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 636
##
637
   638
   ##
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
 639
## 640
   ## 641
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.2857143 0.2857143
   ## 642
```

```
## 643
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000
##
644
645
  646
##
##
647
  648
##
  8 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 649
   ## 650
##
651
  ##
652
653
   ##
654
##
655
  ##
656
657
   ##
658
  ##
659
660
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
  ##
661
##
662
  ##
663
  5 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.7142857 0.0000000
  664
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 665
  ##
666
  ## 667
668
  ##
669
   ##
670
   ##
671
## 672
   ## 673
  ##
674
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
##
675
  5 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.7142857 0.0000000
676
  ##
677
  ##
678
679
  ## 680
  681
  ##
  ##
682
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
683
684
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.1428571 0.0000000
##
  ##
685
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
686
##
  687
  ## 688
##
689
  ## 690
## 691
  692
   ##
   ##
693
##
694
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 695
  ## 696
```

```
## 697
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
698
699
  700
##
##
701
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
  702
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
703
  ## 704
705
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
706
707
  708
  ##
##
709
  ## 710
## 711
  ## 712
  ## 713
714
  ##
715
##
716
  ##
717
  ## 718
  ## 719
  720
  ## 721
722
  723
  ##
  ##
724
725
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
726
  ## 727
  ##
728
  ##
729
730
  ##
731
  ##
732
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
## 733
  6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
## 734
  ## 735
  ## 736
  8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
737
738
  ##
  ##
739
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
740
##
  ## 741
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 742
  ##
743
  ## 744
##
745
  2 0.0000000 0.0000000 0.8571429 0.1428571 0.0000000 0.0000000 0.0000000
746
  ##
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
747
## 748
  ## 749
  ## 750
```

```
## 751
752
 753
 754
##
##
755
 756
##
 757
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 758
759
 ##
760
761
 2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
762
 ##
##
763
 ##
764
## 765
 766
 ##
 ##
767
768
 769
 ##
##
770
 ##
771
 772
 ## 773
 774
 ## 775
776
 777
 ##
 ##
778
 3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
779
##
 9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 780
## 781
 ##
782
 ##
783
784
 ##
785
 786
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
787
 ## 788
 789
 ## 790
 791
792
 ##
 793
 ##
794
 795
 ## 796
 2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
797
 ##
798
799
 800
##
 ##
801
## 802
 ## 803
 ## 804
```

```
## 805
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 806
807
  ## 808
##
809
  ## 810
  ## 811
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 812
## 813
  ## 814
## 815
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 816
##
817
  ## 818
## 819
  ## 820
  ## 821
822
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
823
  ##
824
  ##
825
  ## 826
  ## 827
  ## 828
  ## 829
830
  831
  ##
  ##
832
## 833
  ## 834
  ## 835
  ##
836
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
837
838
  ##
839
  ##
840
## 841
  ## 842
  ## 843
  ## 844
  845
  ##
846
  847
  4 0.1428571 0.1428571 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
##
848
  ## 849
  ## 850
## 851
  ## 852
## 853
  854
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ##
855
856
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 857
  ## 858
```

```
## 859
   ##
860
861
   862
   ##
##
863
   864
##
   865
   ## 866
867
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
868
869
   ##
870
##
871
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 872
## 873
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 874
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
##
875
876
   ##
877
878
   ##
879
   880
   ## 881
   882
   ## 883
884
   885
   ##
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
 886
   ##
887
888
   ## 889
   ##
890
   ##
891
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
##
892
893
   ##
894
895
   ## 896
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 897
   9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
   ## 898
   899
900
   ##
   ##
901
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
902
## 903
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   8 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 904
## 905
   3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000 0.0000000
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 906
## 907
   908
   ##
909
## 910
   8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 911
   ## 912
```

```
## 913
  ## 914
## 915
  ## 916
  1 0.0000000 0.4285714 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000
## 917
  ## 918
  ## 919
  ## 920
## 921
  5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.5714286 0.0000000
## 922
923
  924
  ##
##
925
  ## 926
  ## 927
  ## 928
  3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.1428571 0.0000000
  ## 929
930
  ## 931
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
932
  ##
933
  ## 934
  ## 935
  ## 936
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.1428571 0.0000000
## 937
938
  939
  ##
  ##
940
  ## 941
## 942
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 943
  ##
944
  945
  ##
946
947
  ## 948
## 949
  ## 950
  ## 951
  ## 952
  953
  ##
954
  955
  ##
956
  ## 957
  ## 958
## 959
  ## 960
## 961
  962
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
##
  ##
963
## 964
  ## 965
  ## 966
```

```
## 967
 ## 968
## 969
 1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
 ## 970
## 971
 ## 972
 ## 973
 ## 974
## 975
  6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 976
## 977
 ## 978
 ##
979
 ## 980
## 981
 ## 982
 ##
983
984
 985
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
986
 ##
987
 988
 ## 989
 ## 990
 ## 991
992
 993
 994
 995
## 996
 ## 997
 ## 998
 ## 999
1000
 1001
 ## 1002
 ## 1003
 ## 1004
 ## 1005
 ## 1006
1007
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1008
 1009
 ## 1010
 ## 1011
## 1012
 ## 1013
 ## 1014
## 1015
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1016
 ## 1017
## 1018
 ## 1019
 ## 1020
 2 0.0000000 0.0000000 0.8571429 0.1428571 0.0000000 0.0000000 0.0000000
```

```
## 1021
  ## 1022
  ## 1023
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 1024
  1025
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1026
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1027
  ## 1028
## 1029
  ## 1030
## 1031
  1032
  1033
  ## 1034
## 1035
  ## 1036
  4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
## 1037
## 1038
  ## 1039
  1040
  ## 1041
  ## 1042
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.1428571 0.0000000
## 1043
  ## 1044
  ## 1045
## 1046
  1047
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  9 0.0000000 0.2857143 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
1048
  ## 1049
## 1050
  ## 1051
  ## 1052
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1053
1054
  1055
  ## 1056
  ## 1057
  ## 1058
  ## 1059
  ## 1060
## 1061
  ## 1062
  1063
  1064
  ## 1065
  ## 1066
  ## 1067
  ## 1068
## 1069
  1070
  ## 1071
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1072
  ## 1073
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1074
```

```
## 1075
   ## 1076
## 1077
   ## 1078
1079
   ## 1080
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1081
   ## 1082
## 1083
   ## 1084
## 1085
   1086
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1087
   ## 1088
## 1089
   1\ 0.0000000\ 0.8571429\ 0.0000000\ 0.1428571\ 0.0000000\ 0.0000000\ 0.0000000
## 1090
   ## 1091
   ## 1092
   ## 1093
   1094
   ## 1095
   ## 1096
   ## 1097
   ## 1098
   ## 1099
## 1100
   ## 1101
   ## 1102
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1103
   ## 1104
## 1105
   ## 1106
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1107
## 1108
   ## 1109
   ## 1110
## 1111
   ## 1112
   ## 1113
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1114
   ## 1115
   ## 1116
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1117
   ## 1118
   4 0.0000000 0.2857143 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000
## 1119
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1120
   ## 1121
   ## 1122
## 1123
   ## 1124
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1125
## 1126
   8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 1127
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1128
```

```
## 1129
   ## 1130
## 1131
   ## 1132
## 1133
   ## 1134
   ## 1135
   ## 1136
## 1137
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1138
## 1139
   ## 1140
   ## 1141
   ## 1142
## 1143
   ## 1144
   ## 1145
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 1146
   ## 1147
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.2857143 0.0000000
## 1148
   ## 1149
   ## 1150
   ## 1151
   ## 1152
   4 0.2857143 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.2857143
## 1153
## 1154
   5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000
## 1155
   ## 1156
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1157
## 1158
   ## 1159
   ## 1160
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
   ## 1161
## 1162
   ## 1163
   ## 1164
   ## 1165
   ## 1166
   ## 1167
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1168
   ## 1169
## 1170
   3 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1171
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1172
   ## 1173
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1174
   ## 1175
   ## 1176
## 1177
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1178
   3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000 0.0000000
## 1179
## 1180
   ## 1181
   3 0.0000000 0.0000000 0.1428571 0.5714286 0.0000000 0.0000000 0.0000000
   ## 1182
```

```
## 1183
 ## 1184
## 1185
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1186
## 1187
 ## 1188
 ## 1189
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1190
## 1191
 9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
 ## 1192
## 1193
 ## 1194
 ## 1195
 ## 1196
## 1197
 ## 1198
 ## 1199
## 1200
 ## 1201
 ## 1202
 6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
## 1203
 ## 1204
 ## 1205
 ## 1206
 ## 1207
## 1208
 ## 1209
 ## 1210
 ## 1211
## 1212
 ## 1213
 ## 1214
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1215
## 1216
 ## 1217
 ## 1218
## 1219
 ## 1220
 ## 1221
 ## 1222
 ## 1223
## 1224
 ## 1225
 ## 1226
 ## 1227
 ## 1228
 ## 1229
 ## 1230
## 1231
 ## 1232
 ## 1233
## 1234
 ## 1235
 ## 1236
```

```
## 1237
 ## 1238
## 1239
 ## 1240
 1241
 ## 1242
 ## 1243
 ## 1244
## 1245
 ## 1246
## 1247
 ## 1248
 ## 1249
 ## 1250
## 1251
 ## 1252
 ## 1253
 ## 1254
 ## 1255
 1256
 ## 1257
 ## 1258
 ## 1259
 ## 1260
 ## 1261
## 1262
 ## 1263
 1264
## 1265
 ## 1266
 ## 1267
 ## 1268
 ## 1269
 ## 1270
 1271
 ## 1272
 ## 1273
 ## 1274
 ## 1275
 ## 1276
 ## 1277
## 1278
 ## 1279
 ## 1280
 ## 1281
 ## 1282
 2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1283
 ## 1284
## 1285
 1286
 ## 1287
## 1288
 ## 1289
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1290
```

```
## 1291
  5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000
  ## 1292
## 1293
  ## 1294
  ## 1295
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1296
  ## 1297
  ## 1298
## 1299
  4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
## 1300
## 1301
  1302
  1303
  ## 1304
## 1305
  ## 1306
  ## 1307
  ## 1308
  ## 1309
  ## 1310
  ## 1311
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1312
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1313
  ## 1314
  ## 1315
## 1316
  ## 1317
  ## 1318
  ## 1319
## 1320
  ## 1321
  ## 1322
  ## 1323
## 1324
  1325
  ## 1326
  ## 1327
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 1328
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1329
  ## 1330
## 1331
  ## 1332
  ## 1333
  ## 1334
  ## 1335
  ## 1336
  ## 1337
  ## 1338
## 1339
  1340
  ## 1341
  ## 1342
  ## 1343
  ## 1344
```

```
## 1345
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1346
## 1347
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1348
  1349
  ## 1350
  ## 1351
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1352
## 1353
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 1354
## 1355
  1356
  1357
  ## 1358
## 1359
  ## 1360
  ## 1361
## 1362
  1363
  1364
  9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.1428571 0.0000000
## 1365
  ## 1366
  ## 1367
  ## 1368
  ## 1369
## 1370
  ## 1371
  1372
  ## 1373
## 1374
  ## 1375
  ## 1376
  ## 1377
## 1378
  4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
1379
  ## 1380
  ## 1381
  ## 1382
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1383
  ## 1384
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1385
## 1386
  1387
  1388
  ## 1389
  ## 1390
  ## 1391
  ## 1392
## 1393
  1394
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1395
## 1396
  ## 1397
  9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 1398
```

```
## 1399
   8 0.0000000 0.2857143 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
   ## 1400
## 1401
   ## 1402
   1403
   ## 1404
   ## 1405
   ## 1406
## 1407
   5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.8571429 0.0000000
   ## 1408
## 1409
   3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.2857143 0.0000000
   ## 1410
## 1411
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1412
## 1413
   ## 1414
   ## 1415
## 1416
   ## 1417
   ## 1418
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1419
   ## 1420
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1421
   6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1422
   ## 1423
## 1424
   ## 1425
   9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
   ## 1426
   9 0.0000000 0.0000000 0.1428571 0.1428571 0.0000000 0.0000000 0.0000000
## 1427
## 1428
   ## 1429
   ## 1430
   ## 1431
   ## 1432
   1433
   ## 1434
## 1435
   ## 1436
   ## 1437
   ## 1438
   ## 1439
## 1440
   ## 1441
   ## 1442
   ## 1443
   ## 1444
## 1445
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
   ## 1446
## 1447
   1448
   ## 1449
## 1450
   8\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.1428571\ 0.0000000
## 1451
   ## 1452
```

```
## 1453
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1454
## 1455
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
  ## 1456
1457
  ## 1458
  ## 1459
  ## 1460
## 1461
  ## 1462
## 1463
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1464
  ## 1465
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1466
## 1467
  ## 1468
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1469
## 1470
  ## 1471
  ## 1472
  ## 1473
  ## 1474
  ## 1475
  ## 1476
  ## 1477
## 1478
  ## 1479
  2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1480
  ## 1481
## 1482
  ## 1483
  ## 1484
  ## 1485
## 1486
  1\ 0.0000000\ 0.8571429\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
1487
  ## 1488
## 1489
  ## 1490
  9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.4285714 0.0000000
## 1491
  ## 1492
## 1493
  ## 1494
  ## 1495
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 1496
  ## 1497
  ## 1498
  ## 1499
  3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000 0.0000000
## 1500
## 1501
  1502
  1503
  ##
## 1504
  8 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000
## 1505
  ## 1506
```

```
## 1507
   ## 1508
   1509
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1510
1511
   2 0.0000000 0.0000000 0.7142857 0.1428571 0.0000000 0.0000000 0.0000000
   ## 1512
   ## 1513
   ## 1514
## 1515
   1 0.0000000 0.5714286 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 1516
## 1517
   1518
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
1519
   ## 1520
## 1521
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1522
   1 0.0000000 0.8571429 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1523
## 1524
   ## 1525
   1526
   ## 1527
   ## 1528
   ## 1529
   ## 1530
   ## 1531
## 1532
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1533
   1534
   ## 1535
   ## 1536
## 1537
   ## 1538
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ##
1539
1540
   ##
 1541
   ## 1542
   ## 1543
   9 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
## 1544
   ## 1545
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1546
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1547
## 1548
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   1549
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1550
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1551
   ## 1552
   ## 1553
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1554
1555
   8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
 1556
   ##
1557
## 1558
   ## 1559
   ## 1560
```

```
## 1561
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1562
## 1563
   6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
   9 0.1428571 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.1428571
1564
1565
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1566
   ## 1567
   ## 1568
## 1569
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1570
## 1571
   1572
   1573
   ## 1574
## 1575
   ## 1576
    6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.1428571 \ 0.0000000 \ 0.8571429 \\
## 1577
## 1578
   1579
   1580
   6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
##
1581
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1582
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1583
   ## 1584
   ## 1585
## 1586
   1587
   1588
   1589
## 1590
   ## 1591
   1592
   1593
1594
   1595
   ## 1596
   4 0.0000000 0.1428571 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000
## 1597
   ## 1598
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1599
   ## 1600
1601
   ## 1602
   1603
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1604
   ## 1605
   ## 1606
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1607
   ## 1608
## 1609
   1610
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
1611
## 1612
   ## 1613
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1614
```

```
## 1615
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1616
## 1617
  ## 1618
  1619
  ## 1620
  ## 1621
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1622
## 1623
  ## 1624
## 1625
  1626
  ##
##
1627
  ## 1628
## 1629
  ## 1630
  ## 1631
## 1632
  1633
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
1634
  ## 1635
  ## 1636
  ## 1637
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
  ## 1638
  ## 1639
## 1640
  ## 1641
   6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
  1642
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1643
## 1644
  3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
## 1645
  ## 1646
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
1647
1648
  ##
1649
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1650
  ## 1651
  ## 1652
  ## 1653
  ## 1654
  ## 1655
1656
  1657
  1\ 0.0000000\ 0.8571429\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
1658
##
  ## 1659
  ## 1660
  ## 1661
  ## 1662
## 1663
  1664
  1665
  ##
## 1666
  ## 1667
  ## 1668
```

```
## 1669
 ## 1670
 ## 1671
 ## 1672
1673
 ## 1674
 ## 1675
 1 0.0000000 0.4285714 0.0000000 0.2857143 0.0000000 0.2857143 0.0000000
## 1676
## 1677
 ## 1678
## 1679
 1680
 ##
##
1681
 ## 1682
## 1683
 ## 1684
 1\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000
 ## 1685
1686
 1687
 8 0.0000000 0.0000000 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000
1688
 ##
1689
 ## 1690
 ## 1691
 ## 1692
 ## 1693
## 1694
 1695
 1696
 1697
## 1698
 ## 1699
 ## 1700
 ## 1701
## 1702
 1703
 ## 1704
 ## 1705
 6\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000
## 1706
 ## 1707
 ## 1708
 ## 1709
## 1710
 3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
 ## 1711
 ## 1712
 ## 1713
 ## 1714
 ## 1715
 ## 1716
## 1717
 ## 1718
 ## 1719
## 1720
 ## 1721
 ## 1722
```

```
## 1723
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   ## 1724
## 1725
   8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1726
## 1727
   ## 1728
   ## 1729
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1730
## 1731
   ## 1732
## 1733
   ## 1734
   ## 1735
   ## 1736
## 1737
   ## 1738
   4\ 0.0000000\ 0.0000000\ 0.0000000\ 0.0000000\ 1.0000000\ 0.0000000\ 0.0000000
   ## 1739
## 1740
   ## 1741
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1742
   ## 1743
   ## 1744
   ## 1745
   ## 1746
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1747
## 1748
   ## 1749
   ## 1750
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1751
   ## 1752
## 1753
   ## 1754
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1755
## 1756
   1757
   ## 1758
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1759
   ## 1760
   ## 1761
   9 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
   ## 1762
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1763
## 1764
   ## 1765
   ## 1766
   ## 1767
   ## 1768
   ## 1769
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1770
## 1771
   ## 1772
   ## 1773
   ## 1774
## 1775
   ## 1776
```

```
## 1778
## 1779
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1780
1781
  ## 1782
  ## 1783
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1784
## 1785
  ## 1786
## 1787
  ## 1788
  ## 1789
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1790
## 1791
  ## 1792
   \hbox{8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.00000000 } \\
## 1793
## 1794
  ## 1795
  1796
  ## 1797
  8 0.0000000 0.2857143 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000
## 1798
  ## 1799
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1800
  ## 1801
## 1802
  1803
  1804
  ## 1805
## 1806
  3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1807
  ## 1808
  ##
1809
## 1810
  1811
  ## 1812
  ## 1813
  ## 1814
  ## 1815
  ## 1816
  ## 1817
## 1818
  ## 1819
  ## 1820
  ## 1821
  ## 1822
  ## 1823
  ## 1824
## 1825
  1826
  5 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.7142857 0.0000000
## 1827
## 1828
  ## 1829
  ## 1830
```

```
## 1831
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
   8 0.0000000 0.0000000 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1832
## 1833
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1834
   1835
   ## 1836
   ## 1837
   ## 1838
## 1839
   ## 1840
## 1841
   1842
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1843
   ## 1844
## 1845
   2 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1846
   ## 1847
## 1848
   1849
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1850
   ##
1851
   ## 1852
   ## 1853
   ## 1854
   ## 1855
1856
   1857
   1858
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
1859
##
## 1860
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
## 1861
   ## 1862
   3 0.0000000 0.0000000 0.0000000 0.8571429 0.0000000 0.0000000 0.0000000
   ##
1863
1864
   ##
1865
   1866
   3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
## 1867
   ## 1868
   ## 1869
   ## 1870
   9 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.0000000 0.0000000
## 1871
## 1872
   1873
   7 0.0000000 0.0000000 0.0000000 0.4285714 0.0000000 0.0000000 0.0000000
## 1874
   ## 1875
   ## 1876
   ## 1877
## 1878
   ## 1879
   1880
   9 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
1881
   ##
## 1882
   ## 1883
   3 0.0000000 0.0000000 0.0000000 0.5714286 0.0000000 0.1428571 0.0000000
   ## 1884
```

```
## 1885
    1886
    1887
    1888
    ##
##
 1889
    ## 1890
    3 0.0000000 0.0000000 0.0000000 0.7142857 0.0000000 0.0000000 0.0000000
## 1891
    ## 1892
## 1893
    ## 1894
 1895
    1896
    ##
##
 1897
    8 0.0000000 0.1428571 0.0000000 0.1428571 0.0000000 0.0000000 0.0000000
## 1898
    ## 1899
    ## 1900
    ## 1901
    ## 1902
    ## 1903
    ## 1904
    ## 1905
    ## 1906
    ## 1907
    3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
    ## 1908
    ## 1909
 1910
    1911
    ##
    3 0.0000000 0.0000000 0.0000000 1.0000000 0.0000000 0.0000000 0.0000000
##
 1912
     6 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 0.0000000 \ 1.0000000 
## 1913
##
 1914
    ##
     prob.7
         prob.8
              prob.9
## 1
   0.0000000 0.0000000 0.0000000
##
 2
   0.0000000 0.0000000 0.0000000
   0.0000000 1.0000000 0.0000000
##
 3
   0.0000000 0.0000000 0.8571429
##
   0.0000000 0.0000000 0.0000000
## 5
##
 6
   0.0000000 0.0000000 0.0000000
##
 7
   0.0000000 0.0000000 0.5714286
   1.0000000 0.0000000 0.0000000
##
 8
 9
   0.0000000 0.0000000 0.1428571
##
   0.0000000 0.0000000 0.0000000
##
 10
##
   0.0000000 0.0000000 0.0000000
 11
##
 12
   0.0000000 0.0000000 0.0000000
##
   0.0000000 0.8571429 0.1428571
 13
   1.0000000 0.0000000 0.0000000
## 14
   0.0000000 0.0000000 0.0000000
## 15
##
 16
   0.0000000 0.0000000 0.4285714
   0.1428571 0.0000000 0.8571429
##
 17
##
 18
   0.0000000 0.0000000 0.0000000
##
 19
   0.0000000 0.0000000 0.0000000
 20
   0.0000000 0.0000000 1.0000000
##
## 21
   0.1428571 0.0000000 0.1428571
   0.8571429 0.0000000 0.1428571
## 22
## 23
   0.0000000 0.0000000 0.0000000
```

```
## 24
        0.0000000 0.0000000 0.0000000
##
  25
        0.0000000 0.0000000 0.0000000
##
   26
        0.0000000 0.0000000 0.1428571
##
   27
        0.0000000 0.0000000 0.0000000
##
   28
        0.0000000 1.0000000 0.0000000
##
   29
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   30
##
   31
        0.0000000 0.0000000 0.0000000
##
   32
        1.0000000 0.0000000 0.0000000
##
   33
        0.0000000 0.0000000 0.0000000
##
   34
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   35
##
   36
        0.0000000 0.0000000 0.0000000
##
   37
        0.0000000 0.5714286 0.0000000
##
   38
        0.0000000 1.0000000 0.0000000
##
   39
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   40
##
   41
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   42
##
   43
        0.0000000 0.0000000 0.0000000
##
   44
        0.0000000 0.0000000 0.0000000
   45
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   46
        0.0000000 0.0000000 0.0000000
##
   47
##
   48
        0.0000000 0.0000000 0.0000000
##
   49
        0.0000000 0.0000000 1.0000000
   50
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   51
        0.0000000 0.0000000 1.0000000
##
   52
##
   53
        0.0000000 0.0000000 0.0000000
##
   54
        0.0000000 0.0000000 0.0000000
##
   55
        0.0000000 0.0000000 0.0000000
##
   56
        0.0000000 0.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
##
   57
##
   58
        0.0000000 0.0000000 0.0000000
   59
        0.0000000 0.0000000 0.0000000
##
##
   60
        0.0000000 0.8571429 0.0000000
##
  61
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   62
        0.0000000 0.0000000 0.0000000
##
   63
        0.0000000 0.0000000 0.0000000
##
   64
   65
        1.0000000 0.0000000 0.0000000
##
##
   66
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   67
##
   68
        0.0000000 0.0000000 0.0000000
   69
        0.0000000 0.0000000 0.0000000
##
##
   70
        0.0000000 0.0000000 0.0000000
##
   71
        0.0000000 0.0000000 0.0000000
##
   72
        0.0000000 0.0000000 0.8571429
##
   73
        0.0000000 0.0000000 0.0000000
        0.0000000 0.5714286 0.0000000
##
   74
##
  75
        1.0000000 0.0000000 0.0000000
## 76
        0.0000000 0.0000000 0.0000000
## 77
        0.0000000 0.0000000 0.0000000
```

```
## 78
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  79
##
  80
        0.0000000 1.0000000 0.0000000
##
  81
        0.0000000 0.0000000 0.0000000
##
   82
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
  83
        0.0000000 0.0000000 0.0000000
##
  84
##
  85
        0.0000000 0.0000000 0.0000000
##
   86
        0.0000000 0.0000000 1.0000000
##
  87
        0.0000000 0.0000000 0.0000000
##
   88
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   89
##
   90
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  91
  92
        0.0000000 0.0000000 0.0000000
##
##
  93
        0.0000000 0.0000000 0.0000000
        0.1428571 0.0000000 0.4285714
##
   94
##
   95
        1.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.5714286
  96
##
  97
        0.1428571 0.0000000 0.2857143
##
  98
        0.0000000 0.0000000 0.0000000
  99
        0.0000000 0.0000000 0.0000000
##
## 100
        0.0000000 0.0000000 0.4285714
        0.0000000 0.0000000 0.0000000
##
  101
  102
##
        0.0000000 1.0000000 0.0000000
  103
        0.0000000 0.0000000 0.0000000
  104
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   105
   106
        0.0000000 1.0000000 0.0000000
##
  107
        1.0000000 0.0000000 0.0000000
##
  108
        0.0000000 0.0000000 0.0000000
##
  109
        0.0000000 0.7142857 0.0000000
##
  110
        0.0000000 0.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
##
  111
   112
        0.0000000 0.0000000 0.0000000
        0.0000000 0.8571429 0.0000000
##
  113
## 114
        0.0000000 0.0000000 0.0000000
## 115
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  116
        0.0000000 0.0000000 0.0000000
## 117
        0.0000000 0.0000000 0.0000000
  118
  119
        0.0000000 0.0000000 0.0000000
##
##
  120
        0.0000000 0.0000000 0.0000000
##
  121
        0.0000000 0.0000000 0.0000000
## 122
        1.0000000 0.0000000 0.0000000
## 123
        0.0000000 0.0000000 0.0000000
##
  124
        0.0000000 0.0000000 0.0000000
  125
##
        0.0000000 0.0000000 0.0000000
  126
        0.0000000 0.0000000 0.0000000
##
   127
        0.0000000 0.0000000 0.0000000
  128
        0.0000000 0.0000000 0.0000000
##
##
  129
        0.0000000 0.0000000 0.8571429
## 130
        0.0000000 0.8571429 0.0000000
## 131
       0.0000000 1.0000000 0.0000000
```

```
## 132
       0.0000000 0.0000000 0.0000000
## 133
       0.0000000 0.0000000 0.0000000
       0.0000000 0.0000000 0.0000000
## 134
  135
       0.0000000 0.0000000 0.0000000
##
##
  136
       0.0000000 0.0000000 0.0000000
  137
       0.0000000 0.0000000 0.0000000
##
       0.0000000 0.0000000 0.0000000
## 138
## 139
       0.0000000 0.0000000 0.0000000
##
  140
       0.0000000 0.0000000 0.0000000
##
  141
        1.0000000 0.0000000 0.0000000
  142
       0.0000000 0.0000000 0.0000000
  143
       0.0000000 0.0000000 0.0000000
##
##
   144
        1.0000000 0.0000000 0.0000000
  145
##
       0.0000000 0.0000000 0.0000000
## 146
       0.0000000 0.0000000 0.0000000
## 147
       0.0000000 0.0000000 0.0000000
  148
       0.0000000 0.0000000 1.0000000
##
  149
       0.0000000 0.5714286 0.0000000
  150
       0.0000000 0.0000000 0.0000000
##
   151
       0.0000000 0.0000000 0.0000000
##
  152
       0.0000000 0.0000000 0.0000000
  153
       0.0000000 0.0000000 0.0000000
       0.0000000 0.0000000 0.0000000
## 154
       0.0000000 1.0000000 0.0000000
  155
## 156
       0.1428571 0.1428571 0.0000000
  157
       0.0000000 0.1428571 0.0000000
  158
       0.0000000 0.0000000 0.7142857
##
        1.0000000 0.0000000 0.0000000
##
   159
  160
       0.0000000 1.0000000 0.0000000
##
## 161
       0.0000000 0.0000000 0.2857143
##
  162
       0.0000000 0.0000000 0.0000000
##
  163
       0.0000000 0.0000000 0.0000000
##
  164
       0.0000000 0.0000000 0.0000000
  165
       1.0000000 0.0000000 0.0000000
##
   166
        0.0000000 0.0000000 1.0000000
##
  167
       0.0000000 0.0000000 0.5714286
##
  168
       0.0000000 0.0000000 0.0000000
## 169
       0.7142857 0.0000000 0.2857143
  170
       0.0000000 0.0000000 0.0000000
## 171
       0.0000000 0.0000000 1.0000000
       0.0000000 0.0000000 0.0000000
  172
  173
       0.0000000 0.0000000 0.2857143
  174
       1.0000000 0.0000000 0.0000000
  175
       0.0000000 0.8571429 0.0000000
## 176
       0.0000000 0.0000000 0.5714286
## 177
       0.0000000 0.0000000 0.0000000
##
  178
       0.0000000 0.0000000 0.0000000
  179
##
       0.0000000 0.5714286 0.0000000
  180
       0.0000000 0.0000000 0.0000000
##
   181
       0.0000000 1.0000000 0.0000000
   182
       0.0000000 0.7142857 0.0000000
##
##
  183
       0.0000000 0.0000000 0.0000000
## 184
       0.0000000 0.0000000 0.0000000
## 185
       0.0000000 0.0000000 0.0000000
```

```
## 186
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
  187
  188
        0.0000000 0.0000000 0.0000000
  189
        0.0000000 0.0000000 0.0000000
##
##
   190
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
  191
        0.0000000 0.0000000 0.0000000
  192
## 193
        0.0000000 0.0000000 0.0000000
##
  194
        0.0000000 0.0000000 0.0000000
##
  195
        0.0000000 0.0000000 0.0000000
  196
        0.0000000 0.0000000 0.0000000
   197
        1.0000000 0.0000000 0.0000000
##
##
   198
        1.0000000 0.0000000 0.0000000
##
   199
        0.0000000 0.0000000 1.0000000
  200
        1.0000000 0.0000000 0.0000000
##
##
  201
        0.0000000 0.0000000 0.0000000
  202
        0.0000000 0.0000000 0.0000000
##
   203
        1.0000000 0.0000000 0.0000000
  204
        0.0000000 1.0000000 0.0000000
##
##
   205
        0.0000000 0.0000000 0.1428571
        0.0000000 1.0000000 0.0000000
##
  206
  207
        0.0000000 0.0000000 0.0000000
## 208
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  209
## 210
        0.0000000 1.0000000 0.0000000
  211
        0.0000000 1.0000000 0.0000000
  212
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  213
  214
        0.0000000 0.0000000 0.0000000
## 215
        0.0000000 0.0000000 0.0000000
## 216
        0.0000000 0.0000000 0.0000000
##
  217
        0.0000000 0.0000000 0.1428571
  218
        0.0000000 0.0000000 0.0000000
  219
        1.0000000 0.0000000 0.0000000
##
  220
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  221
## 222
        0.0000000 0.0000000 0.0000000
## 223
        0.0000000 0.0000000 0.0000000
  224
        0.0000000 0.0000000 1.0000000
  225
        0.0000000 0.0000000 1.0000000
##
  226
        1.0000000 0.0000000 0.0000000
  227
        0.0000000 0.0000000 0.0000000
##
##
  228
        0.0000000 0.0000000 0.0000000
  229
        0.0000000 0.0000000 0.0000000
##
  230
        0.0000000 0.0000000 0.0000000
## 231
        0.0000000 0.0000000 0.0000000
##
  232
        0.0000000 0.0000000 0.0000000
   233
##
        0.0000000 0.0000000 0.0000000
##
  234
        0.0000000 0.0000000 0.0000000
##
   235
        0.0000000 0.0000000 0.0000000
   236
        1.0000000 0.0000000 0.0000000
##
##
  237
        1.0000000 0.0000000 0.0000000
## 238
        0.0000000 0.0000000 0.0000000
## 239
        0.0000000 0.0000000 0.0000000
```

```
## 240
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  241
        0.0000000 0.0000000 1.0000000
  242
  243
        0.0000000 1.0000000 0.0000000
##
##
  244
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
  245
        0.0000000 0.0000000 0.0000000
  246
##
  247
        0.0000000 0.0000000 0.0000000
##
  248
        0.0000000 1.0000000 0.0000000
##
   249
        1.0000000 0.0000000 0.0000000
   250
        0.0000000 0.2857143 0.5714286
   251
        0.0000000 0.8571429 0.0000000
##
##
   252
        0.0000000 0.0000000 0.1428571
   253
        1.0000000 0.0000000 0.0000000
##
  254
        0.0000000 0.0000000 0.0000000
##
##
  255
        0.0000000 0.0000000 0.0000000
  256
        0.0000000 0.0000000 0.0000000
##
##
   257
        1.0000000 0.0000000 0.0000000
  258
        0.0000000 0.0000000 0.0000000
##
##
   259
        0.0000000 0.0000000 0.0000000
##
  260
        0.0000000 0.0000000 0.0000000
  261
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  262
##
        0.0000000 0.0000000 0.0000000
##
  263
##
  264
        0.0000000 0.0000000 0.0000000
  265
        0.0000000 1.0000000 0.0000000
   266
        1.0000000 0.0000000 0.0000000
##
##
   267
        0.0000000 0.0000000 0.0000000
   268
        0.0000000 0.0000000 0.0000000
##
  269
        0.0000000 0.0000000 0.0000000
##
  270
        0.0000000 0.0000000 0.4285714
##
  271
        0.0000000 0.0000000 1.0000000
  272
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
  273
##
  274
        0.0000000 1.0000000 0.0000000
##
##
        0.0000000 0.0000000 0.0000000
  275
  276
        0.0000000 0.0000000 0.0000000
## 277
        0.0000000 0.0000000 0.0000000
  278
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  279
        0.0000000 0.0000000 0.0000000
  280
  281
        0.0000000 0.0000000 0.0000000
##
##
   282
        0.0000000 0.0000000 0.0000000
   283
        0.0000000 0.0000000 0.0000000
##
  284
        0.0000000 0.0000000 0.0000000
  285
        0.0000000 0.0000000 0.0000000
##
##
   286
        0.0000000 0.0000000 0.0000000
##
   287
        0.0000000 0.0000000 0.0000000
##
   288
        0.0000000 0.0000000 0.0000000
##
   289
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 1.0000000
##
   290
##
  291
        0.0000000 0.0000000 0.0000000
  292
        0.0000000 0.0000000 0.7142857
## 293
        0.0000000 0.0000000 0.0000000
```

```
## 294
        0.0000000 0.0000000 0.0000000
  295
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  296
  297
        0.0000000 0.0000000 0.4285714
##
##
  298
        0.0000000 0.0000000 0.0000000
  299
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  300
##
  301
        0.0000000 0.0000000 0.0000000
##
   302
        1.0000000 0.0000000 0.0000000
##
   303
        1.0000000 0.0000000 0.0000000
   304
        0.0000000 0.0000000 0.0000000
   305
        0.0000000 0.0000000 0.0000000
##
##
   306
        0.0000000 0.0000000 0.0000000
##
   307
        0.0000000 0.0000000 0.0000000
   308
        0.0000000 0.0000000 0.0000000
##
##
   309
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  310
   311
        0.0000000 0.0000000 0.0000000
  312
        0.0000000 0.0000000 1.0000000
##
##
  313
        0.0000000 0.0000000 0.0000000
##
  314
        1.0000000 0.0000000 0.0000000
  315
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  316
##
        0.0000000 0.0000000 0.0000000
##
  317
  318
        0.0000000 0.0000000 0.0000000
  319
        0.0000000 0.0000000 0.0000000
  320
        0.0000000 0.0000000 1.0000000
##
        0.0000000 0.0000000 0.0000000
##
   321
   322
        0.0000000 0.0000000 0.0000000
##
  323
        0.0000000 0.0000000 0.0000000
##
  324
        0.0000000 0.0000000 0.0000000
##
  325
        0.0000000 0.0000000 0.2857143
   326
##
        1.0000000 0.0000000 0.0000000
  327
        0.0000000 0.0000000 0.0000000
##
   328
        0.0000000 0.7142857 0.0000000
##
  329
        0.0000000 0.0000000 1.0000000
##
  330
        0.0000000 0.0000000 0.0000000
  331
        0.0000000 0.0000000 0.0000000
##
  332
        0.0000000 0.0000000 0.0000000
  333
        0.0000000 0.0000000 0.0000000
##
   334
        0.0000000 0.0000000 0.0000000
   335
        0.0000000 0.0000000 0.0000000
##
##
   336
        1.0000000 0.0000000 0.0000000
   337
        0.0000000 0.0000000 0.0000000
##
   338
        0.0000000 0.0000000 0.0000000
  339
        0.0000000 0.0000000 0.0000000
##
##
   340
        0.0000000 0.0000000 0.5714286
   341
##
        0.0000000 0.8571429 0.1428571
##
   342
        0.0000000 0.2857143 0.1428571
##
   343
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   344
##
   345
        1.0000000 0.0000000 0.0000000
  346
        1.0000000 0.0000000 0.0000000
##
## 347
        0.0000000 0.0000000 0.0000000
```

```
## 348
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  349
   350
        1.0000000 0.0000000 0.0000000
  351
        0.0000000 0.0000000 0.0000000
##
##
   352
        0.0000000 0.0000000 0.0000000
   353
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
   354
##
  355
        0.0000000 0.0000000 0.0000000
##
   356
        0.0000000 0.0000000 0.0000000
##
   357
        0.0000000 0.0000000 0.0000000
   358
        0.0000000 0.0000000 1.0000000
   359
        0.0000000 0.0000000 0.0000000
##
##
   360
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   361
   362
        0.0000000 1.0000000 0.0000000
##
##
   363
        0.0000000 0.1428571 0.0000000
   364
        0.0000000 0.0000000 1.0000000
##
##
   365
        0.0000000 0.0000000 0.0000000
  366
        0.0000000 0.0000000 0.7142857
##
##
   367
        0.0000000 0.0000000 0.0000000
##
   368
        0.0000000 0.0000000 0.0000000
   369
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
  370
##
        0.0000000 0.0000000 0.0000000
##
   371
  372
        0.0000000 0.0000000 0.0000000
  373
        0.0000000 0.0000000 0.0000000
  374
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   375
   376
        0.0000000 0.0000000 0.0000000
##
   377
        0.0000000 0.1428571 0.0000000
##
  378
        0.0000000 0.0000000 0.0000000
##
   379
        0.0000000 0.0000000 0.0000000
##
   380
        0.0000000 0.0000000 0.0000000
   381
        0.0000000 0.0000000 0.0000000
##
   382
        0.0000000 0.0000000 0.0000000
##
   383
        0.0000000 0.0000000 0.0000000
##
   384
        0.0000000 1.0000000 0.0000000
  385
        1.0000000 0.0000000 0.0000000
##
   386
        0.0000000 0.0000000 0.0000000
##
  387
        0.0000000 0.0000000 0.0000000
##
   388
        0.0000000 0.0000000 0.0000000
   389
        0.0000000 0.0000000 0.8571429
##
##
   390
        1.0000000 0.0000000 0.0000000
   391
        1.0000000 0.0000000 0.0000000
##
   392
        0.0000000 0.0000000 0.0000000
  393
        1.0000000 0.0000000 0.0000000
##
##
   394
        0.0000000 0.0000000 0.0000000
   395
##
        0.0000000 0.0000000 0.0000000
##
   396
        0.0000000 0.0000000 0.0000000
##
   397
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
   398
##
   399
        0.0000000 0.0000000 0.0000000
  400
        0.0000000 0.0000000 0.0000000
##
## 401
        0.0000000 0.0000000 0.0000000
```

```
## 402
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  403
  404
        0.0000000 0.0000000 0.0000000
  405
        1.0000000 0.0000000 0.0000000
##
##
   406
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
   407
##
        0.0000000 0.0000000 0.0000000
  408
## 409
        0.0000000 0.0000000 0.0000000
##
  410
        0.0000000 0.0000000 0.0000000
##
  411
        0.0000000 0.0000000 0.0000000
  412
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
  413
##
  414
        0.0000000 0.0000000 0.0000000
##
  415
        0.0000000 0.0000000 0.0000000
  416
        0.0000000 1.0000000 0.0000000
##
##
  417
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.7142857
##
  418
  419
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  420
##
  421
        0.0000000 0.0000000 0.0000000
##
  422
        0.0000000 0.0000000 0.0000000
  423
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  424
##
        0.0000000 0.0000000 0.0000000
##
  425
##
  426
        0.0000000 0.1428571 0.0000000
  427
        0.0000000 0.7142857 0.0000000
  428
        0.0000000 0.0000000 1.0000000
##
        0.0000000 0.0000000 0.0000000
##
   429
   430
        0.0000000 0.0000000 0.0000000
##
  431
        0.0000000 0.0000000 0.0000000
##
  432
        0.0000000 0.4285714 0.0000000
##
   433
        0.0000000 0.0000000 1.0000000
##
   434
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  435
##
   436
        0.0000000 0.0000000 0.0000000
##
  437
        0.0000000 0.0000000 1.0000000
##
  438
        0.0000000 0.0000000 0.0000000
  439
        0.0000000 0.0000000 0.0000000
##
  440
        0.0000000 0.0000000 0.0000000
        0.0000000 0.1428571 0.0000000
##
  441
        0.0000000 0.0000000 0.0000000
  442
  443
        0.0000000 0.0000000 0.0000000
##
##
   444
        0.0000000 0.0000000 0.0000000
  445
        0.0000000 0.0000000 0.0000000
##
  446
        0.0000000 0.0000000 0.0000000
  447
        0.0000000 0.0000000 0.0000000
##
##
   448
        0.0000000 0.0000000 0.0000000
##
   449
        0.0000000 0.2857143 0.1428571
##
  450
        0.0000000 0.0000000 0.0000000
##
   451
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
   452
##
   453
        0.0000000 0.0000000 0.0000000
  454
        0.0000000 0.0000000 0.8571429
##
## 455
       0.0000000 0.0000000 0.0000000
```

```
## 456
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  457
        0.0000000 0.0000000 0.0000000
  458
  459
        0.0000000 0.0000000 0.0000000
##
##
   460
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
   461
##
        0.0000000 0.0000000 0.7142857
   462
##
  463
        0.0000000 0.0000000 0.0000000
##
   464
        0.0000000 0.0000000 0.0000000
##
  465
        0.0000000 0.0000000 0.2857143
  466
        0.0000000 1.0000000 0.0000000
   467
        0.0000000 0.0000000 0.1428571
##
##
   468
        0.0000000 0.0000000 0.0000000
##
   469
        0.0000000 0.0000000 0.0000000
  470
        0.0000000 0.0000000 0.0000000
##
##
  471
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  472
  473
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  474
##
  475
        1.0000000 0.0000000 0.0000000
##
  476
        1.0000000 0.0000000 0.0000000
  477
        0.0000000 0.0000000 0.1428571
        0.0000000 0.0000000 0.0000000
  478
##
        0.0000000 1.0000000 0.0000000
##
  479
##
  480
        0.0000000 0.0000000 0.0000000
  481
        0.0000000 0.0000000 1.0000000
   482
        0.0000000 1.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   483
   484
        1.0000000 0.0000000 0.0000000
##
##
   485
        0.0000000 0.4285714 0.0000000
##
   486
        0.0000000 0.0000000 0.0000000
##
   487
        0.4285714 0.0000000 0.1428571
##
   488
        0.0000000 0.0000000 0.0000000
   489
        0.0000000 0.0000000 0.0000000
##
   490
        1.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  491
  492
        0.0000000 0.0000000 0.0000000
  493
        0.0000000 0.0000000 0.0000000
##
  494
        0.0000000 0.0000000 0.8571429
  495
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
   496
  497
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   498
   499
        0.0000000 0.0000000 0.0000000
##
  500
        0.0000000 0.0000000 0.0000000
  501
        0.0000000 0.0000000 0.0000000
##
##
   502
        0.0000000 0.0000000 0.0000000
##
   503
        0.0000000 0.0000000 1.0000000
##
  504
        0.0000000 0.0000000 0.0000000
##
   505
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
   506
##
  507
        0.0000000 0.0000000 0.0000000
## 508
        0.0000000 0.0000000 0.7142857
## 509
        0.0000000 0.0000000 0.0000000
```

```
## 510
       0.0000000 1.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
## 511
## 512
        0.0000000 0.0000000 0.0000000
  513
        0.0000000 0.0000000 0.0000000
##
  514
        0.0000000 0.1428571 0.0000000
  515
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.8571429 0.0000000
  516
## 517
        0.0000000 0.1428571 0.0000000
  518
        1.0000000 0.0000000 0.0000000
  519
        0.0000000 0.0000000 0.2857143
  520
        0.0000000 0.0000000 0.0000000
  521
        0.0000000 0.0000000 0.8571429
##
##
   522
        0.0000000 0.0000000 1.0000000
  523
##
        0.0000000 0.0000000 1.0000000
  524
        0.0000000 0.0000000 0.0000000
##
## 525
        0.0000000 0.0000000 0.0000000
  526
        0.0000000 0.0000000 0.8571429
##
  527
        0.0000000 0.0000000 0.0000000
  528
        0.0000000 0.0000000 0.0000000
##
##
  529
        0.0000000 0.0000000 0.0000000
##
  530
        1.0000000 0.0000000 0.0000000
  531
        0.0000000 1.0000000 0.0000000
## 532
        0.0000000 0.0000000 0.0000000
  533
        0.0000000 0.0000000 0.0000000
##
##
  534
        0.0000000 0.0000000 0.0000000
   535
        0.0000000 0.0000000 0.0000000
   536
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   537
   538
        0.0000000 1.0000000 0.0000000
##
  539
        0.0000000 1.0000000 0.0000000
## 540
        0.0000000 0.0000000 0.0000000
##
  541
        0.0000000 0.0000000 0.0000000
##
  542
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  543
  544
        0.0000000 0.0000000 0.0000000
##
  545
        0.0000000 0.0000000 0.0000000
##
## 546
        0.0000000 0.0000000 0.0000000
  547
        0.0000000 0.0000000 1.0000000
##
  548
        0.0000000 0.0000000 0.8571429
  549
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
   550
  551
        0.0000000 0.0000000 0.0000000
##
##
   552
        0.0000000 0.0000000 0.0000000
   553
        0.0000000 0.0000000 0.0000000
##
  554
        0.0000000 0.0000000 0.0000000
  555
        0.0000000 1.0000000 0.0000000
##
##
   556
        0.0000000 0.0000000 0.0000000
##
   557
        0.0000000 0.0000000 0.0000000
##
   558
        0.0000000 0.0000000 0.0000000
##
   559
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
   560
##
  561
        0.0000000 0.0000000 0.0000000
  562
        0.0000000 1.0000000 0.0000000
##
## 563
        0.0000000 0.0000000 0.0000000
```

```
## 564
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  565
  566
        0.0000000 0.0000000 0.0000000
  567
        1.0000000 0.0000000 0.0000000
##
##
   568
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
   569
##
        0.0000000 0.0000000 0.0000000
  570
## 571
        0.0000000 1.0000000 0.0000000
  572
        0.0000000 0.0000000 0.0000000
  573
        0.0000000 0.0000000 0.0000000
  574
        0.7142857 0.2857143 0.0000000
  575
        0.0000000 0.0000000 0.0000000
##
##
   576
        0.0000000 0.0000000 0.0000000
##
  577
        0.7142857 0.1428571 0.0000000
  578
        0.0000000 0.0000000 0.1428571
##
##
  579
        0.0000000 0.0000000 0.0000000
  580
        0.0000000 0.0000000 1.0000000
##
   581
        0.0000000 0.1428571 0.0000000
  582
        0.0000000 0.0000000 0.0000000
##
   583
        0.0000000 0.0000000 0.0000000
##
   584
        0.0000000 0.0000000 0.0000000
   585
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 1.0000000
  586
##
        0.0000000 0.0000000 0.0000000
##
   587
##
  588
        0.0000000 0.0000000 0.0000000
   589
        0.0000000 1.0000000 0.0000000
   590
        0.0000000 0.0000000 0.0000000
##
        0.0000000 1.0000000 0.0000000
##
   591
   592
        0.0000000 0.0000000 0.0000000
##
   593
        1.0000000 0.0000000 0.0000000
##
  594
        0.0000000 0.0000000 0.0000000
##
  595
        0.0000000 0.0000000 0.0000000
##
   596
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  597
   598
        0.0000000 0.0000000 1.0000000
  599
        0.0000000 0.0000000 0.0000000
##
  600
        0.0000000 0.0000000 0.0000000
  601
        1.0000000 0.0000000 0.0000000
##
   602
        0.0000000 0.0000000 0.0000000
        0.0000000 0.7142857 0.0000000
##
  603
        0.0000000 0.0000000 0.0000000
   604
   605
        1.0000000 0.0000000 0.0000000
##
##
   606
        0.0000000 0.0000000 0.4285714
   607
        0.0000000 0.0000000 0.0000000
##
   608
        0.0000000 0.0000000 1.0000000
  609
        1.0000000 0.0000000 0.0000000
##
##
  610
        0.0000000 0.0000000 1.0000000
##
  611
        0.0000000 0.0000000 0.0000000
##
  612
        0.0000000 0.0000000 0.0000000
##
   613
        0.0000000 0.0000000 0.0000000
   614
        1.0000000 0.0000000 0.0000000
##
##
  615
        0.0000000 0.0000000 0.0000000
## 616
        0.0000000 0.0000000 0.0000000
## 617
       0.0000000 0.0000000 0.0000000
```

```
## 618
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.2857143
  619
        0.0000000 0.0000000 0.5714286
  620
  621
        0.0000000 0.0000000 0.7142857
##
##
   622
        0.0000000 0.0000000 0.1428571
  623
        0.0000000 0.0000000 0.0000000
##
        0.0000000 1.0000000 0.0000000
  624
## 625
        0.0000000 0.0000000 0.0000000
##
   626
        0.0000000 0.0000000 0.0000000
##
  627
        0.0000000 0.0000000 0.0000000
   628
        0.0000000 0.0000000 0.4285714
   629
        0.0000000 0.0000000 1.0000000
##
##
   630
        0.0000000 0.0000000 0.0000000
##
   631
        0.0000000 0.0000000 0.0000000
  632
        0.0000000 1.0000000 0.0000000
##
##
   633
        0.0000000 0.0000000 1.0000000
  634
        0.0000000 0.0000000 0.0000000
##
   635
        0.0000000 0.0000000 1.0000000
##
  636
        0.0000000 0.0000000 0.0000000
##
##
   637
        0.0000000 0.8571429 0.0000000
##
   638
        0.0000000 0.0000000 0.0000000
   639
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 1.0000000
  640
##
        0.0000000 0.0000000 0.2857143
##
   641
##
  642
        0.0000000 0.0000000 0.0000000
   643
        0.0000000 0.0000000 0.0000000
   644
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   645
   646
        0.0000000 0.0000000 0.0000000
##
   647
        1.0000000 0.0000000 0.0000000
##
  648
        0.0000000 0.0000000 0.0000000
##
   649
        0.0000000 0.7142857 0.0000000
##
   650
        0.0000000 0.0000000 0.0000000
   651
        0.0000000 1.0000000 0.0000000
##
   652
        1.0000000 0.0000000 0.0000000
##
   653
        0.0000000 0.0000000 0.0000000
##
   654
        0.0000000 0.0000000 0.0000000
  655
        1.0000000 0.0000000 0.0000000
##
   656
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  657
        0.0000000 0.0000000 0.0000000
   658
   659
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   660
   661
        0.0000000 0.0000000 0.0000000
##
##
   662
        0.0000000 0.7142857 0.0000000
  663
        0.0000000 0.0000000 0.0000000
##
##
   664
        0.0000000 0.0000000 0.0000000
##
   665
        0.0000000 0.0000000 0.0000000
##
   666
        0.0000000 0.0000000 0.0000000
   667
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   668
##
   669
        0.0000000 0.2857143 0.0000000
  670
        0.0000000 0.0000000 0.0000000
##
## 671
       0.0000000 0.0000000 0.0000000
```

```
0.0000000 0.0000000 0.0000000
        0.1428571 0.0000000 0.8571429
  673
        0.0000000 0.1428571 0.0000000
  674
  675
        0.0000000 0.1428571 0.0000000
##
##
   676
        0.0000000 1.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
   677
        0.0000000 0.0000000 0.0000000
  678
##
  679
        0.0000000 0.0000000 1.0000000
##
   680
        0.0000000 0.0000000 0.0000000
##
   681
        0.0000000 0.0000000 0.0000000
   682
        1.0000000 0.0000000 0.0000000
   683
        0.0000000 0.0000000 0.1428571
##
##
   684
        0.0000000 0.0000000 0.0000000
##
   685
        1.0000000 0.0000000 0.0000000
   686
        0.0000000 0.0000000 0.0000000
##
##
   687
        1.0000000 0.0000000 0.0000000
   688
        1.0000000 0.0000000 0.0000000
##
   689
        0.0000000 0.0000000 0.0000000
##
  690
        0.0000000 0.0000000 0.0000000
##
##
   691
        0.0000000 1.0000000 0.0000000
##
   692
        0.0000000 0.0000000 0.0000000
   693
        0.0000000 1.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
  694
##
   695
        0.4285714 0.0000000 0.0000000
##
##
  696
        0.0000000 0.0000000 0.0000000
   697
        1.0000000 0.0000000 0.0000000
   698
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.8571429
##
   699
   700
        0.0000000 0.0000000 0.0000000
##
  701
        0.0000000 0.0000000 0.0000000
##
  702
        0.0000000 0.0000000 0.8571429
##
  703
        0.0000000 0.0000000 0.0000000
##
  704
        0.0000000 0.0000000 0.0000000
  705
        0.0000000 0.0000000 0.0000000
##
   706
        0.0000000 0.0000000 0.0000000
##
  707
        1.0000000 0.0000000 0.0000000
##
  708
        1.0000000 0.0000000 0.0000000
  709
        0.0000000 0.0000000 0.0000000
##
  710
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  711
        0.0000000 0.0000000 0.2857143
  712
  713
        0.0000000 0.0000000 0.0000000
##
  714
        1.0000000 0.0000000 0.0000000
  715
        0.0000000 0.5714286 0.0000000
##
        0.0000000 0.0000000 0.0000000
  716
## 717
        0.0000000 0.0000000 0.2857143
##
  718
        1.0000000 0.0000000 0.0000000
  719
##
        0.0000000 0.0000000 0.0000000
##
  720
        0.0000000 0.1428571 0.4285714
##
  721
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
  722
  723
        0.0000000 0.0000000 0.0000000
  724
        0.0000000 0.0000000 0.0000000
##
## 725
       0.0000000 0.0000000 0.0000000
```

```
## 726
        0.0000000 0.0000000 0.8571429
        0.0000000 0.0000000 0.0000000
  727
  728
        0.0000000 0.0000000 0.0000000
  729
        1.0000000 0.0000000 0.0000000
##
##
   730
        0.0000000 0.0000000 0.0000000
        0.0000000 0.5714286 0.0000000
##
  731
        0.0000000 0.0000000 0.0000000
  732
##
  733
        0.0000000 0.0000000 0.0000000
##
  734
        0.0000000 0.0000000 0.0000000
  735
##
        1.0000000 0.0000000 0.0000000
   736
        0.0000000 0.0000000 0.0000000
  737
        0.0000000 0.8571429 0.0000000
##
##
   738
        0.0000000 0.0000000 1.0000000
##
  739
        0.0000000 0.0000000 0.8571429
  740
        0.0000000 0.0000000 0.0000000
##
##
  741
        0.0000000 0.0000000 0.0000000
  742
        0.0000000 0.0000000 0.0000000
##
  743
        0.0000000 0.0000000 0.0000000
  744
        0.0000000 0.0000000 0.0000000
##
##
  745
        0.0000000 0.0000000 0.0000000
##
  746
        0.0000000 0.0000000 0.0000000
  747
        0.0000000 0.0000000 0.0000000
  748
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  749
##
  750
        0.0000000 0.0000000 0.0000000
  751
        0.1428571 0.0000000 0.2857143
  752
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   753
  754
        0.0000000 0.0000000 0.0000000
##
##
  755
        0.0000000 0.0000000 0.0000000
##
  756
        0.0000000 0.0000000 0.0000000
##
  757
        0.0000000 0.0000000 0.0000000
  758
##
        0.0000000 0.0000000 0.0000000
  759
        1.0000000 0.0000000 0.0000000
##
   760
        1.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  761
  762
        0.0000000 0.0000000 0.0000000
  763
        0.0000000 0.0000000 0.0000000
##
  764
        0.0000000 0.0000000 0.0000000
##
  765
        0.0000000 0.0000000 0.0000000
##
        1.0000000 0.0000000 0.0000000
   766
  767
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   768
  769
        0.0000000 0.1428571 0.0000000
##
        0.0000000 0.0000000 0.0000000
  770
  771
        0.0000000 0.0000000 1.0000000
##
##
  772
        0.0000000 0.0000000 0.0000000
  773
##
        0.0000000 0.0000000 0.0000000
##
  774
        0.0000000 0.0000000 0.0000000
##
   775
        1.0000000 0.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
##
  776
##
  777
        0.0000000 0.0000000 1.0000000
  778
        0.0000000 0.0000000 0.0000000
##
## 779
        0.0000000 0.0000000 0.1428571
```

```
## 780
        0.0000000 0.0000000 0.8571429
  781
        0.0000000 0.0000000 0.8571429
  782
        0.0000000 0.0000000 0.0000000
  783
        0.0000000 0.0000000 0.0000000
##
##
   784
        0.0000000 0.0000000 0.0000000
   785
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
   786
##
  787
        0.0000000 0.0000000 0.0000000
##
   788
        1.0000000 0.0000000 0.0000000
##
  789
        1.0000000 0.0000000 0.0000000
   790
        0.0000000 0.0000000 1.0000000
   791
        0.0000000 1.0000000 0.0000000
##
##
   792
        0.0000000 0.0000000 0.0000000
##
  793
        0.0000000 0.0000000 0.0000000
  794
        0.0000000 0.0000000 1.0000000
##
##
  795
        0.0000000 0.0000000 0.1428571
  796
        1.0000000 0.0000000 0.0000000
##
  797
        0.0000000 0.0000000 0.0000000
  798
        0.0000000 1.0000000 0.0000000
##
##
   799
        0.0000000 0.0000000 0.0000000
##
  800
        0.0000000 0.0000000 0.0000000
   801
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
  802
##
        0.0000000 0.8571429 0.1428571
##
  803
##
  804
        0.0000000 0.0000000 0.0000000
  805
        0.0000000 0.0000000 0.0000000
  806
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   807
   808
        0.0000000 0.0000000 0.0000000
##
##
  809
        0.0000000 0.0000000 0.0000000
##
  810
        0.0000000 1.0000000 0.0000000
##
  811
        0.0000000 0.0000000 1.0000000
##
  812
        0.0000000 0.0000000 0.0000000
        1.0000000 0.0000000 0.0000000
##
  813
  814
        0.0000000 0.0000000 0.0000000
  815
        1.0000000 0.0000000 0.0000000
##
  816
        0.0000000 0.0000000 0.0000000
  817
        0.0000000 0.0000000 0.0000000
##
  818
        0.0000000 0.0000000 0.1428571
  819
        0.0000000 0.0000000 0.0000000
##
  820
        0.0000000 0.0000000 0.0000000
  821
        0.0000000 0.0000000 0.0000000
##
##
  822
        0.0000000 0.0000000 0.0000000
  823
        0.0000000 0.0000000 0.0000000
##
  824
        0.0000000 0.0000000 0.0000000
## 825
        0.0000000 0.0000000 0.0000000
##
  826
        0.0000000 0.0000000 1.0000000
  827
##
        0.0000000 0.0000000 1.0000000
##
  828
        0.0000000 0.0000000 0.0000000
##
   829
        0.0000000 0.0000000 0.0000000
   830
        0.0000000 0.0000000 0.0000000
##
##
   831
        1.0000000 0.0000000 0.0000000
  832
        0.0000000 1.0000000 0.0000000
##
## 833
       0.0000000 0.0000000 0.0000000
```

```
## 834
        0.0000000 0.0000000 0.0000000
  835
        0.8571429 0.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
  836
  837
        0.0000000 0.0000000 0.0000000
##
##
   838
        0.1428571 0.0000000 0.0000000
  839
        0.0000000 1.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  840
## 841
        0.0000000 0.0000000 0.0000000
##
  842
        0.0000000 0.0000000 0.0000000
##
  843
        0.0000000 0.7142857 0.0000000
  844
        0.0000000 0.1428571 0.0000000
  845
        0.0000000 0.0000000 0.0000000
##
##
   846
        0.0000000 0.0000000 0.0000000
##
   847
        0.0000000 0.0000000 0.0000000
  848
        0.0000000 0.0000000 0.0000000
##
##
  849
        0.0000000 0.0000000 1.0000000
  850
        0.0000000 0.0000000 0.0000000
##
##
   851
        0.0000000 0.0000000 0.0000000
  852
        0.0000000 0.0000000 1.0000000
##
##
   853
        0.0000000 0.0000000 1.0000000
##
   854
        0.0000000 0.0000000 0.0000000
   855
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.1428571
  856
##
        0.0000000 0.5714286 0.0000000
##
   857
##
  858
        0.0000000 0.0000000 0.0000000
  859
        0.0000000 0.0000000 0.8571429
  860
        0.0000000 0.0000000 0.0000000
##
        1.0000000 0.0000000 0.0000000
##
   861
   862
        0.0000000 1.0000000 0.0000000
##
##
  863
        0.0000000 0.0000000 0.0000000
##
  864
        0.0000000 0.0000000 0.0000000
##
   865
        0.0000000 0.0000000 0.0000000
##
   866
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
  867
   868
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
   869
  870
        0.1428571 0.0000000 0.8571429
  871
        0.0000000 0.0000000 0.0000000
##
  872
        0.0000000 0.0000000 0.0000000
  873
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  874
  875
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.8571429
##
   876
        0.0000000 0.0000000 0.0000000
##
   877
  878
        0.0000000 0.0000000 0.0000000
## 879
        0.0000000 0.0000000 0.0000000
##
  880
        0.0000000 0.0000000 0.0000000
   881
##
        0.0000000 0.1428571 0.0000000
##
   882
        0.0000000 0.0000000 0.0000000
##
   883
        0.0000000 0.0000000 0.0000000
   884
        0.0000000 0.0000000 1.0000000
##
##
   885
        0.0000000 0.0000000 0.0000000
  886
        0.0000000 0.0000000 0.0000000
##
## 887
        0.0000000 0.0000000 0.0000000
```

```
## 888
        0.0000000 1.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  889
  890
        0.0000000 0.0000000 0.0000000
  891
        0.0000000 0.0000000 0.0000000
##
##
   892
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  893
        0.0000000 0.0000000 0.0000000
  894
##
  895
        0.0000000 0.0000000 0.0000000
##
   896
        0.0000000 0.0000000 0.0000000
##
  897
        0.0000000 0.1428571 0.5714286
  898
        0.0000000 0.0000000 0.0000000
  899
        0.0000000 0.0000000 0.0000000
##
##
   900
        0.0000000 0.0000000 0.0000000
##
   901
        0.0000000 0.0000000 0.0000000
  902
        0.0000000 0.0000000 0.0000000
##
##
  903
        0.0000000 0.0000000 0.0000000
##
  904
        0.0000000 0.4285714 0.2857143
   905
        0.0000000 0.0000000 0.2857143
        0.0000000 0.0000000 0.0000000
##
  906
##
  907
        0.0000000 0.0000000 0.0000000
##
  908
        1.0000000 0.0000000 0.0000000
  909
        0.0000000 0.0000000 0.0000000
        0.0000000 1.0000000 0.0000000
## 910
        0.0000000 0.0000000 0.0000000
## 911
## 912
        0.0000000 0.0000000 0.0000000
  913
        0.0000000 1.0000000 0.0000000
## 914
        1.0000000 0.0000000 0.0000000
        0.4285714 0.0000000 0.5714286
##
  915
        0.0000000 0.4285714 0.0000000
  916
## 917
        0.0000000 0.0000000 0.0000000
## 918
        0.0000000 0.0000000 0.0000000
##
  919
        0.0000000 1.0000000 0.0000000
  920
        0.1428571 0.0000000 0.8571429
  921
        0.0000000 0.0000000 0.0000000
##
  922
        0.2857143 0.0000000 0.0000000
  923
        0.0000000 0.0000000 0.0000000
##
## 924
        0.0000000 1.0000000 0.0000000
## 925
        0.0000000 0.0000000 0.0000000
  926
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  927
        0.0000000 0.0000000 0.1428571
  928
  929
        0.0000000 1.0000000 0.0000000
##
##
  930
        0.0000000 0.0000000 0.0000000
  931
        0.0000000 0.0000000 0.0000000
##
  932
        1.0000000 0.0000000 0.0000000
## 933
        0.1428571 0.0000000 0.8571429
##
  934
        0.0000000 0.0000000 0.0000000
  935
##
        0.0000000 0.0000000 0.0000000
##
  936
        1.0000000 0.0000000 0.0000000
##
   937
        0.0000000 0.0000000 0.0000000
   938
        0.0000000 0.0000000 0.0000000
##
  939
        0.0000000 0.0000000 0.1428571
## 940
        0.0000000 0.0000000 0.0000000
## 941
        0.0000000 0.0000000 0.0000000
```

```
## 942
        0.0000000 0.0000000 0.0000000
## 943
        1.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  944
  945
        0.0000000 0.0000000 0.0000000
##
##
  946
        0.0000000 0.0000000 1.0000000
        0.0000000 0.0000000 0.0000000
##
  947
        0.0000000 0.0000000 0.0000000
  948
## 949
        0.0000000 0.0000000 0.5714286
##
  950
        0.0000000 0.0000000 0.0000000
##
  951
        1.0000000 0.0000000 0.0000000
  952
        1.0000000 0.0000000 0.0000000
  953
        0.0000000 0.0000000 0.0000000
##
##
   954
        0.0000000 0.0000000 0.0000000
##
   955
        0.0000000 0.0000000 0.0000000
  956
        0.0000000 1.0000000 0.0000000
##
##
  957
        0.0000000 0.0000000 0.0000000
  958
        0.0000000 0.0000000 0.0000000
##
   959
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
##
  960
##
  961
        0.0000000 0.0000000 0.0000000
##
  962
        0.0000000 0.0000000 0.1428571
  963
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.0000000
  964
##
        0.0000000 0.0000000 1.0000000
##
  965
##
  966
        0.0000000 0.0000000 0.0000000
  967
        0.0000000 0.0000000 0.0000000
  968
        0.0000000 0.0000000 1.0000000
##
        0.0000000 0.0000000 0.0000000
##
   969
  970
        0.0000000 0.0000000 0.0000000
##
  971
        0.0000000 0.0000000 0.0000000
## 972
        0.0000000 0.8571429 0.0000000
##
  973
        0.0000000 0.0000000 0.0000000
  974
        0.0000000 0.0000000 0.0000000
        0.0000000 0.0000000 0.1428571
##
  975
   976
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
##
  977
  978
        0.0000000 0.0000000 0.0000000
## 979
        0.0000000 1.0000000 0.0000000
  980
        0.0000000 0.0000000 0.0000000
  981
        0.0000000 0.0000000 0.0000000
##
        0.0000000 0.0000000 0.0000000
  982
  983
        0.0000000 0.0000000 0.0000000
##
##
  984
        0.7142857 0.0000000 0.2857143
   985
        0.0000000 0.0000000 0.0000000
##
  986
        0.0000000 0.0000000 1.0000000
  987
        0.0000000 0.0000000 0.0000000
##
##
  988
        0.0000000 0.0000000 0.0000000
##
   989
        0.0000000 0.0000000 0.0000000
##
  990
        0.0000000 0.0000000 0.0000000
##
   991
        0.0000000 0.0000000 1.0000000
        0.0000000 0.8571429 0.0000000
##
   992
##
  993
        0.1428571 0.0000000 0.8571429
  994
        0.0000000 0.0000000 0.0000000
##
## 995
       0.0000000 0.0000000 0.0000000
```

```
## 996
       1.0000000 0.0000000 0.0000000
       0.0000000 0.0000000 1.0000000
## 997
       1.0000000 0.0000000 0.0000000
## 999
       0.0000000 0.0000000 0.0000000
## 1000 0.0000000 0.0000000 0.0000000
## 1001 1.0000000 0.0000000 0.0000000
## 1002 0.0000000 0.0000000 0.0000000
## 1003 1.0000000 0.0000000 0.0000000
## 1004 0.0000000 0.0000000 0.0000000
## 1005 1.0000000 0.0000000 0.0000000
## 1006 0.0000000 0.0000000 0.0000000
## 1007 0.0000000 0.0000000 0.0000000
## 1008 0.0000000 0.0000000 0.0000000
## 1009 0.0000000 0.0000000 0.0000000
## 1010 0.0000000 0.0000000 0.0000000
## 1011 0.0000000 0.0000000 0.0000000
## 1012 0.0000000 0.0000000 0.0000000
## 1013 0.0000000 0.0000000 0.0000000
## 1014 1.0000000 0.0000000 0.0000000
## 1015 0.0000000 0.0000000 0.0000000
## 1016 0.0000000 0.0000000 0.0000000
## 1017 1.0000000 0.0000000 0.0000000
## 1018 0.0000000 0.0000000 0.0000000
## 1019 0.0000000 0.0000000 0.0000000
## 1020 0.0000000 0.0000000 0.0000000
## 1021 0.0000000 0.0000000 0.8571429
## 1022 0.0000000 0.0000000 0.0000000
## 1023 0.0000000 1.0000000 0.0000000
## 1024 0.0000000 0.0000000 0.0000000
## 1025 0.0000000 0.0000000 0.1428571
## 1026 0.0000000 0.0000000 0.0000000
## 1027 0.0000000 0.0000000 0.0000000
## 1028 0.0000000 0.0000000 0.0000000
## 1029 0.0000000 0.0000000 0.0000000
## 1030 0.0000000 0.0000000 0.0000000
## 1031 0.0000000 0.0000000 0.0000000
## 1032 0.0000000 0.0000000 0.0000000
## 1033 0.0000000 0.0000000 0.0000000
## 1034 1.0000000 0.0000000 0.0000000
## 1035 1.0000000 0.0000000 0.0000000
## 1036 0.0000000 0.0000000 0.0000000
## 1037 0.0000000 0.0000000 0.0000000
## 1038 0.0000000 0.0000000 0.0000000
## 1039 0.0000000 1.0000000 0.0000000
## 1040 0.0000000 0.0000000 1.0000000
## 1041 0.0000000 0.0000000 0.0000000
## 1042 0.0000000 0.0000000 0.0000000
## 1043 0.8571429 0.0000000 0.1428571
## 1044 1.0000000 0.0000000 0.0000000
## 1045 0.0000000 0.0000000 0.0000000
## 1046 0.0000000 0.0000000 0.0000000
## 1047 0.0000000 0.0000000 0.0000000
## 1048 0.0000000 0.0000000 0.5714286
## 1049 1.0000000 0.0000000 0.0000000
```

```
## 1050 0.0000000 0.0000000 0.0000000
## 1051 0.0000000 0.0000000 0.0000000
## 1052 0.0000000 0.1428571 0.0000000
## 1053 0.0000000 0.0000000 0.0000000
## 1054 0.0000000 0.0000000 0.0000000
## 1055 0.0000000 0.0000000 0.0000000
## 1056 0.0000000 0.0000000 0.0000000
## 1057 1.0000000 0.0000000 0.0000000
## 1058 0.0000000 1.0000000 0.0000000
## 1059 0.0000000 0.0000000 0.0000000
## 1060 0.0000000 0.0000000 0.0000000
## 1061 0.0000000 1.0000000 0.0000000
## 1062 0.0000000 0.0000000 0.0000000
## 1063 1.0000000 0.0000000 0.0000000
## 1064 0.0000000 0.0000000 0.0000000
## 1065 0.0000000 0.0000000 0.0000000
## 1066 0.0000000 0.0000000 0.0000000
## 1067 0.0000000 0.0000000 0.0000000
## 1068 0.0000000 0.0000000 0.0000000
## 1069 0.0000000 0.0000000 0.0000000
## 1070 0.0000000 1.0000000 0.0000000
## 1071 0.0000000 0.0000000 0.0000000
## 1072 0.0000000 0.0000000 0.0000000
## 1073 0.0000000 0.0000000 0.0000000
## 1074 0.0000000 0.0000000 0.0000000
## 1075 0.0000000 0.0000000 0.0000000
## 1076 0.0000000 0.0000000 0.0000000
## 1077 0.0000000 0.0000000 0.0000000
## 1078 0.0000000 0.0000000 1.0000000
## 1079 0.0000000 0.0000000 0.0000000
## 1080 1.0000000 0.0000000 0.0000000
## 1081 0.0000000 0.0000000 0.0000000
## 1082 0.0000000 0.0000000 0.0000000
## 1083 0.0000000 1.0000000 0.0000000
## 1084 0.0000000 0.0000000 0.0000000
## 1085 0.0000000 0.0000000 0.0000000
## 1086 0.0000000 0.0000000 0.0000000
## 1087 0.0000000 0.0000000 0.0000000
## 1088 0.0000000 0.0000000 0.0000000
## 1089 0.0000000 0.0000000 0.0000000
## 1090 0.0000000 0.0000000 0.0000000
## 1091 1.0000000 0.0000000 0.0000000
## 1092 0.0000000 0.0000000 0.0000000
## 1093 0.0000000 0.0000000 0.0000000
## 1094 0.0000000 0.0000000 0.0000000
## 1095 0.0000000 0.0000000 0.0000000
## 1096 0.0000000 0.0000000 0.0000000
## 1097 0.0000000 0.0000000 1.0000000
## 1098 0.0000000 0.0000000 0.0000000
## 1099 0.0000000 0.0000000 0.0000000
## 1100 0.0000000 0.0000000 0.0000000
## 1101 0.0000000 0.0000000 0.0000000
## 1102 1.0000000 0.0000000 0.0000000
## 1103 0.0000000 0.0000000 0.0000000
```

```
## 1104 0.0000000 1.0000000 0.0000000
## 1105 0.0000000 0.0000000 0.0000000
## 1106 0.0000000 0.0000000 0.0000000
## 1107 0.0000000 1.0000000 0.0000000
## 1108 0.0000000 0.0000000 0.0000000
## 1109 0.0000000 0.0000000 0.0000000
## 1110 0.0000000 0.8571429 0.0000000
## 1111 0.0000000 0.0000000 1.0000000
## 1112 0.0000000 0.0000000 0.0000000
## 1113 0.0000000 1.0000000 0.0000000
## 1114 0.0000000 0.0000000 0.0000000
## 1115 0.0000000 0.0000000 0.2857143
## 1116 0.0000000 0.0000000 0.0000000
## 1117 0.0000000 0.0000000 0.0000000
## 1118 0.0000000 1.0000000 0.0000000
## 1119 0.0000000 0.0000000 0.0000000
## 1120 0.0000000 0.0000000 0.8571429
## 1121 0.0000000 0.0000000 1.0000000
## 1122 0.0000000 0.0000000 0.0000000
## 1123 0.0000000 0.0000000 0.0000000
## 1124 0.0000000 0.0000000 0.0000000
## 1125 0.0000000 0.0000000 0.0000000
## 1126 0.0000000 0.7142857 0.2857143
## 1127 0.0000000 0.0000000 0.0000000
## 1128 0.0000000 0.1428571 0.0000000
## 1129 0.0000000 1.0000000 0.0000000
## 1130 0.0000000 0.0000000 0.0000000
## 1131 0.0000000 0.0000000 0.0000000
## 1132 0.0000000 0.0000000 0.0000000
## 1133 1.0000000 0.0000000 0.0000000
## 1134 0.0000000 0.8571429 0.0000000
## 1135 0.0000000 0.0000000 0.0000000
## 1136 0.0000000 0.8571429 0.0000000
## 1137 0.0000000 1.0000000 0.0000000
## 1138 0.0000000 0.0000000 0.0000000
## 1139 0.0000000 0.0000000 0.8571429
## 1140 0.0000000 0.0000000 0.0000000
## 1141 0.0000000 0.0000000 1.0000000
## 1142 1.0000000 0.0000000 0.0000000
## 1143 1.0000000 0.0000000 0.0000000
## 1144 0.0000000 0.0000000 0.0000000
## 1145 0.0000000 0.0000000 0.0000000
## 1146 1.0000000 0.0000000 0.0000000
## 1147 0.0000000 0.0000000 0.5714286
## 1148 0.0000000 0.0000000 0.0000000
## 1149 0.0000000 0.0000000 0.0000000
## 1150 1.0000000 0.0000000 0.0000000
## 1151 0.0000000 0.0000000 0.0000000
## 1152 0.0000000 0.0000000 1.0000000
## 1153 0.0000000 0.0000000 0.0000000
## 1154 0.0000000 0.0000000 0.0000000
## 1155 0.0000000 1.0000000 0.0000000
## 1156 1.0000000 0.0000000 0.0000000
## 1157 0.0000000 0.0000000 0.1428571
```

```
## 1158 0.0000000 0.0000000 0.8571429
## 1159 1.0000000 0.0000000 0.0000000
## 1160 0.0000000 0.0000000 0.8571429
## 1161 0.0000000 1.0000000 0.0000000
## 1162 0.0000000 0.0000000 0.0000000
## 1163 0.0000000 1.0000000 0.0000000
## 1164 0.0000000 0.0000000 0.0000000
## 1165 0.0000000 0.0000000 1.0000000
## 1166 0.0000000 0.0000000 0.0000000
## 1167 0.0000000 0.0000000 0.0000000
## 1168 0.0000000 0.0000000 0.0000000
## 1169 0.7142857 0.0000000 0.2857143
## 1170 0.0000000 0.0000000 0.0000000
## 1171 0.0000000 0.0000000 0.0000000
## 1172 0.0000000 0.0000000 0.0000000
## 1173 0.0000000 0.0000000 0.0000000
## 1174 0.0000000 0.0000000 0.8571429
## 1175 0.0000000 0.0000000 0.0000000
## 1176 0.0000000 0.0000000 0.0000000
## 1177 0.0000000 0.0000000 0.0000000
## 1178 0.0000000 0.0000000 0.0000000
## 1179 0.0000000 0.2857143 0.0000000
## 1180 0.0000000 0.0000000 0.0000000
## 1181 0.0000000 0.2857143 0.0000000
## 1182 0.0000000 0.0000000 0.0000000
## 1183 0.0000000 0.0000000 0.0000000
## 1184 0.1428571 0.0000000 0.0000000
## 1185 0.0000000 0.0000000 0.0000000
## 1186 0.0000000 0.0000000 0.0000000
## 1187 0.0000000 0.0000000 0.0000000
## 1188 0.0000000 0.0000000 0.0000000
## 1189 0.0000000 0.0000000 0.5714286
## 1190 0.0000000 0.0000000 0.0000000
## 1191 0.0000000 0.0000000 0.8571429
## 1192 0.0000000 0.0000000 0.0000000
## 1193 0.0000000 0.0000000 0.0000000
## 1194 0.0000000 0.0000000 0.0000000
## 1195 0.0000000 0.0000000 0.0000000
## 1196 0.0000000 0.0000000 0.0000000
## 1197 0.0000000 0.0000000 0.0000000
## 1198 1.0000000 0.0000000 0.0000000
## 1199 0.0000000 0.0000000 0.0000000
## 1200 0.0000000 1.0000000 0.0000000
## 1201 0.0000000 1.0000000 0.0000000
## 1202 0.0000000 0.0000000 0.0000000
## 1203 0.0000000 0.7142857 0.0000000
## 1204 0.0000000 0.0000000 0.0000000
## 1205 0.0000000 0.0000000 0.0000000
## 1206 0.0000000 0.0000000 0.0000000
## 1207 0.0000000 0.0000000 0.0000000
## 1208 0.0000000 0.0000000 1.0000000
## 1209 0.0000000 0.0000000 0.0000000
## 1210 1.0000000 0.0000000 0.0000000
## 1211 0.0000000 0.0000000 0.0000000
```

```
## 1212 0.0000000 0.0000000 0.0000000
## 1213 1.0000000 0.0000000 0.0000000
## 1214 1.0000000 0.0000000 0.0000000
## 1215 0.0000000 0.0000000 0.0000000
## 1216 0.0000000 0.0000000 0.0000000
## 1217 0.0000000 0.1428571 0.0000000
## 1218 0.0000000 0.0000000 0.0000000
## 1219 0.0000000 0.0000000 0.0000000
## 1220 0.0000000 0.0000000 0.0000000
## 1221 1.0000000 0.0000000 0.0000000
## 1222 0.0000000 0.0000000 0.0000000
## 1223 0.0000000 0.0000000 0.0000000
## 1224 0.0000000 0.0000000 0.0000000
## 1225 0.0000000 0.0000000 0.0000000
## 1226 0.0000000 0.0000000 0.0000000
## 1227 0.0000000 0.0000000 0.0000000
## 1228 0.0000000 0.0000000 0.0000000
## 1229 0.0000000 0.0000000 0.0000000
## 1230 0.0000000 0.0000000 0.0000000
## 1231 0.0000000 0.0000000 1.0000000
## 1232 0.0000000 1.0000000 0.0000000
## 1233 0.0000000 0.0000000 0.0000000
## 1234 0.0000000 0.0000000 0.0000000
## 1235 0.0000000 0.0000000 0.0000000
## 1236 0.0000000 0.0000000 0.0000000
## 1237 0.0000000 0.0000000 1.0000000
## 1238 0.0000000 0.0000000 0.0000000
## 1239 0.0000000 0.0000000 0.0000000
## 1240 1.0000000 0.0000000 0.0000000
## 1241 0.0000000 0.0000000 0.0000000
## 1242 0.0000000 0.0000000 0.0000000
## 1243 0.0000000 1.0000000 0.0000000
## 1244 0.0000000 0.0000000 0.0000000
## 1245 0.0000000 0.0000000 0.0000000
## 1246 0.0000000 0.0000000 0.0000000
## 1247 1.0000000 0.0000000 0.0000000
## 1248 0.0000000 0.0000000 0.0000000
## 1249 0.0000000 0.0000000 0.0000000
## 1250 0.0000000 0.8571429 0.0000000
## 1251 0.0000000 0.0000000 0.2857143
## 1252 0.0000000 0.0000000 1.0000000
## 1253 1.0000000 0.0000000 0.0000000
## 1254 0.0000000 0.0000000 0.0000000
## 1255 0.0000000 0.0000000 0.0000000
## 1256 0.0000000 0.0000000 1.0000000
## 1257 1.0000000 0.0000000 0.0000000
## 1258 0.0000000 0.0000000 0.0000000
## 1259 0.0000000 0.0000000 0.0000000
## 1260 0.0000000 0.0000000 1.0000000
## 1261 0.0000000 0.0000000 0.0000000
## 1262 1.0000000 0.0000000 0.0000000
## 1263 1.0000000 0.0000000 0.0000000
## 1264 0.0000000 0.0000000 0.0000000
## 1265 0.0000000 0.0000000 0.0000000
```

```
## 1266 0.0000000 0.0000000 0.0000000
## 1267 0.0000000 0.0000000 0.0000000
## 1268 0.0000000 0.0000000 0.0000000
## 1269 0.0000000 0.0000000 0.0000000
## 1270 0.5714286 0.0000000 0.2857143
## 1271 0.0000000 0.0000000 0.0000000
## 1272 0.0000000 0.0000000 0.0000000
## 1273 0.0000000 0.0000000 0.0000000
## 1274 0.0000000 0.0000000 0.0000000
## 1275 0.0000000 0.0000000 0.0000000
## 1276 0.0000000 0.0000000 0.0000000
## 1277 0.0000000 0.0000000 0.0000000
## 1278 0.0000000 0.0000000 1.0000000
## 1279 0.0000000 0.0000000 0.0000000
## 1280 0.0000000 0.0000000 0.0000000
## 1281 0.0000000 0.0000000 0.0000000
## 1282 0.0000000 0.0000000 1.0000000
## 1283 0.0000000 0.0000000 0.0000000
## 1284 0.0000000 0.0000000 0.0000000
## 1285 0.0000000 0.0000000 0.0000000
## 1286 0.0000000 0.0000000 0.0000000
## 1287 0.0000000 0.0000000 0.0000000
## 1288 0.0000000 0.0000000 1.0000000
## 1289 0.0000000 0.1428571 0.0000000
## 1290 0.0000000 0.0000000 0.0000000
## 1291 0.0000000 0.0000000 0.0000000
## 1292 0.0000000 0.4285714 0.1428571
## 1293 0.0000000 0.0000000 0.0000000
## 1294 0.0000000 0.0000000 0.0000000
## 1295 0.0000000 0.0000000 0.0000000
## 1296 0.0000000 0.0000000 0.0000000
## 1297 0.0000000 0.8571429 0.0000000
## 1298 0.0000000 0.0000000 0.0000000
## 1299 0.0000000 1.0000000 0.0000000
## 1300 0.0000000 0.0000000 0.0000000
## 1301 0.1428571 0.1428571 0.7142857
## 1302 0.0000000 0.0000000 0.4285714
## 1303 0.0000000 0.0000000 0.0000000
## 1304 0.0000000 0.0000000 0.0000000
## 1305 1.0000000 0.0000000 0.0000000
## 1306 1.0000000 0.0000000 0.0000000
## 1307 0.0000000 0.0000000 0.0000000
## 1308 0.1428571 0.0000000 0.0000000
## 1309 0.0000000 0.0000000 0.0000000
## 1310 0.0000000 0.0000000 0.0000000
## 1311 0.0000000 0.0000000 0.0000000
## 1312 0.0000000 0.0000000 0.0000000
## 1313 0.0000000 0.0000000 0.0000000
## 1314 0.0000000 0.0000000 0.0000000
## 1315 0.0000000 0.0000000 0.0000000
## 1316 0.0000000 0.0000000 0.1428571
## 1317 1.0000000 0.0000000 0.0000000
## 1318 0.0000000 0.0000000 0.0000000
## 1319 0.0000000 0.0000000 0.0000000
```

```
## 1320 0.0000000 0.0000000 0.2857143
## 1321 0.0000000 0.8571429 0.0000000
## 1322 0.0000000 0.0000000 0.0000000
## 1323 0.0000000 0.0000000 0.0000000
## 1324 0.0000000 0.0000000 0.8571429
## 1325 0.0000000 0.0000000 1.0000000
## 1326 0.0000000 1.0000000 0.0000000
## 1327 0.0000000 1.0000000 0.0000000
## 1328 0.0000000 0.0000000 0.0000000
## 1329 0.0000000 1.0000000 0.0000000
## 1330 0.0000000 0.0000000 0.0000000
## 1331 0.0000000 1.0000000 0.0000000
## 1332 0.0000000 0.0000000 0.0000000
## 1333 0.0000000 0.0000000 0.0000000
## 1334 0.0000000 1.0000000 0.0000000
## 1335 0.0000000 0.0000000 0.0000000
## 1336 0.0000000 0.0000000 0.0000000
## 1337 0.0000000 0.0000000 0.0000000
## 1338 0.0000000 0.0000000 0.0000000
## 1339 0.0000000 0.0000000 0.0000000
## 1340 0.0000000 0.0000000 0.0000000
## 1341 0.0000000 1.0000000 0.0000000
## 1342 1.0000000 0.0000000 0.0000000
## 1343 0.0000000 0.0000000 1.0000000
## 1344 0.0000000 0.0000000 0.0000000
## 1345 0.0000000 0.0000000 0.0000000
## 1346 0.0000000 0.0000000 0.0000000
## 1347 0.0000000 0.0000000 0.1428571
## 1348 0.0000000 0.0000000 0.0000000
## 1349 1.0000000 0.0000000 0.0000000
## 1350 0.0000000 0.0000000 0.0000000
## 1351 0.8571429 0.0000000 0.0000000
## 1352 0.0000000 0.0000000 0.0000000
## 1353 0.0000000 0.0000000 0.0000000
## 1354 0.0000000 0.0000000 0.0000000
## 1355 0.0000000 0.0000000 0.0000000
## 1356 0.0000000 0.0000000 0.0000000
## 1357 0.0000000 0.0000000 0.0000000
## 1358 0.0000000 0.0000000 0.0000000
## 1359 0.0000000 0.1428571 0.0000000
## 1360 0.1428571 0.0000000 0.8571429
## 1361 0.0000000 1.0000000 0.0000000
## 1362 0.0000000 1.0000000 0.0000000
## 1363 0.0000000 0.0000000 0.0000000
## 1364 0.1428571 0.0000000 0.4285714
## 1365 0.0000000 0.0000000 0.0000000
## 1366 0.0000000 0.0000000 1.0000000
## 1367 0.0000000 0.0000000 0.0000000
## 1368 0.0000000 1.0000000 0.0000000
## 1369 0.0000000 0.0000000 1.0000000
## 1370 1.0000000 0.0000000 0.0000000
## 1371 0.0000000 0.0000000 0.0000000
## 1372 0.0000000 0.0000000 0.0000000
## 1373 0.0000000 0.0000000 0.0000000
```

```
## 1374 0.1428571 0.0000000 0.2857143
## 1375 0.0000000 0.0000000 0.0000000
## 1376 0.0000000 0.0000000 0.0000000
## 1377 1.0000000 0.0000000 0.0000000
## 1378 0.0000000 0.0000000 0.0000000
## 1379 0.0000000 0.0000000 0.0000000
## 1380 0.0000000 0.0000000 0.0000000
## 1381 1.0000000 0.0000000 0.0000000
## 1382 0.0000000 0.0000000 0.0000000
## 1383 0.0000000 0.0000000 0.0000000
## 1384 1.0000000 0.0000000 0.0000000
## 1385 0.0000000 0.0000000 0.8571429
## 1386 0.0000000 0.0000000 0.0000000
## 1387 0.7142857 0.0000000 0.0000000
## 1388 0.0000000 0.0000000 0.0000000
## 1389 0.0000000 0.0000000 0.0000000
## 1390 0.0000000 0.0000000 0.0000000
## 1391 0.0000000 1.0000000 0.0000000
## 1392 0.0000000 0.0000000 0.0000000
## 1393 1.0000000 0.0000000 0.0000000
## 1394 0.0000000 0.0000000 0.0000000
## 1395 0.0000000 0.0000000 0.0000000
## 1396 1.0000000 0.0000000 0.0000000
## 1397 0.0000000 0.0000000 0.0000000
## 1398 0.0000000 0.0000000 0.7142857
## 1399 0.0000000 0.2857143 0.1428571
## 1400 0.0000000 0.0000000 0.0000000
## 1401 0.0000000 0.0000000 0.0000000
## 1402 0.0000000 0.0000000 0.0000000
## 1403 0.0000000 0.0000000 0.0000000
## 1404 0.0000000 0.0000000 0.0000000
## 1405 0.0000000 0.0000000 0.0000000
## 1406 0.0000000 0.0000000 0.0000000
## 1407 0.0000000 0.0000000 0.0000000
## 1408 0.0000000 0.0000000 0.0000000
## 1409 0.0000000 0.0000000 0.0000000
## 1410 0.0000000 0.0000000 0.0000000
## 1411 0.0000000 0.0000000 0.0000000
## 1412 0.0000000 0.0000000 0.0000000
## 1413 0.0000000 0.0000000 0.0000000
## 1414 0.0000000 0.0000000 0.0000000
## 1415 0.0000000 0.0000000 0.0000000
## 1416 0.0000000 0.0000000 0.0000000
## 1417 0.0000000 0.0000000 0.1428571
## 1418 0.0000000 0.0000000 0.1428571
## 1419 0.0000000 0.0000000 0.0000000
## 1420 0.0000000 0.0000000 0.0000000
## 1421 0.0000000 0.0000000 0.0000000
## 1422 0.0000000 0.0000000 0.0000000
## 1423 0.0000000 0.0000000 0.0000000
## 1424 1.0000000 0.0000000 0.0000000
## 1425 0.0000000 0.0000000 0.7142857
## 1426 0.0000000 0.0000000 1.0000000
## 1427 0.0000000 0.2857143 0.4285714
```

```
## 1428 0.0000000 0.0000000 0.0000000
## 1429 0.0000000 0.0000000 0.0000000
## 1430 0.0000000 0.0000000 0.0000000
## 1431 0.0000000 0.0000000 0.0000000
## 1432 0.0000000 0.0000000 0.0000000
## 1433 0.0000000 0.0000000 0.0000000
## 1434 0.0000000 0.0000000 0.0000000
## 1435 1.0000000 0.0000000 0.0000000
## 1436 0.0000000 0.7142857 0.0000000
## 1437 0.0000000 0.0000000 0.1428571
## 1438 0.0000000 0.0000000 0.0000000
## 1439 0.0000000 0.7142857 0.2857143
## 1440 0.0000000 0.0000000 0.0000000
## 1441 0.0000000 0.0000000 0.0000000
## 1442 0.0000000 0.0000000 0.0000000
## 1443 0.0000000 0.0000000 0.0000000
## 1444 0.0000000 0.0000000 0.1428571
## 1445 0.0000000 0.0000000 0.1428571
## 1446 0.0000000 0.0000000 0.0000000
## 1447 0.0000000 1.0000000 0.0000000
## 1448 0.0000000 0.0000000 0.0000000
## 1449 0.0000000 0.0000000 0.0000000
## 1450 0.0000000 0.7142857 0.1428571
## 1451 0.0000000 0.0000000 0.0000000
## 1452 0.0000000 1.0000000 0.0000000
## 1453 0.0000000 0.0000000 0.0000000
## 1454 0.0000000 0.0000000 0.0000000
## 1455 0.0000000 0.5714286 0.4285714
## 1456 0.0000000 0.0000000 0.0000000
## 1457 0.0000000 0.0000000 0.0000000
## 1458 0.0000000 0.0000000 0.0000000
## 1459 0.0000000 0.0000000 0.0000000
## 1460 1.0000000 0.0000000 0.0000000
## 1461 0.0000000 0.0000000 0.0000000
## 1462 0.0000000 0.0000000 1.0000000
## 1463 0.0000000 0.0000000 0.0000000
## 1464 0.0000000 0.0000000 0.0000000
## 1465 0.0000000 0.0000000 0.0000000
## 1466 0.0000000 0.0000000 0.0000000
## 1467 0.0000000 0.0000000 0.0000000
## 1468 0.0000000 0.0000000 0.0000000
## 1469 1.0000000 0.0000000 0.0000000
## 1470 0.0000000 0.0000000 0.0000000
## 1471 0.0000000 0.0000000 0.0000000
## 1472 0.0000000 0.0000000 0.0000000
## 1473 0.0000000 0.0000000 0.0000000
## 1474 0.0000000 0.0000000 0.0000000
## 1475 1.0000000 0.0000000 0.0000000
## 1476 0.0000000 1.0000000 0.0000000
## 1477 0.0000000 1.0000000 0.0000000
## 1478 0.0000000 0.0000000 0.0000000
## 1479 0.0000000 0.0000000 0.0000000
## 1480 0.0000000 0.0000000 0.0000000
## 1481 1.0000000 0.0000000 0.0000000
```

```
## 1482 0.0000000 0.0000000 1.0000000
## 1483 1.0000000 0.0000000 0.0000000
## 1484 0.0000000 0.0000000 0.0000000
## 1485 0.0000000 0.0000000 0.0000000
## 1486 0.0000000 0.1428571 0.0000000
## 1487 0.0000000 0.0000000 1.0000000
## 1488 0.0000000 0.0000000 1.0000000
## 1489 0.0000000 0.0000000 0.0000000
## 1490 0.0000000 0.0000000 0.4285714
## 1491 0.0000000 0.0000000 0.0000000
## 1492 0.0000000 1.0000000 0.0000000
## 1493 0.0000000 0.0000000 0.0000000
## 1494 0.0000000 0.0000000 0.0000000
## 1495 0.0000000 0.8571429 0.1428571
## 1496 0.0000000 0.0000000 0.0000000
## 1497 0.0000000 0.0000000 0.0000000
## 1498 0.0000000 0.0000000 0.0000000
## 1499 0.0000000 0.0000000 0.0000000
## 1500 0.0000000 0.0000000 0.2857143
## 1501 0.0000000 0.0000000 0.0000000
## 1502 0.0000000 0.0000000 1.0000000
## 1503 0.0000000 0.0000000 0.0000000
## 1504 0.0000000 1.0000000 0.0000000
## 1505 0.0000000 0.8571429 0.1428571
## 1506 0.0000000 0.0000000 0.0000000
## 1507 0.0000000 0.0000000 0.0000000
## 1508 0.0000000 0.0000000 0.0000000
## 1509 1.0000000 0.0000000 0.0000000
## 1510 0.0000000 0.0000000 0.0000000
## 1511 0.0000000 0.1428571 0.0000000
## 1512 0.0000000 0.7142857 0.0000000
## 1513 0.0000000 0.0000000 0.7142857
## 1514 0.0000000 0.0000000 0.0000000
## 1515 0.0000000 0.0000000 0.0000000
## 1516 0.0000000 0.0000000 0.1428571
## 1517 0.0000000 0.0000000 0.0000000
## 1518 0.0000000 0.0000000 0.0000000
## 1519 0.0000000 0.0000000 0.0000000
## 1520 0.0000000 1.0000000 0.0000000
## 1521 0.0000000 0.0000000 0.0000000
## 1522 0.0000000 0.0000000 0.0000000
## 1523 0.0000000 0.0000000 0.1428571
## 1524 0.0000000 0.0000000 0.0000000
## 1525 0.0000000 0.0000000 0.0000000
## 1526 1.0000000 0.0000000 0.0000000
## 1527 0.0000000 0.0000000 0.0000000
## 1528 0.0000000 0.0000000 0.0000000
## 1529 0.0000000 0.0000000 0.0000000
## 1530 0.0000000 1.0000000 0.0000000
## 1531 0.0000000 0.0000000 0.0000000
## 1532 0.0000000 0.0000000 0.0000000
## 1533 0.0000000 0.0000000 0.0000000
## 1534 0.0000000 0.7142857 0.0000000
## 1535 0.0000000 0.0000000 0.0000000
```

```
## 1536 0.0000000 0.0000000 0.0000000
## 1537 0.0000000 0.0000000 0.0000000
## 1538 0.0000000 0.0000000 0.0000000
## 1539 0.1428571 0.0000000 0.0000000
## 1540 0.0000000 0.0000000 0.0000000
## 1541 1.0000000 0.0000000 0.0000000
## 1542 0.0000000 0.0000000 1.0000000
## 1543 0.0000000 0.0000000 0.7142857
## 1544 0.0000000 0.0000000 0.0000000
## 1545 0.0000000 0.0000000 0.0000000
## 1546 0.0000000 0.0000000 1.0000000
## 1547 0.0000000 0.0000000 0.0000000
## 1548 0.0000000 0.0000000 0.0000000
## 1549 0.0000000 0.0000000 0.0000000
## 1550 0.0000000 0.0000000 0.0000000
## 1551 0.0000000 0.0000000 0.8571429
## 1552 0.0000000 0.0000000 0.0000000
## 1553 0.0000000 0.0000000 0.0000000
## 1554 0.0000000 0.0000000 0.0000000
## 1555 0.0000000 0.8571429 0.0000000
## 1556 0.0000000 0.0000000 0.0000000
## 1557 1.0000000 0.0000000 0.0000000
## 1558 0.0000000 0.0000000 0.0000000
## 1559 0.0000000 0.0000000 0.0000000
## 1560 0.0000000 0.0000000 0.0000000
## 1561 1.0000000 0.0000000 0.0000000
## 1562 0.0000000 0.0000000 0.0000000
## 1563 0.0000000 0.0000000 0.0000000
## 1564 0.0000000 0.1428571 0.4285714
## 1565 0.0000000 0.0000000 0.0000000
## 1566 0.0000000 0.0000000 0.8571429
## 1567 1.0000000 0.0000000 0.0000000
## 1568 0.0000000 0.0000000 0.0000000
## 1569 0.0000000 0.0000000 0.0000000
## 1570 0.0000000 0.0000000 0.0000000
## 1571 0.0000000 0.0000000 0.0000000
## 1572 0.0000000 0.0000000 0.0000000
## 1573 0.0000000 0.0000000 0.0000000
## 1574 0.0000000 0.0000000 1.0000000
## 1575 0.0000000 0.0000000 0.0000000
## 1576 0.0000000 0.0000000 1.0000000
## 1577 0.0000000 0.0000000 0.0000000
## 1578 0.0000000 1.0000000 0.0000000
## 1579 0.0000000 0.0000000 0.0000000
## 1580 0.0000000 0.0000000 0.0000000
## 1581 0.0000000 0.0000000 0.0000000
## 1582 0.0000000 0.0000000 0.1428571
## 1583 0.0000000 0.0000000 0.0000000
## 1584 0.0000000 0.0000000 0.0000000
## 1585 0.0000000 0.8571429 0.1428571
## 1586 0.0000000 0.0000000 0.0000000
## 1587 0.0000000 0.0000000 0.0000000
## 1588 0.0000000 0.0000000 0.0000000
## 1589 0.0000000 0.0000000 0.0000000
```

```
## 1590 0.0000000 1.0000000 0.0000000
## 1591 0.0000000 0.0000000 0.0000000
## 1592 0.0000000 0.0000000 0.0000000
## 1593 0.0000000 0.0000000 0.0000000
## 1594 0.0000000 1.0000000 0.0000000
## 1595 0.0000000 0.0000000 0.0000000
## 1596 0.0000000 0.0000000 0.0000000
## 1597 1.0000000 0.0000000 0.0000000
## 1598 0.0000000 0.0000000 0.0000000
## 1599 0.0000000 0.0000000 1.0000000
## 1600 0.0000000 0.0000000 0.0000000
## 1601 0.0000000 0.0000000 0.1428571
## 1602 0.0000000 0.0000000 0.2857143
## 1603 0.0000000 1.0000000 0.0000000
## 1604 0.0000000 0.0000000 0.0000000
## 1605 0.0000000 0.0000000 0.0000000
## 1606 0.0000000 0.0000000 0.0000000
## 1607 0.0000000 0.0000000 0.0000000
## 1608 0.0000000 0.0000000 1.0000000
## 1609 0.0000000 1.0000000 0.0000000
## 1610 0.0000000 0.0000000 0.0000000
## 1611 0.0000000 0.0000000 0.0000000
## 1612 0.0000000 0.0000000 1.0000000
## 1613 0.0000000 0.0000000 0.0000000
## 1614 0.0000000 0.0000000 0.0000000
## 1615 0.0000000 0.0000000 0.0000000
## 1616 0.0000000 0.0000000 0.0000000
## 1617 0.0000000 0.0000000 0.0000000
## 1618 0.0000000 0.0000000 0.0000000
## 1619 1.0000000 0.0000000 0.0000000
## 1620 0.0000000 0.0000000 0.0000000
## 1621 0.0000000 0.0000000 0.0000000
## 1622 0.0000000 0.0000000 0.0000000
## 1623 0.0000000 0.0000000 0.2857143
## 1624 0.0000000 0.0000000 0.0000000
## 1625 0.0000000 0.0000000 0.0000000
## 1626 0.0000000 0.0000000 1.0000000
## 1627 0.0000000 1.0000000 0.0000000
## 1628 0.0000000 0.0000000 0.0000000
## 1629 0.0000000 0.0000000 0.0000000
## 1630 0.0000000 1.0000000 0.0000000
## 1631 0.0000000 0.0000000 1.0000000
## 1632 0.0000000 0.0000000 0.0000000
## 1633 0.0000000 0.0000000 0.0000000
## 1634 0.0000000 0.0000000 0.0000000
## 1635 0.0000000 0.0000000 0.0000000
## 1636 0.0000000 0.0000000 0.0000000
## 1637 0.0000000 0.0000000 0.0000000
## 1638 0.0000000 0.0000000 0.0000000
## 1639 0.0000000 0.0000000 0.0000000
## 1640 0.0000000 0.0000000 0.0000000
## 1641 0.0000000 0.0000000 0.0000000
## 1642 0.0000000 0.0000000 0.0000000
## 1643 0.0000000 0.0000000 0.0000000
```

```
## 1644 0.0000000 0.0000000 0.1428571
## 1645 0.0000000 0.0000000 0.0000000
## 1646 0.0000000 0.0000000 0.0000000
## 1647 0.0000000 0.0000000 0.0000000
## 1648 1.0000000 0.0000000 0.0000000
## 1649 0.0000000 0.0000000 0.0000000
## 1650 0.0000000 1.0000000 0.0000000
## 1651 0.0000000 0.0000000 0.0000000
## 1652 0.0000000 0.0000000 0.0000000
## 1653 0.0000000 0.0000000 0.0000000
## 1654 0.0000000 1.0000000 0.0000000
## 1655 1.0000000 0.0000000 0.0000000
## 1656 0.0000000 0.0000000 0.0000000
## 1657 0.0000000 0.0000000 0.0000000
## 1658 0.0000000 0.1428571 0.0000000
## 1659 0.0000000 0.0000000 0.0000000
## 1660 0.7142857 0.0000000 0.1428571
## 1661 0.0000000 0.0000000 0.0000000
## 1662 0.0000000 0.0000000 0.0000000
## 1663 0.0000000 0.8571429 0.0000000
## 1664 0.0000000 0.0000000 0.0000000
## 1665 0.0000000 0.0000000 0.0000000
## 1666 0.0000000 0.0000000 0.0000000
## 1667 0.0000000 0.0000000 0.0000000
## 1668 0.0000000 0.0000000 0.0000000
## 1669 0.0000000 0.0000000 0.0000000
## 1670 0.0000000 0.0000000 0.0000000
## 1671 0.0000000 0.0000000 0.0000000
## 1672 0.0000000 0.0000000 0.0000000
## 1673 0.0000000 0.8571429 0.0000000
## 1674 0.0000000 0.0000000 0.0000000
## 1675 0.0000000 0.0000000 0.0000000
## 1676 0.0000000 0.0000000 0.0000000
## 1677 0.0000000 0.0000000 1.0000000
## 1678 0.0000000 0.0000000 0.5714286
## 1679 0.0000000 1.0000000 0.0000000
## 1680 0.0000000 0.0000000 0.0000000
## 1681 0.0000000 0.0000000 0.0000000
## 1682 0.0000000 0.0000000 0.0000000
## 1683 0.0000000 0.0000000 0.0000000
## 1684 0.0000000 0.0000000 0.0000000
## 1685 0.0000000 0.5714286 0.0000000
## 1686 0.0000000 0.0000000 0.0000000
## 1687 0.0000000 0.7142857 0.0000000
## 1688 0.0000000 0.0000000 0.0000000
## 1689 0.0000000 0.0000000 0.0000000
## 1690 0.0000000 0.0000000 1.0000000
## 1691 0.0000000 0.0000000 0.0000000
## 1692 0.0000000 0.0000000 1.0000000
## 1693 0.0000000 0.0000000 0.0000000
## 1694 0.0000000 0.0000000 0.0000000
## 1695 0.0000000 0.0000000 0.0000000
## 1696 0.0000000 0.0000000 0.0000000
## 1697 0.0000000 0.0000000 0.0000000
```

```
## 1698 0.0000000 0.0000000 0.0000000
## 1699 0.0000000 0.0000000 0.0000000
## 1700 1.0000000 0.0000000 0.0000000
## 1701 1.0000000 0.0000000 0.0000000
## 1702 0.0000000 0.0000000 0.0000000
## 1703 0.0000000 0.0000000 0.0000000
## 1704 0.0000000 0.0000000 0.0000000
## 1705 0.0000000 0.0000000 0.0000000
## 1706 0.0000000 0.0000000 0.0000000
## 1707 0.0000000 0.0000000 0.0000000
## 1708 0.0000000 0.0000000 0.0000000
## 1709 0.0000000 0.0000000 0.0000000
## 1710 0.0000000 0.0000000 0.0000000
## 1711 0.0000000 0.0000000 1.0000000
## 1712 1.0000000 0.0000000 0.0000000
## 1713 0.0000000 0.0000000 0.0000000
## 1714 0.0000000 1.0000000 0.0000000
## 1715 0.0000000 0.0000000 0.0000000
## 1716 0.7142857 0.0000000 0.1428571
## 1717 1.0000000 0.0000000 0.0000000
## 1718 0.0000000 0.0000000 0.0000000
## 1719 0.0000000 0.0000000 0.0000000
## 1720 0.0000000 0.0000000 0.0000000
## 1721 0.0000000 0.0000000 0.0000000
## 1722 0.0000000 0.0000000 0.0000000
## 1723 0.0000000 0.0000000 0.0000000
## 1724 0.8571429 0.0000000 0.1428571
## 1725 0.0000000 0.0000000 0.0000000
## 1726 0.0000000 0.8571429 0.0000000
## 1727 0.0000000 0.0000000 0.0000000
## 1728 0.0000000 0.0000000 0.2857143
## 1729 0.0000000 0.0000000 1.0000000
## 1730 0.0000000 0.0000000 0.0000000
## 1731 0.0000000 0.0000000 0.0000000
## 1732 0.0000000 0.0000000 0.0000000
## 1733 0.0000000 0.0000000 0.0000000
## 1734 0.0000000 1.0000000 0.0000000
## 1735 0.0000000 0.0000000 0.0000000
## 1736 0.0000000 0.0000000 0.0000000
## 1737 0.0000000 0.0000000 0.0000000
## 1738 0.0000000 0.0000000 0.0000000
## 1739 0.0000000 0.0000000 0.0000000
## 1740 0.0000000 0.0000000 0.0000000
## 1741 0.0000000 0.0000000 0.0000000
## 1742 0.0000000 0.0000000 0.0000000
## 1743 0.0000000 0.0000000 0.0000000
## 1744 1.0000000 0.0000000 0.0000000
## 1745 0.0000000 0.0000000 1.0000000
## 1746 0.0000000 0.0000000 0.0000000
## 1747 0.0000000 0.0000000 0.0000000
## 1748 0.0000000 0.8571429 0.0000000
## 1749 0.0000000 0.0000000 0.0000000
## 1750 0.0000000 0.0000000 0.0000000
## 1751 0.0000000 0.0000000 0.0000000
```

```
## 1752 0.0000000 0.0000000 0.0000000
## 1753 0.0000000 0.0000000 0.0000000
## 1754 0.0000000 0.0000000 0.0000000
## 1755 0.0000000 0.0000000 0.0000000
## 1756 0.0000000 0.0000000 0.0000000
## 1757 0.0000000 0.0000000 0.0000000
## 1758 0.0000000 0.0000000 0.8571429
## 1759 0.0000000 0.0000000 0.0000000
## 1760 0.0000000 0.0000000 0.0000000
## 1761 0.0000000 0.0000000 0.8571429
## 1762 0.0000000 0.1428571 0.0000000
## 1763 0.0000000 0.0000000 0.0000000
## 1764 0.5714286 0.0000000 0.4285714
## 1765 1.0000000 0.0000000 0.0000000
## 1766 0.0000000 0.7142857 0.0000000
## 1767 0.0000000 1.0000000 0.0000000
## 1768 0.0000000 0.8571429 0.0000000
## 1769 0.0000000 0.0000000 0.0000000
## 1770 0.0000000 0.0000000 0.0000000
## 1771 0.0000000 0.8571429 0.0000000
## 1772 0.0000000 0.0000000 0.0000000
## 1773 0.4285714 0.0000000 0.0000000
## 1774 0.5714286 0.0000000 0.0000000
## 1775 0.0000000 0.0000000 0.0000000
## 1776 0.0000000 0.0000000 0.0000000
## 1777 0.0000000 0.0000000 0.0000000
## 1778 0.0000000 0.0000000 0.0000000
## 1779 0.0000000 0.0000000 0.0000000
## 1780 0.0000000 0.0000000 0.0000000
## 1781 0.0000000 0.0000000 0.0000000
## 1782 0.0000000 0.0000000 0.0000000
## 1783 0.0000000 0.0000000 0.0000000
## 1784 0.0000000 0.0000000 0.0000000
## 1785 0.0000000 0.0000000 0.0000000
## 1786 0.0000000 0.0000000 0.0000000
## 1787 0.0000000 0.0000000 0.0000000
## 1788 0.0000000 0.0000000 1.0000000
## 1789 0.0000000 0.0000000 0.0000000
## 1790 0.0000000 0.0000000 0.0000000
## 1791 0.0000000 0.7142857 0.0000000
## 1792 0.0000000 1.0000000 0.0000000
## 1793 0.0000000 0.8571429 0.0000000
## 1794 0.0000000 0.0000000 0.0000000
## 1795 0.0000000 0.0000000 0.0000000
## 1796 0.0000000 0.0000000 0.0000000
## 1797 0.0000000 0.5714286 0.0000000
## 1798 0.0000000 0.0000000 0.0000000
## 1799 0.0000000 0.0000000 0.0000000
## 1800 0.0000000 0.0000000 0.0000000
## 1801 0.0000000 0.0000000 0.0000000
## 1802 1.0000000 0.0000000 0.0000000
## 1803 0.0000000 0.0000000 0.0000000
## 1804 0.0000000 1.0000000 0.0000000
## 1805 0.0000000 0.8571429 0.0000000
```

```
## 1806 0.0000000 0.0000000 0.0000000
## 1807 0.0000000 0.0000000 0.0000000
## 1808 0.0000000 0.0000000 0.0000000
## 1809 0.0000000 0.0000000 1.0000000
## 1810 0.0000000 0.0000000 1.0000000
## 1811 0.0000000 0.0000000 0.0000000
## 1812 0.0000000 0.0000000 0.0000000
## 1813 0.0000000 0.0000000 0.0000000
## 1814 0.0000000 0.0000000 0.0000000
## 1815 0.0000000 0.0000000 0.0000000
## 1816 0.0000000 1.0000000 0.0000000
## 1817 0.0000000 0.0000000 0.0000000
## 1818 1.0000000 0.0000000 0.0000000
## 1819 0.0000000 0.0000000 0.0000000
## 1820 0.0000000 0.0000000 0.0000000
## 1821 0.0000000 0.0000000 0.0000000
## 1822 1.0000000 0.0000000 0.0000000
## 1823 0.0000000 0.0000000 1.0000000
## 1824 0.0000000 0.0000000 0.0000000
## 1825 0.0000000 0.0000000 0.0000000
## 1826 0.0000000 0.0000000 0.0000000
## 1827 0.0000000 0.0000000 0.1428571
## 1828 0.0000000 0.0000000 0.0000000
## 1829 0.0000000 0.0000000 0.0000000
## 1830 1.0000000 0.0000000 0.0000000
## 1831 0.0000000 0.0000000 0.0000000
## 1832 0.0000000 0.7142857 0.1428571
## 1833 0.0000000 0.0000000 0.0000000
## 1834 0.0000000 0.0000000 0.0000000
## 1835 0.0000000 0.0000000 1.0000000
## 1836 0.0000000 0.0000000 0.0000000
## 1837 0.0000000 0.0000000 0.0000000
## 1838 0.0000000 0.0000000 0.0000000
## 1839 0.0000000 0.0000000 0.0000000
## 1840 1.0000000 0.0000000 0.0000000
## 1841 0.0000000 0.0000000 0.0000000
## 1842 0.0000000 0.0000000 0.0000000
## 1843 0.0000000 1.0000000 0.0000000
## 1844 0.0000000 0.0000000 1.0000000
## 1845 0.0000000 0.0000000 0.0000000
## 1846 0.0000000 0.0000000 0.0000000
## 1847 0.0000000 0.0000000 0.0000000
## 1848 0.0000000 0.0000000 0.0000000
## 1849 0.0000000 0.0000000 0.0000000
## 1850 0.0000000 0.0000000 0.0000000
## 1851 0.0000000 1.0000000 0.0000000
## 1852 0.0000000 0.0000000 0.0000000
## 1853 0.0000000 0.0000000 0.0000000
## 1854 0.0000000 0.0000000 1.0000000
## 1855 0.0000000 0.0000000 0.0000000
## 1856 1.0000000 0.0000000 0.0000000
## 1857 0.0000000 0.0000000 1.0000000
## 1858 0.0000000 0.0000000 0.1428571
## 1859 0.0000000 0.0000000 0.0000000
```

```
## 1860 0.0000000 0.0000000 0.0000000
## 1861 0.0000000 1.0000000 0.0000000
## 1862 0.1428571 0.0000000 0.0000000
## 1863 0.0000000 0.0000000 0.0000000
## 1864 0.0000000 0.0000000 0.0000000
## 1865 0.0000000 1.0000000 0.0000000
## 1866 0.0000000 0.0000000 0.0000000
## 1867 0.0000000 0.0000000 0.0000000
## 1868 1.0000000 0.0000000 0.0000000
## 1869 0.0000000 0.1428571 0.0000000
## 1870 0.0000000 0.0000000 0.0000000
## 1871 0.0000000 0.0000000 0.5714286
## 1872 1.0000000 0.0000000 0.0000000
## 1873 0.0000000 0.0000000 0.0000000
## 1874 0.5714286 0.0000000 0.0000000
## 1875 0.0000000 0.0000000 0.0000000
## 1876 0.0000000 1.0000000 0.0000000
## 1877 0.0000000 0.0000000 0.0000000
## 1878 0.0000000 0.0000000 0.1428571
## 1879 1.0000000 0.0000000 0.0000000
## 1880 0.0000000 0.0000000 0.7142857
## 1881 1.0000000 0.0000000 0.0000000
## 1882 0.0000000 0.0000000 0.0000000
## 1883 0.0000000 0.0000000 0.2857143
## 1884 0.0000000 0.0000000 0.0000000
## 1885 1.0000000 0.0000000 0.0000000
## 1886 0.0000000 1.0000000 0.0000000
## 1887 0.0000000 0.0000000 1.0000000
## 1888 0.0000000 0.0000000 0.0000000
## 1889 0.0000000 0.0000000 0.0000000
## 1890 0.0000000 0.5714286 0.0000000
## 1891 0.0000000 0.0000000 0.2857143
## 1892 0.0000000 0.0000000 0.0000000
## 1893 0.0000000 0.0000000 0.0000000
## 1894 0.0000000 0.0000000 0.0000000
## 1895 0.0000000 0.0000000 0.0000000
## 1896 0.0000000 0.0000000 1.0000000
## 1897 0.0000000 0.5714286 0.1428571
## 1898 0.0000000 0.0000000 0.0000000
## 1899 0.0000000 0.0000000 0.0000000
## 1900 1.0000000 0.0000000 0.0000000
## 1901 0.0000000 0.0000000 0.0000000
## 1902 0.0000000 0.0000000 0.0000000
## 1903 0.0000000 0.0000000 0.0000000
## 1904 0.0000000 0.0000000 0.0000000
## 1905 0.0000000 0.0000000 0.8571429
## 1906 0.0000000 0.0000000 0.0000000
## 1907 0.0000000 0.0000000 0.0000000
## 1908 0.0000000 0.0000000 0.0000000
## 1909 0.0000000 0.0000000 0.0000000
## 1910 0.0000000 0.0000000 0.0000000
## 1911 0.0000000 0.5714286 0.0000000
## 1912 0.0000000 0.0000000 0.0000000
## 1913 0.0000000 0.0000000 0.0000000
```

### 3.3 Predict on the test data

```
knn_test_model <- kknn(formula, train = train_digitals, test = test_digitals, k = 30, kernel = 'rectang
print(length(knn_test_model$fitted.values))
## [1] 953</pre>
```

# 3.4 Confusion matrices and Misclassification errors for train data and test data

```
train_confusion <- table(train_digitals$V65, train_predictions)</pre>
test_confusion <- table(test_digitals$V65, knn_test_model$fitted.values)</pre>
test_error_rate <- 1 - sum(diag(test_confusion)) / sum(test_confusion)</pre>
train_error_rate <- 1- sum(diag(train_confusion)) / sum(train_confusion)</pre>
# only observer the top 10 rows
cat("Misclassification errors on train data:", train_error_rate, '\n')
## Misclassification errors on train data: 0.02089864
cat("train_confusion:")
## train_confusion:
table(train_digitals$V65[1:10], train_predictions[1:10])
##
       0 1 2 3 4 5 6 7 8 9
##
     0 3 0 0 0 0 0 0 0 0 0
##
     1 0 0 0 0 0 0 0 0 0
##
##
     2 0 0 1 0 0 0 0 0 0 0
##
    3 0 0 0 0 0 0 0 0 0
     4 0 0 0 0 1 0 0 0 0 1
##
##
    5 0 0 0 0 0 1 0 0 0 0
    6 0 0 0 0 0 0 0 0 0 0
##
    7 0 0 0 0 0 0 0 1 0 0
##
    8 0 0 0 0 0 0 0 0 1 0
##
     9 0 0 0 0 0 0 0 0 0 1
cat("Misclassification errors on test data:", test error rate, '\n')
## Misclassification errors on test data: 0.04721931
cat("test confusion:")
## test confusion:
```

```
table(test_digitals$V65[1:10], knn_test_model$fitted.values[1:10])
##
      0 1 2 3 4 5 6 7 8 9
##
##
    0 2 0 0 0 0 0 0 0 0
##
    1 0 1 0 0 0 0 0 0 0 0
    200000000000
##
##
    3 0 0 0 0 0 0 0 0 0 0
    4 0 0 0 0 0 0 0 0 0 0
##
##
    5 0 0 0 0 0 2 0 0 0 0
##
    6 0 0 0 0 0 0 1 0 0 0
    70000000000
   80000000020
##
    90000100001
```

3.5 Filter 2 cases of digit "8" in the training data which were easiest to classify and 3 cases that were hardest to classify

```
# filter the digital '8'
library(dplyr)

train_predict <- data.frame(train_digitals$V65, train_predictions,knn_train_model$prob)
train_predict$max_prob <- apply(train_predict[,3:12], 1, max)

train_predict_8 <- train_predict[train_predict$train_digitals.V65 == 8,]
# do not change the index while sorting
train_predict_8 <- train_predict_8[order(train_predict_8$X8), , drop = FALSE]

# get the 3 cases that were hardest to classify
hardest_cases_for_8 <- train_predict_8 %>% head(3)
easy_cases_for_8 <- train_predict_8 %>% tail(2)
```

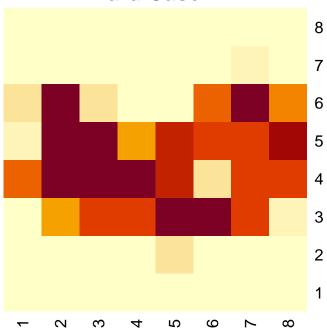
### 3.6 Analysis the difference of the hardest case and easiest cases

we can see on the heatmap that the hardest cases are more complex than the easiest cases. Dark-colored squares concentrated in the middle of the matrix while the easiest cases are more concentrated on the edges which looking more like the number 8.

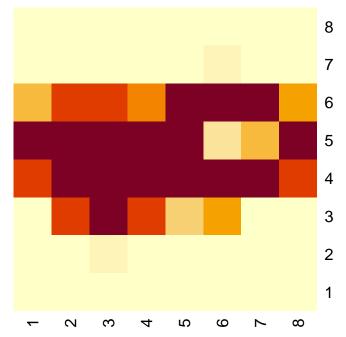
```
hardest_cases_index <- rownames(hardest_cases_for_8)
est_cases_index <- rownames(easy_cases_for_8)
# reindex the row index
row.names(train_digitals) <- NULL
full_hardest_cases <- train_digitals[hardest_cases_index,1:64]
full_est_cases <- train_digitals[est_cases_index,1:64]
hardest_matrixs <- lapply(1:nrow(full_hardest_cases), function(i) matrix(as.numeric(full_hardest_cases[est_matrixs <- lapply(1:nrow(full_est_cases), function(i) matrix(as.numeric(full_est_cases[i, , drop = ])
for (i in 1:length(hardest_matrixs)) {
    mat <- hardest matrixs[[i]]</pre>
```

heatmap(mat, Colv = NA, Rowv = NA, scale = "none", main = paste("Hard Case", i))
}

**Hard Case 1** 



**Hard Case 2** 



# Hard Case 3 8 7 6 5 4 3 2

```
for (i in 1:length(est_matrixs)) {
mat <- est_matrixs[[i]]
heatmap(mat, Colv = NA, Rowv = NA, scale = "none", main = paste("Hard Case", i))
}</pre>
```

2

 $\infty$ 

/

Hard Case 1

8

7

6

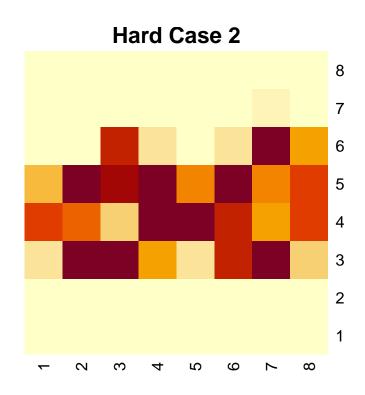
5

4

3

2

1

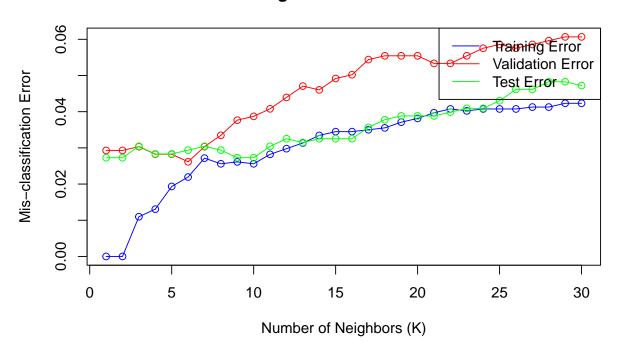


### 3.7 Training via different k in on the training and validation data

according the plot , k=3 is best value on training data and validation data, though the performance of k=1 is better than k=3 on training data, it is not the best value on validation data due to the weak generalization ability, but when we apply it on test data, its performance is not as good as predicted

```
library(ggplot2)
train_error_rates <- list()</pre>
valid_error_rates <- list()</pre>
test_error_rates <- list()</pre>
for (ki in 1:30) {
# cat(paste("current k:",ki,"\n",sep=""))
train_ki_model <- kknn(formula, train = train_digitals, test = train_digitals, k = ki, kernel = 'rectan
valid_ki_model <- kknn(formula, train = train_digitals, test = valid_digitals, k = ki, kernel = 'rectan</pre>
test_ki_model <- kknn(formula, train = train_digitals, test = test_digitals, k = ki, kernel = 'rectangu
train_confusion <- table(train_digitals$V65, train_ki_model$fitted.values)
valid_confusion <- table(valid_digitals$V65, valid_ki_model$fitted.values)</pre>
test_confusion <- table(test_digitals$V65, test_ki_model$fitted.values)</pre>
train_error_rate <- sum(diag(train_confusion)) / sum(train_confusion)</pre>
valid_error_rate <- sum(diag(valid_confusion)) / sum(valid_confusion)</pre>
test_error_rate <- sum(diag(test_confusion)) / sum(test_confusion)</pre>
# print(train_error_rate)
# print(valid error rate)
train_error_rates[[ki]] <- 1 - train_error_rate</pre>
valid_error_rates[[ki]] <- 1 - valid_error_rate</pre>
test_error_rates[[ki]] <- 1 - test_error_rate</pre>
}
plot(1:30, train_error_rates, type = "o", col = "blue", ylim = range(c(train_error_rates, valid_error_r
xlab = "Number of Neighbors (K)", ylab = "Mis-classification Error", main = "Training and Validation E
lines(1:30, valid_error_rates, type = "o", col = "red")
lines(1:30, test_error_rates, type = "o", col = "green")
legend("topright", legend = c("Training Error", "Validation Error", "Test Error"), col = c("blue", "red"
```

# **Training and Validation Errors**



3.8 Change mis-classification error to cross-entropy

```
valid_cross_entropy_errors <- list()</pre>
train_cross_entropy_errors <- list()</pre>
test_cross_entropy_errors <- list()</pre>
for (ki in 1:30) {
  print(ki)
  valid_ki_model <- kknn(formula, train = train_digitals, test = valid_digitals, k = ki, kernel = 'rect
  train_ki_model <- kknn(formula, train = train_digitals, test = train_digitals, k = ki, kernel = 'rect
  test_ki_model <- kknn(formula, train = train_digitals, test = test_digitals, k = ki, kernel = 'rectan
  valid_probs <- valid_ki_model$prob</pre>
  train_probs <- train_ki_model$prob</pre>
  test_probs <- test_ki_model$prob</pre>
  valid_log_probs <- log(valid_probs + 1e-15) # Add small constant to avoid log(0)
  train_log_probs <- log(train_probs + 1e-15) # Add small constant to avoid log(0)
  test_log_probs <- log(test_probs + 1e-15) # Add small constant to avoid log(0)
# -1 means do not contain intercept
# One-hot encoding
 #This type of matrix is typically used in machine learning and statistical modeling for feature
 valid_correct_class <- model.matrix(~V65 - 1, data = valid_digitals) # One-hot encoding</pre>
```

```
train_correct_class <- model.matrix(~V65 - 1, data = train_digitals) # One-hot encoding
  test_correct_class <- model.matrix(~V65 - 1, data = test_digitals) # One-hot encoding
  valid_cross_entropy_errors[[ki]] <- -sum(valid_correct_class * valid_log_probs) / nrow(valid_digitals
  train_cross_entropy_errors[[ki]] <- -sum(train_correct_class * train_log_probs) / nrow(train_digitals</pre>
  test_cross_entropy_errors[[ki]] <- -sum(test_correct_class * test_log_probs) / nrow(test_digitals)</pre>
  print(-sum(valid_correct_class * valid_log_probs) )
  print(-sum(train_correct_class * train_log_probs))
  print(-sum(test_correct_class * test_log_probs) )
## [1] 1
## [1] 967.0857
## [1] -2.124967e-12
## [1] 898.0082
## [1] 2
## [1] 612.1125
## [1] 38.12309
## [1] 476.0368
## [1] 3
## [1] 388.562
## [1] 67.253
## [1] 254.5658
## [1] 4
## [1] 362.3618
## [1] 89.86939
## [1] 225.2532
## [1] 5
## [1] 338.8529
## [1] 110.6789
## [1] 232.5973
## [1] 6
## [1] 311.8849
## [1] 126.1048
## [1] 236.833
## [1] 7
## [1] 284.2781
## [1] 138.6058
## [1] 209.5096
## [1] 8
```

## [1] 259.7015 ## [1] 149.4795 ## [1] 182.5826

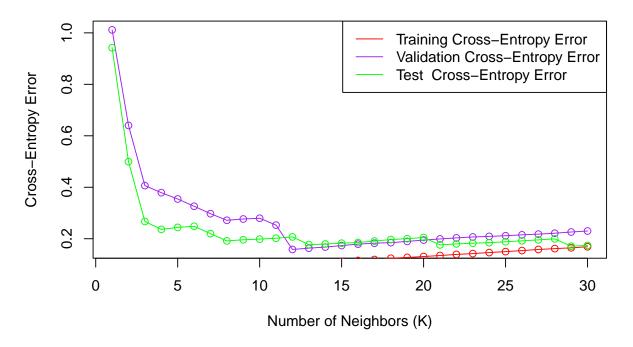
## [1] 264.5245 ## [1] 157.0067 ## [1] 186.7068 ## [1] 10 ## [1] 267.2868 ## [1] 166.6238 ## [1] 189.2299 ## [1] 11 ## [1] 241.7661

## [1] 9

- ## [1] 178.0273
- ## [1] 192.4262
- ## [1] 12
- ## [1] 151.429
- ## [1] 185.4844
- ## [1] 197.3325
- ## [1] 13
- ## [1] 156.0633
- ## [1] 194.9527
- ## [1] 168.8002
- ## [1] 14
- ## [1] 160.3023
- ## [1] 205.5017
- ## [1] 171.0371
- ## [1] 15
- ## [1] 165.7658
- ## [1] 213.1857
- ## [1] 174.0305
- ## [1] 16
- ## [1] 171.1277
- ## [1] 221.096
- ## [1] 176.5297
- ## [1] 17
- ## [1] 174.6855
- ## [1] 228.2865
- ## [1] 181.8136
- ## [1] 18
- ## [1] 176.7252
- ## [1] 237.5138
- ## [1] 187.6836
- ## [1] 19
- ## [1] 181.2064
- ## [1] 243.7894
- ## [1] 190.8063
- ## [1] 20
- ## [1] 186.2564
- ## [1] 250.4809
- ## [1] 195.0437
- ## [1] 21
- ## [1] 190.4043
- ## [1] 257.8845
- ## [1] 167.8248
- ## [1] 22
- ## [1] 194.3442
- ## [1] 266.0269
- ## [1] 171.3782
- ## [1] 23
- ## [1] 197.7436
- ## [1] 272.1304
- ## [1] 174.0031
- ## [1] 24
- ## [1] 199.8902
- ## [1] 279.939
- ## [1] 175.9505

```
## [1] 25
## [1] 202.3265
## [1] 286.8985
## [1] 179.3611
## [1] 26
## [1] 205.6806
## [1] 294.7098
## [1] 182.7899
## [1] 27
## [1] 208.3324
## [1] 302.9172
## [1] 186.4286
## [1] 28
## [1] 211.6151
## [1] 309.1722
## [1] 190.1569
## [1] 29
## [1] 216.1674
## [1] 315.2465
## [1] 162.8209
## [1] 30
## [1] 219.9063
## [1] 322.8643
## [1] 165.8777
```

# **Validation Cross-Entropy Error**



# 4 Assignment 2: Linear regression and ridge regression

### 4.1 set up

We need to download some useful packages before the start.

```
install.packages("caret")

## Warning: package 'caret' is in use and will not be installed
library(caret)
```

### 4.2 Prepare the dataset

Firstly, we read the file and divided the data into training and test data (60/40).

```
data <- read.csv("../data/parkinsons.csv") #
set.seed(42)
ini_sample<- sample(1:nrow(data),0.6*nrow(data))
train_data<- data[ini_sample,]
test_data<- data[-ini_sample,]</pre>
```

And then we scaled the dataset appropriately.

```
sacale_data<- train_data[,names(train_data)!="motor_UPDRS"]
scale_para<- preProcess(sacale_data)
train_data_scaled<- predict(scale_para,train_data)
test_data_scaled<- predict(scale_para,test_data)
train_data_scaled$motor_UPDRS <- train_data$motor_UPDRS
test_data_scaled$motor_UPDRS <- test_data$motor_UPDRS</pre>
```

### 4.3 Build models

Next, we computed a linear regression model, estimate training and test MSE

```
model<- lm(motor_UPDRS ~ .,train_data_scaled)
train_prediction<- predict(model,train_data_scaled)
train_mse<- mean((train_prediction - train_data_scaled$motor_UPDRS)^2)
test_prediction<- predict(model,test_data_scaled)
test_mse<- mean((test_prediction - test_data_scaled$motor_UPDRS)^2)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = motor_UPDRS ~ ., data = train_data_scaled)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                     Max
## -8.4962 -1.3230 0.1978 1.6722 6.7627
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 21.27888
                            0.04240 501.883 < 2e-16 ***
## subject.
                 -0.12900
                             0.04908 -2.628 0.008618 **
## age
                 -0.23517
                          0.04615 -5.095 3.66e-07 ***
                 0.45948
                            0.05173
                                      8.883 < 2e-16 ***
## sex
                            0.04293 -1.204 0.228664
## test_time
                 -0.05169
## total UPDRS
                 7.81829
                            0.04892 159.827 < 2e-16 ***
                 1.48149
                          0.41073
                                     3.607 0.000314 ***
## Jitter...
                 -0.55937
## Jitter.Abs.
                          0.11441 -4.889 1.06e-06 ***
## Jitter.RAP
                -49.61179 52.25757 -0.949 0.342498
## Jitter.PPQ5
                 -0.31807
                            0.23637 -1.346 0.178500
## Jitter.DDP
                 48.67488
                           52.25602
                                     0.931 0.351675
## Shimmer
                 1.00327
                            0.54793
                                     1.831 0.067183 .
## Shimmer.dB.
                 -0.06932
                             0.39046 -0.178 0.859095
## Shimmer.APQ3
                71.26529 209.14155
                                     0.341 0.733311
## Shimmer.APQ5
                -1.36309
                             0.30045 -4.537 5.90e-06 ***
## Shimmer.APQ11 0.57158
                             0.15977
                                      3.577 0.000352 ***
## Shimmer.DDA
                -71.24366 209.14168 -0.341 0.733389
## NHR
                  0.09299
                            0.12189
                                      0.763 0.445542
## HNR
                  0.16756
                             0.09855
                                      1.700 0.089157 .
## RPDE
                 -0.23042
                             0.06213 -3.709 0.000212 ***
## DFA
                 -0.03420
                             0.05639 -0.606 0.544251
## PPE
                  0.46026
                             0.09176
                                     5.016 5.54e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 2.517 on 3503 degrees of freedom
## Multiple R-squared: 0.905, Adjusted R-squared: 0.9045
## F-statistic: 1590 on 21 and 3503 DF, p-value: < 2.2e-16</pre>
```

Implement 4 following functions:

loglikelihiid function that for a given parameter vector theta and dispersion sigma.

```
logLikelihood <- function(theta, sigma, x, y) {
  n <- length(y)
  predictions <- x %*% theta
  residuals <- y - predictions
  log_likelihood <- -0.5 * n * log(2 * pi * sigma^2) - (t(residuals) %*% residuals) / (2 * sigma^2)
  return(as.numeric(log_likelihood))
}</pre>
```

Ridge function that for given vector theta, scalar sigma and scalar lambda and adds up a Ridge penalty to the minus loglikelihood.

```
ridge <- function(theta, sigma, lambda, x, y) {
  log_likelihood <- logLikelihood(theta, sigma, x, y)
  ridge_penalty <- lambda * sum(theta^2)
  return(-log_likelihood + ridge_penalty)
}</pre>
```

Use function optim() with method="BFGS" to find the optimal theta and sigma for the given lambda.

```
ridgeopt <- function(lambda, x, y) {
  n <- ncol(x)
  init_params <- c(rep(0, n), 1)
  ridge_obj <- function(params) {
    theta <- params[1:n]
    sigma <- params[n + 1]
    return(ridge(theta, sigma, lambda, x, y))
}

opt <- optim(init_params, ridge_obj, method = "BFGS")
  theta_opt <- opt$par[1:n]
  sigma_opt <- opt$par[n + 1]
  return(list(theta = theta_opt, sigma = sigma_opt))
}</pre>
```

computes the degrees of freedom of the Ridge model based on the training data.

```
freedom_degree <- function(lambda, x) {
  xT <- t(x) %*% x
  heat <- solve(xT + lambda * diag(ncol(x))) %*% t(x)
  df <- sum(diag(heat)) #trace
  return(df)
}</pre>
```

### 4.4 predict the values

Finally, we can compute optimal theta parameters for different lambda values by using function RidgeOpt.

```
train_data2 <- as.matrix(train_data[,names(train_data)!="motor_UPDRS"])</pre>
test_data2<- as.matrix(test_data[,names(test_data)!="motor_UPDRS"])</pre>
train_value <- train_data$motor_UPDRS</pre>
test_value <- test_data$motor_UPDRS</pre>
lambda_values <- c(1, 100, 1000)
train mse2<- c()
test_mse2<- c()
df < - c()
theta_value<- list()</pre>
for (i in seq_along(lambda_values)){
  lambda<- lambda_values[i]</pre>
  ridgemodel<- ridgeopt(lambda,train_data2,train_value)</pre>
  thetavalue <- ridgemodel $ theta
  theta_value[[i]]<- thetavalue</pre>
  train_predictions<- train_data2 ** thetavalue
  train_mse2[i] <- mean((train_value - train_predictions)^2)</pre>
  test_predictions<- test_data2 %*% thetavalue</pre>
  test mse2[i] <- mean((test value - test predictions)^2)
  df[i] <- freedom_degree(lambda,train_data2)</pre>
 result <- list(</pre>
    train_mse2 = train_mse2,
    test_mse2 = test_mse2,
    df = df,
    theta_value = theta_value
  )
}
print(result)
## $train_mse2
## [1] 6.465518 6.653863 6.846509
##
## $test_mse2
## [1] 6.387589 6.609421 6.787192
##
## $df
## [1] 0.009998311 0.001516241 0.000442187
##
## $theta_value
## $theta_value[[1]]
## [1] -0.0052580550 -0.0202829652 1.0515160348 -0.0008380227 0.7336342412
## [6] 0.0077671729 -0.0008418776 -0.0209940314 -0.0001519663 -0.0628711878
## [11] 0.0367333247 0.8557988044 -0.1154339829 -0.0815733362 0.3909625855
## [16] -0.3463559230 -0.2125478171 0.0539468078 -1.0994645885 -0.1441446539
```

```
## [21] 2.0815333869
##
## $theta value[[2]]
        6.193772e-03 -8.526021e-03 3.650537e-01 -3.961347e-04 7.249791e-01
        2.022569e-03
                      7.405812e-05
                                    1.225060e-03
                                                 1.374508e-03
        9.127526e-03 8.931548e-02 3.340734e-03 4.754327e-03
                                                               9.767899e-03
        9.350434e-03 1.924272e-02 2.616445e-02 -1.872273e-02 6.979124e-03
## [21]
        4.345821e-02
##
## $theta_value[[3]]
        1.590115e-02
                     4.205629e-03
                                   4.653460e-02 1.342374e-04
                                                               6.968982e-01
        2.437015e-04
                      1.712245e-05
                                    1.013762e-04
                                                 1.472975e-04
                                                                3.740594e-04
        9.610700e-04
                      9.501445e-03
                                   3.243690e-04 4.837515e-04
                                                               1.003988e-03
                     2.221216e-03 1.972672e-02 -1.510650e-03 1.318646e-04
## [16]
        1.009101e-03
## [21]
        4.337676e-03
```

In general, a lower test MSE indicates that the model generalizes better. Higher degrees of freedom mean that models are more flexible and tend to fit details in the data, but can lead to overfitting; Lower degrees of freedom mean that the model is smoother, limiting the fit to the training data.

In this example, under penalty parameter equals to 1, the model's train\_mse2 and test\_mse2 are the lowest, and the degree of freedom is small but not too low.So it is the most appropriate parameter choice.

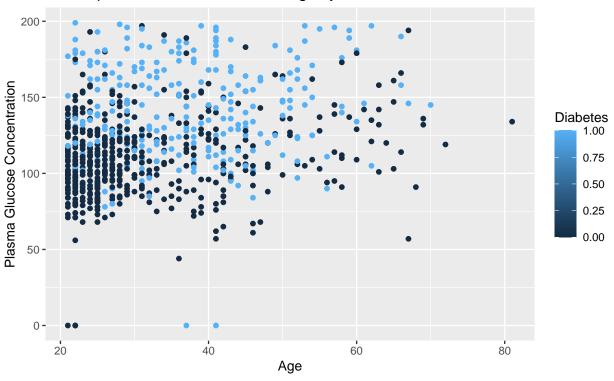
# 5 Assignment 3. Logistic regression and basis function expansion

### 5.1 Read Data and show scatter plot

read data and give a scatter plot showing a Plasma glucose concentration on Age where observations are colored by Diabetes levels

```
diabetes <- read.csv('.../data/pima-indians-diabetes.csv',header = FALSE)
colnames(diabetes) <- c('Pregnancies','Plasma_glucose','blood_pressure','TricepsSkinFoldThickness','Ser
#
ggplot(diabetes,aes( x = diabetes$Age, y = diabetes$Plasma_glucose, color = diabetes$Diabetes)) + geom_glucose( x = "Age", y = "Plasma Glucose Concentration", color = "Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by Diabetes Status")</pre>
```

# Scatterplot of Plasma Glucose vs Age by Diabetes Status



### 5.2 Train a logistic regression model when the threshold r = 0.5

```
formula <- Diabetes ~ Age + Plasma_glucose</pre>
diabetes$Diabetes <- as.factor(diabetes$Diabetes)</pre>
gml_model <- caret::train(formula, data = diabetes, method = "glm", family = "binomial")</pre>
#type = "prob" predict probability
#type = "raw" predict the raw value/ class
#diabetes pred <- predict(qml model, type = "prob")</pre>
classify_pred_res <- function(r,gml_model) {</pre>
  diabetes_pred <- predict(gml_model, type = "prob")</pre>
  diabetes_pred$predict <- lapply(1:nrow(diabetes_pred), function(x) ifelse(diabetes_pred[x,2] > r, 1,
  diabetes_pred$predict <- unlist(diabetes_pred$predict)</pre>
  diabetes_pred$raw <- diabetes$Diabetes</pre>
  diabetes_pred[, 3:4] <- lapply(diabetes_pred[, 3:4], as.factor)</pre>
  trainingData <- gml_model$trainingData %>% select(-.outcome)
  diabetes_pred <- cbind(diabetes_pred, trainingData)</pre>
  diabetes_pred$Age <- gml_model$trainingData$Age</pre>
  diabetes_pred$Plasma_glucose <- gml_model$trainingData$Plasma_glucose
  return(diabetes_pred)
diabetes_pred <- classify_pred_res(0.5,gml_model)</pre>
```

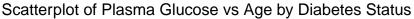
```
diabetes_confusion <- table(diabetes_pred$raw, diabetes_pred$predict)
error_rate <- 1 - (sum(diag(diabetes_confusion)) / sum(diabetes_confusion))
cat(" training misclassification error:",error_rate)</pre>
```

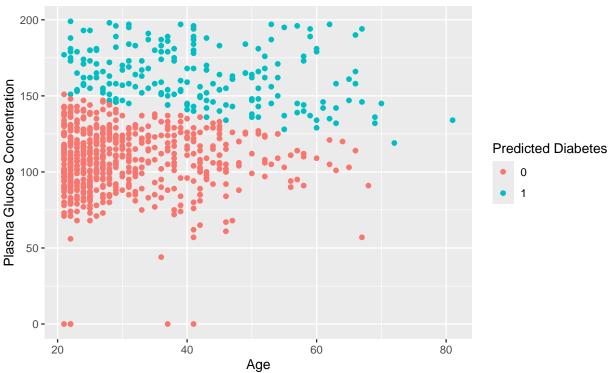
## training misclassification error: 0.2630208

## 5.3 Draw a scatter plot showing the predicted diabetes status

we can see that the logistic regression visually separates the two classes of diabetes status well, but the mis classification error is high due to the overlap of the two classes, maybe change—can improve the performance.we will try later

```
ggplot(diabetes,aes( x = diabetes_pred$Age, y = diabetes_pred$Plasma_glucose, color = diabetes_pred$pred$pred$(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by Diabetes Status")
```



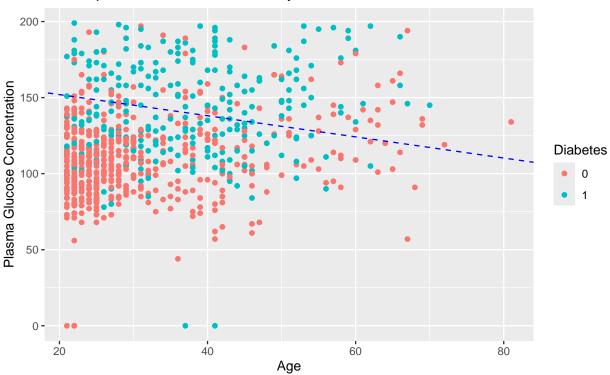


# 5.4 Draw a decision boundary between the two predicted classes

we can see that the boundary line try to split the dots into two classes and put the most the red dots below the line and the most blue dots above the line, but when the age exceed the 50, the performance of the model is not good.it seems that the number of red dot below the boundary line is same as the number above the line, it results the high misclassification error

```
get_boundary_line <- function(gml_model,r, y_name) {</pre>
  coefficients <- gml_model$finalModel$coefficients</pre>
  boundary_parameter <- list()</pre>
  coef_names <- names(coefficients)</pre>
  y_value <- coefficients[[y_name]]</pre>
  boundary_parameter$Intercept <- -(coefficients[['(Intercept)']] / y_value) - (log((1/r) - 1)/y_value)
  # boundary_parameter$intercept <- intercept</pre>
  for (name in coef_names){
    if (name != '(Intercept)'){
      boundary_parameter[[name]] <- -coefficients[[name]] / y_value</pre>
    }
  }
  return(boundary_parameter)
boundary_parameter <- get_boundary_line(gml_model,0.5,'Plasma_glucose')</pre>
ggplot(diabetes,aes( x = diabetes$Age, y = diabetes$Plasma_glucose, color = diabetes$Diabetes)) +
  geom_point()+
  geom_abline(slope = boundary_parameter$Age, intercept = boundary_parameter$Intercept, color = "blue",
  labs(x = "Age", y = "Plasma Glucose Concentration", color = "Diabetes") +
  ggtitle("Scatterplot with Decision Boundary")
```

# Scatterplot with Decision Boundary



### 5.5 Change the thresholds r to 0.2, 0.8 to see the what happened

we can see that when r = 0.2, for the red dots, its TP is relatively high, but the Recall is low, for the blue dots, its TP is lower than red dots, but the Recall is higher than red dots, it means that the model is

more likely to predict the blue dots as the positive class, but the blue dots are more likely to be the negative class, it results in the high misclassification error, when r = 0.8, the model is more likely to predict the red dots as the positive class, but the red dots are more likely to be the negative class, it results in the high misclassification error

```
pred_res_0.2 <- classify_pred_res(0.2,gml_model)
pred_res_0.8 <- classify_pred_res(0.8,gml_model)</pre>
```

### 5.5.1 plot the scatter when r = 0.2

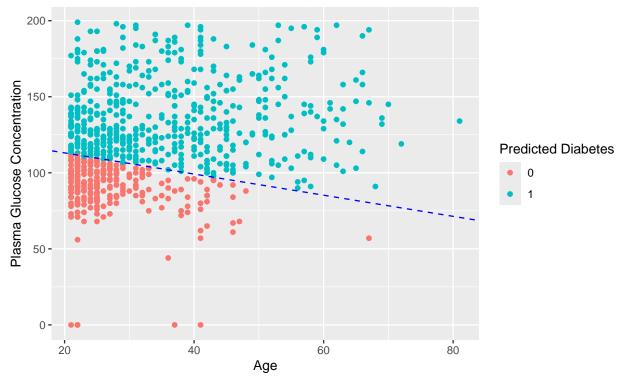
```
boundary_parameter_0.2 <- get_boundary_line(gml_model,0.2,'Plasma_glucose')

ggplot(diabetes,aes( x = pred_res_0.2$Age, y = pred_res_0.2$Plasma_glucose, color = pred_res_0.2$predic

geom_abline(slope = boundary_parameter_0.2$Age, intercept = boundary_parameter_0.2$Intercept, color = "
labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +

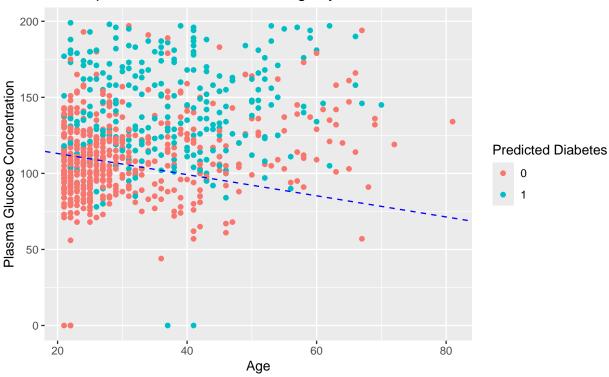
ggtitle("Scatterplot of Plasma Glucose vs Age by predicted diabetes Status")
```

# Scatterplot of Plasma Glucose vs Age by predicted diabetes Status



```
ggplot(diabetes,aes( x = pred_res_0.2$Age, y = pred_res_0.2$Plasma_glucose, color = pred_res_0.2$raw)) =
geom_abline(slope = boundary_parameter_0.2$Age, intercept = boundary_parameter_0.2$Intercept, color = "
labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by raw diabetes Status")
```



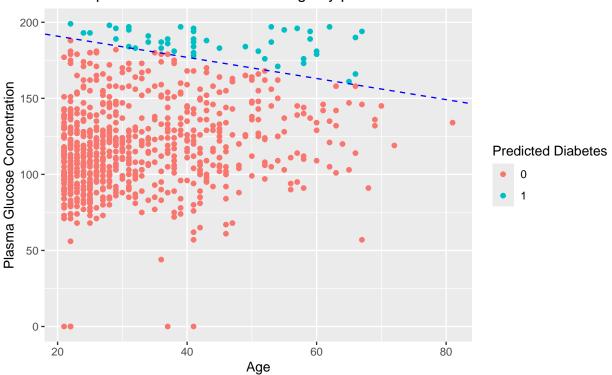


### 5.5.2 plot the scatter when r = 0.8

```
boundary_parameter_0.8 <- get_boundary_line(gml_model,0.8,'Plasma_glucose')

ggplot(diabetes,aes( x = pred_res_0.8$Age, y = pred_res_0.8$Plasma_glucose, color = pred_res_0.8$prediction geom_abline(slope = boundary_parameter_0.8$Age, intercept = boundary_parameter_0.8$Intercept, color = "labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") + ggtitle("Scatterplot of Plasma Glucose vs Age by predicted diabetes Status")
```

# Scatterplot of Plasma Glucose vs Age by predicted diabetes Status



```
ggplot(diabetes,aes( x = pred_res_0.8$Age, y = pred_res_0.8$Plasma_glucose, color = pred_res_0.8$raw)) =
geom_abline(slope = boundary_parameter_0.8$Age, intercept = boundary_parameter_0.8$Intercept, color = "
labs(x = "Age", y = "Plasma Glucose Concentration", color = "Predicted Diabetes") +
ggtitle("Scatterplot of Plasma Glucose vs Age by raw diabetes Status")
```