# Minimum Sum of a Sorted Pair (Hard Version)

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 megabytes

The only difference between the two versions of the problem is the size of the given array.

You are give an array  $a_1, a_2, \ldots, a_n$ . A pair (i, j) is considered sorted if:

- $1 \le i < j \le n$
- And  $a_i < a_j$

Among all sorted pairs your task is to find one with the minimum sum  $a_i + a_j$ .

If there is no pair satisfying the inequality print -1, otherwise print the value of the minimum sum.

## Input

The first line of the input contains a single integer n  $(1 \le n \le 10^5)$ , the size of the array.

The second line contains n integers  $a_1, a_2, \ldots, a_n$   $(1 \le a_i \le 10^9)$ .

# Output

One single integer, the minimum pair sum, or -1 if there are no sorted pairs.

### **Examples**

standard input	standard output
6	5
11 2 5 3 10 1	
5	-1
5 4 3 2 1	

#### Note

In the first testcase all the sorted pairs are: (2-nd, 3-rd), (2-nd, 4-th), (2-nd, 5-th), (3-rd, 5-th) and (4-th, 5-th). The one that has the minimum sum is the pair (2-nd, 4-th) with sum 2+3=5.

In the second testcase, there is no sorted pair in the array, so the answer will be -1.